



# **QCD in Extreme Conditions**

**Use case for the WP1  
of the CN-HPC of the PNRR**

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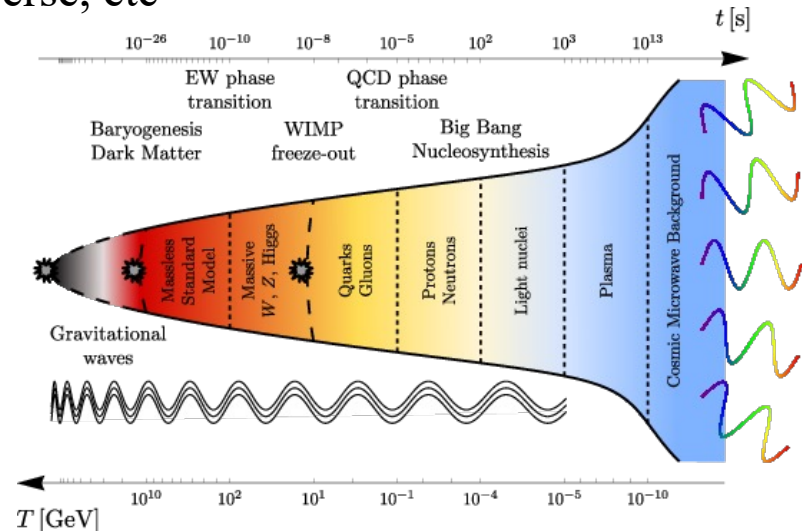
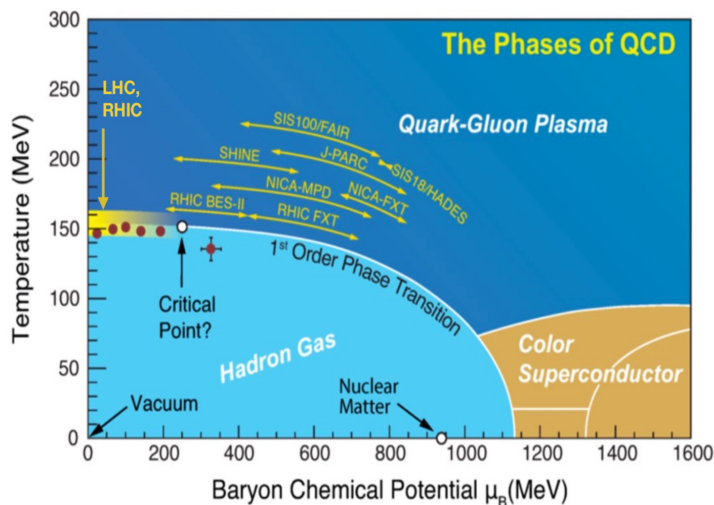
# Context

- Forces in Nature: Strong, Weak, Electro-magnetic and Gravitational

strong but short range:  
scale of particle physics

weak but long range:  
macroscopic scale

- Strong Interactions: responsible of the formation of protons and neutrons, and of their binding to form atomic nuclei (almost 100% of the mass of our body and of what we see)
- Strong Interactions play a crucial role also in nuclear physics and in astrophysics: Quark-Gluon plasma, neutron stars, early Universe, etc



- Extreme Conditions: high temperature, finite density, background fields, etc

# Context

- Thanks to experimental results at particle colliders and to their interpretation and understanding by theorists we have a fundamental quantum theory of Strong Interactions

## Quantum ChromoDynamics (QCD)

### Matter fields

Quark and AntiQuarks:

Up, Down, Strange,  
Charm, Bottom, Top



### Gauge fields

Gluons:

carrier of the interaction  
“glue” that binds quarks

$$\sigma \simeq (0.4\text{Gev})^2 \simeq 10^5\text{N}$$

$$\sigma = M g \quad M \sim 100 \text{ people}$$

As strong as a cm-thick steel cable but 13  
orders of magnitude thinner



The Yang-Mills cableway

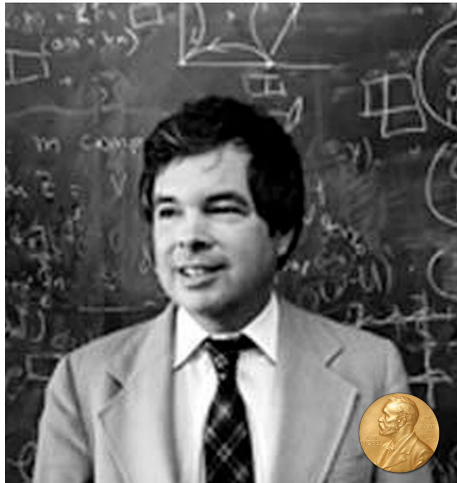
QCD sets the rules but to extract theoretical  
predictions we need to play all the games

