

# Axion field tomography: cosmic birefringence from the epochs of recombination and reionization

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Universita' del Salento, Lecce  
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# Searching for ULA through their coupling to EM

ALP can couple to EM through a Chern-Simons interaction

$$\frac{1}{4} g_{\phi\gamma} \phi F_{\mu\nu} \tilde{F}_{\mu\nu}$$



rotation of the plane of linear polarization  
clockwise on the sky

$$\beta = -\frac{1}{2} g_{\phi\gamma} \int \frac{\partial\phi}{\partial t} dt$$

Komatsu [arXiv:2202.13919]

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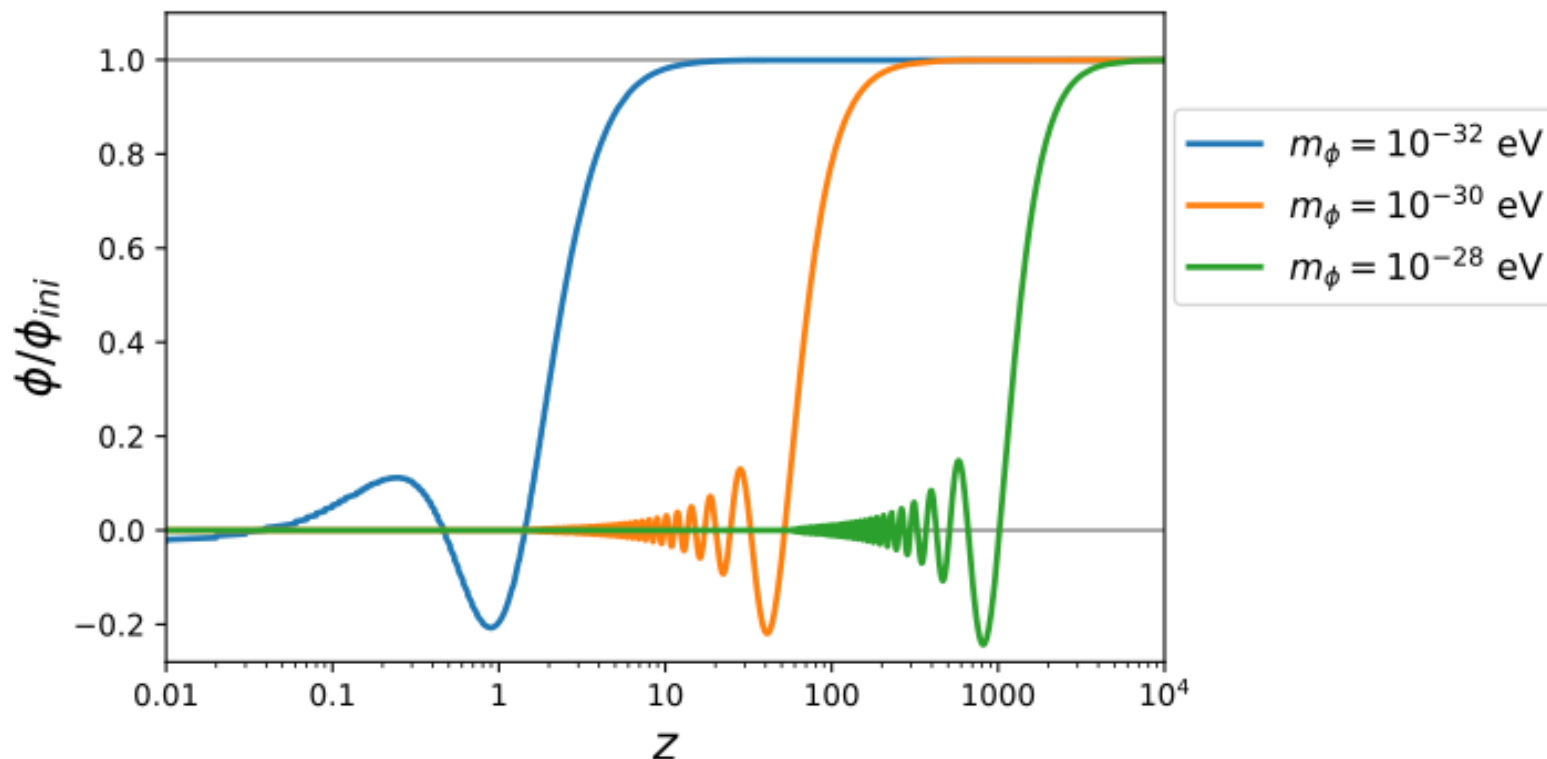
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ALP as dark energy

$$10^{-32} \text{ eV} \lesssim m_\phi \lesssim 10^{-28} \text{ eV}$$



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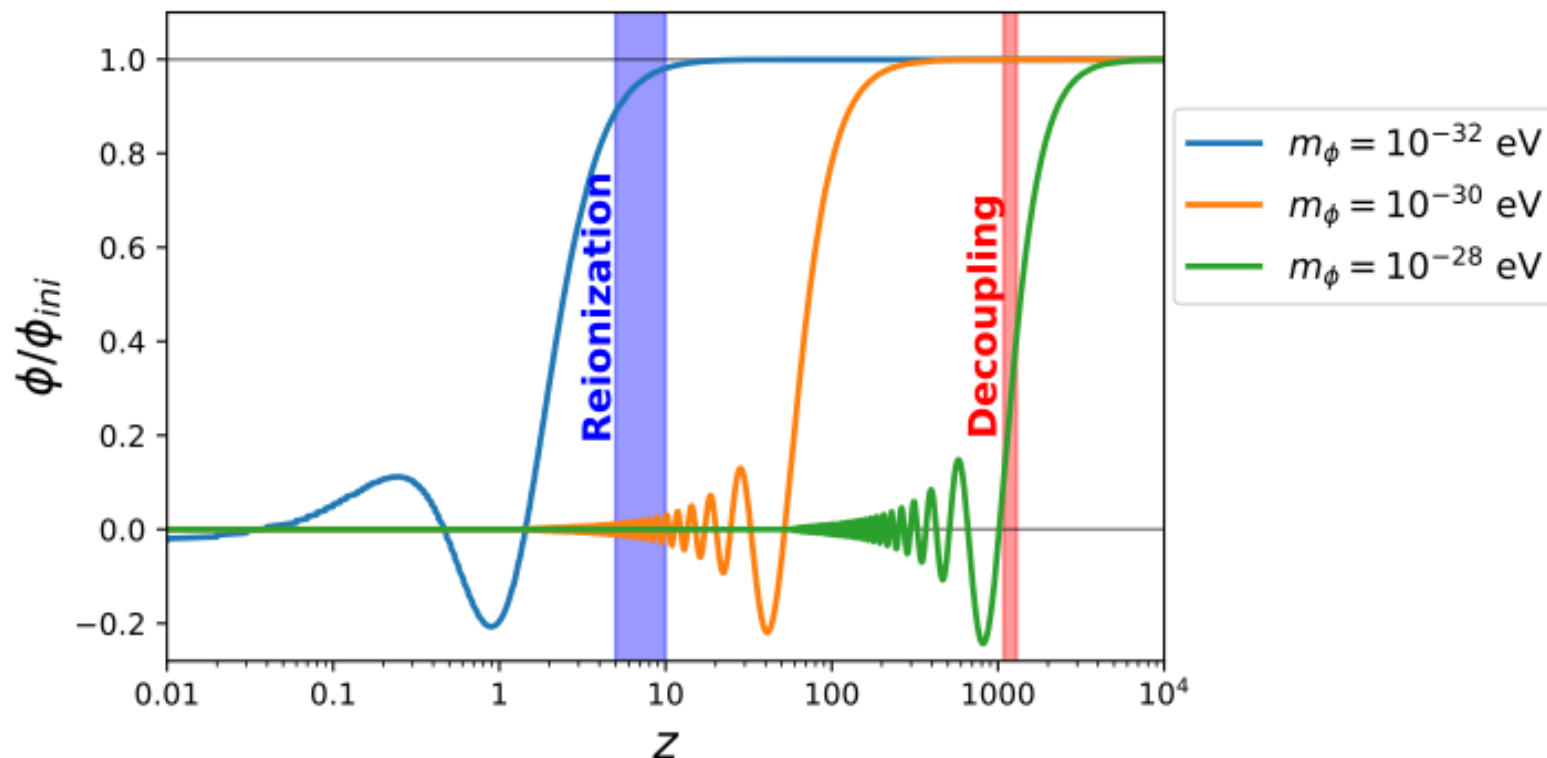
CMB offers two observational windows

- Small angular scales (high- $\ell$ ) are sensitive to  $\beta_{\text{dec}}$
- Large angular scales (low- $\ell$ ) are sensitive to  $\beta_{\text{reio}}$

Tomographic view of the ULA field at  $z \approx 10$  and  $z \approx 1000$

Sherwin&Namikawa[arXiv:2108.09287]

Nakatsuka+[arXiv:2203.08560]



Cosmic birefringence rotates the observed CMB

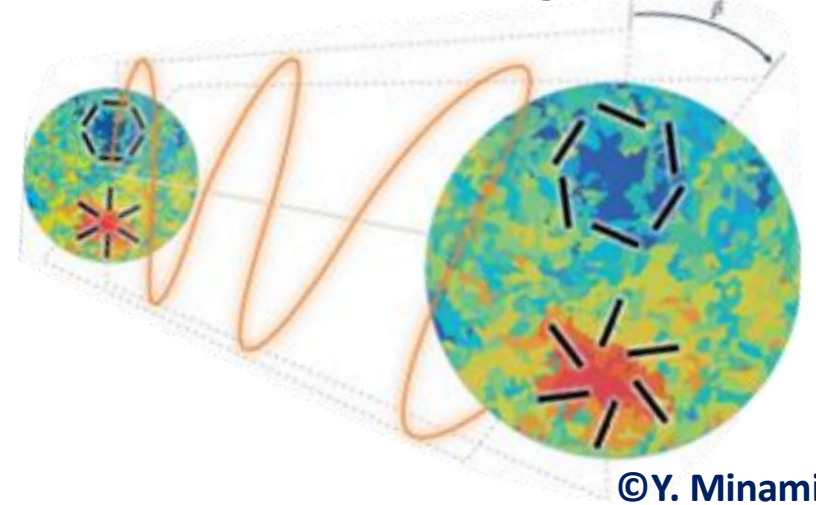
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so the observed angular power spectrum becomes

$$C_{\ell}^{EB,o} = \frac{1}{2} \sin(4\beta) \left( C_{\ell}^{EE,\text{cmb}} - C_{\ell}^{BB,\text{cmb}} \right) + \cos(4\beta) \cancel{C_{\ell}^{EB,\text{cmb}}}$$

$\Lambda$ CDM

## Cosmic birefringence



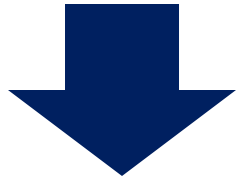
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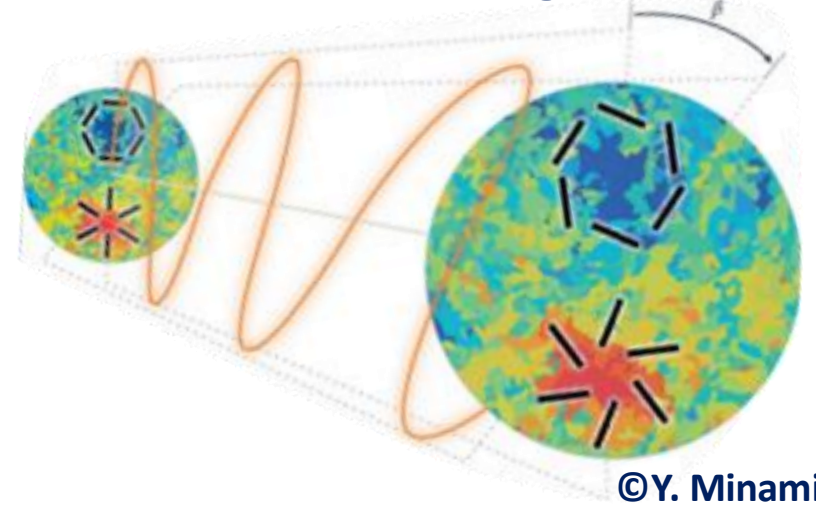
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**Base of most methodologies  
applied in the past**

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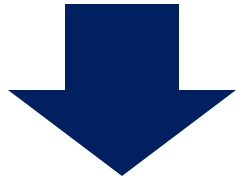
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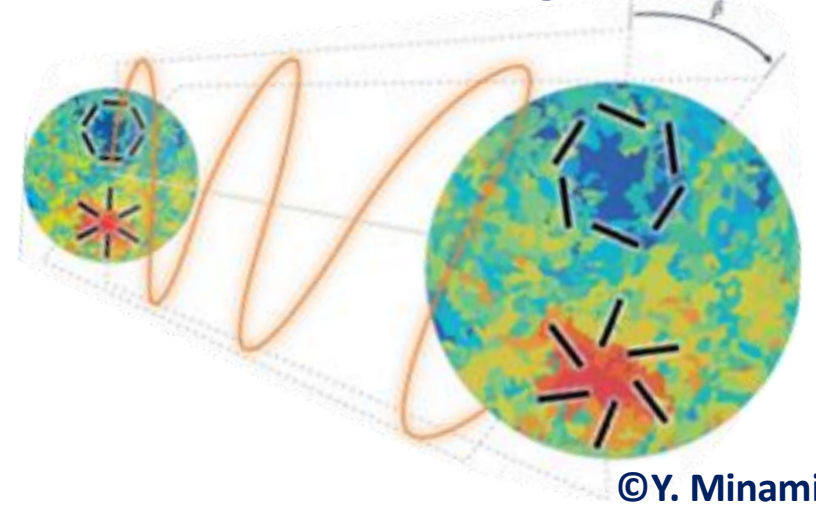
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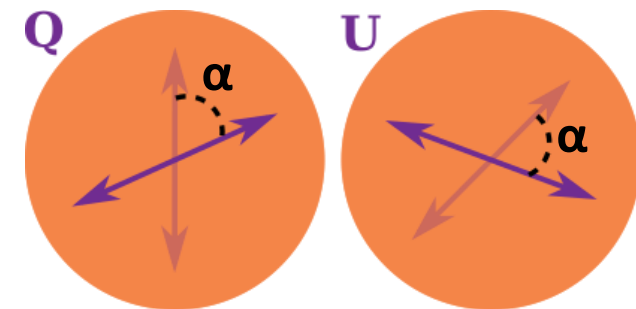
**Base of most methodologies  
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## Cosmic birefringence



OR

## Miscalibration of the detector's polarisation angle



**Unknown  $\alpha$  miscalibration  
Completely degenerate with birefringence**

Krachmalnicoff+[arXiv:2111.09140]



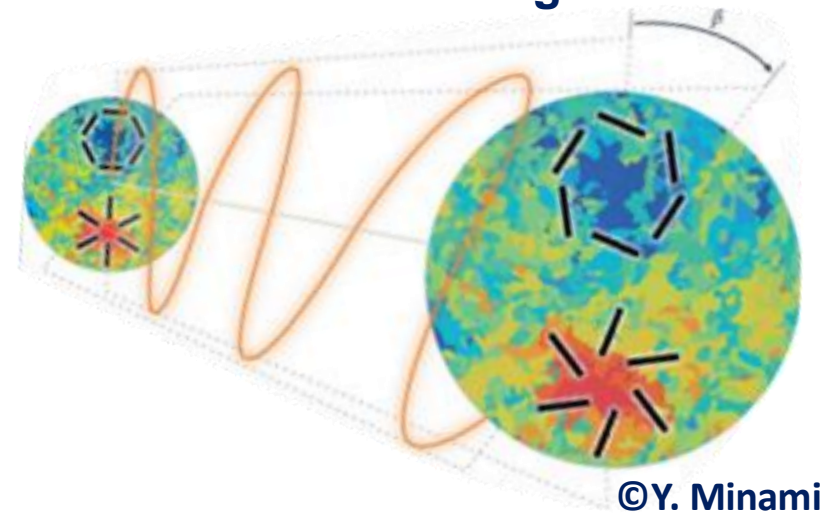
The observed signal is actually

$$\begin{pmatrix} E_{\ell m}^o \\ B_{\ell m}^o \end{pmatrix} = \begin{pmatrix} \cos(2\alpha + 2\beta) & -\sin(2\alpha + 2\beta) \\ \sin(2\alpha + 2\beta) & \cos(2\alpha + 2\beta) \end{pmatrix} \begin{pmatrix} E_{\ell m}^{\text{cmb}} \\ B_{\ell m}^{\text{cmb}} \end{pmatrix}$$

so that **EB** yields  $\alpha + \beta$

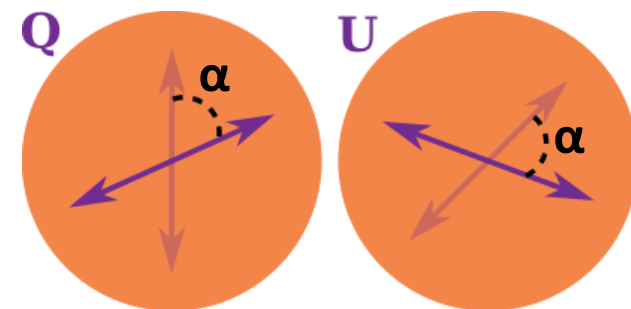
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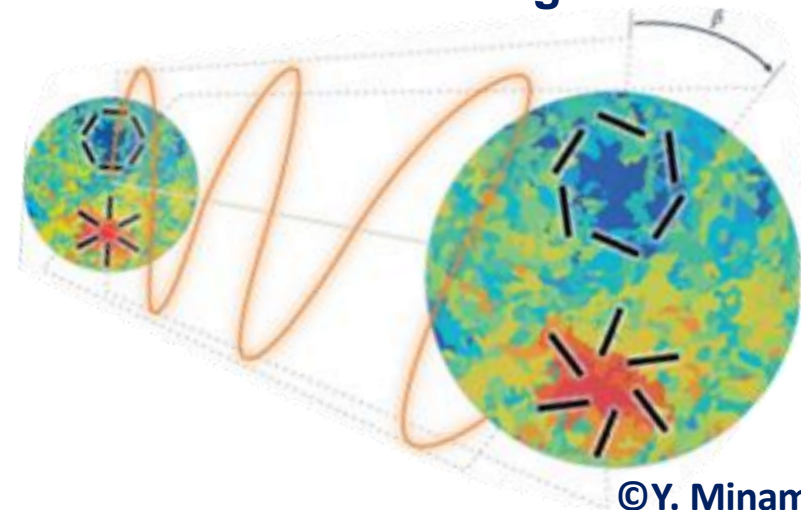
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Requires absolute calibration of instrumental  
polarisation angles

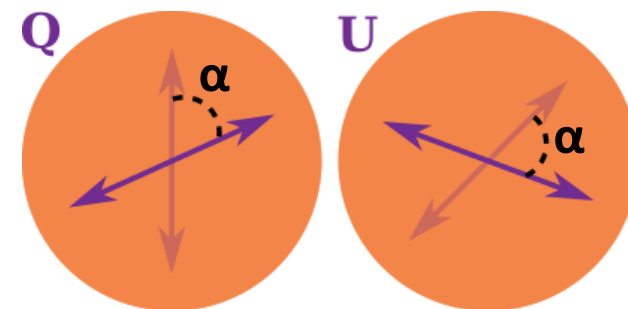
Previous measurements limited to  $\approx 0.5^\circ - 1^\circ$

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Galactic foreground emission not significantly affected by birefringence

Use **foregrounds as our calibrator**

Minami+[arXiv:1904.12440]

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## Synchrotron

**Synch EB statistically compatible with null**

Martire+[arXiv:2110.12803]

QUIJOTE [arXiv:2301.05113]



## Dust

**Misalignment between dust filaments and Galactic magnetic fields creates TB and EB correlations** Clark+[arXiv:2105.00120]

Cukierman+[arXiv:2208.07382]

**Planck reported :**

- **Dust TB > 0**
- **A hint of dust EB > 0**

Planck Collab [arXiv:1801.04945]

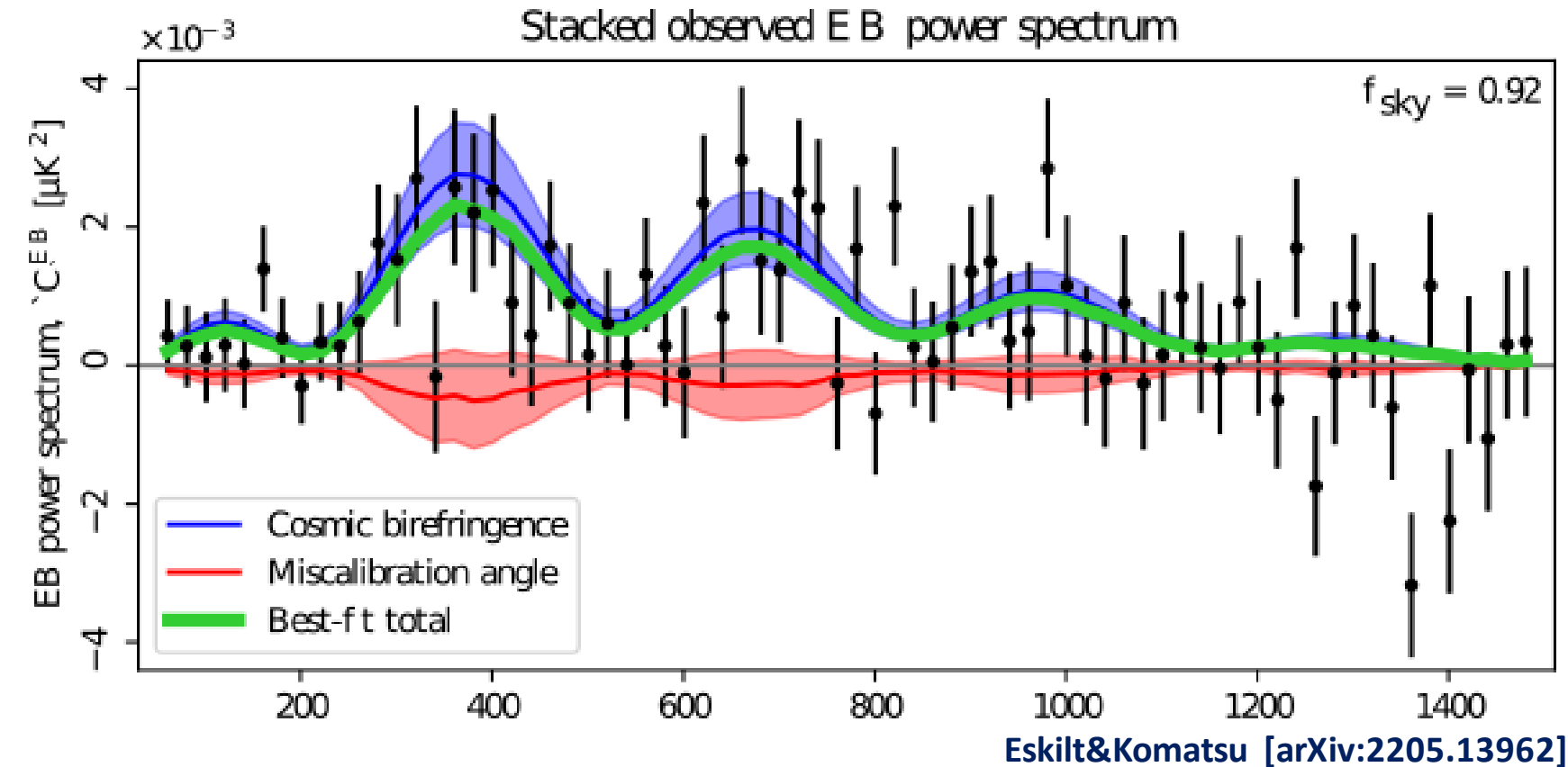
# Promising hint of a non-null $\beta_{\text{dec}}$ at high- $\ell$

Tightest constraint to date ( $3.6\sigma$ )

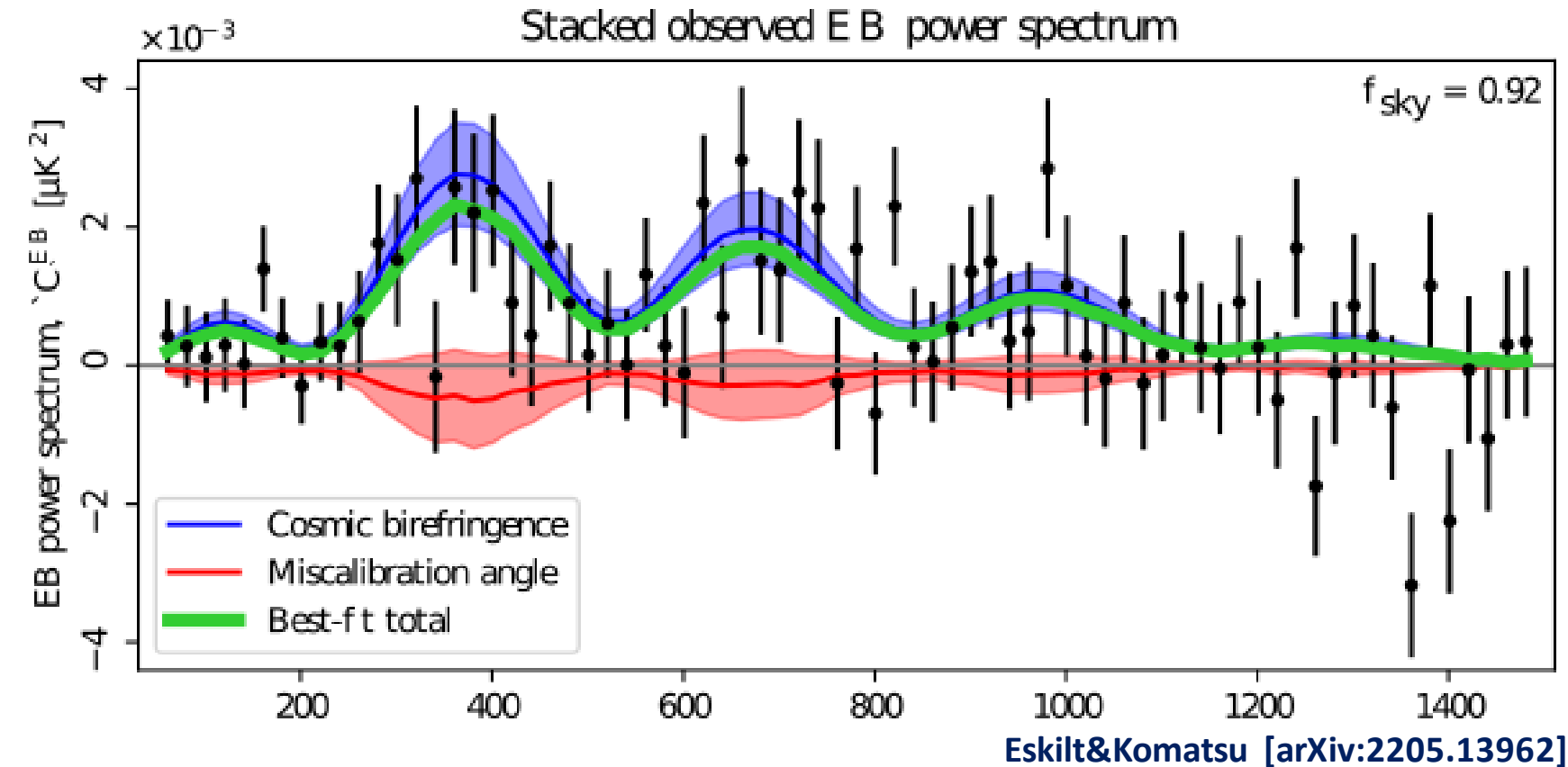
$$\beta = 0.342^\circ \pm^{+0.094^\circ}_{-0.091^\circ}$$

from the analysis of *Planck* and  
**WMAP** data

Eskilt&Komatsu [arXiv:2205.13962]



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Eskilt&Komatsu [arXiv:2205.13962]

Robust against instrumental  
systematics

PDP+[arXiv:2210.07655]

Eskilt+[arXiv:2305.02268]

Sensitive to **dust EB**

- Templates modeling dust as a modified blackbody
- Estimate the misalignment between filaments and magnetic fields

PDP+[arXiv:2201.07682]

