
Novel b-hemisphere jet charge and flavour taggers at FCC-ee

Second ECFA Workshop on e^+e^- Higgs/EW/Top Factories – Paestum

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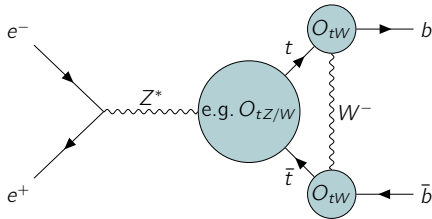
²Laboratoire de Physique de Clermont – Université Clermont-Auvergne

³INFN Pisa

Motivation I

- **Connect energy scales** at future e^+e^- collider to access SM deviations globally
- Possible anomalies translate over a range of energy scales: from Z -pole to top threshold
- Heavy-quark EW measurements as a **probe for new physics** with a common set of dimension-6 operators

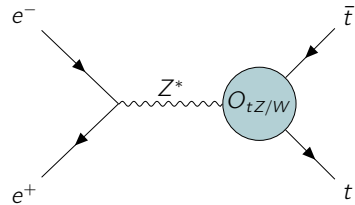
$\mathcal{O}(m_Z) \sim 90 \text{ GeV}$



\Rightarrow Vertex corrections $\approx 1\%$ of R_b in the SM

- **Tight constraints** on Wilson coefficients:
 1. **Very precise measurements at the Z -pole**
 2. **Variety of observables at the top-threshold**

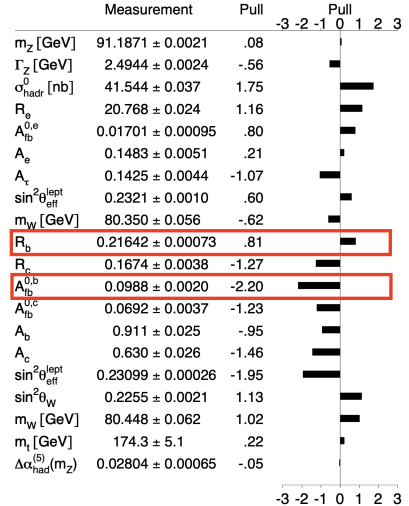
$\mathcal{O}(m_t) \sim 350 \text{ GeV to } 365 \text{ GeV}$



\Rightarrow Anomaly in e. g. the t forward-backward asym.

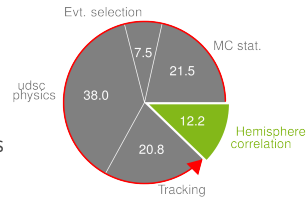
Motivation II

- Today: place focus on b -quark observables at FCC-ee with BSM potential from **vertex corrections**
- Measurements at the Z -pole with $4.2 \cdot 10^{12} Z \rightarrow q\bar{q}$ (4 IPs):
 - $R_b = \frac{\sigma_{b\bar{b}}}{\sigma_{\text{had.}}}$
 - $A_{\text{FB}}^b = \frac{N_F - N_B}{N_F + N_B}$
 → Likely **dominated by systematic uncertainties**
- Interesting terrain for new methods to improve measurement
 - Explore Tera- Z regime with **exclusive b-hadron decay reconstruction as new tagger**

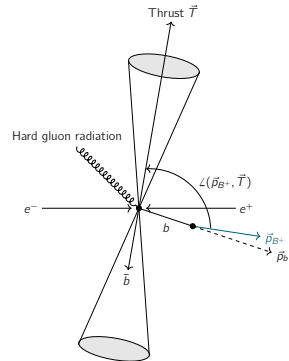


Exclusive b -hadron decays

- LEP σ_{sys} . dominated by $udsc$ -physics and hemisphere correlations
- With Tera-Z σ_{stat} . in reach: measurement limited by systematic uncertainties
- Reconstruct exclusive b -hadron: determine quark-flavour with 100 % purity
 → Stick to **ultra-pure mass region** to assess remaining systematic uncertainties → $\epsilon_b = 1\%$



