

# “Here be SUSY” - Prospects for SUSY searches at future colliders<sup>1</sup>

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CLUSTER OF EXCELLENCE  
QUANTUM UNIVERSE



<sup>1</sup>Largely based on arXiv:2003.12391

# SUSY: What *do* we know ?

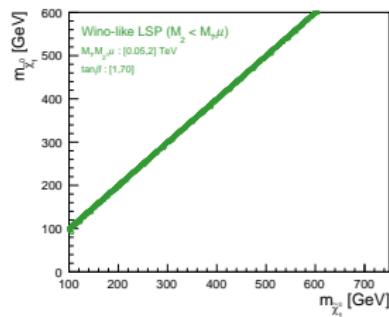
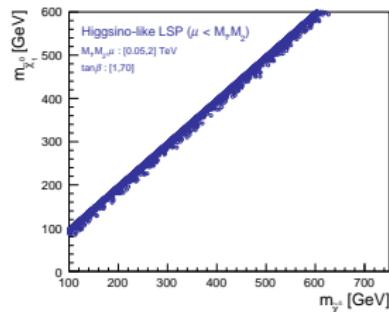
Naturalness, hierarchy, DM, g-2 all prefers **light electro-weak sector**.

- Except for 3d gen. squarks, **the coloured sector** - where pp machines excel - **doesn't enter the game**.
- If the LSP is higgsino or wino, EW sector is “compressed”. Only for bino-LSP can the difference be large.
- So, most sparticle-decays are via cascades, with small  $\Delta(M)$  at the end.
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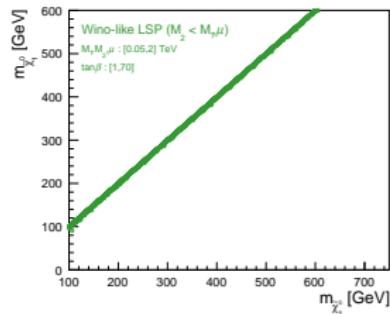
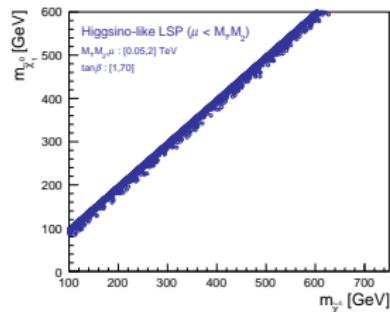
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# What would be seen at colliders in the worst case?

- MSSM, R-parity conservation (R-parity violation always easier at  $e^+e^-$ )
- sfermions not NLSP (**idem**, except  $\tilde{\tau}$  but even worse for  $pp \dots$ )
- Then: LSP is Bino, Wino, or Higgsino (more or less pure), same for the NLSP
- $M_1, M_2$  and  $\mu$  are the main-players.
- Consider **any values**, and combinations of **signs**, up to values that makes the bosinos out-of-reach for any new facility  $\sim$  a few TeV.
- Also vary other parameters ( $\beta, M_A, M_{\text{sfermion}}$ ) with less impact.
- **No other prejudice.**
- Use SPheno 4.0.5beta to calculate spectra and BR:s, and use Whizard 2.8.0 for cross-sections

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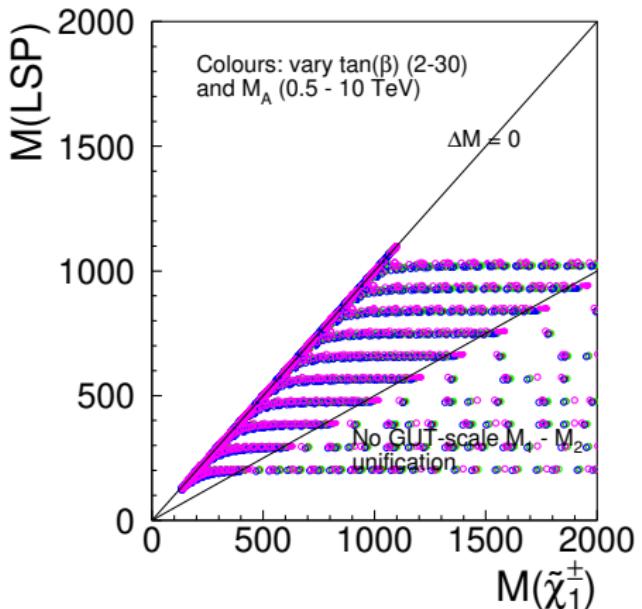
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    - $M_1, M_2$  and  $\mu$  What happens with spectra, cross-sections, BRs when
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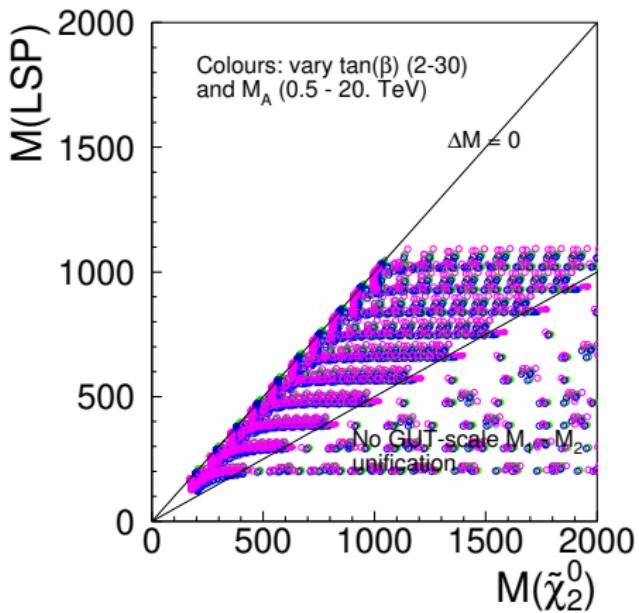
# Aspects of the spectrum

- $M_{LSP}$  vs.  $M_{\tilde{\chi}_1^\pm}$
- $M_{LSP}$  vs.  $M_{\tilde{\chi}_2^0}$
- Colours indicate different settings of the secondary parameters (lesson is that they don't matter much...)
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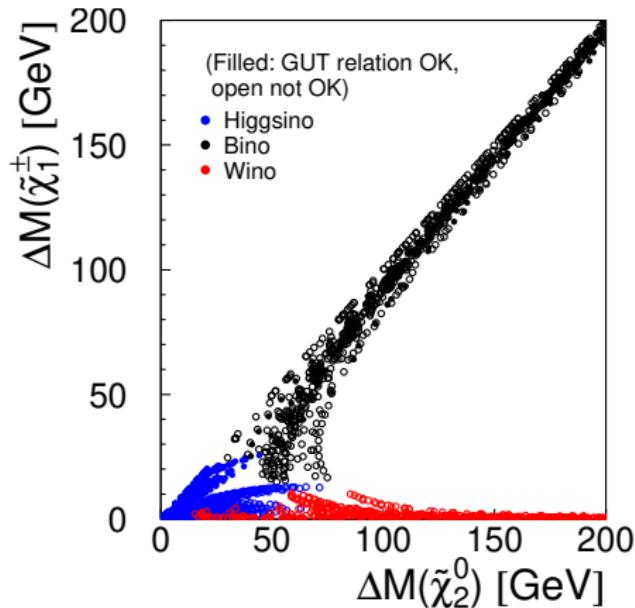
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Another angle:  $\Delta(M)$  for  $\tilde{\chi}_1^\pm$  vs. that of  $\tilde{\chi}_2^0$ : Important experimentally

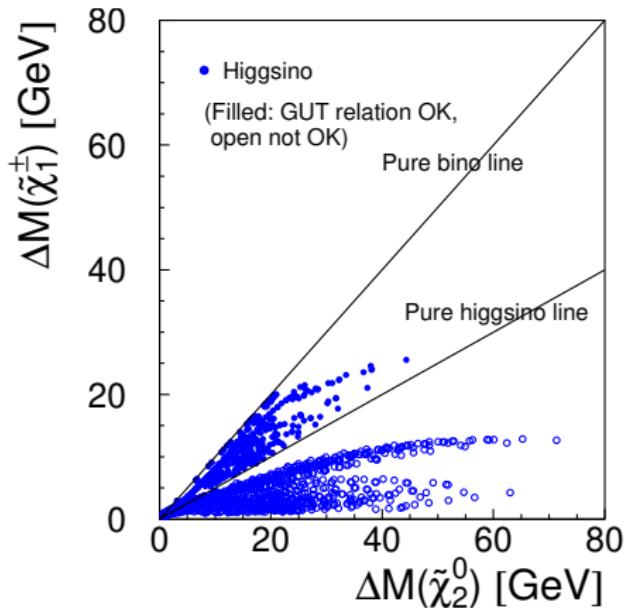
- Three regions:
  - Bino: Both the same, but can be anything.
  - Wino:  $\Delta\tilde{\chi}_1^\pm$  small, while  $\Delta\tilde{\chi}_2^0$  can be anything.
  - Higgsino: Both often small
- But note, seldom on the “Higgsino line”, ie. when the chargino is *exactly* in the middle of mass-gap between the first and second neutralino.



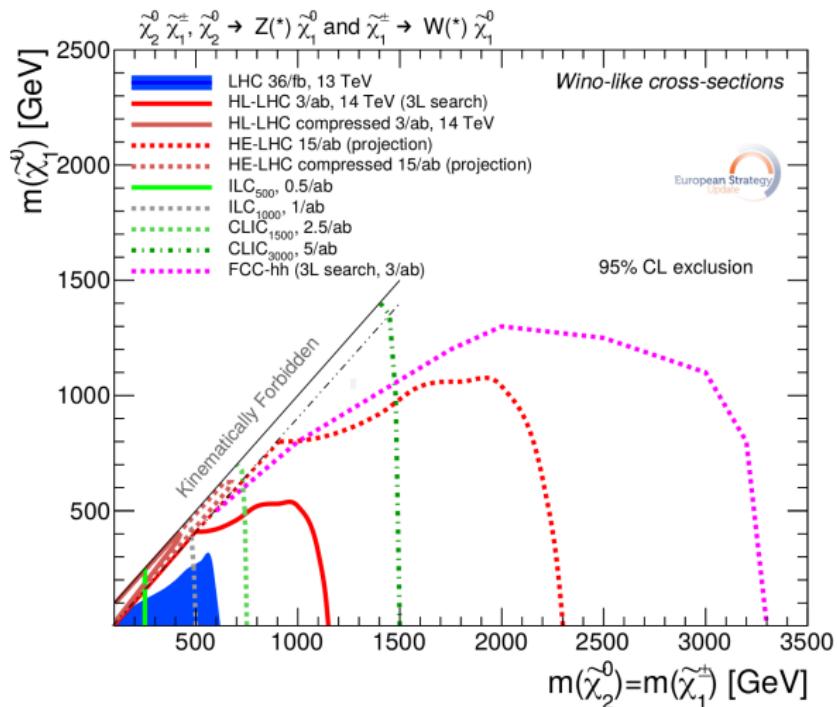
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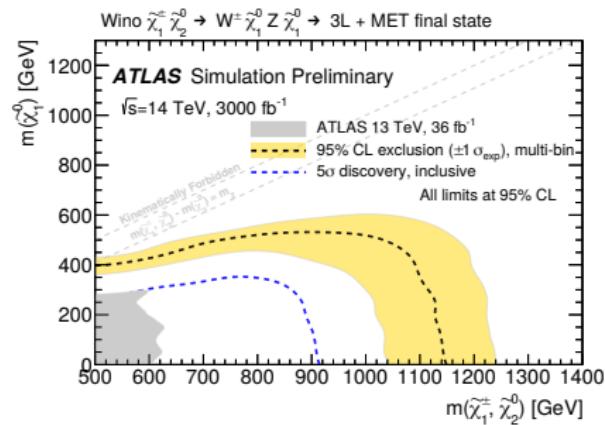
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NB:  $e^+ e^-$  curves are **certain discovery**, pp are **possible exclusion !!!**

