

# $\tilde{\tau}$ searches at future $e^+e^-$ colliders

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- Introduction
- $\tilde{\tau}$ 's at future  $e^+e^-$  colliders
- ILD full simulation analysis
- Impact of ILD/ILC specific features
- Conclusions

Second ECFA Workshop on  $e^+e^-$  Higgs/Top/EW Factories  
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# Introduction:

## SUSY at future $e^+e^-$ Higgs/EW/Tops factories

Supersymmetry is the most complete BSM theory, and ...

... boilerplate for BSM (almost any new topology can be obtained in SUSY)

Excellent scenarios for SUSY searches

Wrt. previous electron-positron colliders:

- increased **luminosity** and centre-of-mass **energy**
- beam **polarisation**
- improved **detector technologies**
- microscopic **beam-spot**

Wrt. hadron colliders:

- cleaner **environment**
- known **initial state**
- **triggerless operation** of the detectors
- **hermetic** detectors

# Introduction:

## SUSY at future $e^+e^-$ Higgs/EW/Tops factories (ctd.)

- Naturalness, the hierarchy problem, the nature of DM, or the measured magnetic moment of the muon **prefer a light electroweak sector** of SUSY
- **Many models** and the **global set of constraints** from observation **point to a compressed spectrum**

**Future  $e^+e^-$  colliders are well adapted to well motivated, and very challenging for hadron colliders, SUSY scenarios**

- **energies** from 90 GeV to 3 TeV, with typically a first run at 240/250 GeV
- both/one/none of the beams **polarised**
- **clean** or very clean conditions
- **hermeticity** excellent for some (down to  $\sim 6$  mrad), still good for others (down to  $\sim 50$  mrad)

# Introduction: Motivation for $\tilde{\tau}$ searches

Searching SUSY focused on best motivated NLSP candidates and most difficult scenarios

$\tilde{\tau}$  satisfies both conditions

Scalar superpartner of  $\tau$ -lepton

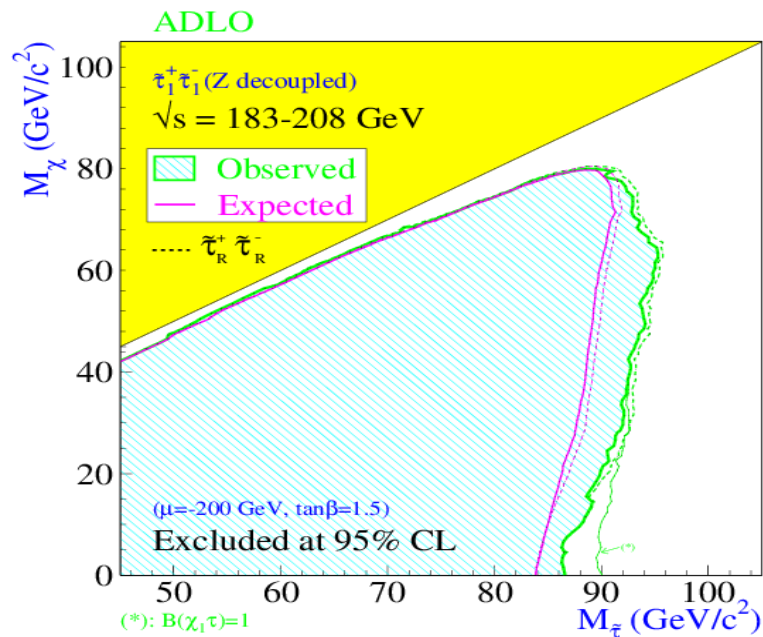
- Two weak hypercharge eigenstates ( $\tilde{\tau}_R, \tilde{\tau}_L$ ) not mass degenerate
- Mixing yields to the physical states ( $\tilde{\tau}_1, \tilde{\tau}_2$ ), the lightest one being with high probability the **lightest sfermion** (stronger trilinear couplings)
- With assumed R-parity conservation:
  - pair produced (s-channel via  $Z^0/\gamma$  exchange, **low**  $\sigma$  since  $\tilde{\tau}$ -mixing suppresses coupling to the  $Z^0$ )
  - decay to LSP and  $\tau$ , implying **more difficult signal identification** than the other sfermions

SUSY models with a light  $\tilde{\tau}$  can accommodate the observed relic density ( $\tilde{\tau}$  - neutralino coannihilation)

# Introduction: Limits at LEP and LHC/HL-LHC

## $\tilde{\tau}$ searches at LEP

Valid for any mixing and any values of the not shown parameters



- $\sqrt{s} = 183-208$  GeV
- **Combined four LEP experiments data**

LEPSUSYWG/04-01.1

Main limitations for LEP searches are energy, luminosity and trigger

According to PDG, most solid limit on  $\tilde{\tau}$  mass comes from DELPHI and is set to 81.9 GeV (valid for any mixing if  $DM > 15$  GeV)

DELPHI suppresses  $\tilde{\tau}$  masses below 26.3 for any mixing and mass difference

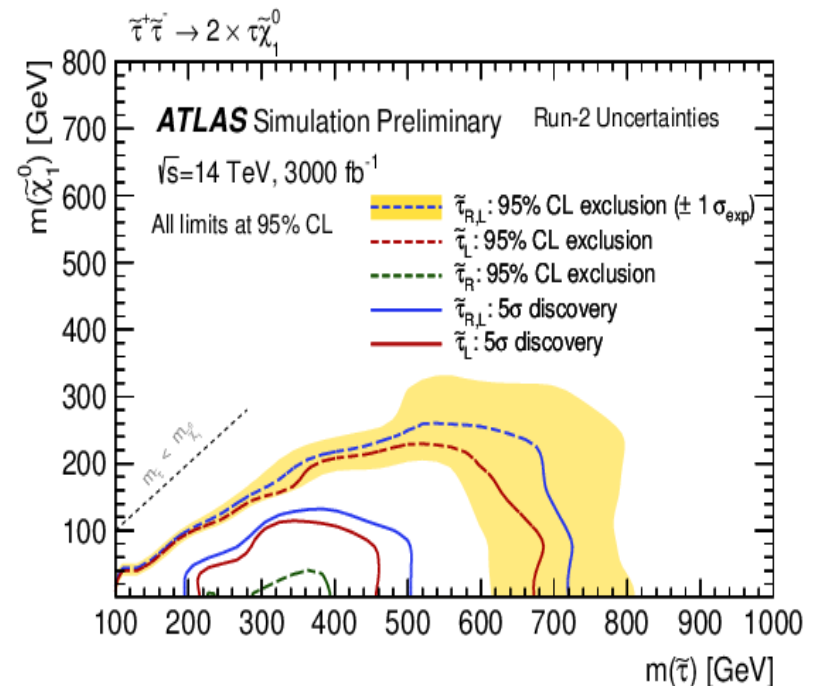
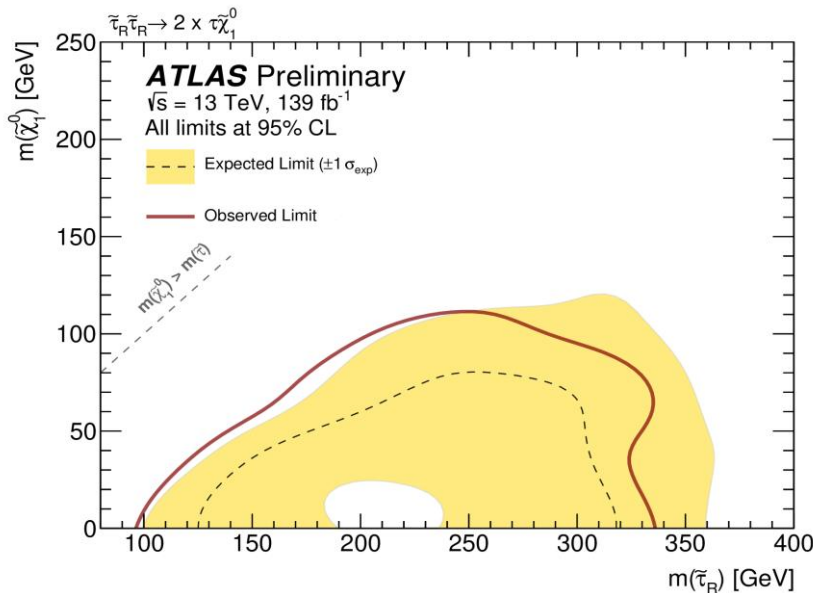
# Introduction: Limits at LEP and LHC/HL-LHC (ctd.)

