

FDIRC optics with Mathematica

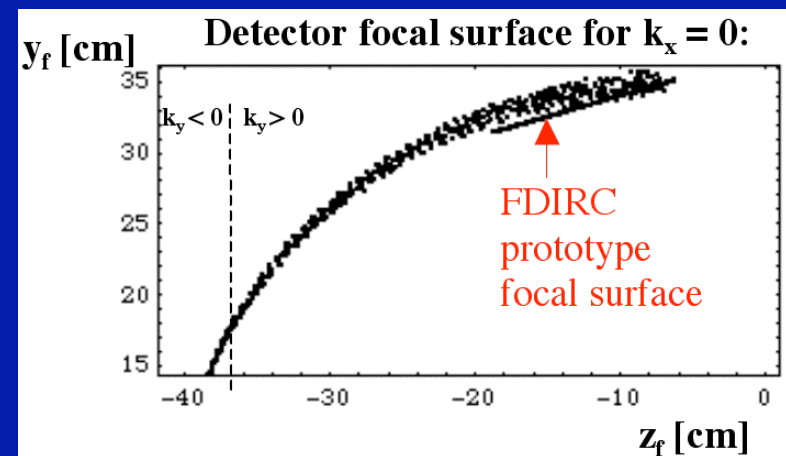
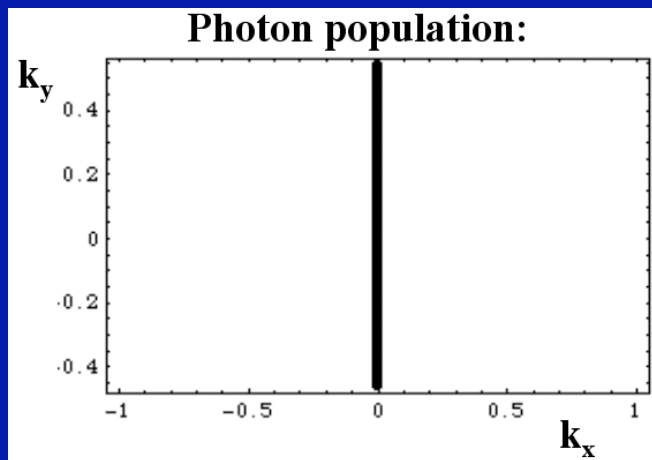
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Content

- The ray-tracing simulation with the Mathematica is employing a geometry similar to the FDIRC prototype, which was originally designed with the Vellum drafting program by a manual ray-tracing.
- Ray-tracing done in Mathematica in 3D (without Optica).
- FDIRC prototype - with spherical mirror, no wedge.
- FDIRC with a wedge and cylindrical mirror.
- Non-focusing DIRC with & without a wedge.

What is a detector surface with a spherical mirror & no wedge ?

```
zbarstart = - barl; zbarend = 0;
Theta = (60 + Random[]*2*30 - 40)/(180/Pi); Phi = 90/(180/Pi);
Thetac = 47.3/(180/Pi); Phic = 180/(180/Pi); Vary Phic
xm0 = 0; ym0 = 23.0; zm0 = -86.6; r = 2*(48.6); Choose r as one has in the FDIRC prototype Vellum study
a11 = 1; a22 = 1; a33 = 1; a12 = 0; a13 = 0; a23 = 0.0; a14 = - xm0; a24 = -ym0; a34 = - zm0; a44 = xm0*xm0 + ym0*ym0 + zm0*zm0 - r*r;
```



- In the region, where the FDIRC prototype works ($z \sim -6$ cm), the calculated focal plane is close to a straight line. So a flat window solution for the FDIRC prototype was OK.

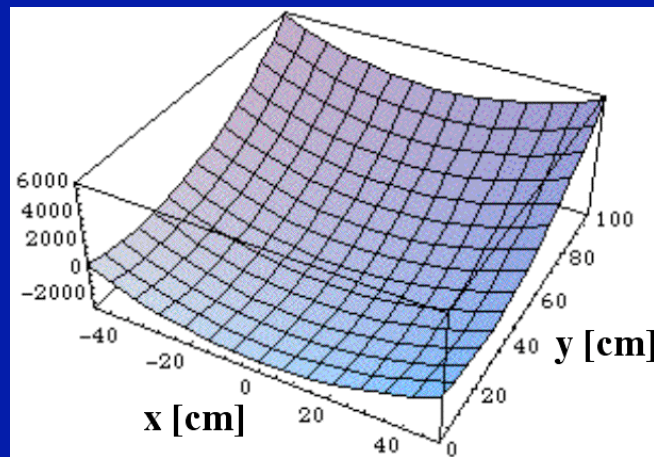
FDIRC prototype: no wedge, spherical mirror, flat detector plane, $\theta_{\text{dip}} = 90^\circ$

