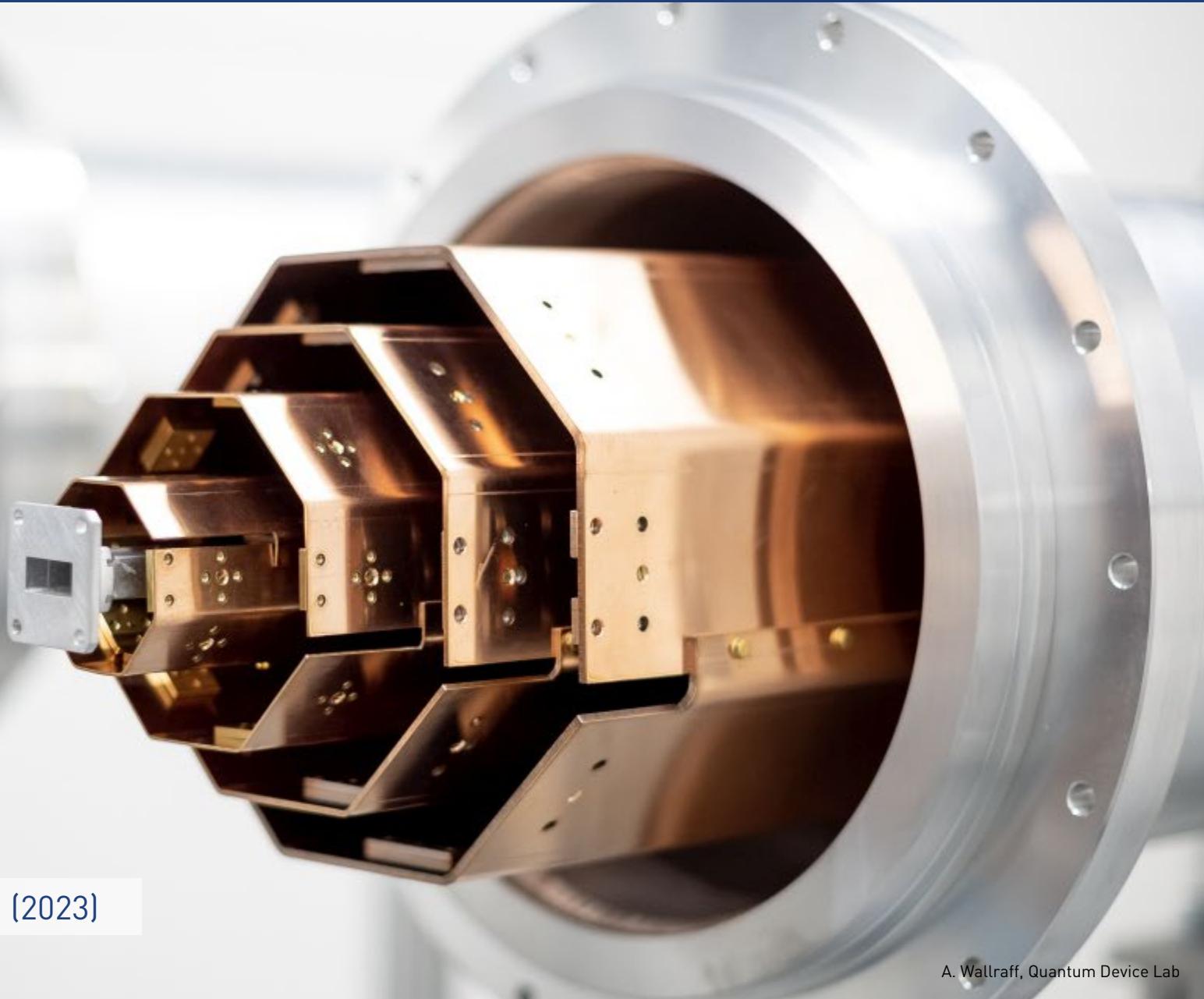




S. Storz et al., Nature **617**, 265-270 (2023)



S. Storz et al., *Nature* **617**, 265-270 (2023)



# Loophole-free Bell Inequality Violation with Superconducting Circuits

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IARPA  
BE THE FUTURE



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[www.qudev.ethz.ch](http://www.qudev.ethz.ch)

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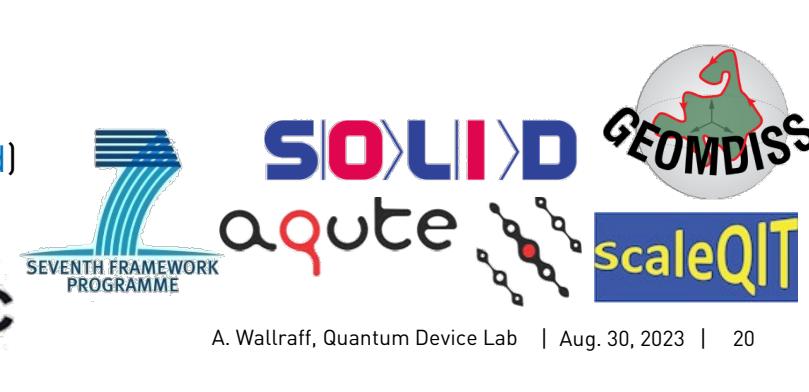
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J. Bylander (Chalmers)  
H. J. Carmichael (Auckland)  
A. Chin (Cambridge)



# Bell Test: Foundations

- Quantum mechanics does not follow the principle of local causality  
A. Einstein, B. Podolsky, N. Rosen, Phys. Rev., 47(10):777-780 (1935)  
N. Brunner et al., Rev. Mod. Phys 86(2) 419--478 (2014)
- Bell, 1964: This property can be tested experimentally  
J.S. Bell, Physics 1:195 (1964)
- A Bell test / non-locality is an important resource  
in *device-independent* quantum information processing
  - Independent verification of quantum devices and networks
  - Secure communication (quantum key distribution)  
U. Vazirani and Thomas Vidick, *Phys. Rev. Lett* 113:140501 (2014)
  - Production of certified random bits  
R. Colbeck, PhD thesis, University of Cambridge (2009)  
S. Pironio *et al.*, *Nature* 464(7291) (2010)  
R. Colbeck and R. Renner, *Nat. Phys.* 8(6):450-454 (2012)  
M. Kessler and R. Arnon-Friedman, IEEE Journal on Selected Areas in Information Theory, 1 no.2, 568-584 (2020)

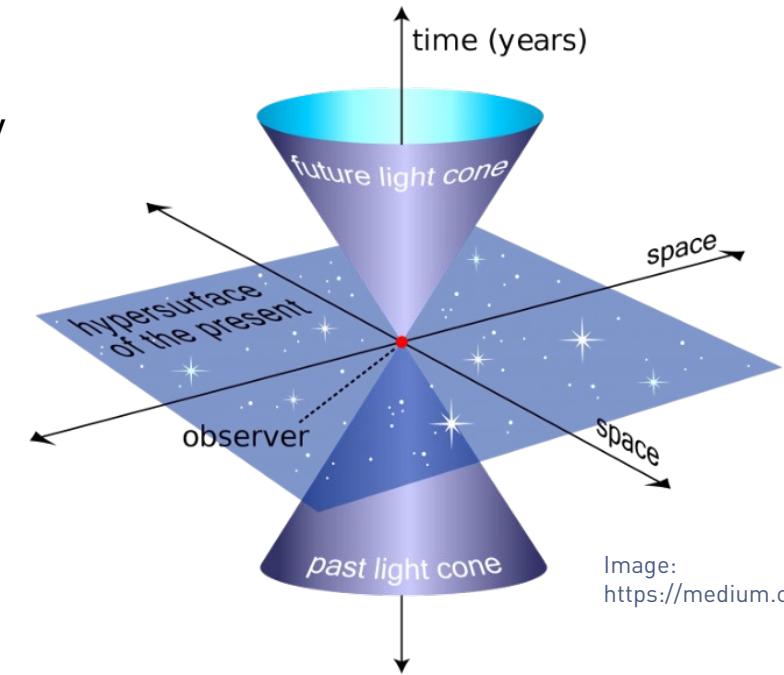


Image:  
<https://medium.com/@felipehime>

**Locality:** Events can only be influenced by actions in their past light-cone

# Bell Test Protocol

Alice and Bob ...

1. ... prepare a shared non-local entangled state  $|\psi^+\rangle = \frac{|g,g\rangle + |e,e\rangle}{\sqrt{2}}$
  2. ... randomly select local measurement bases  $a, b \in \{0,1\}$
  3. ... read out state of qubits with local outcome  $x, y \in \{1, -1\}$
- Repeat steps 1-3

Calculate Clauser-Horne-Shimony-Holt S-value

J.F. Clauser et al., Phys. Rev. Lett., **23** 880-884, (1969)

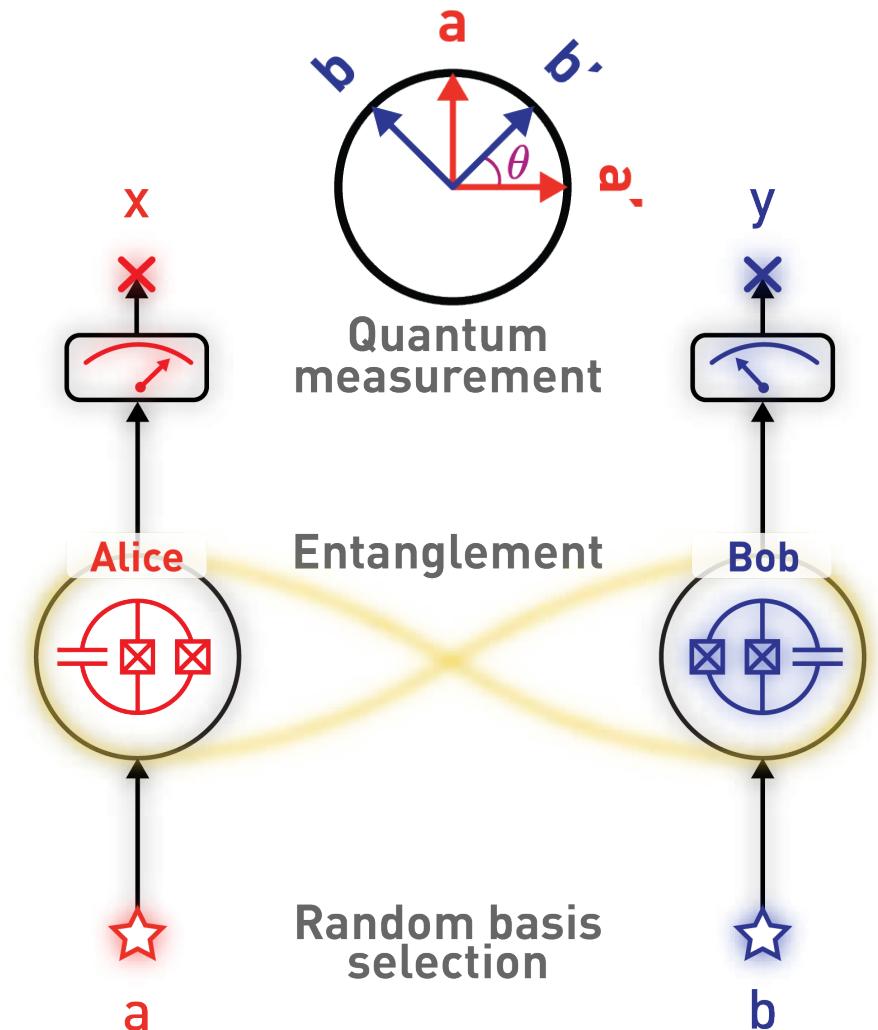
from two qubit correlators  $xy$  with randomly selected basis  $a, b$

$$\langle x \cdot y \rangle_{(a,b)}$$

$$S_{\text{CHSH}} = \langle x \cdot y \rangle_{(0,0)} - \langle x \cdot y \rangle_{(0,1)} + \langle x \cdot y \rangle_{(1,0)} + \langle x \cdot y \rangle_{(1,1)}$$

Expect Bell inequality violation for entangled quantum systems

$$S_{\text{CHSH}} > 2$$



# Closing Loopholes

## The locality loophole

Perform experiments with space-like separation between the entangled qubits being measured and the events defining the basis choice.