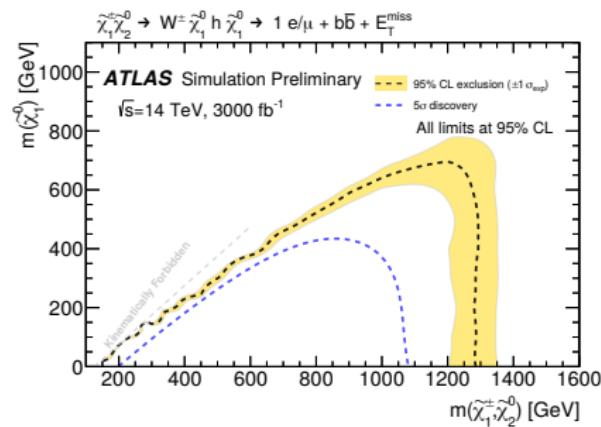
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- ATL-PHYS-PUB-2018-048,  
ATLAS HL-LHC projection,  
extrapolated (up *and* down)
- This is for the best mode!
- The other decay mode
- Better at  $M_{LSP}=0$ , weaker at  
lower  $\Delta_M$ .
- Why is the decay-mode an  
issue? Here's why :
  - Vary signs of  $\mu$ ,  $M_1$ , and  $M_2$
- So: The exclusion-region is  
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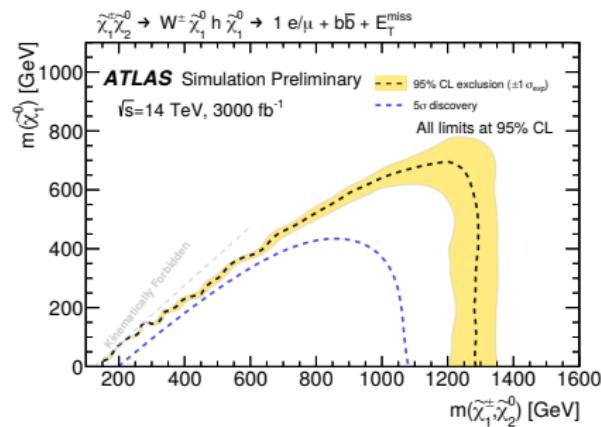
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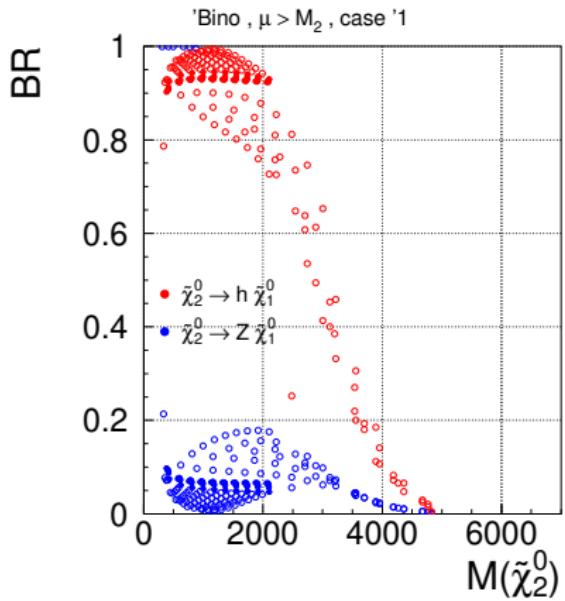
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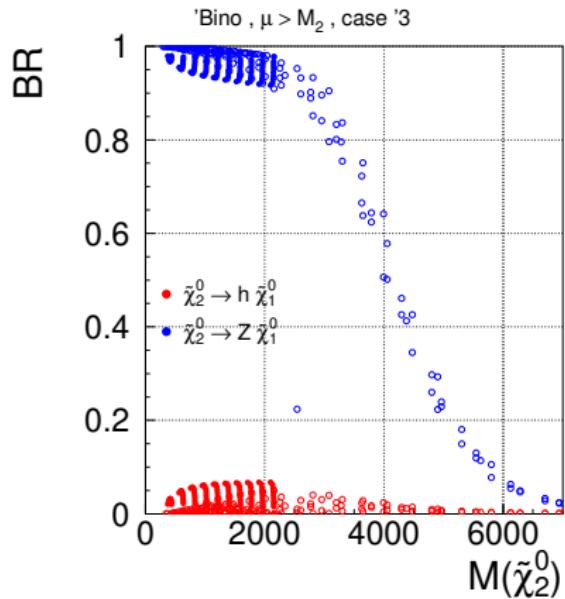
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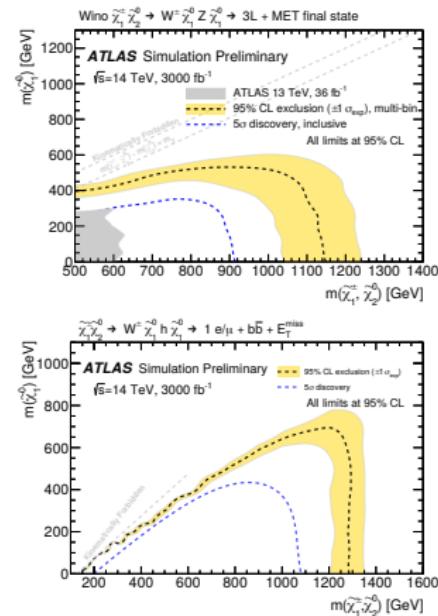
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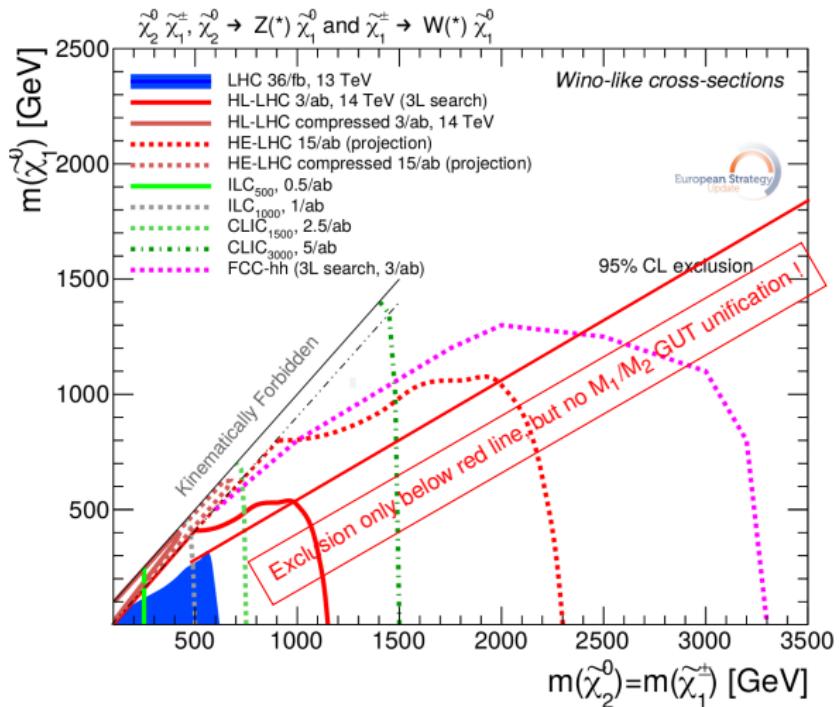


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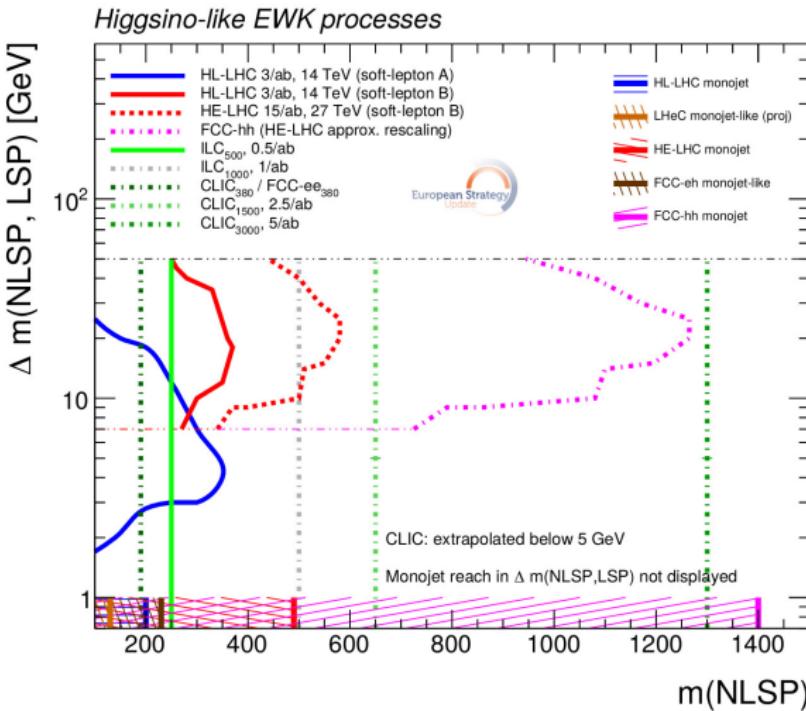


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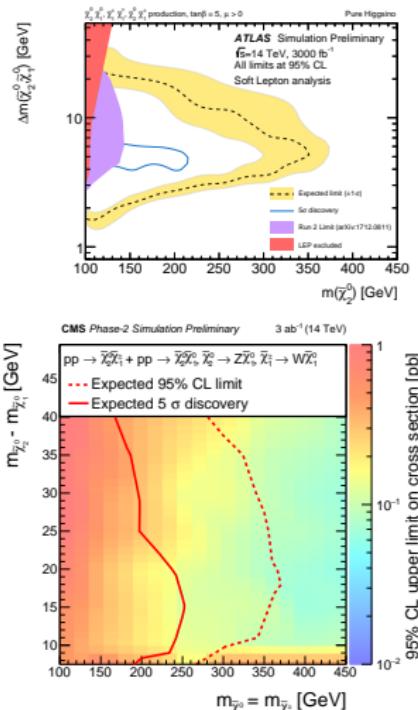
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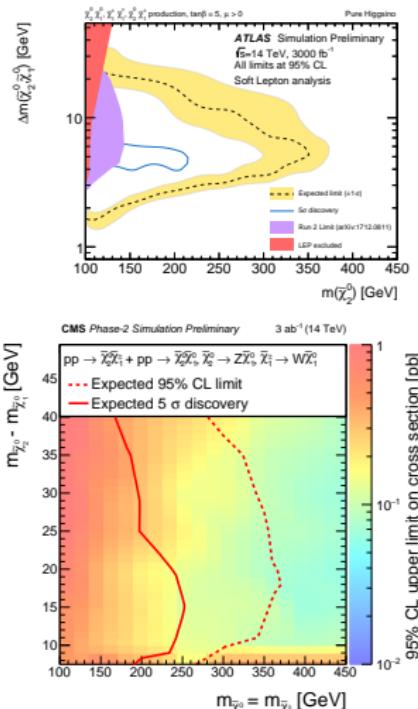
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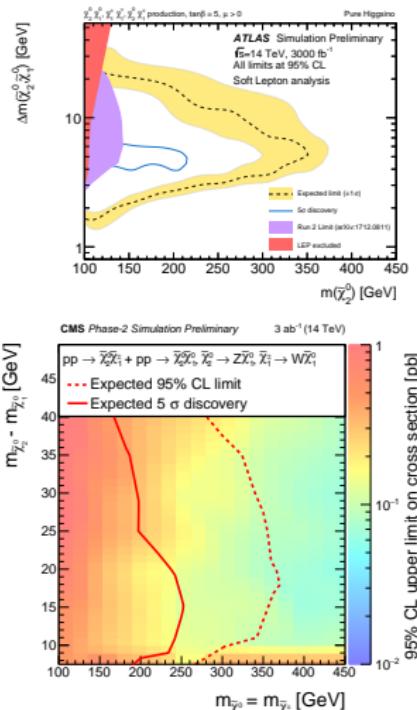
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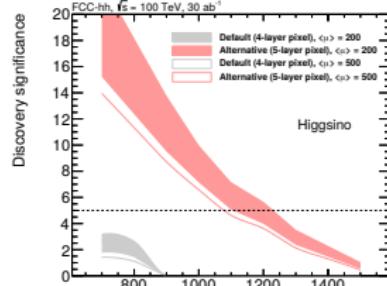
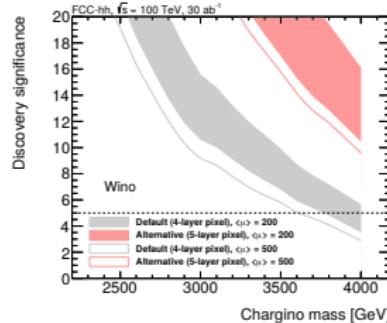
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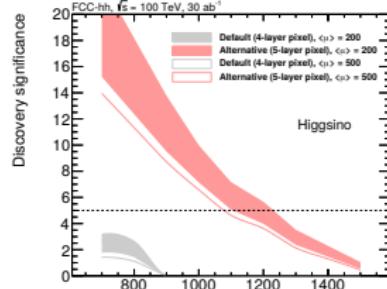
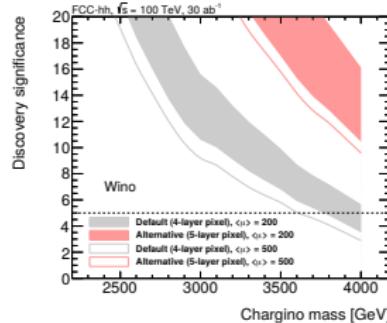
- The “Disappearing tracks” was done by FCChh (in the CDR)
  - FCChh-detector
  - FCChh-ish PU (but still too small: 500 vs. CDR number 955)
  - Assumes **only SM loops** for mass-splitting, i.e. not SUSY mixing: The “other two” mass-parameters very large.
  - For higgsinos: Only just reaches  $2\sigma$
- A study of the “mono-X” method was done in arXiv:1805.00015, but it is too rudimentary in the experimental aspects to allow for any conclusions.