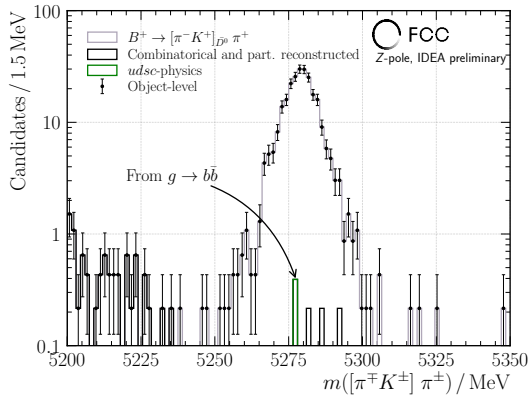
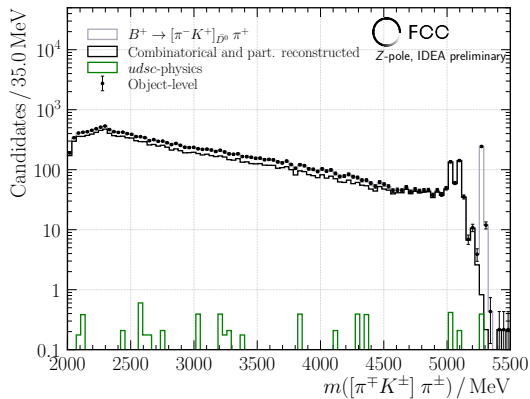
Observable	R_b	A_{FB}^b
b -hadrons	$B^+, B_d^0, B_s^0, \Lambda_b^0$	B^+, Λ_b
Knowledge of. . .	Flavour	Flavour, \vec{p} & Q
Remove $udsc$ -physics contribution		
Advantages		Overcome mixing dilutions and hemisphere confusion
Remaining σ_{sys} .	Hemisphere correlation C_b	QCD corrections



- C_b and QCD corrections evaluated on **Full Simulation sample** and forced decays ($B^\pm \rightarrow [K^+ \pi^-]_{\bar{D}^0} \pi^+$)

Performance I

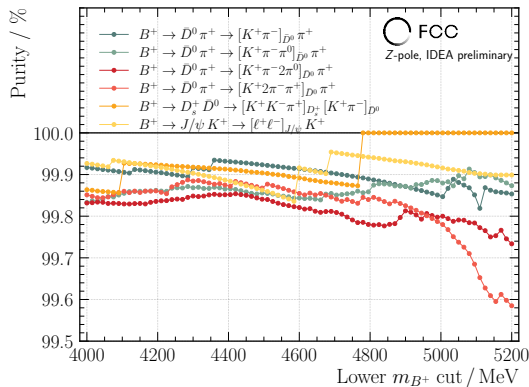
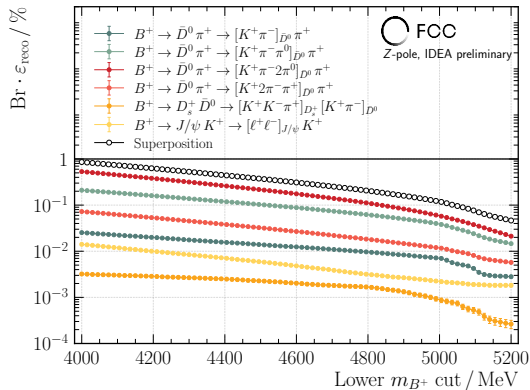
- Include > 200 b -hadron decay modes
 - Evaluate tagger performance from **six representative decay modes** (varying track mult., N_{π^0}, \dots)
- Purity & reconstruction efficiency evaluated on 10^7 $Z \rightarrow q\bar{q}$ **Fast Simulation events** with IDEA detector
- Here: $B^+ \rightarrow [K^+ \pi^-]_{\bar{D}^0} \pi^+$ with $E_B > 20$ GeV to reduce background



- **Purity: 99.8 %**, **reconstruction efficiency: 77 %**
- Background suppressed by three orders of magnitude, contamination in signal region from $g \rightarrow b\bar{b}$

Performance II

- Evaluate actual tagger efficiency ($\text{Br} \cdot \epsilon_{\text{reco}}$) for the six modes when increasing the acceptance range
- **Enlarging mass window** highly increases the tagger-efficiency by keeping purity constant



- Focus on mass peak region to control systematic uncertainties

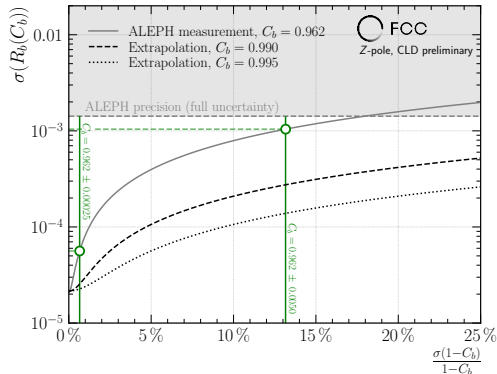
Measurement of R_b : Importance of hemisphere correlation

- State of the art (ALEPH): $R_b = 0.2159 \pm 0.0009$
- With conservative tagger efficiency of 1%: $\sigma_{\text{stat.}}(R_b) = 2.2 \cdot 10^{-5}$ (**factor 45** w. r. t. ALEPH)
- $\sigma_{\text{syst.}}$ reduces to **hemisphere efficiency correlation**