N. Brunner et al., Rev. Mod. Phys. 86, 419-478 (2014)

## The detection loophole

Measure each and every Bell-pair created.

A. Garg et al., Phys. Rev. D 35, 3831-3835 (1987)

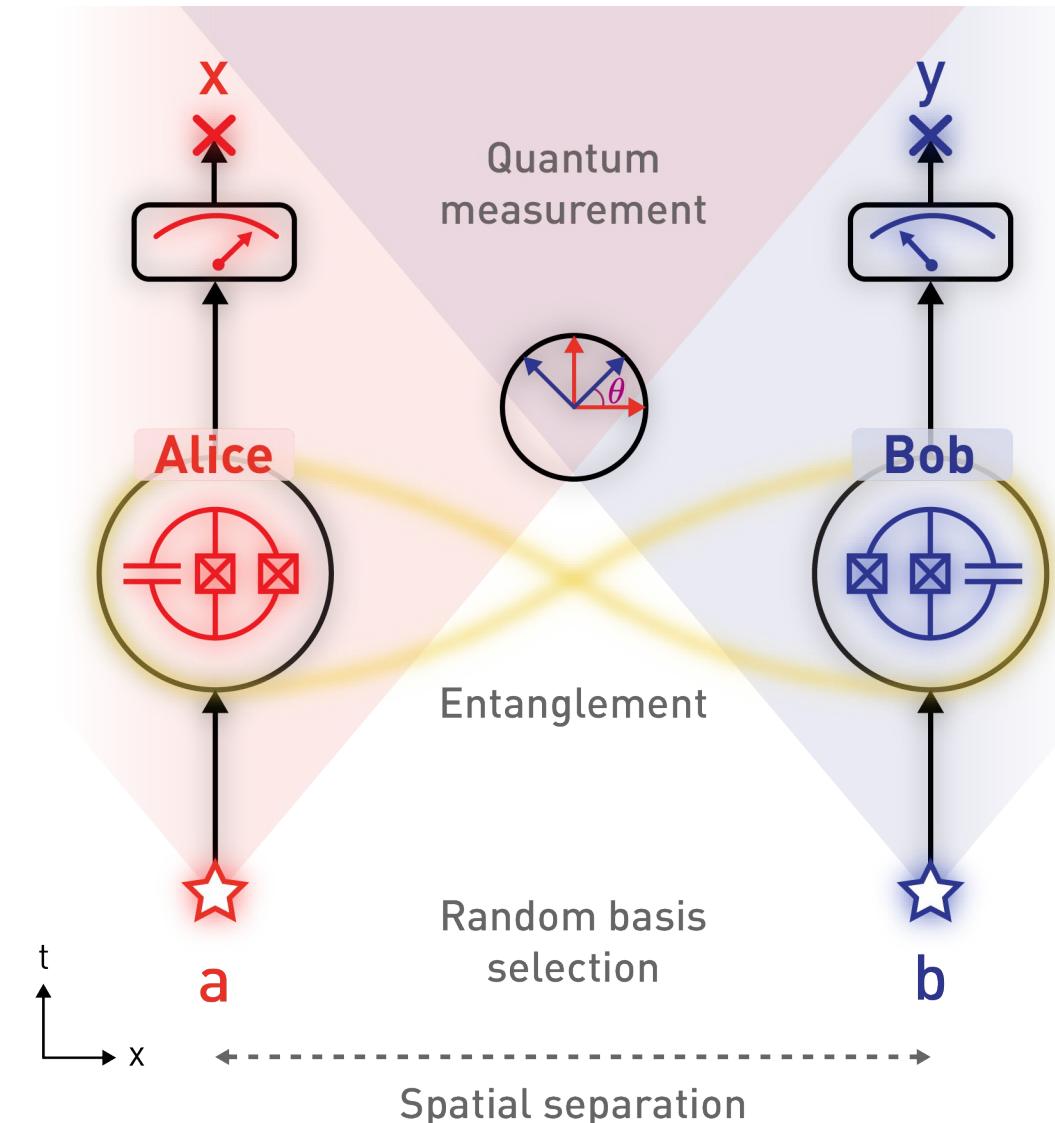
H. Philippe Phys. Rev. A, 47, R747-R750 (1993)

## Freedom-of-choice loophole or Measurement independence

Choose measurement basis statistically independent from the qubits and their measurement devices.

J. S. Bell et al., Cambridge University Press, 2 edition, (2004)

S. Storz et al., Nature 617, 265-270 (2023)



# A Progression of Bell Test Experiments

## A selection of **first experiments**

- 1972: S. J. Freedman, J. F. Clauser, PRL 28:938-941
- 1982: A. Aspect et al., PRL 49(25):1804-1807
- 1982: A. Aspect et al., PRL 49:91-94



relied on additional assumptions  
(were subject to loopholes)

## Many steps taken towards successively closing loopholes

See review: A. Aspect, Closing the Door on Einstein and Bohr's Quantum Debate, Physics 8, 123 (2015).

## Planning of a loophole-free experiment with superconducting circuits

- 2012: At ETHZ; European Research Council (ERC) Advanced Grant (**Superconducting Circuits**)

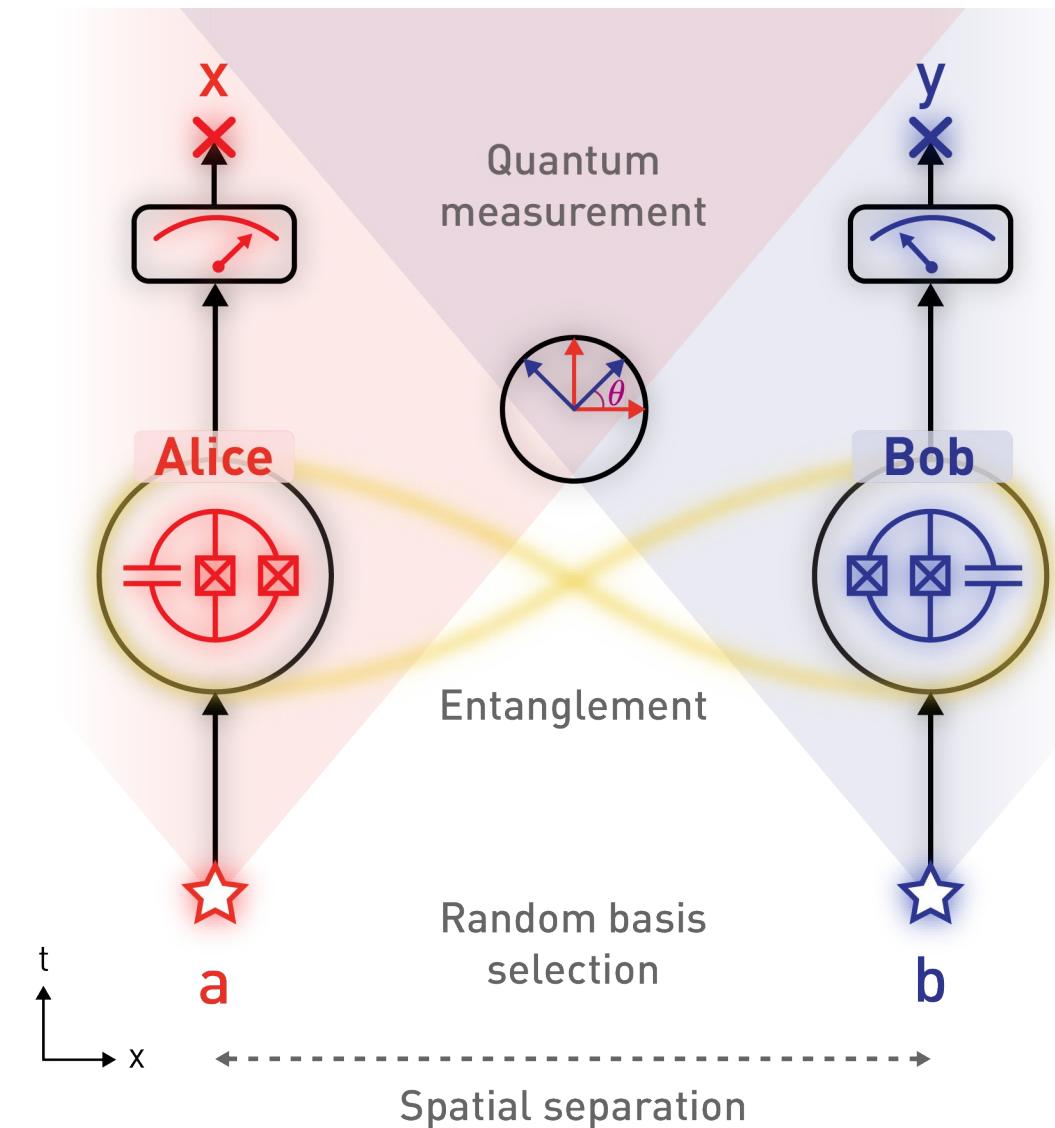
## Successful loophole-free Bell test experiments

- 2015: B. Hensen et al., Nature 526:682-686 (**NV Centers**)
  - M. Giustina et al., PRL 115:250401 (**Photons**)
  - L. Shalm et al., PRL 115:250402 (**Photons**)
- 2017: W. Rosenfeld et al., PRL 119, 010402 (**Neutral atoms**)
- 2018: M. Li et al., PRL 121, 080404 (**Photons**)