Mirror equation: $(x - x_{m0})^2 + (y - y_{m0})^2 + (z - z_{m0})^2 - r^2 = 0$

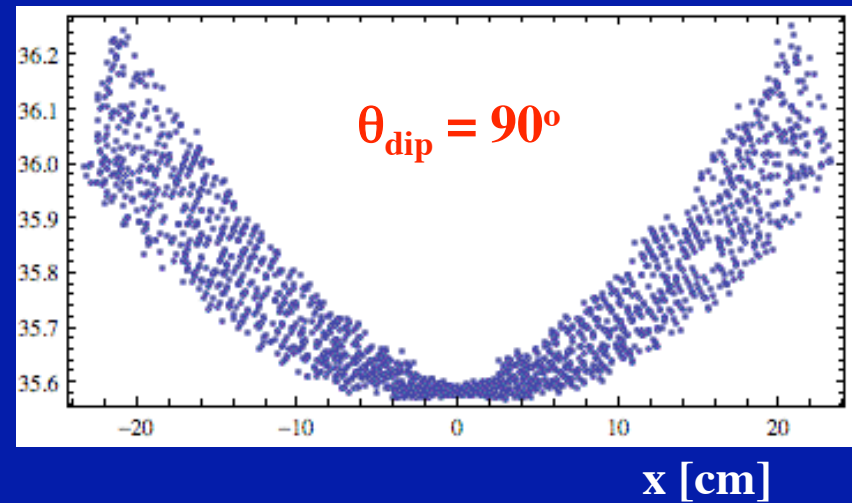
$a_{11}x^2 + a_{22}y^2 + a_{33}z^2 + 2a_{12}xy + 2a_{13}xz + 2a_{23}yz + 2a_{14}x + 2a_{24}y + 2a_{34}z + a_{44} = 0$

$x_{m0} = 0; y_{m0} = 23.0; z_{m0} = -86.6; r = 2*(49.5); \leftarrow$ CRID mirror parameters

$a_{11} = 1; a_{22} = 1; a_{33} = 1; a_{12} = 0; a_{13} = 0; a_{23} = 0.0; a_{14} = -x_{m0}; a_{24} = -y_{m0}; a_{34} = -z_{m0}; a_{44} = x_{m0}^2 + y_{m0}^2 + z_{m0}^2 - r^2;$



y [cm]

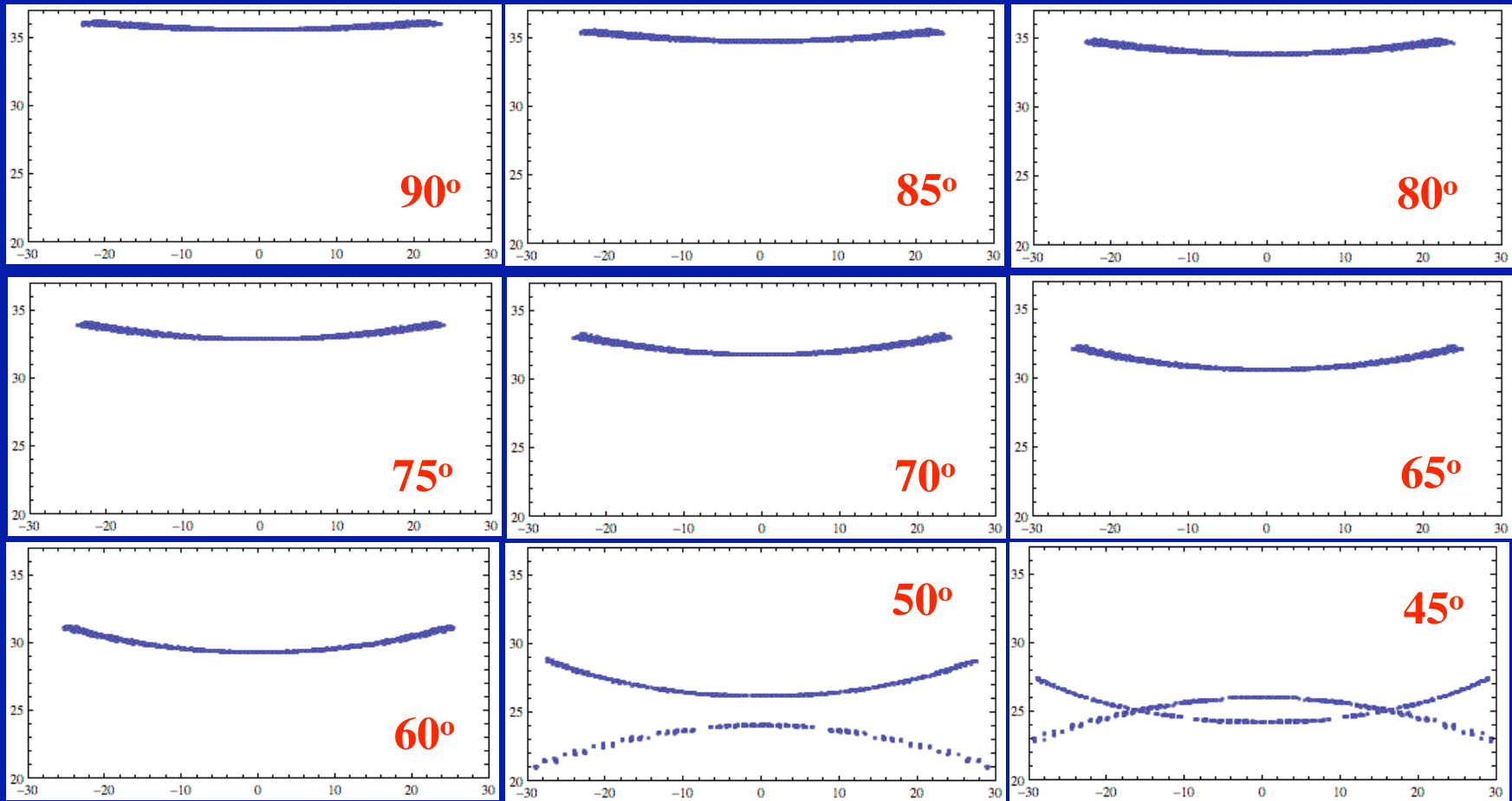


- Detector plane in the bar coordinate system
- Because of the quartz rectangular block at the end of bar, we have only one Cherenkov image for this dip angle.
- Kaleidoscopic wiggles in image come from the bar rectangular structure.

