

# Fitting the correlation function with the Lednicky-Lyuboshitz model

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# General expression (for p-p)

Theoretical expression:

$$C_{pp}(k^*) = \frac{1}{2} \sum_{S=0}^1 \frac{2S+1}{(2s_p + 1)^2} \int d^3\vec{r} S(\vec{r}) |\psi_{-\vec{k}}^S(\vec{r}) + (-1)^S \psi_{\vec{k}}^S(\vec{r})|^2$$

$$S(r) \sim \exp(-\frac{r^2}{4R_{inv}^2}) \quad \text{— assuming Gaussian source}$$

Experimental CF:

$$C_{exp}(k^*, R_{inv}) = 1 + \lambda (C_{pp}(k^*, R_{inv}) - 1)$$

# Wave function (s-wave approximation)

**General expression (assuming that protons are primary: pp->pp scattering):**

$$\psi_{\vec{k}}(\vec{r}) = e^{i\delta_c(\eta)} \sqrt{A_c(\eta)} \left[ e^{i\vec{k}\vec{r}} F(-i\eta, 1, i\xi) + \frac{f(k)}{A_c(\eta)} \frac{\tilde{G}(kr, \eta)}{r} \right]$$

$$\eta = \frac{1}{ka}, \quad a - Bohr\ radius$$

$$A_c(\eta) = \frac{2\pi\eta}{e^{2\pi\eta} - 1} \quad - Gamov\ factor\ (Coulomb\ penetration\ factor)$$

$$\xi = kr - \vec{k}\vec{r}$$

$\delta_0(\eta) = arg[\Gamma(1 + i\eta)]$  – Coulomb s – wave phase shift

$f(k^*)$  – scattering amplitude

$$\tilde{G}(kr, \eta) = \sqrt{A_c(\eta)} \left( G_0(kr, \eta) + iF_0(kr, \eta) \right)$$

$F_0(kr, \eta)$  – regular s – wave Coulomb function

$G_0(kr, \eta)$  – singular s – wave Coulomb function

**This formalism was used in ALICE paper for p-p femtoscopy (Run1):**

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# Coulomb wave equation

**Equation for the wave function (s-wave):**

$$\vec{\nabla}^2 \psi_{\vec{k}}(\vec{r}) + \left( k^2 - \frac{2\mu}{\hbar^2} \frac{e^2}{r} \right) \psi_{\vec{k}}(\vec{r}) = 0$$

**Coulomb wave equation:**

$$\frac{d^2\psi}{d^2\rho} + \left( 1 - \frac{2\nu}{\rho} - \frac{l(l+1)}{\rho^2} \right) \psi = 0$$

**General solution:**

$$\psi = A F_l(\eta, \rho) + B G_l(\eta, \rho)$$

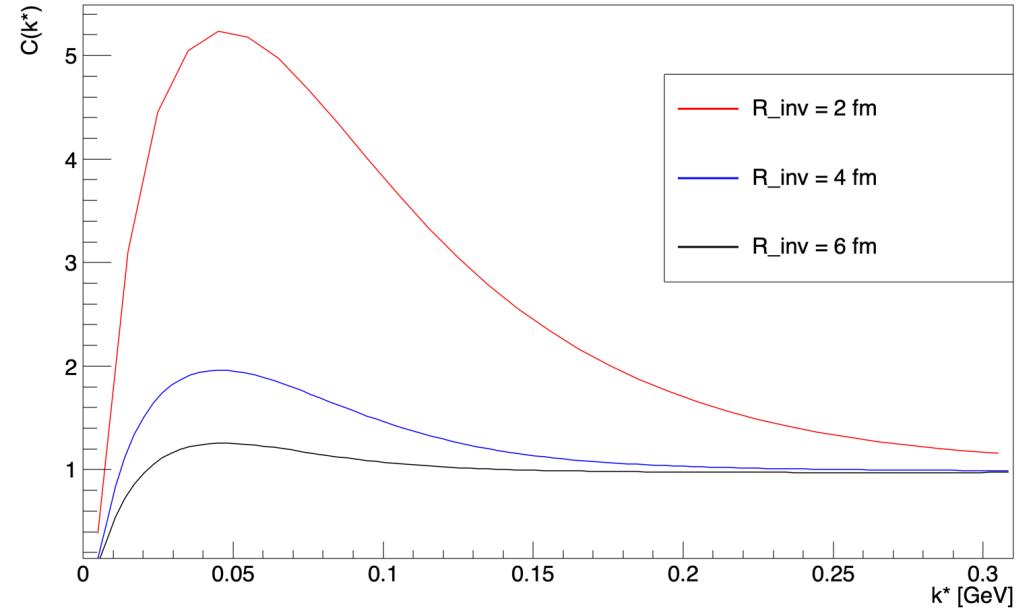
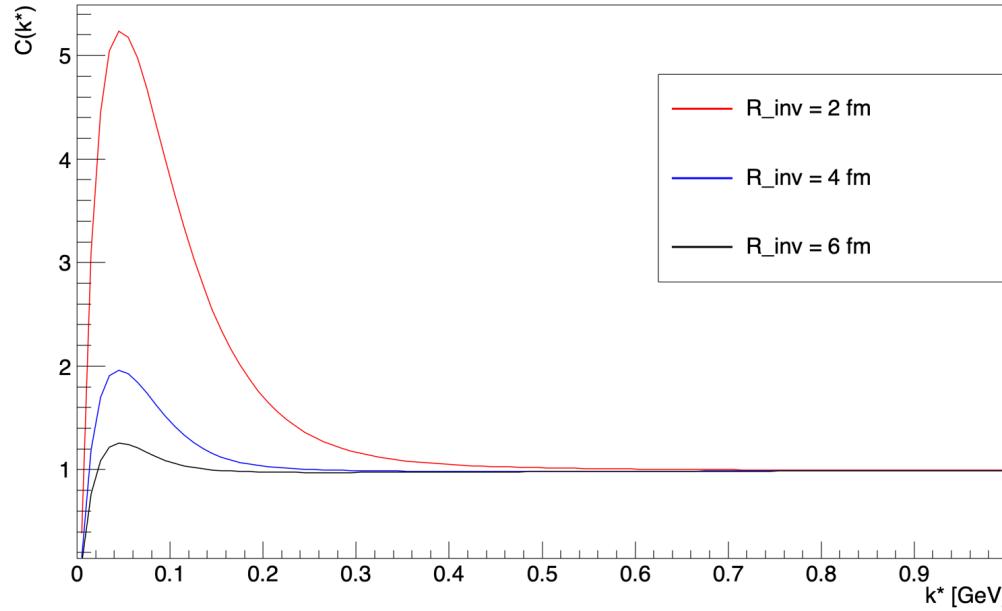
# Wave function (s-wave & small source approximation)