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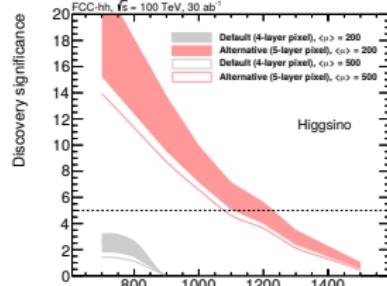
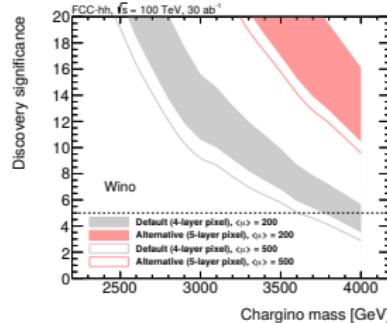
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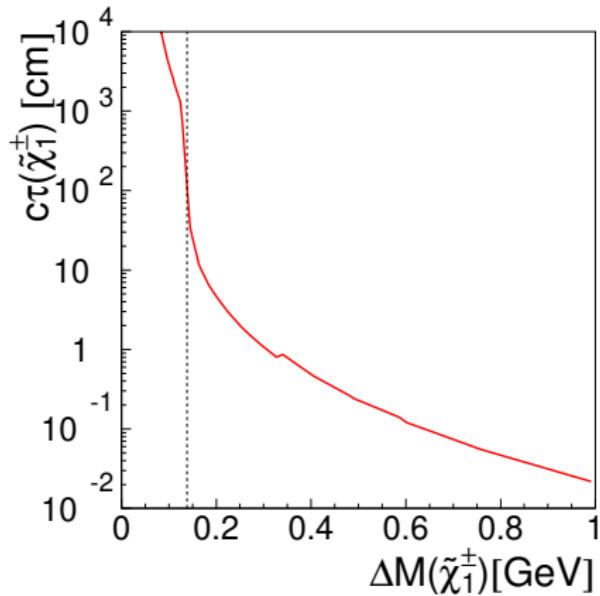
## Why is this important?

- Because  $c_\tau$  depends on  $\Delta(M)$ , and  $c_\tau$  needs to be macroscopic to get “Disappearing tracks”. Cf. ATLAS arXiv:1712.02118:  
 $c_\tau \gtrsim 6 \text{ cm}$  needed.
- So  $\Delta(M) \lesssim 500 \text{ MeV}$  needed.
- $\Delta(M)$  for Higgsino LSP
- ... and Wino LSP
- Conclusion: Not at all sure that that lifetime will be large. Good chances - no guarantee - for Wino, unlikely for Higgsino.

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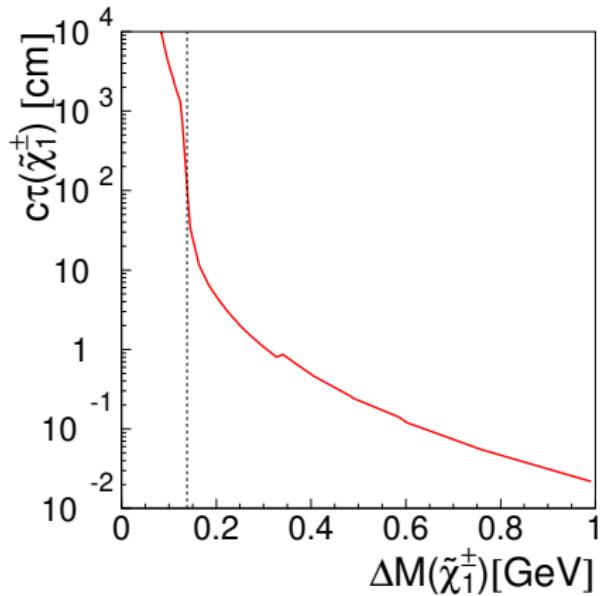
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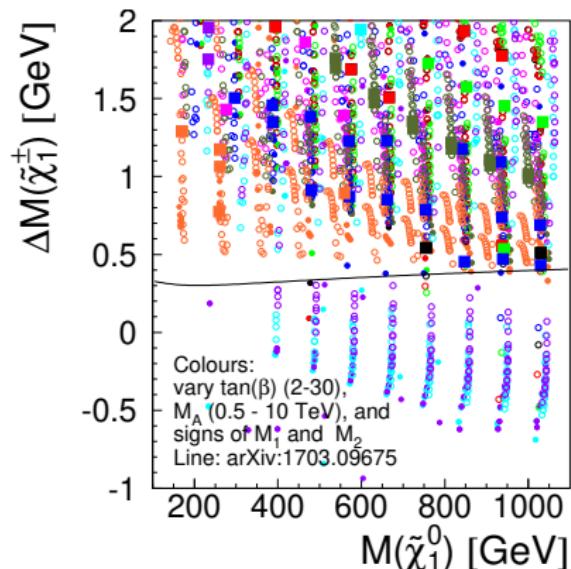
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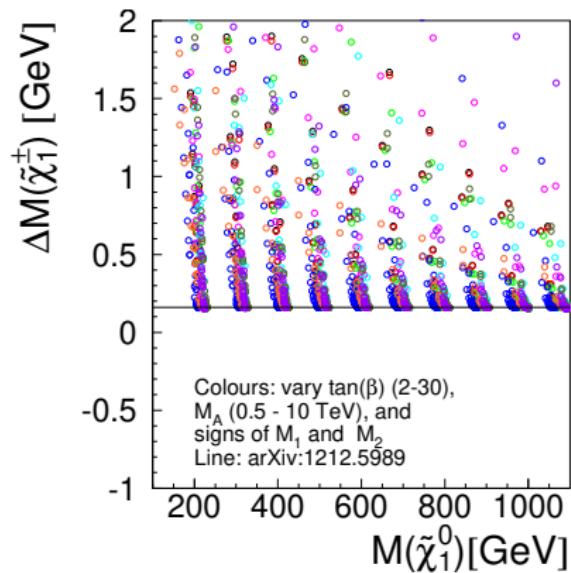


Lines are the “SM-loops only” predictions.

# Key element for “Disappearing tracks”: $\Delta(M)$

Why is this important?

- Because  $c_\tau$  depends on  $\Delta(M)$ , and  $c_\tau$  needs to be macroscopic to get “Disappearing tracks”. Cf. ATLAS arXiv:1712.02118:  $c_\tau \gtrsim 6 \text{ cm}$  needed.
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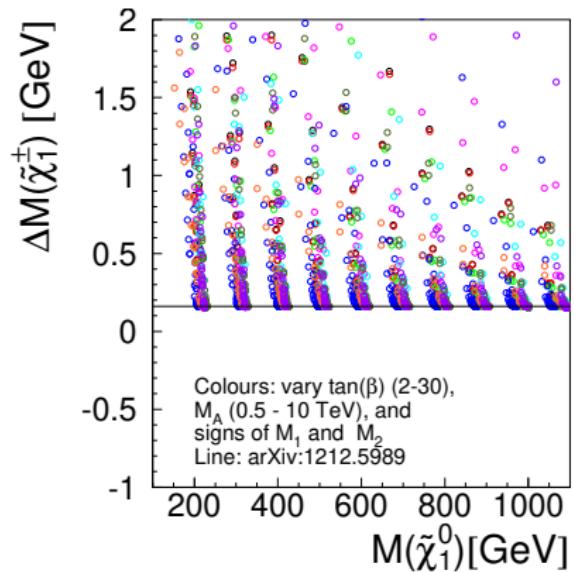


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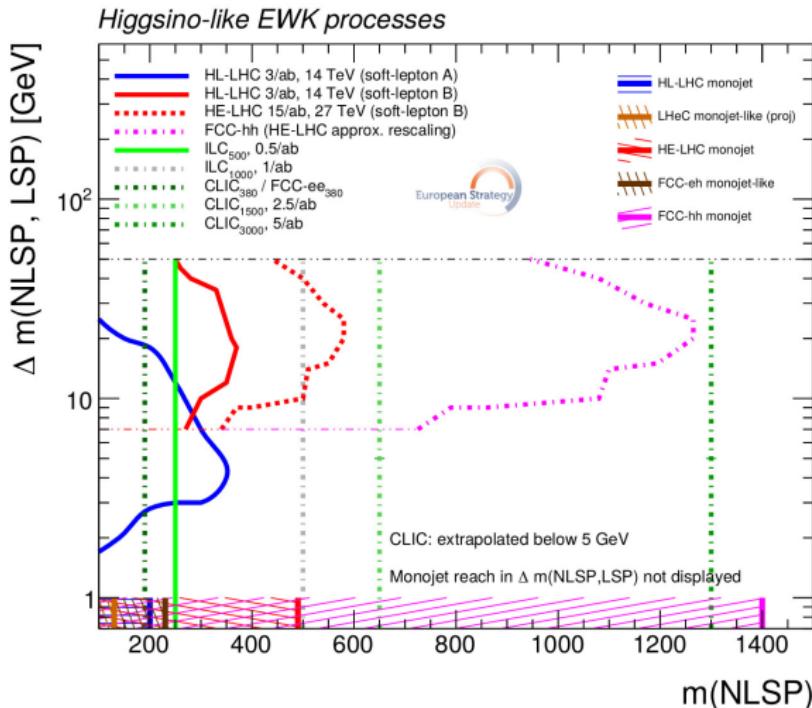
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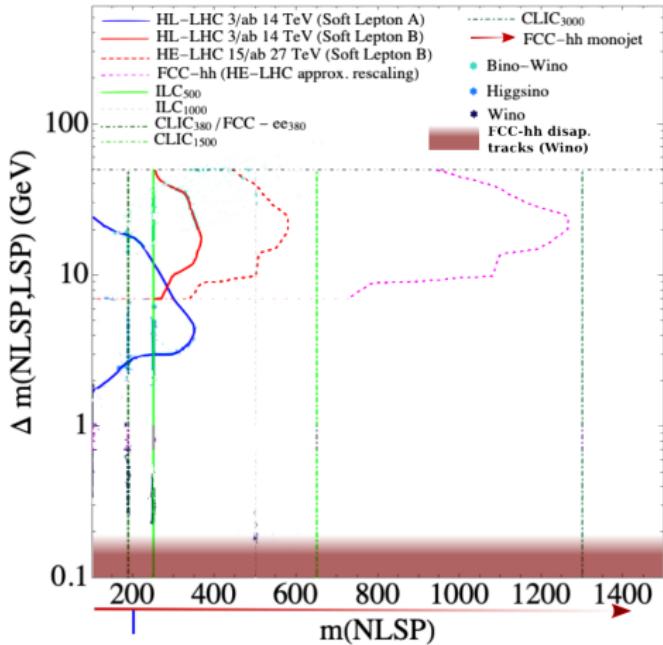
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# SUSY In The Briefing-book: Wino/Higgsino LSP

