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CaloShowerGAN

A GAN model for fast calorimeter shower simulate in HEP

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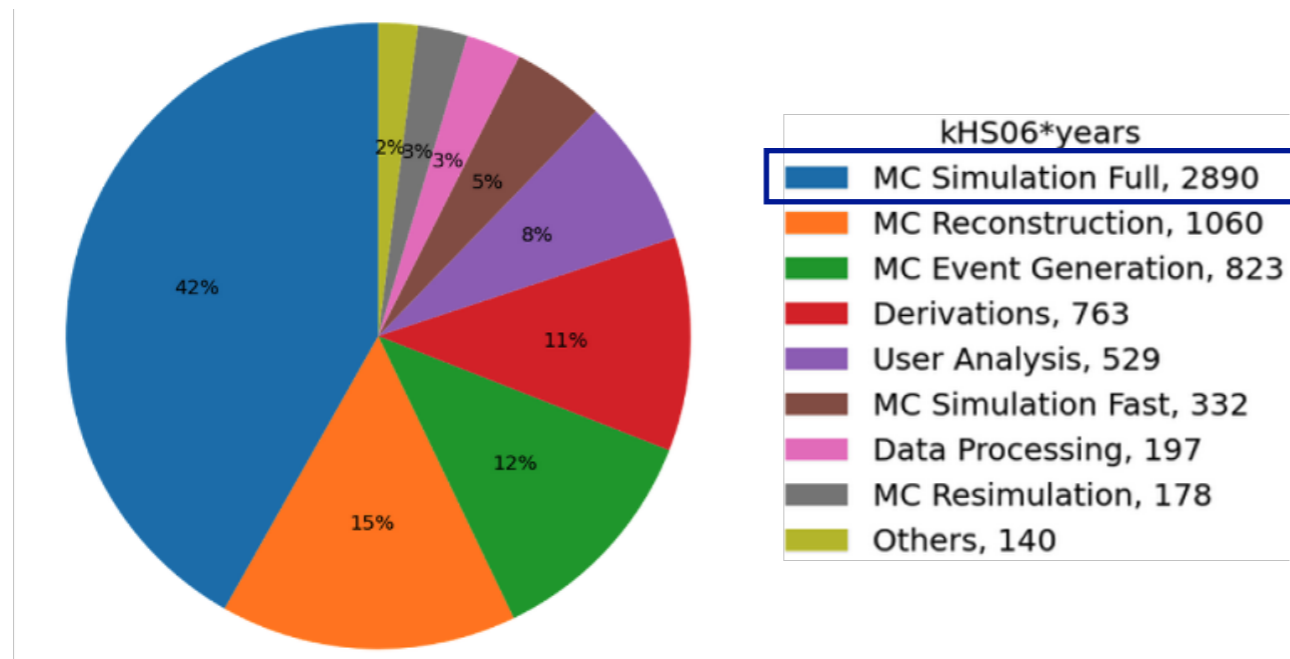
Rui Zhang (Wisconsin)

CaloChallenge Workshop 2023

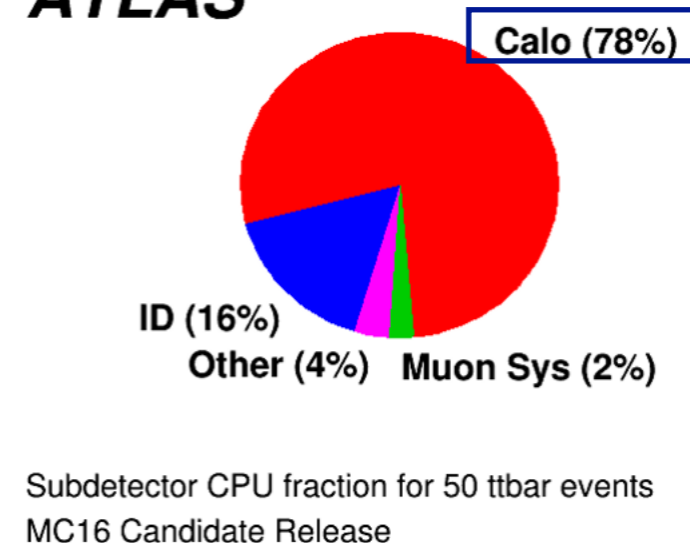
30–31 May 2023, Frascati, Italy

Simulation in HEP

- Monte-Carlo simulation is crucial in understanding and analysing data
 - Simulate interactions happening in calorimeter is time & resource intensive



ATLAS



- Reducing time in calorimeter simulation is the first task to speed up the MC production
- Fast Calorimeter simulation becomes an increasingly essential requirement
 - Generative models assisted calorimeter simulation would be much faster
 - In the meantime, required the generated showers to have high quality and to be as close as with Geant 4

Generative Adversarial Networks (GAN)

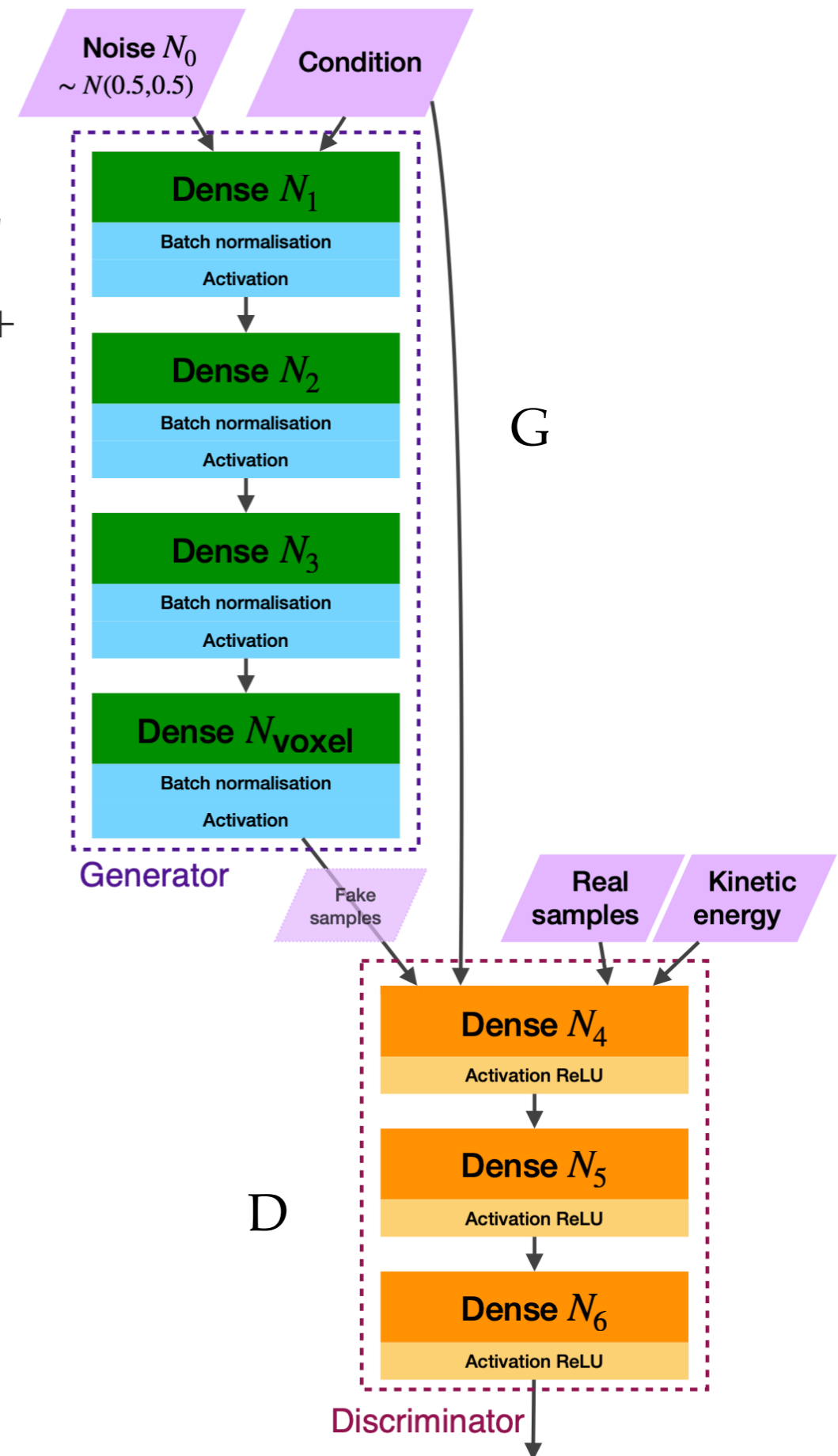
- ◉ GANs are an known approach for **generative models** using deep learning techniques
 - An unsupervised learning task, learn patterns in input dataset and generate new examples that could plausibly have been drawn from the input
- ◉ Training of GANs is framed as supervised learning
 - Two sub-models: the **generator** model is trained to generate new examples and the **discriminator** model is trained to classify examples as either real (from the input) or fake (generated).
 - The two models are trained together in a zero-sum game, until the discriminator model is fooled about half the time, meaning the generator model is generating plausible examples.
- ◉ **Wasserstein GAN** (WGAN) is a variant that introduces the Wasserstein distance (also known as Earth Mover's distance) as a new metric
 - Improved training stability; better gradient flow and vanishing gradients; Mode collapse mitigation; More meaningful loss and evaluation metrics

GAN solution for shower simulation

- ◉ **CaloShowerGAN** is proposed in this talk to use WGAN technique for calorimeter shower simulation
- ◉ It is conditioned by the incident kinetic energy of the particle
- ◉ Will use the Dataset1 from the CaloChallenge [[link](#)] to benchmark
- ◉ Table of Contents:
 - Dataset
 - Model architecture and training
 - Hyperparameter optimisation
 - Model performance
 - Investigation of energy split
 - Summary

CaloShowerGAN

- Generator: 3 hidden layer + 1 output layer
 - Each layer: a dense layer + batch normalisation + activation
 - Consume a noise vector of multi-dimensional Gaussian (mean=0.5, std=0.5)
 - Condition on particle kinetic energy to train/generate
- Discriminator: 3 hidden layer + 1 output layer
 - Each layer: a dense layer + activation (ReLU)
 - Batch normalisation does not help in performance
- Above are common for all particles



Data preprocessing

- ◉ Input values are energies, normalised by the true incident energy
 - After normalisation, all values in the input are in the same order of magnitude and dimensionless
- ◉ Condition label of kinetic energy is normalised to $[0, 1]$ using
 - $$\hat{E} = \frac{\log \frac{E_{\text{kin}}}{E_{\text{min}}}}{\log \frac{E_{\text{max}}}{E_{\text{min}}}}$$
 - Motivated by the expectation that the shower width is logarithmically dependent on the kinetic energy of the incoming particle
- ◉ Removing too low values in training vector
 - It is found not improving or undermining the numerical stability, therefore is not used in the results
- ◉ Normalisation depending on incident energy
 - It is found not improving the performance, therefore is not used in the results

