

# ROTATION SENSORS BASED ON ATOM INTERFEROMETRY

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# Motivation for atom interferometry rotation sensors



Applications in navigation, geodesy, fundamental physics

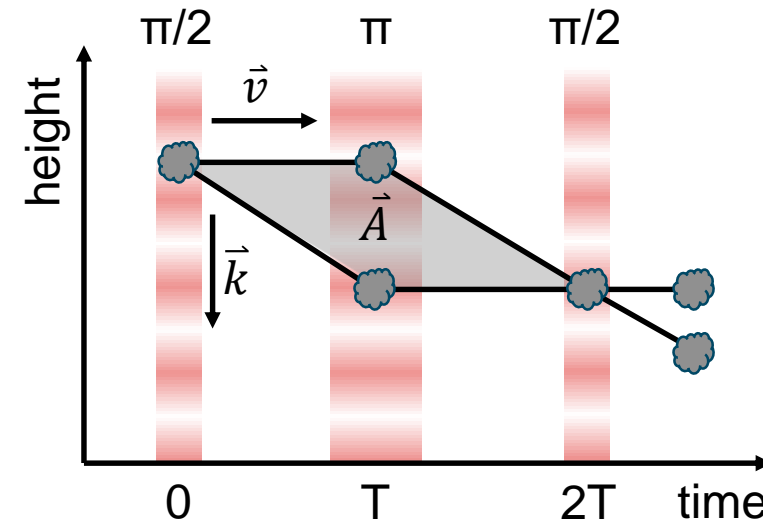
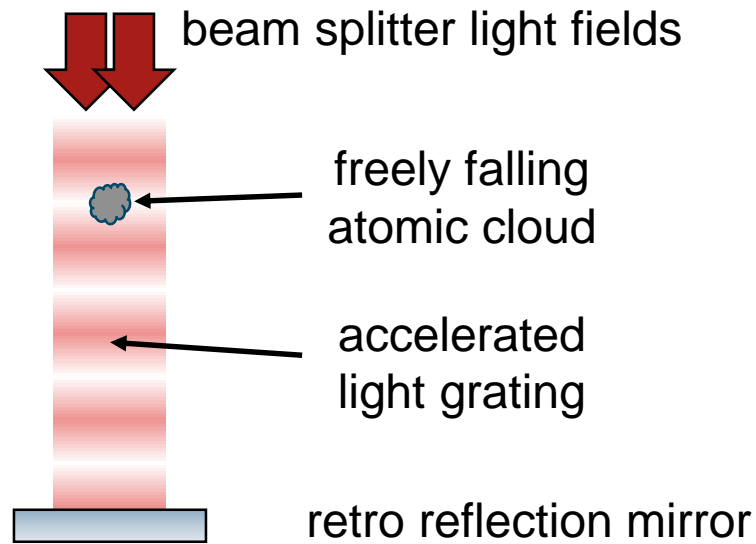
Providing absolute, long-term stable measurements

Complementary to established sensors (MEMS, ring laser gyros, fibre gyros, ...)

Potential for miniaturisation – intermediate sized sensor with high performance

# Atom interferometry

Absolute, stable measurements; atoms in free fall, Mach-Zehnder like  $\pi/2 - \pi - \pi/2$  pulse geometry:



Interferometer phase,  $\phi_i$  imprinted at pulse i:

Acceleration  $\vec{a}$ , effective wave vector  $\vec{k}$ :

Forward drift velocity  $\vec{v}$ , rotation  $\vec{\Omega}$ , enclosed area  $\vec{A}$ :

$$\phi_{tot} = \phi_1 - 2\phi_2 + \phi_3$$

$$\phi_{acc} = \vec{k} \cdot \vec{a} T^2$$

$$\phi_{rot} = 2(\vec{k} \times \vec{v}) \cdot \vec{\Omega} T^2 \sim \vec{A} \cdot \vec{\Omega}$$

# Shot noise limit



3-pulse atom interferometer (AI), Mach-Zehnder like:

$$\sigma_{a,sn} = \frac{1}{C\sqrt{N} \cdot 2 \cdot k \cdot v \cdot T^2} \sqrt{\frac{T_c}{\tau}}$$