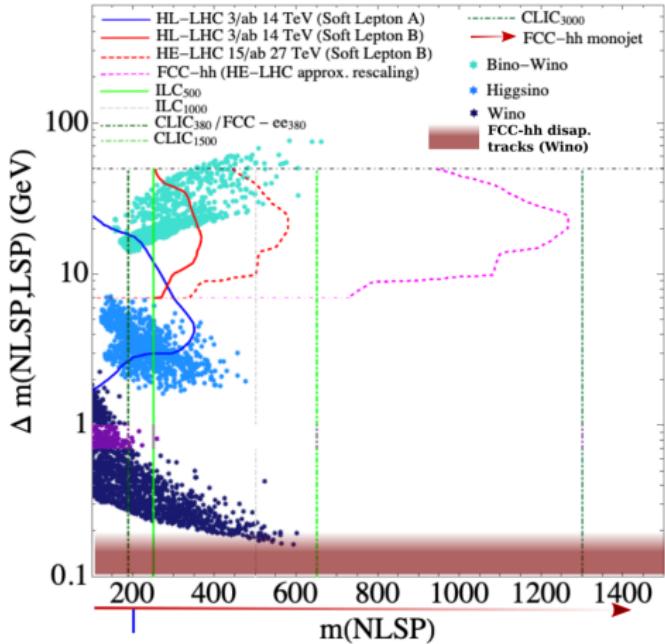


So: Disappearing tracks exclusion is actually off the scale !

# SUSY In The Briefing-book: Re-boot

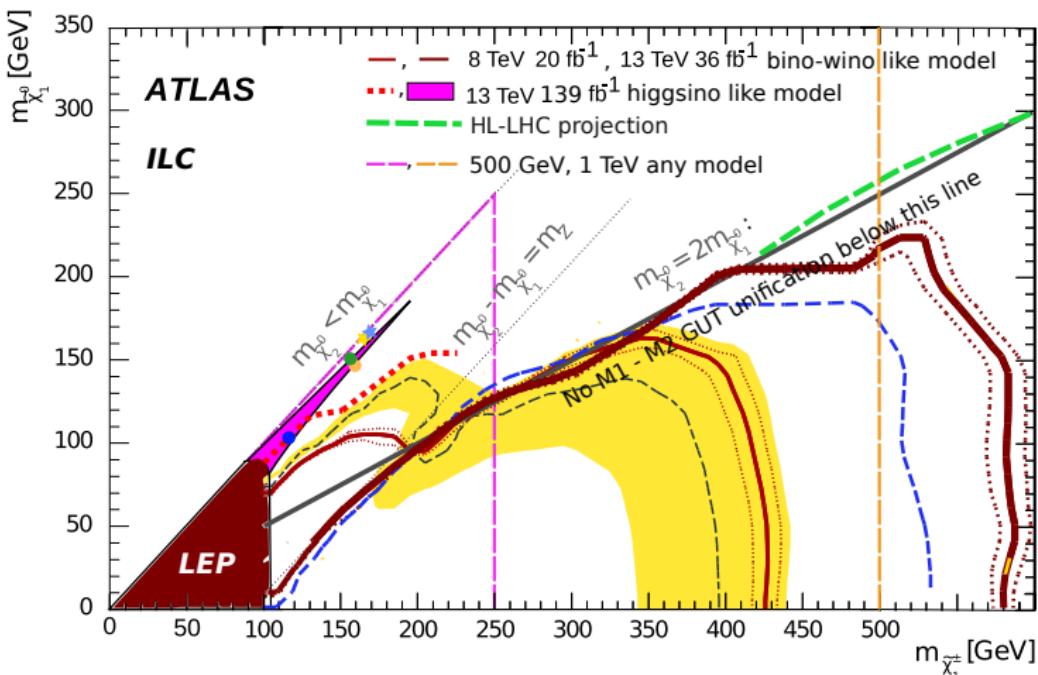


# SUSY In The Briefing-book: Re-boot



With models that are consistent with g-2 and no over-production of DM  
 From arXiv:2103.13403.

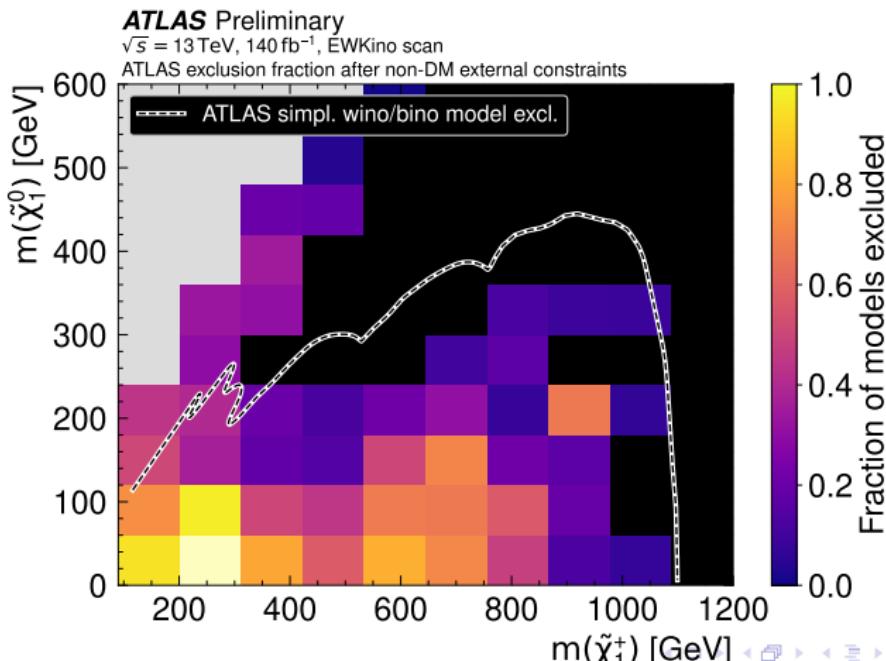
# Summary: SUSY - All-in-one



ATLAS Eur Phys J C 78, 995 (2018), Phys Rev D 101, 052002 (2020), arXiv:2106.01676;

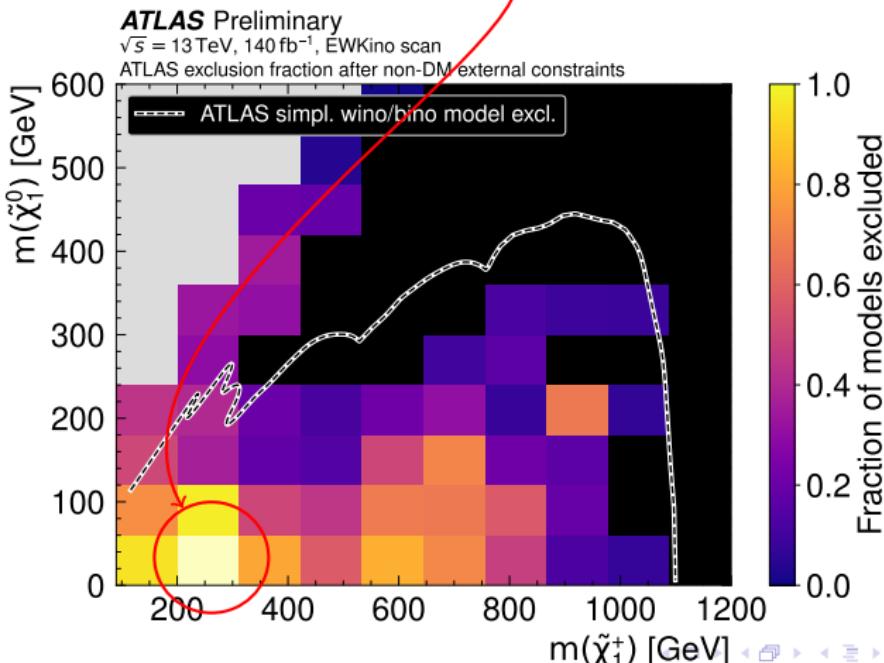
ATLAS HL-LHC ATL-PHYS-PUB-2018-048; ILC arXiv:2002.01239; LEP LEP LEPSUSYWG/02-04.1

# Hot off the press: ATLAS-CONF-2023-055: pMSSM-19 (-7) scan in $M_{LSP}$ vs. $M_{\tilde{\chi}_1^\pm}$



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Only this one is actually excluded !



# Conclusions

- SUSY is **not** excluded.
- Even Plain vanilla SUSY is **not** excluded.
- HL-LHC might well discover SUSY, because future pp machines have
  - discovery potential to very high masses
  - but - to put it bluntly - **NO** exclusion potential: there will always be loopholes.
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## Take-home message

- **Without a TeV scale lepton-collider**, we would not be able exclude SUSY further than today at the end of this century. **LEP2++ would be the final word.**
- Except if a future pp machine discovers SUSY, which is a **problem we'd like to have!**

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# Why the title ?!

# The Hunt-Lenox Globe (c:a 1510)



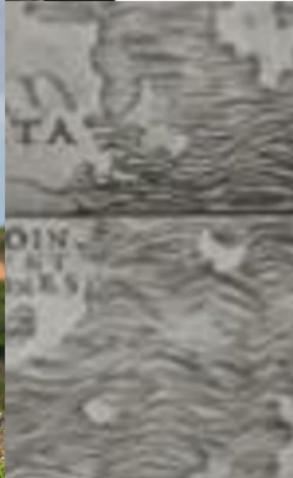
# Hic Sunt Dracones



# That is ~ here

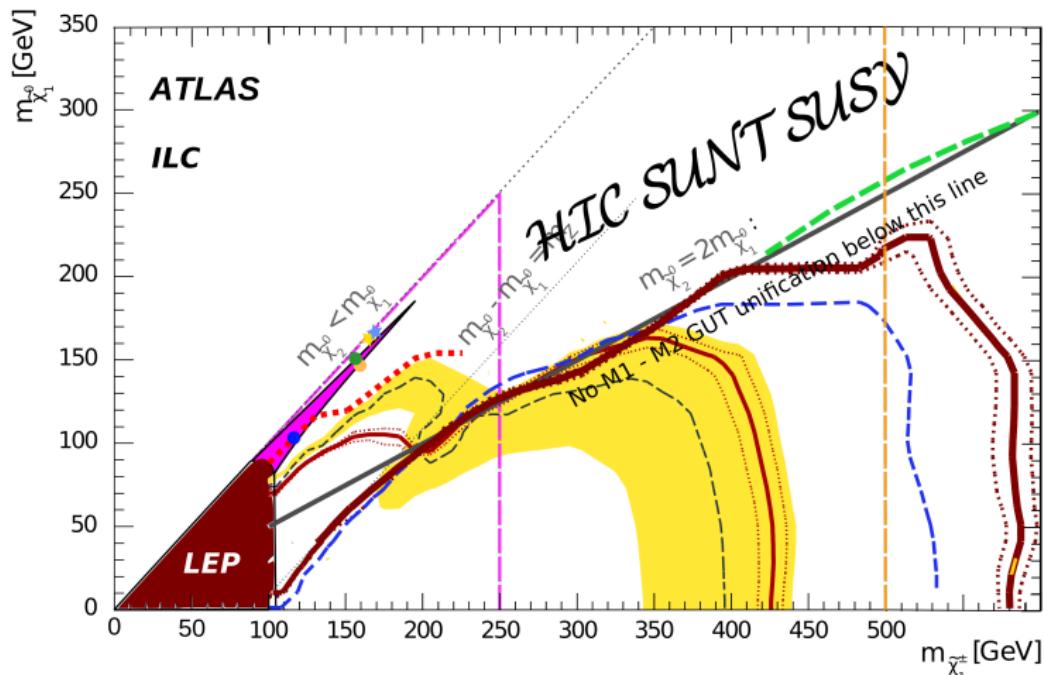


# Yes - there actually *were* dragons there !



So...

