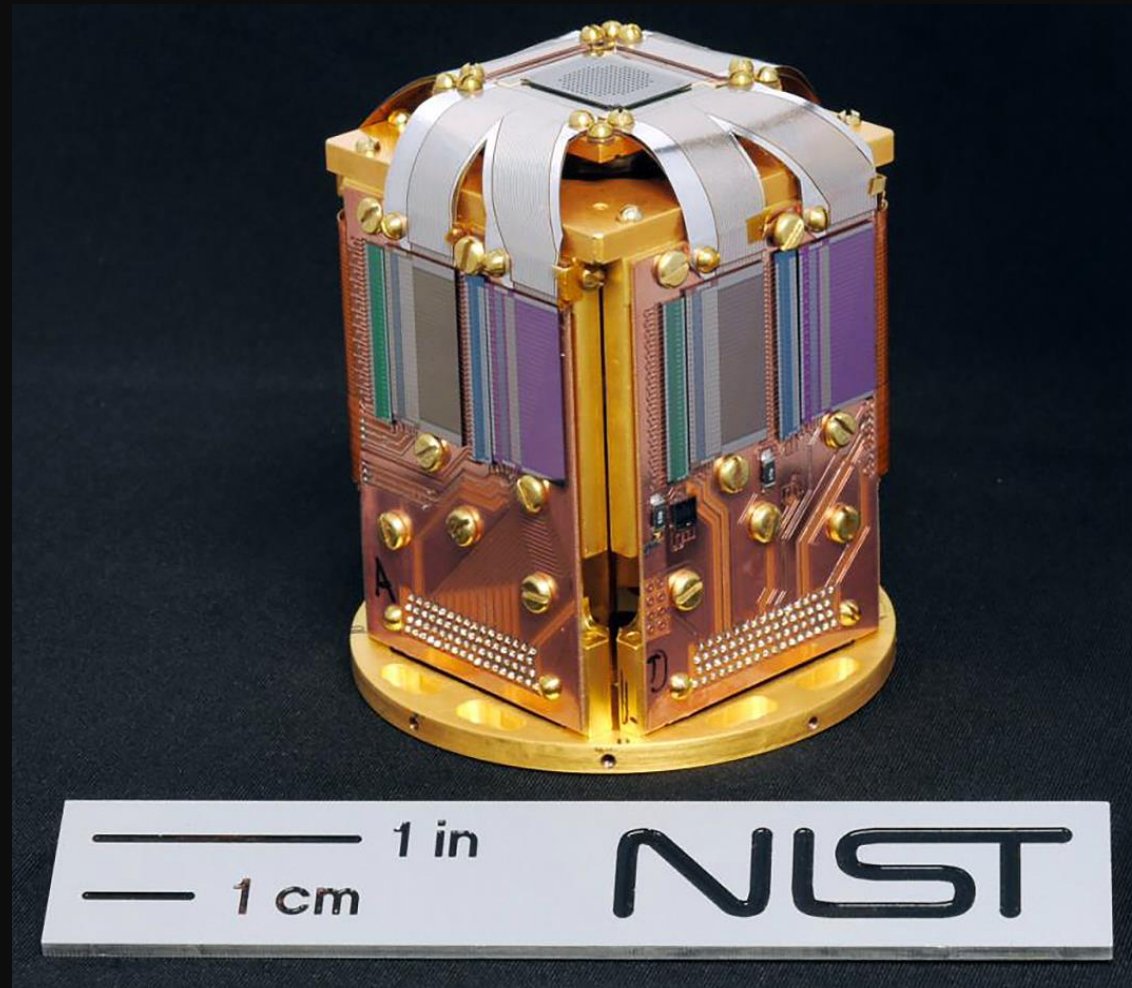
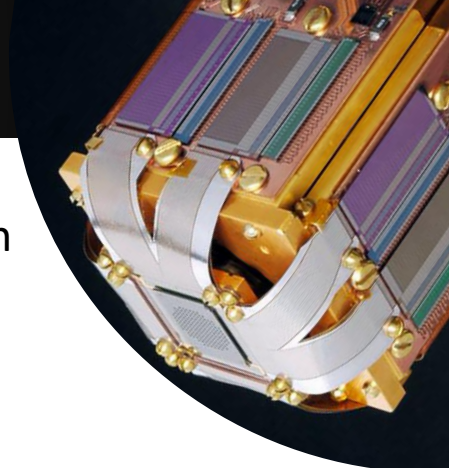


MEASURING THE TEMPERATURE OF X-RAYS

WITH SUPERCONDUCTING DETECTORS

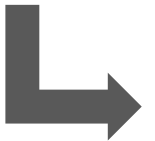


Low temperature detector working principle

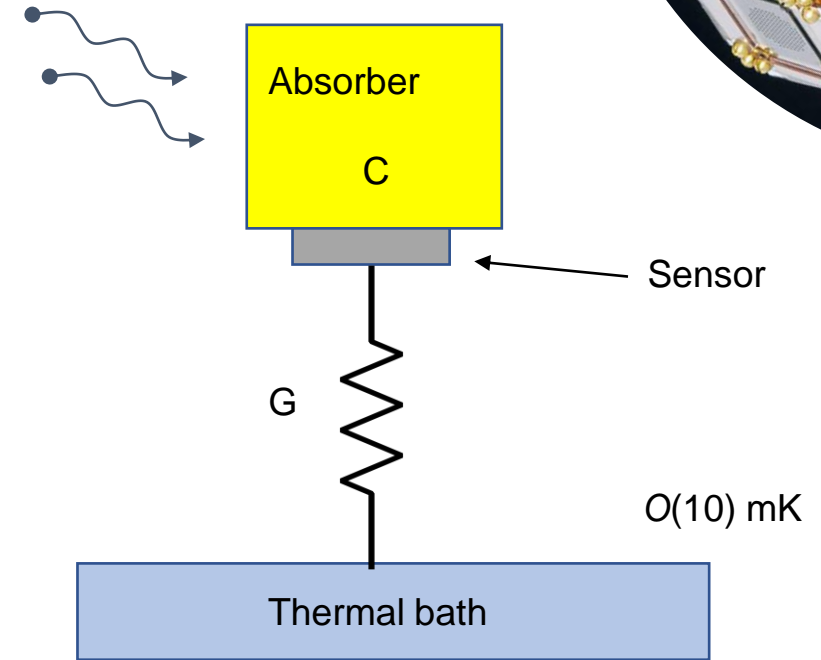
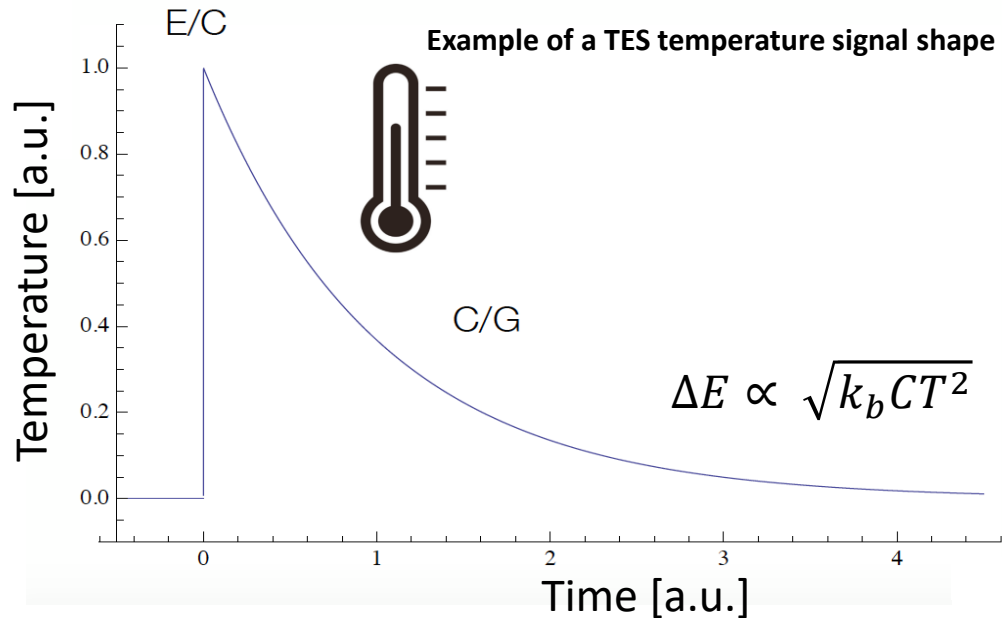


■ Low Temperature Detectors (**LTDs**) are **very sensitive thermometer** able to detect a temperature variation of the order of a fraction of mK

■ The idea is to measure, with a temperature sensor, the energy deposited inside the detector after it has been converted into heat



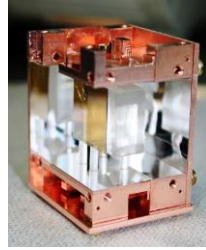
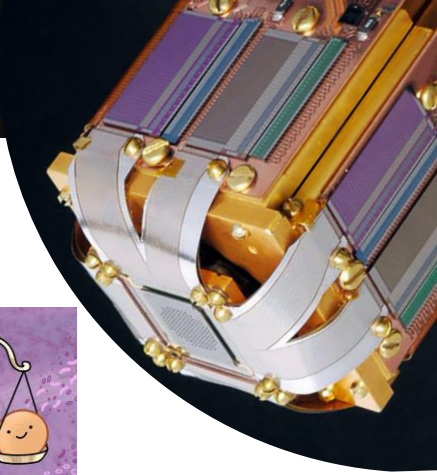
- Perfect calorimeters (in principle)
- Phonon detectors!
- Extremely small signals



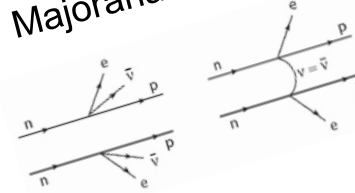
A few definitions:

- **Calorimeter:** it measures the energy
- **Bolometer:** it measures the power.
- **Macrocalorimeter:** mass $O(100)$ g, size $O(1)$ cm
- **Microcalorimeter:** mass $< O(1)$ mg, size $< O(100)$ μ m

LTD application



Majorana neutrino



Neutrino mass

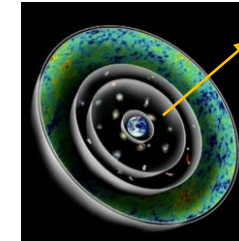
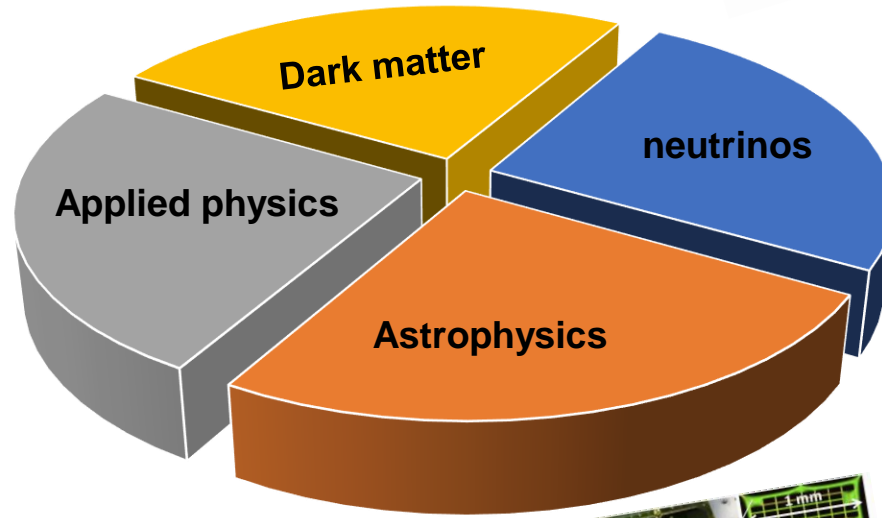


EDS spectroscopy

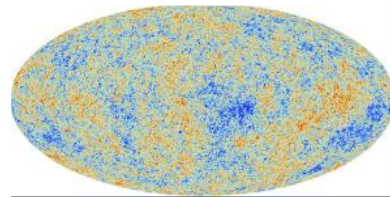
Beamline spectroscopy



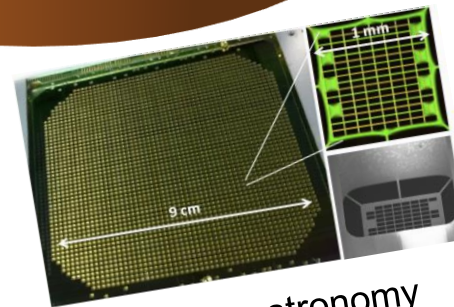
...