C: contrast

N: number of atoms

k: effective wave number

v: drift velocity,  $v \perp k$

T: free evolution time

$T_c$ : cycle time

$\tau$ : integration time

Colder atoms / low expansion rates  $\rightarrow$  increased C, k, T

High flux sources  $\rightarrow$  increased N, decreased  $T_c$

}  $\rightarrow$  **reduced shot noise**

# 4-pulse geometry

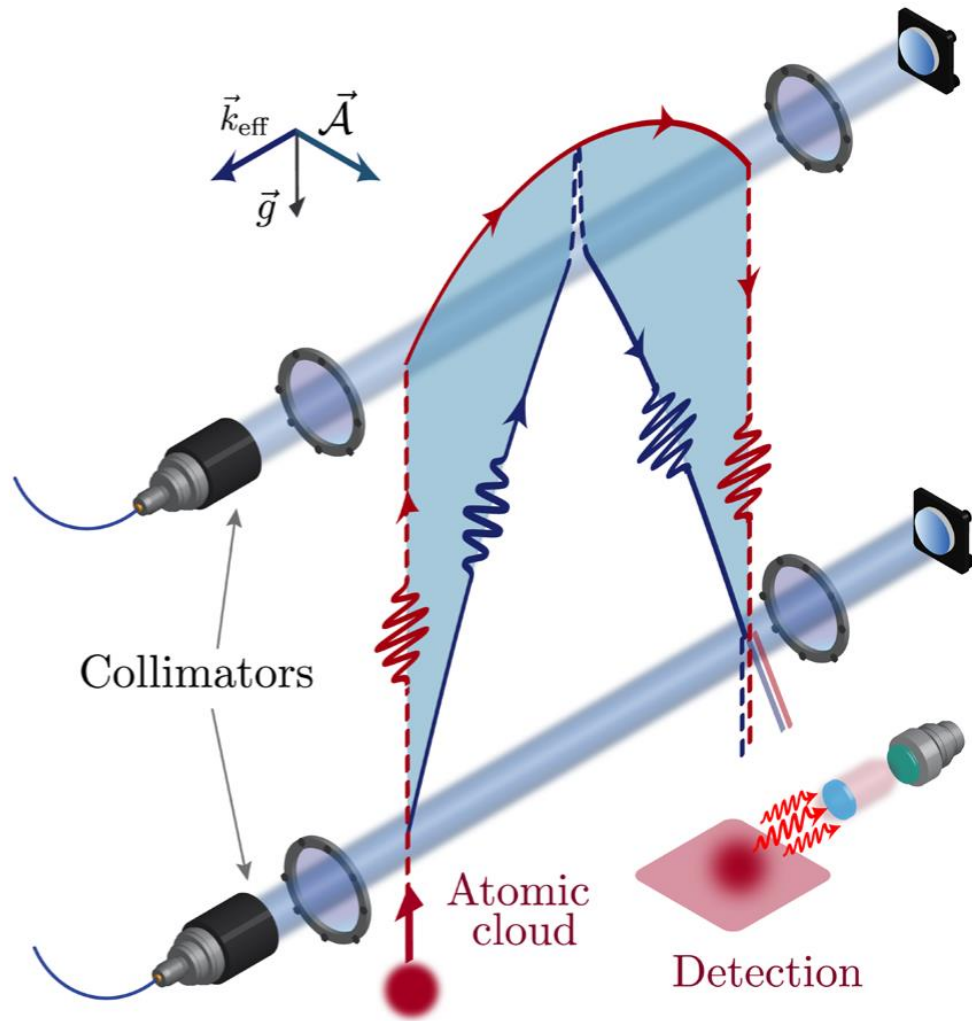


Image from [1]

Atoms in free fall,  $\pi/2 - \pi - \pi - \pi/2$  pulse geometry

Free-fall time  $T$ , effective wave vector  $\vec{k}$ , gravitational acceleration  $\vec{g}$ , rotation  $\vec{\Omega}$ :

$$\phi_{\text{rot}} = \frac{T^3}{2} (\vec{k} \times \vec{g}) \cdot \vec{\Omega}$$

# State of the art in AI-based quantum sensors



## Rotation sensors

### Stability:

- 30 nrad/s in 1s
- 0.1 nrad/s after averaging

### Uncertainty:

- Few nrad/s to 10 nrad/s

## Gravimeters

### Stability:

- 42 nm/s<sup>2</sup> in 1s
- 0.5 nm/s<sup>2</sup> after averaging

### Systematic uncertainty:

- 40 nm/s<sup>2</sup>
- Limited by wave front distortions <sup>1)</sup>

Transportable, sea, flight,  
commercial versions

## Gravity gradiometers

### Stability:

- $3 \cdot 10^{-8}$  1/s<sup>2</sup> in 1s

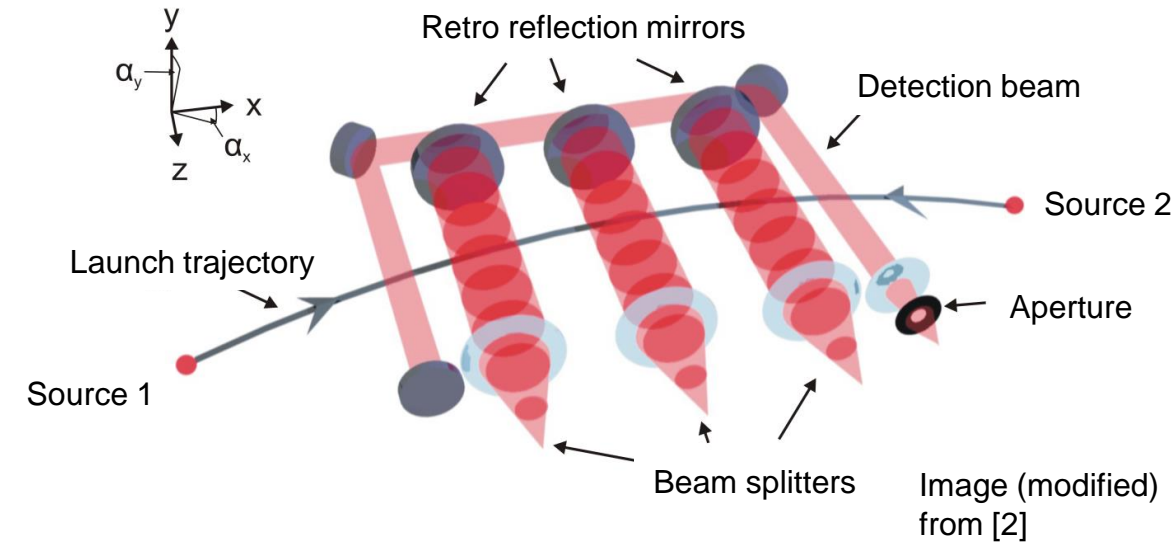
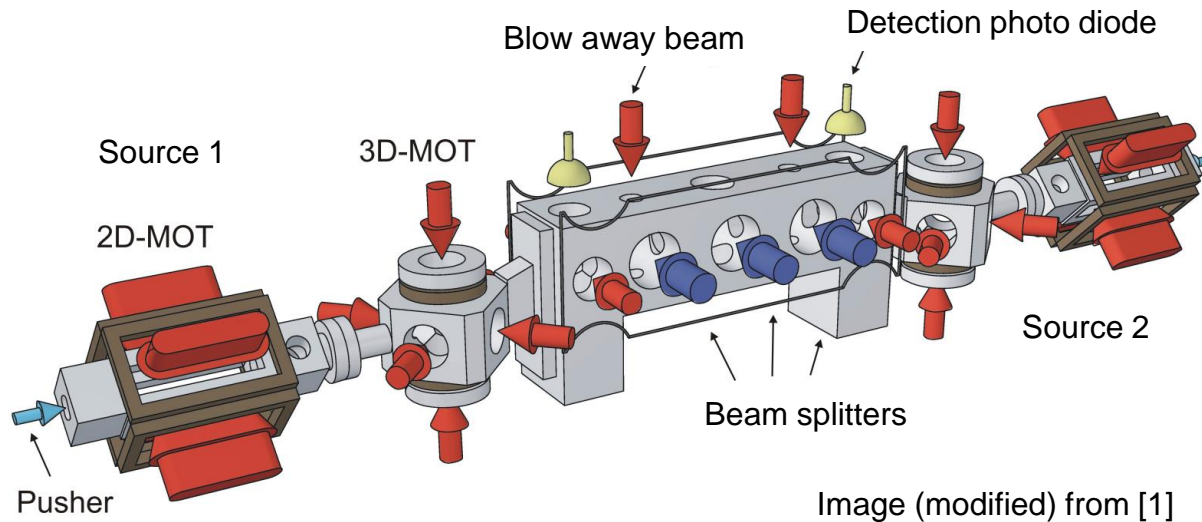
### Systematic uncertainty