# Here be SUSY !

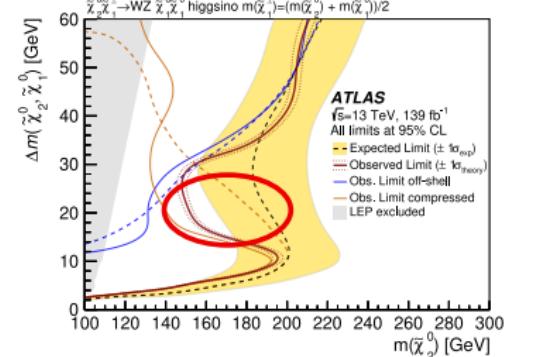
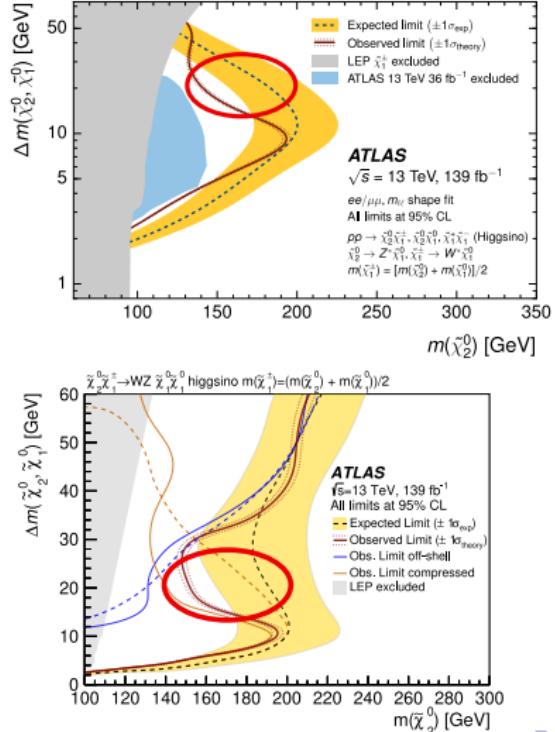
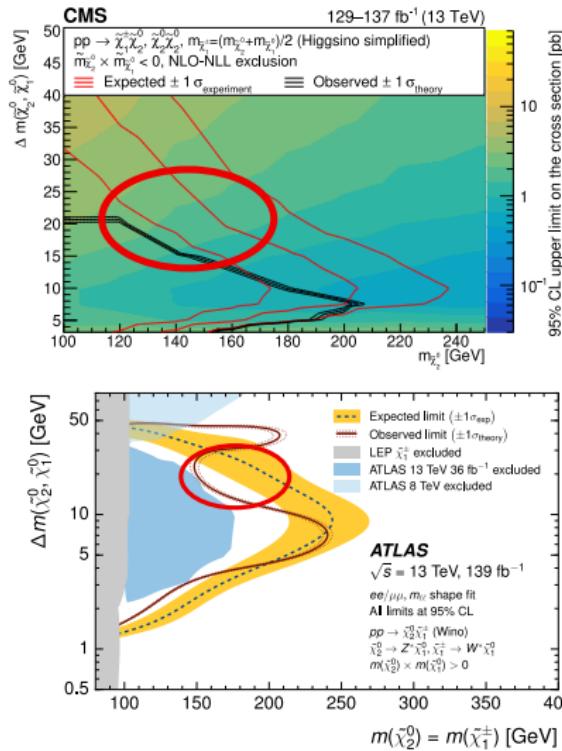


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# And...

# Maybe we start to see the breath of the dragon (latest LHC results...)



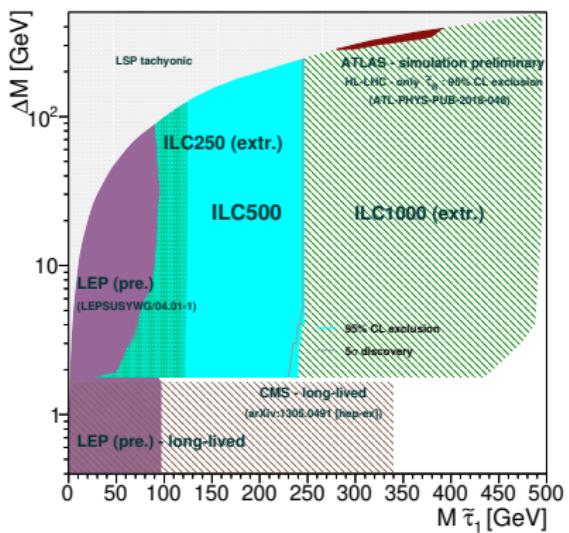
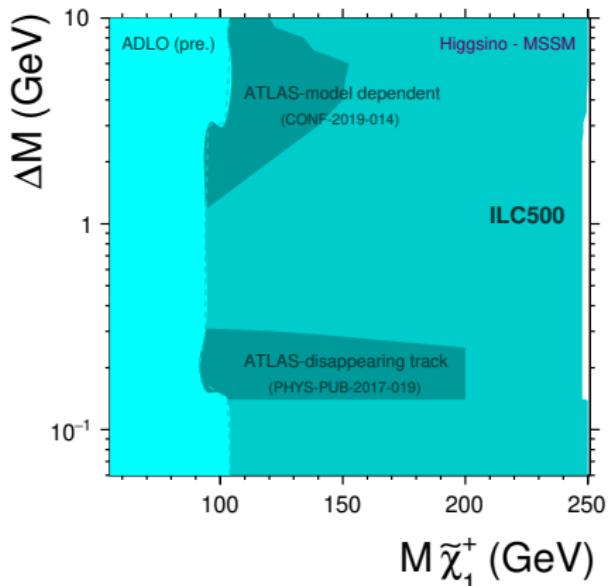
# Thank You !

BACKUP

# BACKUP SLIDES

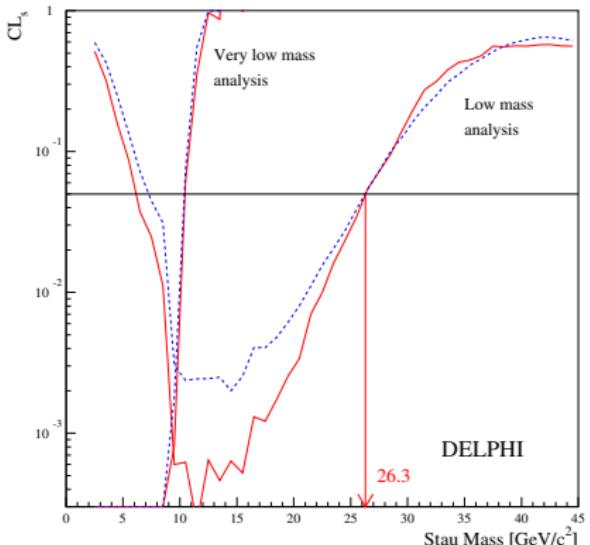
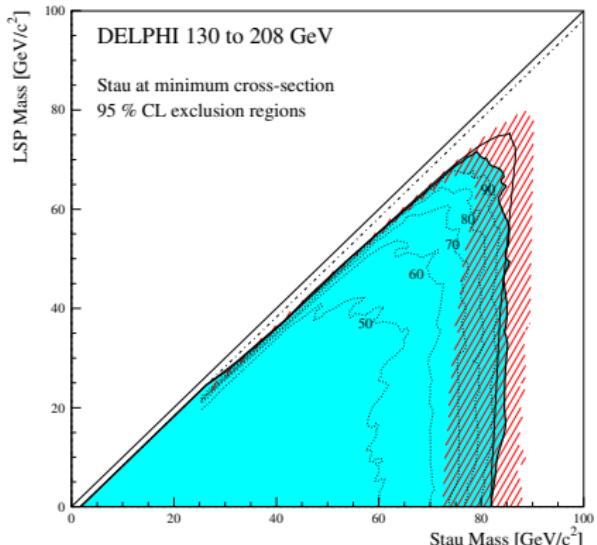
# ILC projection on Higgsinos and $\tilde{\tau}$ :s

From arXiv:2002.01239



From arXiv:2105.08616

# In real life: LEP $\tilde{\tau}$ limits



NB: a  $\tilde{\tau}$  as light as 26.3 GeV is *not* excluded!

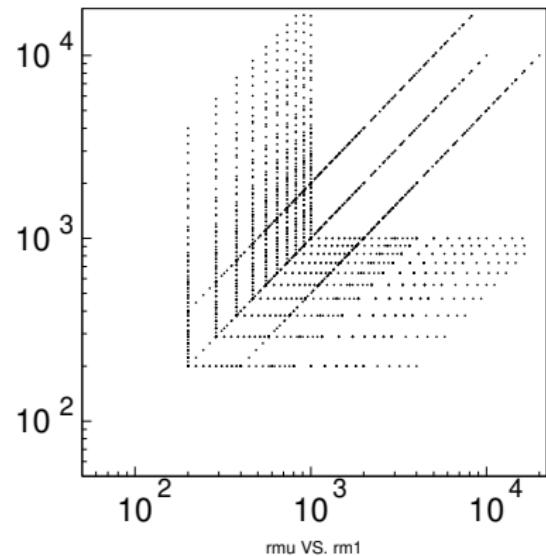
# The cube

Specifically, like this:

- $\mu$  vs.  $M_1$
- $\mu$  vs.  $M_2$
- $M_1$  vs.  $M_2$

Use SPheno 4.0.3 to calculate spectra and BR:s

Use Whizard 2.8.0 for cross-sections



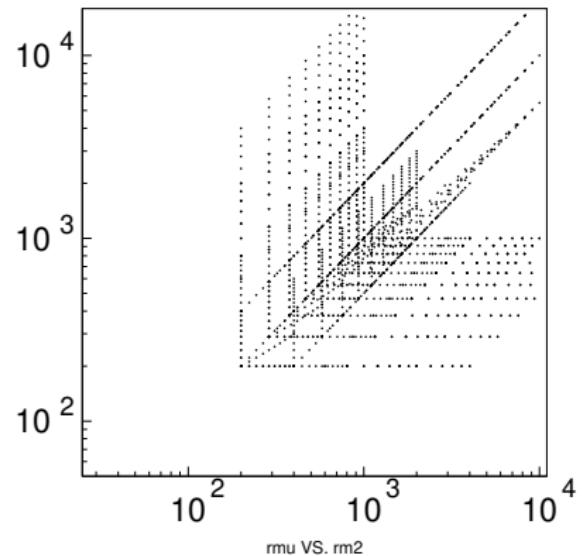
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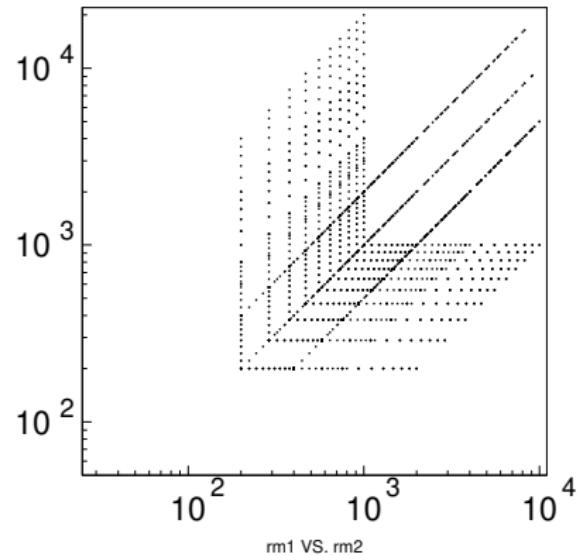
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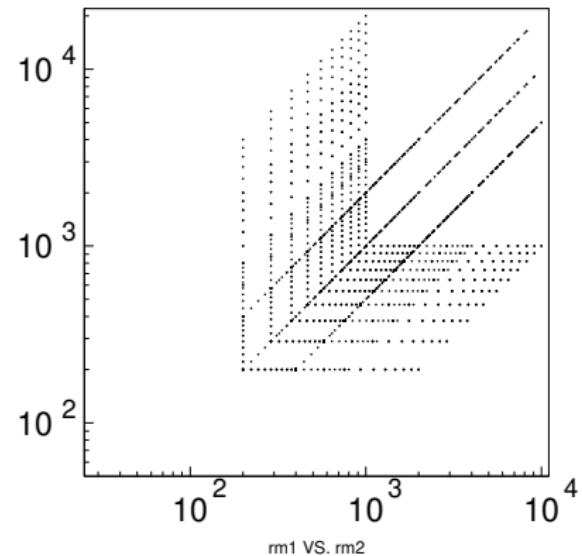
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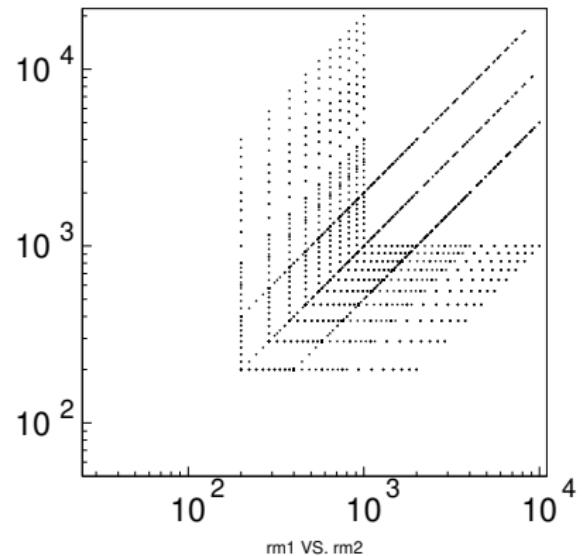
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What happens with spectra,  
cross-sections, BRs when  
exploiting this “cube”?

