

# SECOND • ECFA • WORKSHOP

## on $e^+e^-$ Higgs / Electroweak / Top Factories

11-13 October 2023  
Paestum / Salerno / Italy

### $M_W$ @ future $e^+e^-$ colliders

Topics:

- Physics potential of future Higgs and electroweak/top factories
- Required precision (experimental and theoretical)
- EFT (global) interpretation of Higgs factory measurements
- Reconstruction and simulation
- Software
- Detector R&D

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# W-boson mass measurements vs. prediction from $\mu$ decay

ILC: Baak et al., 1310.6708

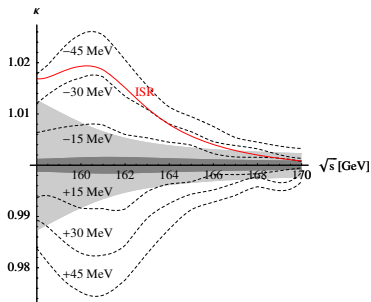
FCC-ee: Freitas et al., 1906.05379

	experimental accuracy				theory uncertainty			
	current	$\sigma_{WW}$ @ threshold			intrinsic			parametric
$\Delta M_W$ [MeV]	13	LEP2	ILC	FCC-ee	current	source	prospect	prospect source
		200	3–6	0.5–1	3	$\alpha^3, \alpha^2 \alpha_s$	1	1(0.6) $\Delta\alpha_{had}$

complicated reconstructions (under current)   
 basically counting experiments (under ILC, FCC-ee)   
 $M_W$  calculated from  $\mu$  decay (under theory uncertainty)

## Sensitivity of $\sigma_{WW}$ to $M_W$ :

Beneke et al. '07

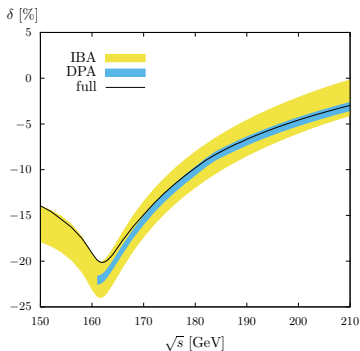
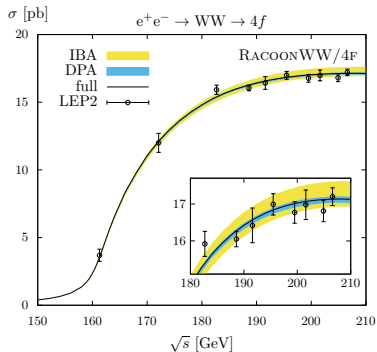


$$\kappa = \frac{\sigma_{WW}(s, M_W + \delta M_W)}{\sigma_{WW}(s, M_W)}$$

$$\Delta\kappa = 0.1\% (0.02\%) \leftrightarrow \delta M_W = 1.5 (0.3) \text{ MeV} \text{ for } \sqrt{s} = 161 \text{ GeV}$$

$\Rightarrow$  FCC-ee requires  $\Delta_{TH} \sim 0.02\%$  in  $\sigma_{WW}$

Shaded areas / ISR curve:  
 some uncertainties of NLO(EFT) calculation,  
 improveable via full NLO( $ee \rightarrow 4f$ ) and NNLO(EFT)



- ▶ IBA = based on leading-log ISR and universal EW corrections ( $\Delta \sim 2\%$ )  
 ↪ shows large ISR impact near threshold (also by GENTLE)
- ▶ DPA = “Double-Pole Approximation” (leading term of resonance expansion)  
 ↪  $\Delta \sim 0.5\%$  above threshold, not applicable at threshold RacoonWW, YFSWW
- ▶ “full” = full NLO prediction for  $e^+e^- \rightarrow 4f$  via charged current Denner et al. '05  
 + leading-log improvements for ISR beyond NLO  
 ↪  $\Delta \sim 0.5\%$  everywhere

## Improvements for $\sigma_{WW}$ @ threshold via EFT

Beneke et al. '07; Actis et al. '08

EFT provides expansion of  $\sigma_{WW}$  for  $\beta = \sqrt{1 - 4M_W^2/s} \sim \sqrt{\Gamma_W/M_W} \sim \sqrt{\alpha}$ :

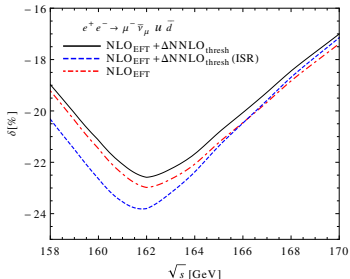
$$\sigma_{WW} = C\alpha^2\beta \left[ 1 + c^{(0)}\beta \right. \quad \text{LO}$$

$$+ \alpha \left( \frac{c_1^{(1)}}{\beta} + c_2^{(1)} \ln \beta L_e + c_3^{(1)} L_e + c_4^{(1)} + c_5^{(1)}\beta \right) \quad \text{NLO}$$

$$\left. + \alpha^2 \left( \frac{c_1^{(2)}}{\beta^2} + \frac{c_2^{(2)}}{\beta} + c_3^{(2)} \ln^2 \beta L_e^2 + c_4^{(2)} \ln \beta L_e^2 + \dots \right) + \dots \right] \quad \text{NNLO}$$

leading NNLO parts known

↓  
required  
for FCC-ee



ISR enhancement factor  $L_e = \ln(m_e/M_W)$

Resummation of leading  $(\alpha L_e)^n$  and subleading  $\alpha(\alpha L_e)^{n-1}$  ISR necessary!

