

WG2/WG1 Monte Carlo generators



HELMHOLTZ

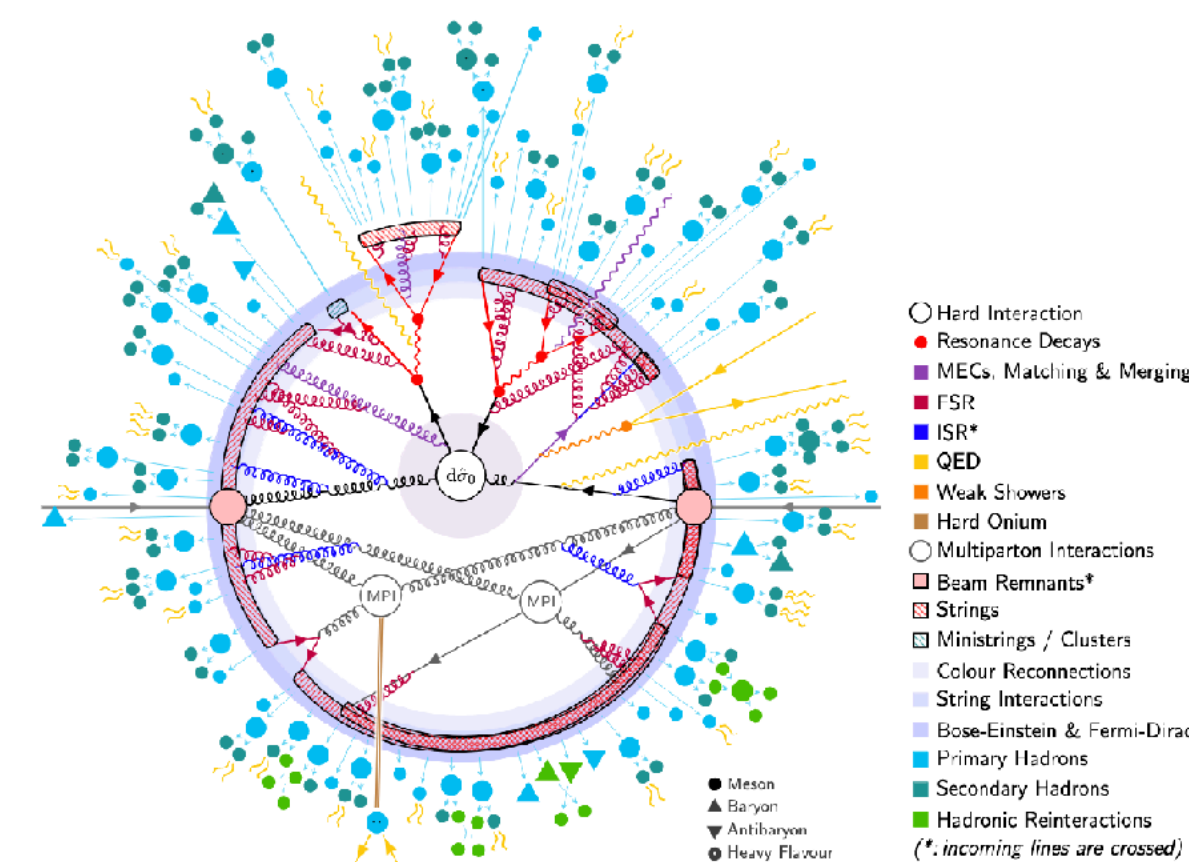


SECOND • ECFA • WORKSHOP
on e^+e^- Higgs / Electroweak / Top Factories

11-13 October 2023
Paestum / Salerno / Italy

Topics:

- Physics potential of future Higgs and electroweak/top factories
- Required precision (experimental and theoretical)
- EFT (global) interpretation of Higgs factory measurements
- Reconstruction and simulation
- Software
- Detector R&D



Universität Hamburg
DER FORSCHUNG | DER LEHRE | DER BILDUNG

CLUSTER OF EXCELLENCE
QUANTUM UNIVERSE

Jürgen R. Reuter



Great to be back at Paestum

2 / 26



September 1992

My first and only visit to Paestum, while ...





September 1992

My first and only visit to Paestum, while ...

LEP was still running on the Z pole !

LEP Operation in 1992 with a 90° optics

R. Bailey, T. Bohl, F. Bordry, H. Burkhardt, K. Cornelis, P. Collier, B. Desforges, A. Faugier, V. Hatton, M. Jonker, M. Lamont, J. Miles, G. de Rijk and H. Schmickler

CERN
CH-1211 Geneva 23, Switzerland

Abstract

The optics for
60° to 90°

The Energy Calibration of LEP in 1992

The working group on LEP energy

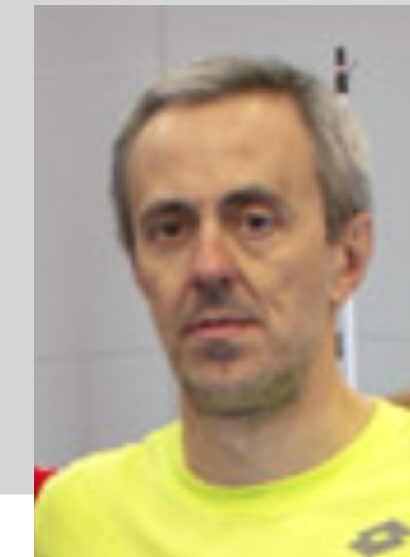
L. Arnaudon¹, R. Assmann², J. Billan¹, W. Birr¹, A. Blondel³, G. Bobbink⁴, F. Bordry¹, H. Burkhardt¹, B. Dehning¹, A. Faugier¹, J. Gascon⁵, A. Grant¹, J. L. Harton⁶, V. Hatton¹, C. M. Hawkes¹, K. N. Henrichsen¹, A. Hofmann¹, R. Jacobsen¹, M. Koratzinos⁷, J. P. Koutchouk¹, G. Musolino¹, S. Myers¹, R. Olsen¹, J. Panman¹, E. Peschardt¹, M. Placidi¹, D. Plane¹, G. Quast⁸, P. Renton^{1,9}, L. Rolandi¹, R. Schmidt¹, H. Wachsmuth¹, J. Wenninger¹.

date	time	week	T_{16} [°C]	$E_{pol} - E_{FD}$ [MeV]	$E_{pol} - E_{FD}$ T-corr. [MeV]
13.9.92	15:42	37	24.15	-37.4 ± 1.0	-34.1 ± 1.3
14.9.92	7:20	37	24.15	-34.8 ± 2.0	-31.5 ± 2.2

ECFA H/EW/Top Factory WG3/2 MC Generators

3 / 26

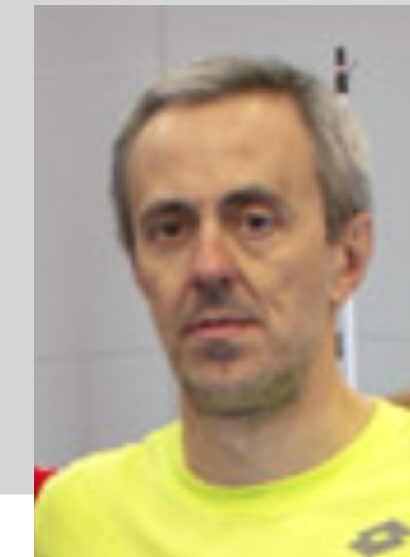
- 1st WG2 Topical WS on Generators / Simulation, @CERN: Nov. 9-10, 2021 <https://indico.cern.ch/event/1078675/>
- Very efficient and effective organization \Rightarrow Conveners: Patrizia Azzi Fulvio Piccinini Dirk Zerwas
- \approx 100 participants, roughly 30 at CERN
- Setting the stage: simulation tools, MCs, software frameworks



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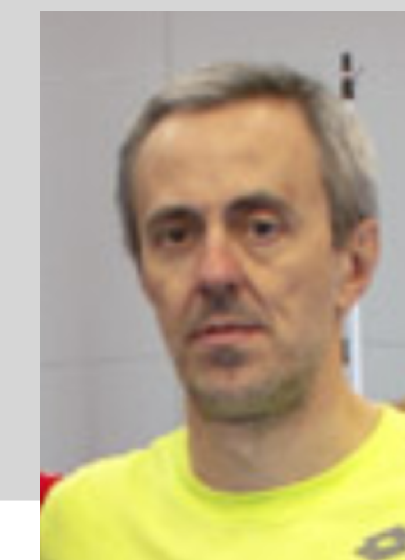


- 2nd WG2 Topical WS on Generators, @Brussels: June 21-22, 2023 <https://indico.cern.ch/event/1266492/>
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- Transfers from IMCC Annual Meeting in Orsay + Les Houches
- Much more focused on MC generators: physics, beam spectra, technical details, benchmarks

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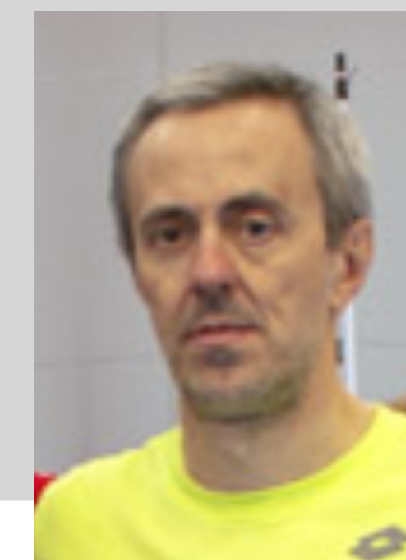
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Jun 7-17, 2022 <https://indico.cern.ch/event/1140580/>
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- Focus: Tools, automation, multi-loop

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- CERN WS “Parton Showers for Future e^+e^- colliders”
Apr 24-28, 2023 <https://indico.cern.ch/event/1233329/>
- \approx 120 participants, roughly 80 at CERN
- Focus: perturbative and non-perturbative QCD

The scope: lessons learned and where to go

4 / 26

-  LHC a huge success story for Monte Carlos (MCs)
-  Assessment of needs for MCs event for (high-energy) e^+e^- colliders?

- 📌 LHC a huge success story for Monte Carlos (MCs)
- 📌 Assessment of needs for MCs event for (high-energy) e^+e^- colliders?

1. Beam simulation / luminosity spectra / polarization
2. QED: ePDFs vs. YFS, collinear vs. soft resummation, cross section predictions ...
3. Hard process (SM): NLO SM automation , NNLO automation (?)
4. Hard process (BSM): any new (crazy) model? SMEFT? tweaks? which order?
5. Exclusive processes (I = QED): photons, QED showers, matching
6. Exclusive processes (II = QCD): jets, QCD/QED/EW showers, fragmentation (!)
7. Special processes & tools: (Bhabha) luminometry, top/WW threshold, WW etc.
8. Specialized topics: event formats & software frameworks
9. Efficiency, speed, sustainability [left out for time reasons]
10. Launch of MC validation effort

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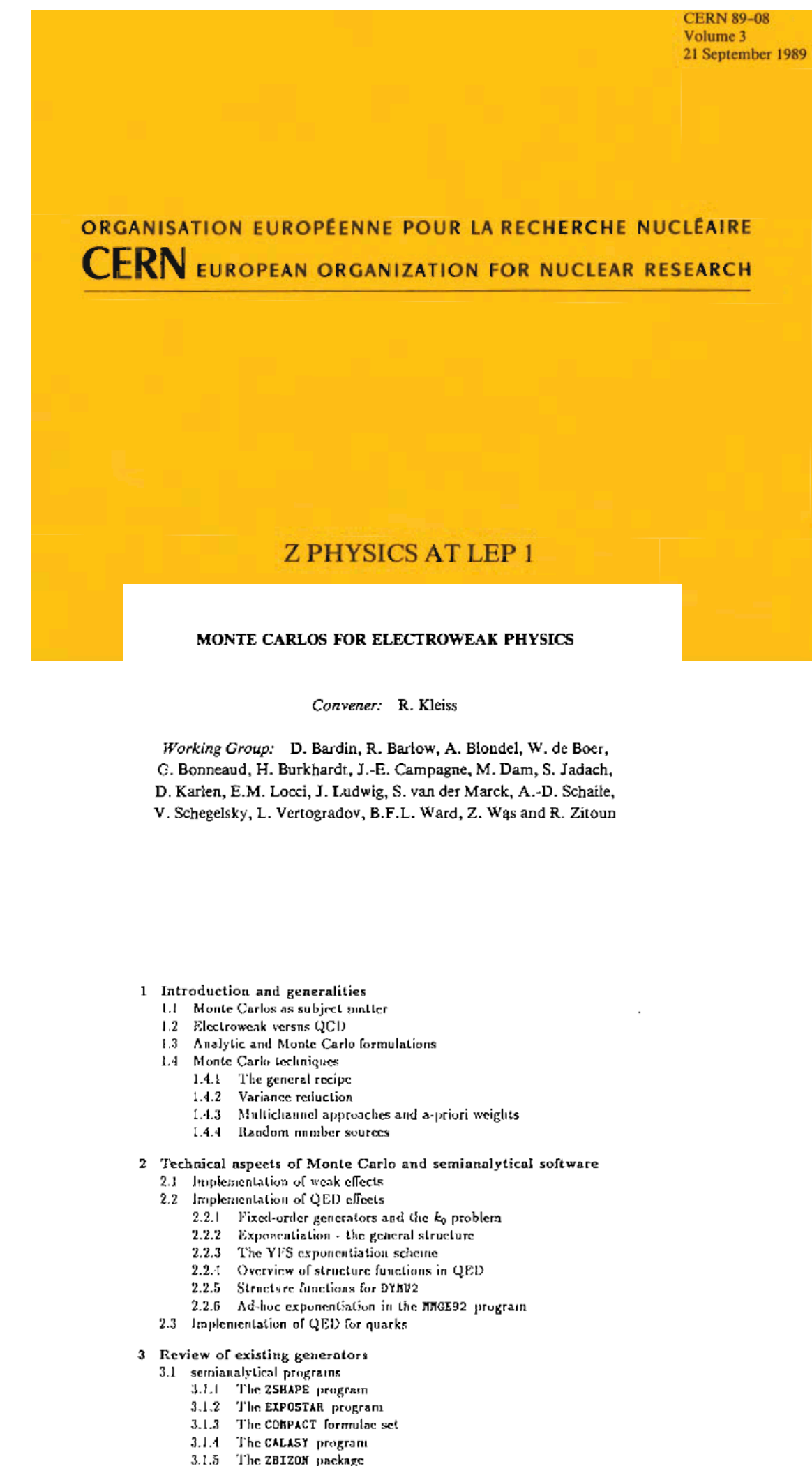
4 / 26

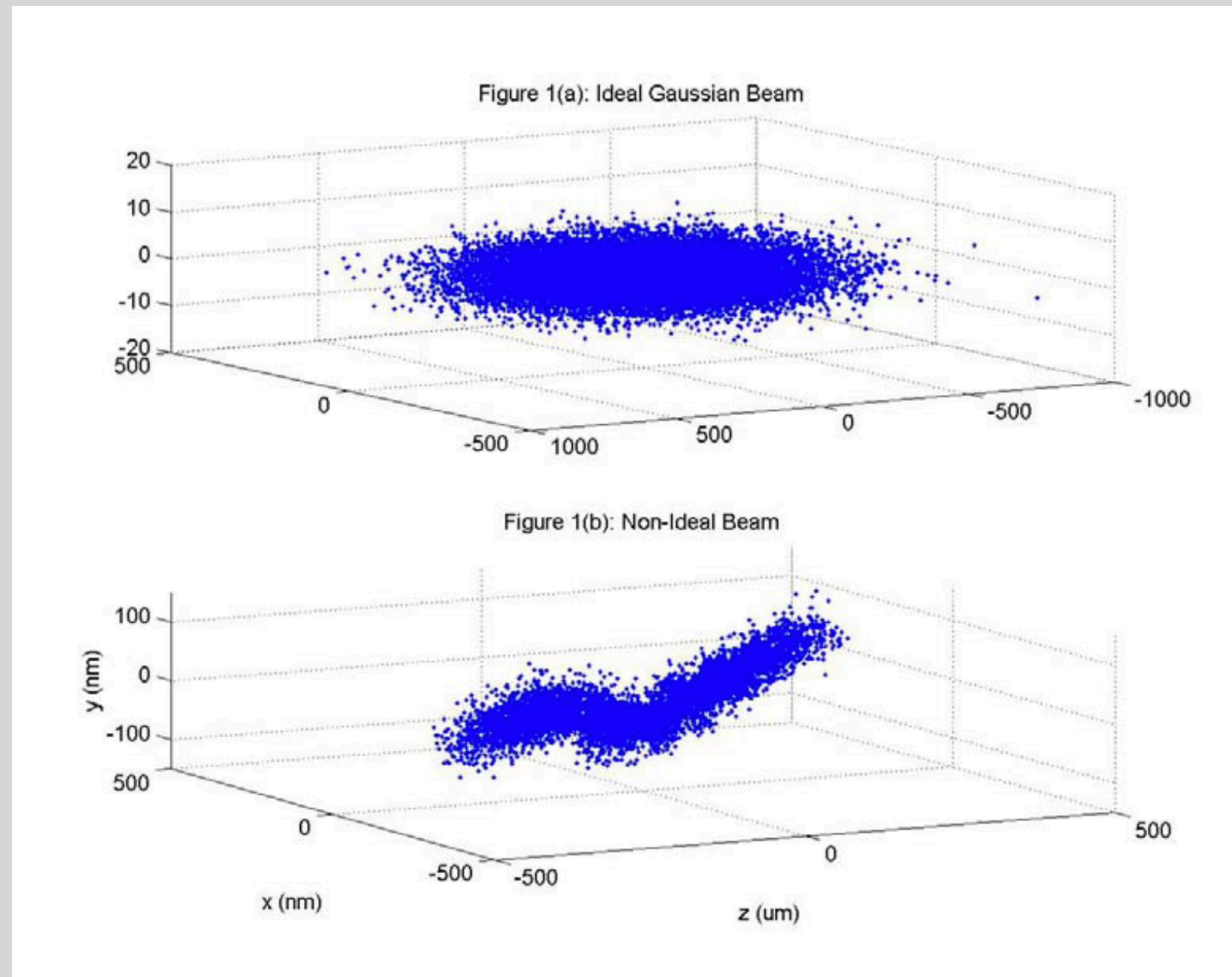
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LEP tradition !

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⇒ Talk by Alan Price

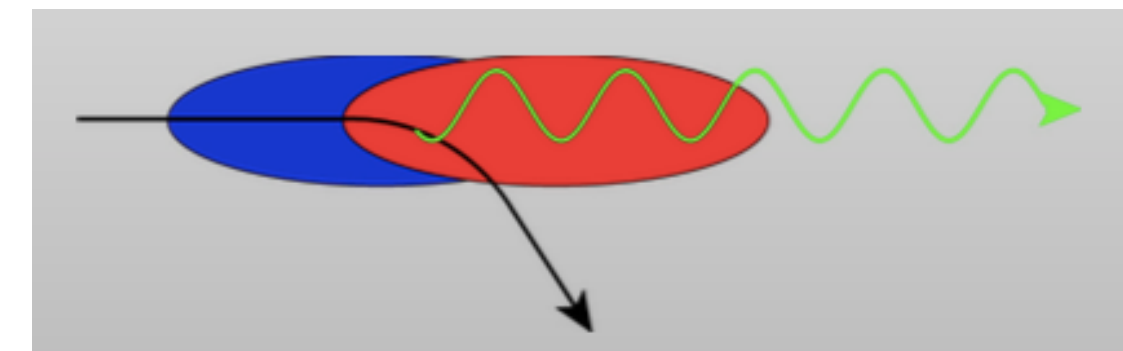




Beam simulations

6 / 26

- Micro-scale bunches create beam structure/-strahlung
- Mostly Gaussian shape for circular machines, but not fully
- Machine simulation with tools like GuineaPig(++), CAIN
- Has to be folded into realistic MC simulations

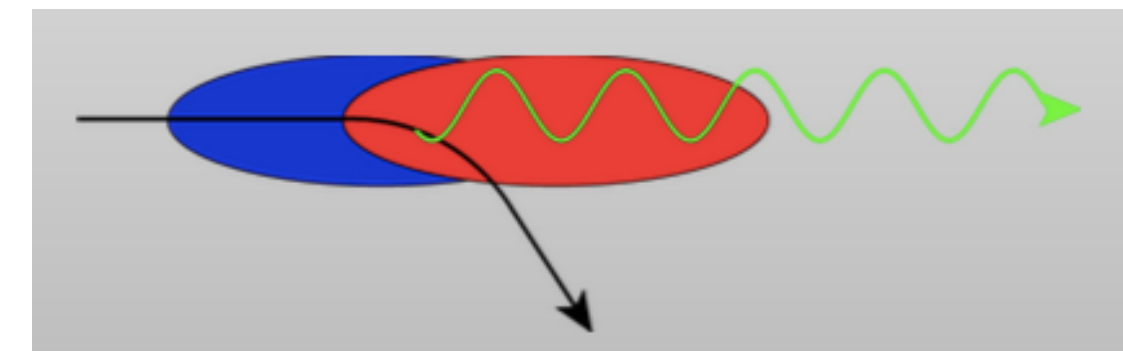


$$L \approx \frac{N}{4\pi\sigma_x\sigma_y} \frac{\eta P_{AC}}{E_{CM}}$$

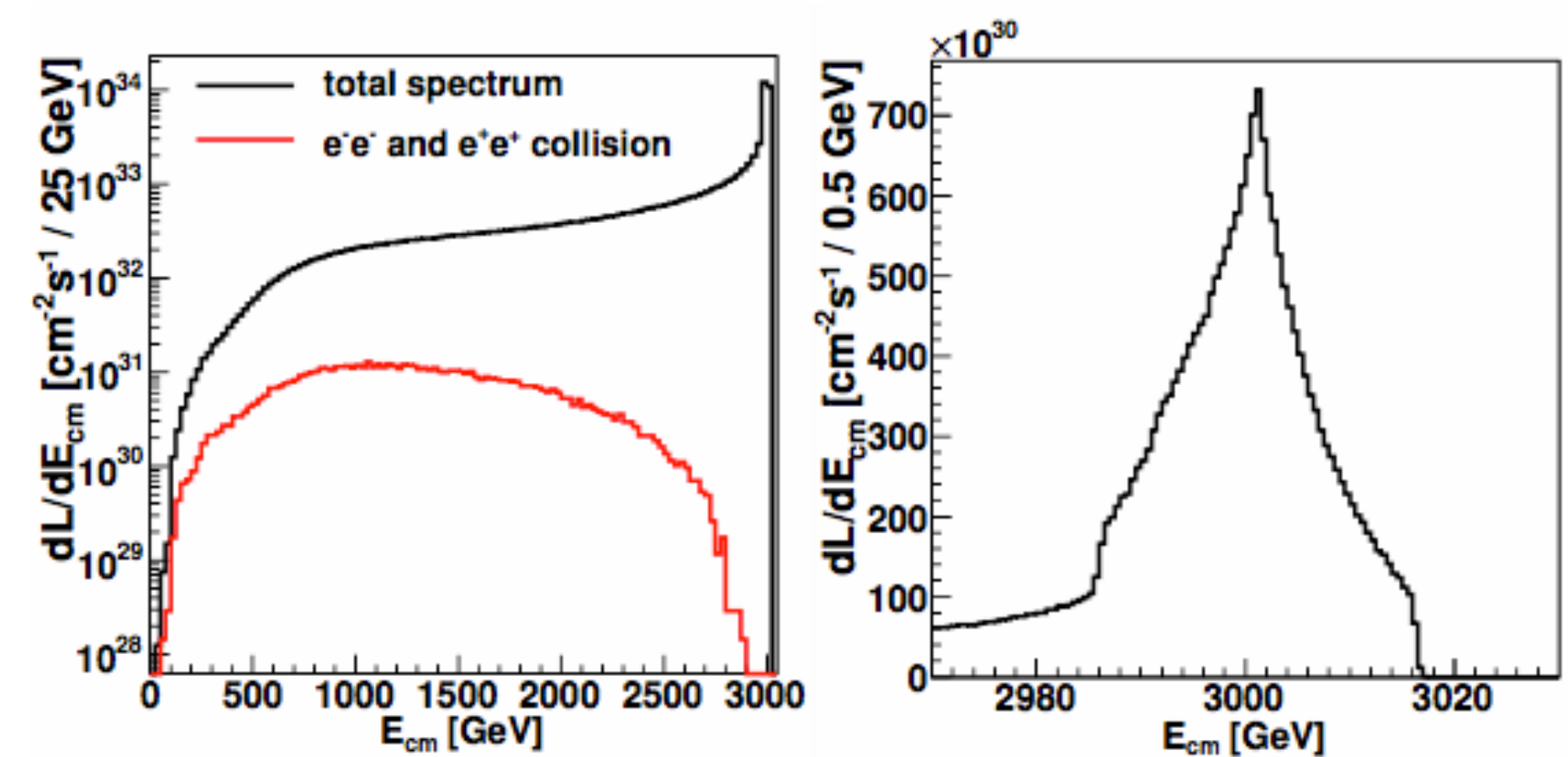
1. Gaussian shape with specific spreads Avail.: ✓
2. Parameterized (delta peak \oplus power law) Avail.: (✓)
3. Generator for 2D histogrammed fit Avail.: [✓]

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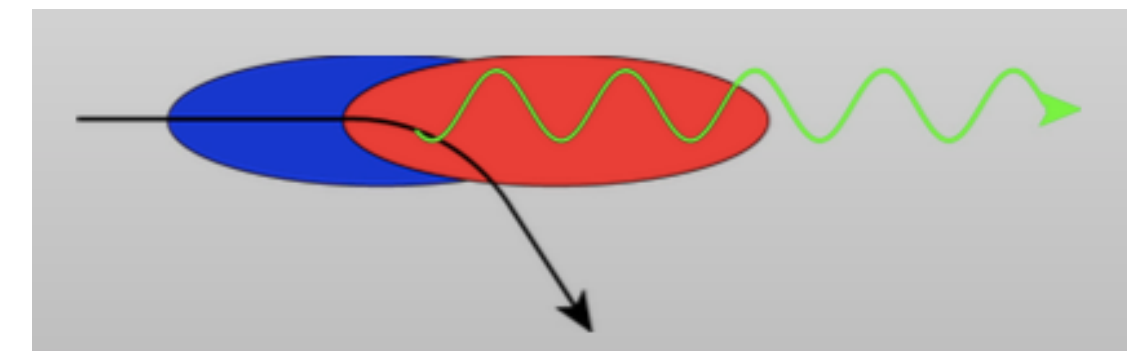
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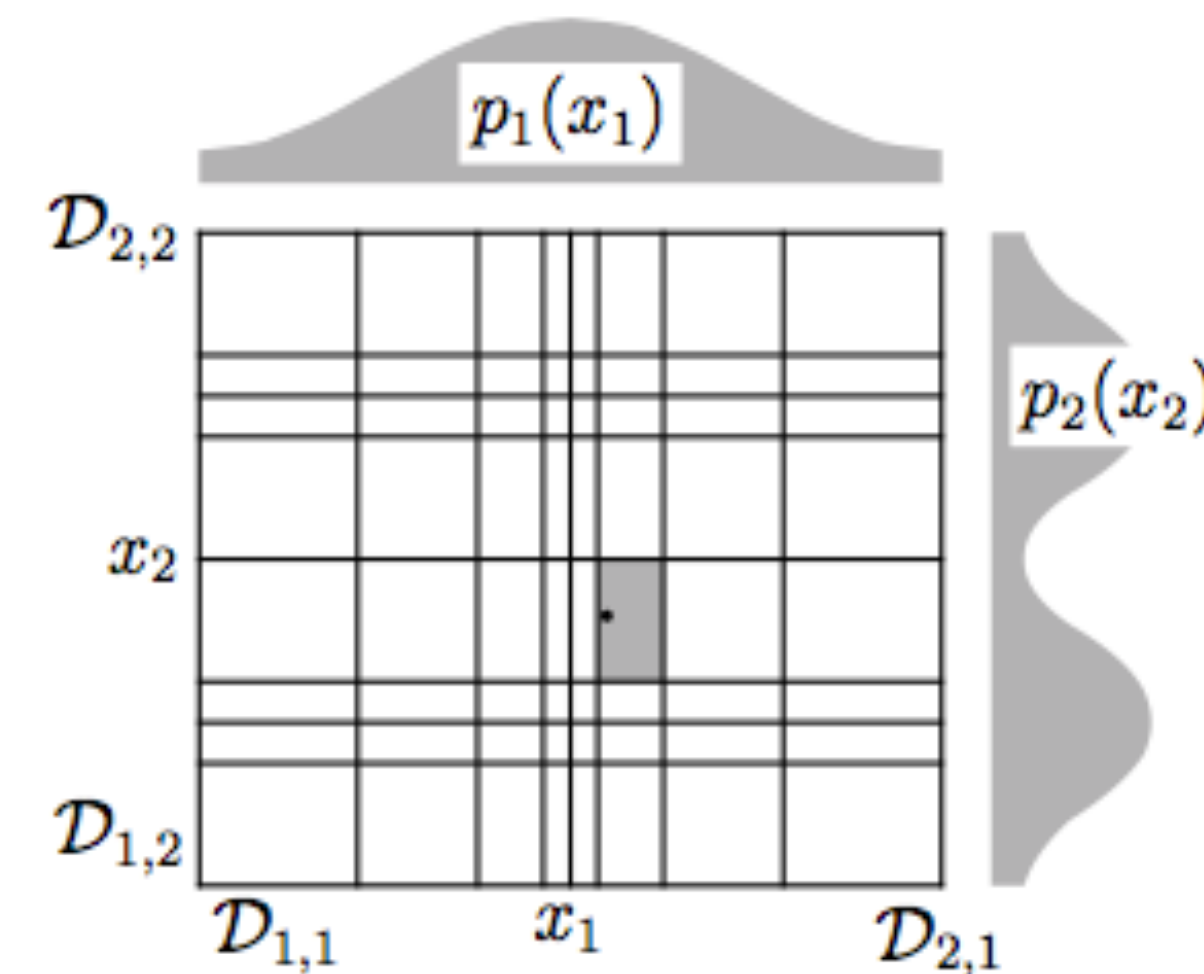
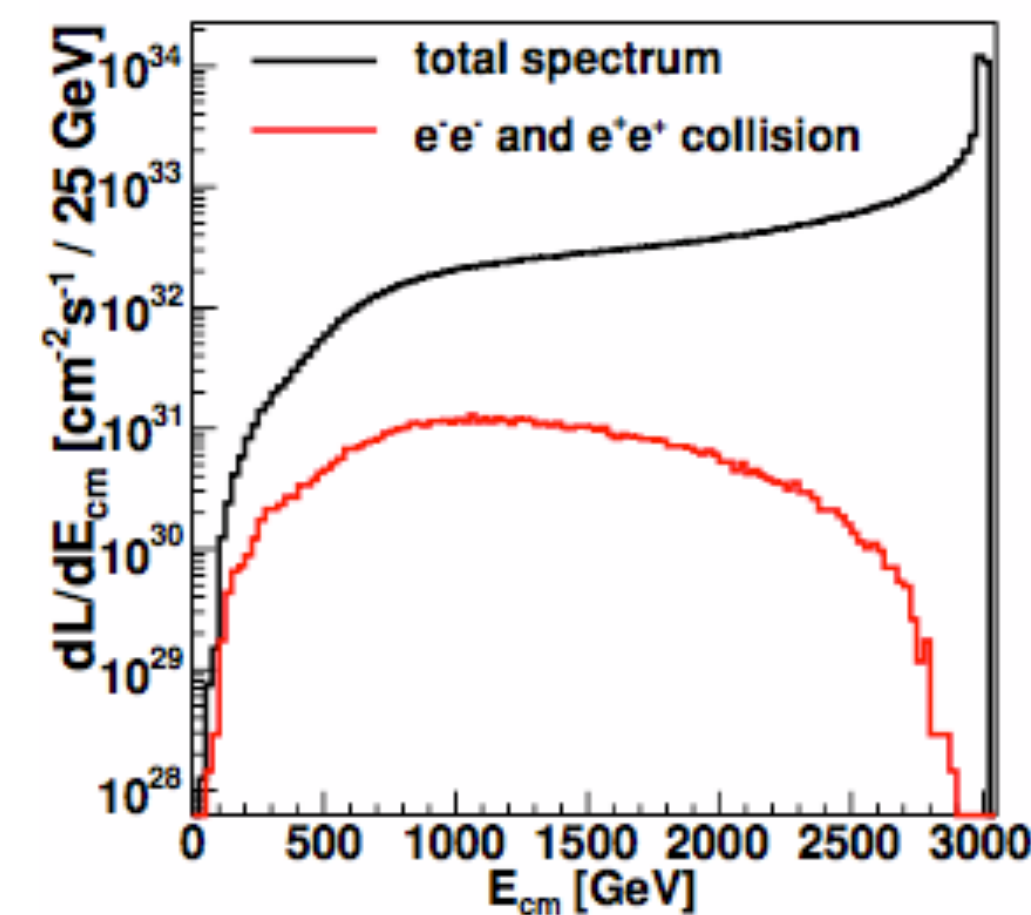
[Dalena/Esbjerg/Schulte \[LCWS 2011\]](#)

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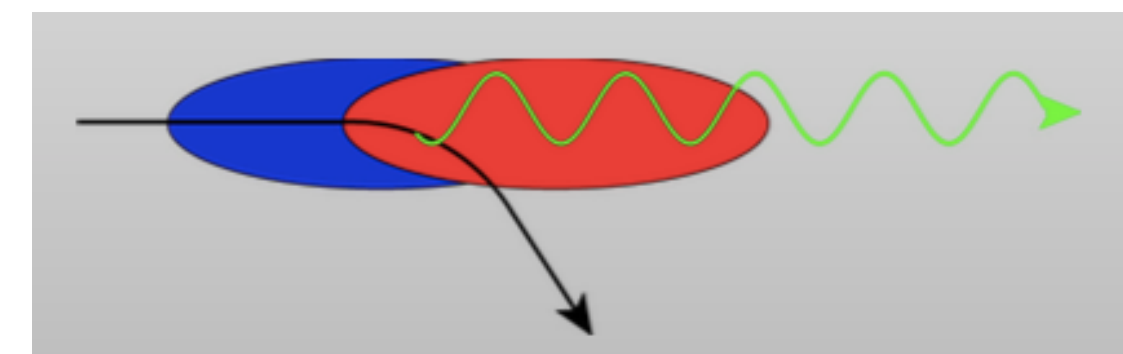


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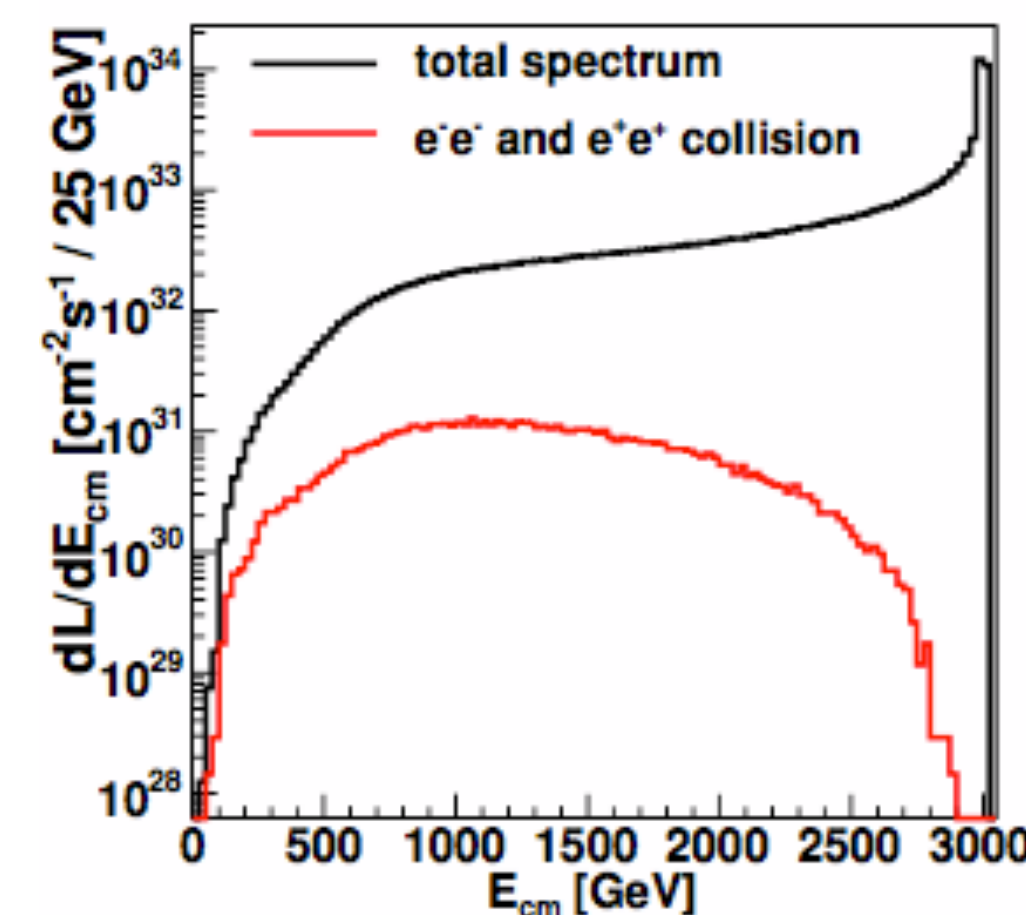
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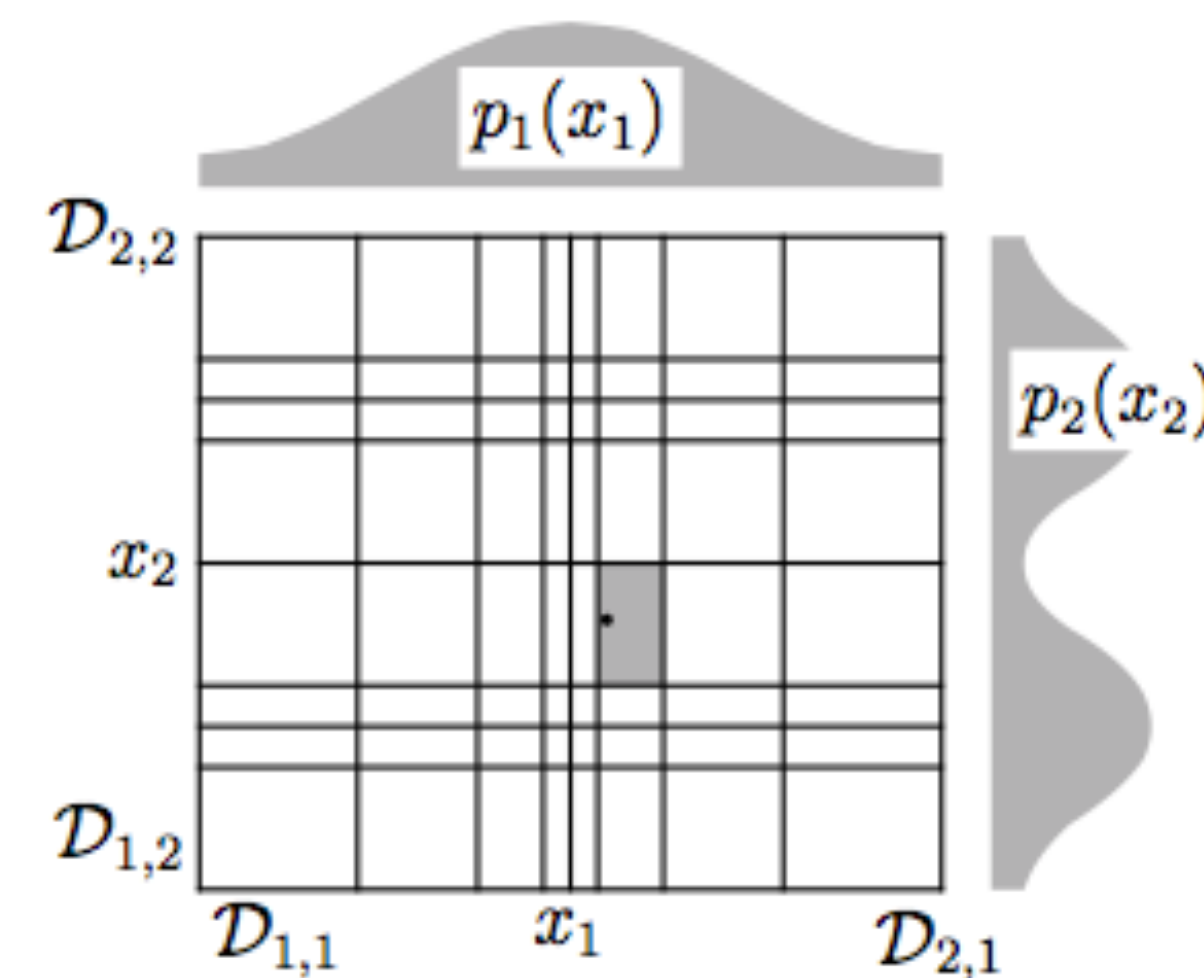
- Pro (1.): Easy implementation, covers main features
- Con (1.): Gaussian approximative, exceeds nominal collider energy
- Pro (2.): Relatively easy implementation
- Con (2.): Delta peak behaves badly in MC, beams maybe not factorizable/simple power law
- Pro (3.): most exact simulation, generator mode avoids artifacts in tails
- Con (3.): only available (yet) in dedicated tools like LumiLinker and CIRCE2



$$L \approx \frac{N}{4\pi\sigma_x\sigma_y} \frac{\eta P_{AC}}{E_{CM}}$$



Dalena/Esbjerg/Schulte [LCWS 2011]

