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Lepton-flavor-violating decays into axion-like particles

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mainly based on LC, D. Redigolo, R. Ziegler, J. Zupan,
JHEP 09 (2021) 173

Assume there is a *light*, *invisible*, new particle "a"
with *flavour-violating couplings* to leptons

Light:

$$m_a \; < \; m_\mu \, , \, m_\tau$$

Invisible:

- Neutral
- Feebly coupled (long-lived)

CLFV modes would then be $\mu \to e\, a, \;\; \tau \to \mu\, a, \;\; \mu \to e\, \gamma\, a,$ etc .

Interesting interplay with cosmo/astro:

- DM candidate? (if long-lived enough)
- Bounds from star cooling/supernovae (if light and feeble enough)

Why should a be light and feebly-coupled?

That's natural, if it is the (pseudo) Nambu-Goldstone boson (PNGB) of a broken global U(1), *aka* an axion-like particle (ALP)

Examples:

Global symmetry:	PNGB:
• Lepton Number	Majoron
• Peccei-Quinn	Axion
• Flavour symmetry	Familon
…	

Wilczek '82

Pilaftsis '93

Feng et al. '97

LC Goertz Redigolo Ziegler Zupan '16

Di Luzio et al. '17, '19

…

Equivalent possibility: light Z' of a local U(1), e.g. L_i-L_j (with $g \ll 1$)

Heeck '16

General couplings to leptons:

Shift symmetry (PNGB!) → m_a from (small) explicit U(1) breaking

$$\mathcal{L}_{a\ell\ell} = \frac{\partial^\mu a}{2 f_a} \left(C_{ij}^V \; \bar{\ell}_i \gamma_\mu \ell_j + C_{ij}^A \; \bar{\ell}_i \gamma_\mu \gamma_5 \ell_j \right)$$

U(1)-breaking scale → coupling suppression

Where does *lepton flavour violation* come from?

- If lepton U(1) charges are flavour non-universal ⇒ naturally flavour-violating couplings
- Alternatively, loop-induced flavour-violating couplings

Explicit examples at the end…

$$\mathcal{L}_{a\ell\ell} = \frac{\partial^\mu a}{2 f_a} \left(C^V_{ij}\ \bar{\ell}_i \gamma_\mu \ell_j + C^A_{ij}\ \bar{\ell}_i \gamma_\mu \gamma_5 \ell_j \right)$$

This generic Lagrangian induces 2-body LFV decays such as:

$$\Gamma(\ell_i \to \ell_j\, a) = \frac{1}{16\pi} \frac{m^3_{\ell_i}}{F^2_{ij}} \left(1 - \frac{m_a^2}{m^2_{\ell_i}} \right)^2 \qquad F_{ij} \equiv \frac{2 f_a}{\sqrt{|C^V_{ij}|^2 + |C^A_{ij}|^2}}$$

Feng et al. '97

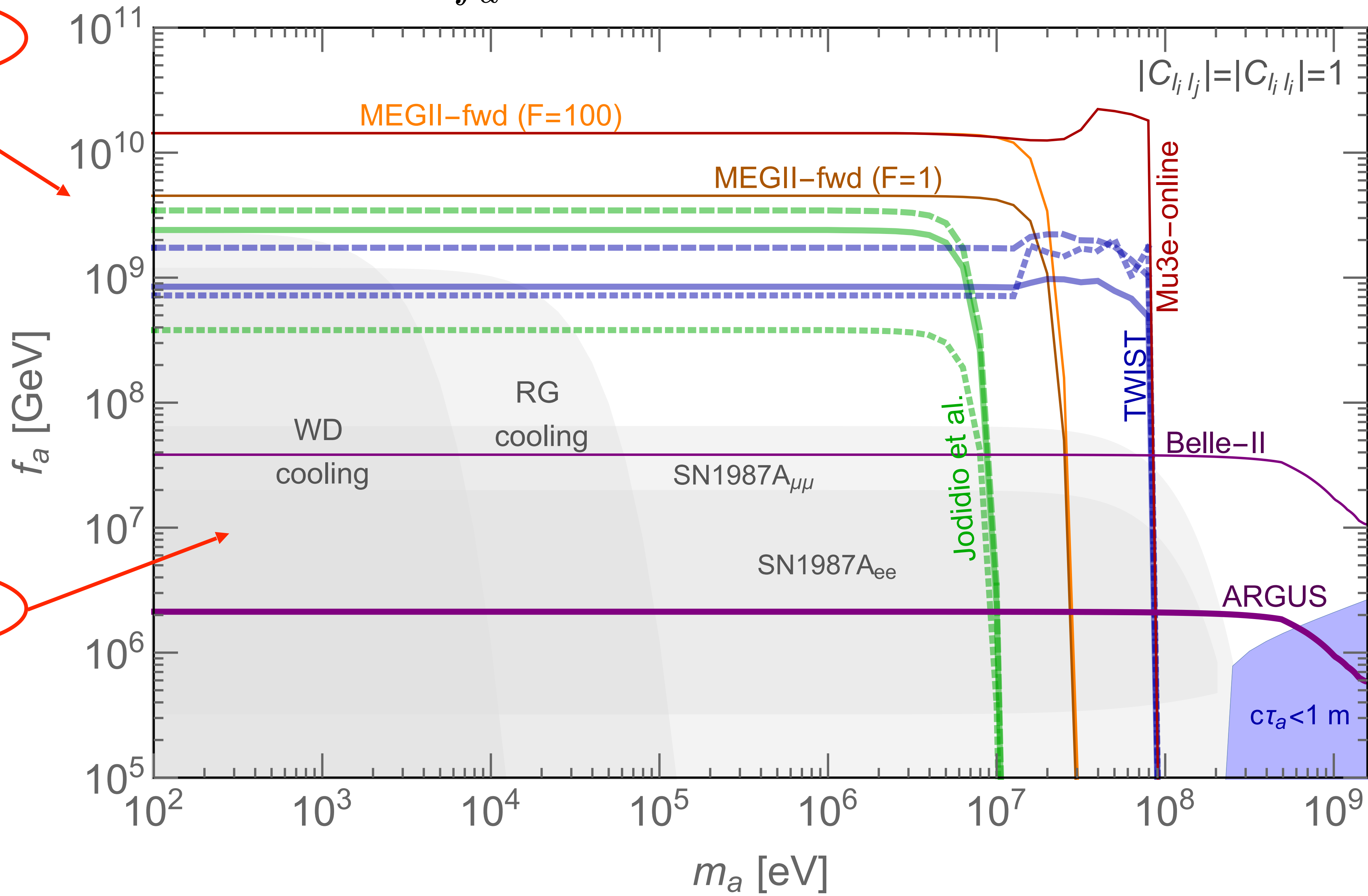
Goal: constrain the effective LFV scales F_{ij} using experimental data

- Which experiments?
- What are the future prospects?

Summary plot

$$\mathcal{L}_{a\ell\ell} = \frac{\partial^\mu a}{2 f_a} \left(C^V_{ij}\ \bar{\ell}_i \gamma_\mu \ell_j + C^A_{ij}\ \bar{\ell}_i \gamma_\mu \gamma_5 \ell_j \right)$$

$\mu \to e a$



$\tau \to \ell a$

star cooling

Decays mediated by dim-5 operators: much larger NP scales can be reached than $\mu \to e\gamma$, $\mu \to 3e$, $\mu \to e$ conv. (from dim-6 ops, NP scale reach ~10^7−10^8GeV)

LFV experiments

$\mu \to e\, a$: signal and background

Signal: monochromatic positron with $p_e = \sqrt{\left(\dfrac{m_\mu^2 - m_a^2 + m_e^2}{2m_\mu}\right)^2 - m_e^2}$

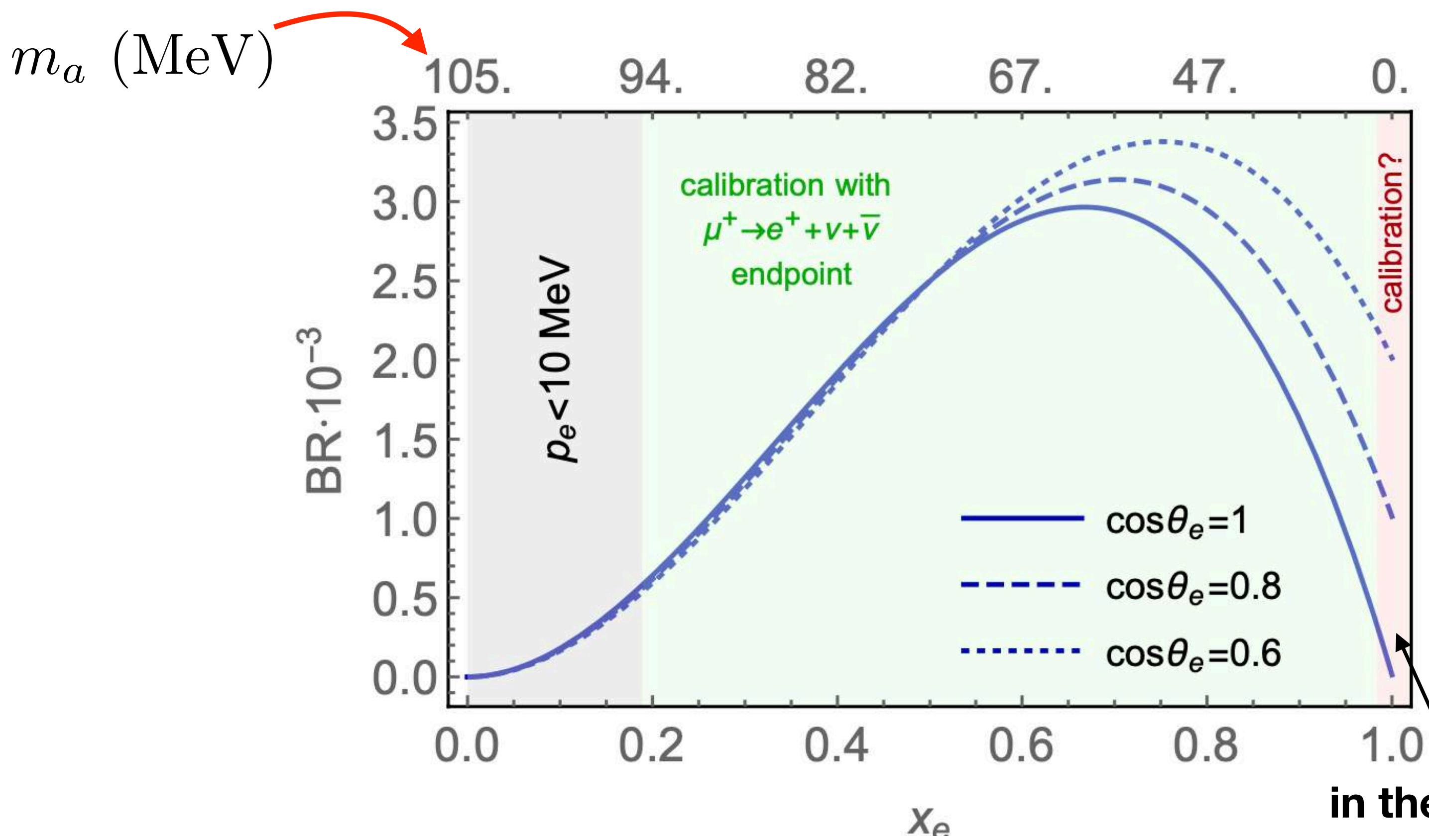
Differential decay rate: $$\frac{\mathrm{d}\Gamma(\ell_i \to \ell_j\, a)}{\mathrm{d}\cos\theta} = \frac{m_{\ell_i}^3}{32\pi F_{\ell_i\ell_j}^2}\left(1 - \frac{m_a^2}{m_{\ell_i}^2}\right)^2 \left[1 + 2P_{\ell_i}\cos\theta \frac{C^V_{\ell_i\ell_j} C^A_{\ell_i\ell_j}}{(C^V_{\ell_i\ell_j})^2 + (C^A_{\ell_i\ell_j})^2}\right]$$

signal depends on the chirality of the couplings

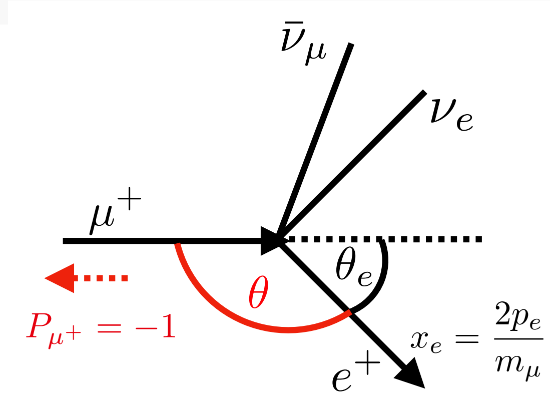
Michel spectrum: $$\frac{\mathrm{d}^2\Gamma(\mu^+ \to e^+\, \nu_e\, \bar\nu_\mu)}{\mathrm{d}x_e\, \mathrm{d}\cos\theta} \simeq \Gamma_\mu\left((3 - 2x_e) - P_\mu (2x_e - 1)\cos\theta\right) x_e^2 \qquad x_e = \frac{2p_e}{m_\mu}$$

μ polarization

And "surface" muons are highly polarized (produced by pion decays at rest on the surface of the production target) $\to$ the SM background can be suppressed



the bkd goes to zero in the "forward"direction (the direction opposite to the muon polarization)

