

Gallex & GNO: the pioneering era of solar neutrino searches at LNGS

Neutrini e massimi sistemi – LNGS 22nd Febbraio 2023

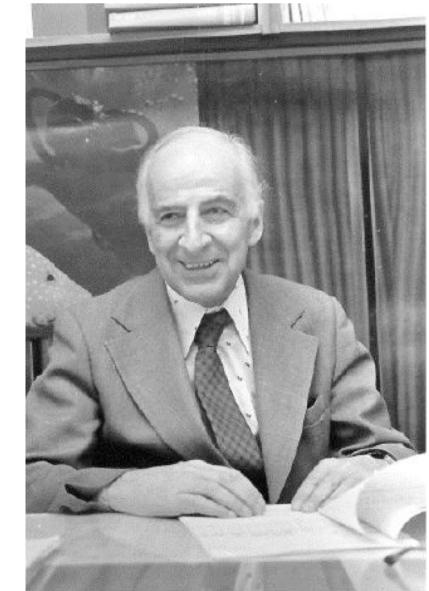
Carla Maria Cattadori

INFN Milano Bicocca



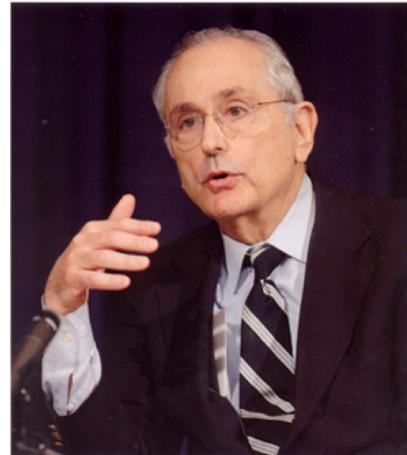
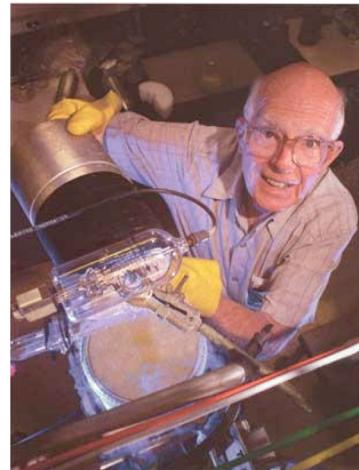
The prologue

- B.M. Pontecorvo - Chalk River Laboratories (1946)
 - Neutrino detection by CC interaction with ^{37}Cl and other nuclei by *Inverse β process*
- F. Reines (1956)
 - Discovery of ν_e by *Inverse β process*



(1918-1998)
1995 Nobel Prize
for the discovery
in 1956 of ν_e by
Inverse β process

(1914-2006)
2002 co-Nobel
Prize (M. Koshiba
and R. Giacconi)
for the first
detection of solar
neutrino



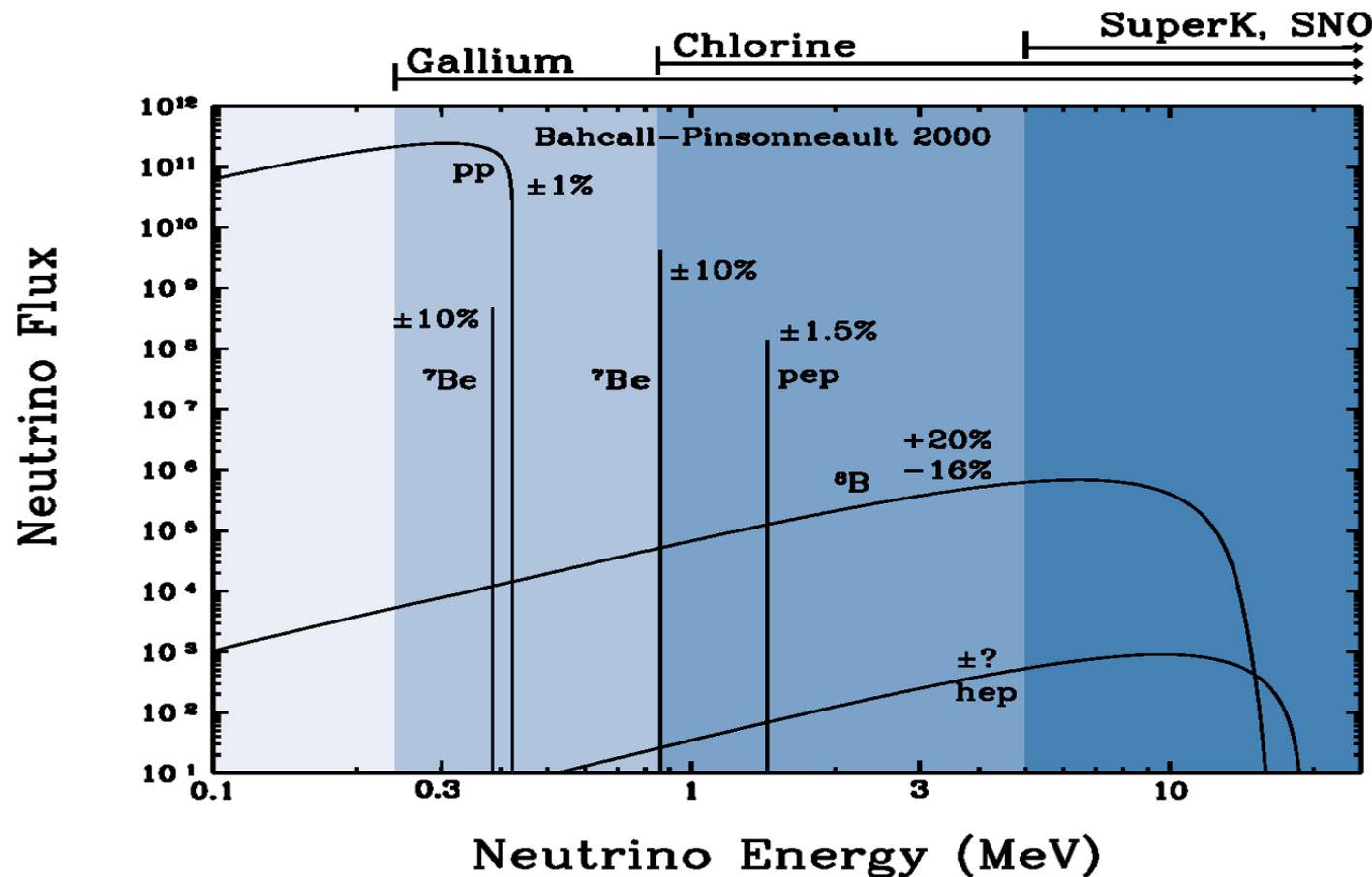
- R. Davis e J. Bahcall publish (Phys. Rev. Lett. – 1964) the feasibility study of a Cl exp.: $E_{thr} = 833 \text{ keV}$ - no access at the pp neutrinos.
- The BNL Department of Chemistry supports the project that get funded
- First solar run: 22 June - 14 October 1967
- **Measured Int. rate** (23 years): **2.56 (0.23) SNU** (8.2 SNU expected from SSM no oscillation). ?????

Birth of the Solar Neutrino Problem

What to do next?

- ❖ Is the lack of ν related to the Standard Solar Model (SSM) and/or its input parameters?
 - Measure the p-p ν flux, by far the more abundant, strictly related to L_{Sun} and almost model independent
 - Gallium → GALLEX e SAGE
- ❖ Is the lack of ν related to intrinsic ν properties (oscillation)?
 - Design an experiment to detect both the ν_e and other ν flavor
 - Deuterium → SNO

The SSM expectations



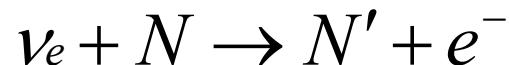
Chain	Flux [$\text{cm}^{-2} \text{ s}^{-1}$]	Flux Uncertainty	T dependence
pp	60 Billion	1%	T_c^{-1}
^7Be	5 Billion	10%	T_c^{18}
^8B	5 Million	C. Cattadori ~20%	T_c^{18}

1960-1980: The proposed radiochemical experiments

- ❖ In the URSS Markov e Zatzepin (e anche O. Ryashskaya)
Proposal to repeat the Cl experiment
- ❖ V. Kuzmin (1965) (URSS) proposes the Gallium
60 ton of metallic Ga will be installed at the Baksan Underground site
The experiment give the first results in 1990
- ❖ Negli USA, Bahcall, Cleveland, Davis....
50 ton of Ga in solution or in metallic form
Phys. Rev. Lett. 40(1978) 1351

Generalities on radiochemical experiments

- CC experiments sensitive only to ν_e . Proposed by Pontecorvo in 1946.



N' (unstable) is then separated from the target with physical-chemical techniques and then quantitatively measured observing its decay back in N .

$$Interaction\ Rate\ (R) = N_{target} \cdot \sum_i \int \sigma_i(E) \cdot \frac{d\Phi_i(E)}{dE} P(\nu_e \rightarrow \nu_e) dE$$

as

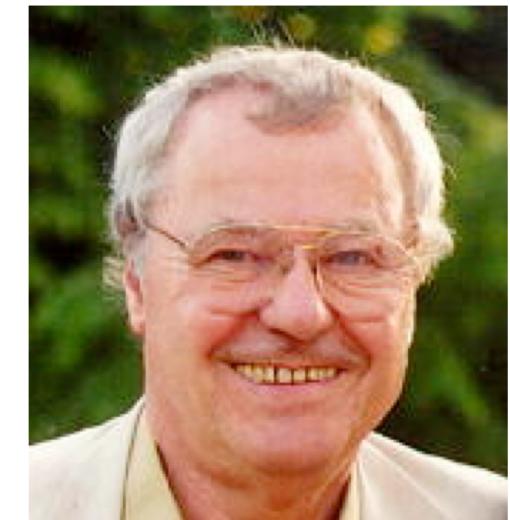
$$\sigma_i \sim 10^{-46} \text{ cm}^2; \Phi_i \sim 6 \times 10^{10} [\text{s cm}^2]^{-1}$$

1 Solar Neutrino Unit [SNU] = 1 ν interaction/sec each 10^{36} target atoms.

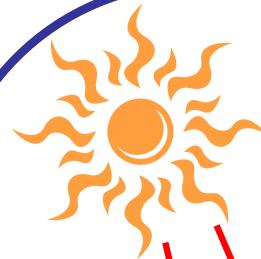
$N_{target} = 10^{29}\text{-}10^{30}$ nuclei, namely O(10-100) tons of target to have O(1) ν interaction/day

The GALLEX Collaboration

- Max Planck Institute – Heidelberg
- ZFK – Karlsruhe
- TUM Monaco
- LNGS
- Milano /Milano Bicocca
- Roma Tor Vergata
- Nice
- Saclay
- Weizmann Institute
- Brookhaven
- Kurciatov e CEA – Grenoble for the Cr source