Assume  $\tilde{\tau}_R$  and  $\tilde{\tau}_L$  to be mass degenerated and not mixing

$\tilde{\tau}$  prospects at HL-LHC

First  $\tilde{\tau}_R$  limits at LHC

ATLAS-CONF-2023-029



No discovery potential for  $\tilde{\tau}$  coannihilation scenarios or  $\tilde{\tau}_R$  pair production

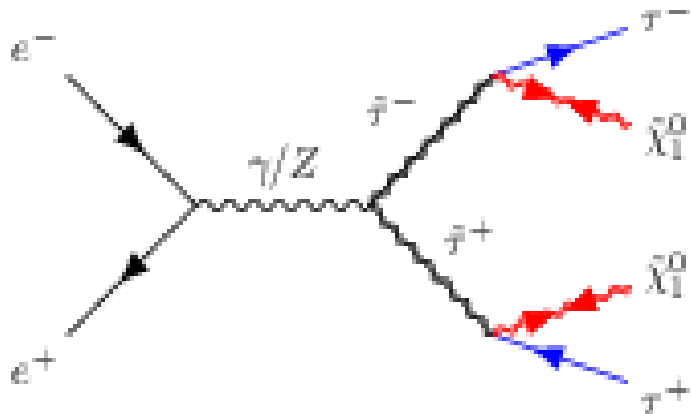
$M_{\tilde{\tau}} - M_{\text{LSP}} > 120 \text{ GeV}$

ATL-PHYS-PUB-2018-048

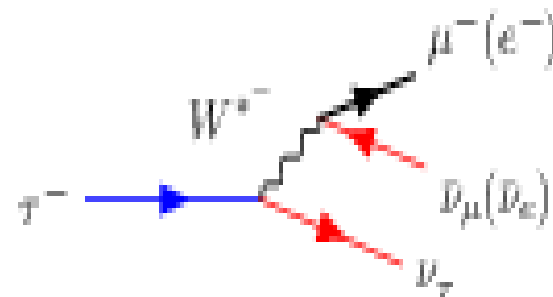


# $\tilde{\tau}$ 's at future $e^+e^-$ colliders: production & decay

s-channel production



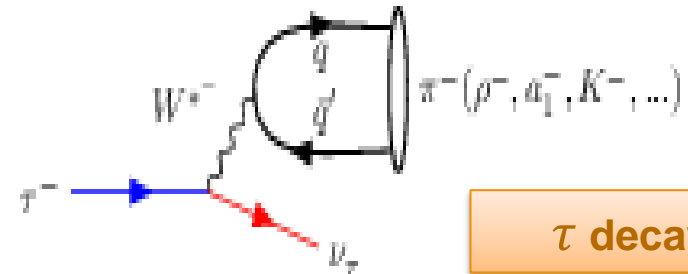
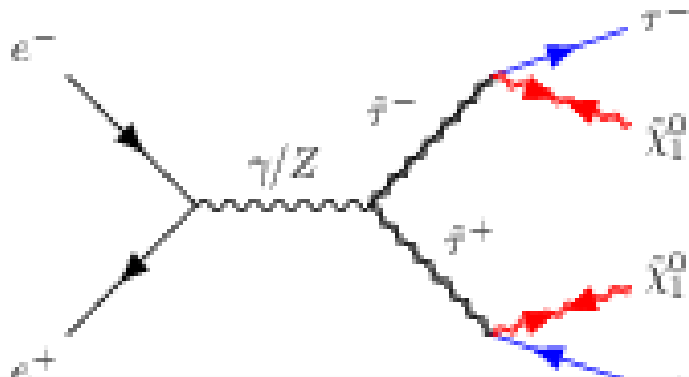
$\tau$  decays



Signal events with the (visible) decay products of two  $\tau$ 's being the only detectable activity

# $\tilde{\tau}$ 's at future $e^+e^-$ colliders: production & decay(ctd.)

## s-channel production



## $\tau$ decays



## Signature:

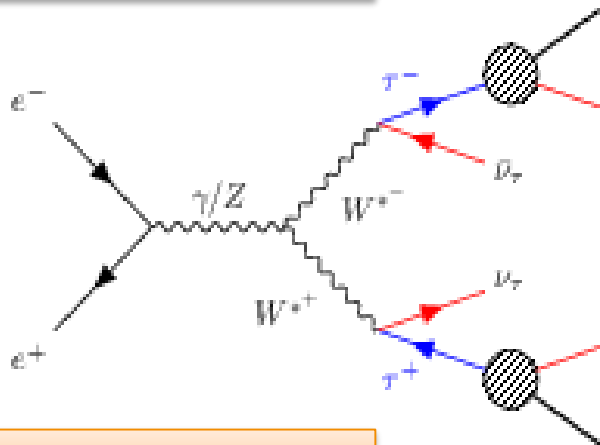
- large missing energy and momentum
- large fraction of detected activity in central detector (isotropic production of scalar particles)
- large angle between the two  $\tau$ -lepton directions
- unbalanced transverse momentum
- zero forward-backward asymmetry



# $\tilde{\tau}$ 's at future $e^+e^-$ colliders: backgrounds

## SM processes with real or fake missing energy

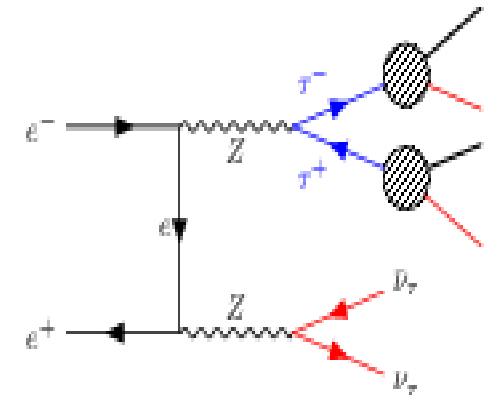
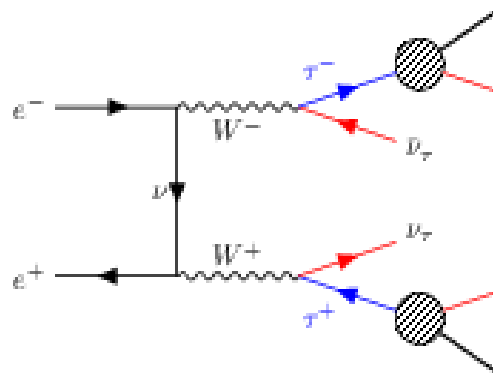
### Irreducible



### Almost irreducible

- $ee \rightarrow \tau\tau$ ,  $ZZ \rightarrow \nu\nu ll$ ,  $WW \rightarrow l\nu l\nu$  ( $l = e$  or  $\mu$ )
- $ee \rightarrow \tau\tau + \text{ISR}$ ,  $ee \rightarrow \tau\tau ee$ ,  $\gamma\gamma \rightarrow \tau\tau$

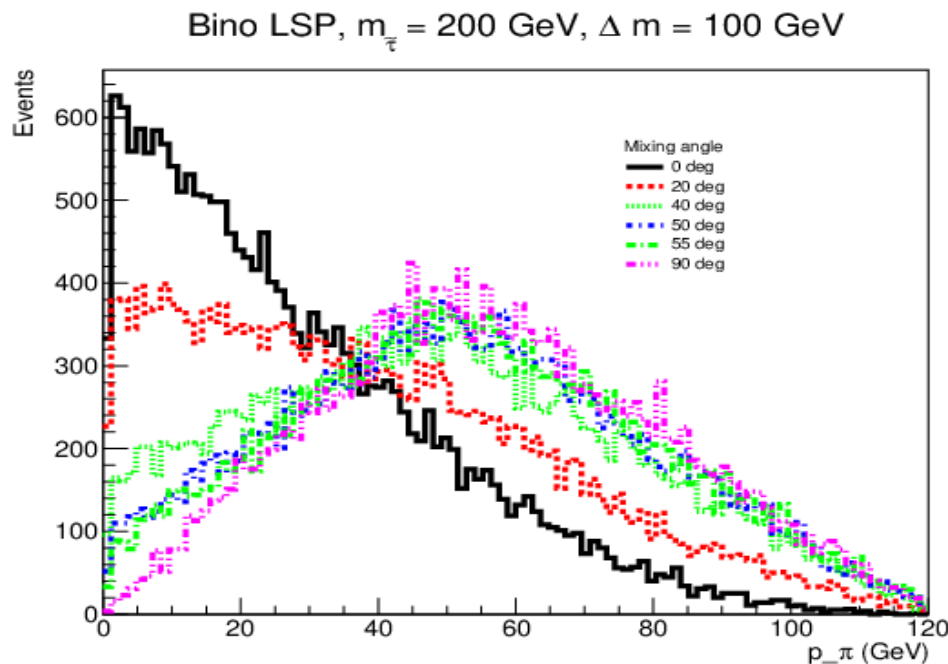
### 4-fermion production with two of the fermions being neutrinos and two $\tau$ 's