Training

- ◉ Training is done separately for particles (γ , π)
- ◉ Optimiser: Adam
- ◉ Train 1 million iterations and checkpoint models every 1k
- ◉ Evaluated by calculating χ^2 of total energy distributions in all 15 energies between generated and Geant 4 simulated showers
 - A good metric which is non-trivial to produce by output vectors
 - The checkpoint that gives the best is χ^2 will be used

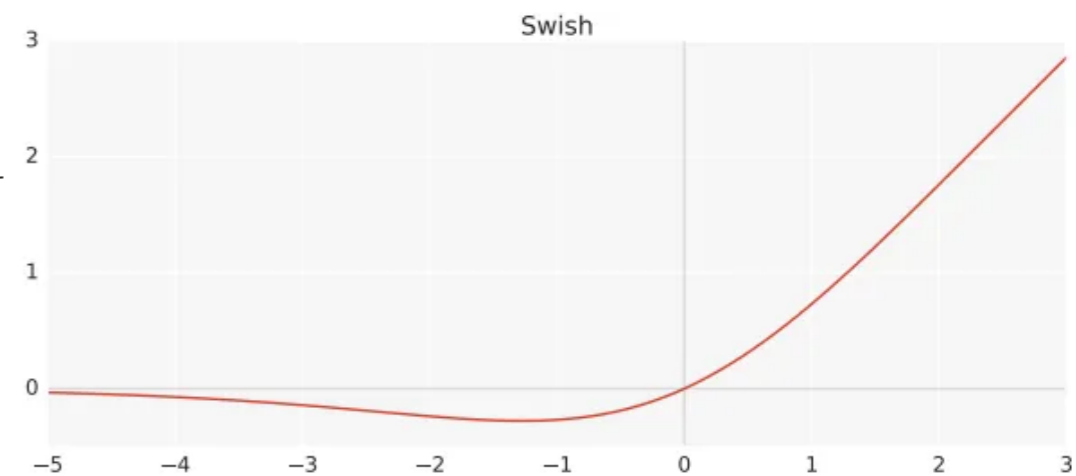
Hyperparameter optimisation

◉ Optimiser

- Learning rate and momentum of both generator and discriminator are tested
- Batch size
- Cyclic learning rate and variant such as RAdam, LookAhead, AdamW do not help

◉ Activation

- Con of Swish: seems to be less stable than ReLU
- Swish in γ G is helpful while ReLU is good in other situations
- More powerful when paring with Glorot Normal initialisation of neuron weights
 - ReLU is best to use with He Uniform



◉ GAN parameters

- D/G ratio: number of training passes of D for each pass of G (always > 1 since < 1 do not offer advantage)
- λ that controls the penalty contribution

Final model hyperparameters

| Hyperparameter | Photon | Pion |
|---|--------------------|--------------------|
| Generator size (N_0, N_1, N_2, N_3) | 100, 100, 200, 400 | 200, 200, 400, 800 |
| Discriminator size (N_4, N_5, N_6) | 368, 368, 368 | 800, 400, 200 |
| Generator optimiser | Adam | Adam |
| Learning rate | 1×10^{-4} | 1×10^{-4} |
| β_1 | 0.5 | 0.5 |
| β_2 | 0.999 | 0.999 |
| Discriminator optimiser | Adam | Adam |
| Learning rate | 1×10^{-4} | 1×10^{-4} |
| β_1 | 0.9 | 0.5 |
| β_2 | 0.999 | 0.999 |
| Batch size | 1024 | 1024 |
| D/G ratio | 8 | 5 |
| λ | 3 | 20 |
| Activation | Swish | ReLU |
| Neuron weight initialisation (generator) | Glorot Normal | He Uniform |
| Neuron weight initialisation (discriminator) | He Uniform | He Uniform |
| Trainable parameters (generator, discriminator) | 261k, 408k | 871k, 829k |

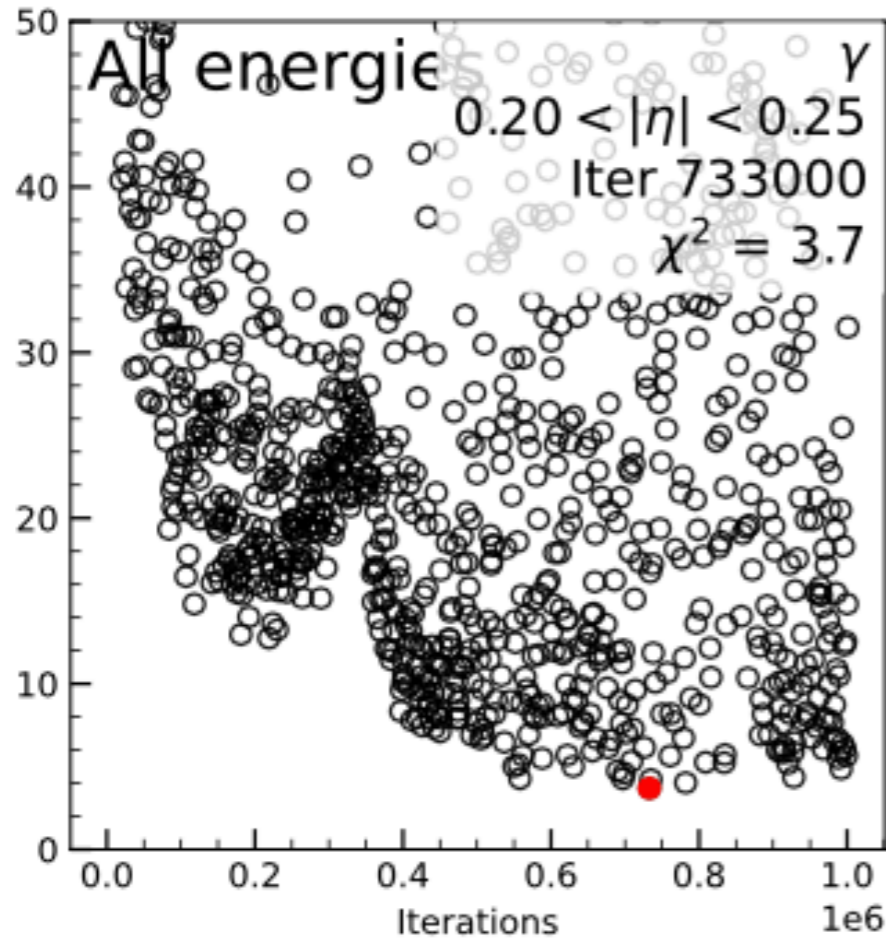
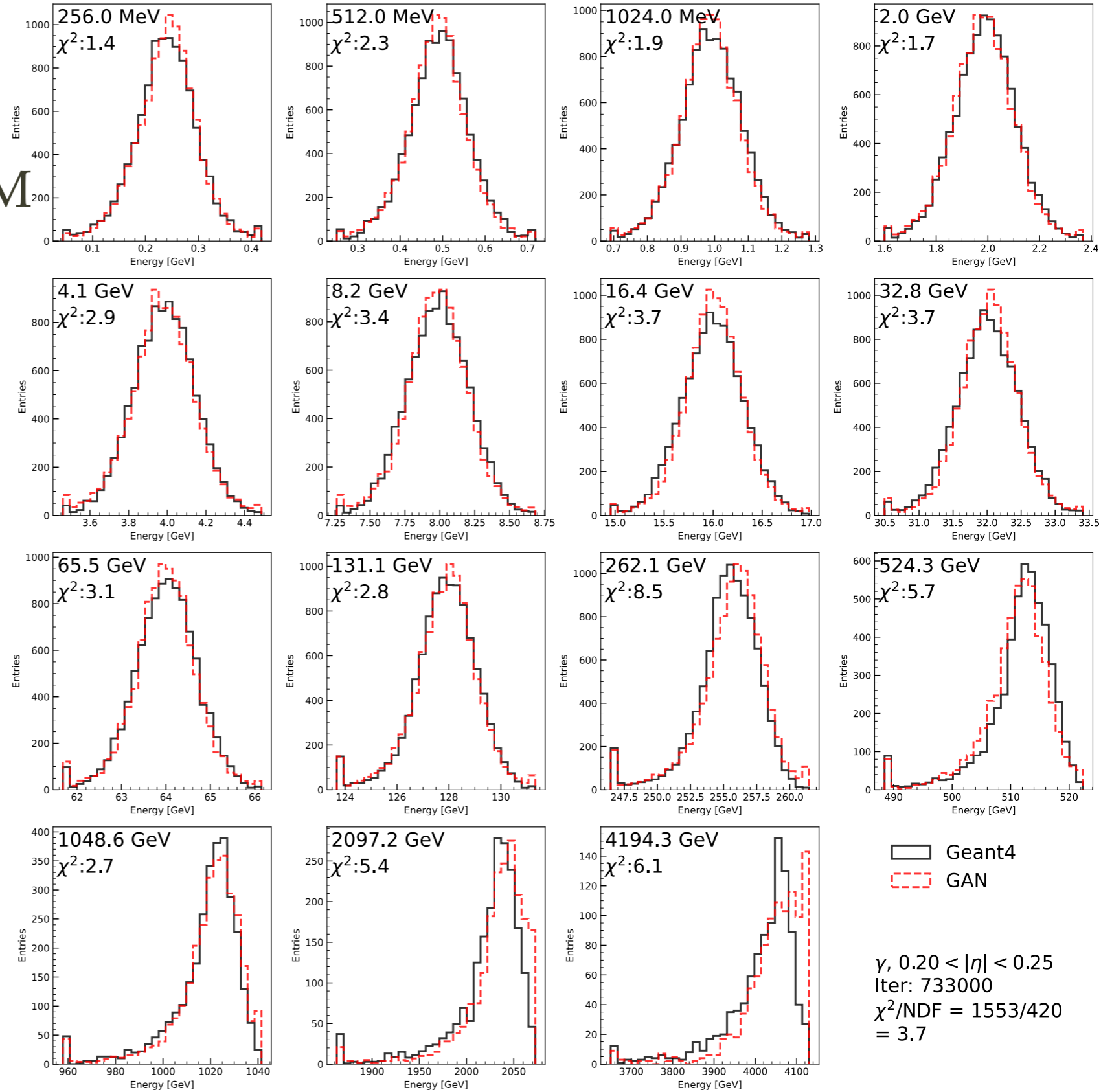
- Pion GAN is larger due to more number of voxels