- $8 \cdot 10^{-8}$  1/s<sup>2</sup>

Determination of gravitational  
constant

[From: Chen et al., arXiv:2303.00239; Gautier et al., Sci. Adv. 8, eabn8009 (2022); Berg et al., PRL 114, 063002 (2015); Stockton et al., PRL 107, 133001 (2011); Gauguier et al., PRA 80, 063604 (2009); Gillot et al., Metrologia 51, L15-L17 (2014); 1) reduced in Karcher et al., NJP 20, 113041 (2018); Freier et al., JoP:CS 723, 012050 (2016); Hu et al., PRA88, 043610 (2013); Wu et al., Sci. Adv. 5, eaax0800 (2019); Bidel et al., Nat.Comm. 9, 2041 (2018); Bidel et al., JoG 94, 1432 (2020); muquans.com; McGuirk et al., PRA 65, 033608 (2002); Fixler et al., Science 315, 74 (2007); Biedermann et al., PRA 91, 033629 (2015); Chiow et al., PRA 93, PRA 93, 013602 (2016); Rosi et al., Nature 510, 518 (2014); Asenbaum et al. PRL 118, 183602 (2017)]

# Cold atom Sagnac interferometer (CASI)



## Double interferometer for measuring the rotation $\Omega_y$ :

- 2 double MOT systems provide molasses cooled  $^{87}\text{Rb}$  atoms at  $10\ \mu\text{K}$
- Moving molasses launch to  $v_{x,1} = 2.79\ \text{m/s}$ ,  $v_{x,2} = -2.79\ \text{m/s}$ ; subsequent velocity filter
- 3 spatially separated interaction zones for Raman type beam splitters
- State-selective fluorescence detection detects  $10^6$  atoms per interferometer

# Discriminating rotations and accelerations



Signal of the two atom interferometers:

$$\phi_{1,2}(k_{1,2}, v_{x,1,2}) = 2(k_{1,2} \cdot v_{x,1,2}) \cdot \Omega_y T^2 + k_{1,2} \cdot a_z T^2 + \phi_{other,1,2}$$

$$k_1 = -k_2 = k, v_{x,1} = -v_{x,2} = v$$

Differential signal – acceleration:

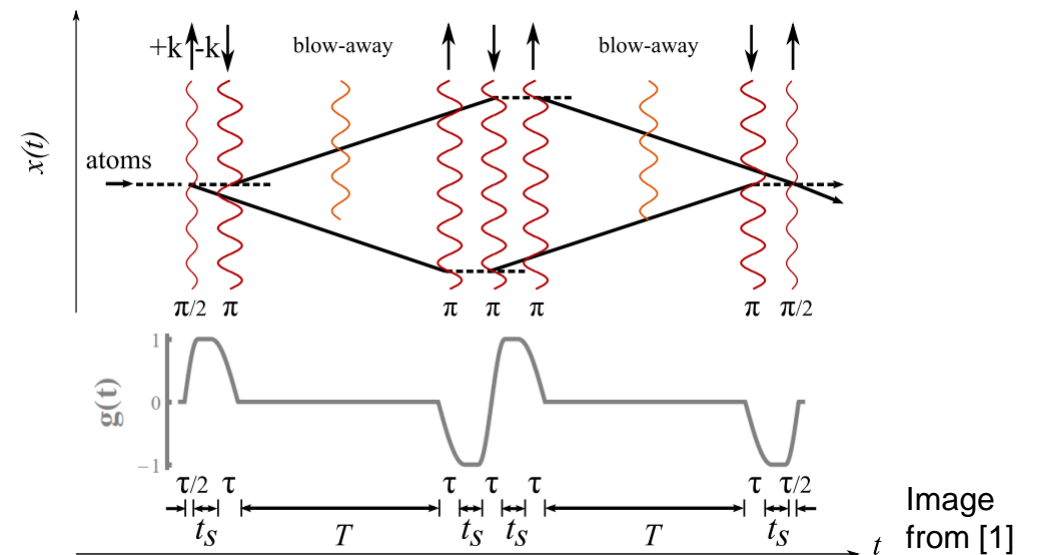
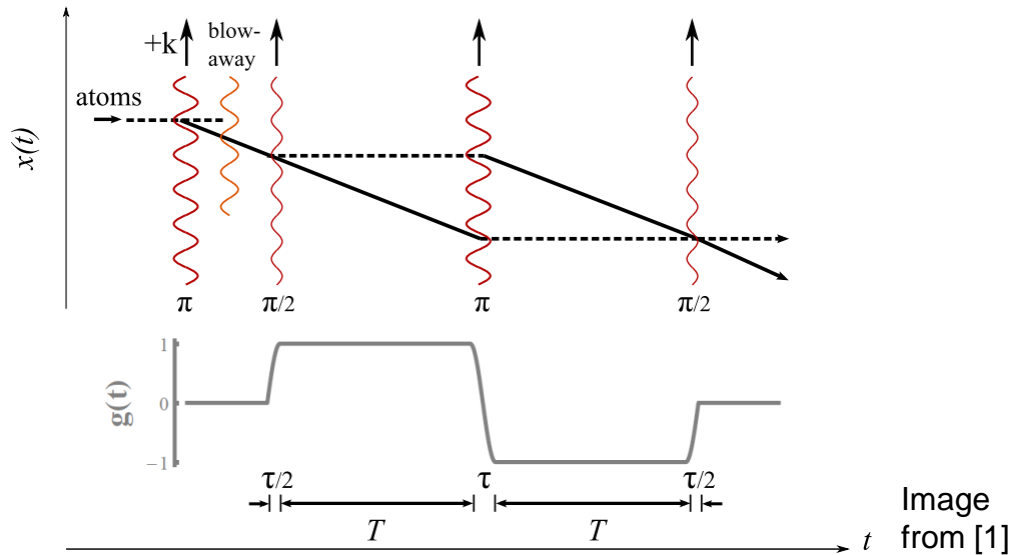
$$\phi_{diff} = [\phi_1(k, v) - \phi_1(-k, -v)]/2 = \mathbf{k} \cdot \mathbf{a}_z T^2 + \phi_{other,diff}$$

Sum signal – rotation:

$$\phi_{sum} = [\phi_1(k, v) + \phi_1(-k, -v)]/2 = 2(\mathbf{k} \cdot \mathbf{v}) \cdot \Omega_y T^2 + \phi_{other,sum}$$



# Symmetrized composite-pulse interferometer (SCI)



## MZI:

$$T_{\text{MZI}} = 24.7 \text{ ms}, k_{\text{MZI}} = 4\pi/(780 \text{ nm}), T_c = 0.5 \text{ s}$$

$$C_{\text{MZI}} = 18 \% \text{ (36 \% at } T_{\text{MZI}} = 23 \text{ ms)}$$

Short-term instability MZI: **610 nrad/s** in **1 s**

## SCI – larger $k$ , noise suppression:

$$T_{\text{SCI}} = 25 \text{ ms}, k_{\text{SCI}} = 8\pi/(780 \text{ nm}), T_c = 0.5 \text{ s}$$

$$C_{\text{SCI}} = 19\%$$

Short-term instability SCI: **120 rad/s** in **1 s**

# Results and limits of CASI in SCI configuration



## Results:

- Short-term instability: **120 rad/s** in **1 s**
- Estimated intrinsic noise: 77 nrad/s in 1 s (detection, technical noise)
- Averaging: **26 rad/s** in **100 s** (higher background noise during operation, 260 rad/s in 1 s)
- Systematic uncertainty: **600 nrad/s** (uncertainty of launch velocity & starting position + wave front errors)