BUT

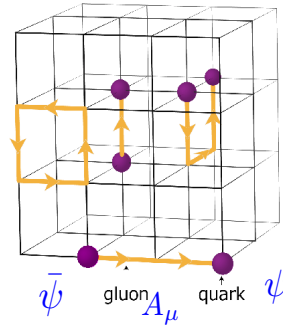
it is not possible to do it analitically



# Lattice Field Theory and HPC

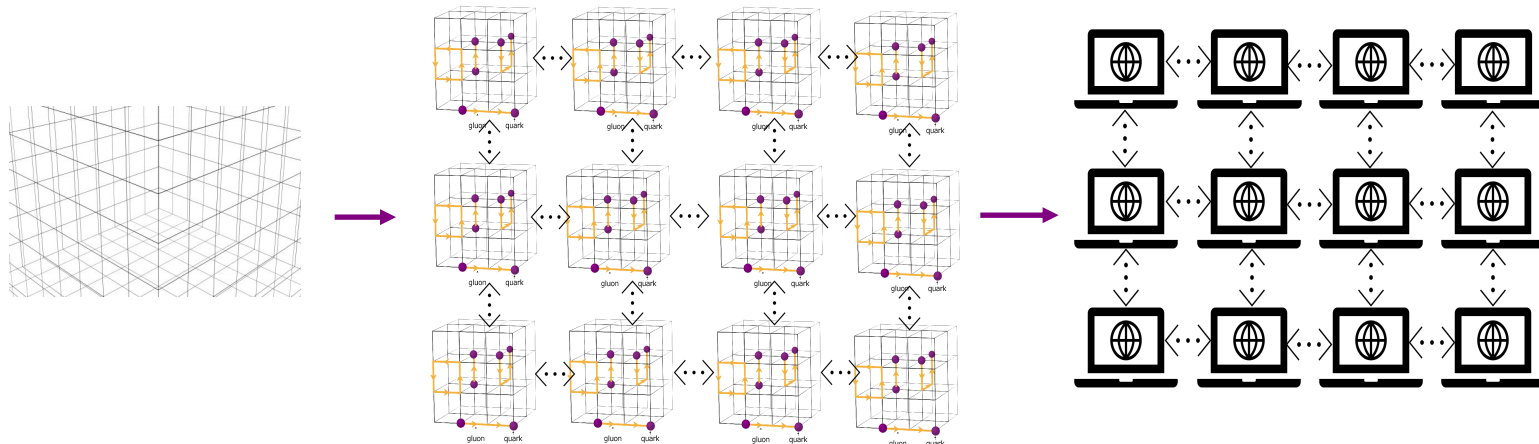


1974: K. Wilson proposes to define QCD on a space-time lattice



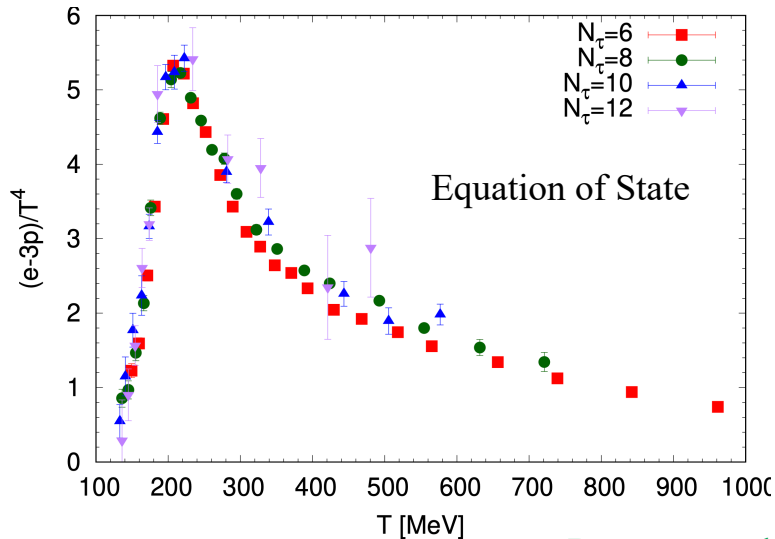
! The theory is formulated in terms of a **discrete** number of variables (=complex numbers);