FDIRC prototype: no wedge, spherical mirror, flat detector plane, vary θ_{dip}

y [cm]

A flat detector plane located in the mirror's focus:

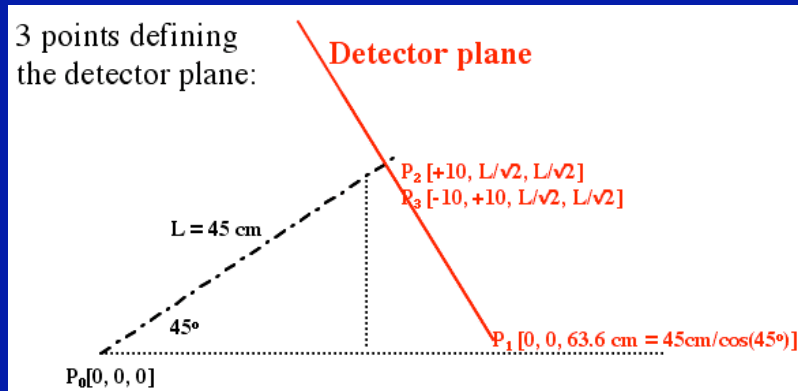


- Keep a “detector image canvas” size constant for all pictures (no auto-scaling)

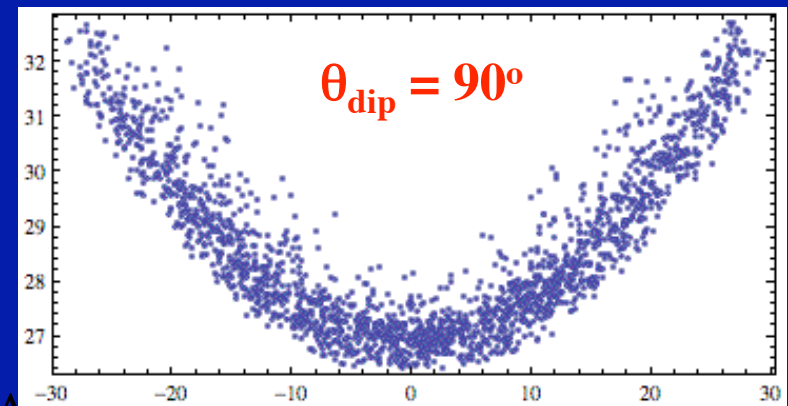
x [cm]

Non-focusing DIRC: no wedge, no mirror, flat detector plane

A flat detector plane:



y [cm]



x [cm]

$\Delta y = 3 \text{ cm}$

x [cm]

Image without a mirror:

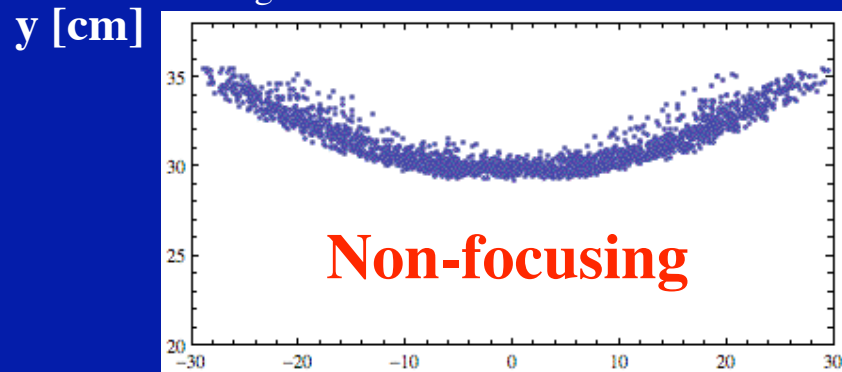
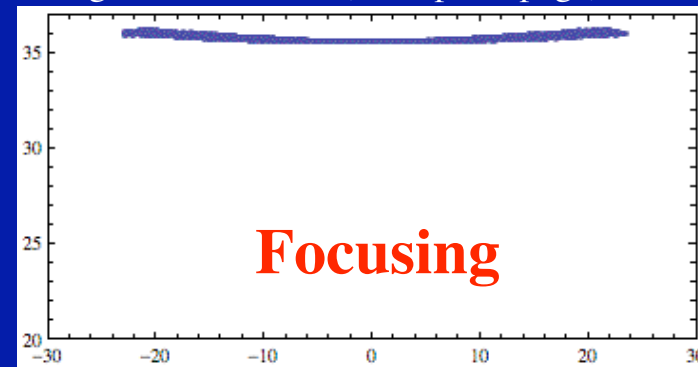


Image with a mirror (from prev. page):