CNB



CMB

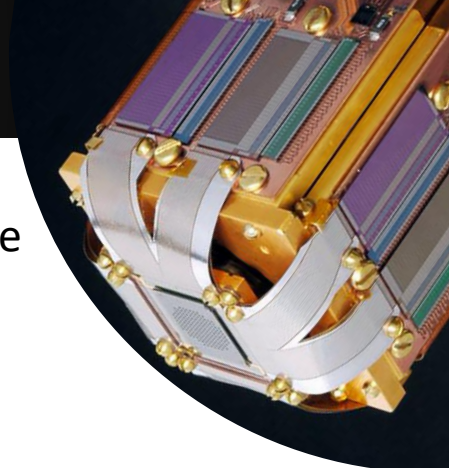


IR, X,... astronomy



Gravitational waves

Transition Edge Sensors (TES) for X-ray detection



- A Transition edge sensor is a superconductor film operated in the narrow temperature region between the resistive and the superconducting state



The resistance is strongly dependent on temperature

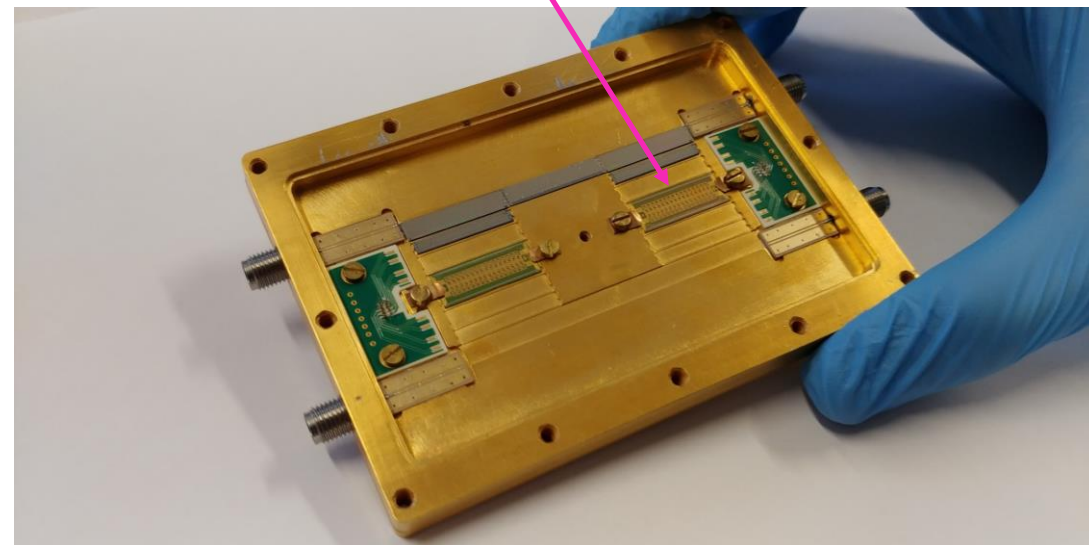
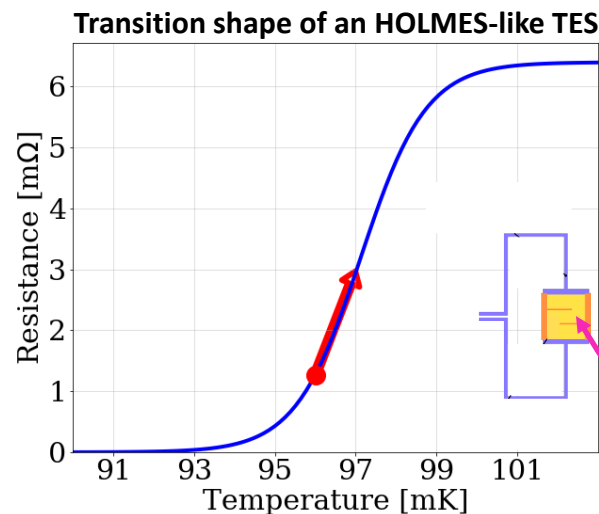
- The TES design can be changed to match different experimental needs

- Typical detector dimension: 10-300 μm
Signal time $O(100-1000) \mu\text{s}$



Practical collecting area and photon counting capability only when built into array of devices

- Competitive with HPGe and solid state and wavelength-dispersive spectrometers



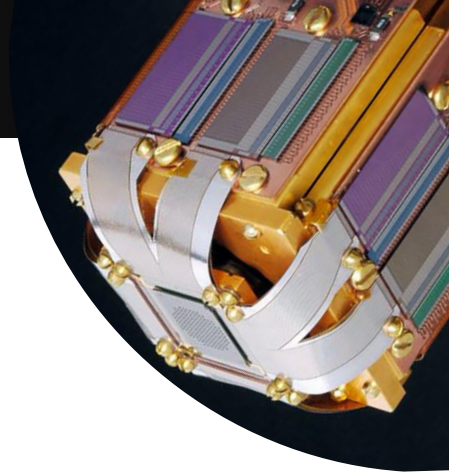
Why use TES

Pros

- Very high energy resolution
- Fully active (no dead layer)
- Low spurious count rate
- Single photon detector
- Wide selection of materials
- Many multiplexing techniques!

Cons

- Slow detectors
- Low temperature $O(100)$ mK
- Non-trivial signal processing
- Multiplexing is mandatory

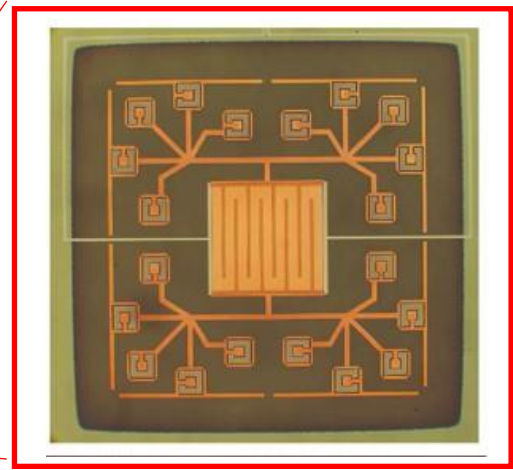
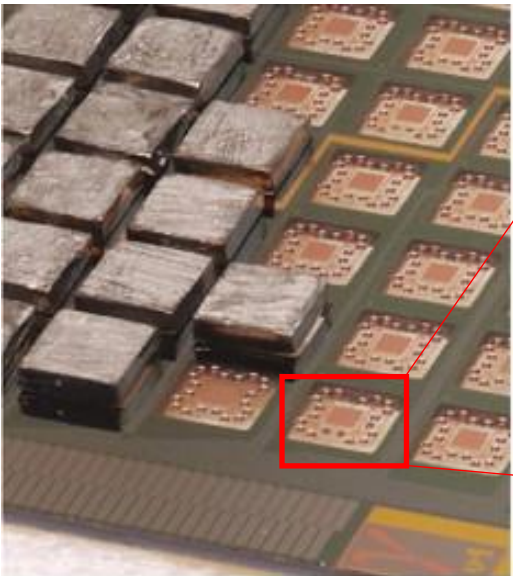


Components of a TES



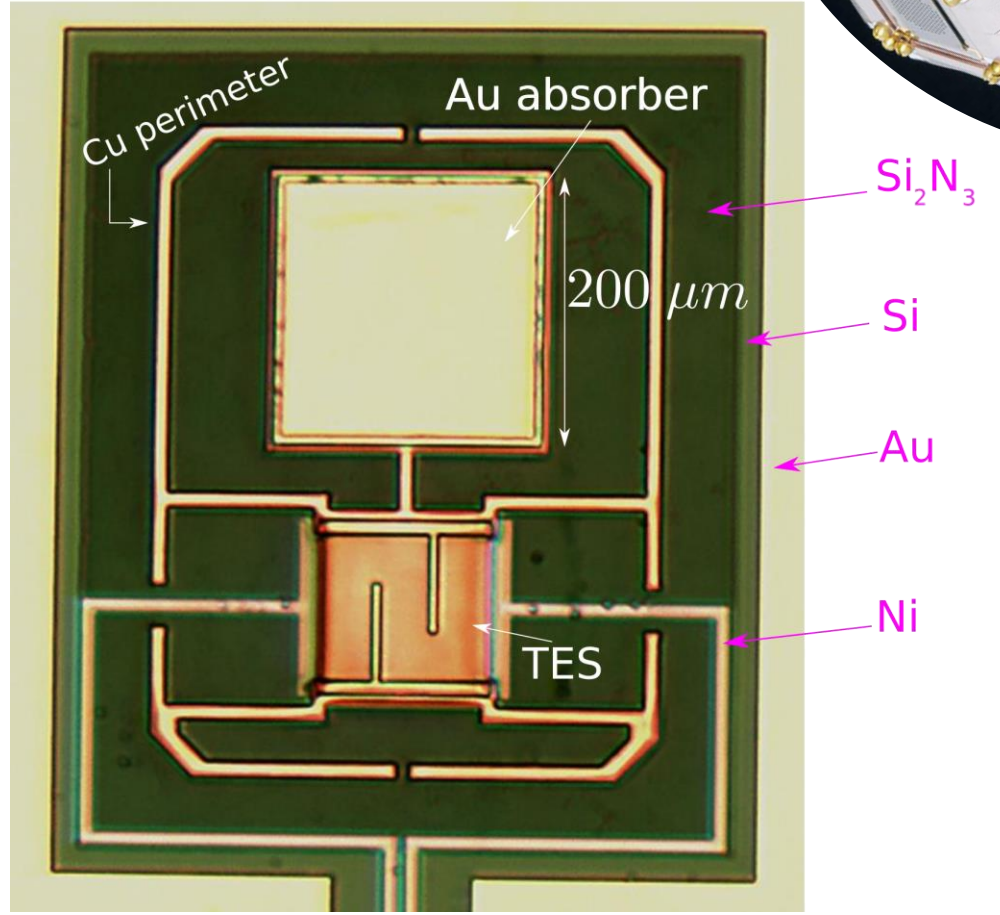
- A TES microcalorimeter is made of 3 elements:
 1. The X-ray interact in the **absorber**.
 2. The temperature variation is detected by the TES **thermometer**
 3. The detector cools down again through the heat exchange with the **thermal bath**

Array of TES for gamma-ray spectroscopy with absorbers attached on top

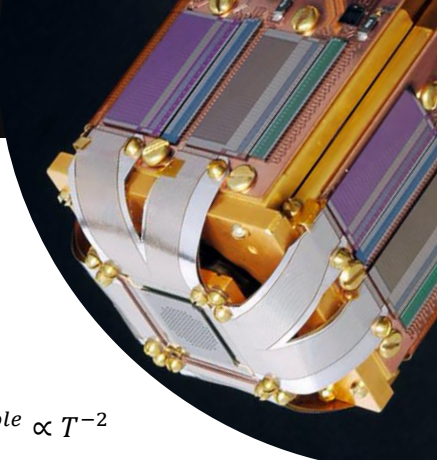


DOI 10.1088/0953-2048/28/8/084003

Topview of a detector design with sidecar geometry



Components of a TES: absorber



■ In an ideal absorber, all the energy of the X-ray is partitioned between the phonon (and the electron) system of the absorber.

■ An absorber can be made of **different materials!** (normal metals, semiconductors, superconductors...)

- Small heat capacity

$$C(T) = c_{tot}(T) \times M$$

$$c_r(T) \propto \left(\frac{T}{\theta_D}\right)^3 \quad T \ll \theta_D$$

$$c_m(T)^{dipole} \propto T^{-2}$$

$$c_e(T)^{metal} \propto \frac{T}{\theta_F}$$

$$c_e(T)^{supercond} \propto \left(1.76 \frac{T_c}{T}\right)^{\frac{3}{2}} e^{-\frac{1.76T_c}{T}}$$

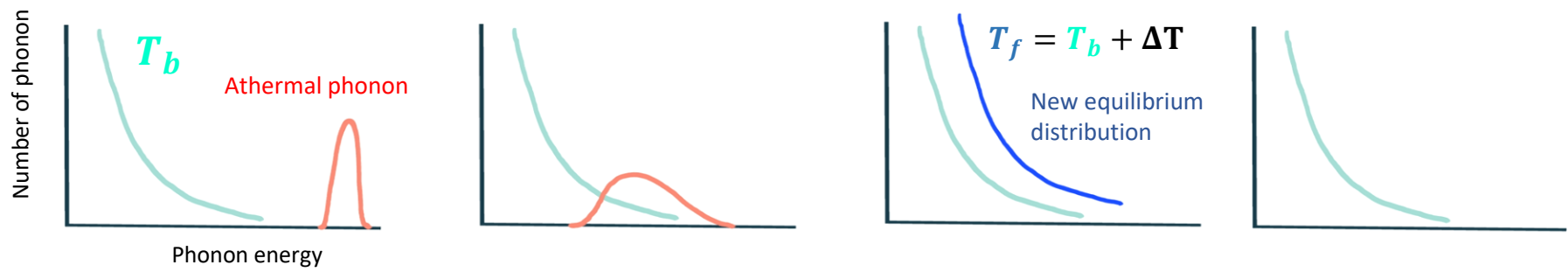
$$c_e(T)^{semicond} = 0$$

$$c_{tot}(T) = c_r(T) + c_e(T) + c_m(T)$$

- Large collecting area

Requirements:

- Fast and efficient thermalization ($O(10^{-10})$ s)



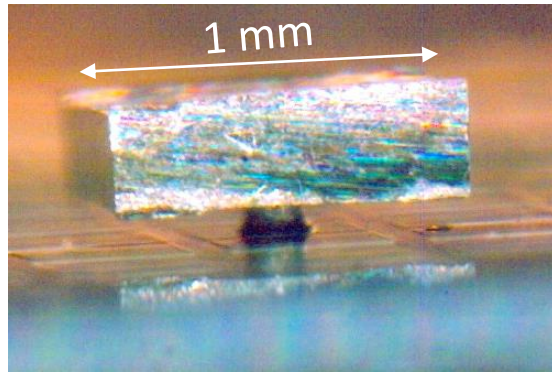
- Stopping power
 - $E < 1$ keV → the sensing structure could be enough
 - $1 < E < 10$ keV → thin film (3 μ m Au 96% @ 6keV)
 - $E > 10$ keV → thick films or bulk foils glued with cryogenic epoxy

Components of a TES: absorber



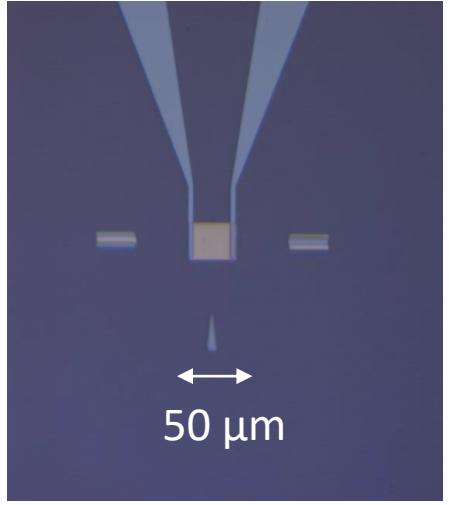
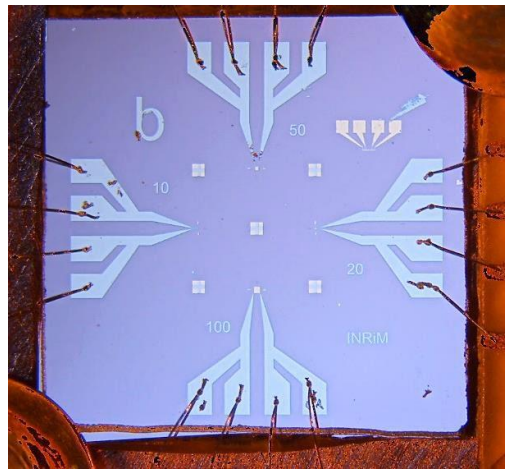
- In an ideal absorber, all the energy of the X-ray is partitioned between the phonon (and the electron) system of the absorber.
- An absorber can be made of **different materials!** (normal metals, semiconductors, superconductors...)