## Possible improvements:

- Ultracold atoms / Bose-Einstein condensates (BECs) → improved contrast, reduced systematic error
- Lattice launch → improved control of launch vector / drift velocity
- Large momentum transfer → larger phase shift / improved sensitivity

# Rapid BEC generation on an atom chip

Atom-chip based BEC source for interferometry:

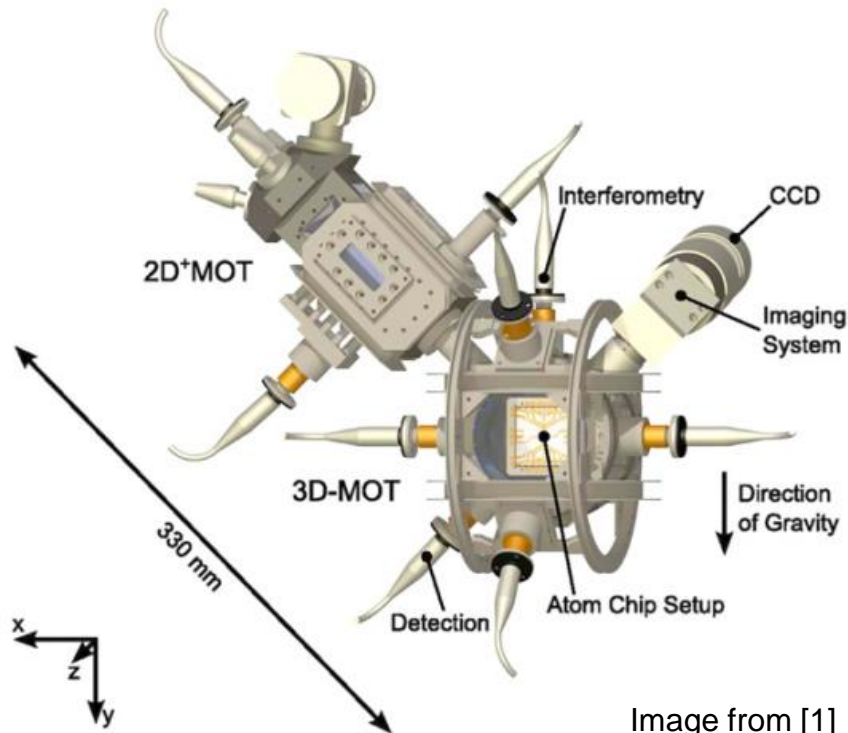


Image from [1]

## Challenge:

- Providing high flux with low expansion rates of the atoms

## Solution:

- Atom-chip based BEC generation + delta-kick collimation

## Demonstrated flux [1]:

- $\{10^5, 4 \cdot 10^5\}$   $^{87}\text{Rb}$  atoms (BEC) in  $\{1 \text{ s}, 1.6 \text{ s}\}$

## Delta-kick collimation – lowering the velocity spread [2]:

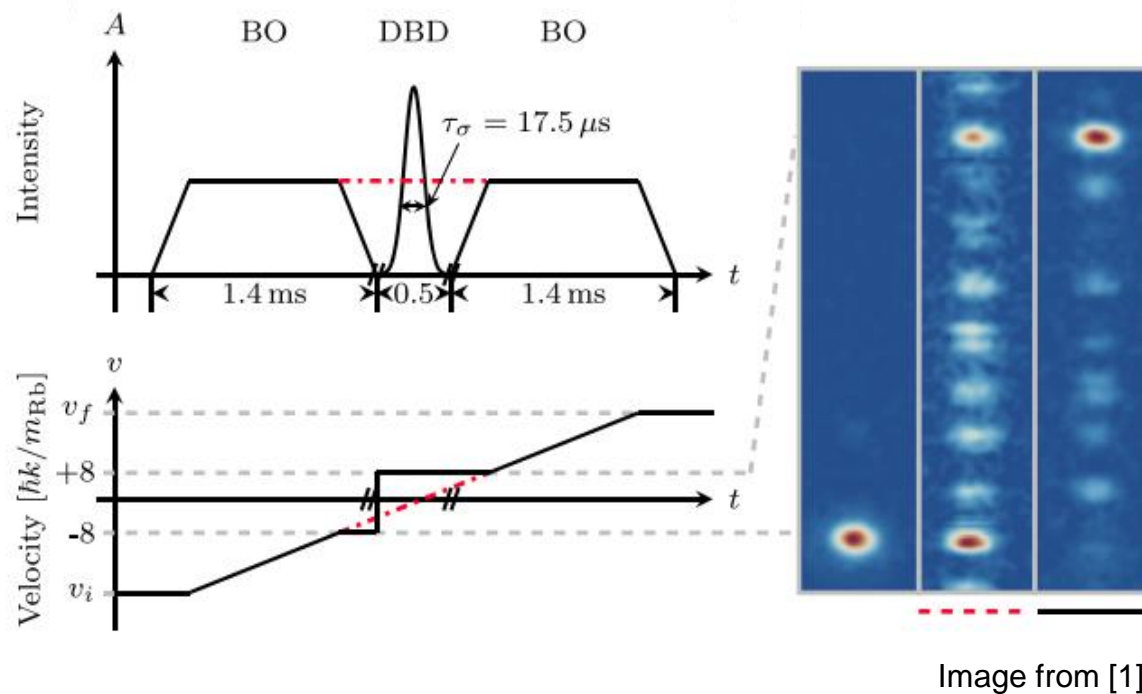
- Down to a kinetic energy of  $(3/2)k_B \cdot 38_{-7}^{+6}$  pK (3D)

→ Reducing systematic errors, increasing short-term stability [3]

[Images and results from: 1) Rudolph et al., NJP 17, 065001 (2015), CC BY 3.0, <https://creativecommons.org/licenses/by/3.0/>; 2) Deppner et al., PRL 127, 100401 (2021); 3) Gebbe et al., Nat. Comm. 12, 2544 (2021); Szigeti et al., NJP 14, 023009 (2012); Louchet-Chauvet et al., NJP 13, 065025 (2011); Debs et al., Phys. Rev. A 84, 033610 (2011); Heine et al., EPJD 74, 174 (2020); Schkolnik et al., APB 120, 311 (2015); see also for rapid evaporation in optical dipole traps: Roy et al., arxiv:1601.05103; Albers et al., Comm. Phys. 5, 60 (2022)]

