

# M R E

# IS

# DIFFERENTLY

# DIFFERENT



The multiphased nature of condensed matter



Jacopo Fiore  
PhD seminars – S06E01  
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SAPIENZA  
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# Summary

- Introduction: how differently?
- Multiphased materials and superconductivity
- Probing phases and their signatures
- Examples: phase coexistence in NbSe<sub>2</sub> and LSCO
- Conclusion: same phase... different faces

(I did not come up with this title...)

FEATURES LOW TEMPERATURE PHYSICS



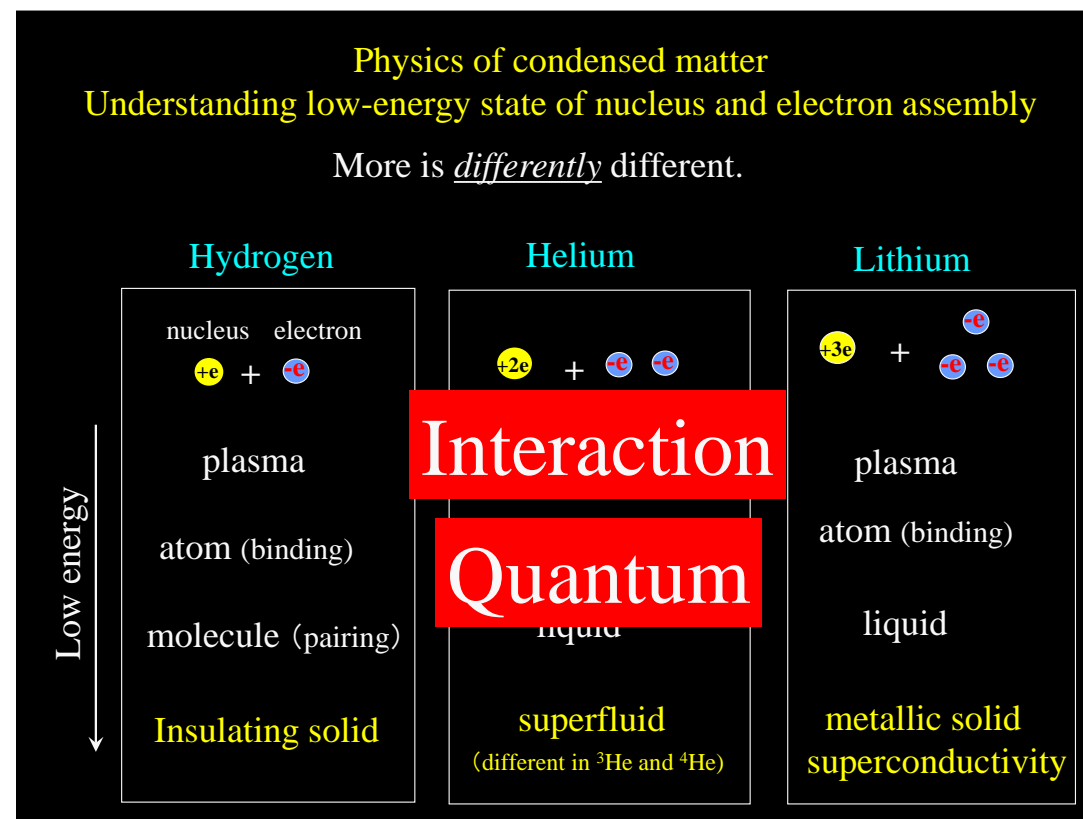
## THE MANY FACES (PHASES) OF STRONG CORRELATIONS

■ Silke Paschen<sup>1</sup> and Qimiao Si<sup>2</sup> – DOI: <https://doi.org/10.1051/epn/2021407>

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There has been considerable recent progress in discovering and understanding quantum phases and fluctuations produced by strong correlations. Heavy fermion systems are an ideal platform for systematic studies because low and competing energy scales make them highly tunable. As such the phases (faces) of strong correlations transform continuously into one another.



Kanoda, 2022

[Paschen&Si, 2021](#)

# Explaining the -ly

*The constructionist hypothesis breaks down when confronted with the twin difficulties of scale and complexity. The behavior of large and complex aggregates of elementary particles, it turns out, is **not** to be understood in terms of a simple extrapolation of the properties of a few particles. Instead, at each level of complexity entirely new properties appear, and the understanding of the new behaviors requires research [...] inspiration and creativity to just as great a degree as in the previous one.*

## More Is Different

Broken symmetry and the nature of the hierarchical structure of science.

P. W. Anderson

The reductionist hypothesis may still be a topic for controversy among philosophers, but among the great majority of active scientists I think it is accepted without question. The workings of our minds and bodies, and of all the animate or inanimate matter of which we have any detailed knowledge, are assumed to be controlled by the same set of fundamental laws, which except under certain extreme conditions we feel we know pretty well.

It seems inevitable to go on uncritically to what appears at first sight to be an obvious corollary of reductionism: that if everything obeys the same fundamental laws, then the only scientists who are studying anything really fundamental are those who are working on those laws. In practice, that amounts to some astrophysicists, some elementary particle physicists, some logicians and other mathematicians, and few

planation of phenomena in terms of known fundamental laws. As always, distinctions of this kind are not unambiguous, but they are clear in most cases. Solid state physics, plasma physics, and perhaps also biology are extensive. High energy physics and a good part of nuclear physics are intensive. There is always much less intensive research going on than extensive. Once new fundamental laws are discovered, a large and ever increasing activity begins in order to apply the discoveries to hitherto unexplained phenomena. Thus, there are two dimensions to basic research. The frontier of science extends all along a long line from the newest and most modern intensive research, over the extensive research recently spawned by the intensive research of yesterday, to the broad and well developed web of extensive research activities based on intensive research of past decades.

The effectiveness of this message may be indicated by the fact that I heard it quoted recently by a leader in the field of materials science, who urged the

less relevance they seem to have to the very real problems of the rest of science, much less to those of society.

The constructionist hypothesis breaks down when confronted with the twin difficulties of scale and complexity. The behavior of large and complex aggregates of elementary particles, it turns out, is not to be understood in terms of a simple extrapolation of the properties of a few particles. Instead, at each level of complexity entirely new properties appear, and the understanding of the new behaviors requires research which I think is as fundamental in its nature as any other. That is, it seems to me that one may array the sciences roughly linearly in a hierarchy, according to the idea: The elementary entities of science X obey the laws of science Y.