- Lattice QCD is the only currently known formulation allowing to study QCD non-perturbatively from first principles; the theory can be put on a computer and solved numerically;
- A very demanding computational challenge: order  $10^{10}$  variables

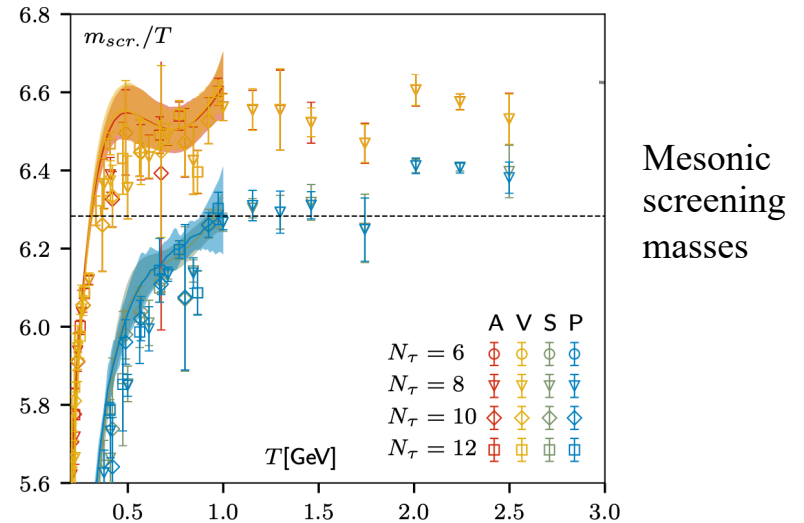


# QCD in Extreme Conditions

- The steady increase of computing power is essential but in many cases is not enough: it is necessary to develop new algorithms and computational methods
- The study of QCD in Extreme Conditions, namely, high temperature, finite density, with external background fields is numerically demanding
- The study of QCD at finite temperature  $T$  is challenging,  $T_{\max} \sim 1$  GeV: two very different energy scales (=length scales),  $T$  and  $T=0$ , have to be simulated at the same time (!)



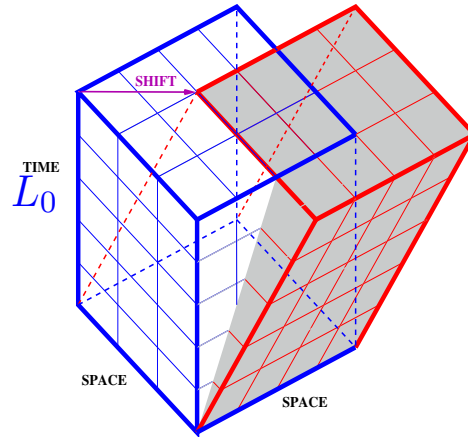
Bazavov et al. (2021)



Bazavov et al. (2019)

# QCD at high temperature

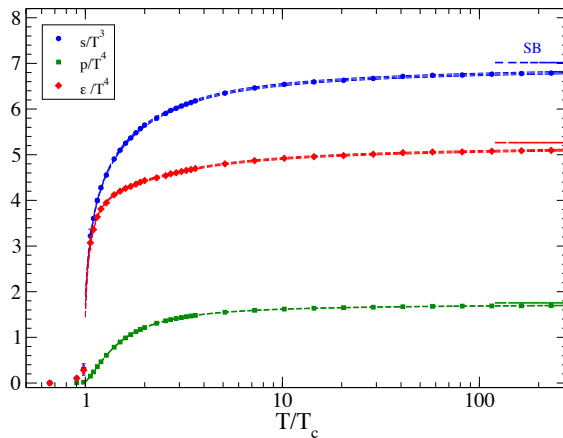
- solution: formulation of QCD in a moving reference frame