Photon CaloShowerGAN result

Total energy γ

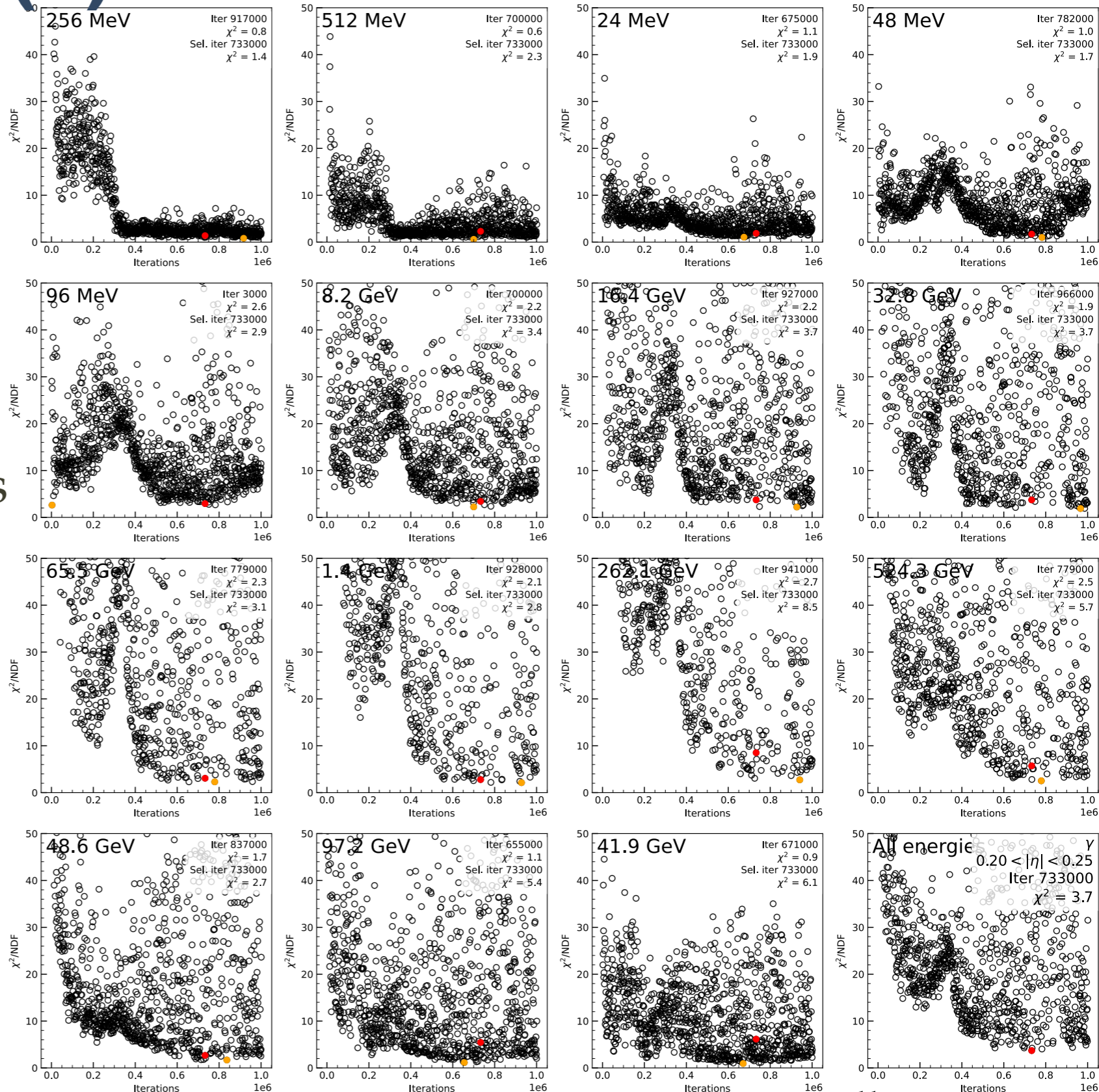
- $\chi^2 = 3.7$

- A structure in χ^2 at $\sim 0.3M$ iteration



Total energy γ (2)

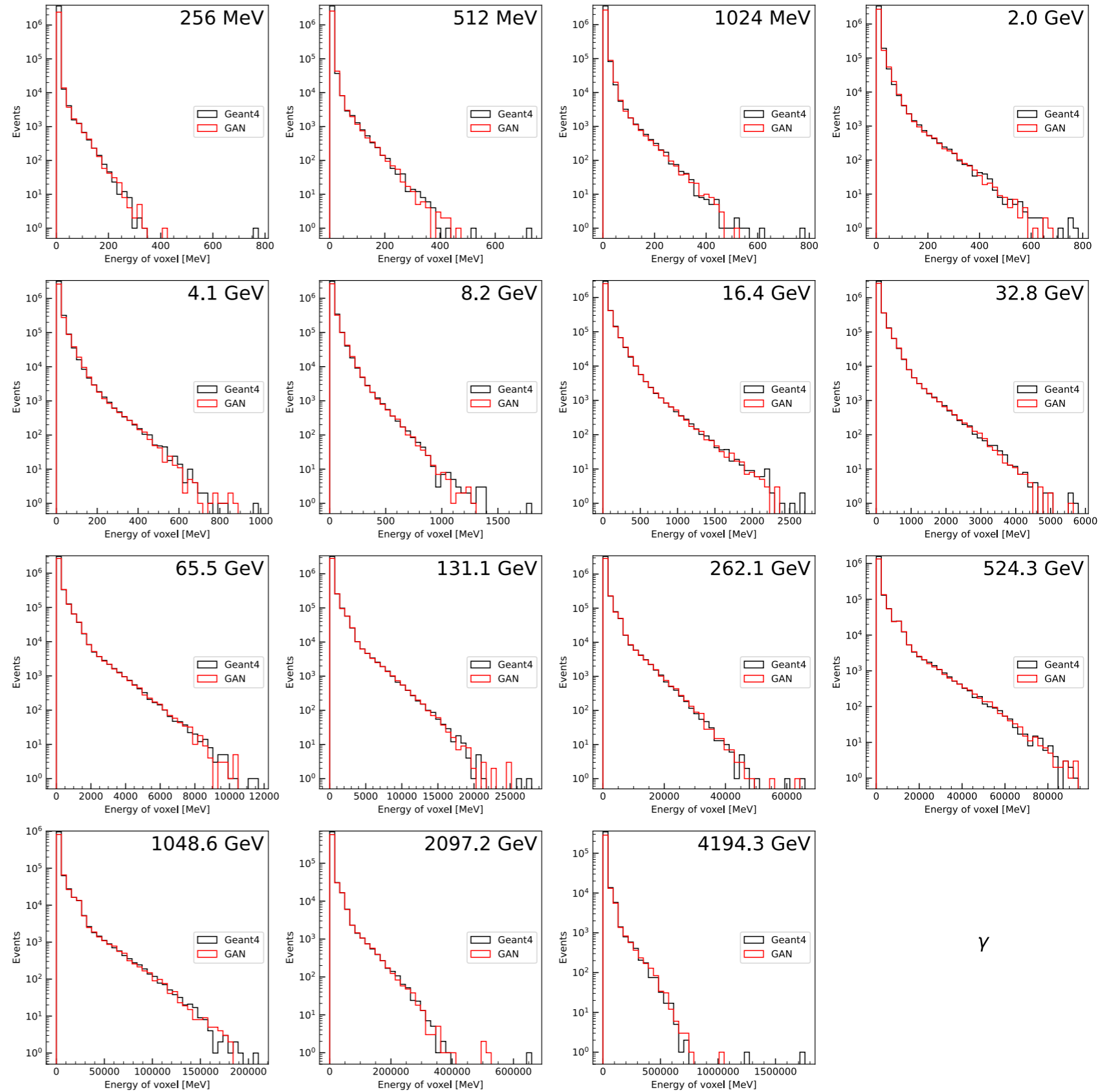
- $\chi^2 = 3.7$
- The global best model performs worse in some energies
- 0.3M iter structure persist in all low energies
- Some energies do not perform well, eg 96 MeV



