

*Workshop on semileptonic decays. Frascati, 12-14/04*

---

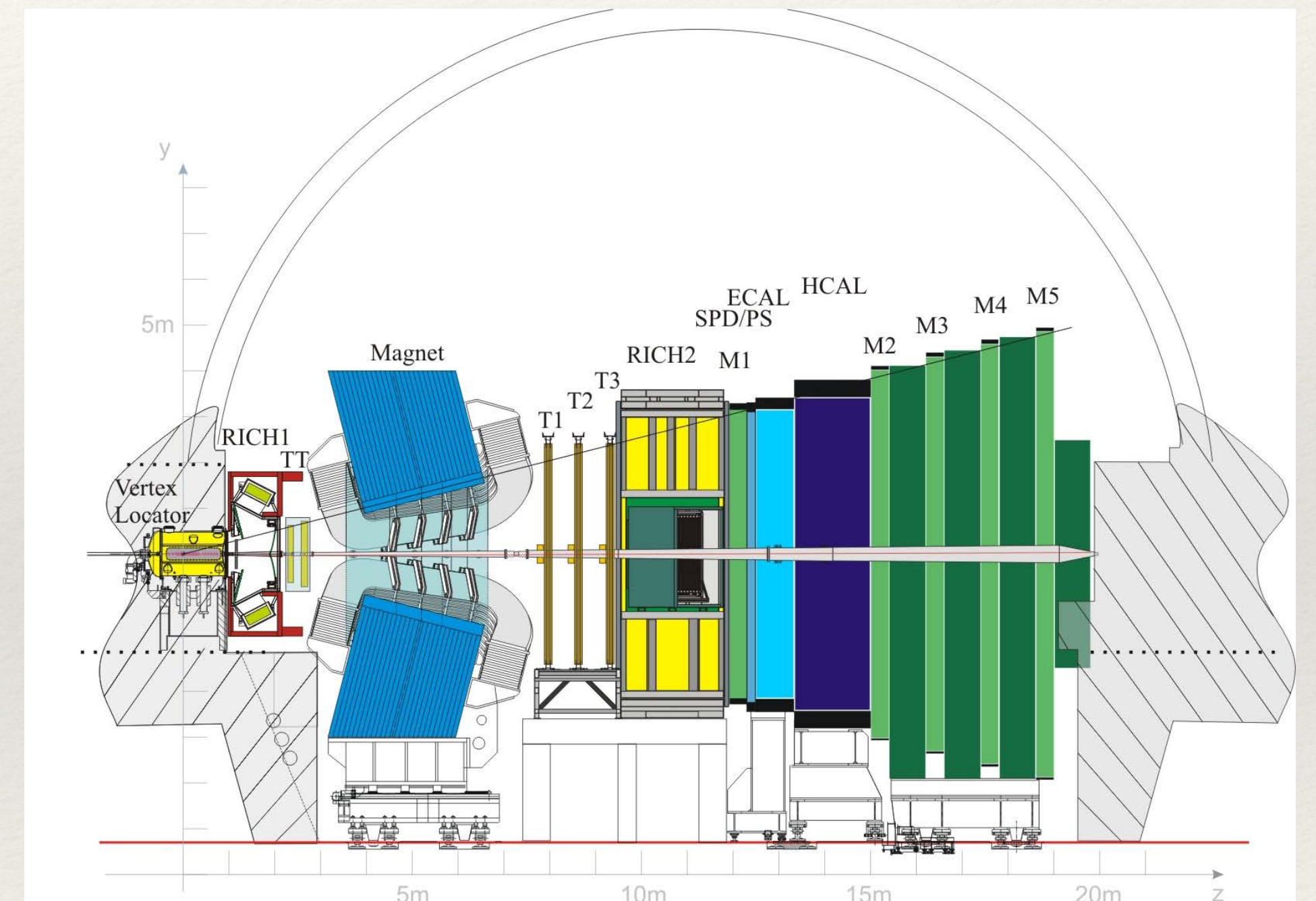
# Exclusive semileptonic measurements and prospects at LHCb

Ricardo Vázquez Gómez (UB)

---

# LHCb detector

- ❖ Likely not the first place one can think to study semileptonic decays.
- ❖ Analyses take profit from:
  - ❖ Large production:  $10^{10} - 10^{11}$  B-hadrons produced in the acceptance per  $\text{fb}^{-1}$ . [PRL 118 (2017) 052002, PRL 119 (2017) 169901].
  - ❖ Excellent vertex resolution (down to  $15\mu\text{m}$  at high  $p_T$ ).
  - ❖ Particle ID capabilities ( $\epsilon_{\text{PID}}(\mu) > 97\%$  for  $\epsilon_{\text{misID}} < 5\%$ )
  - ❖ Good momentum resolution  $\delta p/p$  in  $[0.5-1]\%$  for  $p$  in  $[5-200]\text{GeV}$ .
  - ❖ Flexible and efficient trigger.

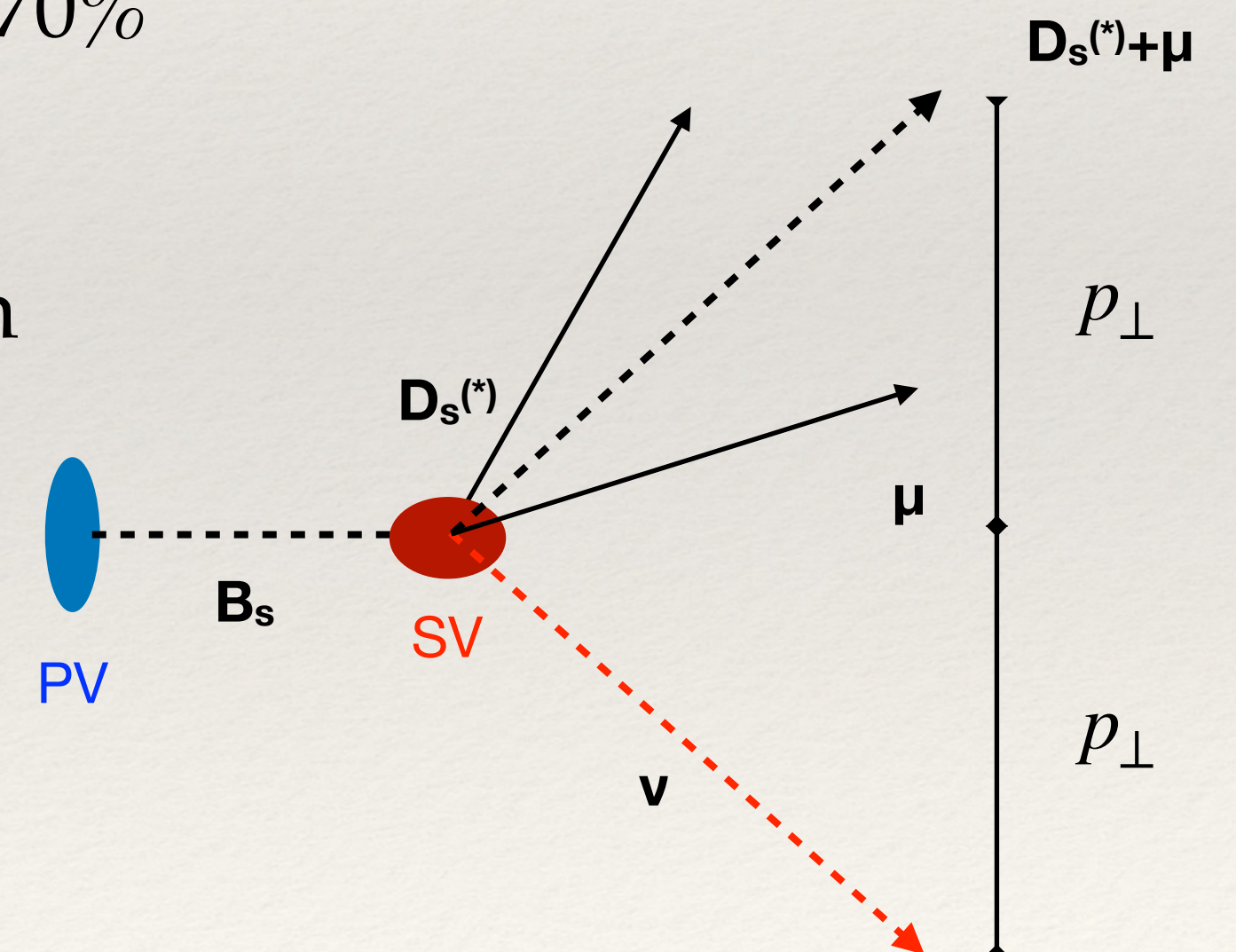


# Reconstructing B kinematics

- ❖ Decays cannot be fully reconstructed. Difficult to get  $q^2$ .
- ❖ B-hadron flight direction is well-measured. Use B-hadron mass to constrain the decay and solve  $q^2$  with a two-fold ambiguity.
- ❖ Improve on finding the correct solution by using an MVA based on the B-hadron flight direction [JHEP 02 (2017) 021]. Gives the correct solution in  $\sim 70\%$  of the cases.
- ❖ Reconstruct the corrected mass ( $m_{corr}$ ) using the imbalance of momentum transverse to B-hadron flight direction.

- ❖  $m_{corr}$  peaks at the  $B_{(s)}$  mass if only one neutrino is missing.

- ❖ 
$$m_{corr} = \sqrt{m_{vis}^2 + p_{\perp}^2} + p_{\perp}$$



---

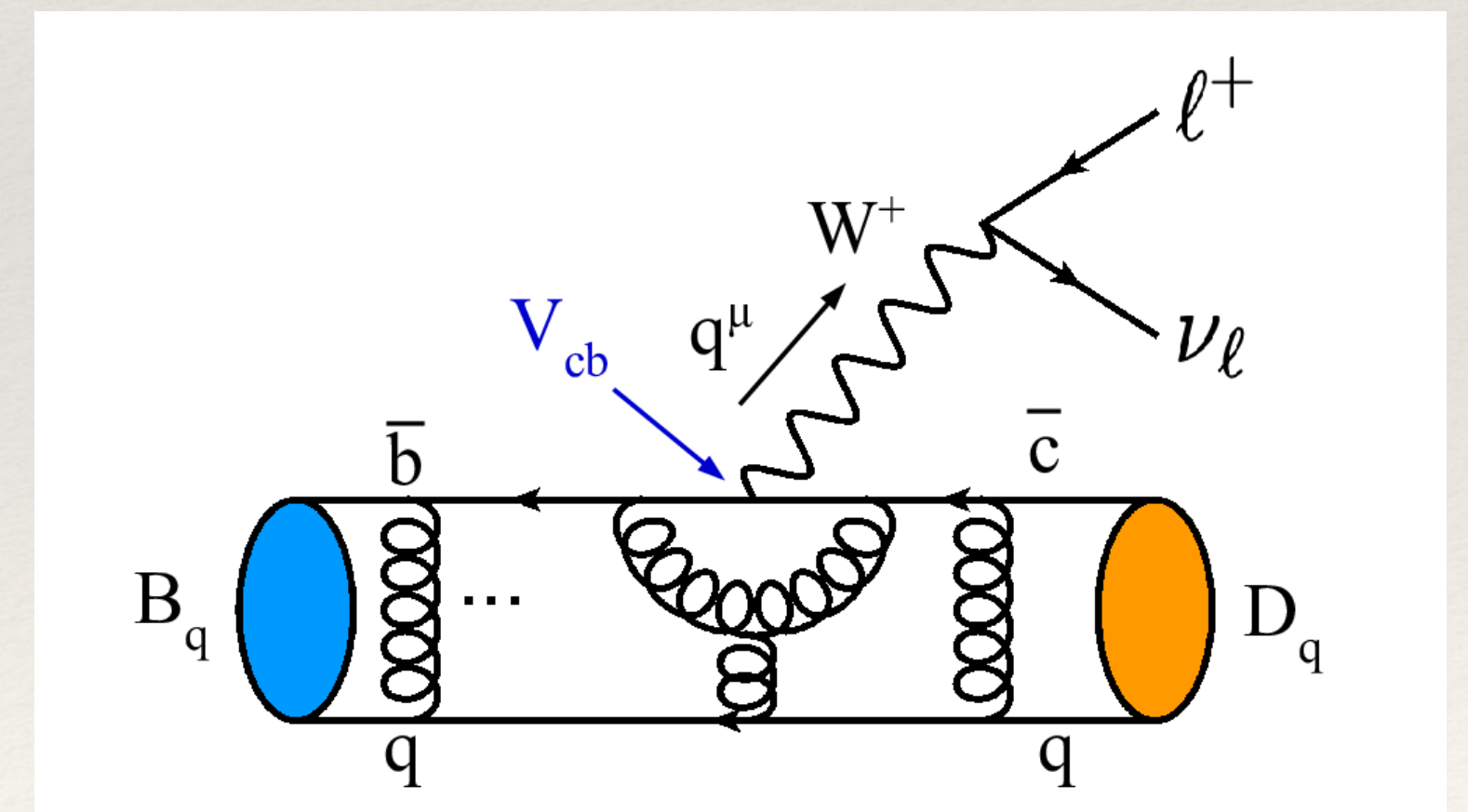
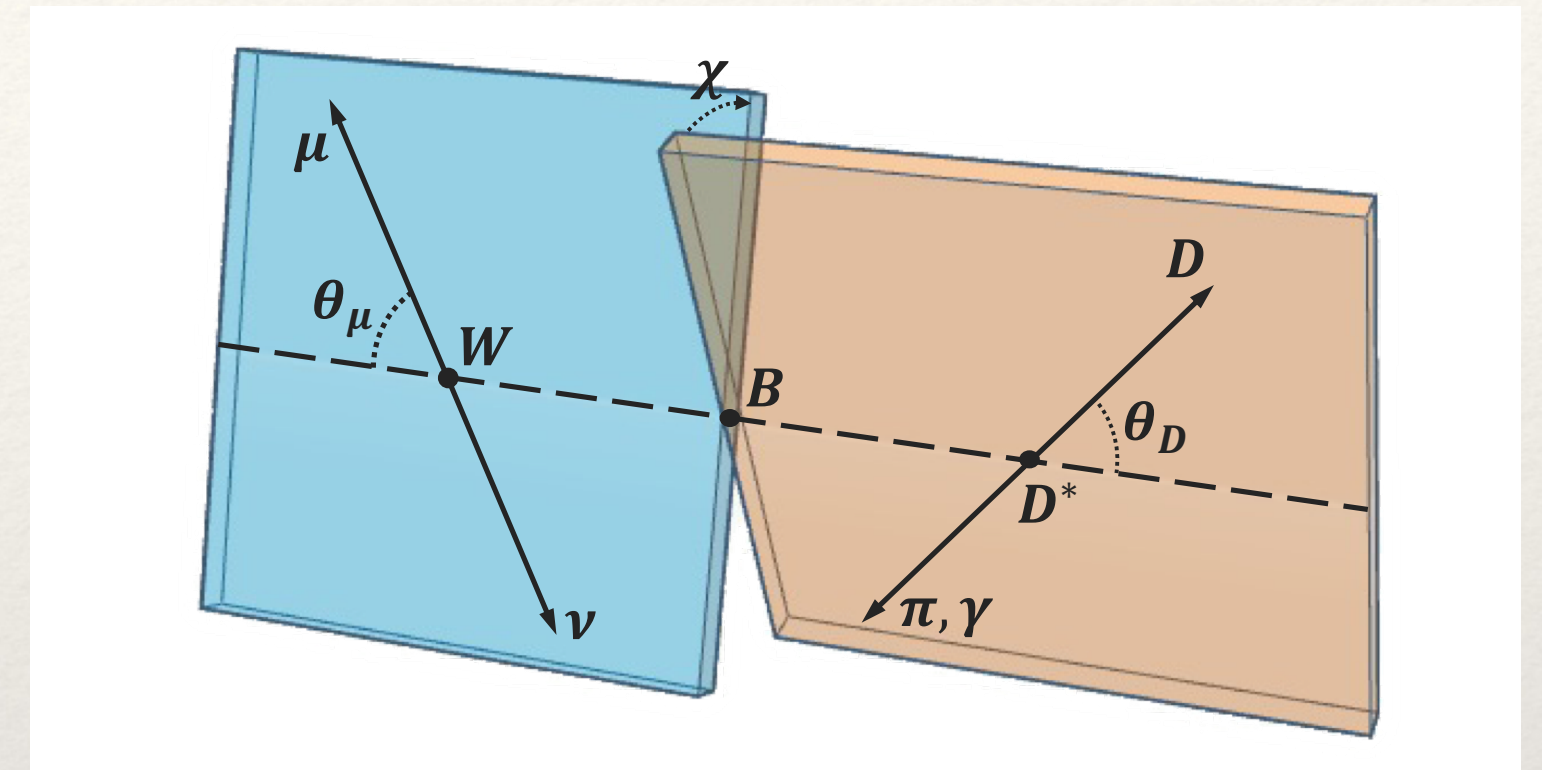
# Measuring CKM matrix elements