X	Y
solid state or many-body physics	elementary particle physics
chemistry	many-body physics
molecular biology	chemistry
cell biology	molecular biology
⋮	⋮
⋮	⋮
psychology	psychology
social sciences	psychology

But this hierarchy does not imply that science X is "just applied Y." At each stage entirely new laws, concepts, and generalizations are necessary, requiring inspiration and creativity to just as great a degree as in the previous one. Psychology is not applied biology, nor is biology applied chemistry.

[Anderson, 1972](#)



# Explaining the –ly... Fifty years later

*Strongly correlated electron systems host a tremendous variety of fascinating macroscopic phenomena [...] the essential physics of many of these systems is still not understood, and we do not have a overall perspective on strong electron correlations. Moreover, our predictive power for such systems is lacking. [...] Is a unified perspective even possible? Or is the “Anna Karenina Principle” in effect – all non-interacting systems are alike; each strongly correlated system is strongly correlated in its own way?*

## The Future of the Correlated Electron Problem

A. Alexandradinata,<sup>1,2</sup> N.P. Armitage,<sup>3,\*</sup> Andrey Baydin,<sup>4</sup> Wenli Bi,<sup>5</sup> Yue Cao,<sup>6</sup> Hitesh J. Changlani,<sup>7,8</sup> Eli Chertkov,<sup>1,2</sup> Eduardo H. da Silva Neto,<sup>9,10</sup> Luca Delacretaz,<sup>11</sup> Ismail El Baggari,<sup>12</sup> G.M. Ferguson,<sup>12</sup> William J. Gannon,<sup>13</sup> Sayed Ali Akbar Ghorashi,<sup>14</sup> Berit H. Goodge,<sup>15</sup> Olga Gouklo,<sup>16,17</sup> Gaël Grissonnanche,<sup>18</sup> Alannah Hallas,<sup>19</sup> Ian M. Hayes,<sup>20</sup> Yu He,<sup>21,22</sup> Edwin W. Huang,<sup>1,2</sup> Anshul Kogar,<sup>23</sup> Divine Kumah,<sup>24</sup> Jong Yeon Lee,<sup>25</sup> Anaëlle Legros,<sup>3</sup> Fahad Mahmood,<sup>26,2</sup> Yulia Maximenko,<sup>2,26</sup> Nick Pellatz,<sup>27</sup> Hryhoriy Polshyn,<sup>28</sup> Tarapada Sarkar,<sup>20</sup> Allen Scheie,<sup>29</sup> Kyle L. Seyler,<sup>30</sup> Zhenzhong Shi,<sup>31</sup> Brian Skinner,<sup>32</sup> Lucia Steinke,<sup>33,8</sup> Komalavalli Thirunavukkuarasu,<sup>34</sup> Thais Victa Trevisan,<sup>35</sup> Michael Vogl,<sup>36,37</sup> Pavel A. Volkov,<sup>38</sup> Yao Wang,<sup>39</sup> Yishu Wang,<sup>3</sup> Di Wei,<sup>40,41</sup> Kaya Wei,<sup>5</sup> Shuolong Yang,<sup>42</sup> Xian Zhang,<sup>43</sup> Ya-Hui Zhang,<sup>25</sup> Jong Yeon Lee,<sup>25</sup> Liuyan Zhao,<sup>44</sup> and Alfred Zong.<sup>45,46</sup>

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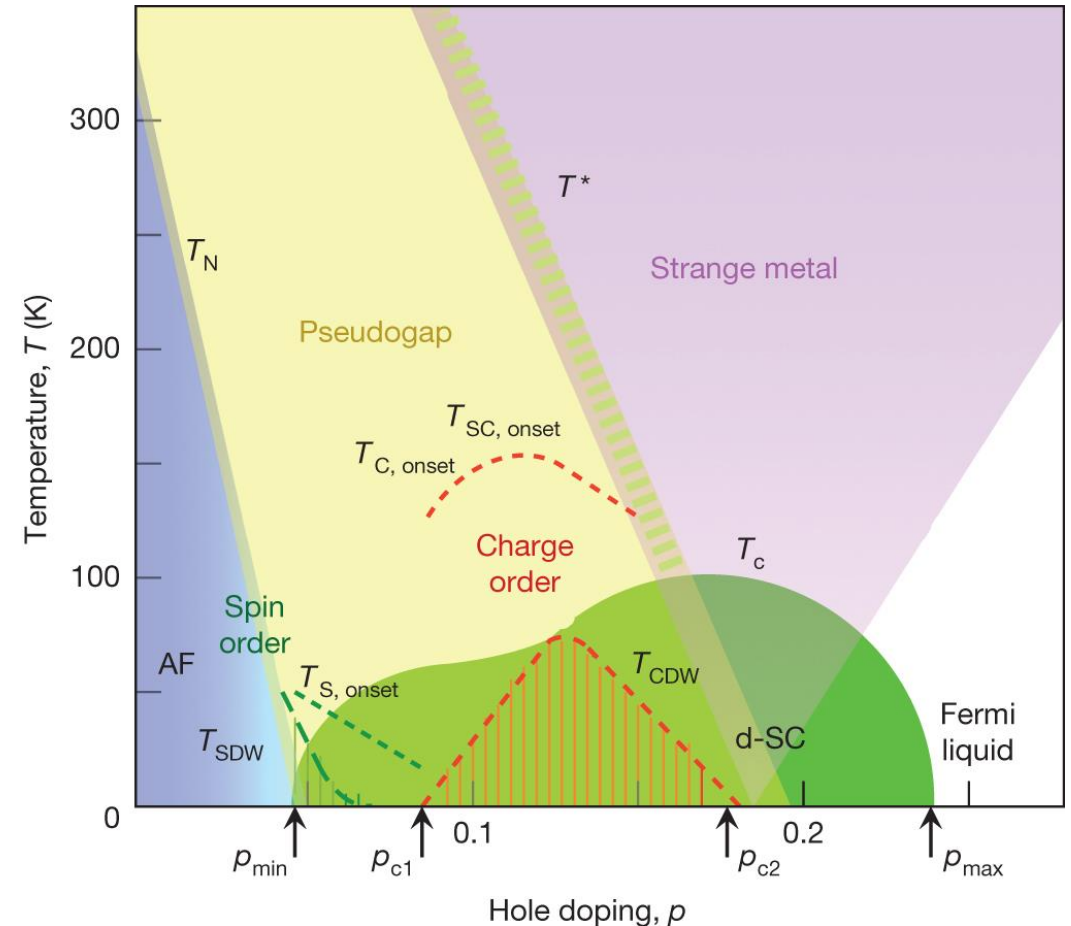
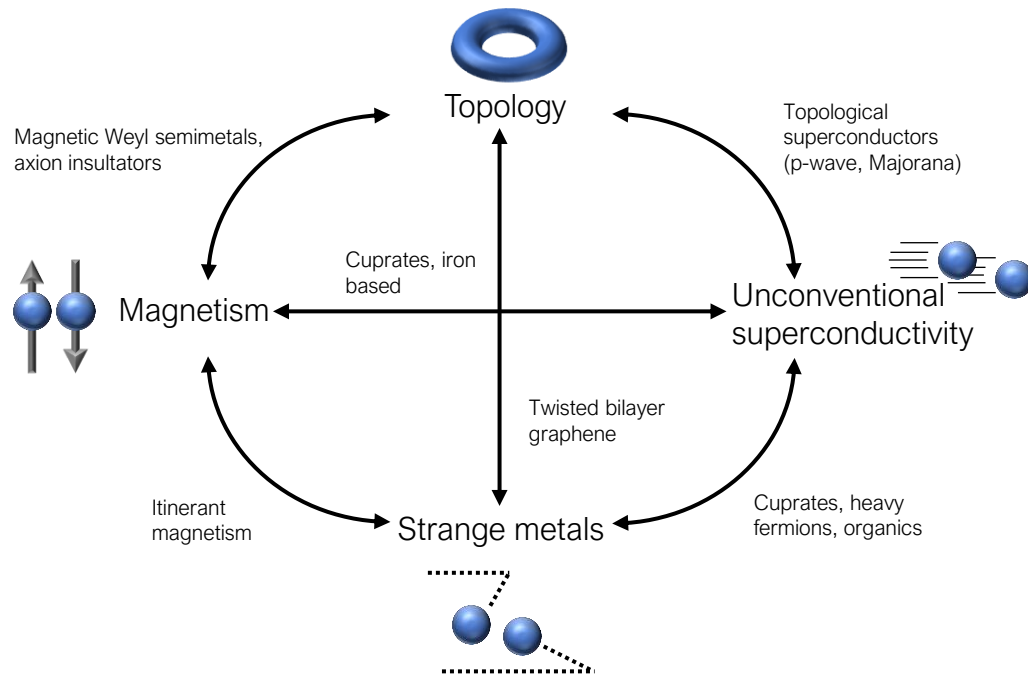
<sup>44</sup>Department of Physics, University of Michigan, Ann Arbor, MI 48109, USA