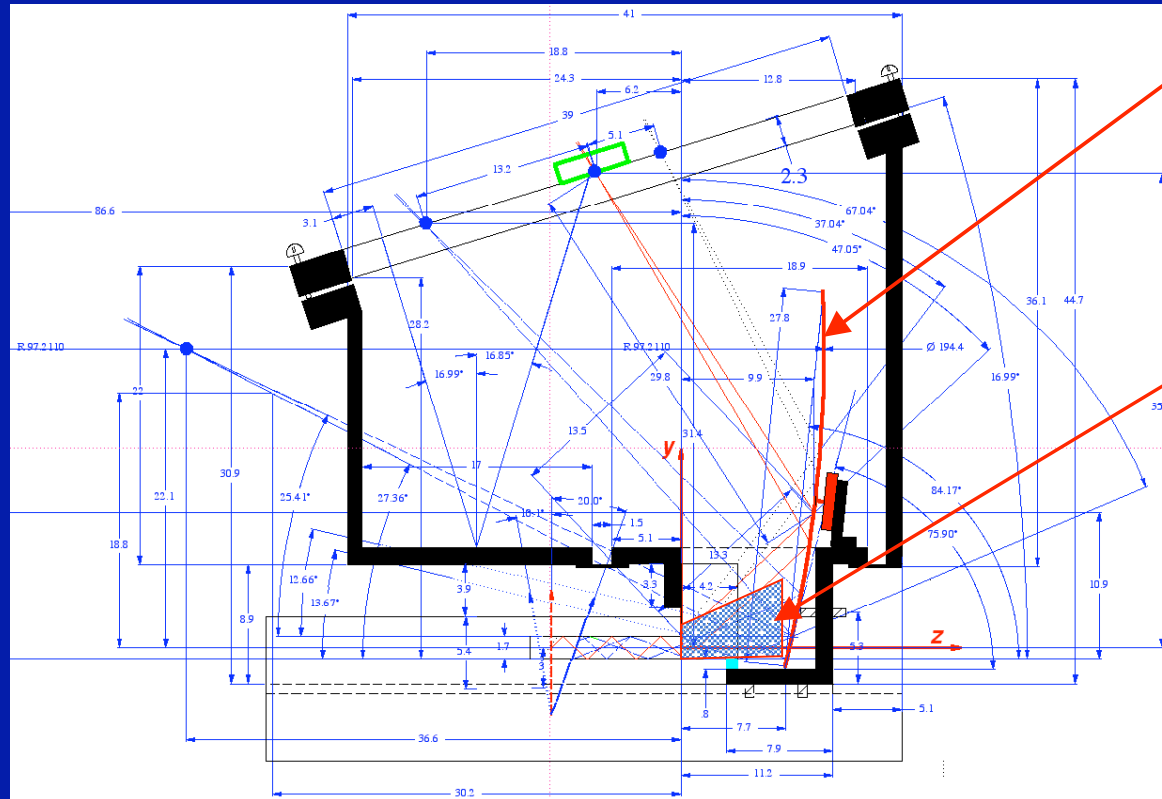


x [cm]

x [cm]

- Focal plane chosen so that 6mmx6mm pixels yield the same resolution as BaBar DIRC
- Image is wider without a mirror.

Add the wedge into FDIRC prototype simulation



Replace the spherical mirror with a cylindrical mirror

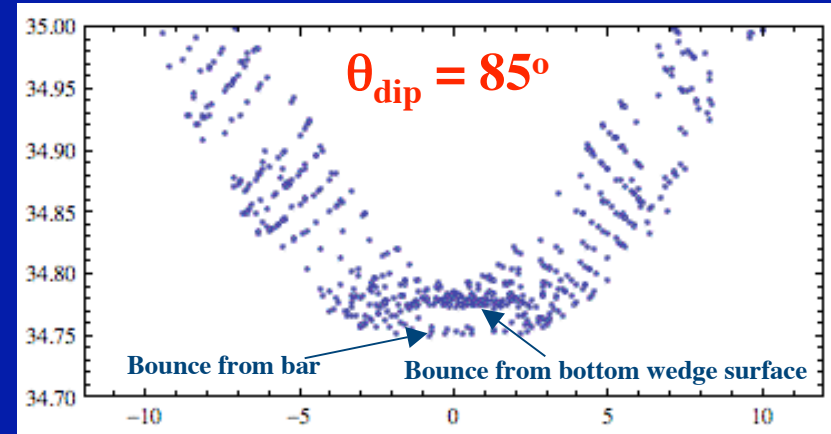
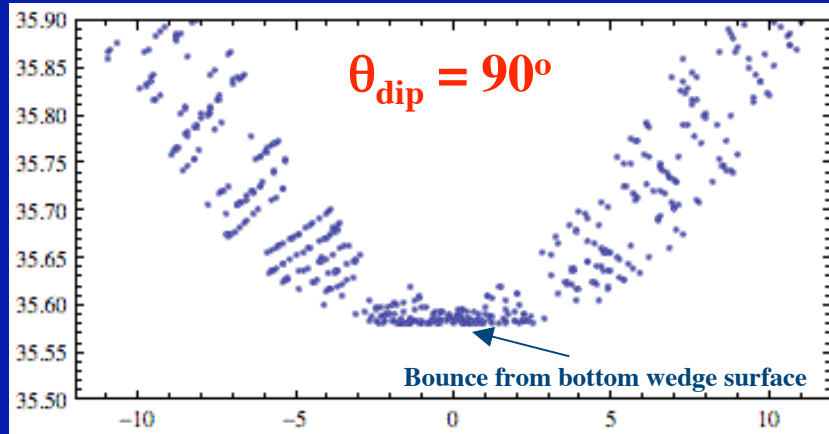
Replace the quartz block with the wedge

- Add the wedge, while keeping other dimensions the same => getting crowded. Intended only for this particular study.
- The reason for adding the wedge: the real DIRC bar boxes have them presently.