→ Quantifies dependence of tagging efficiencies in the two hemispheres:

$$C_b = \frac{\varepsilon_{b\bar{b}}}{\varepsilon_b \cdot \varepsilon_{\bar{b}}}$$

- Its precise knowledge is **the key** for the measurement of R_b



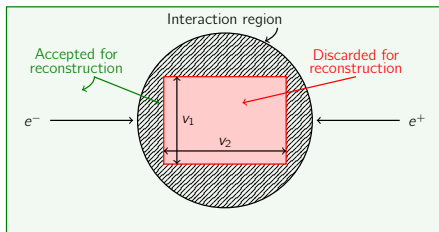
Green: Uncertainty on C_b scaled
Gray: C_b values extrapolated

- Two handles: Uncertainty on C_b and difference to $C_b = 1$

Understanding C_b : The PV resolution

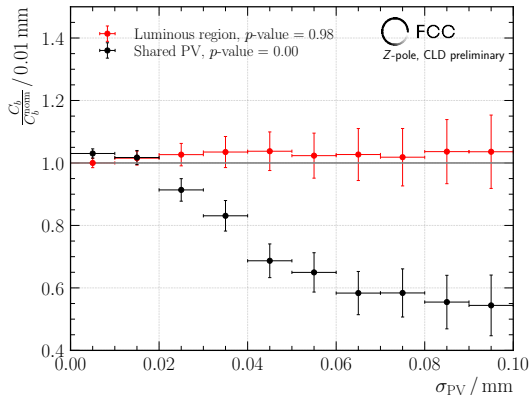
- **Goal:** Find regions of the phase-space which increase C_b (kinematically + event-variables)
 - LEP found: mainly driven by **PV measurement uncertainty**
 - LEP did: PV-separation. Here: cut on **luminous region** from beam spot constraints

Cut on the luminous region:

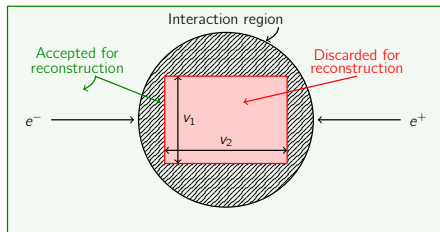


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- **Goal:** Find regions of the phase-space which increase C_b (kinematically + event-variables)
 - LEP found: mainly driven by **PV measurement uncertainty**
 - LEP did: PV-separation. Here: cut on **luminous region** from beam spot constraints
- Focus placed on **differential analysis** of C_b to reduce systematic uncertainties
- All distributions normalised to inclusive C_b value



Cut on the luminous region:



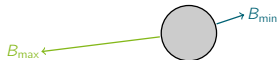
$$\rightarrow \sigma_{PV} = \sqrt{\sum_{i \in [x,y,z]} (PV_i^{\text{Object-level}} - PV_i^{\text{Particle-level}})^2}$$

→ **Strongly dependent** for the shared PV approach

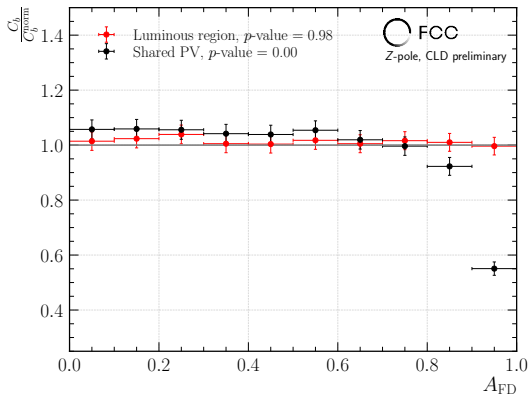
→ **Resolved** with optimised cut on luminous region

Understanding C_b : The flight-distance asymmetry

Interaction region



- Linked to the PV resolution: flight-distance asymmetry $A_{FD} = \frac{FD_{B_{max}} - FD_{B_{min}}}{FD_{B_{max}} + FD_{B_{min}}}$
- One B -meson far away \rightarrow **Reduce PV measurement precision** (captures more tracks) \rightarrow Increase C_b