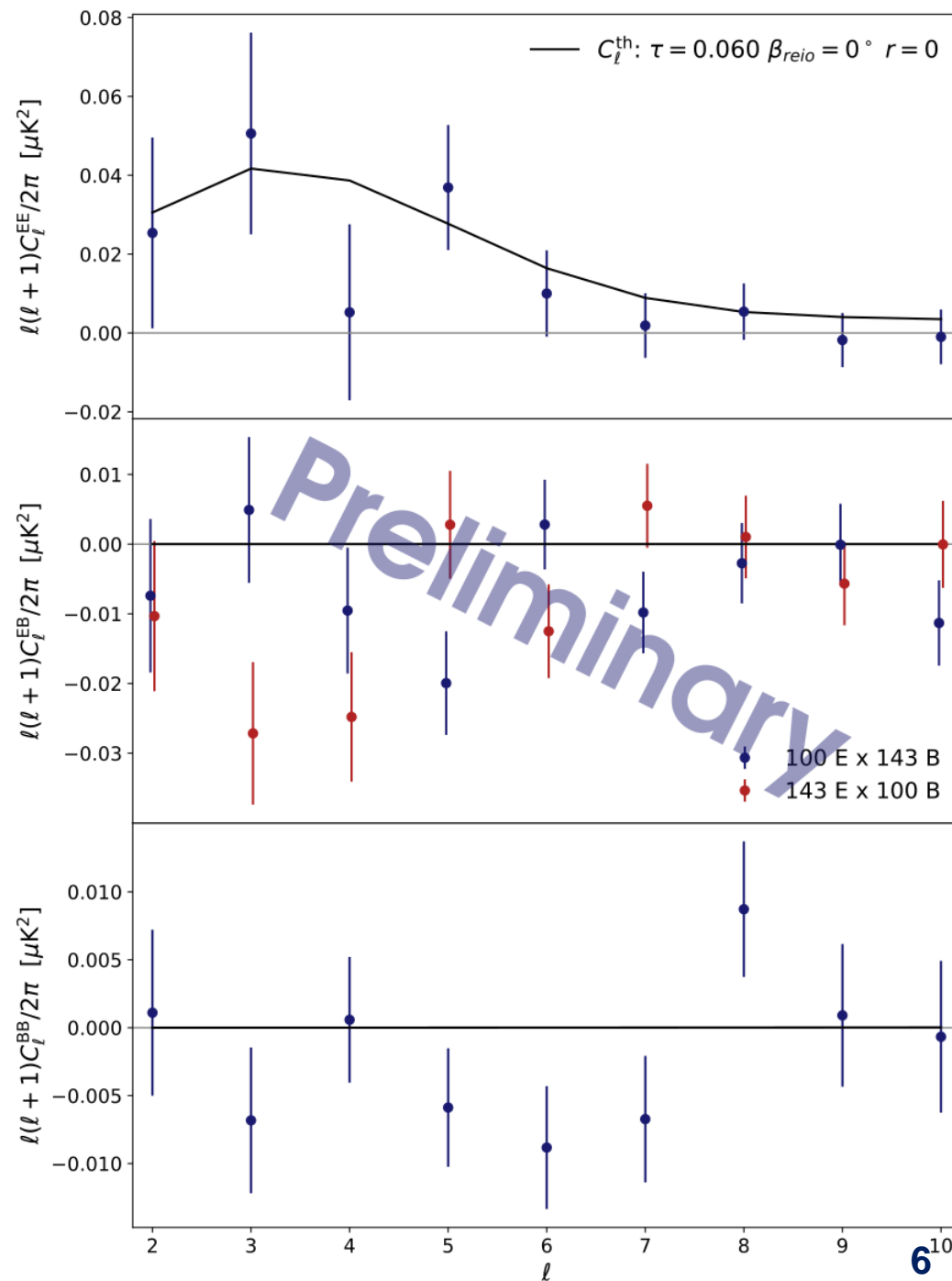
# Measuring $\beta_{\text{reio}}$ from $\ell \leq 10$

Work with CMB instead of frequency maps

Remove foregrounds by fitting and subtracting templates of synchrotron and dust emission

CMB spectra from 100 GHz x 143 GHz of *Planck* SRoll2.0

Delouis+[arXiv:1901.11386]





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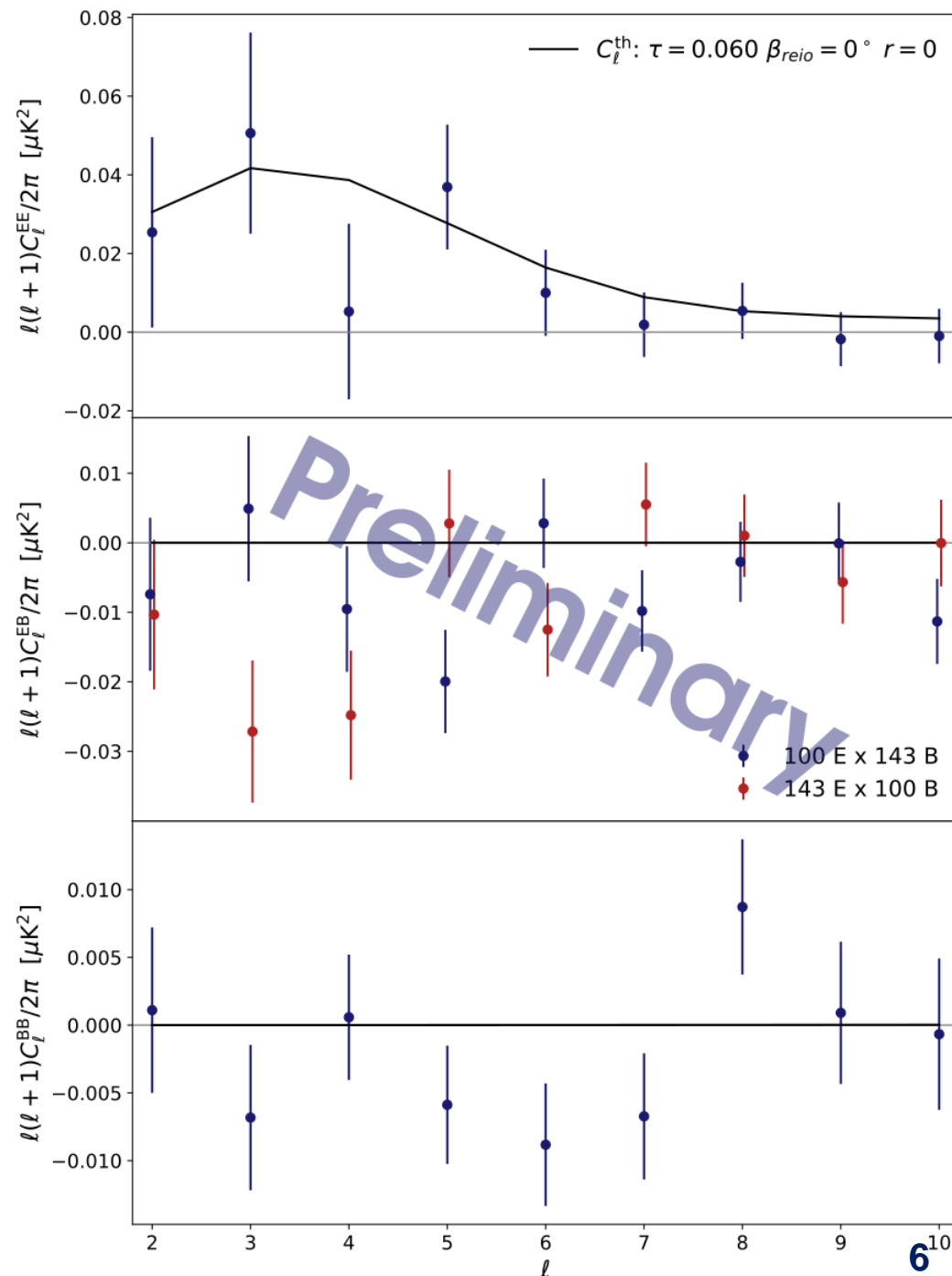
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Delouis+[arXiv:1901.11386]

$$P(\Theta|d, \mathcal{M}) \propto \mathcal{L}(d|\Theta, \mathcal{M}) \Pi(\Theta|\mathcal{M})$$

Sample over  $\Theta = \{\tau, \beta_{\text{reio}}, \beta_{\text{dec}}, \alpha_{100}, \alpha_{143}, r=0\}$

Gaussian prior on  $\beta_{\text{dec}}, \alpha_{100}, \alpha_{143}$  from high- $\ell$  analysis



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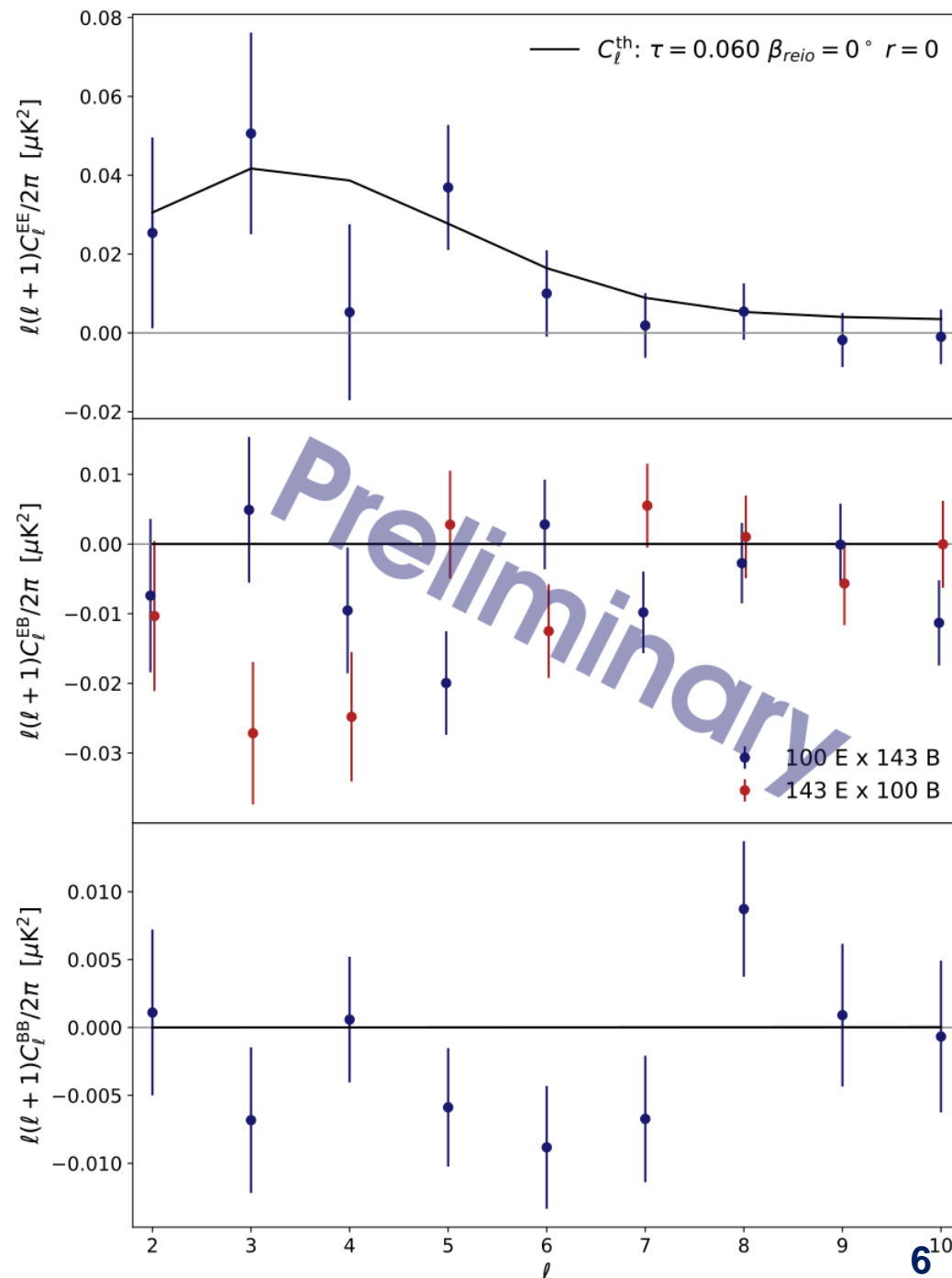
**momento**

Semi-analytical likelihood-approximation based on the principle of maximum entropy

Gratton [arXiv:1708.08479]

de Belsunce+[arXiv:2103.14378]

de Belsunce+[arXiv:2207.04903]



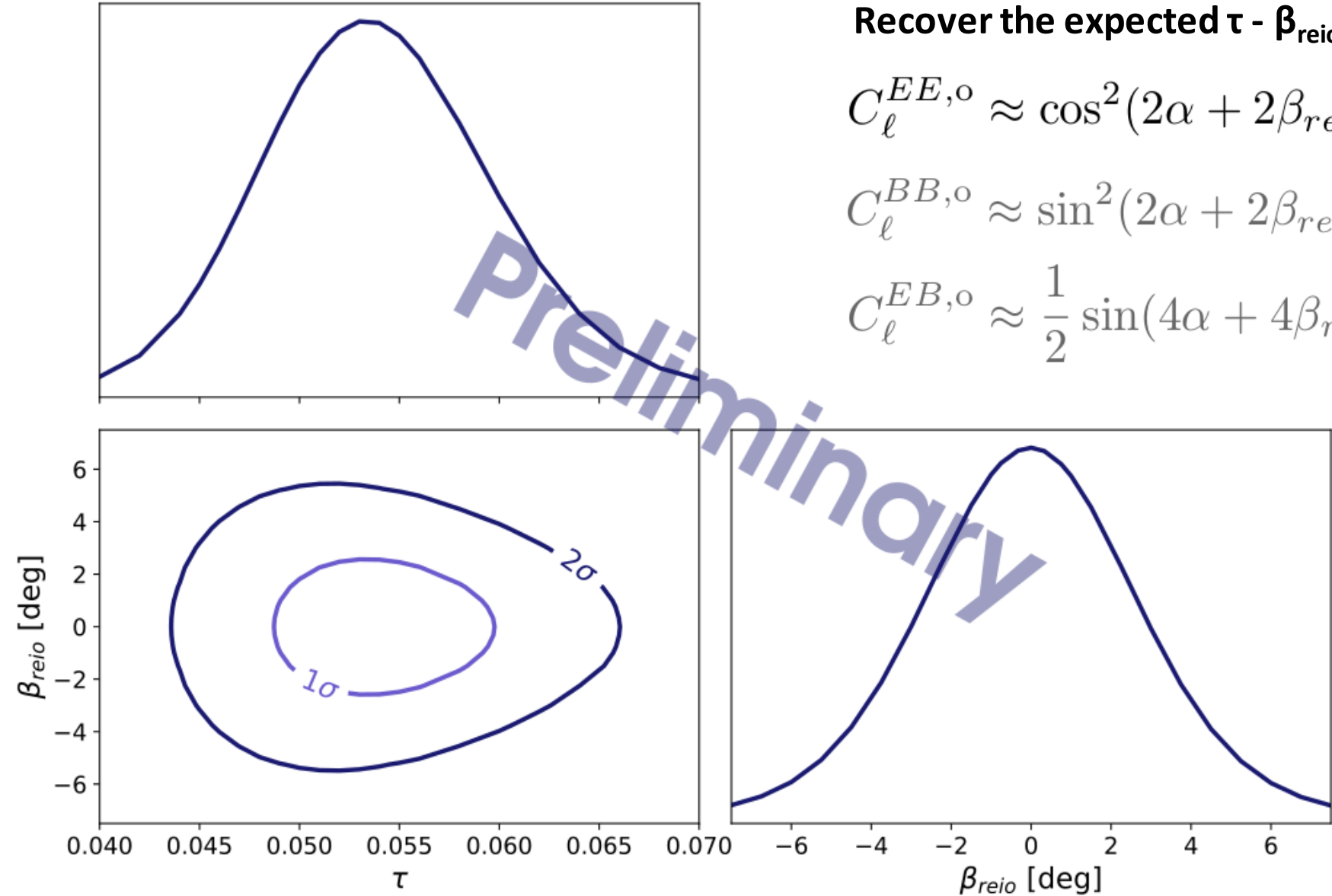
# EE – BB information

Recover the expected  $\tau - \beta_{\text{reio}}$  degeneracy

$$C_{\ell}^{EE,o} \approx \cos^2(2\alpha + 2\beta_{\text{reio}})C_{\ell}^{EE,\text{reio}}$$

$$C_{\ell}^{BB,o} \approx \sin^2(2\alpha + 2\beta_{\text{reio}})C_{\ell}^{EE,\text{reio}}$$

$$C_{\ell}^{EB,o} \approx \frac{1}{2} \sin(4\alpha + 4\beta_{\text{reio}})C_{\ell}^{EE,\text{reio}}$$



Best fit	
$\tau$	$0.054 \pm 0.005$
$\beta_{\text{reio}}$ [deg]	$-0.02 \pm 2.68$
$\beta_{\text{dec}}$ [deg]	$0.38 \pm 0.15$
$\alpha_{100}$ [deg]	$-0.38 \pm 0.16$
$\alpha_{143}$ [deg]	$0.06 \pm 0.15$

# Outlook

CMB polarization offers a tomographic view into of ALP at  $z \approx 10$  and  $z \approx 1000$  through the birefringence angles measured at the largest and smallest angular scales

Promising hint of a  $\approx 0.3^\circ$  birefringence angle from the epoch of recombination

Preliminary results on the first-ever attempt at simultaneously measuring miscalibration angles and the birefringence angle from the epoch of reionization

- $2.7^\circ$  sensitivity with EE - BB information
- Working towards extending the analysis to EB

Currently limited by data  $\rightarrow$  take this work as a demonstrator of the methodology's potential

If confirmed, the observed signal ...

- Could be attributed to an ultra-light axion field with masses around  $10^{-31} \text{ eV} \lesssim m_\phi \lesssim 10^{-28} \text{ eV}$
- Would rule out some simple Grand Unified Theory models [Agrawal+\[arXiv:2206.07053\]](#)
- Would be evidence of parity-violating physics outside the weak interaction



**Backup slides**

## Effect of birefringence on low- $\ell$ CMB spectra

$$C_{\ell}^{EE,o} \approx \cos^2(2\alpha + 2\beta_{reio})C_{\ell}^{EE,reio} + \cos^2(2\alpha + 2\beta_{dec})C_{\ell}^{EE,dec}$$

$$C_{\ell}^{EB,o} \approx \frac{1}{2} \sin(4\alpha + 4\beta_{reio})C_{\ell}^{EE,reio} + \frac{1}{2} \sin(4\alpha + 4\beta_{dec})C_{\ell}^{EE,dec}$$

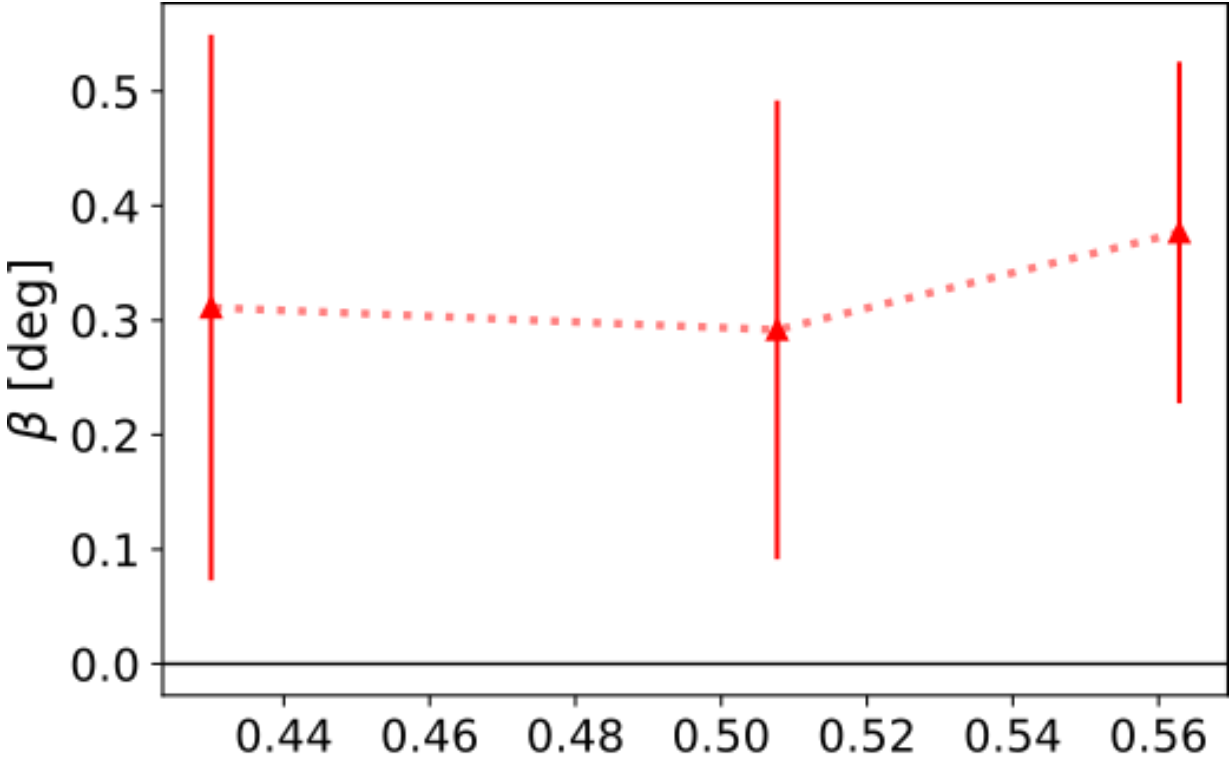
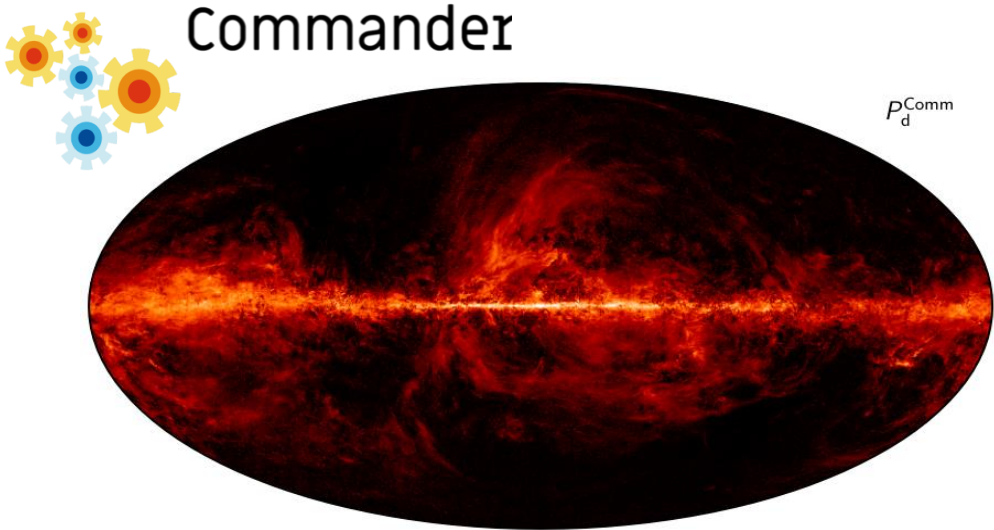
$$C_{\ell}^{BB,o} \approx \sin^2(2\alpha + 2\beta_{reio})C_{\ell}^{EE,reio} + \sin^2(2\alpha + 2\beta_{dec})C_{\ell}^{EE,dec} \\ + C_{\ell}^{BB,cmb}$$



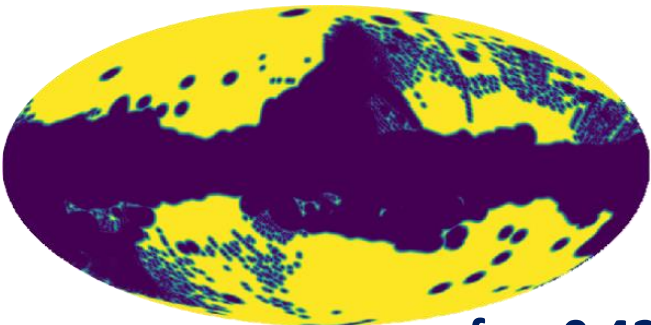
Commander as our sky model

Planck SRoll 2.0 data

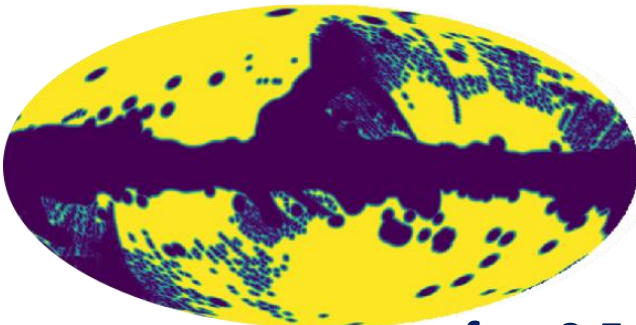
100, 143, 217, 353 GHz half-mission splits



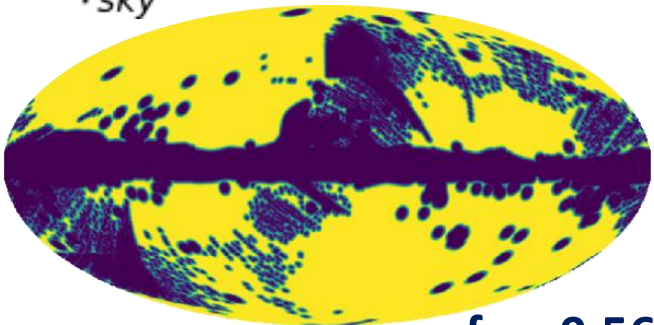
$$\frac{1}{f(\nu)} \left( \frac{\nu}{\nu_d} \right)^{\beta_d - 2} \frac{B(\nu, T_d)}{B(\nu_d, T_d)} \left( \frac{q^{\text{dust}}}{u^{\text{dust}}} \right)_p$$



$f_{\text{sky}}=0.43$



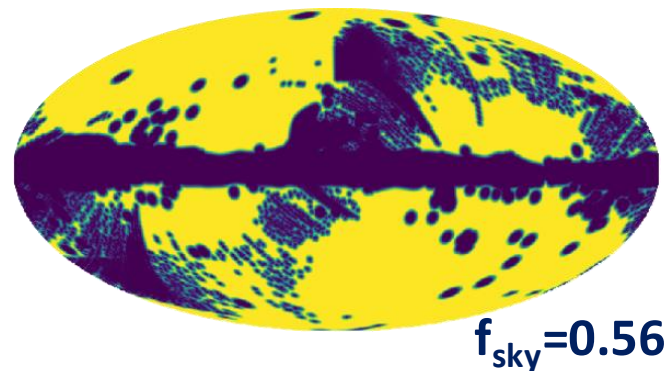
$f_{\text{sky}}=0.51$



$f_{\text{sky}}=0.56$

High- $\ell$ best fit [deg]	
$\beta_{\text{dec}}$	$0.38 \pm 0.15$
$\alpha_{100}$	$-0.38 \pm 0.16$
$\alpha_{143}$	$0.06 \pm 0.15$
$\alpha_{217}$	$0.01 \pm 0.14$
$\alpha_{353}$	$-0.15 \pm 0.13$

Planck SRoll 2.0 data  
100, 143, 217, 353 GHz half-mission splits  
Commander as our sky model



Gaussian prior for low- $\ell$  analysis

$$\begin{pmatrix} \sigma_{\beta}^2 & \rho_{\beta-100}\sigma_{\beta}\sigma_{100} & \rho_{\beta-143}\sigma_{\beta}\sigma_{143} \\ \rho_{\beta-100}\sigma_{\beta}\sigma_{100} & \sigma_{100}^2 & \rho_{100-143}\sigma_{100}\sigma_{143} \\ \rho_{\beta-143}\sigma_{\beta}\sigma_{143} & \rho_{100-143}\sigma_{100}\sigma_{143} & \sigma_{143}^2 \end{pmatrix} = \begin{pmatrix} (0.15^\circ)^2 & -0.9307 & -0.9595 \\ -0.9307 & (0.16^\circ)^2 & 0.8939 \\ -0.9595 & 0.8939 & (0.15^\circ)^2 \end{pmatrix}$$