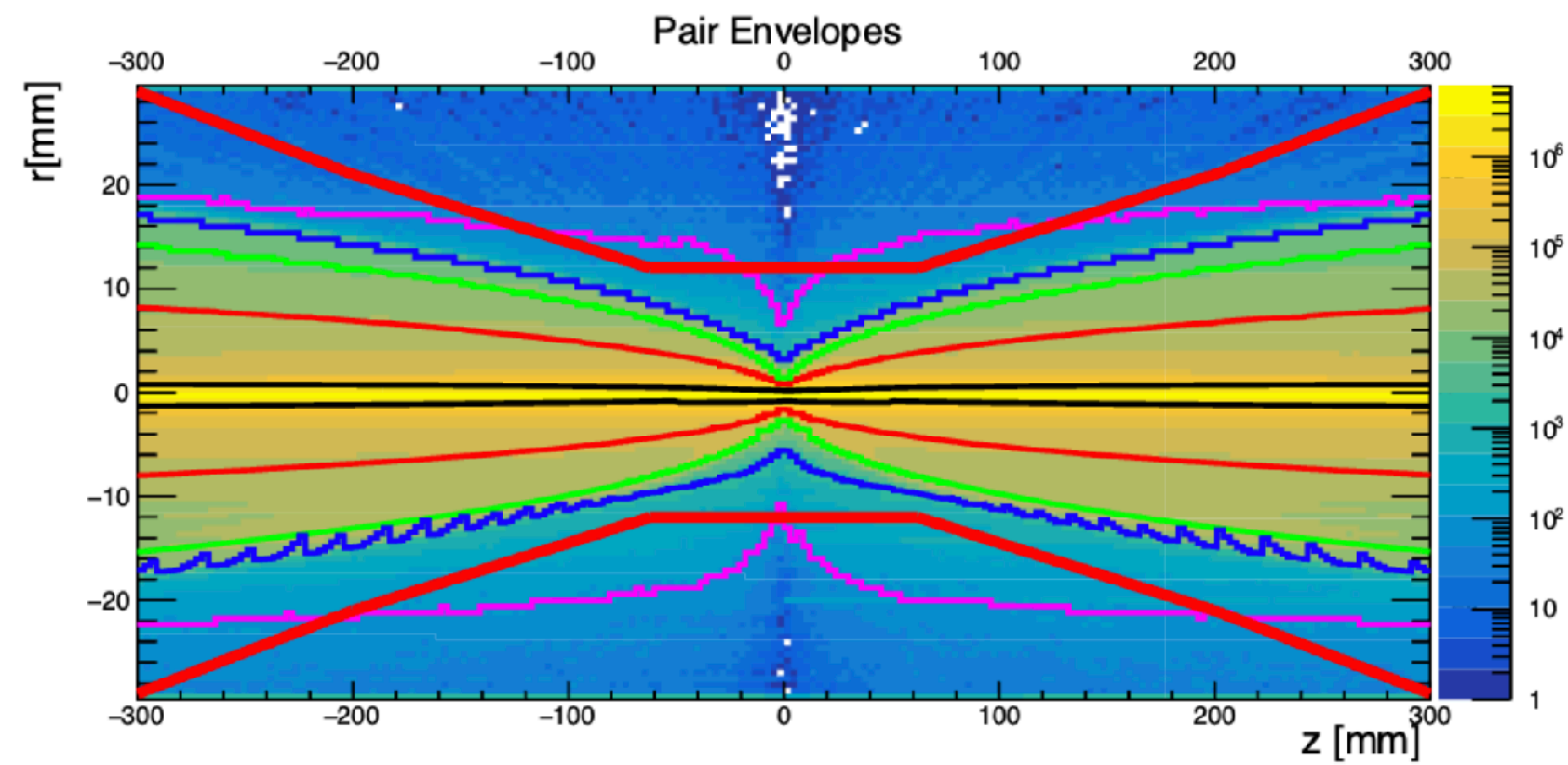


$$D_{B_1 B_2}(x_1, x_2) \neq D_{B_1}(x_1) \cdot D_{B_2}(x_2)$$

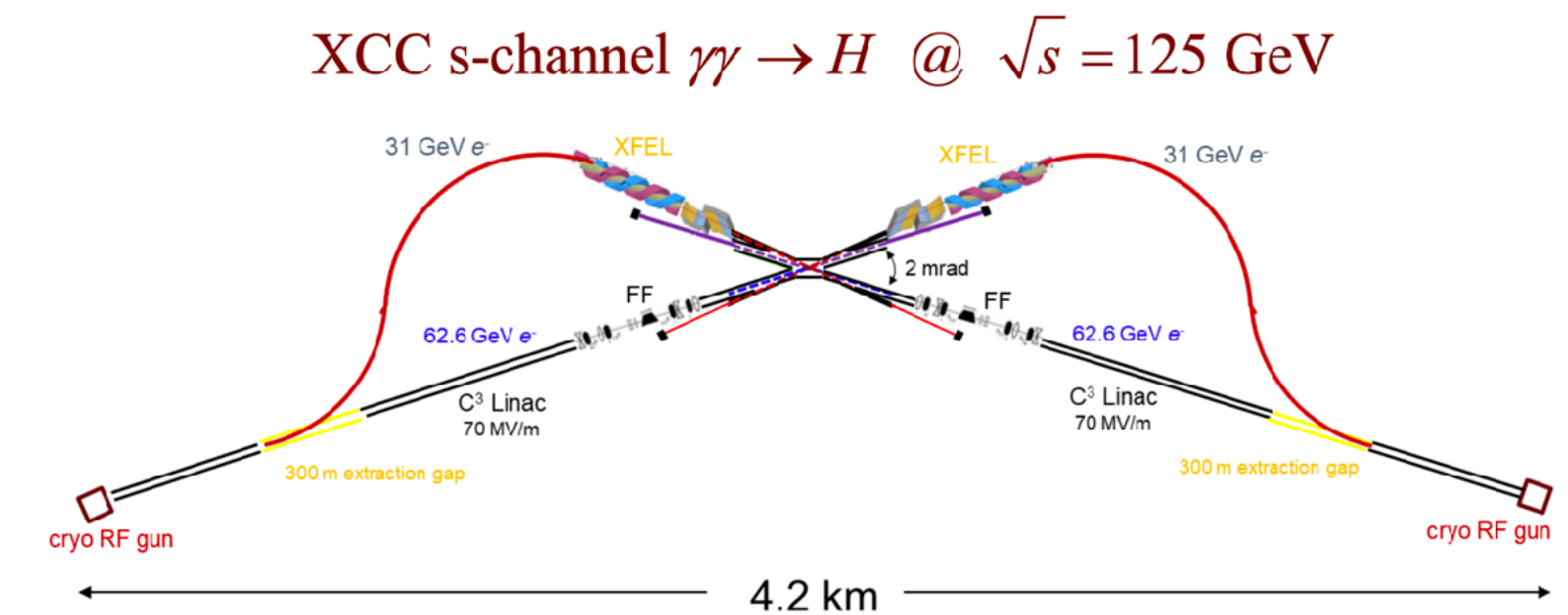
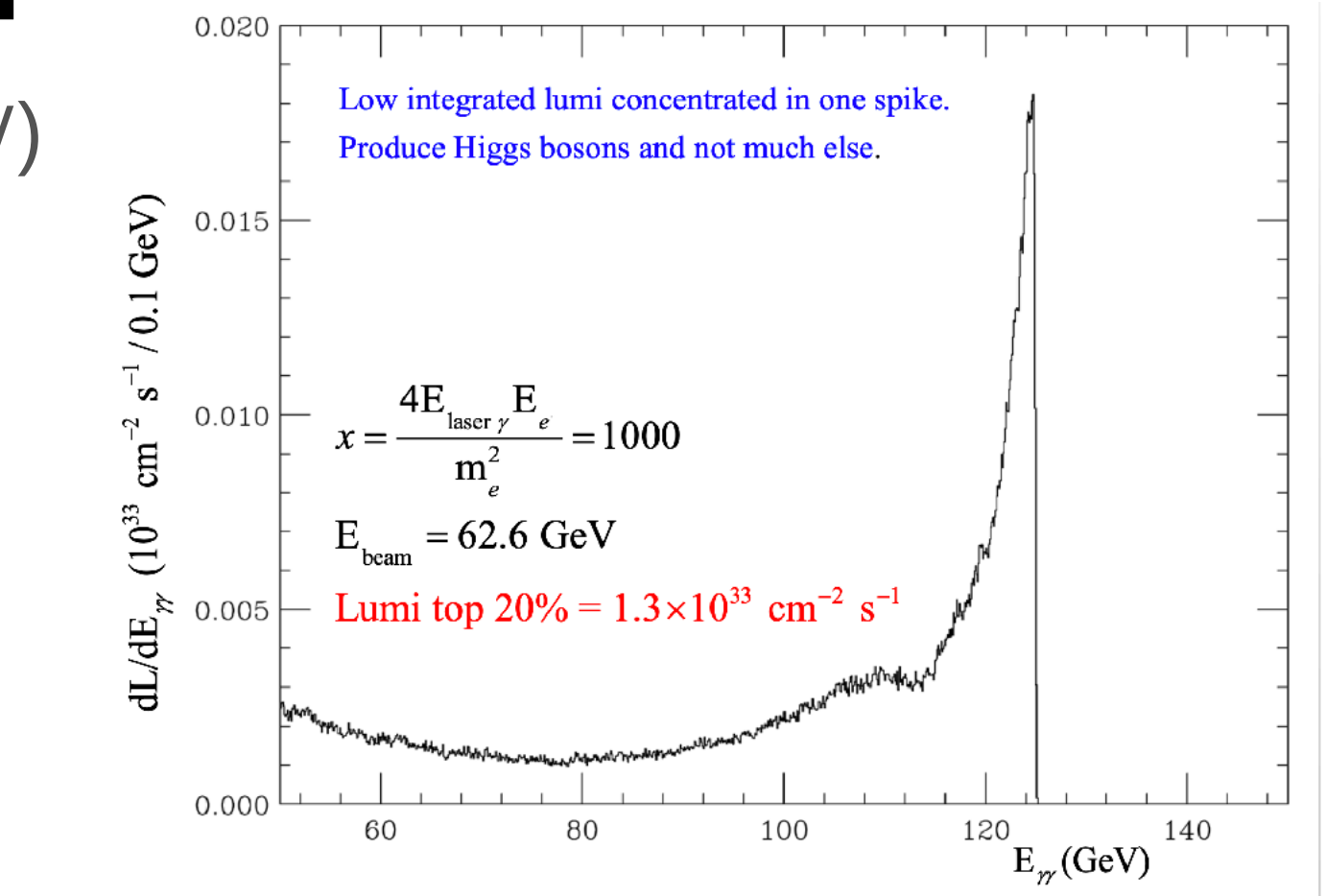
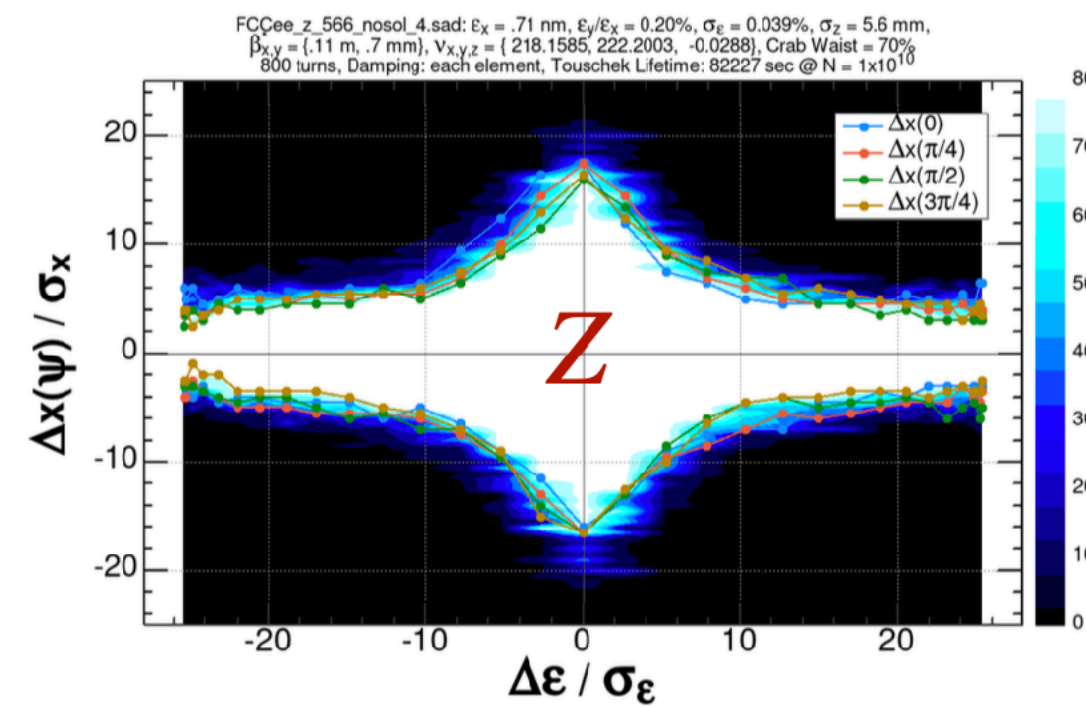
$$D_{B_1 B_2}(x_1, x_2) \neq x_1^{\alpha_1} (1 - x_1)^{\beta_1} x_2^{\alpha_2} (1 - x_2)^{\beta_2}$$

- New beam simulations for FCC-ee: 4 IPs \Rightarrow 1.7x lumi (91 GeV) / 1.8x lumi (161/250 GeV)
- New beam simulations for CCC and XCC (photon collider simulations)
- Photon collider simulations *not* possible with parameterized spectra
- Conclusion: CIRCE2-like sampling most versatile/general approach

[Katsunobu Oide, FCC week]

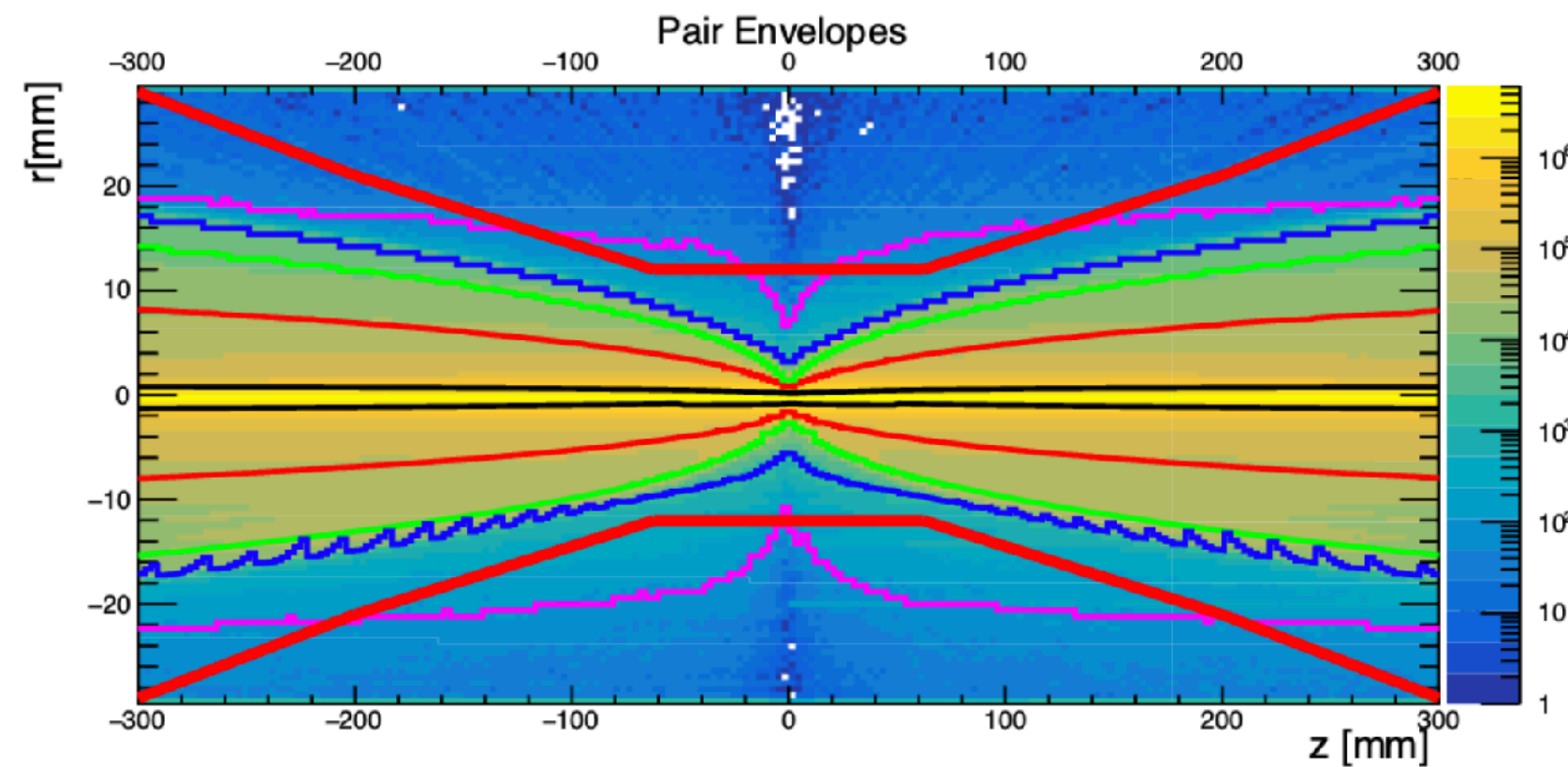


Dynamic aperture (z-x)



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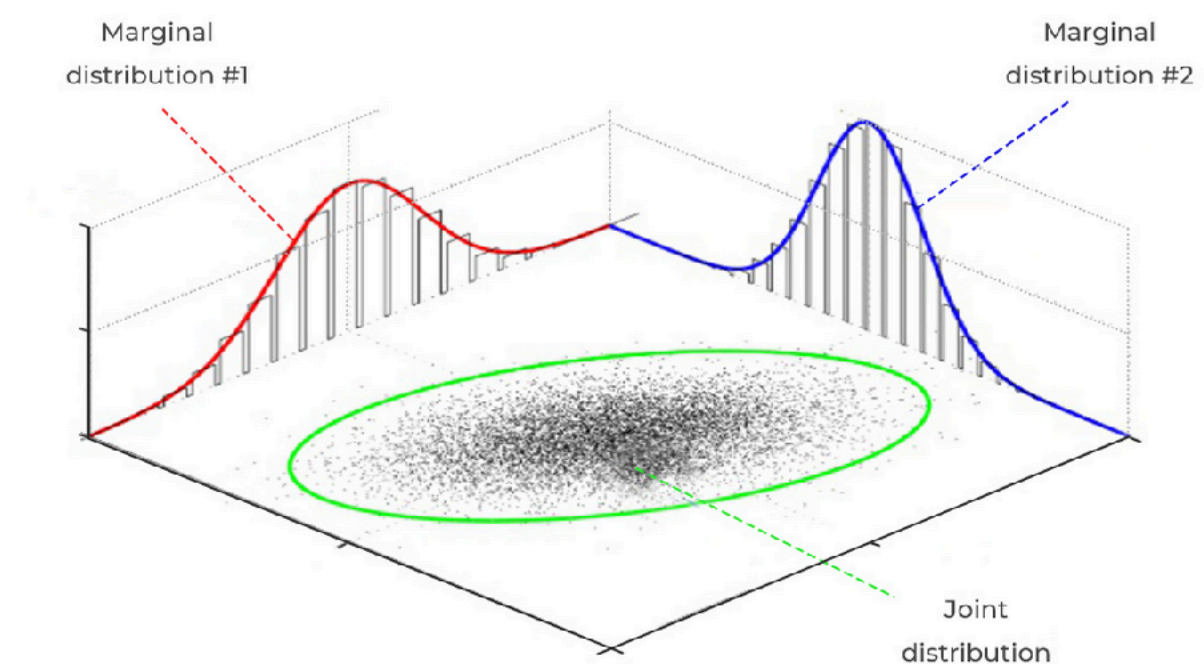
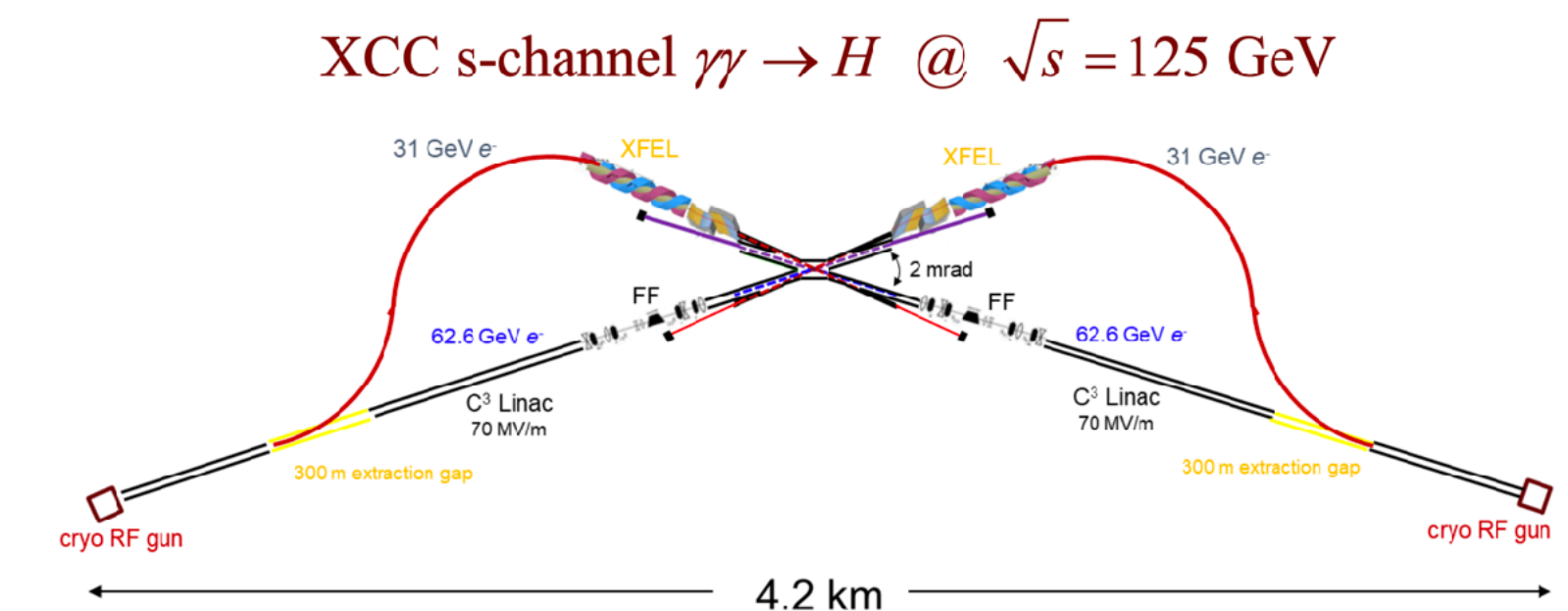
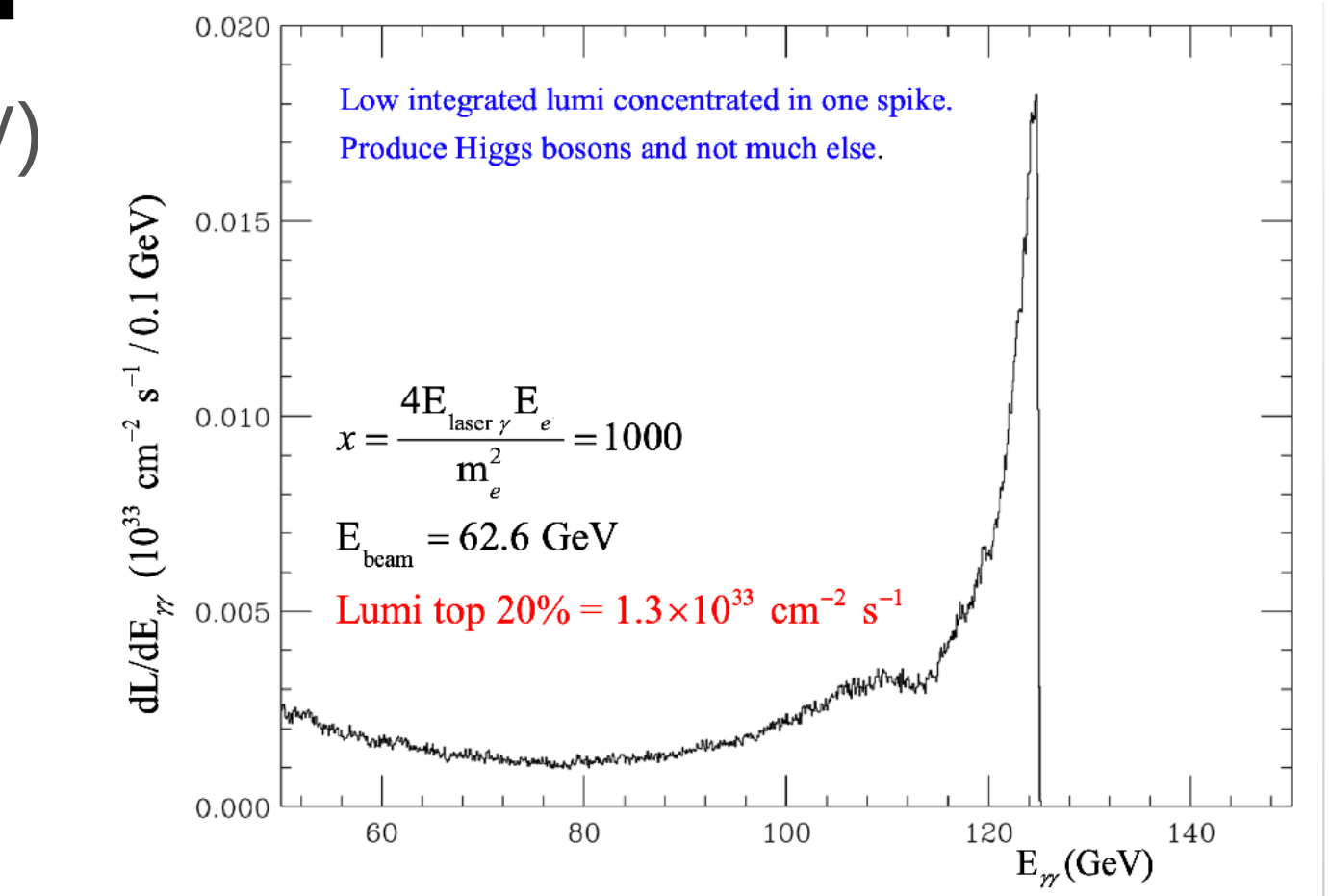
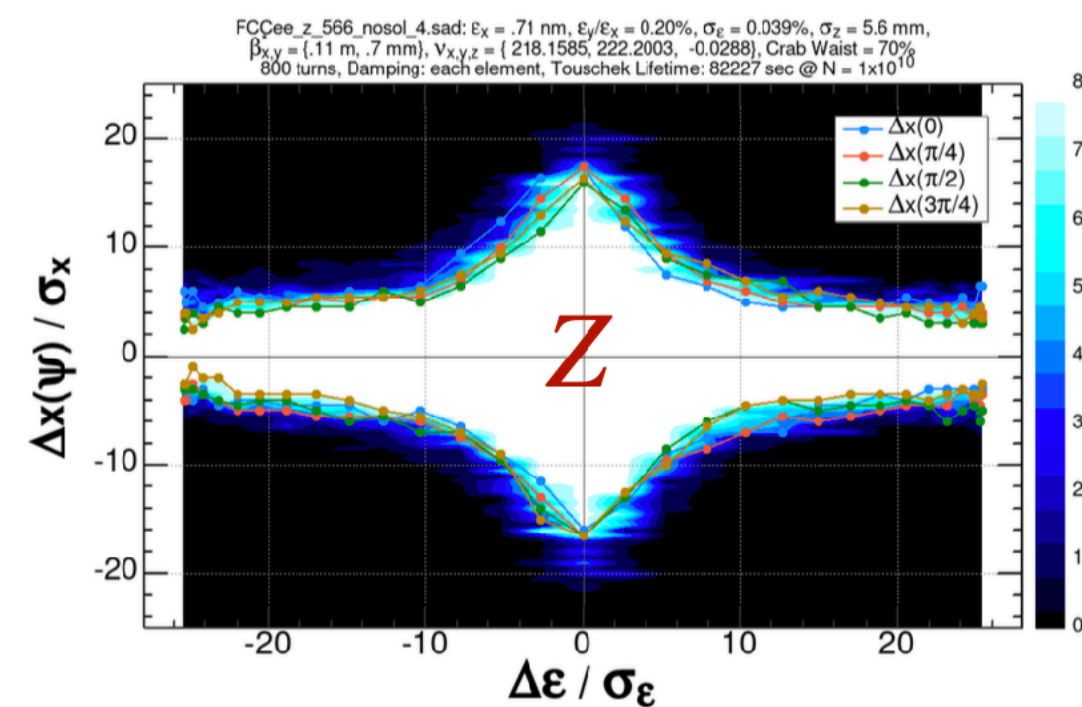
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Open Issues

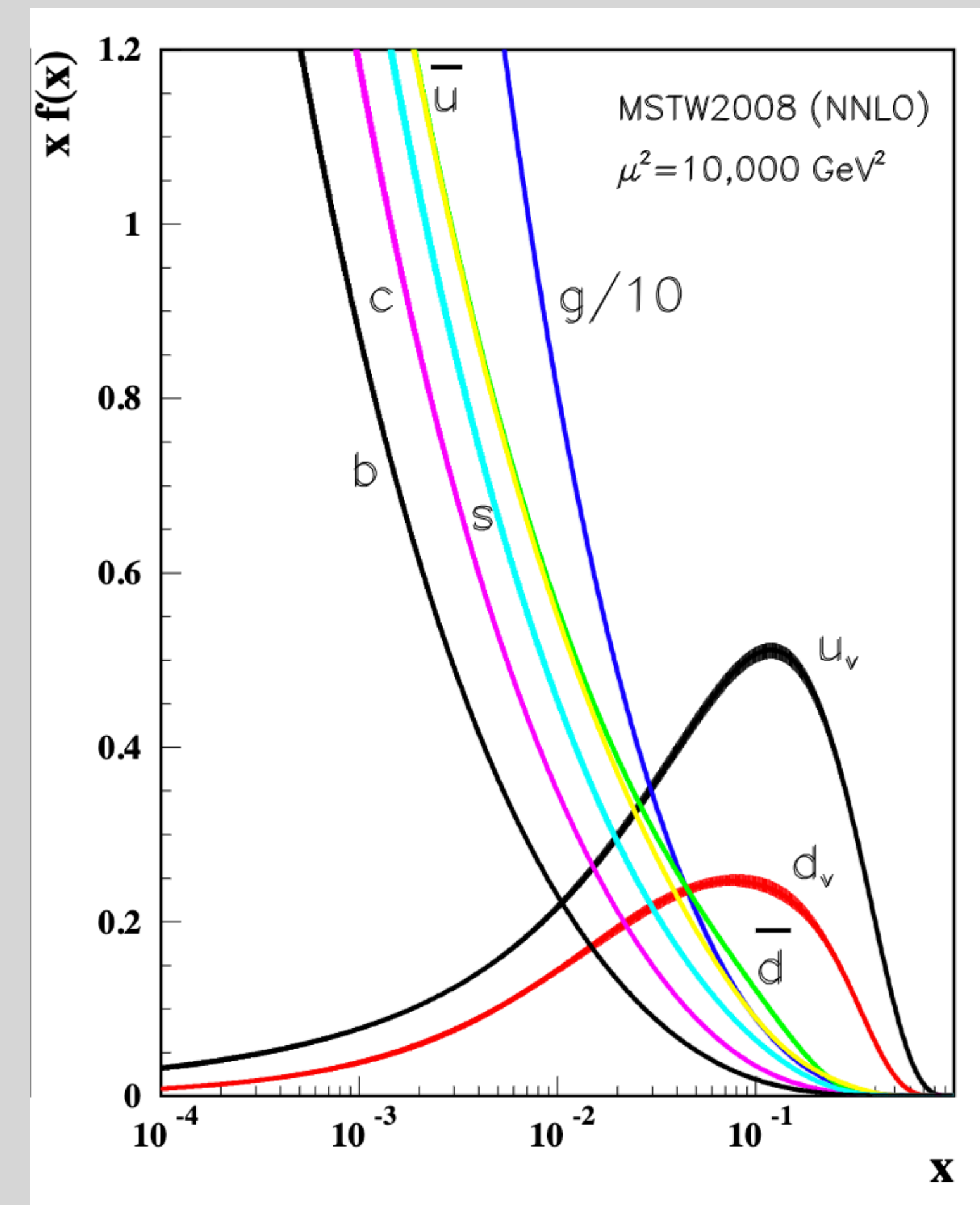
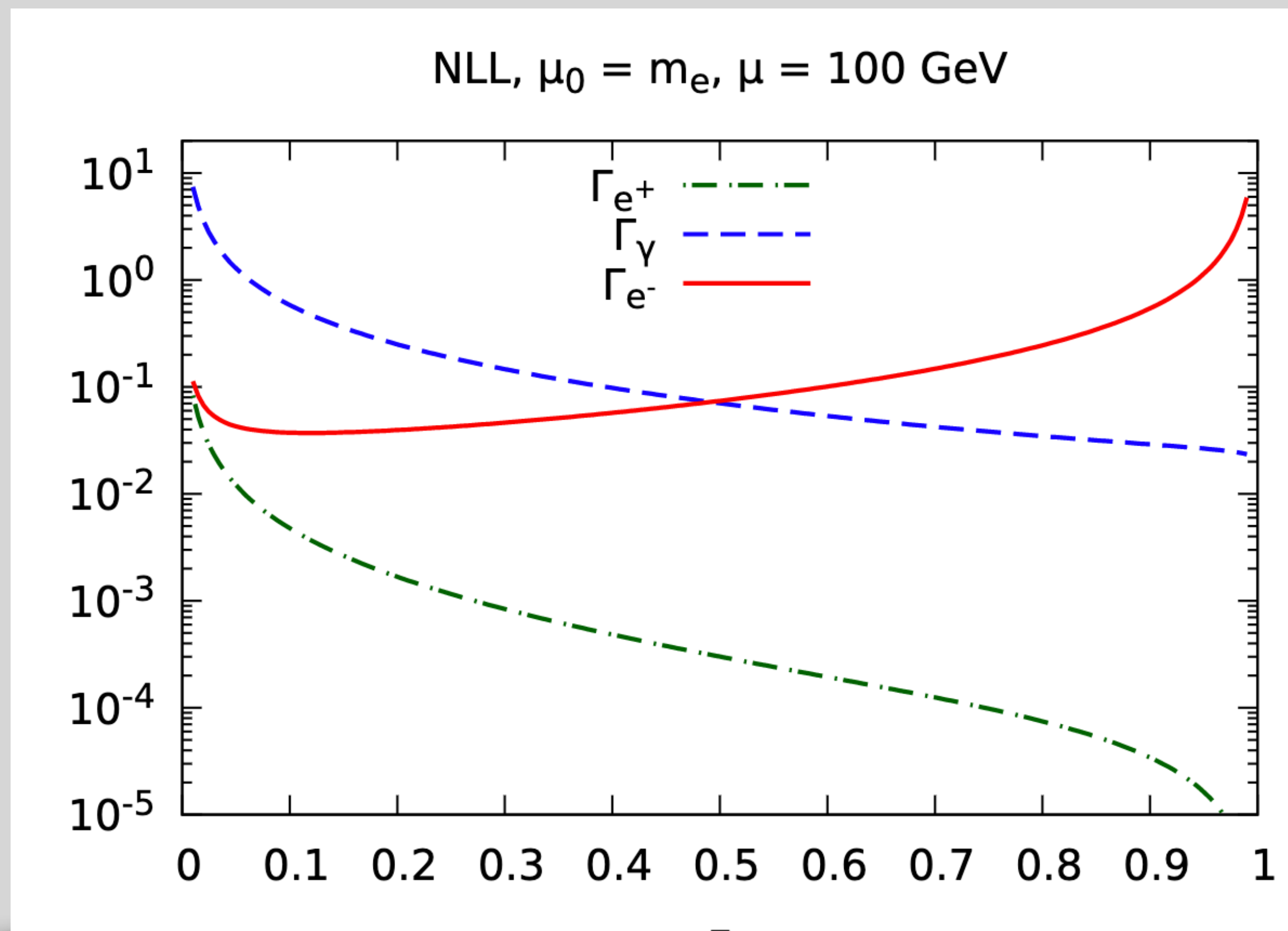
- Still several Higgs factories missing in general beam spectrum repository
- Machine learning for sampling beam spectra not yet started (expected performance?)
- 2D-/3D-structure of beam spectra (z-dependence, copulas)

Dynamic aperture (z-x)



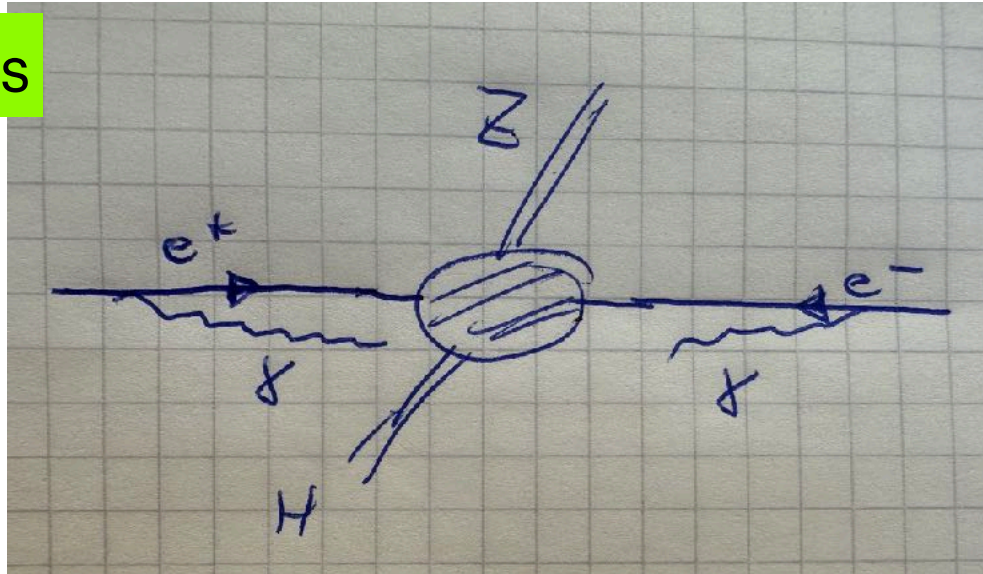
Initial State Radiation — Lepton PDFs

8 / 26



Collinear logarithms

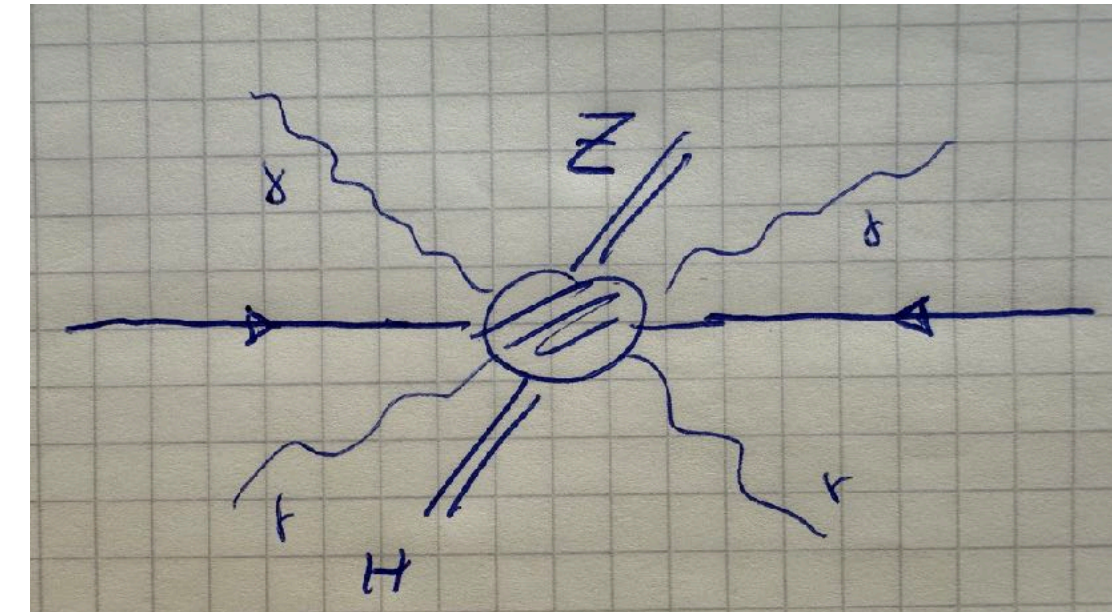
$$L = \log \frac{Q^2}{m^2}$$



$$\sigma = \alpha^b \sum_{n=0}^{\infty} \alpha^n \sum_{i=0}^n \sum_{j=0}^n \varsigma_{n,i,j} L^i \ell^j$$