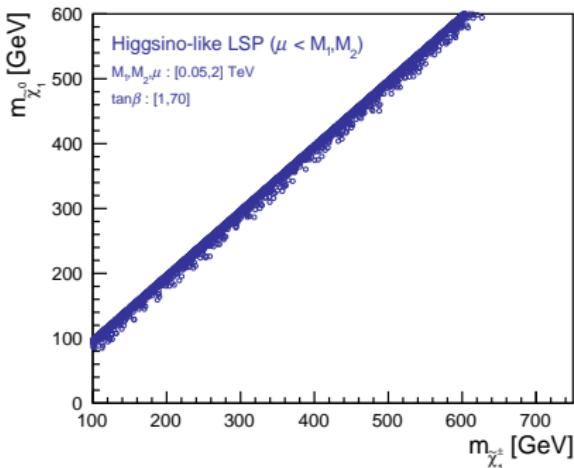


## Why compressed spectra ? Natural SUSY: Light, degenerate higgsinos

Why would one expect the spectrum to be compressed ?

- Natural SUSY:
    - $m_Z^2 = 2 \frac{m_{H_u}^2 \tan^2 \beta - m_{H_d}^2}{1 - \tan^2 \beta}$
    - $\Rightarrow$  Low fine-tuning  $\Rightarrow$   
 $\mu = \mathcal{O}(\text{weak scale})$ .
  - Wino-like LSP: Same conclusion.
  - Only for Bino-like LSP, non-compressed occurs
  - But also: the data ...

quite generic:  
Parameter-scan by T. Tanabe:



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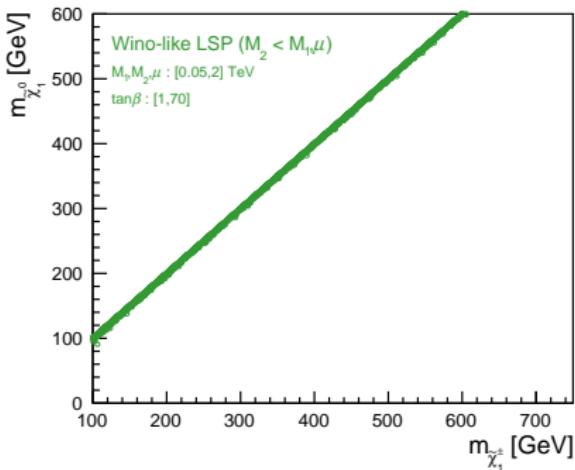
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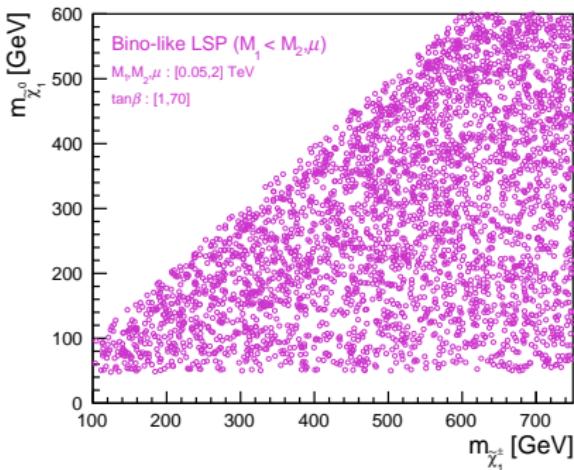
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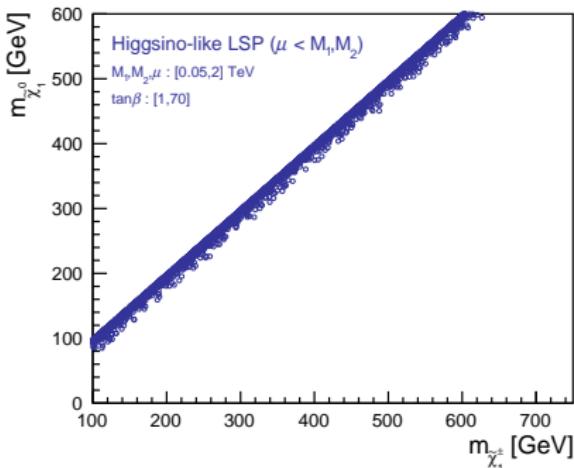
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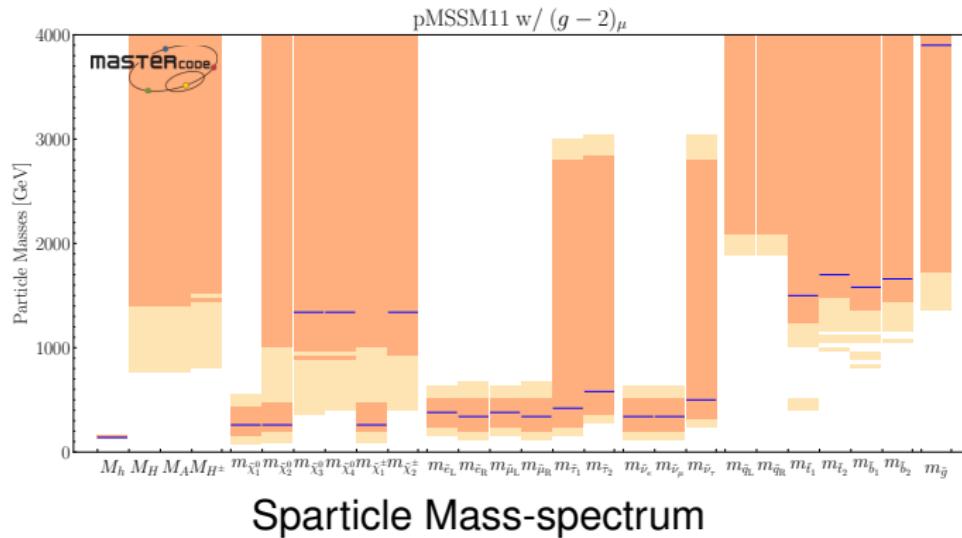
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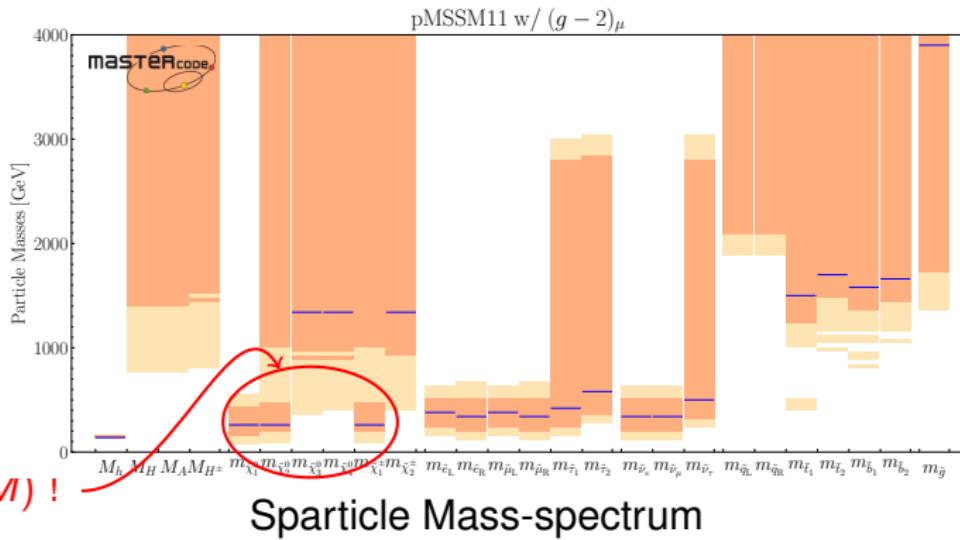
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 (arXiv:1710.11091):



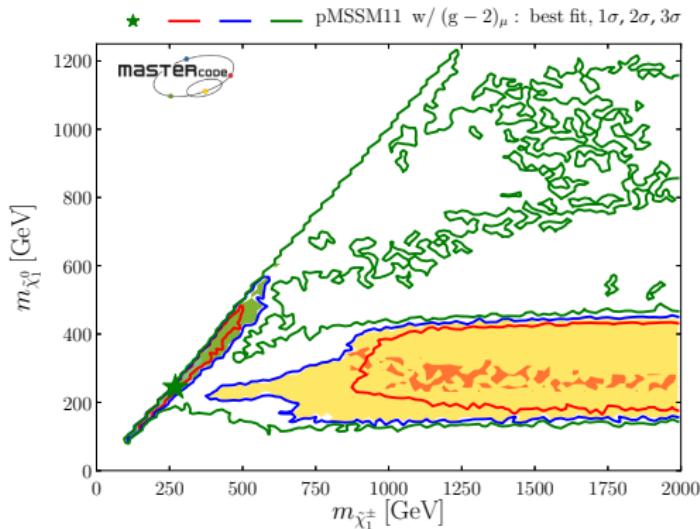
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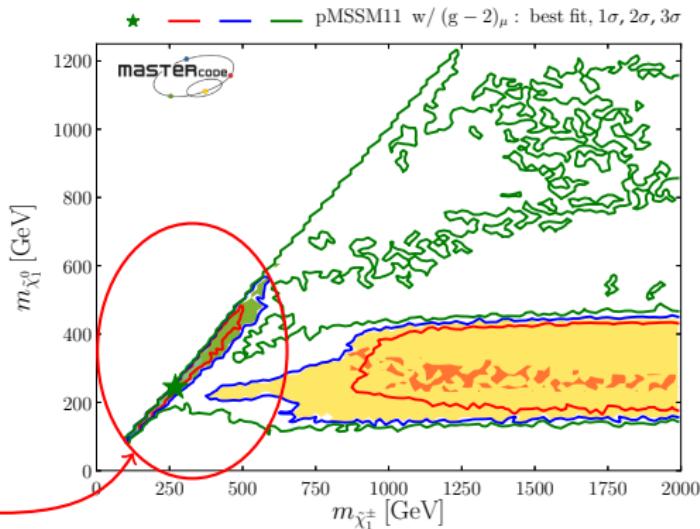
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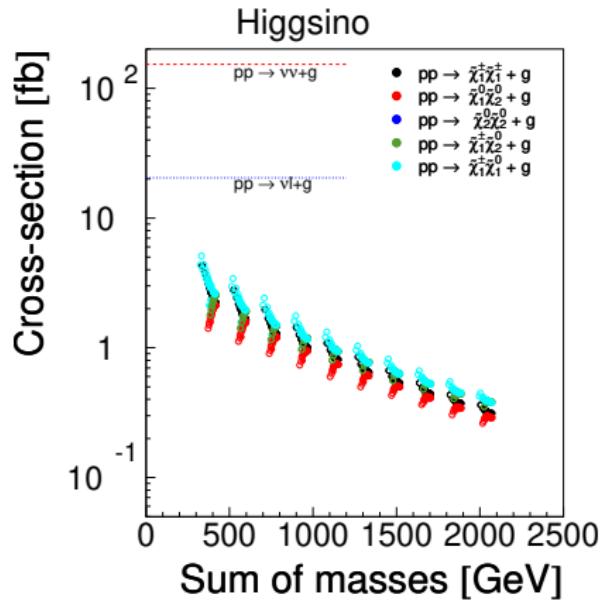
Low  $\Delta(M)$  !