# Requirements for a Successful Experiment ...

... with **superconducting circuits**:

- **Reach  $|S_{\text{CHSH}}| > 2$** 
  - high-fidelity entanglement
  - high-fidelity readout of qubits
- **Measurement independence**
  - Choose input bits using random number generators
- **Close detection loophole**
  - Use result of each and every measurement run
- **Close locality loophole**
  - Realize space-like separation between A and B
    - Readout: ~ 50 ns
    - Basis choice: ~ 30 ns
    - Margin & propagation: ~ 20 ns
    - Total: ~ 100 ns
  - **30 m** separation between qubits



# Requirements on Entanglement Fidelity and Readout

Maximum observable  $S_{CHSH}$  value is limited by readout fidelity  $F_r$  and entanglement concurrence  $C$

W. K. Wootters et al., Phys. Rev. Lett. 80, 2245-2248 (1998)

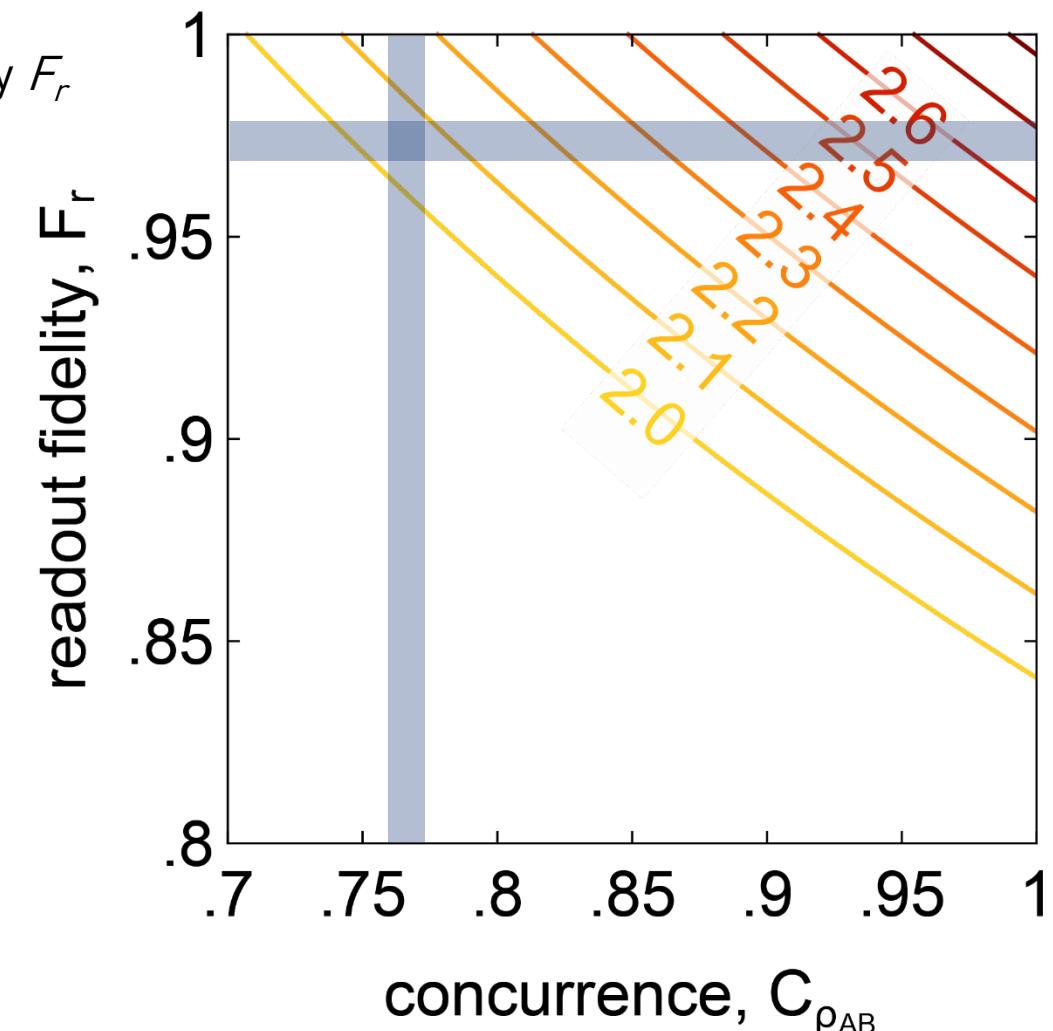
R. Horodecki et al., Physics Letters A 200, 340-344 (1995)

$$S_{CHSH}^{max} = 2\sqrt{2}F_r^2C(\rho_{AB})$$

$S_{CHSH} > 2$  can be realized with available devices

P. Magnard et al., Phys. Rev. Lett. 125, 260502 (2020)

- Concurrence of Bell state  $C(\rho_{AB}) \sim 0.76$
- 50-ns-long single-shot readout with fidelity  $F_r \sim 0.98$

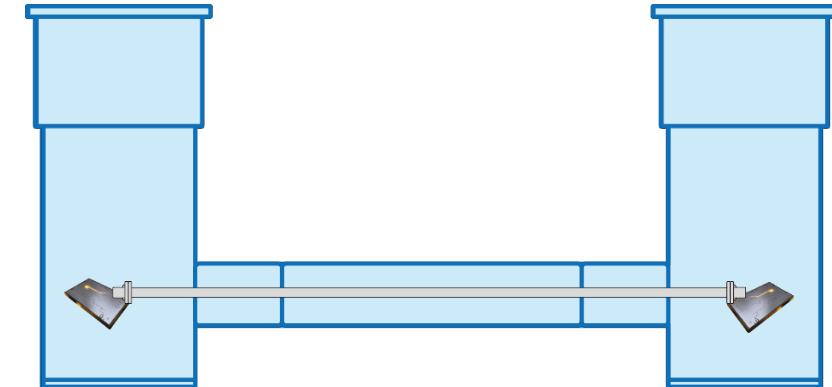


# **How to close the locality loophole with superconducting circuits?**

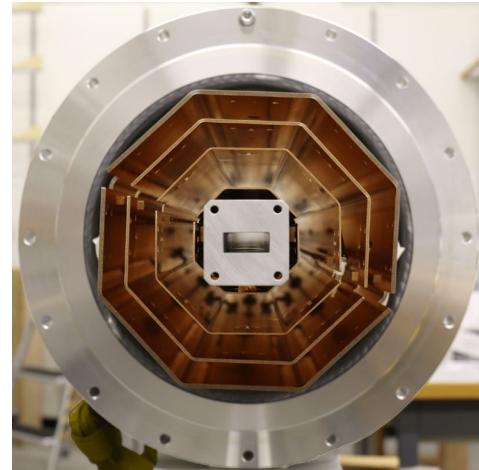
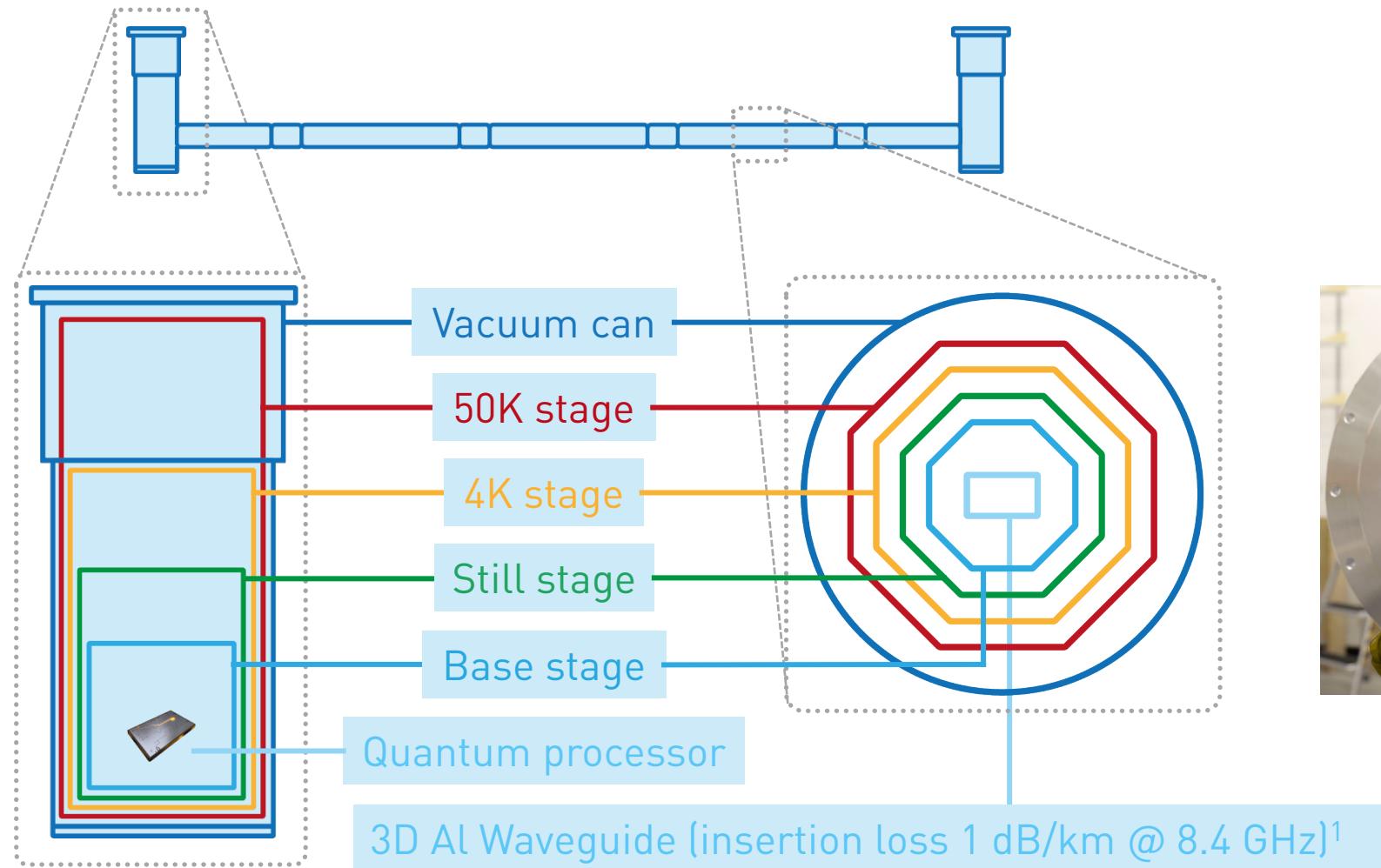
# Quantum Link between two Millikelvin Cryostats