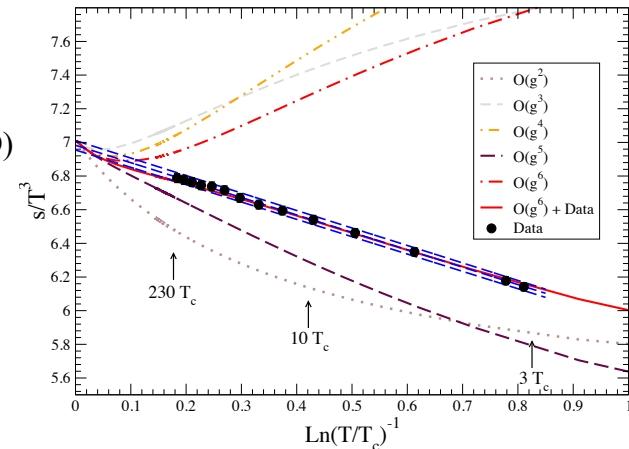
Shifted boundary conditions

$$\phi(\vec{x}, L_0) = \phi(\vec{x} + \vec{\xi}, 0)$$

One measures the thermodynamics quantities **only at the temperature T of interest**



Yang-Mills SU(3)  
(pure gauge sector of QCD)



- Both the theoretical formulation and its computational implementation turn out to be very effective and efficient
- We would like to apply the same technique to QCD

# QCD in Extreme Conditions: Use case

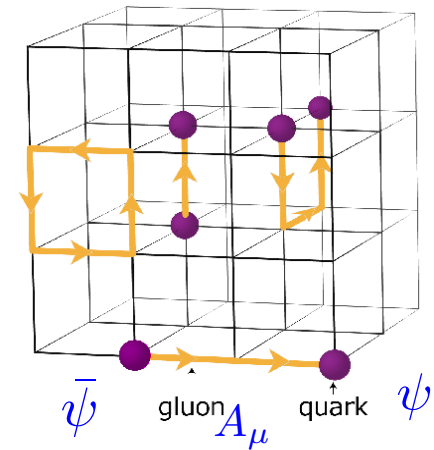
- The main target of this use case is to deploy a parallel code to perform efficient Monte Carlo simulations of QCD in the completely unexplored regime of the very high temperatures
- Definition of the theoretical and algorithmic strategies to compute the entropy density (primary observable) in a moving reference frame
- Development of an efficient **parallel MPI Monte Carlo code** to study **lattice QCD at finite temperature** with shifted boundary conditions with the aim of reaching  $T \sim 100$  GeV.
- The parallel code has to have a good strong scaling in order to run efficiently jobs requiring up to about **5000 -10000 cores**.
- The code will simulate quarks using the  $O(a)$ -improved Wilson formulation; it will be a development of the open source OpenQCD code.
- The use case has also two additional activities:
  - 1) preparation of parallel codes to investigate QCD at finite density and in external background fields with Monte Carlo simulations on the lattice.
  - 2) development of a code to study the spin polarization in the QCD plasma



## An example of target simulation

- Monte Carlo simulation of Lattice QCD: generation of many gauge field configurations; numerically it corresponds to solving many times the Dirac equation

$$\eta = D\chi \quad D: \text{large and sparse } (5 \times 10^9 \text{ by } 5 \times 10^9)$$



- Global system size:  $288^3 \times 16 = 3.8 \times 10^8$  sites
- MPI grid:  $18 \times 18 \times 18$  cores = 5832 cores.      Local lattice  $V=16^4 = 6.5 \times 10^4$  sites
- For each site  $D$  requires to compute several matrix-vector multiplication  $U \cdot v$   
 $U$  is  $3 \times 3$  and  $v$   $3 \times 1$ ; we need 8  $U$  and 36  $v$  giving  $(8 \times 18 + 36 \times 6) \times 8 = 2880$  bytes.  
 Load 2880 bytes and store  $4 \times 6 \times 8 = 192$  bytes, i.e. memory transfer  **$B=3072$  bytes per site** (improved with smart coding)

- The computation consists in multiply&add operations amounting to  **$F=1400$  Flop per site** → For  **$I=B/F=2.2$  bytes/Flop**  
Memory bandwidth limited

- For a Skylake node we have  **$I=256$  Gb/s /  $3.2$  TFlop/s =  $0.08$  bytes/Flop**
- Each core has to pass data continuously to n.n. cores: this is an addition bottleneck w.r.t. the purely computational effort and requires a fast (100-200 GB/s) **infiniband network**



# Computational resources required

- Need to access a small-medium cluster for code development (start&stop) with an infiniband network: CNAF. 3 Mch
- Need to access a larger HPC system for advanced tests and for benchmarking on system of realistic size: Cineca. 20 Mch

## Exchanges with WP5 activity

- Creation of a repository of gauge configurations once the production phase will be entered

## People involved

- INFN – Milano Bicocca

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- INFN – Bari

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