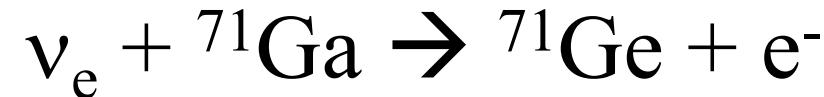
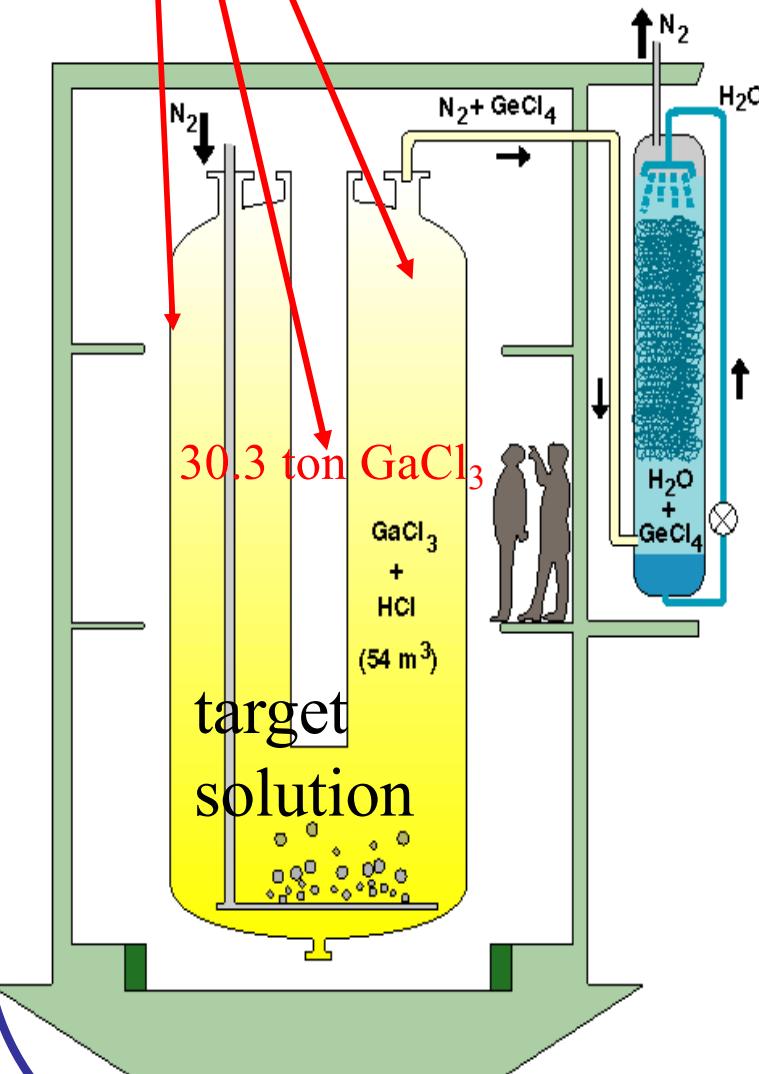


Till Kirsten the
GALLEX spokesperson



GNO/Gallex experiments

ν Radiochemical detector

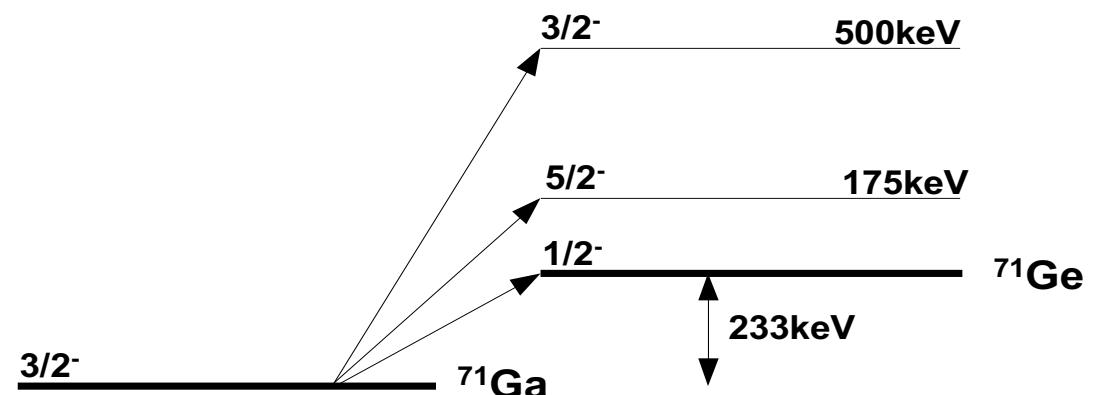


EC
(L/K)
detected

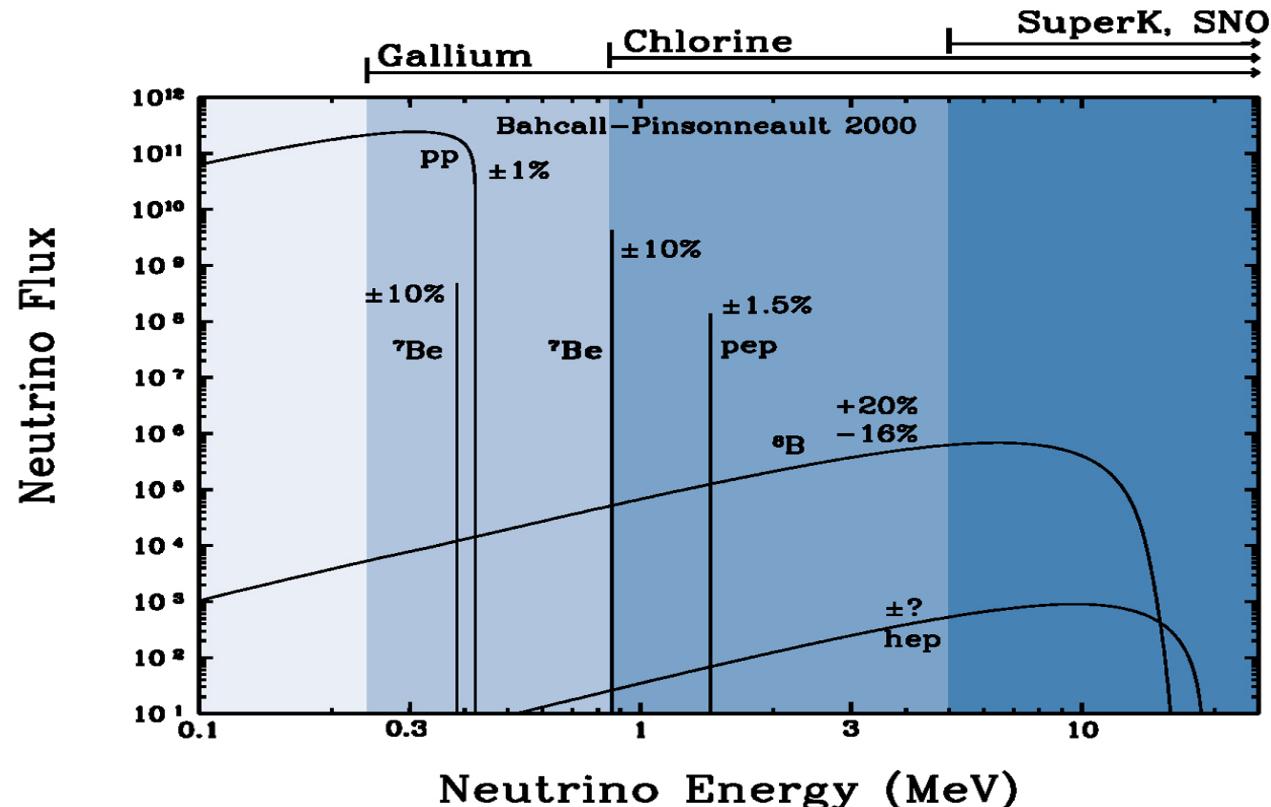
$\tau = 16.5\text{ d}$
 ${}^{71}\text{Ga}^*$

{ X rays
Auger electrons }

Threshold energy: 233 keV
Only sensitive to CC (ν_e)



GALLEX: Solar neutrinos sensitivity



SSM signal [SNU]:

pp+pep	73 (55 %)
hep	0.1
^7Be	35 (27 %)
CNO	8 (8 %)
^8B	13 (10 %)

Total: 129^{+9}_{-7} SNU

J. Bahcall *et al*, BP2000

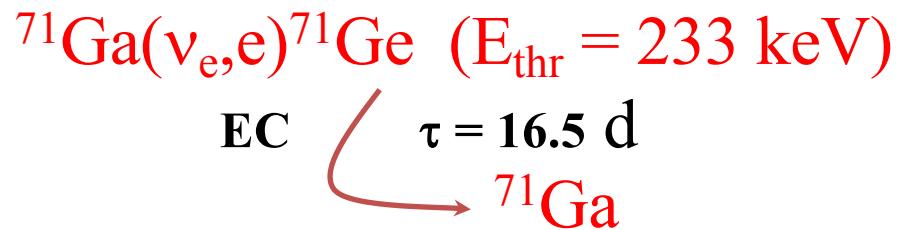
(≈ 1.2 captures/day)

1 Solar Neutrino Unit [SNU] = 1 ν int./sec each 10^{36} target atoms.

Expected signal: 1.2 ν captures per day, but due to decay during exposure + ineff., **9 ^{71}Ge decay detected per extraction** (28 days exposure)

The experiment

The ν_e interaction



The signal composition:
(BP00 SSM)

pp + pep	73 SNU	(55 %)
^7Be	35 SNU	(27 %)
CNO	8 SNU	(8 %)
$^{8\text{B}}$	13 SNU	(10 %)
Tot	129 SNU	$^{+9}_{-7} \text{ } 1\sigma$

The expected int.rate
(SSM)

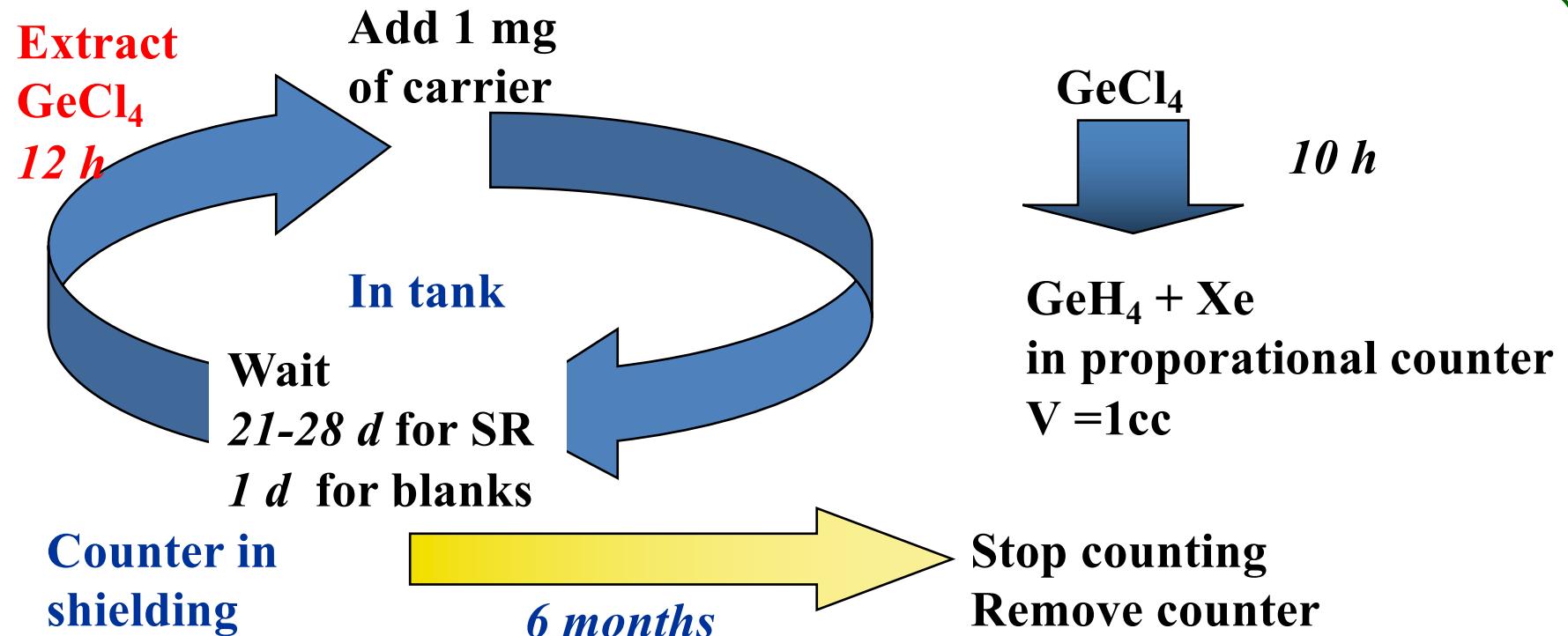
1.2 ν int. per day, but due to decay
during exposure + ineff., 9 ^{71}Ge decay
detected per extraction
(28 days exposure)