Soft logarithms

$$\ell = \log \frac{Q^2}{\langle E_\gamma \rangle^2}$$



• Different factorization schemes: focus on collinear logs, $\log \frac{Q^2}{m_\mu^2}$, vs. soft logs, $\log \frac{Q^2}{E_\gamma^2}$, cf. [2203.12557](#)

• YFS (Yennie-Frautschi-Suura), cf. e.g. [2203.10948](#)

$$d\sigma = \sum_{n_\gamma}^{\infty} \frac{\exp[Y_{res.}]}{n_\gamma!} \prod_{j=1}^{n_\gamma} [d\text{LIPS}_j^\gamma S_{res.}(k_j)] [\sigma_0 + \text{corrections}]$$

- Universal soft exponentiation factor, provides n_γ exclusive resolved photons with (almost) exact kinematics
- Exponentiation at amplitude level (CEEX) oder squared ME level (EEX)
- Implemented in LEP legacy MCs (BHLUMI/BHWIDE, KORAL(W/Z), KKMC-ee, YFS(WW/ZZ), also: Sherpa, w.i.p.: Whizard
- Can be systematically improved at fixed-order level by higher-order corrections

• Collinear factorization: universal QED ePDFs,

$$\text{LL: } (\alpha L)^k, \text{ NLL: } \alpha(\alpha L)^{k-1}$$

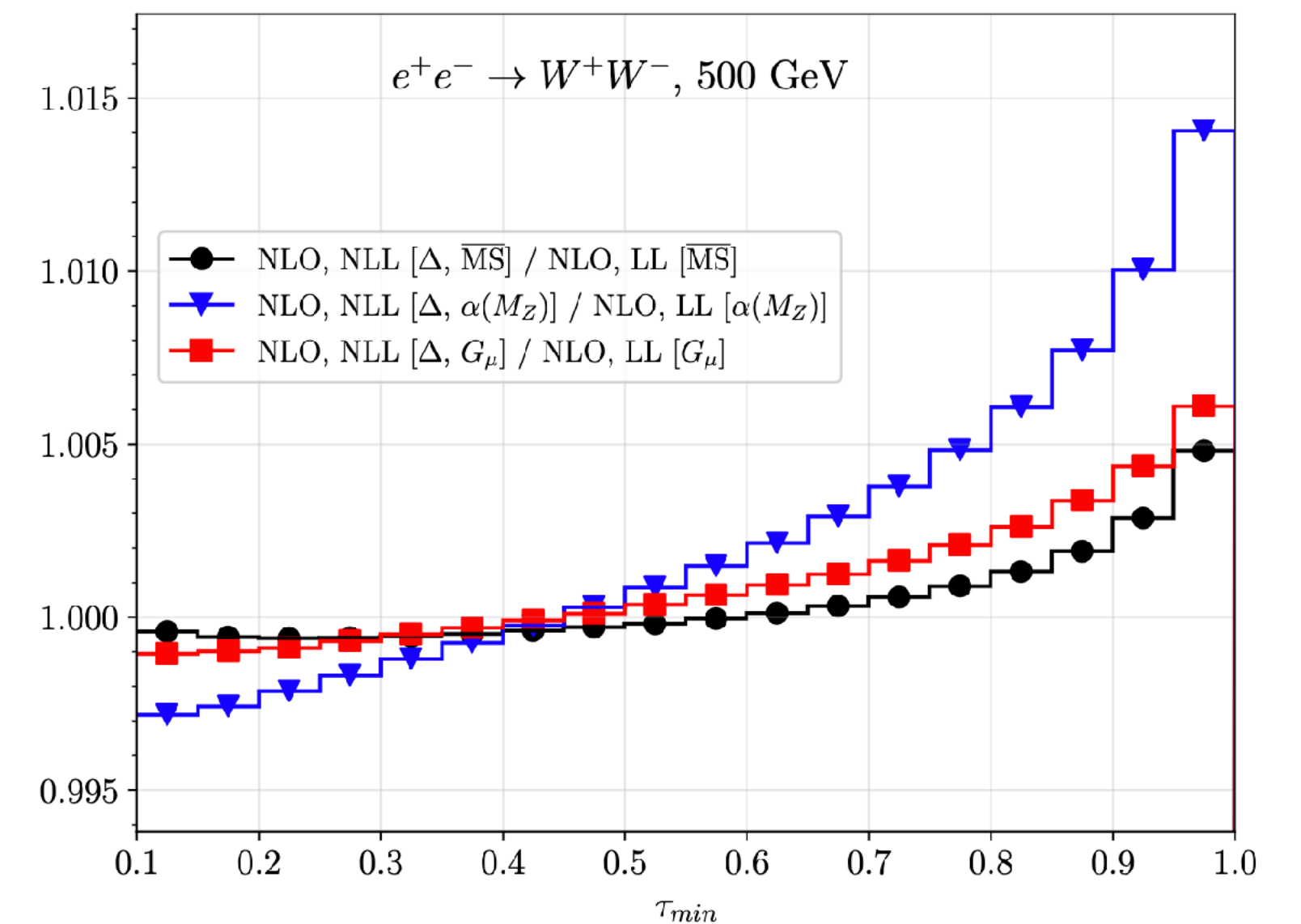
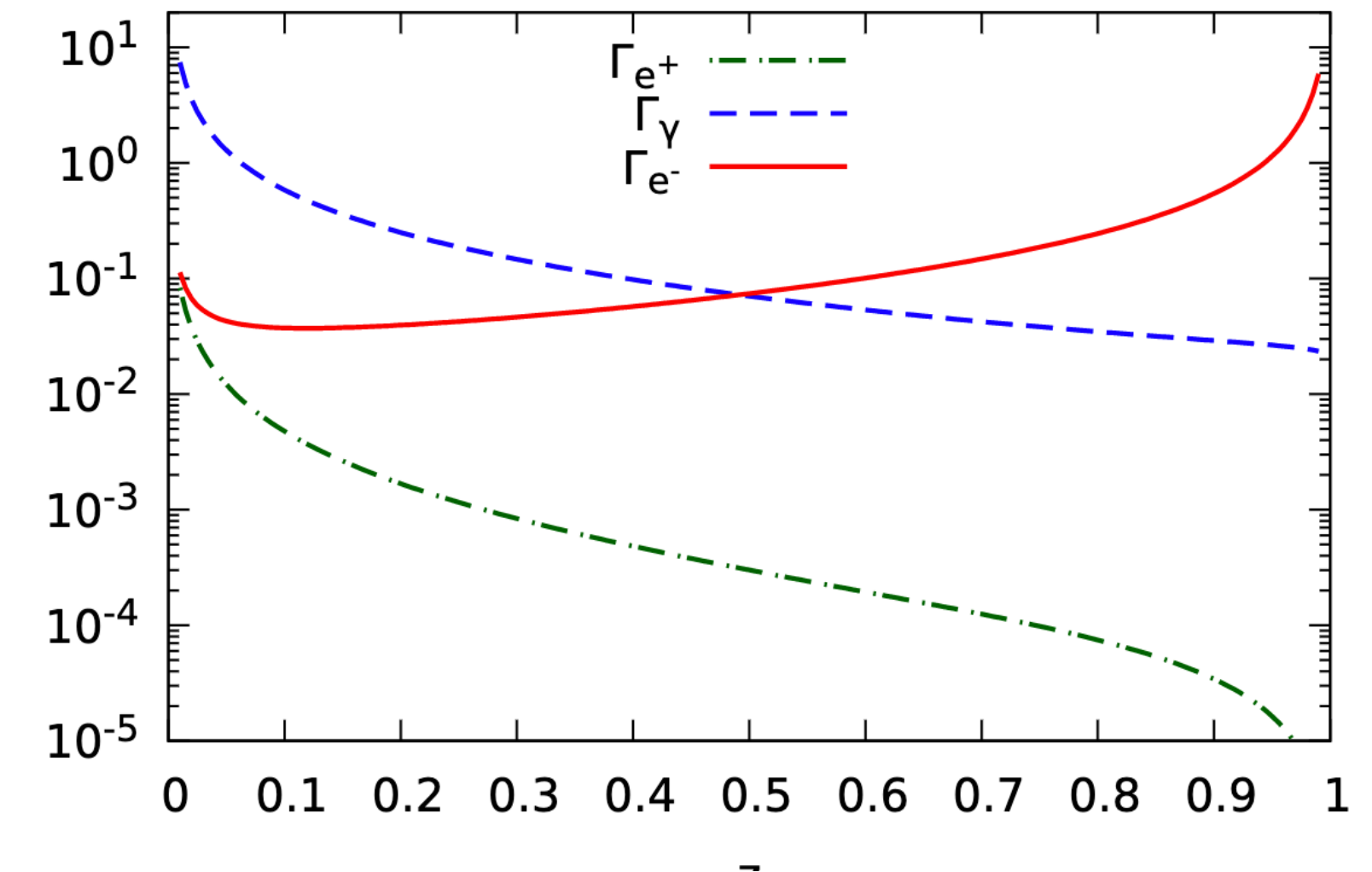
$$d\sigma_{kl}(p_k, p_l) = \sum_{ij=e^+, e^-, \gamma} \int dz_+ dz_- \Gamma_{i/k}(z_+, \mu^2, m^2) \Gamma_{j/l}(z_-, \mu^2, m^2) \times d\hat{\sigma}_{ij}(z_+ p_k, z_- p_l, \mu^2) + \mathcal{O}\left(\left(\frac{m^2}{s}\right)^p\right)$$

Integrable power-like singularity $1/(1-z)$ for $z \rightarrow 1$

- Collinear resummation LO/LL Gribov/Lipatov, 1972; Kuraev/Fadin, 1985;
Skrzypek/Jadach, 1992; Cacciari/Deandrea/Montagna/Nicrosini, 1992
- NLO QED PDFs, collinear evolution @ NLL
Frixione, 1909.0388; Bertone/Cacciari/Frixione/Stagnitto, 1911.12040 + 2207.03265; Talk by Marco Zaro
- **Inclusive in all initial-state photons**
- Gives most precise normalization of total cross section: 2-4 per mille
- Numerical stability differs in different QED renormalization schemes, DIS vs. $\overline{\text{MS}}$
- Also: fast interpolation (CTEQ-like) grids available
- Implementations available in MG5 and Whizard
- Different levels of precision possible: NLL+NLO, LL+NLO, LL+NLO, LL+LO
- Different names in literature: electron structure functions, ISR structure functions
- “Photon PDF” (a.k.a. EPA, Weizsäcker-Williams) Γ_γ , peaked at small z
- Very well known from ILC/CLIC simulations: “virtual photon”-induced processes

ePDFs for polarized leptons !?

NLL, $\mu_0 = m_e$, $\mu = 100 \text{ GeV}$

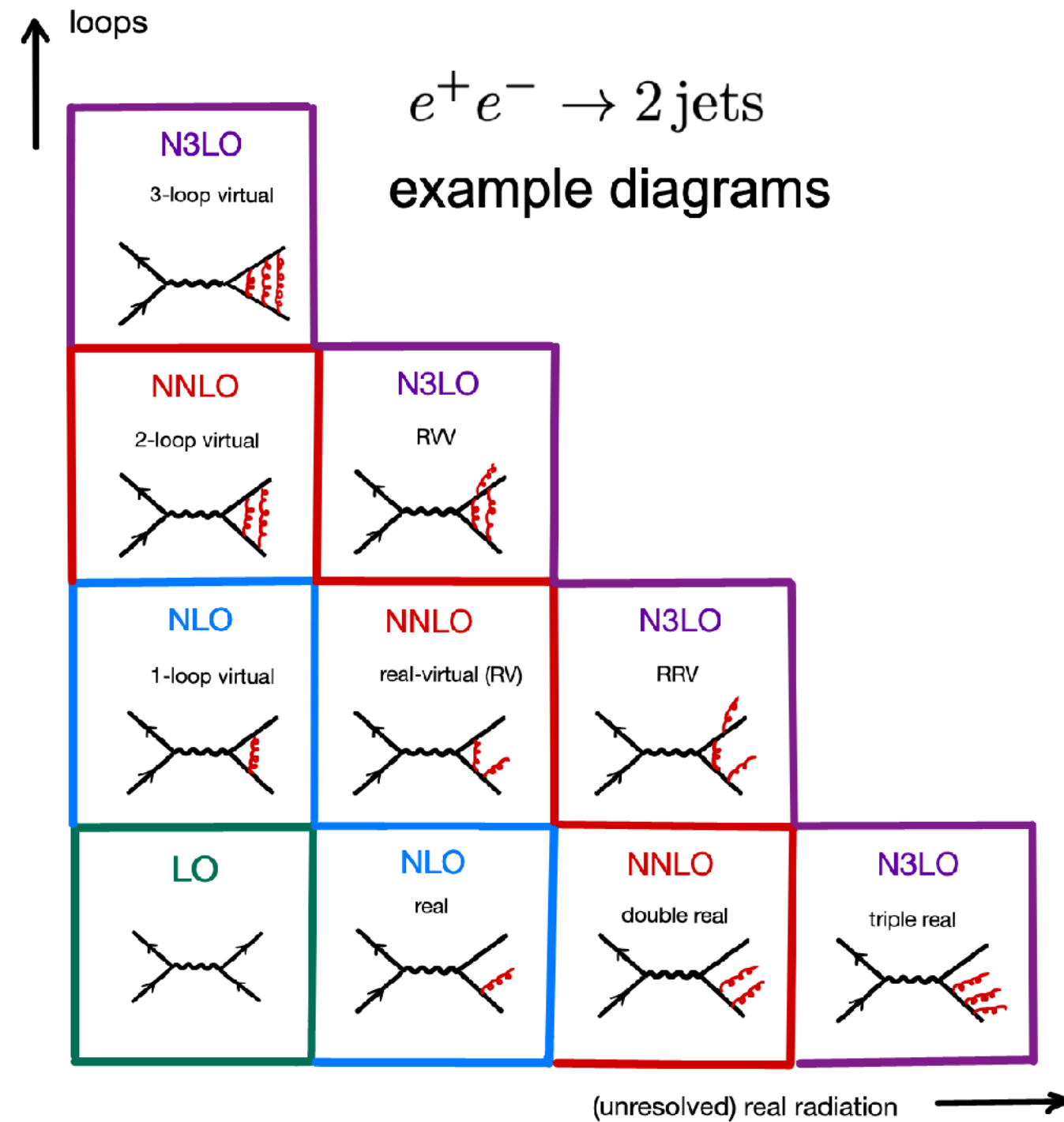




Getty Villa, Pacific Palisades, Etruscan, 525 BC

The “Exclusive” Frontier — fN(N)LO, Automation in MCs

12 / 26



► LO + NLO QCD \oplus EW automated: Sherpa, MG5, Whizard

► Note the fine-prints

► Signal and background samples at full SM QFT interference level

► Need $e^+e^- \rightarrow 2f, 3f, 4f, 5f, 6f, [7-10f]$ @ NLO QCD \oplus EW (arbitrary cuts, fully differential)

NLO QCD

	$\sigma_{\text{LO}}[\text{fb}]$	$\sigma_{\text{NLO}}[\text{fb}]$	K
$e^+e^- \rightarrow jj$	622.737(8)	639.39(5)	1.027
$e^+e^- \rightarrow jjj$	340.6(5)	317.8(5)	0.933
$e^+e^- \rightarrow jjjj$	105.0(3)	104.2(4)	0.992
$e^+e^- \rightarrow jjjjj$	22.33(5)	24.57(7)	1.100
$e^+e^- \rightarrow jjjjjj$	3.583(17)	4.46(4)	1.245
$e^+e^- \rightarrow t\bar{t}$	166.37(12)	174.55(20)	1.049
$e^+e^- \rightarrow t\bar{t}j$	48.12(5)	53.41(7)	1.110
$e^+e^- \rightarrow t\bar{t}jj$	8.592(19)	10.526(21)	1.225
$e^+e^- \rightarrow t\bar{t}jjj$	1.035(4)	1.405(5)	1.357

NLO EW

Pia Bredt, Phd thesis, DESY, 2022

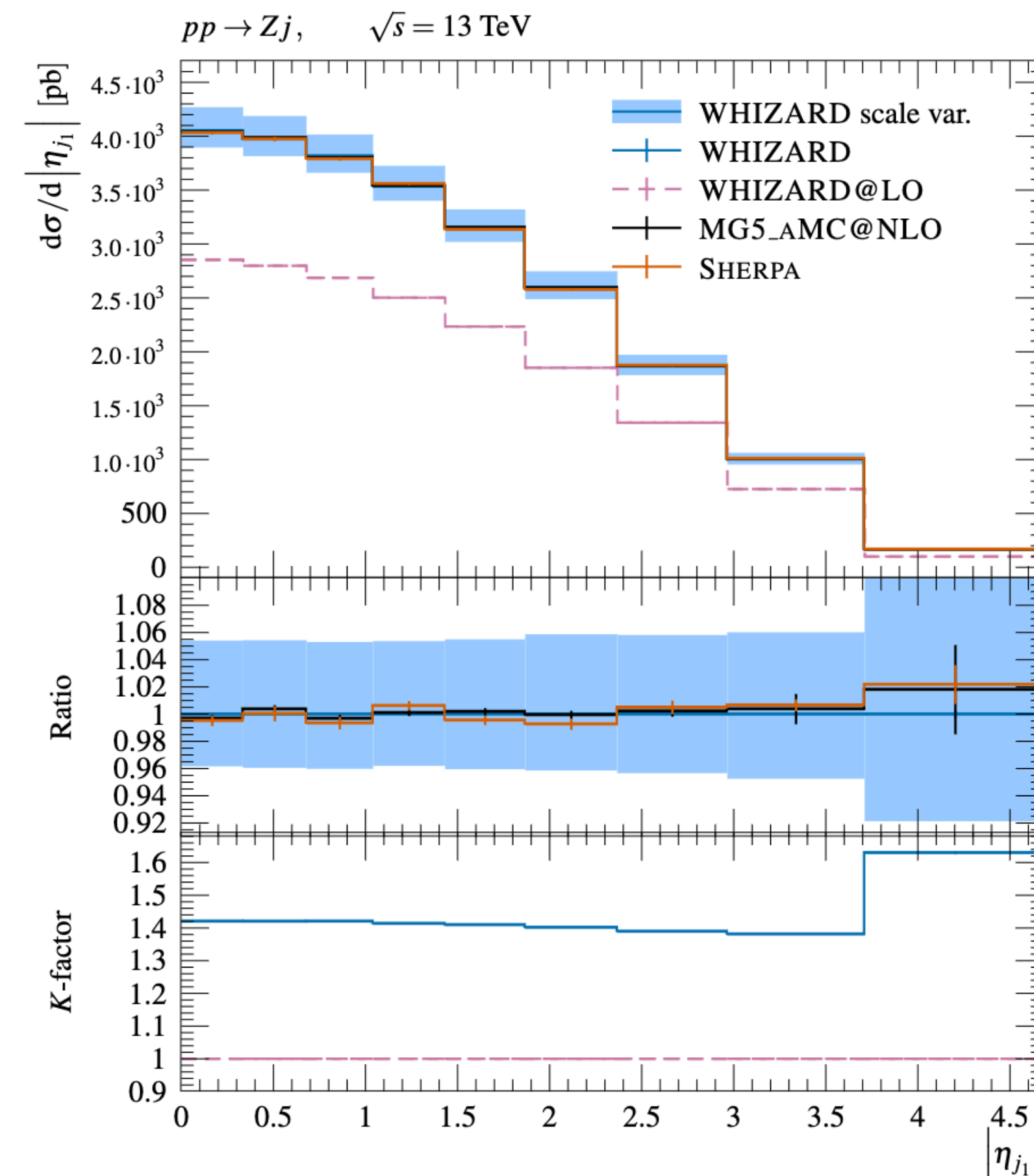
\sqrt{s} [GeV]	MCSANCee[37]		WHIZARD+RECOLA			σ^{sig} (LO/NLO)
	$\sigma_{\text{LO}}^{\text{tot}}$ [fb]	$\sigma_{\text{NLO}}^{\text{tot}}$ [fb]	$\sigma_{\text{LO}}^{\text{tot}}$ [fb]	$\sigma_{\text{NLO}}^{\text{tot}}$ [fb]	δ_{EW} [%]	
250	225.59(1)	206.77(1)	225.60(1)	207.0(1)	−8.25	0.4/2.1
500	53.74(1)	62.42(1)	53.74(3)	62.41(2)	+16.14	0.2/0.3
1000	12.05(1)	14.56(1)	12.0549(6)	14.57(1)	+20.84	0.5/0.5



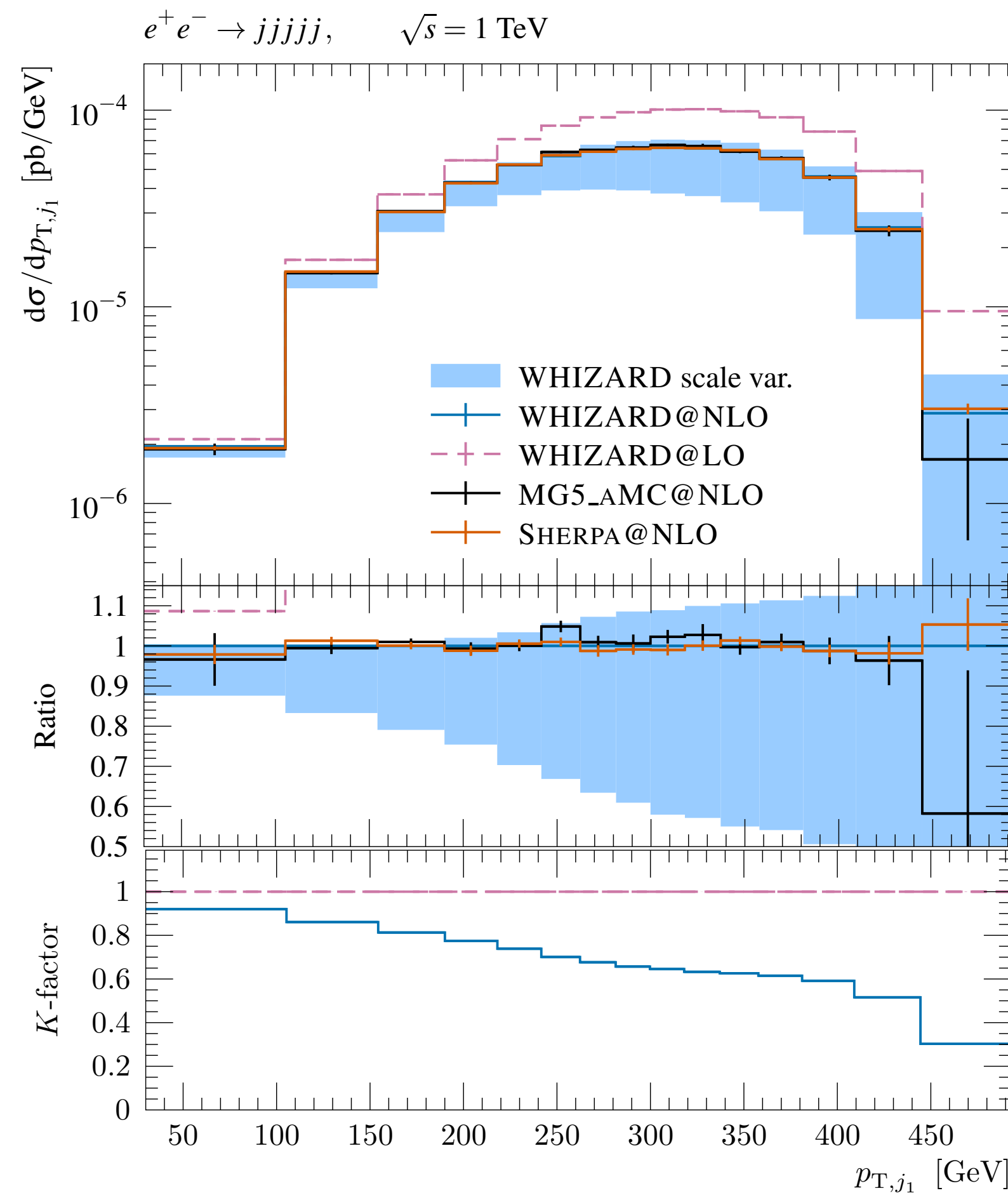
The “Exclusive” Frontier — fN(N)LO, Automation in MCs

13 / 26

pp @ 13 TeV, NLO QCD

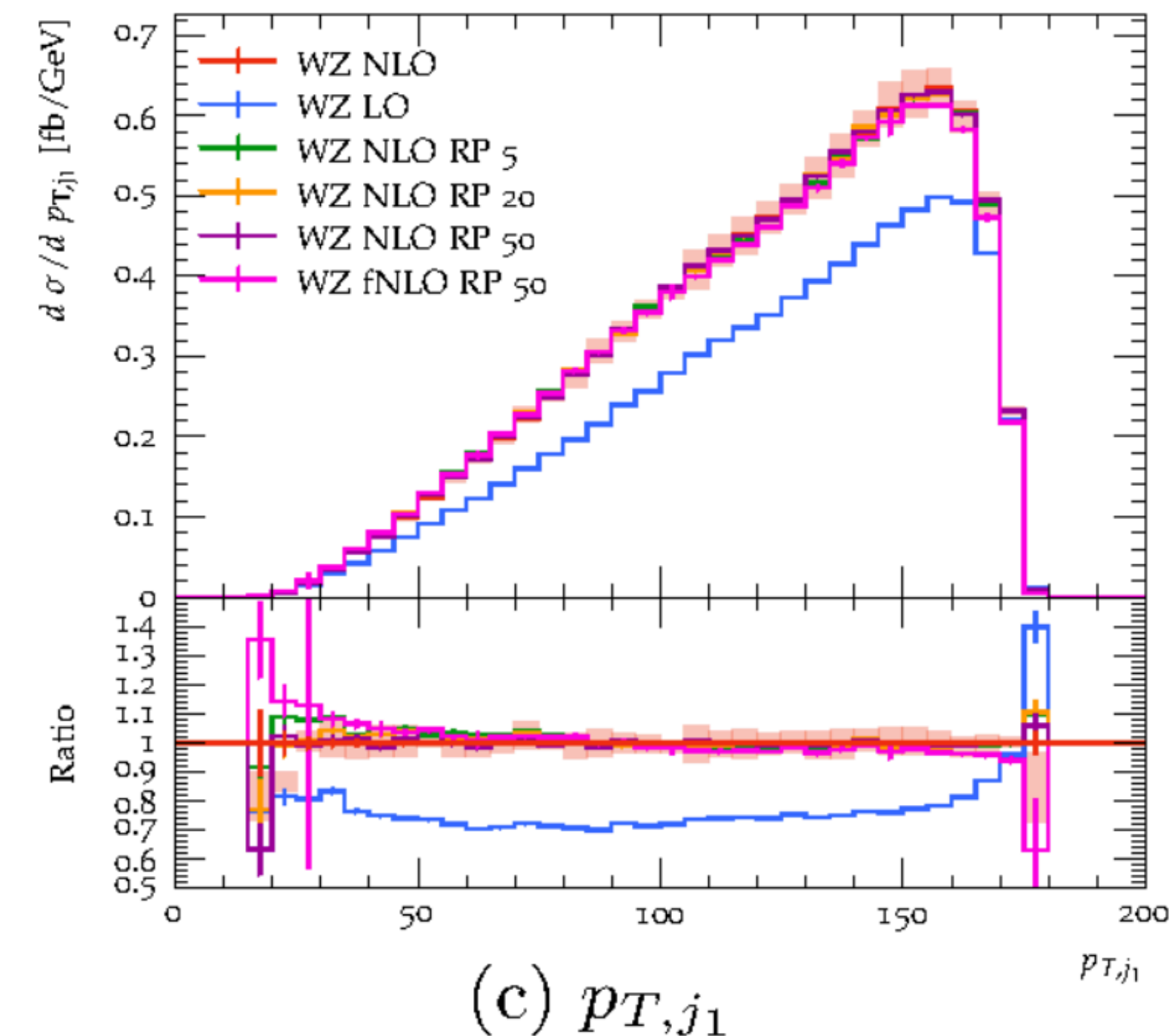


ee @ 1 TeV, NLO QCD



ILC 500: $e^+e^- \rightarrow t\bar{t}j$

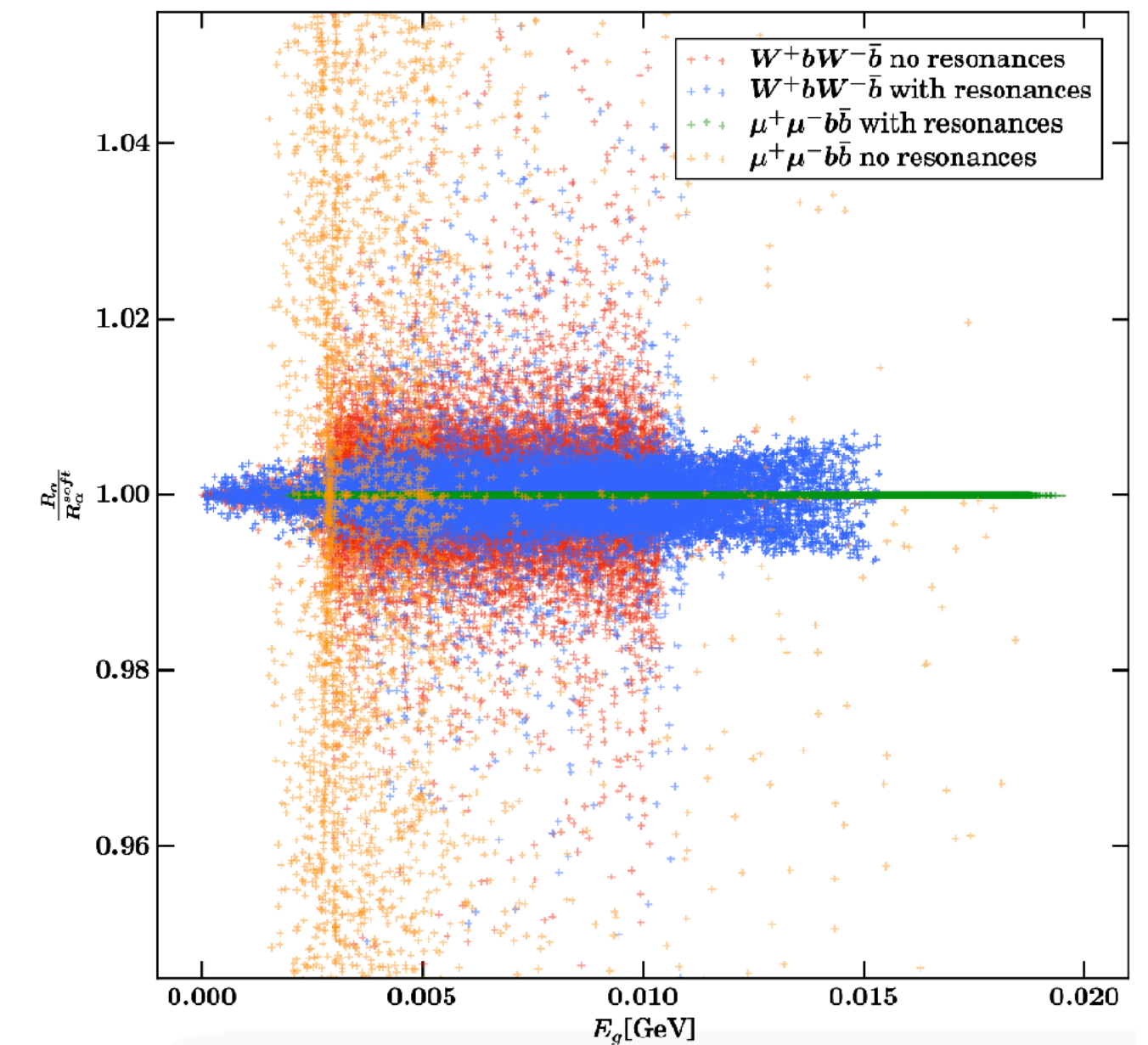
$$\mu_R = H_T/2 \quad \text{with} \quad H_T := \sum_i \sqrt{p_{T,i}^2 + m_i^2}$$



N(N)LO Automation in MC — Going beyond

14 / 26

- MC NLO implementation relies on 2 building blocks: Subtraction (Catani-Seymour or Frixione/Kunszt/Soper)
- also: resonance-aware FKS subtraction [cf. Ježo/Nason, 1509.09071; Chokoufé, 2017](#)
- Photon isolation, photon recombination, light-, b-, c-jet selection
- Covers also loop-induced processes (“LO”, virtual-squared)



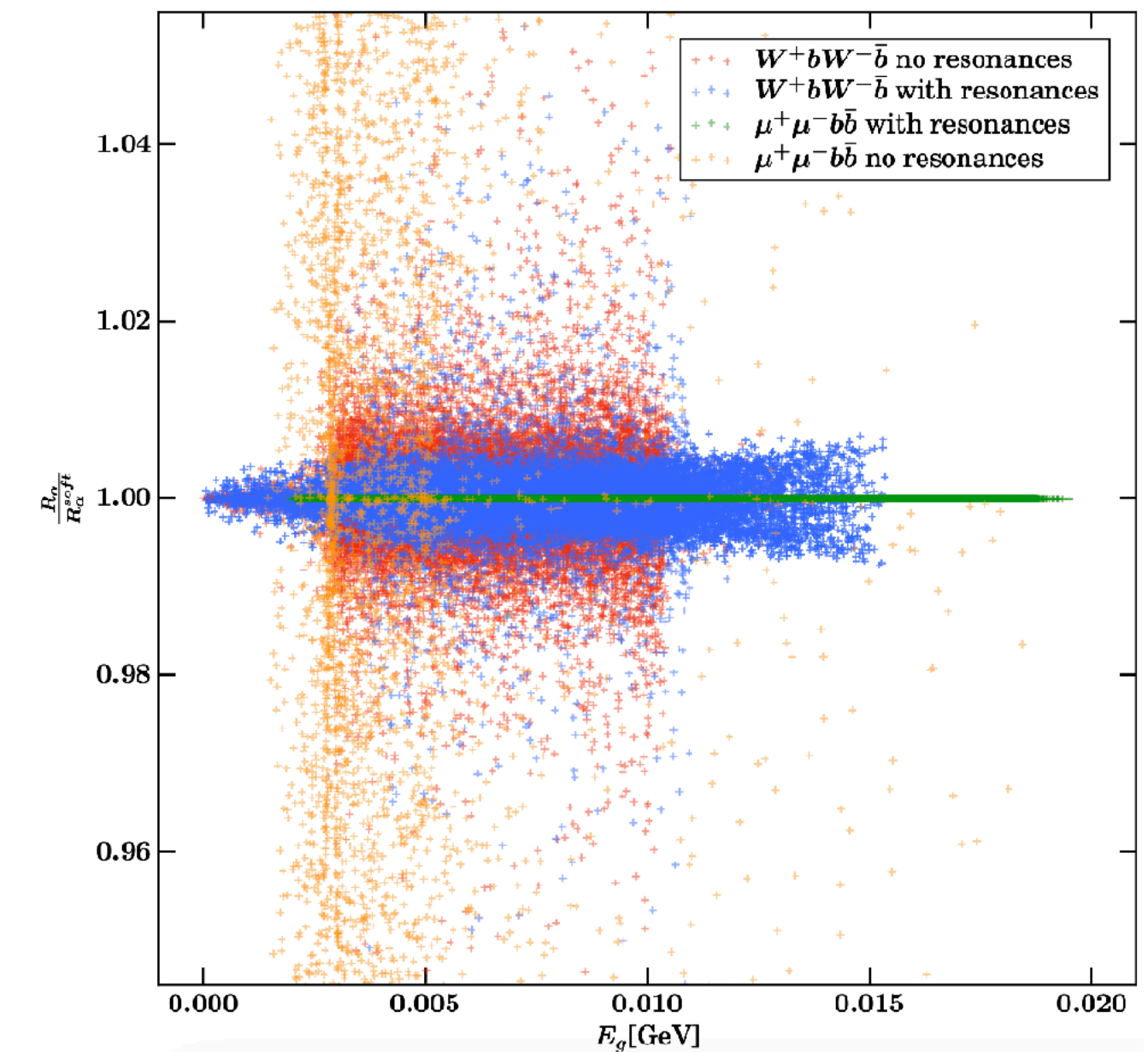
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14 / 26

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Two major bottlenecks to NNLO

- Virtual integrals with many mass scales / off-shell legs
[Abreu ea., Badger ea., Baglio ea., Brønnum-Hansen ea.](#)
- IR pole treatment / subtraction [CS, FKS, NS, Stripper, qT/sub-jettiness etc.](#)

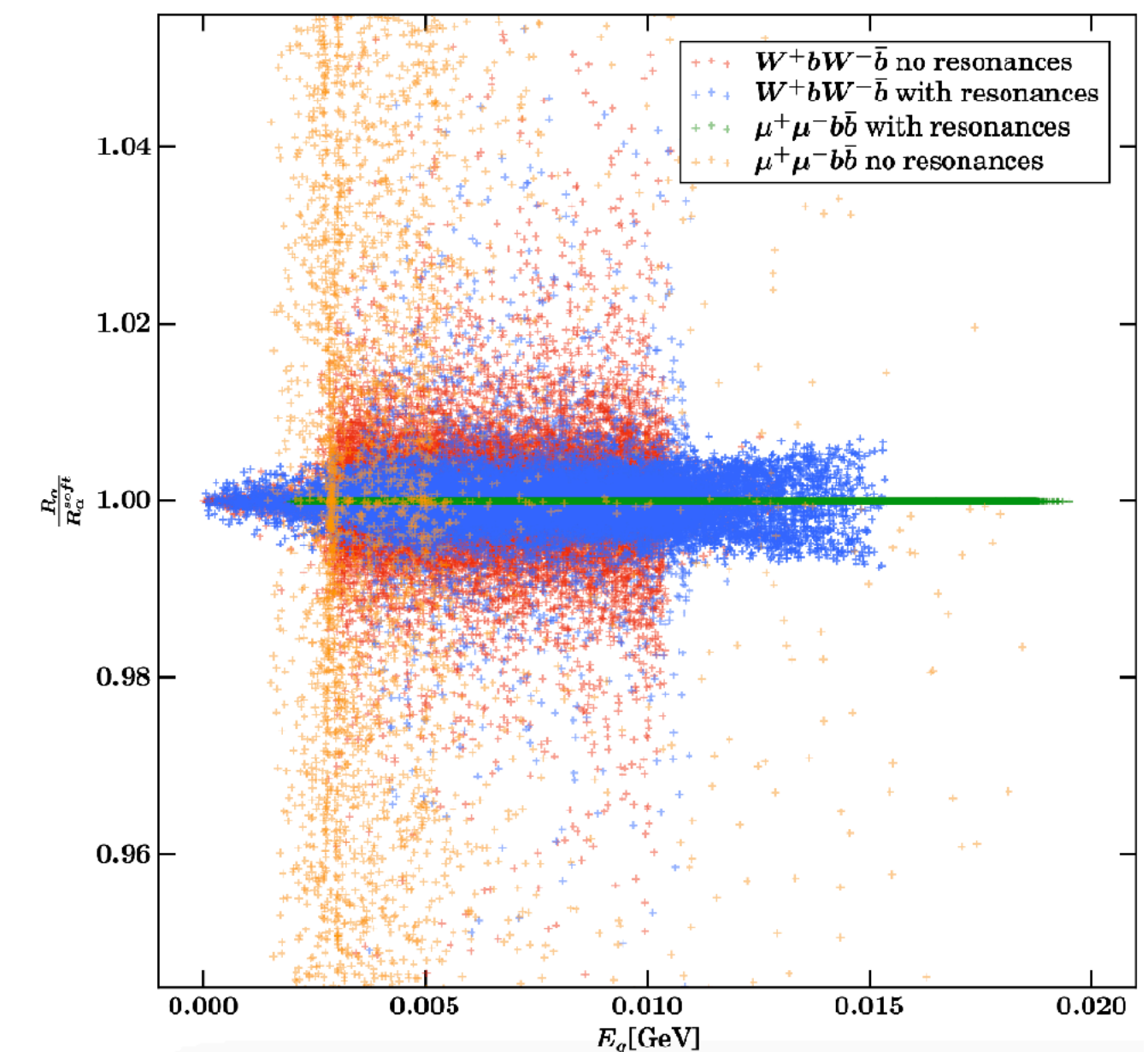


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- ☒ FKS soft/eikonal subtraction sufficient for low-energy machines
- ☒ NNLO QED (massive, virtuals pending): [McMule](#) [Signer ea.](#) [Whizard]
- ☒ Baby steps to NNLO automation: [Griffin](#) [Chen/Freitas, 2023](#)
- ☒ for NNLO EW need for full-fledged soft+collinear NNLO subtraction