TES designed for gamma ray detection

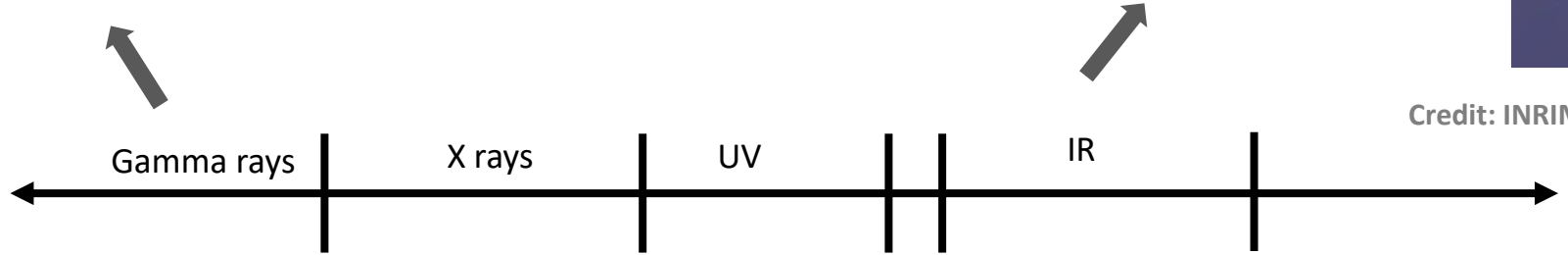


Credit: J. Ullom, NIST

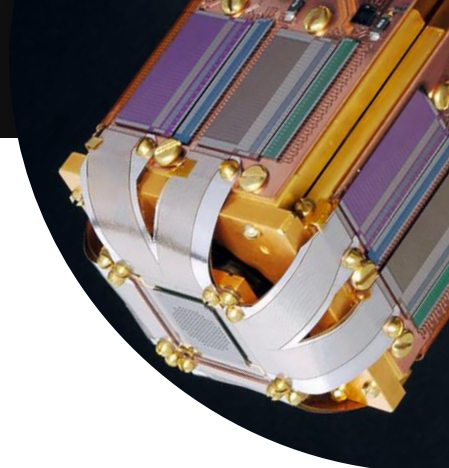
TES designed for IR SPD



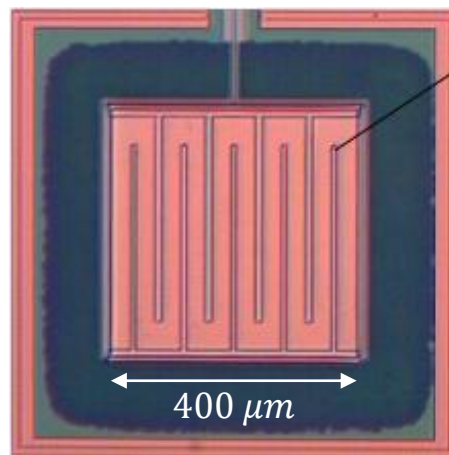
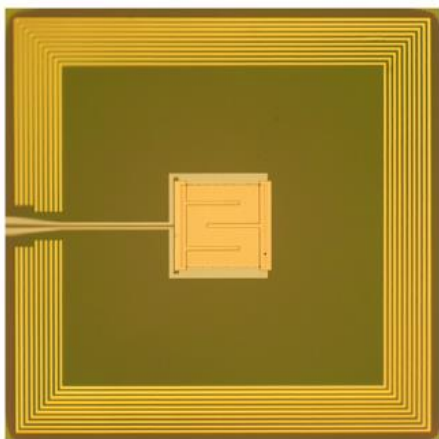
Credit: INRIM



Components of a TES: sensor

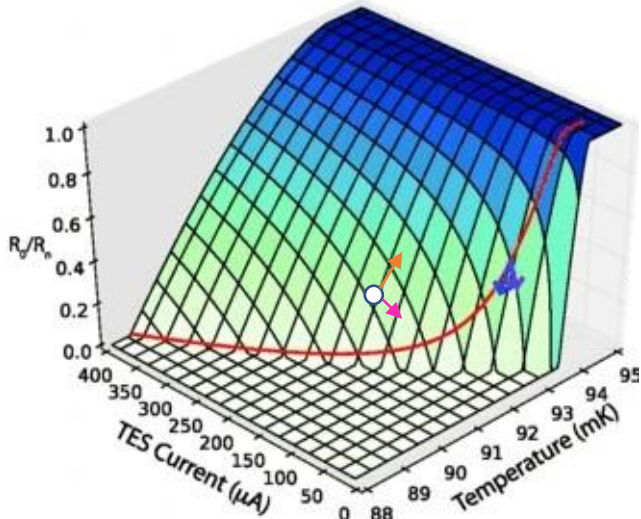


- TES thermometer: superconducting film (usually a bilayer normal metal- superconductor) biased to reach the superconducting-to-normal transition region



T_C usually chosen to be as low as can be achieved \rightarrow 30-100 mK

- The shape of the film resistance is not trivial. $R_{TES}(T, I, B)$ depends on different things, such as: the material and the dimension of the film, the geometry of the TES, ...



- The TES is biased to a point $\circ R_0(T_0, I_0)$ where the dynamic range and the sensitivity is highest $\rightarrow \sim 20\% R_N$
- Complexity of the curve captured by the two derivatives:

<https://doi.org/10.1007/s10909-011-0431-4>

$$\alpha = \left. \frac{T_0}{R_0} \frac{dR}{dT} \right|_{T_0} \quad \beta = \left. \frac{I_0}{R_0} \frac{dR}{dI} \right|_{I_0}$$

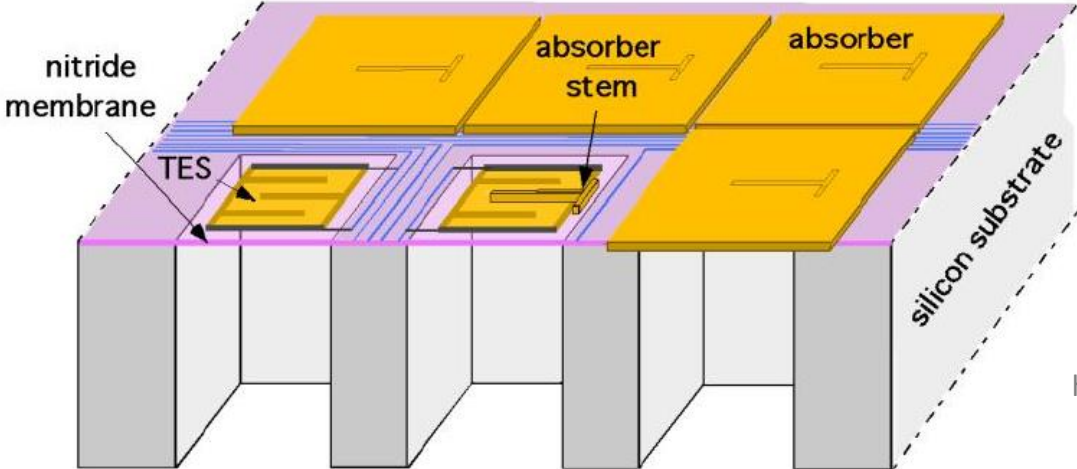
Components of a TES: thermal isolation



■ Thermal isolation necessary to avoid escape of phonons and to match the bandwidth of the amplifiers

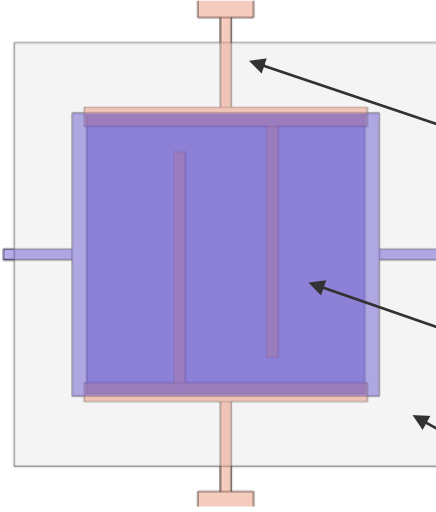
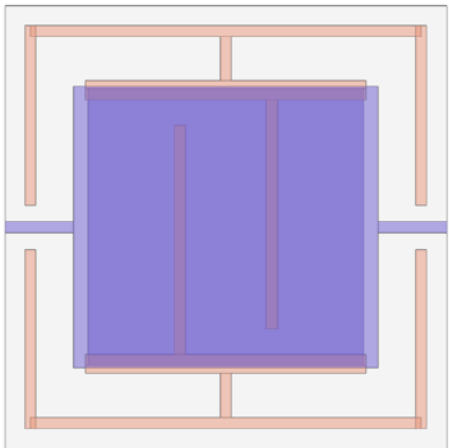
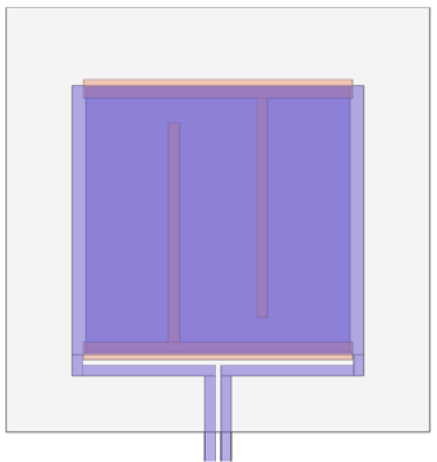


- Electron-phonon decoupling
- Limiting phonon transport
- ...



<https://doi.org/10.1117/12.734830>

■ But high thermal conductivity is crucial to reduce the dead time

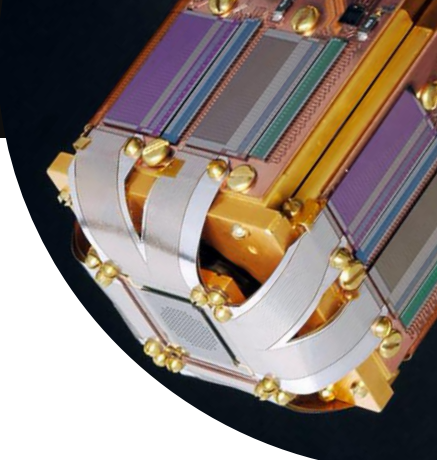


Thermal bath
Copper
TES
Silicon nitride membrane

Credit: Hays-Wehle

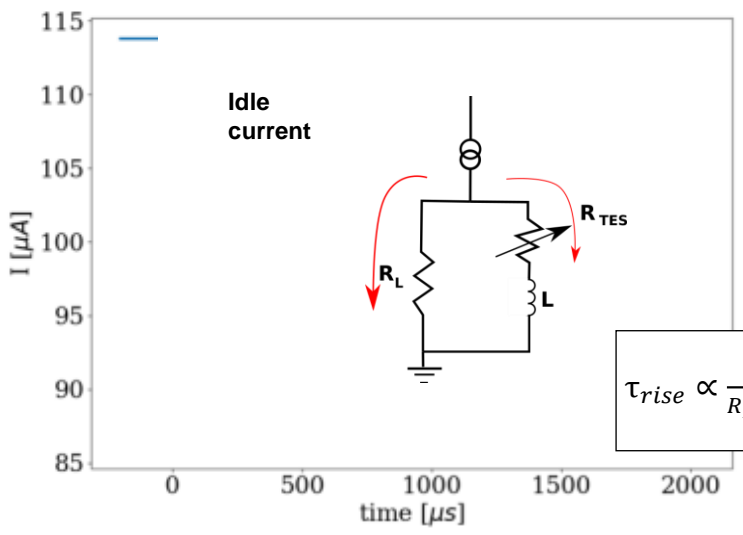
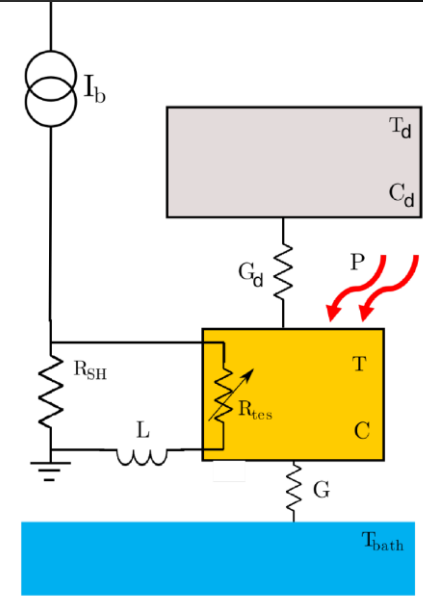
Matteo Borghesi, HPXM 2023

TES signal shape

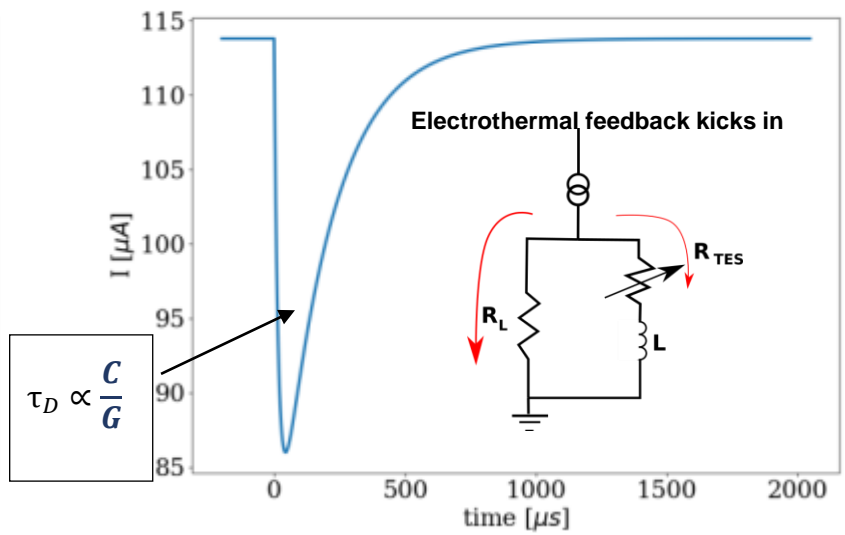
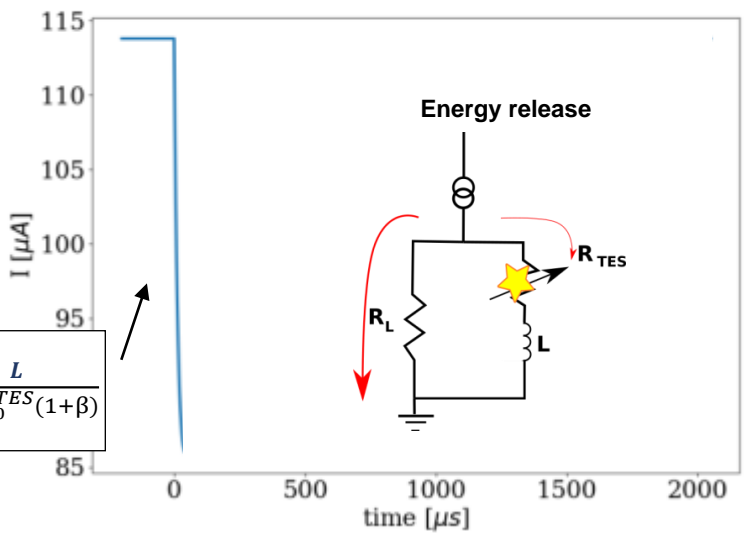