Extraction

N_2 Gas stripping of GeCl_4 (gas phase in acid environment) from 30.3 t of $\text{Ga}_3\text{Cl} + \text{HCl}$.
 $N = N_0 \exp(-f V_{\text{gas}}/V_{\text{sol}})$

The apparatus

See f.i. PL B490(2000)16
PL B314(1993)445



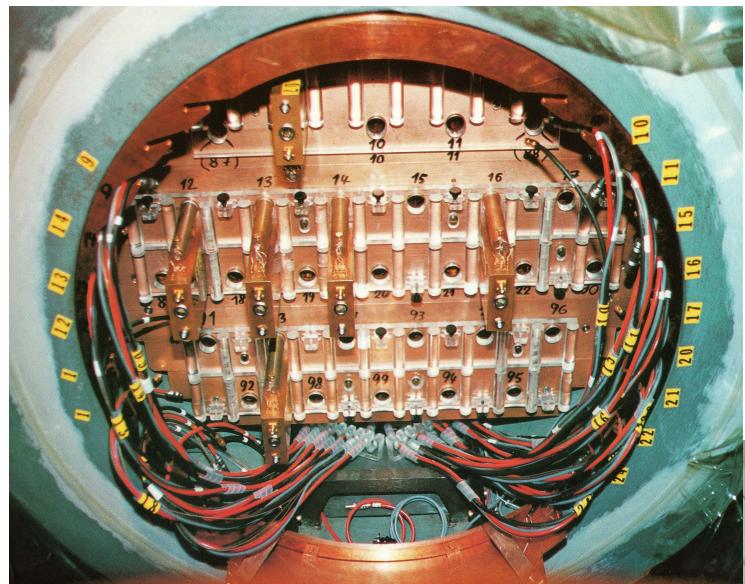
The preparation of the experimental site

- Digging of the containment pit
(to prevent environment & recover in case of leak from the Ga tank)
- Building construction (TOF outside) and Hall A
- Two tanks (one spare) for GaCl_3
- The extraction system
- The counting system (shielding tank+ cali system)
- The readout electronics





The GeH_4 synthesis and counter filling



The counter shielded box, the counting shield hosting counters



The proportional counter,



C. Cat

Relevant costs

- Gallium • 22M SF (**7 M SF**)
- Buildings • 1 M Euro
- Tanks & Chemistry • 1 M Euro
- Counter tanks& elect. • 0.5 M Euro

- Electronics 2 • 0.4 M Euro
- Cr source • 2.5 M Euro
- Running costs • ~ 0.15 M Euro/anno

GALLEX Start-up & Commissioning

- GaCl₃ received, weighted at TOF and then carried underground
- 1990: The first «cleaning» extraction
- Huge amount of Ge released daily:
ca. 100 atoms/day



- ⁶⁸Ge (cosmogenico) trapped in the solution
- Decision: warm up the tank
- Huge release of ⁶⁸Ge
- Back at room T the Ge daily release is greatly reduced
- 14/05/1991 → First solar neutrino run

NEUTRINO 92, Granada 7-12 June 1992

THE ν_Θ PP
FUSION
BOMB

*Summary
Talk*

*de Rujula
Conference
Summary Talk*

[DETONATED OVER
GRANADA BY
T. KIRSTEN
AT 6:15 P.M., JUNE 8th
1992]

Courtesy: Till Kirsten

The first GALLEX result @ Neutrino '92

- Interaction rate
 - Measured: **83.4 ± 19 SNU (stat) ± 8 SNU (syst)**
 - Expected from SSM: 129^{+9}_{-7} SNU
- Meas/SSM > 100 % of the pp- expectation
⇒ Hydrogen fusion in the Sun observed
- Meas/SSM ~ 60 % of the total SSM-expectation
⇒ Deficit of pp- and/or ${}^7\text{Be}$ -neutrinos observed
- Result marginally compatible with a SSM
- No claim of neutrino oscillations

The GALLEX chrono-history

1986 - 1990

Construction of the detector

May 1991 – May 1992

GALLEX I data taking
15 Solar runs, 5 Blanks

PL B285 (1992) 376
PL B285 (1992) 390

83.4 ± 19 SNU

Jun 1994 – Oct 1994

1st ^{51}Cr source experiment

PL B342 (1995) 440

Oct 1995 – Feb 1996

2nd source ^{51}Cr experiment

PL B420 (1998) 114

Feb. 1997

End of Solar Data Taking

PL B447 (1999) 127

GALLEX Final Result

1594 days – 65 runs: 77.5 ± 7.7 SNU

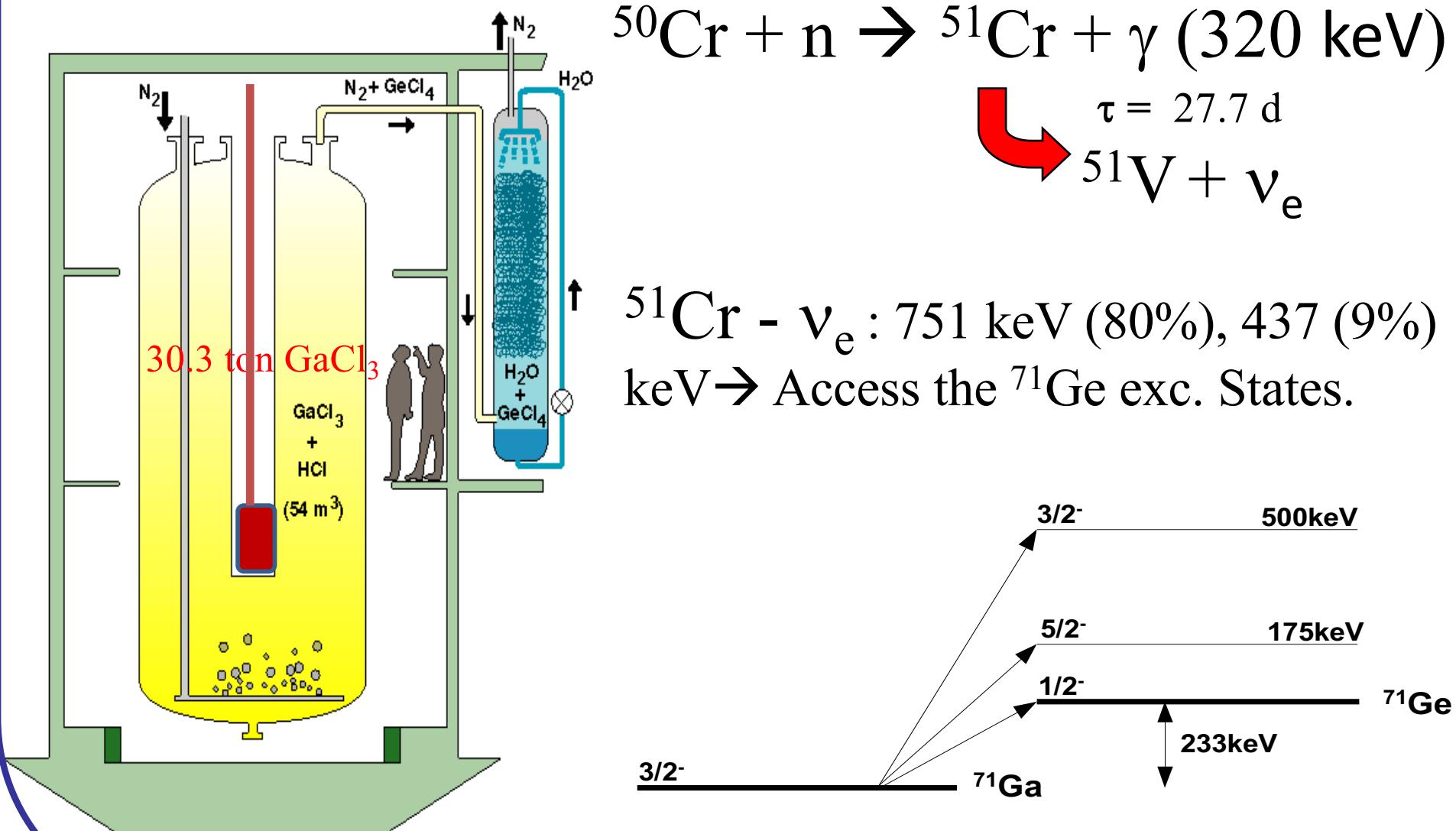
Feb 1997 – Apr 1997

Test of the detector with ^{71}As
Extraction efficiency 100%

PL B436 (1998) 158

The ^{51}Cr experiment

✓ Artificial source



^{51}Cr Source results

		Strength	63.4 PBq	69.1 PBq
500 keV	3/2-	R (meas/expt)	1.01	0.84
175 keV	5/2-		$\pm 11.5\%$	$\pm 11.5\%$
g.s. ^{71}Ge	1/2-	Average	0.93 ± 0.08	
		New c.ter eff.	0.91 ± 0.08	

Energy (keV)	^{51}Cr	^7Be
862	-	90%
751	80.6%	-
746	9.5%	-
431	8.8%	-
426	1.1%	-
384	-	10%

Arsenic test

Hot chemistry?



Study Ge chemistry in GaCl_3 env.: standing time, conc., extraction parameters etc.