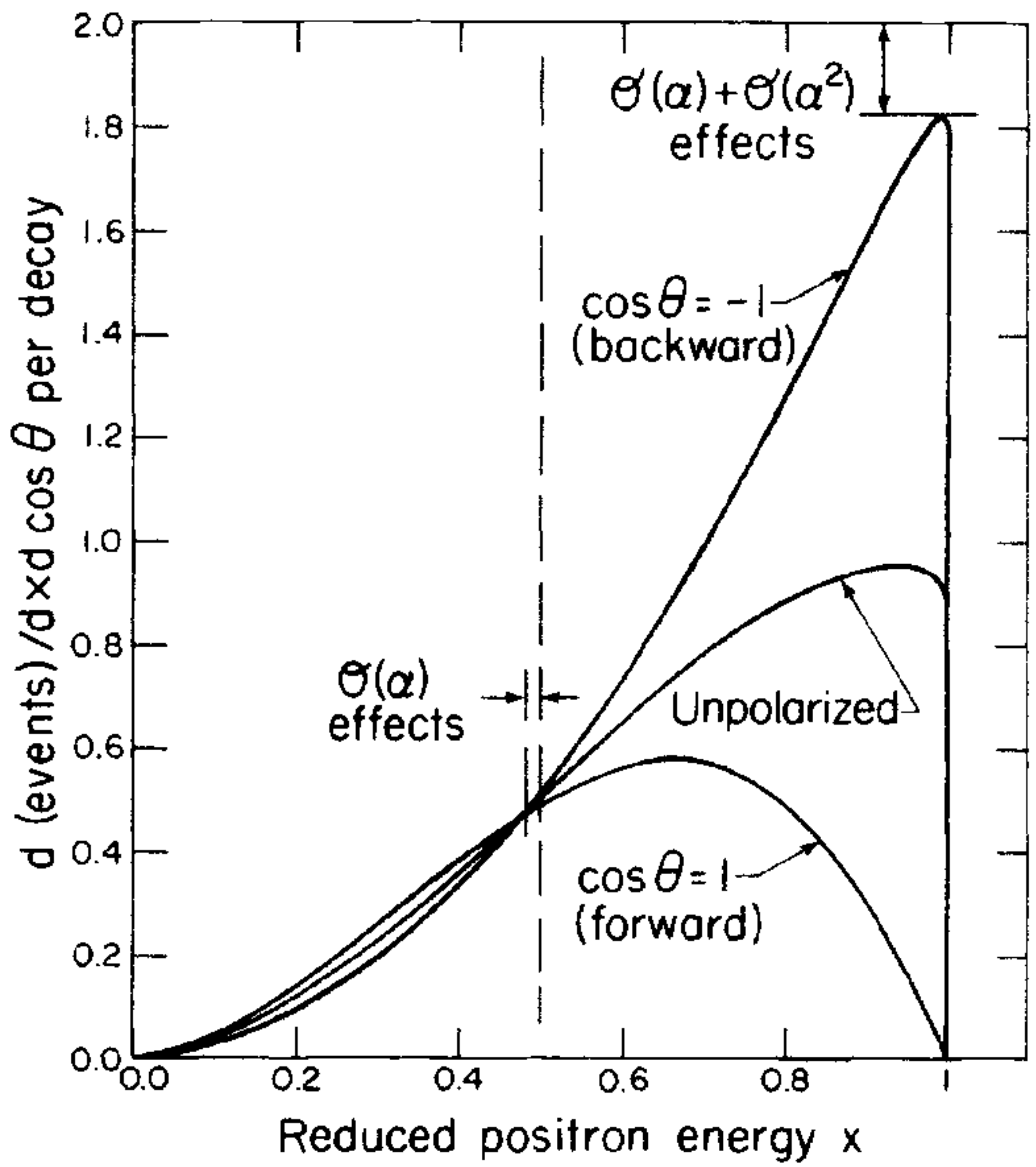


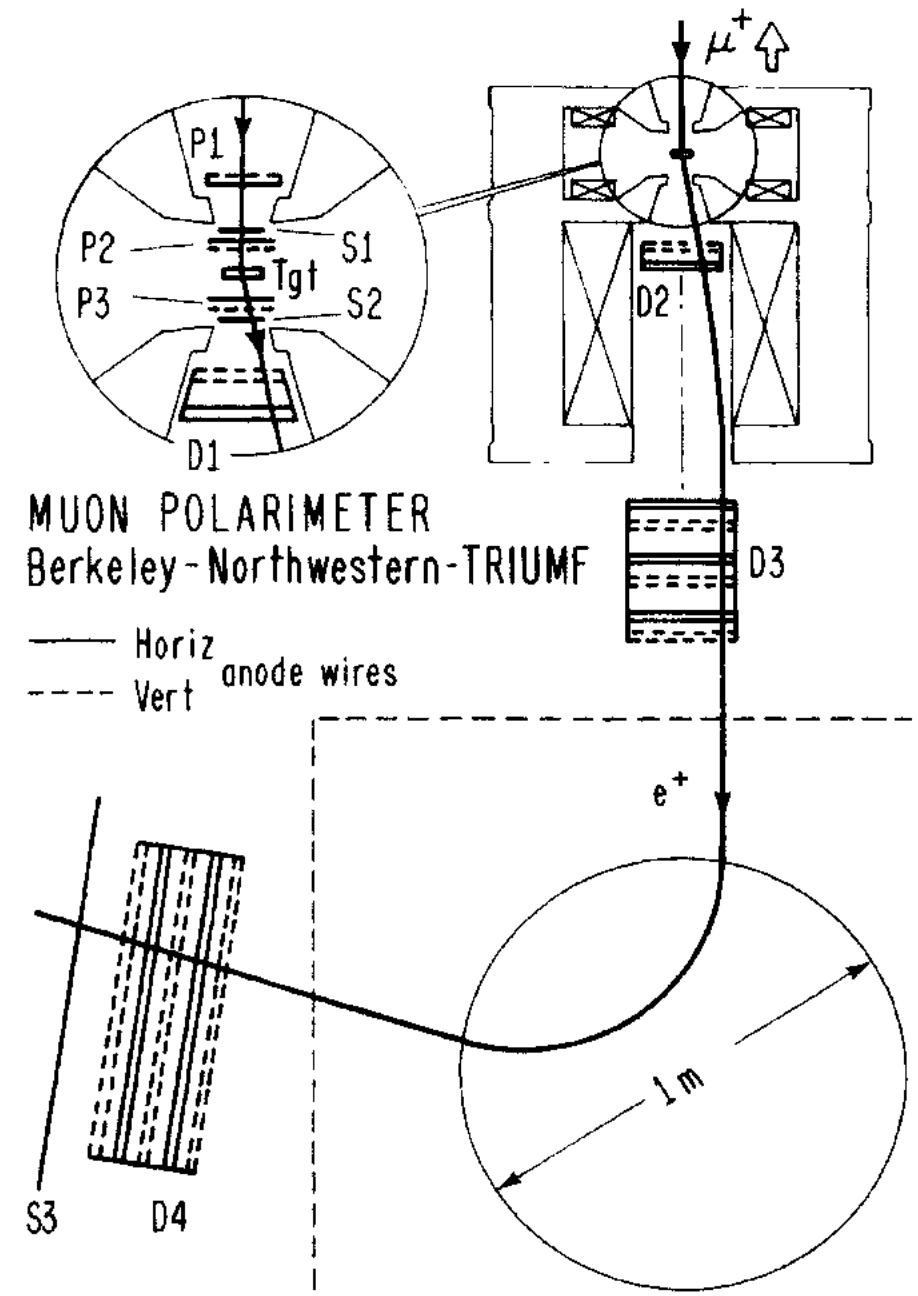
- Jodidio et al. (TRIUMF) 1986 — Search for RH currents with $1.8{\times}10^7$ polarized μ^+

Ordinary $\mu \to e\bar{\nu}\nu$

$$\frac{d^2\Gamma}{dx\, d\cos\theta} = \Gamma_\mu \left((3-2x) - P(2x-1)\cos\theta\right) x^2$$

$$x = 2E_e/m_\mu$$





Very good e+ momentum resolution (~70 KeV at the e.p.)

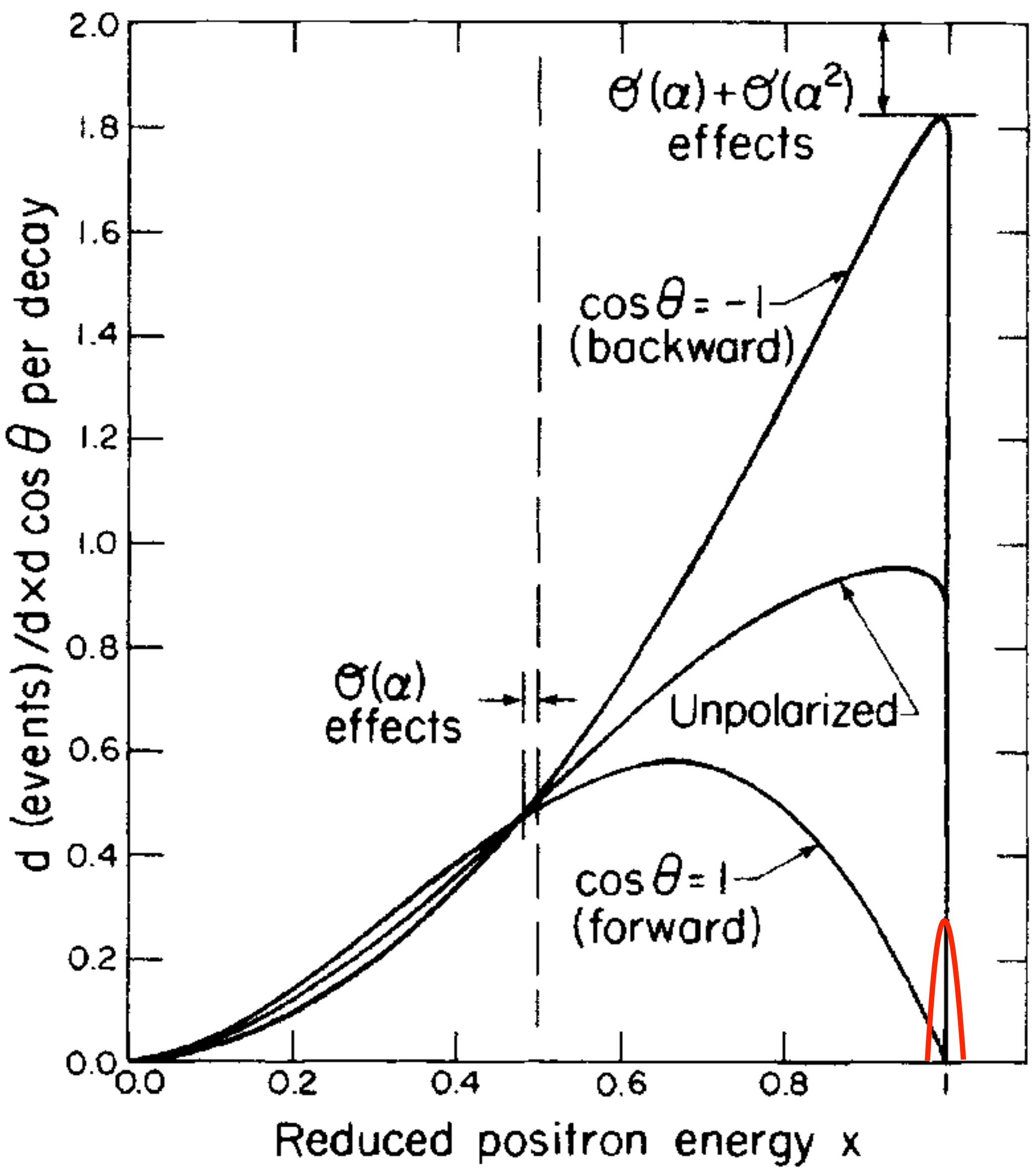
- Jodidio et al. (TRIUMF) 1986

Search for RH currents with 1.8×10^7 polarized μ^+ interpreted in terms of $\mu \to ea$ too

Ordinary $\mu \to e\bar{\nu}\nu$

$$\frac{d^2\Gamma}{dx\, d\cos\theta} = \Gamma_\mu \left((3-2x) - P(2x-1)\cos\theta\right) x^2$$

$$x = 2E_e/m_\mu$$



$\mu \to e\, a$ signal for $m_a \approx 0$: monochromatic e^+ at $m_\mu/2$

Unless it couples (V-A) like in the SM:

$$\frac{d\Gamma(\mu^+ \to e^+ a)}{d\cos\theta} = \frac{\Gamma_{\mu\to e\, a}}{2}\left[1 + 2P\cos\theta \frac{C^V_{e\mu} C^A_{e\mu}}{(C^V_{e\mu})^2 + (C^A_{e\mu})^2}\right]$$

for the *isotropic* case, they set the limit

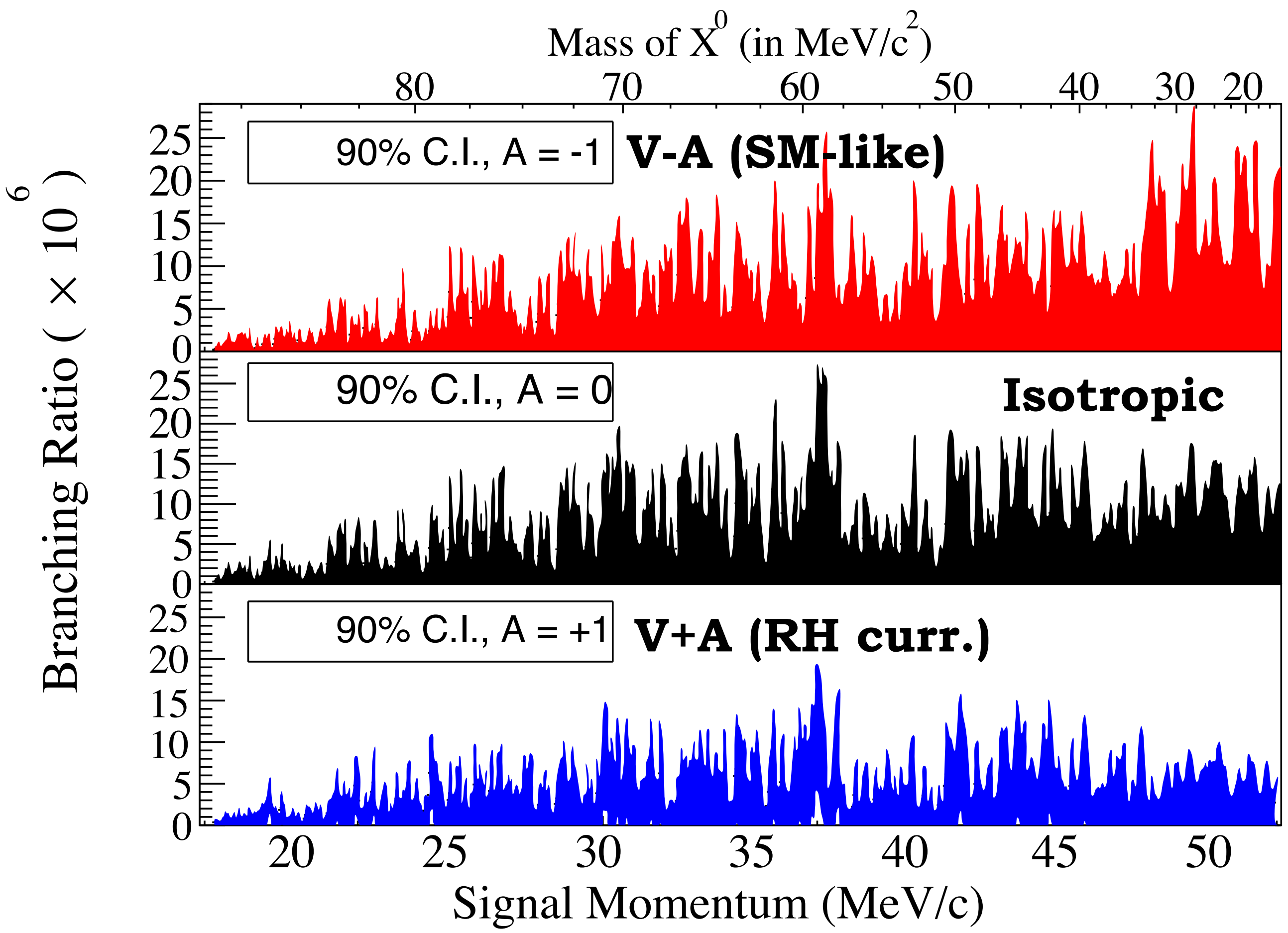
$$\boxed{\Rightarrow \quad \mathrm{BR}(\mu^+ \to e^+ a) < 2.6 \times 10^{-6}}$$

thus one gets

$$\boxed{\Rightarrow \quad F_{\mu e} > 4.8 \times 10^9 \text{ GeV}}$$

- <u>TWIST 2014</u> Precise measurement of Michel parameters plus dedicated search for $\mu \to ea$ in the whole m_a range considering anisotropy of the signal

Limits (with $5.8{\times}10^8$ μ^+):



Decay Signal		90% C.L. (in ppm)	p-value
$A = 0$	Average	9	
	$p = 37.03$ MeV/c	26	0.66
	Endpoint	21	0.81
$A = -1$ SM-like	Average	10	
	$p = 37.28$ MeV/c	26	0.60
	Endpoint	58	0.80
$A = +1$	Average	6	
	$p = 19.13$ MeV/c	6	0.59
	Endpoint	10	0.90

For V-A coupl. and $m_a \approx 0$: $\mathrm{BR}(\mu \to ea) < 5.8 \times 10^{-5}$

$$\Rightarrow \quad F_{\mu e} > 1.0 \times 10^9\ \mathrm{GeV}$$

- Crystal Box 1988

PHYSICAL REVIEW D VOLUME 38, NUMBER 7 1 OCTOBER 1988

Search for rare muon decays with the Crystal Box detector

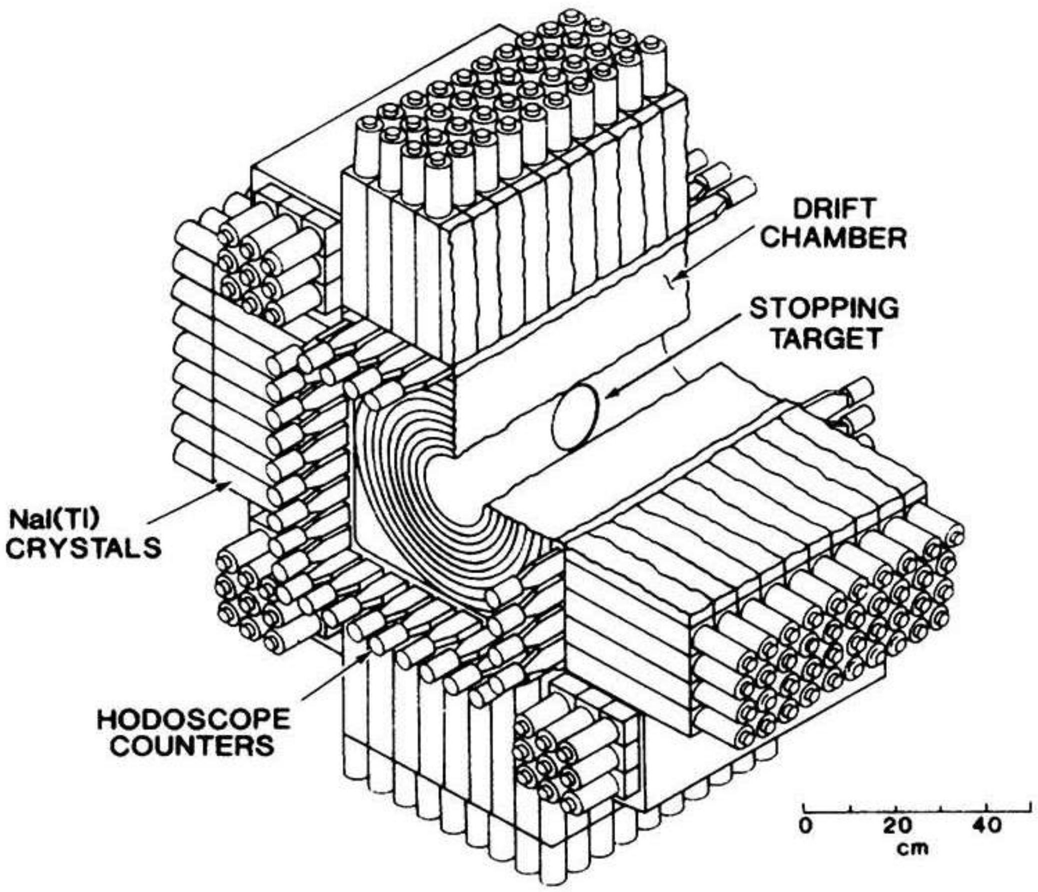


TABLE I. Types of events generated with the Monte Carlo program.