■ The TES behavior can be described by a set of n differential equations:

$$\begin{cases} L \frac{dI}{dt} = V - IR_{sh} - IR_{TES}(T, I) \\ C \frac{dT}{dt} = -K(T^n - T_b^n) - K_d(T^{n_d} - T_d^{n_d}) + P_j + P \\ C \frac{dT_d}{dt} = K_d(T^{n_d} - T_d^{n_d}) \end{cases}$$

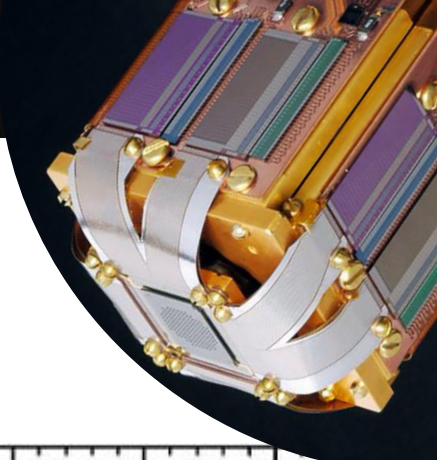


$$\tau_{rise} \propto \frac{L}{R_L + R_0^{TES}(1+\beta)}$$

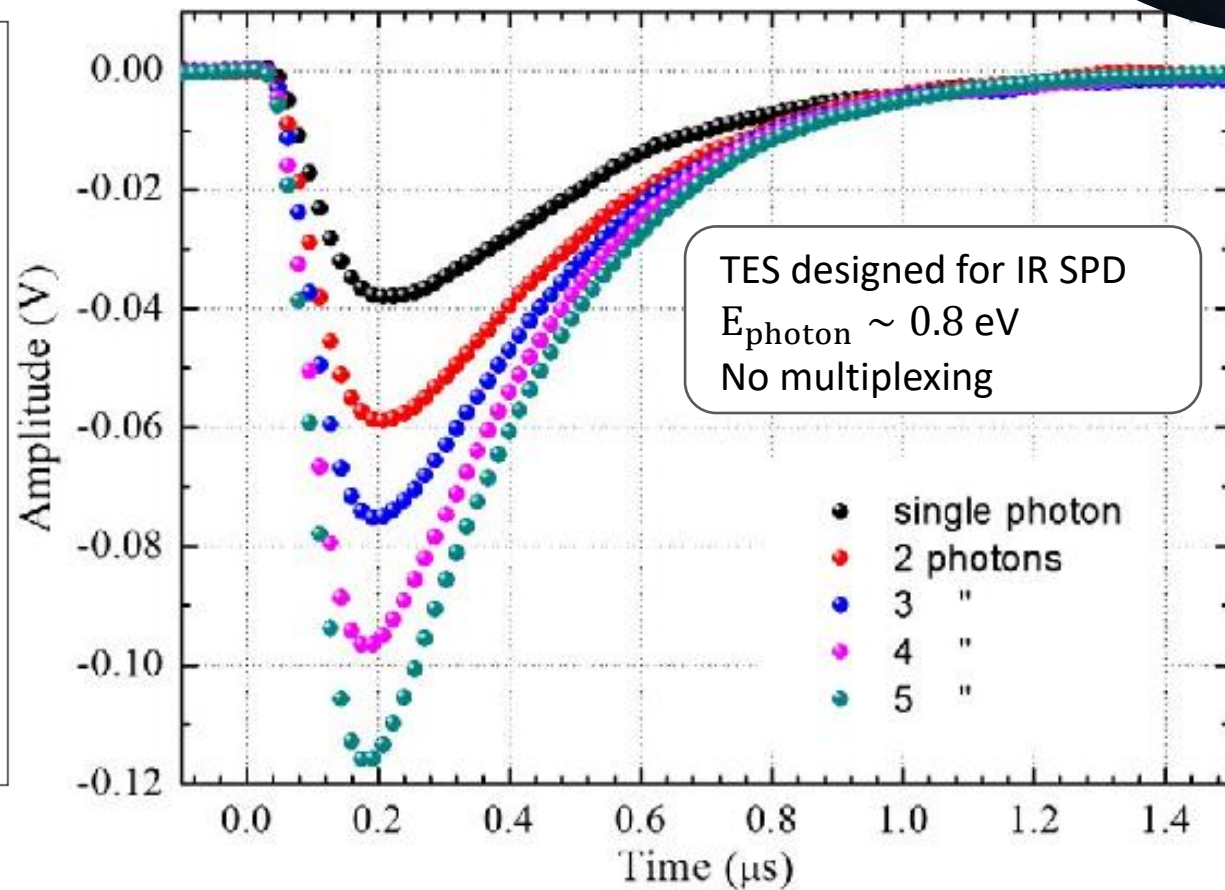
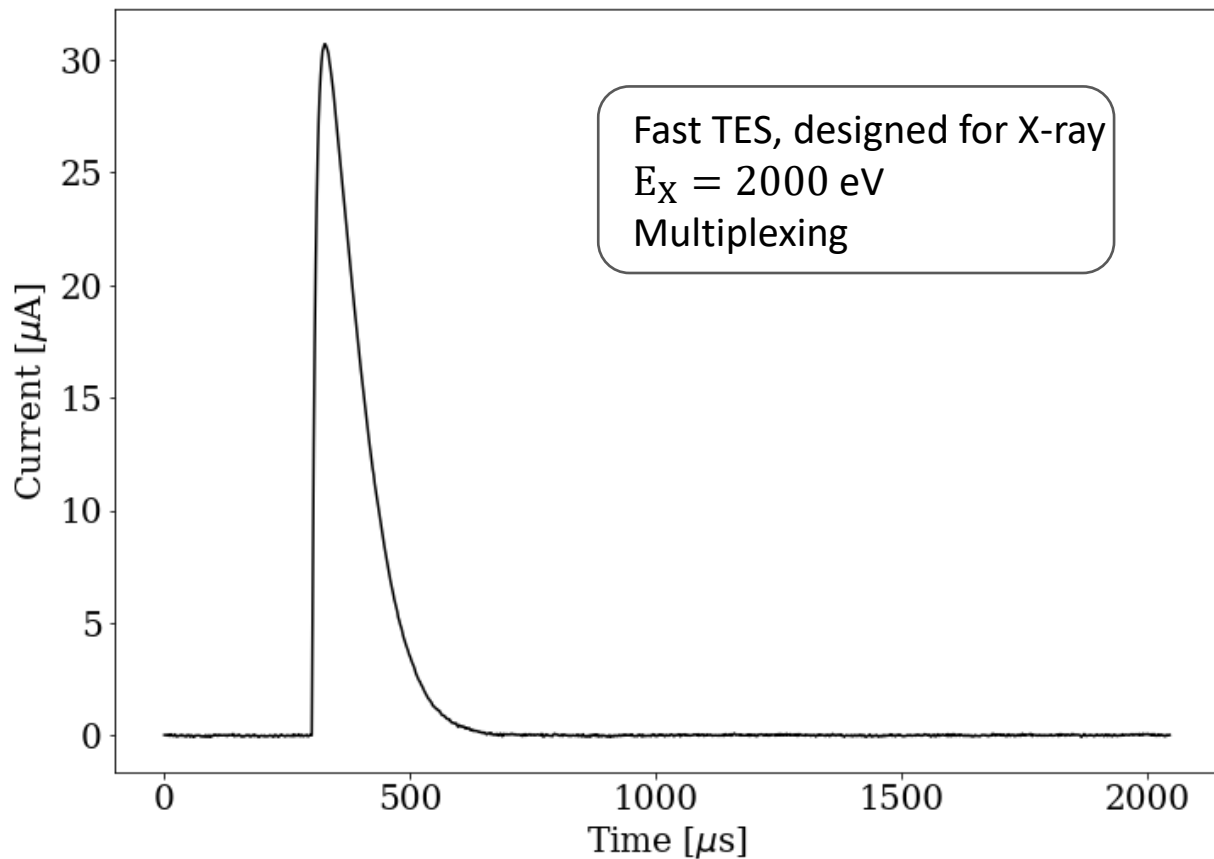


$$\tau_D \propto \frac{C}{G}$$

TES signal shape

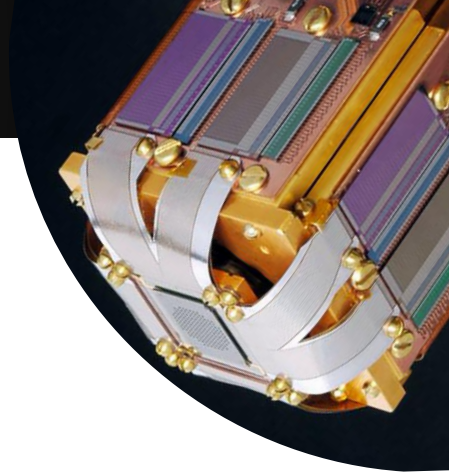


■ Tuning the parameter of the electrical circuit (and of the TES), the signal time can remarkably change



DOI: 10.1109/TASC.2013.2238981

Cryogenics: from 300K to 20mK



Mechanical cryocooler from 300K to 4K

Thermodynamic cycle on sealed 4He gas

- Plug and play
- Consume “only” electricity
- Small vibration

From 4K to mK



$^3\text{He}/^4\text{He}$ dilution refrigerator



- $T_{\min} \sim 10$ mK
- Infinite operation time (duty cycle 100%)
- $^3\text{He}/^4\text{He}$ mixture
- Not compact

Adiabatic demagnetization refrigerator (ADR)

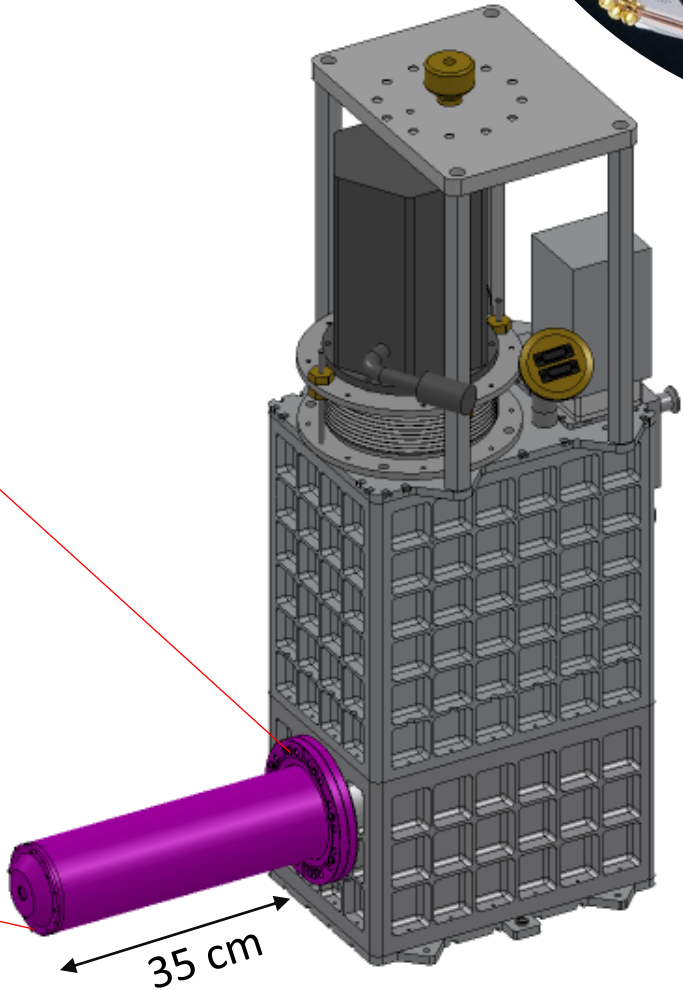
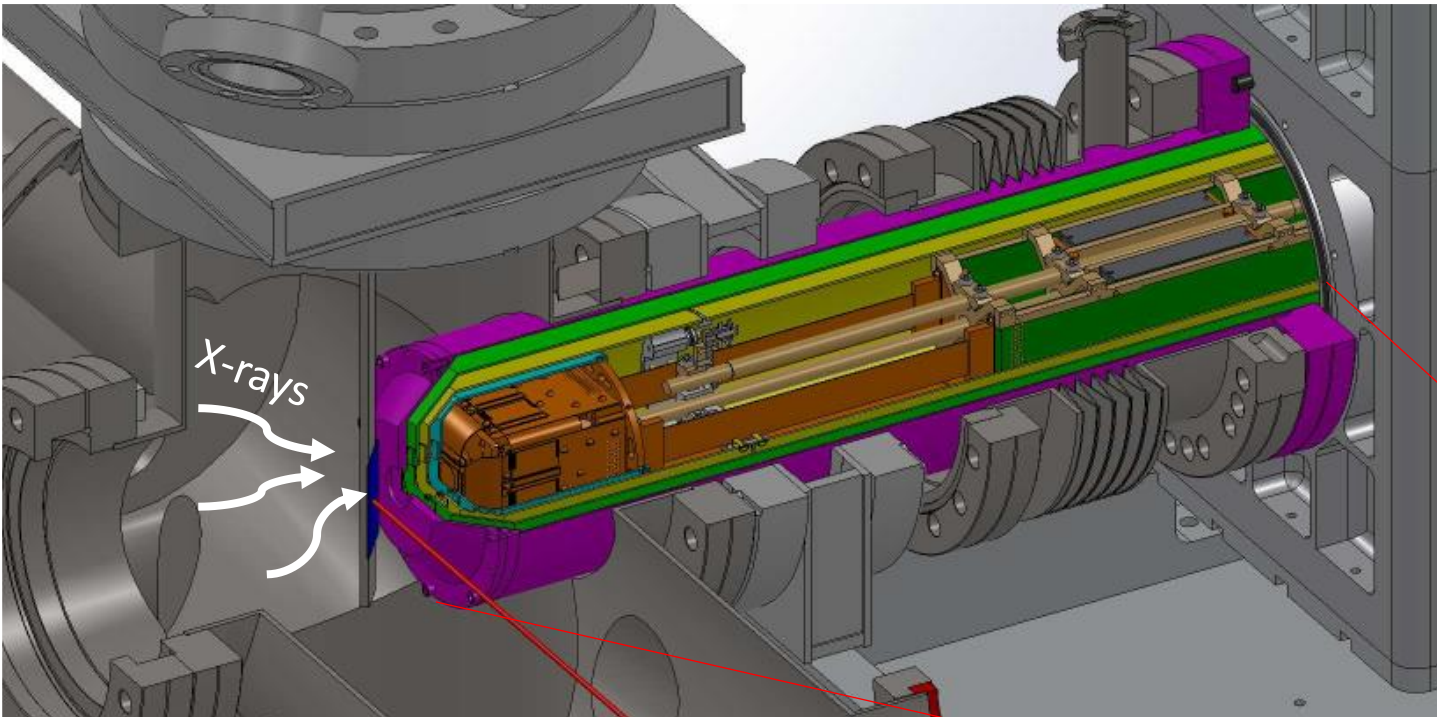


- $T_{\min} \sim 50$ mK
- Good operation time (duty cycle $\sim 85\%$)
- No liquid cryogenic
- “Compact” !