if  $r \ll |a|$ ;  $kr \lesssim 1$

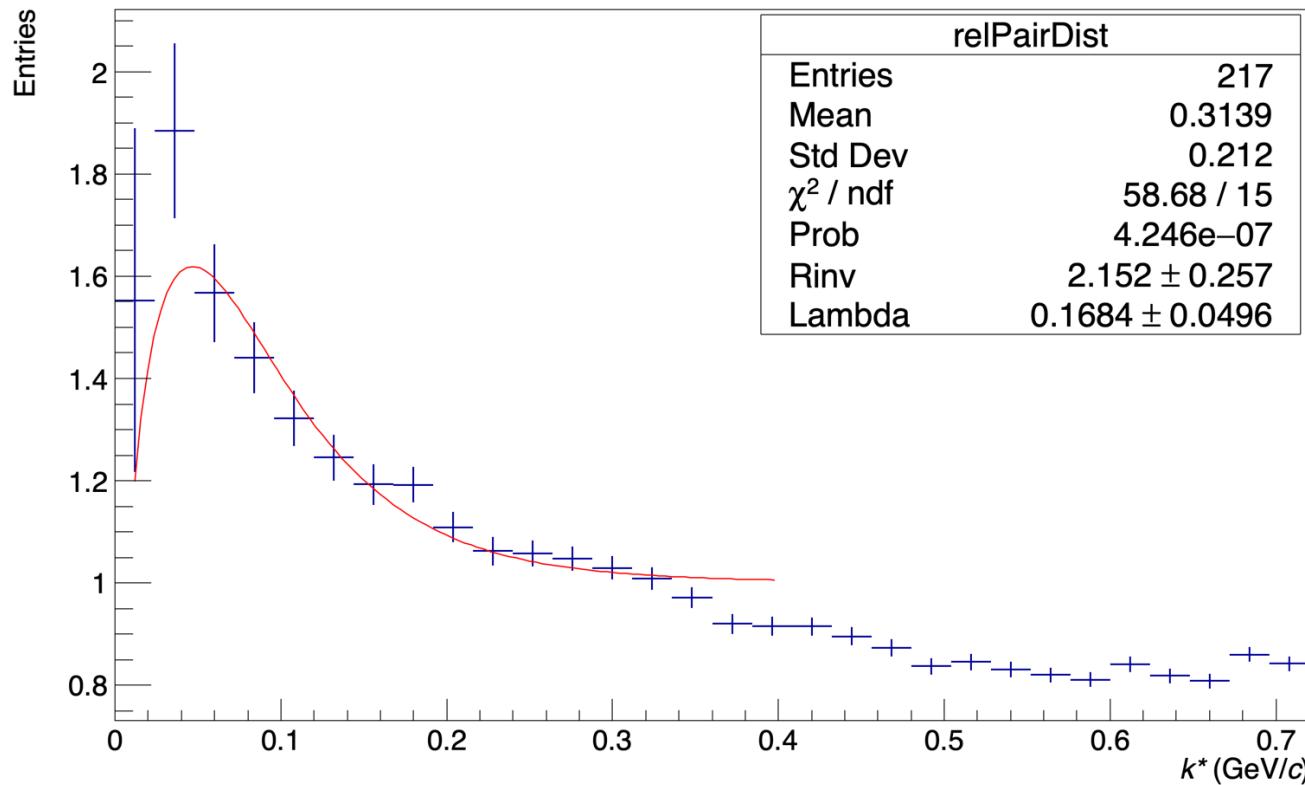
$$\psi_{\vec{k}}(\vec{r}) = e^{i\delta_c(\eta)} \sqrt{A_c(\eta)} \left[ e^{i\vec{k}\vec{r}} + \frac{f(k)}{A_c(\eta)} \frac{\cos(kr) + iA_c(\eta) \sin(kr)}{r} \right]$$