FDIRC: with wedge, cylindrical mirror, flat detector plane, $\theta_{\text{dip}} = 90^\circ$ & 85°

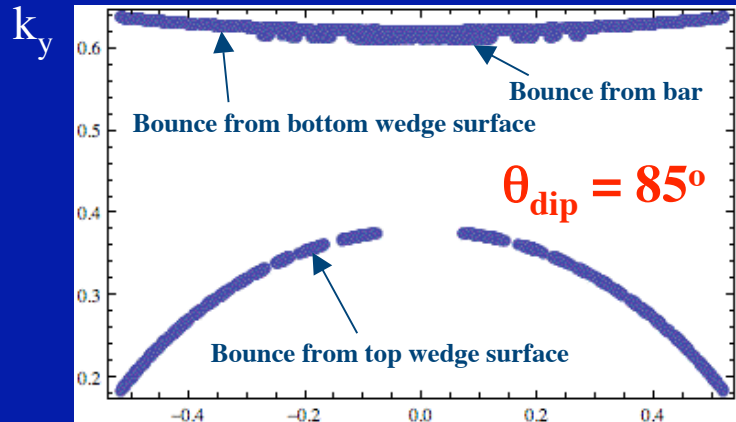
A flat detector plane located in the mirror's focus:

y [cm]

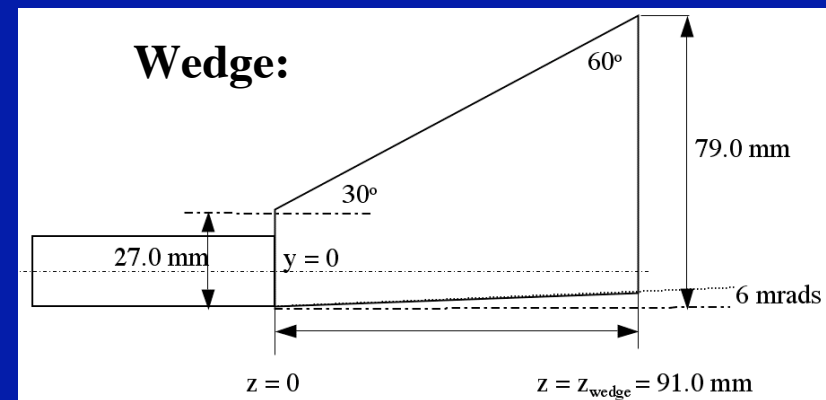


x [cm]

x [cm]

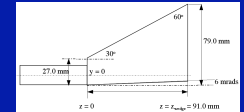


k_x



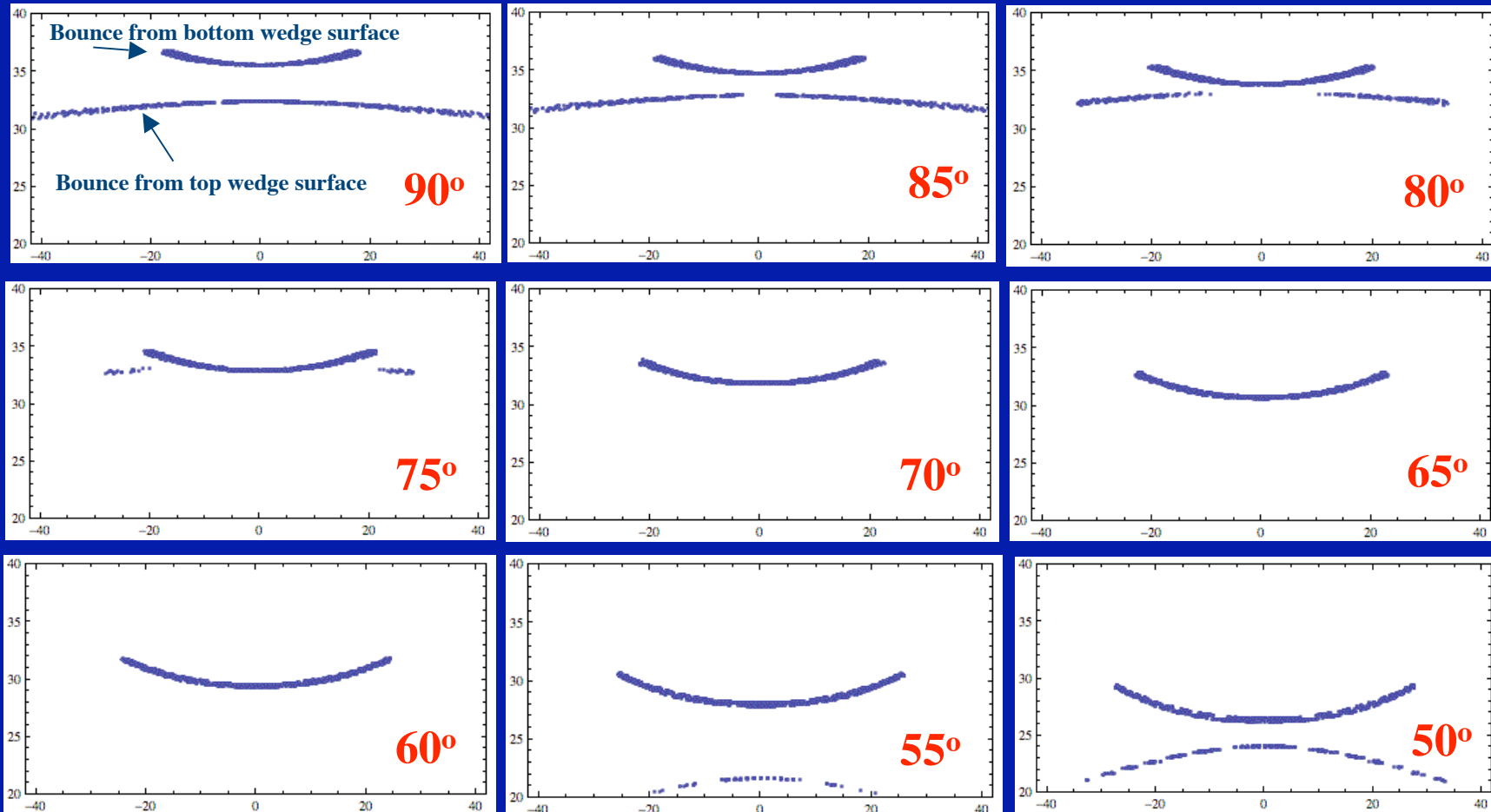
FDIRC: with wedge, cylindrical mirror, flat detector plane, vary θ_{dip}