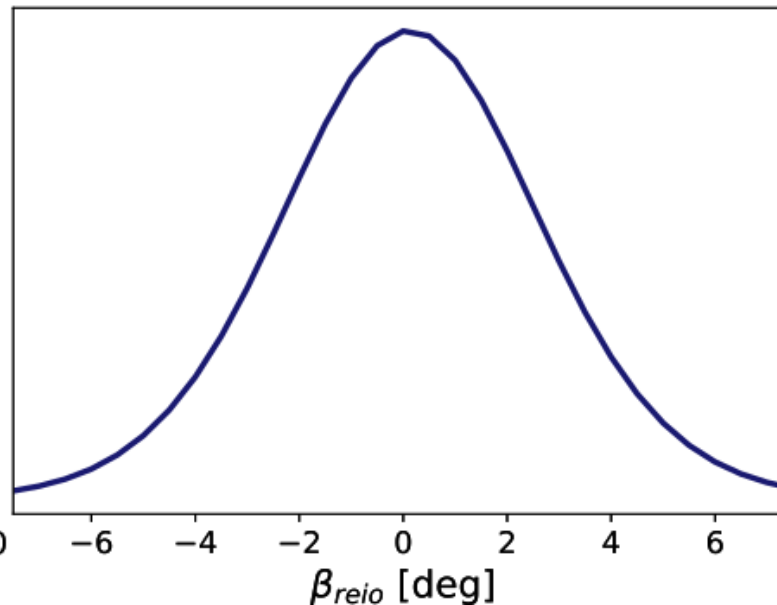
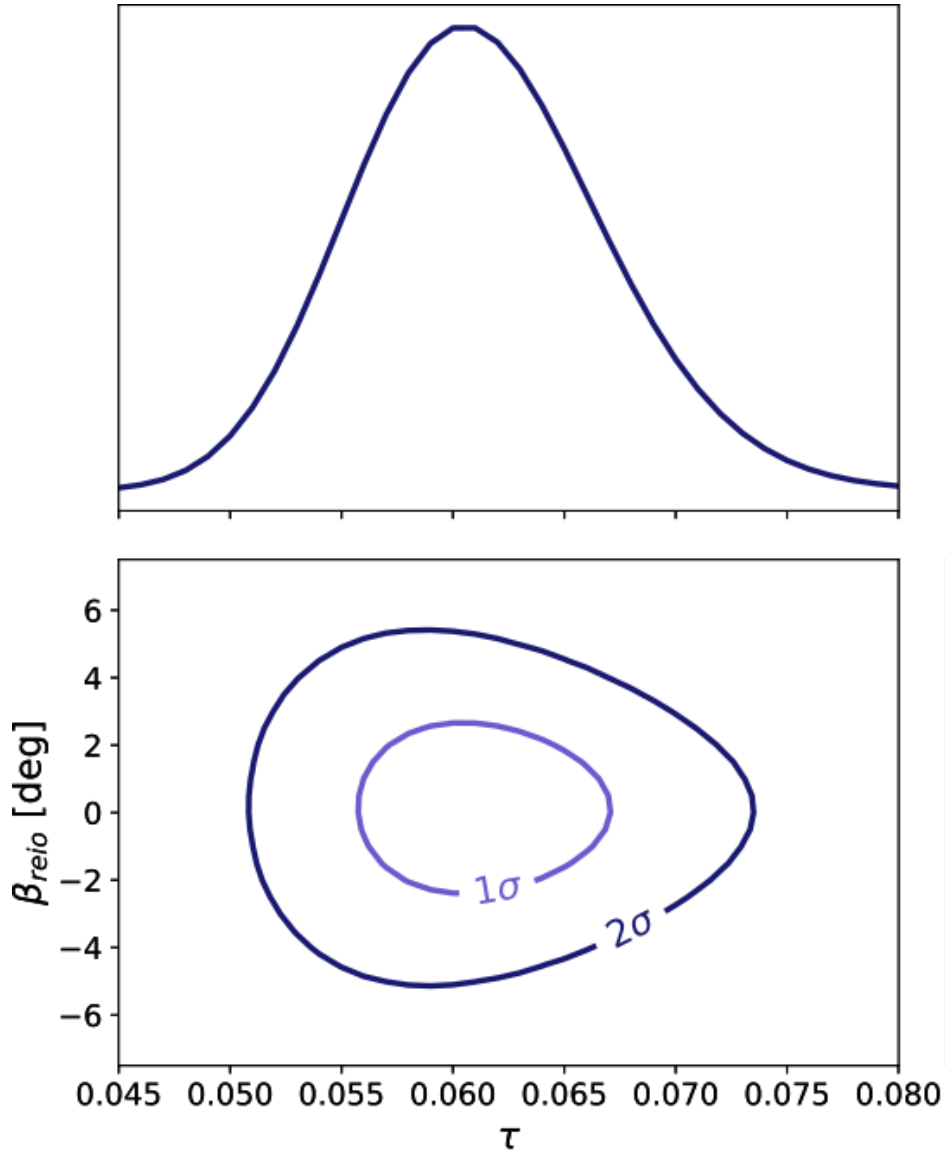
# EE – BB information

## Test on CMB + realistic noise simulations

Not affected by foreground residuals

Covariance matrix perfectly describes the data

Parameter	Input	Recovered
$\tau$	0.060	$0.061 \pm 0.006$
$\beta_{\text{reio}}$ [deg]	0.15	$0.12 \pm 2.56$



# Searching for ULA through their gravitational imprint

CMB Rogers+[arXiv:2301.08361]

kSZ Farren+[arXiv:2109.13268]

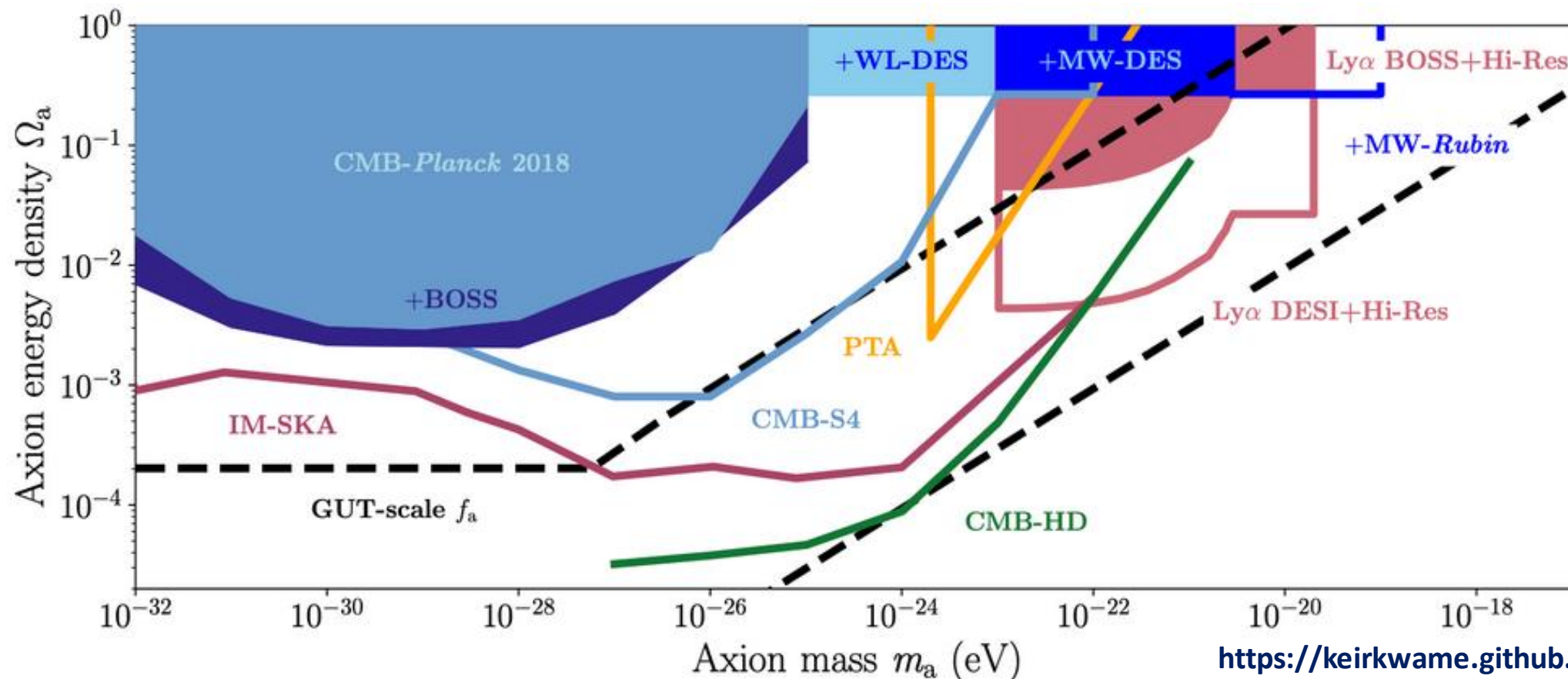
Galaxy clustering Laguë+[arXiv:2104.07802]

Galaxy weak lensing Dentler+[arXiv:2111.01199]

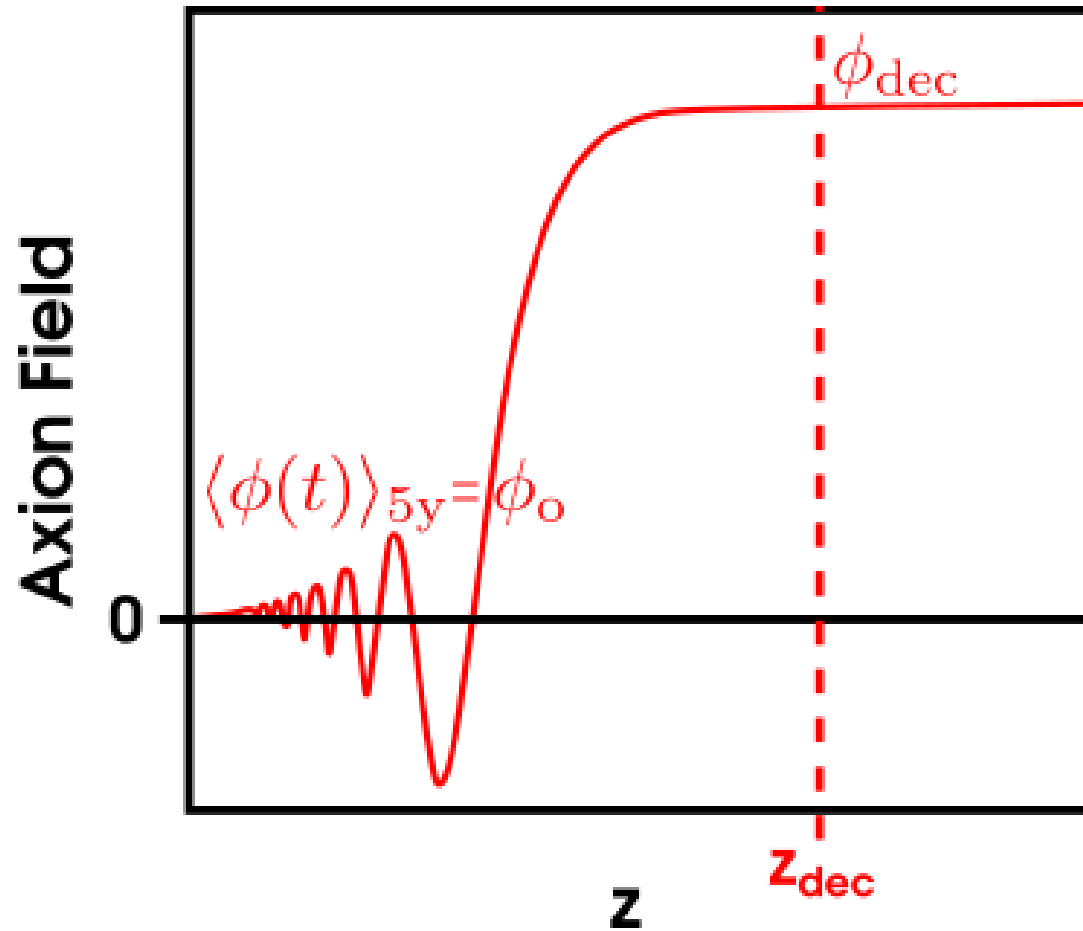
Lyman-alpha forest Rogers&Peiris[arXiv:2007.12705]

Dwarf galaxies Dalal&Kravtsov[arXiv:2203.05750]

21cm observations Flitter&Kovetz[arXiv:2207.05083]



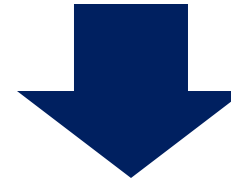
[https://keirkwame.github.io/DM\\_limits](https://keirkwame.github.io/DM_limits)



Suppose that ALP field is homogeneous and **varies with time**

$$m_\phi \leq H_{dec} \quad \text{For ALP to start oscillating after decoupling}$$

$$m_\phi \geq H_o \quad \text{For ALP to start oscillating before today}$$



$$10^{-33} \text{eV} \leq m_\phi \leq 10^{-28} \text{eV}$$

**Constant birefringence angle**, mainly sensitive to the ALP field value during decoupling

$$\beta = -\frac{1}{2}g_{\phi\gamma} \int \frac{\partial\phi}{\partial t} dt = -\frac{1}{2}g_{\phi\gamma}(\phi_o - \phi_{dec}) \approx \frac{1}{2}g_{\phi\gamma}\phi_{dec}$$

# Improved calibration strategies for upcoming data

## Artificial calibrators:

- Rotating polarised source  
BICEP3 recently achieved  $\approx 0.03^\circ$  precision [Cornelison+\[arXiv:2207.14796\]](#)  
**Exciting results coming soon!**
- Drone/satellite carrying a polarised source  
Expected to reach  $\approx 0.01^\circ$  [Nati+\[arXiv:1704.02704\]](#), [Casas-Reinares+\[DOI:10.3390/s21103361\]](#)

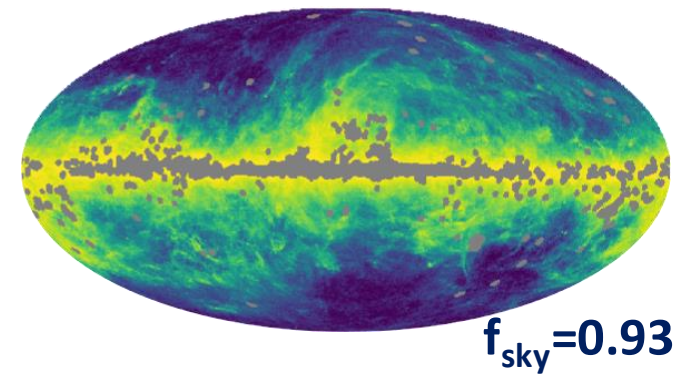
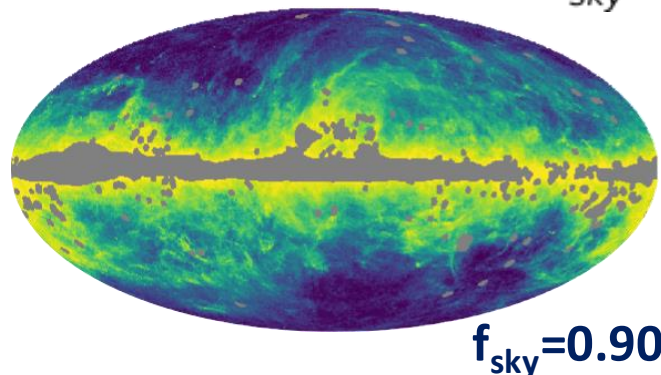
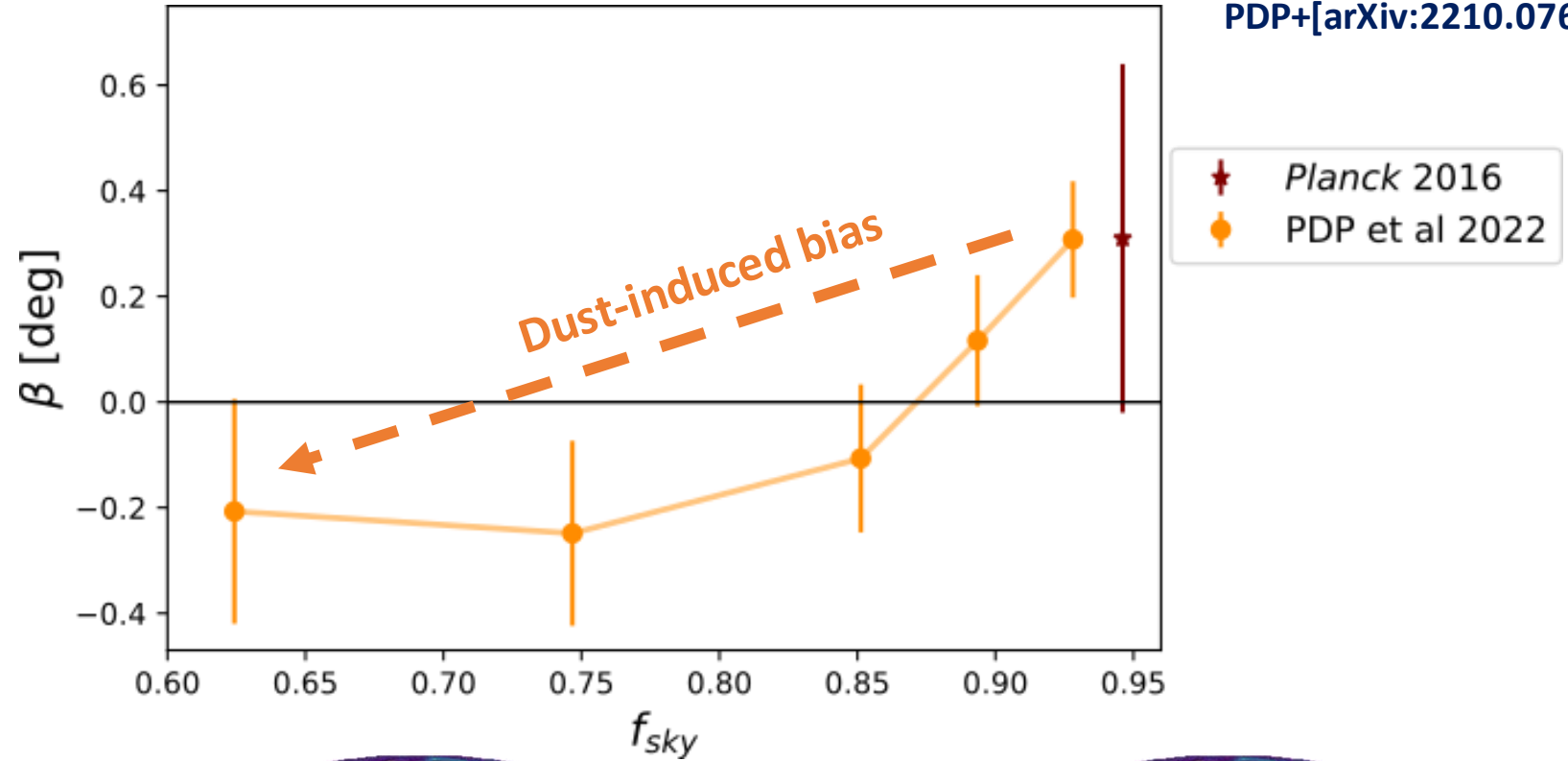
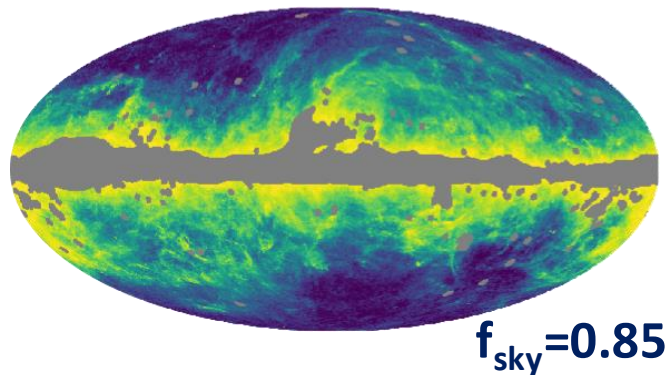
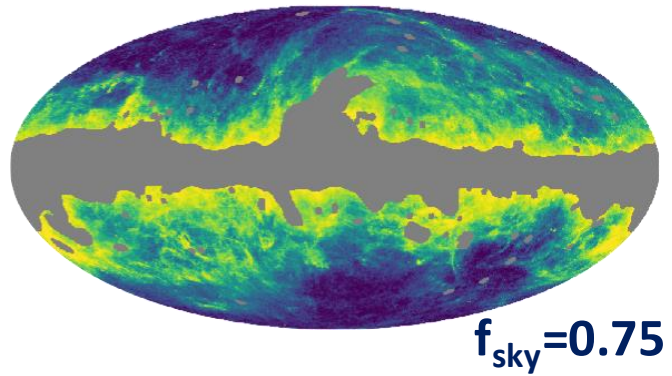
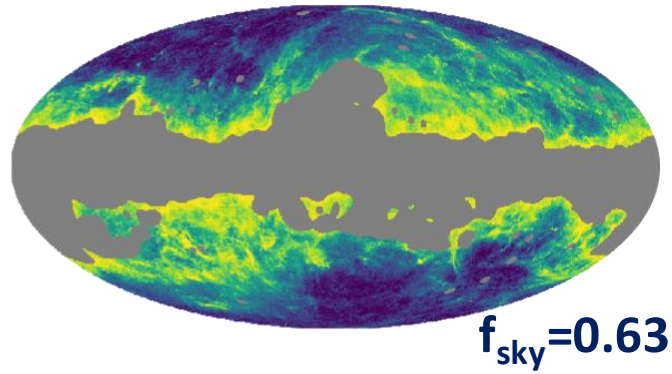
## Astrophysical calibrators:

- Crab Nebula  
Measured to  $0.33^\circ$  precision [Ritacco+\[arXiv:1804.09581\]](#), [Aumont+\[arXiv:1805.10475\]](#)
- **Galactic thermal dust emission** [Minami+\[arXiv:1904.12440\]](#), [Minami&Komatsu\[arXiv:2011.11254\]](#)



Using dust as a calibrator, birefringence measurements are...  
... robust against the miscalibration of polarisation angles and other systematics  
... **sensitive to dust EB**

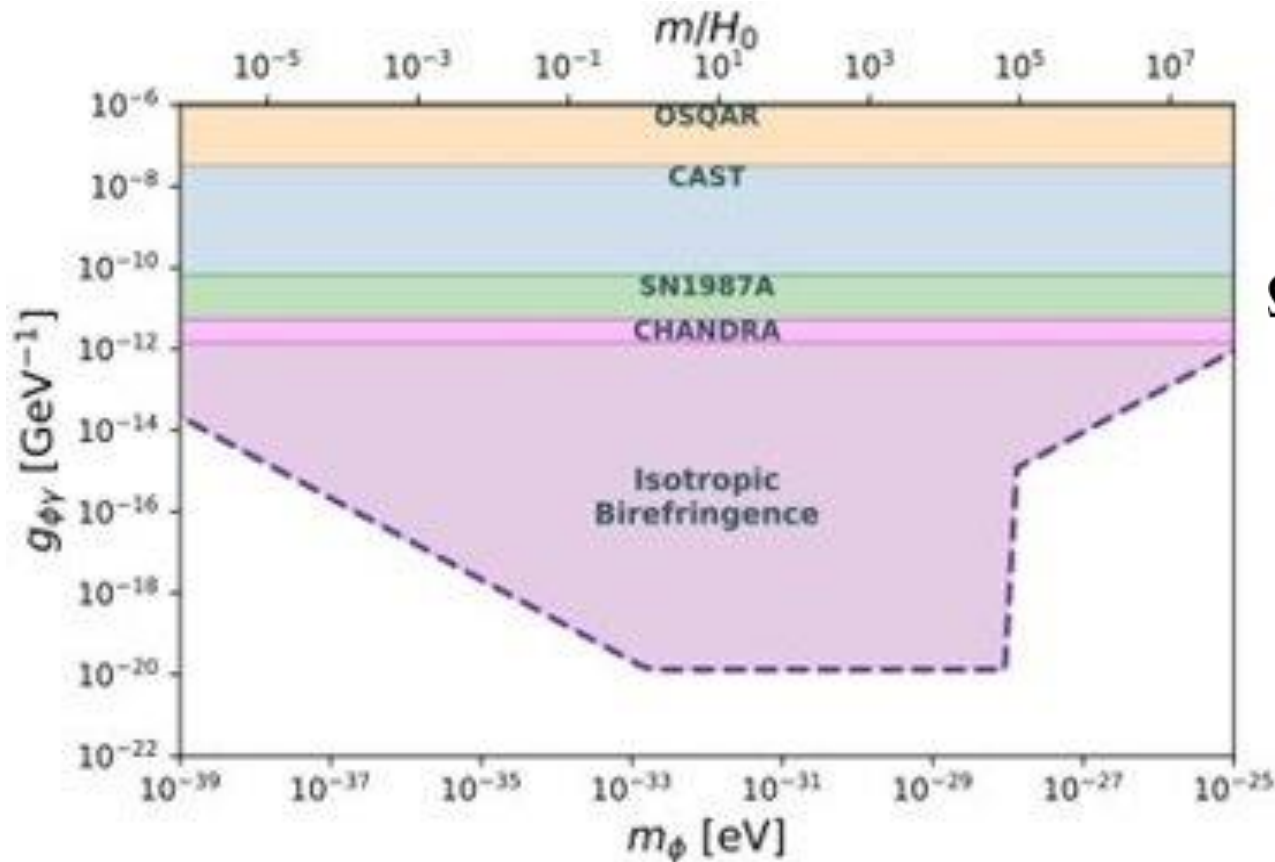
PDP+[arXiv:2201.07682]  
PDP+[arXiv:2210.07655]





# Constraining power of CMB observations alone was the $\beta \approx 0.3^\circ$ measurement confirmed

Fujita+[arXiv:2008.02473]

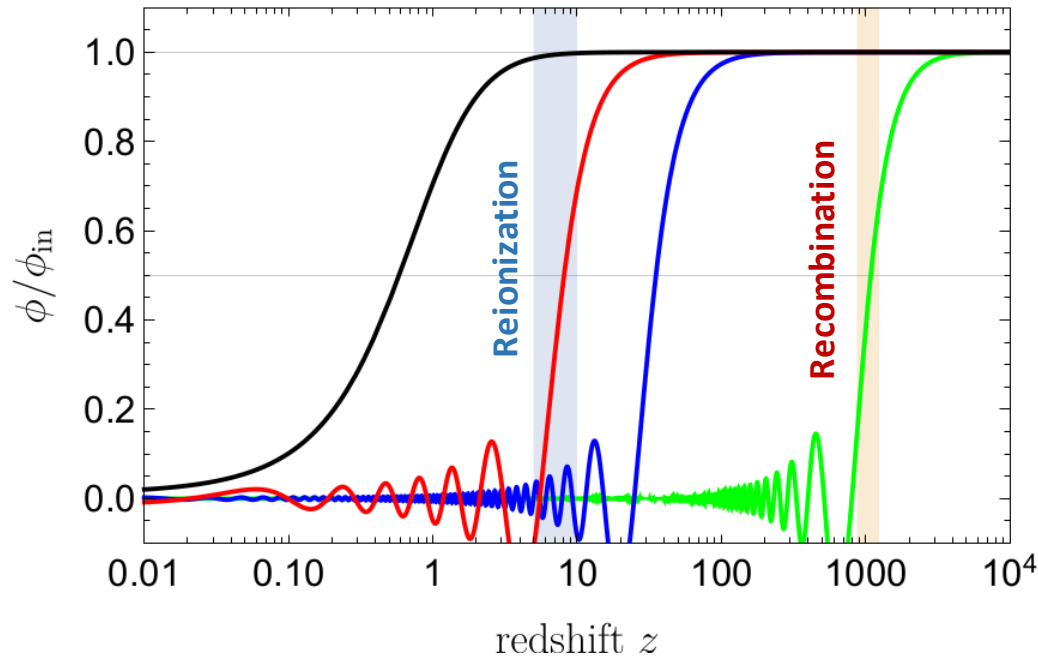


Assuming the **largest ALP abundance allowed**

$$\Omega_{\phi} \begin{cases} \Omega_{\Lambda} = 0.69 & m_{\phi} \leq 9.26 \times 10^{-34} \text{eV} \\ 0.006 h^{-2} & 10^{-32} \text{eV} \leq m_{\phi} \leq 10^{-25.5} \text{eV} \end{cases}$$

*Planck* Collab [arXiv:1807.06209]

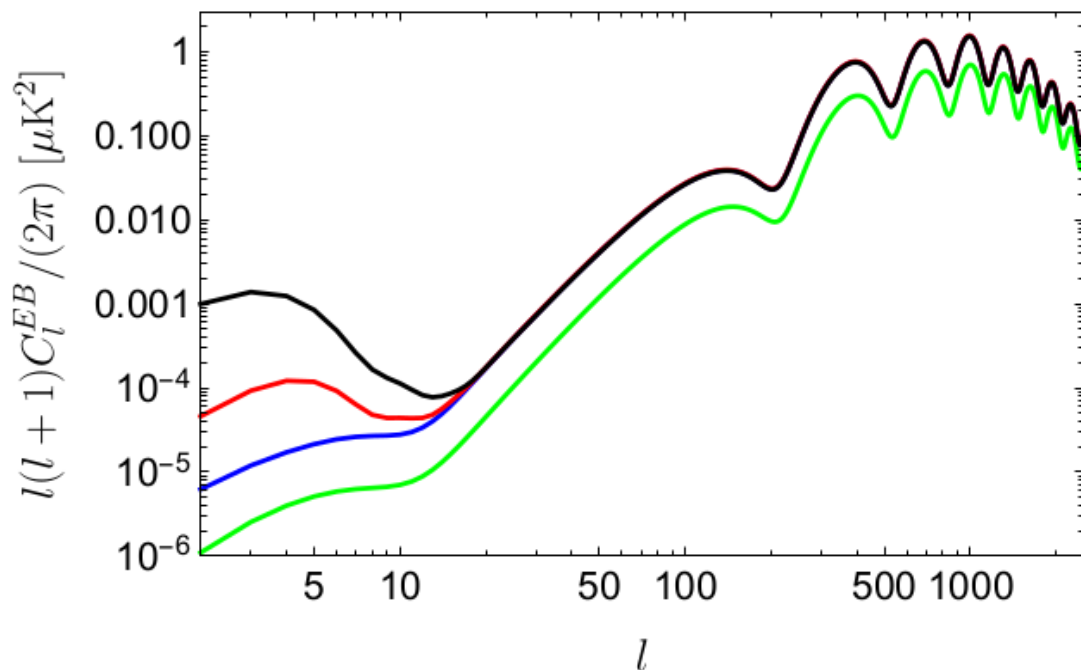
with ALP density only bounded from above, putting an upper constraint on the ALP-photon coupling is not possible