<sup>45</sup>Department of Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

<sup>46</sup>Department of Chemistry, University of California Berkeley, Berkeley, CA 94720, USA

[Alexandradinata&al., 2020](#)

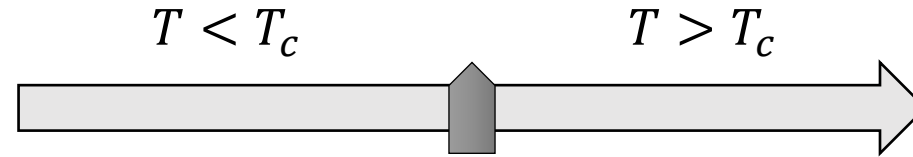
# Multiphaseted materials



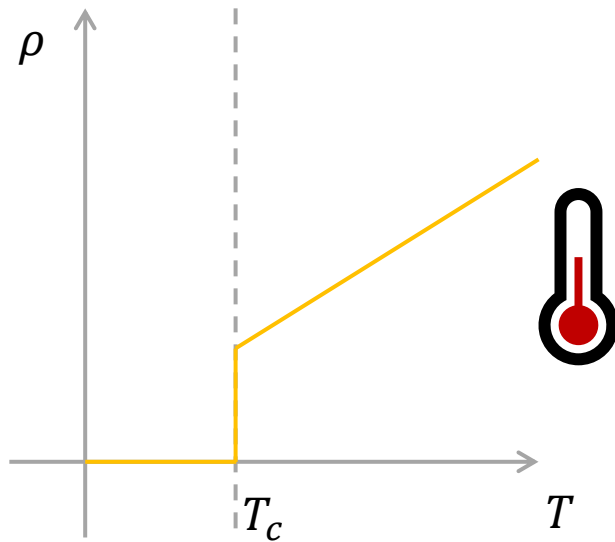
[Alexandradinata et al., 2020](#)

[Keimer et al., 2015](#)