$^{71}\text{As} \rightarrow (\beta^+ \text{ or EC}) \rightarrow ^{71}\text{Ge} \rightarrow ^{71}\text{Ga}$ ($Q_{\text{EC}} \approx 4 \text{ MeV}$)

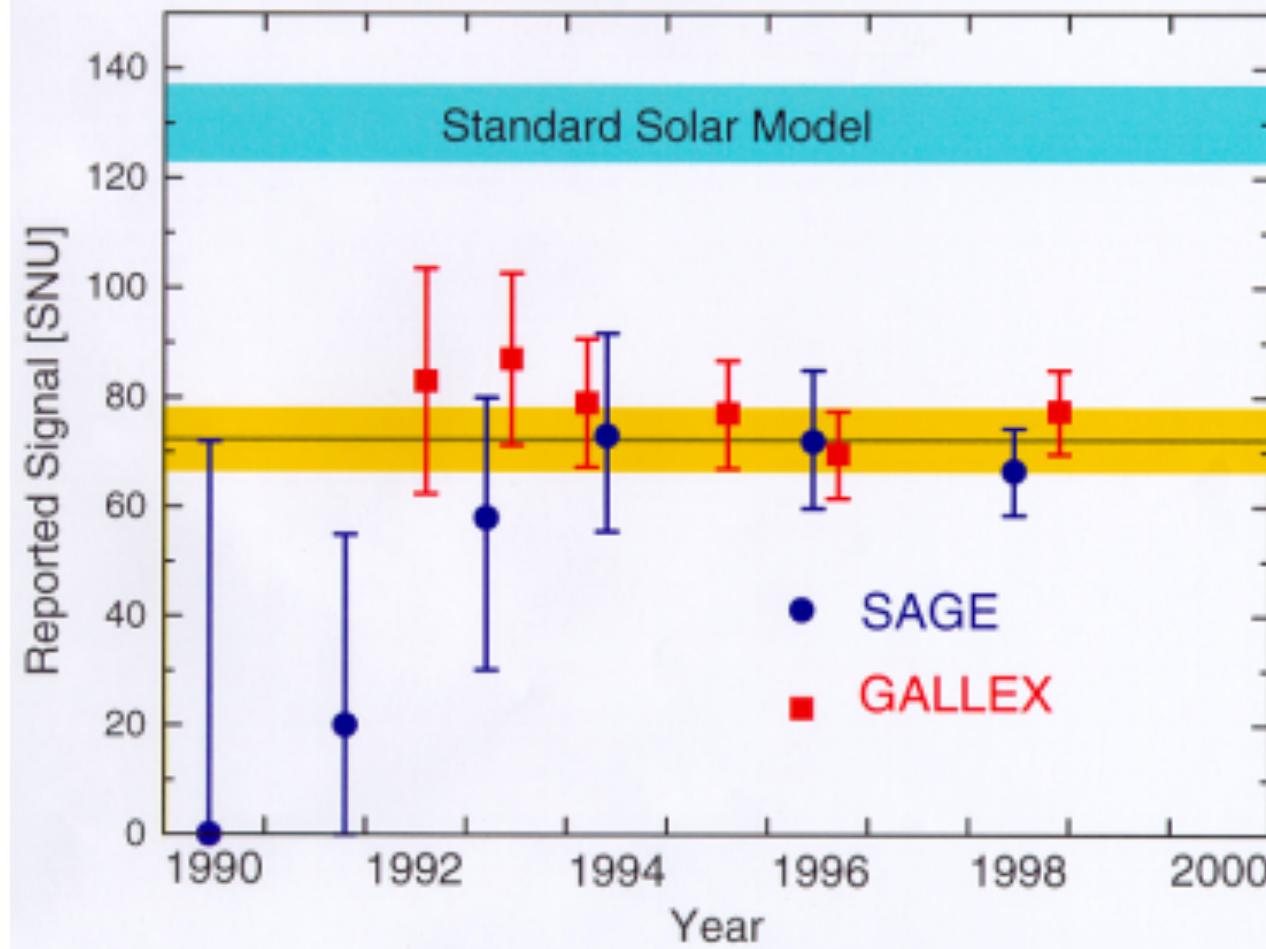
$\approx 10\ 000\ ^{71}\text{As}$ atoms added to three batches :

- Tank sample
- External sample
- Calibration sample (γ -spectrom.)

Result: Ge Extraction/recovery eff. $\sim 99\%$ (small error)

GALLEX Final Result

1594 days – 65 runs: 77.5 ± 7.7 SNU



GNO

Start of solar runs: **20 May 1998**

Three data releases
For a total of 1687 days

Rate 62.9 ± 6 SNU



Improvements

Many improvements resulting in a reduction of a factor of ≈ 2 in the systematic error

Item	Gallex	GNO
Target size	0.8%	0.8%
Chemical yield	2.0%	2.0%
Counting efficiency (active vol determination)	4.0%	2.2%
Pulse shape cuts	2.0%	1.3%*
Event sel. (others)	0.3%	0.6%
Side reactions	1.2 SNU	1.2 SNU
Rn-cut inefficiency	1.2 SNU	0.5 SNU
^{68}Ge contamination	+1.8 SNU -2.6 SNU	-

GALLEX

65 Solar runs = 1594 d

23 Blank runs

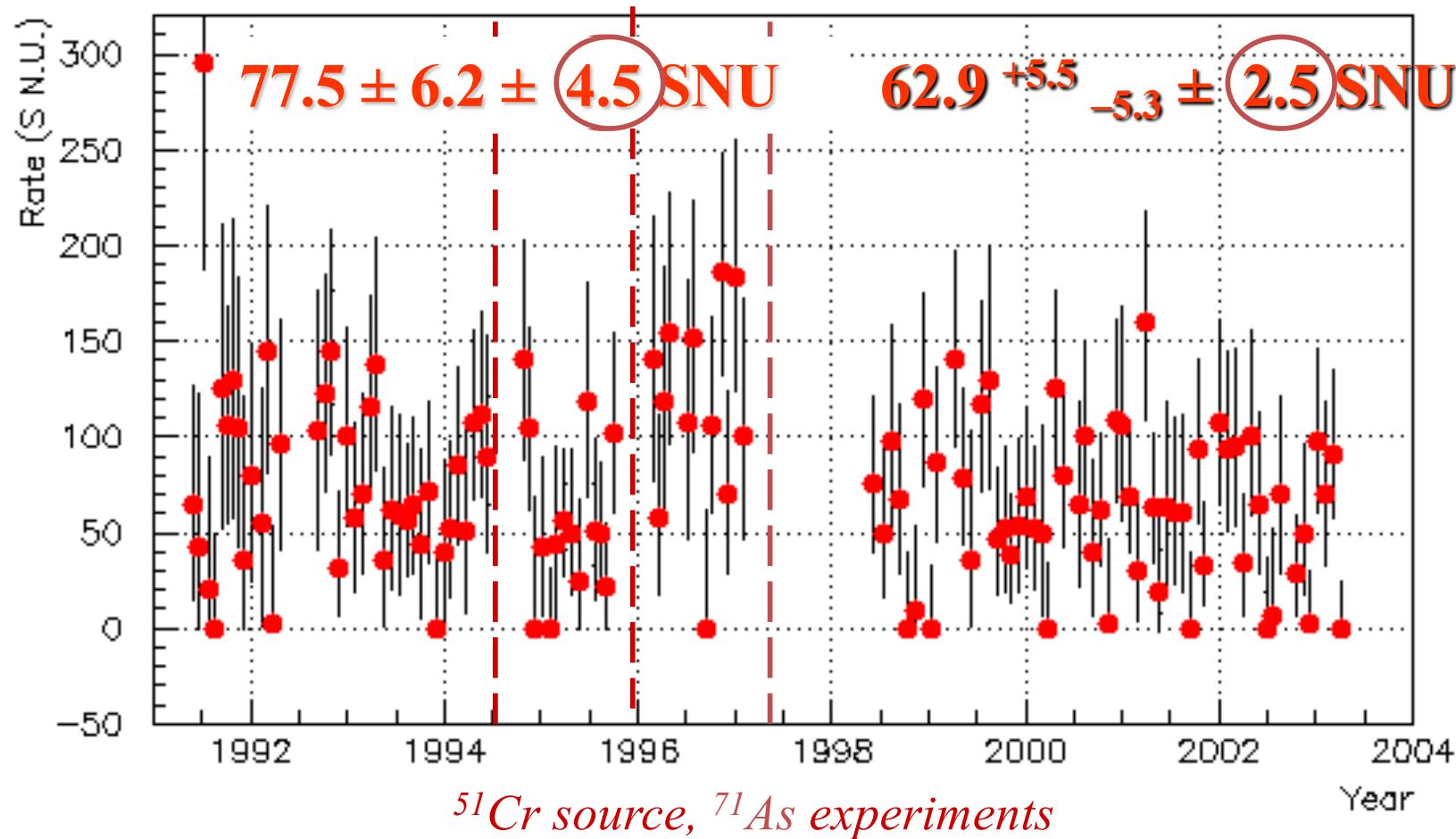
PL B447 (1999) 127

GNO

58 Solar runs = 1713 d

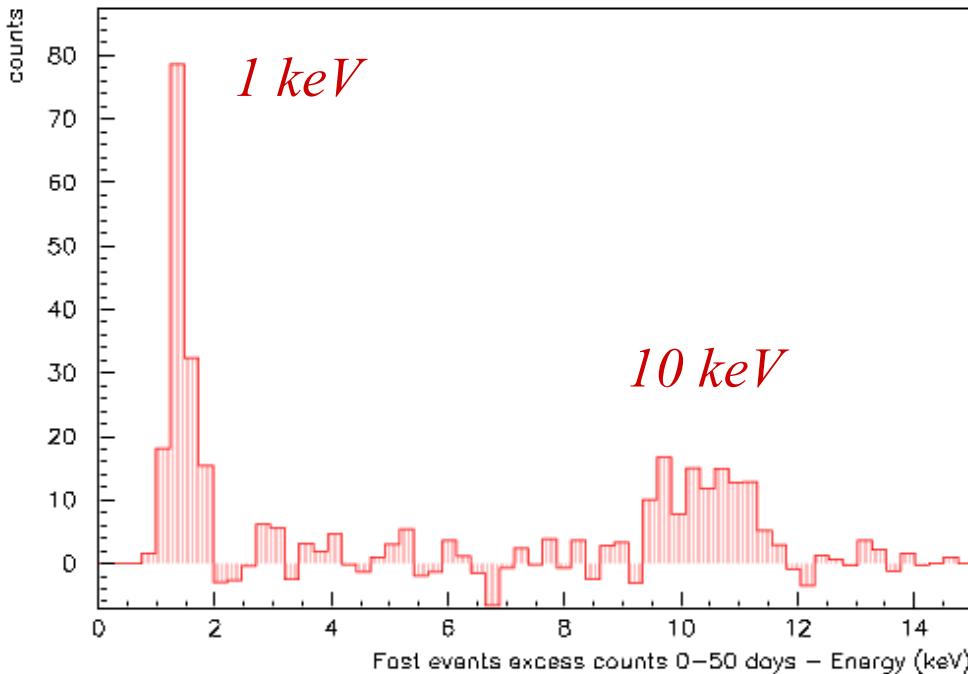
12 Blank runs

PL B 616 (2005) 174-190



Rate 69.3 ± 4.1 (stat.) ± 3.6 (syst.) SNU

The observed signal is validated by



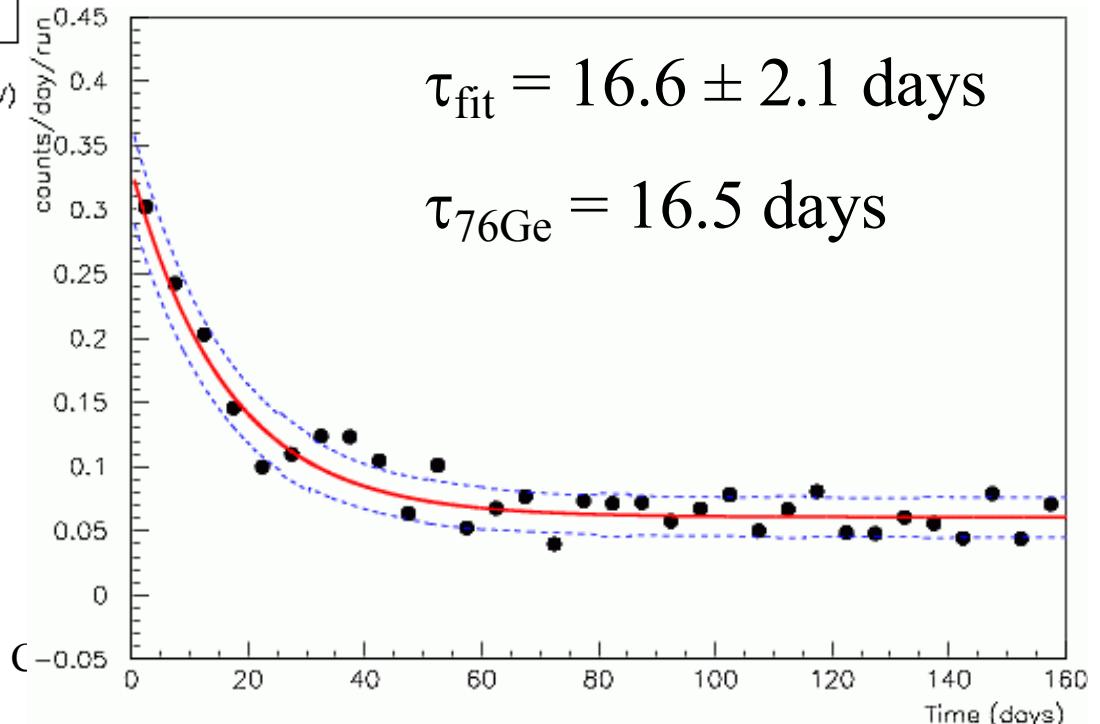
Event time distribution.