---

- ❖ Semileptonic B decays are used to extract the magnitude of  $V_{ub}$  and  $V_{cb}$ .
  - ❖ Two approaches: **inclusive** vs **exclusive**
- ❖ Experimental and theoretical techniques are independent and complementary.
  - ❖ **Inclusive**: Sum of all possible final states. Uncertainty dominated by theory inputs.
  - ❖ **Exclusive**: Decays involve a specific meson. Uncertainty contributions from theory and experiment are comparable.
- ❖ Expect both approaches to be compatible but observed long lasting discrepancy.

# Exclusive measurements

- ❖ Measure the differential decay rate of  $B_{(s)} \rightarrow D_{(s)}^{(*)} \mu \nu$  decays as a function of the di-lepton momentum transfer squared ( $q^2$ ).
- ❖ Factorise the EW and strong parts of the decay.
  - ❖ The strong part can be described in terms of scalar functions, **form factors**, as a function of  $q^2$ . **FF cannot be computed in perturbation theory.**
  - ❖ Experimental measurement is  $V_{cb} \times \text{FF}(q^2)$ . The determination of  $V_{cb}$  requires a determination of the form factors (either from data or from lattice QCD).

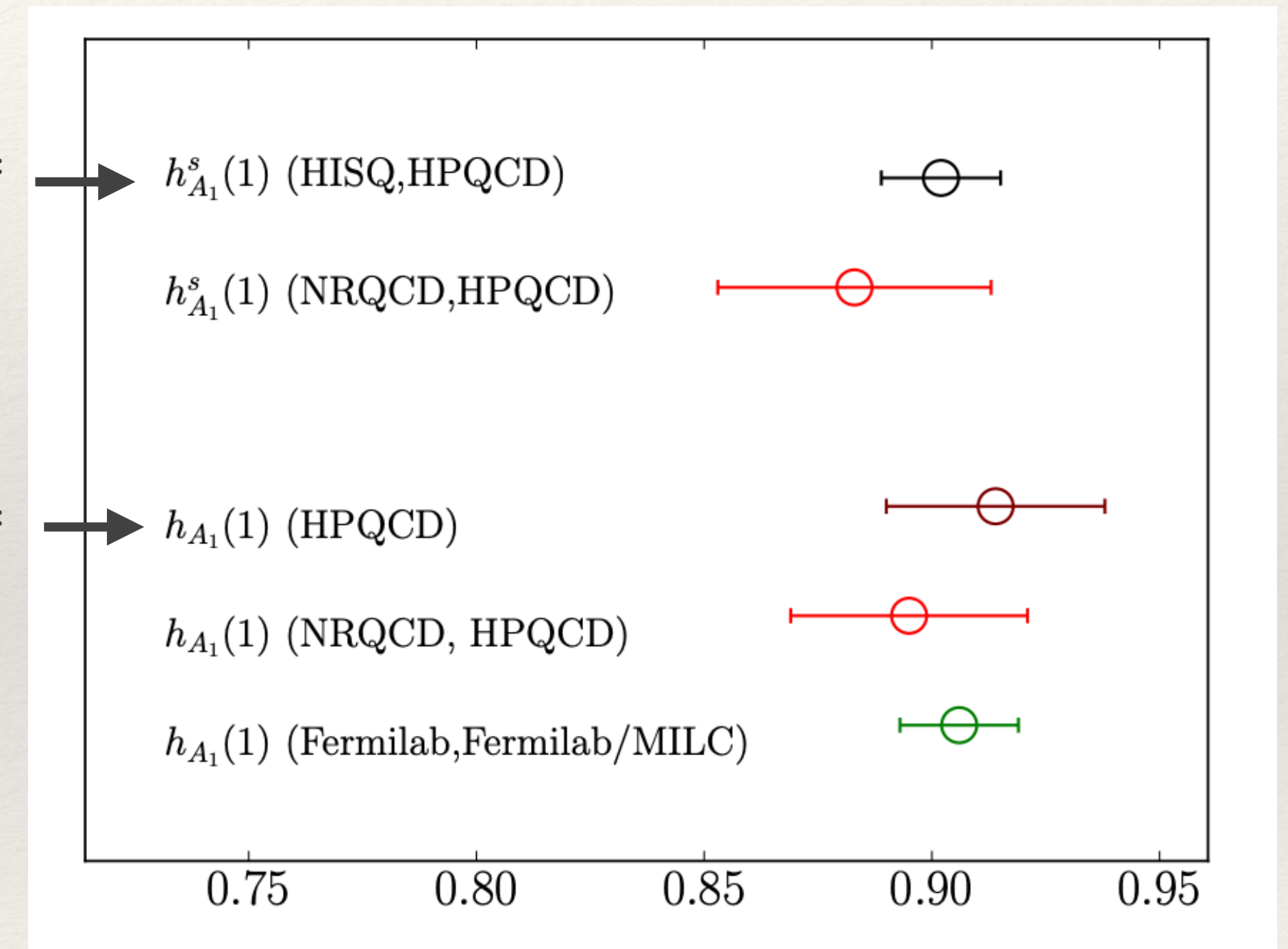


# Beyond $B^0$ and $B^+$

- ❖ Measurements on  $B_s$  and  $\Lambda_b$  are complementary to those from  $B^0$  and  $B^+$ .
- ❖ Lattice QCD calculations are easier due to the heavier spectator quark  $\rightarrow$  more precise predictions [PRD 99 (2019) 114512].
- ❖ In  $B_s$  decays, Different background composition from excited  $D_s$  mesons than in  $B \rightarrow D^{(*)}$  decays.
  - ❖ Above certain mass of the  $D_s^{**}$  mesons, the decay is through  $D^{(*)}K$ .

$B_s \rightarrow D_s^*$

$B \rightarrow D^*$



# The measurements

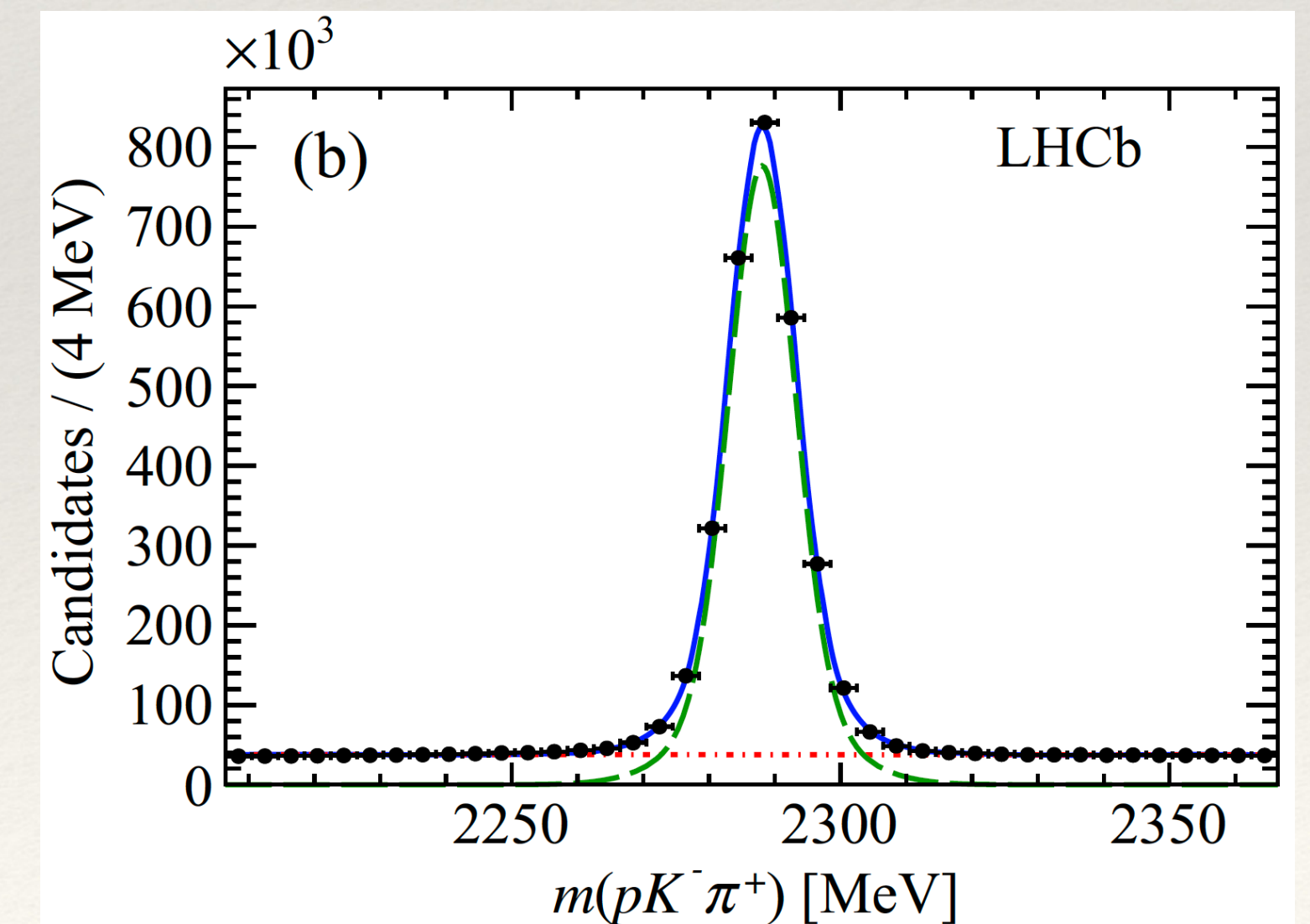
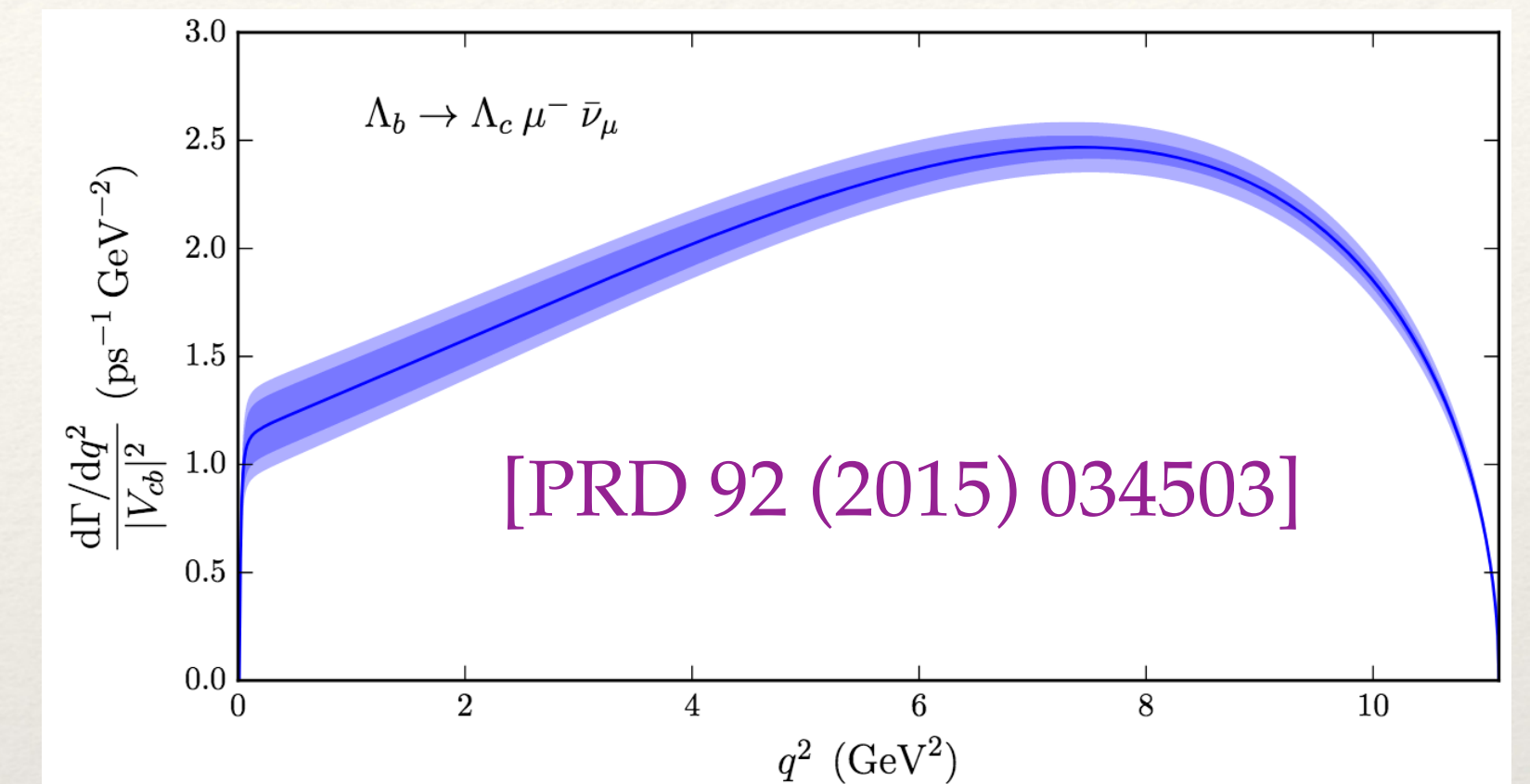
# $\Lambda_b \rightarrow \Lambda_c \mu \nu$ differential spectrum