## Theory issues in scan of $\sigma_{WW}(s)$ over WW threshold

### ▶ Definition of $\sigma_{WW}$ via 4f final states

- ▶  $e^\pm$  final states: separation or inclusion of single-W channels?  
↪ TH precision versus EXP accuracy
- ▶ Hadronic final states: separation of multi-jet events (2j,3j,4j,...)  
↪ TH precision versus EXP accuracy

### ▶ Required for the best achievable theory prediction for $\sigma_{WW}$ :

- ▶ Full NLO  $e^+e^- \rightarrow 4f$  prediction for each 4f type (interferences with ZZ and forward- $e^\pm$  channels)
- ▶ **full NNLO EFT calculation** (only leading terms available)
- ▶ **leading 3-loop Coulomb-enhanced EFT corrections**
- ▶ matching of all fixed-order  $e^+e^- \rightarrow 4f$  and threshold-EFT ingredients
- ▶ convolution of matched and corrected XS with higher-order ISR

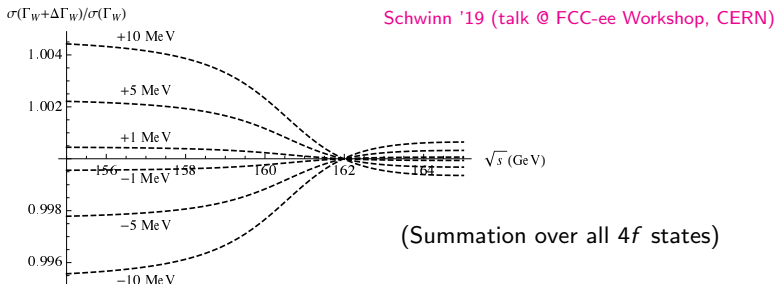
↪ Estimate of theory uncertainty:

$$\Delta \sim 0.01\text{--}0.04\% \text{ for } \sigma_{WW} \text{ @ threshold} \quad \text{Freitas et al., 1906.05379}$$

## Improved $M_W$ prediction from $\mu$ decay

- ▶ Massive 3-loop computations (vacuum graphs, self-energies)

## $\Gamma_W$ determination from energy scan @ WW threshold:



Simultaneous fit of  $M_W$  and  $\Gamma_W$  by scan of  $\sigma_{WW}$ :

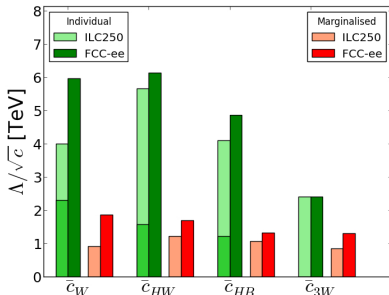
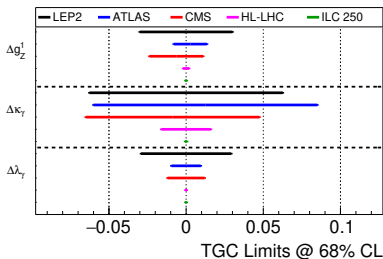
- ▶ FCC-ee study: 1703.01626  
2-point fit ( $15 \text{ ab}^{-1}$ ):  $M_W = 0.41 \text{ MeV}$ ,  $\Gamma_W = 1.1 \text{ MeV}$
- ▶ CEPC study: 1812.09855  
3-point fit ( $2.6 \text{ ab}^{-1}$ ):  $M_W = 1 \text{ MeV}$ ,  $\Gamma_W = 2.8 \text{ MeV}$

## WW production beyond LEP2 energy range

- ▶ Ideal for precision study of anomalous TGCs (no formfactors for damping required)
- ▶ SMEFT framework: sensitivity to dim-6 operators complementary to Higgs analyses

Ellis, You '15

Bambade et al. '19



- ▶ Impact of  $\Delta \kappa_\gamma$  on  $d\sigma_{WW}$ :

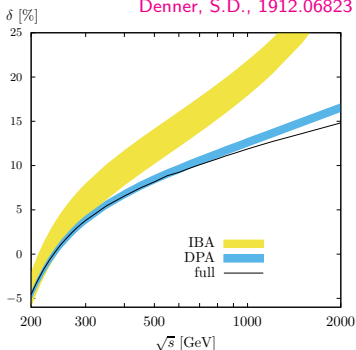
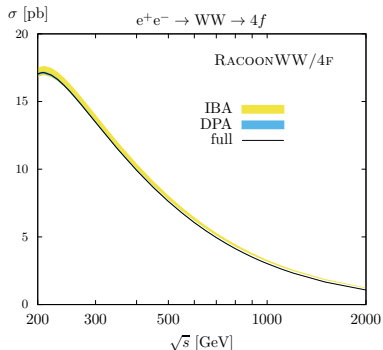
$\sqrt{s}/\text{GeV}$	200	250	500
$\Delta \kappa_\gamma$	0.05	0.004	0.001
$d\sigma_{WW}(\kappa_\gamma)/d\sigma_{WW}^{\text{SM}} - 1$	3%	$\sim 0.5\%$	$\sim 0.5\%$

↪ SM precision limits reach in TGCs for moderate  $\sqrt{s}$ !

## WW production beyond LEP2 energy range

### Fixed-order NLO + leading-log ISR prediction:

Denner, S.D., 1912.06823



Note: large non-universal weak corrections + sizeable off-shell effects

### Achievable precision:

- ▶ by full NLO for  $e^+e^- \rightarrow 4f$  + leading NNLO corrections + ISR resummation
- ▶ estimate:  $\Delta \sim 0.5\%$  in distributions ( $\sim 1\%$  in tails) up to  $\sqrt{s} \sim 1$  TeV