## Desired Features

- Operates at microwave frequencies
  - Through a waveguide or coaxial cable
  - Compatibility with existing gates and protocols
- Operates at mK temperatures (just like on-chip quantum bus)
  - Uses low-loss waveguide (as low as telecom fiber)  
P. Kurpiers et al., *EPJ Quantum Technology* **4**, 8 (2017)
  - No thermal background
- Short cool down time
  - Similar to standard dilution refrigerators (1-2 days)
- Extensible solution
  - Modular design



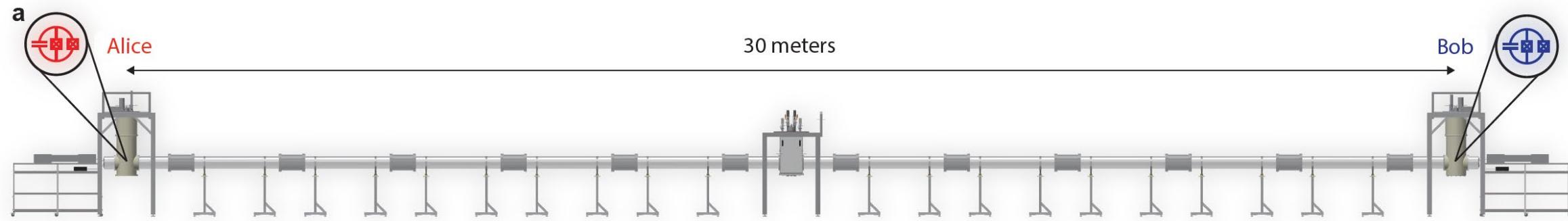
# Concept for Realizing a Cryogenic Microwave Quantum Link



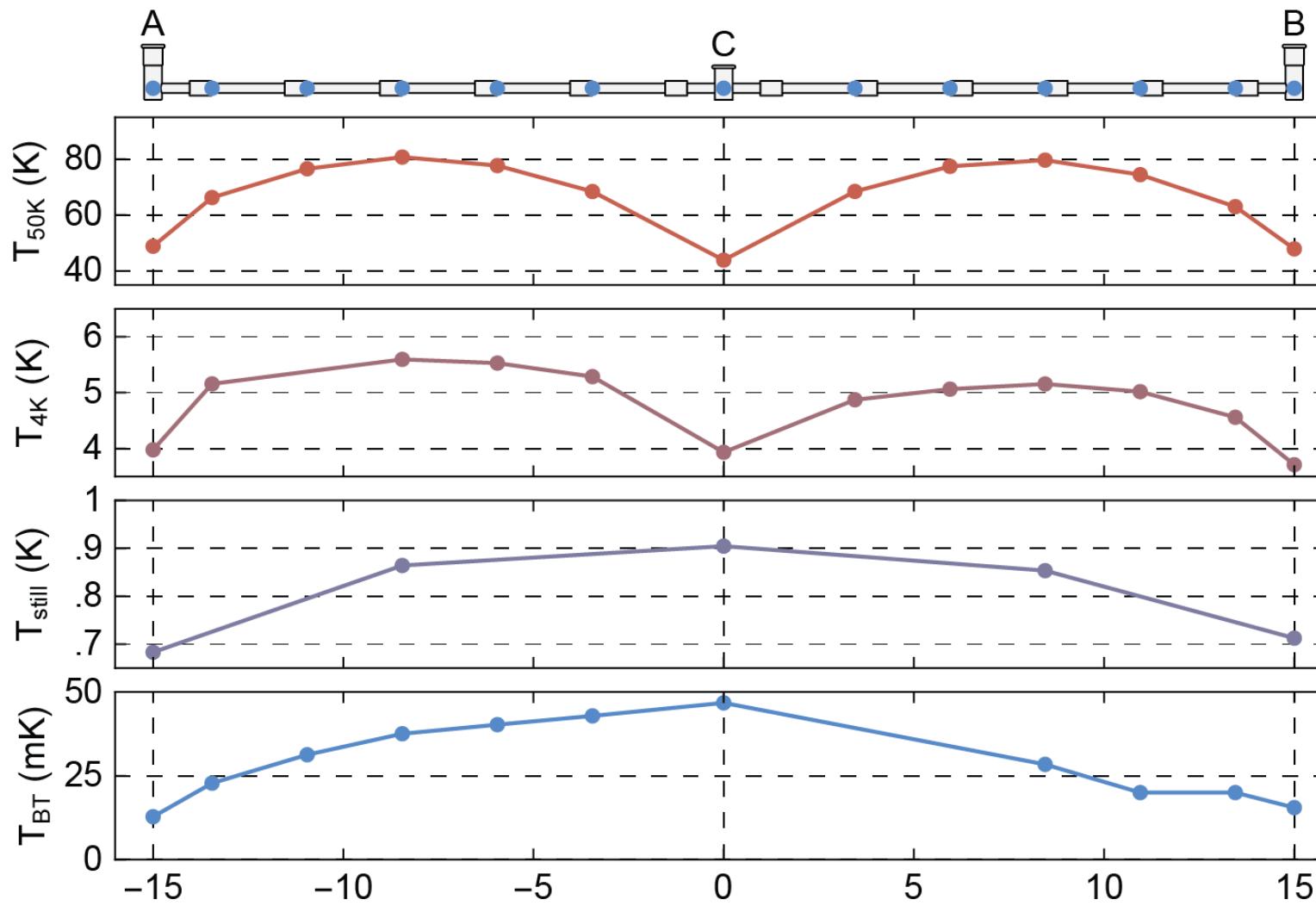
P. Magnard et al., *Phys. Rev. Lett.* **125**, 260502 (2020)

P. Kurpiers et al., *EPJ Quantum Technology* **4**, 8 (2017)

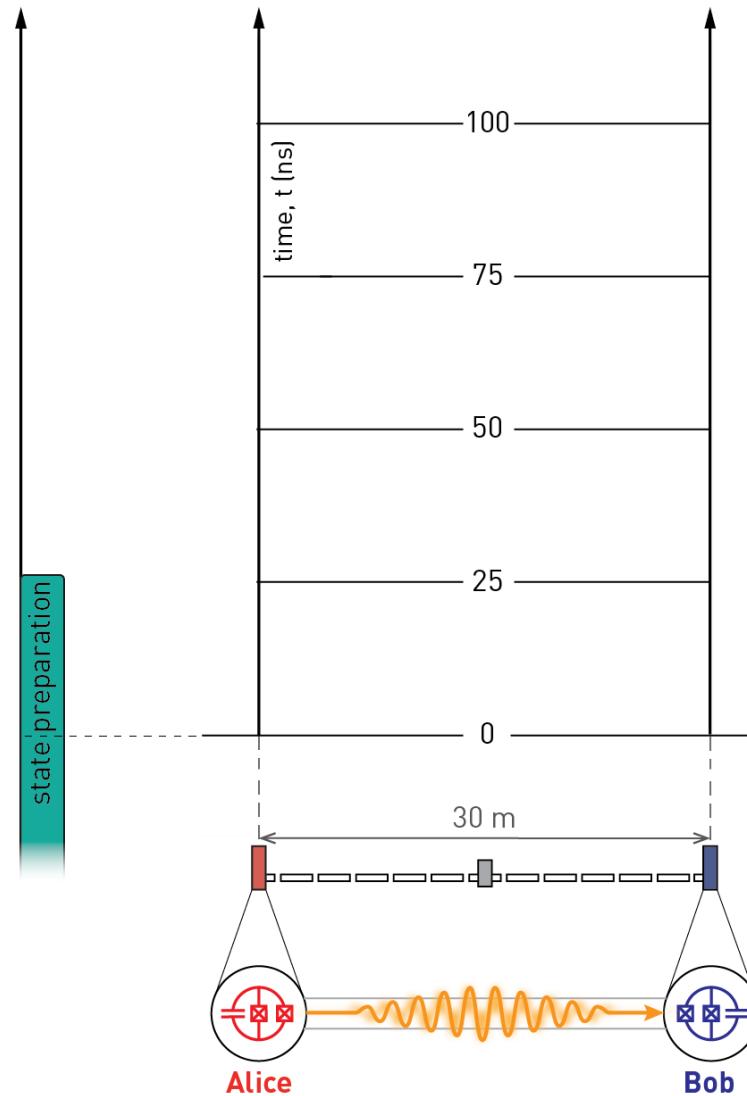
# 30-Meter-Long Cryogenic Microwave Quantum Link



# Temperature Profile of 30-m Cryogenic Link



# Preparation for Bell Test: Entanglement Generation



S. Storz *et al.*, *Nature* **617**, 265-270 (2023)

- Deterministic generation of remote entanglement

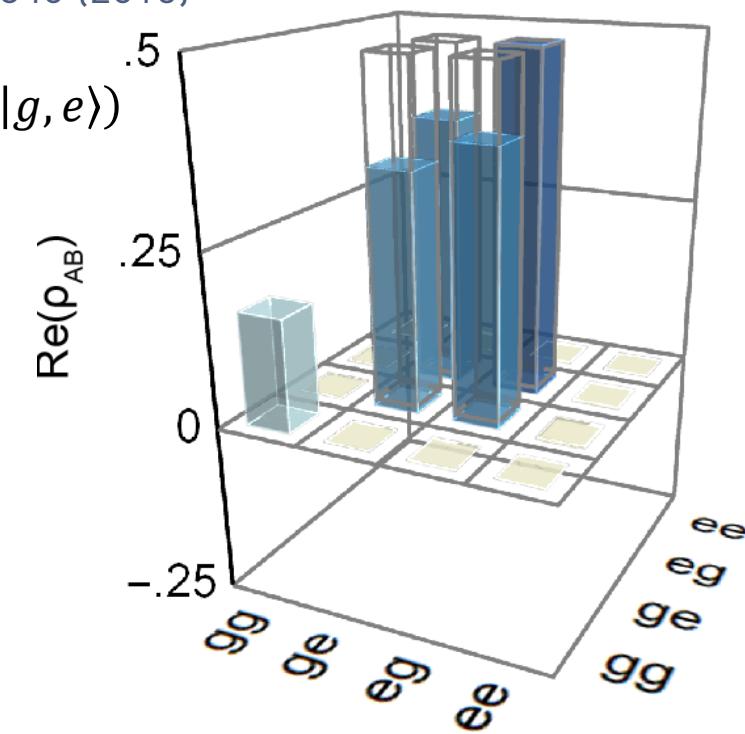
P. Kurpiers *et al.*, *Nature* **558**, 264 (2018)

J.I. Cirac *et al.*, *Phys. Rev. Lett* **78**, 3221-3224 (1997)

