

# *Quantum field corrections to the cosmological free-streaming*

## *Topics*

- ★ Quantum fields in curved spacetime
- ★ Quantum statistical mechanics
- ★ Robertson Walker Friedman spacetime

Based on:

- ★ D. R. and F. Becattini: *Class. Quant. Grav.* 40 (2023) 17, 175007
- ★ D. R. and F. Becattini: In preparation



daniele.roselli@unifi.it

## Fluid in an expanding universe

RWF metric;  
Perfect fluid;

$$ds^2 = dt^2 - a^2(t)(dx^2 + dy^2 + dz^2)$$

$$T^{\mu\nu} = (\epsilon + p)u^\mu u^\nu - pg^{\mu\nu}$$

energy density

pressure

## Classical free-streaming

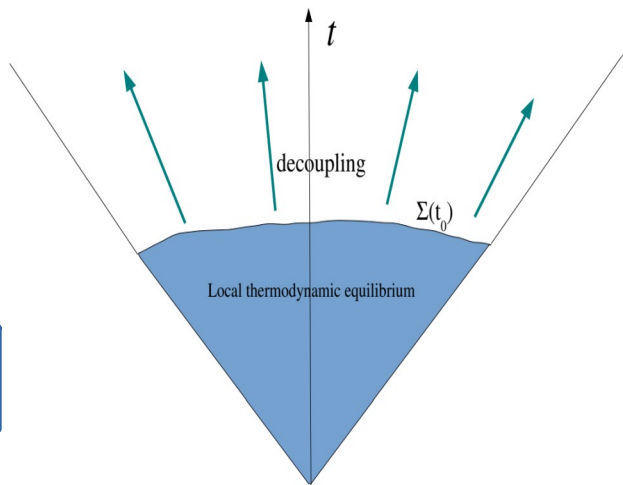
Boltzmann approach

$$\epsilon \propto mN a^{-3}(t)$$

$$p \propto a^{-5}(t)$$

### Equation of state

$$W = \frac{p}{\epsilon}, \quad W \geq 0$$



## Quantum theory

★ State of local thermodynamic equilibrium

LTE density operator

$$\hat{\rho} = Z^{-1} \exp[-\hat{H}(t_0)/T(t_0)]$$

$$\langle \hat{T}_{\mu\nu} \rangle = \text{Tr}[\hat{\rho} \hat{T}_{\mu\nu}] - \langle 0 | \hat{T}_{\mu\nu} | 0 \rangle$$

depends on  $a(t)$  and its derivatives

★ Matter as a quantum field

$$\hat{\phi} = \int d^3k (\hat{a}_k v_k e^{i\omega_k t} + c.c.), \quad v''_k + \Omega_k^2 v_k = 0$$