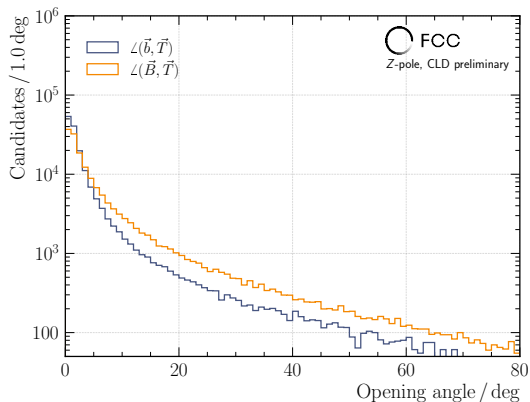
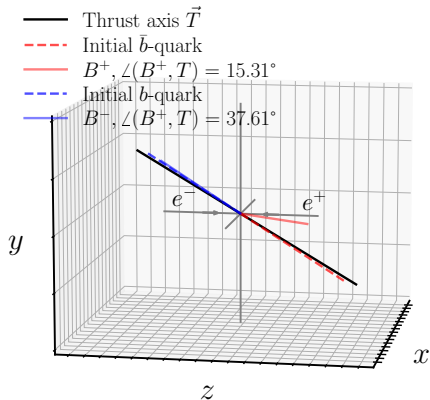
- Large asymmetries: correlation decreases
- Flat distribution for luminous region

■ R_b conclusions:

1. Crucial to minimise the remaining systematic uncertainty on R_b
2. Handle to reduce C_b differentially: luminous region approach minimises PV dependencies
3. Larger FullSim sample in order to make quantitative statements

Measurement of A_{FB}^b

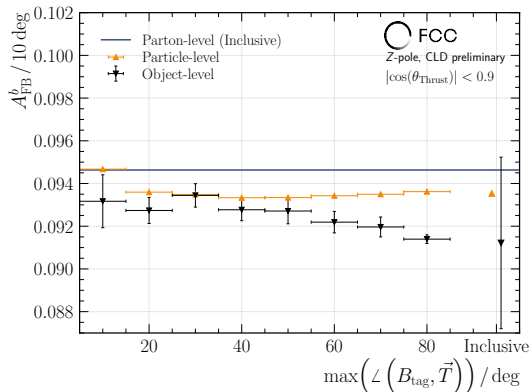
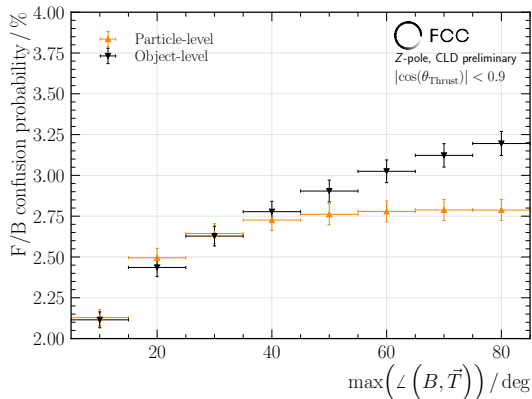
- Forward/backward determined from thrust-axis \vec{T} , charge from reconstructed B -candidate
- **Remove mixing dilution** by using B^+ and Λ_b^0 decays
- Hard gluon radiation can still confuse hemispheres, **but:** direction of B^+ is known



- B -meson direction estimator altered through gluon emission + fragmentation
- Use this information to **minimise QCD corrections**

Controlling the gluon radiations?

- Control g -radiation through $\angle(B^\pm, \vec{T})$
 → Hard gluon emission **increases opening angle** between \vec{T} and B -meson
- Evaluate A_{FB}^b by cutting events with large opening angles



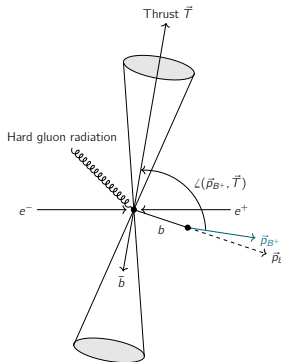
→ Removing events with large $\angle(B^\pm, \vec{T})$: **closer to parton-level** A_{FB}^b

Conclusions and Outlook

- Novel b -hemisphere charge and flavour taggers for application at Tera- Z programme
- Promising performance: purity above 99.6 % for representative modes
- R_b and A_{FB}^b : overcome syst. limitations from $udsc$ -quark physics by reconstructing exclusively b -hadrons

- R_b
1. Overcome syst. limitations from $udsc$ -quark physics
 2. Reduction of C_b through cut on the luminous region

- A_{FB}^b
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 3. Gluon radiation control with angle between B -meson and \vec{T} ?

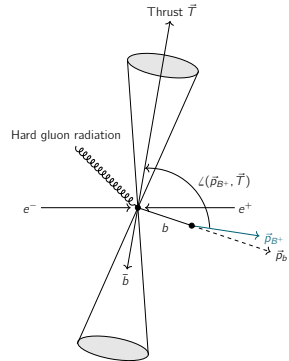


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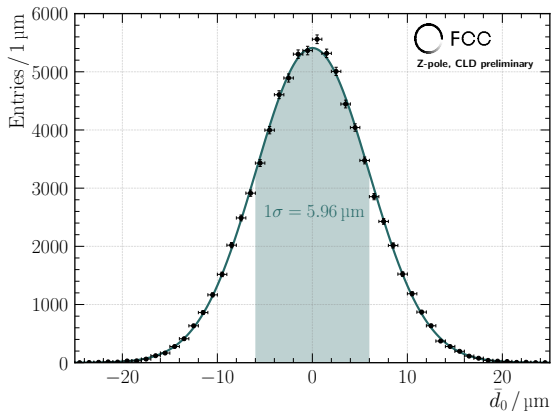
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Thanks for your attention!