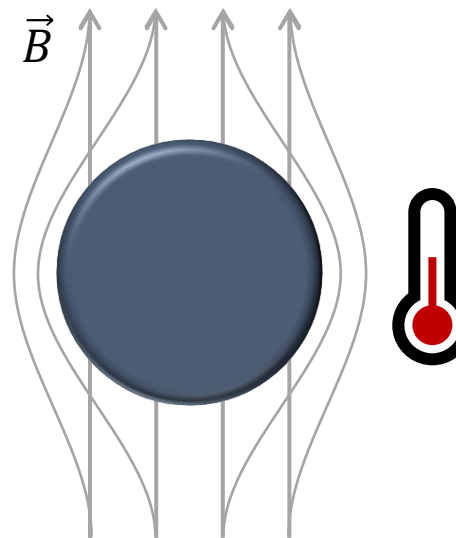
# The superconducting state



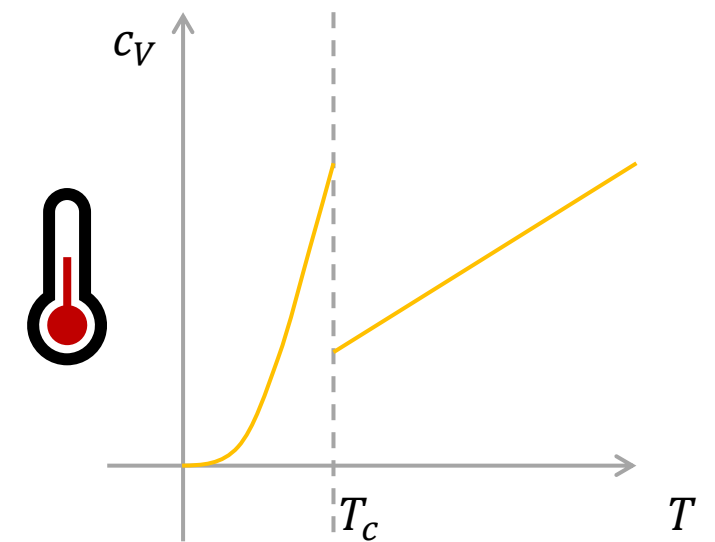
Breakdown of resistivity



Meissner effect



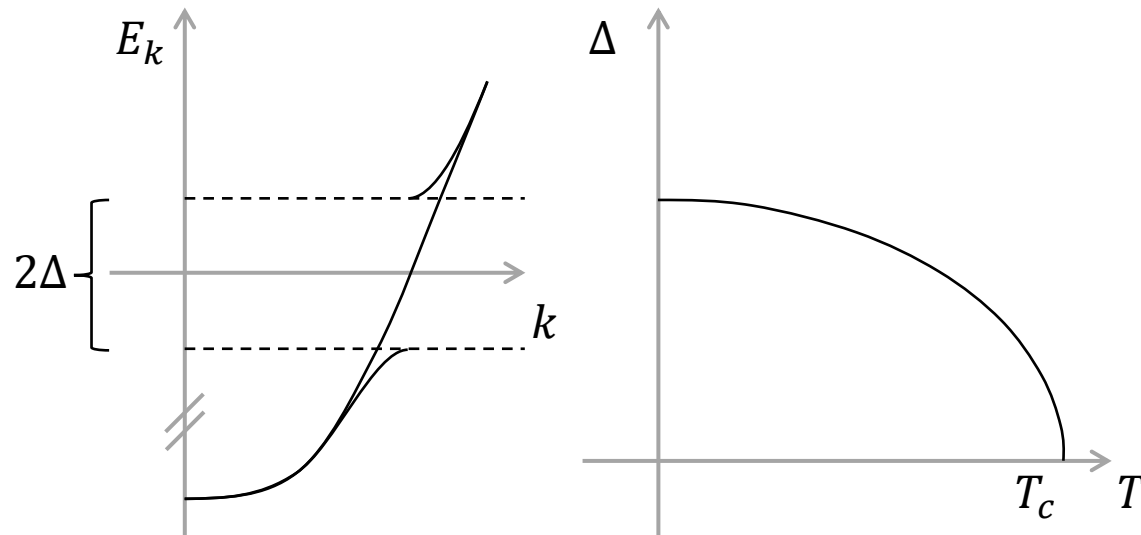
Discontinuity of specific heat



# The superconducting state

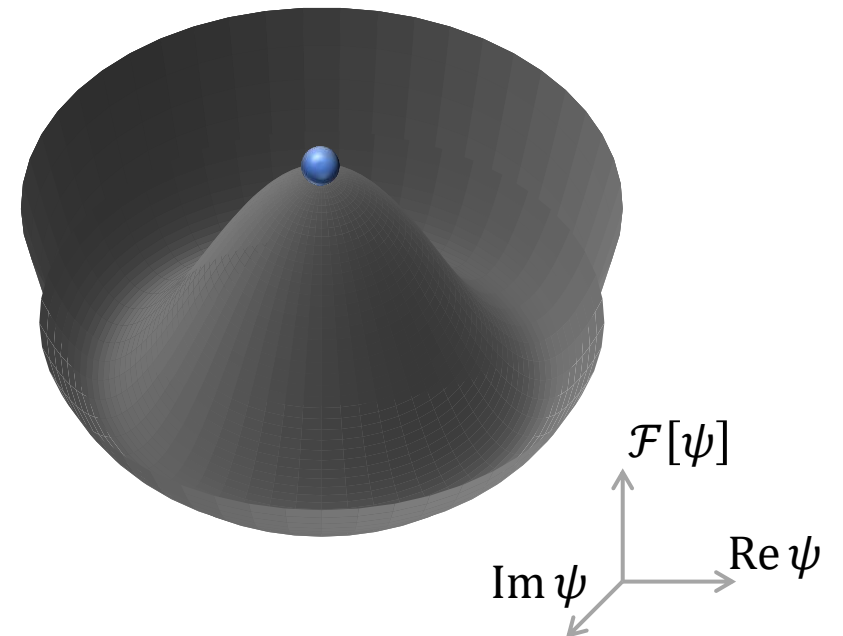
[Bardeen, Cooper&Schrieffer, 1957](#)

$$H = \sum_{k\sigma} \xi_k c_{k\sigma}^\dagger c_{k\sigma} - \sum_{kk'} V_{kk'} c_{k\uparrow}^\dagger c_{-k\downarrow}^\dagger c_{-k'\downarrow} c_{k'\uparrow}$$



Ginzburg&Landau, 1950

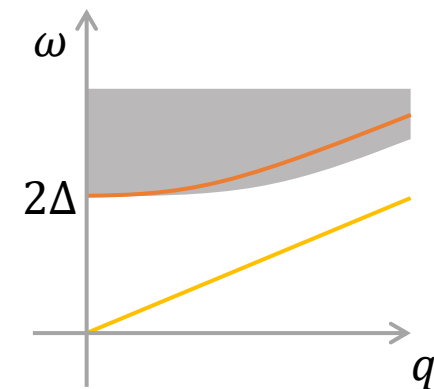
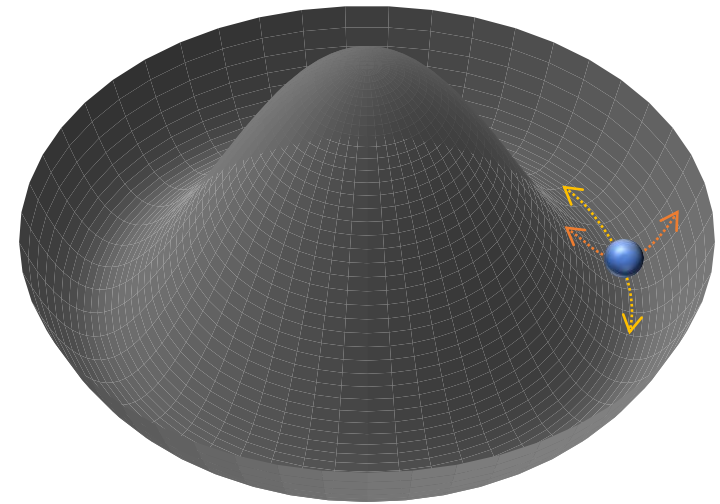
$$\mathcal{F}[\psi] = \mathcal{F}_n + \alpha(T - T_c)|\psi|^2 + \frac{\beta}{2}|\psi|^4$$