Process	Trigger
$\mu^+ \to e^+\gamma$	e-γ
$\mu^+ \to e^+\gamma\nu\bar{\nu}$	e-γ, 1-γ
$\mu^+ \to e^+\gamma\gamma$	e-γ-γ, e-γ
$\mu^+ \to e^+e^+e^-$	e-e-e
$\mu^+ \to e^+e^+e^-\nu\bar{\nu}$	e-e-e
$\mu^+ \to e^+\nu\bar{\nu}$	1-e
$\boxed{\mu^+ \to e^+\gamma f\ (f = \text{familon})}$	e-γ
$\pi^0 \to \gamma\gamma$	γ-γ, 1-γ
$\pi^- p \to n\gamma$	1-γ

Past searches: $\mu \to e\,\gamma\,a$

- Crystal Box 1988

Analysis for massless familon $m_a \approx 0$
(with 1.4×10^{12} stopped μ^+) yields:

$$\mathrm{BR}(\mu \to e\,a\,\gamma) < 1.1 \times 10^{-9} \quad (90\%\ \mathrm{CL})$$

$$\mathrm{BR}(\mu \to e\,a\,\gamma) \approx \frac{\alpha_{\rm em}}{2\pi}\mathcal{I}(x_{\rm min}, y_{\rm min})\mathrm{BR}(\mu \to e\,a)$$

Hirsch et al. ‘09

$$\mathcal{I}(x_{\rm min}, y_{\rm min}) = \int_{x_{\rm min}, y_{\rm min}}^{1} \mathrm{d}x\mathrm{d}y \frac{(x-1)(2-xy-y)}{y^2(1-x-y)}$$

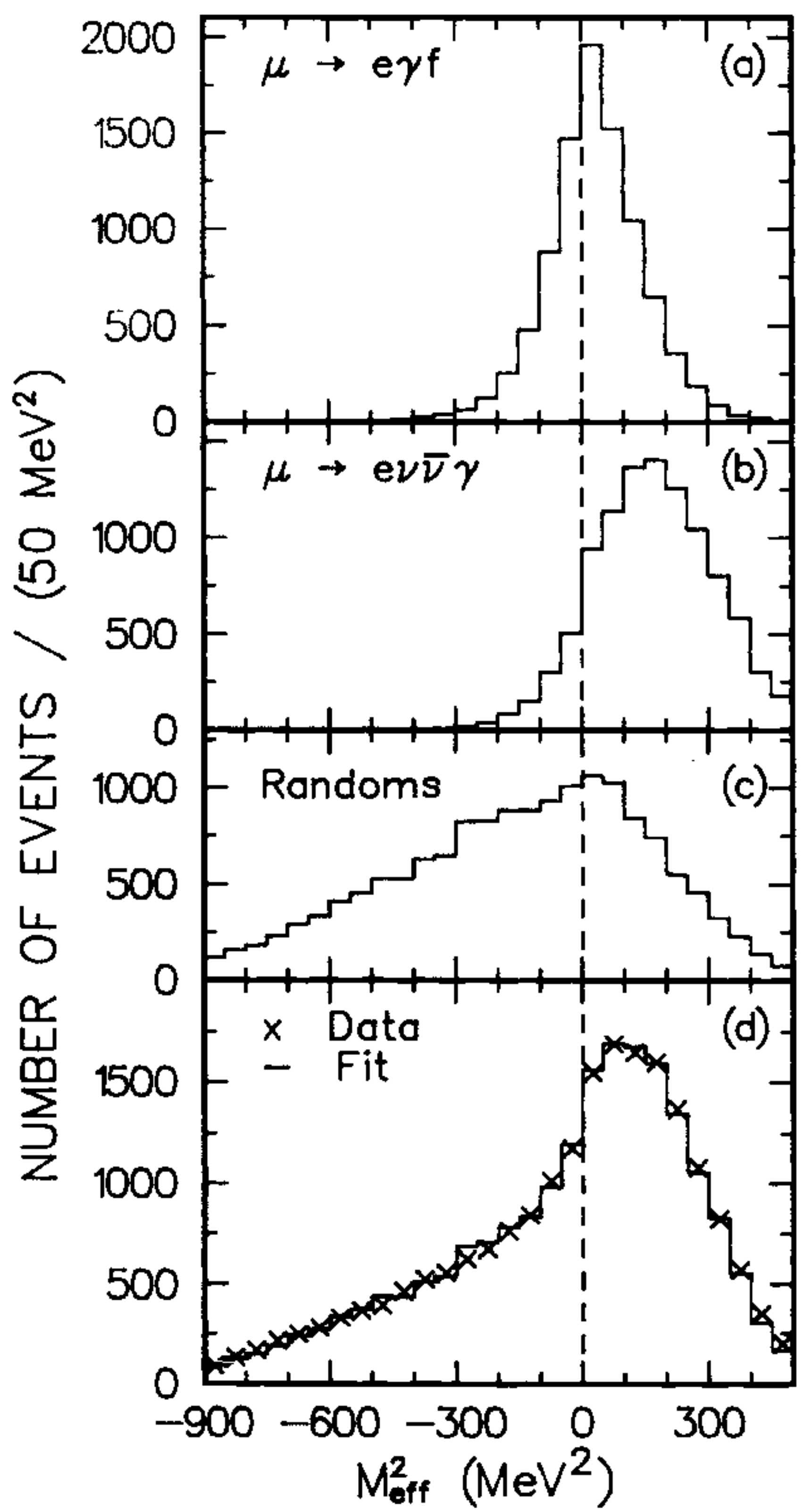
$$x = 2E_e/m_\mu \qquad y = 2E_\gamma/m_\mu$$

Crystal Box energy thresholds:

$$E_e > 38-43\ \mathrm{MeV}\,, \quad E_\gamma > 38\ \mathrm{MeV} \quad \Rightarrow \quad x_{\rm min} = 0.72-0.81\,,\ y_{\rm min} = 0.72$$

$$\boxed{\Rightarrow \quad F_{e\mu} \ > \ (5.1-8.3)\times 10^8\ \mathrm{GeV}}$$

weaker but independent
of V/A nature of the couplings



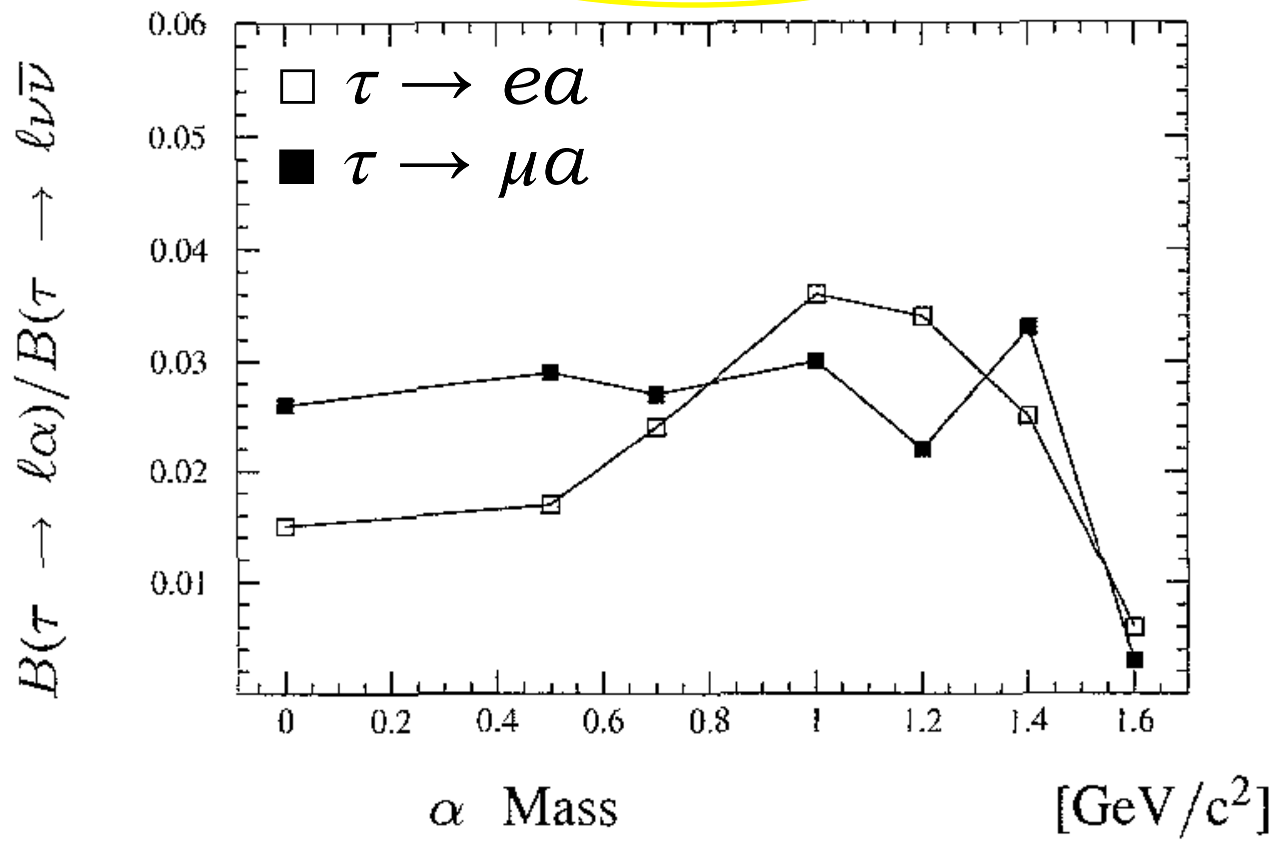
- ARGUS 1995

A search for the lepton-flavour violating decays $\tau \longrightarrow e\alpha$, $\tau \longrightarrow \mu\alpha$

Z. Phys. C 68, 25–28 (1995)

ARGUS Collaboration

With 472 pb^{-1}:

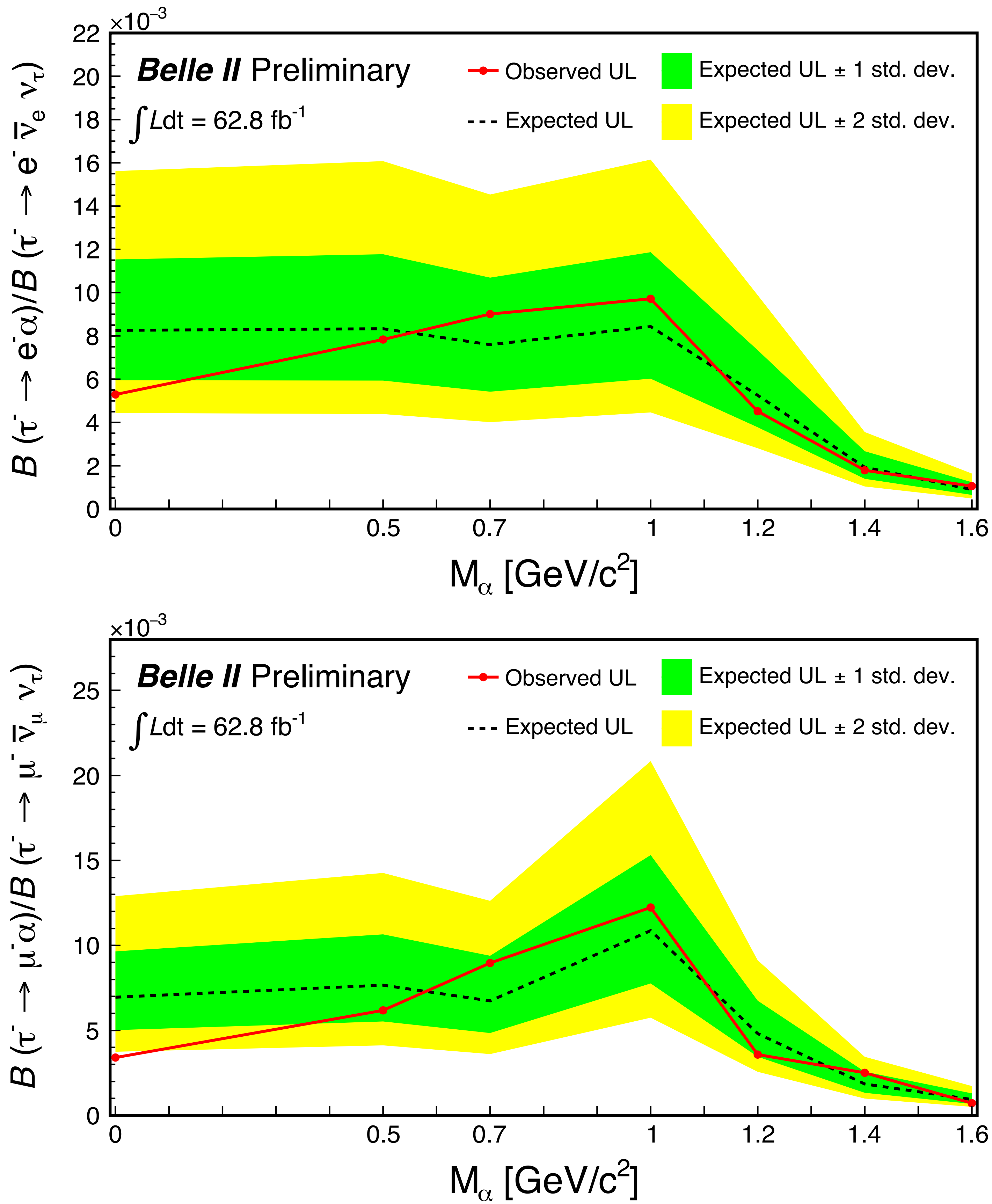


$m_a \approx 0$:

$$\mathrm{BR}(\tau \to e\, a) < 2.7 \times 10^{-3} \quad (95\%\ \mathrm{CL}) \quad \Rightarrow \quad F_{\tau e} \gtrsim 4.3 \times 10^{6}\ \mathrm{GeV}\,,$$
$$\mathrm{BR}(\tau \to \mu\, a) < 4.5 \times 10^{-3} \quad (95\%\ \mathrm{CL}) \quad \Rightarrow \quad F_{\tau \mu} \gtrsim 3.3 \times 10^{6}\ \mathrm{GeV}\,.$$

Past searches: $\tau \to e\, a\,,\, \tau \to \mu\, a$

- NEW! Belle II arXiv:2212.03634



- ARGUS 19

Phys. C 68, 25–28 (1995)

$m_a \approx 0$:

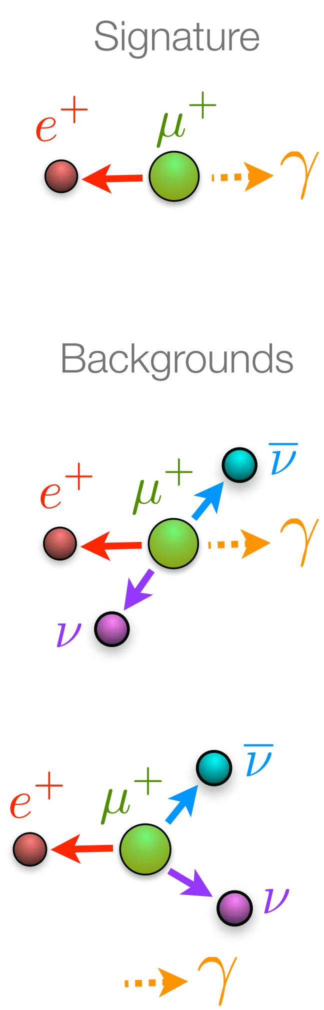
Present bounds based on old experiments and/or not-so-high luminosities ($<10^9$ total muon decays)

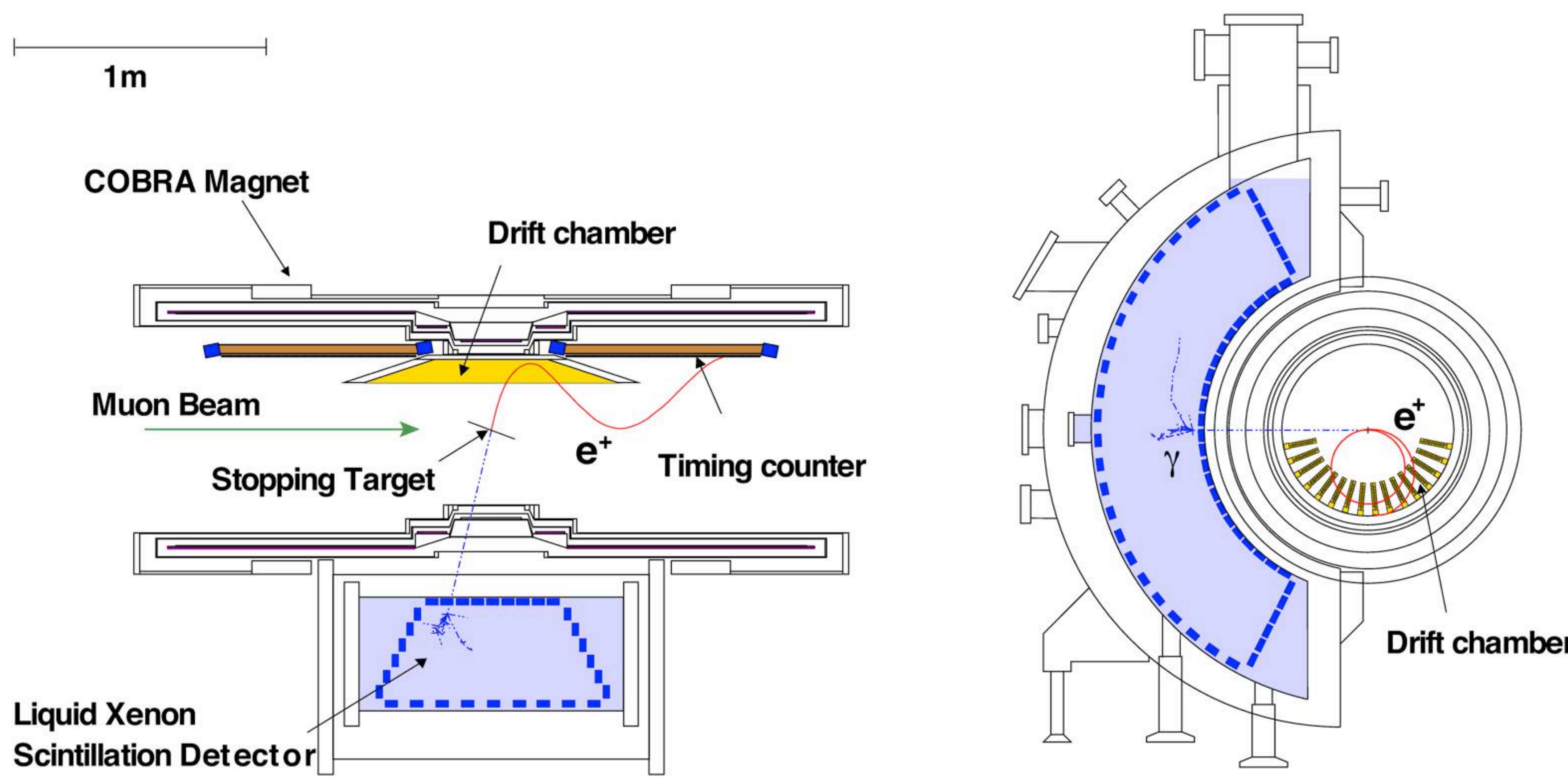
$\pi E5$ beamline at PSI (where MEGII and Mu3e are located) can deliver $>10^8$ muons *per second*: next generation experiment must do better!

slide borrowed from A. Papa

MEG: Signature and experimental setup

- The MEG experiment aims to search for $\mu^+ \to e^+ \gamma$ with a sensitivity of $\sim 10^{-13}$ (previous upper limit $BR(\mu^+ \to e^+ \gamma) \leq 1.2 \times 10^{-11}$ @90 C.L. by MEGA experiment)
- Five observables (E_g, E_e, t_{eg}, ϑ_{eg}, ϕ_{eg}) to characterize $\mu \to e\gamma$ events