- ❖  $\Lambda_b$  (udb) has a different spin structure than  $B^0/B^+$  and because the (ud) di-quark has  $j=0$ , HQET makes cleaner predictions.

- ❖ Measure the differential spectrum  $\frac{d\Gamma}{dq^2} = GK(q^2)\xi_B^2(q^2)$ .

Extract the information on  $\xi_B(q^2)$  assuming parametrisations based on phenomenological models or simple expansion around  $w=1$ .

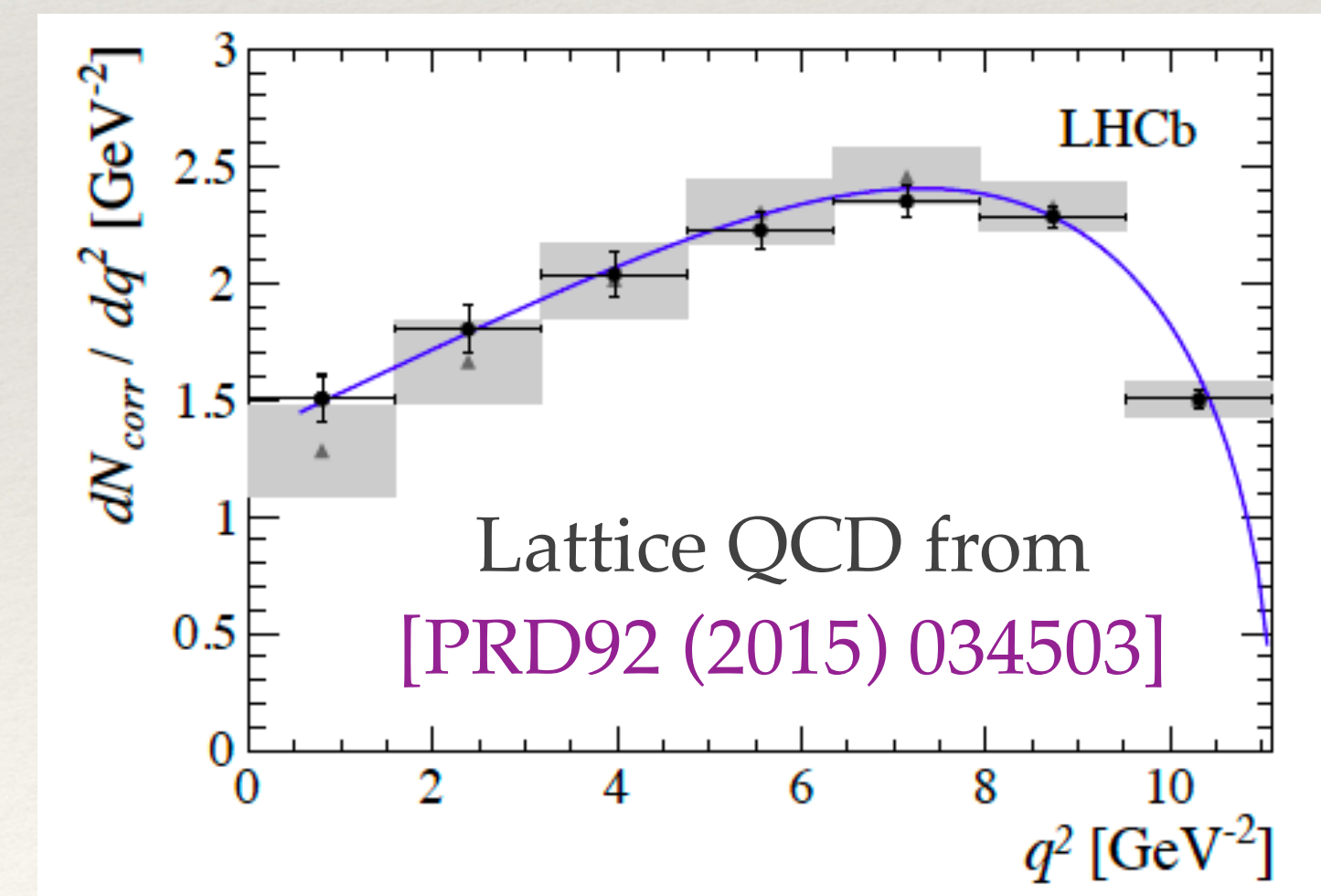
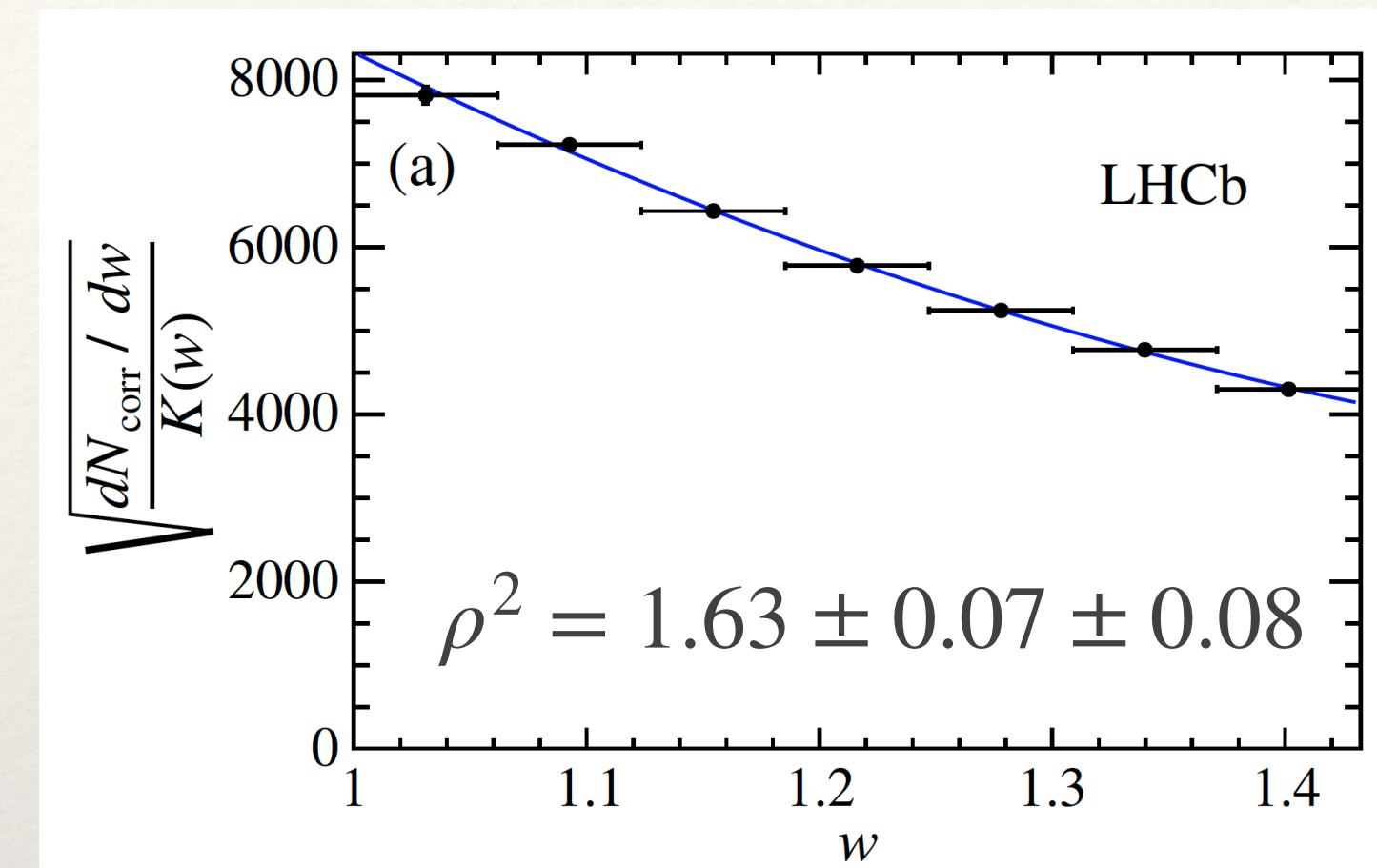
- ❖ Large and clean sample of  $\Lambda_b \rightarrow \Lambda_c \mu \nu X$ , with main backgrounds from  $\Lambda_b \rightarrow \Lambda_c^* \mu \nu$  and  $\Lambda_b \rightarrow \Sigma_c^{++/0} \pi \mu \nu$