Parton Showers, Matching, Hadronization

15 / 26



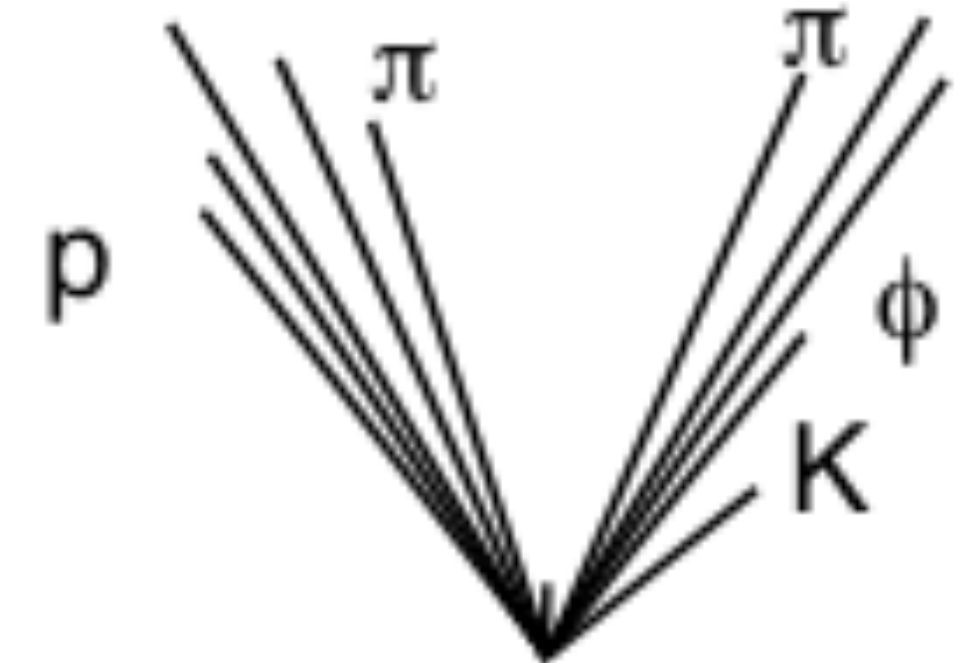
LO partons



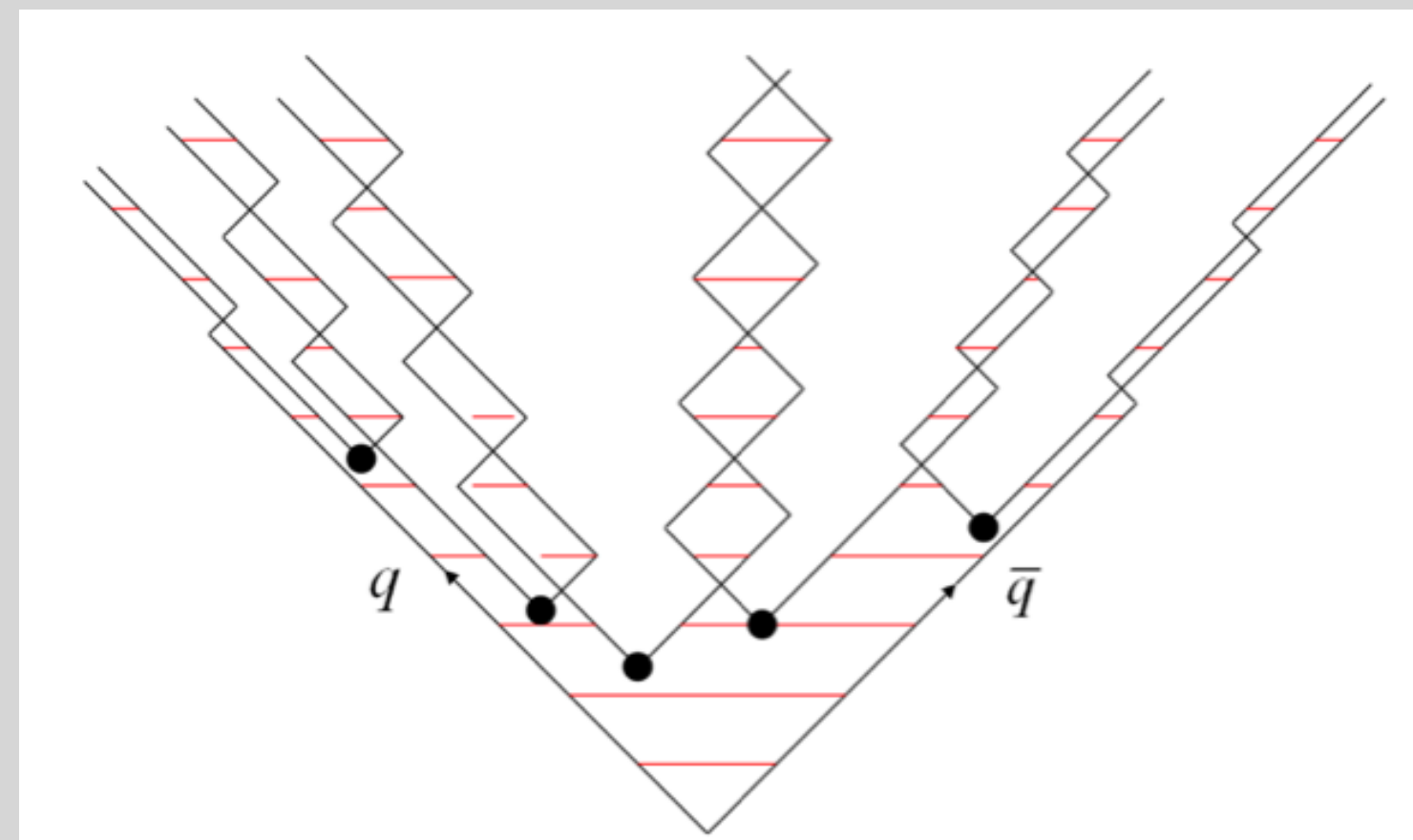
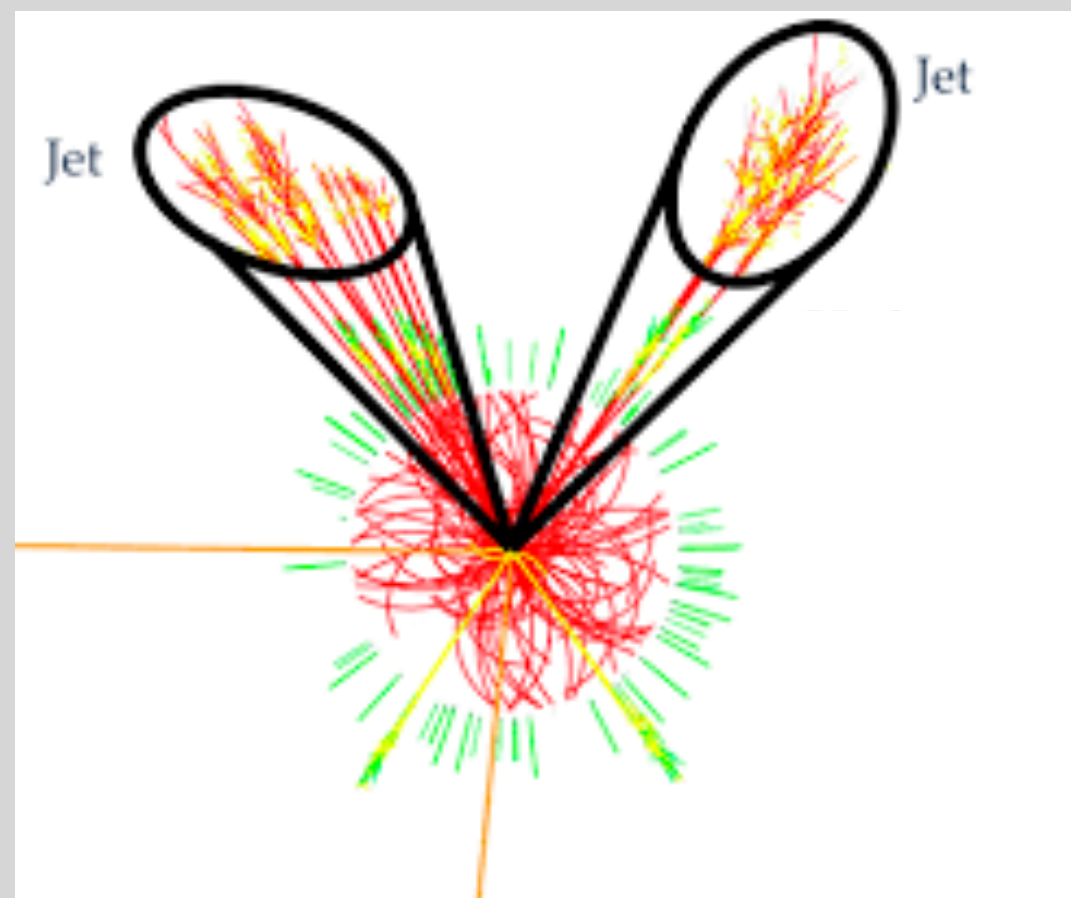
NLO partons



parton shower



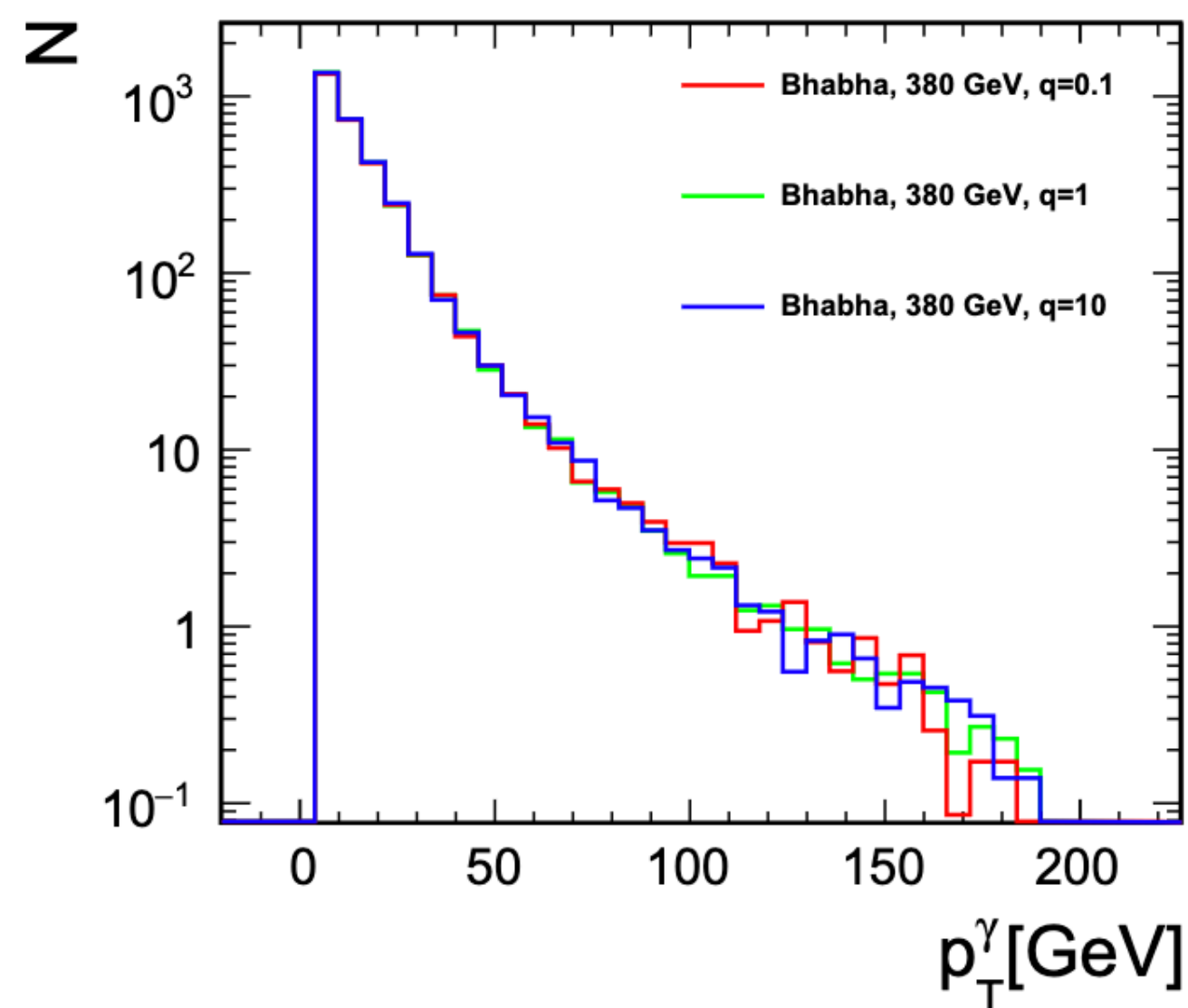
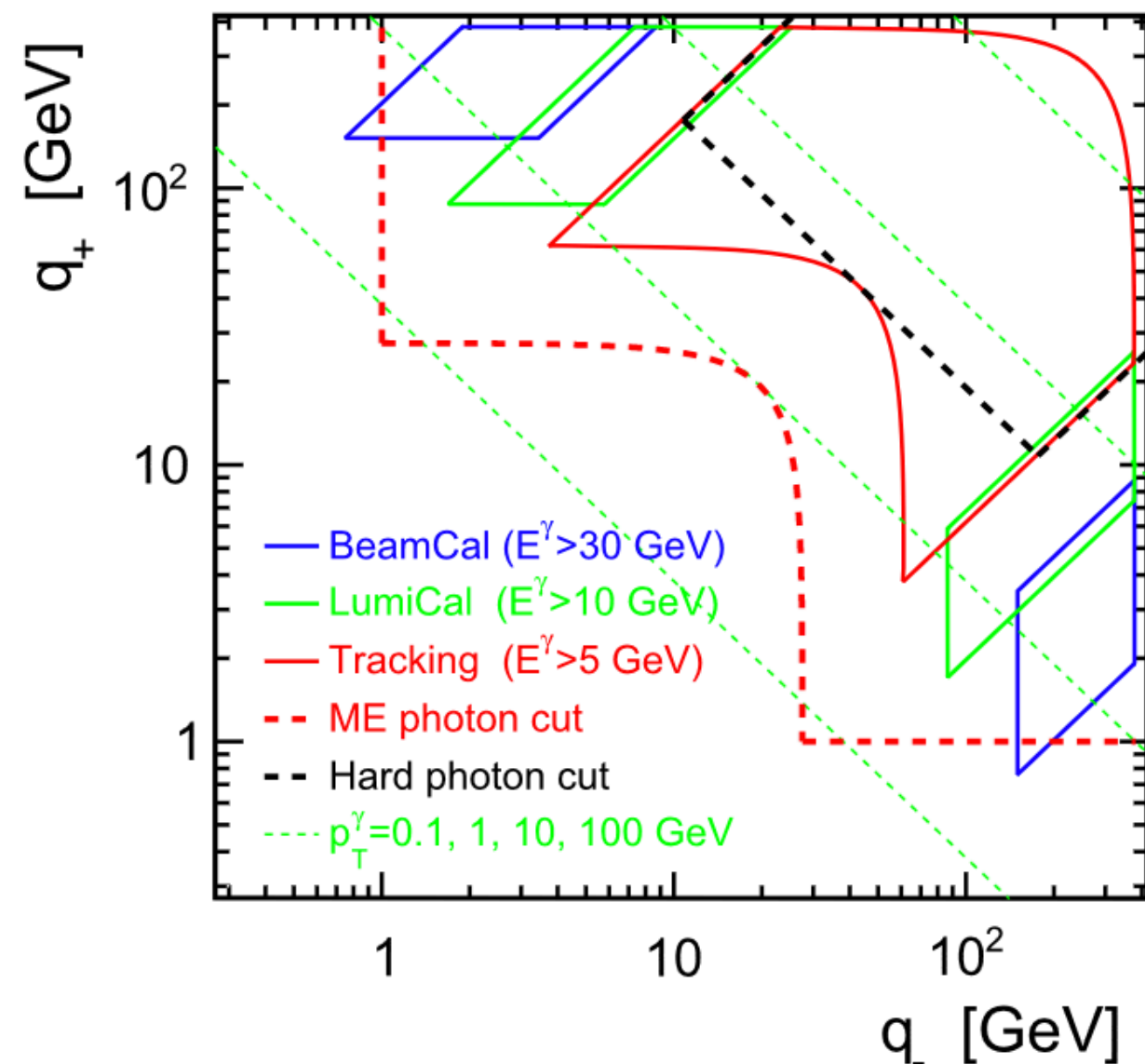
hadron level



Exclusive photons

QED ISR [+FSR], matching

- Explicit photon from fix-order (LO/NLO/NNLO) matrix element (best description)
- “Shower-recoil approach”: generate p_{\perp} according to $\frac{\alpha}{\pi} \cdot \log \frac{p_{\perp}^2}{m_e^2}$
- Boost according to the generated p_{\perp} (avail. for for ISR, EPA or ISR+EPA)
- Algorithm applied recursively (similar to massive NLO EW ISR PS construction)
- Recursive algorithm resembles a photon shower with n exclusive photons



J. Kalinowski/W. Kotlarski/P. Sopicki/A.F. Zarnecki, 2020



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Full QED shower

- Based either on dipoles or antennae, for ISR separate, for FSR interleaved [?]
- Can then be combined with POWHEG/MC@NLO/XXX-type matching
- Can be combined with resummation in (semi-)automated ways ... w.i.p.

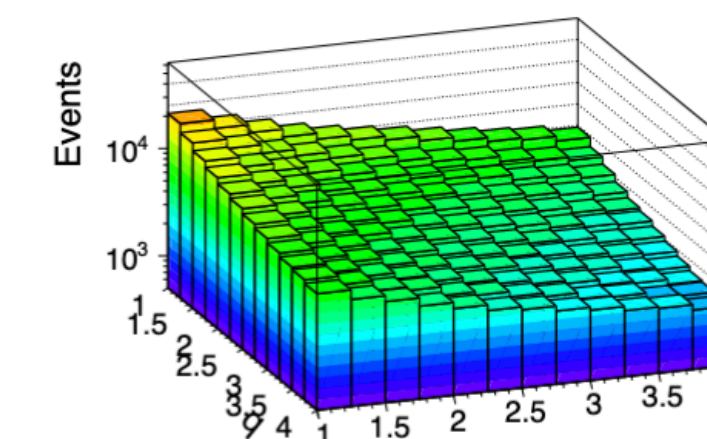
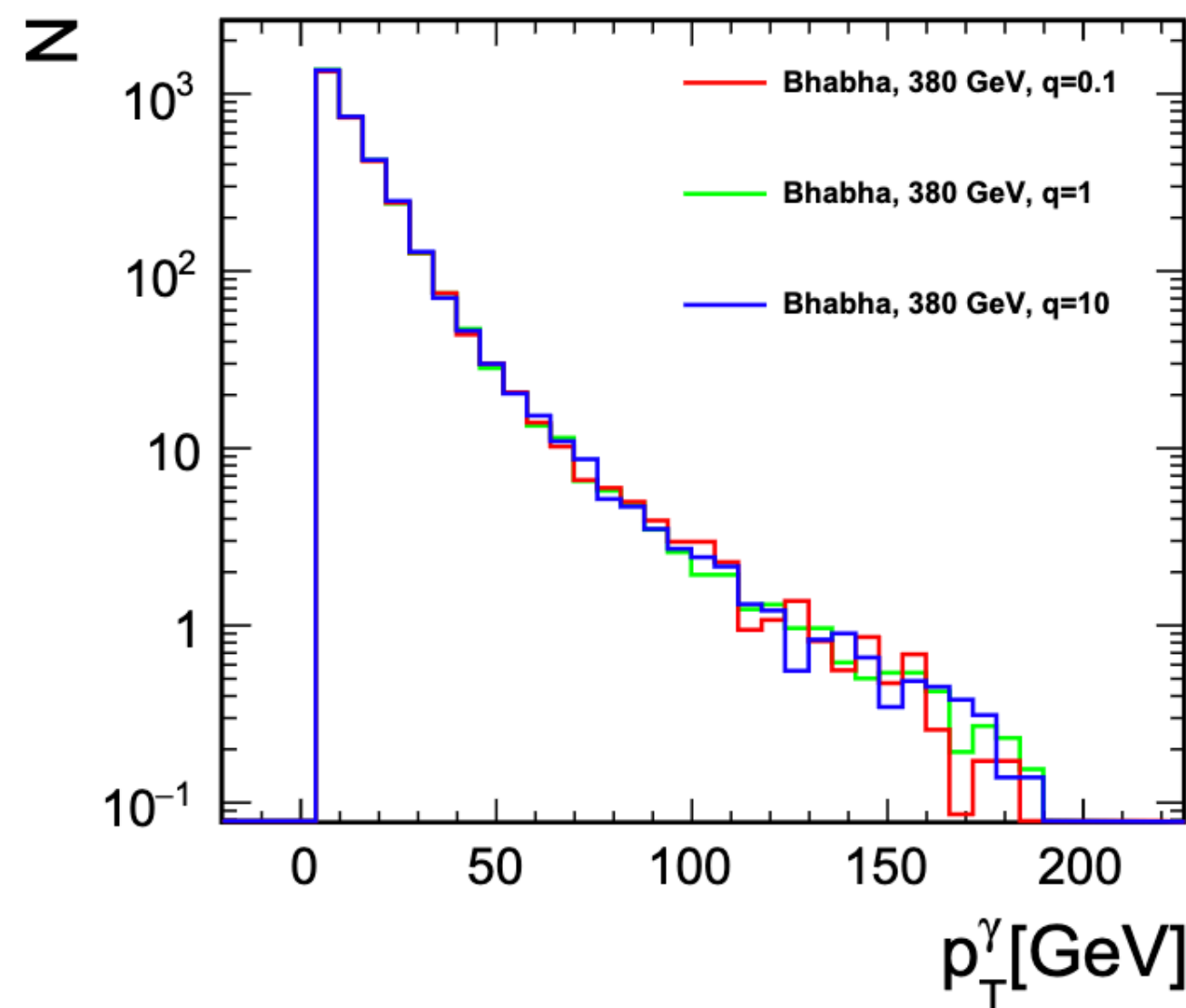
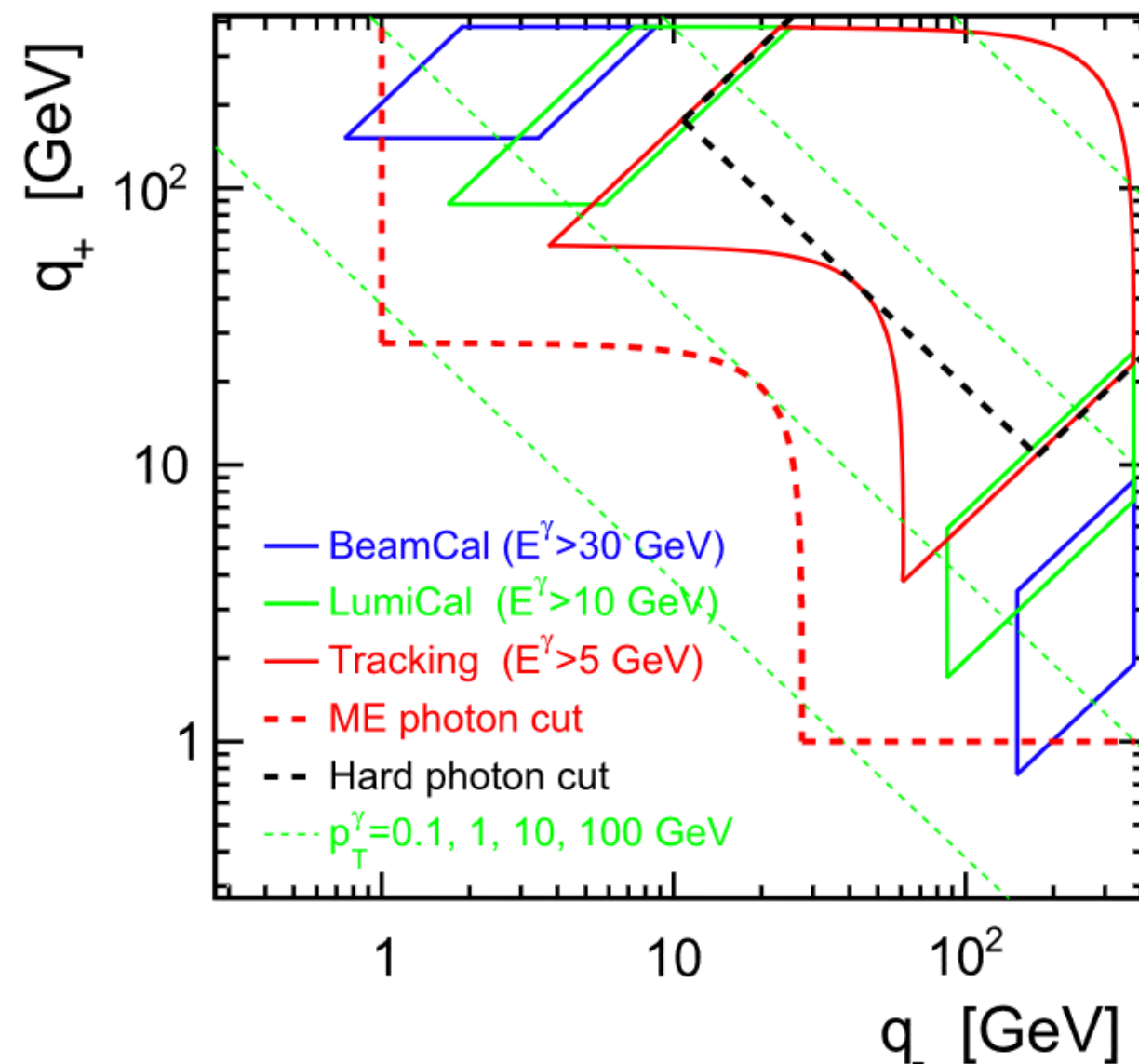
Matching between EPA/ γ PDF + beam γ

M. Berggren/W. Kilian/K. Mękała/JRR

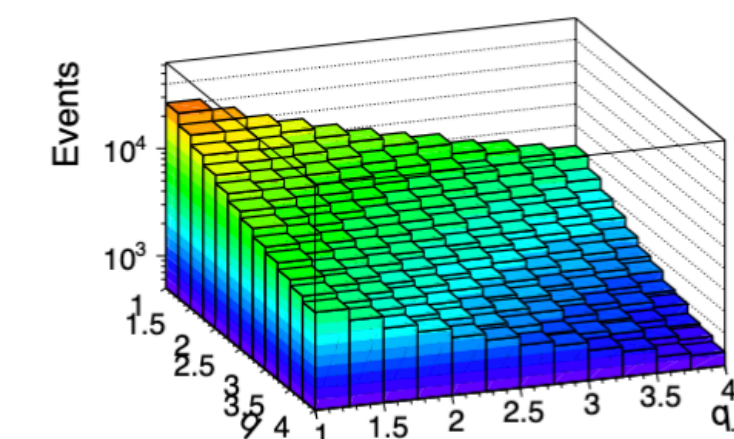
J. Kalinowski/W. Kotlarski/P. Sopicki/A.F. Zarnecki, 2020

J. R. Reuter, DESY

2nd ECFA HET Factory Workshop, Paestum, 13.10.2023



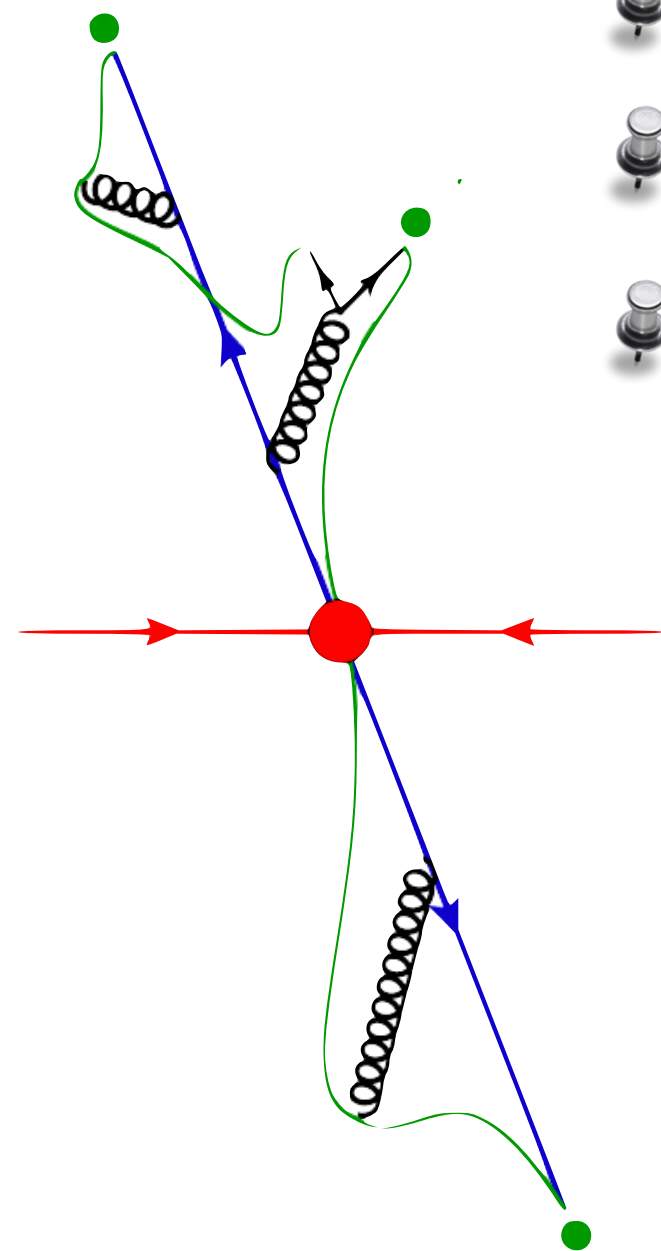
(a) Double EPA



(b) Full matrix elements

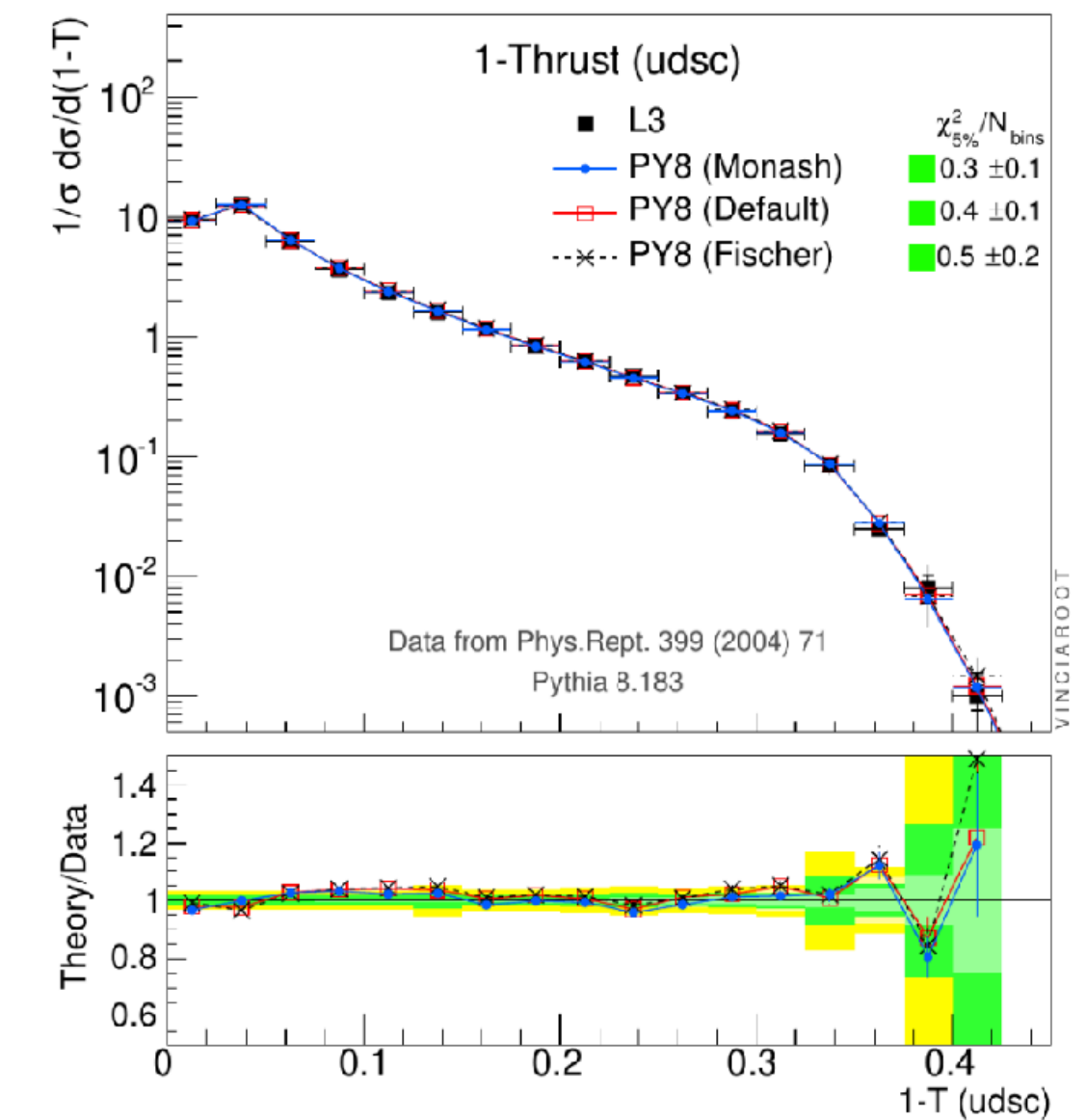
Parton shower / hadronization

17 / 26



- Machinery of parton showers well advanced, recap of CERN workshop 04/2023
- Tuning: automated tools w/ built-in correlations (Professor, AutoTunes, Apprentice, ...)
- Global event shapes, α_s , charge multiplicity, hadron multiplicity
- Possible NLL parton showers (final state only!) for e^+e^- :

Shower	Ordering	NLL Validation
PanScales [2002.11114]	$10 \leq \beta < 1$	Fixed and all order numerical tests for a range of observables
Alaric [2208.06057]	k_t ($\beta = 0$)	Analytical, numerical tests for global event shapes
Deductor [2011.04777]	k_t, Λ ($\beta = 0, 1$)	Analytical and numerical tests for thrust
Manchester-Vienna [2003.06400]	k_t ($\beta = 0$)	Analytical for thrust and multiplicity