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# SUSY cross-sections at FCChh

Variation of cross-section for  $pp \rightarrow$  uncoloured bosinos + gluon  
(CTEQ6L1 pdfs)

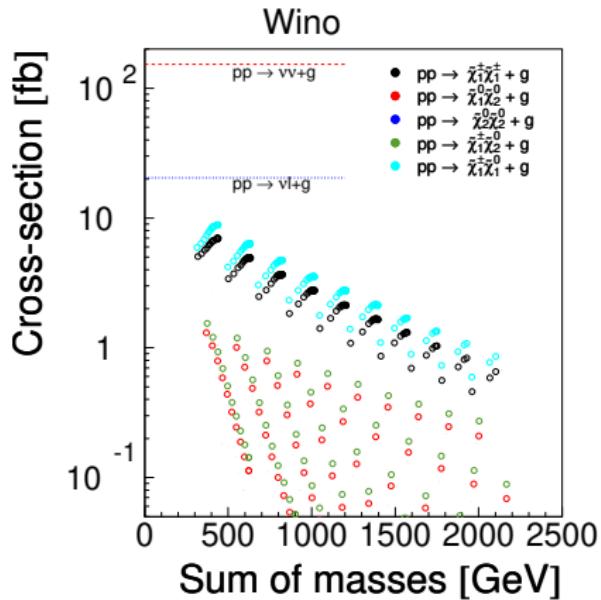
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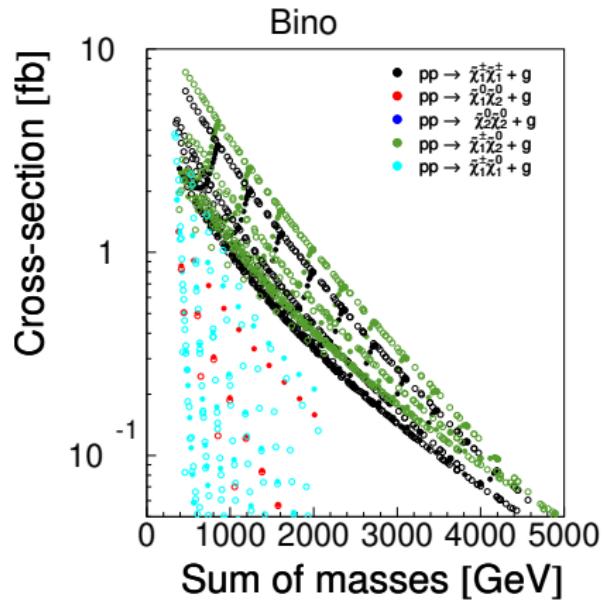
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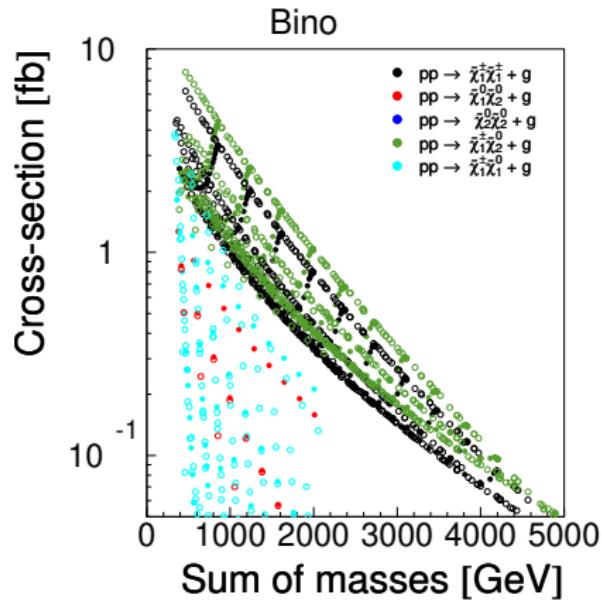
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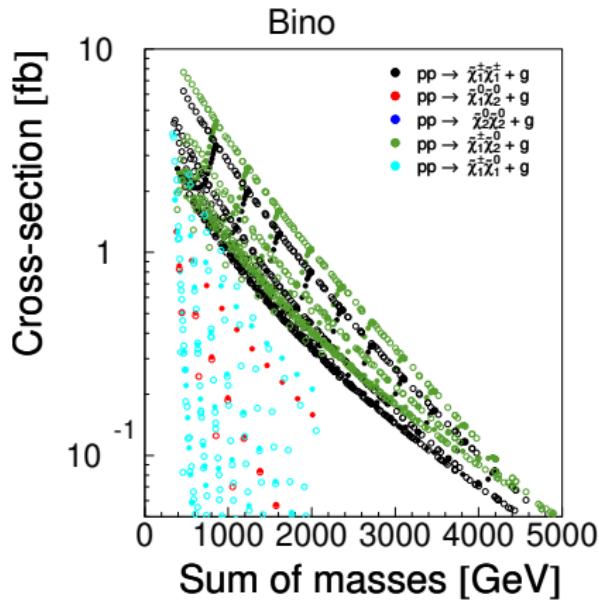
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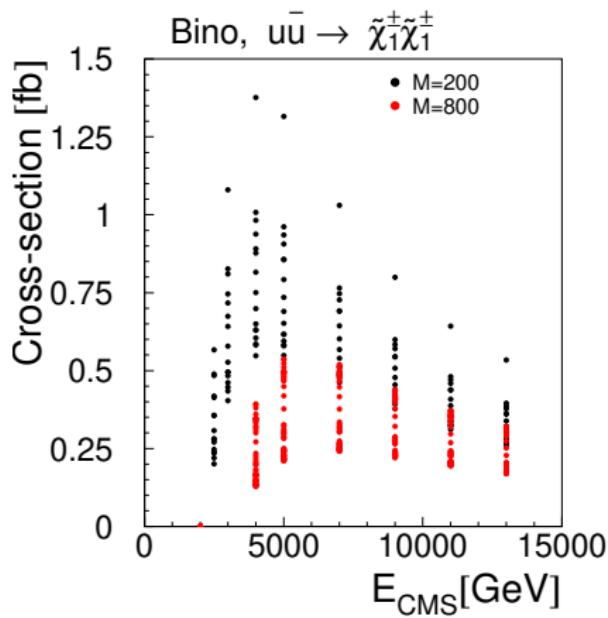
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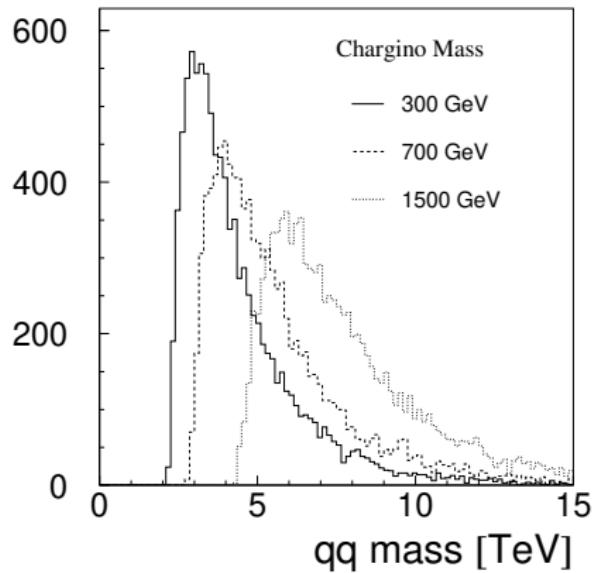
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- Consider *fixed*  $m_{qq}$ , at two masses: First rise w/  $\beta$ , then fall-off w/  $1/s$ .
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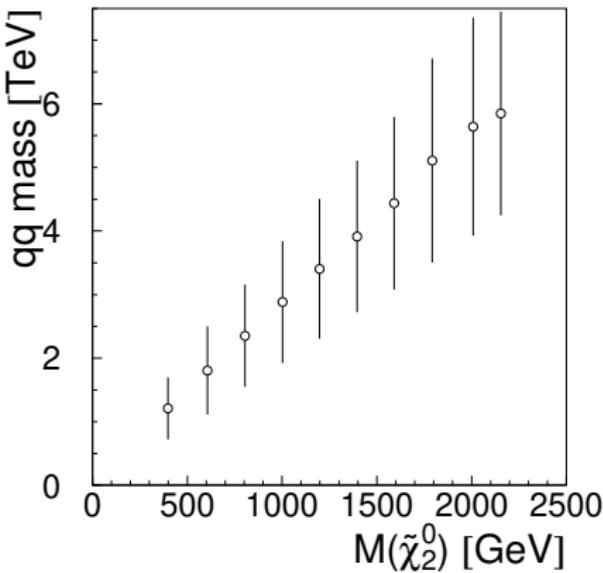
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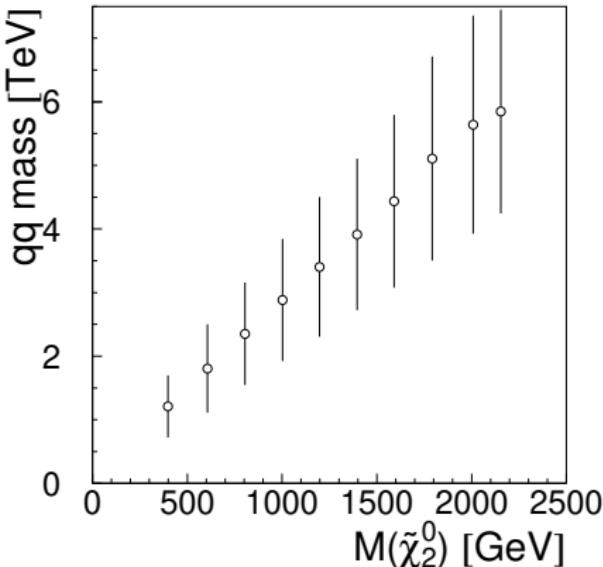
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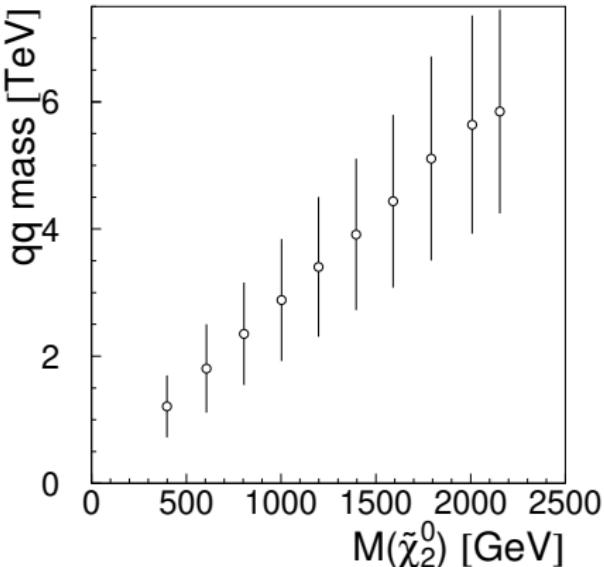
# SUSY cross-sections at FCChh: Why exponential fall-off