Luminous region

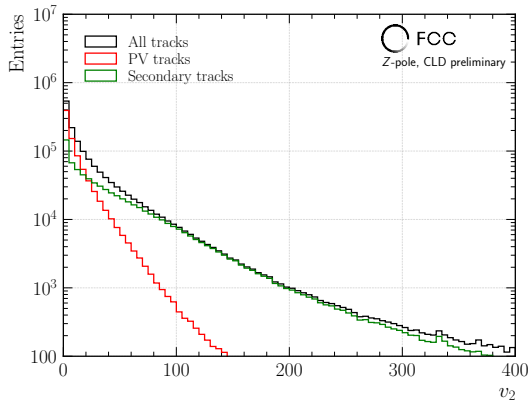
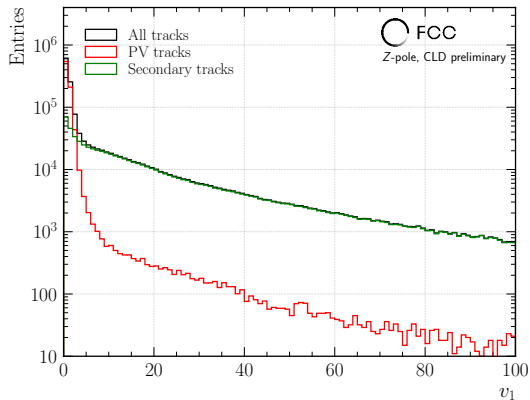
- $\bar{d}_0 = \text{sign}(PV_z^{\text{Particle-level}}) \cdot \sqrt{(PV_x^{\text{Particle-level}})^2 + (PV_y^{\text{Particle-level}})^2}$



- $v_1 = \frac{d_0 - \mu(\bar{d}_0)}{\sqrt{\sigma(d_0)^2 + \sigma(\bar{d}_0)^2}}$ and $v_2 = \frac{z_0 - \mu(\bar{d}_0)}{\sqrt{\sigma(z_0)^2 + \sigma(\bar{d}_0)^2}}$, d_0 and z_0 are the track parameters

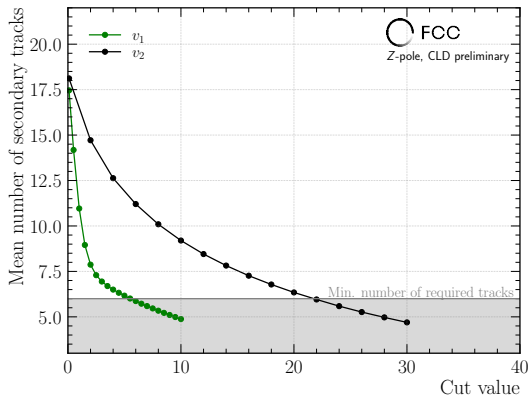
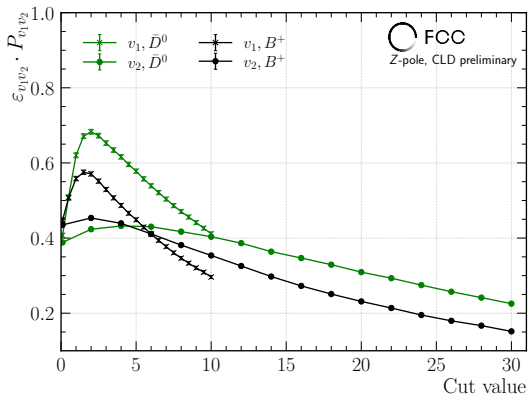
Luminous region: primary and secondary

- Is there a possibility to distinguish between primary and secondary tracks? →Yes!
- Use truth-matched tracks to compute v_1 and v_2 distributions