Cryogenics: shields



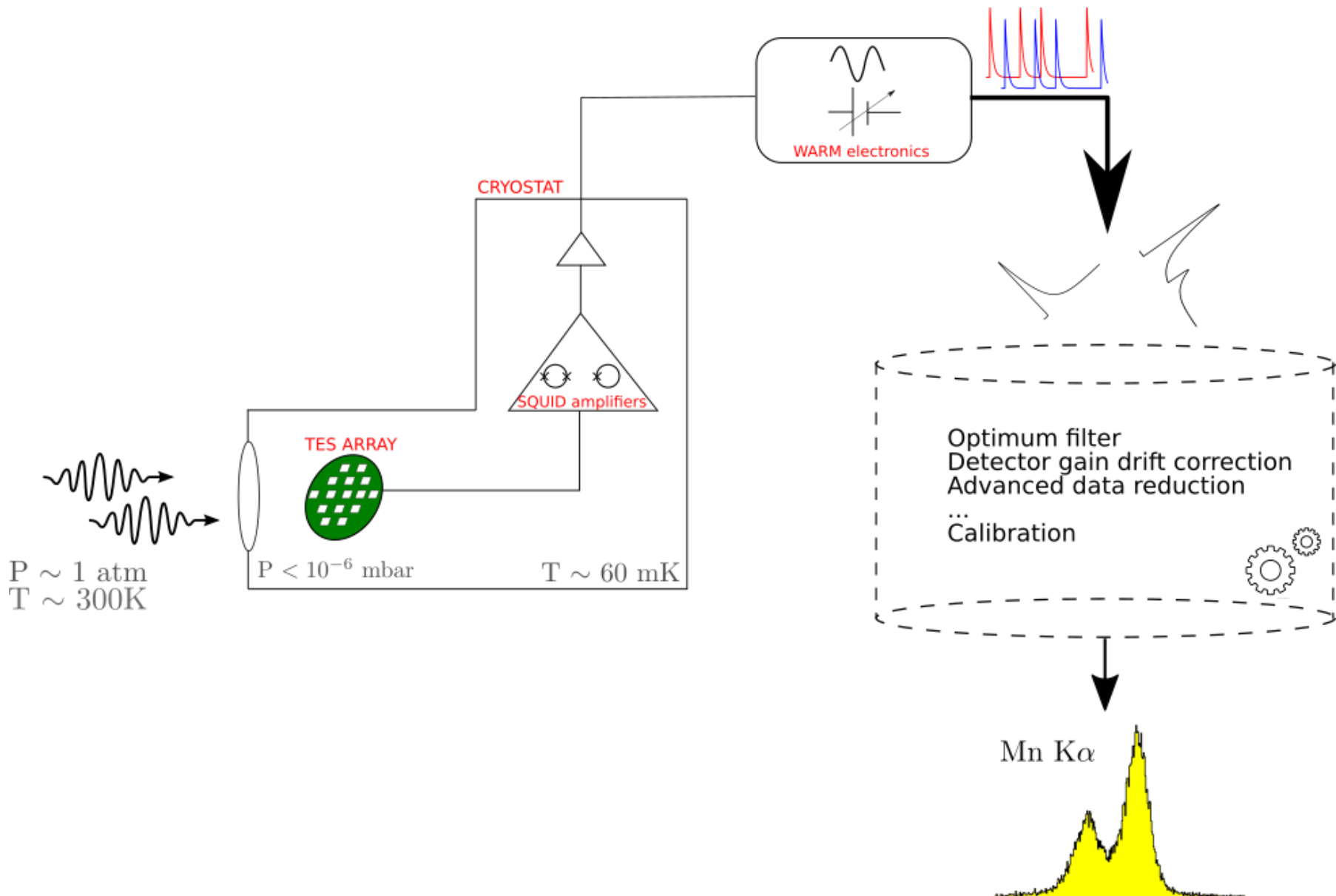
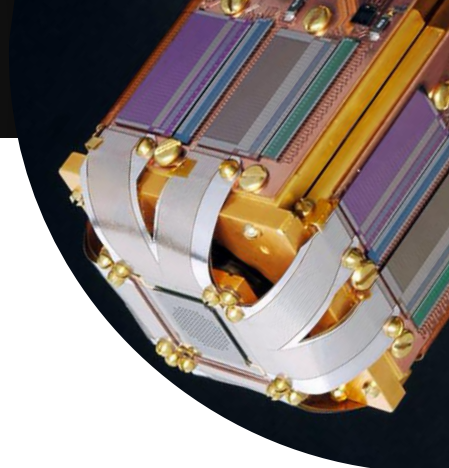
- Different shields in order to: keep the vacuum, block the thermal radiation and the magnetic fields.
X-ray transmitting windows: commercial polymer and thin Al foil.



- [300 K] Stainless steel vacuum shield
- [50K/3K] Mu-metal shield with Al radiation window
- [65 mK] Al shield with Al radiation window

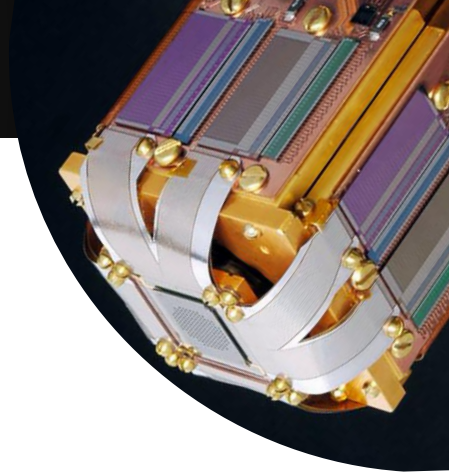
<https://doi.org/10.1063/1.4983316>

Measurement workflow with an array of TES



e.g. : 100 cps x 250 det x 24h
=
O(10) Tb triggered pulse data

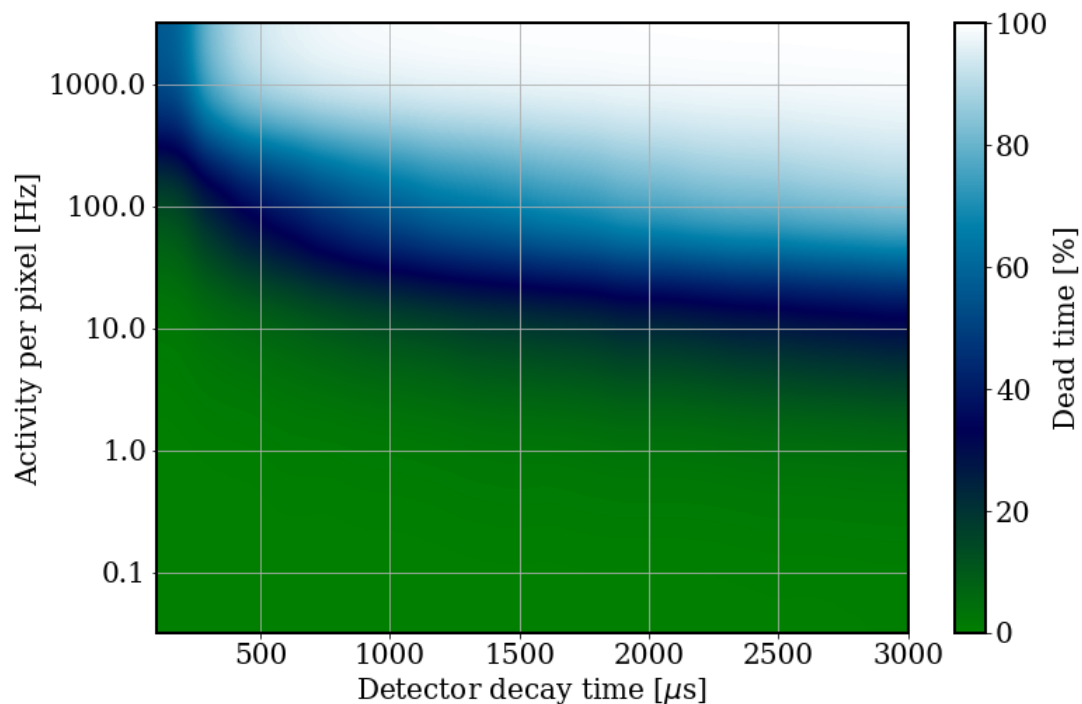
Reducing the dead time



- The analysis of microcalorimeters designed for X-rays requires great care, because their excellent intrinsic energy resolution can hardly be achieved without an accurate analysis
- The amplitude (**energy**) of an event is **evaluated with the optimum filter technique**

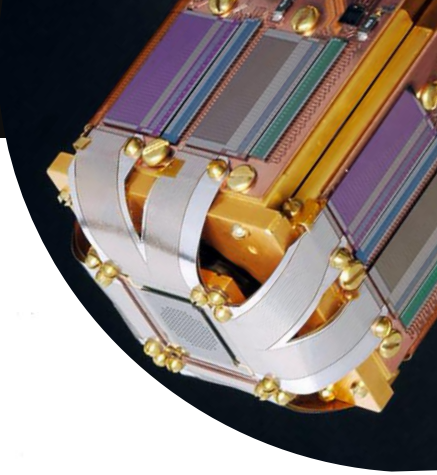


To not spoil the energy resolution, all the sample of the signals need to be recorded



- Given a source activity, faster TES and/or larger array are needed to reduce the dead time
- **Efficient multiplexing schemes to readout large array of TESs are as important as the detectors themselves**

Readout: SQUID!

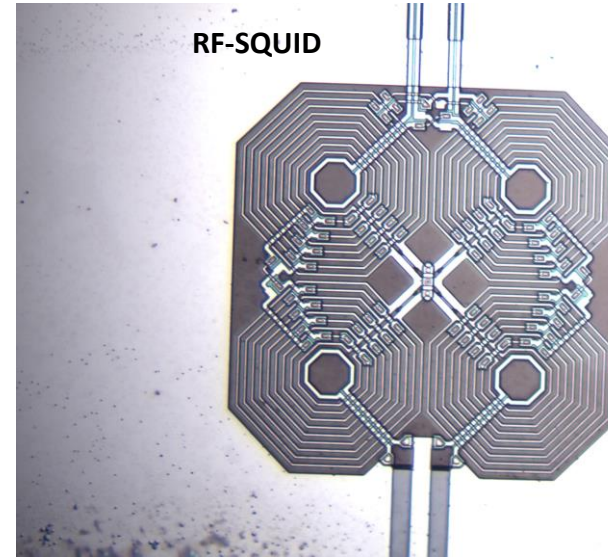
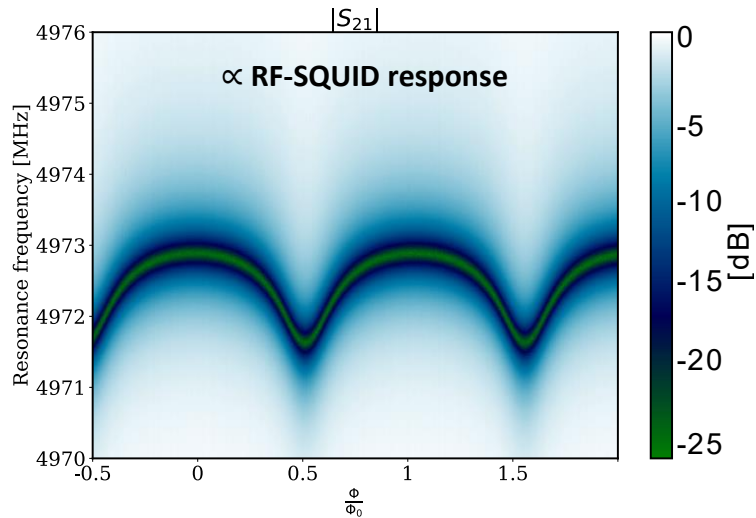


■ The TES is measured using SQUID: Superconducting loop with two (DC-SQUID) or one (RF-SQUID) Josephson junctions

- Most sensitive detectors of magnetic flux known

$$\text{Able to detect } \sim 2 \times 10^{-21} T \frac{m^2}{\sqrt{Hz}} = 10^{-6} \Phi_0 / \sqrt{Hz}$$

- Very large operational bandwidth: quasistatic $\rightarrow > 1$ GHz
- Their response to a variation of magnetic flux is a non invertible function