# (Re)launching atoms

Retro-reflected beam setup – well-defined pointing of launch vector normal to mirror surface:



## Challenge:

- Losses due to simultaneous interaction with two moving lattices

## Solution [1]:

- (De-)acceleration via Bloch oscillations (BO)
- $16 \hbar\kappa$  double-Bragg pulse (DBD) inverts momentum around 0 momentum

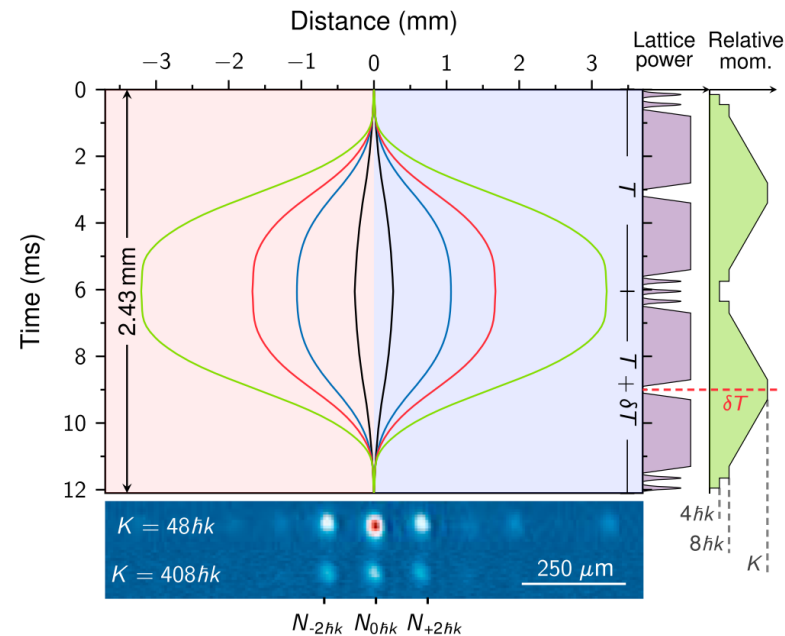
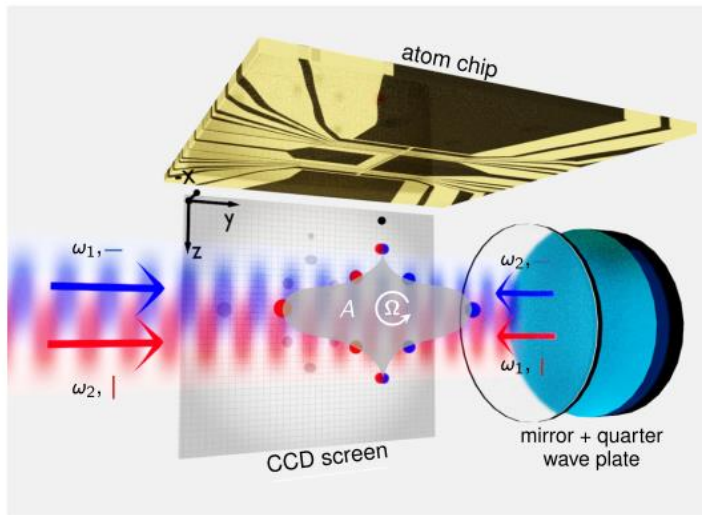
## Demonstrated results [1]:

- Launch efficiency of 75 % observed

→ Control of launch vector / drift velocity

# Large momentum transfer – twin lattice atom interferometer

Increasing the enclosed area / effectively  $k$ :



## Challenge:

- Increasing  $k$  without losing contrast

## Solution:

- Delta-kick collimated BEC
- Combining Bloch oscillations and double Bragg diffraction

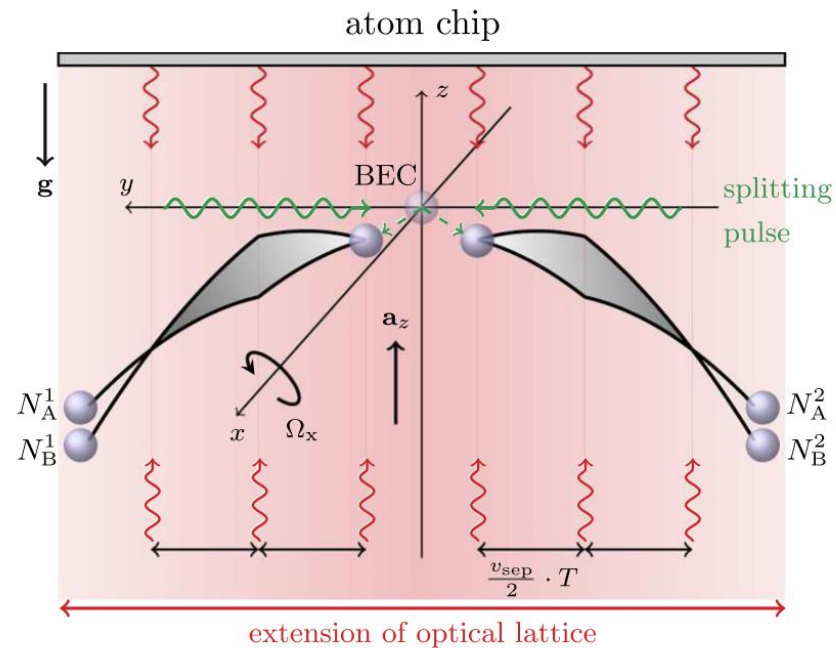
## Experimental results [1]:

- Realisation of interferometers with up to 408  $\hbar k$  beam splitters
- Total transfer of up to 1632  $\hbar k$
- Remaining contrast: 14%