- $10^{-28.0}$  eV
- $10^{-30.3}$  eV
- $10^{-31.2}$  eV
- $10^{-32.3}$  eV

$$\beta(z) = \begin{cases} 0 & \text{for } z = 0 \\ \beta_{\text{rei}} & \text{for } 0 < z \leq 10, \\ \beta_{\text{rec}} & \text{for } 10 < z \end{cases}$$

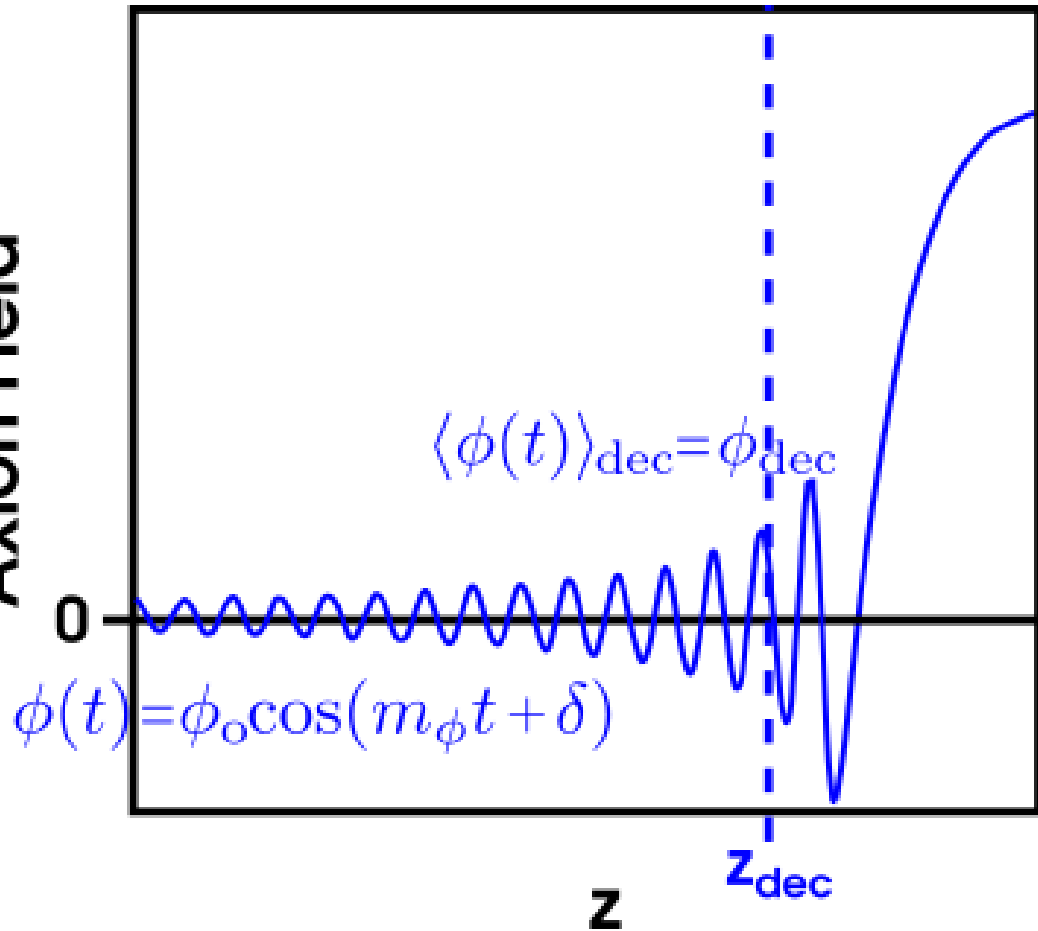
**CMB photons emitted at recombination and reionization will suffer different rotations**



$$\begin{aligned} C_\ell^{EB,o} \approx & \frac{1}{2} \sin(4\beta_{\text{rec}}) C_\ell^{E_{\text{rec}} E_{\text{rec}}} \\ & + \frac{1}{2} \sin(4\beta_{\text{rei}}) C_\ell^{E_{\text{rei}} E_{\text{rei}}} \\ & + \sin(2\beta_{\text{rec}} + 2\beta_{\text{rei}}) C_\ell^{E_{\text{rec}} E_{\text{rei}}} \end{aligned}$$

**The study of low-multipoles gives a tomographic view of the ALP field**

Axion Field



Suppose that ALP field is homogeneous and **varies with time**

$$m_\phi \geq H_{\text{dec}} \quad \text{For ALP to start oscillating before decoupling}$$

$$\Rightarrow 10^{-28} \text{eV} \leq m_\phi$$

(Q,U) rotating as if the polarisation angle oscillated with a period

$$T_\phi \sim 1y \left( \frac{10^{-22} \text{eV}}{m_\phi} \right)$$

*Planck, LiteBIRD*  $\sim 1y$   
*BICEP/Keck, SPT*  $\sim 1h$

$$10^{-24} \text{eV} \leq m_\phi \leq 10^{-19} \text{eV}$$

**Oscillation depending on ALP field at absorption**

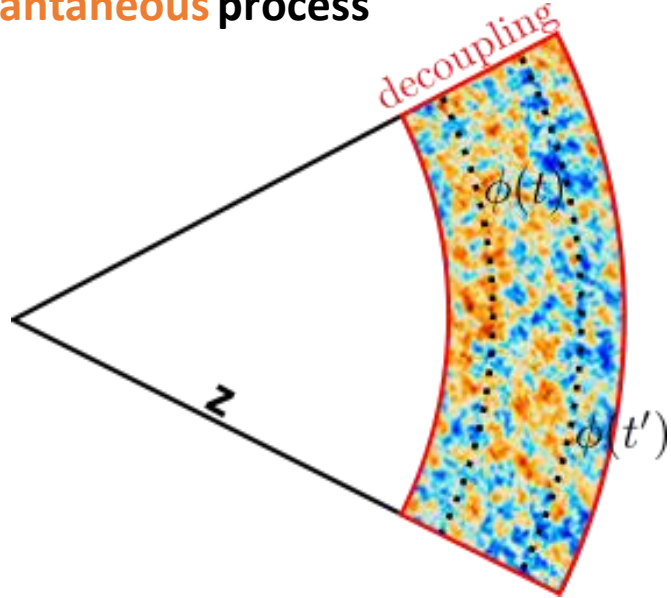
$$(Q \pm iU)(t, \vec{n}) = \underbrace{J_0[g_{\phi\gamma}\phi_{\text{dec}}]}_{\text{Washout depending on ALP field at emission}} \exp[\mp 2i(\overbrace{\frac{g_{\phi\gamma}}{2}\phi_o \cos(m_\phi t + \delta)})] (Q \pm iU)_0(\vec{n})$$

Washout depending on ALP field at emission

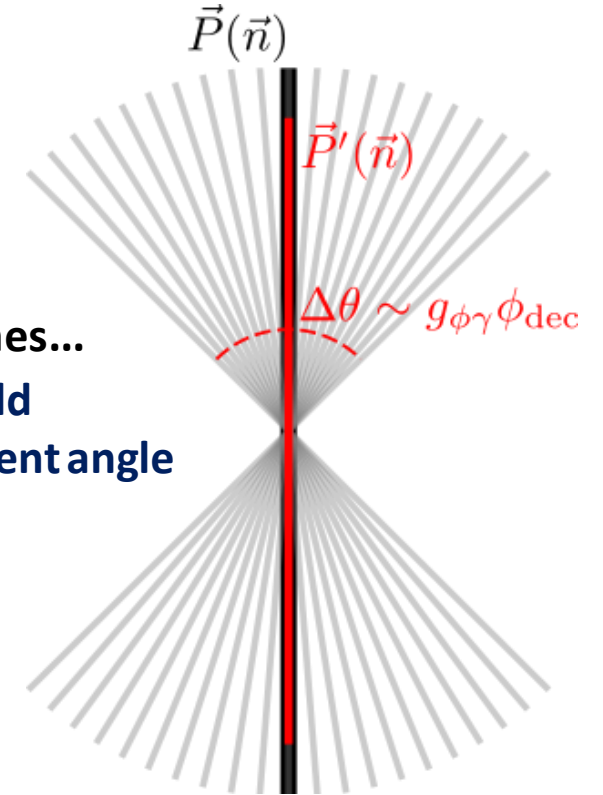
Fedderke+[arXiv:1903.02666]

Fedderke+[arXiv:1903.02666]

Washout is a consequence of **decoupling not being an instantaneous process**



Photons emitted at different times...  
... see a slightly **different ALP field**  
... are rotated by a slightly **different angle**



CMB detectors do an **incoherent sum** over the fanned-out states



**Reduction of polarization intensity**

$$J_0[g_{\phi\gamma}\phi_{\text{dec}}] \approx 1 - \frac{1}{4}(g_{\phi\gamma}\phi_{\text{dec}})^2$$

# Constraints from time-dependent birefringence

## Planck washout

Fedderke+[arXiv:1903.02666]

$$g_{\phi\gamma} \lesssim 9.6 \times 10^{-13} \text{ GeV}^{-1} \times \left( \frac{m_\phi}{10^{-21} \text{ eV}} \right) \times \left( \kappa \times \frac{\Omega_c^0 h^2}{0.11933} \right)^{-1/2}$$

## SPT-3G data

Ferguson+[arXiv:2203.16567]

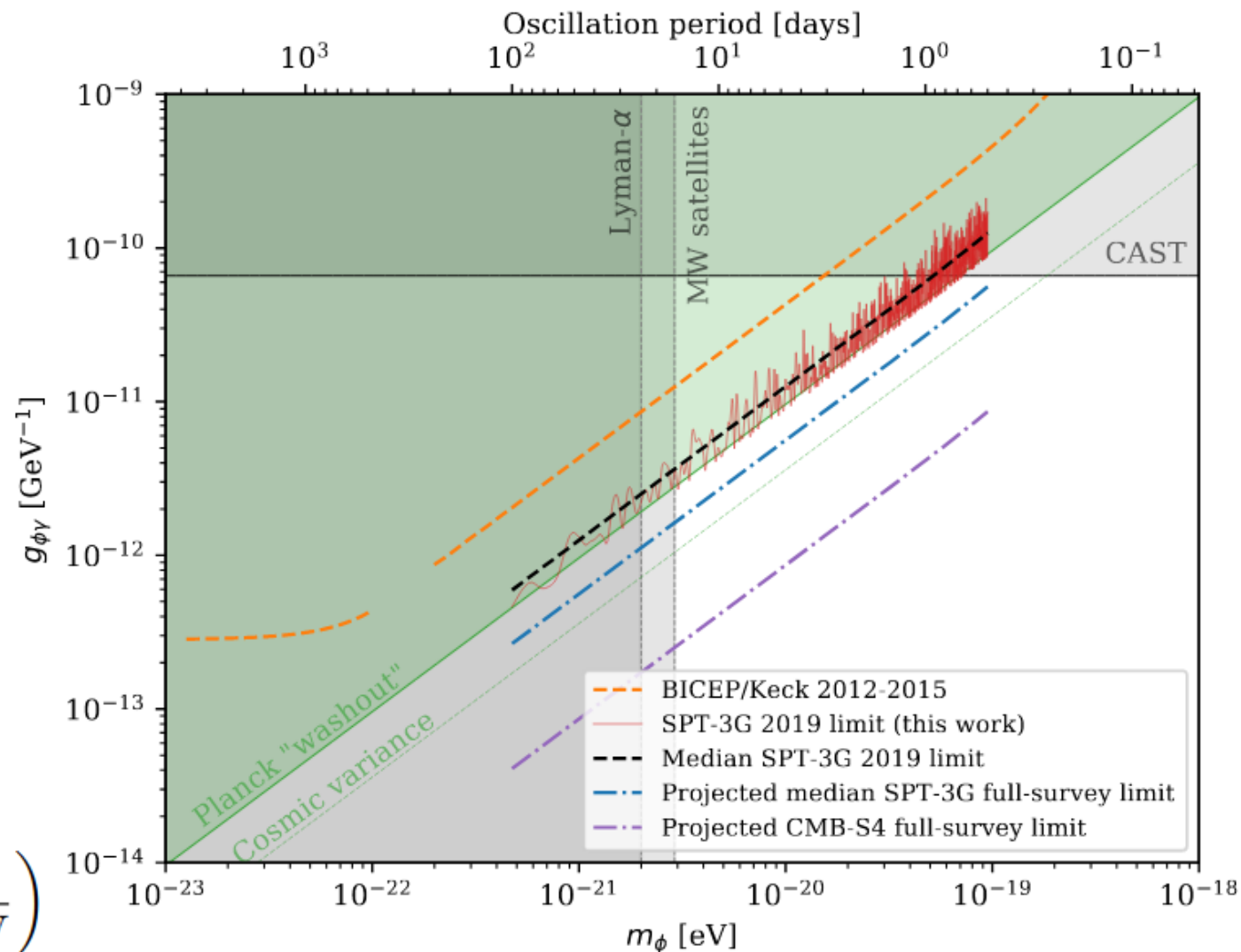
For periods  $1 \text{ day} \leq T_\phi \leq 100 \text{ days}$  ...

... probing  $10^{-22} \text{ eV} \leq m_\phi \leq 10^{-19} \text{ eV}$

... upper limit  $(\beta + \alpha)(t) \leq 0.071^\circ$

Assuming DM made of one ALP species with local density of  $0.3 \text{ GeV/cm}^3$

$$g_{\phi\gamma} < 1.18 \times 10^{-12} \text{ GeV}^{-1} \times \left( \frac{m_\phi}{1.0 \times 10^{-21} \text{ eV}} \right)$$



# Based on...

Minami et al 2019, PTEP, 083E02

Minami 2020, PTEP, 063E01

Minami & Komatsu 2020, PTEP, 103E02

Minami & Komatsu 2020, PRL, 125, 221301

PDP et al 2022, PRL, 128, 091302

Eskilt 2022, A&A, 662, A10

Eskilt & Komatsu 2022, PRD, 106, 063503

PDP et al 2022 [arXiv:2210.07655]

Accepted at JCAP

The original presentation of the methodology

Extension to **partial-sky** observations

Extension to **frequency cross-spectra**

Application to **Planck HFI PR3**

**Without** foreground modeling

Application to **Planck HFI PR4**

**With** foreground modeling

Application to **Planck LFI & HFI PR4**

Study of the **frequency dependence of** birefringence

Joint analysis of **Planck LFI & HFI PR4 and WMAP 9-year**

Alternative **semi-analytical** implementation

Simulation study and assessment of the **impact of systematics**

# Polarization primer

Cabella & Kamionkowski 2003 [arXiv:astro-ph/0403392]

Linearly polarized light propagating along the z direction

$$E_x = a_x \cos(\omega t - \delta_x) \quad E_y = a_y \cos(\omega t - \delta_y)$$

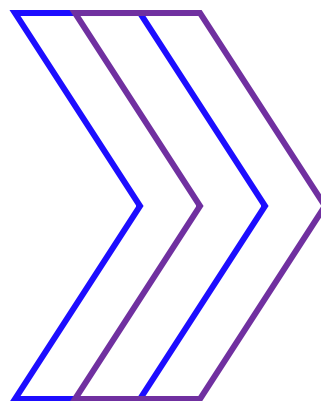
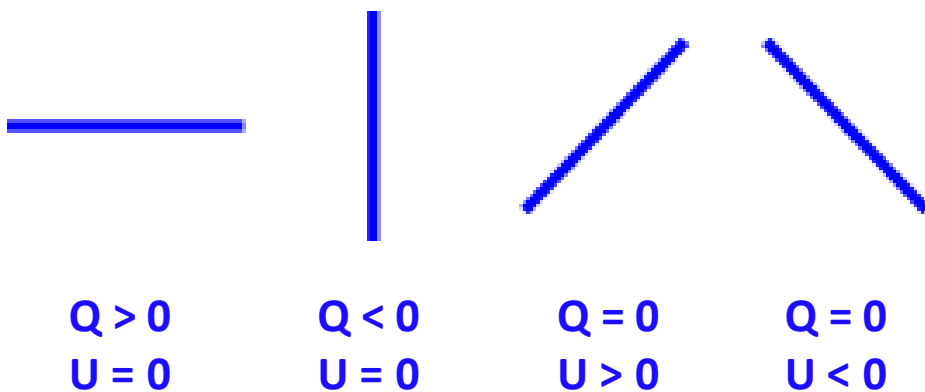
can be described through the Stoke's parameters

$$I = a_x^2 + a_y^2$$

$$Q = a_x^2 - a_y^2$$

$$U = 2a_x a_y \cos(\delta_x - \delta_y)$$

Relative to the chosen coordinate system



Helmholtz's theorem

Express vector fields as the sum of curl-free and divergence-free fields

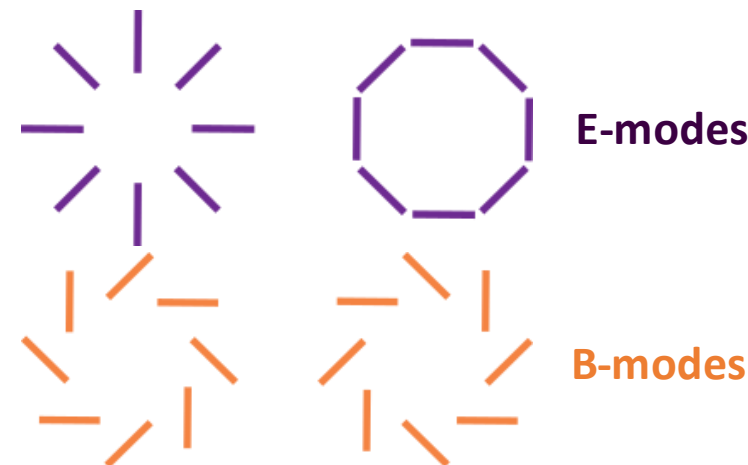
Q and U define a spin-2 field

$$P_{ab} = \frac{1}{2} \begin{pmatrix} Q(\vec{r}) & U(\vec{r}) \\ U(\vec{r}) & -Q(\vec{r}) \end{pmatrix}$$

Express the polarization field in terms of its gradient and curl components

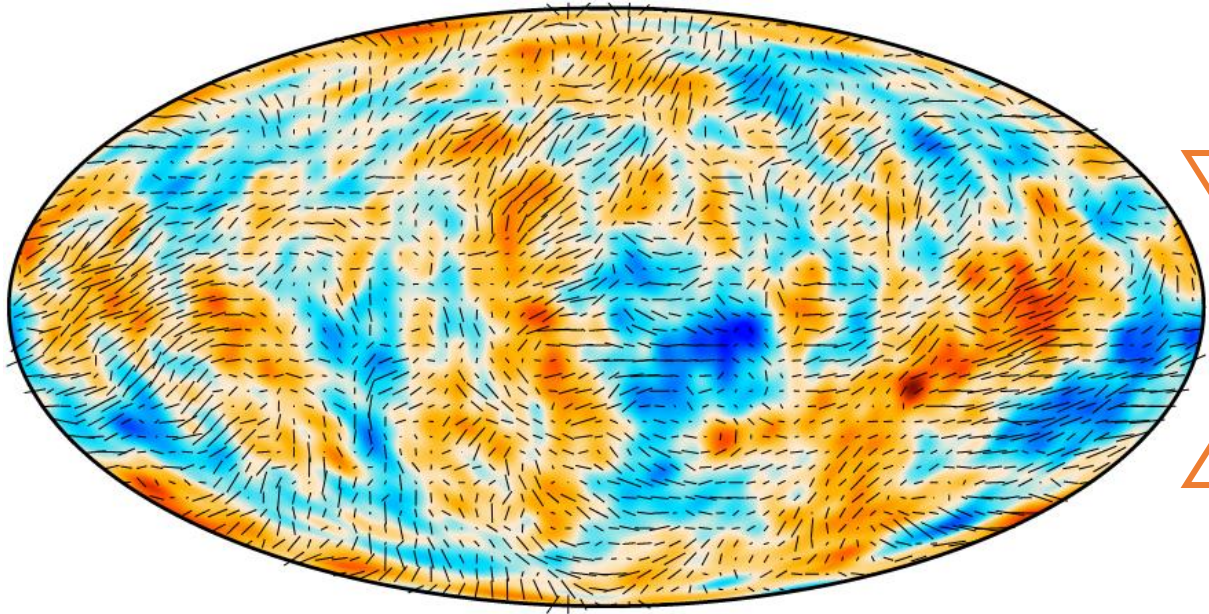
$$\nabla^2 E = \partial_a \partial_b P_{ab} \quad \nabla^2 B = \epsilon_{ac} \partial_b \partial_c P_{ab}$$

Locally independent





## Decompose CMB maps into spherical harmonics

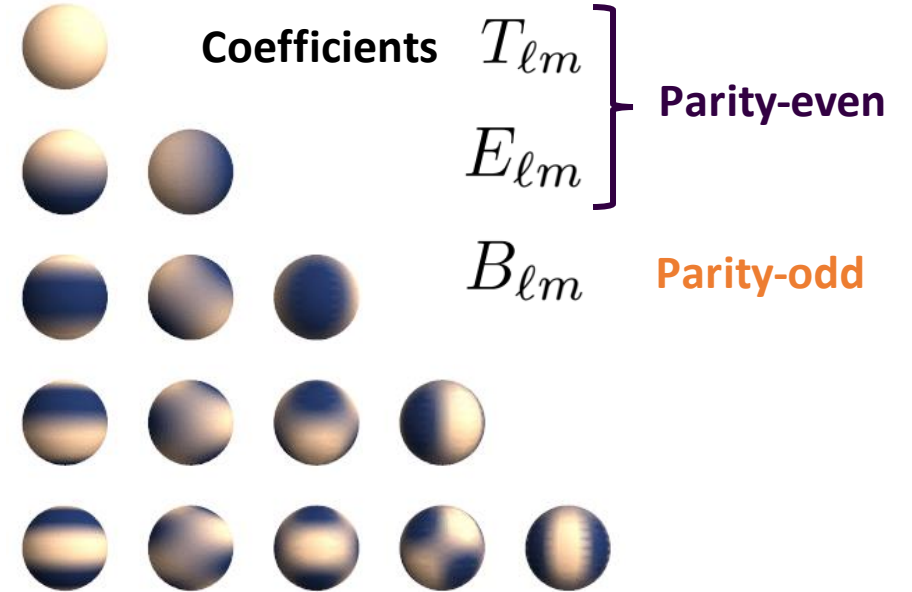


1 0.41  $\mu\text{K}$

-160

160  $\mu\text{K}$

Planck Collaboration I. 2020, A&A, 641, A1



Zaldarriaga & Seljak 1997, PRD, 55, 1830

Kamionkowski et al 1997, PRD, 55, 7368

## Analyzing CMB polarization in terms of spherical harmonics

$$\left. \begin{aligned} \langle E_{\ell m} E_{\ell' m'}^* \rangle &= \delta_{mm'} \delta_{\ell\ell'} C_{\ell}^{EE} \\ \langle B_{\ell m} B_{\ell' m'}^* \rangle &= \delta_{mm'} \delta_{\ell\ell'} C_{\ell}^{BB} \end{aligned} \right\} \text{Parity-even}$$

$$\langle E_{\ell m} B_{\ell' m'}^* \rangle = \delta_{mm'} \delta_{\ell\ell'} C_{\ell}^{EB} \quad \text{Parity-odd}$$

## $\Lambda\text{CDM}$

The Universe has no preferred direction so the statistics of CMB anisotropies must be invariant under parity transformation

EB $\neq$ 0 evidence of parity-violating physics

Lue et al 1999, PRL, 83, 1506

# Past measurements

early WMAP & BOOMERANG	$\alpha+\beta = -6.0^\circ \pm 4.0^\circ \text{ (stat)} \pm ?? \text{ (sys)}$	Feng et al 2006, PRL, 96, 221302
QUaD	$\alpha+\beta = 0.55^\circ \pm 0.82^\circ \text{ (stat)} \pm 0.5^\circ \text{ (sys)}$	Wu et al 2009, PRL, 102, 161302
WMAP 9-year	$\alpha+\beta = -0.36^\circ \pm 1.24^\circ \text{ (stat)} \pm 1.5^\circ \text{ (sys)}$	Hinshaw et al 2013, ApJS, 208, 19
Planck 2015	$\alpha+\beta = 0.31^\circ \pm 0.05^\circ \text{ (stat)} \pm 0.28^\circ \text{ (sys)}$	Planck Collaboration XLIX. 2016, A&A, 596, A110
POLARBEAR 2020	$\alpha+\beta = -0.61^\circ \pm 0.22^\circ \text{ (stat)} \pm ?? \text{ (sys)}$	Polarbear Collaboration 2020, ApJ, 897, 55
ACT 2020	$\alpha+\beta = -0.07^\circ \pm 0.09^\circ \text{ (stat)} \pm ?? \text{ (sys)}$	Choi et al 2020, JCAP, 12, 045
SPT 2020	$\alpha+\beta = 0.63^\circ \pm 0.04^\circ \text{ (stat)} \pm ?? \text{ (sys)}$	Bianchini et al 2020, PRD, 102, 083504

Systematic uncertainties dominate the analysis

Current calibration strategies set a  $\approx 0.5^\circ$ - $1^\circ$  limit

DM/DE could be a parity-violating pseudoscalar field  $\phi(-\vec{n}) = -\phi(\vec{n})$

Carroll et al 1990, PRD, 41, 1231

Carroll & Field 1991, PRD, 43, 3789

Harari & Sikivie 1992, PLB, 289, 67

Chern-Simons coupling to EM  $\frac{1}{4} g_{\phi\gamma} \phi F_{\mu\nu} \tilde{F}_{\mu\nu}$

Axion-like particles

Marsh 2016, Phys Rep, 643, 1

Early Dark Energy

Murai et al 2022 [arXiv:2209.07804]

rotation of the plane of linear  
polarization clockwise on the sky



$$\beta = -\frac{1}{2} g_{\phi\gamma} \int \frac{\partial \phi}{\partial t} dt$$

Faraday rotation from primordial magnetic fields

Subramanian 2016, Rep Prog Phys, 79, 076901

Superluminal Lorentz-violating electrodynamics  
emerging from a non-vanishing Weyl tensor

Shore 2005, Nucl Phys B, 717, 86118

Quantum gravity models that modify the  
dispersion relation of photons

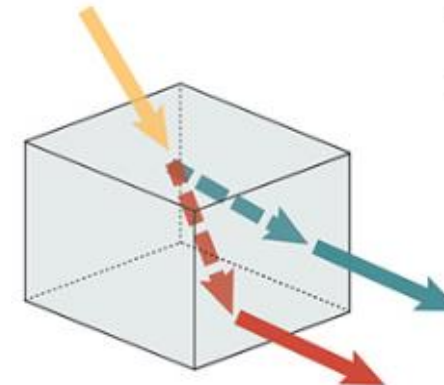
Gleiser & Kozameh 2001, PRD, 64, 8, 083007

$\beta(\nu)$

disfavored by data

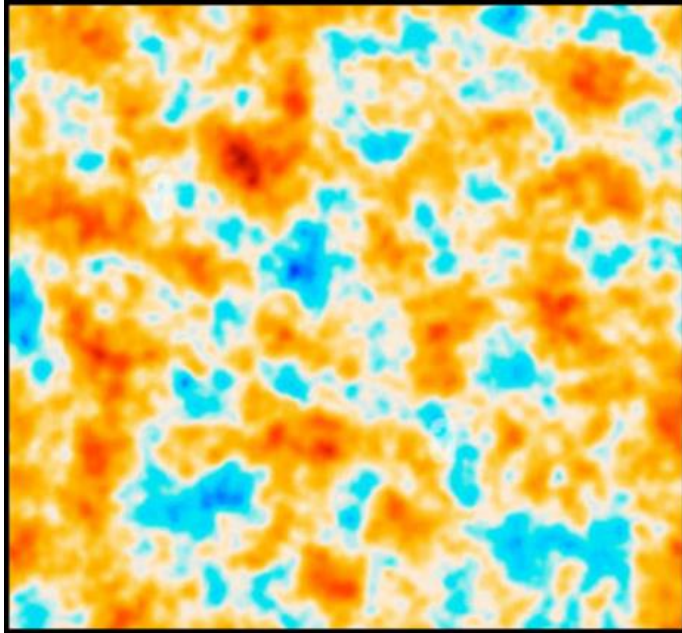
Eskilt 2022, A&A, 662, A10

## Cosmic birefringence



**BIREFRINGENCE** Birefringence describes the optical property where a ray of light is split by polarization into two rays taking slightly different paths.