### Mis-identification of $\tau$ 's or of missing momentum

# $\tilde{\tau}$ 's at future $e^+e^-$ colliders: impact of mixing and LSP nature

## Impact on signal efficiency



- **Signal efficiency** depends on spectrum of detectable  $\tau$  decays
- **Spectrum of  $\tau$  decay products** depends on  $\tau$  polarisation
- $\tau$  polarisation depends on  $\tilde{\tau}$  and **LSP mixing angles**

Higgsino changes chirality but Bino does not

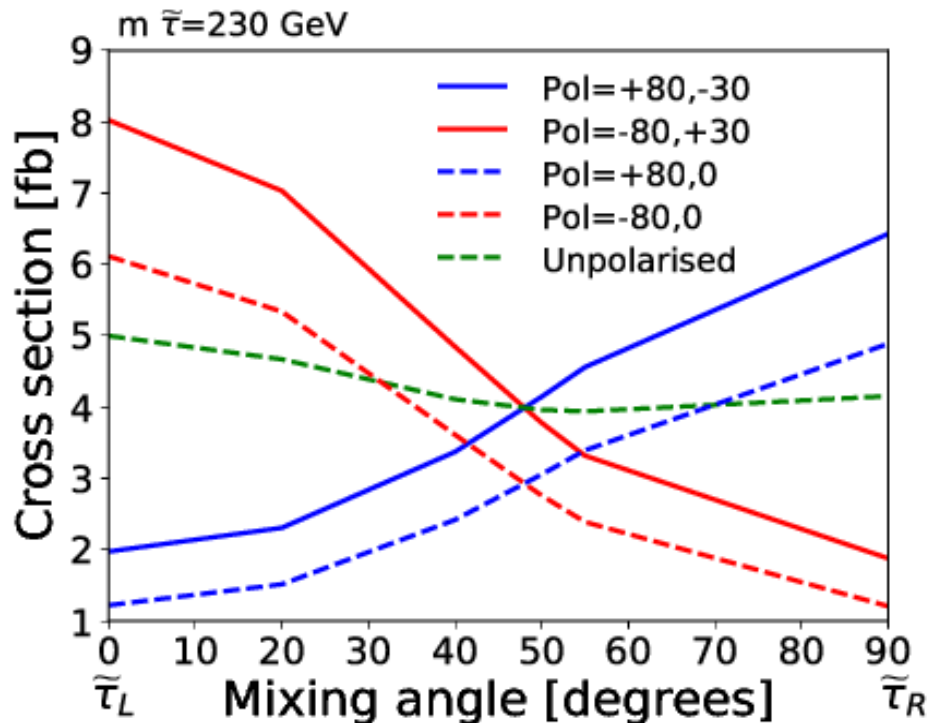
$\tilde{\tau}_L$  + Bino LSP ( $\tilde{\tau}_R$  + Higgsino LSP) softer visible decay products

# $\tilde{\tau}$ 's at future $e^+e^-$ colliders:

## impact of mixing and LSP nature (ctd.)

### Search for “worst” scenario

53 degrees  $\tilde{\tau}$  mixing angle corresponds to the worst case for (unpolarized) LEP conditions



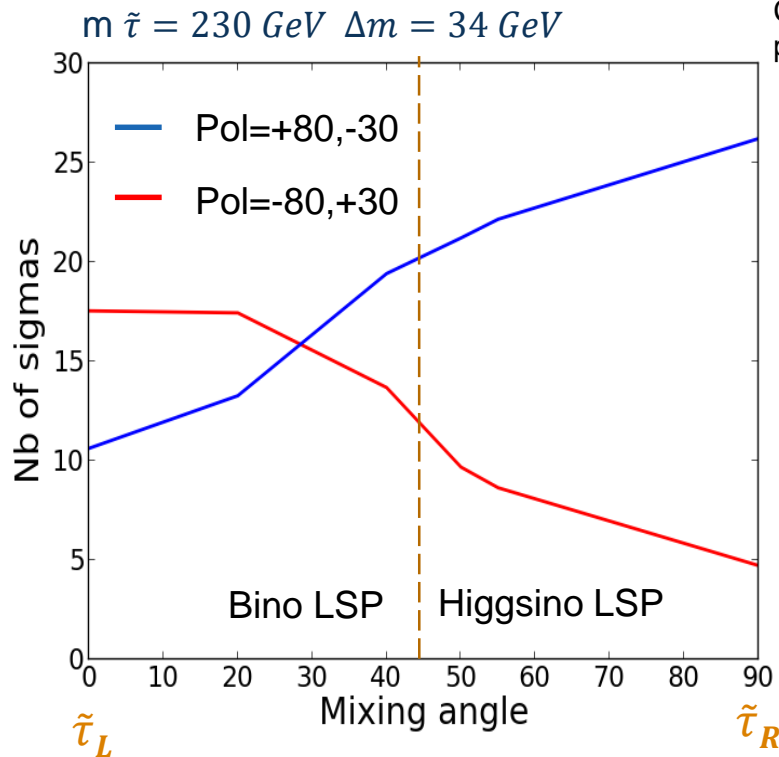
When using polarised beams the contribution of the different polarisation configurations should be weighted

Take into account effect of mixing on cross-section and signal efficiency

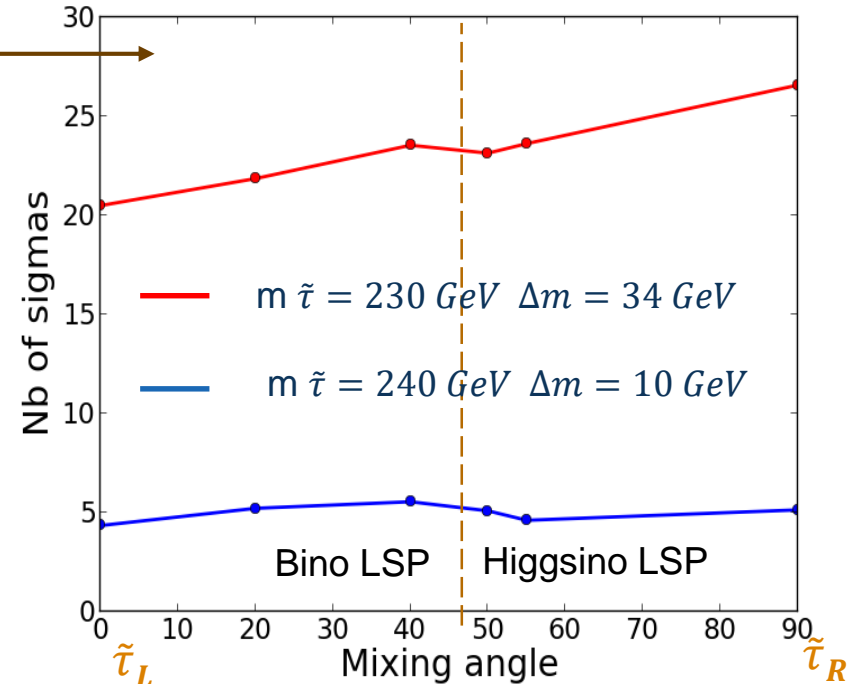
# $\tilde{\tau}$ 's at future $e^+e^-$ colliders:

## impact of mixing and LSP nature (ctd.)

Likelihood-ratio statistic used to weight both polarisations



Combination for polarised case



# ILD full simulation analysis: MC samples and event selection

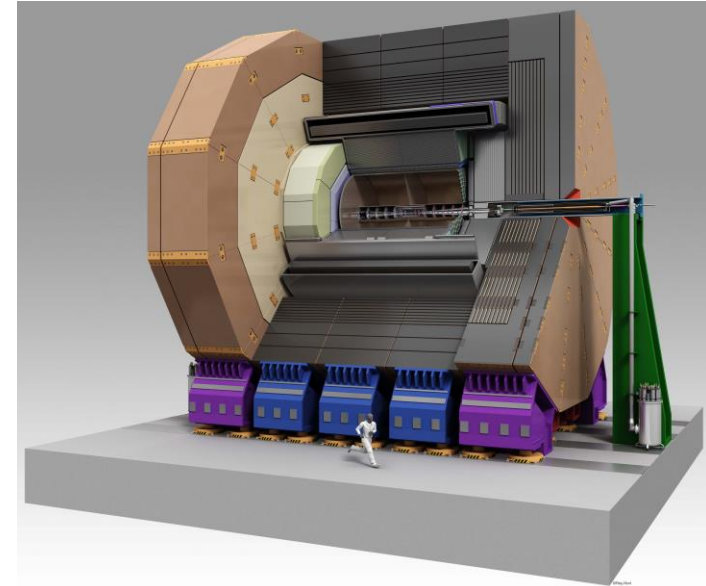
## ILD concept ...

- High granularity calorimeters optimised for particle flow
- Power-pulsing for low material

## ... satisfying Physics requirements for BSM ...

- Jet energy resolution 3-4%
- Asymptotic momentum resolution  $\sigma(1/p_{\perp}) = 2 \times 10^{-5} \text{ GeV}^{-1}$
- Impact parameter resolution  $\sigma(d_0) < 5 \mu\text{m}$
- Hermeticity down to 6 mrad
- Triggerless operation

... developed for the ILC, now studying adjustments for other colliders, esp. FCCee.



**Studies using the full Geant4 simulation of the ILC version of the ILD and the existing 500GeV MC samples covering the full SM background with all  $e^+e^-/e^{\pm}\gamma$  gamma/gammagamma processes ( $>10^7$  events)**

# ILD full simulation analysis:

## MC samples and event selection (ctd.)

### Properties $\tilde{\tau}$ -events “must” have

- **Missing energy** ( $E_{\text{miss}}$ ).  $E_{\text{miss}} > 2 \times M_{\text{LSP}}$  GeV
- **Visible mass** ( $m_{\text{vis}}$ ).  $m_{\text{vis}} < 2 \times (M_{\tilde{\tau}} - M_{\text{LSP}})$  GeV
- **Momentum of all jets** ( $p_{\text{jet}}$ ).  $p_{\text{jet}} < 70\%$  Beam Momentum (or  $M_{\tilde{\tau}}/M_{\text{LSP}}$  dependent)
- **Two well identified  $\tau$ 's and little other activity**

### Event selection

Well known initial state  
Hermeticity

Clean final state  
(‘no’ pile-up)

- **Maximum jet momentum:**

Above 95 % signal efficiency for each of these cuts  
(excluding for the  $\tau$ -identification)

$$P_{\text{max}} = \frac{\sqrt{s}}{4} \left( 1 - (M_{\text{LSP}} / M_{\tilde{\tau}})^2 \right) \left( 1 + \sqrt{1 - \frac{4M_{\tilde{\tau}}^2}{s}} \right)$$

# ILD full simulation analysis:

## MC samples and event selection (ctd.)

Properties  $\tilde{\tau}$ -events “might” have, but background “rarely” has

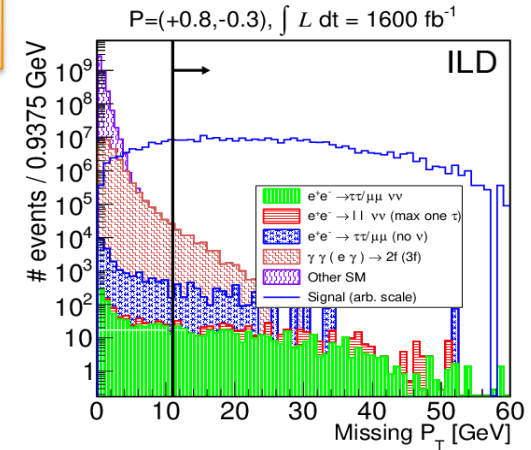
- Missing transverse momentum
- Large acoplanarity
- Large transverse momentum wrt. thrust-axis ( $\rho$ )
- High angles to beam

Cuts against properties of irreducible sources of background

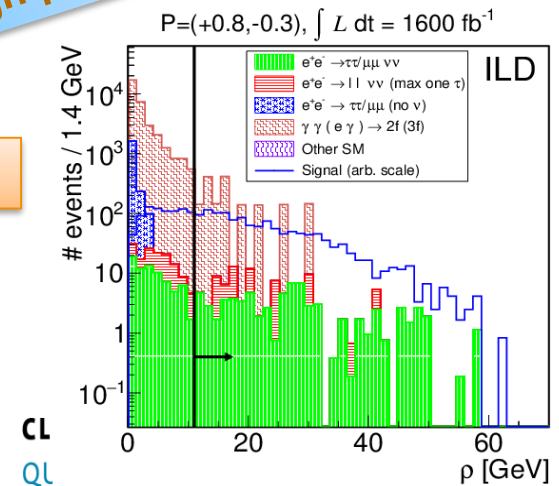
- Charge asymmetry ( $\Sigma \text{charge} * \cos(\text{polar\_angle})$ )
- Difference between visible mass and Z mass

Properties that the background often “does not” have

- Low energy in small angles
- Low energy of isolated neutral clusters

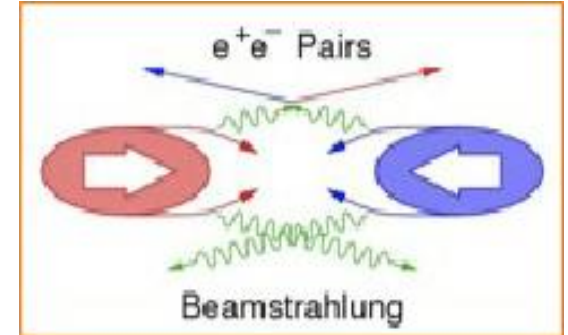


High polarised beams



# ILD full simulation analysis: beam induced backgrounds

$e^+e^-$  beams are accompanied by real (beamstrahlung) and virtual (Weizsäcker-Williams process) photons



Interactions between real and/or virtual photons produce:

- **low  $p_T$  hadrons**
  - produced by vector meson fluctuations of real or virtual photons
  - e.g. at ILC500  $\langle N \rangle = 1.05/BX$ , CLIC380(3000)  $\langle N \rangle = 0.17(3.1)/BX$ , FCCee  $\langle N \rangle \sim 0/BX$
  - low  $p_T$ , travelling through the detector
- **$e^+e^-$  pairs**
  - produced by scattering of two real photons
  - $10^5$  pairs per bunch crossing
  - very low  $p_T$  ( $< 1\text{ GeV}$ ), curl up in magnetic field, interesting for BeamCal studies

$\gamma\gamma$  interactions are independent of the  $e^+e^-$  process, but can happen simultaneously to it (overlay-on-physics events) or not (overlay-only events)