Wedge:



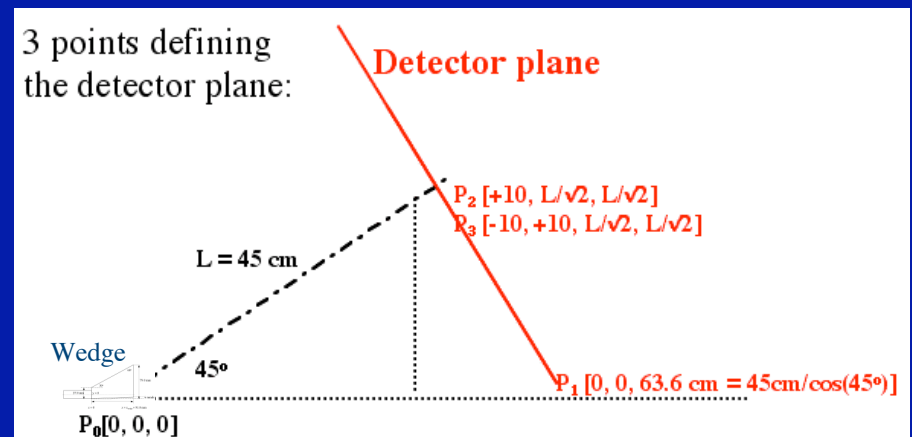
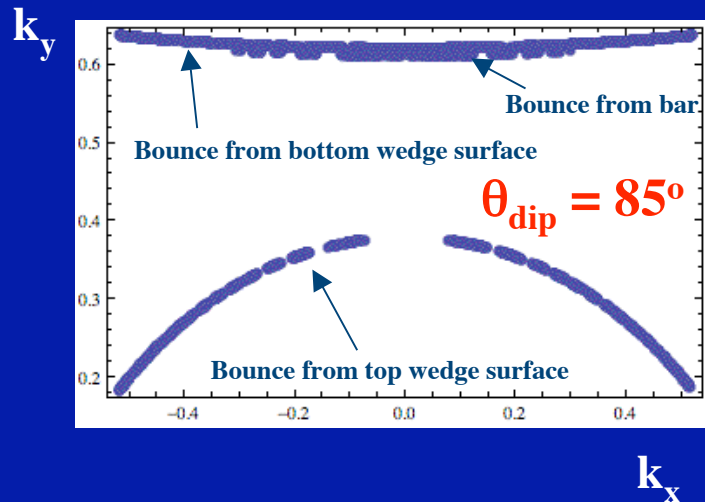
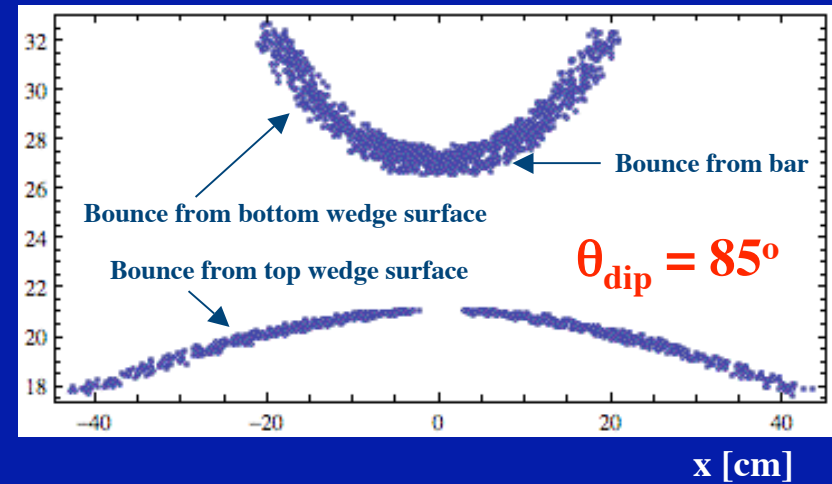
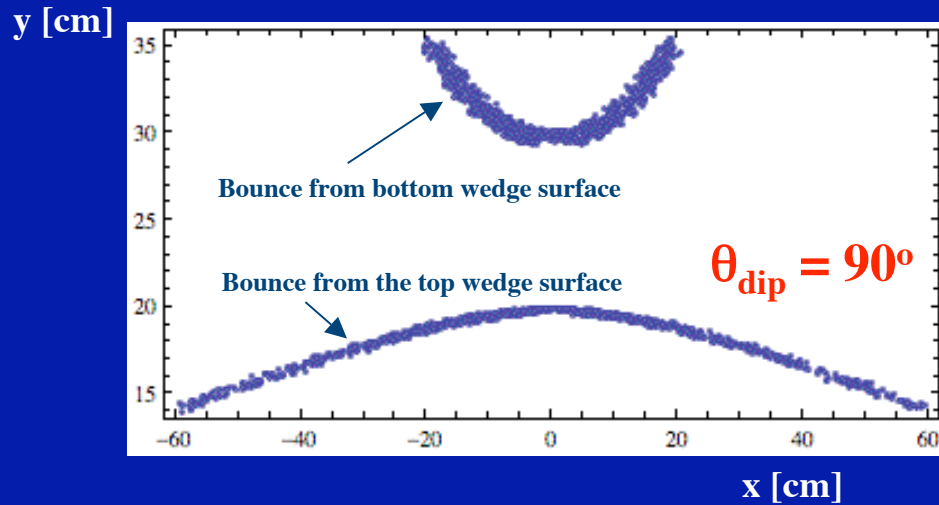
y [cm]