All energies

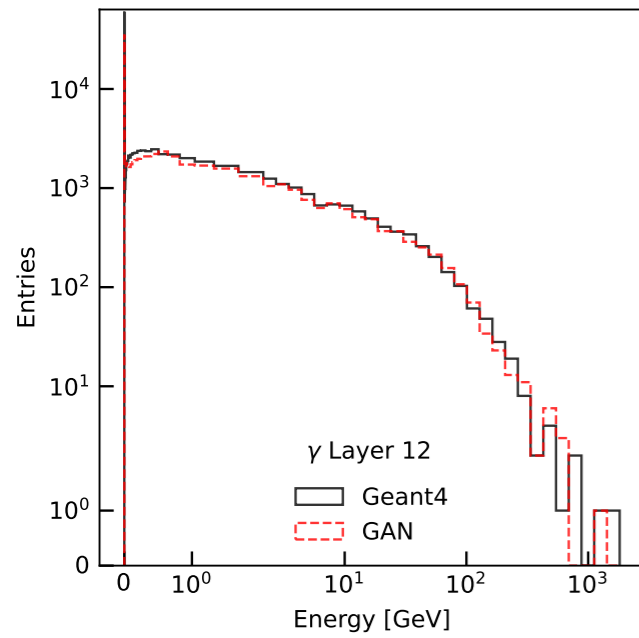
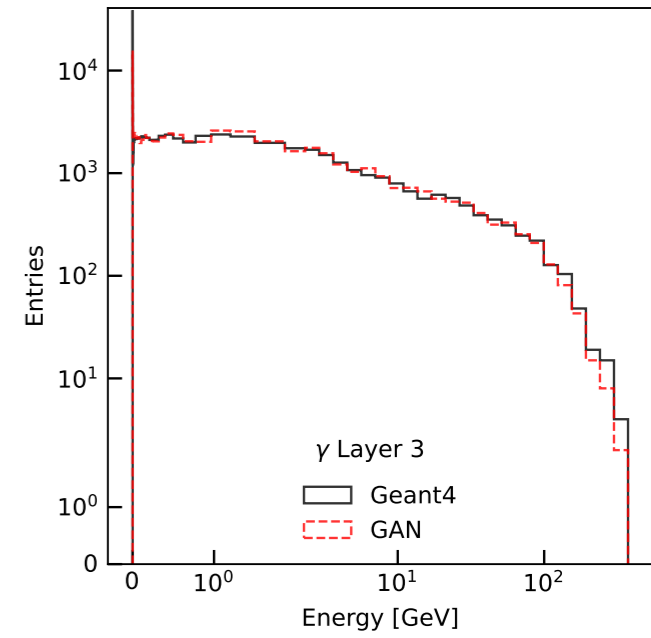
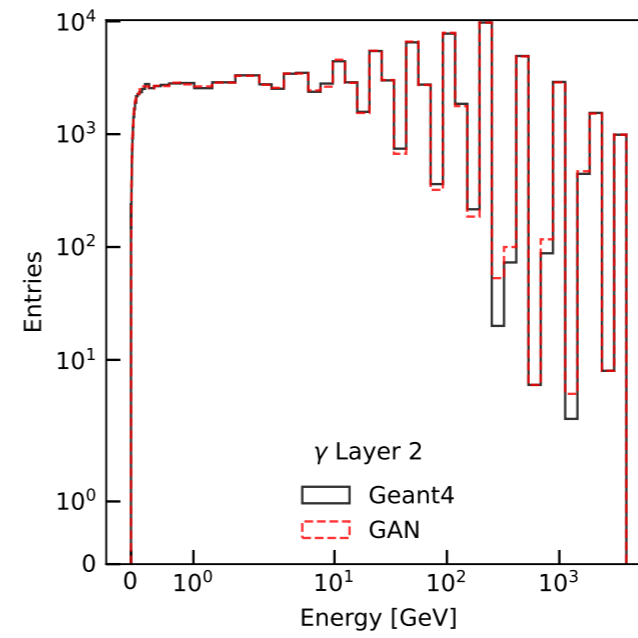
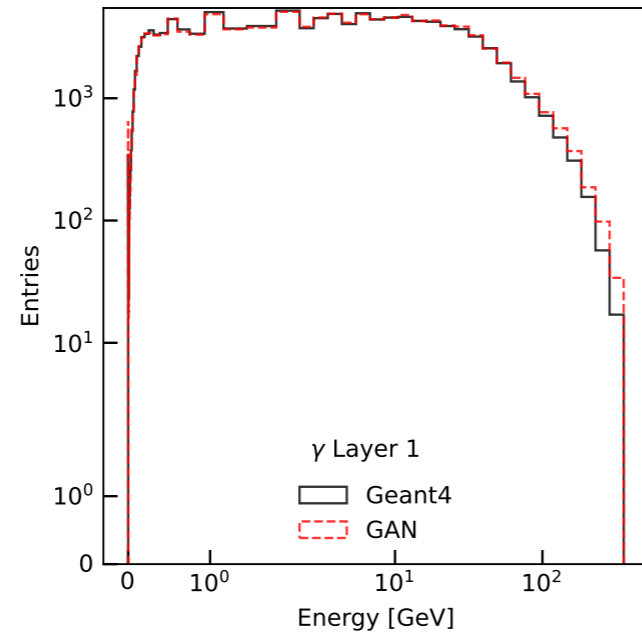
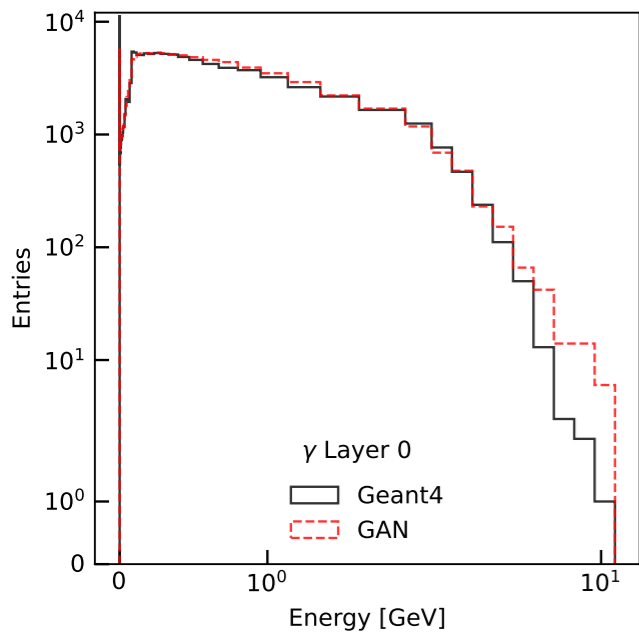
Voxel energy γ

- CaloShowerGAN can reproduce voxel energy distributions



γ

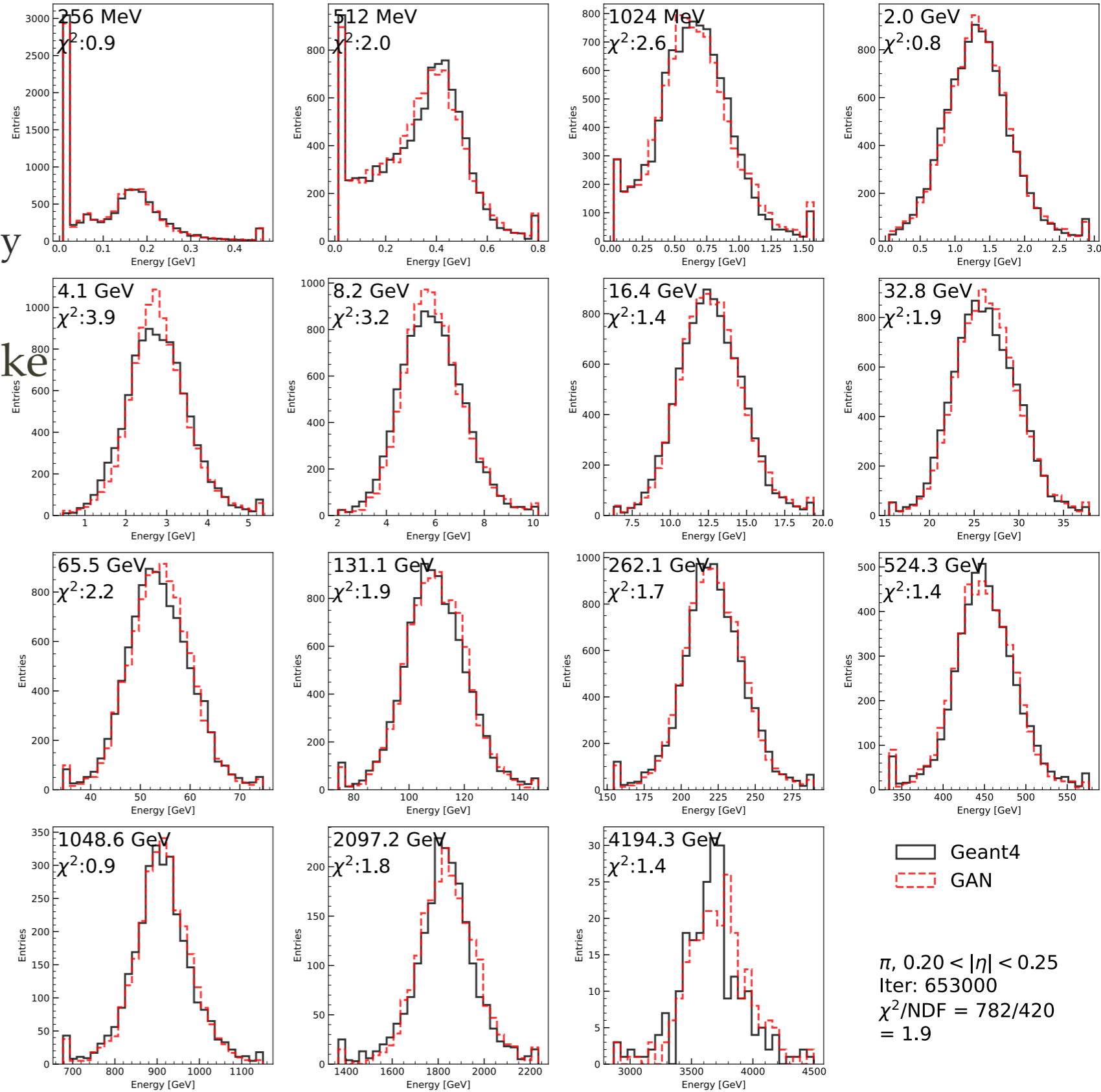
Layer energy γ



Pion CaloShowerGAN result

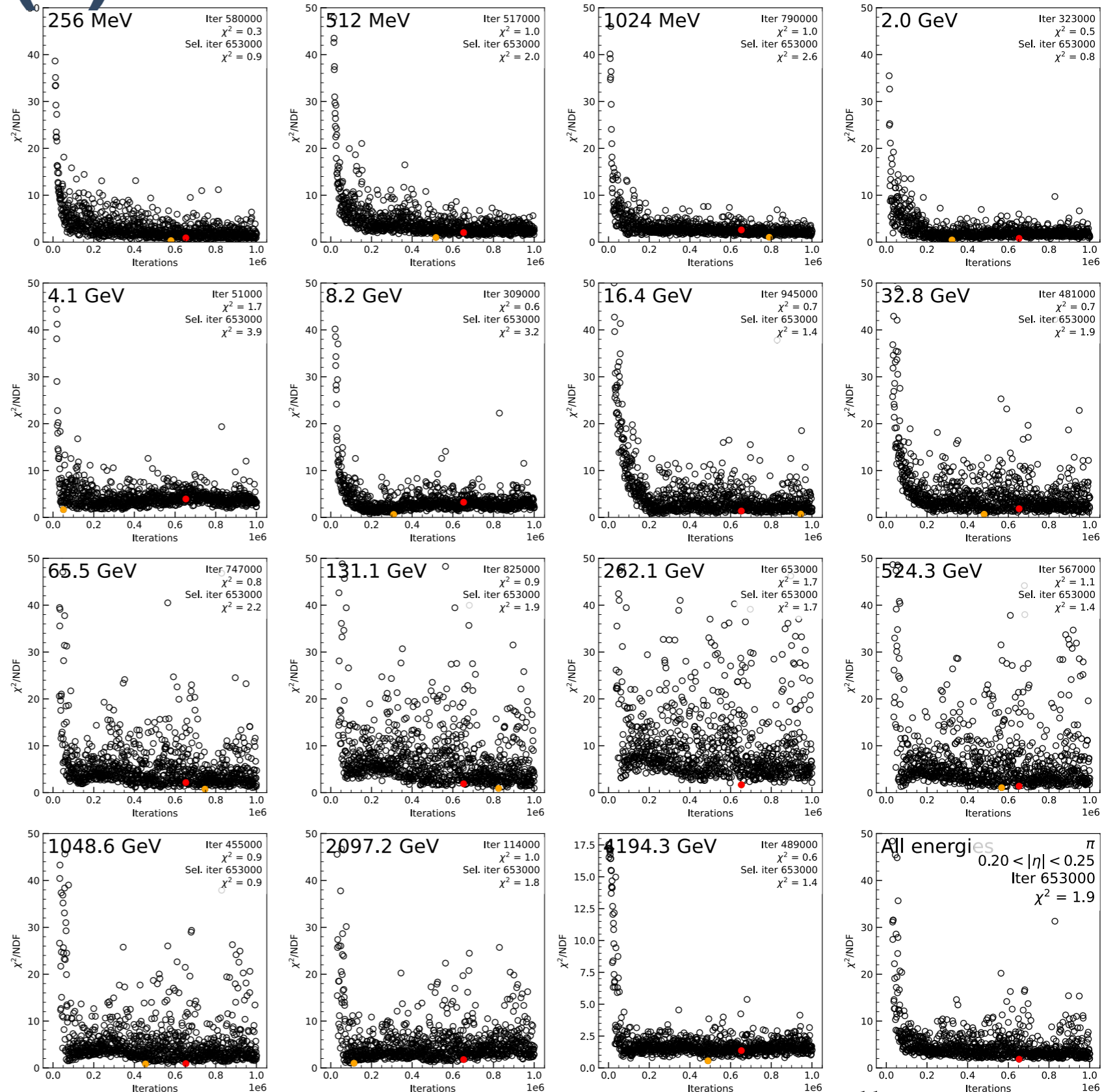
Total energy π

- $\chi^2 = 1.9$
- Training is fast and stable
 - Plateau around 0.2M and slowly improve until 0.6M
- Can produce low energy spike