→ Increasing the scale factor for future interferometers

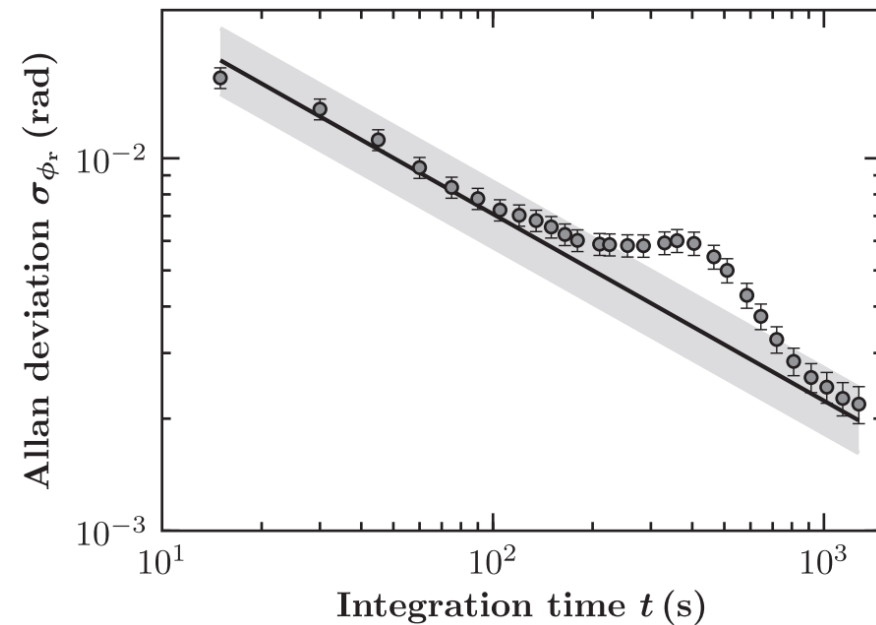
# Differential BEC interferometer

Demonstrating a double-interferometer scheme with a single BEC source:



$$T = 5 \text{ ms}, k = 4\pi/(780\text{nm}),$$

$$v = \hbar k/m \approx 24 \text{ mm/s}, T_c = 15 \text{ s}$$

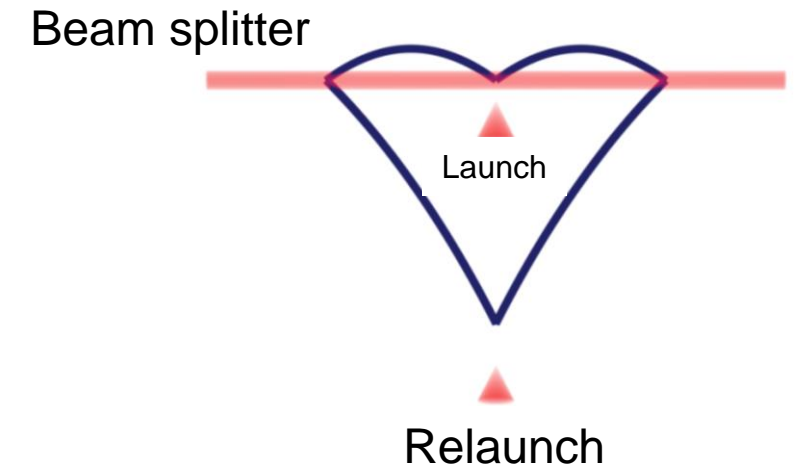


Short-term instability: **1.7 mrad/s in 15 s**  
(compatible with estimated shot noise limit)

# Novel multi-loop scheme – motivation

Stable, absolute rotation measurement with freely falling atoms

- Multiple round trips of the atoms → linear increase in effectively enclosed area similar to fibre optical gyroscopes [1] → boosted sensitivity without increasing the size of the vacuum vessel / sensor head [2]
- Multi-loop scheme based on symmetric beam splitting and relaunches [2]
- Anticipated sensitivity:  $2 \cdot 10^{-11}$  rad/s in 1 s [2], comparable to the large ring laser gyroscope in Wettzell [3]



# Previously published results & features of novel multi-loop scheme



## Previous implementations [1-3]:

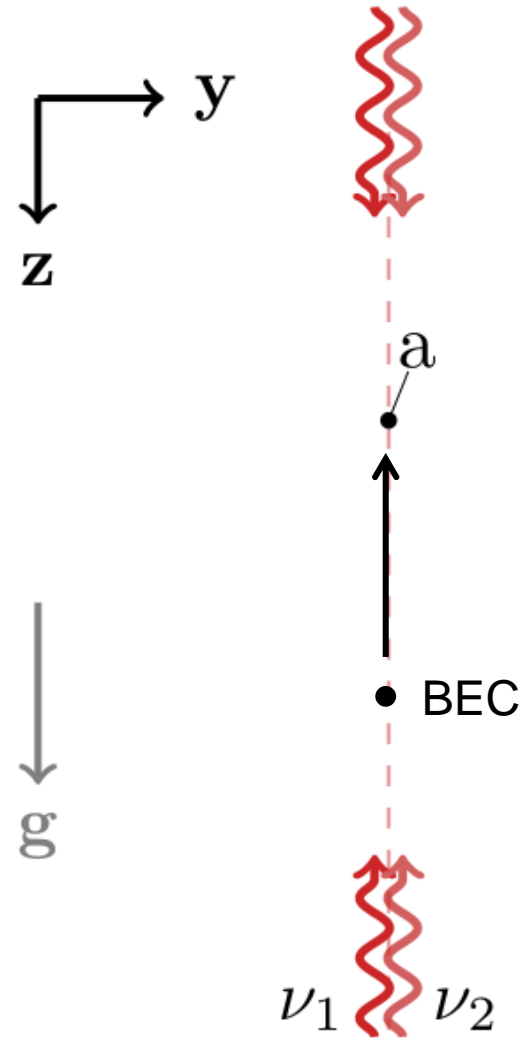
- Based on 3-pulse, Mach-Zehnder-like or 4-pulse, 'butterfly' geometries
- Thermal Cs beam, molasses cooled Cs / Rb injected into the interferometer
- Tuneability of pulse-separation time typically limited by optical access / spatially separated beam splitters
- Spatially separated atom-light-interaction zones require fine adjustment

## Features of proposed scheme [4]:

- Tunable free-fall time → scalable area
- Coherent atom-light interactions imprint velocities → well-defined area
- Beam splitting on single axis → no relative alignment required
- Symmetric beam splitting → reduced biases due to light shifts
- Multiple beam splitting axes → compatible with measurements of tilt, gravity