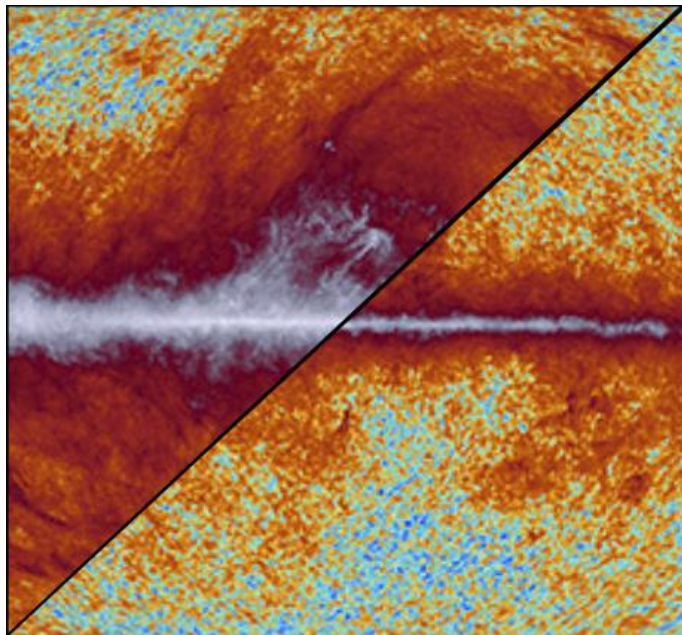
## Improve instrument calibration

- Provides **tighter constraints** and does **not directly depend on foregrounds** (subject to the foreground residuals)
- Optimal strategy for **ground-based experiments** as new calibration sources allow a precise measurement of polarization angles

**BICEP3**: rotating polarized source

**systematic error of  $<0.1^\circ$  with a  $\approx 0.03^\circ$  statistical uncertainty on the calibration of polarization angles**

Cornelison & Vergès Proc SPIE Int Soc Opt Eng 12190 (2022) 829



## Use Galactic foregrounds as calibrator

- (Currently) optimal strategy for **satellite missions** where calibration is limited by prior knowledge of astrophysical sources
- Proven to be **robust against instrumental systematics** but sensitive to dust EB

PDP et al 2022 [arXiv:2210.07655]

PDP et al 2022, PRL, 128, 091302

Tightest constraint to date coming from

**Planck PR4 + WMAP-9y  $\beta = 0.342^\circ \pm 0.093^\circ$**

Eskilt & Komatsu 2022, PRD, 106, 063503

**Observed signal is a rotation of the CMB and Galactic foreground emissions**

$$\begin{pmatrix} E_{\ell m}^o \\ B_{\ell m}^o \end{pmatrix} = \begin{pmatrix} \cos(2\alpha) & -\sin(2\alpha) \\ \sin(2\alpha) & \cos(2\alpha) \end{pmatrix} \begin{pmatrix} E_{\ell m}^{\text{fg}} \\ B_{\ell m}^{\text{fg}} \end{pmatrix} + \begin{pmatrix} \cos(2\alpha + 2\beta) & -\sin(2\alpha + 2\beta) \\ \sin(2\alpha + 2\beta) & \cos(2\alpha + 2\beta) \end{pmatrix} \begin{pmatrix} E_{\ell m}^{\text{cmb}} \\ B_{\ell m}^{\text{cmb}} \end{pmatrix}$$

**so the observed EB is**

$$C_{\ell}^{EB,o} = \frac{\tan(4\alpha)}{2} (C_{\ell}^{EE,o} - C_{\ell}^{BB,o}) + \frac{1}{\cos(4\alpha)} C_{\ell}^{EB,\text{fg}} + \frac{\sin(4\beta)}{2 \cos(4\alpha)} (C_{\ell}^{EE,\text{cmb}} - C_{\ell}^{BB,\text{cmb}})$$

*Planck* Collaboration XI. 2020, A&A, 641, A11  
 Martire et al 2022, JCAP, 04, 003

**Build a Gaussian likelihood to simultaneously determine both angles**

$$-2 \ln \mathcal{L} = \sum_{b=1}^{N_{\text{bins}}} (\mathbf{A} \bar{C}_b^o - \mathbf{B} \bar{C}_b^{\text{cmb}})^T \mathbf{M}_b^{-1} (\mathbf{A} \bar{C}_b^o - \mathbf{B} \bar{C}_b^{\text{cmb}}) + \sum_{b=1}^{N_{\text{bins}}} \ln |\mathbf{M}_b|$$

**Only two ingredients needed:**

**Cross-correlation of frequency bands of any CMB experiment**

$$\bar{C}_b^o = \begin{pmatrix} C_b^{E_i E_j, o} & C_b^{B_i B_j, o} & C_b^{E_i B_j, o} \end{pmatrix}^T$$

**Theoretical prediction for CMB angular power spectra**

# Planck PR4 (NPIPE reprocessing)

Planck Collaboration 2020, A&A, 643, A42

The NPIPE pipeline processes **raw, uncalibrated detector data** from **both LFI and HFI** into polarized frequency and detector-set maps. NPIPE fits and corrects for **gain fluctuations, ADCNL, bolometric transfer-function residuals and bandpass mismatch** by fitting time-domain templates while solving for the polarized map.

NPIPE achieves a smaller noise by:

- (1) including **data acquired during repointing maneuvers** between scans
- (2) better modeling the data via a **short baseline offset model for noise**, suppressing degree-scale noise residuals
- (3) **multi-frequency polarization model** used in calibration greatly reduces large-scale polarization uncertainty but introduces a pipeline transfer-function that suppresses CMB polarization power at  $\ell < 20$
- (4) **second-order analog-to-digital conversion nonlinearity (ADCNL) model**

The net effect on polarization is a **scale-dependent reduction in the total uncertainty**:

- (1)  $\sim 50$  % lower  $N_\ell$  at  $\ell \sim 10$
- (2) 20–30 % lower  $N_\ell$  at  $\ell \sim 100$
- (3) 10–20 % lower  $N_\ell$  at  $\ell \sim 1000$  (also in temperature)

# Planck PR4 (NPIPE reprocessing)

- Reprocessing of raw LFI and HFI *Planck* data
- Scale-dependent reduction of total uncertainty due to
  - Addition of data acquired during repointing maneuvers
  - Improved modeling of instrumental noise and systematics

*Planck* Collaboration 2020, A&A, 643, A42

- NPIPE 100, 143, 217, 353 GHz data
- Focus on small-scale information ( $\ell > 50$ ) to target the birefringence angle from recombination
- Cross-correlating A/B detector splits  $\rightarrow \beta, \alpha_i$  ( $i=1,\dots,8$ )
- Start by considering a null foreground EB

Consistent results across 4 independent pipelines

Pipeline	Implementation	Pseudo- $C_\ell$
JRE	Posterior distribution via MCMC	PolSpice
MT		Xpol
YM		NaMaster
PDP	Analytical minimization	

PDP et al 2022, PRL, 128, 091302

PDP et al 2022 [arXiv:2210.07655]

Minami & Komatsu 2020, PRL, 125, 221301

PDP et al 2022, PRL, 128, 091302

*Planck* 2018 (PR3)

*Planck* 2020 (PR4 or NPIPE)

100, 143, 217, 353 GHz data

100, 143, 217, 353 GHz data

Half-mission splits  $\rightarrow \beta, \alpha_i$  ( $i=1,\dots,4$ )

A/B detector splits  $\rightarrow \beta, \alpha_i$  ( $i=1,\dots,8$ )

High- $\ell$  data  $\rightarrow$  bin  $C_\ell/M_\ell$  from  $\ell_{\min}=51$  to  $\ell_{\max}=1490$  with  $\Delta\ell = 20$  spacing

High- $\ell$  data  $\rightarrow$  bin  $C_\ell/M_\ell$  from  $\ell_{\min}=51$  to  $\ell_{\max}=1490$  with  $\Delta\ell = 20$  spacing

Specific mask for each band

Common mask for all bands

Neglecting foreground EB

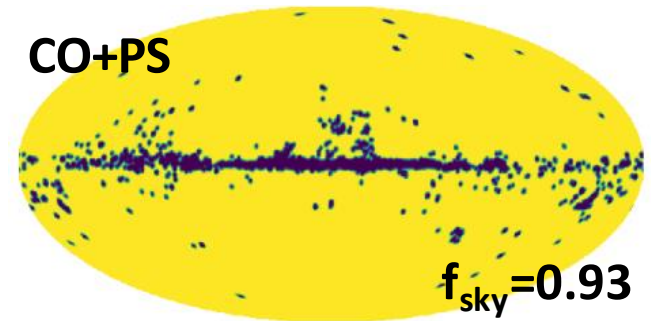
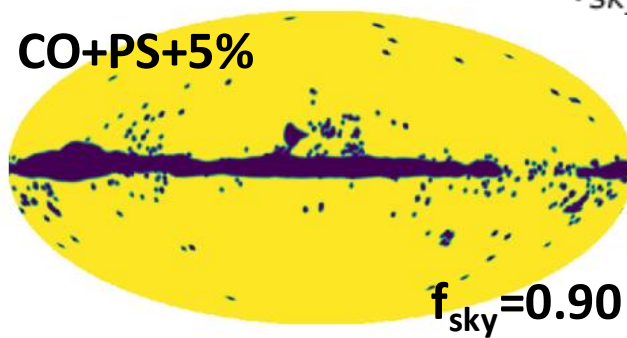
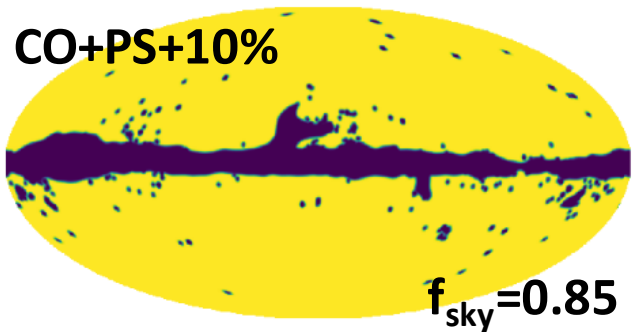
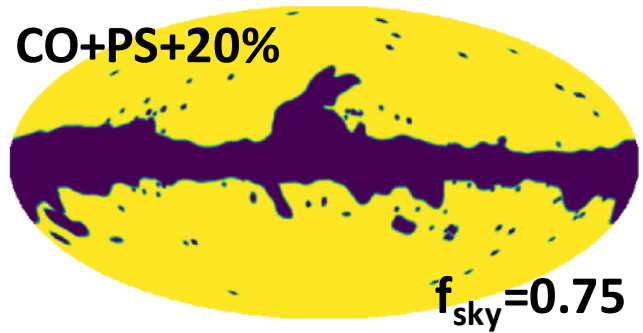
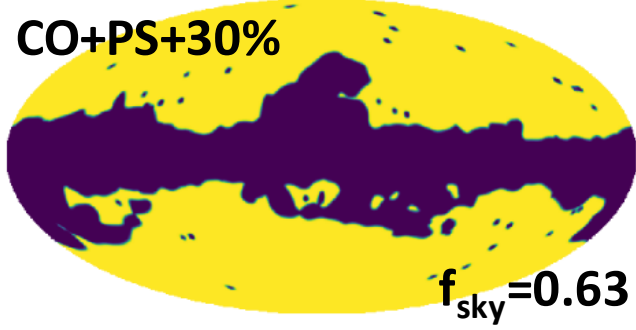
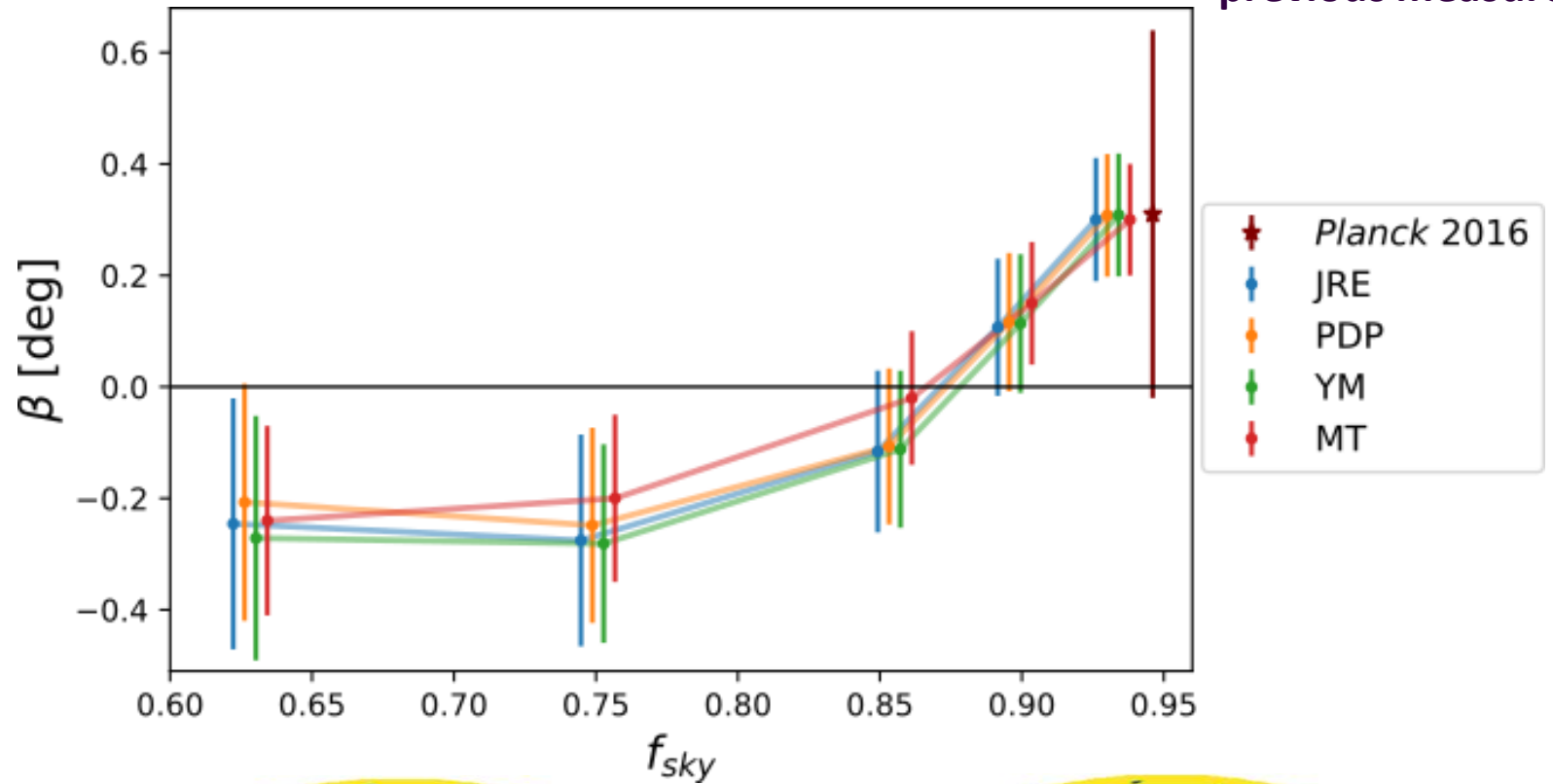
Correcting for foreground EB

$\beta = 0.35^\circ \pm 0.14^\circ$  ( $2.4\sigma$ )  
for nearly full-sky

$\beta = 0.30^\circ \pm 0.11^\circ$  ( $2.7\sigma$ )  
for nearly full-sky



For nearly full-sky:  $\beta = 0.30^\circ \pm 0.11^\circ$  ( $2.7\sigma$ )  $\rightarrow$  Consistent with and more precise than previous measurements!



... but our inferred value of  $\alpha$  depends on Galactic dust

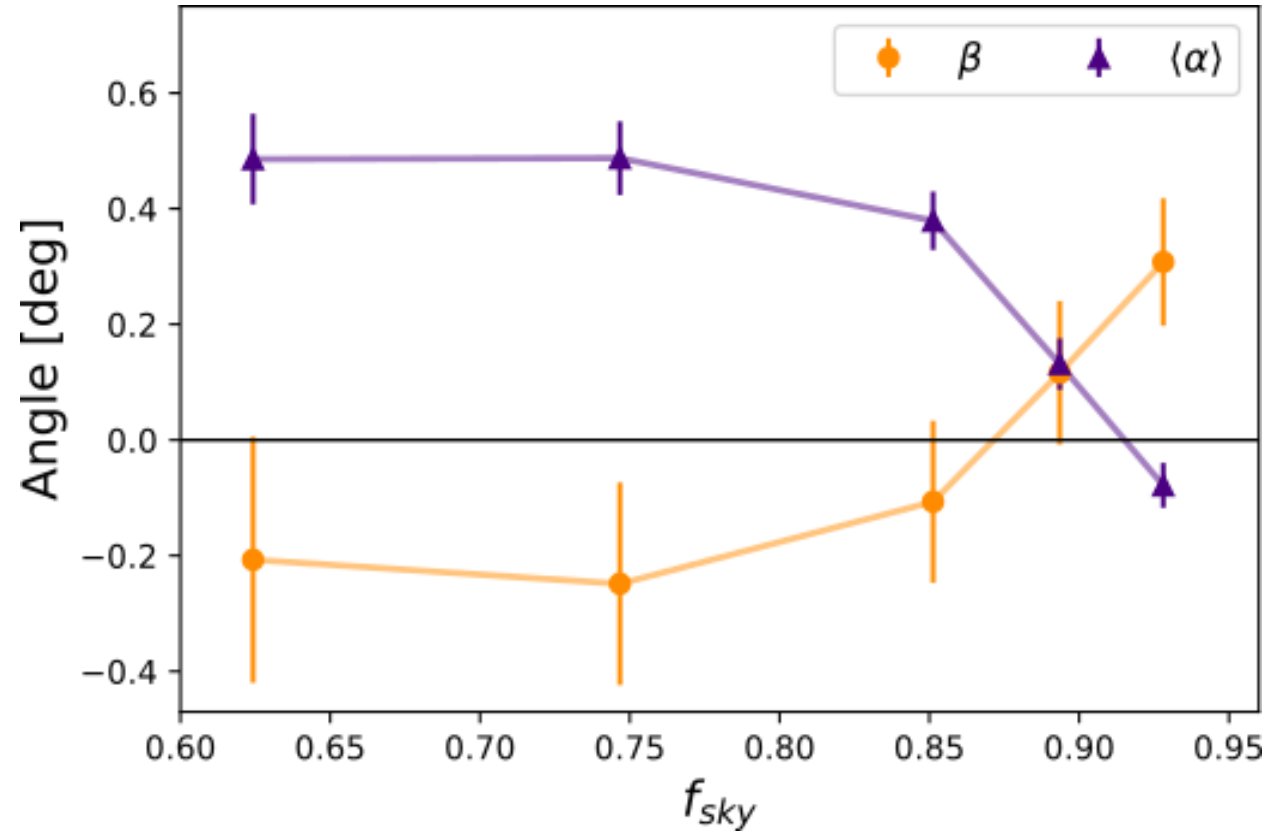
Dust EB biases our estimation of miscalibration angles, dragging with them the measurement of  $\beta$

Misalignment of dust filaments and Galactic magnetic fields produces TB and EB

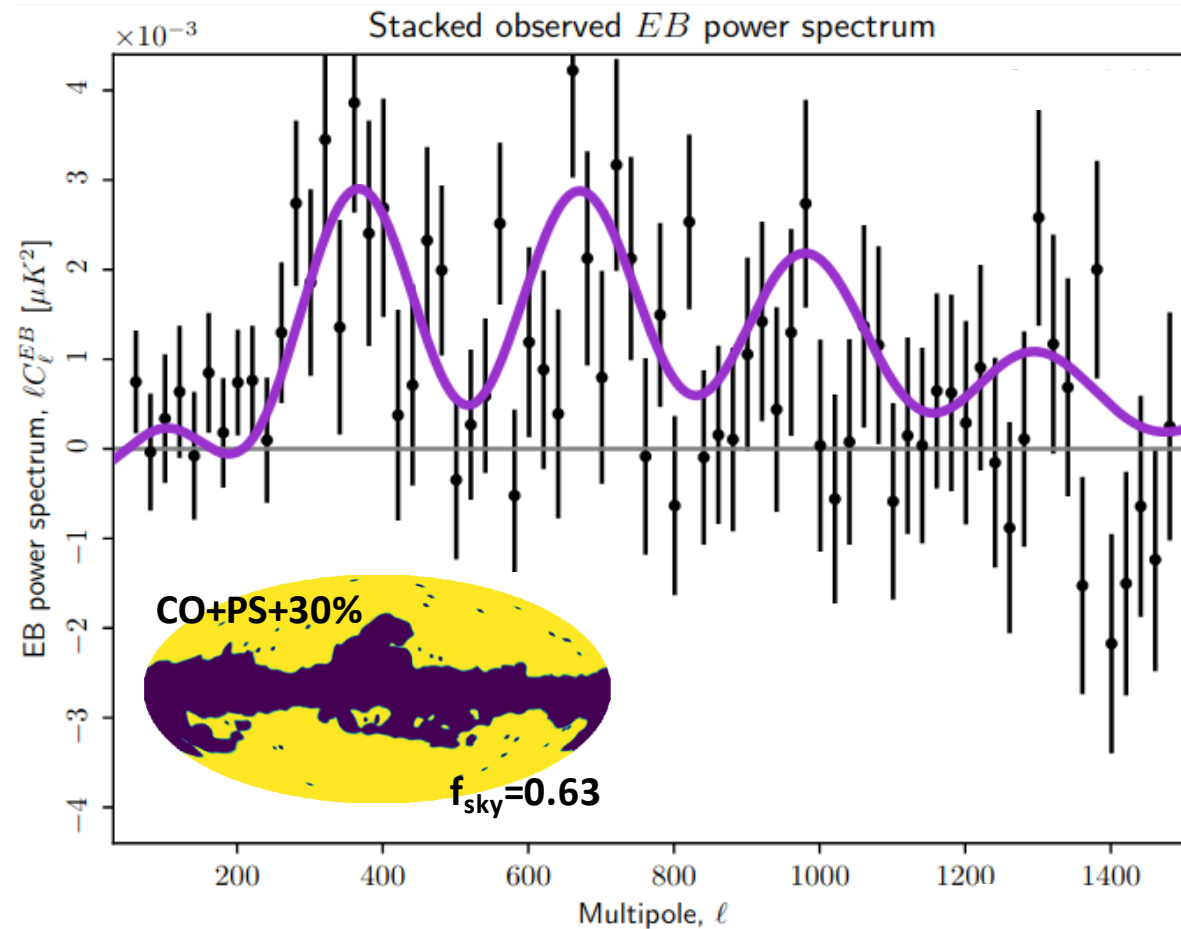
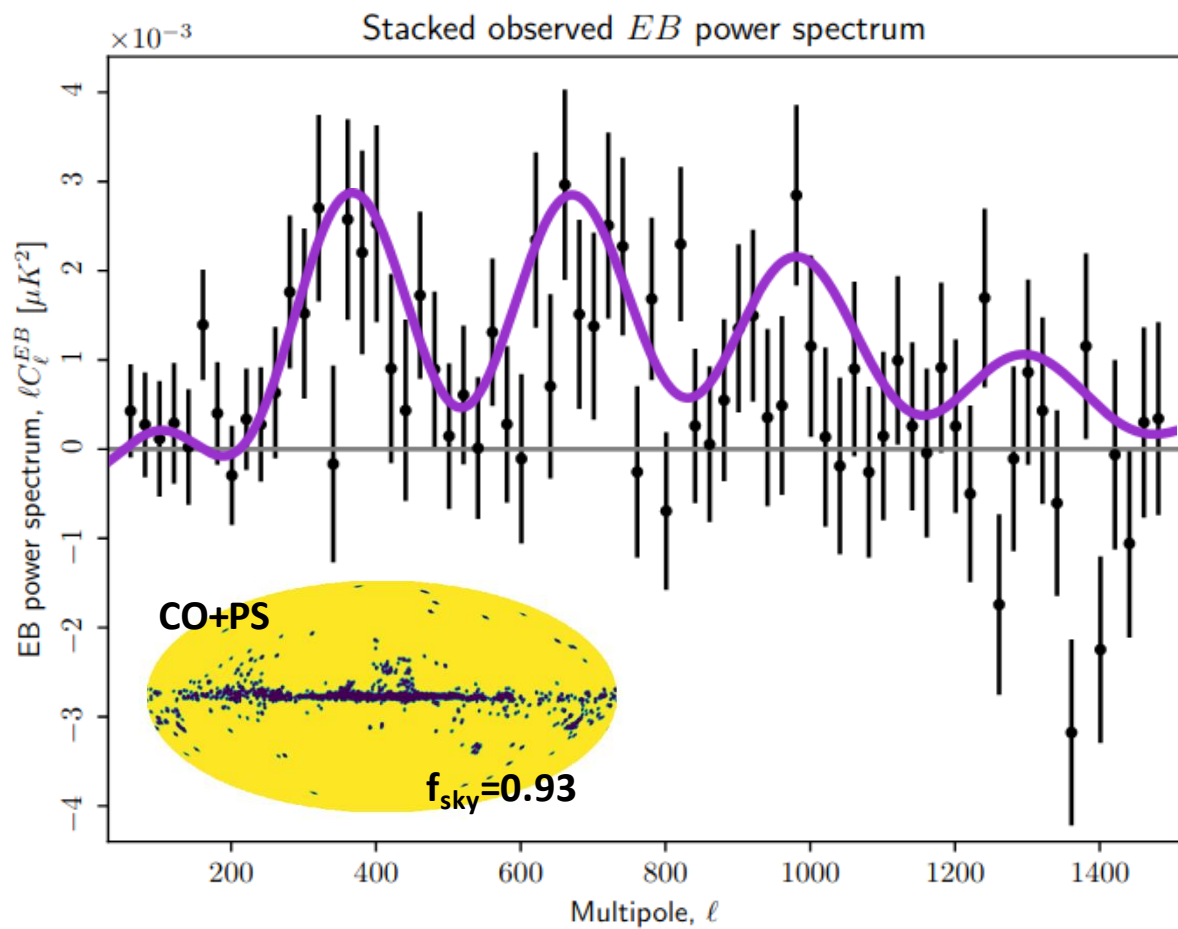
Clark et al 2021, ApJ, 919, 53

- Dust **TB** > 0 detected by *Planck*  
*Planck* Collaboration XI. 2020, A&A, 641, A11
- Expected dust **EB** > 0

Indirect detection of dust EB



The EB signal created by birefringence exists regardless of the Galactic mask ...