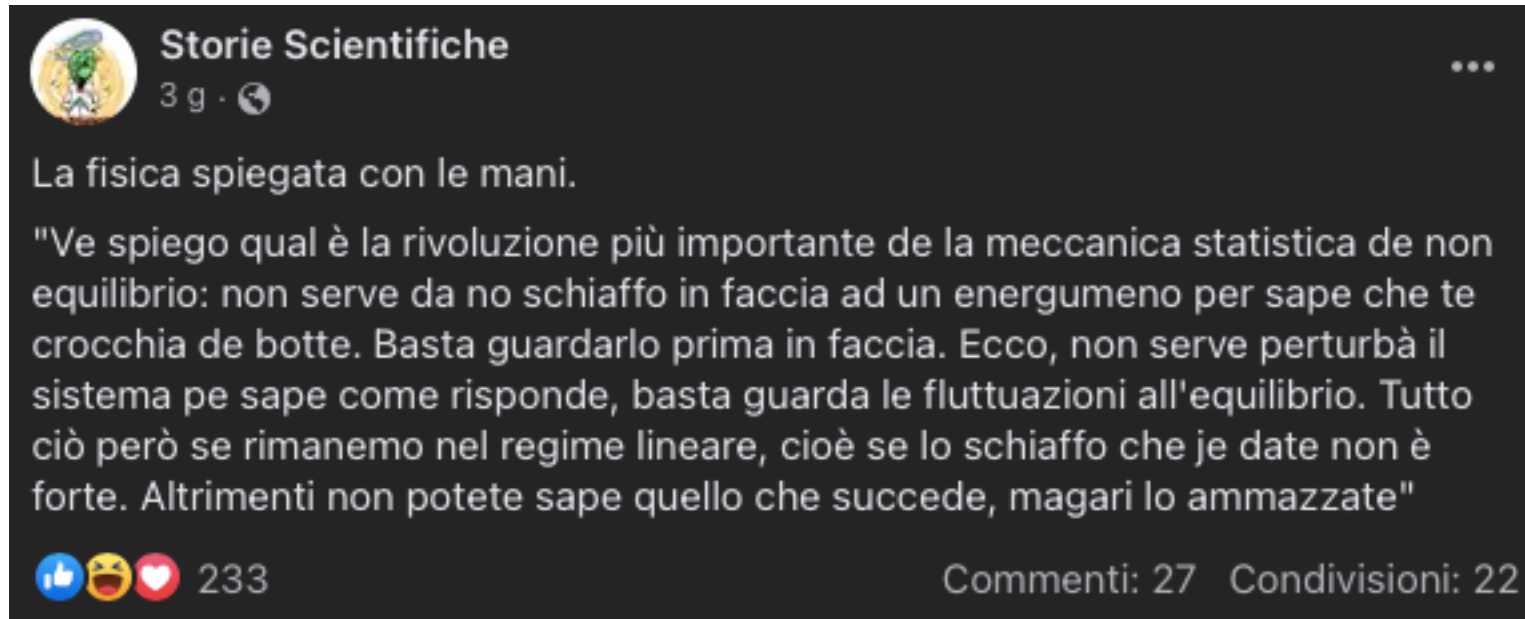


# Collective modes of superconductors

- Fluctuations of the complex order parameter  
$$\psi \rightarrow |\psi_0 + \delta\psi| e^{i(\theta_0 + \delta\theta)}$$
- $\delta\psi$  amplitude or Higgs fluctuations have mass  $2\Delta$
- $\delta\theta$  phase or Goldstone fluctuations are massless
- Do not miss the quasiparticle continuum!



# Probing collective modes...



A screenshot of a Facebook post from the page "Storie Scientifiche". The post features a profile picture of a globe with a tree growing on it, the name "Storie Scientifiche", and a timestamp of "3 g" with a globe icon. The main text of the post is in Italian and discusses the importance of statistical mechanics in non-equilibrium states. At the bottom of the post, there are icons for likes, reactions, and shares, along with the number "233". To the right of these icons, it says "Commenti: 27" and "Condivisioni: 22".

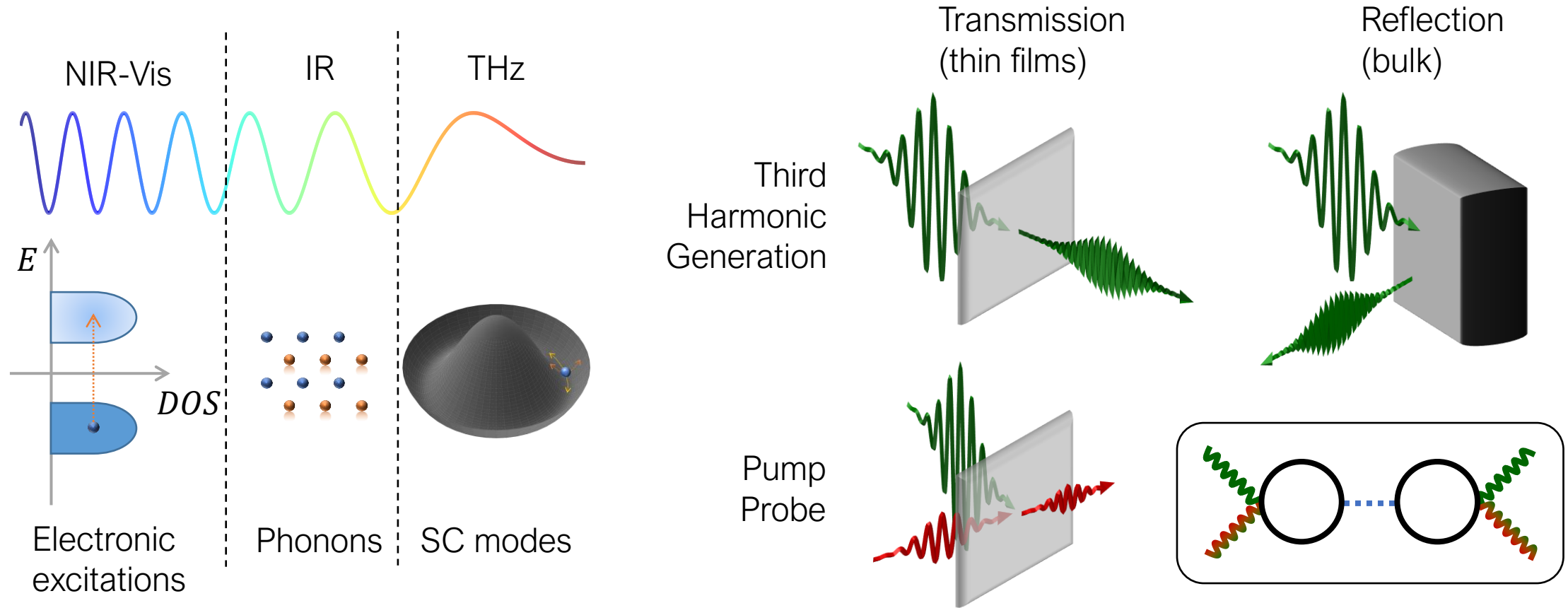
**Storie Scientifiche**  
3 g · 🌐

La fisica spiegata con le mani.