Total energy π (2)

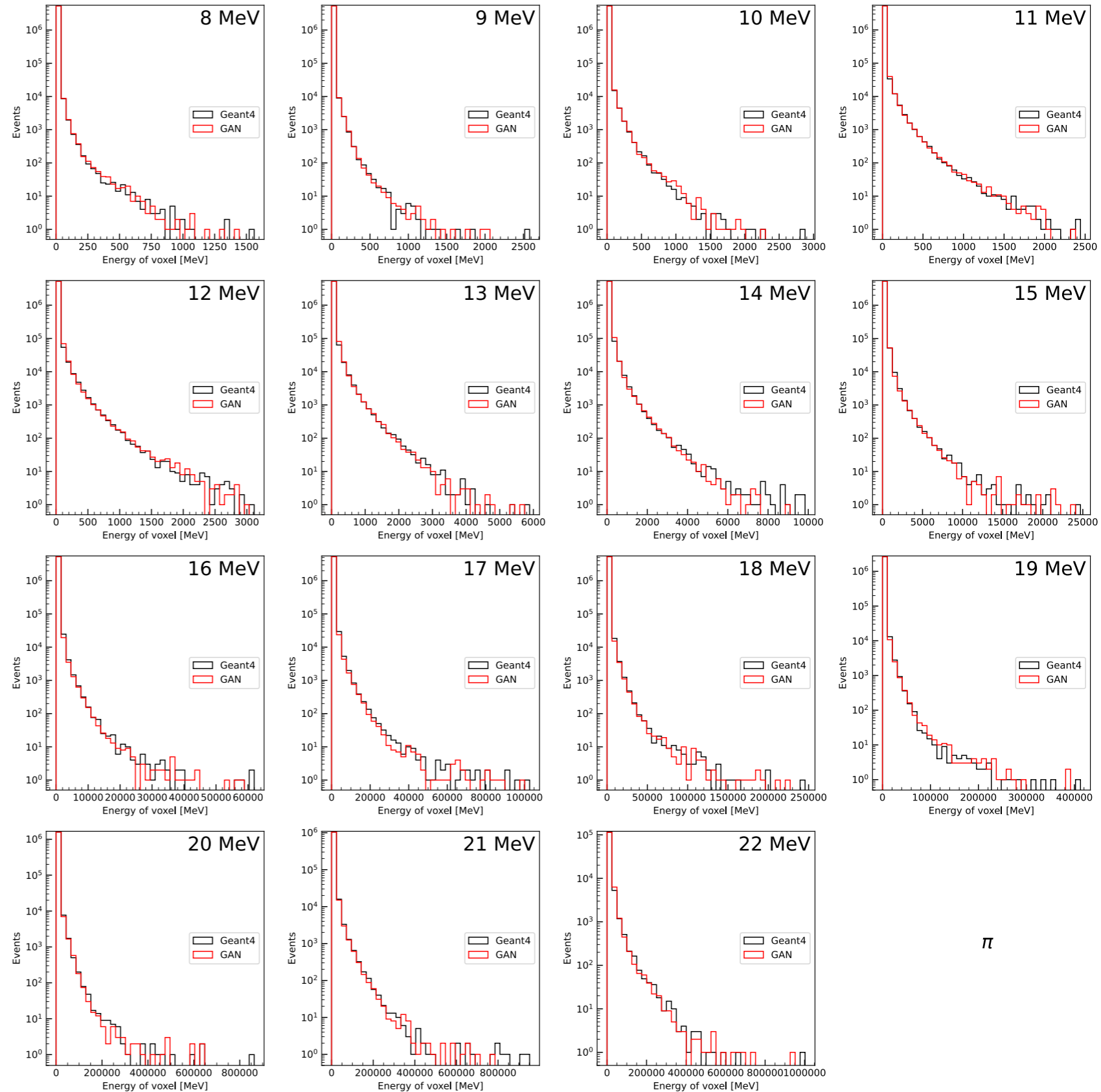
- $\chi^2 = 1.9$
- The global best model performs worse in some energies
- Some energies do not perform well, eg 4.1 GeV and 2.1 TeV



All energies

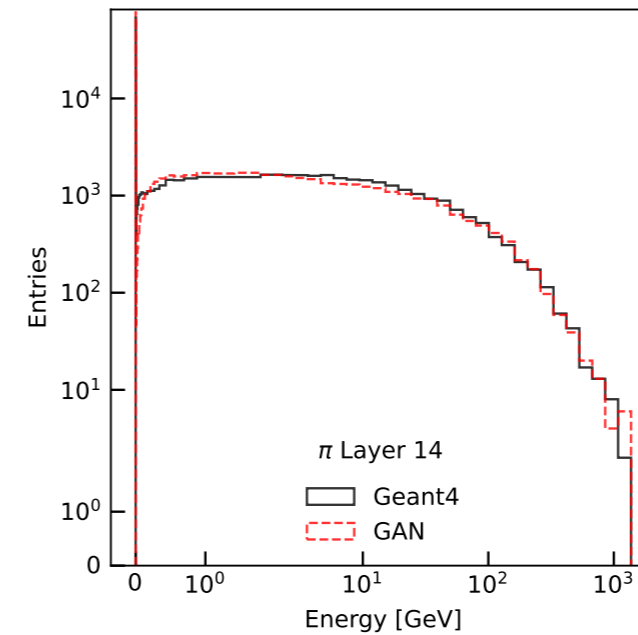
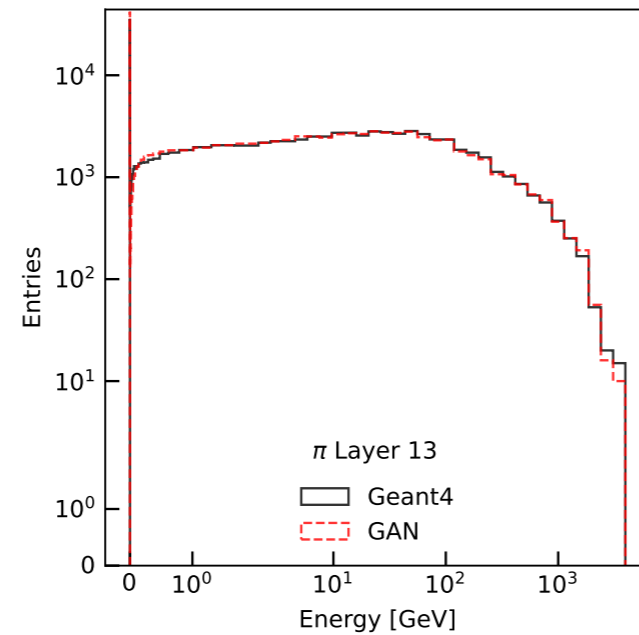
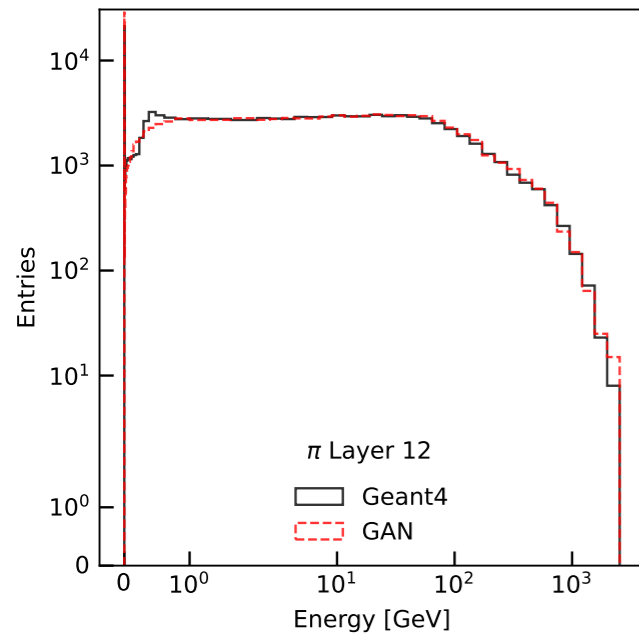
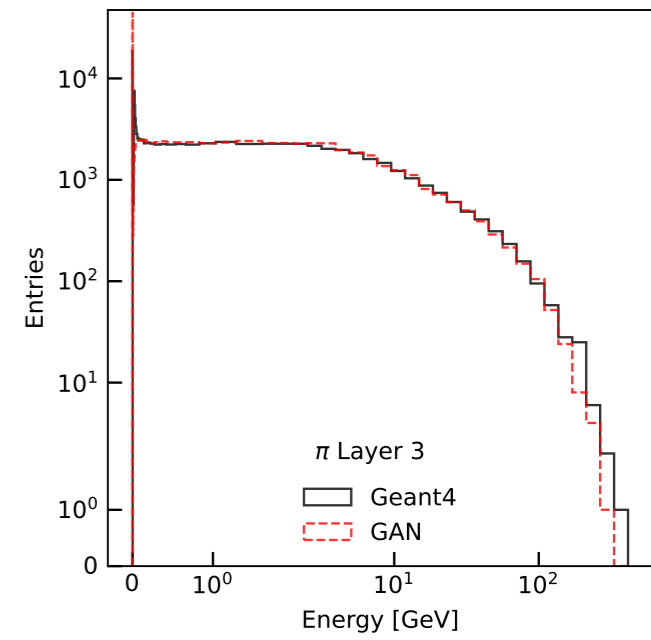
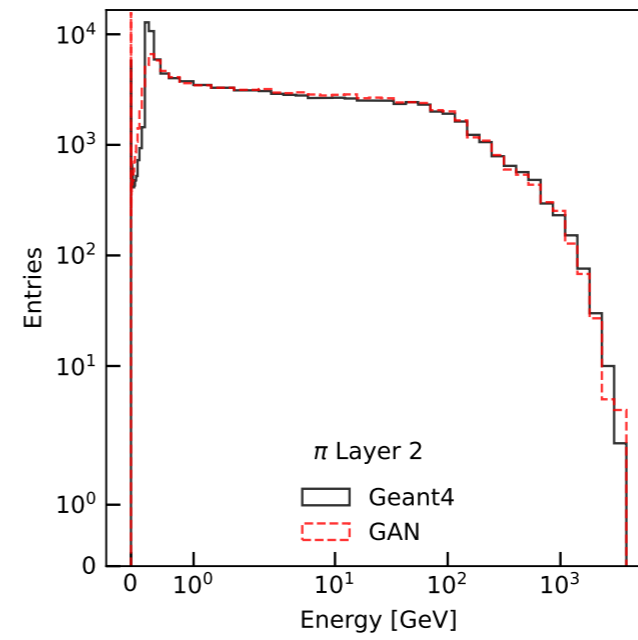
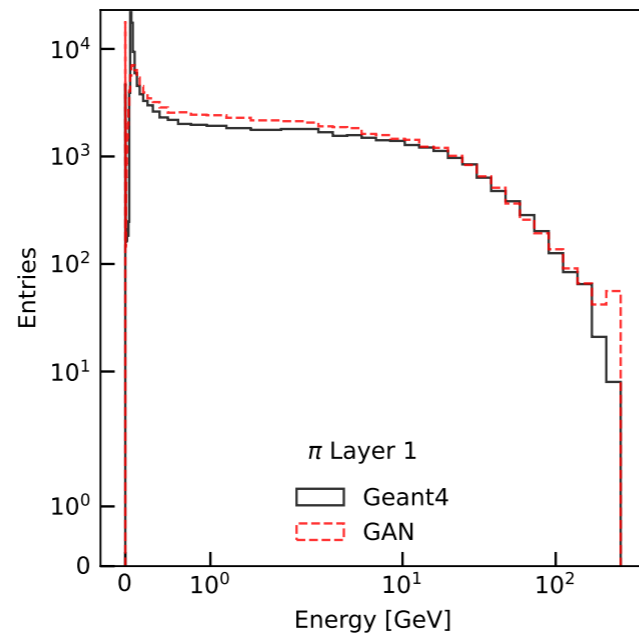
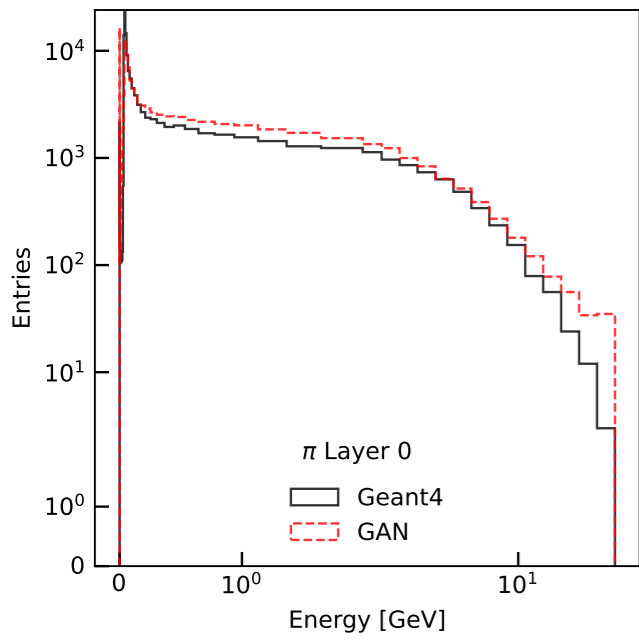
Voxel energy π