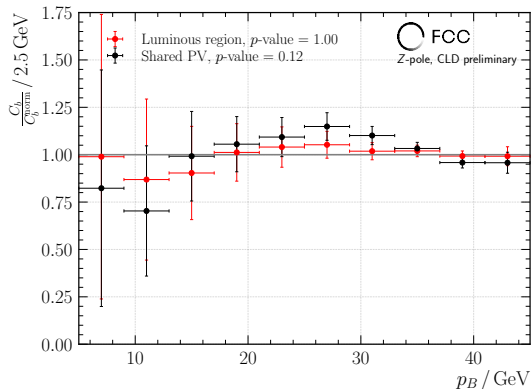
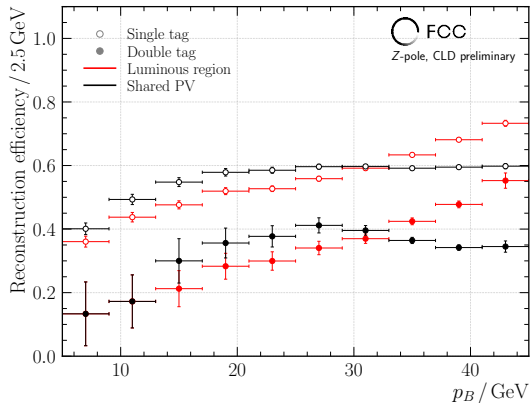
Optimising the luminous region cuts

- Scan over a range of v_1 and v_2 independently
- Evaluate product of purity and efficiency of the D^0 - and B -mesons & mean number of secondary tracks
- $P_{v_1 v_2} = \frac{N_{\text{sig}}}{N_{\text{sig}} + N_{\text{bkg}}}$, N_{bkg} estimated and scaled from the sidebands
- $\epsilon_{v_1 v_2} = \frac{N_{\text{sig}}}{N_{\text{total}}}$, $N_{\text{total}} = (10^4 \cdot N_B)$ and $N_B = 2$

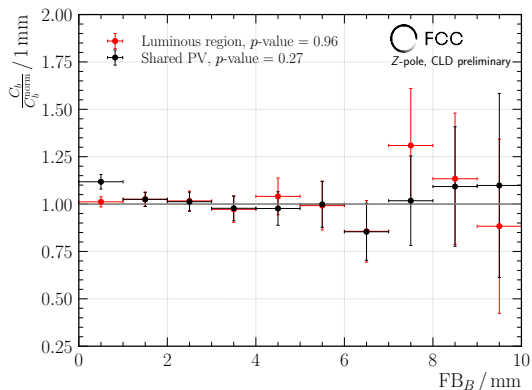
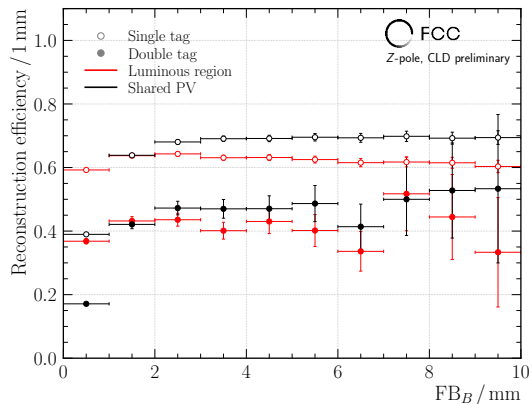


→ Choose maximum for v_1 from $P_{v_1 v_2} \cdot \epsilon_{v_1 v_2}$, v_2 taken from the mean number of tracks

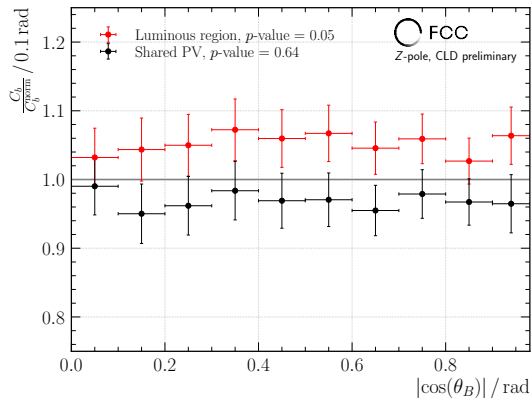
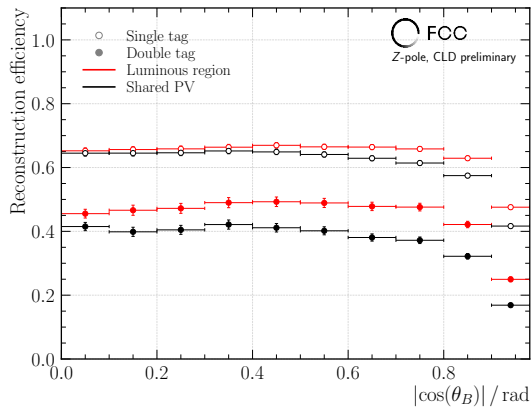
Differential hemisphere correlations: B -momentum