"Ve spiego qual è la rivoluzione più importante de la meccanica statistica de non equilibrio: non serve da no schiaffo in faccia ad un energumeno per sape che te crocchia de botte. Basta guardarlo prima in faccia. Ecco, non serve perturbà il sistema pe sape come risponde, basta guarda le fluttuazioni all'equilibrio. Tutto ciò però se rimanemo nel regime lineare, cioè se lo schiaffo che je date non è forte. Altrimenti non potete sape quello che succede, magari lo ammazzate"

👍 🤔 ❤️ 233      Commenti: 27    Condivisioni: 22

# Probing collective modes...



[Nicoletti&Cavalleri, 2016](#)

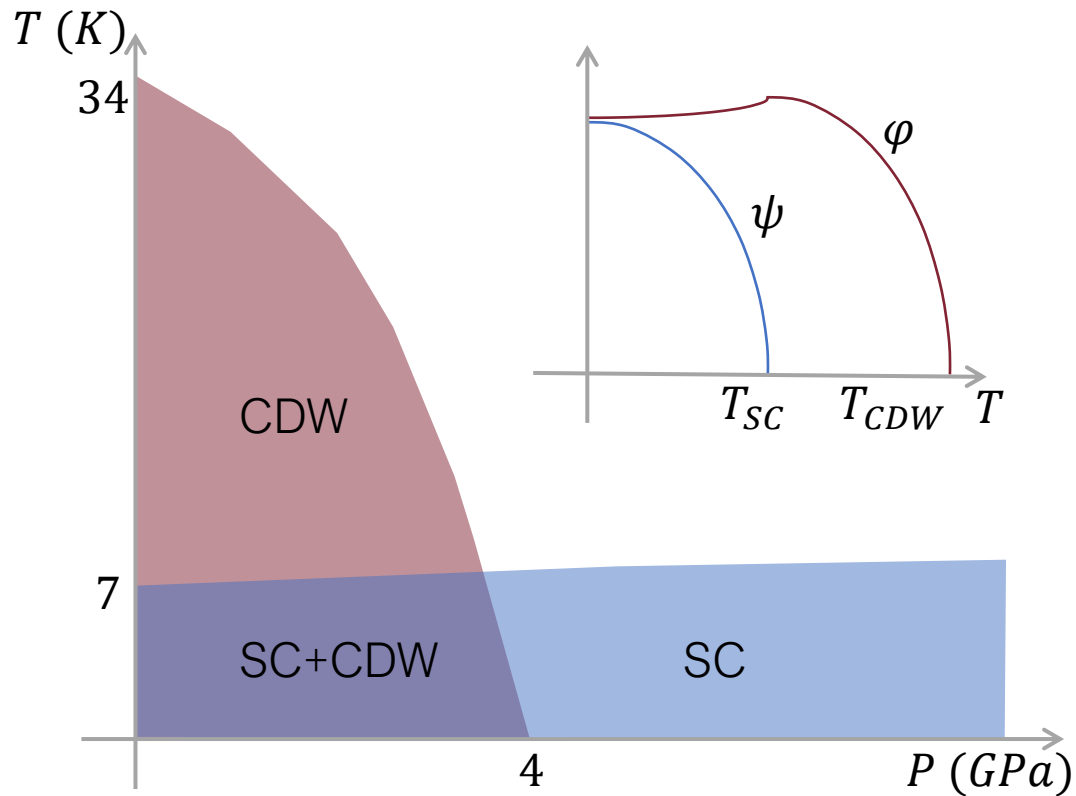
08/02/2023

More is differently different

[Udina&al., 2019/ Udina&al., 2022](#)

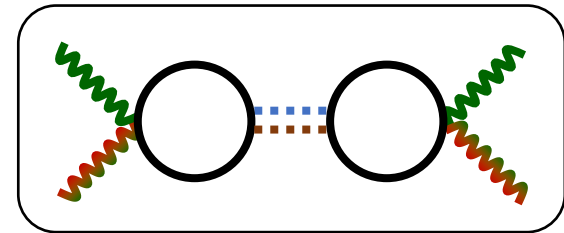
11

# An example: NbSe<sub>2</sub>



$$\mathcal{F}[\psi, \varphi] = \underbrace{-\alpha|\psi|^2 + \frac{\beta}{2}|\psi|^4}_{SC} - \underbrace{a|\varphi|^2 + \frac{b}{2}|\varphi|^4}_{CDW} + \underbrace{\lambda|\psi|^2|\varphi|^2}_{coupling} + \underbrace{\varepsilon A^2|\varphi|}_{driving}$$

$$\begin{cases} (\omega^2 - \omega_\psi^2)|\psi| + \lambda|\varphi| = 0 \\ (\omega^2 - \omega_\varphi^2)|\varphi| + \lambda|\psi| = \varepsilon A^2 \end{cases}$$