Analysis: M.L. analysis.

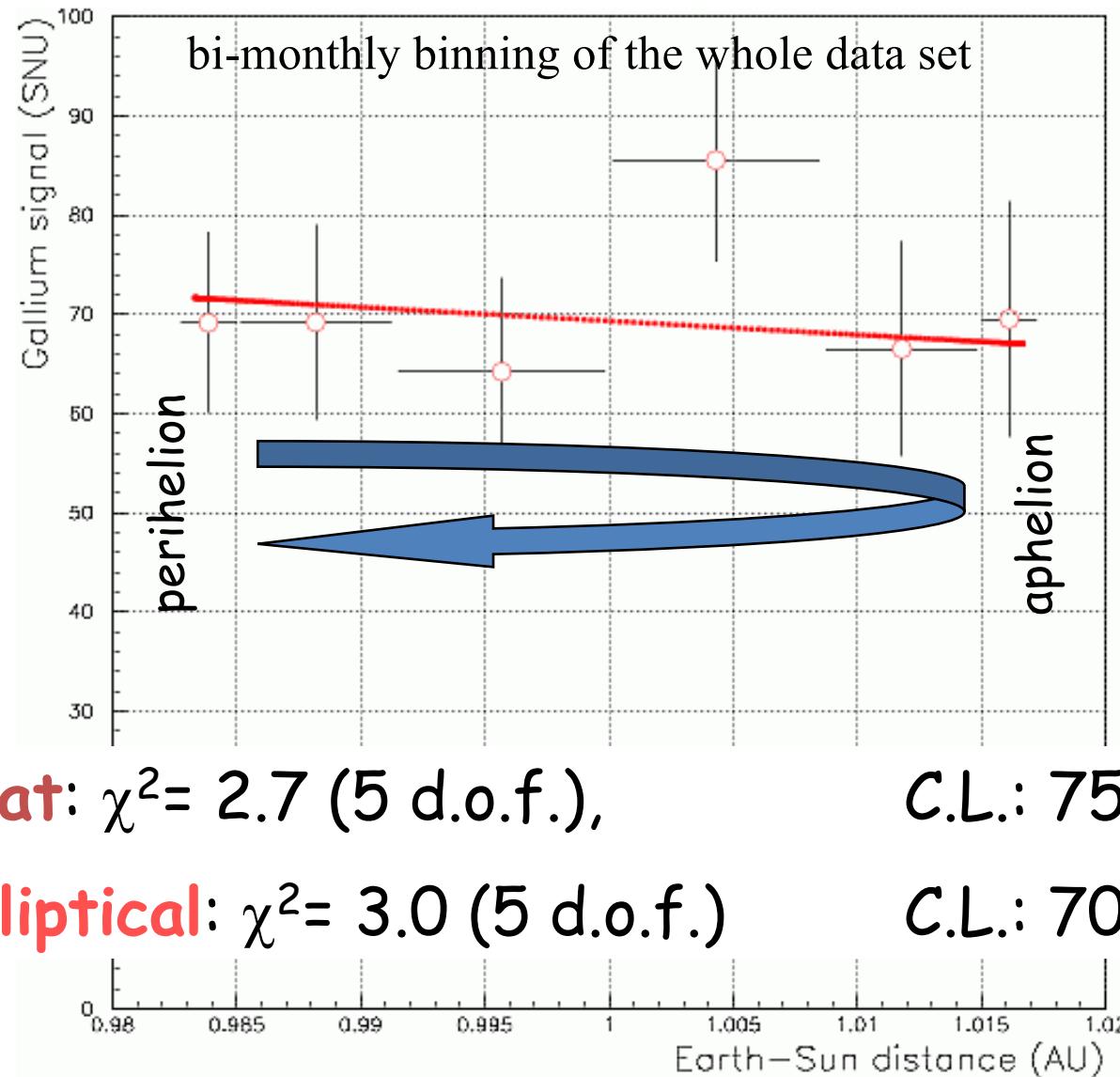
Null hypotheses: 1 decaying isotope + flat backgrd (independent /each run)

Event energy distribution

Important! No other peaks appear in the spectrum



GALLEX/GNO searches of seasonal variation



Gallium Experiments

	Data taking	N runs	Average Efficieny <i>Tank to counter</i>	Hot chem check	Source calib	R_{ex} [SNU]
GALLEX /GNO LNGS Italy	1991- 2003 stopped	123	97 %	^{71}As	Yes twice ^{51}Cr source	$69.3 \pm 4.1 \pm 3.6$ 5.9% 5.2% 69.3 ± 5.5
SAGE Baksan Kabardino Balkaria	1990- ongoing	121	90 %	No	Yes ^{51}Cr ^{37}Ar	$66.9 \pm 3.9 \pm 3.6$ 5.8% 5.2% $66.9^{+5.3}_{-5.0}$

Combined value

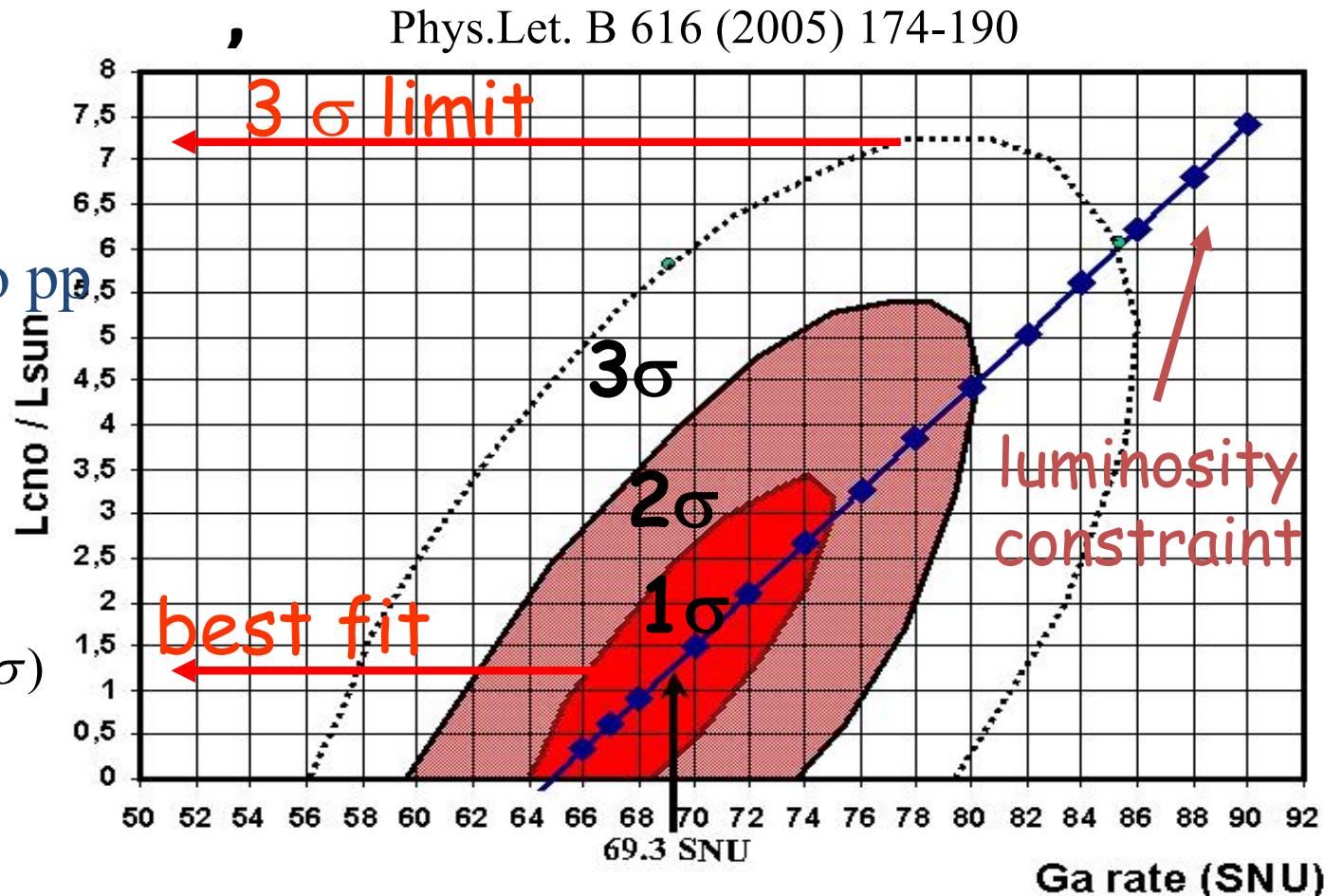
$68.1 \pm 3.75 (5.5\%)$

Constraining the CNO ν flux with Gallium data

- ${}^8\text{B}$ from SNO+SK
- ${}^7\text{Be}$ take from BP04
- pep strictly related to pp

$$\left[\frac{L_{\text{CNO}}}{L_{\text{Sun}}} \right]_{G+G} \leq 7\% \text{ (3}\sigma\text{)}$$

$$\left[\frac{L_{\text{CNO}}}{L_{\text{Sun}}} \right]_{\text{SAGE}+G+G} \leq 5 - 6 \% \text{ (3}\sigma\text{)}$$