A flat detector plane located in the mirror's focus:



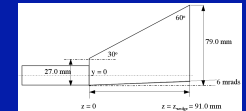
x [cm]

Non-focusing DIRC: with wedge, no mirror, flat detector plane, $\theta_{\text{dip}} = 90^\circ$ & 85°

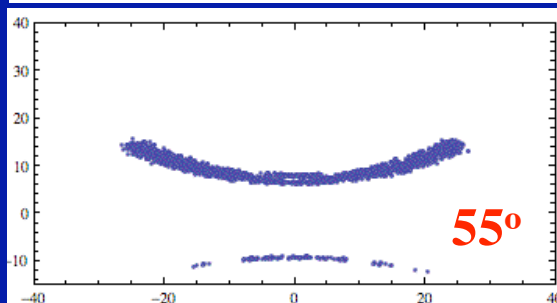
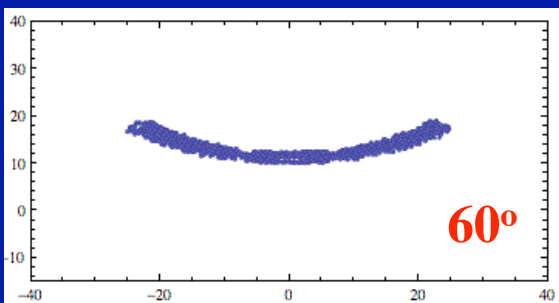
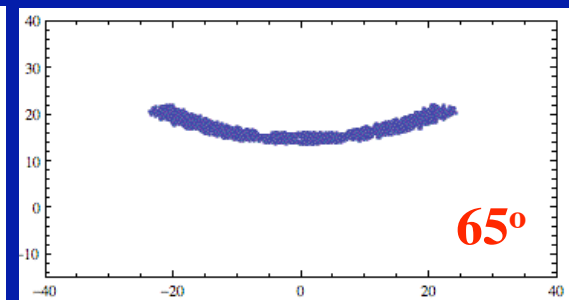
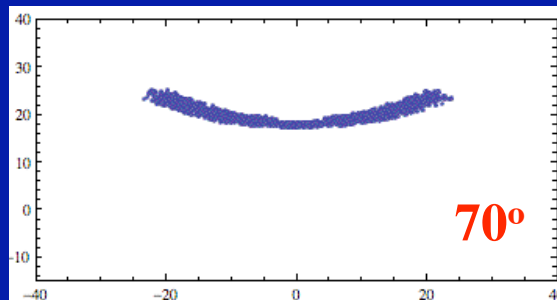
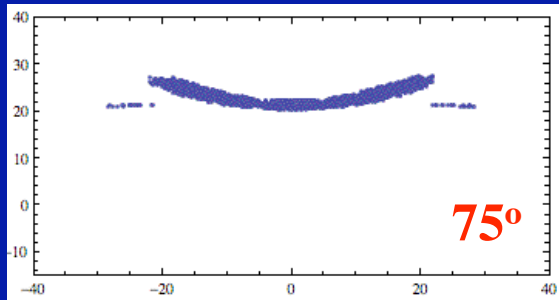
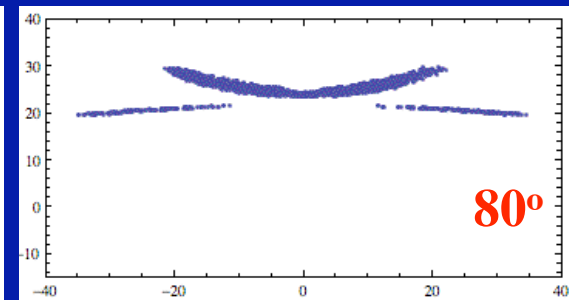
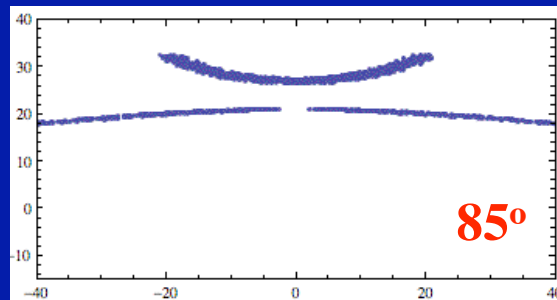
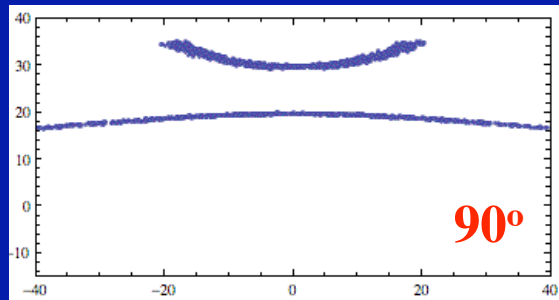