- CaloShowerGAN can reproduce voxel energy distributions



π

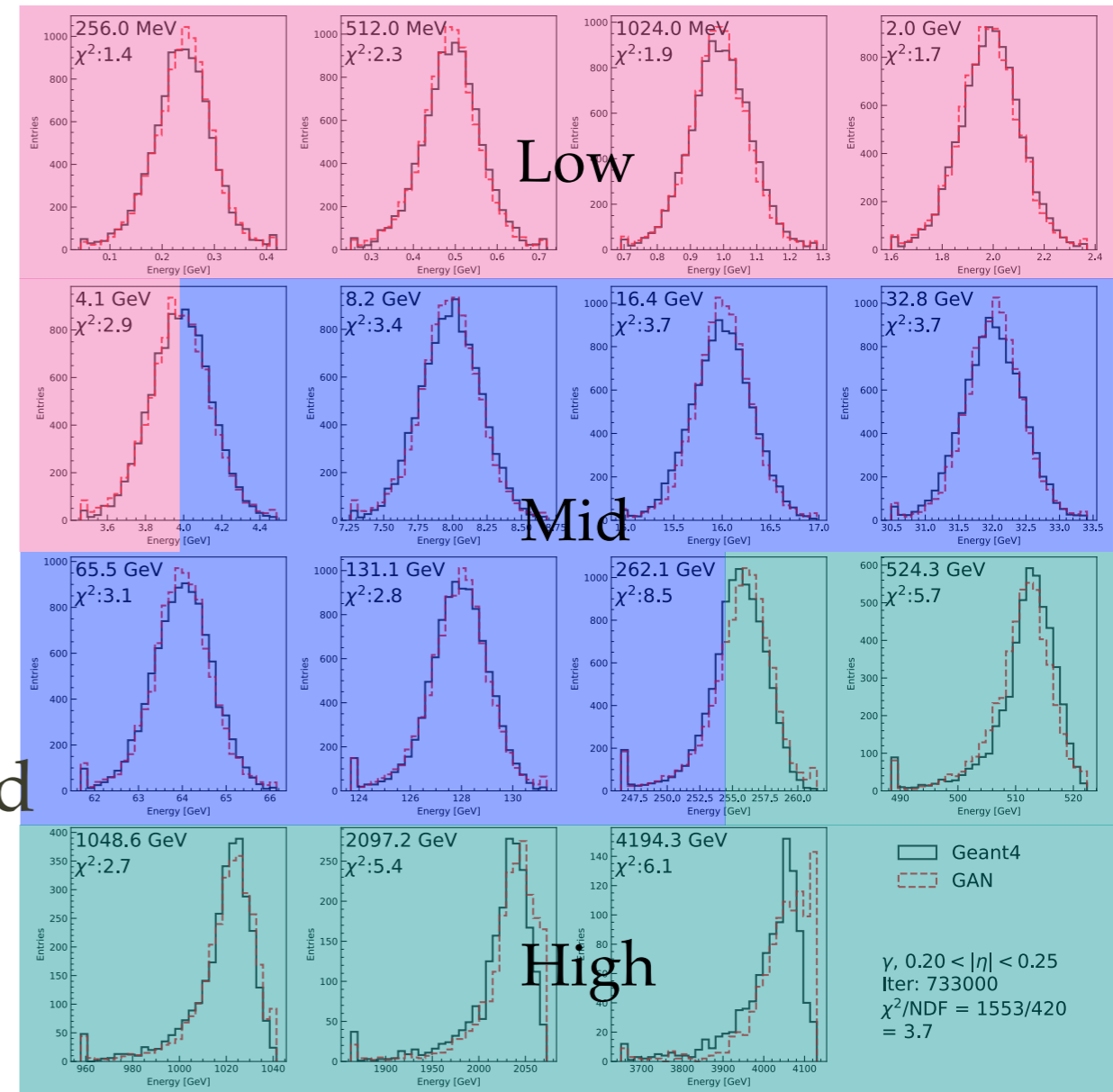
Layer energy π



Energy split — Photon

Energy split in photons

- Low energy and high energy photon responses are quite different
 - May make sense to use different GAN models for low and high energies
- Two scenarios are tested
 - Split at 4.1 GeV — 2 GANs
 - Split at 4.1 GeV and 262 GeV — 3 GANs
- Use the same hyperparameter for Mid and High as the previous photon
- Use ReLU for low instead of Swish



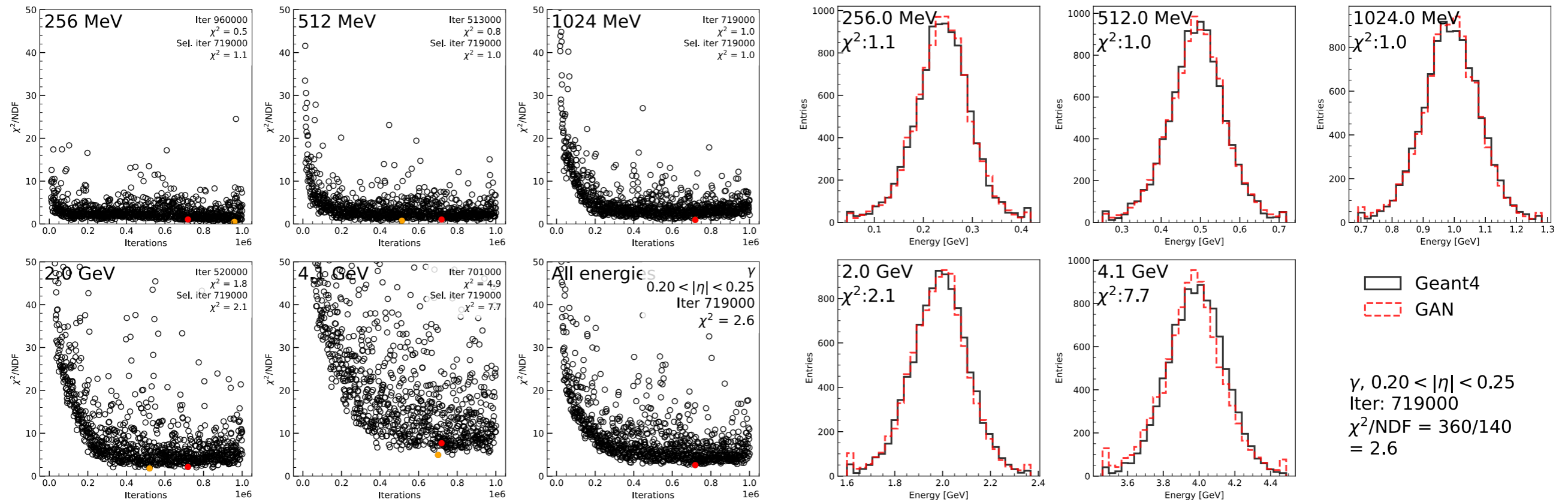
| | 1 GAN | Low | Mid | High | Mid+Hig |
|------------|----------------|--------------|------------------|------|---------|
| G size | 100, 100, 200, | 50, 50, 100, | 50, 50, 100, 200 | | |
| Activation | Swish | ReLU | Swish | | |