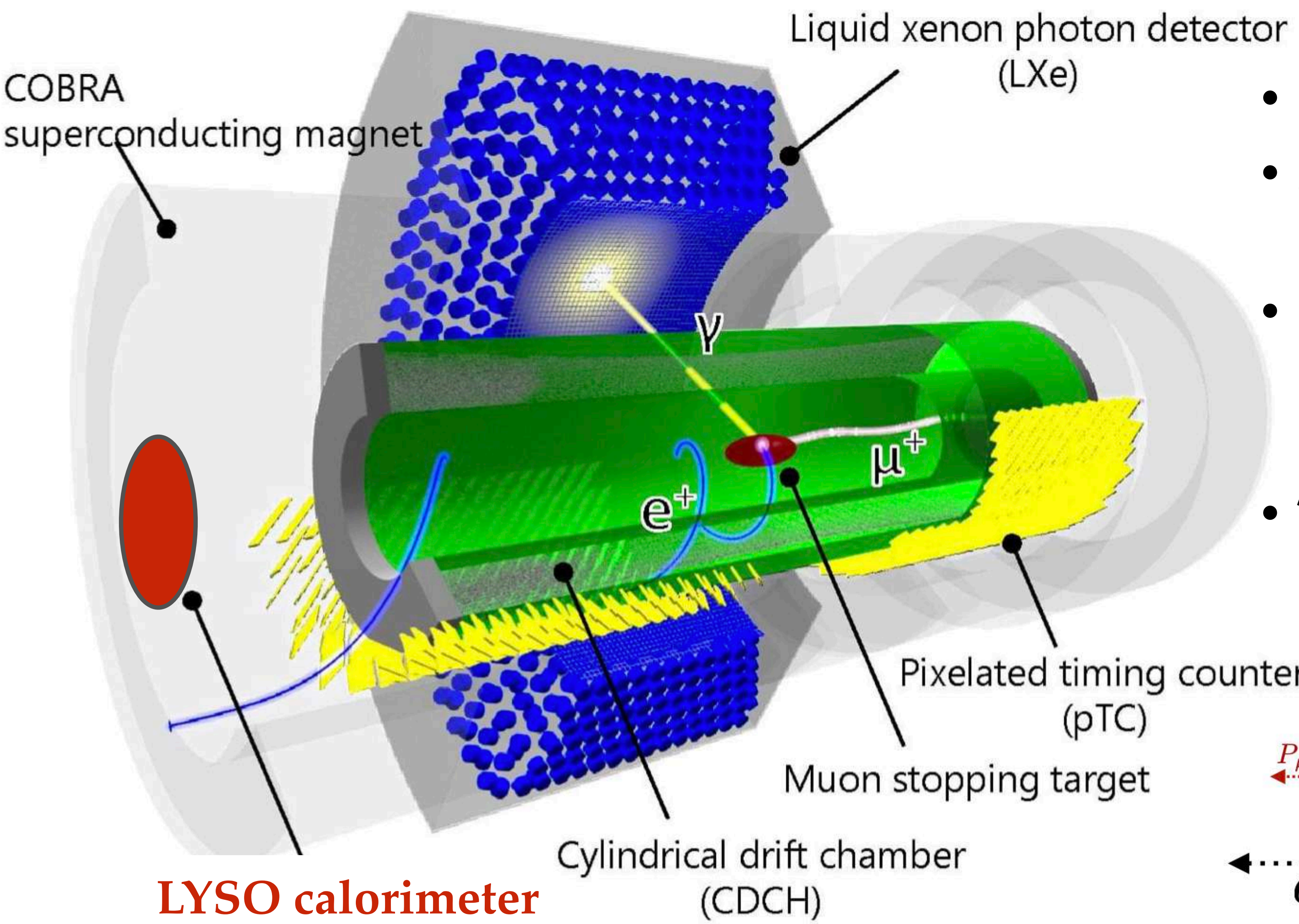


53

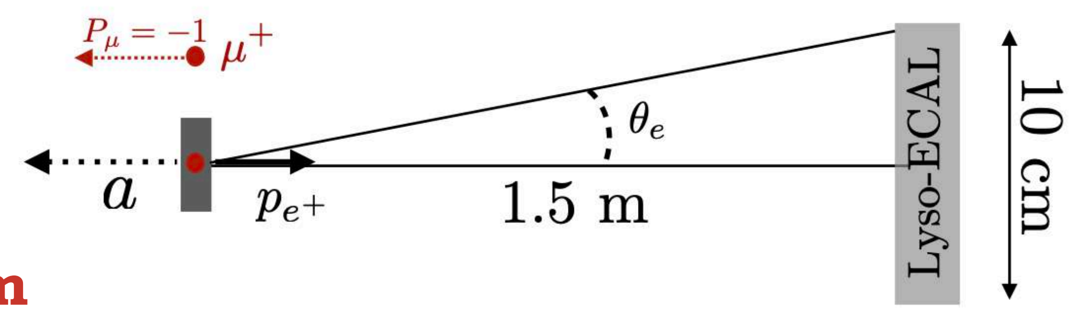
Final result (with 7.5x10^{14} μ^+ on target): $\mathrm{BR}(\mu \to e\gamma) < 4.2 \times 10^{-13}$ (90% CL)

- Prospect at MEG II for $\mu \to e\, a$

What about a Jodidio-like search at MEG II for $m_a \approx 0$ with a *forward calorimeter*?
We propose a modified setup of MEG II ("MEGII-fwd") and ~2 weeks dedicated run
idea from discussions with A. Papa and G. Signorelli, thanks!



- Muon beam already polarized
- A suitable magnetic field can reduce depolarization effects
- Reconfiguring the field we can also increase the acceptance ("magnetic focusing" up to F~100)
- Two weeks of run after MEG II main run are enough to improve the bound (even with F=0)



~1.5 m from the target, diameter ~ 10 cm

- Prospect at MEG II for $\mu \to e\, a$

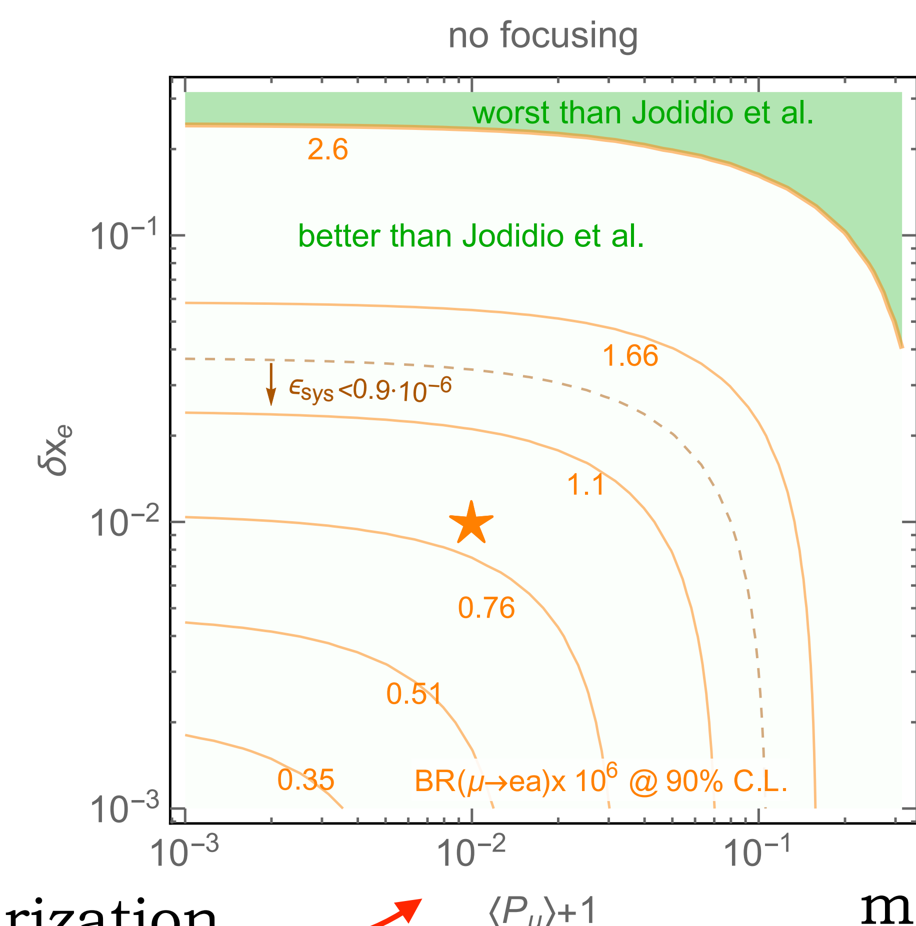
What about a Jodidio-like search at MEG II for $m_a \approx 0$ with a *forward calorimeter*?

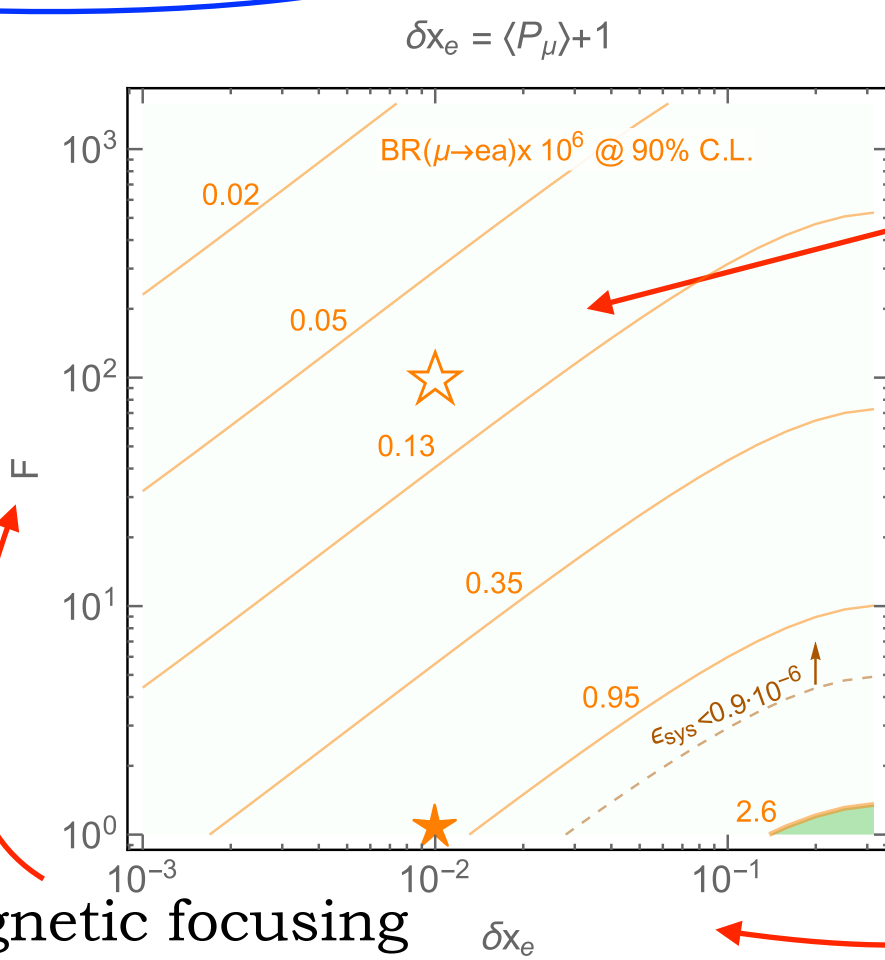
We propose a modified setup of MEG II ("MEGII-fwd") and ~2 weeks dedicated run

idea from discussions with A. Papa and G. Signorelli, thanks!

Our estimate of the sensitivity of a dedicate run (2 weeks with 10^8 μ^+/s):

$$F = 0 \qquad \text{MEGII-fwd}: \ 10^{14} \mu^+$$





$F = 100$
$\text{BR} \sim 10^{-7}$

Positron momentum resolution

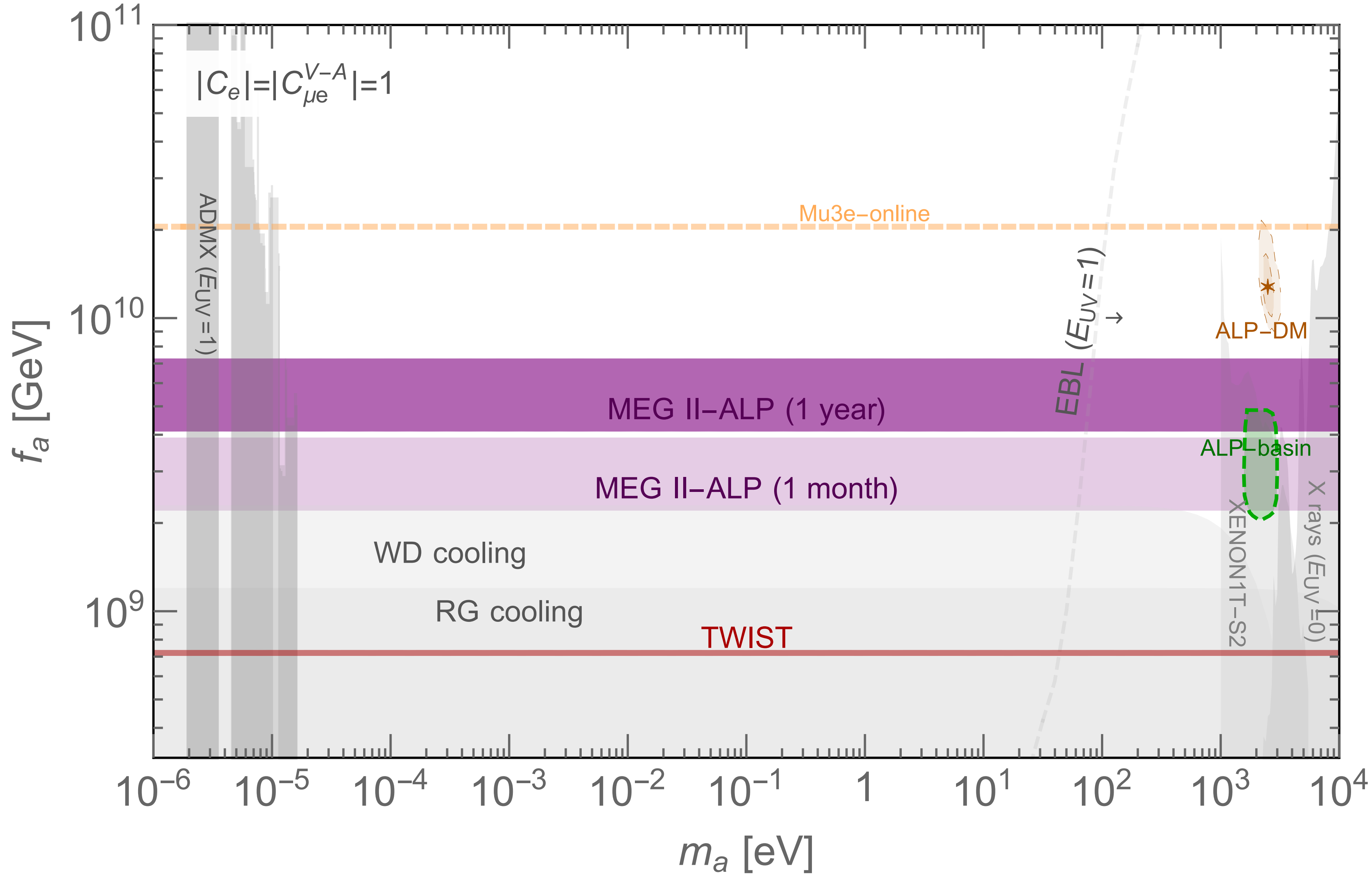
$$x_e = \frac{2p_e}{m_\mu}$$

polarization

magnetic focusing

- Prospect at MEG II for $\mu \to e\, a\, \gamma$

Search sensitive to V-A couplings too, requires a dedicated trigger:



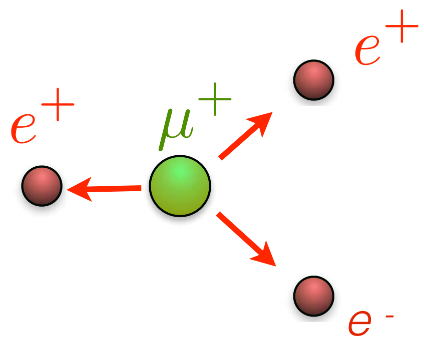
Jho Knapen Redigolo '22

Mu3e: The $\mu^+ \to e^+e^+e^-$ search

slide borrowed from A. Papa

- The Mu3e experiment aims to search for $\mu^+ \to e^+ e^+ e^-$ with a sensitivity of ~10^{-15} (Phase I) up to down ~10^{-16} (Phase II). Previous upper limit $BR(\mu^+ \to e^+ e^+ e^-) \leq 1 \times 10^{-12}$ @90 C.L. by SINDRUM experiment)
- Observables (E_e, t_e, vertex) to characterize $\mu \to eee$ events