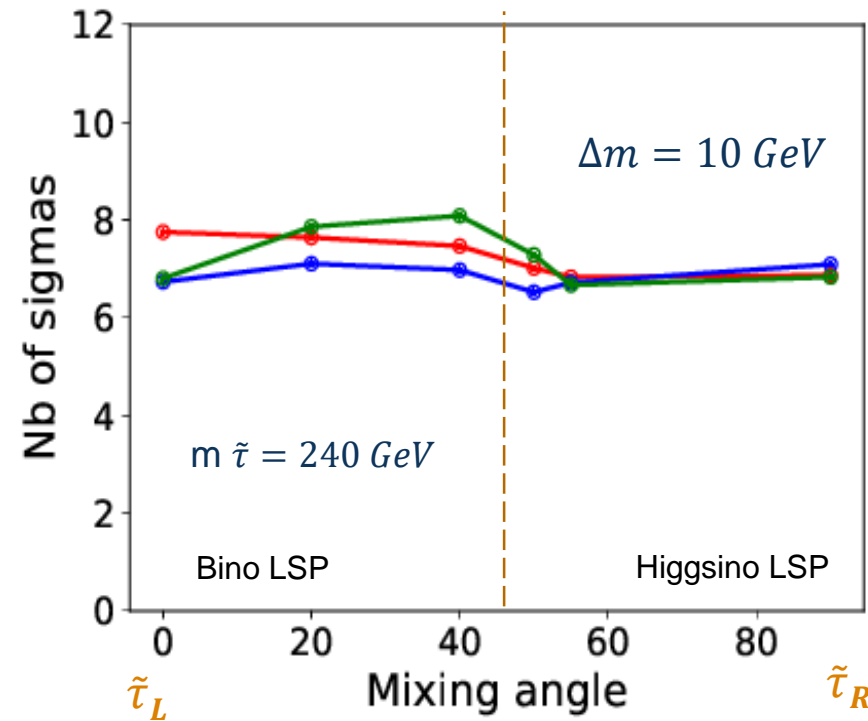
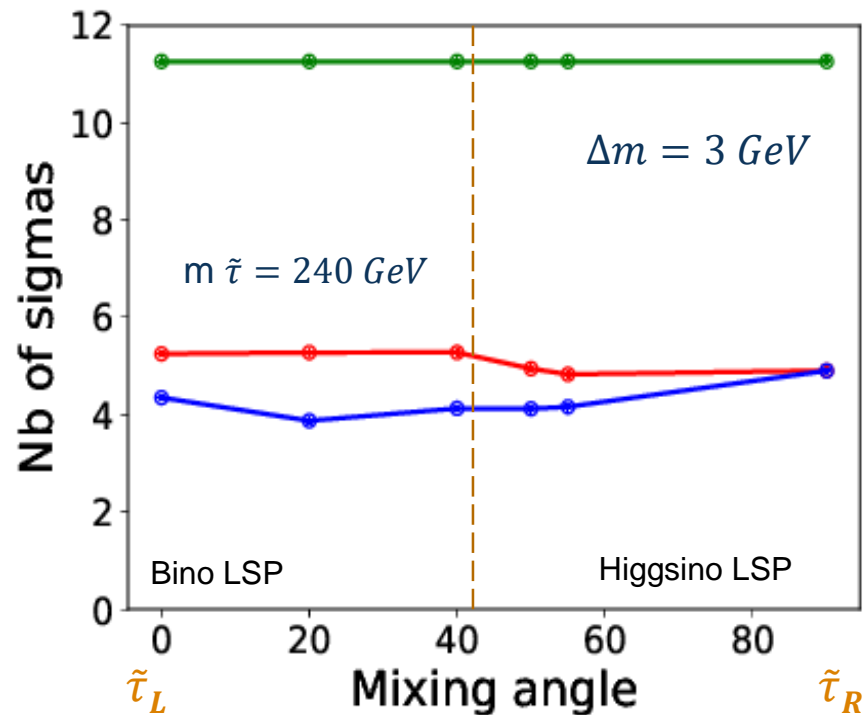
# ILD full simulation analysis: beam induced backgrounds

Full simulation

- Not cut on overlay tracks
- Cut on tracks based on transverse momentum, angular distribution and input parameter significance

ILC500: effect of overlay-on-physics events

— Fast simulation (SGV) – not overlay tracks



Larger effect of overlay tracks in low DM case since they are more similar to the signal ones: strong reduction of significance

# ILD full simulation analysis: beam induced backgrounds

Overlay-only events are  $\sim 10^3$  times higher than any SM background included in the analysis

Motivation for only-overlay analysis

- Overlay-only events:  $\sim 10^3$  per train  
( $\langle 1.05 \rangle$  low  $p_T$  hadrons +  $\sim 1$  seeable  $e^+e^-$  pair)/BX
- SM background:  $\sim 1$  per train
- Signal:  $\sim 10^{-6}$  per train

ILC500 conditions

$\gamma\gamma \rightarrow$  low  $p_T$  hadrons similar to visible products from  $\tilde{\tau}$  production for small ( $\leq 10$  GeV) LSP-  $\tilde{\tau}$  mass differences

Overlay-only events can be misidentified as signal events

A suppression stronger than  $10^{-9}$  is needed to make the background from overlay-only events negligible

# ILD full simulation analysis: beam induced backgrounds

Identify a set of **independent** cuts (not enough Monte Carlo statistics to get the suppression by sequential cuts)

Compute **total rejection factor** as the **product of the factors** obtained with either of these cuts

**Independent** set of cuts from the “standard” ones, based on kinematics:

- missed  $p_T + \rho^1$
- remaining cuts<sup>2</sup>

**Overlay-only analysis strategy**

**Additional independent** requirements based on:

- Initial State Radiation photons (ISR)
- vertex

Study of two different mass differences between  $\tilde{\tau}$  and LSP masses (2 and 10 GeV) since general cuts depend on space point

# ILD full simulation analysis: beam induced backgrounds

Identify a set of **independent** cuts (not enough Monte Carlo statistics to get the suppression by sequential cuts)

Com **Achieved rejection factor:  $8.2 \times 10^{-11}$  (  $1.8 \times 10^{-10}$ ) at the DM = 2 ( DM= 10) GeV model point** ther of

Index **70 (30) overlay-only events expected for each polarisation at the DM = 2 ( DM= 10) GeV model point**

- missing  $p_T$
- remaining cuts<sup>2</sup>

Additional **independent** requirements based on:

- In
  - v
- For  $\Delta M = 2$  ( $\Delta M = 10$ ) GeV, remaining SM background of the order of (two orders of magnitude larger than) the remaining overlay-only events**

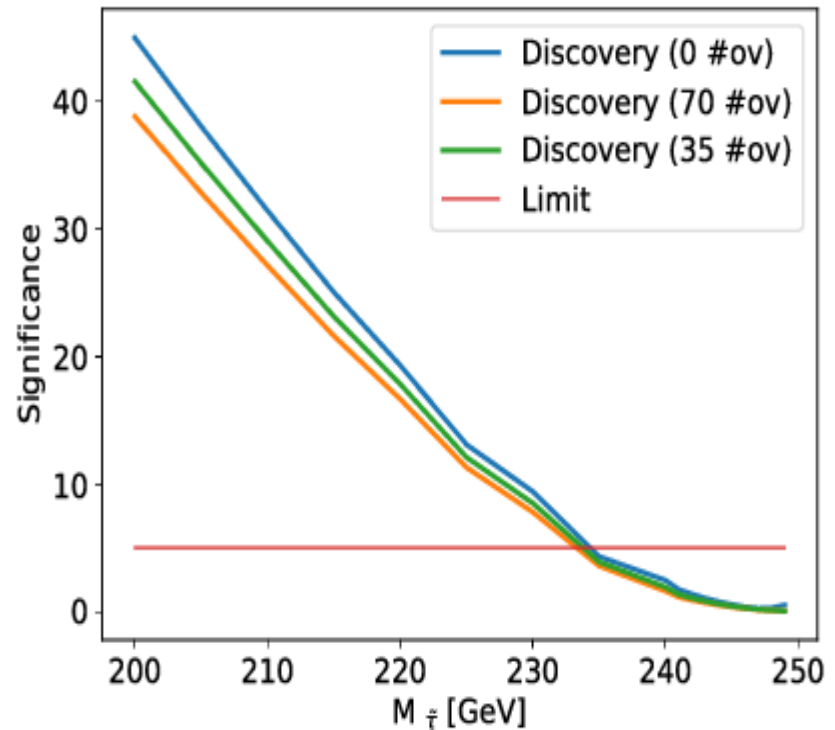
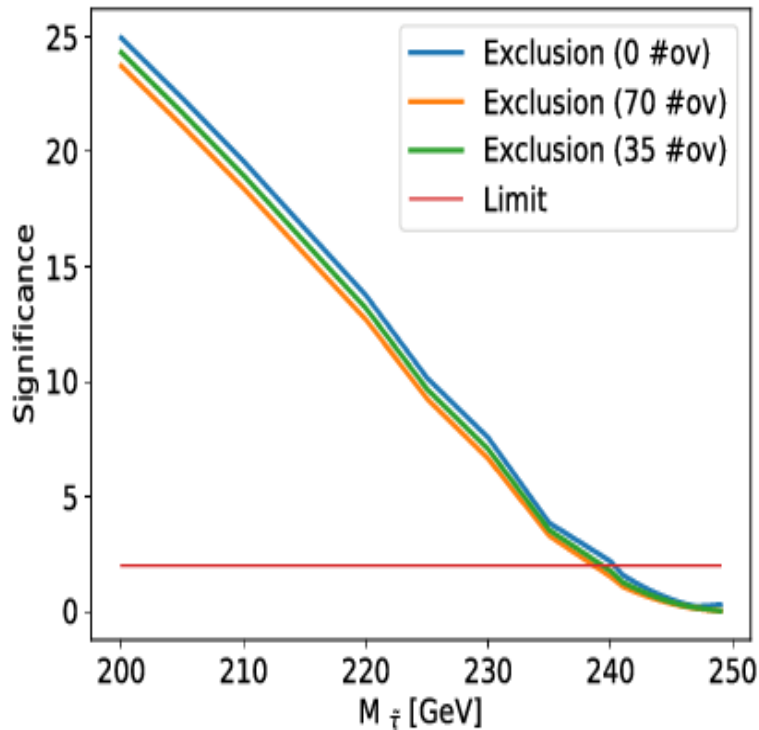
**Negligible effect for  $\Delta M = 10$**