Split energy result γ

- χ^2 : 3.7 \rightarrow 3.1 \rightarrow 2.5
- If use 3x larger node in G in 1 GAN, $\chi^2 = 8.2$

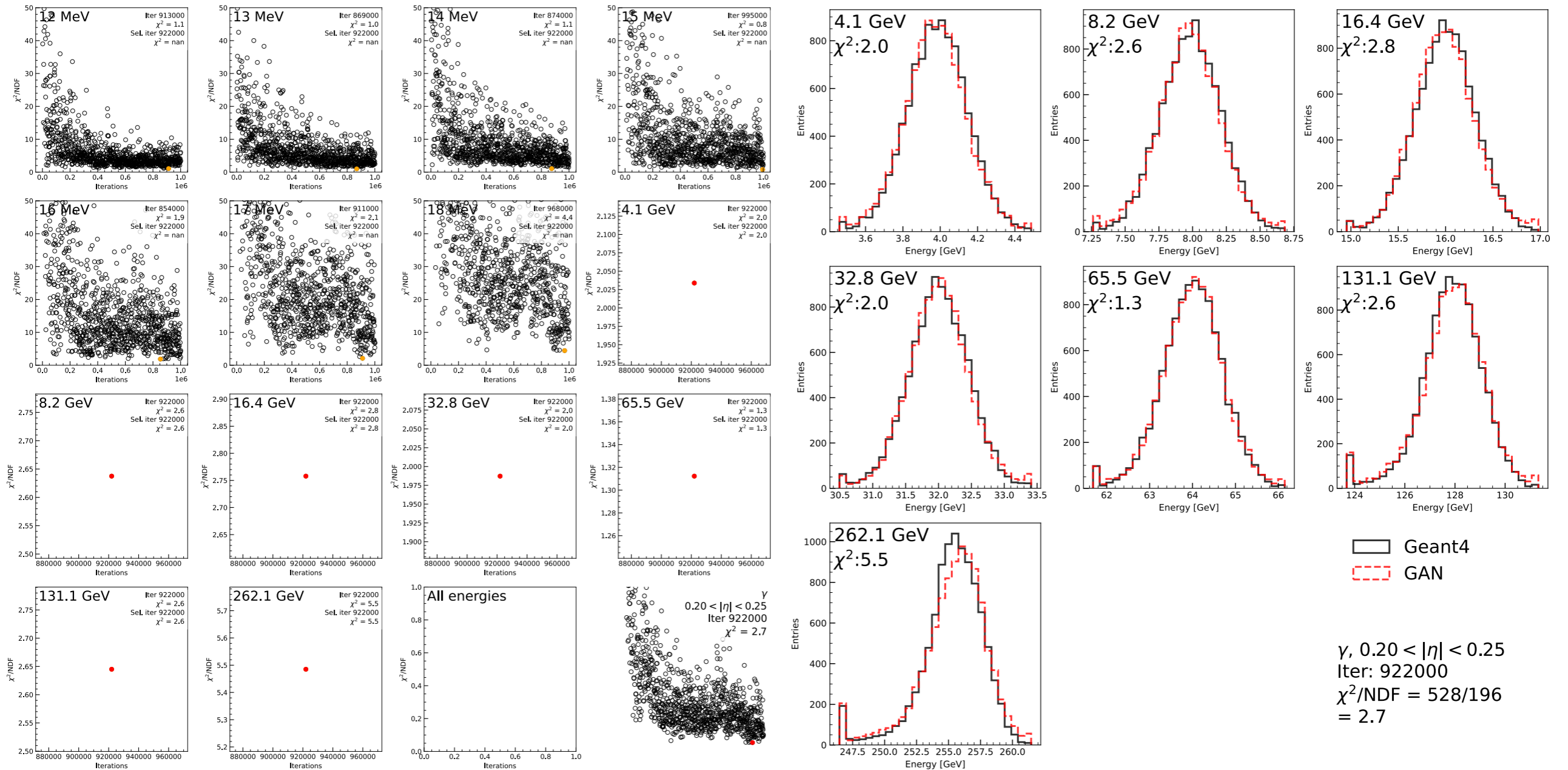
| Energy range | Total χ^2 | NDF | χ^2 /NDF |
|---|----------------|-----|---------------|
| ≤ 4.1 GeV | 360 | 140 | 2.6 |
| ≥ 4.1 GeV | 1042 | 308 | 3.4 |
| 4.1 GeV–262.1 GeV | 528 | 196 | 2.7 |
| ≥ 262.1 GeV | 299 | 140 | 2.1 |
| ≤ 4.1 GeV + ≥ 4.1 GeV | 1402 | 448 | 3.1 |
| ≤ 4.1 GeV + 4.1 GeV–262.1 GeV + ≥ 262.1 GeV | 1187 | 476 | 2.5 |

Low energy γ



● Very good low energy model

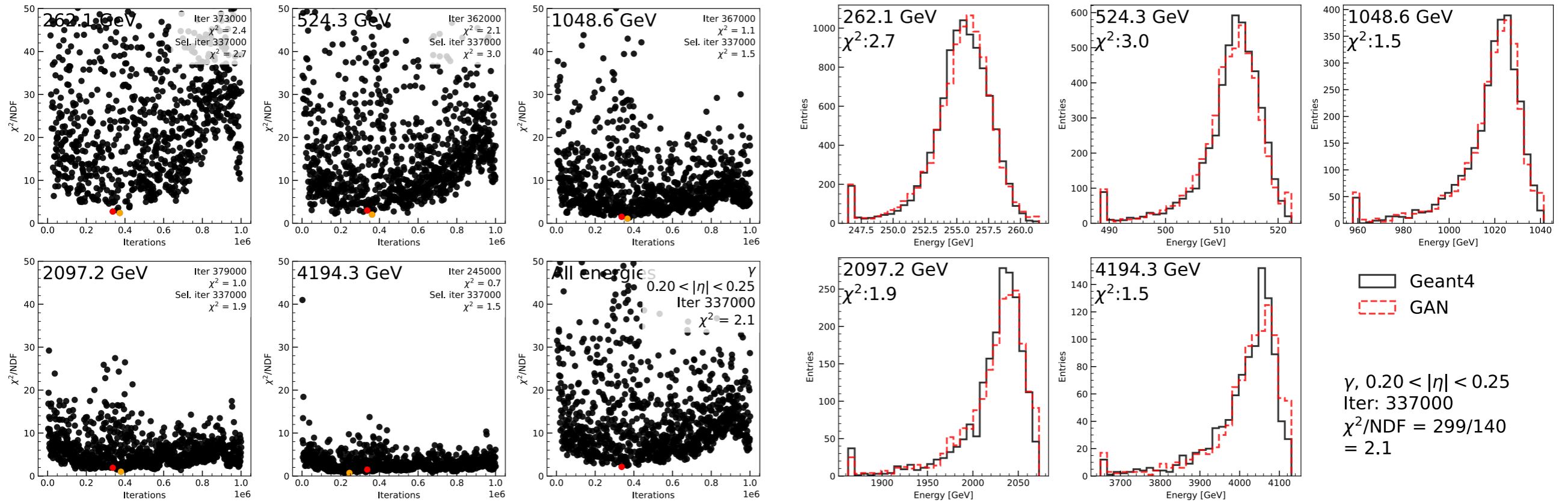
Mid energy γ



Some plotting issue

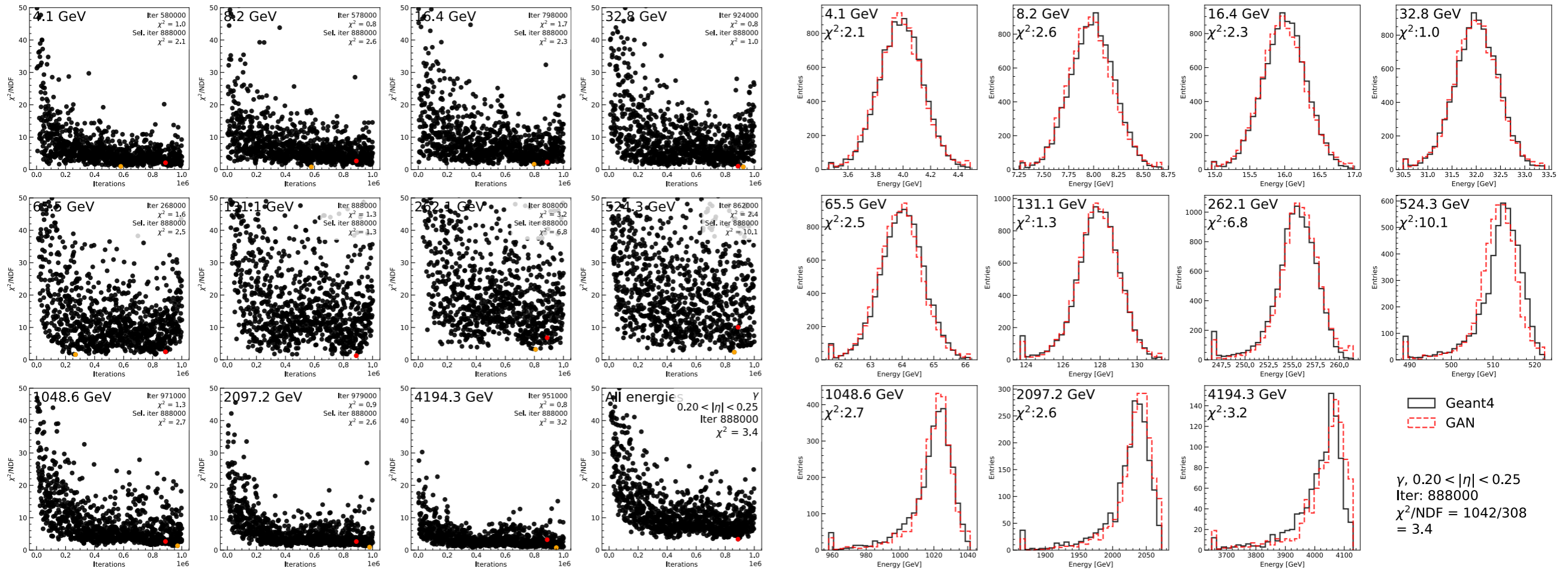
When energy goes high, training becomes unstable