- $m_{qq}$  (linear) function of bosino-mass
- At these mass-ratios, missing  $p_T$  is proportional to  $m_{qq}$
- $\Rightarrow$  missing  $p_T$  increases linearly with bosino-mass.
- $\Rightarrow$  can increase missing  $p_T$ -cut linearly when looking for higher masses, with the same efficiency
- Then the background decreases as much.
- S/B remains constant along lines in  $M_{\tilde{\chi}_1^\pm}$  vs.  $M_{LSP}$



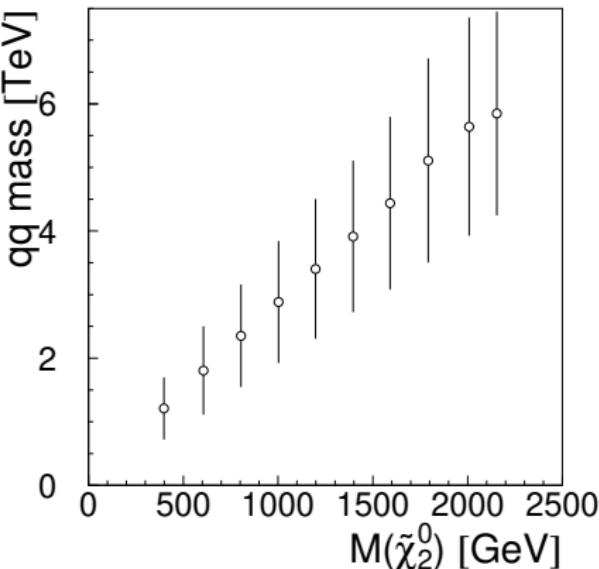
# SUSY cross-sections at FCChh: Why exponential fall-off

- $m_{qq}$  (linear) function of bosino-mass
- At these mass-ratios, missing  $p_T$  is proportional to  $m_{qq}$
- $\Rightarrow$  missing  $p_T$  increases linearly with bosino-mass.
- $\Rightarrow$  can increase missing  $p_T$ -cut linearly when looking for higher masses, with the same efficiency
- Then the background decreases as much.
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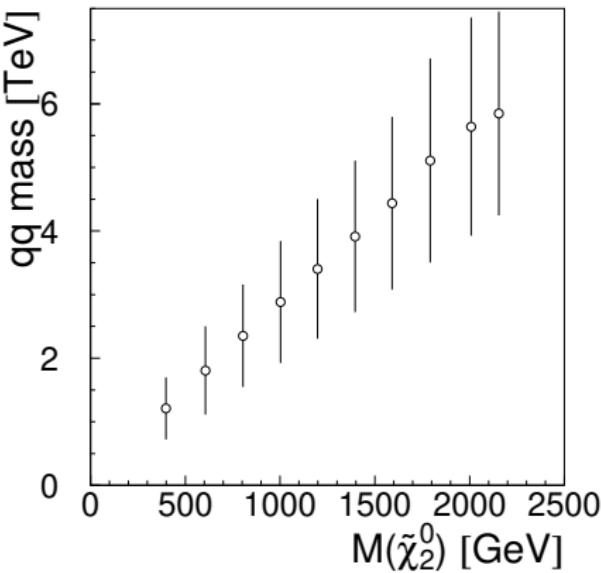
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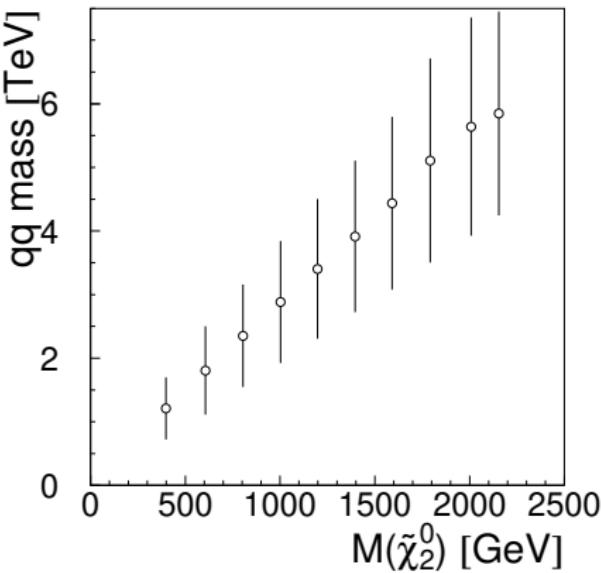
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## Uptake

Expect that the limit sticks to the **same diagonal** as energy is increased.

- Then the background decreases as much.
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# Key element for “Disappearing tracks”: $c\tau$

## Why is this important?

- $c\tau$  needs to be macroscopic to get “Disappearing tracks”. Cf. ATLAS arXiv:1712.02118:  
 $c\tau \gtrsim 6$  cm needed.
- $c\tau$  for Higgsino LSP
- ... and Wino LSP
- Conclusion: Not at all sure that that lifetime will be large. Good chances - no guarantee - for Wino, unlikely for Higgsino.

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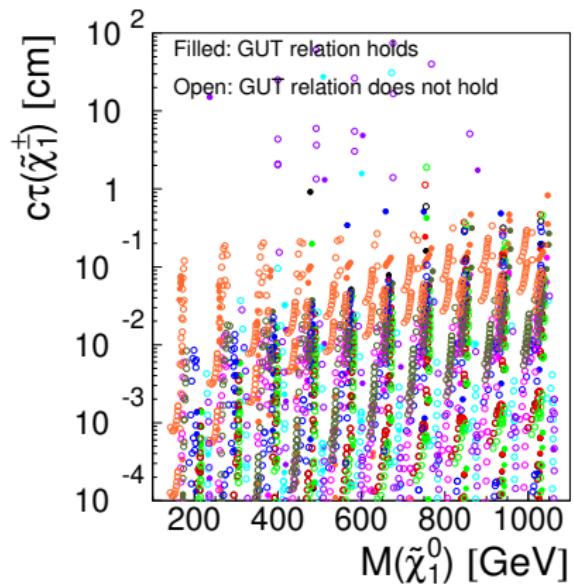
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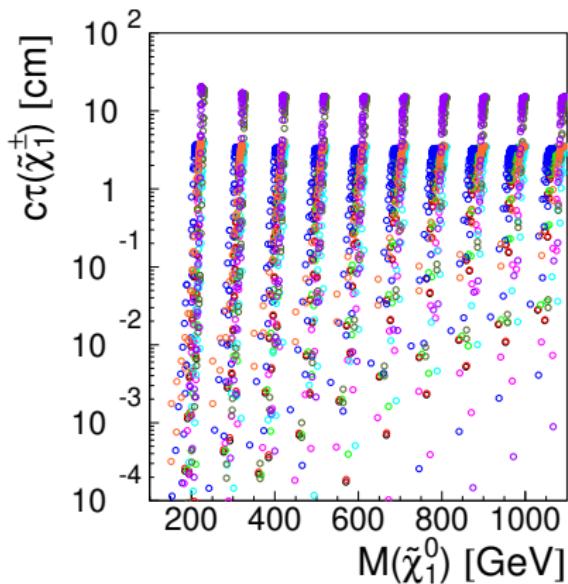
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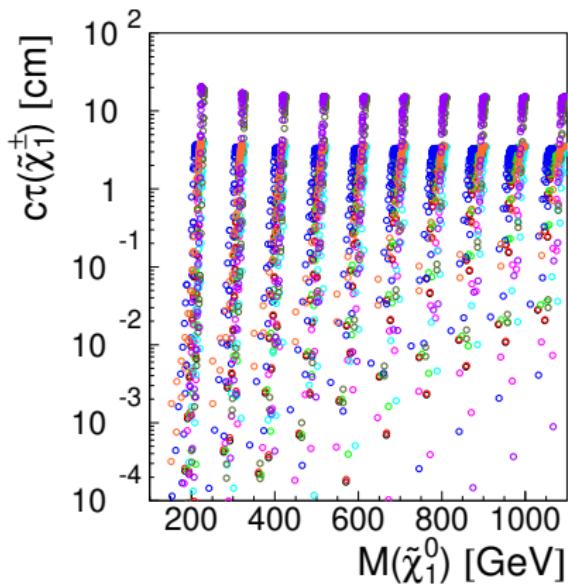
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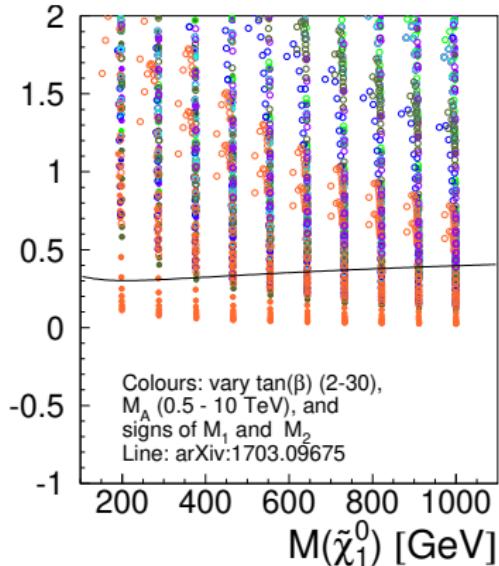
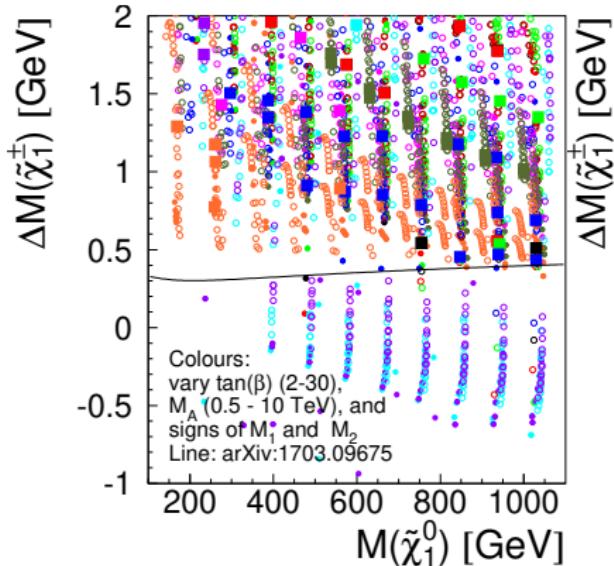
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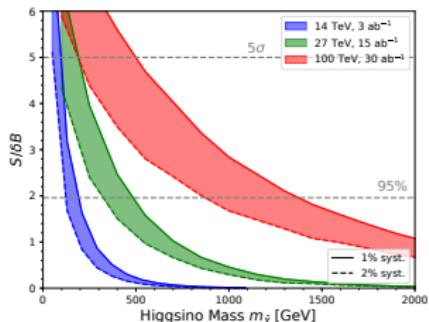
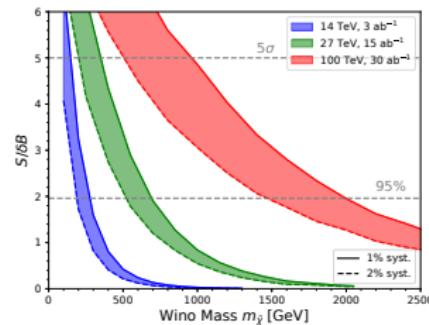


# second opinion on Higgsino $\Delta(M)$ : feynhiggs



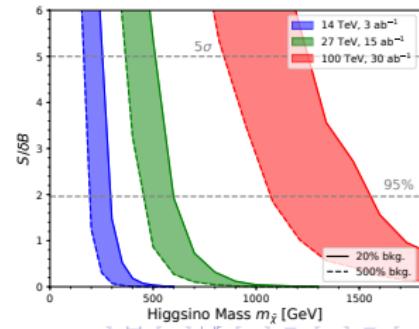
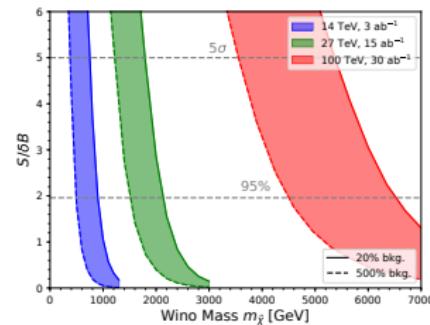
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