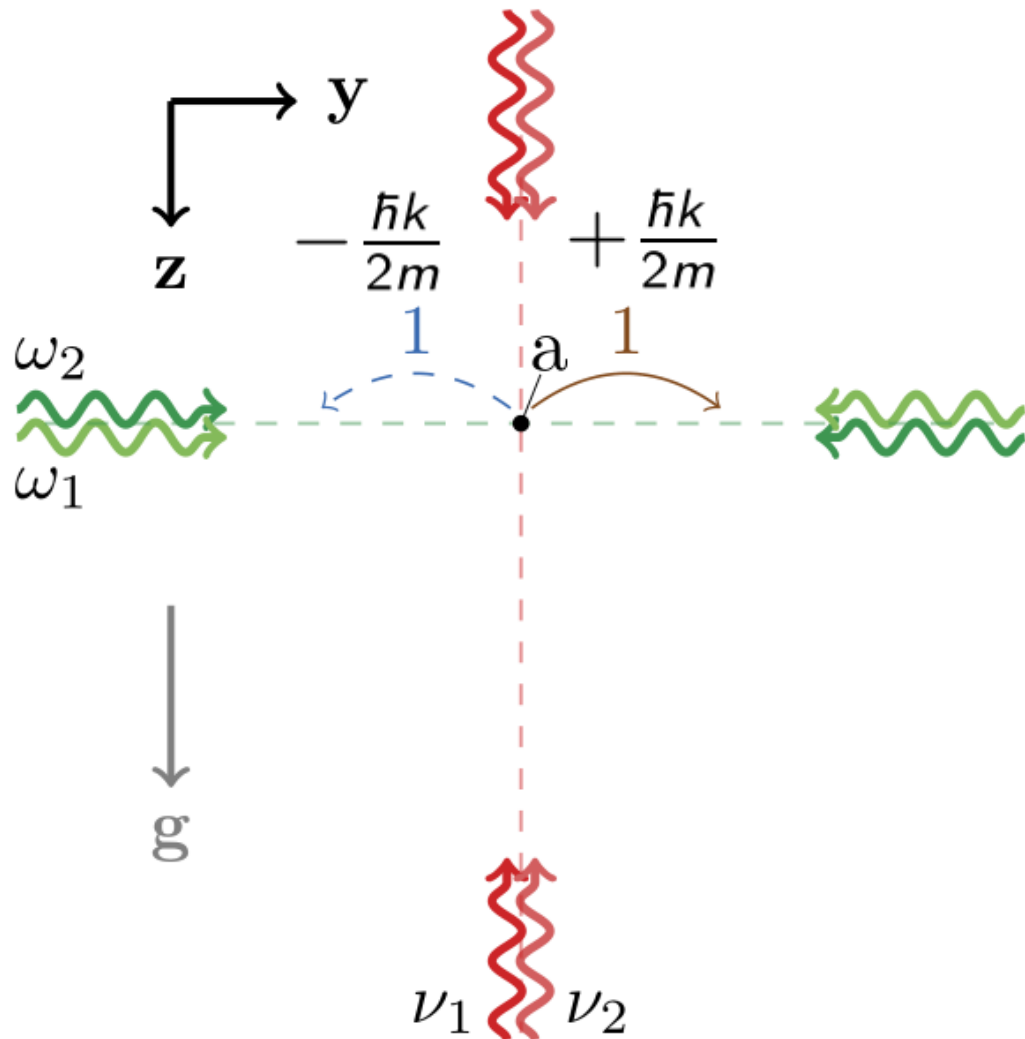


# Implementation of the multi-loop geometry



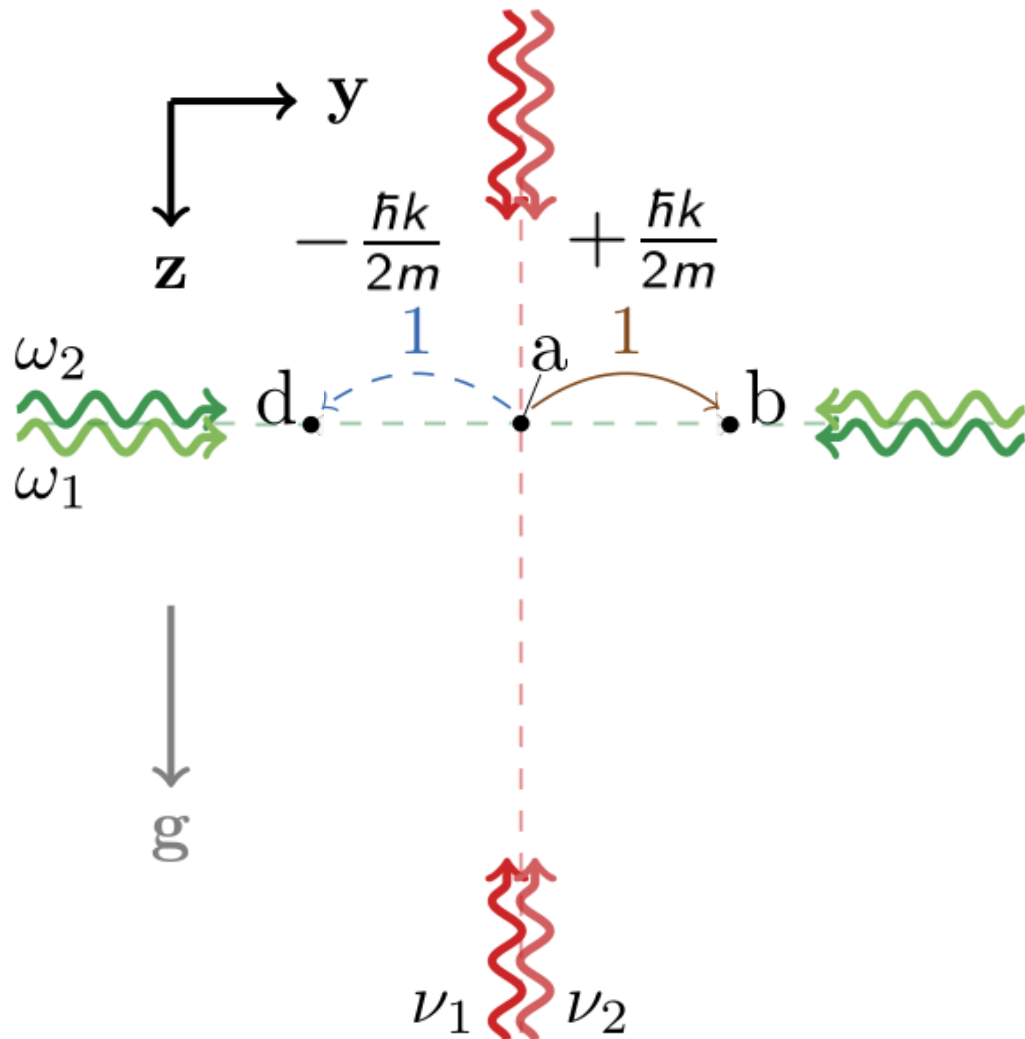
- Launch BEC (small initial momentum & low expansion rate)