High energy γ



● High energy is most difficult to train

M+H energy γ



Good mid energy training, but χ^2 is still large

Time consumption

| | Training time V100 GPU [s/1k iter] | Inference time Intel(R) Core(TM) i9-9900K CPU @ 3.60GHz [s/training events] |
|-----------------|------------------------------------|---|
| γ 1 GAN | 38 | 0.54/121000 |
| π 1 GAN | 40 | 1.2/120230 |
| γ 2 GANs | 23+22 | 0.54 |
| γ 3 GANs | 23+23+23 | |

Summary

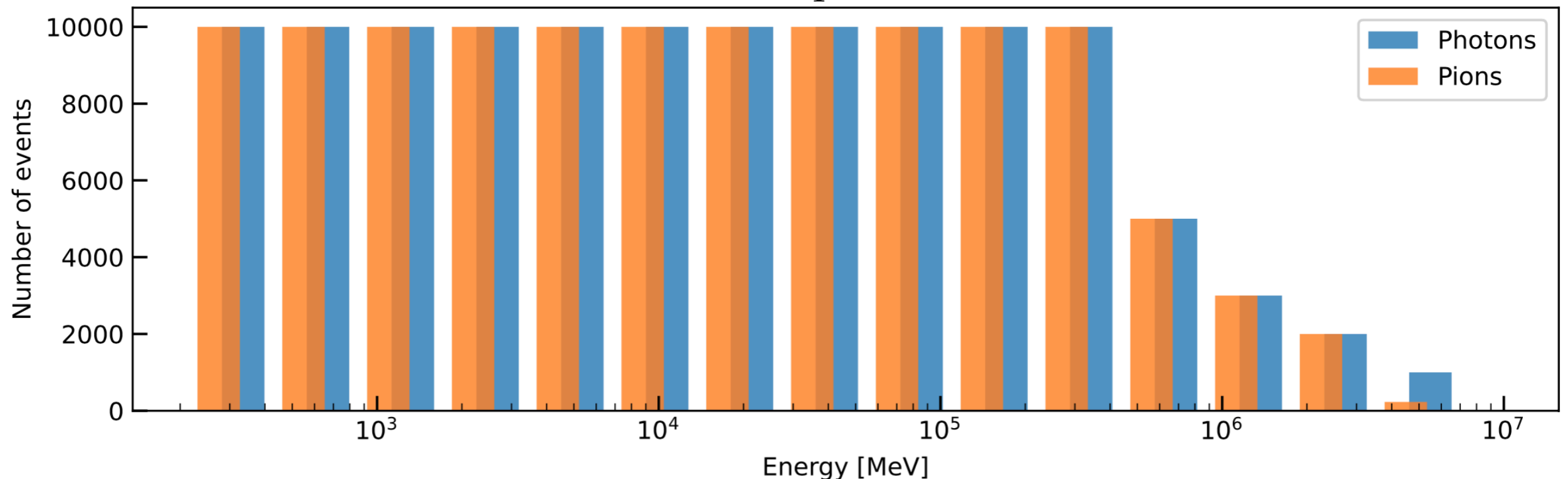
- CaloShowerGAN is proposed in this talk for fast calorimeter simulation
- Used Dataset1 from CaloChallenge to benchmark the performance
- Great π performance: $\chi^2 = 1.9$
- Good γ performance: $\chi^2 = 3.2$
 - Responses in energies are quite different
 - Train separate GANs for different energy range can further improve the performance $\chi^2 = 3.7 \rightarrow 3.1 \rightarrow 2.5$
 - Train a GAN with 3 times the parameters does not achieve the same results!

Backup

Input datasets

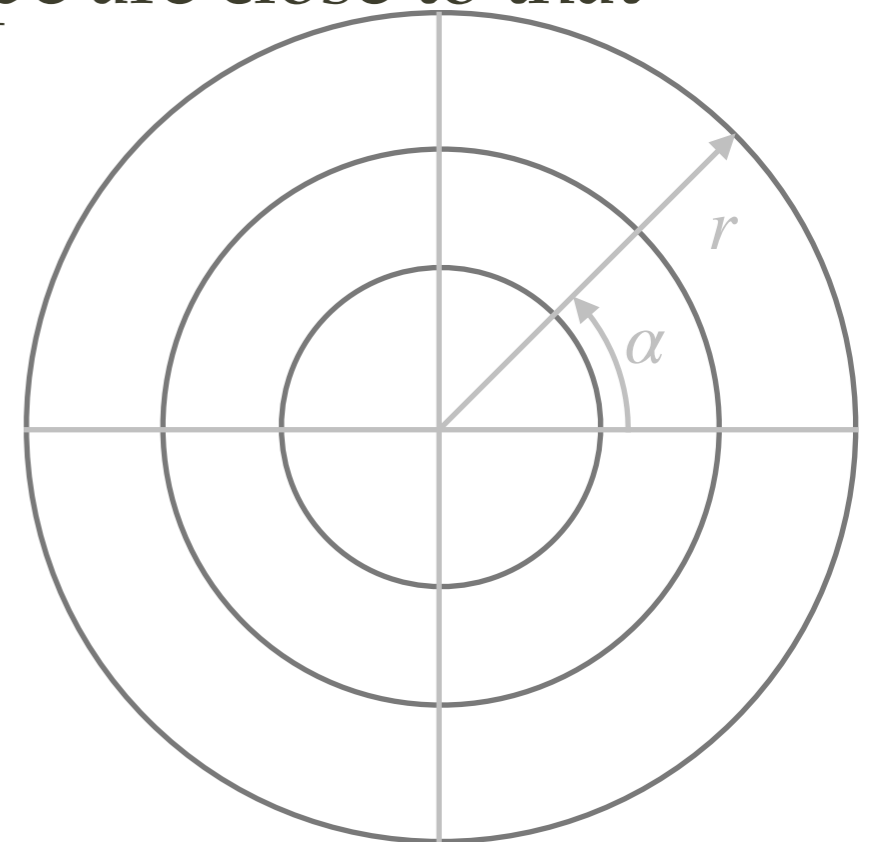
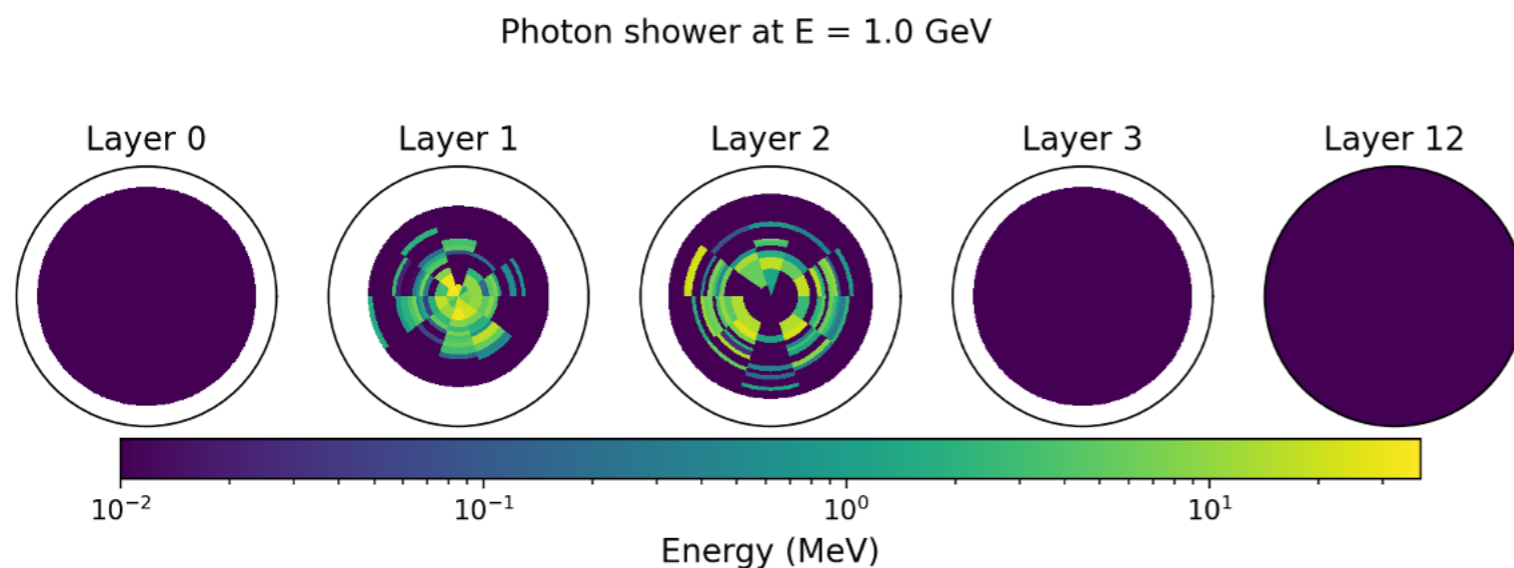
- We used DataSet 1 from CaloChallenge [[link](#)]
 - Known as the ATLAS voxelised data used in [AtlFast3](#)
 - Separate datasets for single particle photons and pions due to their different calorimeter responses
 - Consists of discrete kinetic energies from 256 MeV to 4 TeV
 - Will condition the GANs on kinetic energies to generate showers with different kinetic energies

Statistics of the input datasets



Input datasets (2)

- Data structure of the machine learning task is the deposit energies in a group of calorimeter cells called “Voxels”
- Since responses dependent on the incidental pseudo-rapidity (η), the provided dataset is in a slice of $2.0 < \eta < 2.05$
- For a calorimeter layer, shower shape is transformed into r — α plane
- The task of CaloShowerGAN is to generate numbers in each voxel, such that the shower energy and shower shape are close to that simulate by Giant 4



| Photons | iter x1000 | chi2/ndf | iter x1000 | chi2/ndf |
|-----------------------------|------------|----------|------------|----------|
| swish + he | 524000 | 12.052 | | |
| Goroth | 601000 | 11.15 | 254000 | 6.195 |
| Goroth_DoubleSize | 726000 | 5.413 | 758000 | 3.952 |
| ReLu_DoubleSize | 899000 | 5.566 | 794000 | 3.311 |
| Goroth_DoubleSize_Mask1KeV | 972000 | 6.481 | 808000 | 3.909 |
| Goroth_DoubleSize_Mask10KeV | 867000 | 6.145 | 905000 | 3.587 |
| Goroth_DoubleSize_Mask100eV | 912000 | 5.712 | 610000 | 3.609 |