I used this to obtain an analytical expression for fit

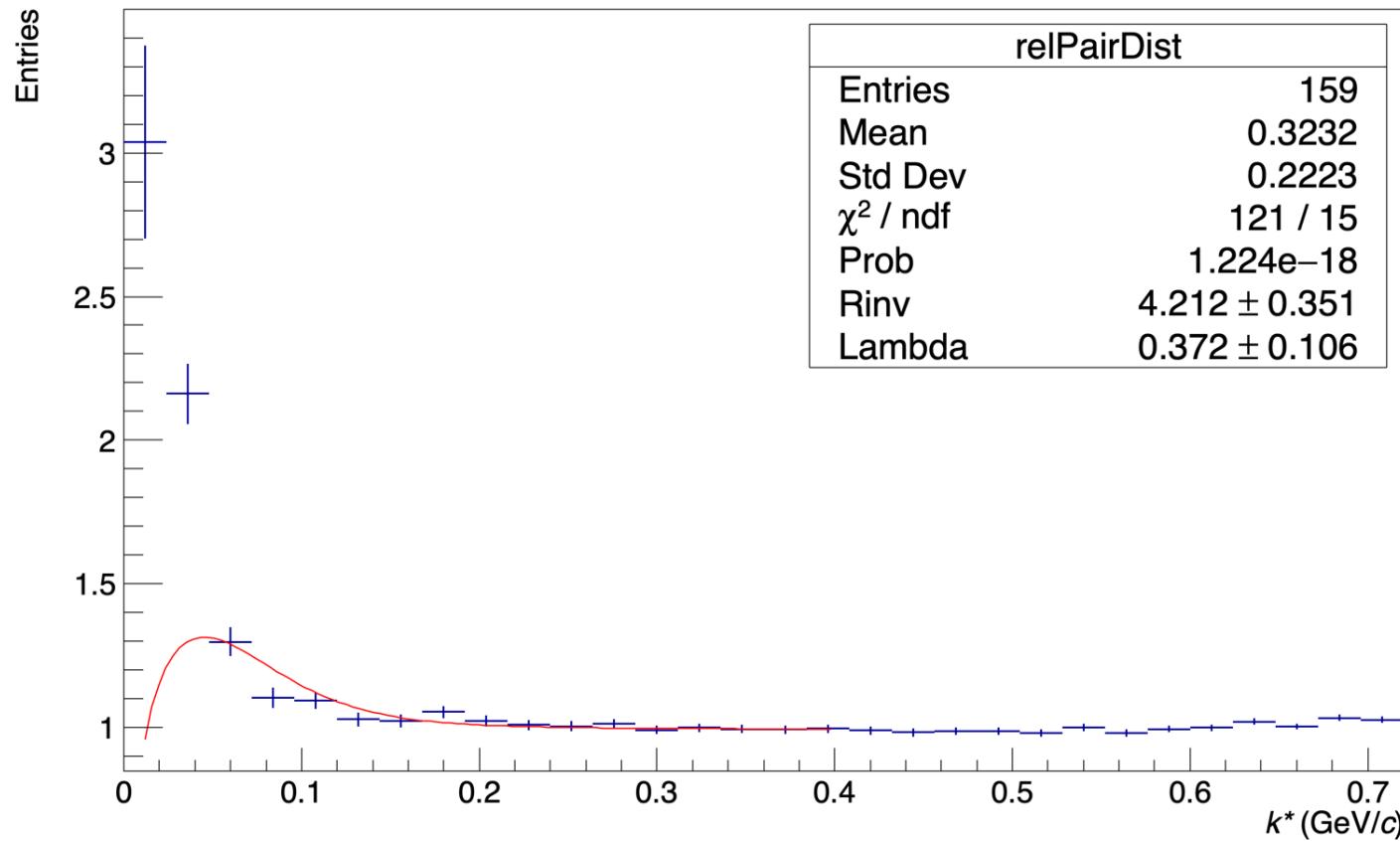
# Result



# Trying to fit (pilot beam 900 GeV)



# Trying to fit (LHC22f\_pass2)



# LHC22f\_pass2 & Pilot beam