Study of two different mass differences between  $\tau$  and LSP masses (2 and 10 GeV) since general cuts depend on space point

# ILD full simulation analysis: beam induced backgrounds

Significance with/wo overlay-only events  
DM = 2 GeV

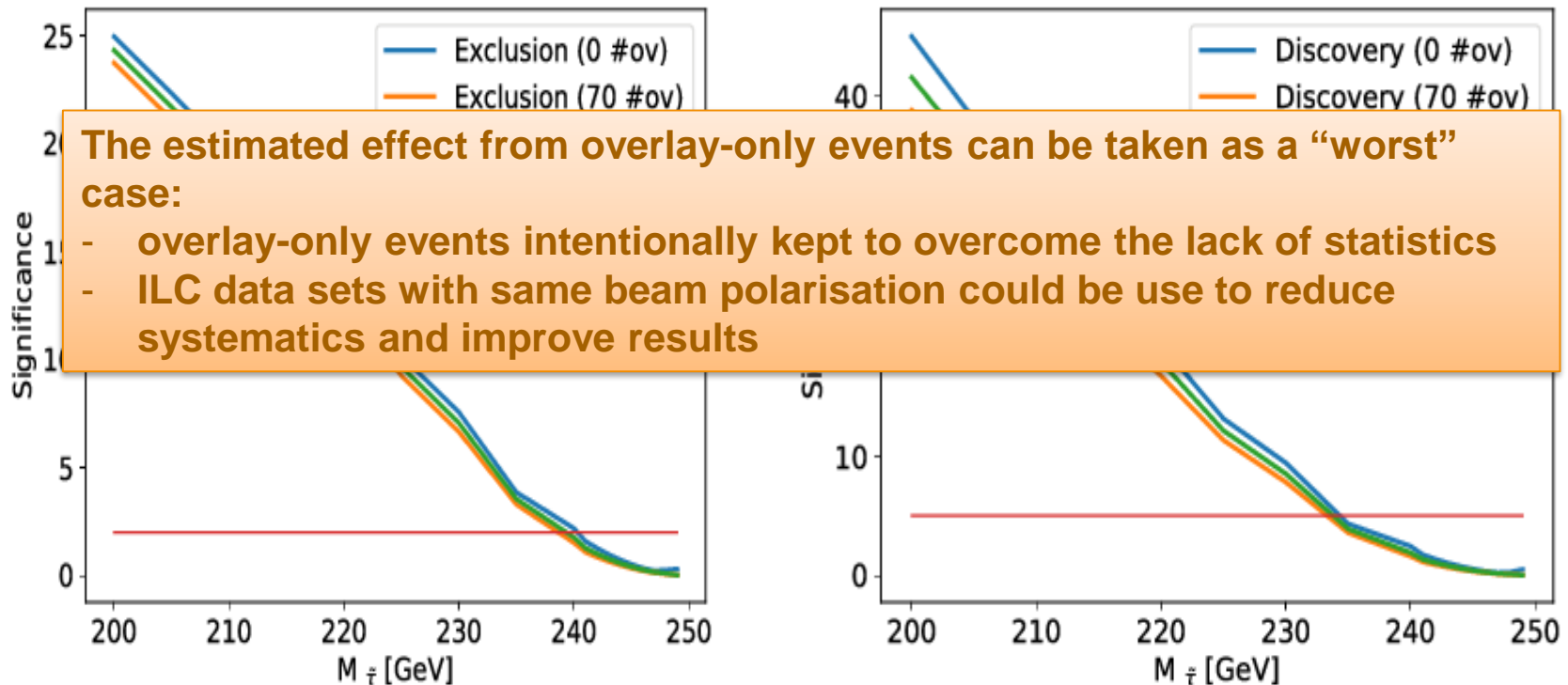
#overlay-only events ~70 per polarisation  
(complete running time, both polarisations)



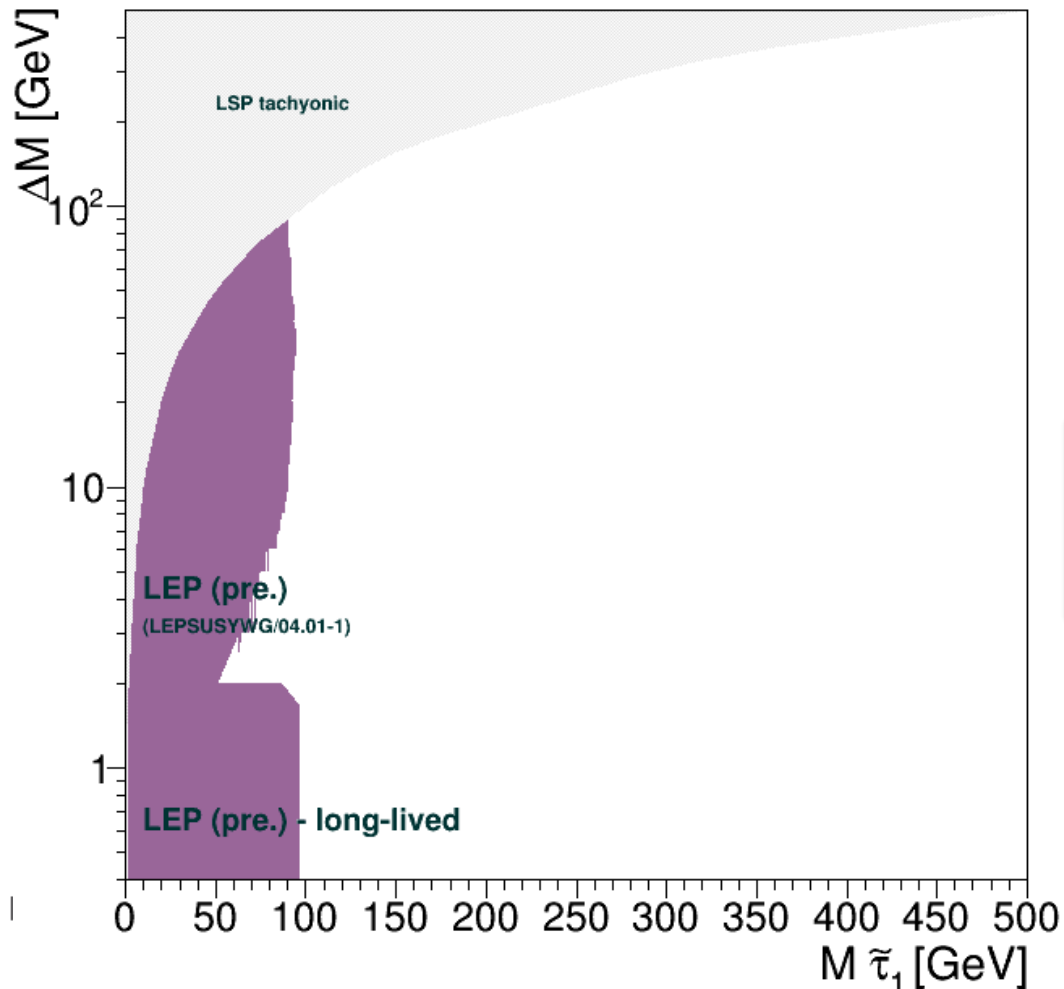
# ILD full simulation analysis: beam induced backgrounds