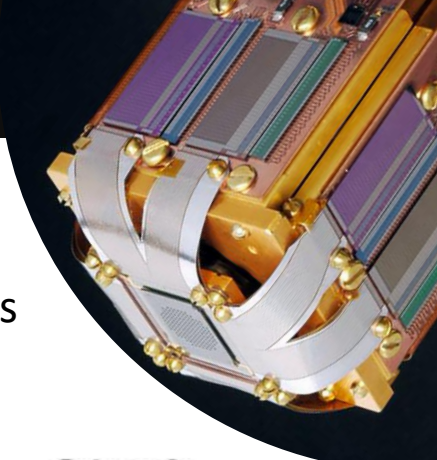
- Requirement to readout a single TES pixel with a DC SQUID
 - 5 cable from 300K to mK
 - $O(10)$ k€ for the warm electronics



Unsustainable for multi-pixel array

■ TES current seen as a variation of magnetic flux

Readout: multiplexing



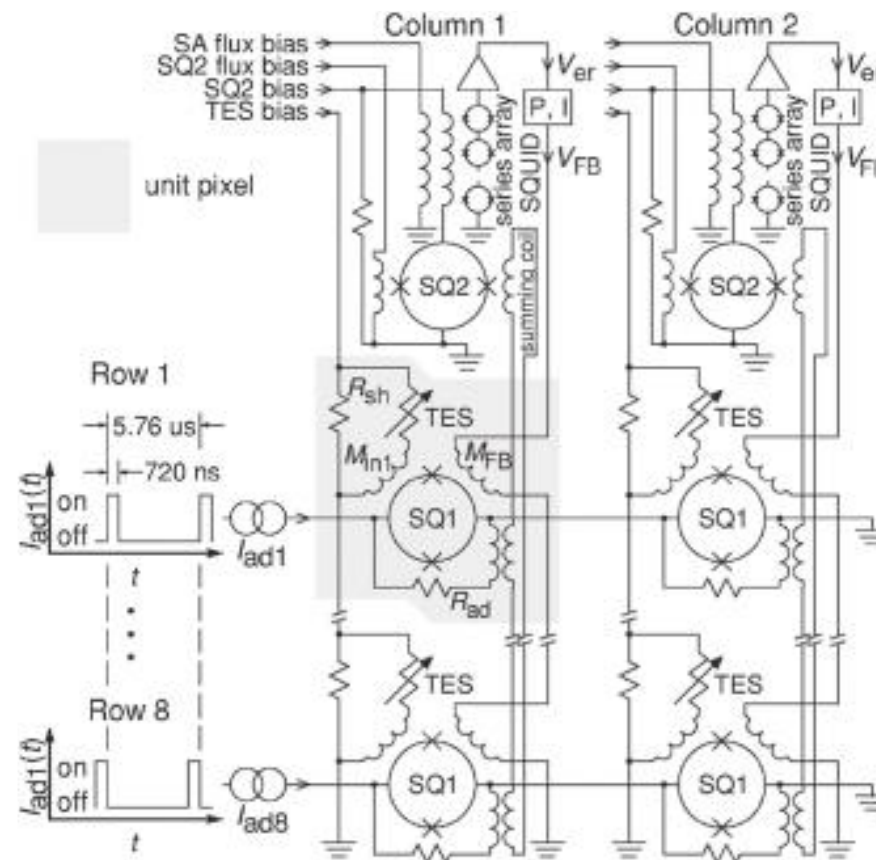
- Large TES array is needed to boost collection efficiency and count rate.
- Multiplexing (combination of different sensor signals into a smaller number of channel) is crucial it reduces the mechanical, thermal (and financial) burden of having readout circuitry for each pixel.

Time Domain Multiplexing (TDM)

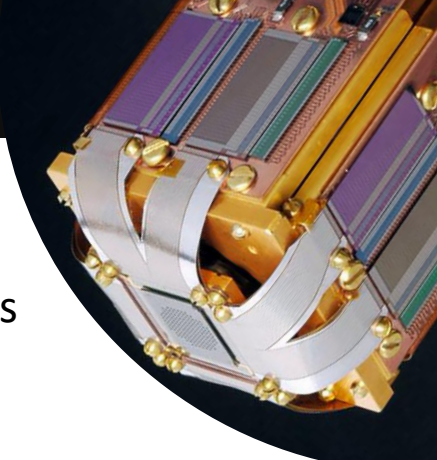
- IDEA: separating the signal in time domain
- DC-SQUIDS
- **Most mature technology**
- **Simplest operational stage**
- $\sqrt{\# \text{ channels}}$ noise penalty
- $f_{\text{samp}} \approx \frac{1}{2 \times \text{channels} \times 160 \text{ ns}}$
- 40:1 multiplexing readout best
- $\Delta E = 2.4 \text{ eV}$ with 32 multiplexed TDM TES

e.g. : 32 channel $\rightarrow f_{\text{samp}}^{\text{max}} \approx 100 \text{ kHz}$

<https://doi.org/10.1088/0953-2048/28/8/084003>



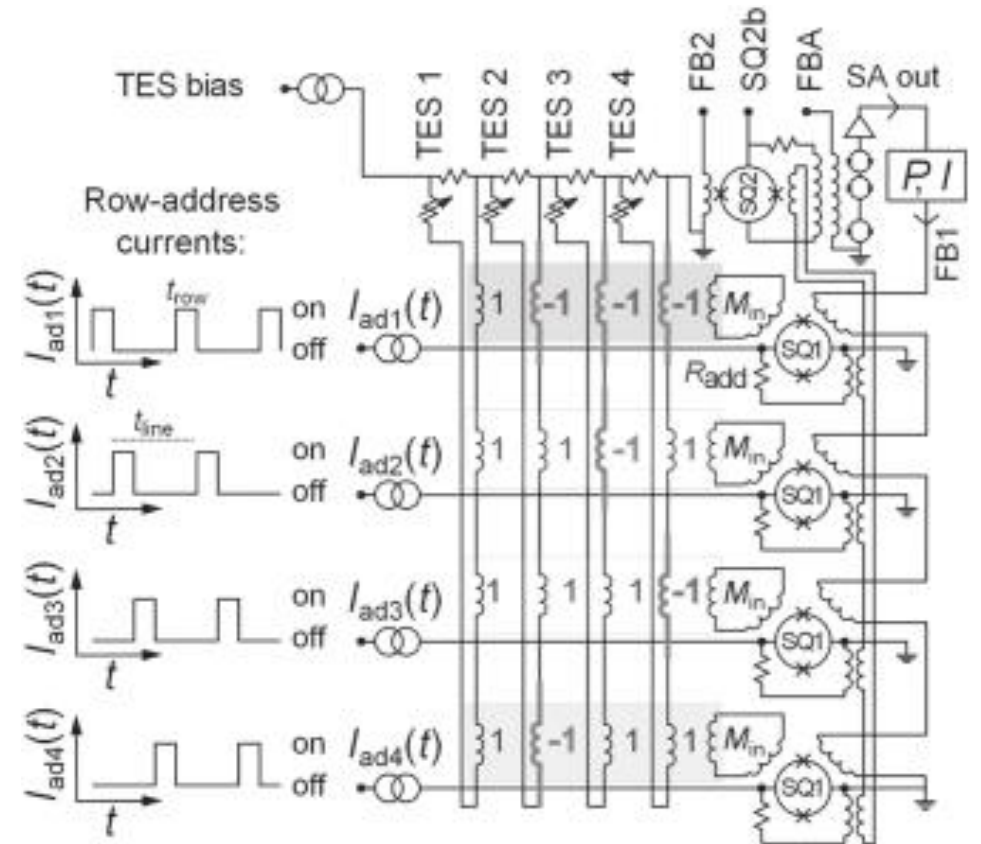
Readout: multiplexing



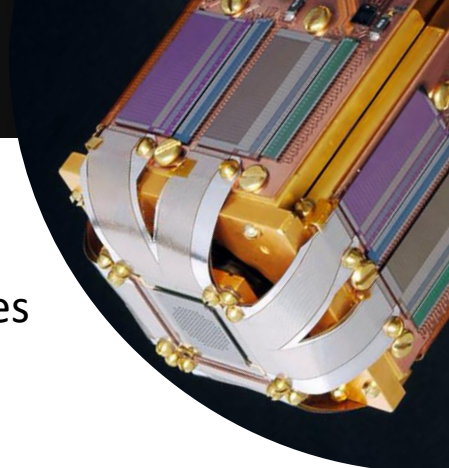
- Large TES array is needed to boost collection efficiency and count rate.
- Multiplexing (combination of different sensor signals into a smaller number of channel) is crucial it reduces the mechanical, thermal (and financial) burden of having readout circuitry for each pixel.

CDM

- IDEA: separating the signal in time domain, but smarter
- DC-SQUIDS
- No $\sqrt{\# \text{ channels}}$ noise penalty
- **Capability of readout mega-pixel array** but demonstrated at small pixel counts
- Technology in development
- $\Delta E = 2.7 \text{ eV}$ with 30 multiplexed CDM TES



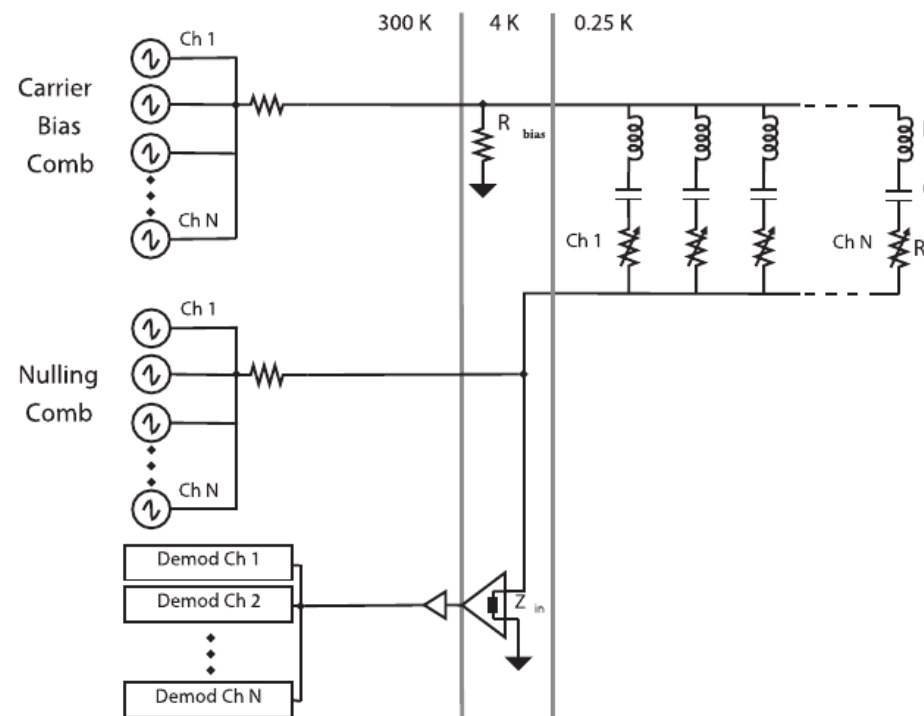
Readout: multiplexing



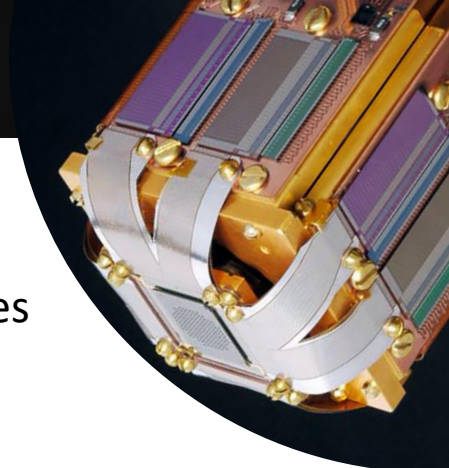
- Large TES array is needed to boost collection efficiency and count rate.
- Multiplexing (combination of different sensor signals into a smaller number of channel) is crucial it reduces the mechanical, thermal (and financial) burden of having readout circuitry for each pixel.

Frequency Division Multiplexing (FDM)

- IDEA: separating the signal in frequency domain
- DC-SQUIDS
- No $\sqrt{\text{channels}}$ noise penalty
- Limited dynamic range (the BW of the SQUID is divided into the different channels)
- Unwanted noise features due to non-trivial shape of the TES resistance
- **It's possible to tune the bias for each sensor**
- Amplitude modulator
- $\Delta E = 2.2$ eV with 37 multiplexed FDM TES



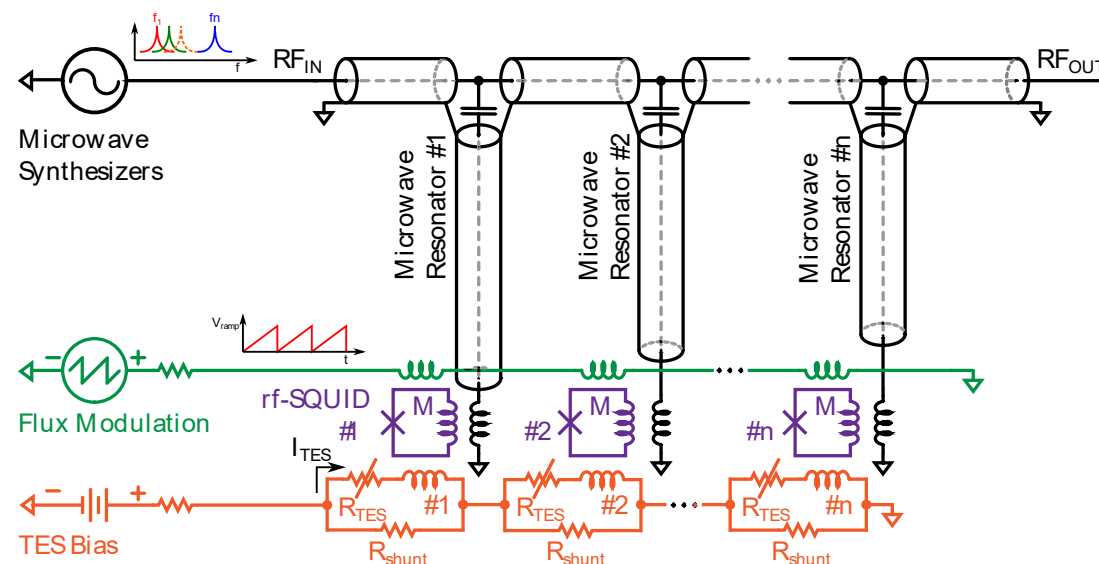
Readout: multiplexing



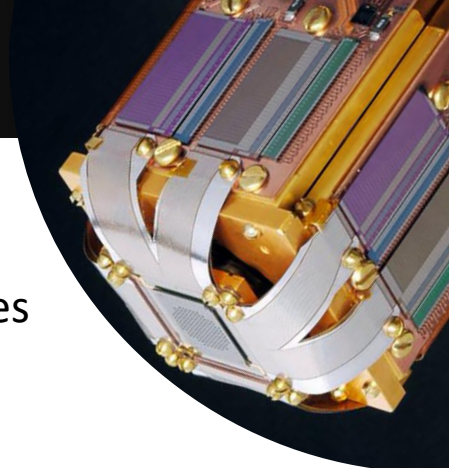
- Large TES array is needed to boost collection efficiency and count rate.
- Multiplexing (combination of different sensor signals into a smaller number of channel) is crucial it reduces the mechanical, thermal (and financial) burden of having readout circuitry for each pixel.