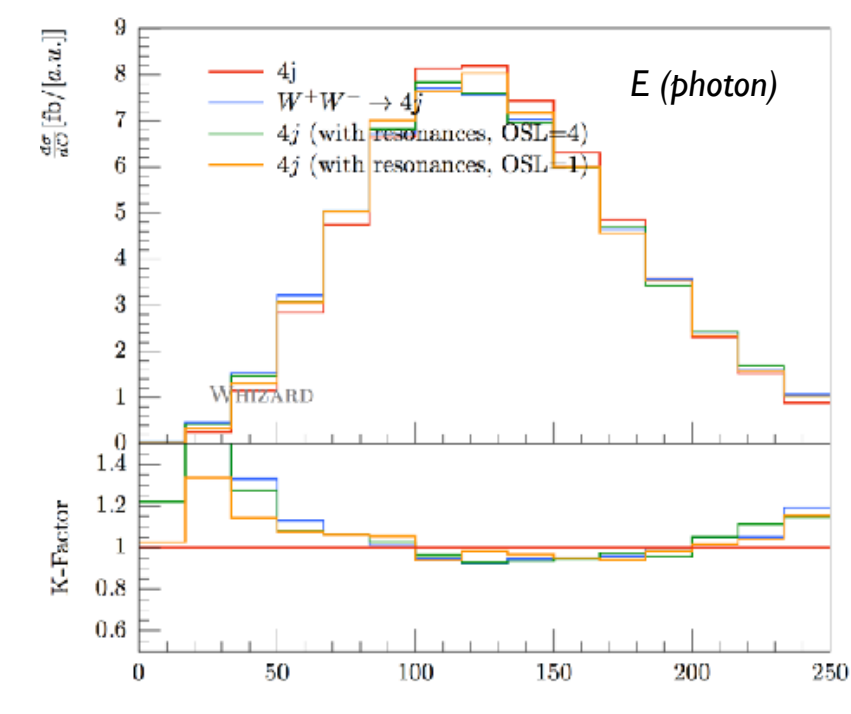
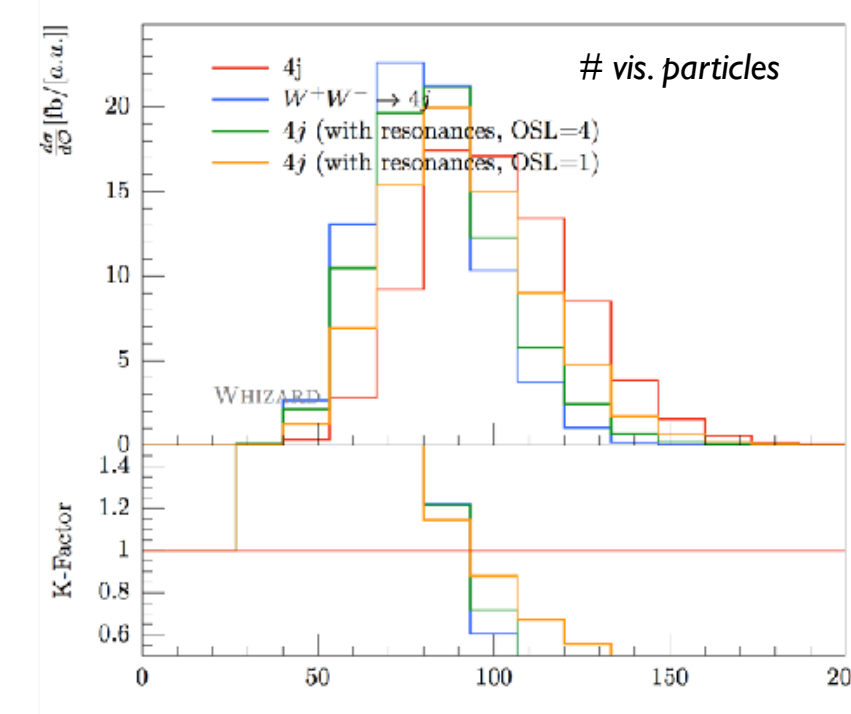
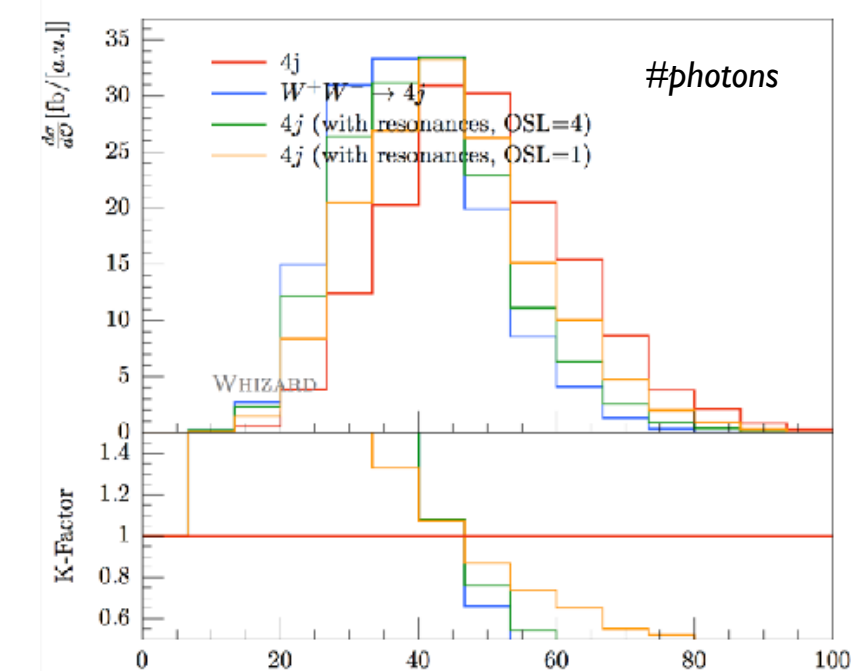
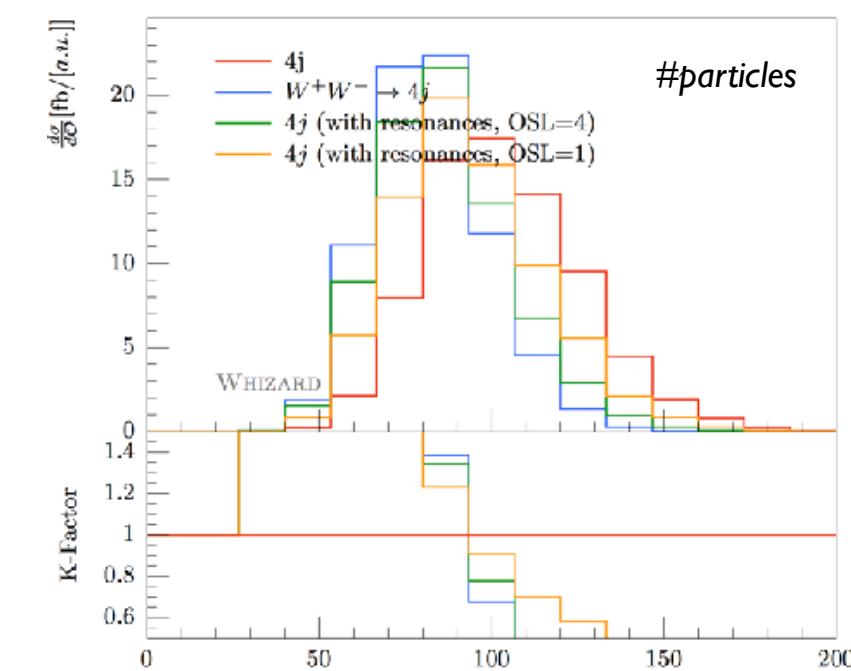
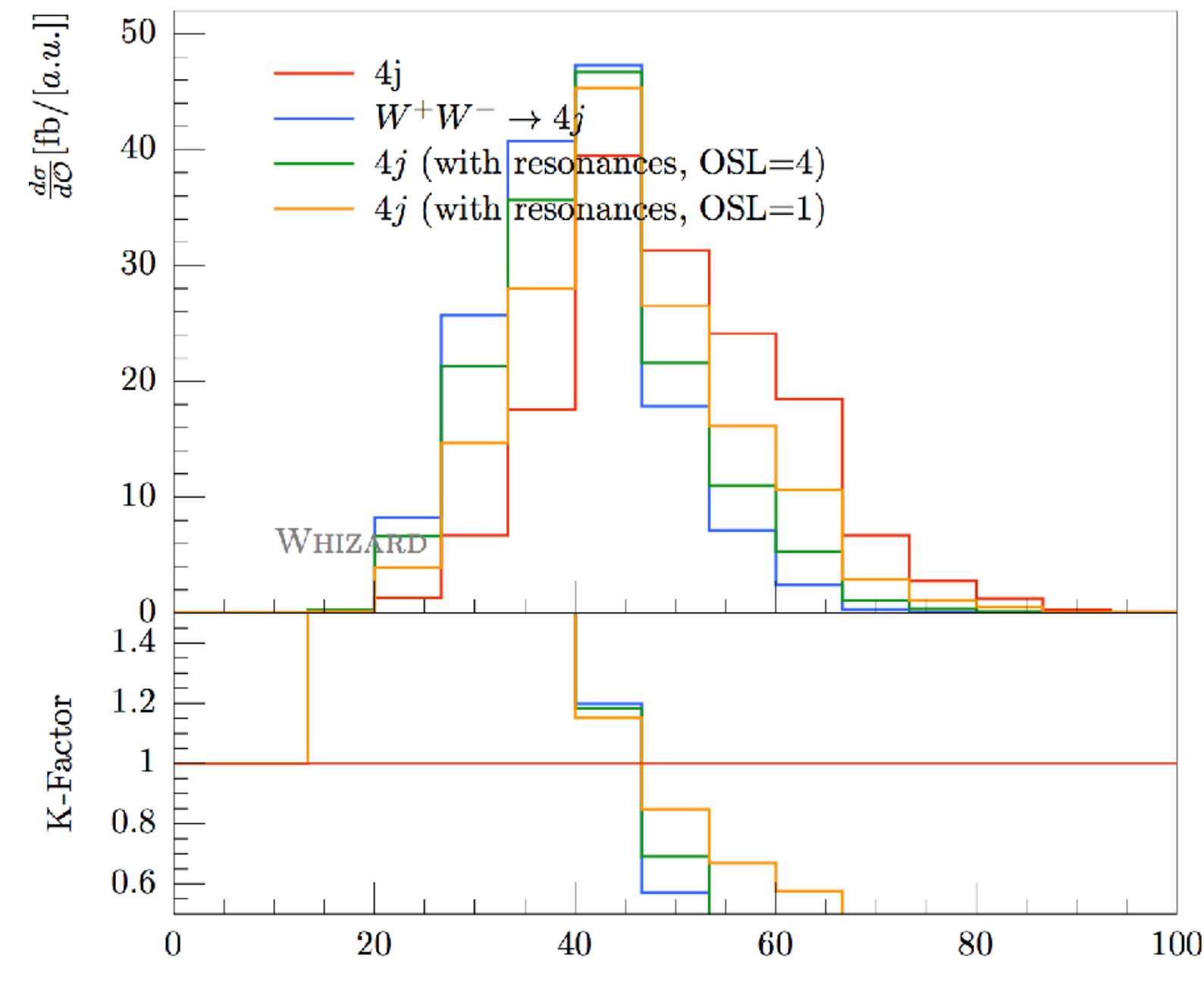
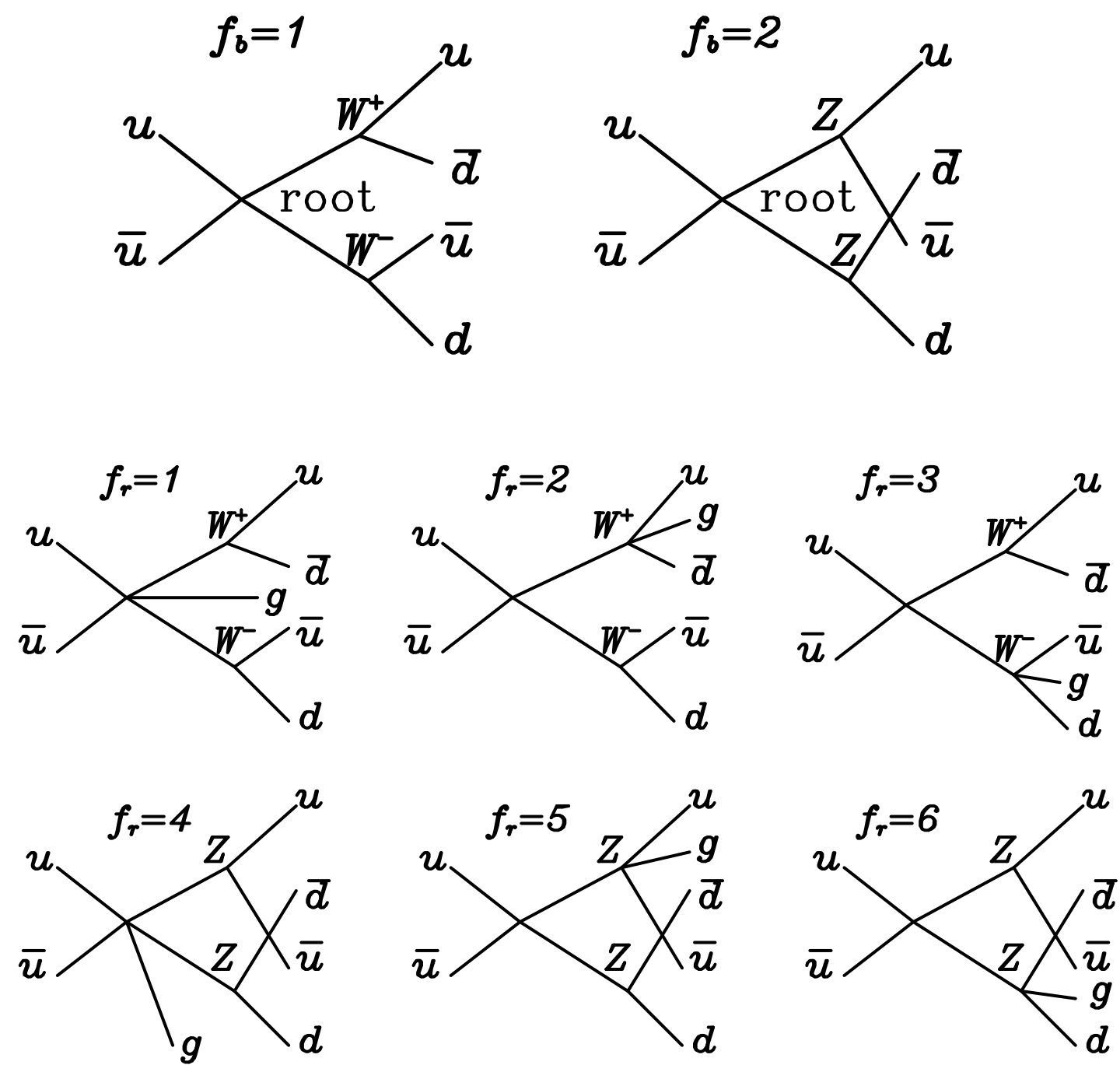
Talks by Jack Helliwell + Leif Gellersen

- Ongoing work towards NNLL showers, sub-leading color (FCC = full color correlations)
 - NLO matching automated, different approaches, different error estimates;
 - NNLO matching still process-dependent; also does not yet preserve NNLL accuracy
 - Elephant in the room: fragmentation \Rightarrow no paradigm shift/quantum leap in last 30 years
- Gigantic clean data sets from Z pole and above will necessitate new models / theory

(Resonance) Matching to shower / hadronization

18 / 26

- ❖ **Problem:** $e^+e^- \rightarrow jjjj$ not dominated by highest α_s power, but by resonances
- ❖ **Solution:** proper merging w/ resonant subprocesses by resonance histories
- ❖ **MC generators allow to pass resonance history to Shower MC**



PACKED WITH PRECISION-MADE,
MISSION-SPECIFIC TOOLS.



GRIP. PUNCH. ADJUST. DRIVE. WRENCH. PICK.
SCRAPE. HAMMER. OH YEAH...AND CUT.

In memoriam: Staszek Jadach

20 / 26



Stanisław ("Staszek") Jadach, 1943 — 2023

**RAPIDITY GENERATOR FOR MONTE-CARLO CALCULATIONS
OF CYLINDRICAL PHASE SPACE**

S. JADACH

Institute of Physics, Jagellonian University, Cracow, Poland

Received 1 November 1974

Potentially a severe impact on the development of LEP legacy Monte Carlos,
YFS-style tools (the whole KKMC, YFS-WW/ZZ, Photos, Tauola, BHLumi/BHWide !

Important rôle of Belle 2 program: active usage of many of these programs!

Bhabha cross sect. depends on detector acceptance angles

$$\sigma_{Bh} \simeq 4\pi\alpha^2 \left(\frac{1}{t_{\min}} - \frac{1}{t_{\max}} \right) = 4\pi\alpha^2 \left(\frac{t_{\max} - t_{\min}}{\bar{t}^2} \right), \quad \bar{t} = \sqrt{t_{\min} t_{\max}}$$

Machine	$\theta_{\min} \div \theta_{\max}$ [mrad]	\sqrt{s} [GeV]	$\bar{t}/s \simeq \bar{\theta}^2/4$	$\sqrt{\bar{t}}$ [GeV]
LEP	28÷50	M_Z	3.5×10^{-4}	1.70
FCCee	64÷86	M_Z	13.7×10^{-4}	3.37
FCCee	64÷86	240	13.7×10^{-4}	8.9
FCCee	64÷86	350	13.7×10^{-4}	13.0
ILC	31÷77	500	6.0×10^{-4}	12.2
ILC	31÷77	1000	6.0×10^{-4}	24.4
CLIC	39÷134	3000	13.0×10^{-4}	108

[Maciej Skrzypek; Brussels Topical Workshop]

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Current BHLUMI precision forecast for FCCee			
Type of correction / Error	M_Z (2019) [1]	240 GeV	350 GeV [2]
(a) Photonic $\mathcal{O}(L_e\alpha^2)$	0.027%	0.032%	0.033%
(b) Photonic $\mathcal{O}(L_e^3\alpha^3)$	0.015%	0.026%	0.028%
(c) Vacuum polariz.	0.009%	0.020%	0.022%
(d) Light pairs	0.010%	0.015%	0.015%
(e) Z and s-channel γ exchange	0.09%	0.25% (0.034%)	0.5% (0.07%)
(f) Up-down interference	0.009%	0.010%	0.010%
(g) Technical Precision	[0.027%]		
Total	10×10^{-4}	25×10^{-4} (6×10^{-4})	50×10^{-4} (8.7×10^{-4})

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(c) Vacuum polariz.	0.6×10^{-4}	1.0×10^{-4}	1.1×10^{-4}
(d) Light pairs	0.5×10^{-4}	0.4×10^{-4}	0.4×10^{-4}
(e) Z and s-channel γ exch.	0.1×10^{-4}	$1.0 \times 10^{-4(*)}$	$1.0 \times 10^{-4(*)}$
(f) Up-down interference	0.1×10^{-4}	0.09×10^{-4}	0.1×10^{-4}
Total	1.0×10^{-4}	1.5×10^{-4}	1.6×10^{-4}



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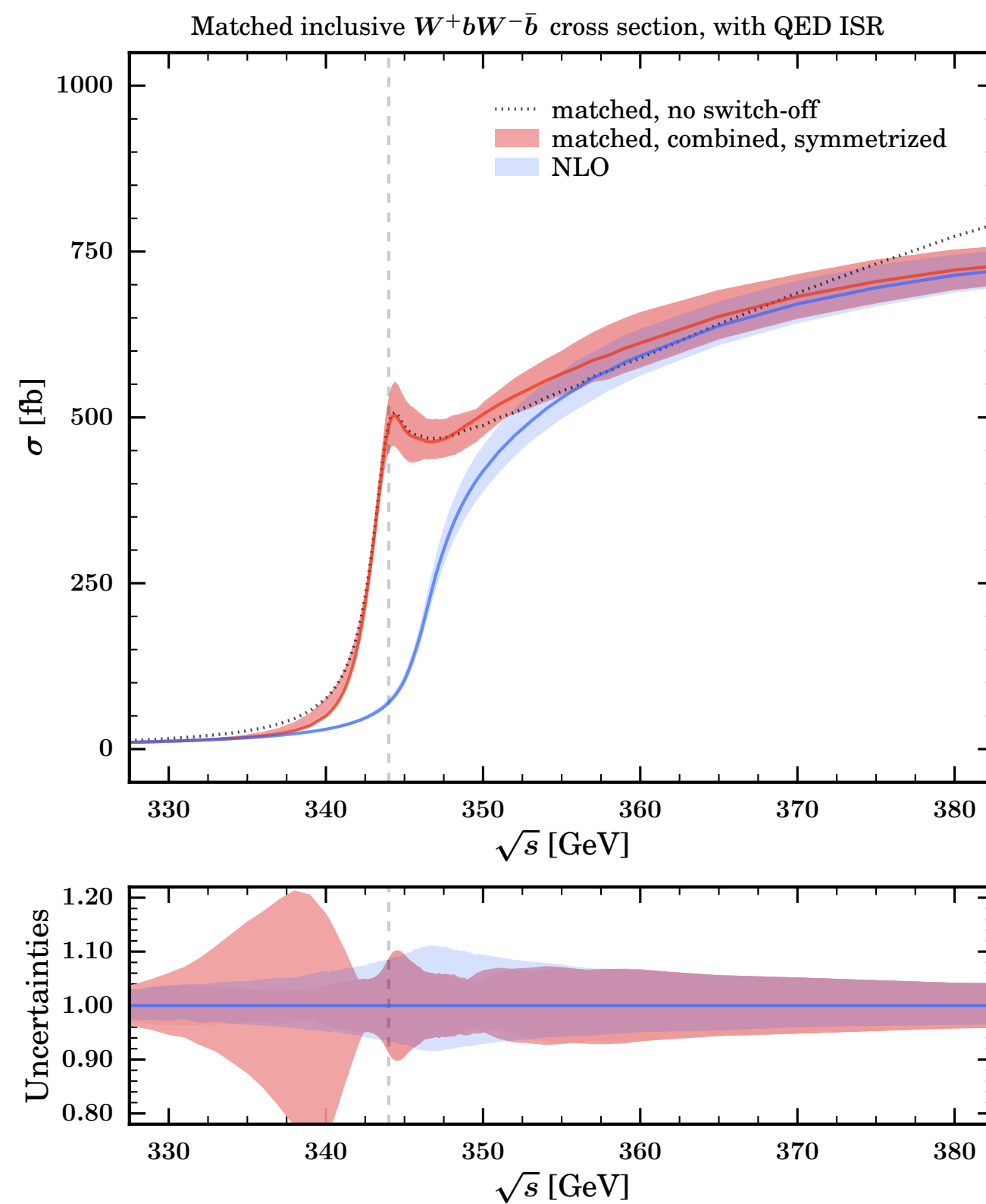
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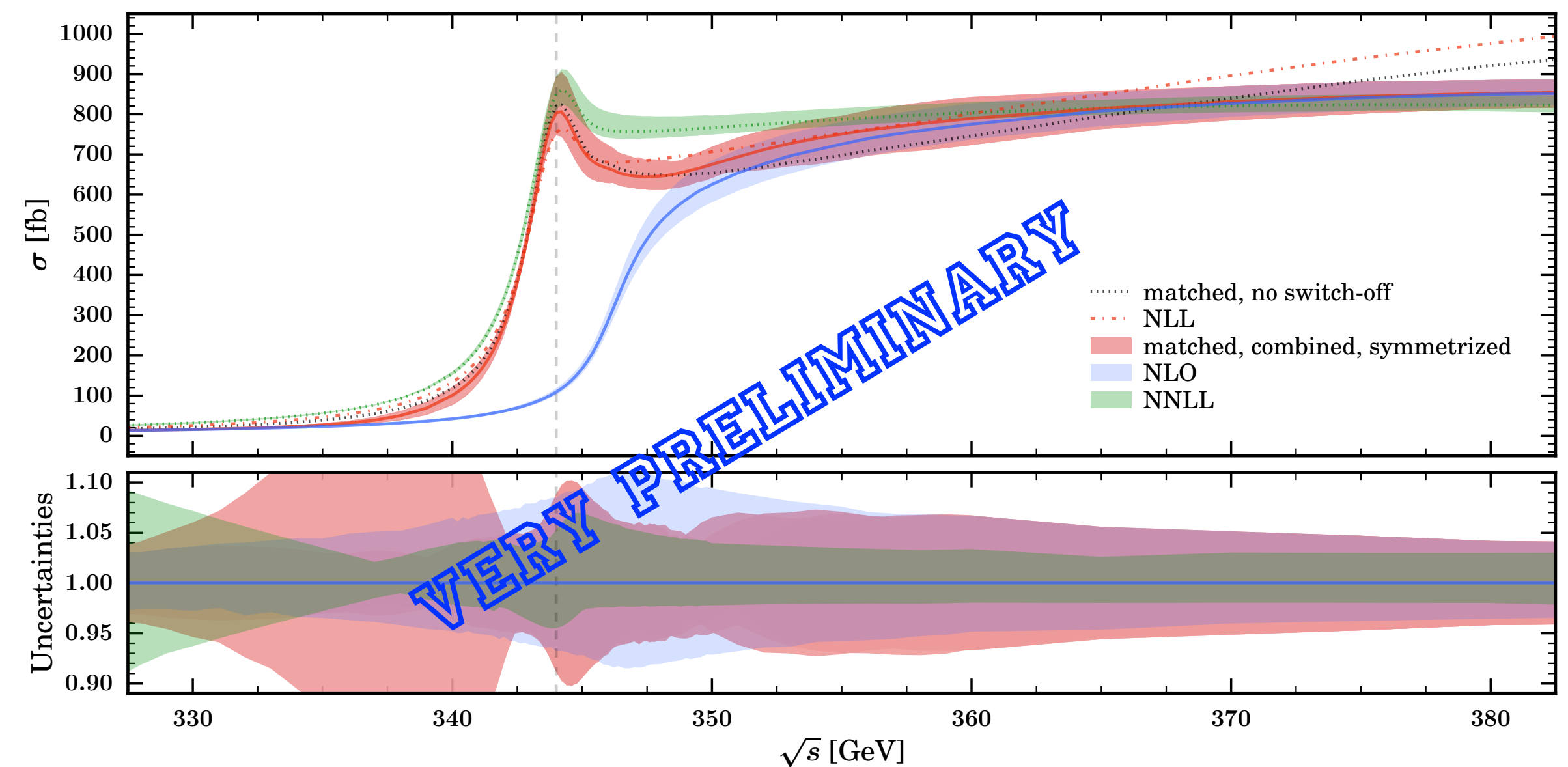
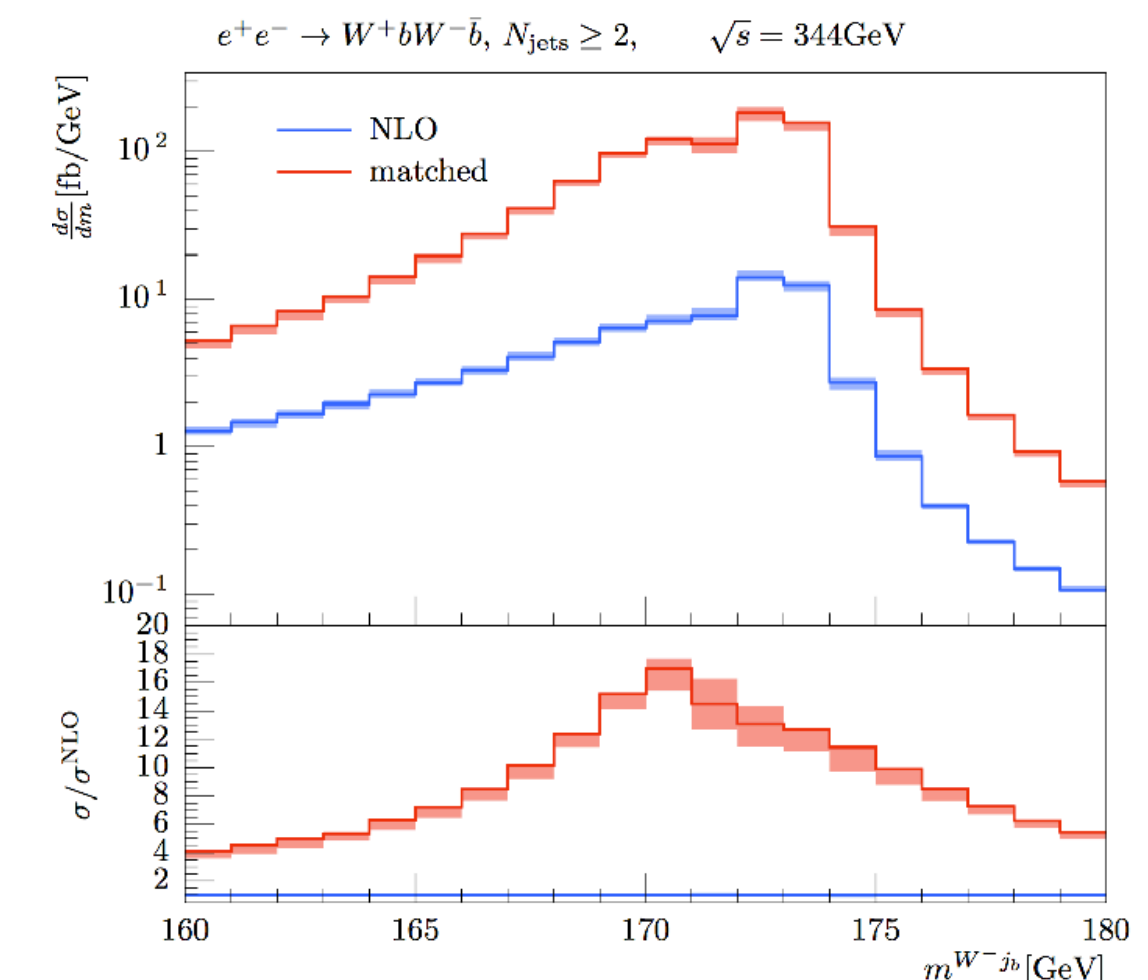
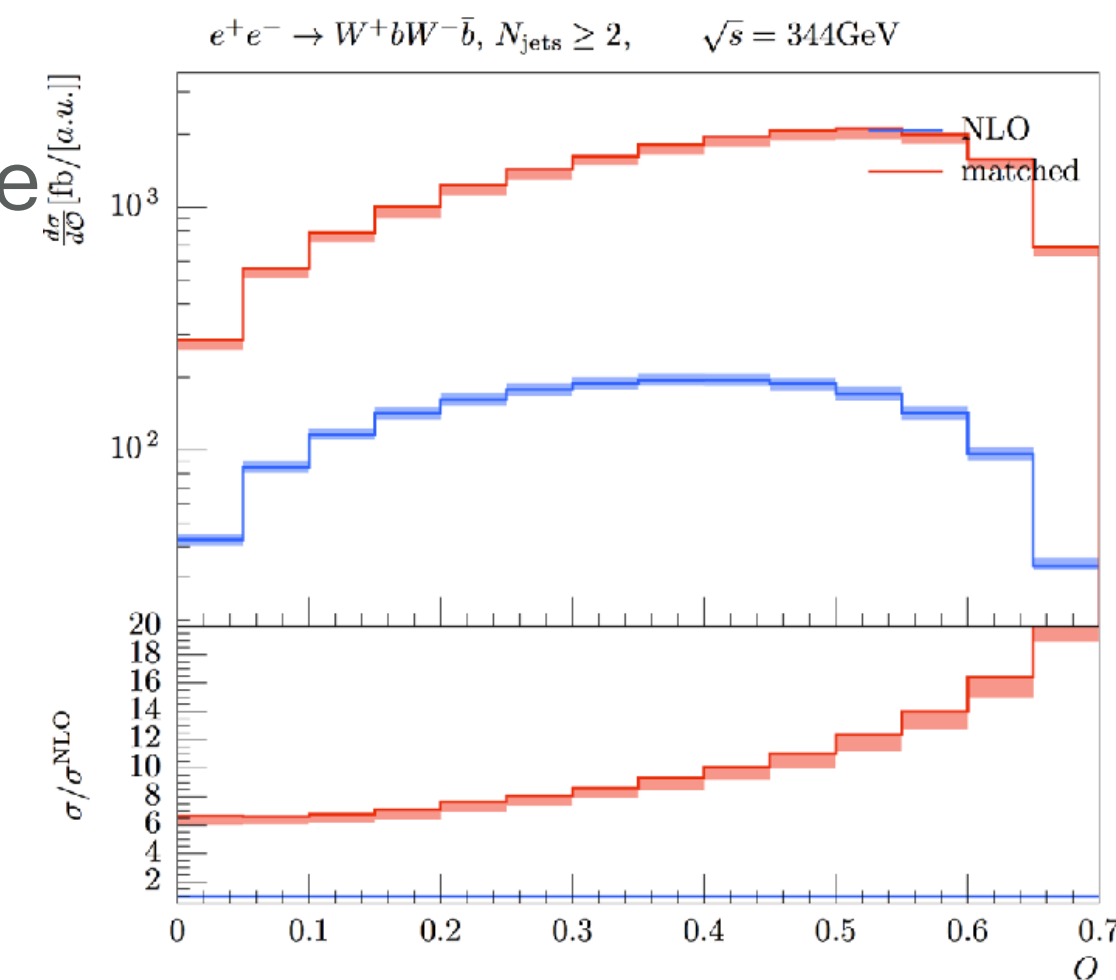
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Total	1.0×10^{-4}	1.5×10^{-4}	1.6×10^{-4}

- Technical precision needs 2nd code: BHLumi vs. BabaYaga (NNLO in hard process possible)
- Major ingredients: hadronic vacuum polarization, EW corrections, light fermion pairs
- Inclusion of 4f, 4f + γ , 5f, 6f backgrounds necessary at matrix element level

- Differential distributions at top threshold, systematics
- Exclusive Top threshold NLL-NLO QCD matched available
- Recent improvement in axial form factor matching
- Technical issues (person power)
- Improvement needed (e.g. shower



J. R. Reuter, DESY



2nd ECFA HET Factory Workshop, Paestum, 13.10.2023

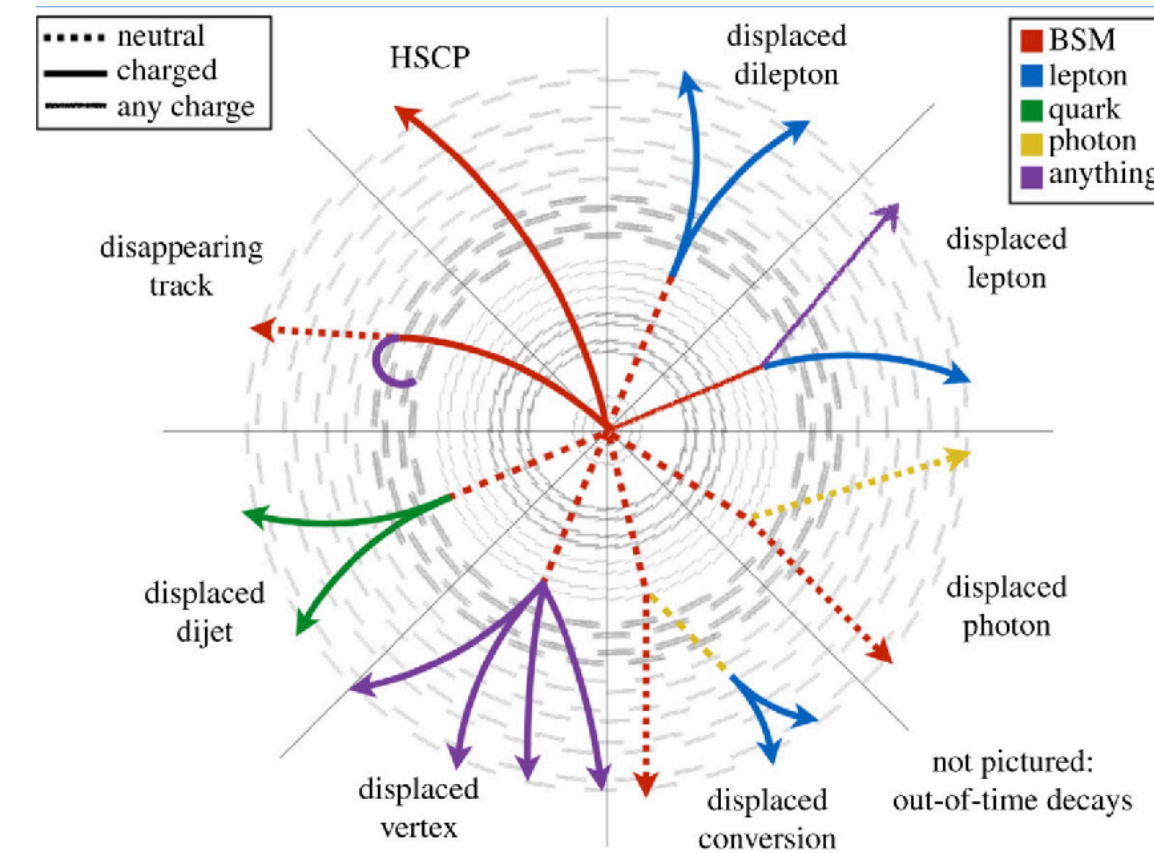
BSM Modelling in Simulation

23 / 26



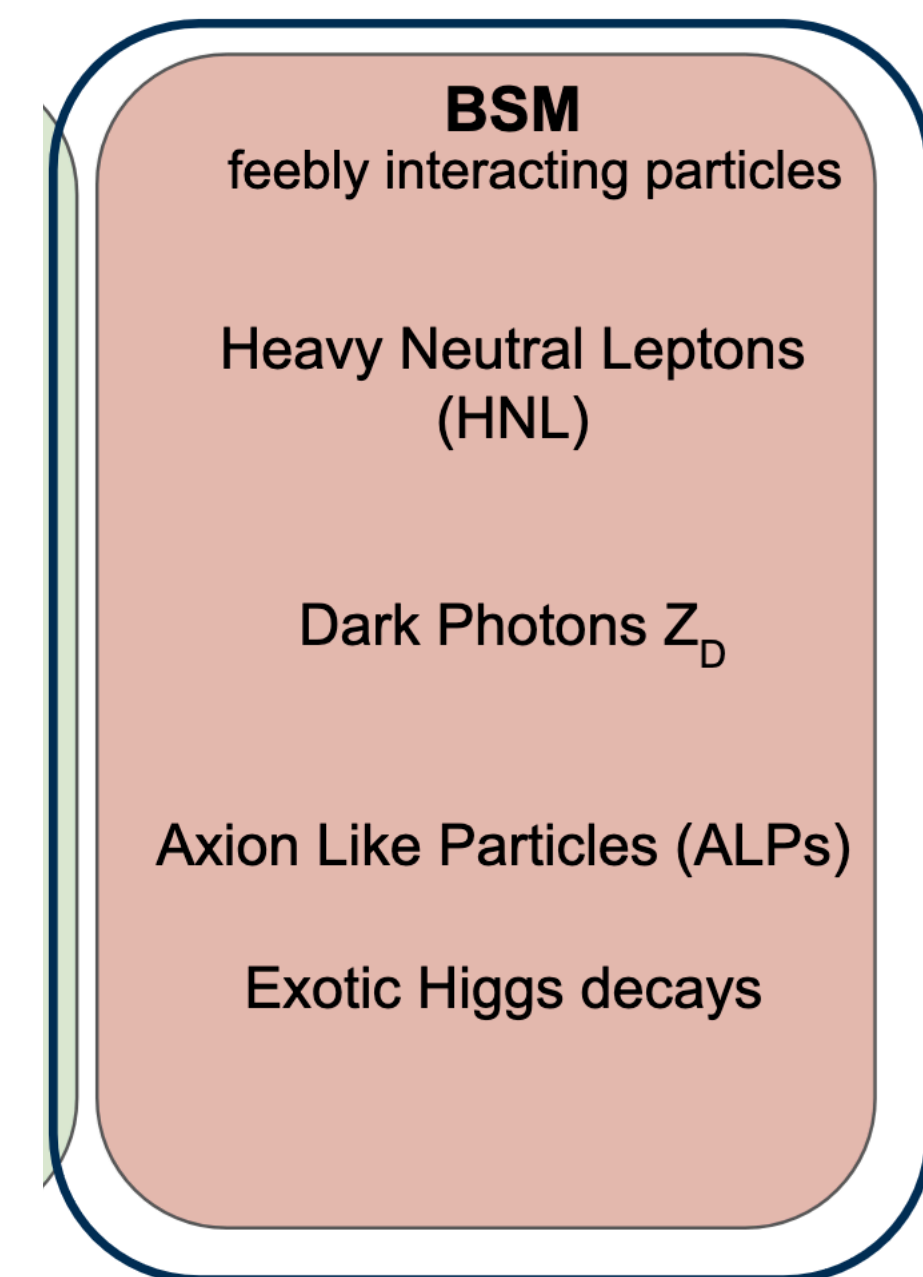
- BSM models from Lagrangian level tools (LanHEP, SARAH, FeynRules)
- Transferred to MC generator via UFO format: v1 [1108.2040](#) v2: [2304.09883](#)
- Allows for all Lagrangian-based BSM models

- ☒ Spin 0, 1/2, 1, 3/2, 2 supported (some 3/2, 2 features missing in some MC)
- ☒ Majorana fermions and fermion-number violating vertices
- ☒ 5-, 6-, 7-, 8-, ... point vertices (optimization for code generation pending)
- ☒ Arbitrary Lorentz structures in vertices
- ☒ Keeping track of the order of insertions
- ☒ Customized propagators
- ☒ Exotic colored objects (sextets, decuplets, epsilon structures)
- ☒ (S)LHA-style input files from spectrum generators to MC generators (scans!)
- ☒ Automated calculations of widths (UFO side vs. MC generator side)
- ☐ Long-lived particles, displaced vertices, oscillations in decays (not all MCs yet)
- ☒ Lots of bug reports and constructive feedback from many different users
- ☐ LO fully supported, NLO (QCD) available on UFO side, but not all MCs



LLPs that are semi-stable or decay in the sub-detectors are predicted in a variety of BSM models:

- Heavy Neutral Leptons (HNLs)
- RPV SUSY
- Dark photons
- ALPs
- Dark sector models



Conclusions & Outlook

25 / 26



- Monte-Carlo event generators implement *all* necessary SM and BSM physics
- Modularity and redundancy of codes very important
- Fixed-order NLO QCD+EW for SM and NLO QCD BSM under control (mostly)
- First attempts to go to NNLO for QED (with certain caveats)
- LL/NLL ePDF in collinear factorization vs. YFS soft/eikonal factorization
- Matching prescriptions for exclusive photon radiation
- Different focus in different generators: no *a priori* best strategy for QED (and EW) corrections
- More studies, test cases and benchmarks needed: also 2nd and 3rd implementations important!
- Will depend a lot on support on young researchers/theorists working
- Also need for dedicated MCs, e.g. for luminosity measurement ($e^+e^- \rightarrow e^+e^-, \gamma\gamma$)
- Not to forget: QCD showers + fragmentation [Higgs/EW/top factories will boost to new precision!]

Optimistic conclusions

A lot remains to be done (e.g. *exclusive simulations*), but we are a generation away: there is plenty of time

Optimistic conclusions

A lot remains to be done (e.g. exclusive simulations), but we are a generation away: there is plenty of time

Pessimistic conclusions

A lot remains to be done (e.g. exclusive simulations), but we are a generation away: there is ~~plenty~~ of too much time

BACKUP

The importance of MC event generators

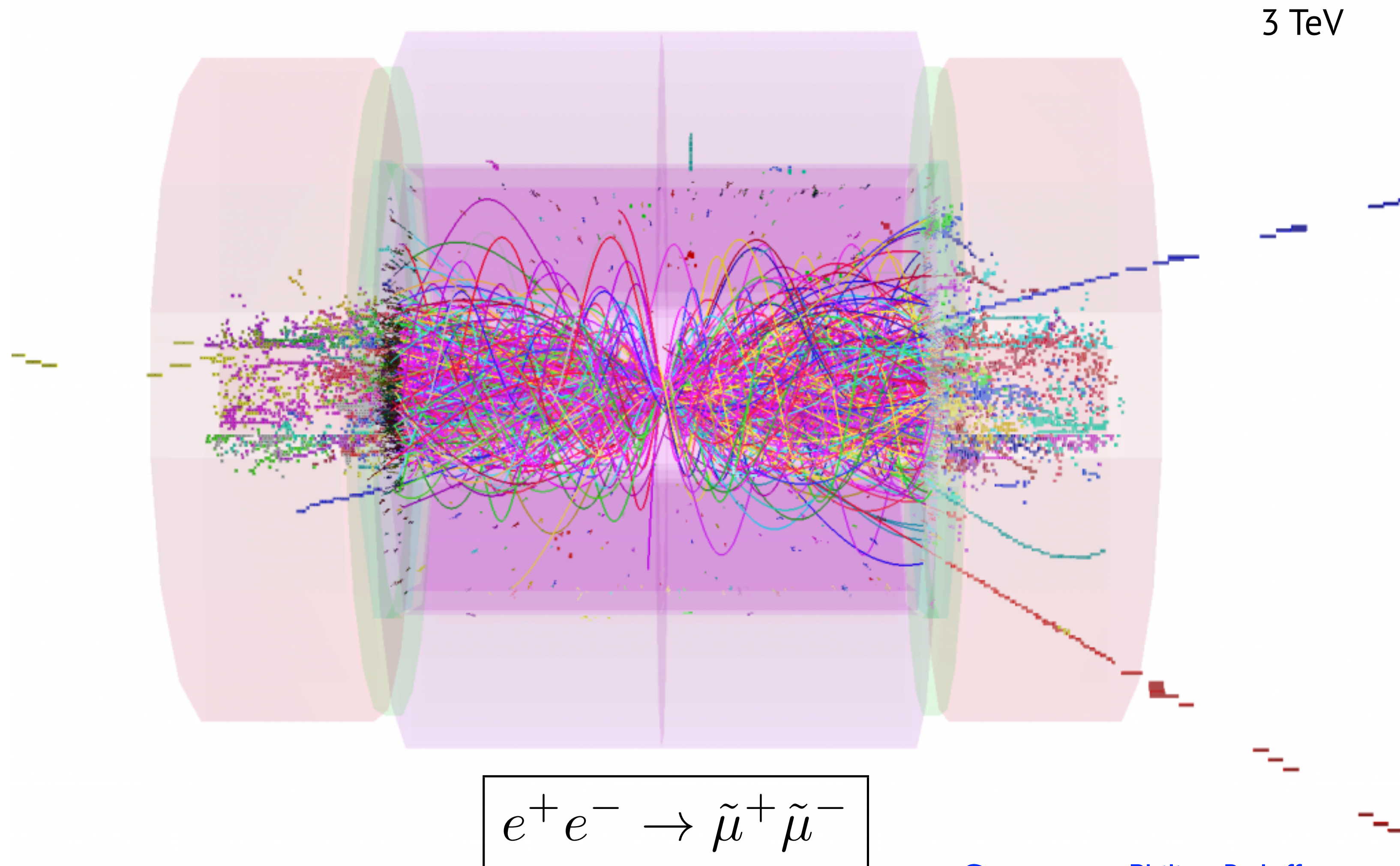
28 / 26

Why are event generators important?

Because all our forward simulation chain depends on them!

Why are event generators non-trivial?

Because they contain *all* our knowledge of particle physics!