Significance with/wo overlay-only events  
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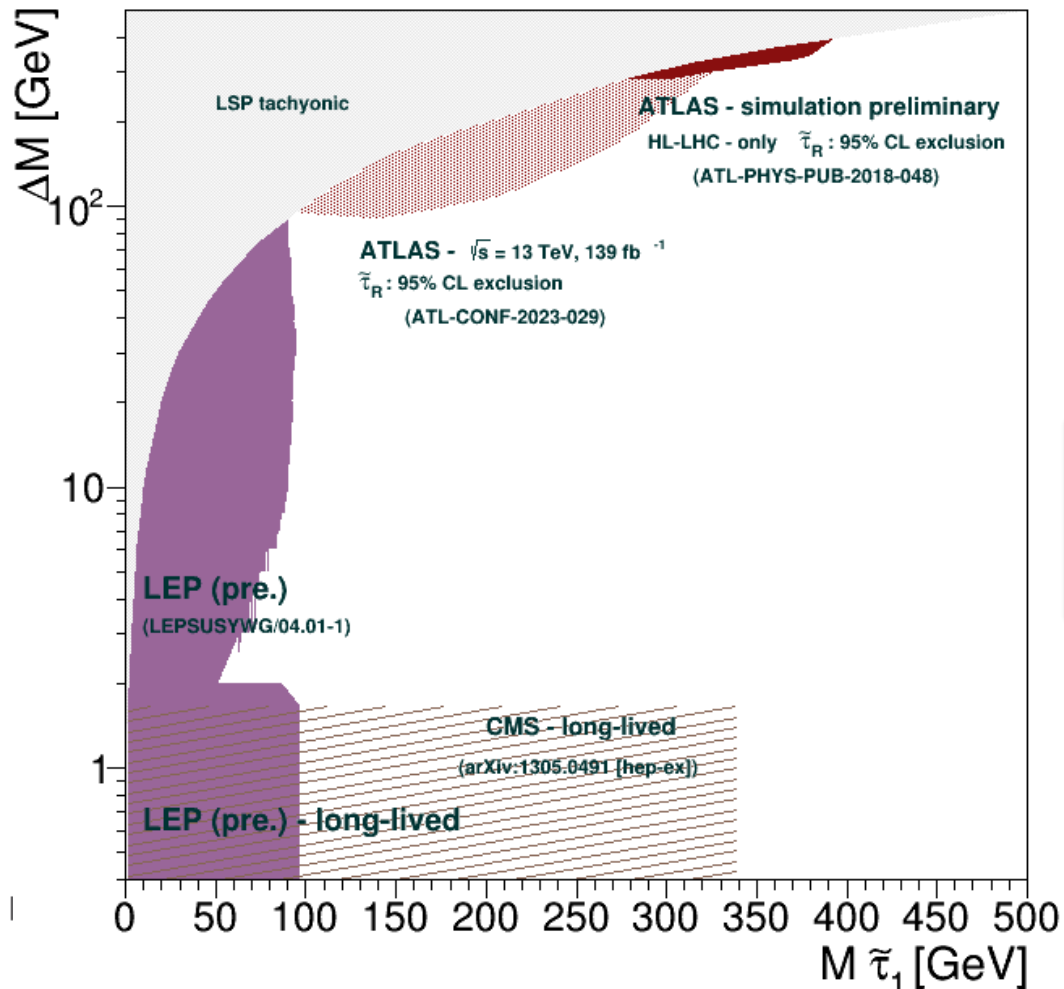
# ILD full simulation analysis: results



Current model-independent  
limits for  $\Delta M > \tau$  mass come  
from LEP



# ILD full simulation analysis: results

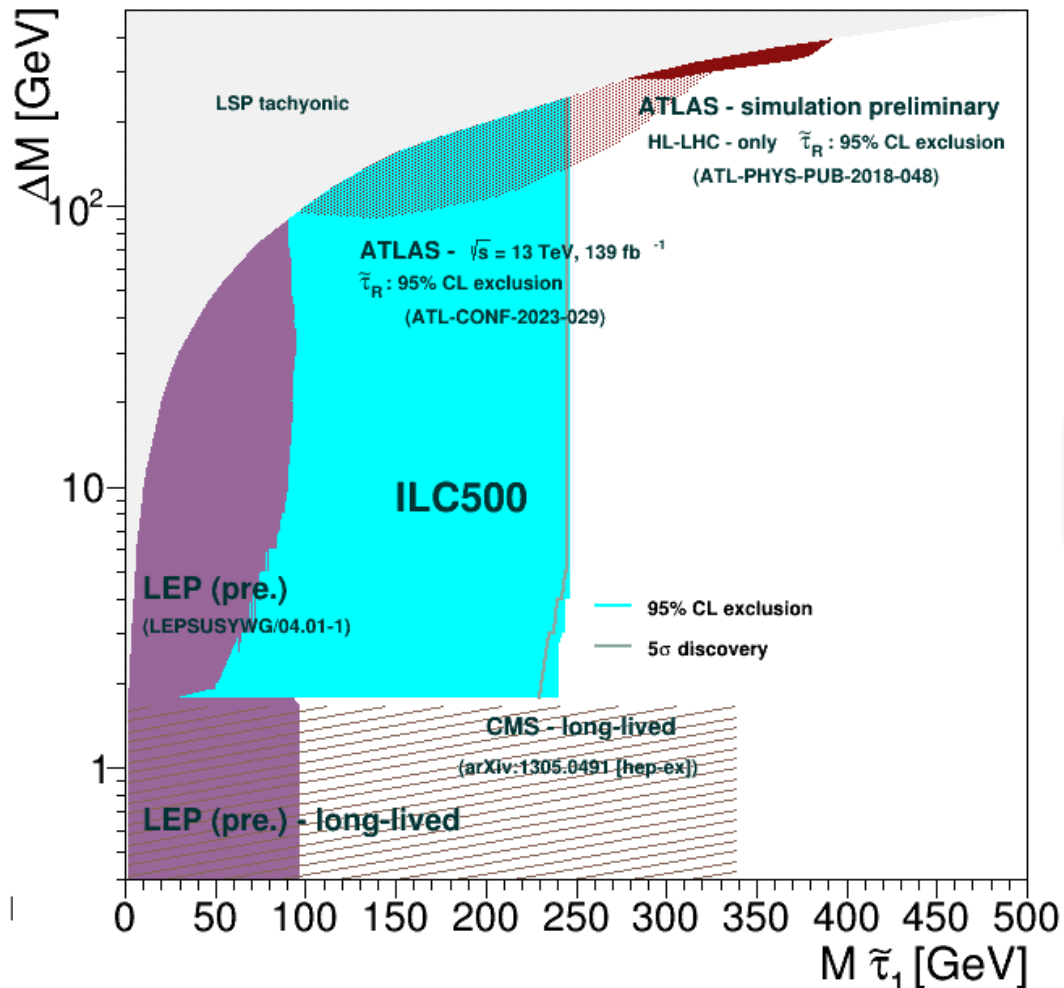


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# ILD full simulation analysis: results