Microwave Multiplexing ($\mu\text{w-MUX}$)

- IDEA: separating the signal frequency domain
- RF-SQUIDS
- Higher noise
- High dynamic range (the BW of the HEMT id divided into the different channels)
- New technology!
- **Capable of 256:1 multiplexing with a $f_{\text{samp}}^{\text{max}} \approx 500 \text{ kHz}$**

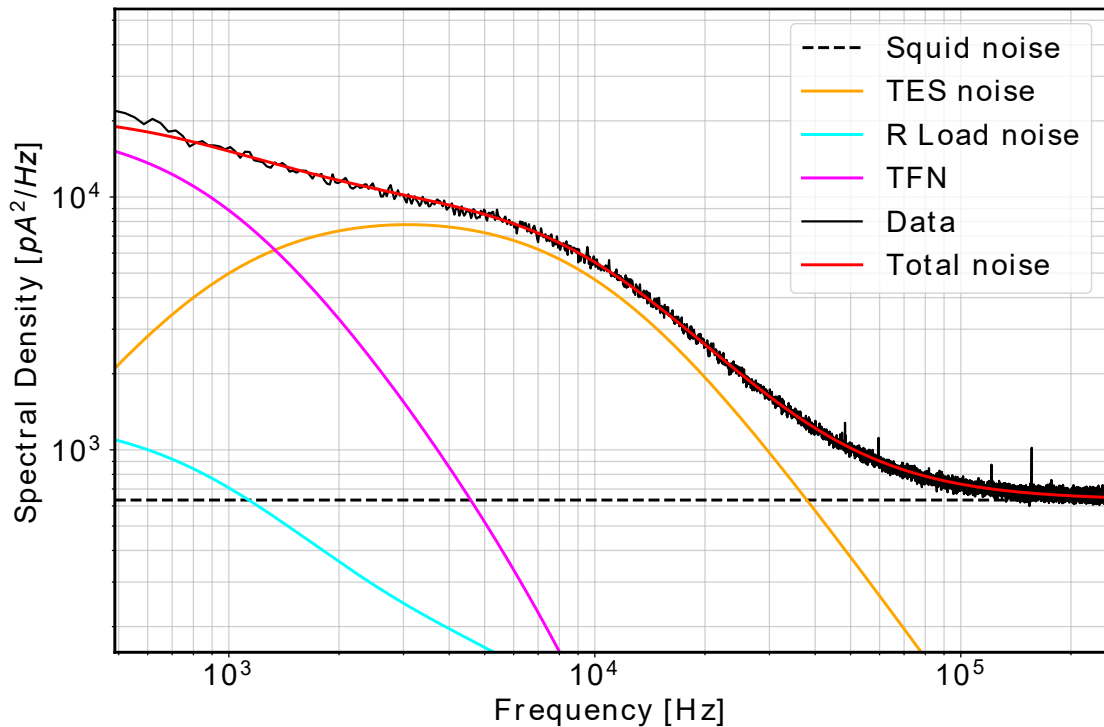


Readout: multiplexing

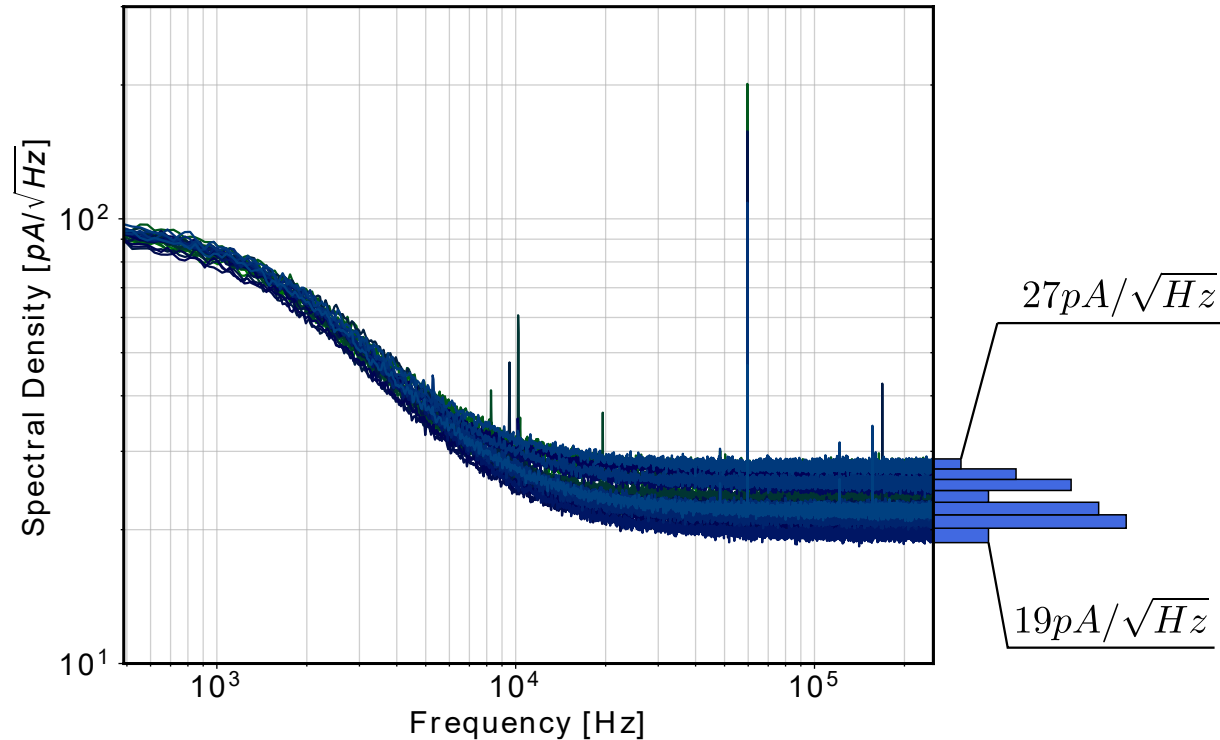


- Large TES array is needed to boost collection efficiency and count rate.
- Multiplexing (combination of different sensor signals into a smaller number of channel) is crucial it reduces the mechanical, thermal (and financial) burden of having readout circuitry for each pixel.

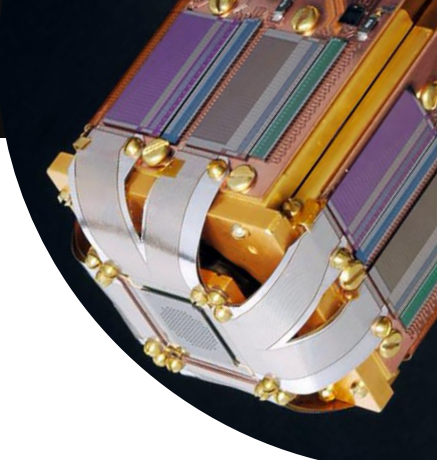
Noise of a single TES readout with uw-MUX



Noise of a 32 TES detectors readout with uw-MUX



TES application: energy dispersive X-ray spectroscopy



Semiconductors detectors:

- Poor energy resolution
- High count rate



Wavelength dispersive spectrometers

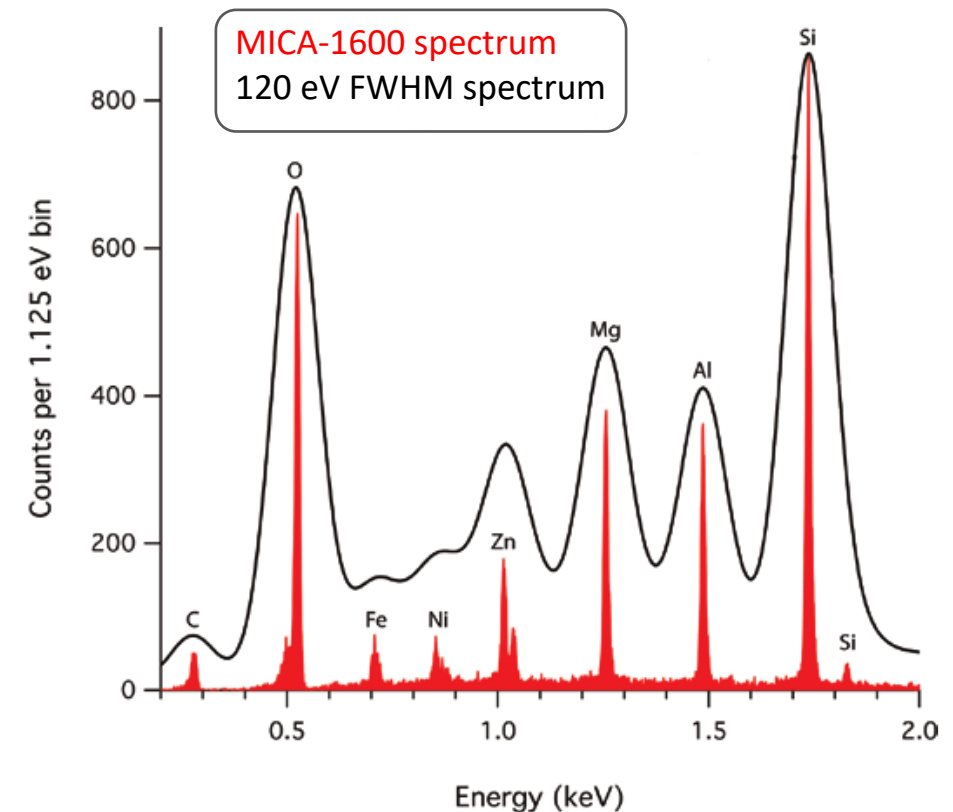
- High energy resolution
- Slow, hard to operate

■ MICA-1600 commercial TES spectrometer by Star Cryoelectronics



- ADR refrigerator
- Array of 16 TES
- TDM multiplexing ?
- Maximum count rate 10 kcps

	Microcalorimeter	WDS	EDS
Energy Resolution	< 10 eV	5–10 eV	125–130 eV
Acquisition Time	Short	Long	Short
Detection Efficiency	~100%	< 30%	~100%
Full Spectral Detection	Yes	No	Yes
Required Beam Current	10 pA–1 nA	1 nA–100 nA	10 pA–1 nA
Sample Damage	Low	High	Low



<https://doi.org/10.1017/S1551929512000429>

TES application: X-ray spectrometer for beamline



65 mK compact detector package

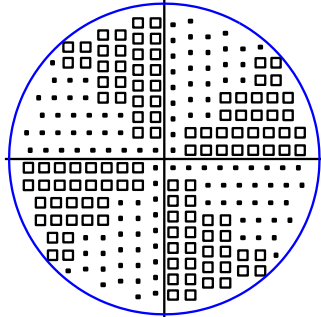


TDM multiplexing chip

- $f_{\text{samp}} \sim 100 \text{ kHz}$

Bias resistor and inductors

$\sim 1 \text{ cm}$



Chip of 240 detectors
Two types of Mo/Cu TES:

124 μm with Bi absorber (2.5 μm thick)

350 μm with Bi absorber (4.1 μm thick)

- soft X-rays
- $E_{\text{max}} = 2.1 \text{ keV}$
- $\Delta E = 1.1 \text{ eV}$ (@500 eV)

- hard X-rays
- $E_{\text{max}} = 16.7 \text{ keV}$
- $\Delta E = 3.3 \text{ eV}$ (@6keV)