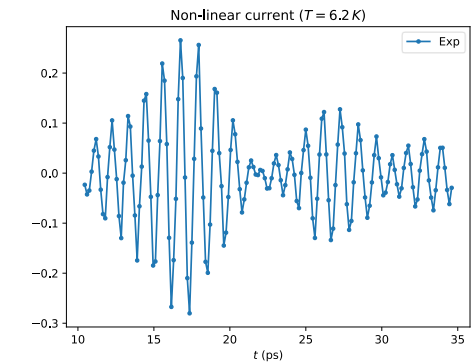
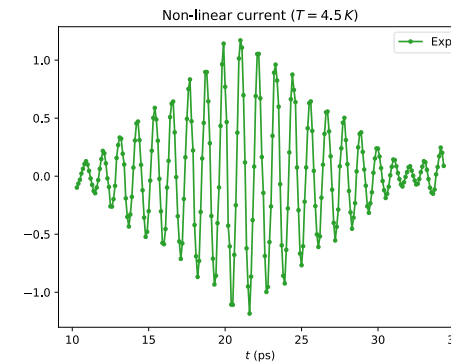
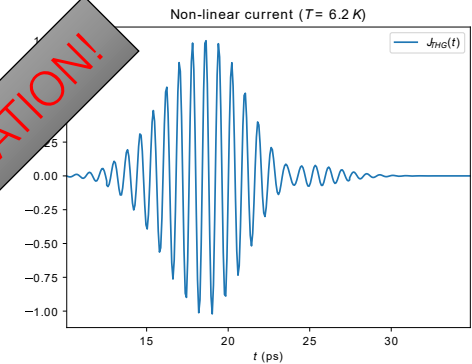
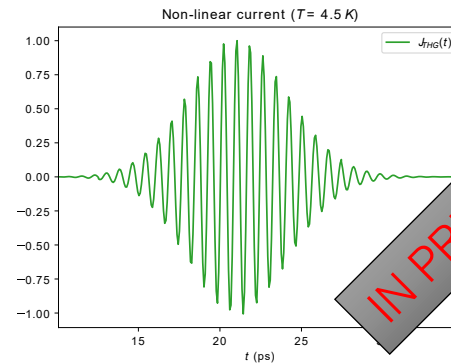
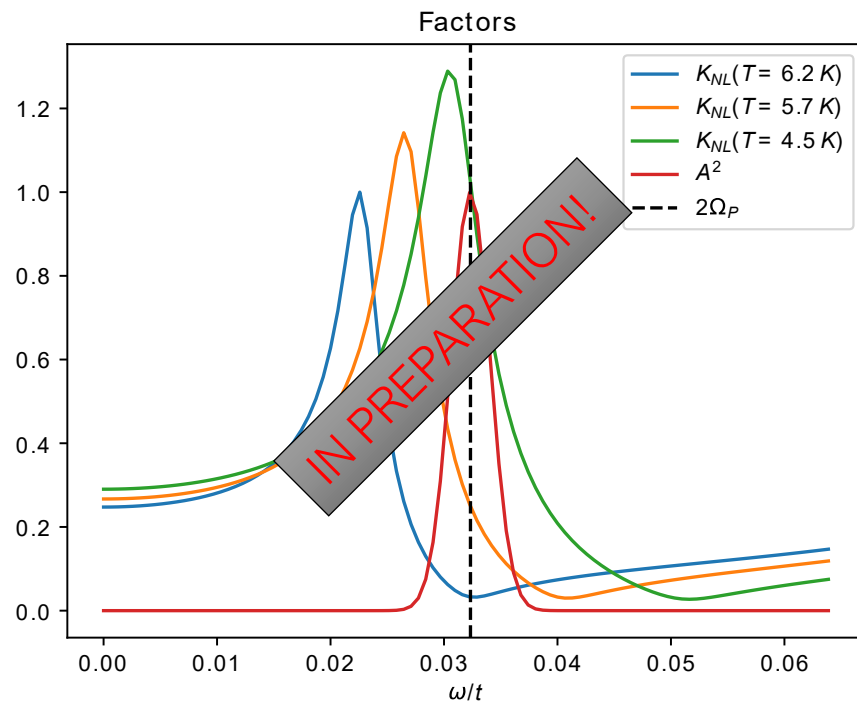
[Grasset&al., 2018/](#) [Cea&Benfatto, 2014](#)

# An example: NbSe<sub>2</sub>

$$\delta A_{pp} \propto \frac{\partial \mathcal{F}}{\partial \varepsilon} = \underbrace{\frac{(\omega^2 - \omega_\psi^2)}{(\omega^2 - \omega_1^2)(\omega^2 - \omega_2^2)}}_{K_{NL}} A^2$$

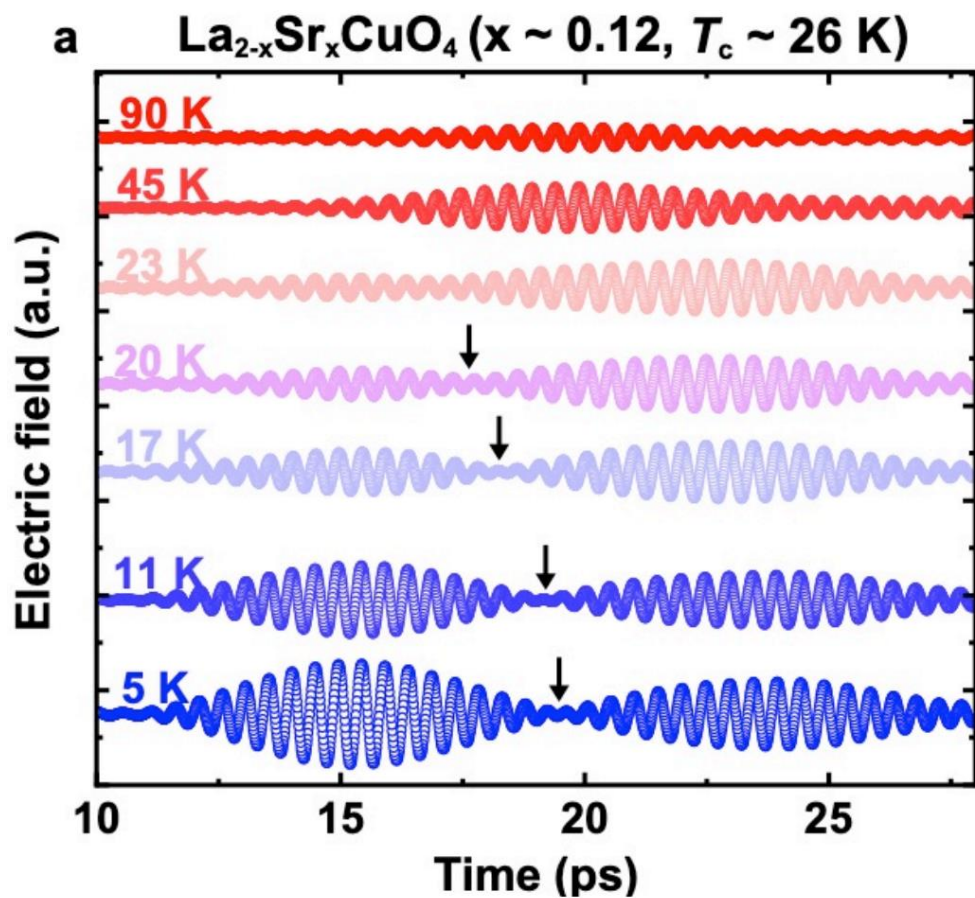
$$K_{NL} \propto \frac{1}{\omega^2 - \omega_1^2}$$