Signature

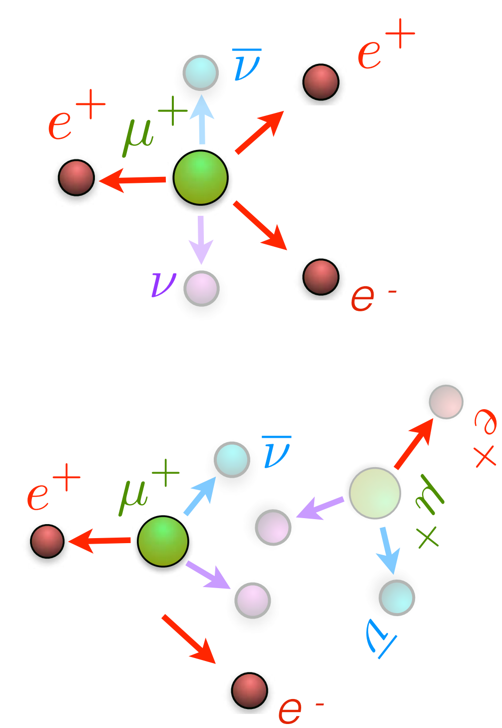


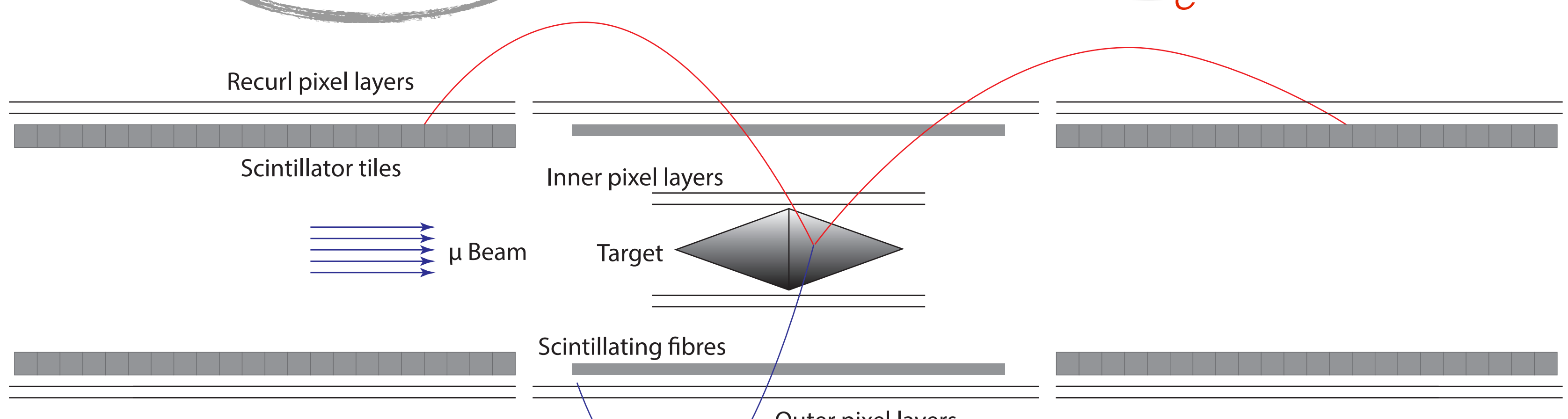
$\Delta t_{eee} = 0$

$\Sigma \overline{p}_e = 0$

$\Sigma E_e = m_\mu$

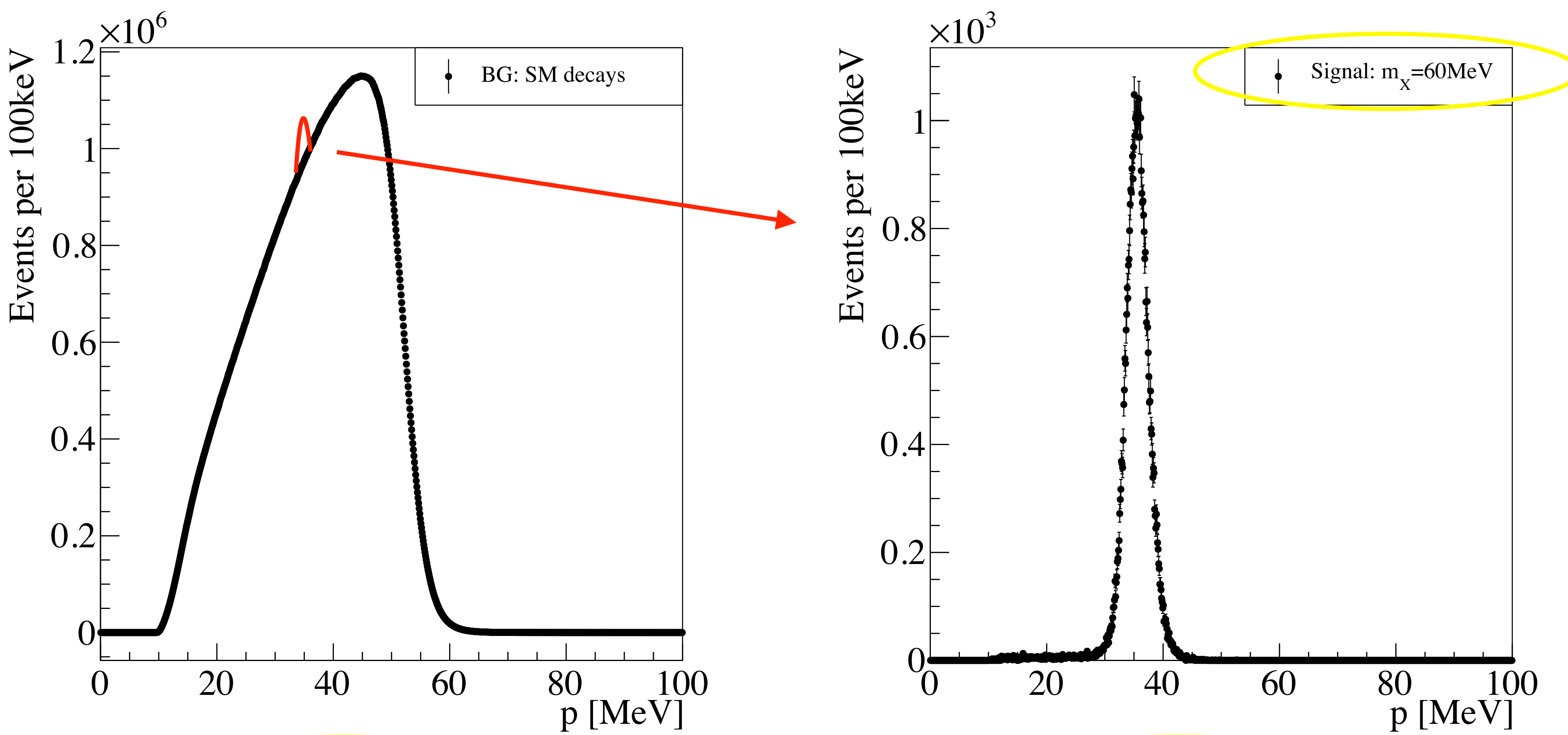
Background





- Mu3e prospect for $\mu \to e\, a$ (Perrevoort '18)

Potential search for performed on positron momentum histograms filled with *online* reconstructed short tracks



(a) Simulated background events.

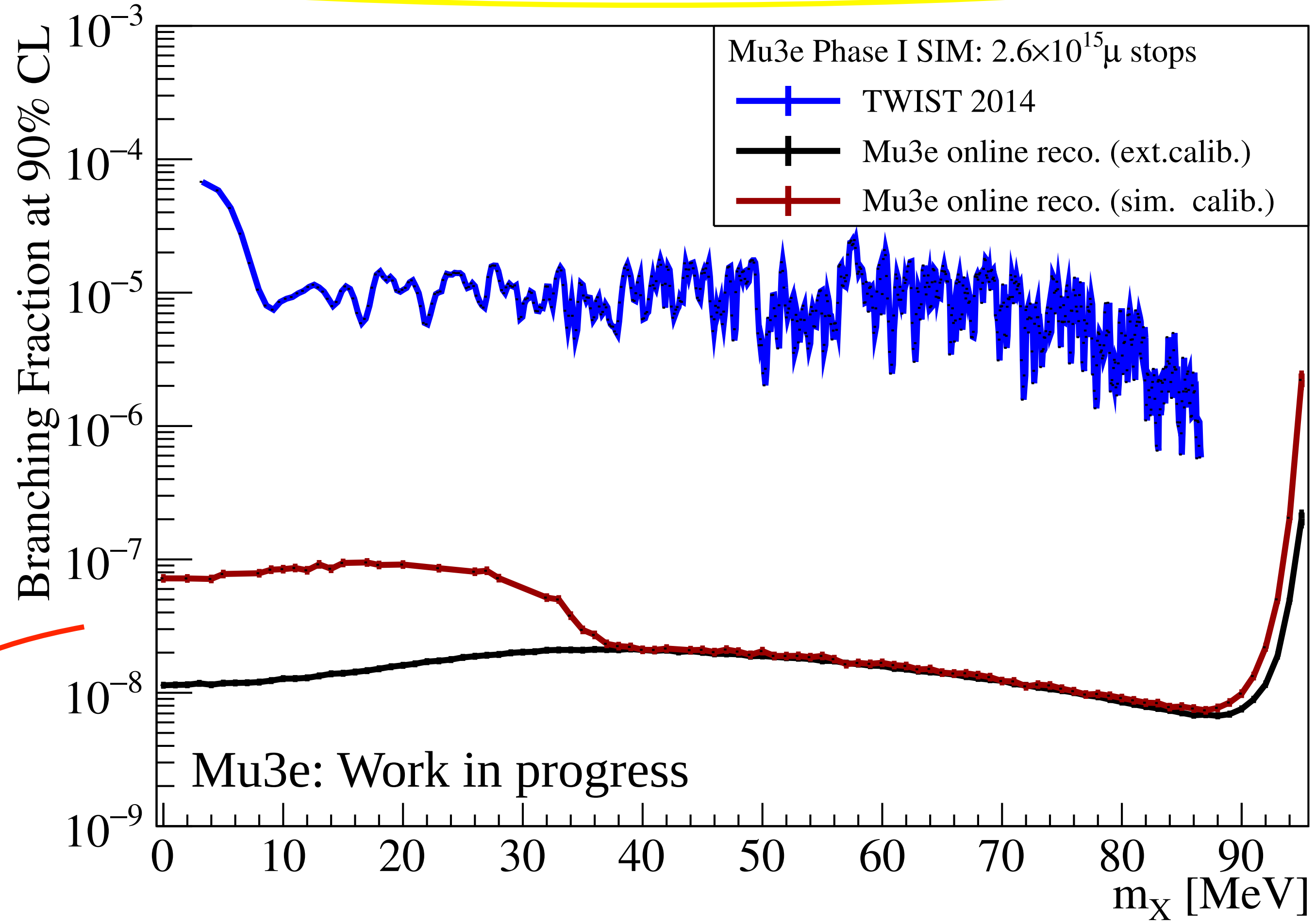
(b) Simulated $\mu \to eX$ signal events.

Perrevoort (Mu3e) '18

- Mu3e prospect for $\mu \to e\, a$ (Perrevoort '18)

Potential search for performed on positron momentum histograms filled with *online* reconstructed short tracks

Expected limit for phase I ($2.6\times10^{15}\ \mu^+$):

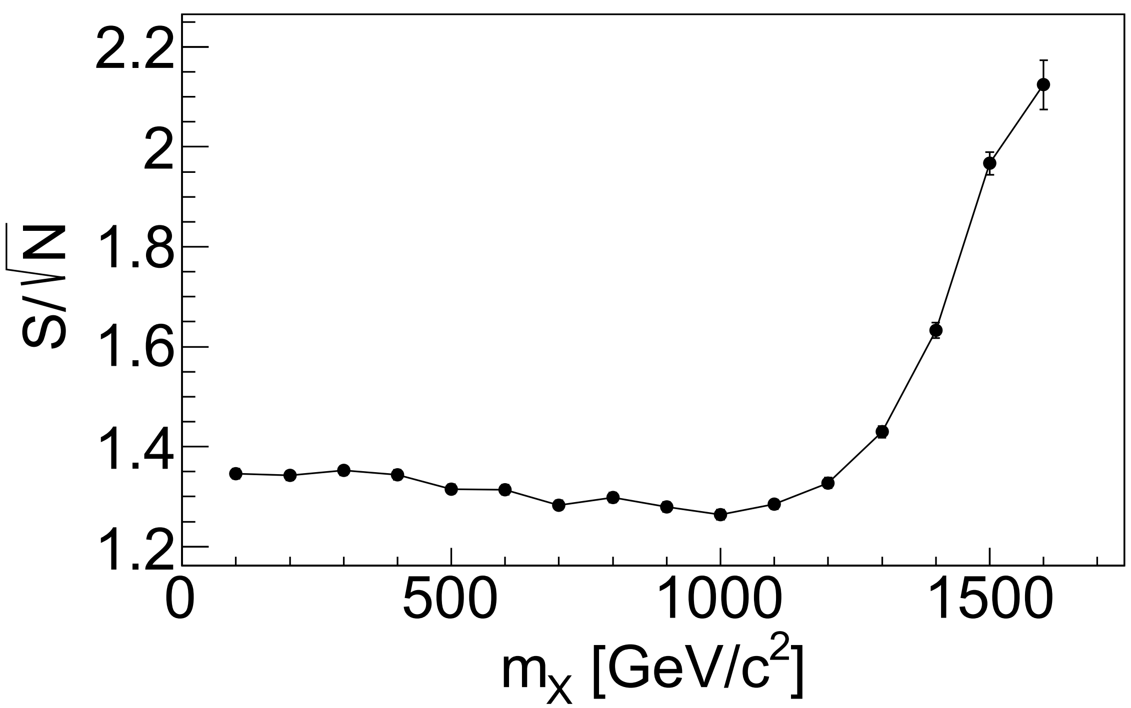


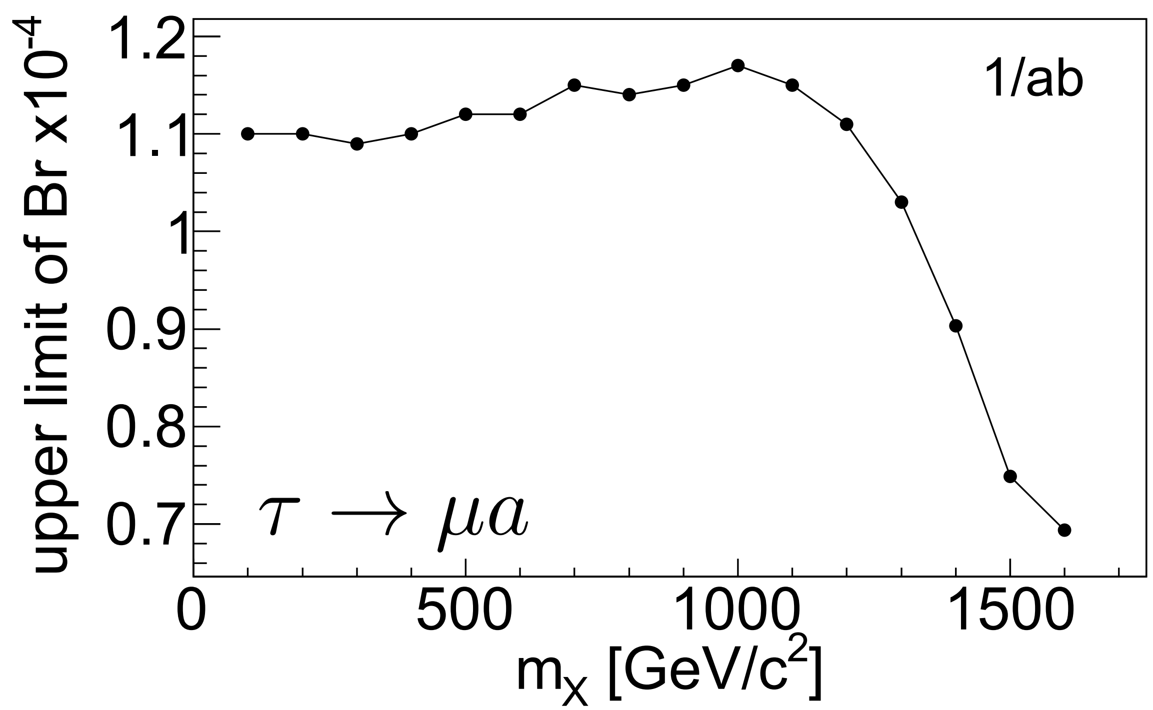
Perrevoort (Mu3e) '18

$$m_a \approx 0\ :\quad \mathrm{BR}(\mu \to ea) < 7\times10^{-8} \quad \Rightarrow \quad F_{\mu e} \gtrsim 3\times10^{10}\ \mathrm{GeV}$$

- Belle prospect for $\tau \to \mu\, a$ (Yoshinobu Hayasaka '17)

Simulation of S and B and limit that can be set using the Belle data set (1/ab):





Yoshinobu Hayasaka (Belle) '17

$m_a \approx 0$:

Belle (1/ab) prospect: $\mathrm{BR}(\tau \to \mu\, a) < 1.1 \times 10^{-4} \quad \Rightarrow \quad F_{\tau\mu} \gtrsim 2.1 \times 10^{7}$ GeV

Belle-II (50/ab) prospect: $\mathrm{BR}(\tau \to \mu\, a) < 2.0 \times 10^{-5} \quad \Rightarrow \quad F_{\tau\mu} \gtrsim 4.9 \times 10^{7}$ GeV

Estimated by rescaling as $\sqrt{\mathcal{L}}$

Astrophysics and cosmology

Astrophysical bounds

Well-known bounds on ALP-electron couplings from energy loss in star systems [red giants (RG), white dwarfs (WD)] due to processes like:

Raffelt Weiss '94

$$e^- + N \to e^- + N + a$$

(possible if a is not much heavier than T inside the star)

$$\Rightarrow \quad F^A_{ee} \gtrsim 4.6 \times 10^9 \text{ GeV (WD)} \qquad F^A_{ee} \gtrsim 2.4 \times 10^9 \text{ GeV (RG)} \quad (m_a \lesssim 1 - 10 \text{ keV})$$

Bertolami at al '14 Viaux at al '13

Hints (~3σ) for non-standard WD cooling require: $F^A_{ee} \approx 6 \times 10^9$ GeV

Giannotti at al '17

We extend the bounds to the case of massive ALP: Boltzmann suppression we need to rescale the energy loss rate by the ratio

Raffelt Phys. Rept. '90

$$R(m_a, T) \equiv \mathcal{E}_a(m_a, T)/\mathcal{E}_a(0, T)$$

energy density: $\mathcal{E}_a(m_a, T) = \frac{1}{2\pi^2} \int_{m_a}^{\infty} \frac{E^2 \sqrt{E^2 - m_a^2}}{e^{E/T} - 1} dE = \begin{cases} \frac{\pi^2}{30} T^4 & m_a \ll T \\ \frac{1}{(2\pi)^{3/2}} T^4 \left(\frac{m_a}{T}\right)^{5/2} e^{-m_a/T} & m_a \gg T \end{cases}$

$$T_{\rm RG} \approx 10^8 K \approx 8.6\,\text{keV} \qquad T_{\rm WD} \approx 10^7 K \approx 0.8\,\text{keV}$$

Astrophysical bounds

Above ~0.1 MeV, supernova bounds become important

We get a bound from the cooling of the proto-neutron star in the SN1978A explosion to the ALP coupling to electrons (new!)

energy loss in highly-degenerate conditions: $$\epsilon = \frac{\pi}{15}\alpha_{\rm em}^2 \frac{T^4}{m_n (F_{ee}^A)^2} Y_p F = 1.2 \times 10^{20}\,\frac{\rm erg}{\rm g\,s}\left(\frac{10^7\,{\rm GeV}}{F_{ee}^A}\right)^2$$

angular integral (including plasma screening)

$$m_a \lesssim T_{SN} \approx 30\ {\rm MeV}: \quad F_{ee}^A \gtrsim 3.4 \times 10^7\,{\rm GeV}\ \ ({\rm SN1987A})$$