TES application: X-ray spectrometer for beamline



Seven working spectrometer systems deployed in different facilities

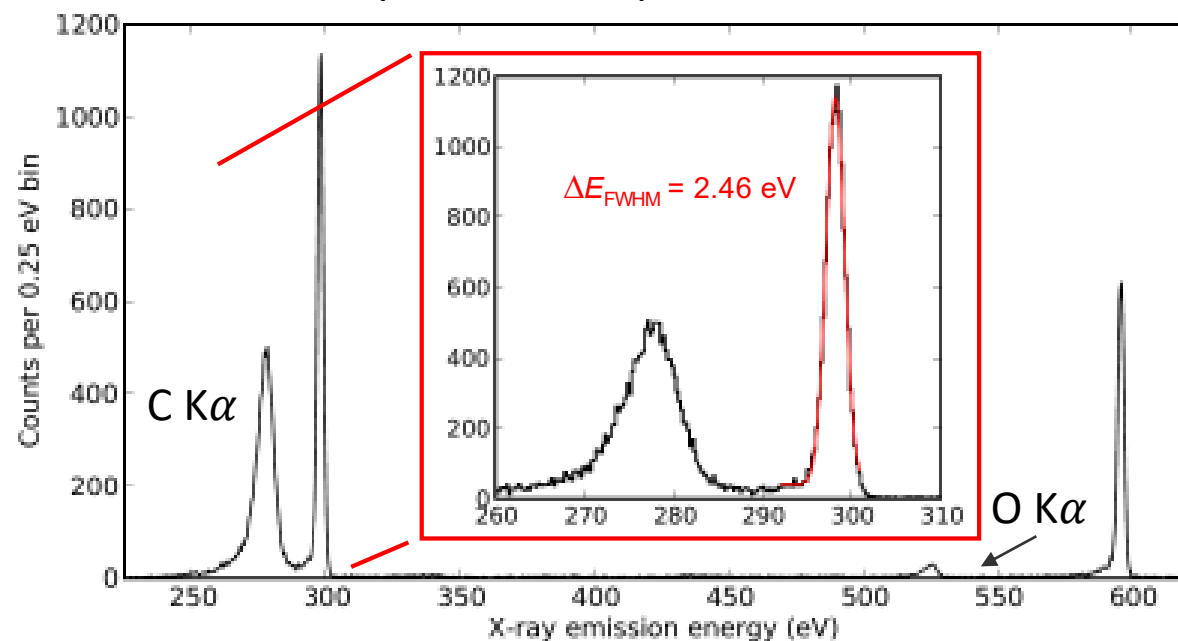
Spectrometer	Technique(s)	E (keV) of expts.	Date deployed	array type	pixel types (# of pixels)	TDM C×R	t _{row} (ns)	collimator thickness	sample dist.(cm)
A. Lund Kemencentrum	TR-XAS; TR-XES	2–10	Oct., 2010 Dec., 2013	ar13 ar13	7b (24) 7b (80); 9b (80)	4×6 8×20	640 320	full full	20 4–20
B. NIST TR	TR-XAS; TR-XES	2–10	Jan., 2013 Jan., 2015	ar13 ar14	8b (80); 9b (80) 8b(240)	8×20 8×30	640 320	full full	– –
C. NIST metrology	XRF line metrology	2–10	Nov., 2012	ar13	8b (80); 9b (80)	8×20	640	full	13
D. NSLS beamline U7A (NIST)	PFY-NEXAFS; XES	0.25–1	Oct., 2011 Apr., 2014	ar13 ar14	7b (60) 3b(120); 8b(120)	3×20 8×30	640 320	full thinned	≥ 2 ≥ 2
E. APS 29-ID	RSXS	0.25–1	Jul., 2014	ar14	3b(240)	8×30	320	thinned	≥ 5
F. Jyväskylä Pelletron	PIXE	1–14	Feb., 2011 Feb., 2014	ar13 ar13	8b (12) 8b (80); 9b (80)	2×6 8×20	640 320	full full	30 15
G. PSI πM1	π ⁻ -atom spectroscopy	4–15	Oct., 2014	ar14	8b(240)	8×30	320	full	4–8



Five more planned!

<https://doi.org/10.1063/1.4983316>

Example of a combined spectra of 60 detectors



TES application: X-ray astrophysics (ATHENA X-IFU)



- Instrument for X-ray imaging, timing and high-resolution spectroscopy on satellite

Observation of hot gas and accretion around black holes

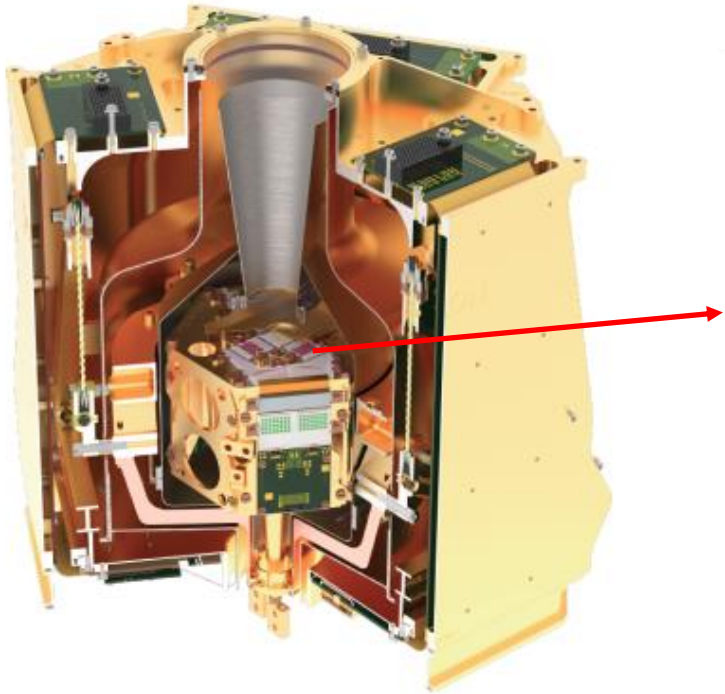
- Target: 3000 TES pixels ($T_c \sim 90$ mK, energy range 0.2-12 keV, $\Delta E = 2.5$ eV @7keV)



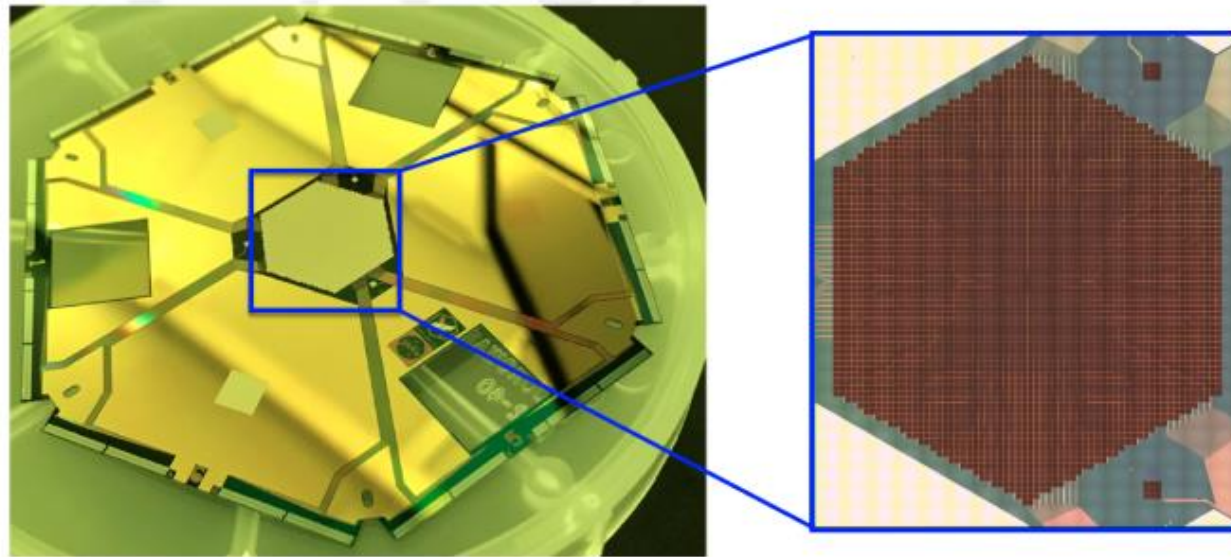
- Single pixel ΔE better than 2 eV
- Pixel filling factor better than 0.97

- Initially FDM, now TDM multiplexing?

X-IFU focal plane assembly model

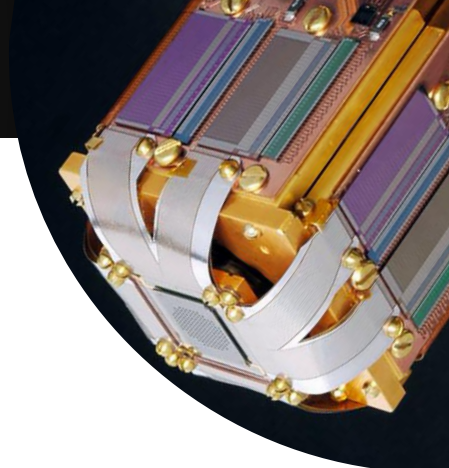


Prototype array from NASA-GSFC (3000 pixels)



<https://doi.org/10.3390/app11093793>

TES application: X-ray astrophysics (Lynx)

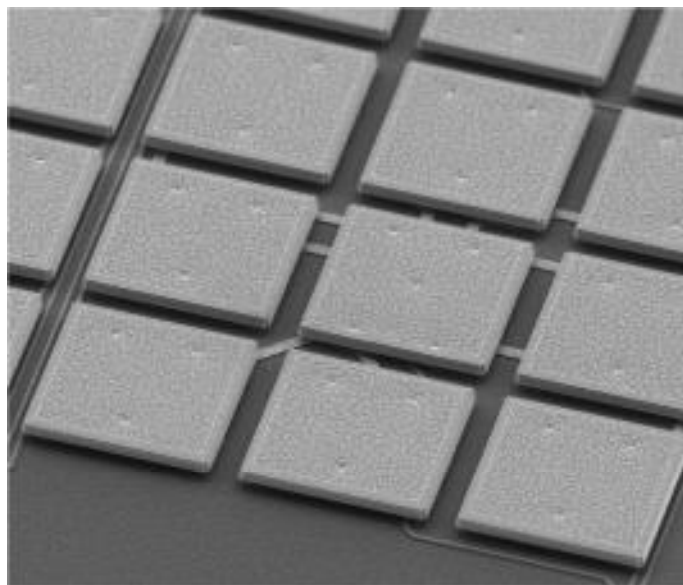
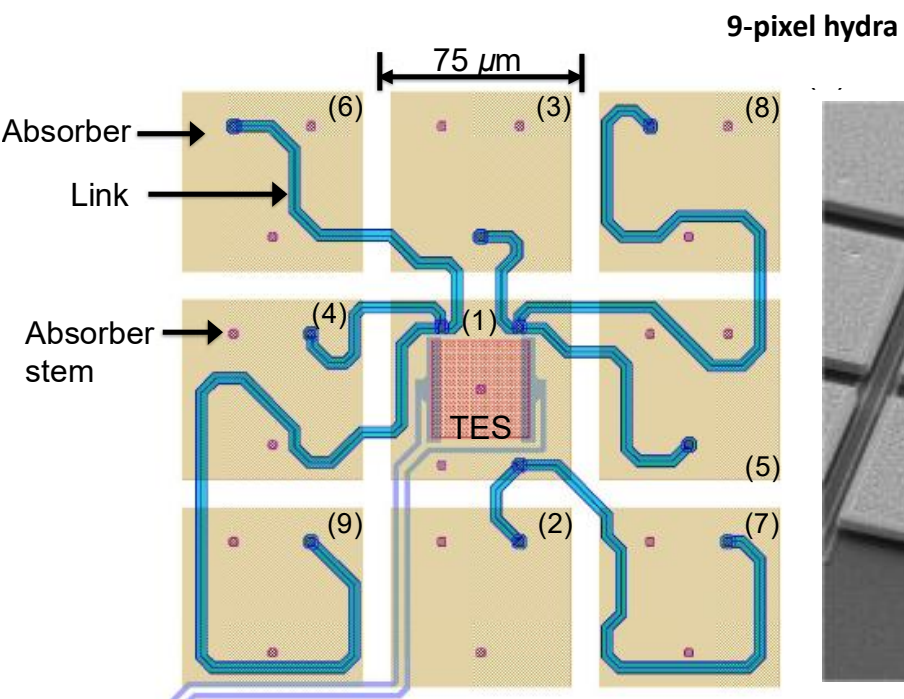


■ Next generation X-ray observatory on satellite

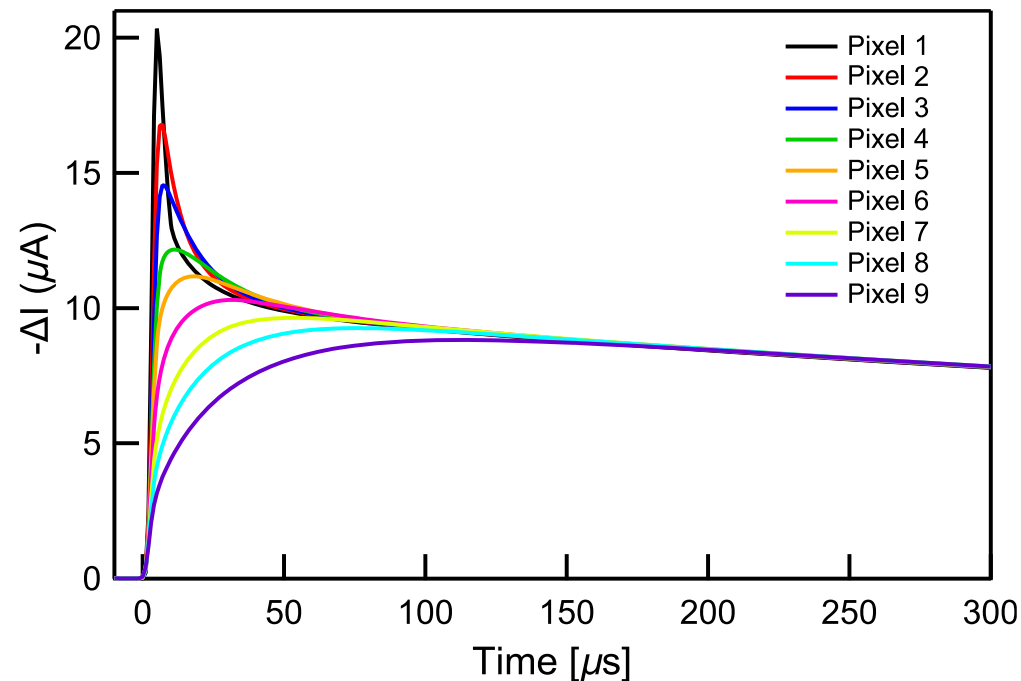
■ Ambitious goal: 100000 pixels!

Challenging requirements for the sensors and the readout

■ Possible solution: hydra TES design and μw -MUX multiplexing

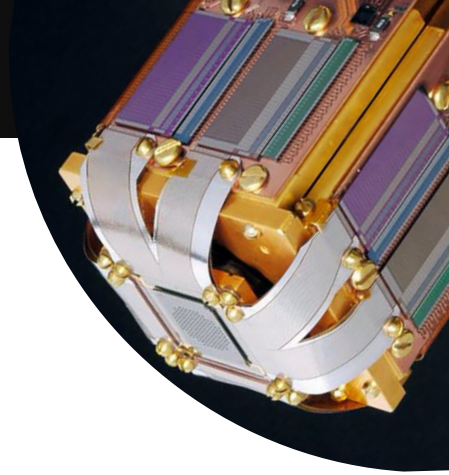


Pulses @6keV x-rays interacting in the different absorbers



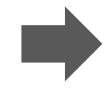
<https://doi.org/10.1117/1.JATIS.5.2.021008>

Conclusions



- Superconducting Transition Edge Sensors are very high-resolution detectors for X-rays

- An array of Transition Edge Sensors is essential for practical applications.



Multiplexing is important!

- Active field of research, multiple improvements expected in the next years!