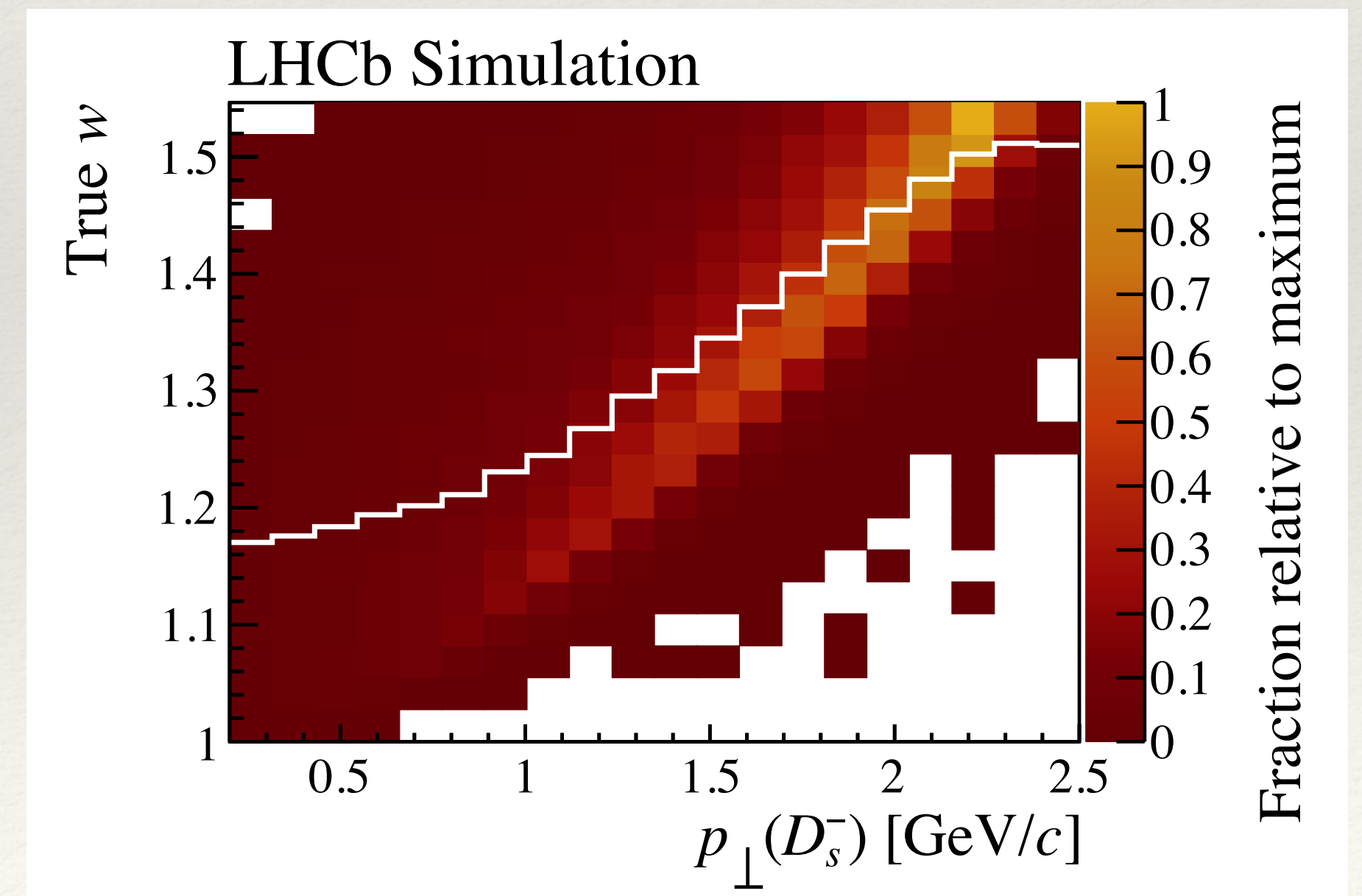
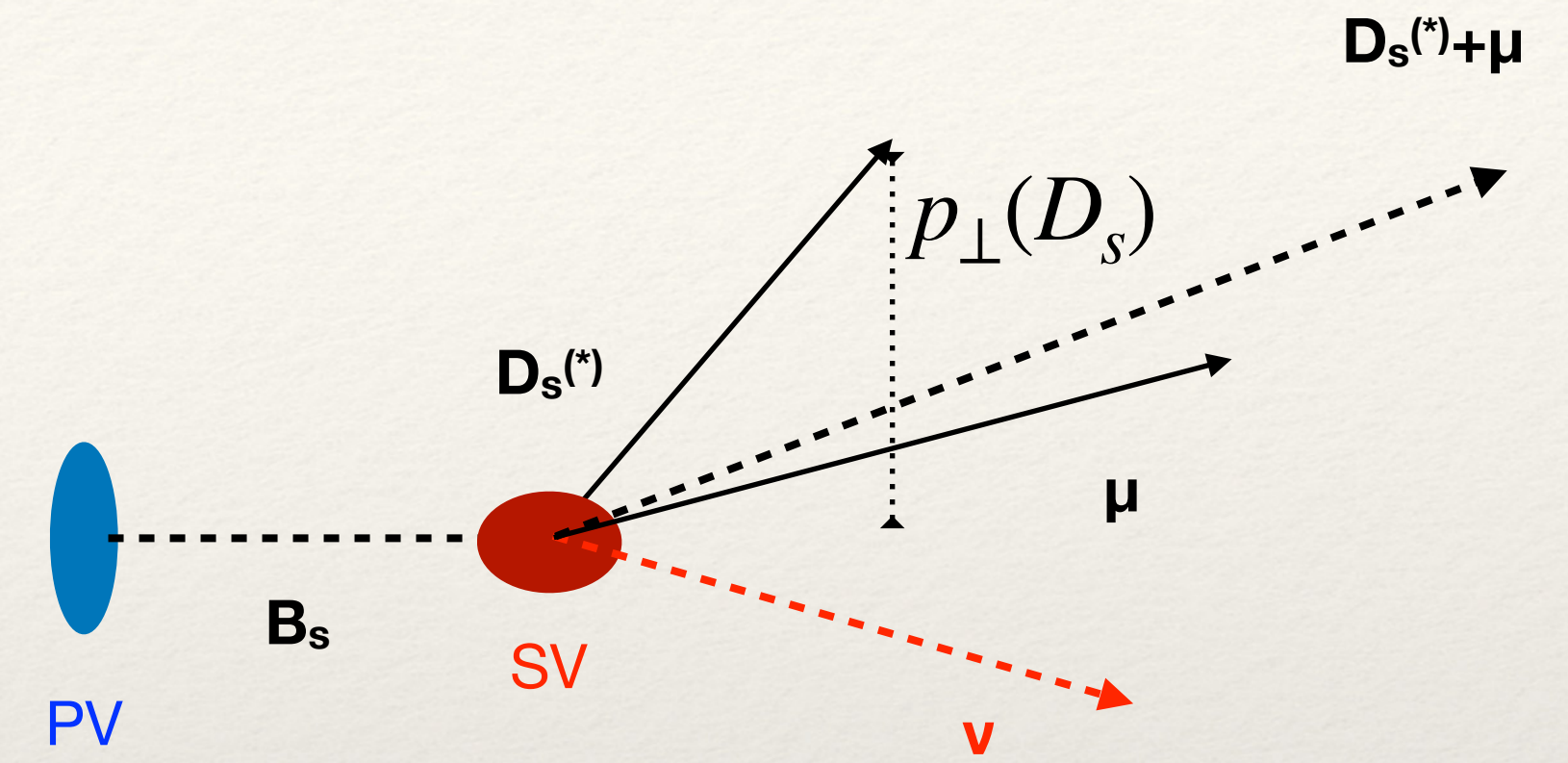
# $\Lambda_b \rightarrow \Lambda_c \mu \nu$ differential spectrum

- ❖  $\Lambda_b$  yield in bins of  $q^2$ . Correct for feed-down from background, efficiencies and unfold.
- ❖ Different parametrisations have good fit quality. Data/HQET predictions agree.
- ❖ Knowledge of  $\Lambda_b \rightarrow \Lambda_c$  FF crucial for  $R(\Lambda_c)$ .
- ❖ Opened the route to measurements of FF in other B-hadrons.
- ❖ Significant yields of excited states O(10k). Good opportunity to study them.



# $V_{cb}$ from $B_s$ decays

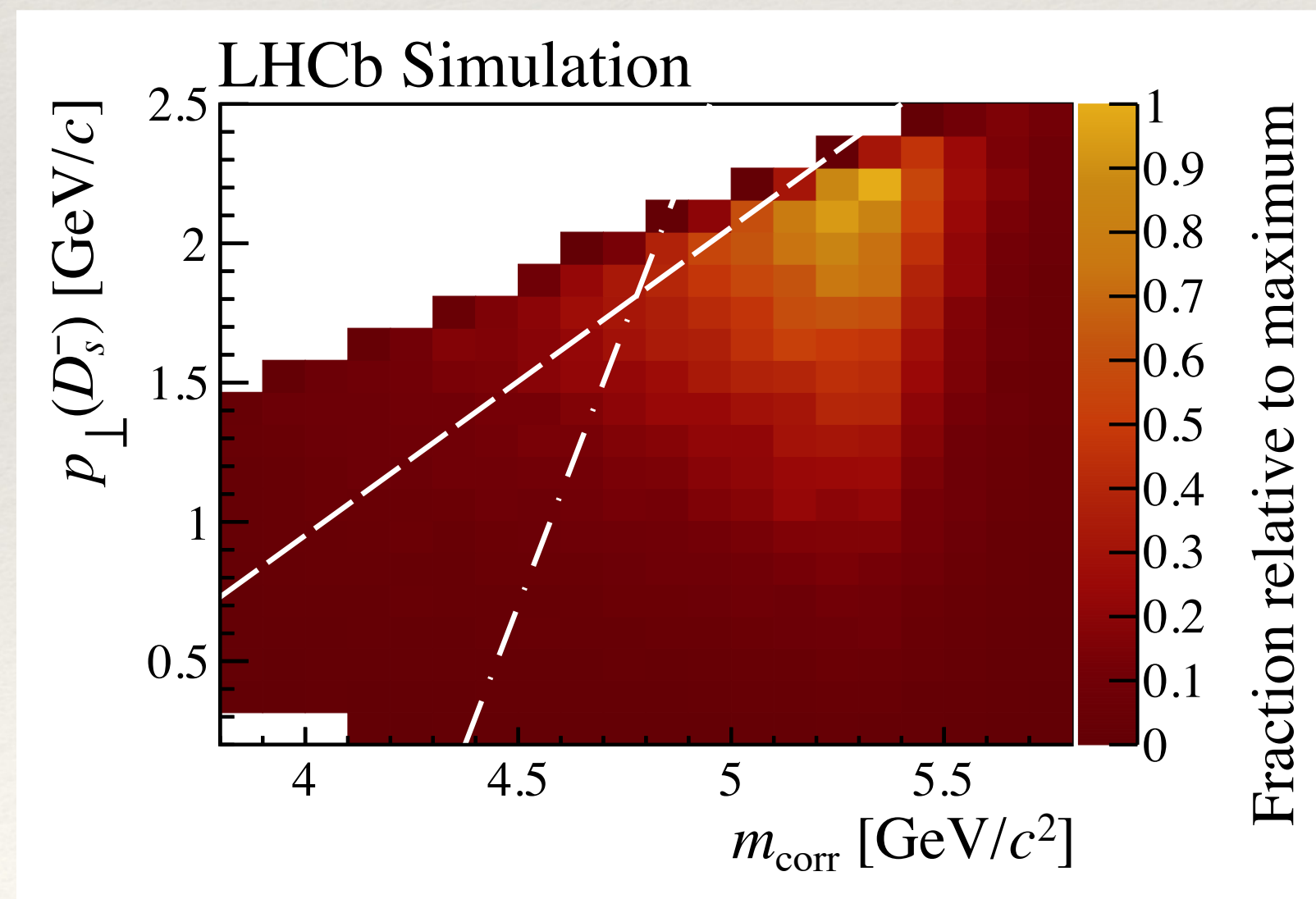
- ❖ Extract the value of  $V_{cb}$  from  $B_s \rightarrow D_s^- \mu^+ \nu$  and  $B_s \rightarrow D_s^{*-} \mu^+ \nu$  decays reconstructing only the  $D_s^- (\rightarrow K^- K^+ \pi^-) \mu^+$  final state.
- ❖ Use  $B^0 \rightarrow D^{-(*)} \mu^+ \nu$  as normalisation. Ratio of yields is proportional to  $V_{cb}$ .  $BR(B^0 \rightarrow D^{-(*)} \mu^+ \nu)$  and  $f_s/f_d$  are taken as external inputs. Kinematically identical decays  $\rightarrow$  reduce systematic uncertainties.
- ❖ Use  $p_{\perp}(D_s)$  which is correlated with  $w$ . Avoid to use any approximation.



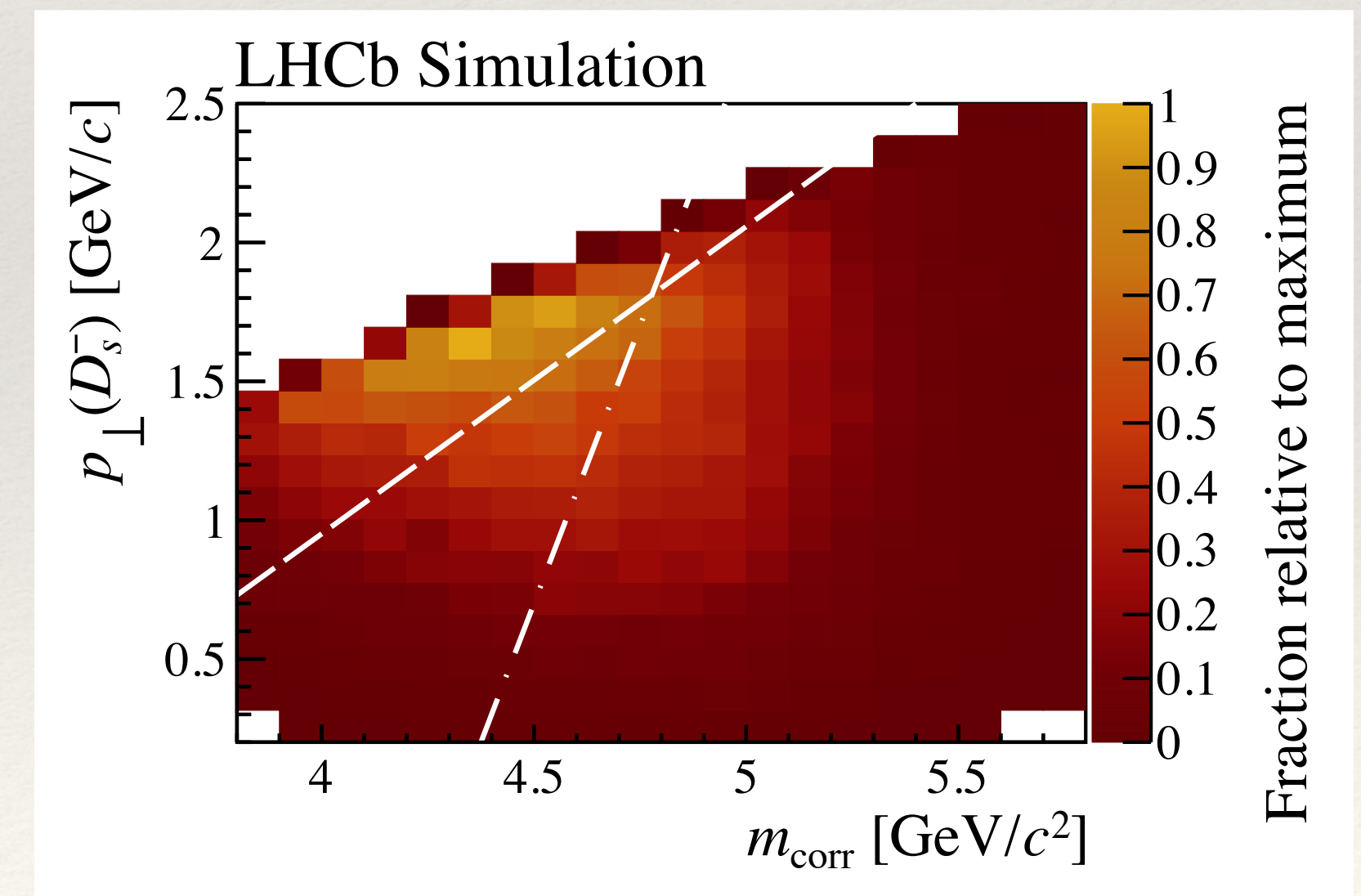
# Analysis strategy

- ❖ Template fit to  $m_{corr}$  and  $p_{\perp}$  to identify the signal decays and to measure  $V_{cb}$  and the form factors.
- ❖ Signal templates depend on form factors which are recalculated at each fit iteration. Use CLN and BGL parametrisations.
- ❖ Fit is simultaneous to signal and normalisation mode. Also provide sensitivity to form factors.