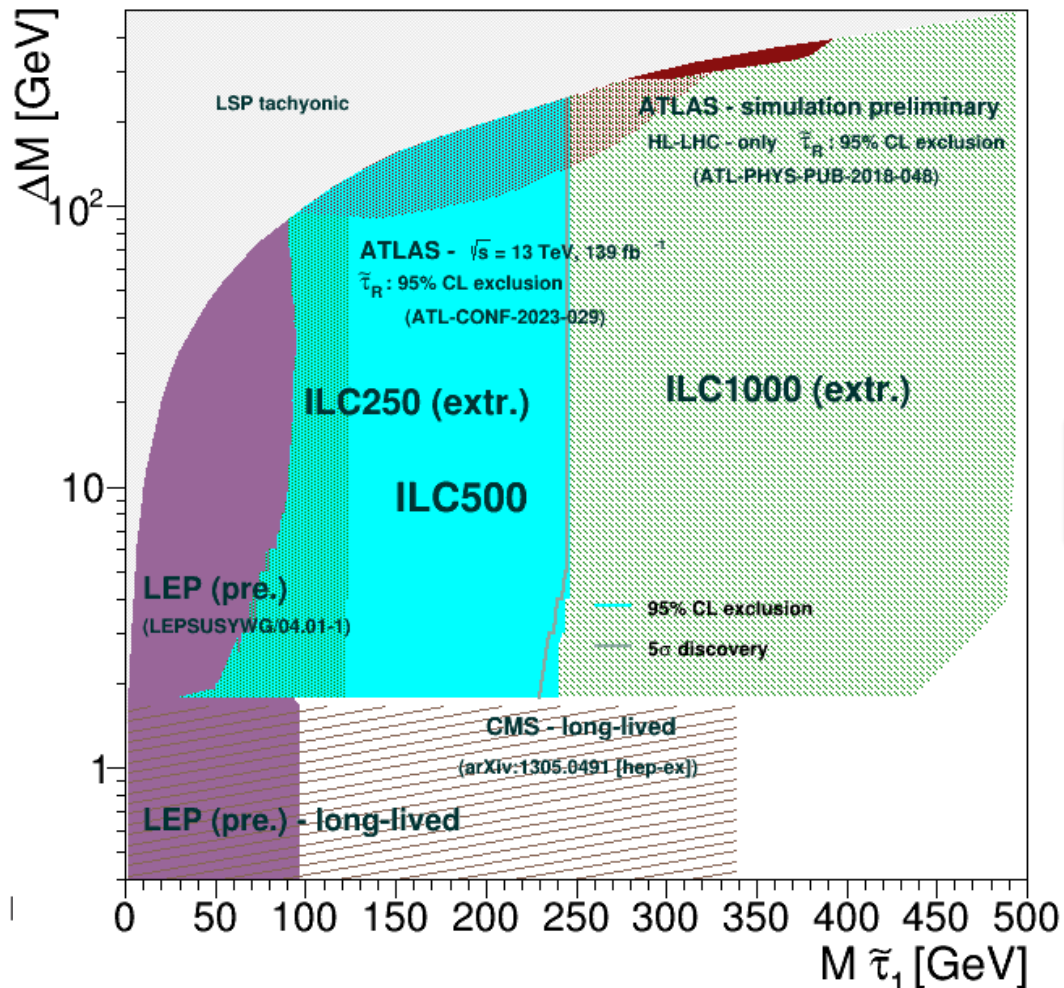


At ILC discovery and exclusion are almost the same

[arXiv:2105.08616](https://arxiv.org/abs/2105.08616)



# ILD full simulation analysis: results



At ILC discovery and exclusion are almost the same

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# Impact of specific ILD/ILC features: polarisation, luminosity, energy

## Polarisation:

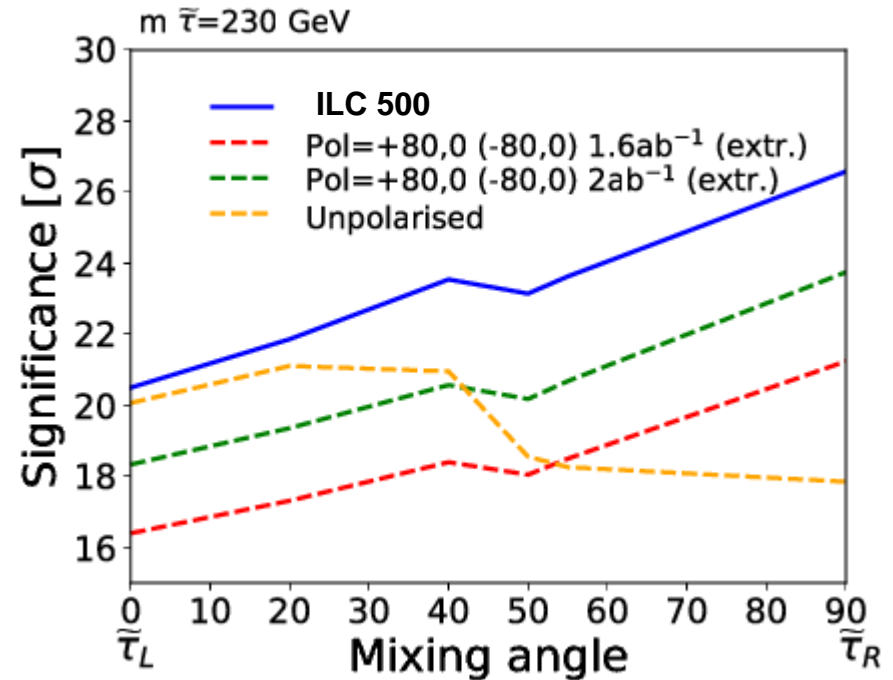
- combination of data-taking with different polarisation signs enables equal sensitivity to all mixing angles
- polarisation of both beams provides higher sensitivity than one beam or none

CLIC, C3, foresee only the electron beam to be polarised, FCCee does not foresee longitudinal polarisation of the beams, CEPC studies the possibility of electron polarization.

## Luminosity:

- higher luminosity gives only very little improvement

Ex. 2 to 5 ( $10$ )  $\text{ab}^{-1}$  at 250 GeV for  $\text{DM} = 2$  GeV changes excl. limit on  $M\tilde{\tau}$  from 122 to 117 (117) GeV, negligible for  $\text{DM} = 10$  GeV



## Energy:

- increase in centre-of-mass energy covers much more parameter space, up to close to kinematic limit



# Impact of specific ILD/ILC features : beam-induced backgrounds

## Beam-induced backgrounds:

- possible lost of significance mitigated applying cuts based on transverse momentum and transverse parameter significance (overlay-on-physics) and on vertex (overlay-only)

Impact of less than 1 GeV for highest reachable masses and smallest mass differences, negligible for the rest of the parameter space

Mitigation makes profit of the microscopic beam-spot: similar order of magnitude at CLIC and C3; larger in circular colliders, but no-existent beam-induced backgrounds.

Estimated impact apply to ILC500, smaller at ILC250. No-existent at FCCee, CEPC. CLIC, where the detector needs to integrate over many BX, suffers for more overlay events, but provides timing information that can reduce them substantially

# Impact of specific ILD/ILC features: hermeticity, triggerless operation

## Hermeticity:

- crucial when searching for missing momentum signatures

Ex. 50 mrad instead of 6 mrad (ILC) decreases the significance from ...

... 34.9 to 10.7 for  $M_{\tilde{\tau}} = 230$  GeV  $DM = 34$  GeV

... 2.08 to 0.7 for  $M_{\tilde{\tau}} = 245$  GeV  $DM = 10$  GeV

Similar order for other linear collider, ex. 10 mrad CLIC, but not for circular ones, ~50 mrad

## Triggerless operation:

- big advantage when searching for unexpected signatures

Possible at linear colliders due to low collision frequency, not possible at circular colliders

# Conclusions

- Even after HL-LHC  $\tilde{\tau}$ -LSP mass plane will remain almost completely unexplored
- Future electron-positron colliders are ideally suited for  $\tilde{\tau}$  searches
- $\tilde{\tau}$  mixing and LSP nature influence production cross-sections and decay kinematics -> picked “worst scenario” for actual analysis
- **Polarised beams:** combination of data-taking with different signs enables equal sensitivity to all mixing angles
- **Beam-induced backgrounds** at Linear Colliders can be mitigated up to small residual impact of  $\sim 1\text{GeV}$  on highest reachable mass for lowest  $\Delta M$
- **Higher centre-of-mass energies** cover much more parameter space, higher luminosity gives only very little improvement, ex. increase of ILC250 luminosity from 2 to 10  $\text{ab}^{-1}$  affects the  $\tilde{\tau}$  mass limit only by 5 GeV
- Hermeticity of detector crucial

**Future electron-positron colliders are well suited for discovering/excluding  $\tilde{\tau}$ 's for any  $\tilde{\tau}$ -LSP mass difference and any  $\tilde{\tau}$ -mixing nearly up to the kinematic limit – hermetic detector and ECM reach crucial**