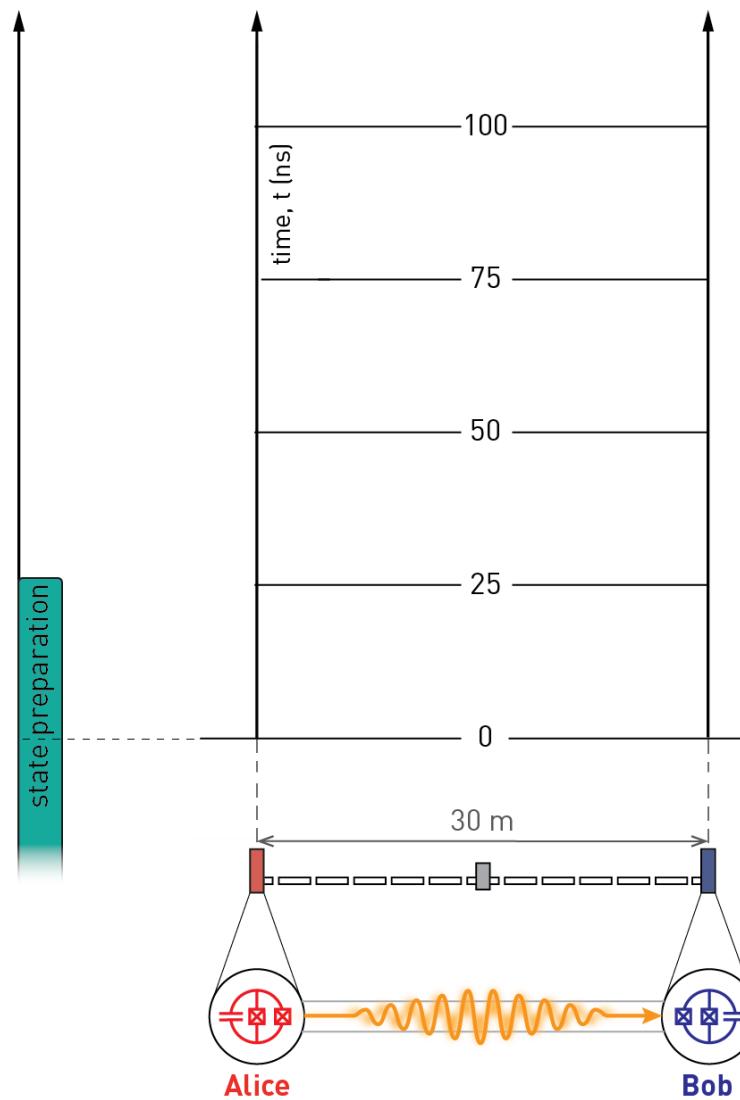
M. Pechal *et al.*, *PRX* **4**, 041010 (2014)

S. Zeytinoglu *et al.*, *PRA* **91**, 043846 (2015)

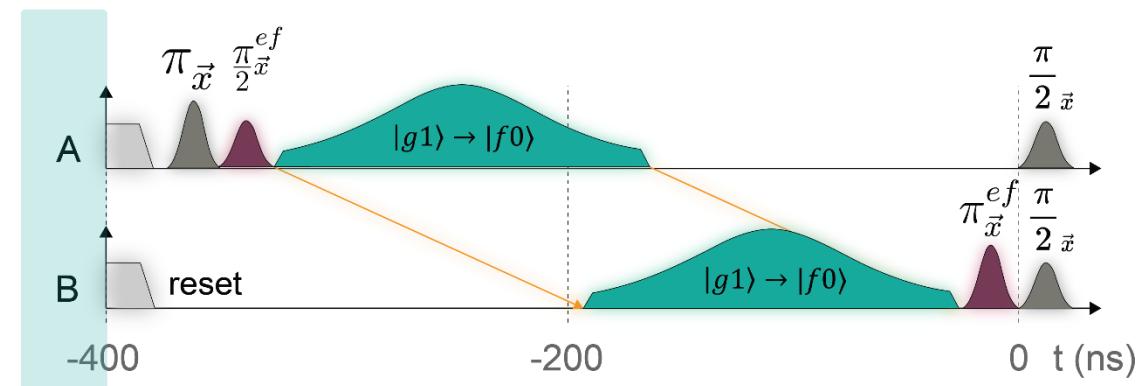
- Bell state  $|\psi^+\rangle = \frac{1}{\sqrt{2}}(|e,g\rangle + |g,e\rangle)$
- Bell state fidelity: 80.4%
- Main source of infidelity: photon loss



# Entanglement Generation: Pulse Sequence



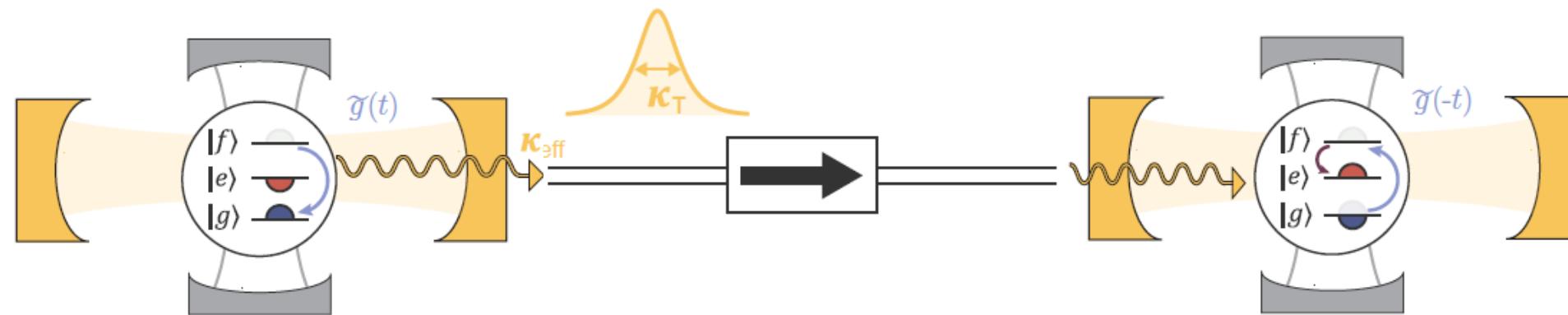
S. Storz et al., *Nature* **617**, 265-270 (2023)



- Excite qubit A from g to e state
- Create superposition of e and f states
- Entangle qubit A with emitted photon
- Reabsorb photon and entangle with qubit B
- Map this state to  $|\phi^+\rangle = \frac{1}{\sqrt{2}}(|g,g\rangle + |e,e\rangle)$

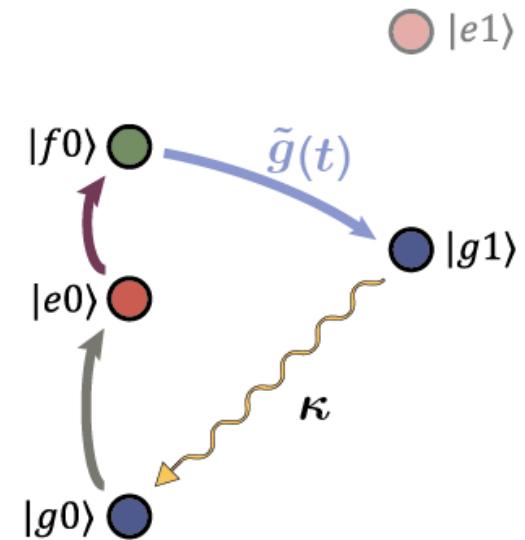
P. Kurpiers et al., *Nature* **558**, 264 (2018)  
 J.I. Cirac et al., *Phys. Rev. Lett* **78**, 3221-3224 (1997)

# Generating Entanglement Between Remote Qubits



## Emitter node:

- Qubit coupled to a transfer resonator
- Sideband transition
- $\tilde{g}(t) \rightarrow$  time-symmetric photon



## Receiver node:

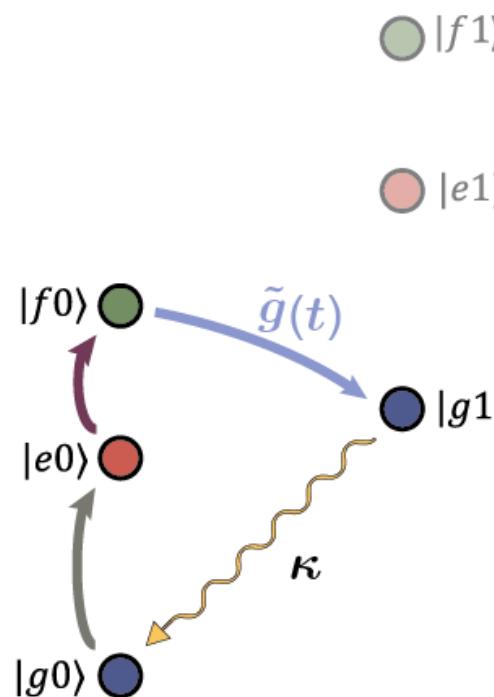
- Identical chip
- Time-reversed drive  $\tilde{g}(-t)$
- Unit absorption

I. Cirac *et al.*, PRL 78, 3221 (1997)

P. Kurpiers\*, P. Magnard\* *et al.* Nature 558, 264-267 (2018)

# Time-Reversal Symmetric Photon Emission

## Cavity QED



$$H_{\text{eff}} = \tilde{g}(t)|g, 1\rangle\langle f, 0| + h.c$$

$$\tilde{g}(t) \propto g\Omega(t) e^{i\phi}$$

M. Pechal *et al.*, Phys. Rev. X 4, 041010 (2014)

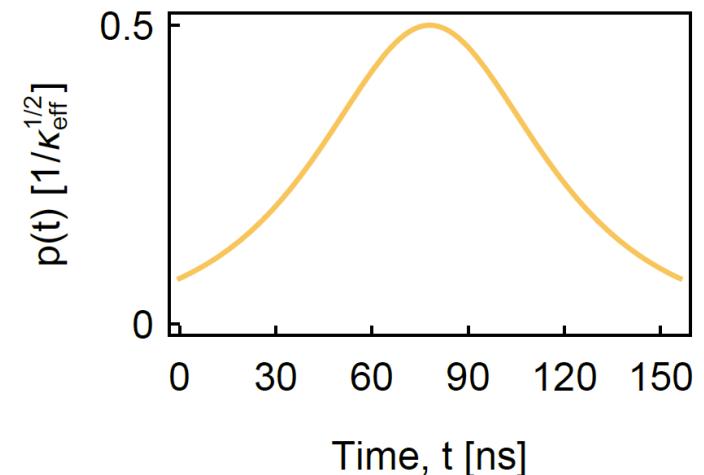
S. Zeytinoglu *et al.*, Phys. Rev. A 91, 043846 (2015)