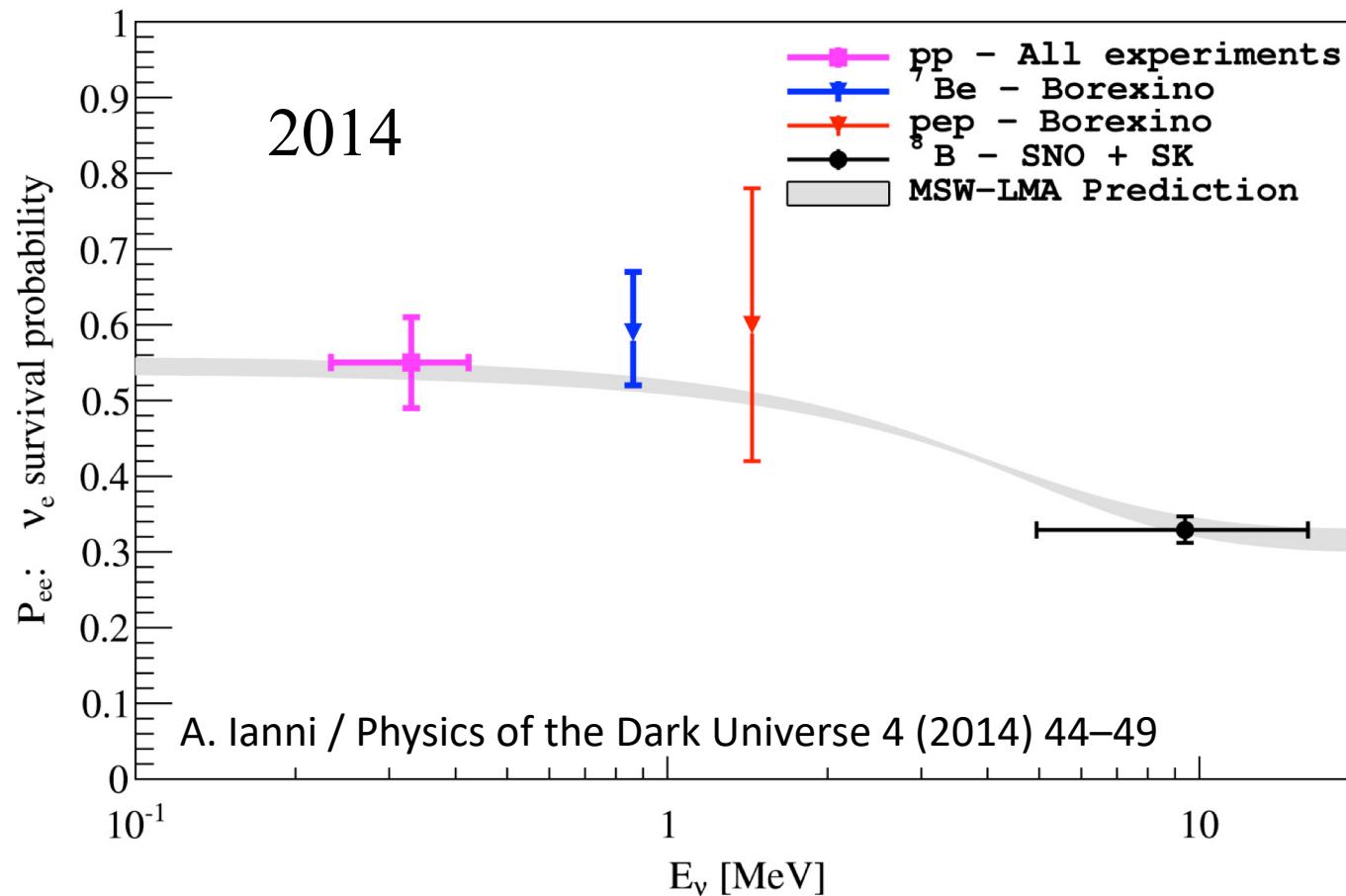
Important! The solar model N14 (Bahcall nomenclature) is used as reference, i.e. the CNO expectations take into account the reduced flux due to new $S_0({}^{14}\text{N}(p,\gamma){}^{15}\text{O})$ measurement

.....with the listed assumptions and from the Ga capture rate the pp ν_e flux is determined

R_{Ga}	Φ_{pp} [$10^9 \text{ cm}^{-2} \text{ s}^{-1}$]	$\Phi_{\text{pp}} /$ $\Phi_{\text{pp}}^{(\text{BP04+N14})}$
69.3 (G+G)	$59.9 (1 \pm 0.02 \pm 0.01_{\text{theo}})$	1.00(2)
68.1 (G+G+S)	$58.8 (1 \pm 0.02)$	0.98(4)

Fantastic agreement !!

Ga results confirm/constrain the ν_e survival probability at low energies



Survival probability for solar ν_e using the low-Z SSM.
The LMA-MSW prediction corresponds to 1σ band

Conclusions

- Gallium experiments confirmed the thermonuclear origin of the solar energy
- The dominant cycle is the pp
- The CNO and the Be contribution are properly described by the SSM
- ν oscillation are confirmed at sub-Mev energies (small matter effect at low energies) by solar models and neutrino oscillation mechanism
- No time modulations (seasonal, monthly, bimonthly, yearly) observed. No sensitivity
- Gallium experiments have been calibrated with high intensity neutrino sources. Hot chemistry effects have been excluded.

Technological results

- Few atoms chemistry
- Low level counting techniques
- Intense neutrino sources production (intensity calibration, know-how to produce and manipulate safely etc..)
- Radiochemistry techniques
- Radon counting and quantitative determination at level of few atoms.
- Ultra-low activity miniaturized proportional counters

In memoriam

- Luciano Paoluzi
2002
- Burkhard Freudiger
05.09.2005
- Dario Motta
2005
- Michael Altmann
31.07.2006
- Nicola Ferrari
31.07.2006
- Keith Rowley
29.10.2006
- Evry Schatzman
25.04.2010
- Israel Dostrovsky
28.09.2010
- Rudolf Mößbauer
14.11.2011
- Silio d'Angelo
02.02.2015

In memoriam



Enrico (Puccio) Bellotti
11 Settembre 2021



BACKUP

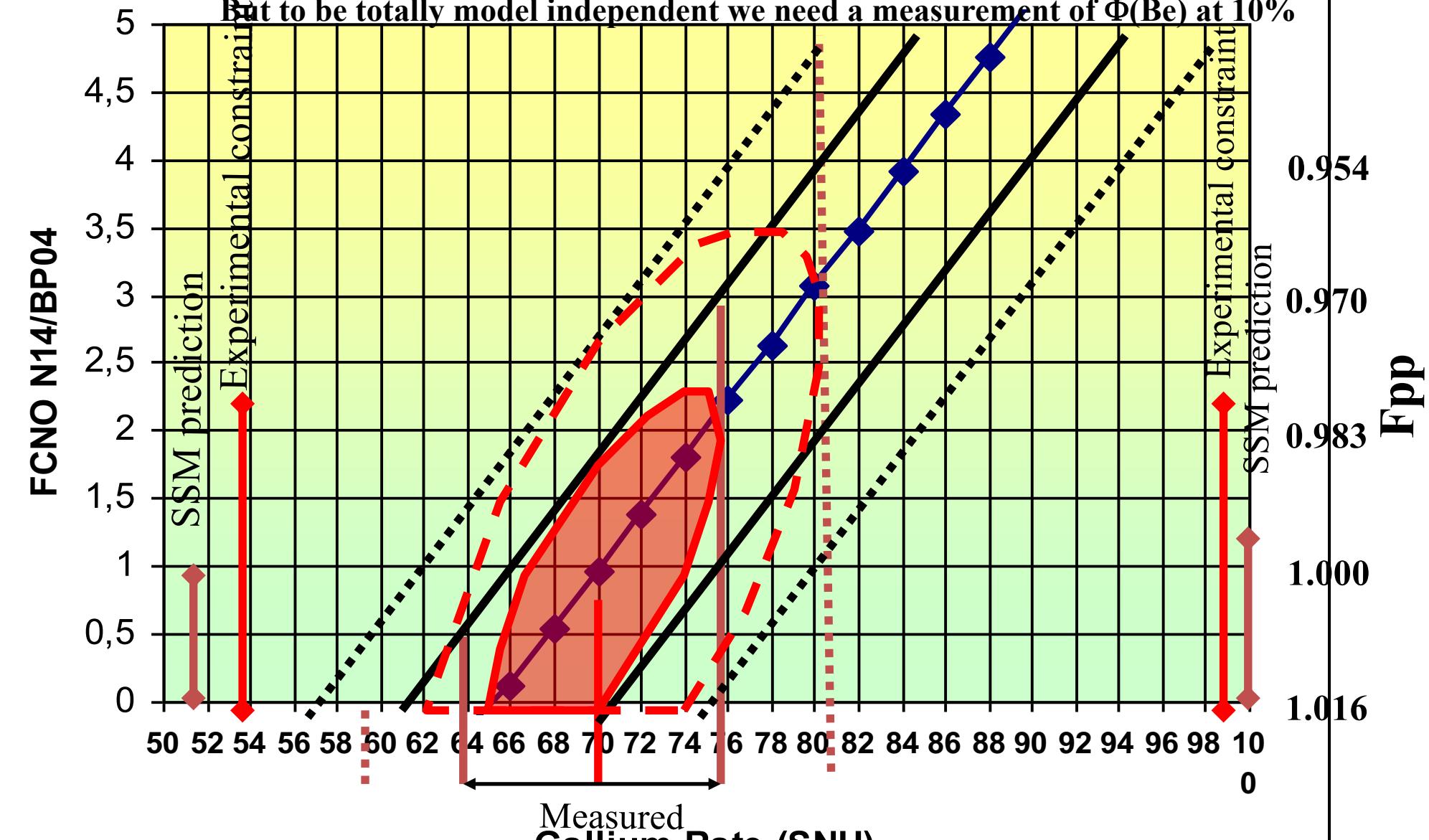
GALLEX/GNO - all uncertainties

Comments: perfect agreement of Ga rate with SSM + oscillation scenario

$\Phi(pp)$ probed at 2% level (1 sigma)

$\Phi(CNO) < 3.5$ SSM (2 sigma)

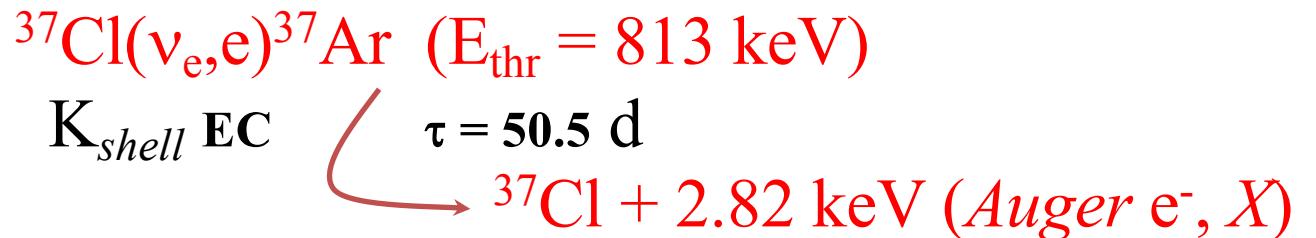
But to be totally model independent we need a measurement of $\Phi(Be)$ at 10%





The Pioneer: Chlorine Experiment

The interaction



ν Signal Composition:
(BP04+N14 SSM+ ν osc)

pep+hep	0.15 SNU	(4.6%)
⁷ Be	0.65 SNU	(20.0%)
⁸ B	2.30 SNU	(71.0%)
CNO	0.13 SNU	(4.0%)
Tot	3.23 SNU	± 0.68 1σ

Expected Signal
(BP04 + N14)

8.2 SNU $+1.8_{-1.8}$ 1σ

Results of Chlorine experiment

1. First measurement of solar neutrino interaction rate
2. Raised the problem of missing neutrinos
3. Opened a field of research that is not yet closed. Davis awarded in 2002, with the Nobel prize together with Koshiba and R. Giacconi

“for pioneering contributions to astrophysics, in particular for the detection of cosmic neutrinos”

$$\begin{aligned} \mathbf{R} &= \mathbf{2.56 \pm 0.16 \pm 0.16 \text{ SNU}} \\ &= \mathbf{2.56 \pm 0.23} \end{aligned}$$

Constancy of the solar neutrino flux (over 23 years): no correlation has been found between $R_{\nu^{\text{Sun}}}$ and the solar cycle (many speculation on this item in the ‘90)

Generalities on radiochemical experiments

Nowadays, in the neutrino community, radiochemical experiment are considered like *turtles* (“protected” ancient animals):

- they are slow, low statistic experiment
- they are sensitive only to ν_e
- they measure only one quantity (the integral solar neutrino interaction rate).
- they do not measure neither the spectrum nor the incoming direction of solar neutrinos.