Free equation

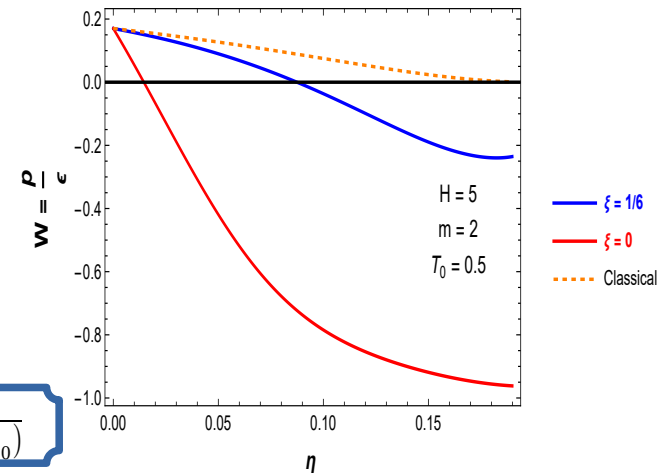
Quantum effects

- Energy density is enhanced
- Pressure can become negative

### Caveat

$$H \gg m, \quad H(t_0) \gg \sqrt{mT(t_0)}$$

De Sitter Universe

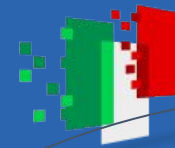




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# Mauro Giliberti

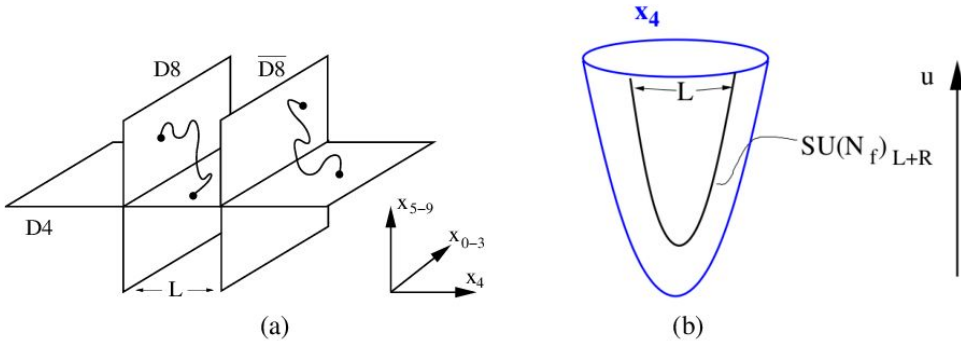
PhD student at  
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New Frontiers in  
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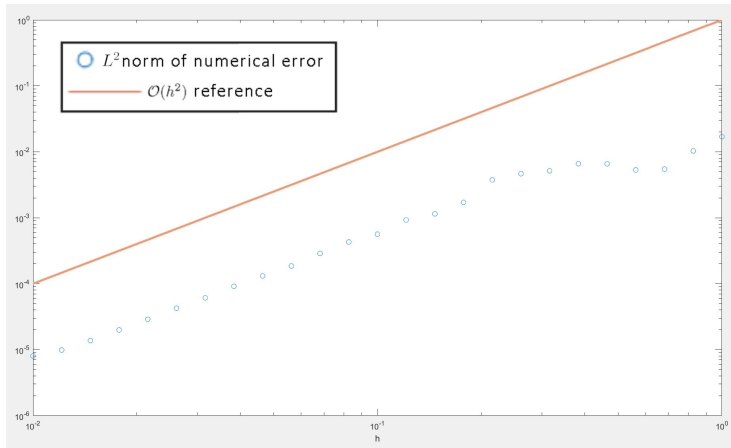
## Numerical Study of Bubble Dynamics in Holographic Vacuum Decay

## Cosmological phase transition: chiral bubble nucleation with MATLAB

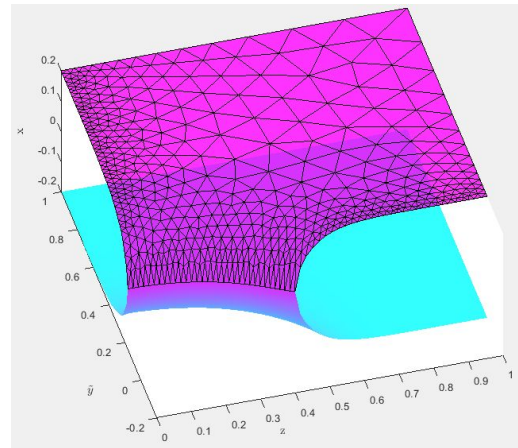
Holographic theory of branes: Witten-Sakai-Sugimoto model



Tests of numerical methods



Bubble transition profile

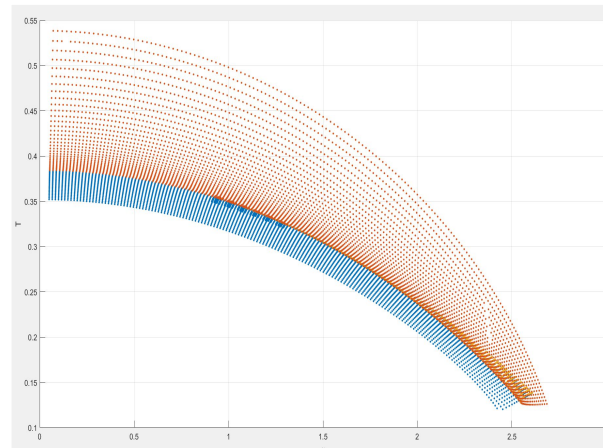


## Astrophysical phase transition: finite-density bubble evolution with Julia

Holographic theory of metric-scalar-gauge

$$\mathcal{L} = \frac{1}{2\kappa^2} \left[ R - \frac{f(\phi)}{4} F_{\mu\nu}^2 - \frac{1}{2} (\partial\phi)^2 - V(\phi) \right]$$

Finite-density phase diagram



Bubble evolution dynamics