P. Magnard *et al.*, Phys. Rev. Lett. 121, 060502 (2018)

- Strong coupling
- Detuned dressed state level diagram

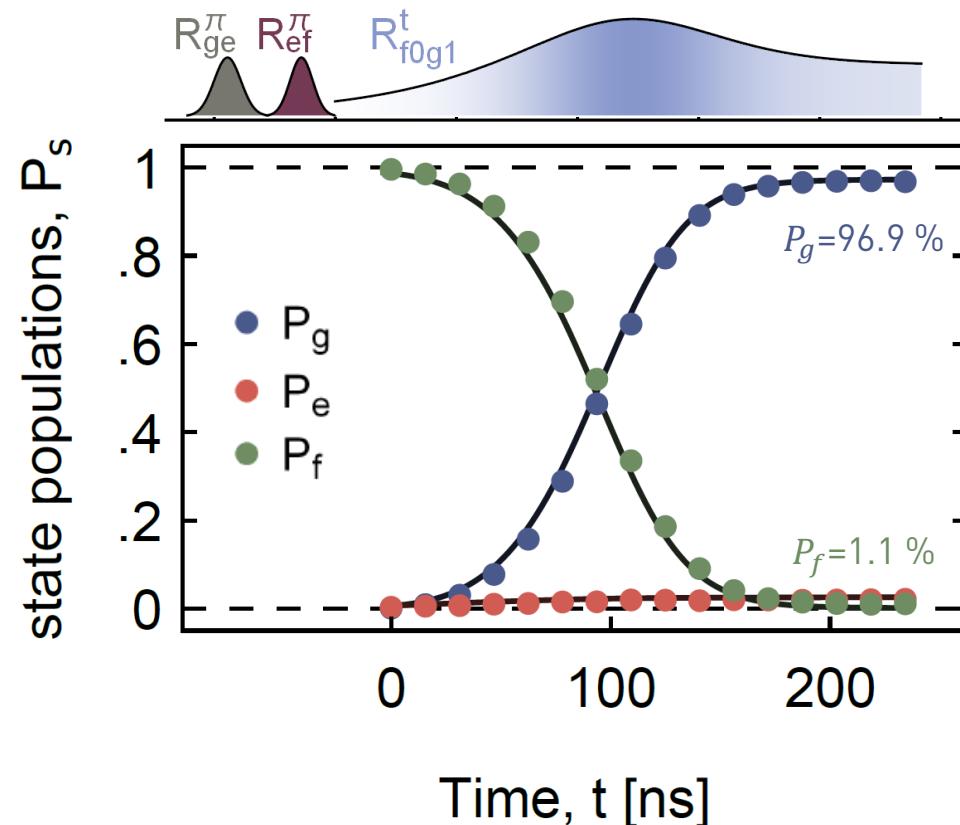
- time-symmetric photon with envelope

$$\frac{\sqrt{\kappa_{\text{eff}}}}{2 \cosh(\kappa_{\text{eff}} t/2)}$$

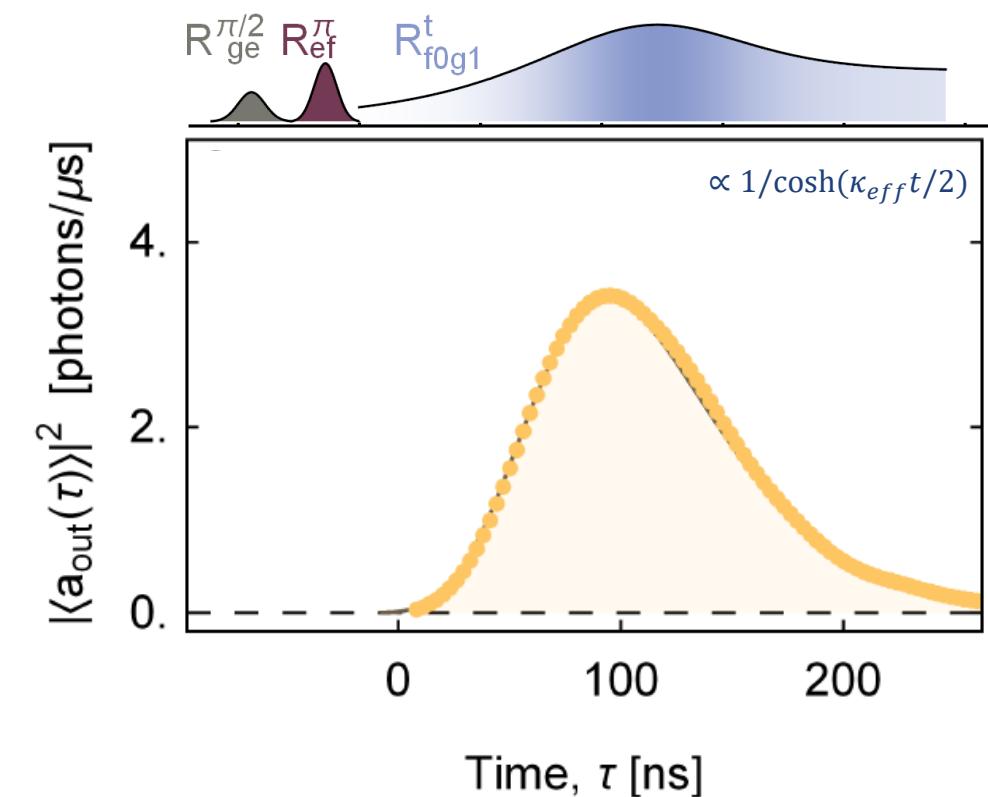


# Example of Qutrit Population Dynamics upon Photon Emission

Qutrit population at node B:

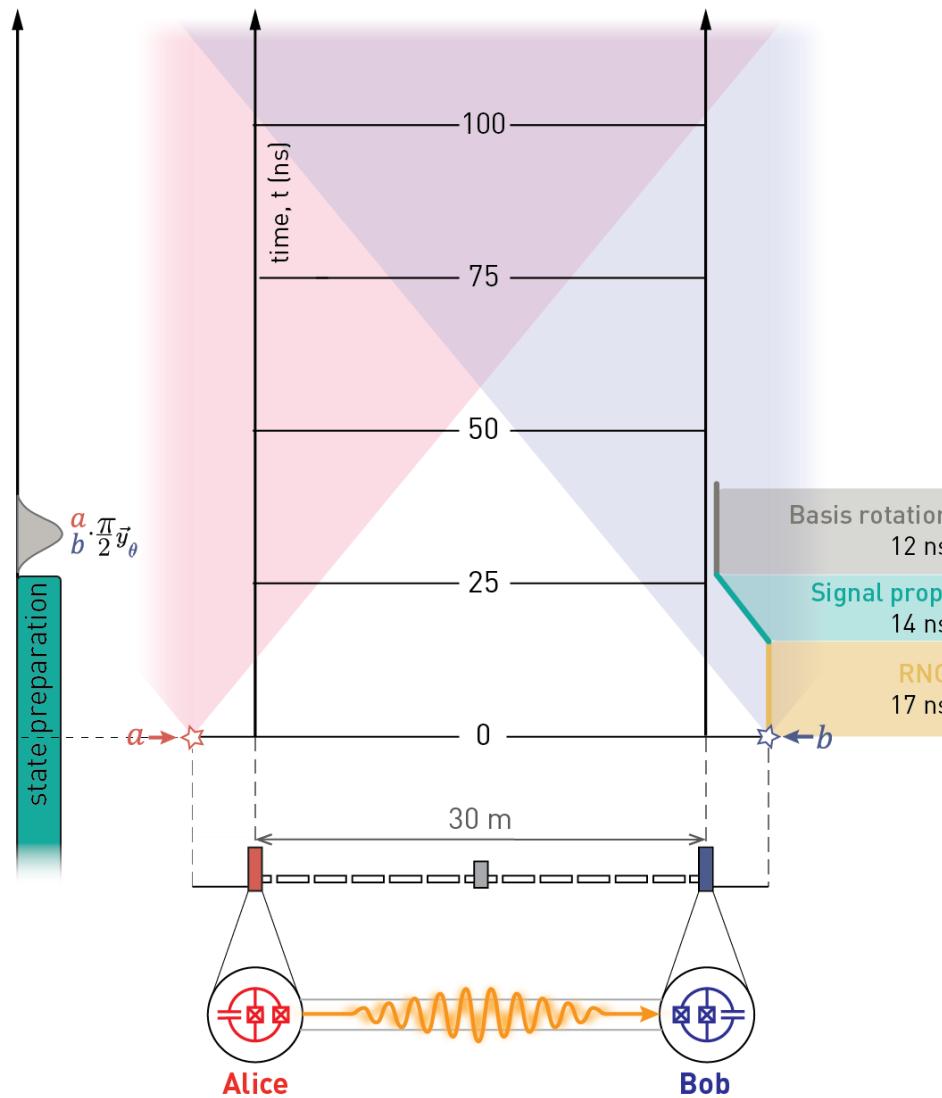


Envelope of emitted photon:

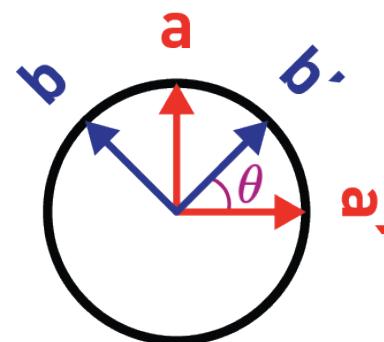


- Excellent agreement with master equation simulation

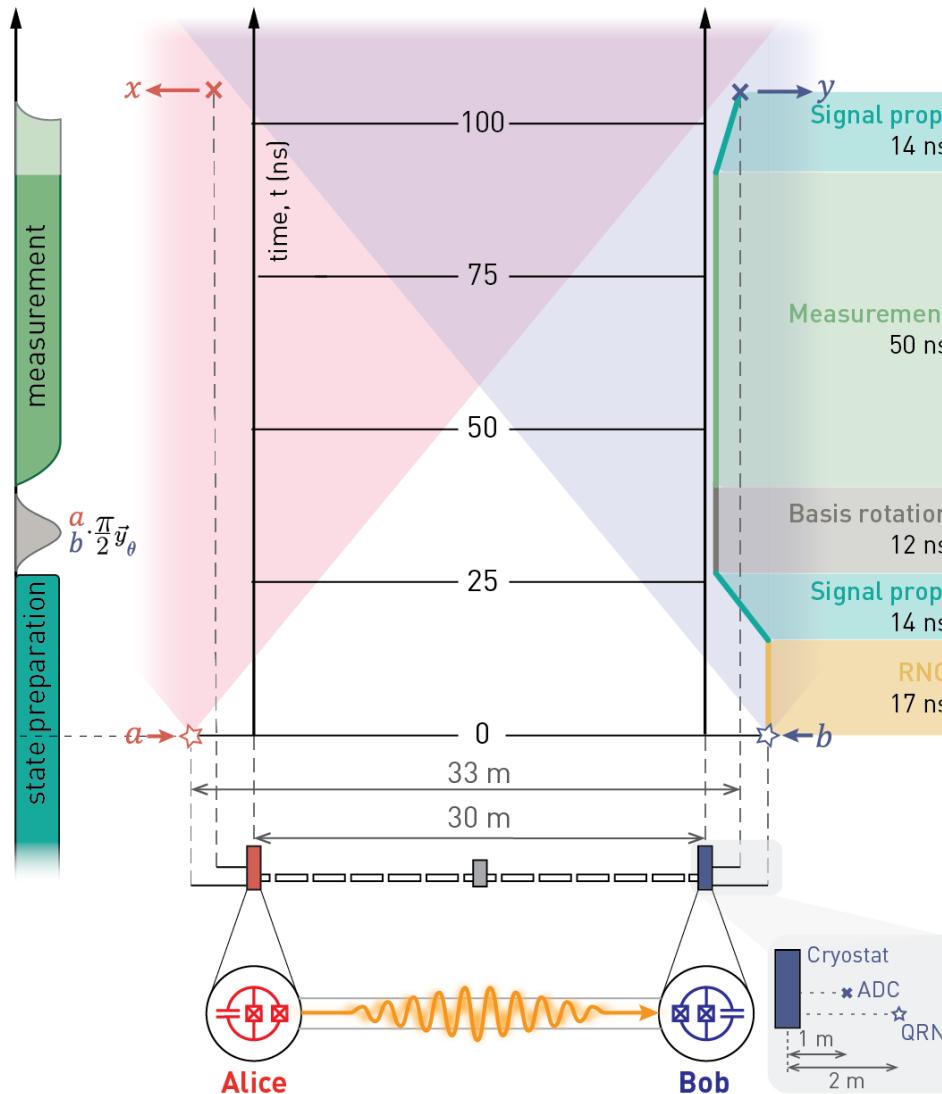
# Start of Bell Test: Random Basis Selection



- Select input bits  $a, b$  using random number generators (bit generation time 17 ns)  
C. Abellan *et al.*, *Phys. Rev. Lett.* **115**, 250403 (2015)
- $a, b$  control the measurement basis choices
- Measurement basis choice is physically implemented using a microwave switch (signal propagation delay 14 ns) ...
- ... applying (or not) a  $\pi/2$  pulse (duration of 12 ns) to the qubit



# Finalizing the Bell Test: Qubit Readout



- Perform single-shot qubit readout
    - ... in 50 ns
    - ... with high readout fidelity 98%

T. Walter *et al.*, *Phys. Rev. Applied* 7, 054020 (2017)
  - Record readout signal with ADC (propagation delay 14 ns)
  - Assign integrated readout signal to local measurement outcome at each qubit, either
- $|g\rangle \rightarrow x = +1$
- or
- $|e\rangle \rightarrow x = -1$

# Reminder: Bell Test Protocol

Alice and Bob ...

1. ... prepare a shared non-local entangled state  $|\psi^+\rangle = \frac{|g,g\rangle + |e,e\rangle}{\sqrt{2}}$
  2. ... randomly select local measurement bases  $a, b \in \{0,1\}$
  3. ... read out state of qubits with local outcome  $x, y \in \{1, -1\}$
- Repeat steps 1-3

Calculate Clauser-Horne-Shimony-Holt S-value

J.F. Clauser et al., Phys. Rev. Lett., 23(15):880-884, Oct 1969

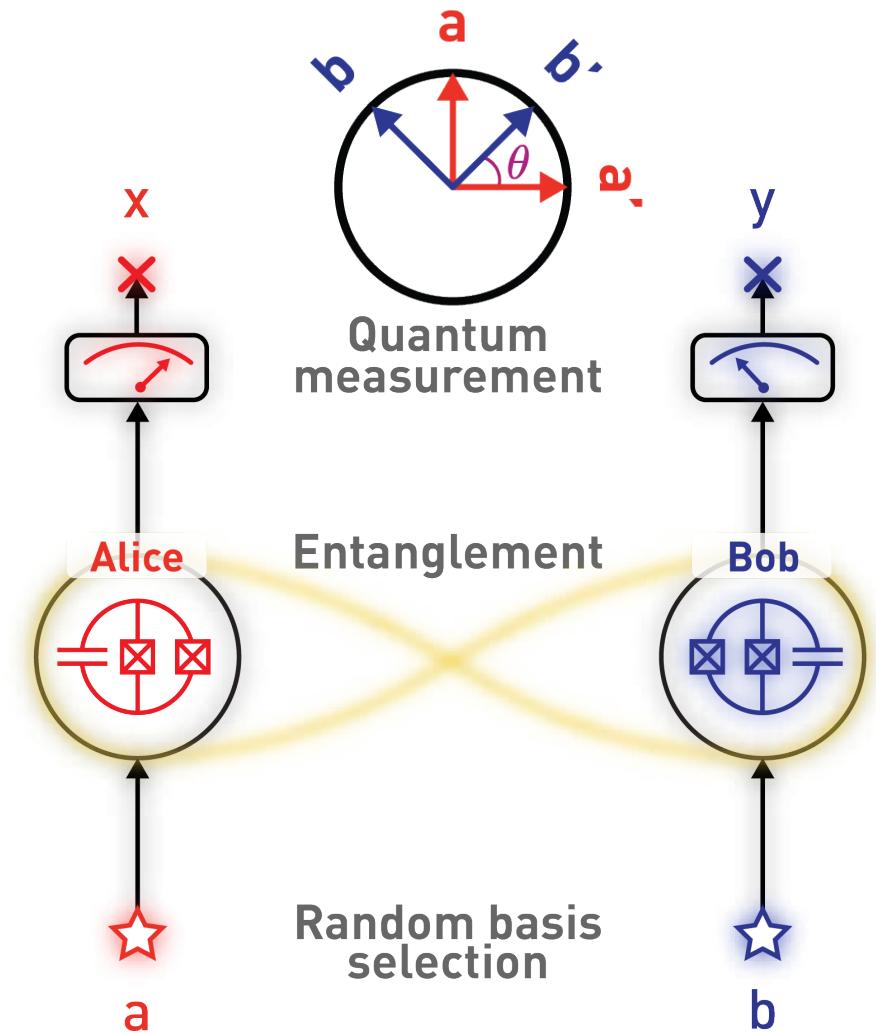
from two qubit correlators  $xy$  with randomly selected bases  $a, b$

$$\langle x \cdot y \rangle_{(a,b)}$$

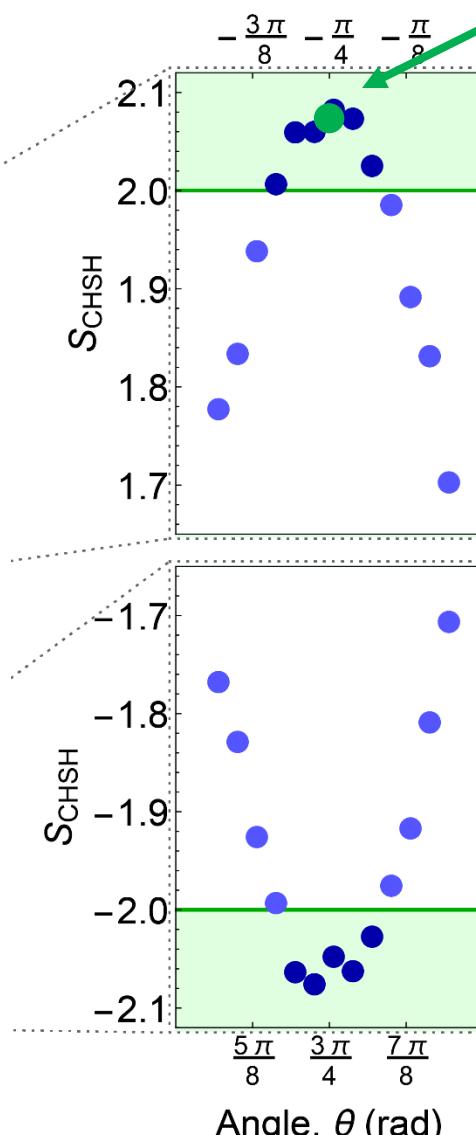
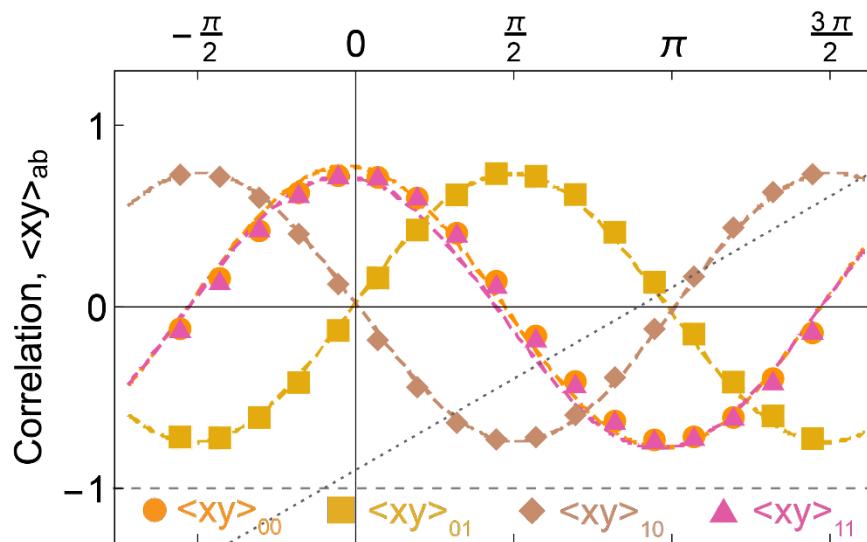
$$S_{\text{CHSH}} = \langle x \cdot y \rangle_{(0,0)} - \langle x \cdot y \rangle_{(0,1)} + \langle x \cdot y \rangle_{(1,0)} + \langle x \cdot y \rangle_{(1,1)}$$

Expect Bell inequality violation for entangled quantum systems

$$S_{\text{CHSH}} > 2$$



# Experimental Results



$$S = 2.0747 \pm 0.0033 > 2$$

- Determine correlators from msrmnts
  - Sinusoidal oscillations
  - Contrast slightly reduced from 1
- Calculate  $S_{\text{CHSH}}$ -value
  - Observe  $S_{\text{CHSH}} > 2$
- Good agreement with Master equation simulation (---)
- Repeat experiment at maximum violation
- Perform experiment at optimal angle
  - $2^{20} (\sim 10^6)$  repetitions
- Violates Bell inequality by
  - $22 \sigma$
  - p-value of  $p = 10^{-108}$