Non-focusing DIRC: with wedge, no mirror, flat detector plane, vary θ_{dip}

Wedge:



y [cm]

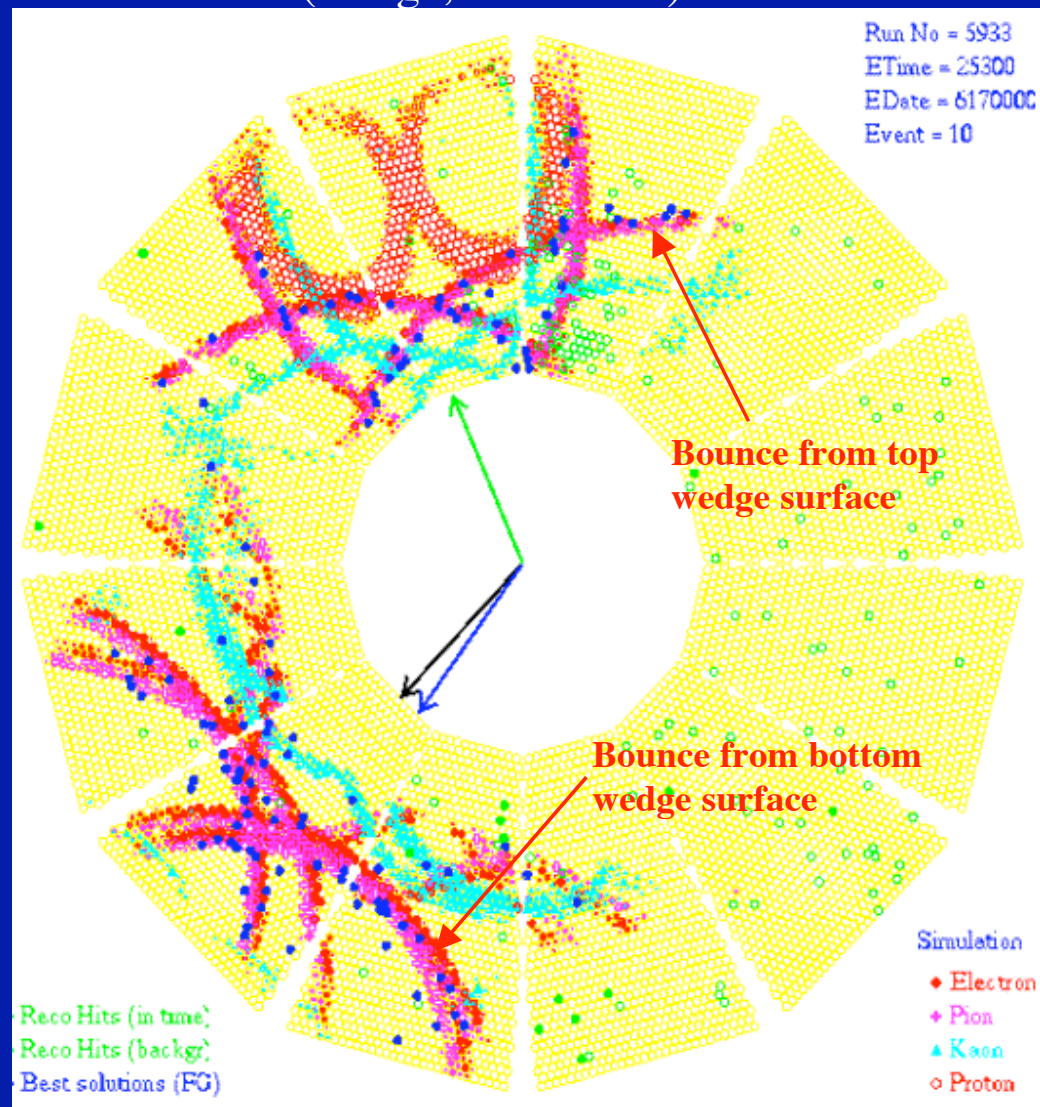


x [cm]

- Non-focusing DIRC with no mirror has a wider image, and a larger overall detector canvas size ($\sim 2x$)
 => need more pixels to cover the area

Images in BaBar DIRC

(wedge, no mirrors)



Conclusion

- We have developed a useful tool to study the optics.
- Cylindrical mirror requires a non-flat detector focal plane in principle, although a flat detector plane may be good enough approximation. One needs to quantify this.
- Non-focusing DIRC requires $\sim 2x$ larger pixel area to cover compared to the FDIRC with a cylindrical mirror.
- The wedge does not seem to be too big obstacle even for the FDIRC.