... but our inferred value of  $\alpha$  depends on Galactic dust

Observed foreground signal can be rewritten as

$$C_{\ell}^{EB,fg,o} = \frac{1}{2} \sin(4\alpha) \left( C_{\ell}^{EE,fg} - C_{\ell}^{BB,fg} \right) + \cos(4\alpha) C_{\ell}^{EB,fg}$$

$$= \frac{1}{2} \sqrt{4 \left( C_{\ell}^{EB,fg} \right)^2 + \left( C_{\ell}^{EE,fg} - C_{\ell}^{BB,fg} \right)^2} \sin(4\alpha + 4\gamma_{\ell})$$

Within the small angle approximation

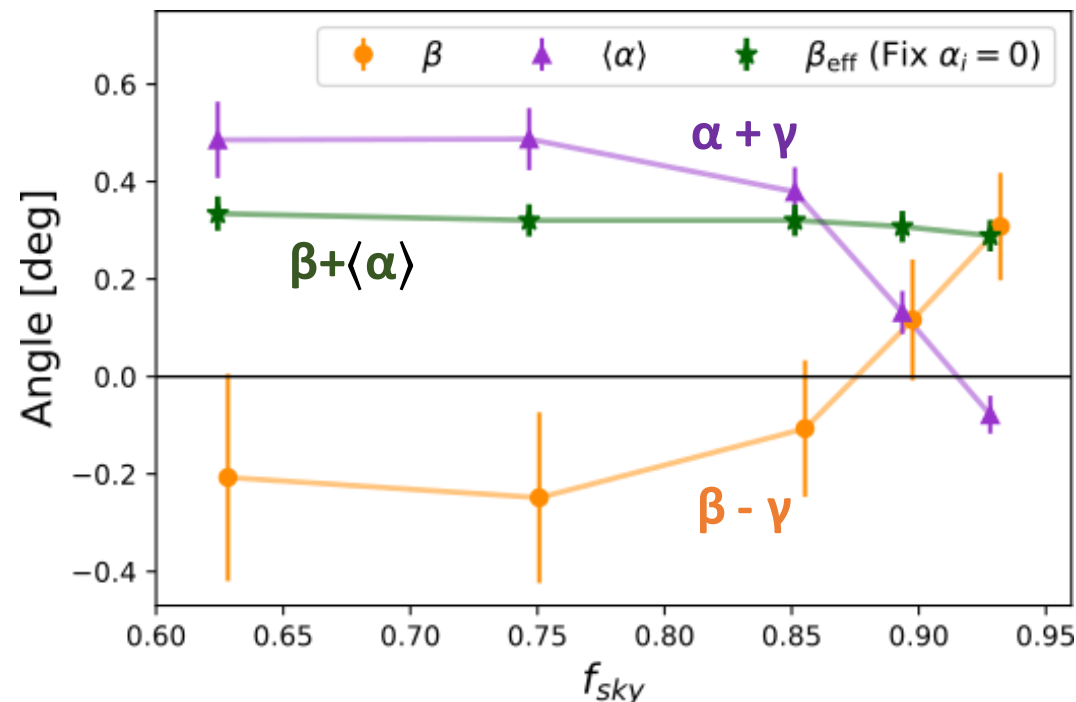
$$\gamma_{\ell} \approx \frac{C_{\ell}^{EB,fg}}{C_{\ell}^{EE,fg} - C_{\ell}^{BB,fg}}$$

If  $C_{\ell}^{EB,fg} \propto C_{\ell}^{EE,fg} - C_{\ell}^{BB,fg}$

then  $\gamma_{\ell} = \gamma \rightarrow$  degenerate with  $\alpha$

measure  $\alpha + \gamma$  and  $\beta - \gamma$

does not affect  $\alpha + \beta \rightarrow$  By fixing  $\alpha_i=0$  we effectively measure  $\beta + \langle \alpha \rangle$



Planck Collaboration XI. 2020, A&A, 641, A11

Planck reported dust TB > 0  $\rightarrow$  Plausible dust EB > 0  $\rightarrow$  Expect  $\uparrow \alpha$  and  $\downarrow \beta$

Observed foreground signal can be rewritten as

$$C_{\ell}^{EB,fg,o} = \frac{1}{2} \sqrt{4 \left( C_{\ell}^{EB,fg} \right)^2 + \left( C_{\ell}^{EE,fg} - C_{\ell}^{BB,fg} \right)^2} \sin(4\alpha + 4\gamma_{\ell})$$

Within the small angle approximation  $\gamma_{\ell} \approx \frac{C_{\ell}^{EB,fg}}{C_{\ell}^{EE,fg} - C_{\ell}^{BB,fg}}$

If  $C_{\ell}^{EB,fg} \propto C_{\ell}^{EE,fg} - C_{\ell}^{BB,fg}$  then  $\gamma_{\ell} = \gamma \rightarrow$  degenerate with  $\alpha$   $\left\{ \begin{array}{l} \text{measure } \alpha + \gamma \text{ and } \beta - \gamma \\ \text{does not affect } \alpha + \beta \end{array} \right.$

## Synchrotron

Synch EB statistically compatible with null

Martire et al 2022, JCAP, 04, 003

No physical process known to produce synch EB

## Dust

Misalignment between dust filaments and Galactic magnetic fields creates TB and EB correlations

Clark et al 2021, ApJ, 919, 53

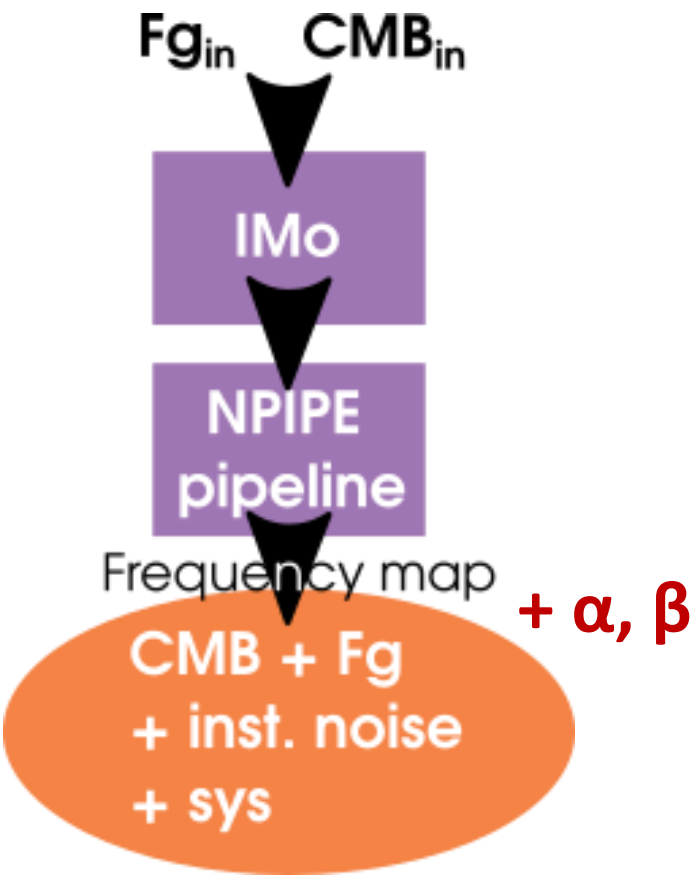
Planck reported :

- Dust TB > 0
- A hint of dust EB > 0 (still statistically compatible with null)

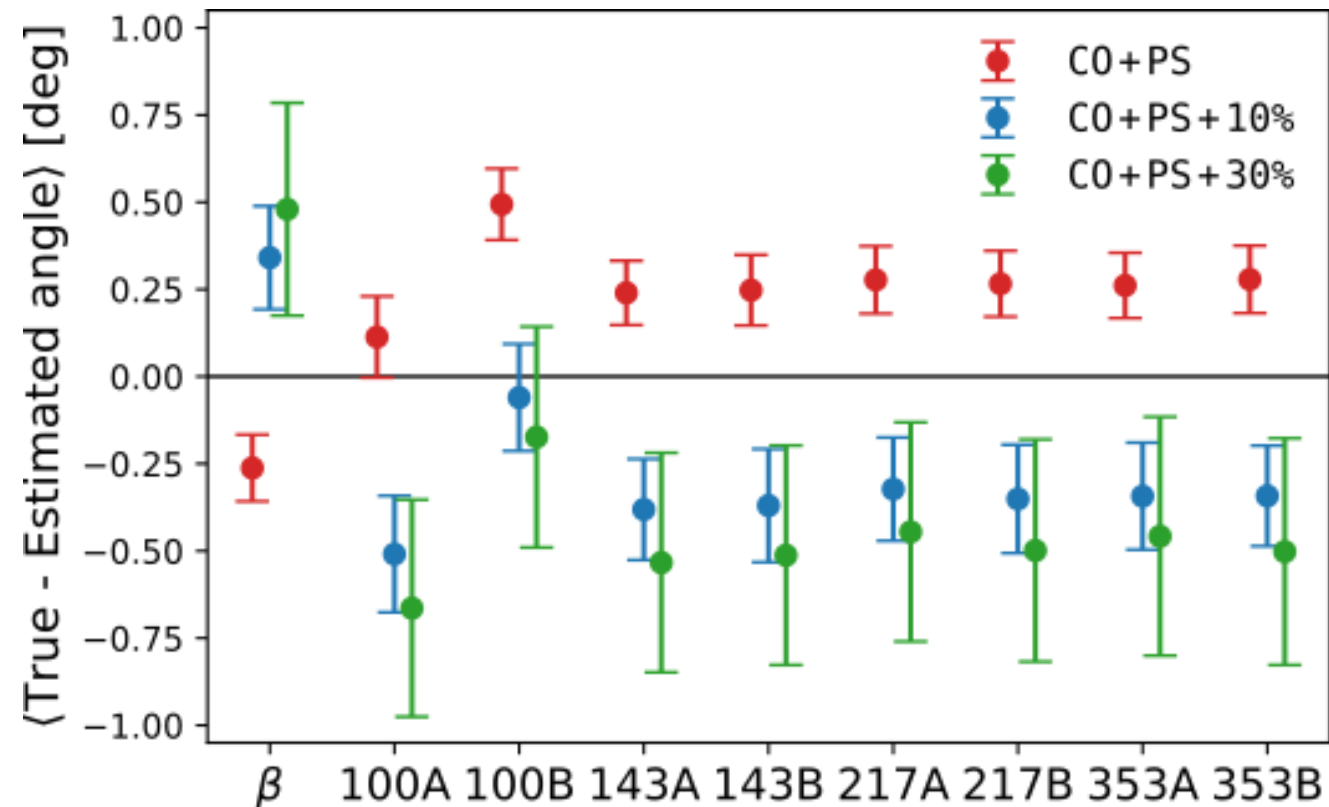
Planck Collaboration XI. 2020, A&A, 641, A11

→ Expect  $\gamma > 0$  leading to  $\uparrow \alpha$  and  $\downarrow \beta$

# NPIPE end-to-end simulations

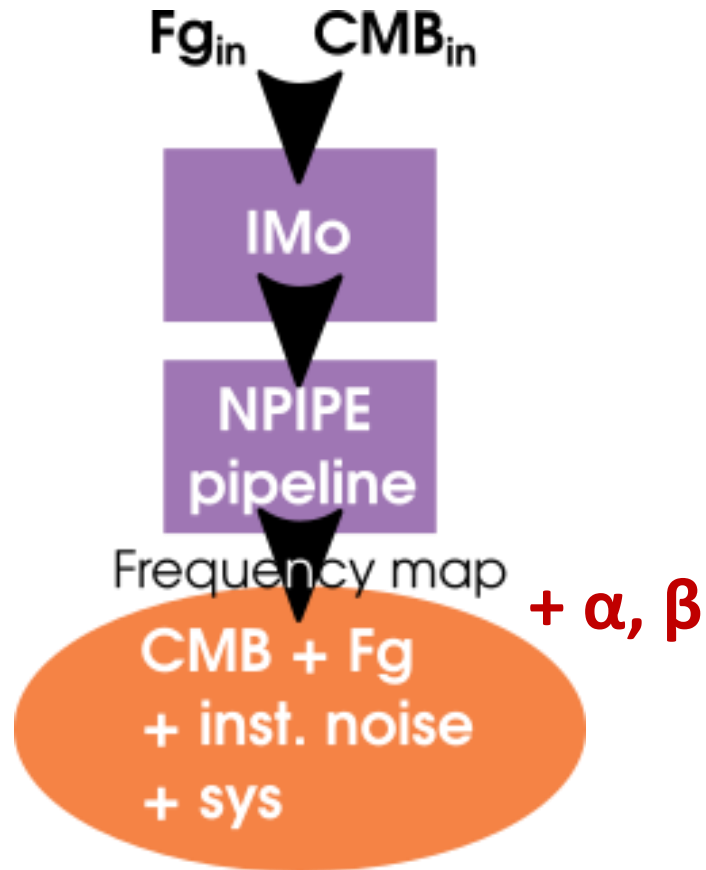


## Ignoring dust EB



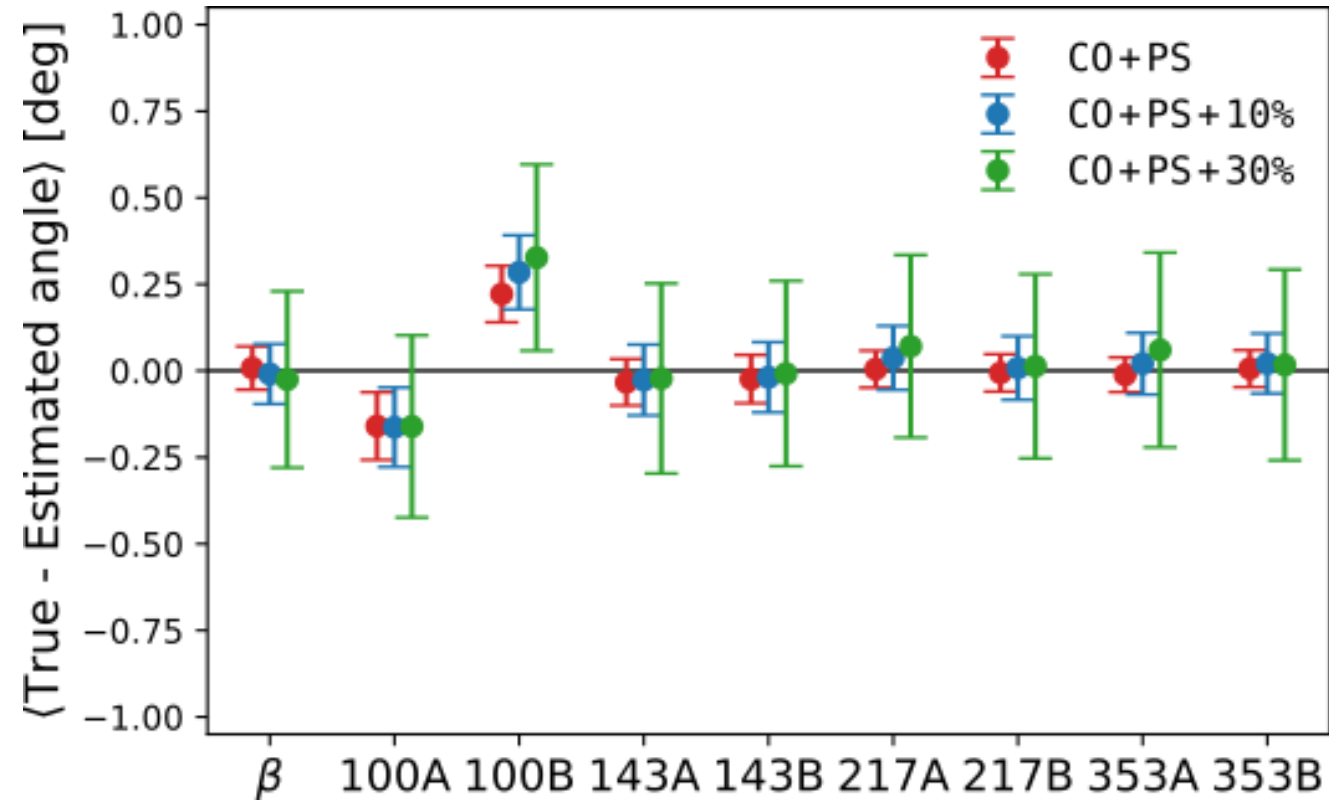
Average over 100 simulations  
Error bar = simulations dispersion

# NPIPE end-to-end simulations



## Correcting for dust EB

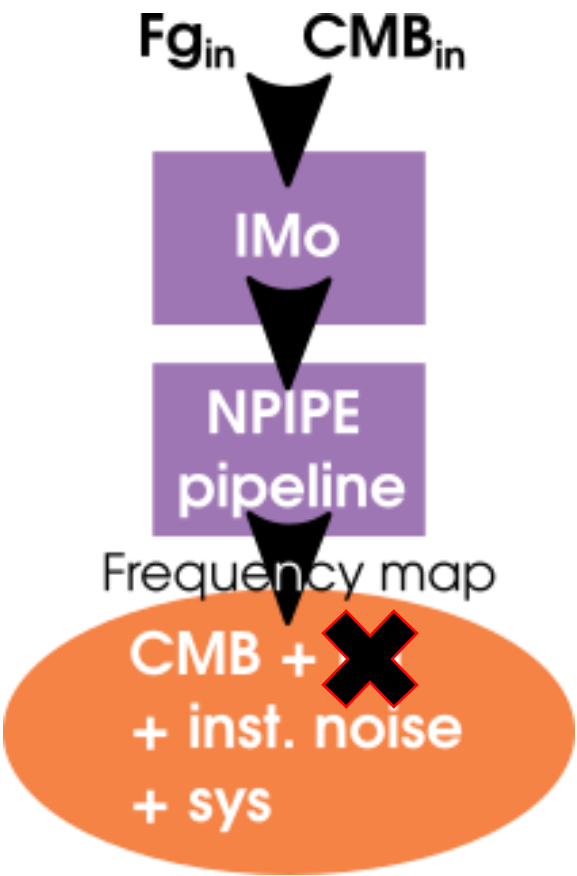
Exact description of the fiducial foreground model



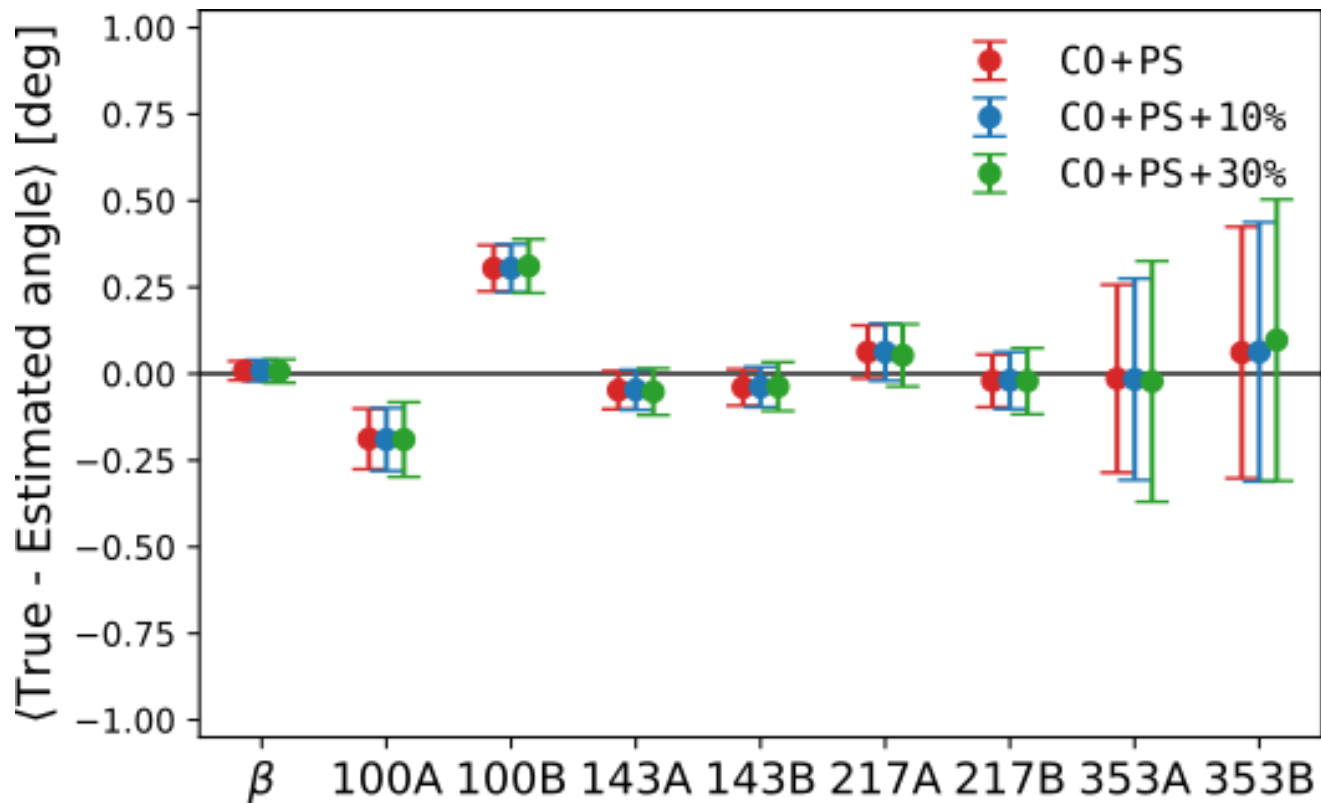
Average over 100 simulations

Error bar = simulations dispersion

# NPIPE end-to-end simulations



## Removing foregrounds Sims of CMB + Noise + Systematics

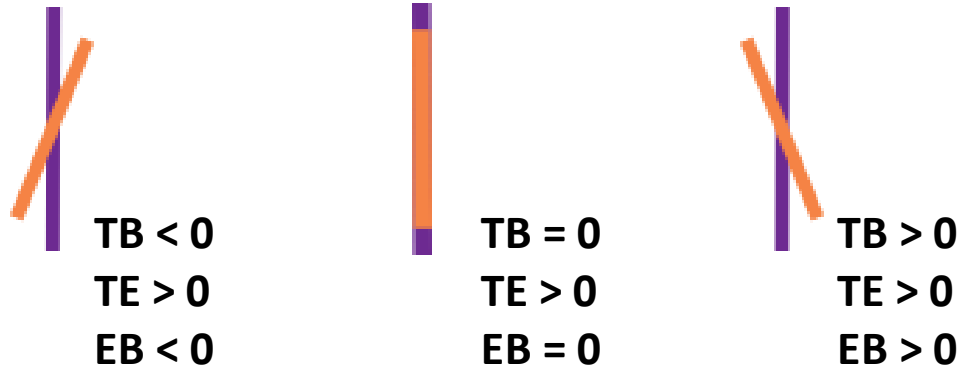


Average over 100 simulations  
Error bar = simulations dispersion



## Misalignment between the filamentary dust structures of the ISM and the plane-of-sky orientation of the Galactic magnetic field

Filament  
Magnetic Field



$$C_{\ell}^{TB,\text{dust}} \propto \sin(2\psi)$$

$$C_{\ell}^{TE,\text{dust}} \propto \cos(2\psi)$$

$$C_{\ell}^{EB,\text{dust}} \propto \sin(4\psi)$$

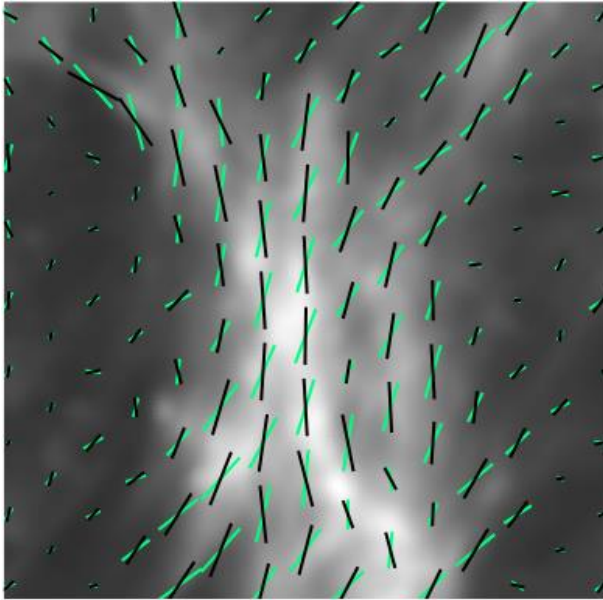
Sign and magnitude of **EB** can be predicted by measuring **TE** and **TB**

↓ **Our take**

$$C_{\ell}^{EB,\text{dust}} = r_{\ell}^{TB,\text{dust}} \sqrt{C_{\ell}^{EE,\text{dust}} C_{\ell}^{BB,\text{dust}}} \sin \left( 2 \arctan \left( \frac{C_{\ell}^{TB,\text{dust}}}{C_{\ell}^{TE,\text{dust}}} \right) \right)$$

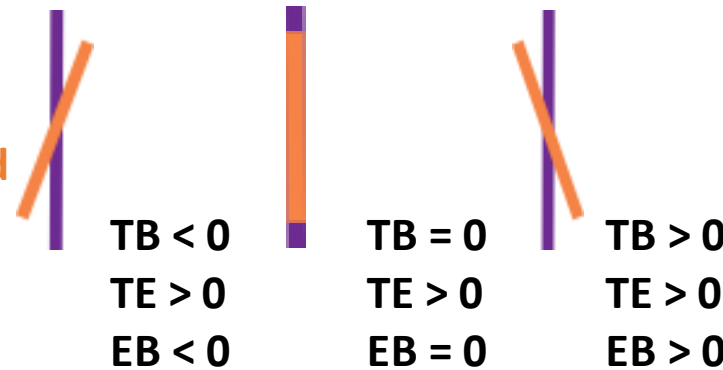
Small angle approximation

$$\left. \begin{aligned} C_{\ell}^{BB,\text{dust}} &\propto C_{\ell}^{EE,\text{dust}} \text{ thus } \sqrt{C_{\ell}^{EE,\text{dust}} C_{\ell}^{BB,\text{dust}}} \rightarrow C_{\ell}^{EE,\text{dust}} \\ |r_{\ell}^{TB,\text{dust}}| &\rightarrow A_{\ell} \text{ free amplitude parameter } 0 \leq A_{\ell} \ll 1 \end{aligned} \right\} C_{\ell}^{EB,\text{dust}} \approx A_{\ell} C_{\ell}^{EE,\text{dust}} \frac{C_{\ell}^{TB,\text{dust}}}{C_{\ell}^{TE,\text{dust}}}$$



Misalignment between the dust filaments of the ISM and the plane-of-sky orientation of the Galactic magnetic field sources TE, TB, EB correlations

Filament  
Magnetic Field



$$C_{\ell}^{TB,\text{dust}} \propto \sin(2\psi)$$

$$C_{\ell}^{TE,\text{dust}} \propto \cos(2\psi)$$

$$C_{\ell}^{EB,\text{dust}} \propto \sin(4\psi)$$

Sign and magnitude of **EB** predicted from **EE**, **TE**, and **TB**

$$C_{\ell}^{EB,\text{dust}} \approx A_{\ell} C_{\ell}^{EE,\text{dust}} \frac{C_{\ell}^{TB,\text{dust}}}{C_{\ell}^{TE,\text{dust}}}$$

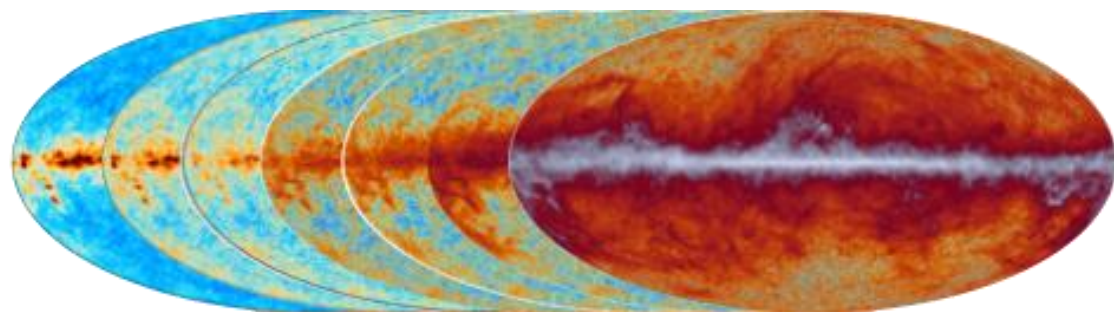
Take dust  $C_{\ell}$  to be that of NPIPE @ 353GHz

$A_{\ell}$  free amplitude parameter  $0 \leq A_{\ell} \ll 1$



### Caveats and limitations

- Assumes that all dust is sourcing the misalignment while **only filaments are expected to produce EB**
- Noisy proxy** as it is built from Planck polarization measurements



Frequency maps

$f(\nu)$  conversion from  
thermodynamic to  
antenna units

$B(\nu, T)$  Planck's law

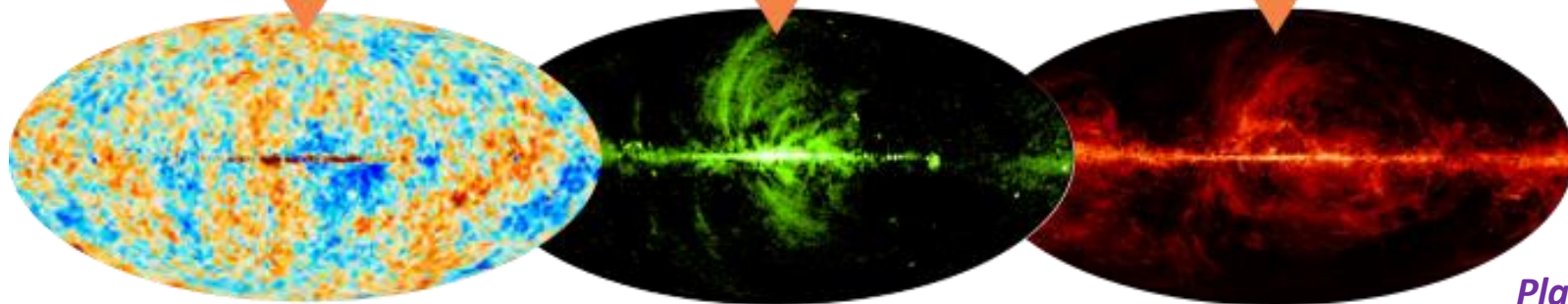
$$\left(\frac{Q}{U}\right)_p = \left(\frac{q^{\text{cmb}}}{u^{\text{cmb}}}\right)_p + \frac{1}{f(\nu)} \left(\frac{\nu}{\nu_s}\right)^{\beta_s} \left(\frac{q^{\text{synch}}}{u^{\text{synch}}}\right)_p + \frac{1}{f(\nu)} \left(\frac{\nu}{\nu_d}\right)^{\beta_d-2} \frac{B(\nu, T_d)}{B(\nu_d, T_d)} \left(\frac{q^{\text{dust}}}{u^{\text{dust}}}\right)_p$$