$B_s \rightarrow D_s^{(*)} \mu \nu$



Physics  
background



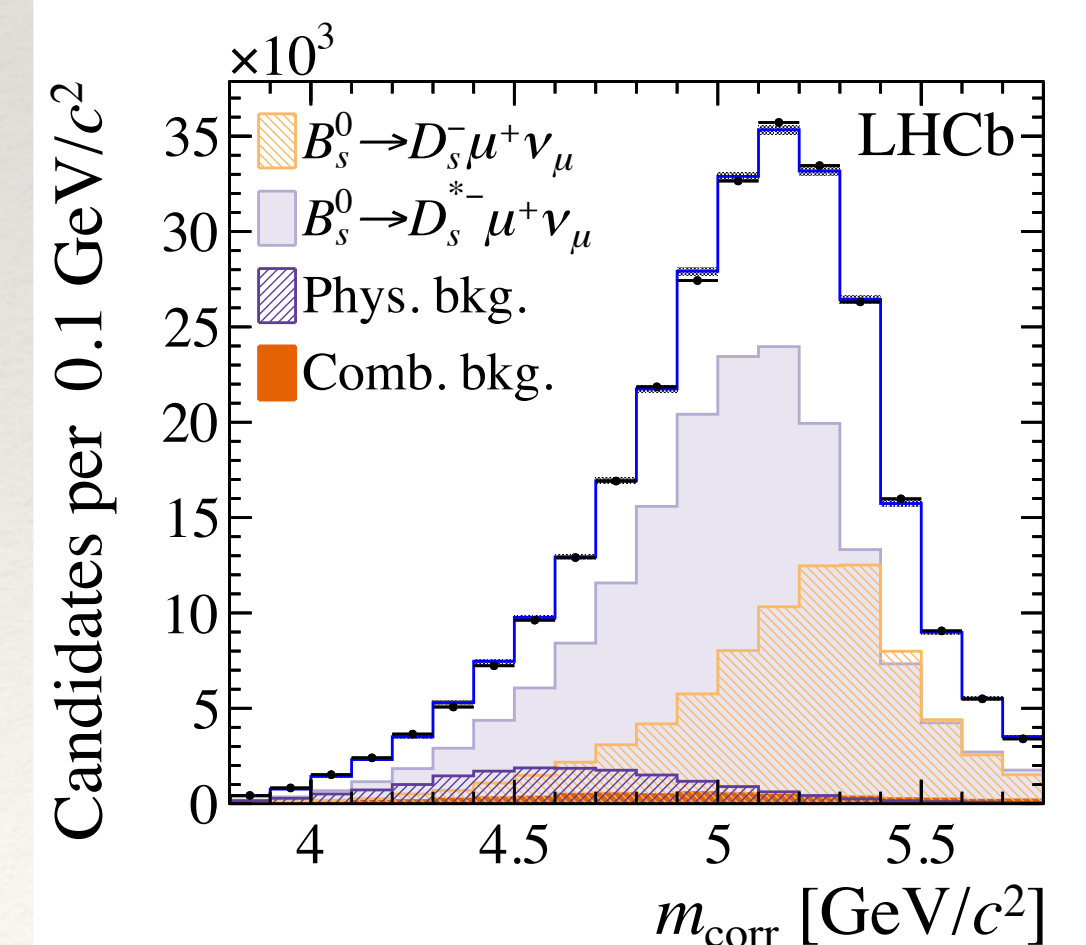
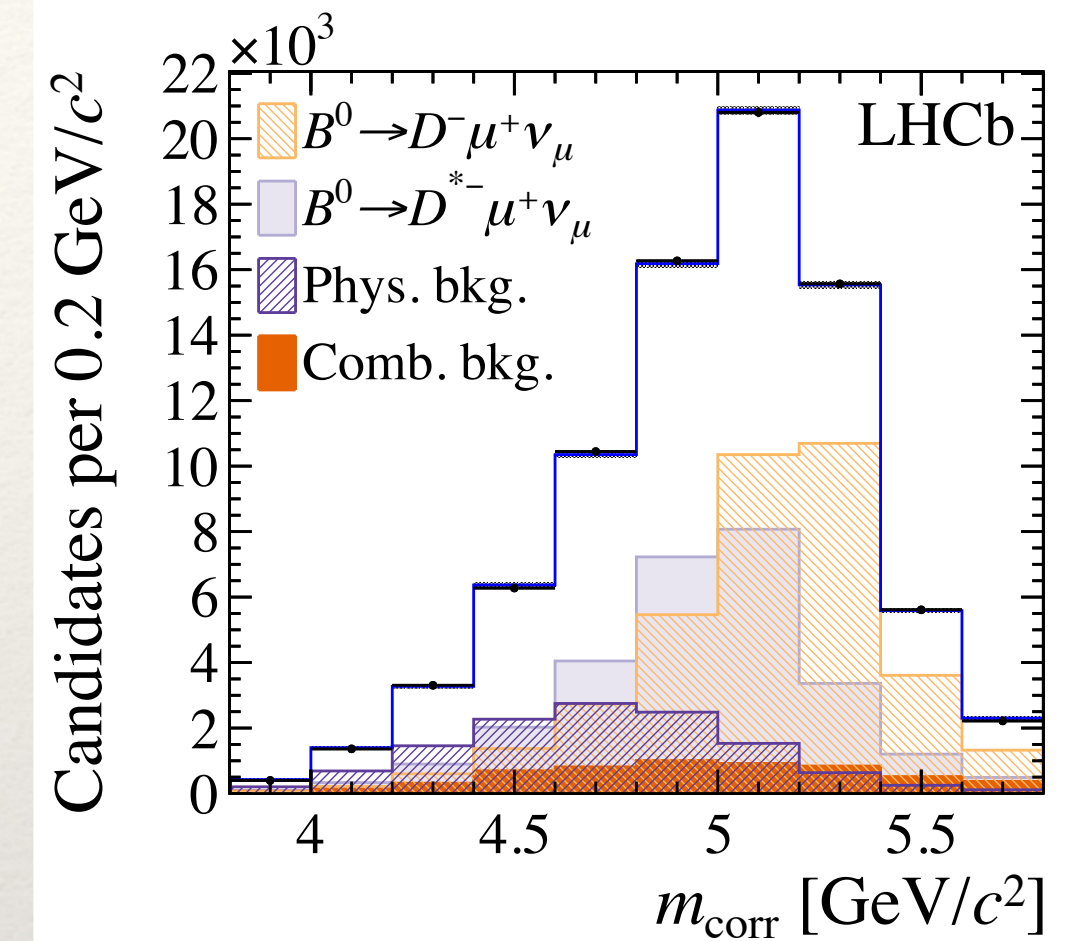
# Fit results

- ❖ Yields for signal, normalisation and form factors are free parameters.
  - ❖ Use only CLN for the normalisation as it contain less parameters.
  - ❖ FF in normalisation mode consistent with world averages.
- ❖ For the signal use CLN and BGL parametrisations. No significant differences found between both parametrisations.

$$|V_{cb}|_{CLN} = (41.4 \pm 0.6 \pm 0.9 \pm 1.2) \times 10^{-3}$$

$$|V_{cb}|_{BGL} = (42.3 \pm 0.8 \pm 0.9 \pm 1.2) \times 10^{-3}$$

- ❖ Parametrisation does not seem to be responsible for the exclusive vs inclusive disagreements.



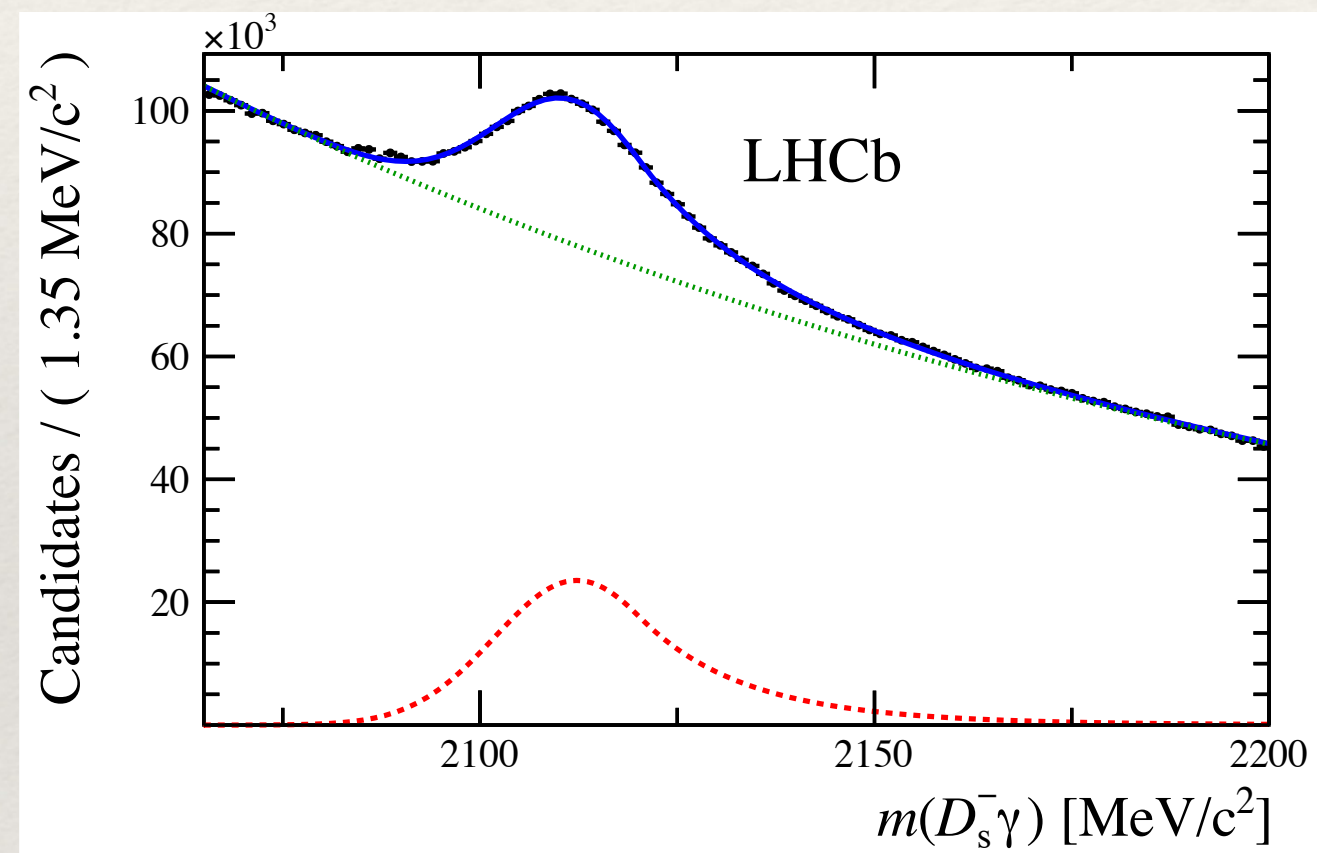
# $B_s \rightarrow D_s^*$ FF measurement

- ❖ Aim to measure more accurately the  $B_s \rightarrow D_s^*$  FF.
- ❖ Extract the differential decay rate of  $B_s \rightarrow D_s^{*-} \mu^+ \nu$  decays as a function of  $w$  by fitting  $m_{corr}$ 
  - ❖ Full reconstruction of  $D_s^{*-} \rightarrow D_s^- \gamma$  decay.
- ❖ Correct the raw yields for detector resolution (unfolding) and selection and reconstruction efficiencies.
- ❖ Fit the unfolded and efficiency corrected spectrum with CLN (extract  $\rho^2$ ) and BGL parametrisations (extract  $a_1^f, a_2^f$ ).
  - ❖ Other parameters are taken from external sources.