Similarly, bounds can be obtained for the $\mu\mu$ coupling and the μe coupling

Summary of astro-bounds ($m_a \approx 0$)

Process	Decay constant	Bound (GeV)	Experiment
	F_{ee}^A	4.6×10^9	WD
	F_{ee}^A	2.4×10^9	RG
Star cooling	F_{ee}^A	3.4×10^7	$\mathrm{SN1987A}_{ee}$
	$F_{\mu\mu}^A$	1.3×10^8	$\mathrm{SN1987A}_{\mu\mu}$
	$F_{\mu e}$	1.4×10^8	$\mathrm{SN1987A}_{\mu e}$

Bollig et al '20

equivalent to $\mathrm{BR}(\mu \to e a) \lesssim 4 \times 10^{-3}$

ALP dark matter

- Obvious requirement, cosmological lifetime

$$\frac{H_0}{\Gamma_{\rm tot}} = H_0 \tau_a > 1$$

- More stringent bound: extragalactic background light (from $a \to \gamma\gamma$)

Coupling to photons $(m_a \ll m_{\ell_i})$: $\qquad \mathcal{L}_{\rm eff} = E_{\rm UV} \frac{\alpha_{\rm em}}{4\pi} \frac{a}{f_a} F \tilde{F}$

depends on UV completion,
e.g. anomaly coefficient (QCD axion: $E_{\rm UV} = E/2N$)

- Production: misalignment mechanism

$$\Omega_a^{T\text{-indep.}} h^2 = 0.12 \times 10^{-2} \sqrt{\frac{m_a}{\rm eV}} \left(\frac{f_a}{10^{10}\rm GeV}\right)^2 \left(\frac{\theta_0}{\pi}\right)^2 \left(\frac{90}{g_*(T_{\rm osc})}\right)^{1/4}$$

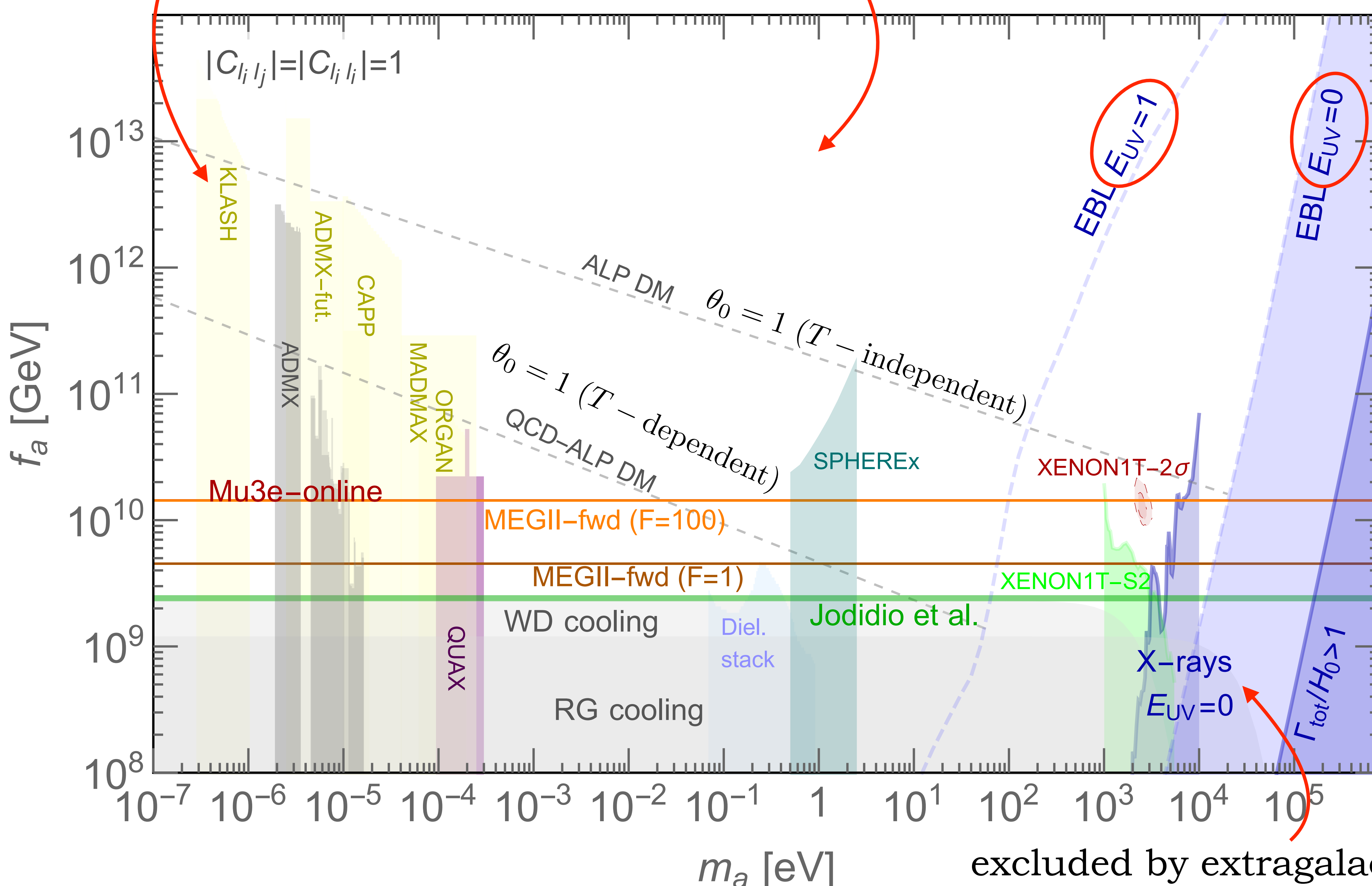
misalign. angle

it can be enhanced if ALP mass suppressed at
finite temperature (e.g. QCD axion)

ALP dark matter

axion/ALP
DM searches
$(E_{\rm UV} = 1)$

everywhere here ALP can be DM

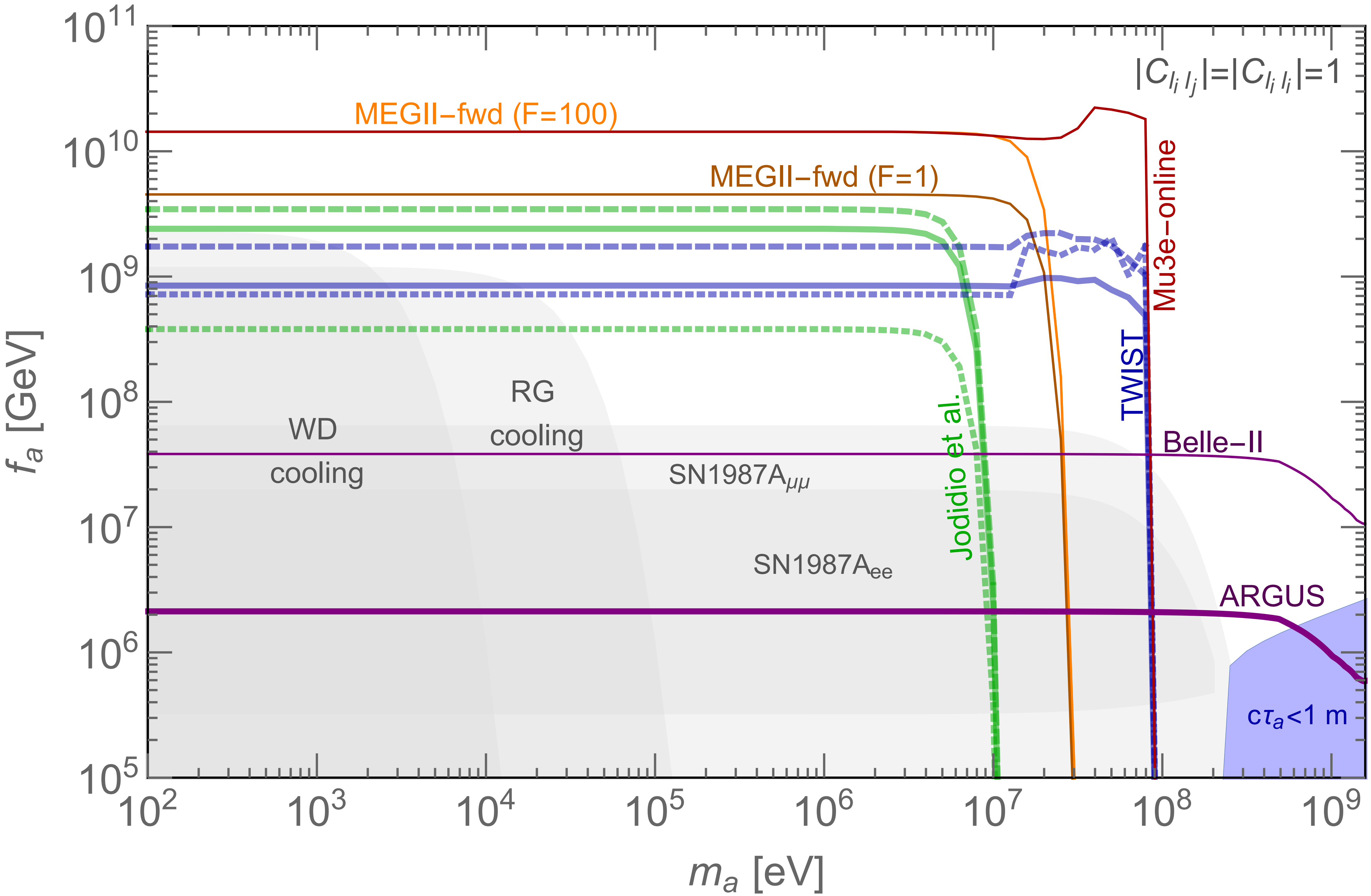


excluded by extragalactic
background light/X-rays

Putting everything together…

Summary of model-independent bounds

$$\mathcal{L}_{a\ell\ell} = \frac{\partial^\mu a}{2 f_a} \left(C^V_{ij} \, \bar{\ell}_i \gamma_\mu \ell_j + C^A_{ij} \, \bar{\ell}_i \gamma_\mu \gamma_5 \ell_j \right)$$



Models

Models for LFV ALPs

- How generic is a PNGB with flavour-violating couplings to leptons?
- Can we test ALPs with LFV *beyond stars*?
- That is, how are FC and FV couplings related (F_{ee}, $F_{\mu e}$, etc.) ?

To answer these questions, we need to consider specific models

- LFV QCD axion:

QCD axion (DSFZ type) with leptons carrying non-universal PQ

- LFV axiflavon:

QCD axion obtained by identifying PQ = Froggatt-Nielsen U(1)
(FV axion-quark couplings suppressed by an additional flavour SU(2))

- Leptonic familon

PNGB from spontaneously broken Froggatt-Nielsen U(1) (acting on leptons only)

- Majoron

spontaneously broken lepton number (in the context of low-energy seesaw)

LFV QCD axion

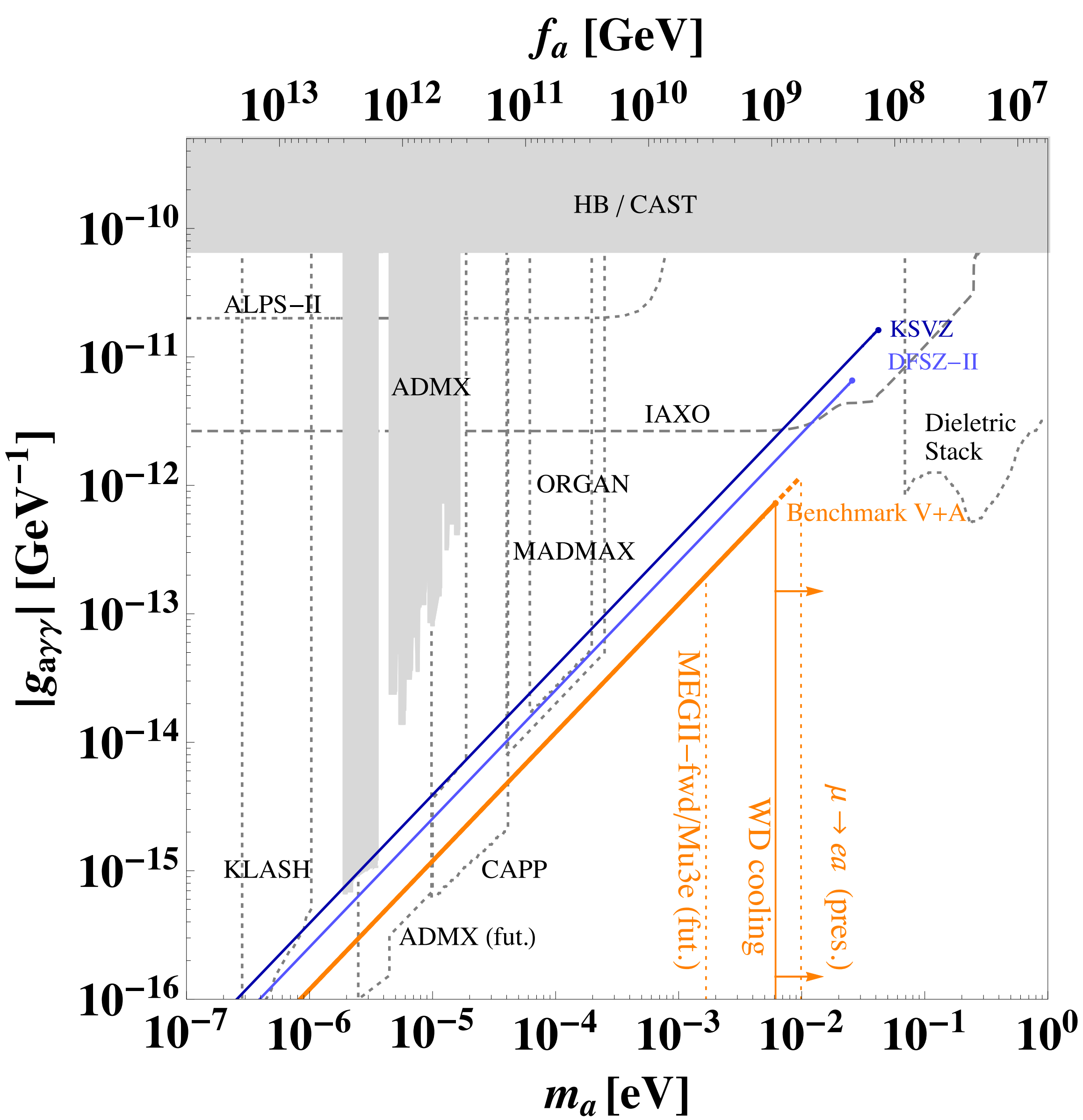
flavor non-universal charges
→ flavor-violating couplings

$$C^{V,A}_{f_i f_j} = \frac{1}{2N}\left(V^{f\,\dagger}_R X_{f_R} V^f_R \pm V^{f\,\dagger}_L X_{f_L} V^f_L\right)_{ij}$$

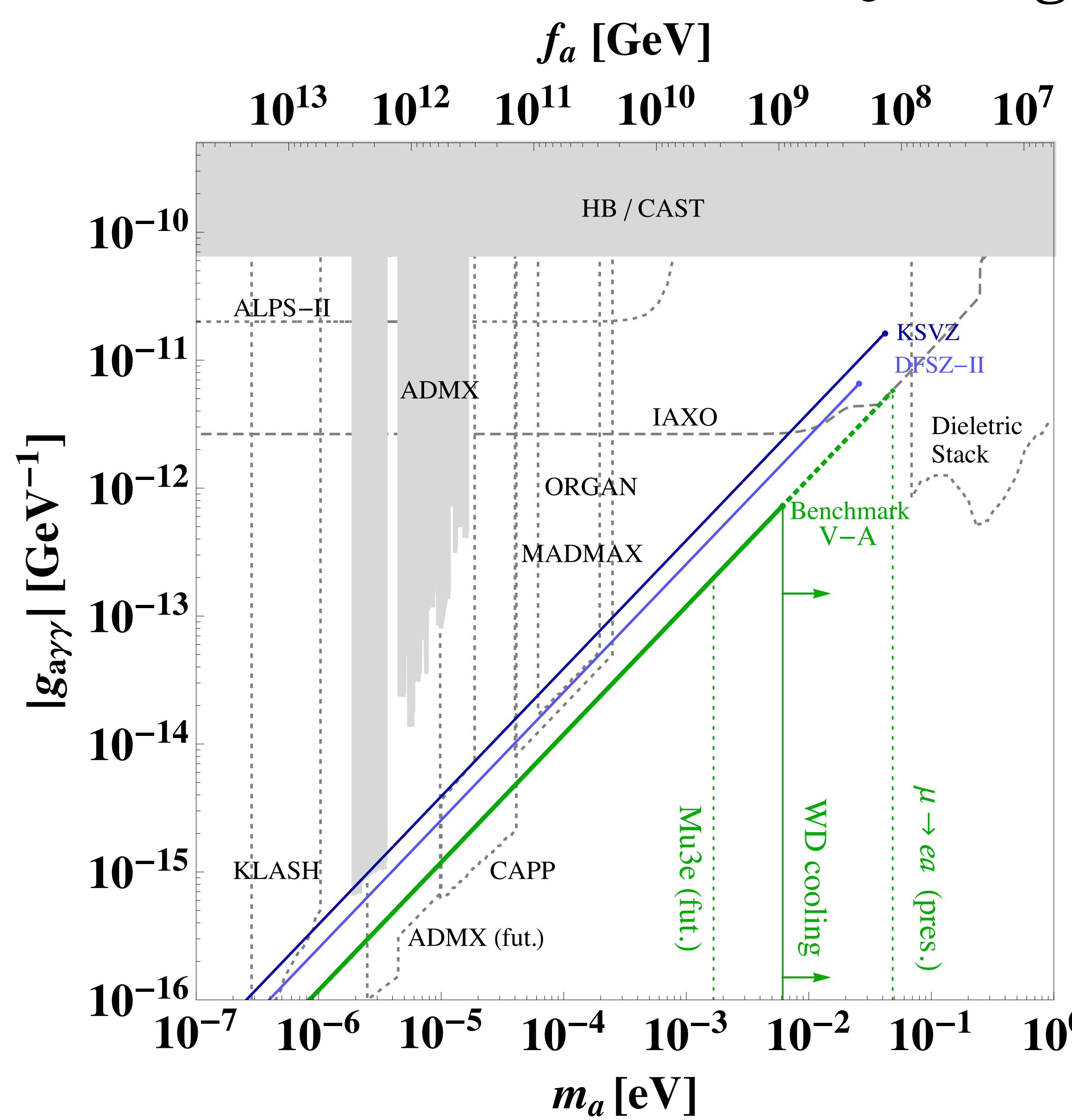
$$V_L^\dagger Y^e V_R = Y^e_{diag}$$

L and R unitary rotations to the lepton mass basis

matrices of PQ charges



V+A axion (large R rotations)