S. Storz et al., Nature 617, 265-270 (2023)

# Addressing the Loopholes

## Freedom-of-choice loophole

Closed by choosing measurement basis at random using RNGs

## Detection loophole

Closed by taking into account each and every measurement result

## Locality loophole

Closed by measurements of the space-time distance of the start & stop events:

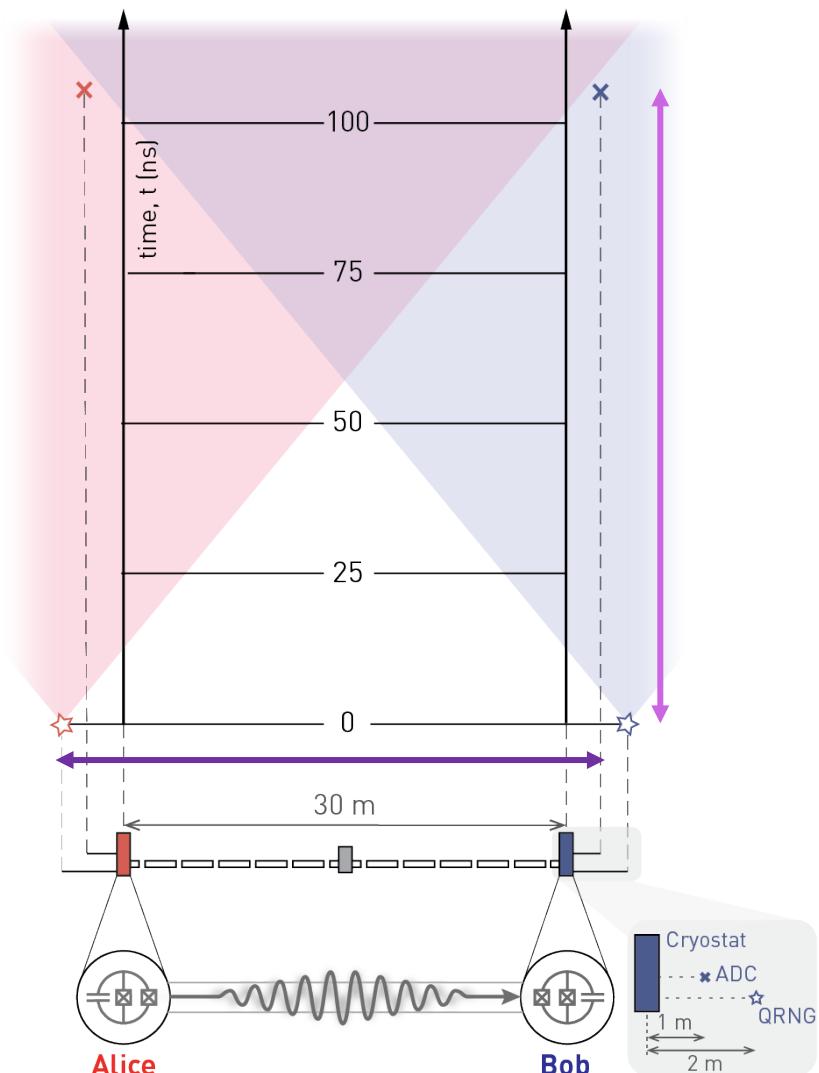
Distance between start & stop events =  $32.824 \pm 0.05$  m

Time budget: =  $109.48 \pm 0.02$  ns

Protocol duration: =  $107.4 \pm 0.25$  ns

Margin: = 2.08 ns

→  $8\sigma$  (std. devs.)



# Bell Violation (S-2) and Repetition Rates of Loophole-Free Bell Tests 0.82 (max)

## Comparison of Bell tests with

- **polarization-encoded photons** ▲

High repetition rates, low S-value

- **NV-centers ♦/ neutral atoms** ○

Low repetition rates, high S-value

- **superconducting circuits** ●

Combination of high repetition rates *and* S-value

- **High rate and high violation** is interesting for implementation of device-independent QIP protocols

- Quantum key distribution

U. Vazirani and Thomas Vidick, *Phys. Rev. Lett.* 113:14050

- Randomness generation

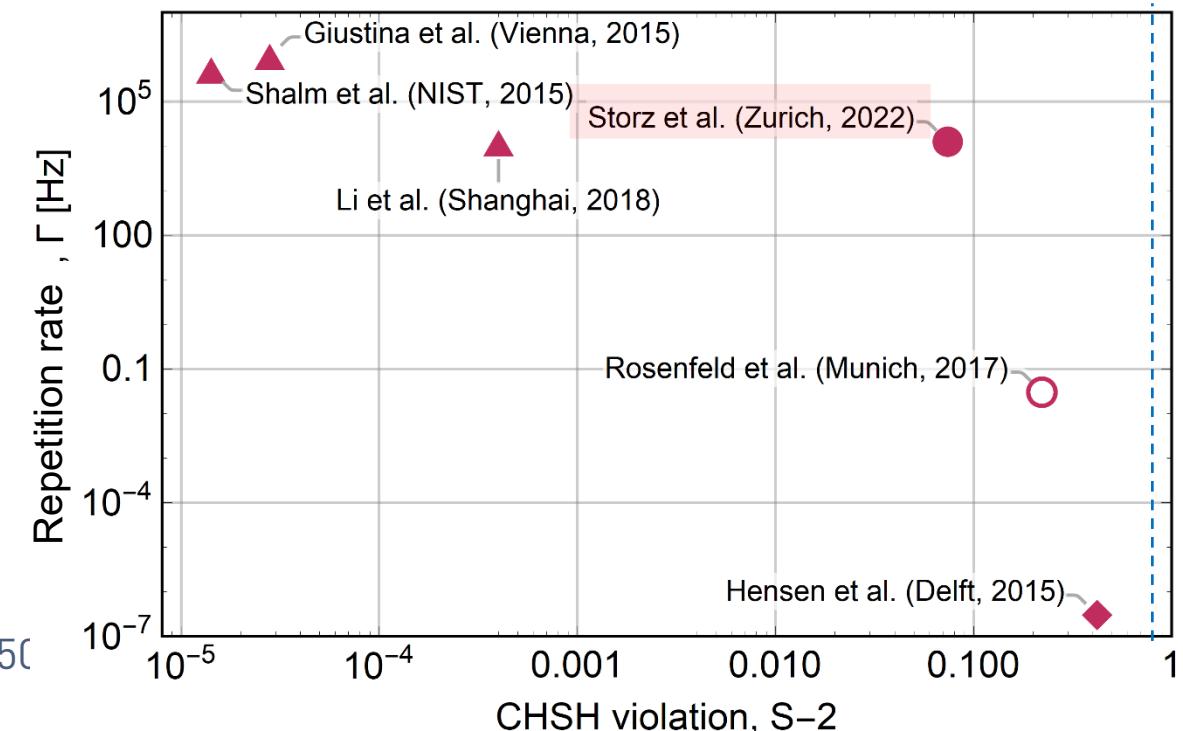
R. Colbeck, *PhD thesis*, University of Cambridge (2009)

- Randomness expansion

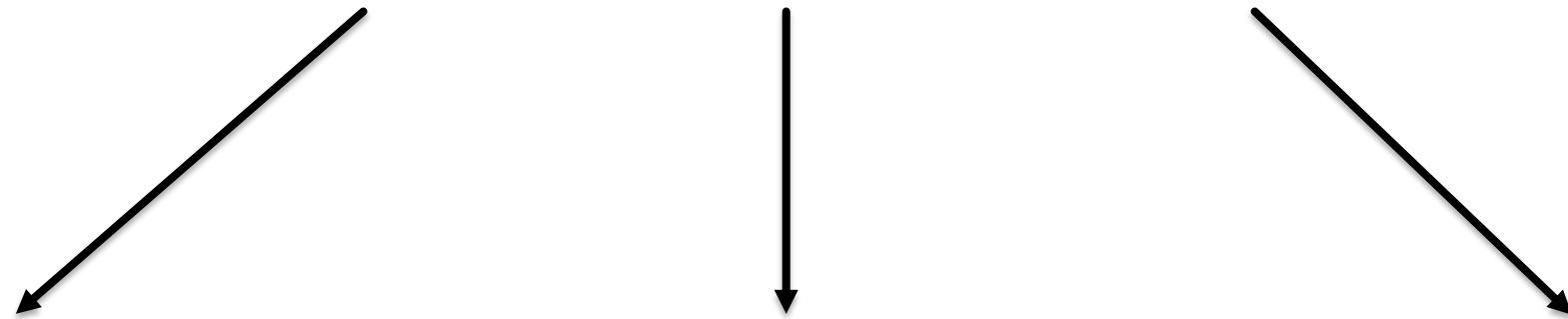
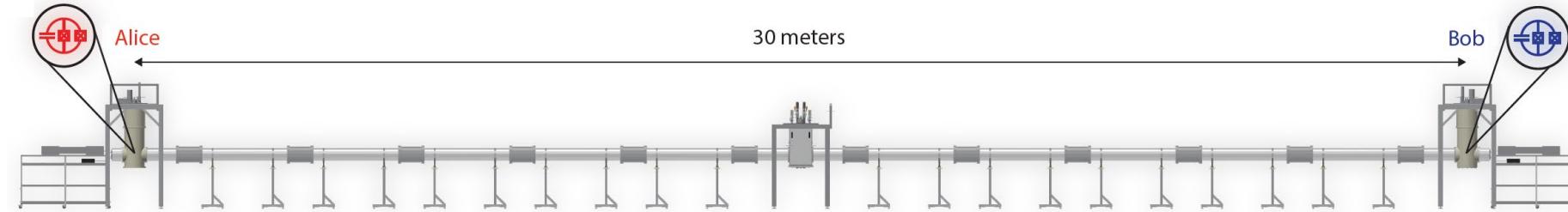
S. Pironio *et al.*, *Nature* 464(7291) (2010)

- Randomness amplification

R. Colbeck and R. Renner, *Nat. Phys.* 8(6):450-454 (2012); M. Kessler and R. Arnon-Friedman, *IEEE J. on Selected Areas in Information Theory*, 1 no.2, 568-584 (2020)



# Potential Future Experiments



- Demonstrations of device independence
- Exploration of non-local physics
- Waveguide QED physics with 30-m line
- Demonstration of basic building blocks of a networked QC
- Realization of distributed quantum algorithms

# The ETH Zurich Quantum Device Lab

with spring term project students



# Want to work with us? Looking for Grad Students, PostDocs and Technical Staff.



S. Storz et al., *Nature* **617**, 265-270 (2023)