CMB

Synch

Dust

Power law synchrotron and one-  
component modified blackbody  
dust models



Commander

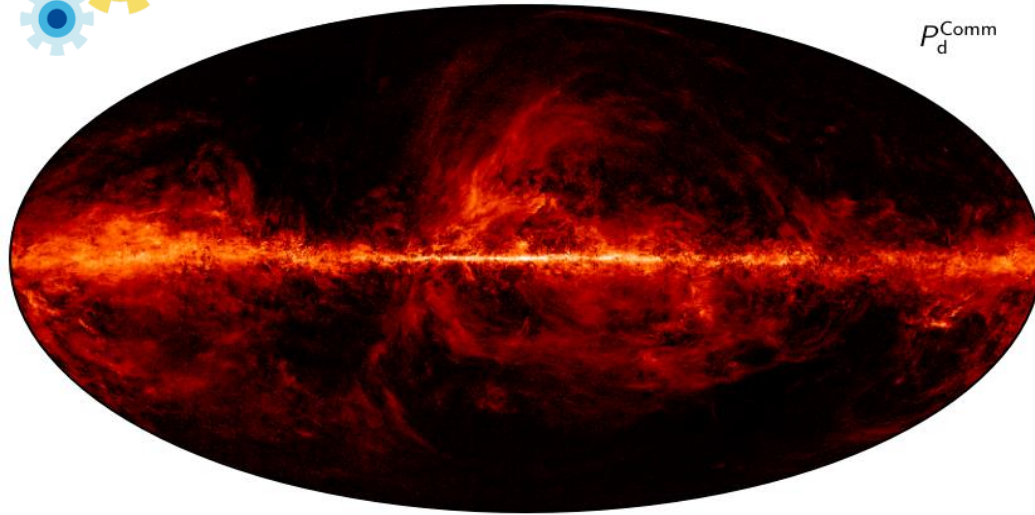
Planck Collaboration IV. 2020, A&A, 641, A4

Take the Commander sky model as our foreground model

$$C_\ell^{EB,o} = \frac{\tan(4\alpha)}{2} \left( C_\ell^{EE,o} - C_\ell^{BB,o} \right) + \frac{\mathcal{D}}{\cos(4\alpha)} C_\ell^{EB,fg} + \frac{\sin(4\beta)}{2 \cos(4\alpha)} \left( C_\ell^{EE,cmb} - C_\ell^{BB,cmb} \right)$$



Commander



$$\frac{1}{f(\nu)} \left( \frac{\nu}{\nu_d} \right)^{\beta_d - 2} \frac{B(\nu, T_d)}{B(\nu_d, T_d)} \left( q^{\text{dust}} \right)_p$$



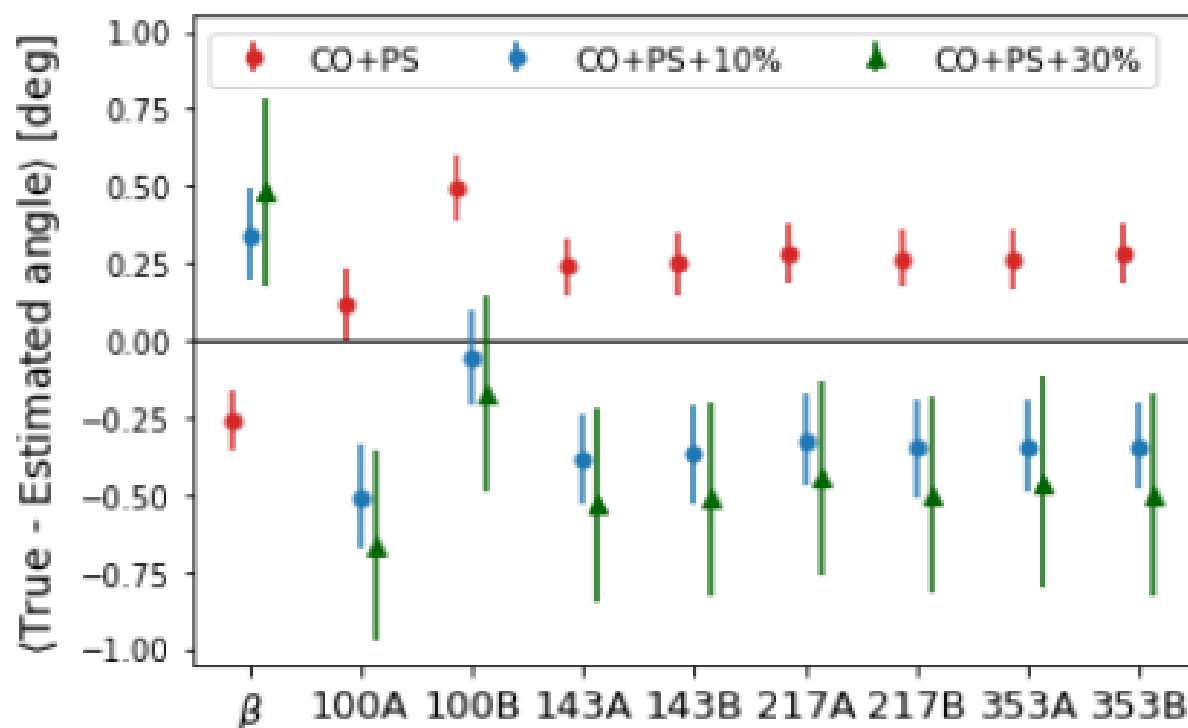
## Caveats and limitations

- **Limited signal-to-noise** of EB template leads to a 20% underestimation of uncertainties  
PDP et al 2022 [arXiv:2210.07655]  
→ **High-precision measurements from next-generation experiments**
- **Spurious EB correlations through ignoring instrumental polarization angles** in the SED model  
→ **Inclusion of polarization angles in SED**  
de la Hoz et al 2022, JCAP, 03, 032
- **Spurious EB correlations from the integration of different dust clouds along the line-of-sight**  
Vacher et al 2022 [arXiv:2210.14768]  
→ **Dust model beyond the single modified blackbody**

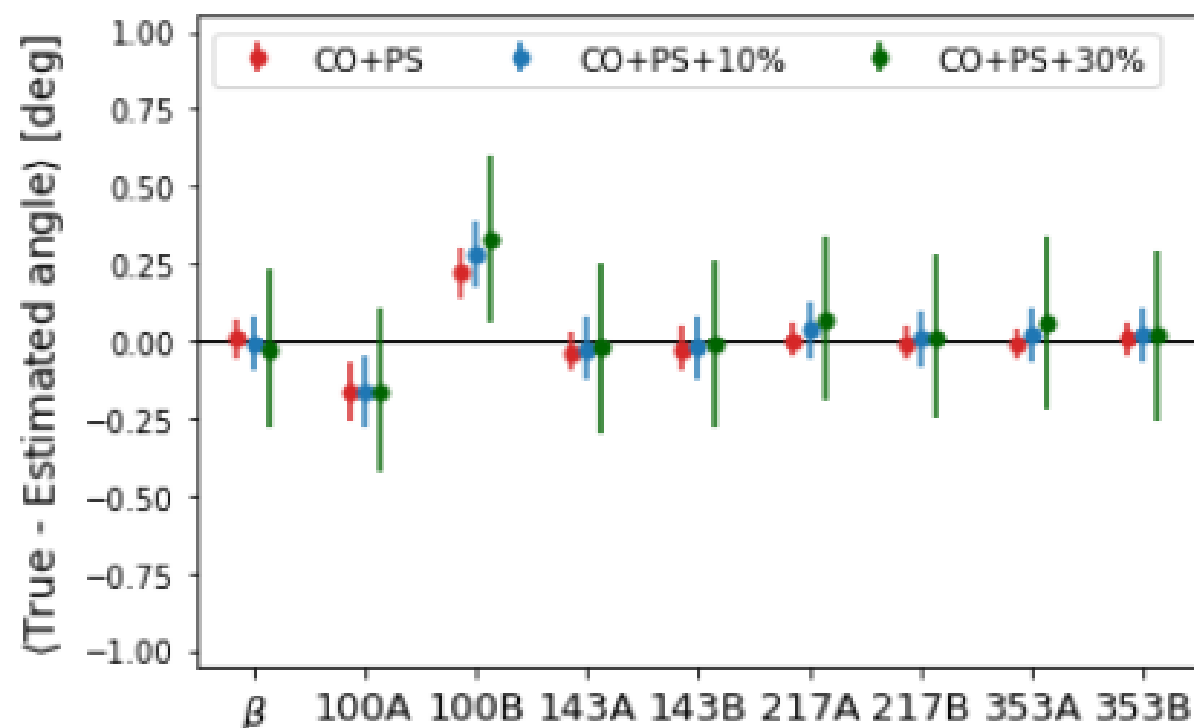
# NPIPE end-to-end simulations

Simulations of **CMB + Foregrounds + Noise + Systematics**

**Baseline analysis** (ignoring foreground EB)



**Modeling foreground EB (Commander)**



Average over 100 simulations  
Error bar = simulations dispersion

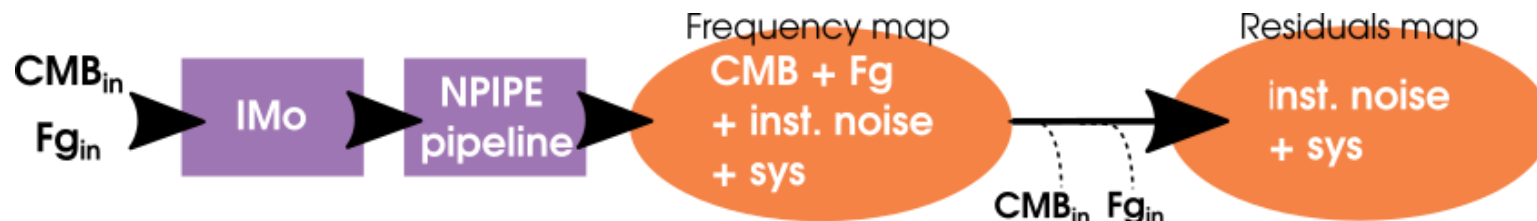
PDP et al 2022 [arXiv:2210.07655]



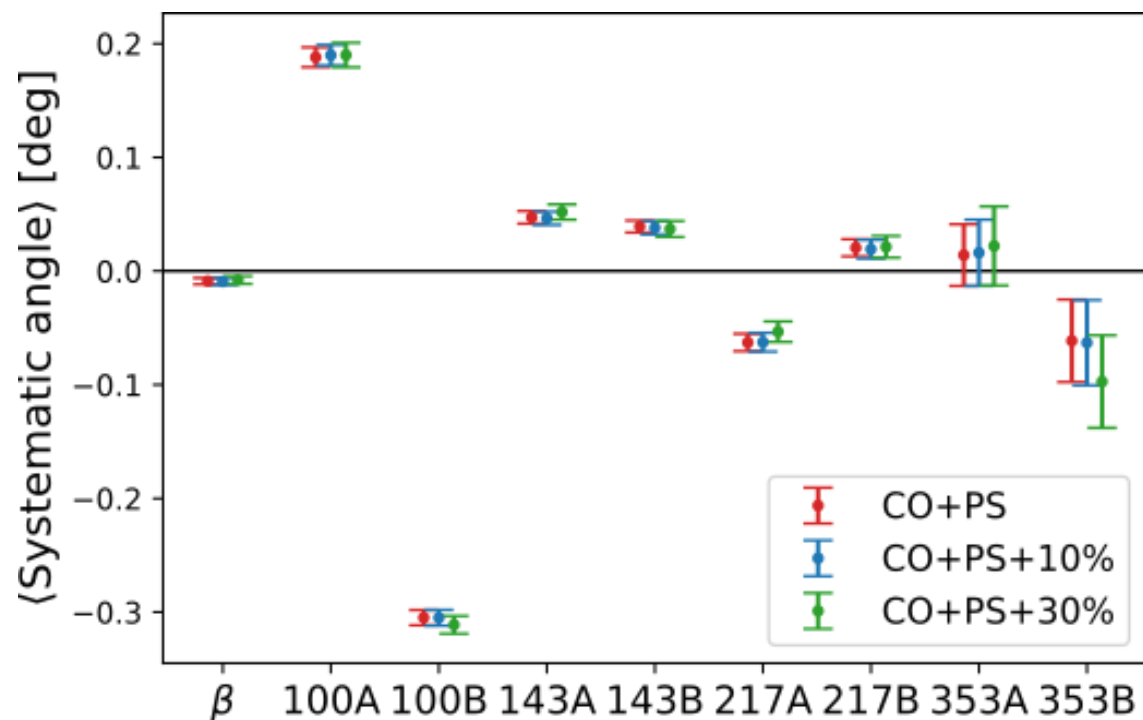
# Quantifying systematics with NPIPE end-to-end simulations

PDP et al 2022 [arXiv:2210.07655]

## Simulations of CMB + Noise + Systematics



No foreground to break the  $\alpha + \beta$  degeneracy



Average over 100 sims

Error bar = sim' dispersion / sqrt(100)

different angle for each detector split  $\rightarrow \alpha_i$   
 same angle for all frequency bands  $\rightarrow \beta$

	From sims	$\sigma_{\text{stat}}$ fit to data
$\langle \alpha_{100A} \rangle$	$0.188^\circ \pm 0.009^\circ$	$0.13^\circ$
$\langle \alpha_{100B} \rangle$	$-0.305^\circ \pm 0.007^\circ$	$0.13^\circ$
$\langle \alpha_{143A} \rangle$	$0.047^\circ \pm 0.006^\circ$	$0.11^\circ$
$\langle \alpha_{143B} \rangle$	$0.039^\circ \pm 0.005^\circ$	$0.11^\circ$
$\langle \alpha_{217A} \rangle$	$-0.063^\circ \pm 0.008^\circ$	$0.11^\circ$

$\rightarrow$  cross-polarization effect

$\rightarrow$  beam leakage

$\alpha_{\text{sys}}$  don't need to agree with data

$\rightarrow$  simulations can't include the real  $\alpha_i$  in the data

Negligible impact on  $\beta$

$\langle \beta_{\text{sys}} \rangle$	$-0.009^\circ \pm 0.003^\circ$	$0.11^\circ$
--------------------------------------	--------------------------------	--------------

Intensity-to-polarization leakage  $\rightarrow C_\ell^{EB} \propto C_\ell^{TT}$

Cross-polarization effect  $\rightarrow C_\ell^{EB} \propto C_\ell^{EE}$

A combination of both  $\rightarrow C_\ell^{EB} \propto C_\ell^{TE}$

Beam leakage

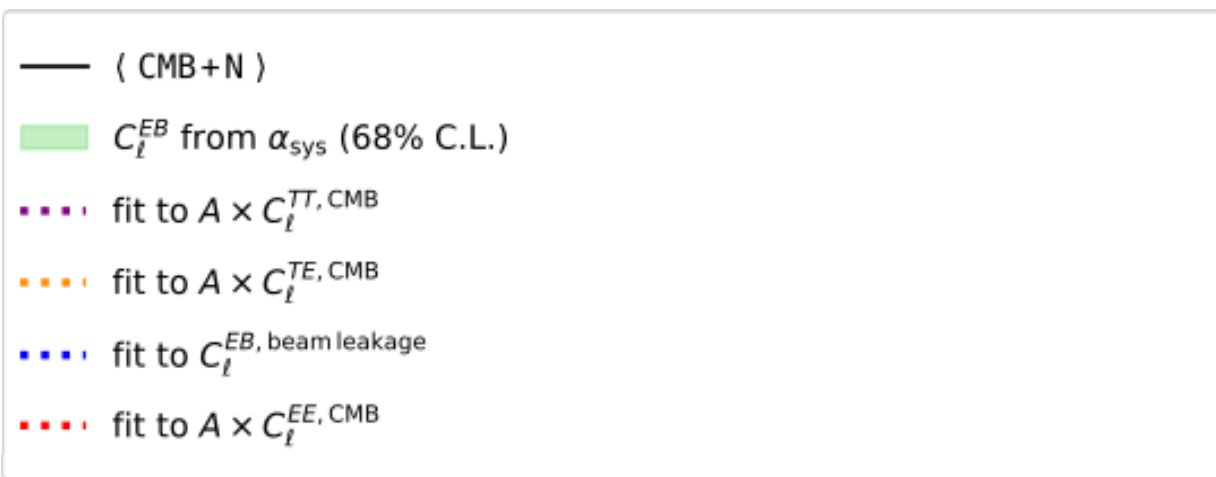
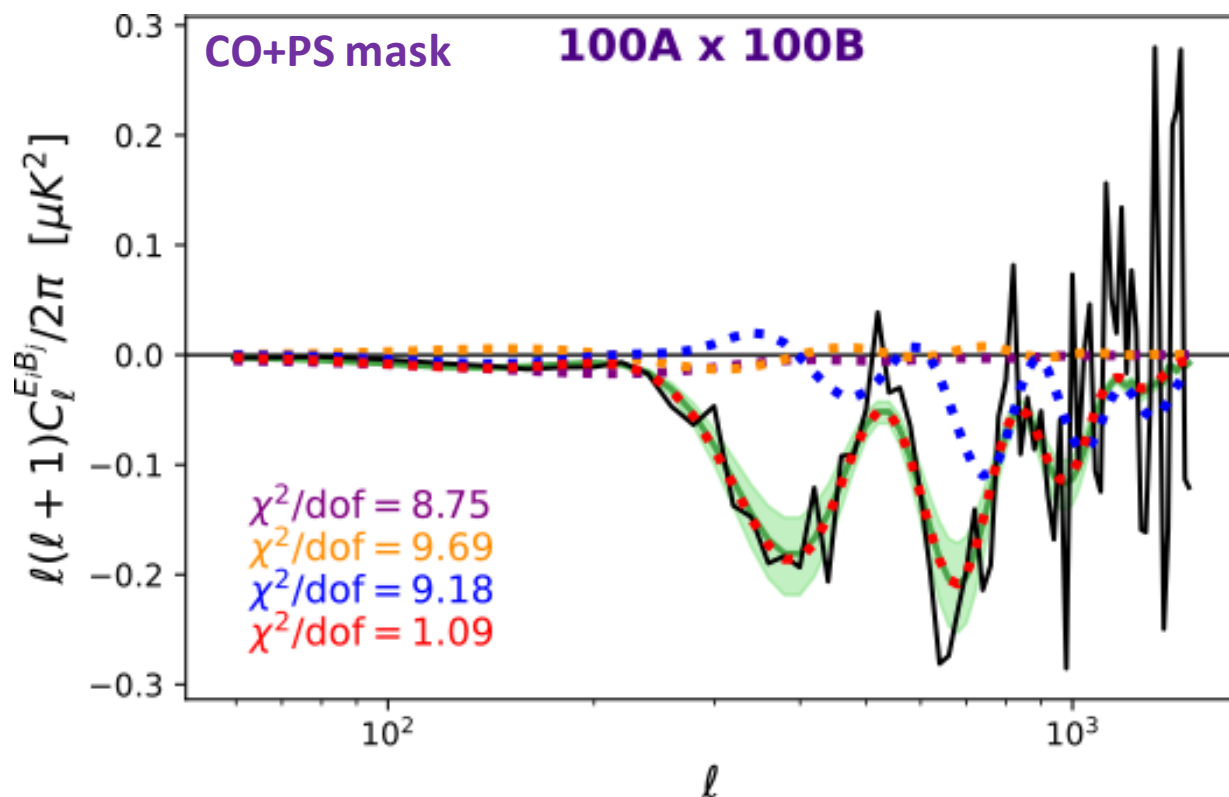
$$C_\ell^{EB} = \omega_{\ell, \text{pix}}^2 \sum_{XY} W_\ell^{EB, XY} C_\ell^{XY, \text{cmb}}$$

$$XY \in \{TT, EE, BB, TE\}$$

QuickPol's polarization matrices

Hivon et al 2017, A&A, 598, A25

PDP et al 2022 [arXiv:2210.07655]



Particularly dangerous since our estimator relies on finding a signal resembling  $EE^{\text{cmb}}$  in EB

Intensity-to-polarization leakage  $\rightarrow C_\ell^{EB} \propto C_\ell^{TT}$

Cross-polarization effect  $\rightarrow C_\ell^{EB} \propto C_\ell^{EE}$

A combination of both  $\rightarrow C_\ell^{EB} \propto C_\ell^{TE}$

Beam leakage

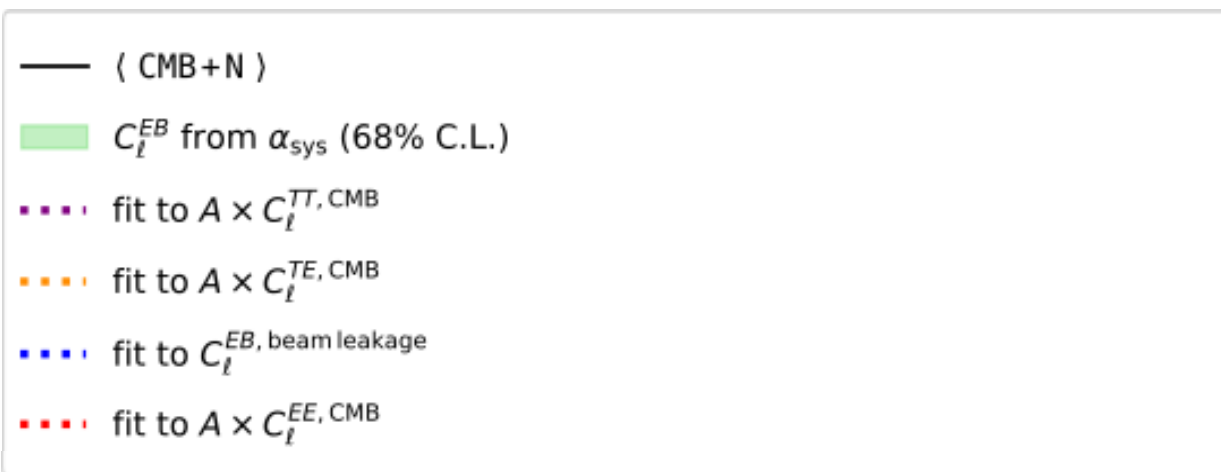
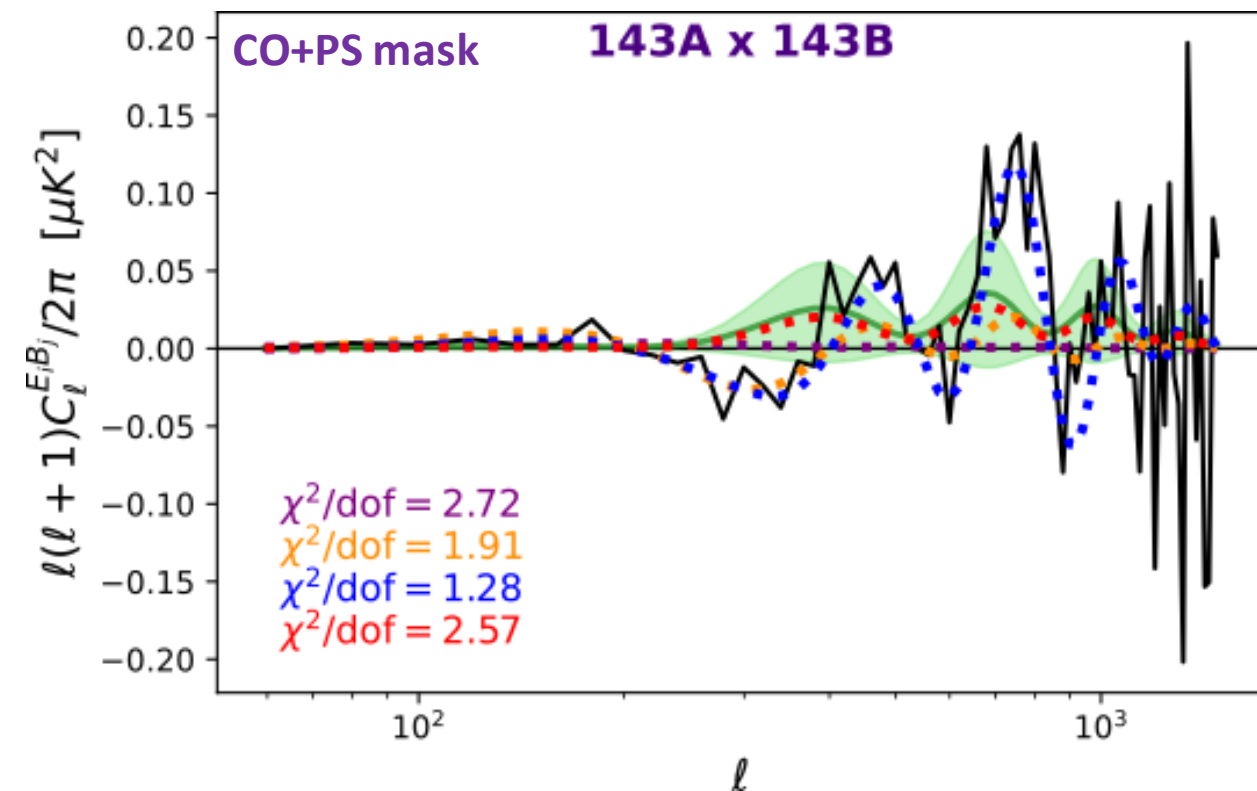
$$C_\ell^{EB} = \omega_{\ell, \text{pix}}^2 \sum_{XY} W_\ell^{EB, XY} C_\ell^{XY, \text{cmb}}$$

$$XY \in \{TT, EE, BB, TE\}$$

QuickPol's polarization matrices

Hivon et al 2017, A&A, 598, A25

PDP et al 2022 [arXiv:2210.07655]

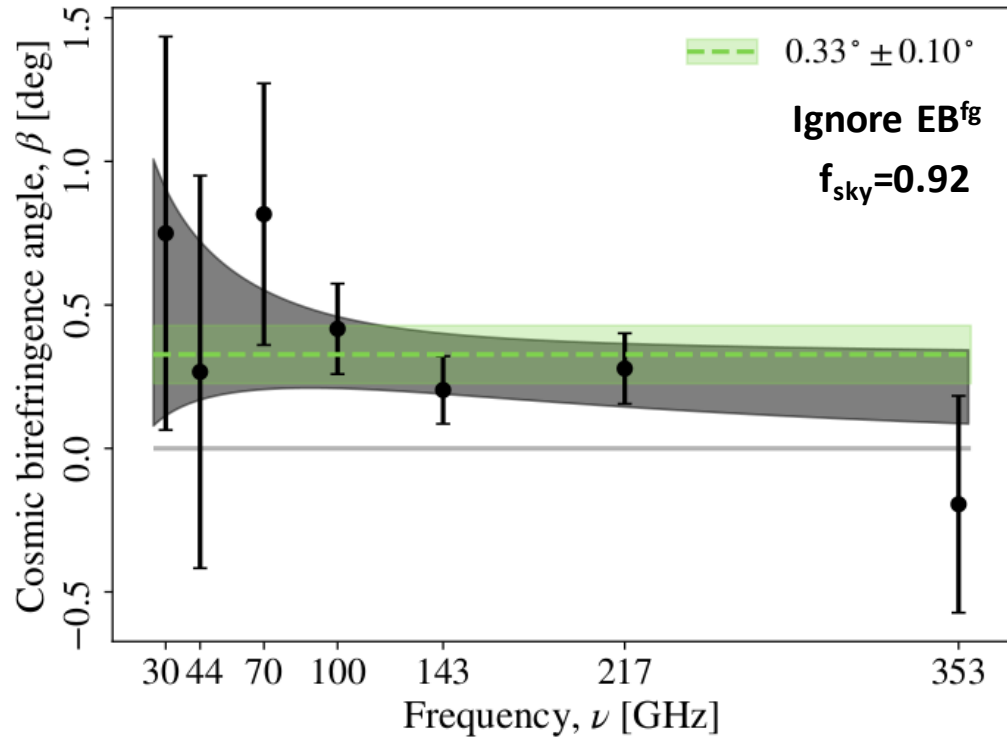


The estimator is trying to accommodate beam leakage as a rotation of EE



# Frequency-dependent constraints on cosmic birefringence from the LFI and HFI Planck data release 4

Eskilt 2022, A&A, 662, A10



$$\beta_\nu = \beta_o (\nu/\nu_o)^n \begin{cases} \beta_o = 0.29^{+0.10}_{-0.11} \text{deg} \\ n = -0.35^{+0.48}_{-0.47} \end{cases}$$

First follow-up work adding *Planck* low-frequency bands  
→  $\beta = 0.33^\circ \pm 0.10^\circ$  (3.3 $\sigma$ ) for nearly full-sky data

Forcing an integer index

n	$\Delta\chi^2$ - Ignore EB <sup>fg</sup>	$\Delta\chi^2$ - Model EB <sup>fg</sup>
2	8.21	9.45
1	4.67	5.60
0	0.00	0.00
-2	2.25	3.01