It is common opinion that having reached a statistical accuracy almost equal to the systematic accuracy they have almost accomplished their role.



SAGE

	Collaboration	ν_e interaction reaction	Target comp. and mass	Exp. Time [d]	Data taking
GALLEX/ GNO LNGS Italy	D (MPIK,TUM), I (INFN), F (CEA), USA (BNL), Israel	$\nu_e(^{71}\text{Ga}, ^{71}\text{Ge})e^-$	GaCl ₃ • HCl in H_2O 103 t (30 t Ga)	21-28 28	1991- 2003
		3500 mwe 0.6 μ [h m ²] ⁻¹			
SAGE Baksan Kabardino Balkaria	RU (INR, RAS) USA (LNL,BNL)	$\nu_e(^{71}\text{Ga}, ^{71}\text{Ge})e^-$	Metallic Ga 50 tons	28	1990- ongoing
		4800 mwe 0.1 μ [h m ²] ⁻¹			

GALLIUM Experiments

The interaction
(proposed by
Kuzmin in 1966)

$^{71}\text{Ga}(\nu_e, e) ^{71}\text{Ge}$ ($E_{\text{thr}} = 233 \text{ keV}$)
K,L shell EC $\tau = 16.5 \text{ d}$
 $\rightarrow ^{71}\text{Ga} + 10 \text{ keV}, 1 \text{ keV}$
(Auger e^- , X)

ν Signal Composition:
(BP04 + N14 SSM + ν osc)

pp + pep	41.7 SNU	(62 %)
^7Be	19.0 SNU	(28 %)
CNO	2.6 SNU	(3.9 %)
^8B	4.1 SNU	(6.1 %)
Tot	67.4 SNU	$+2.6_{-2.3}^{}$ 1σ
No osc	127 SNU	$+12_{-10}^{}$

Expected Signal
(SSM + ν osc)

LNFS - 22 February 2023

0.6 ν int. per day in GNO (1 in SAGE), but due to decay during exposure + ineff., 4.7 ^{71}Ge decay detected per extraction (28 days exposure).

Determination of Gallium- ν_e capture cross section

Ga- ν_e capture cross sections are needed to compute fluxes from rate

At low energy (< 410 keV, namely for pp ν_s) only g.s.-g.s.transitions are present; for this transition cross sections are evaluated from ^{71}Ge E.C.

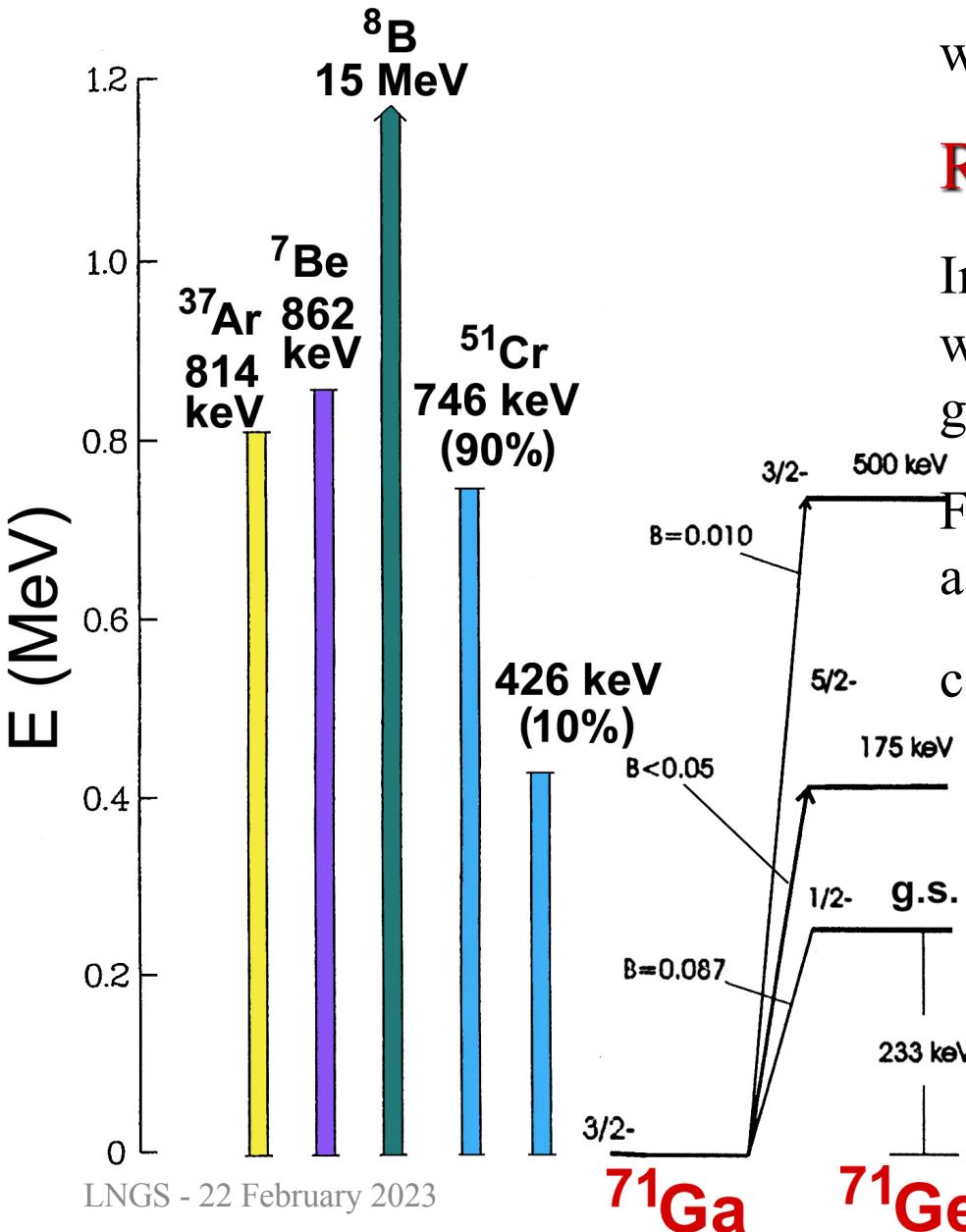
good accuracy (2.3% at 1σ)

At the ^7Be energies, the first two excited state (at 175 and 500 keV) must be considered; BGT estimated from (p,n) reactions;

estimated accuracy $-3\% +5\%$

Direct measurement desirable

Experimental situation



Two GALLEX and one SAGE calibrations,
with strong ^{51}Cr sources

$$R_{\text{meas}} = 0.93 \pm 0.07 R_{\text{theo}}$$

Improvements are well possible irradiating
with a 2MCi source f.i. 20 tons of metallic
gallium

Final accuracy 5% or better = theoretical
accuracy to address the question:

corrections to

g.s.-e.s. only

or to g.s.-g.s. also?

GALLEX sources: 1.71 MCi
1.87 MCi

0.52 MCi

Gas processing efficiencies evaluation

Data from neutrino source experiments can be used to infer on the cross section only once the extraction + gas processing efficiencies are exactly determined, and “hot chemistry” effect are excluded.

This has been done by the GALLEX collaboration, spiking the target with O(10000) atoms of ^{37}As , that beta decay to ^{76}Ge , kinematically mimicking the ν interaction.

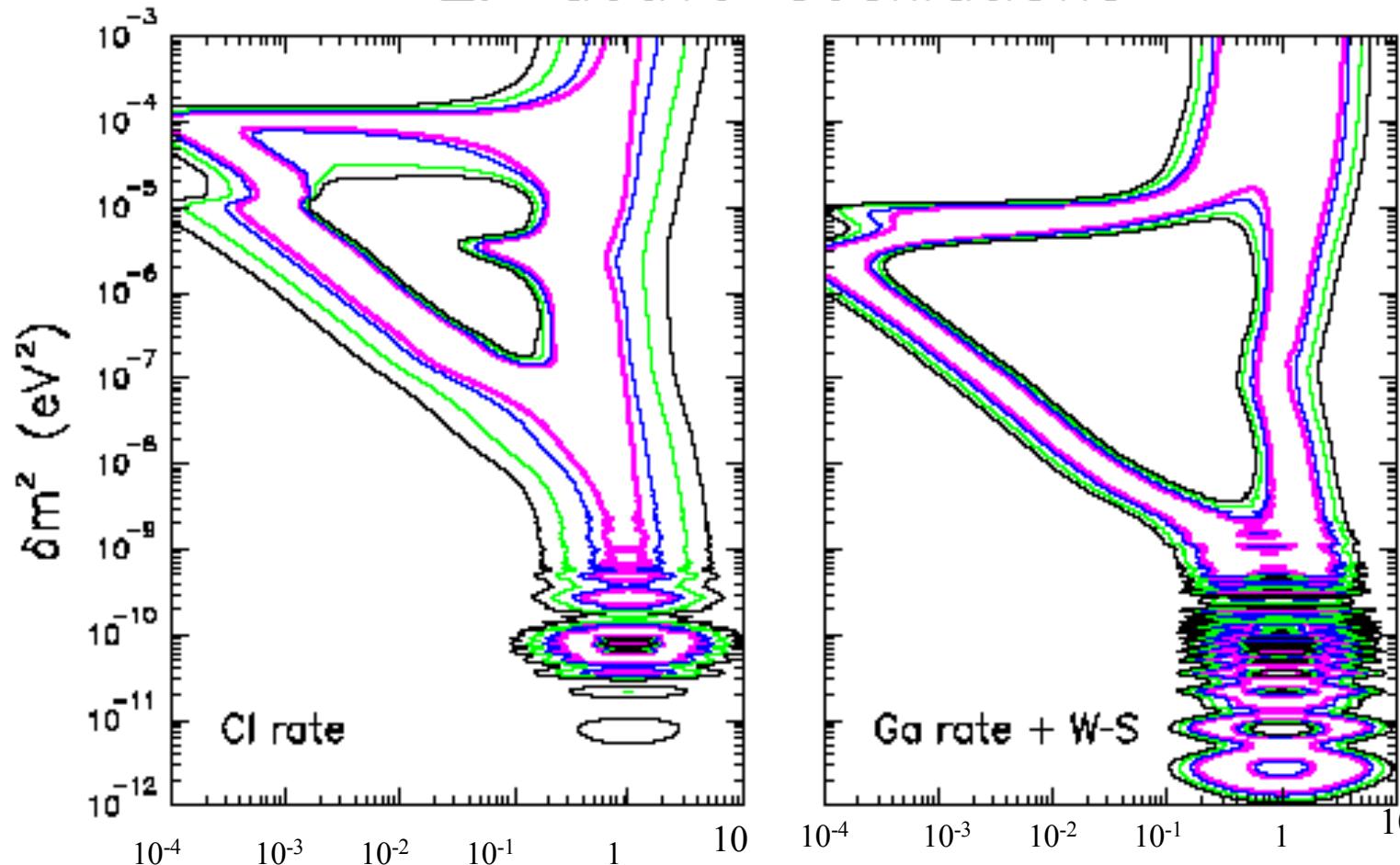
The processing efficiency has been found to be correctly estimated (from the methods routinely adopted at each run)
=100% with 1% error.