Differential hemisphere correlations: B -flight distance

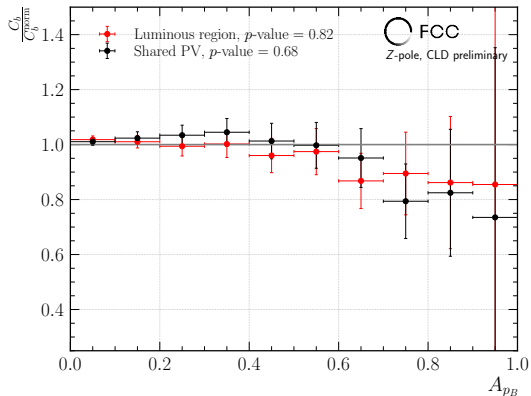
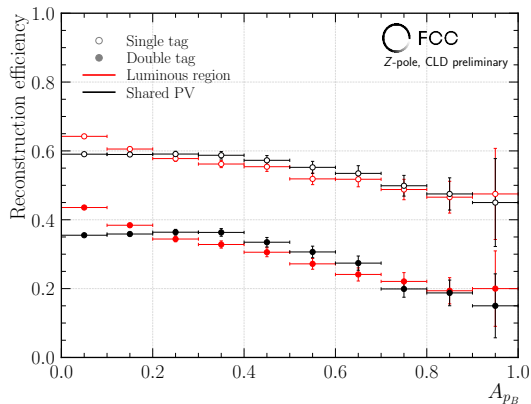


Differential hemisphere correlations: B -polar angle

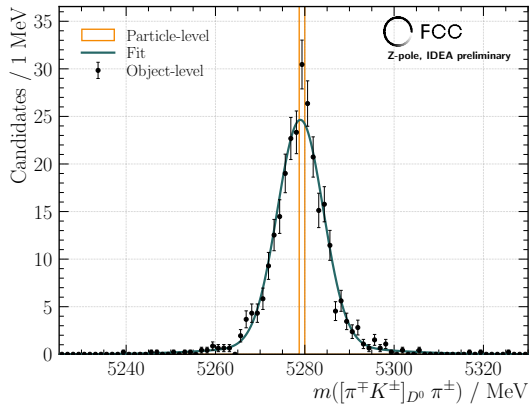
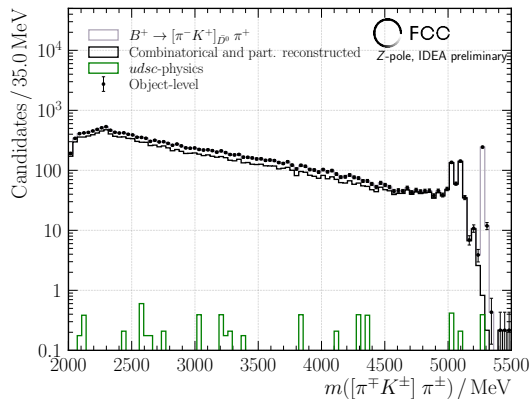


Differential hemisphere correlations: B -momentum asymmetry

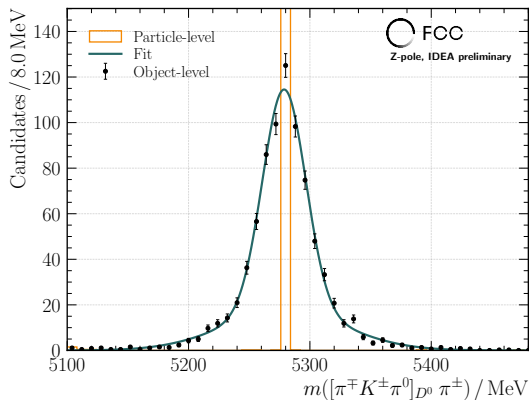
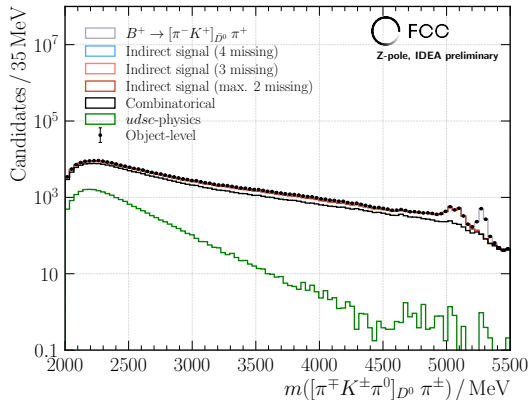
$$A_{p_B} = \frac{p_{B_{\max}} - p_{B_{\min}}}{p_{B_{\max}} + p_{B_{\min}}}$$