Courtesy to Philipp Roloff

The importance of MC event generators

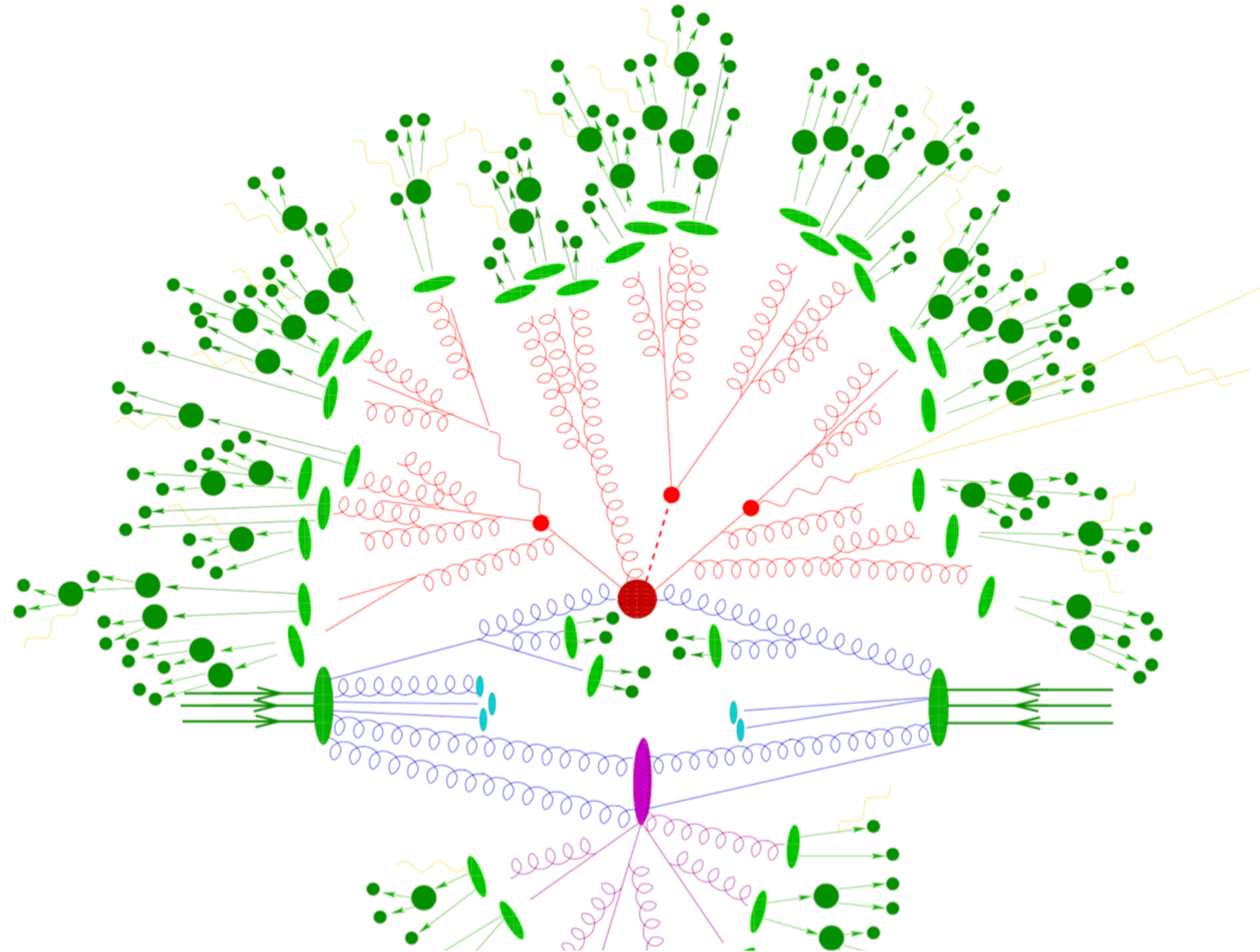
28 / 26

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The importance of MC event generators

28 / 26

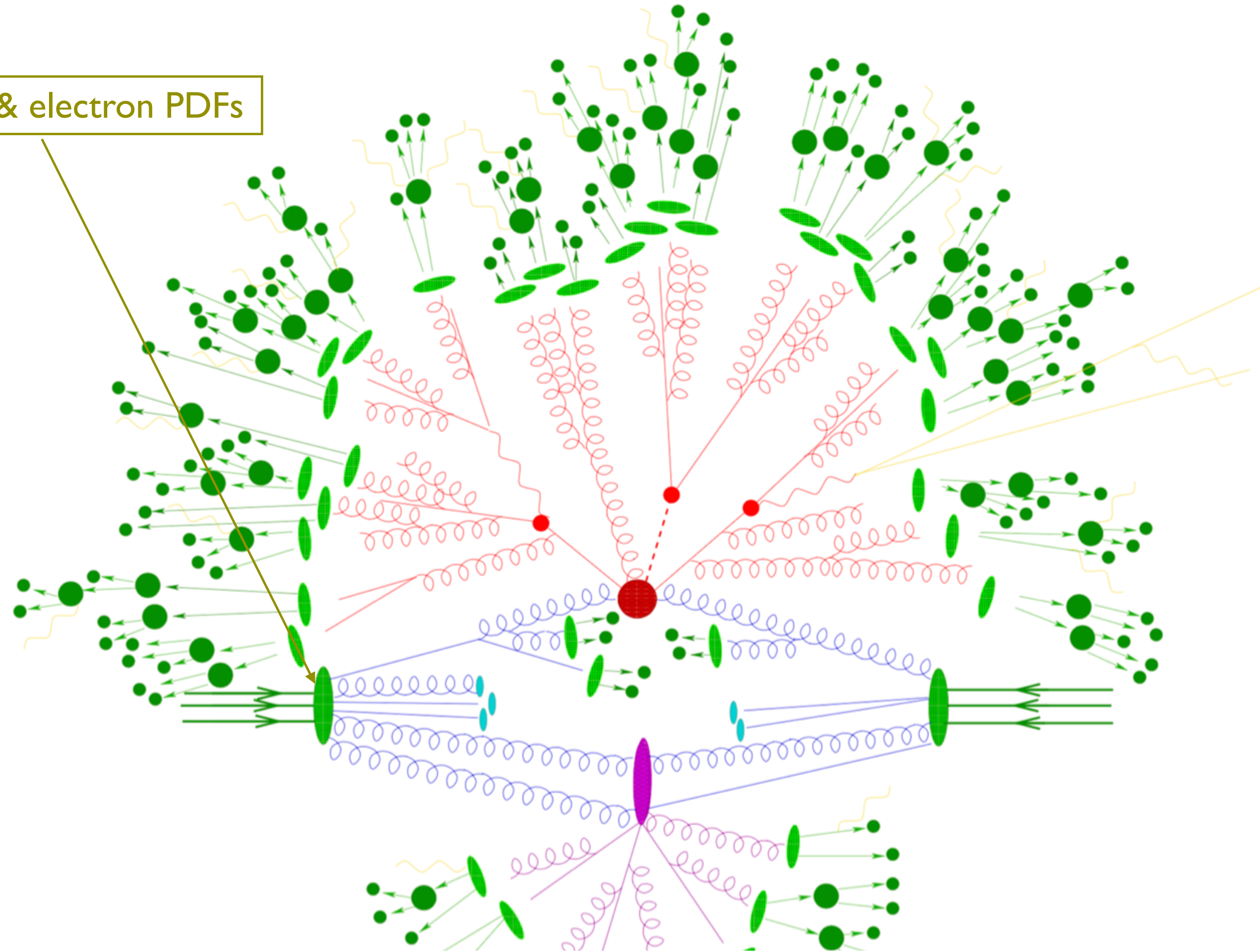
Why are event generators important?

Because all our forward simulation chain depends on them!

Why are event generators non-trivial?

Because they contain *all* our knowledge of particle physics!

Beam spectra & electron PDFs



The importance of MC event generators

28 / 26

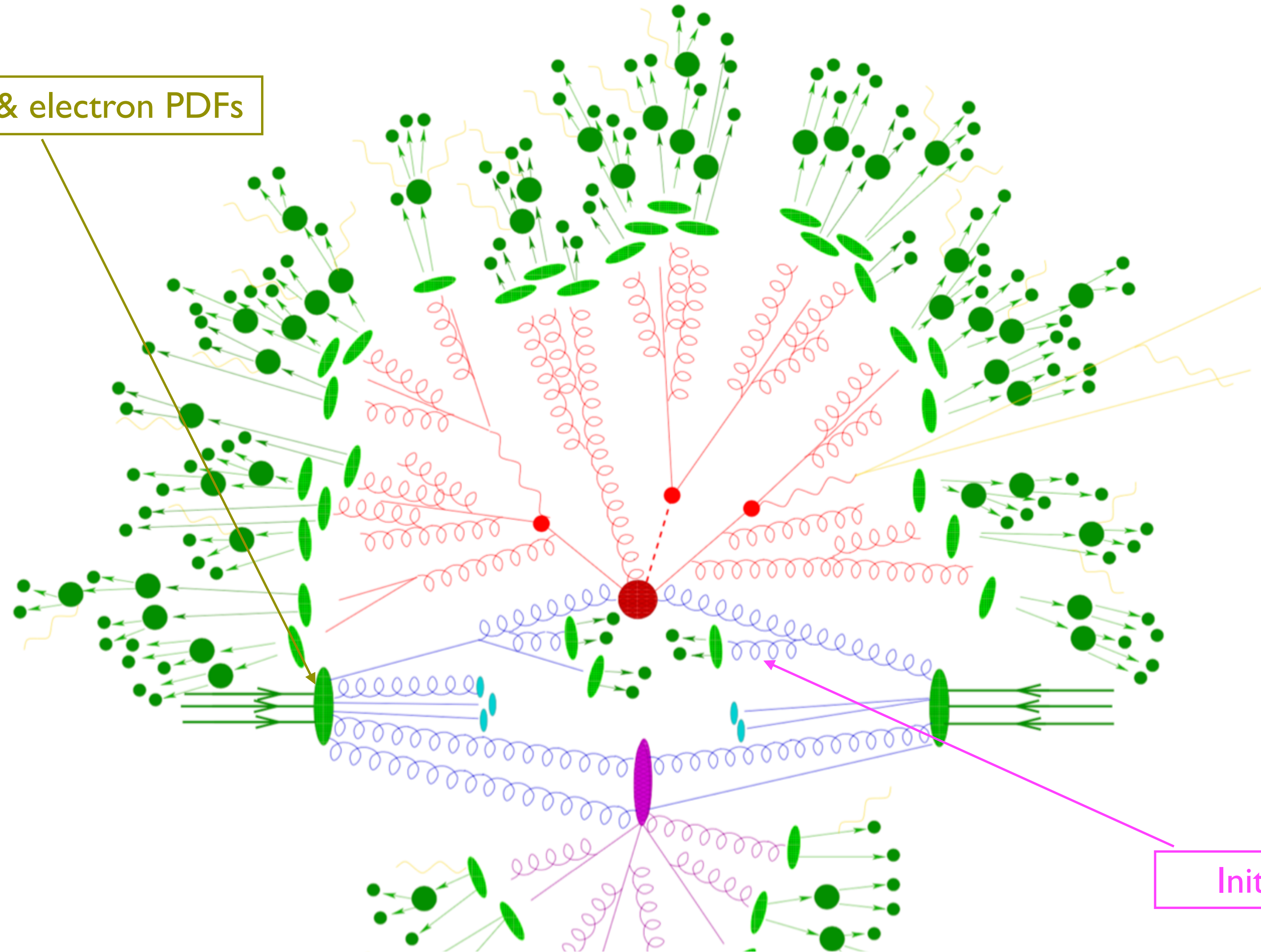
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Initial state QED radiation

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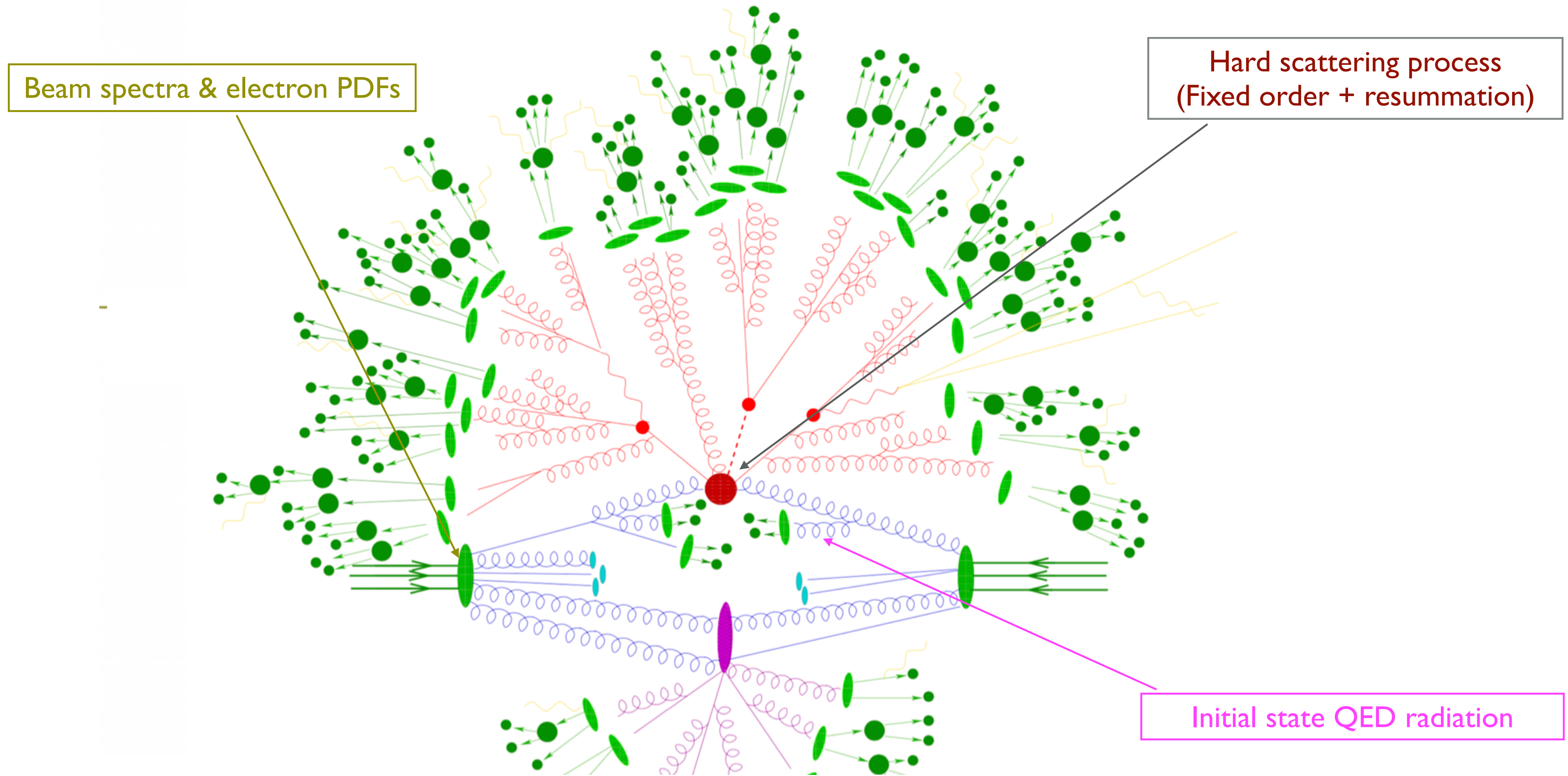
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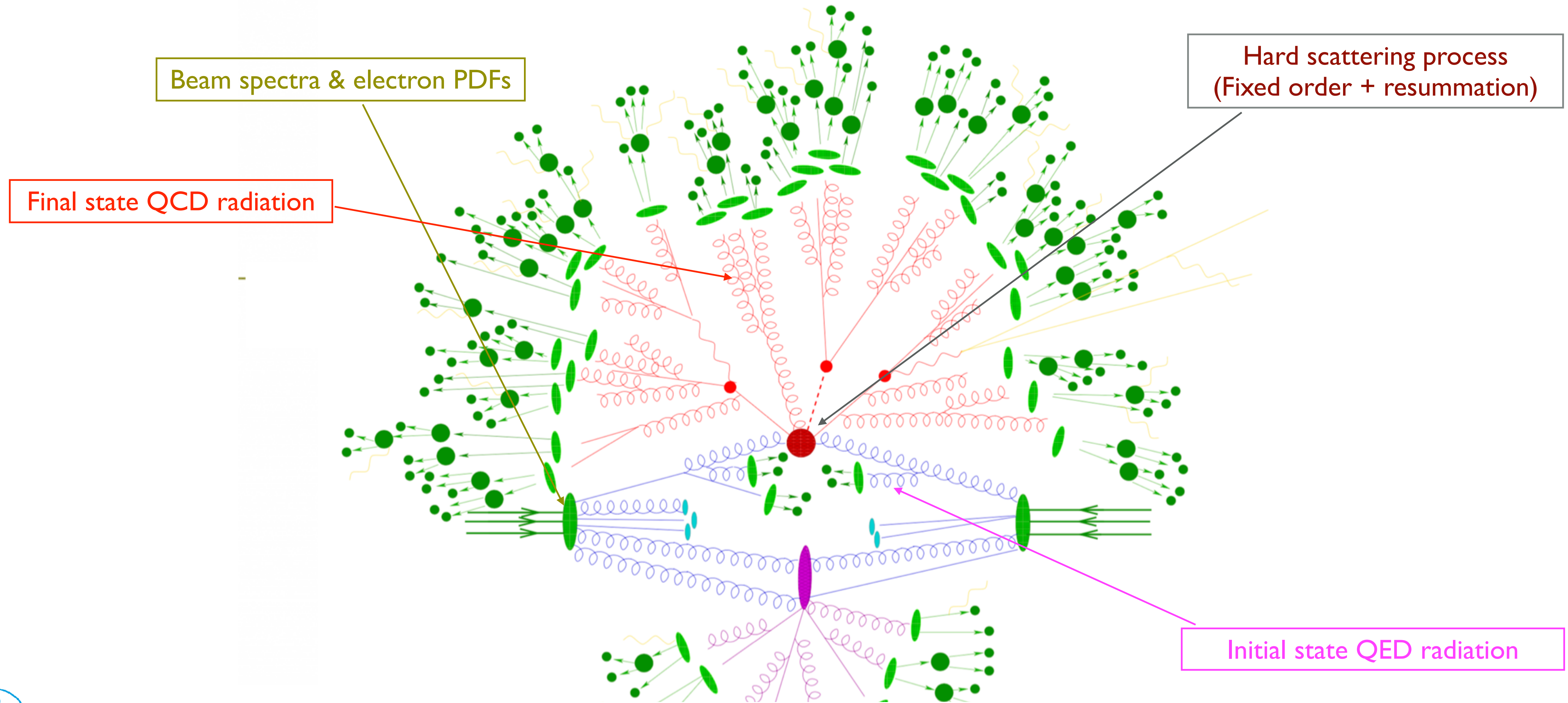
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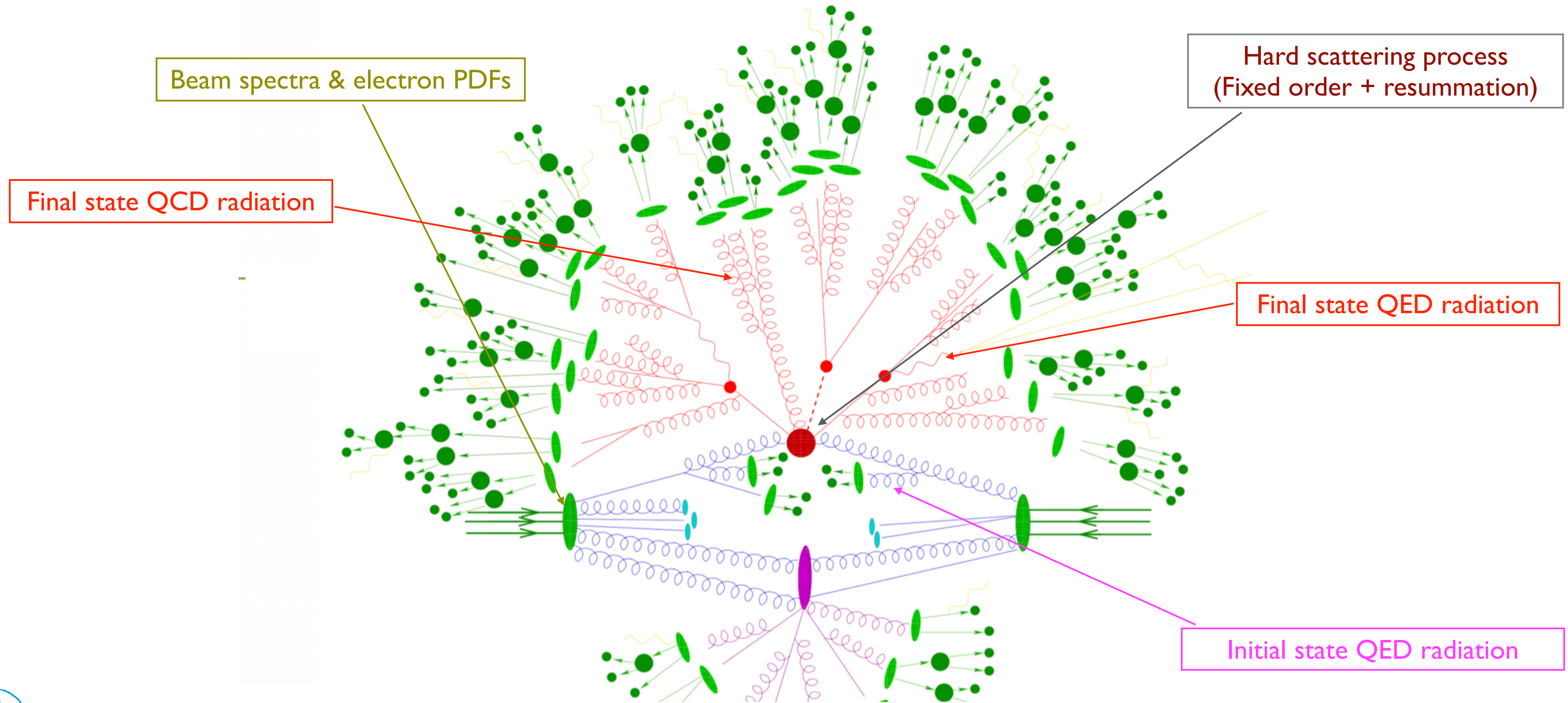
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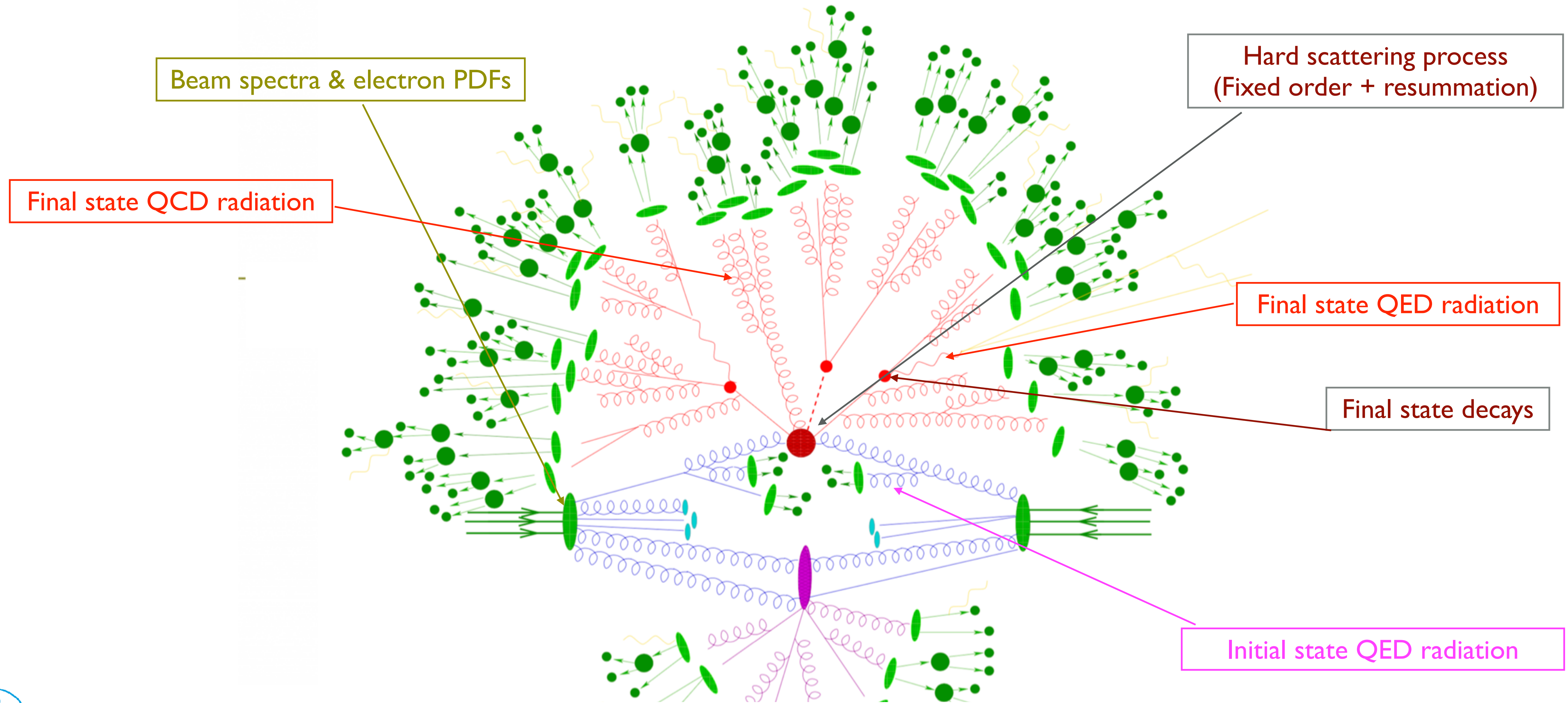
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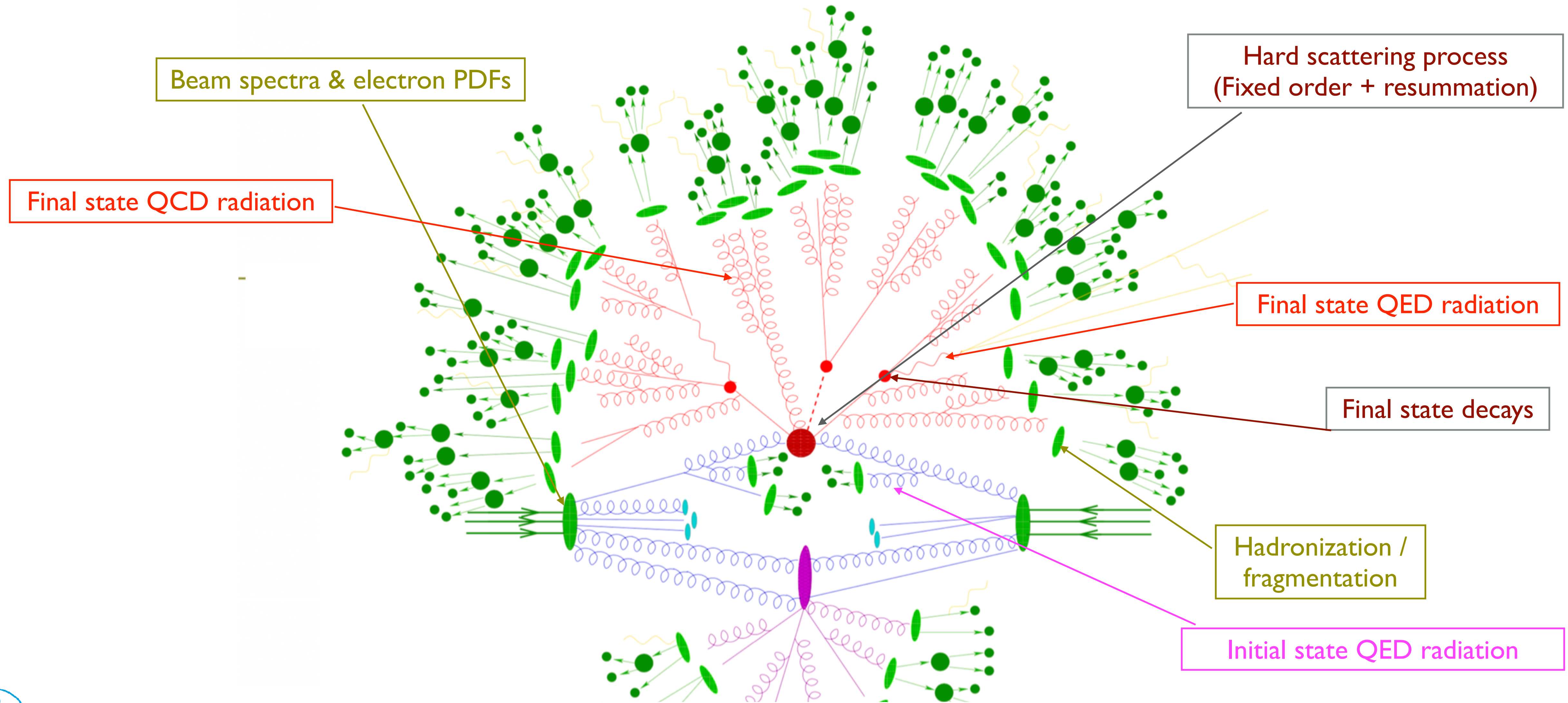
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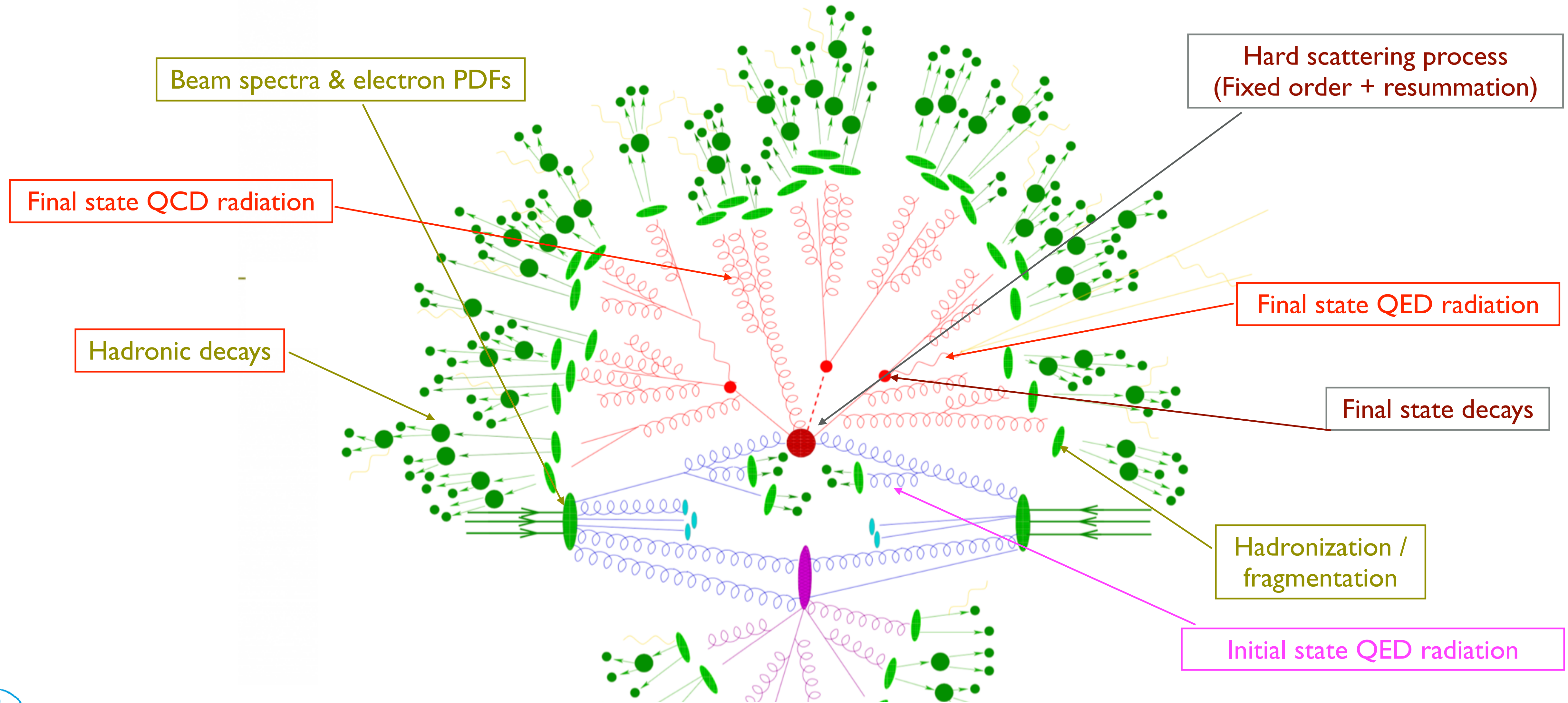
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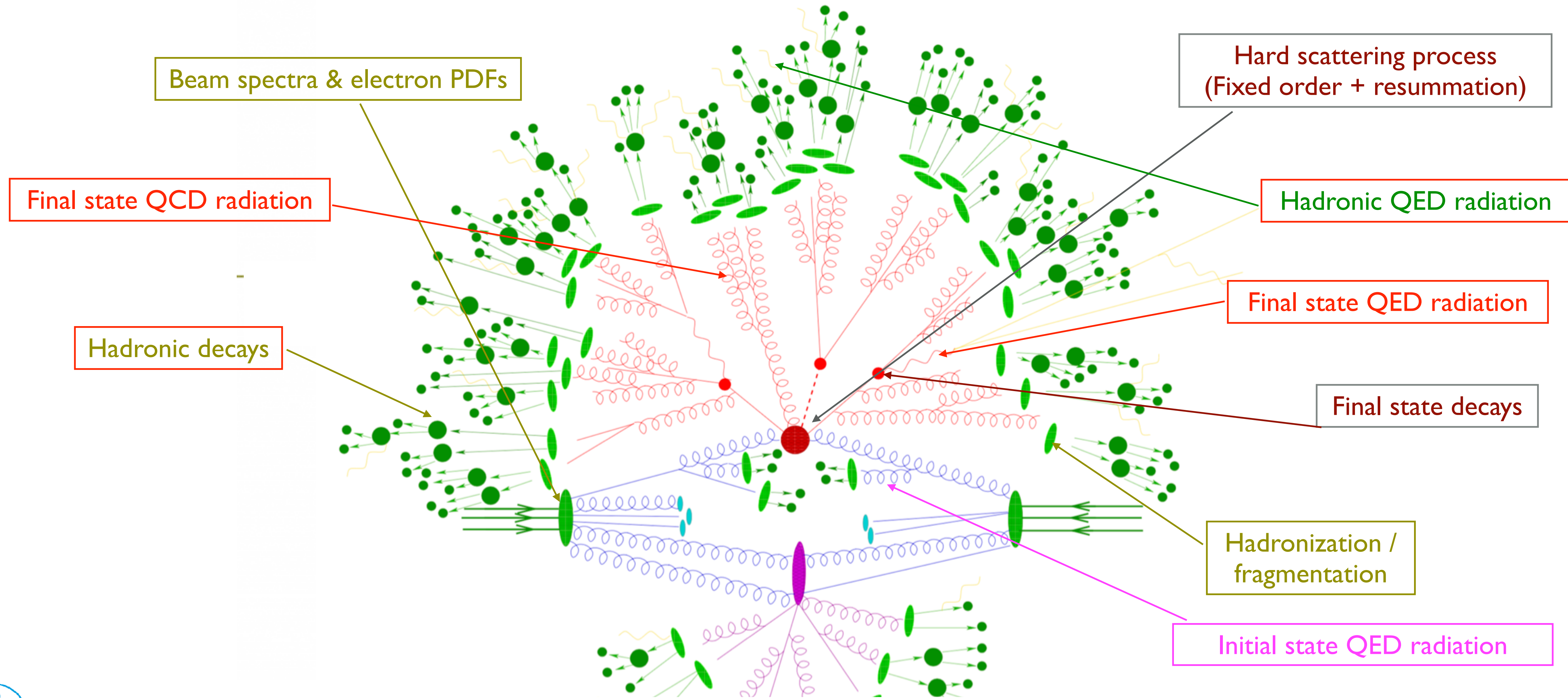
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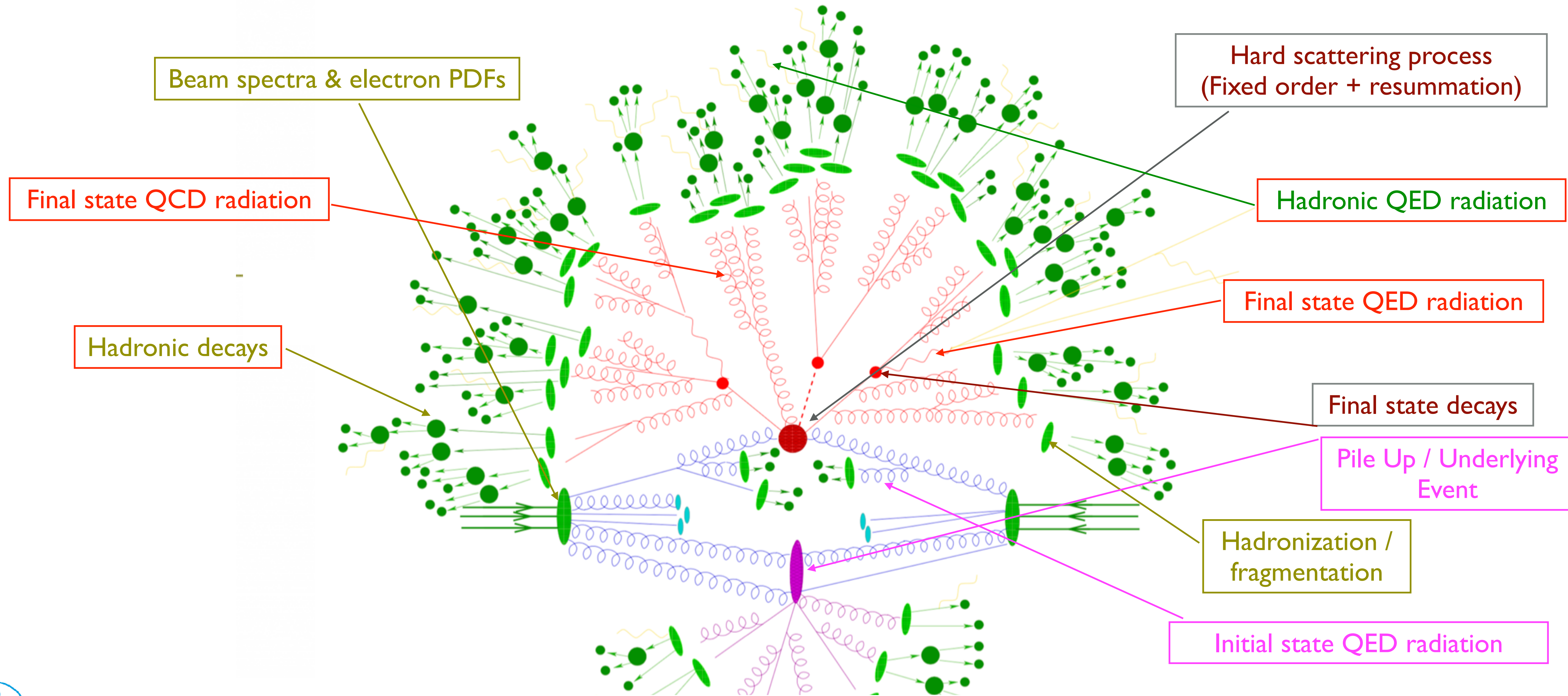
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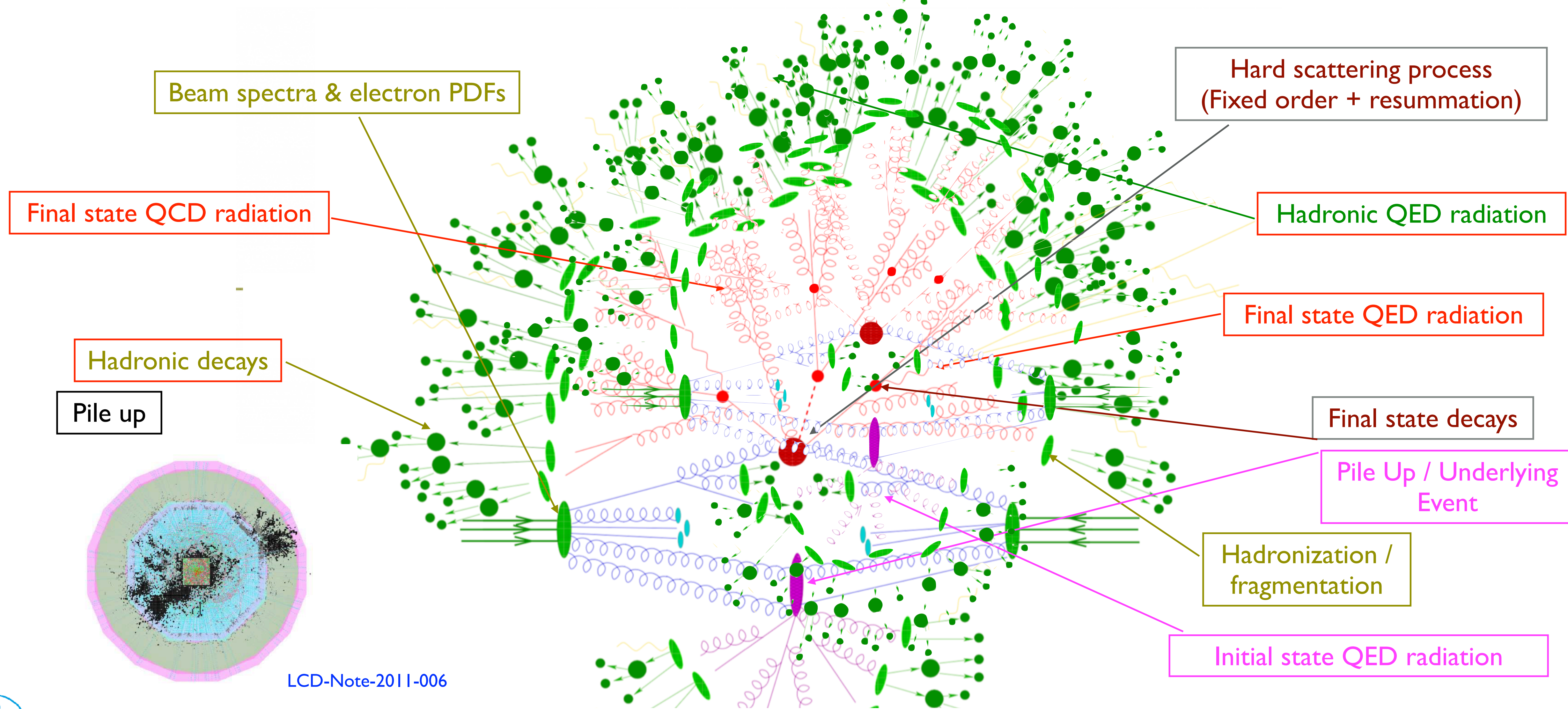
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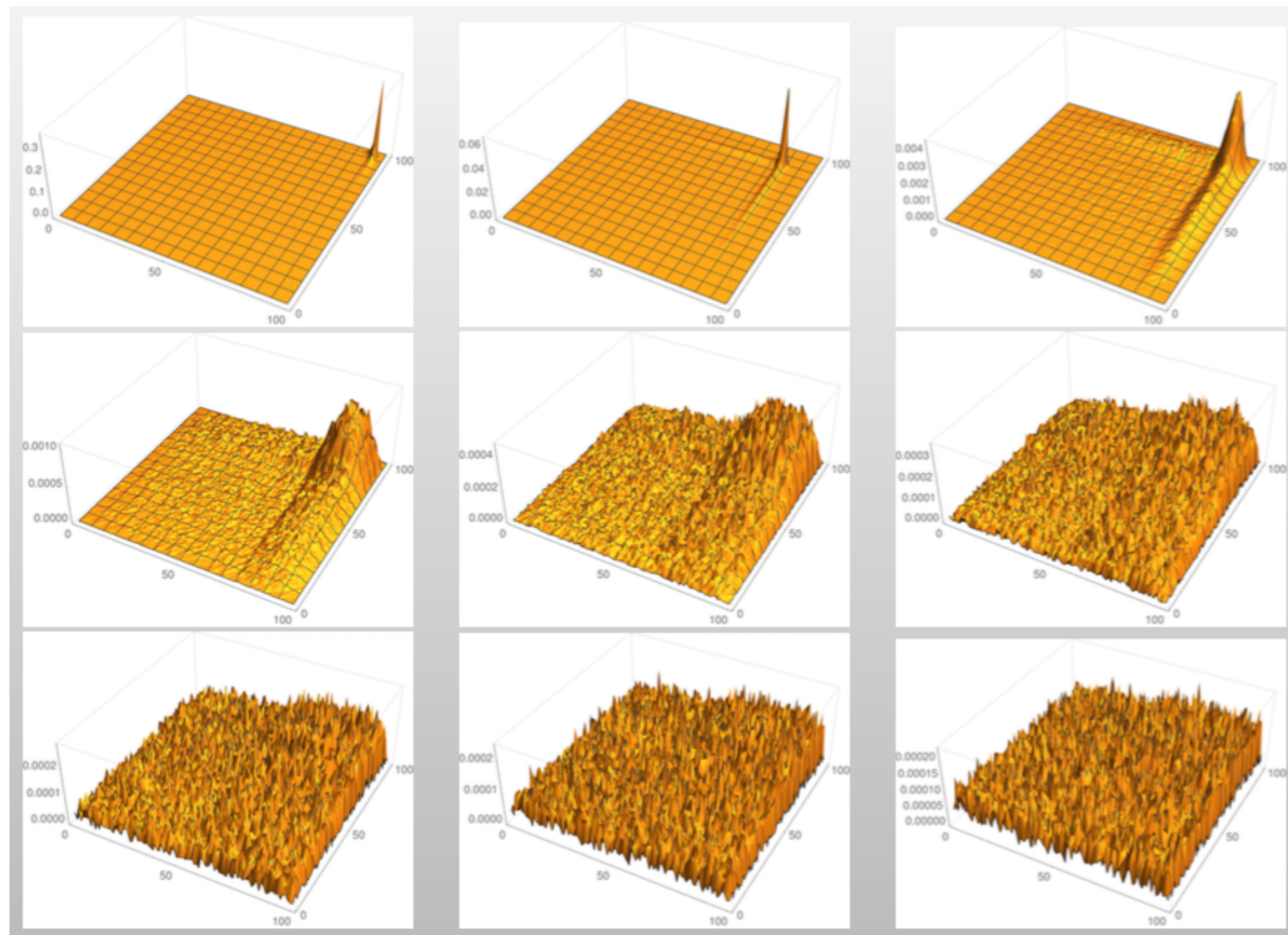
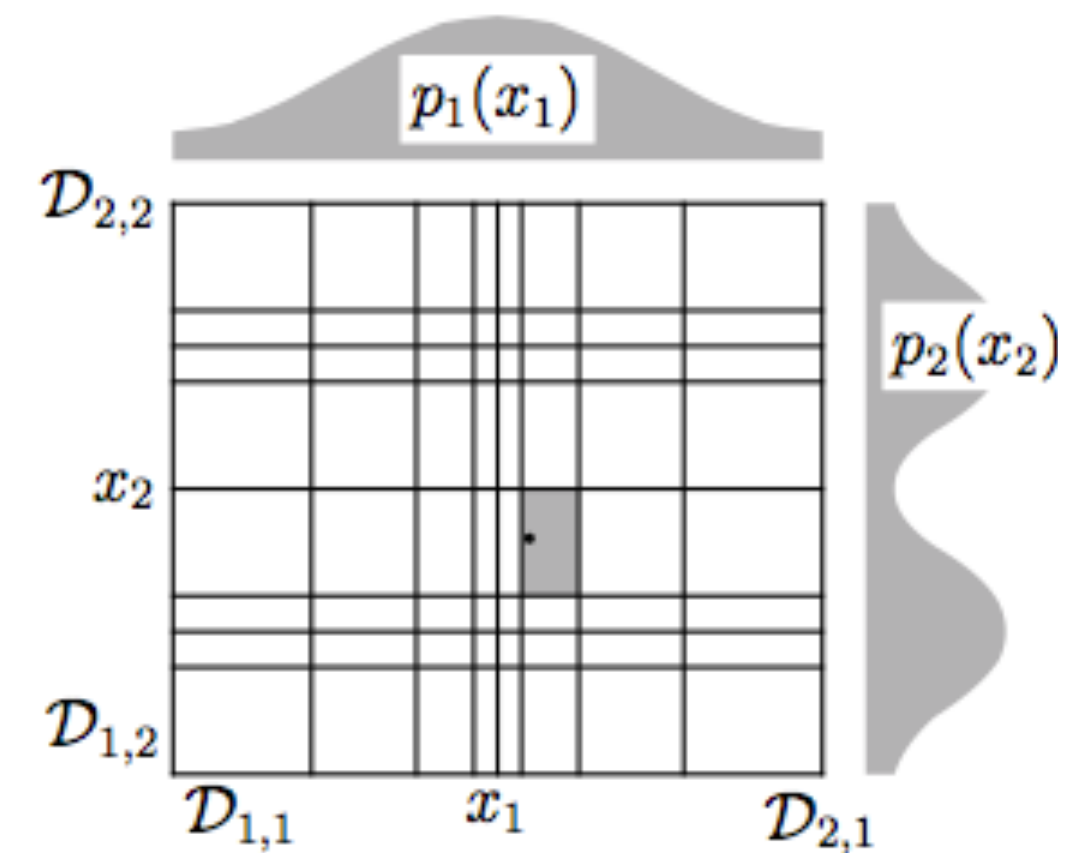
Beam simulations (technical details)