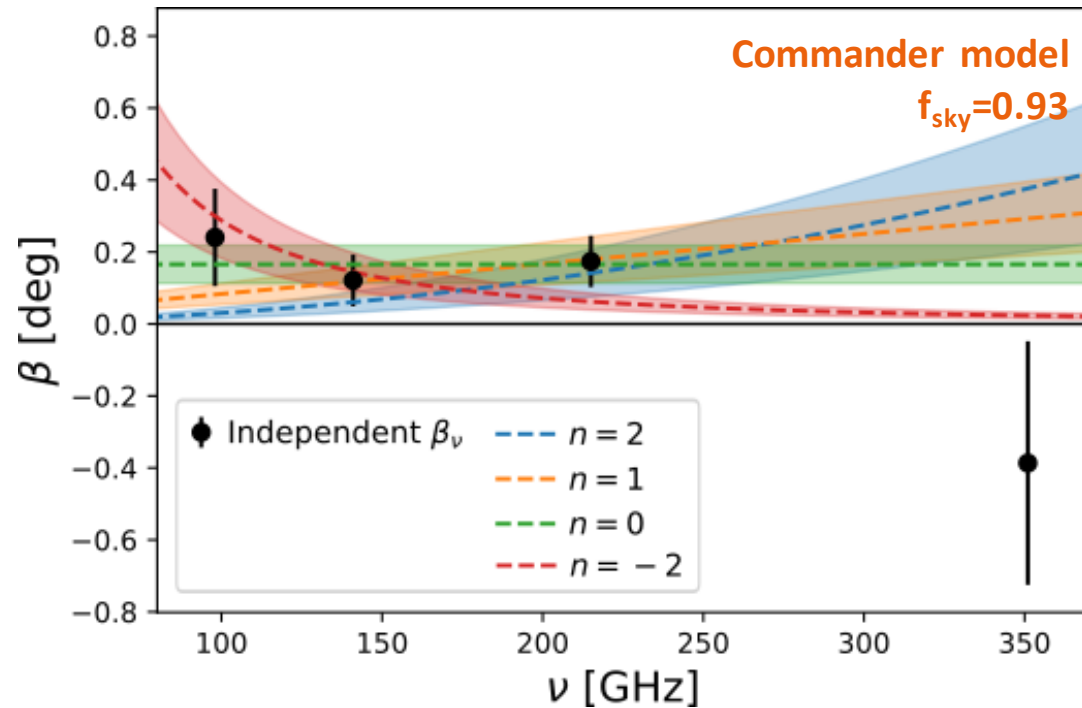
Data seems to favor a **frequency-independent** birefringence

→ Quantum gravity theories  $\beta \propto \nu^2$

→ Lorentz-violating electrodynamics  $\beta \propto \nu$

→ **Chern-Simons coupling to a light pseudoscalar field**  $\beta \propto \nu^0$

→ Faraday rotation from primordial magnetic fields  $\beta \propto \nu^{-2}$



$n$	$\beta_0$ [deg]	$\Delta\chi^2$
2	$0.07 \pm 0.03$	5.08
1	$0.13 \pm 0.04$	1.77
0	$0.17 \pm 0.05$	0.00
-2	$0.13 \pm 0.05$	2.15

Independent  $\beta_\nu$  for each frequency

$\beta_\nu = \beta_0 \nu^2$  Quantum gravity models that modify the dispersion relation of photons

Gleiser & Kozameh 2001, PRD, 64, 8, 083007

$\beta_\nu = \beta_0 \nu$  Superluminal Lorenz-violating electrodynamics emerging from a non-vanishing Weyl tensor

Shore 2005, Nucl Phys B, 717, 86118

$\beta_\nu = \beta_0$  Chern-Simons coupling to a light pseudoscalar field like that of axion-like particles

$\beta_\nu = \beta_0 \nu^{-2}$  Faraday rotation from Galactic or Primordial magnetic fields

Subramanian 2016, Rep Prog Phys, 79, 076901

Data seems to favor a frequency-independent birefringence

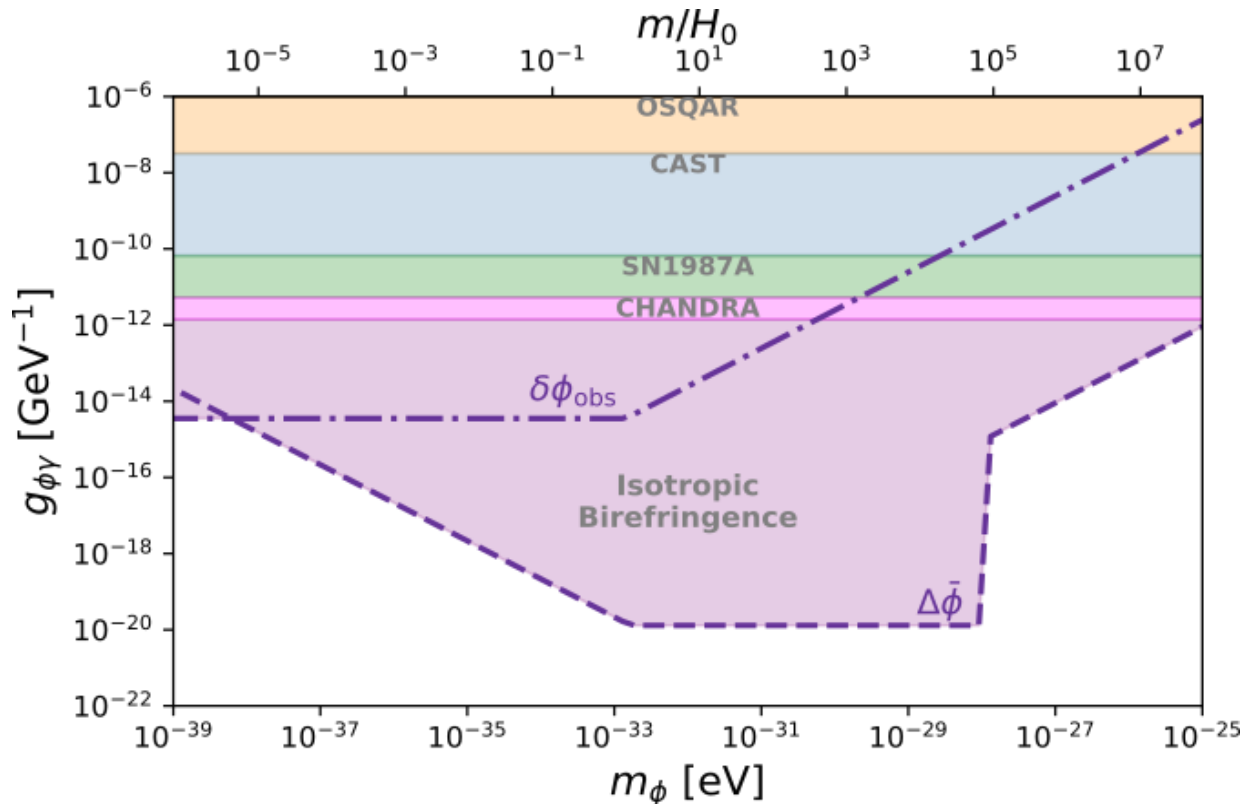
See Eskilt 2022, A&A, 662, A10 for a more detailed analysis

# Constraining power of CMB observations on ALP parameter space

Fujita et al 2021, PRD, 103, 063508

Assuming:

- A **simple potential**  $V(\phi) = \frac{1}{2}m_\phi^2\phi^2$
- A **scale-invariant** power spectrum for the ALP field



- A spatially flat FLRW universe, leading to **EoM**

$$\bar{\phi}'' + 2\mathcal{H}\bar{\phi}' + a^2m_\phi^2\bar{\phi} = 0$$

$$\delta\phi'' + 2\mathcal{H}\delta\phi' - \nabla^2\delta\phi + a^2m_\phi^2\delta\phi = 0$$

- The **largest allowed ALP abundance**

$$\Omega_\phi \begin{cases} \Omega_\Lambda = 0.69 & m_\phi \leq 9.26 \times 10^{-34} \text{eV} \\ 0.006h^{-2} & 10^{-32} \text{eV} \leq m_\phi \leq 10^{-25.5} \text{eV} \end{cases}$$

Planck Collaboration VI. 2020, A&A, 641, A6

- **$r < 0.032$**  Tristram et al 2022, PRD, 105, 083524
- **$\beta \approx 0.30^\circ$**

Chern-Simons coupling to a light ( $m < 10^{-27}\text{eV}$ ) pseudoscalar field

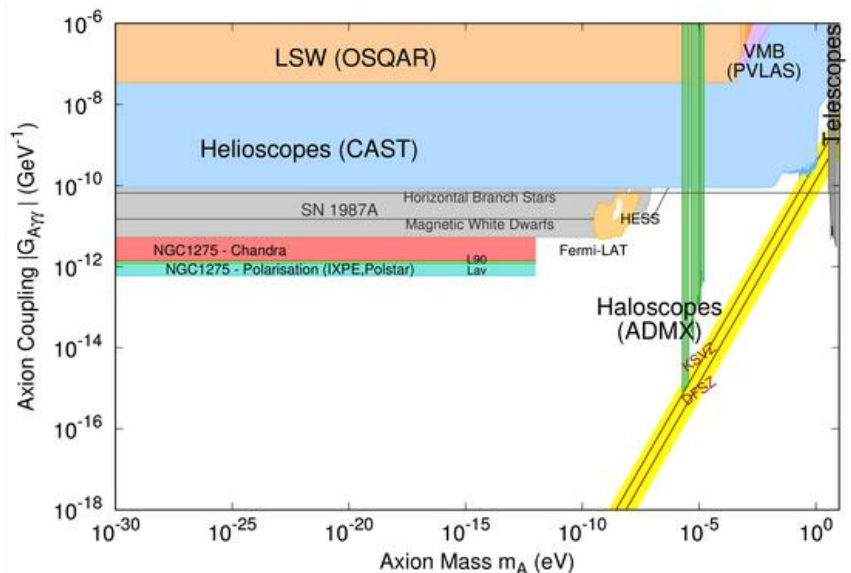
$$\mathcal{L} = -\frac{1}{2}\partial^\mu\phi\partial_\mu\phi - V(\phi) - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} + \frac{1}{4}g_{\phi\gamma}\phi F_{\mu\nu}\tilde{F}^{\mu\nu}$$

Marsh 2016, Phys Rep, 643, 1

## Axion-like particles (ALP)

Initially proposed to solve the strong-CP problem

Evolved beyond the QCD axion to the more general axion-like particles from supersymmetry or string theories ( $10^{-33}\text{eV} < m < 10^{-18}\text{eV}$ )



Day & Krippendorf 2018, Galaxies 2018, 6(2), 45

Kamionkowski & Riess 2022 [arXiv:2211.04492]

## Early Dark Energy (EDE)

Early-time solution to the Hubble tension that modifies the sound horizon, increasing the  $H_0$  inferred from CMB data

Fluid that behaves like a cosmological constant before matter-radiation equality ( $\approx 10\%$  contribution to the total energy density briefly before recombination) and decays faster than radiation afterward so that late-time evolution is unchanged



Suppresses the growth of perturbations at early times, potentially increasing  $\sigma_8$

→ worsening the tension between CMB and LSS measurements

Hill et al 2020, PRD, 102, 043507

Global U(1) shift symmetry, broken by non-perturbative effects (instantons)

$$V(\phi) = m_\phi^2 f^2 \left[ 1 - \cos \left( \frac{\phi}{f} \right) \right]^n$$

Integer values of  $n$

**Axion-like particles (ALP)**

$$n = 1$$

$$V(\phi) \rightarrow \frac{1}{2} m_\phi^2 \phi^2$$

$$\Omega_\phi \propto a^{-3}$$

ALP dilute like matter

Around the minimum behaves as

$$w_\phi = \frac{n-1}{n+1}$$

$$\Omega_\phi \propto a^{-3(w_\phi+1)}$$

**Early Dark Energy (EDE)**

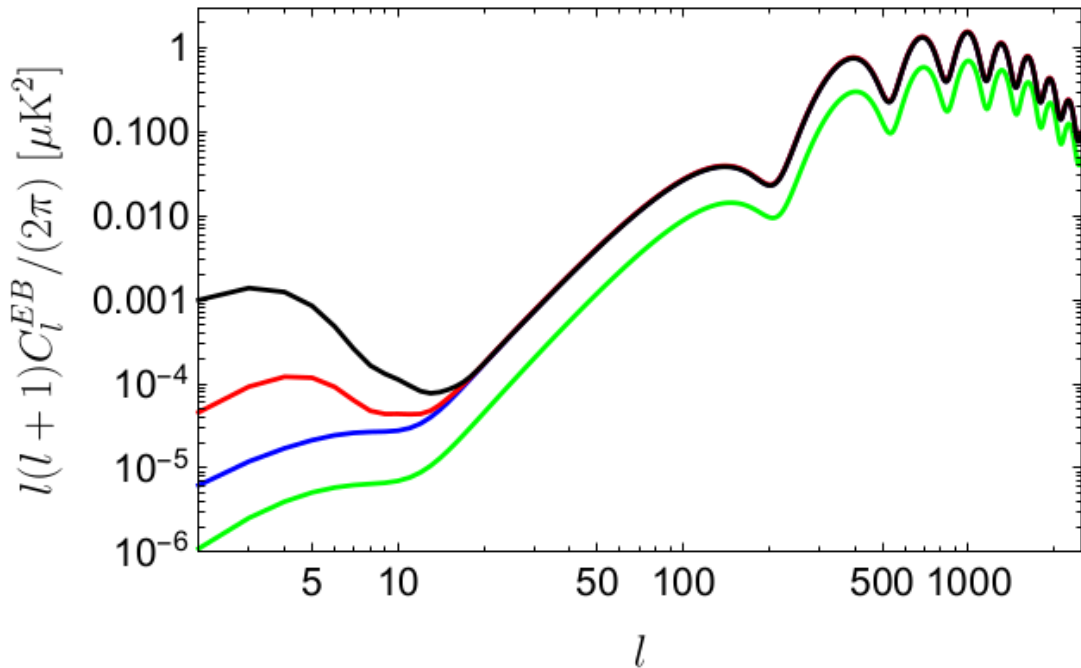
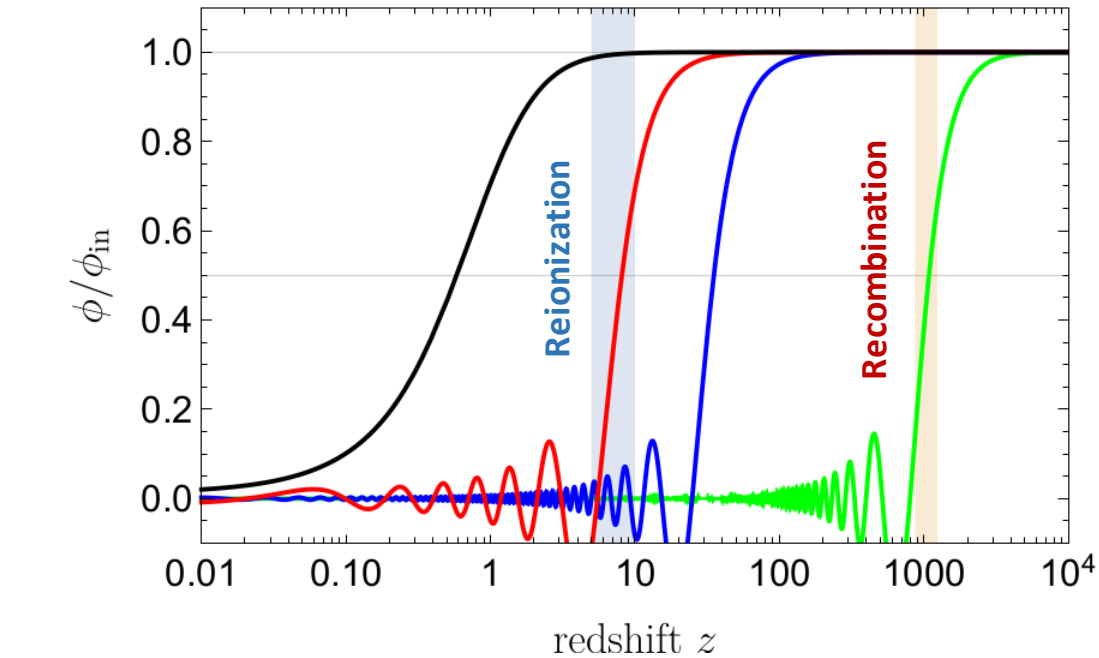
$$n \geq 3$$

$$\Omega_\phi \propto a^{-4.5}$$

(or steeper)



**EDE dilutes faster than radiation**



$$\beta = -\frac{1}{2}g_{\phi\gamma} \int \frac{\partial\phi}{\partial t} dt$$

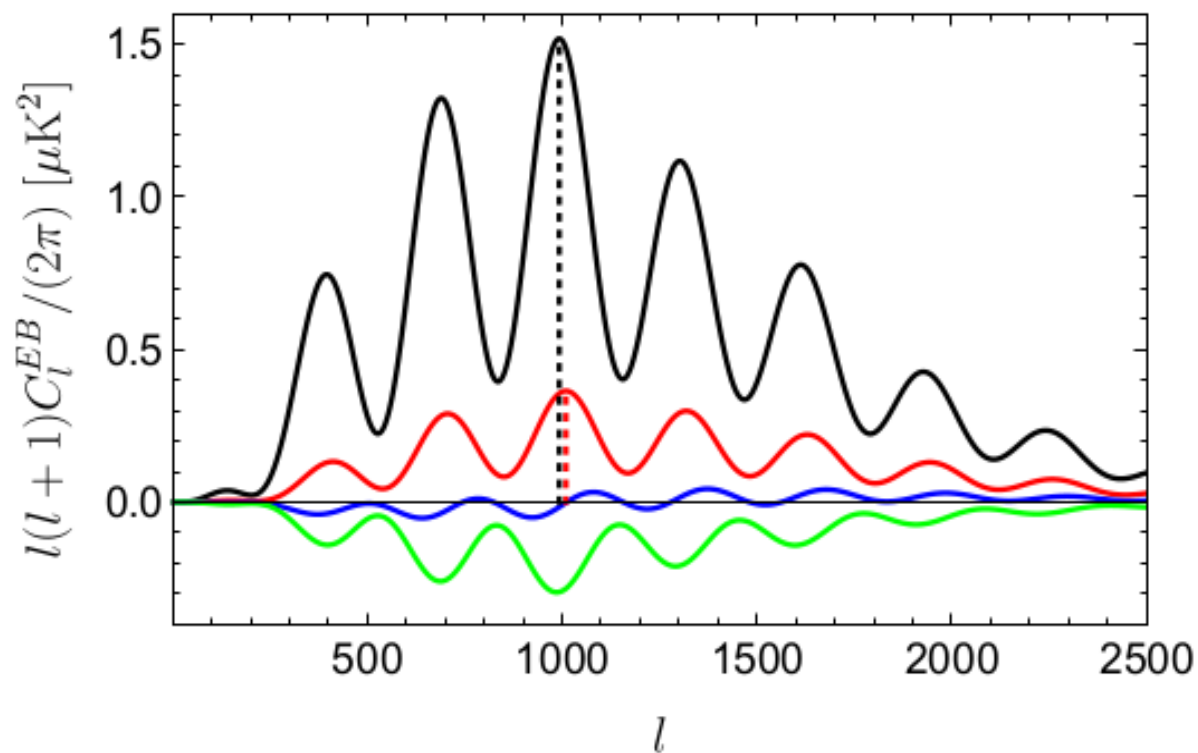
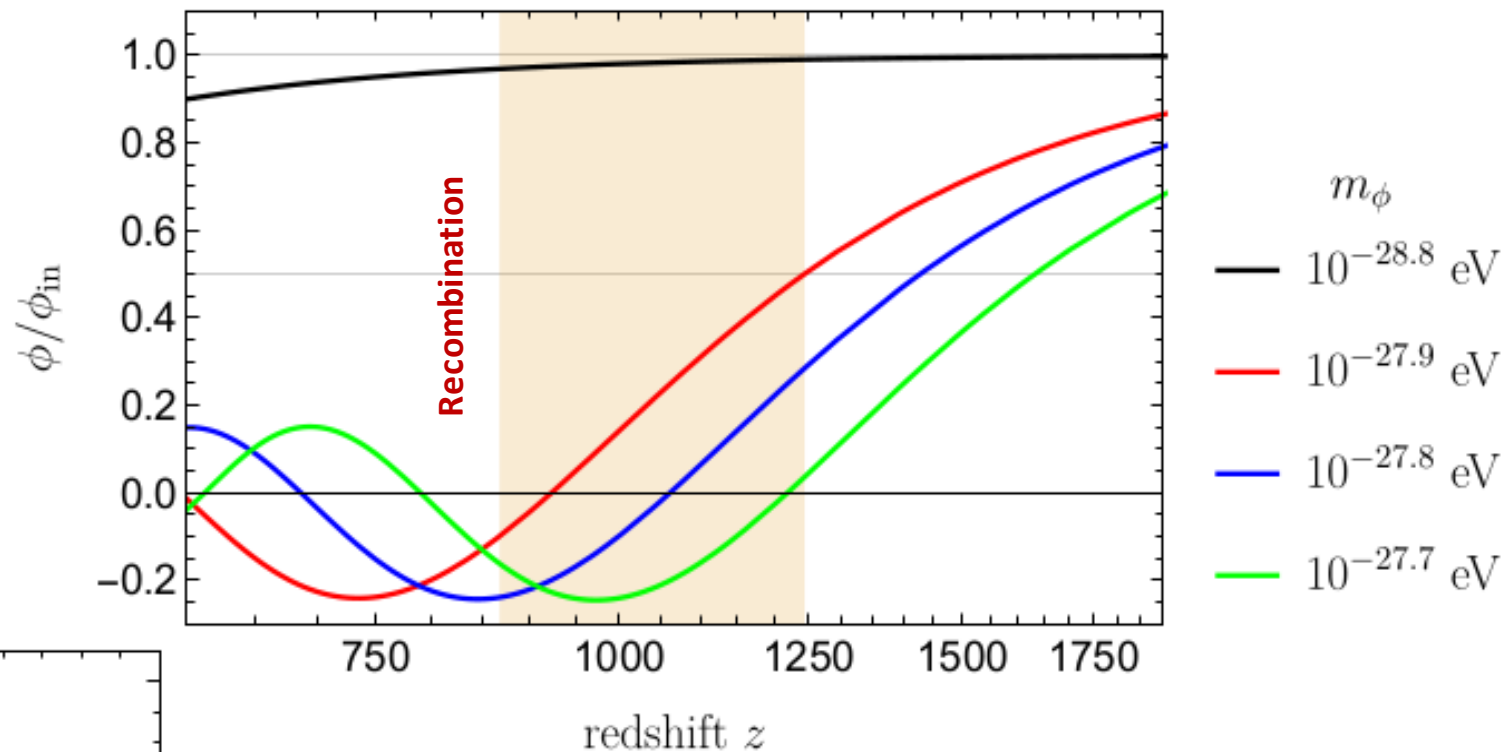
**Birefringence depends on the value of the field at photon emission and absorption**

$$\beta(z) = \begin{cases} 0 & \text{for } z = 0 \\ \beta_{\text{rei}} & \text{for } 0 < z \leq 10, \\ \beta_{\text{rec}} & \text{for } 10 < z \end{cases}$$

**CMB photons emitted at recombination and reionization will suffer different rotations**

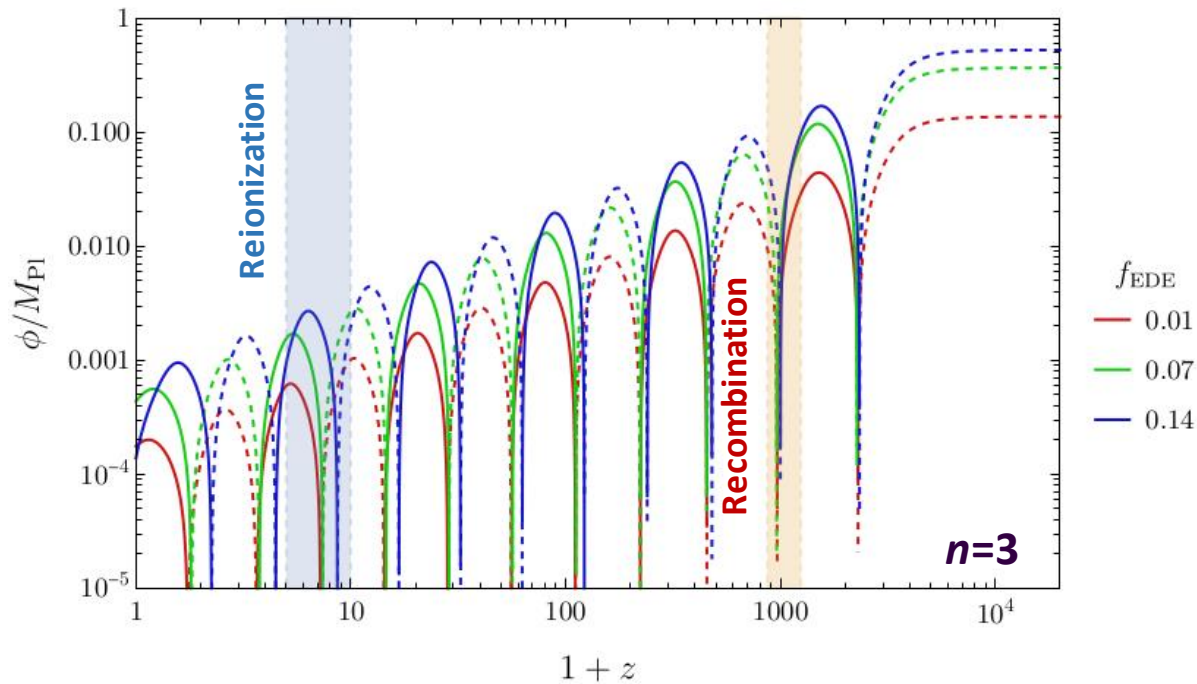
$$\begin{aligned} C_\ell^{EB,o} &\approx \frac{1}{2} \sin(4\beta_{\text{rec}}) C_\ell^{E_{\text{rec}} E_{\text{rec}}} \\ &+ \frac{1}{2} \sin(4\beta_{\text{rei}}) C_\ell^{E_{\text{rei}} E_{\text{rei}}} \\ &+ \sin(2\beta_{\text{rec}} + 2\beta_{\text{rei}}) C_\ell^{E_{\text{rec}} E_{\text{rei}}} \end{aligned}$$

For fields undergoing a significant **evolution** during the epoch of recombination...



... the EB spectrum produced by birefringence no longer resembles a constant rotation of EE

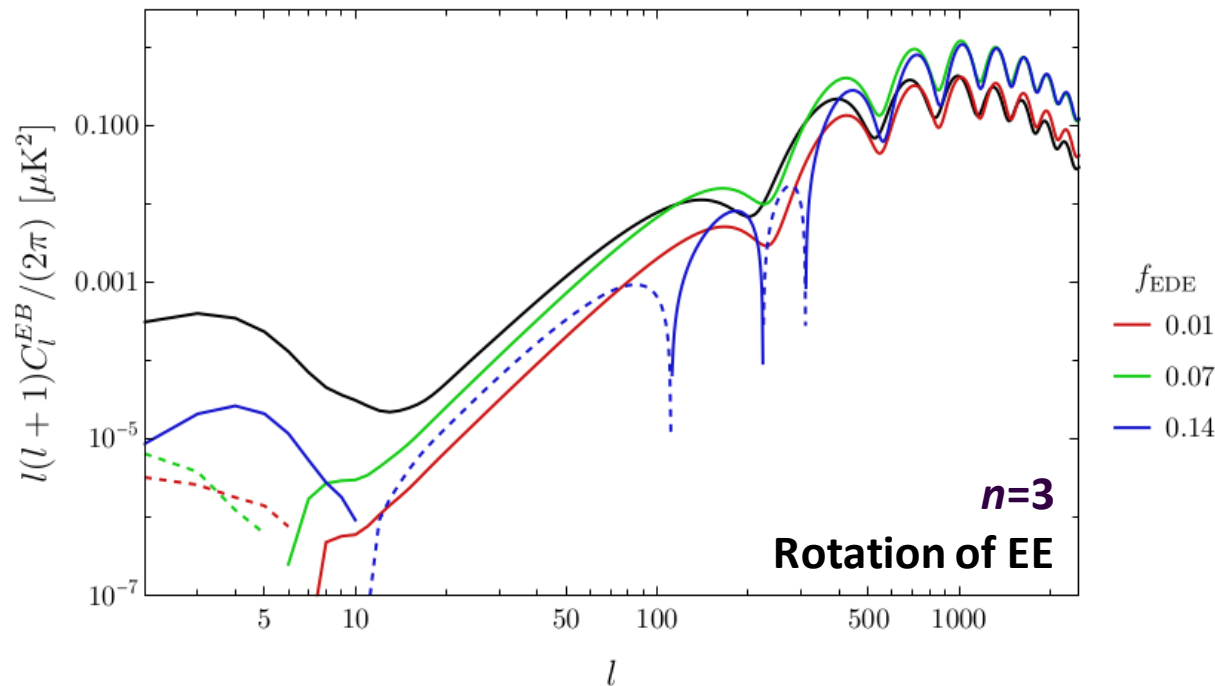




By definition, the EDE field must evolve before recombination

EB no longer resembles a constant EE rotation

EB is strongly dependent on the EDE model ( $n$  and  $f_{\text{EDE}}$ )



CMB data alone can discern between ALPs and EDE as the source of birefringence

→ in the next decade, experiments like CMB-S4 will have enough sensitivity

**WIP:**

Obtain the **first measurement of  $\beta$  from the epoch of reionization** using only low- $\ell$  information