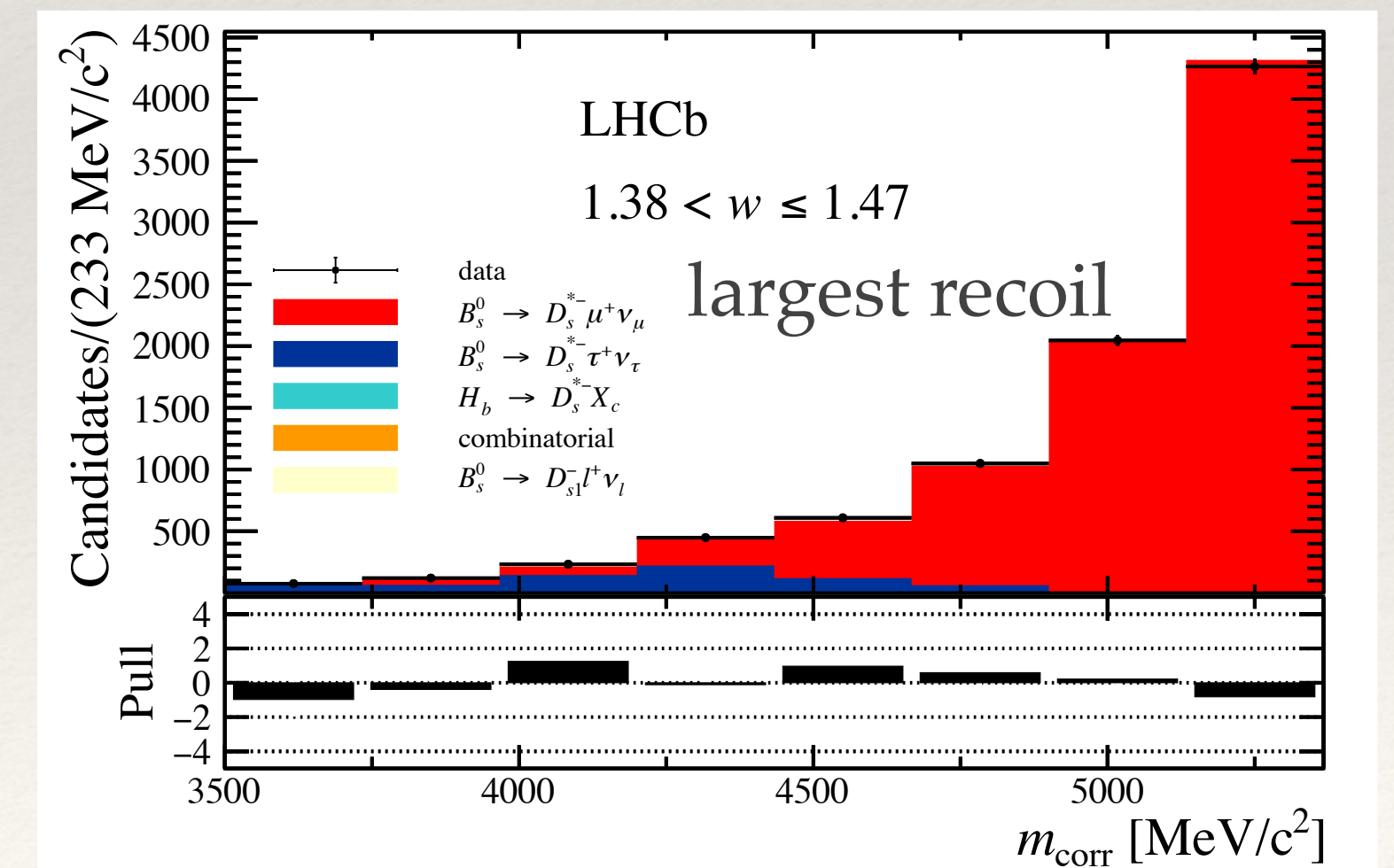
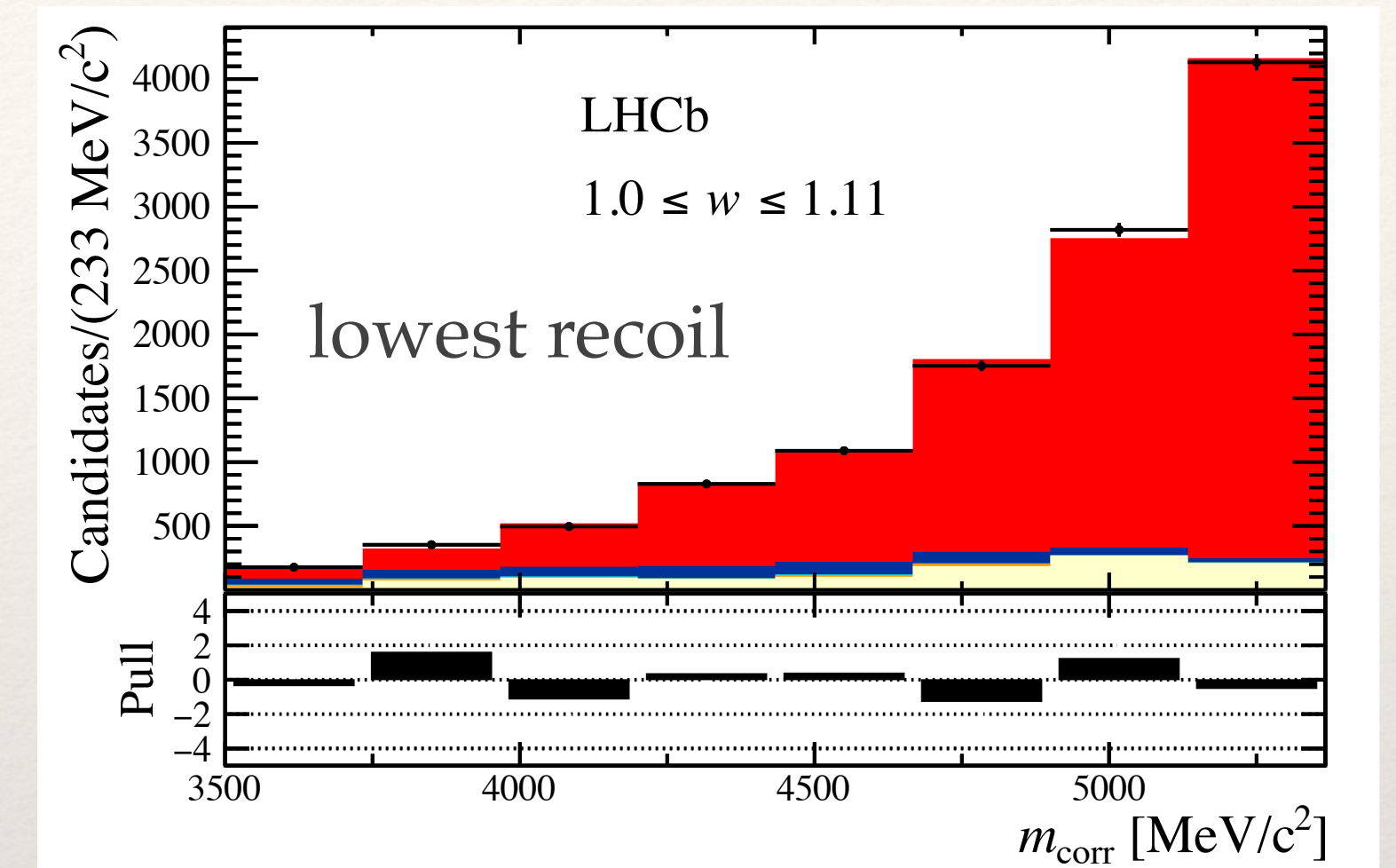
# Selection and signal yields

[JHEP 12 (2020) 144]

- ❖ Consider only photons close to the  $D_s^-$  flight direction.
- ❖ Use sPlot to subtract the combinatorial photon background.

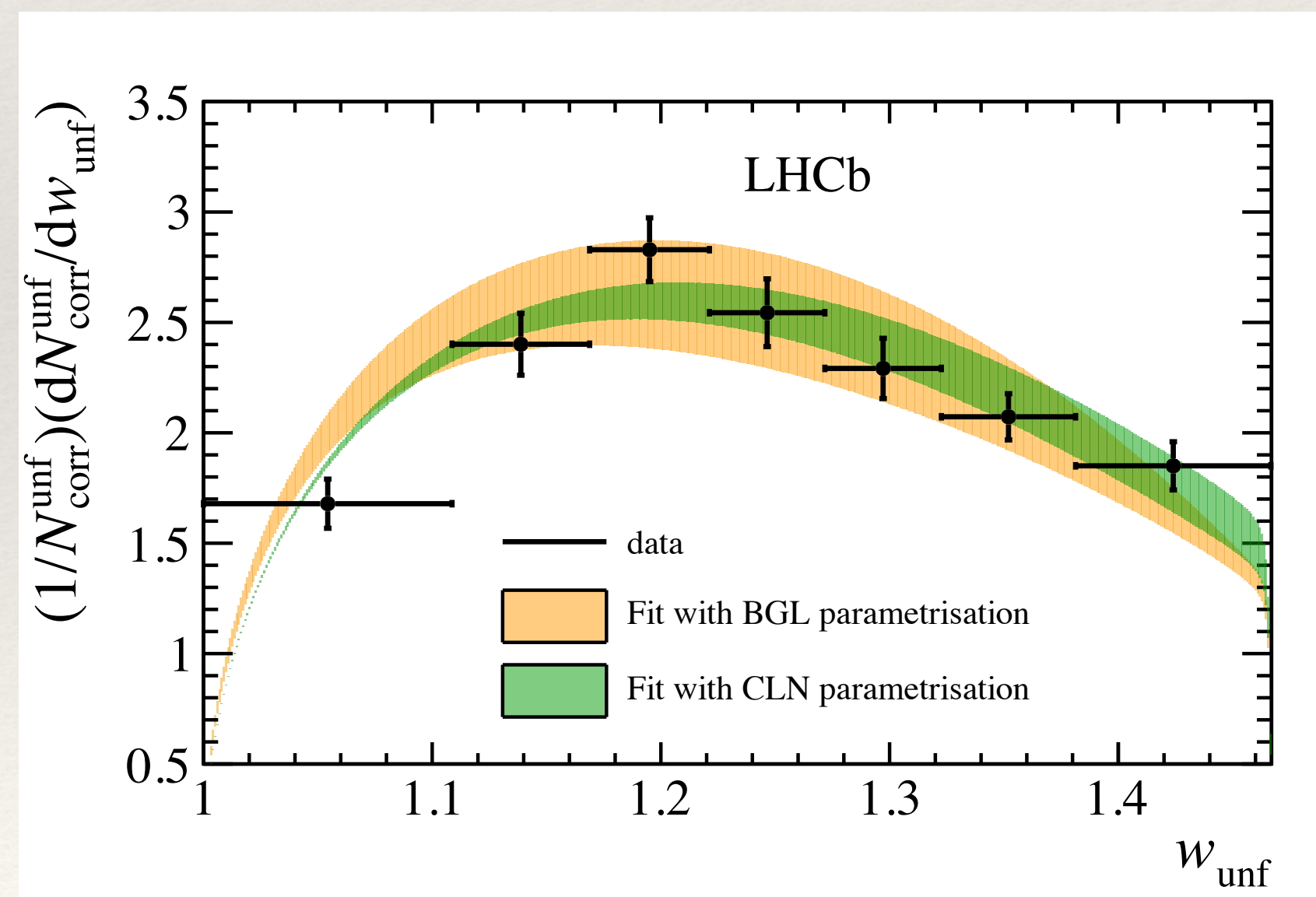


- ❖ Efficiencies extracted from data calibration samples



# FF results

- ❖ After unfolding and correcting the measured yield for the efficiencies, fit the differential decay rate with CLN and BGL parametrisations. No significant differences found between both.
- ❖ Provide unfolded spectrum for phenomenological analysis for the first time.



For CLN:

$$\rho^2 = 1.17 \pm 0.05 \pm 0.07$$

in agreement with those from  $B^0 \rightarrow D^{*-}\mu^+\nu$

No flavour SU(3) breaking.

For BGL:

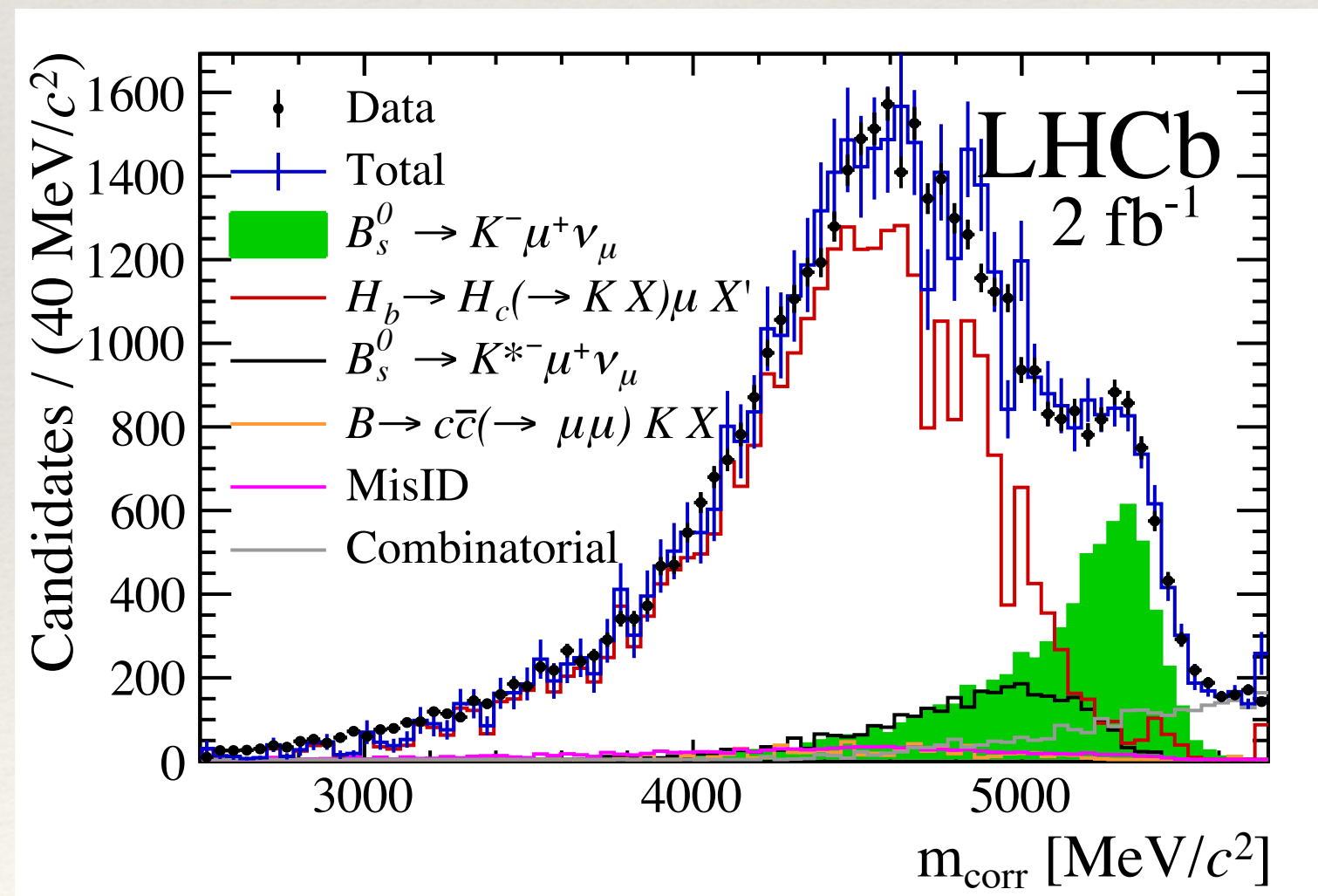
$$a_1^f = -0.002 \pm 0.034 \pm 0.046$$

$$a_2^f = 0.93^{+0.05+0.04}_{-0.20-0.38}$$

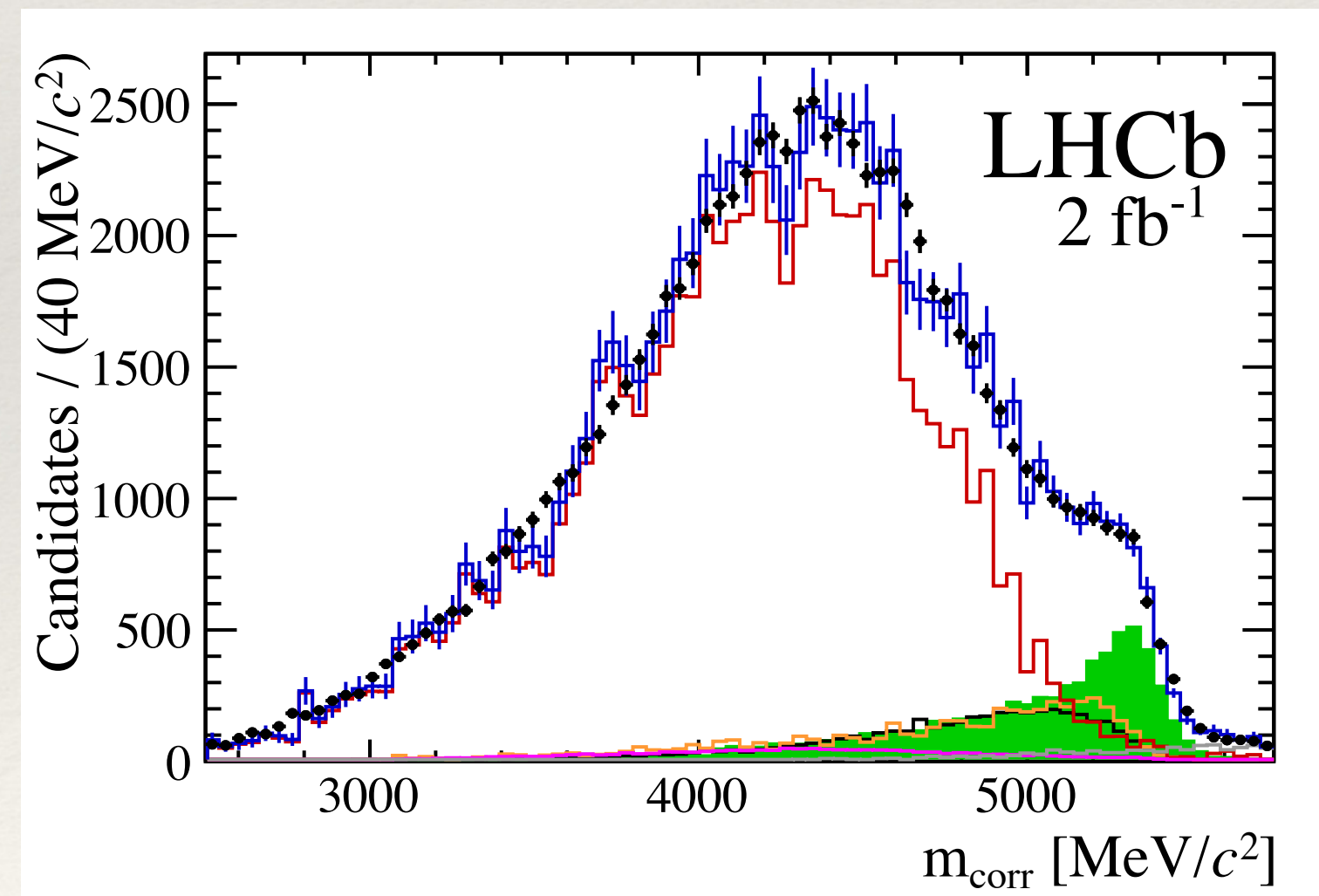
# $V_{ub}/V_{cb}$ from $B_s \rightarrow K^+ \mu^- \nu$

[PRL 126 (2021) 081804]

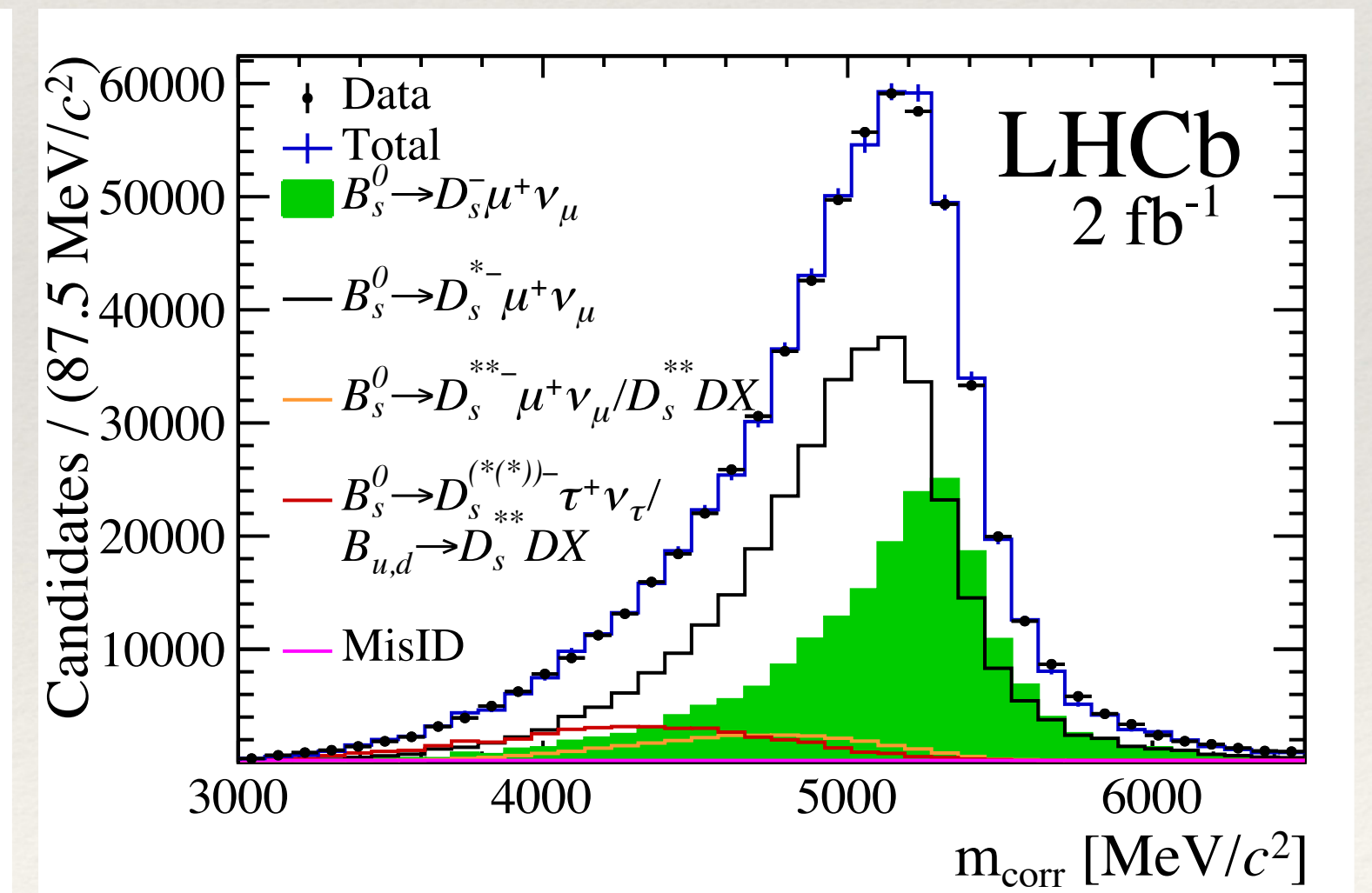
- ❖ Use  $B_s \rightarrow K^- \mu^+ \nu$  decays to measure  $V_{ub}$ . First observation of  $B_s \rightarrow K^- \mu^+ \nu$  decay.
  - ❖ Normalise with  $B_s \rightarrow D_s^- \mu^+ \nu$  so the measurement is  $V_{ub}/V_{cb}$ . Use  $m_{corr}$  to discriminate signal and background.
- ❖ Divide signal in two bins of  $q^2$  with equal number of signal events.



signal at  $q^2 < 7 \text{ GeV}^2$



signal at  $q^2 > 7 \text{ GeV}^2$



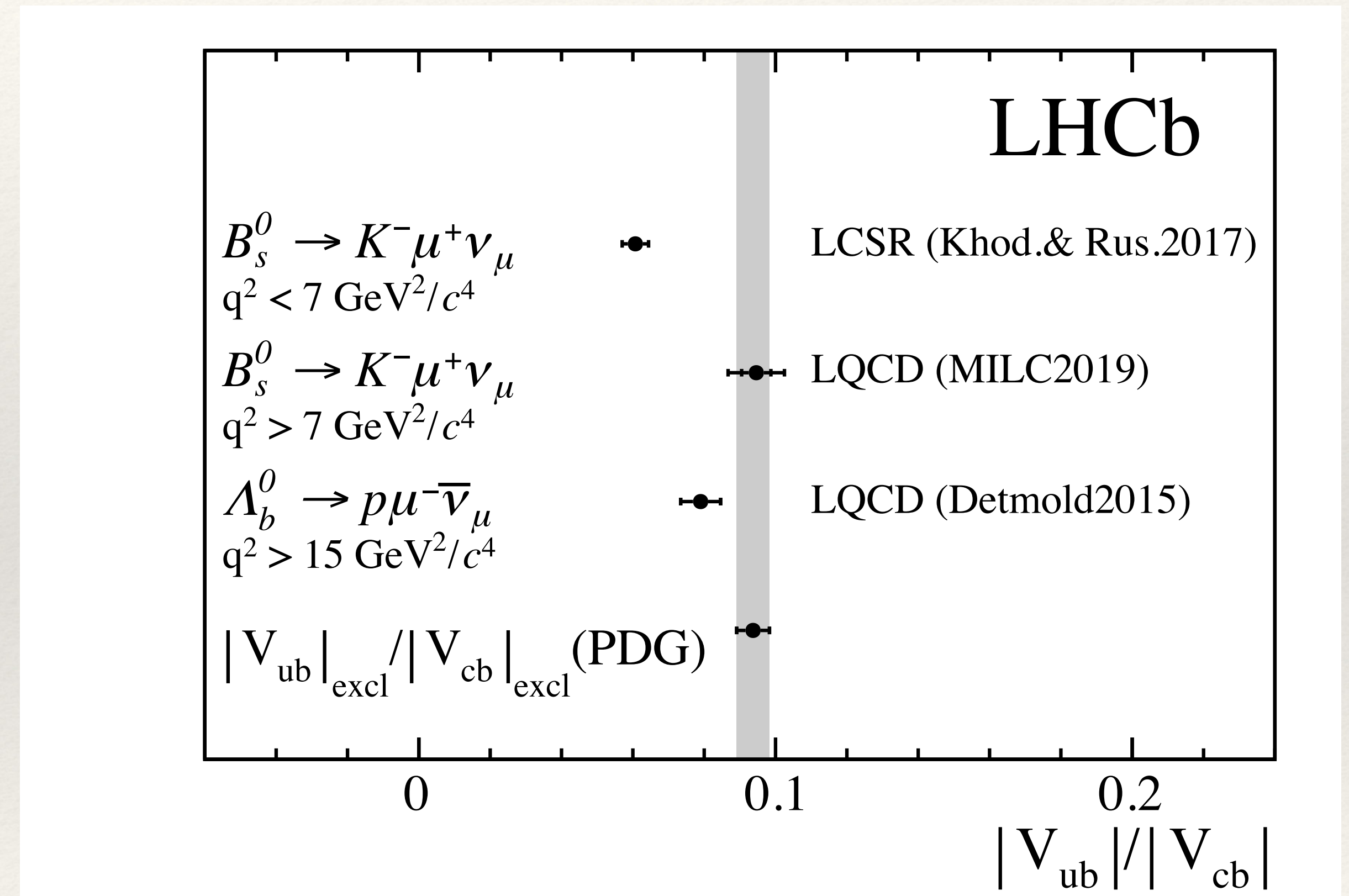
normalisation



# $V_{ub}/V_{cb}$ from $B_s \rightarrow K^+ \mu^- \nu$

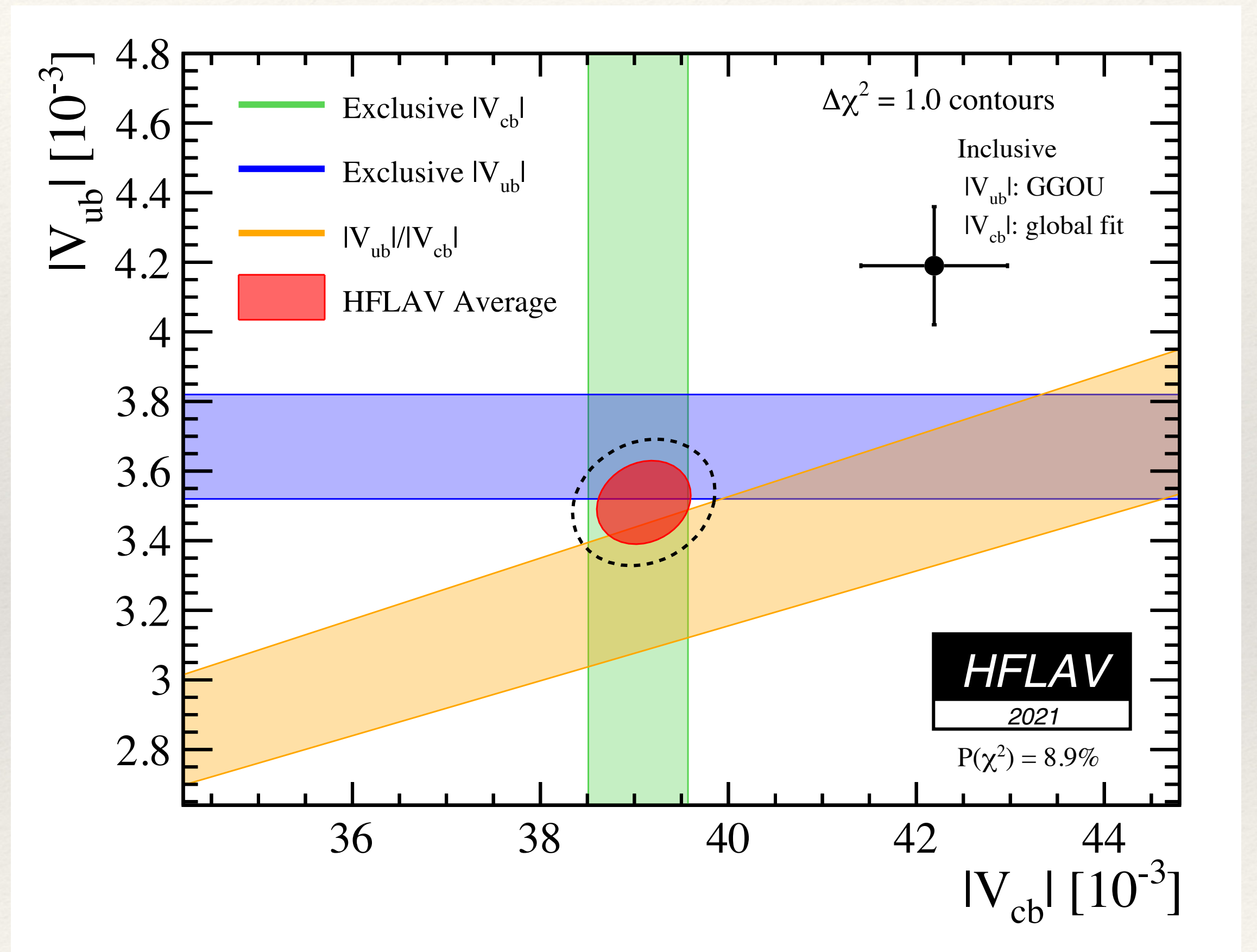
[PRL 126 (2021) 081804]

- ❖ Two different FF predictions for  $B_s \rightarrow K^- \mu^+ \nu$  used to extract  $V_{ub}$ .
- ❖ Low  $q^2$ : LCSR based on [JHEP 08 (2017) 112].
- ❖ High  $q^2$ : LQCD based on [PRD 100 (2019) 034501].
- ❖ Provide two values of  $V_{ub}$ .