V-A axion (large L rotations)

LFV QCD axion

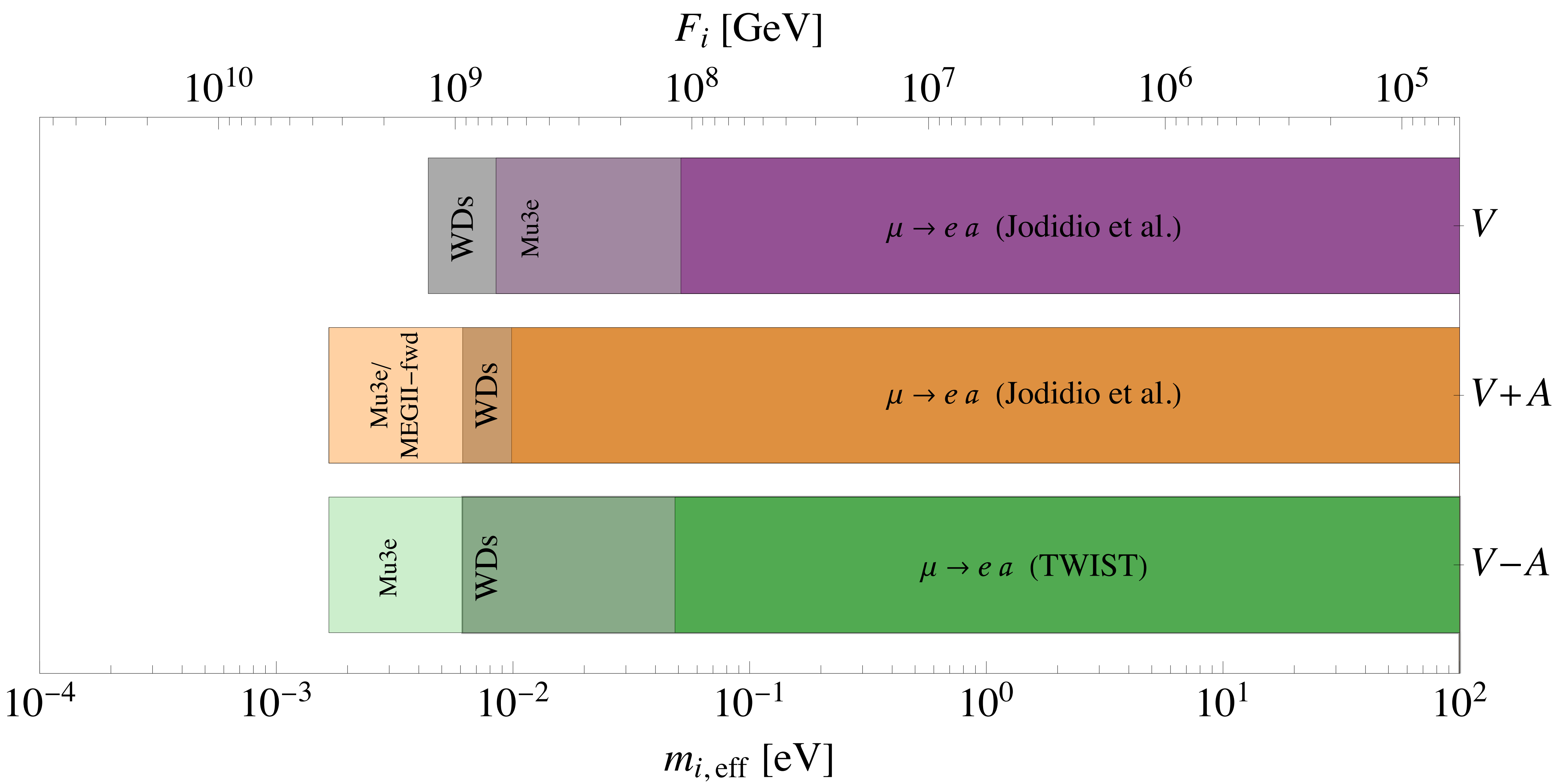
flavor non-universal charges
→ flavor-violating couplings

$$C^{V,A}_{f_i f_j} = \frac{1}{2N}\left(V_R^{f\,\dagger} X_{f_R} V_R^f \pm V_L^{f\,\dagger} X_{f_L} V_L^f\right)_{ij}$$

$$V_L^\dagger Y^e V_R = Y^e_{diag}$$

L and R unitary rotations to the lepton mass basis

matrices of PQ charges



Type I seesaw: $\mathcal{L} = \mathcal{L}_{\rm SM} + i\overline{N}\not{\partial}N - \left(Y_N \overline{N}\widetilde{\Phi}^\dagger L + \frac{1}{2}M_N\overline{N}N^c + \text{h.c.}\right)$

L-breaking term

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & Y_N^T v/\sqrt{2} \\ Y_N v/\sqrt{2} & M_N \end{pmatrix} \quad \xRightarrow{M_N \gg Y_N v} \quad m_\nu = -\frac{v^2}{2} Y_N^T M_N^{-1} Y_N$$

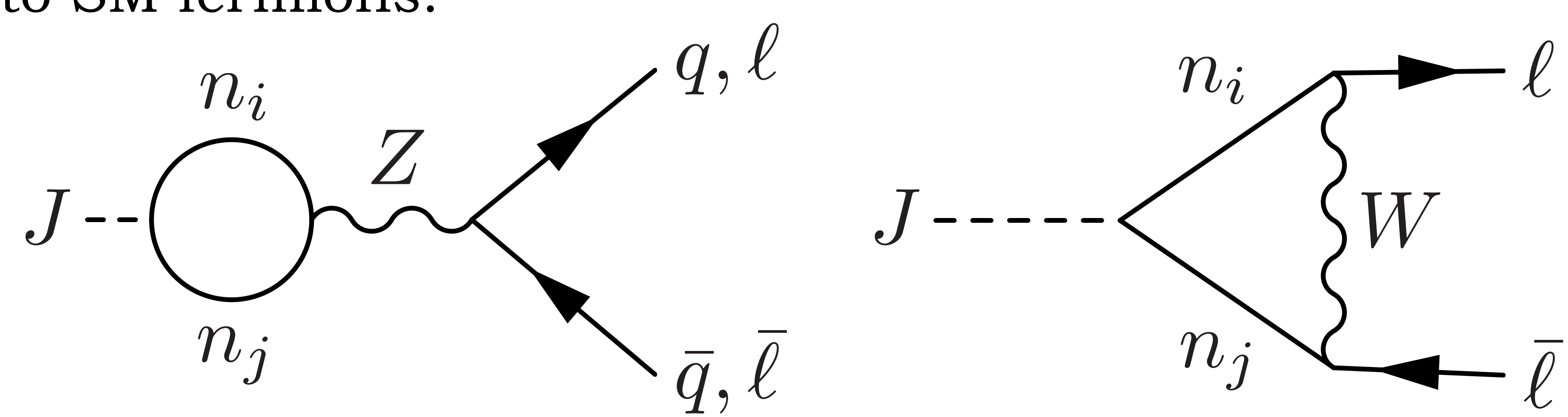
Spontaneous breaking of the lepton number:

$$\frac{1}{2}\lambda_N\,\sigma \bar{N}^c N, \quad \sigma = \frac{f_N + \hat{\sigma}}{\sqrt{2}} e^{iJ/f_N} \quad \Longrightarrow \quad M_N = \lambda_N f_N/\sqrt{2}$$

PNGB: Majoron!

Chikashige Mohapatra Peccei ‘80

Couplings to SM fermions:



Majoron

Type I seesaw: $\mathcal{L} = \mathcal{L}_{\text{SM}} + i\overline{N}\partial\!\!\!/ N - \left(Y_N \overline{N}\widetilde{\Phi}^\dagger L + \frac{1}{2} M_N \overline{N} N^c + \text{h.c.} \right)$

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PNGB: Majoron!

Chikashige Mohapatra Peccei '80

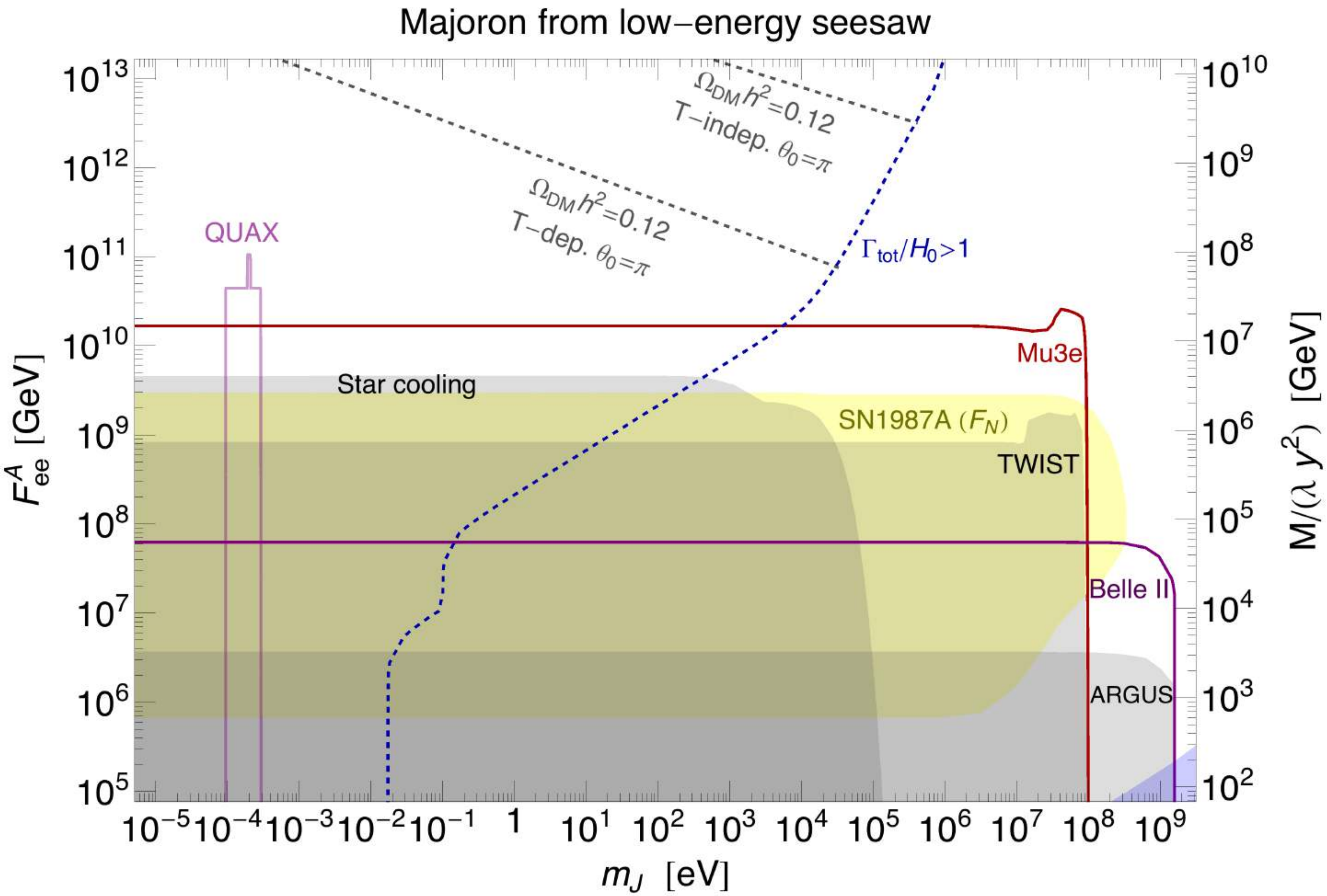
Couplings to SM fermions:

$$C^V_{q_i q_j} = 0\,, \qquad C^A_{q_i q_j} = -\frac{T_3^q}{16\pi^2}\delta_{ij}\,\text{Tr}\left(Y_N Y_N^\dagger\right)\,,$$

$$C^V_{\ell_i \ell_j} = \frac{1}{16\pi^2}\left(Y_N Y_N^\dagger\right)_{ij}\,, \qquad C^A_{\ell_i \ell_j} = \frac{1}{16\pi^2}\left[\frac{\delta_{ij}}{2}\text{Tr}\left(Y_N Y_N^\dagger\right) - (Y_N Y_N^\dagger)_{ij}\right]$$

Generically flavour-violating, (V-A)

Pilaftsis '94
Garcia-Cely Heeck '17



Lepton number anomaly free: suppressed coupling to photons ($E_{\rm UV}$=0)

$$\Gamma(a \to \gamma\gamma) = \frac{\alpha_{\rm em}^2 E_{\rm eff}^2}{64\pi^3}\frac{m_a^3}{f_a^2}, \qquad m_a \ll m_{\ell_i}: \; E_{\rm eff} \simeq E_{\rm UV} \qquad \mathcal{L}_{\rm eff} = E_{\rm UV}\frac{\alpha_{\rm em}}{4\pi}\frac{a}{f_a}F\tilde{F}$$

Summary

PNGBs from non-universal global U(1)s (or due to loop effects) give rise to lepton-flavour-violating decays

We have huge room for improvement over the old limits
We propose to start with a MEGII-fwd phase of MEG II

Essential interplay among μ, τ, and astrophysical bounds

Very large symmetry-breaking scales can be probed

Future CLFV limits can supersede stellar bounds even for small ALP masses and start testing the ALP DM region

Thank you!

谢谢

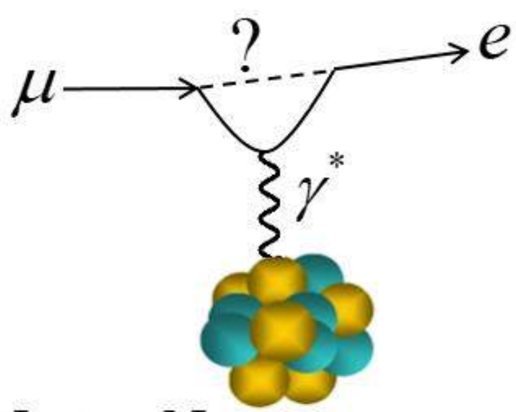
Additional slides

Comparison in the case $m_a \approx 0$

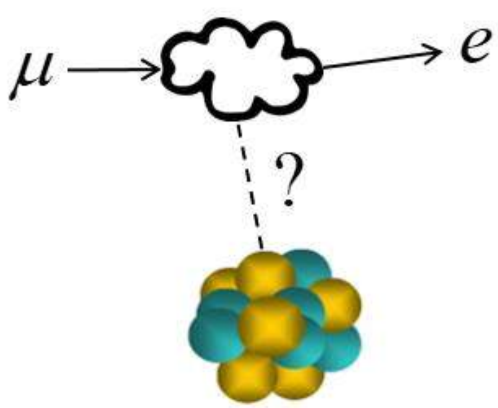
$$\mathcal{L}_{a\ell\ell} = \frac{\partial^\mu a}{2f_a}\left(C^V_{ij}\ \bar{\ell}_i\gamma_\mu\ell_j + C^A_{ij}\ \bar{\ell}_i\gamma_\mu\gamma_5\ell_j\right) \qquad F^{V,A}_{ij} \equiv \frac{2f_a}{C^{V,A}_{ij}} \qquad F_{ij} \equiv \frac{2f_a}{\sqrt{|C^V_{ij}|^2 + |C^A_{ij}|^2}}$$

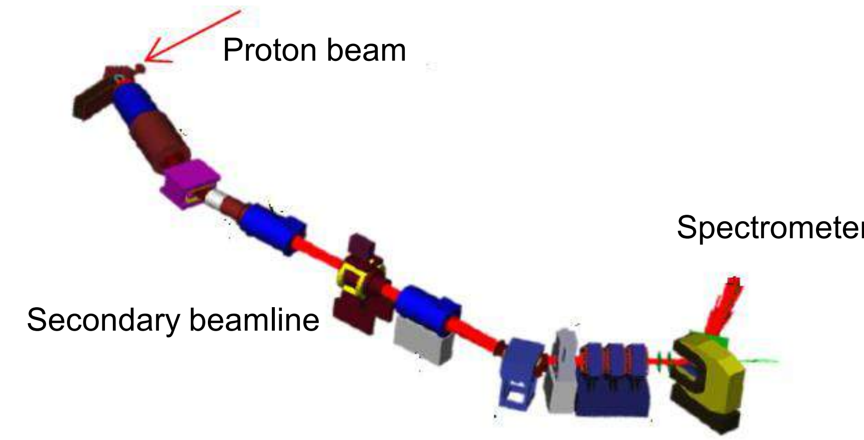
Present best limits				
Process	BR Limit	Decay constant	Bound (GeV)	Experiment
Star cooling	–	F^A_{ee}	4.6×10^9	WDs [44]
	–	$F^A_{\mu\mu}$	1.6×10^6	SN1987A$_{\mu\mu}$ [45]
	4×10^{-3}	$F_{\mu e}$	1.4×10^8	SN1987A$_{\mu e}$ (Sec. 6.1)
$\mu \to e\, a$	$2.6 \times 10^{-6*}$	$F_{\mu e}$ (V or A)	4.8×10^9	Jodidio at al. [9]
$\mu \to e\, a$	$2.5 \times 10^{-6*}$	$F_{\mu e}$ ($V + A$)	4.9×10^9	Jodidio et al. [9]
$\mu \to e\, a$	$5.8 \times 10^{-5*}$	$F_{\mu e}$ ($V - A$)	1.0×10^9	TWIST [10]
$\mu \to e\, a\, \gamma$	$1.1 \times 10^{-9*}$	$F_{\mu e}$	$5.1 \times 10^{8\#}$	Crystal Box [46]
$\tau \to e\, a$	$2.7 \times 10^{-3**}$	$F_{\tau e}$	4.3×10^6	ARGUS [43]
$\tau \to \mu\, a$	$4.5 \times 10^{-3**}$	$F_{\tau\mu}$	3.3×10^6	ARGUS [43]