$$K_{NL} \propto \omega^2 - \omega_\psi^2$$

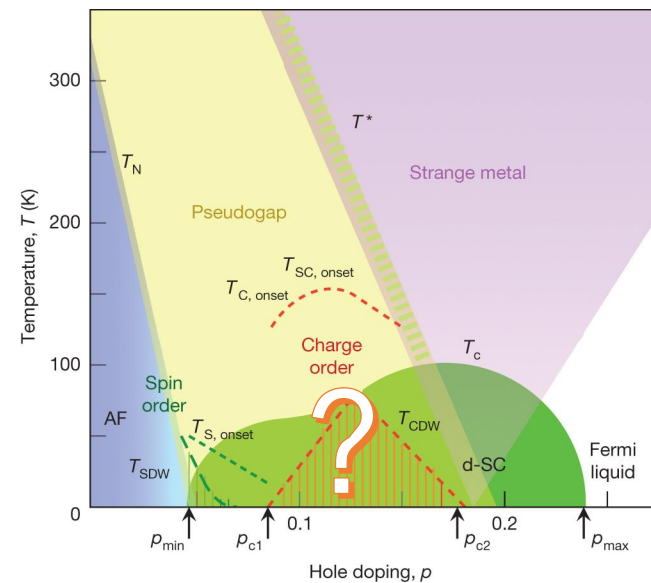


[Feng&al.,2022](#)

# Perspective: LSCO

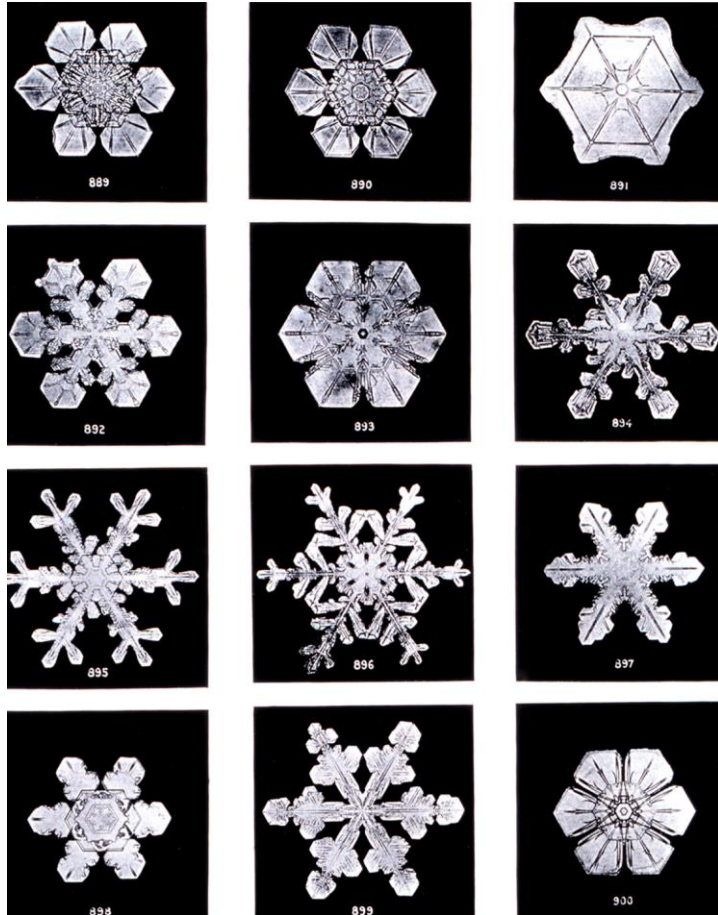


[Feng&al.,2022](#)

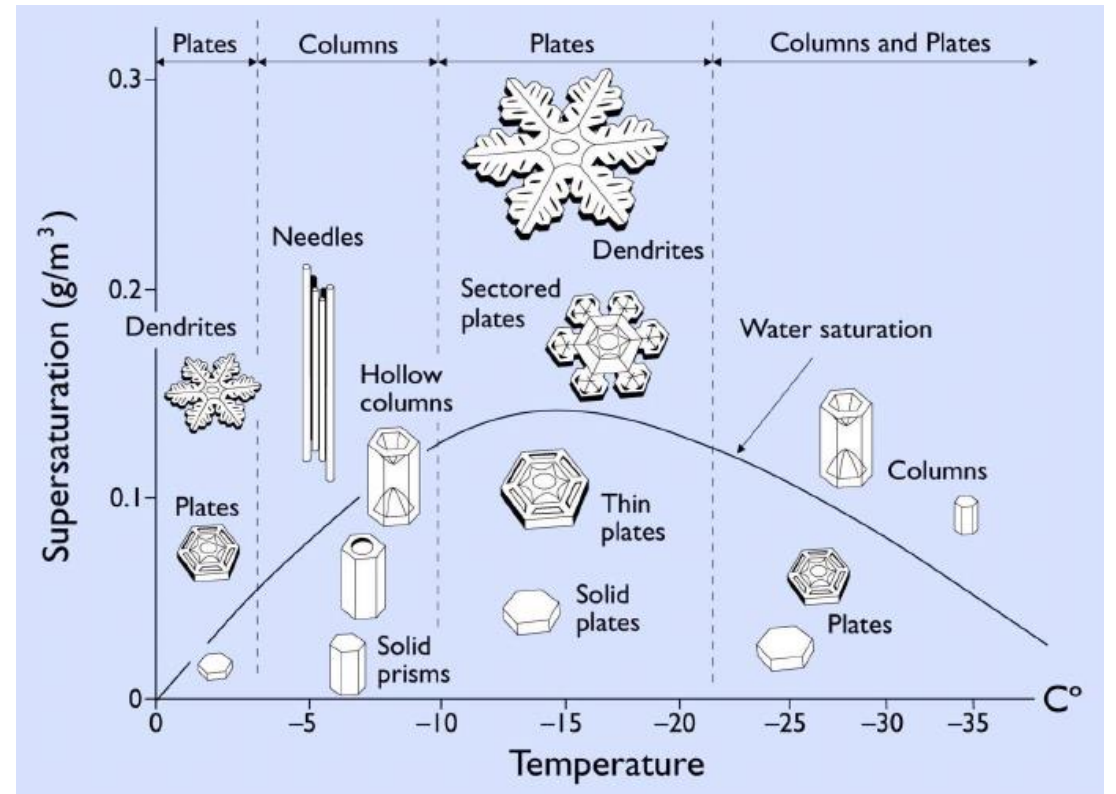




# Conclusion: same phase... different faces



[Bentley, 1902](#)



[Libbrecht, 2005](#)