# Exclusive $V_{ub}$ vs $V_{cb}$

- ❖ Averaging all the results shown and adding  $V_{ub}$  from  $\Lambda_b \rightarrow p\mu\nu$  normalised to  $\Lambda_b \rightarrow \Lambda_c\mu\nu$  [Nature Phys. 11 (2015) 743].
- ❖ Contains updates on normalisation  $\text{BR}(\Lambda_c \rightarrow pK\pi)$ , and LQCD for  $q^2 > 7 \text{ GeV}^2$
- ❖ Tension between exclusive and inclusive measurements still present.



---

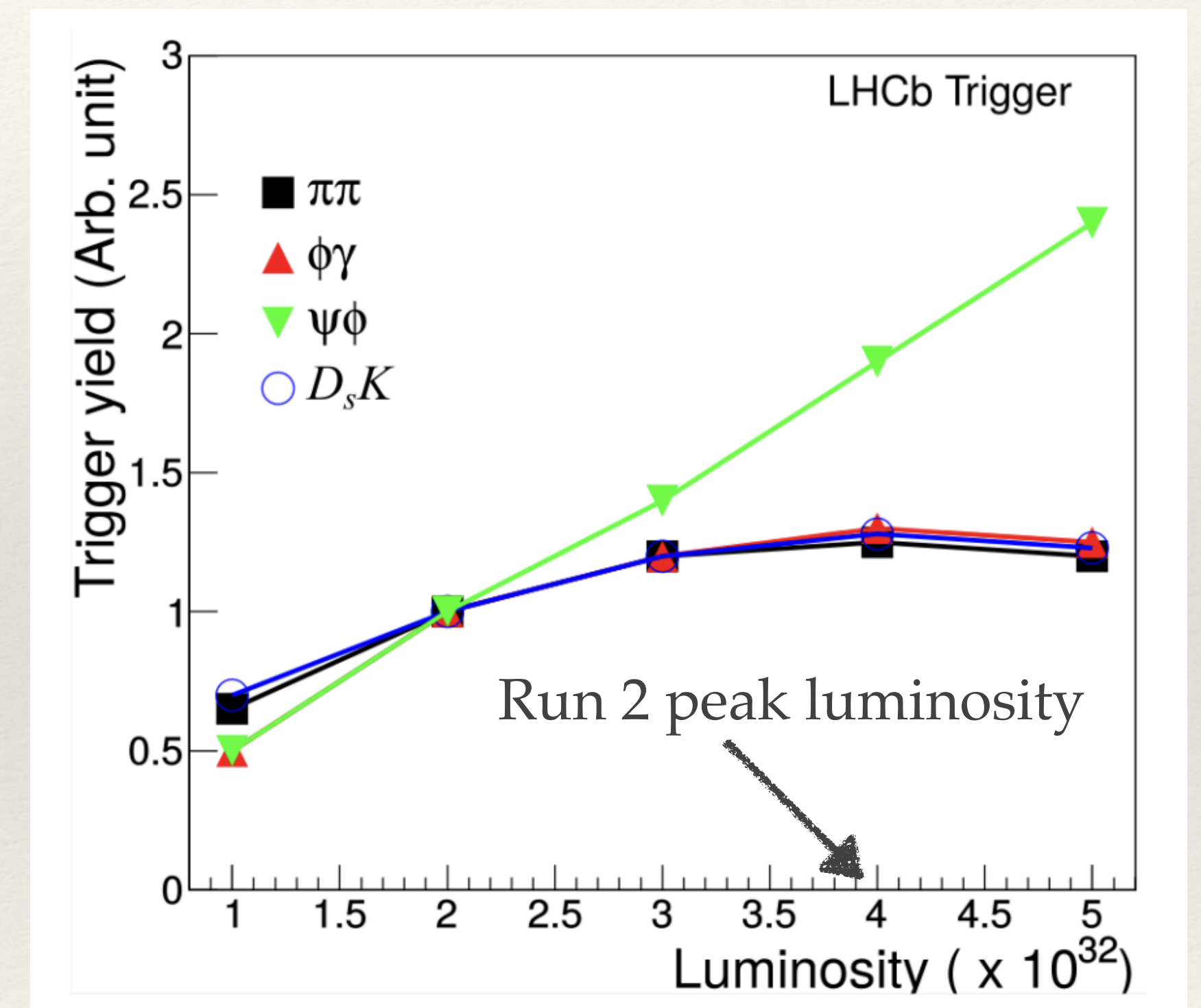
# The future

---

- ❖  $V_{cb}$  from  $\Lambda_b \rightarrow \Lambda_c \mu \bar{\nu}_\mu$ 
  - ❖ Based on PRD 96 (2017) 112005 to measure  $d\Gamma/dq^2$  by fitting the corrected mass in bins of  $q^2$  and compare with lattice predictions to obtain  $V_{cb}$ .
  - ❖ Additionally, will produce a precise measurement of  $BF(\Lambda_b \rightarrow \Lambda_c \mu \nu)$  and get the fraction of inclusive rate going to  $\Lambda_c^*$  ( $N(\Lambda_c^* \mu \nu / \Lambda_c \mu \nu X)$ ).
- ❖  $V_{ub}/V_{cb}$  from  $B_c \rightarrow D^{(*)0} \mu \nu$ 
  - ❖ Normalise to  $B_c \rightarrow J/\psi \mu \nu$ . Use LQCD and QCDSR to get the ratio of FF. [PRD 105, 014503; PRD 102, 094518; JHEP 02 (2020) 171 ]
  - ❖ Analysis strategy formulated to reduce the sensitivity to  $q^2$ . Single fit to  $m_{corr}$

# The LHCb upgrade

- ❖ In Run3 LHCb has removed the hardware trigger, being able to reconstruct in software the 30MHz of visible collisions.
- ❖ The removal of L0 is crucial for hadronic modes as their yield saturated with luminosity.
- ❖ Effects on the majority of  $b \rightarrow c l \nu_l$  decays as the hadrons are (partly) used to select the events.
- ❖ When only muons were used to trigger, now hadrons can provide extra statistics.
- ❖ Hadronic triggers are mandatory to access low  $p_T$  muons.



---

# Conclusions

---

- ❖ Properties of B-hadrons can be studied in LHCb with semileptonic decays with high precision.
- ❖ Several measurements of FF done, fundamental inputs for  $R(X_c)$  measurements.
- ❖ CKM matrix elements  $V_{ub}$ ,  $V_{cb}$  measured exclusively with similar precision as the inclusive.
  - ❖ Long lasting  $\sim 3\sigma$  tension between inclusive and exclusive measurements is still present.
- ❖ Crucial collaboration with the theory community.
- ❖ New measurements of CKM matrix elements ongoing with  $\Lambda_b$  and  $B_c^+$ .
- ❖ Run 3 with the upgraded detector and fully software trigger will provide more data.

# Backup

# Form factors from $B_s \rightarrow D_s^* \mu \nu$ decays

- ❖ The decays  $B_s \rightarrow D_s^* \mu \nu$  are described by four form factors.

EW + phase space contribution

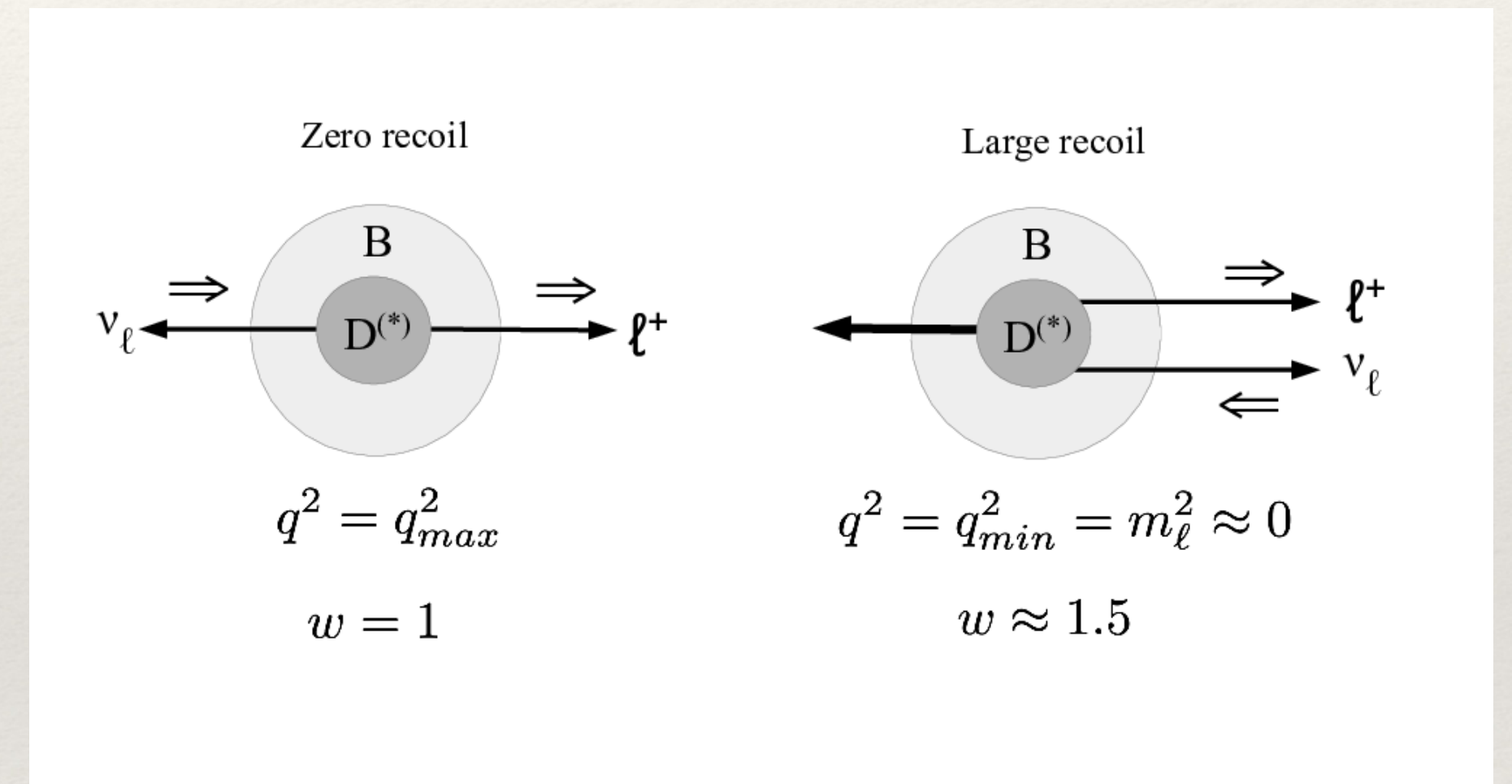
$$\frac{d\Gamma(B_s^0 \rightarrow D_s^{*-} \mu^+ \nu_\mu)}{dq^2} = \frac{G_F^2 |V_{cb}|^2 |\eta_{EW}|^2 |\vec{p}| q^2 \left(1 - \frac{m_\mu^2}{q^2}\right)^2}{96 \pi^3 m_{B_s}^2} \times \left[ (|H_+|^2 + |H_-|^2 + |H_0|^2) \left(1 + \frac{m_\mu^2}{2q^2}\right) + \frac{3}{2} \frac{m_\mu^2}{q^2} |H_t|^2 \right]$$

QCD contribution

- ❖ The helicity amplitudes ( $H_{+,-,0,t}$ ) can be described in terms of the form factors.
- ❖ At the zero recoil point ( $q^2_{\max}$ ) the FF can be computed with precision in LQCD.
- ❖ Experimentally the zero recoil point is not accessible as the phase space vanishes.
  - ❖ Need an extrapolation of the measured distribution of the decay rate to  $q^2_{\max}$ .
  - ❖ The extrapolation relies on the FF parametrisation: CLN [Nucl. Phys. B530 (1998) 153] vs BGL [PRL 74 (1995) 4603, PLB 353 (1995) 306].

# q<sup>2</sup> vs w

- The quantity  $q^2$  represents the di-lepton momentum transfer squared. Commonly used by the experimentalists.
  - Easier to obtain experimentally **after accessing the B momentum.**
- The quantity  $w$  represents the hadron recoil (Lorentz boost of the D meson in the B rest frame). Commonly used by the theorists.
  - Dimensionless and better defined properties in the  $m_{b,c} \gg \Lambda_{\text{QCD}}$  limit ( $w=1$ ).
- Related by  $w = \frac{m_B^+ + m_D^2 - q^2}{2m_B m_D}$ . The **zero recoil point** means  $q^2 = q_{max}^2$  or  $w = 1$ .





# FF results

[JHEP 12 (2020) 144]