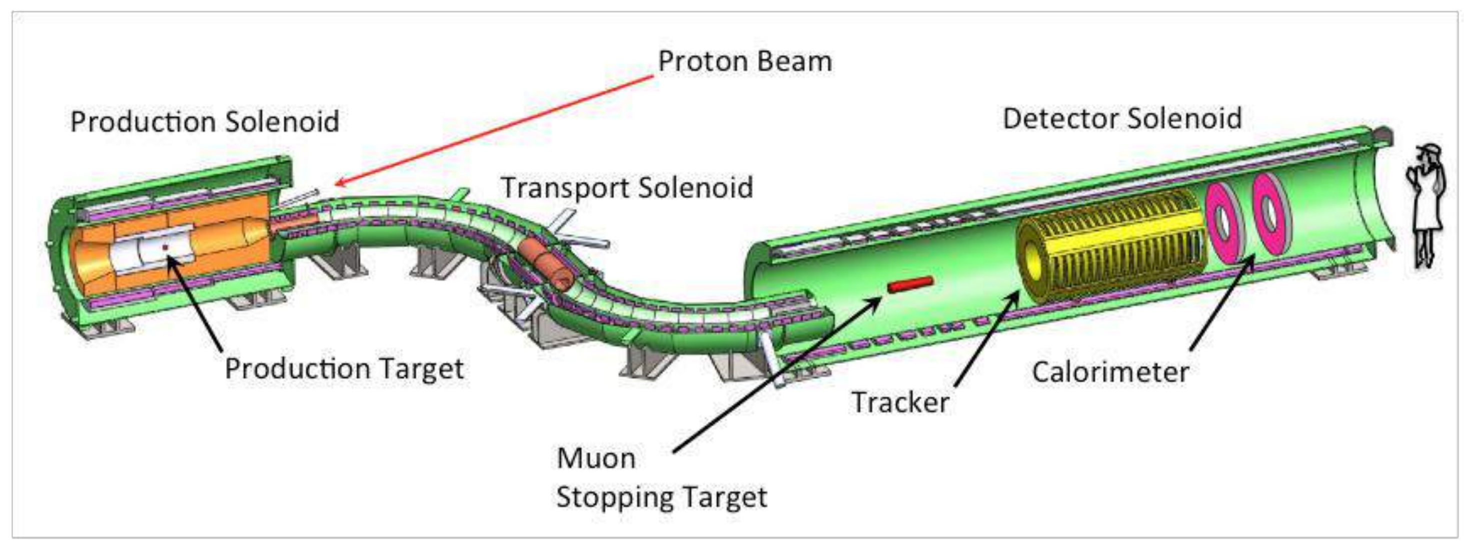
$\mu \to e$ conversion in nuclei experiments

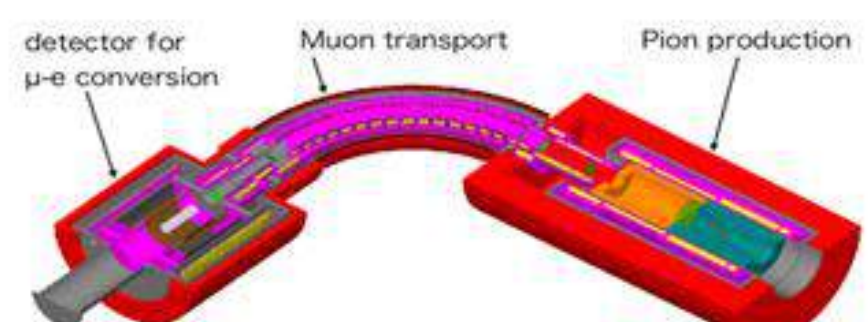


$\mu N \to e N$







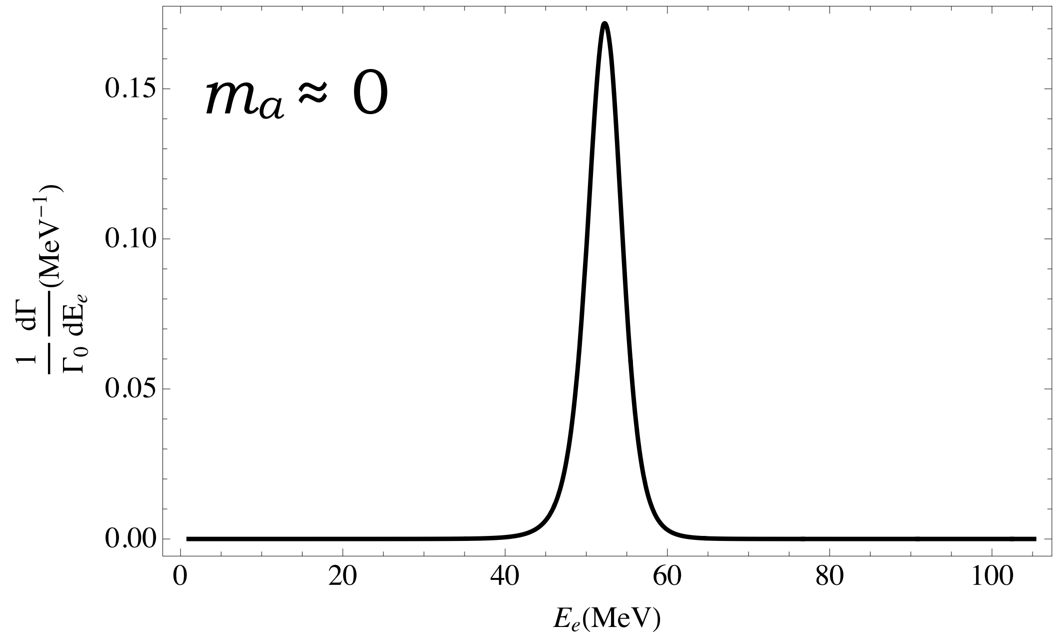


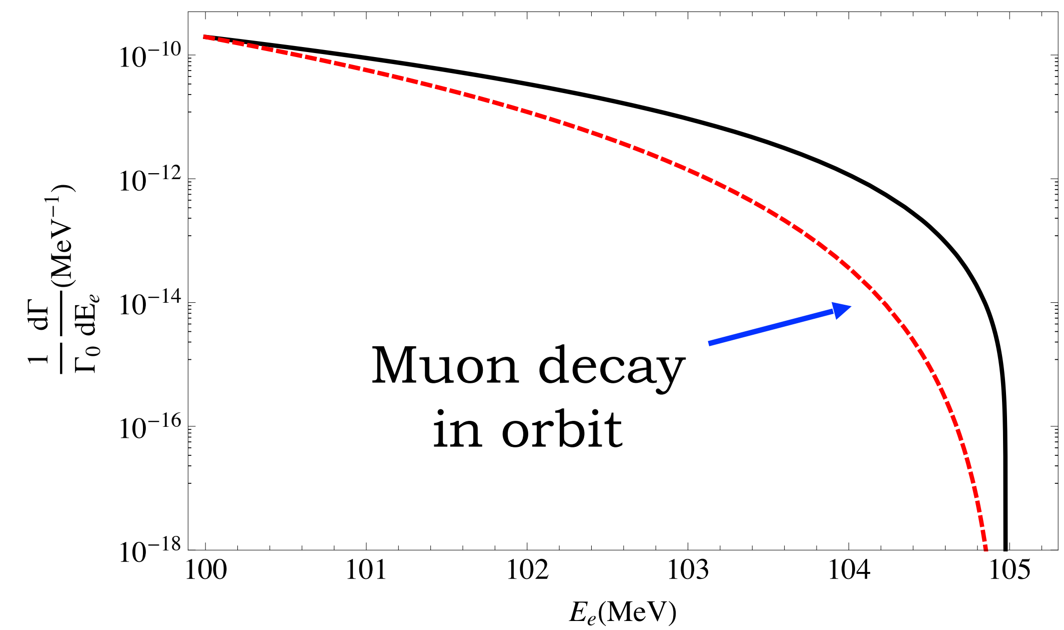
David Hitlin
Beijing CLFV School
June 3-7, 2019
Lecture 1

Future prospects: COMET/Mu2e

- Prospect at $\mu \to e$ conversion experiments (Garcia i Tomo et al. '11)

Spectrum of $\mu \to ea$ emission in orbit (for Al):





Sensitivity in terms of the $\mu \to e$ conv. limit:

27 (in Al)

10^{-17}

Phase-space correction factor

$$B(\mu \to eJ) \sim \frac{N_R R_{\mu e}}{f_J}\frac{\Gamma_{\text{capture}}}{\Gamma(\mu \to e\nu_\mu\bar{\nu}_e)} \sim \frac{N_R R_{\mu e}}{f_J}1.5 \Rightarrow 2\times10^{-6}$$

Fraction of $\mu \to ea$ events in the signal region

2×10^{-10} (E_e > 100 MeV)

Possible bound at the level of Jodidio et al.

Limited by the $\mu \to e$ conv. signal region (only the tail included): dedicated search?

Low-energy seesaw: pseudo-Dirac neutrinos → approximately conserved (generalised) lepton number

Ibarra Molinaro Petcov ‘11

$$M_N = \begin{pmatrix} 0 & M \\ M & 0 \end{pmatrix} = \frac{\lambda}{\sqrt{2}} \begin{pmatrix} 0 & f_N \\ f_N & 0 \end{pmatrix} \qquad y_N = \begin{pmatrix} y_{e1} & y_{e2} \\ y_{\mu 1} & y_{\mu 2} \\ y_{\tau 1} & y_{\tau 2} \end{pmatrix}$$

Global U(1) symmetry in the limit $y_{\ell 1} \to 0$

After imposing fit to neutrino obs., two free parameters: M, $y = \max\left[\mathrm{eig}(y_N y_N^\dagger)\right]$

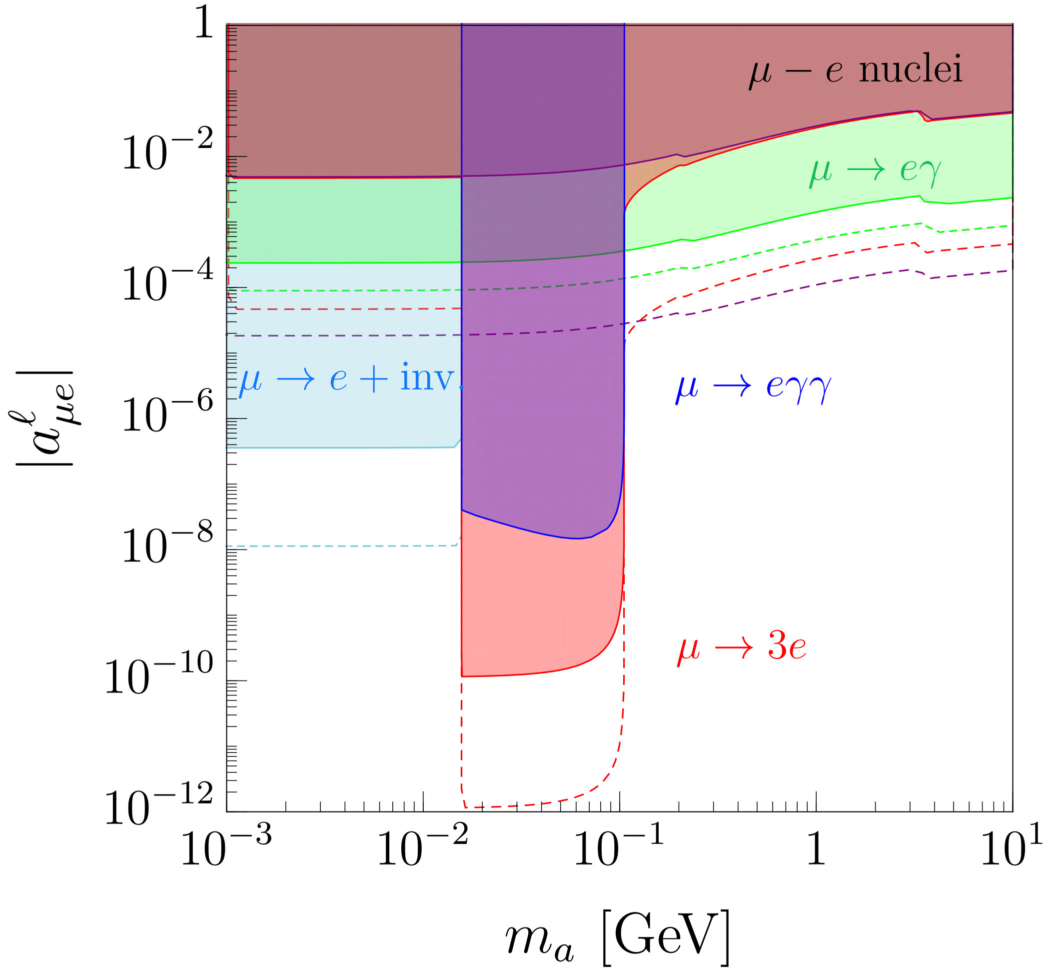
$$y_N y_N^\dagger \approx y^2 \frac{m_3}{m_2+m_3} A_i^* A_j\,, \qquad \text{where } A_i = U_{i3} + i U_{i2}\sqrt{m_2/m_3}$$

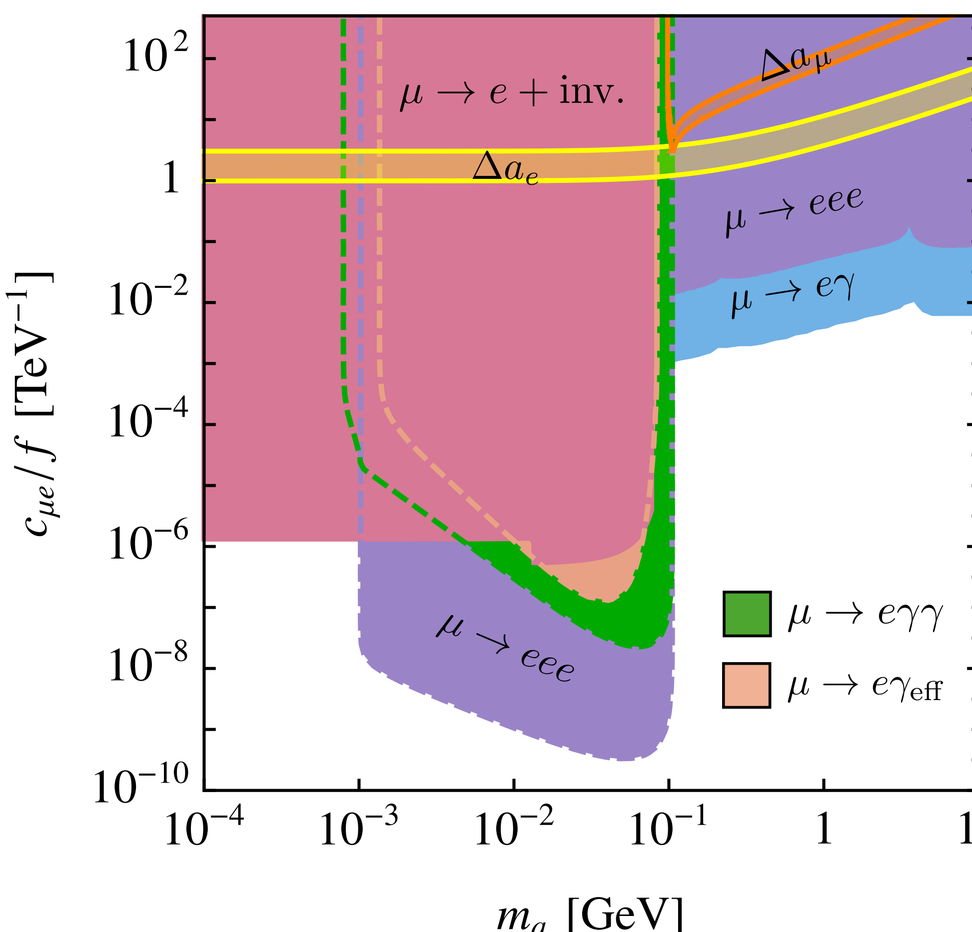
$$\Rightarrow \quad F^A_{ee} = \frac{1.1\times 10^{10}\,\mathrm{GeV}}{\lambda y^2}\left(\frac{M}{10^7\,\mathrm{GeV}}\right), \qquad F_{\mu e} = \frac{1.4\times 10^{10}\,\mathrm{GeV}}{\lambda y^2}\left(\frac{M}{10^7\,\mathrm{GeV}}\right)$$

$$F_{\tau e} = \frac{1.6\times 10^{10}\,\mathrm{GeV}}{\lambda y^2}\left(\frac{M}{10^7\,\mathrm{GeV}}\right), \qquad F_{\tau\mu} = \frac{0.71\times 10^{10}\,\mathrm{GeV}}{\lambda y^2}\left(\frac{M}{10^7\,\mathrm{GeV}}\right)$$

CLFV from short-lived ALPs

Bauer et al. '19
Cornella et al. '19





$c_{ee}/f = 1\,\text{TeV}$

$$\Gamma(a \to \ell_i \ell_j) = \frac{m_a}{2\pi}\left[\left(\frac{m_{\ell_i} - m_{\ell_j}}{F^V_{ij}}\right)^2 + \left(\frac{m_{\ell_i} + m_{\ell_j}}{F^A_{ij}}\right)^2\right]\sqrt{1 - \frac{2(m^2_{\ell_i} + m^2_{\ell_j})}{m_a^2}};$$

$$\Gamma(a \to \gamma\gamma) = \frac{\alpha^2_{\text{em}} E^2_{\text{eff}}}{64\pi^3}\frac{m_a^3}{f_a^2}$$

$$E_{\text{eff}} = E_{\text{UV}} + \sum_f C^A_f B(\tau_f),$$

$$B(\tau) = \tau \arctan^2 \frac{1}{\sqrt{\tau - 1}} - 1$$

$$\tau_f = 4m_f^2/m_a^2 - i\epsilon$$