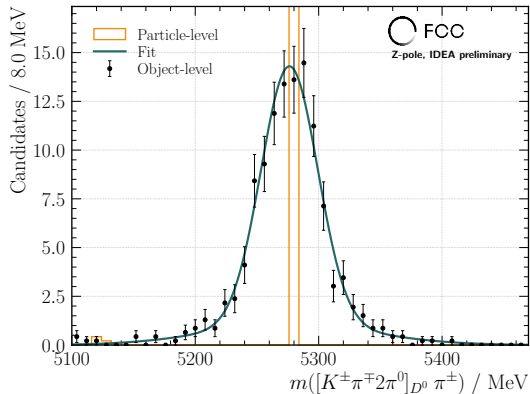
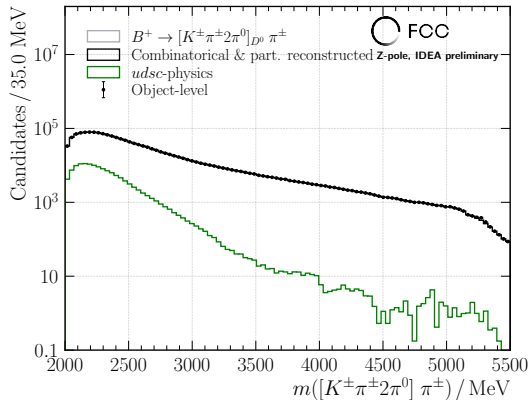
Fast Simulation: Decay mode $B^+ \rightarrow [K^+ \pi^-]_{D^0} \pi^+$



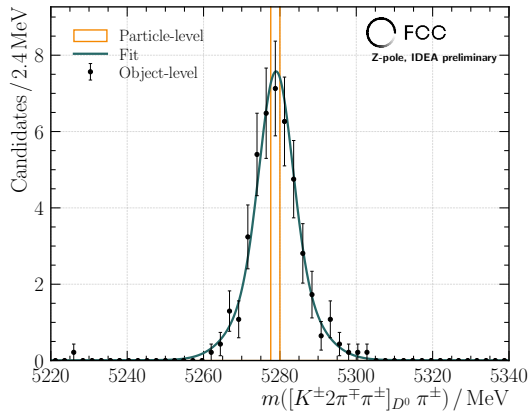
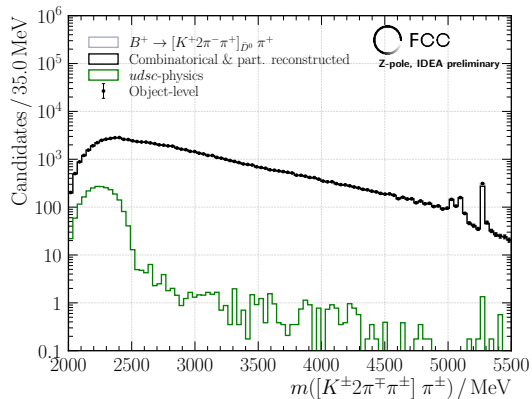
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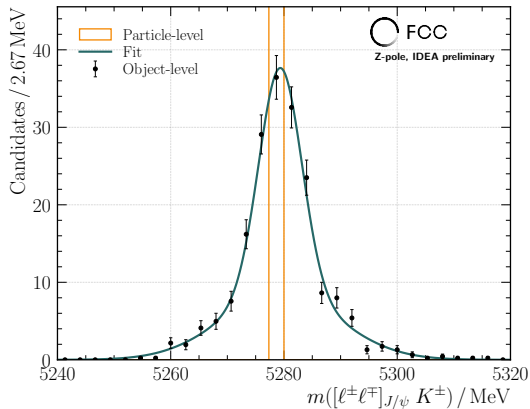
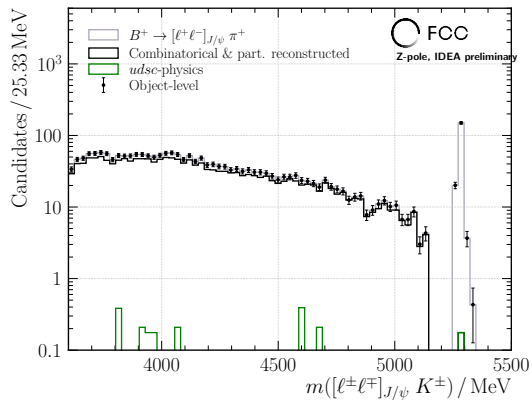
Fast Simulation: Decay mode $B^+ \rightarrow [K^+ \pi^- 2\pi^0]_{D^0} \pi^+$



Fast Simulation: Decay mode $B^+ \rightarrow [K^+ 2\pi^- \pi^+]_{D^0} \pi^+$



Fast Simulation: Decay mode $B^+ \rightarrow [\ell^+\ell^-]_{J/\psi} K^+$



Fast Simulation: Decay mode $B^+ \rightarrow [K^+K^-\pi^+]_{D_s^+} [K^+\pi^-]_{\bar{D}^0}$