29 / 26

CIRCE2 algorithm T. Ohl, 1996, 2005

↪ Talk by Thorsten Ohl 06/2023: <https://indico.cern.ch/event/1266492/>

- Adapt **2D factorized variable width histogram** to steep part of distribution
- Smooth correlated fluctuations with moderate **Gaussian filter** [suppresses artifacts from limited GuineaPig statistics]
- Smooth **continuum/boundary bins separately** [avoid artificial beam energy spread]



(171,306 GuineaPig events in 10,000 bins)

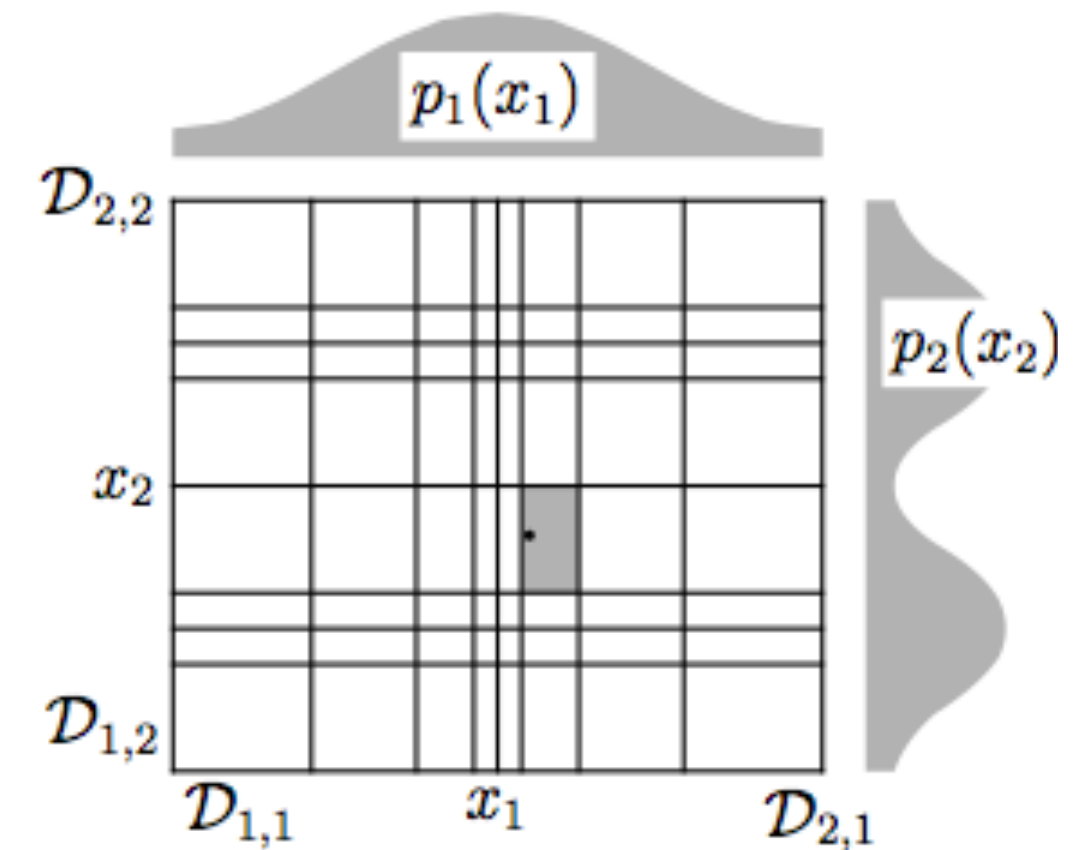
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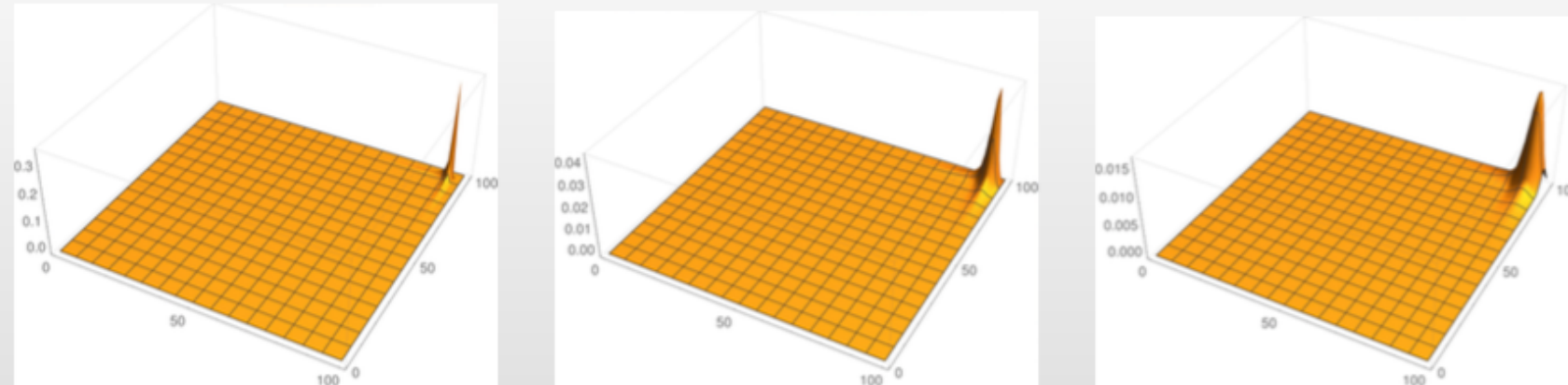
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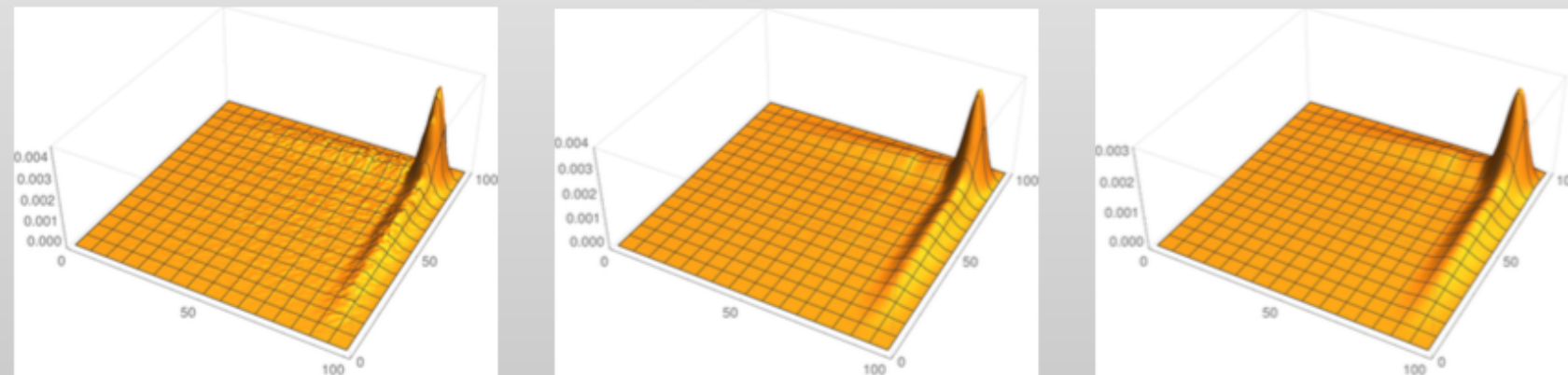
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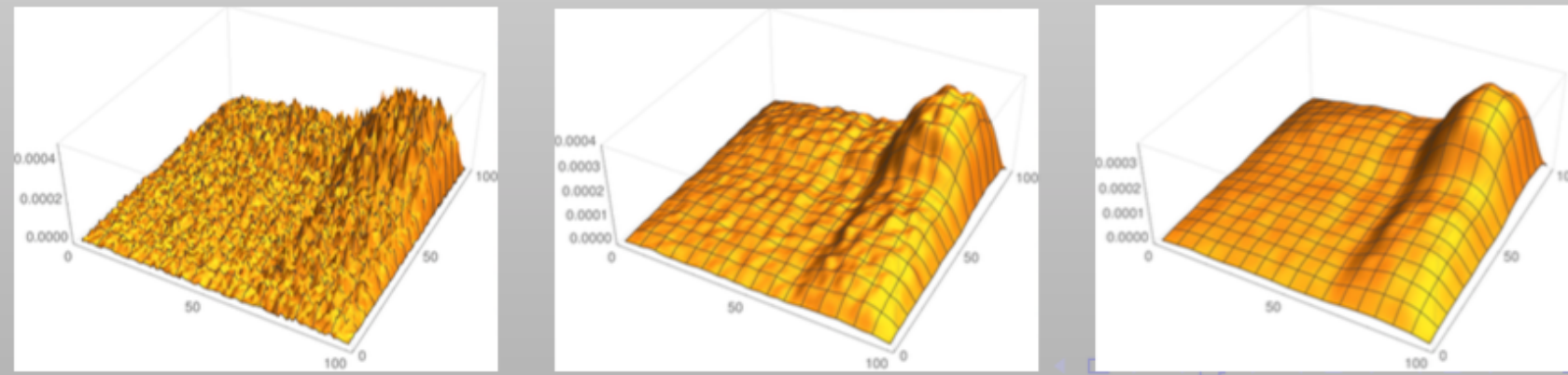
► **iterations** = 0 and **smooth** = 0, 3, 5:



► **iterations** = 2 and **smooth** = 0, 3, 5:



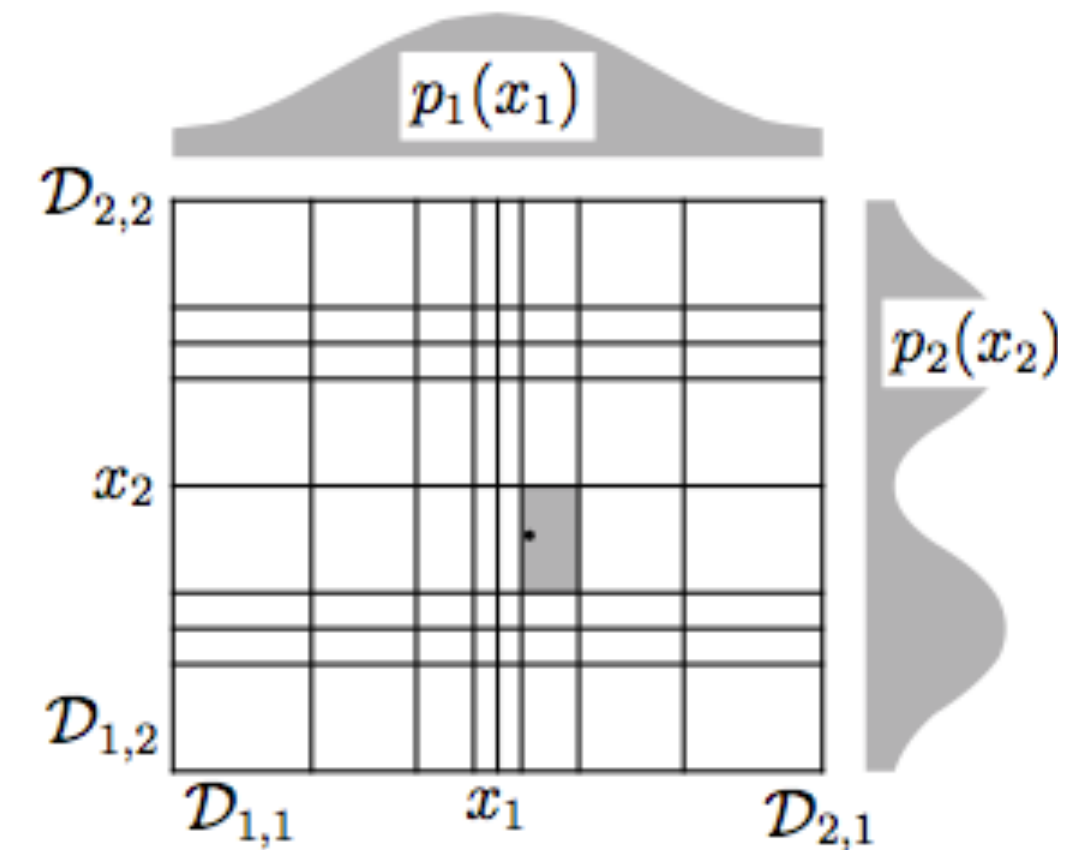
► **iterations** = 4 and **smooth** = 0, 3, 5:



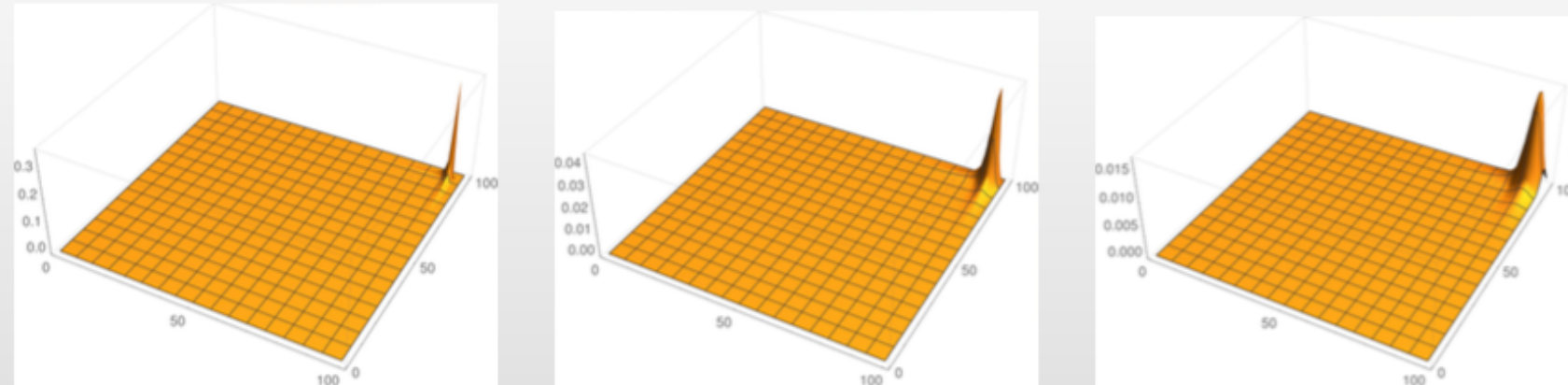
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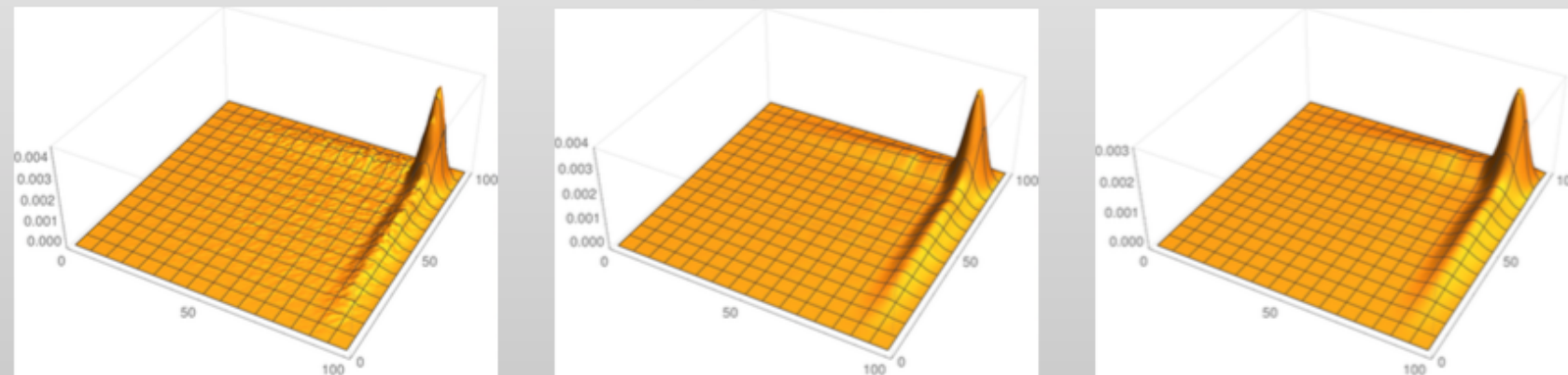
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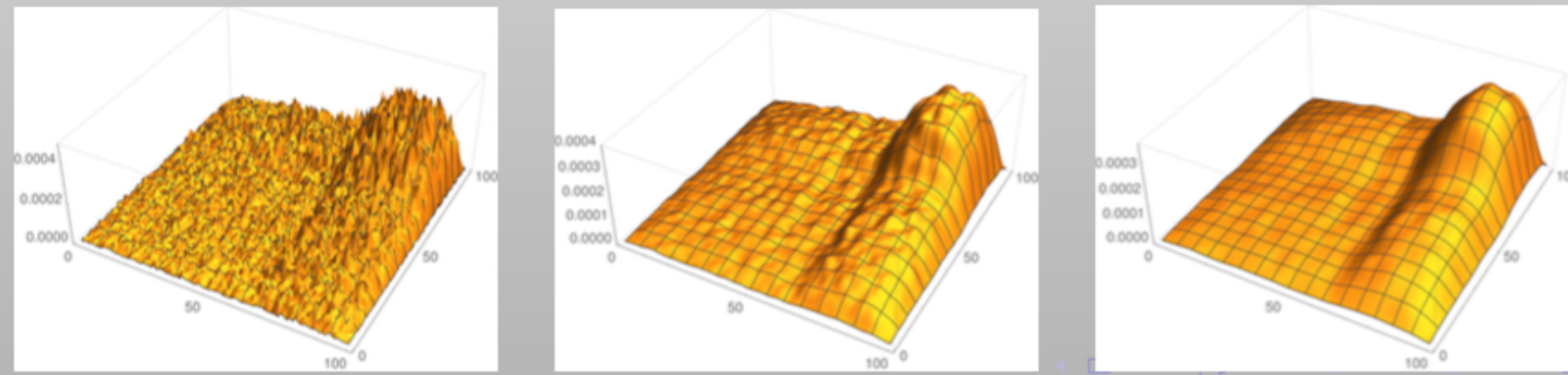
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1. Run Guinea-Pig++ with

```
do_lumi=7; num_lumi=100000000; num_lumi_eg=100000000; num_lumi_gg=100000000;
```

to produce lumi.[eg][eg].out with (E_1, E_2) pairs.

[Large event numbers, as Guinea-Pig++ will produce only a small fraction!]

2. Run circe2_tool.opt with steering file

```
{ file="ilc500/beams.circe"
  { design="ILC" roots=500 bins=100 scale=250
    { pid/1=electron pid/2=positron pol=0
      events="ilc500/lumi.ee.out" columns=2
      lumi = 1564.763360
      iterations = 10
      smooth = 5 [0,1) [0,1)
      smooth = 5 [1] [0,1) smooth = 5 [0,1) [1] } } }
```

to produce correlated beam description

3. Run WHIZARD with SINDARIN input:

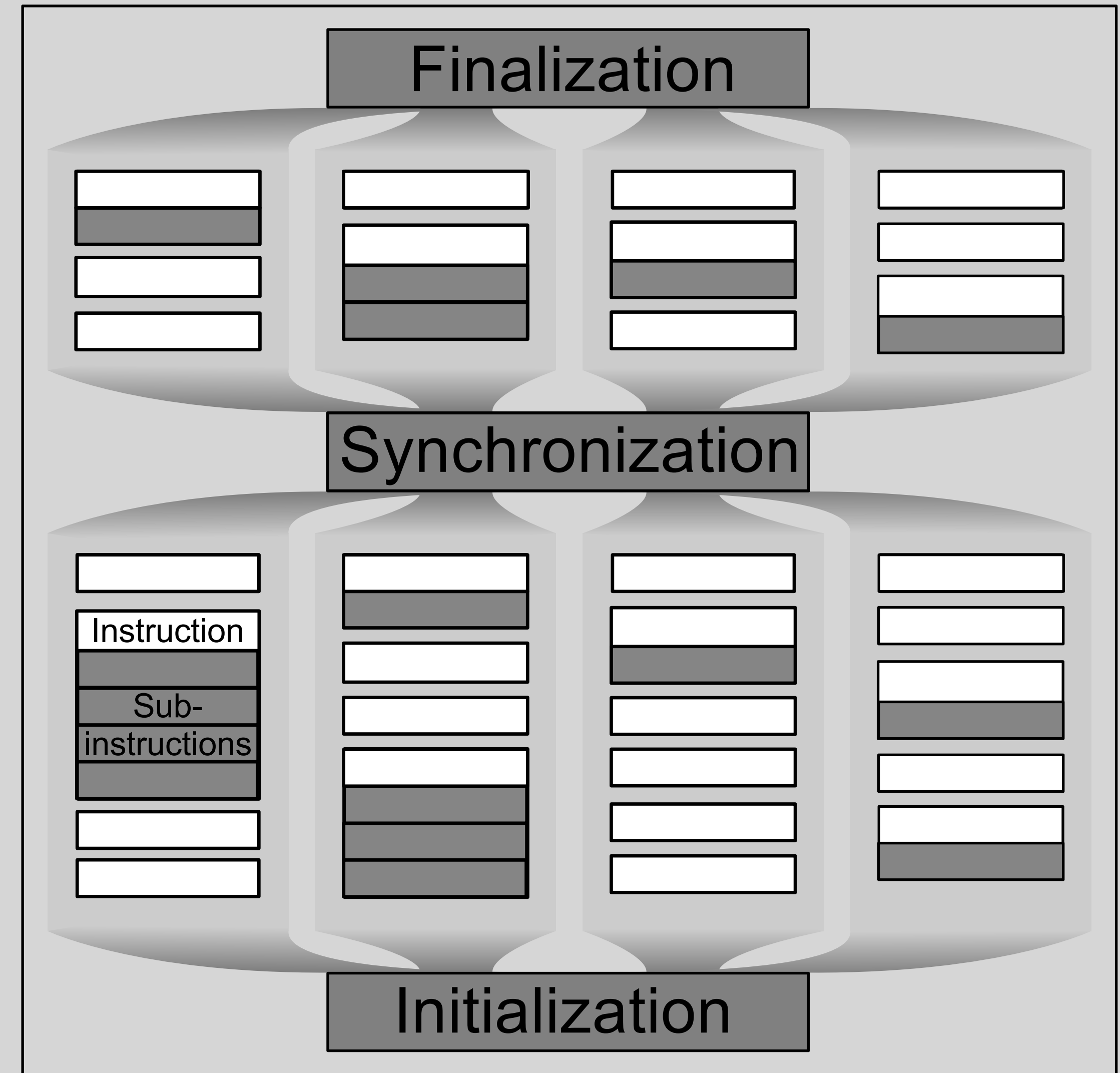
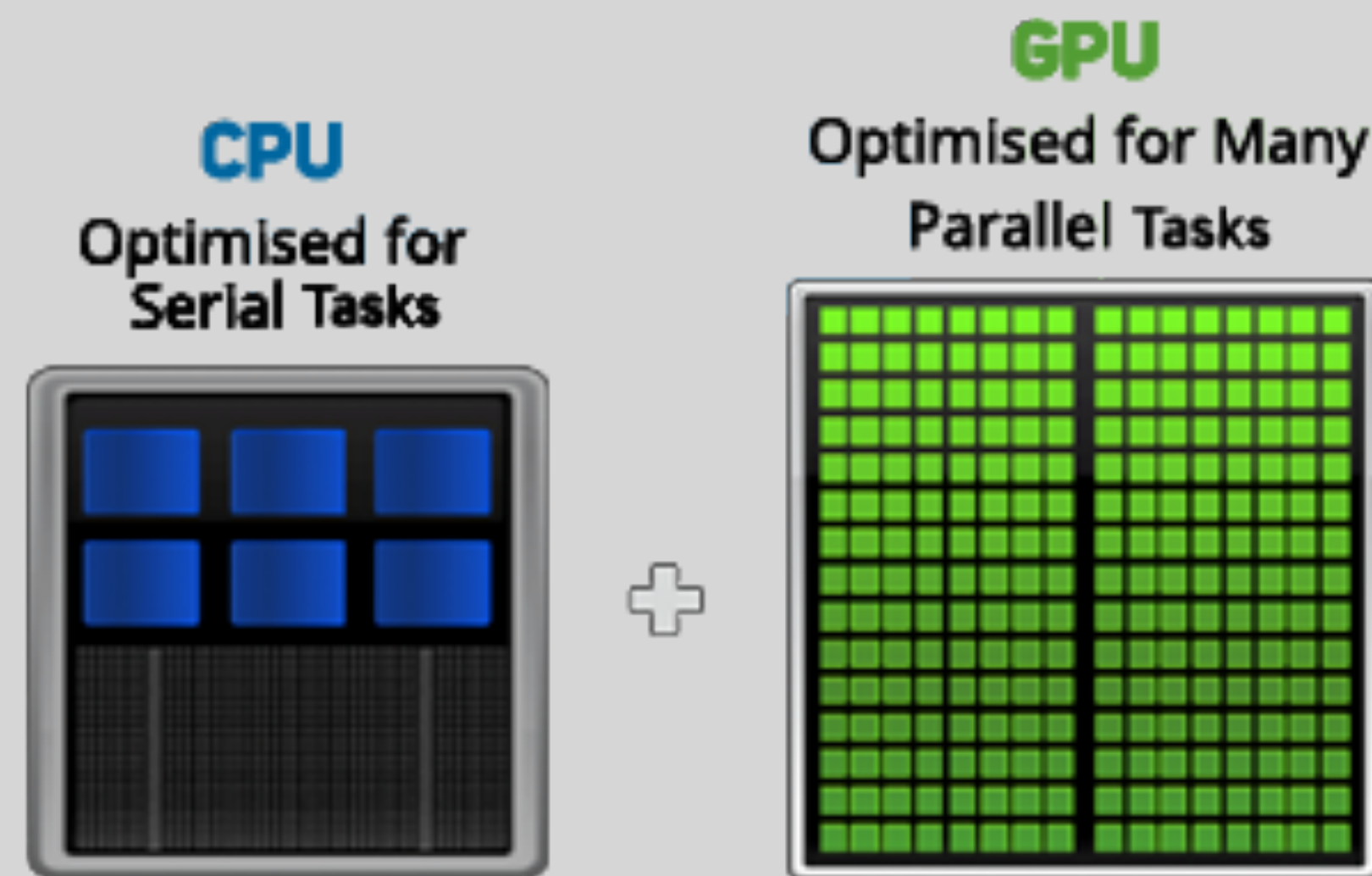
3 simulation options

```
beams = e1, E1 => circe2
$circe2_file = "ilc500.circe"
$circe2_design = "ILC"
?circe_polarized = false
```

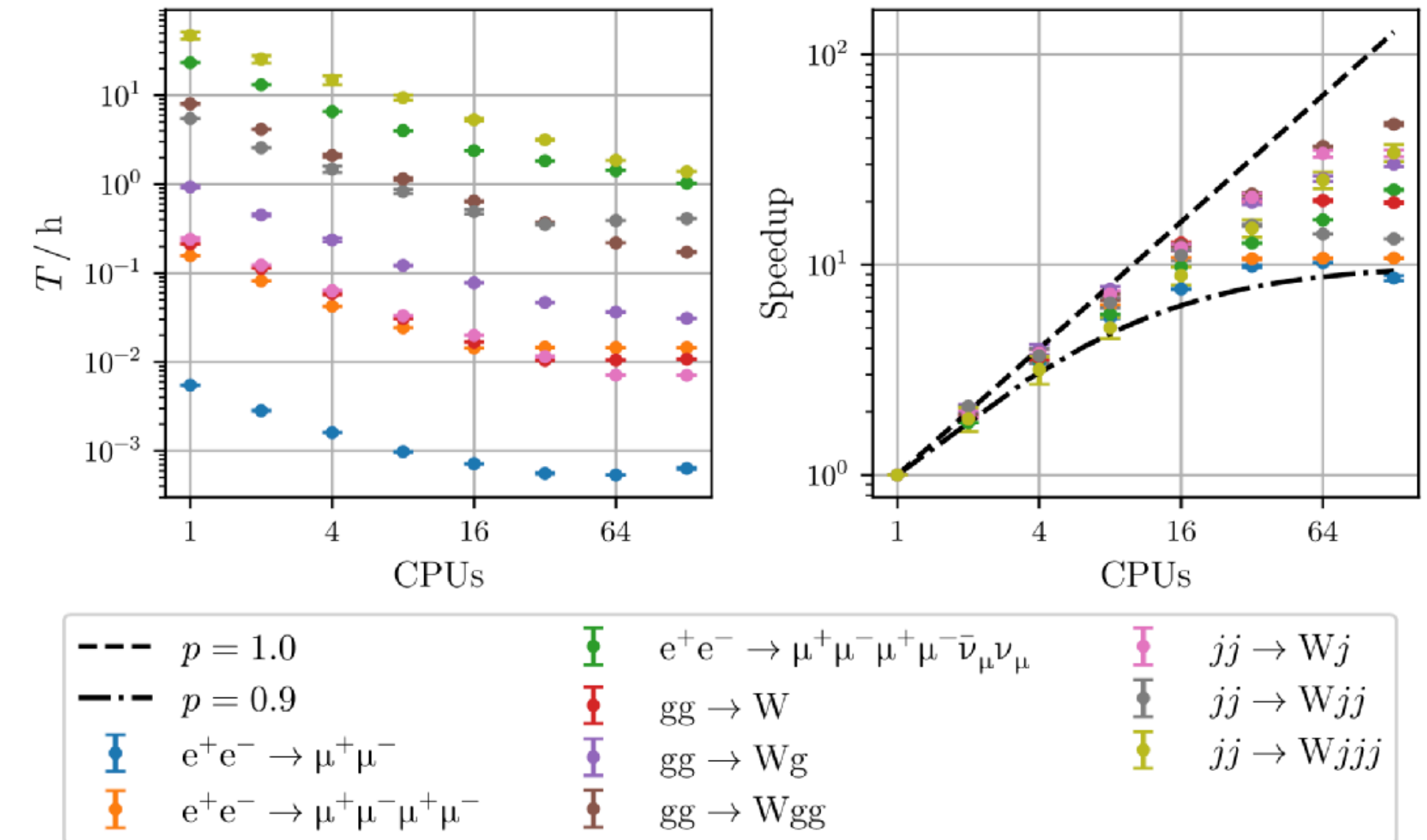
1. Unpolarized simulation with unpol. spectra
2. Pol. simulation: unpol. spectra + pol. beams
3. Polarized spectrum with helicity luminosities