Impact of Gallium experimental results on neutrino oscillation parameters determination.

Almost irrelevant with the actual experimental accuracy in the actual experimental scenario

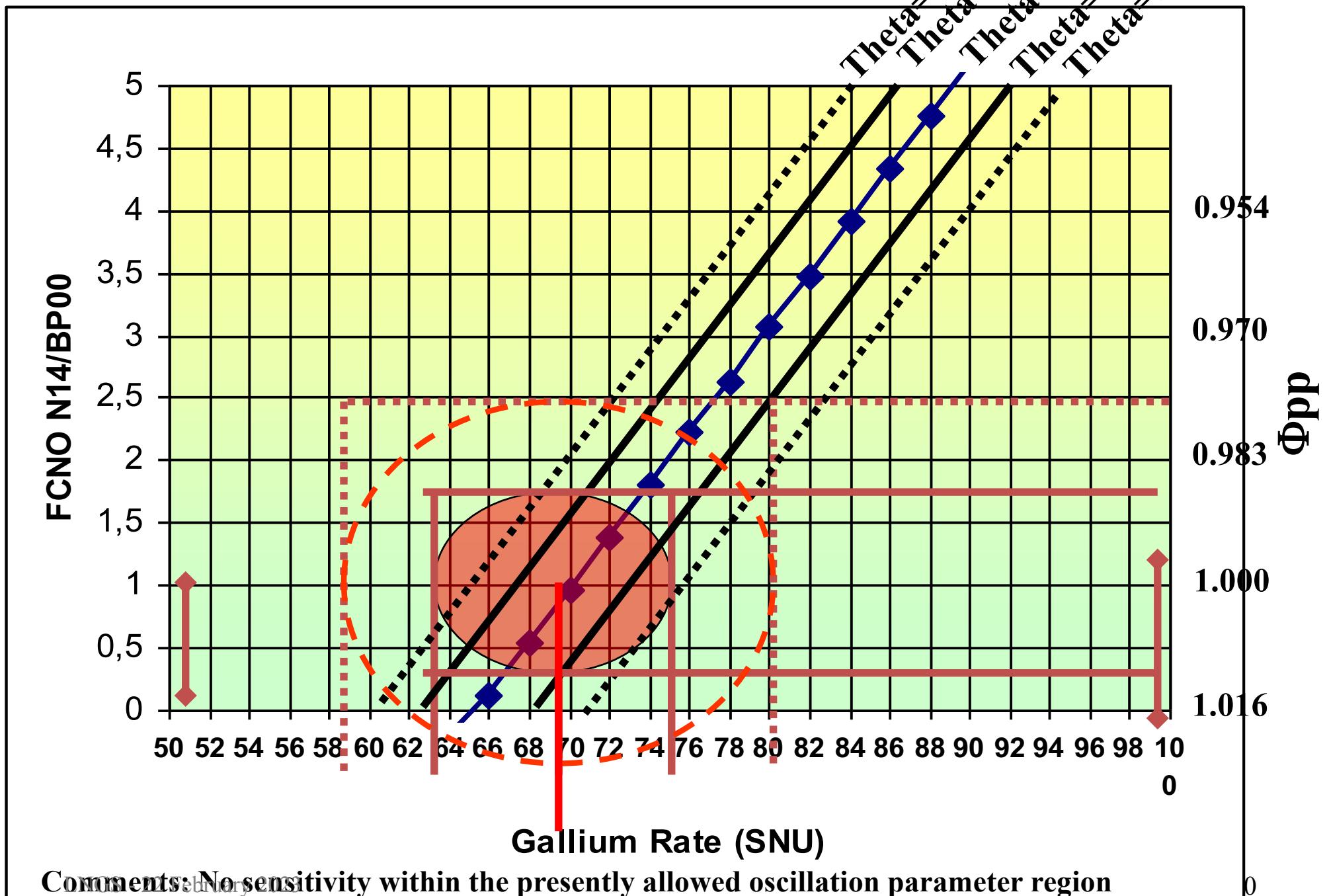
Allowed $(\Delta m^2, \tan^2 \theta_{12})$ regions from Radiochemical experiments

2ν active oscillations



Ga experiments are more sensitive to $\tan^2 \theta_{12}$ than to Δm^2

Oscillation parameters vs (Ga rate + SSM)



Impact of Gallium Results on Astrophysics

Solar Models R previsions for Radiochemical experiments

from LUNA experiment on $^{14}\text{N}(p, \gamma)^{15}\text{O}$

$$\text{New } S_0(^{14}\text{N} + p) = 1.77 \text{ keV} \pm 0.2$$

Flux ($\text{cm}^{-2}\text{s}^{-1}$)	BP00	BP04	BP04 + N14	BP04 ⁺ + N14	P_{ee} $\Delta m^2 = 7.1 \times 10^{-5} \text{ eV}^2$ $\theta_{12} = 32.5$
pp (10^9)	59.5 ($\pm 1\%$)	5.94 ($\pm 1\%$)	59.8	60.3	0.578 (vac)
pep (10^8)	1.40 ($\pm 2\%$)	1.40 ($\pm 2\%$)	1.42	1.44	0.531(vac)
hep (10^3)	9.24	7.88 ($\pm 16\%$)	7.93	8.09	~ 0.3 matter
^7Be (10^9)	4.77 ($\pm 10\%$)	4.86 ($\pm 12\%$)	4.86	4.65	0.557 vac
^8B (10^6)	$5.05^{+20\%}_{-16\%}$	5.79 ($\pm 23\%$)	5.77	5.24	0.324 matter
^{13}N (10^8)	$5.48^{+21\%}_{-17\%}$	5.71	$3.23^{+37\%}_{-35\%}$	2.30	0.557 vac
^{15}O (10^8)	$4.80^{+25\%}_{-19\%}$	5.03	$2.54^{+43\%}_{-39\%}$	1.79	0.541 vac
^{17}F (10^6)	$5.63^{+25\%}_{-25\%}$	5.91	$5.85^{+44\%}_{-44\%}$	3.93	

increased accuracy in $^7\text{Be}(p, \gamma)^8\text{B}$ measurement

Columns 2,3,4 from BP04

..... to summarize

$$\text{BP00 with } Z/X_{old} = 0.0229 \longrightarrow R_{CZ} = 0.715 R_\Theta$$

BP04 = BP00 + New data on EOS, Nucl Phys.(Cross sections)

$$N14 = BP04 + S_0(^{14}N+p) = 1.77 \text{ keV} \pm 0.2$$

$$BP04+ = BP04 + Z/X_{new} = 0.0176 \longrightarrow R_{CZ} = 0.725 R_\Theta$$

to be compared with

$$R_{meas} = 0.713 \pm 0.001$$

Solar Models *R* previsions for Radiochemical experiments

Experimental	Δm^2 , $\tan^2 \theta_{12}$	from experiments	BP00	BP04	BP04 + N14	BP04 ⁺⁺ N14
SNO/ SK 5.21 ± 0.27 (cm ⁻² s ⁻¹)	7.1, 0.45 †	1.00 ^{+6%} _{-6%} 1.01 ^{+6%} _{-6%}				
	7.3, 0.42 *					
	no osc		5.05 ^{+20%} _{-16%}	5.79 (± 23%)	5.77	5.24
C1 2.56 ± 0.23 [SNU]	7.1, 0.45 †	3.06 ± 0.04				
		2.79 ± 0.18		3.35 (± 21%)	3.23	2.95
	7.3, 0.42 *					
	no osc		7.6 ^{+1.3} _{-1.1}	8.5 ^{+1.8}_{-1.8}	8.2	7.7
Ga 68.1 ± 3.75 [SNU]	7.1, 0.45 †	69.4 ± 2.6				
		65.8 ± 4.5				
	7.3, 0.42		C. Cattadori	67.7 ± 5.5	69.3 ± 5.3	67.7 ± 5.3

Comparison of solar model predictions with experimental results

- Neutrinos prefer a Sun having “low metallicity” solar interior, as the recent photospheric measurements indicate
- when this data are included in the SSM → tension with helioseismology as the depth of the convective zone goes to $0.726 R_{\text{sun}}$ (instead of 0.713 as measured i.e. 18% discrepancy).

L_{CNO} estimate from Gallium experimental results imposing the luminosity constraint

1. From R_{Ga} (which come from the sum of all the neutrino components, weighted by the cross section and P_{ee})

$$R = N_{\text{target}} \cdot \sum_i \int \sigma_i(E) \cdot \frac{d\Phi_i(E)}{dE} P(\nu_e \rightarrow \nu_e) dE$$

2. And the Luminosity constraint: nuclear fusion reactions are the only source of energy in the Sun \rightarrow relates the Sun energy release in photons to energy release in ν

$$L_{Sun} = \sum_i \Phi_i \cdot \alpha_i = 8.53 \cdot 10^{11} MeV cm^{-2} s^{-1}$$

$\alpha_i = MeV \text{ in photons per emitted neutrino}$

Gallium

Uncertainties for evaluation of pp and CNO ν flux

Parameter	Parameter Uncertainty	Rga Uncertainty (SNU)
Theta	+/- 2.5° SNO+kam+SK	2.9
⁷ Be	10% SSM	1.9
Cross section GS -GS	2.3%	1.5
Cross section GS –ES(1,2)	50%	0.7
Cross section GS-ES>2	35%	1.5
8B	9 % SNO	0.4
pep	1.5 % SSM	0.1
		4.2

.....it is possible to estimate at the same time Φ_{pp} and Φ_{CNO} once we know the 8B , 7Be , pep fluxes

$$\frac{L_{CNO}}{L_{Sun}} = \frac{\Phi_O \cdot \alpha_O + \Phi_N \cdot \alpha_N}{\sum_i \Phi_i \cdot \alpha_i}$$

- 8B take from experiments
- 7Be take from SSM
- pep strictly related to pp

$$\left[\frac{L_{CNO}}{L_{Sun}} \right]_{G+G}^{best\ fit} = 1.2_{-1.2}^{+2.3} \left[\frac{L_{CNO}}{L_{Sun}} \right]_{N14} \cong 0.6 \left[\frac{L_{CNO}}{L_{Sun}} \right]_{BP04}$$

$$\left[\frac{L_{CNO}}{L_{Sun}} \right]_{SAGE+G+G}^{best\ fit} = 1.0_{-??}^{+??} \left[\frac{L_{CNO}}{L_{Sun}} \right]_{N14} \cong 0.5 \left[\frac{L_{CNO}}{L_{Sun}} \right]_{BP04}$$

$$\left[\frac{L_{CNO}}{L_{Sun}} \right]_{BP04} = (1.6 \pm 0.6)\%$$

$$\left[\frac{L_{CNO}}{L_{Sun}} \right]_{G+G} \leq 7\% \text{ } (3\sigma)$$

$$\left[\frac{L_{CNO}}{L_{Sun}} \right]_{SAGE+G+G} \leq 5 - 6 \% \text{ } (3\sigma)$$

.... for ^8B and ^7Be

$$\Phi(^8\text{B})_{\text{meas}} = (0.89 \pm 0.04_{\text{ex}} \pm 0.23_{\text{theo}}) \Phi(^8\text{B})_{\text{BP04 + N14}}$$

$$\Phi(^7\text{Be})_{\text{meas}} = (0.91^{+0.24}_{-0.62 \text{ ex}} \pm 0.11_{\text{theo}}) \Phi(^7\text{Be})_{\text{BP04+N14}}$$

from BP04

Gallium- 5% error