Monte Carlo Efficiency / Speed Up

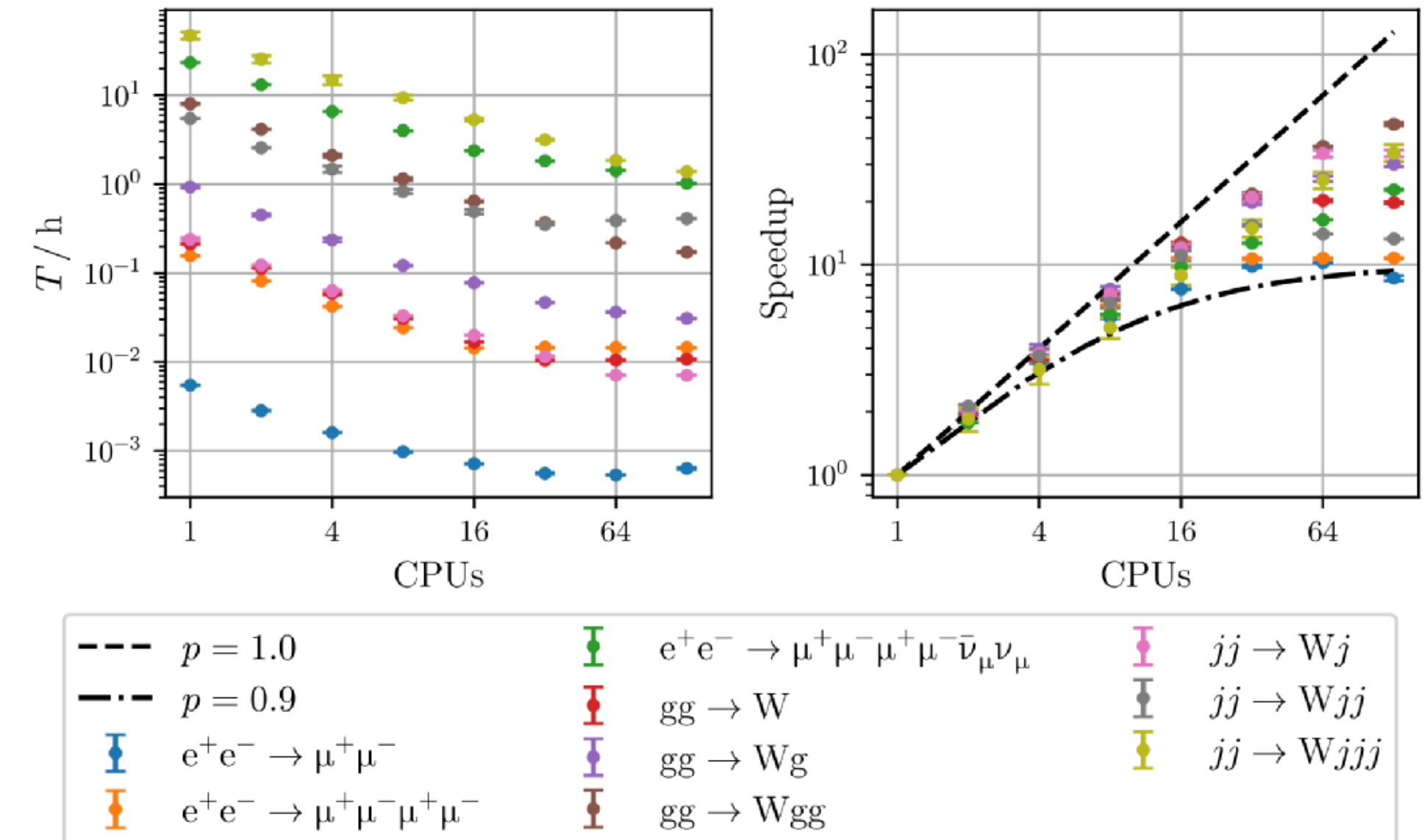
30 / 26



- Braß/Kilian/JRR, 1811.09711

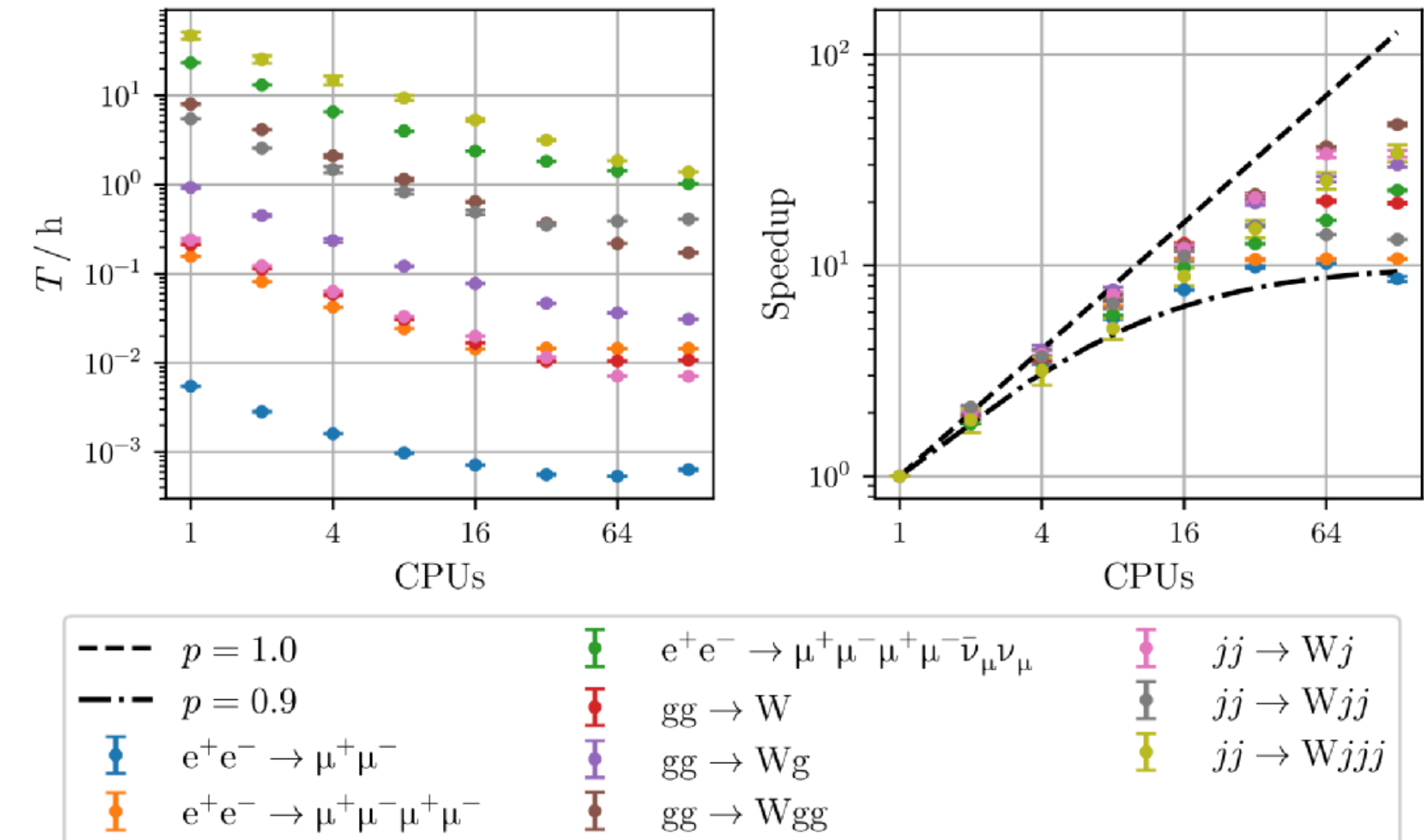


- Parallelization of integration: OMP multi-threading for different helicities / PS channels [can do also parallel event generation]
- MPI parallelization (using OpenMPI or MPICH) Braß/Kilian/JRR, 1811.09711
- Distributes workers over multiple cores
- Grid adaption needs non-trivial communication
- Speedups of 10 to 30, saturation at O(100) tasks
- Load balancer / non-blocking communication
- Offloading of MEs / parts of infrastructure code to GPU



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- Bottleneck: cache of GPU allows only for small-ish code chunks transferred
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Very preliminary:

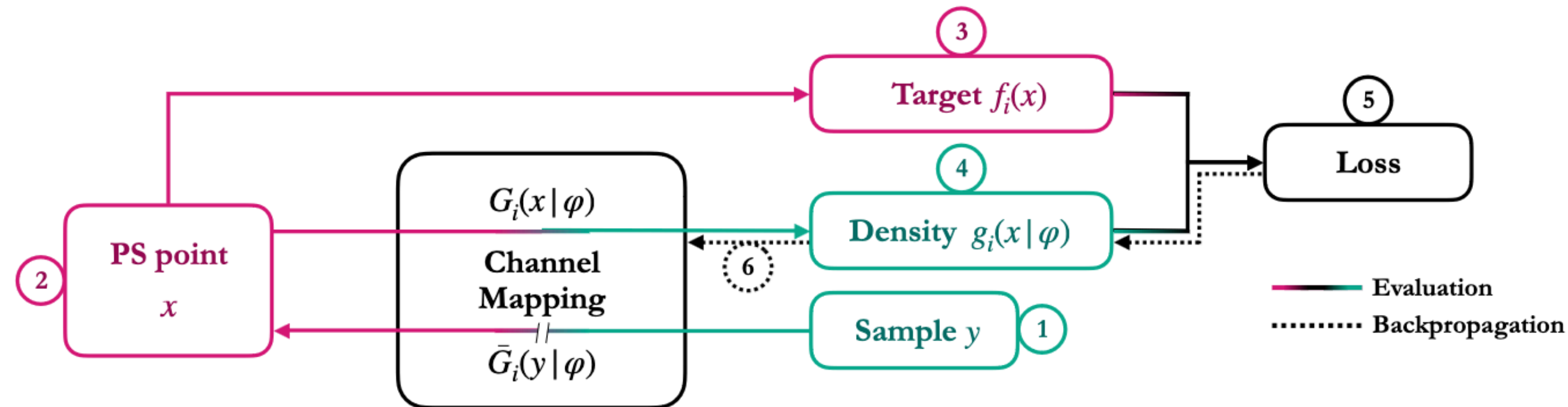
Process	$t^{CPU}[s]$	$t^{GPU}[s]$
$e^+e^- \rightarrow t\bar{t}$	0.98	4.28
$e^+e^- \rightarrow bW^+\bar{b}W^-$	28.8	23.1
$e^+e^- \rightarrow bW^+\bar{b}W^-H$	57.5	37.8
$e^+e^- \rightarrow b\bar{b}\bar{\nu}_e e^- \bar{\nu}_\mu \mu^+$	154	124
$e^+e^- \rightarrow 2j$	1.9	5.4
$e^+e^- \rightarrow 3j$	45	65
$e^+e^- \rightarrow 4j$	870	608
$e^+e^- \rightarrow 5j$	4106	978
$pp \rightarrow jj$	42	86
$pp \rightarrow W^+W^-W^+W^-$	670	192

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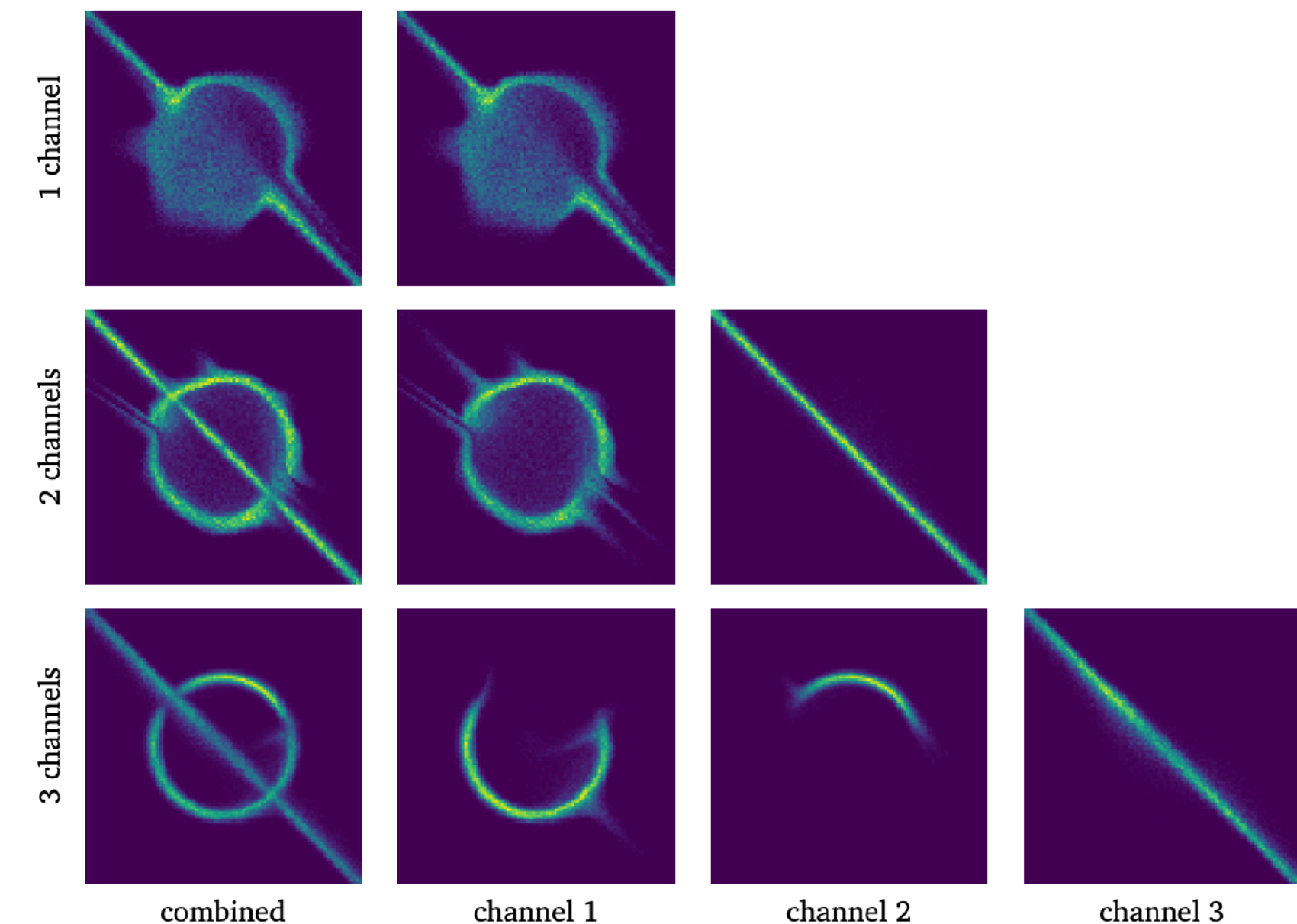
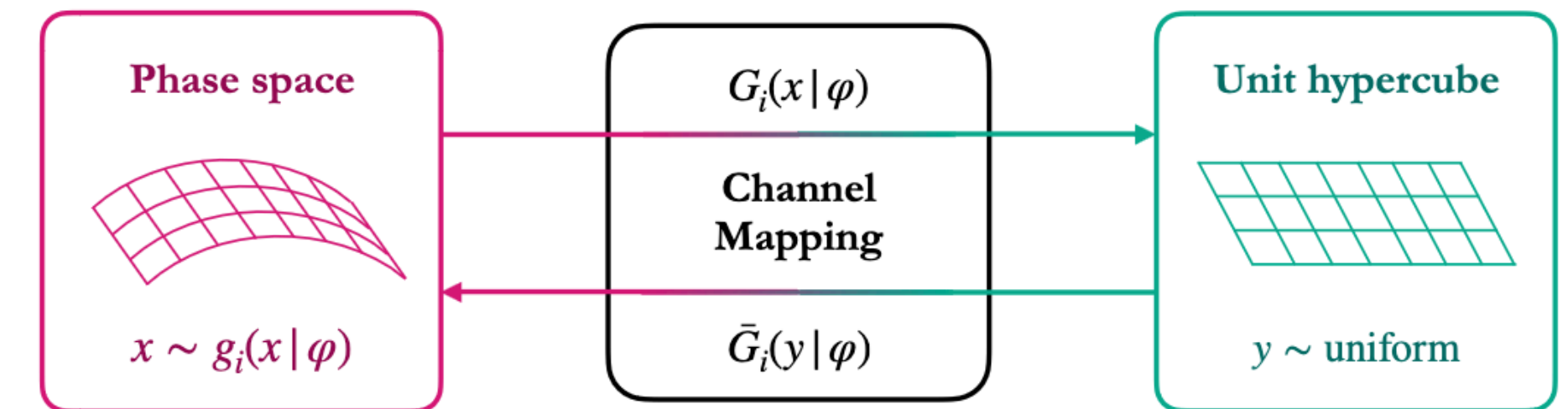
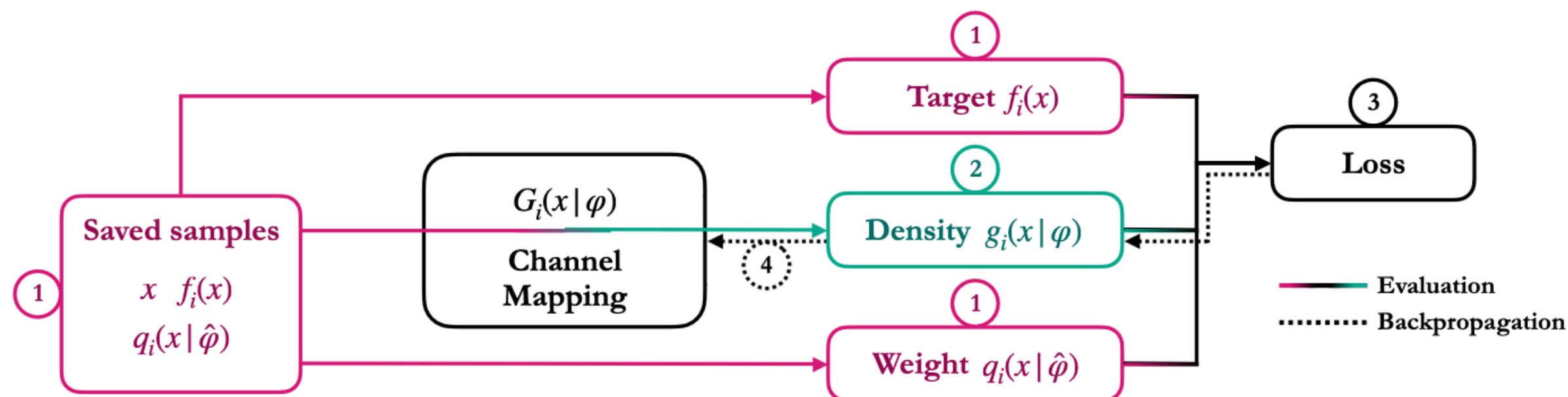
- Phase space integration / adaptation by Invertible Neural Networks (INNs) / normalizing flows
- Define divergence-based loss function
- Use of buffered losses and training

Hoeche et al., 2001.10028, Heimgartner / Winterhalder et al., 2212.06172

Online training:

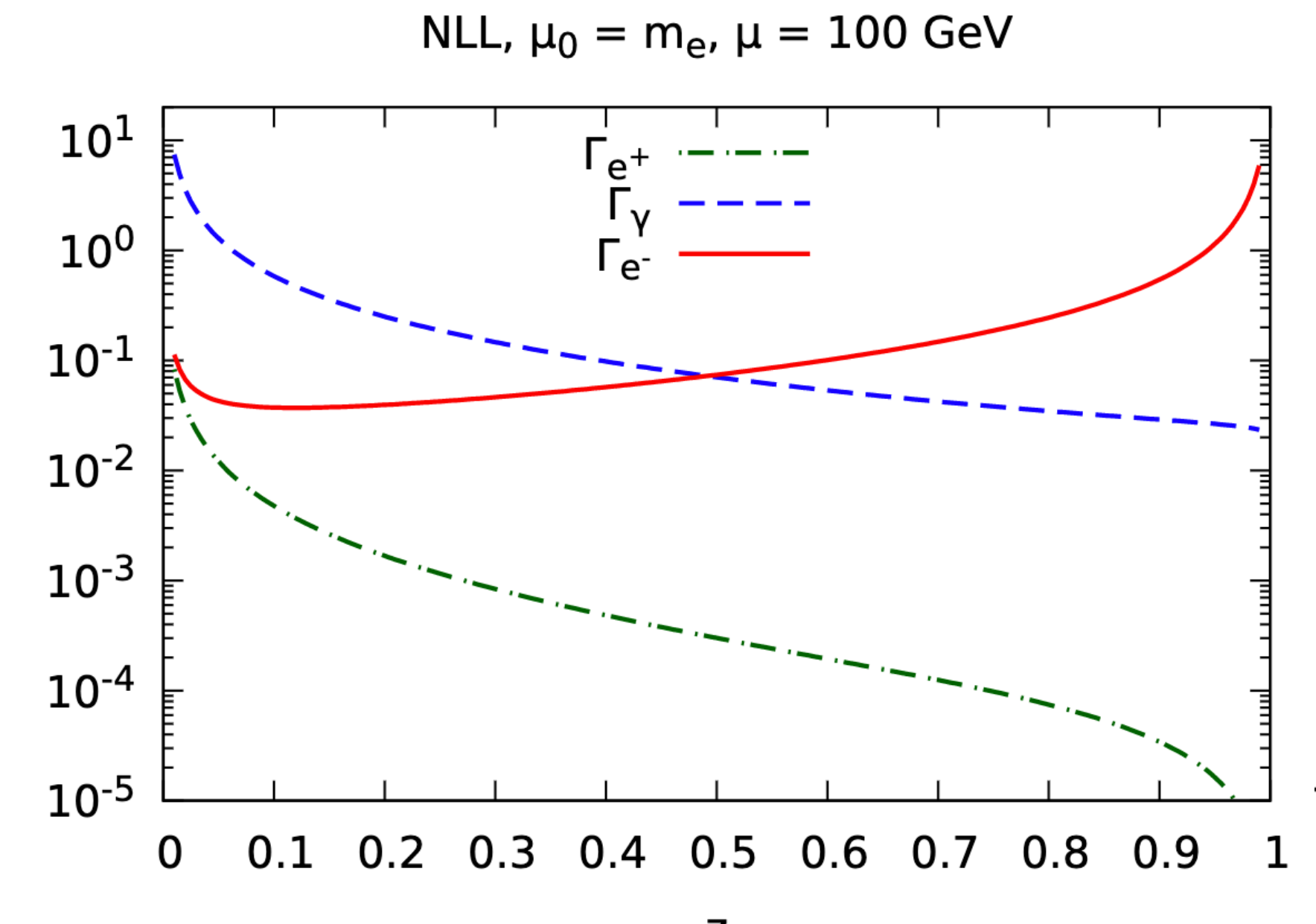


Buffered training:

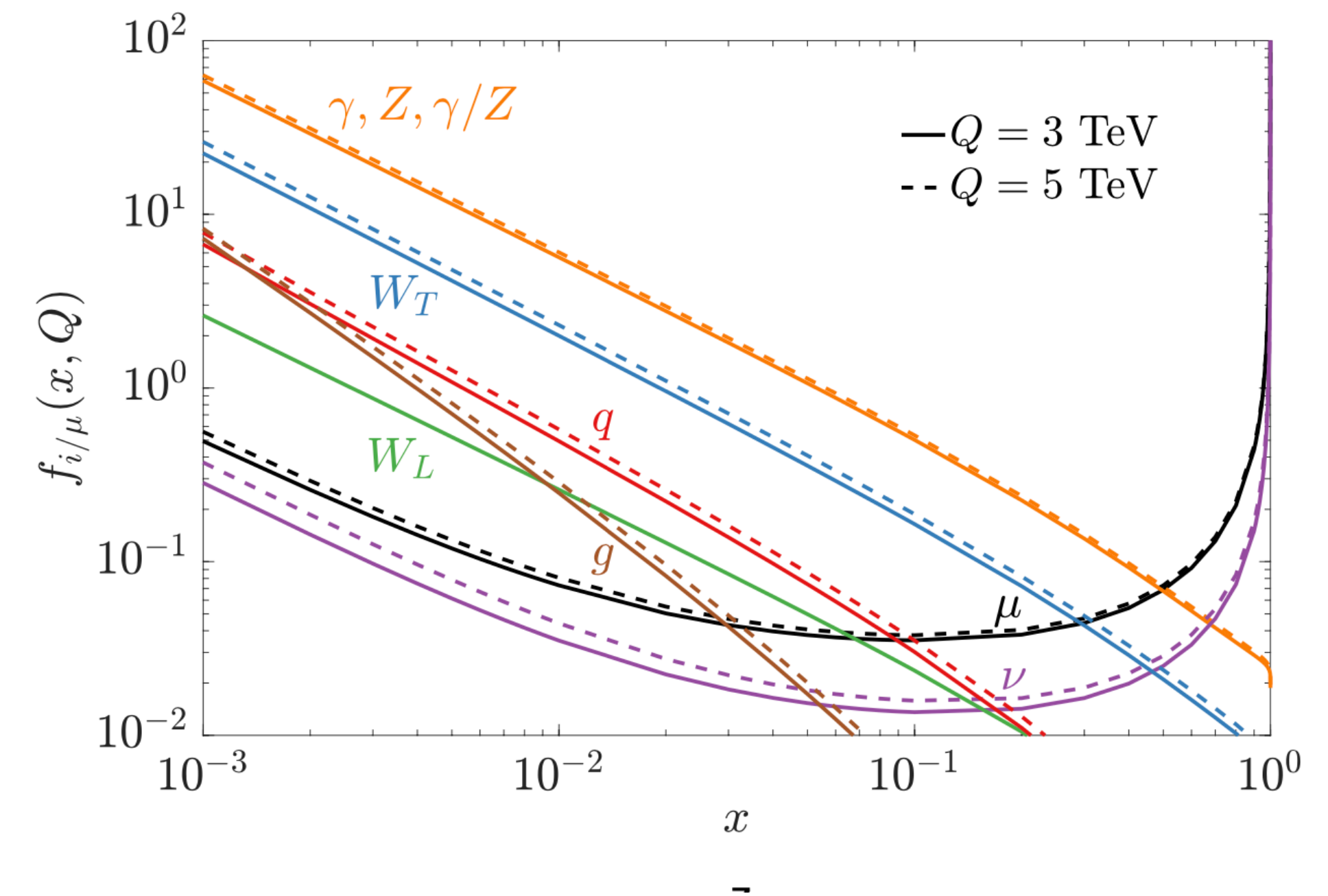


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[Han/Ma/Xie, 2007.14300, 2103.09844](#)
- ❑ Ancient name (from SSC times!): EWA (“Effective W approximation)
- ❑ Fully inclusive in collinear/forward/beam direction
- ❑ Also: fast interpolation (CTEQ-like) grids available

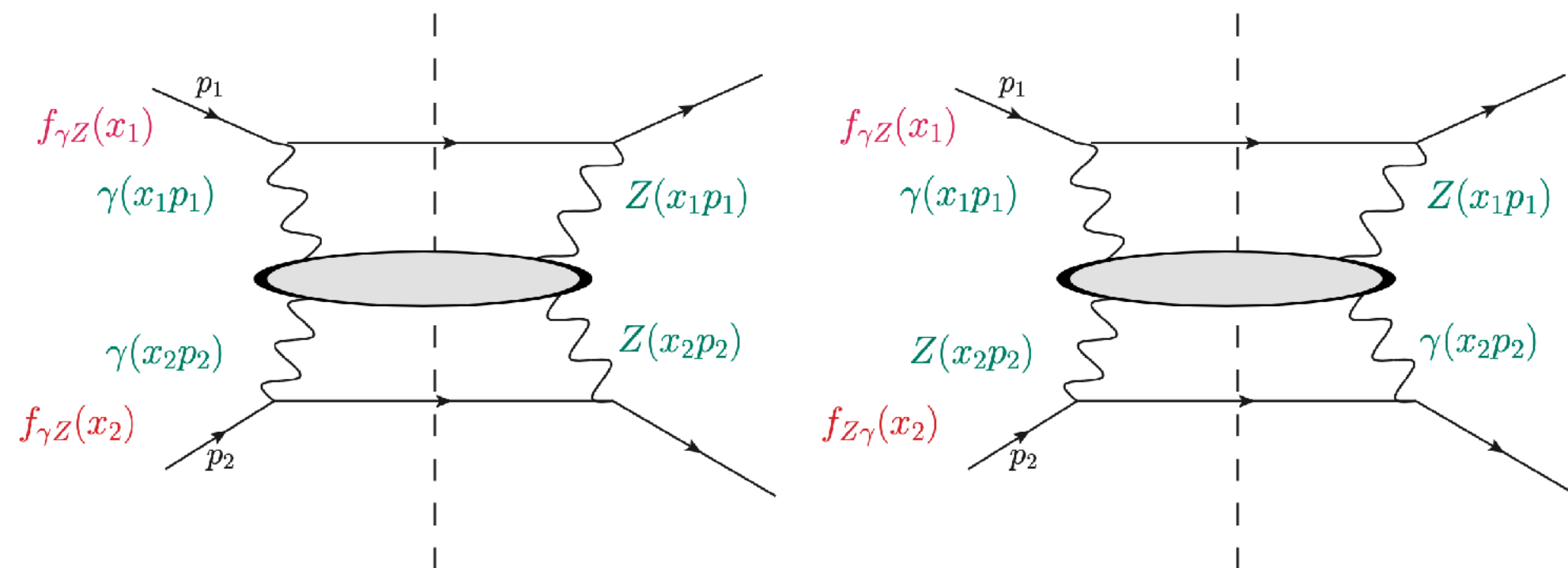
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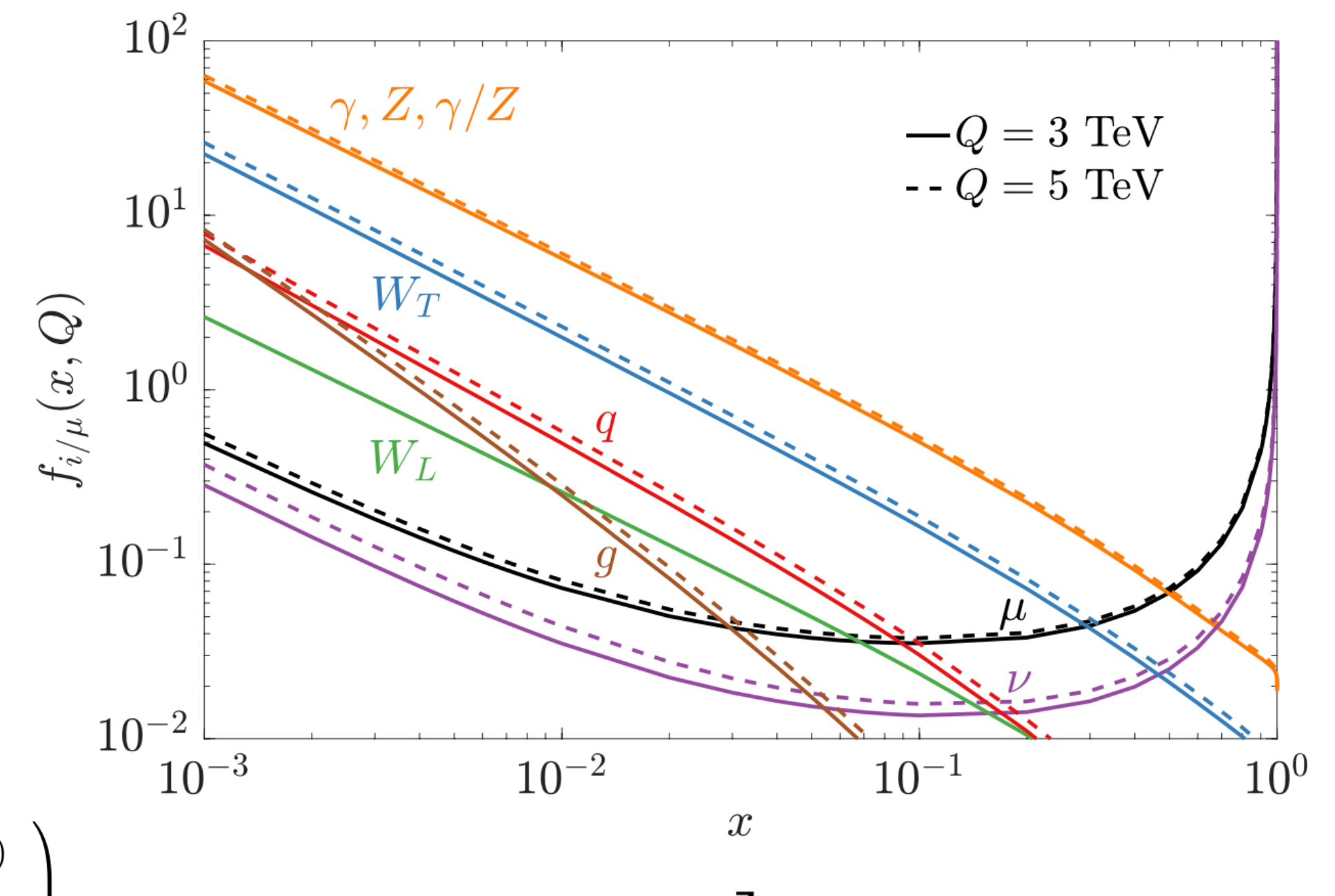
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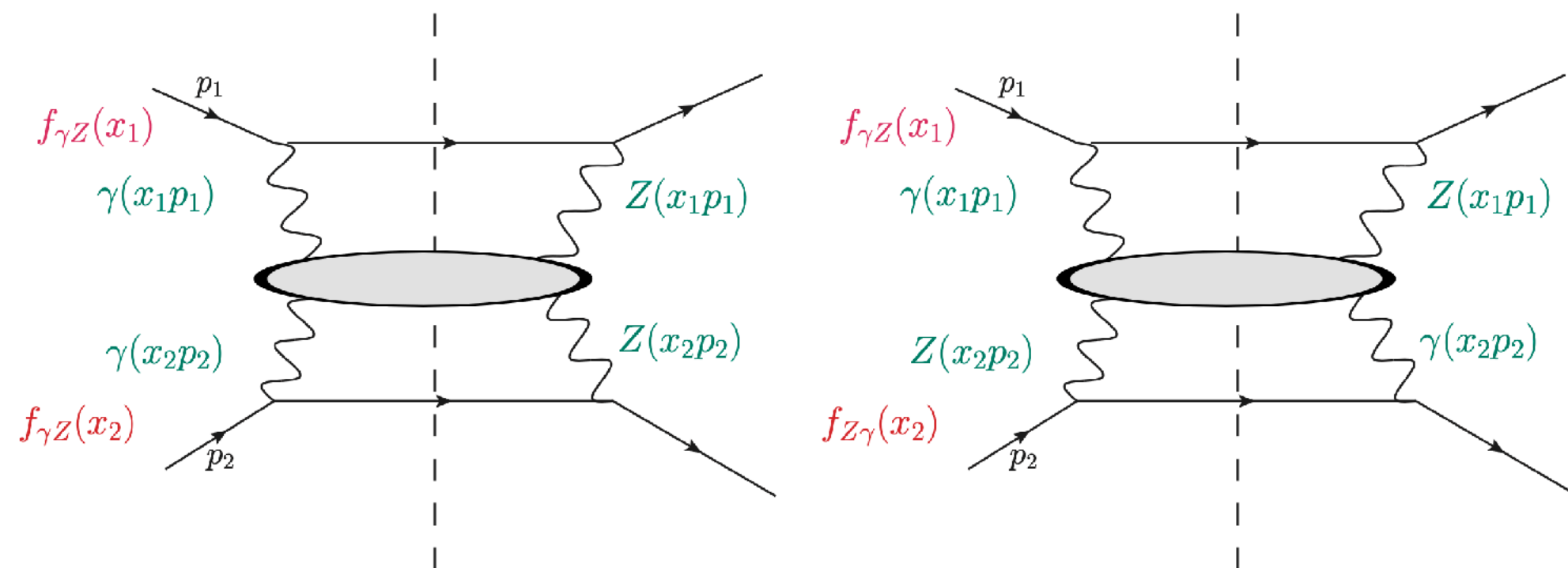


$$\begin{array}{c}
 \gamma \quad Z \quad \gamma/Z \\
 \begin{array}{l}
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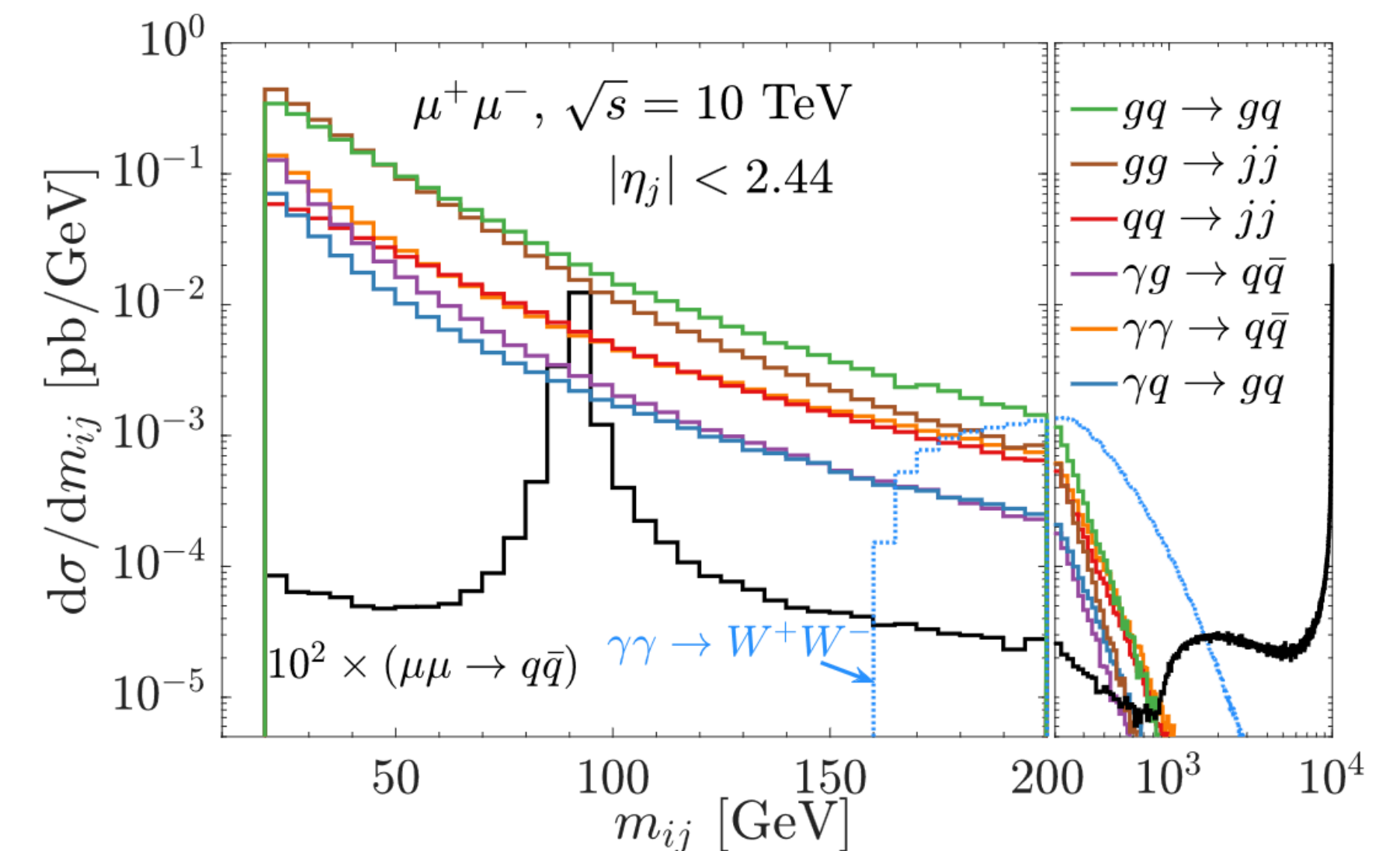
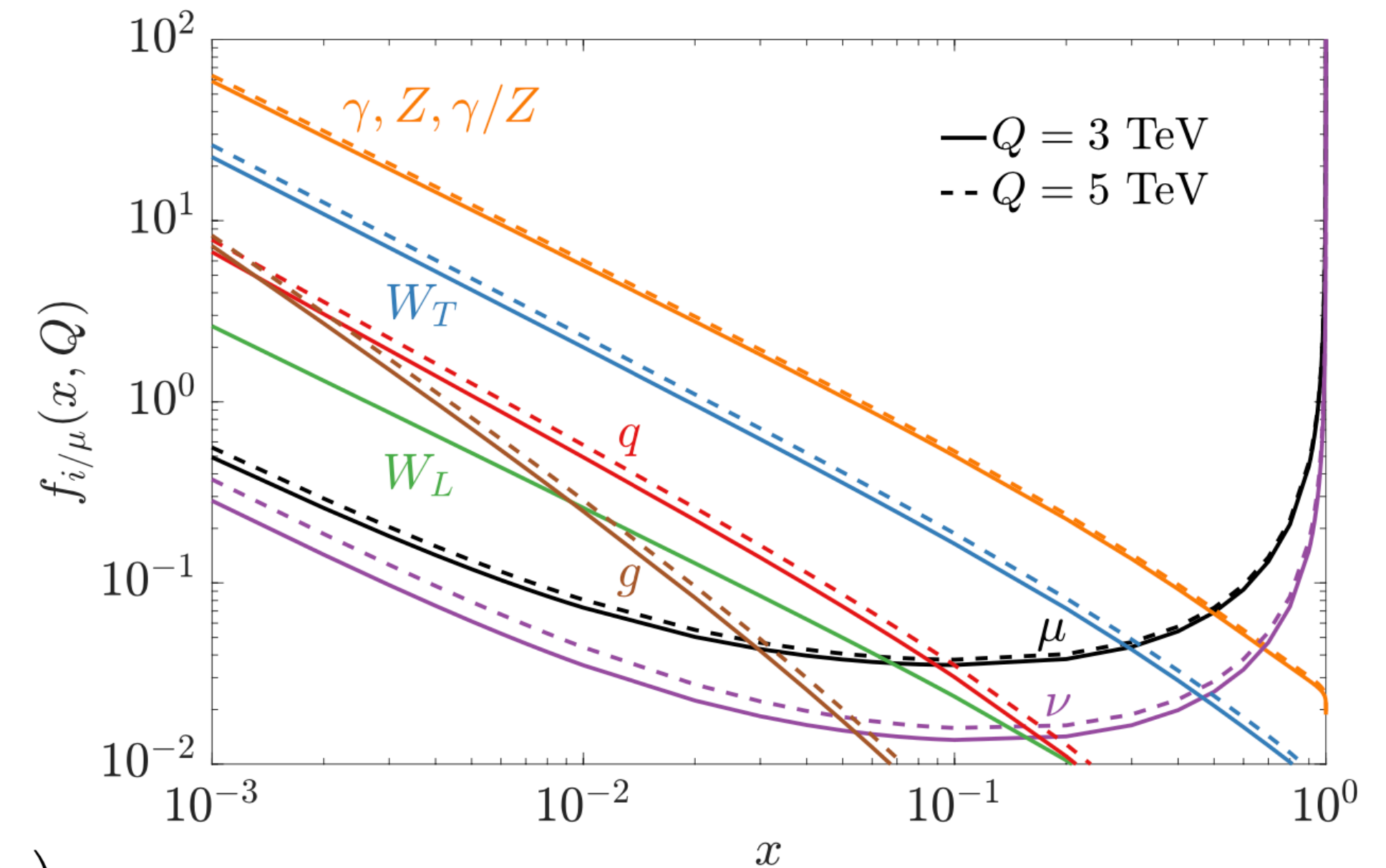


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