# Implementation of the multi-loop geometry



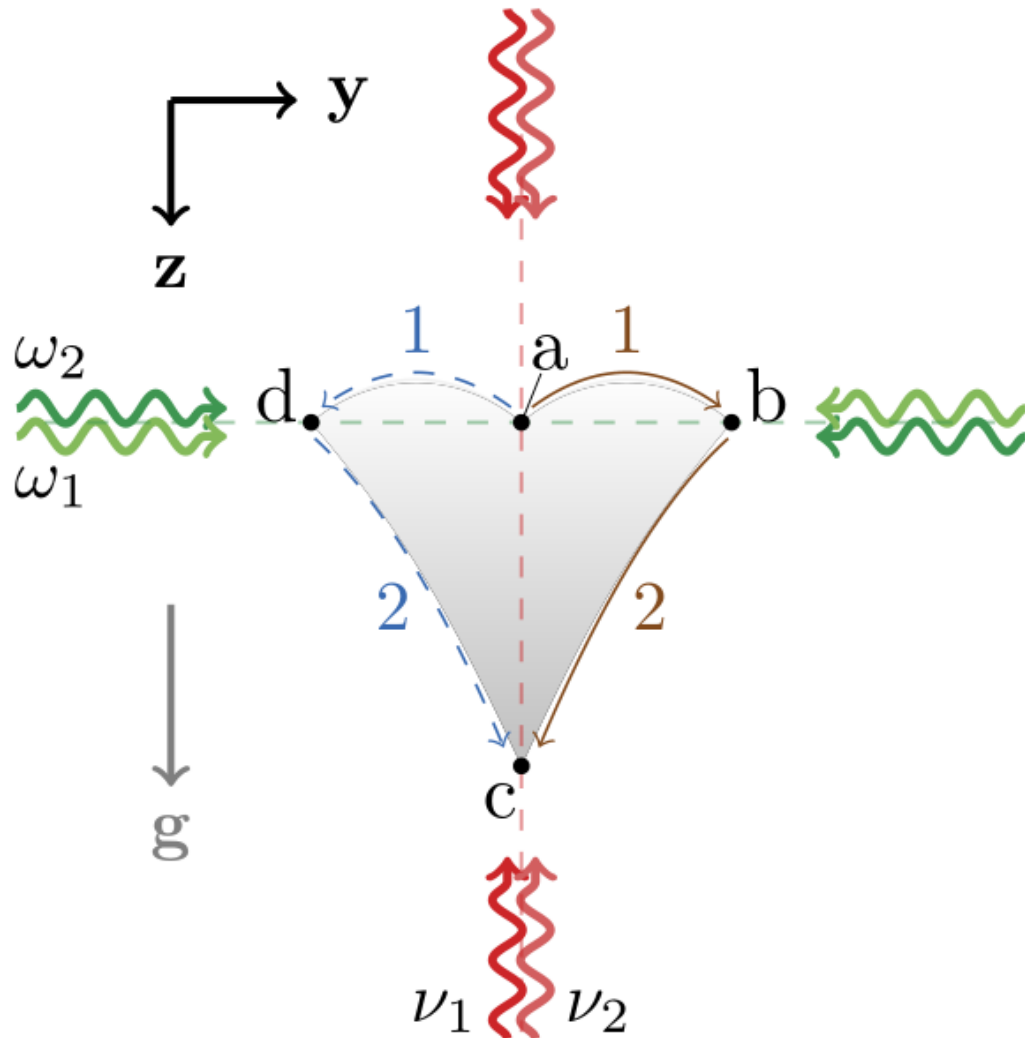
- Launch BEC (small initial momentum & low expansion rate)
- Horizontal beam splitter: two wave packets drifting apart (a)

# Implementation of the multi-loop geometry



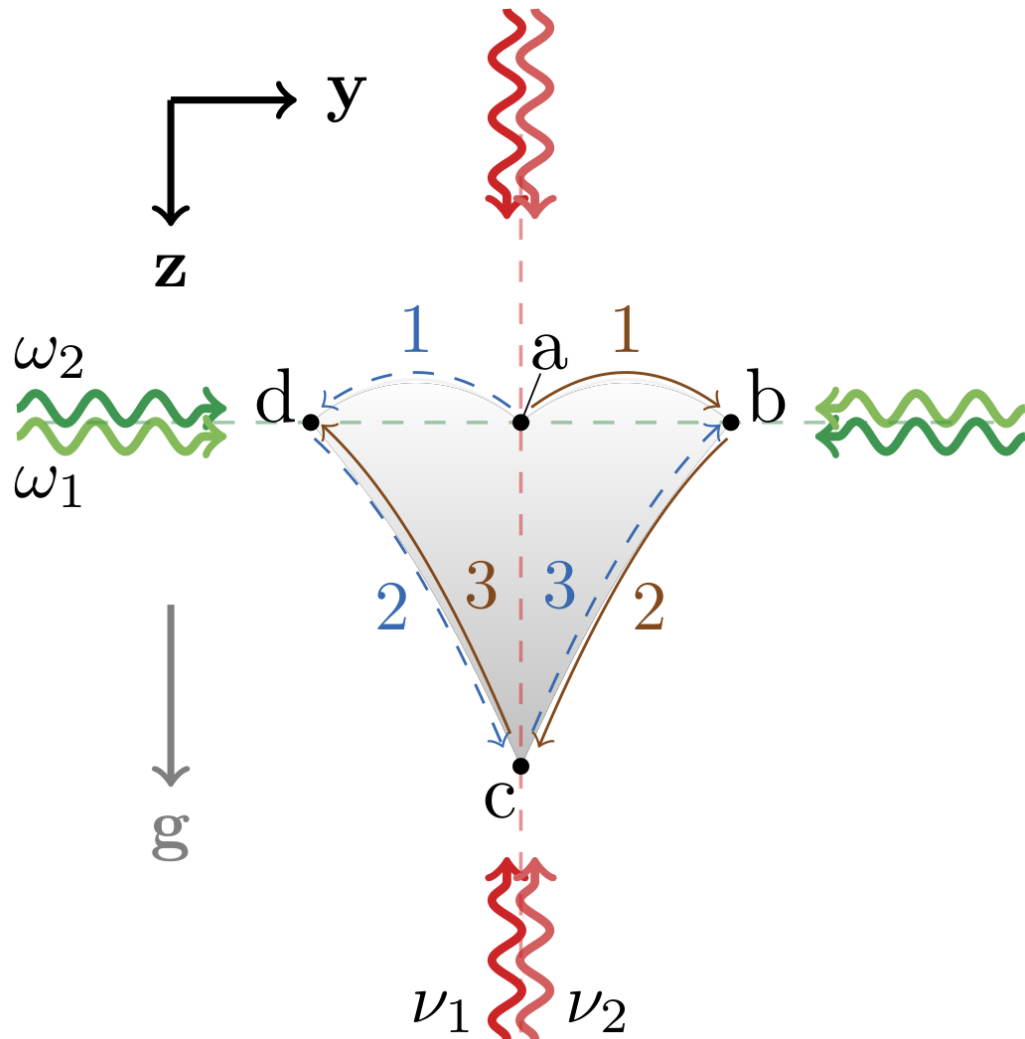
- Launch BEC (small initial momentum & low expansion rate)
- Horizontal beam splitter: two wave packets drifting apart (a)
- After time  $T$ , invert the movement of the atoms (b,d)

# Implementation of the multi-loop geometry



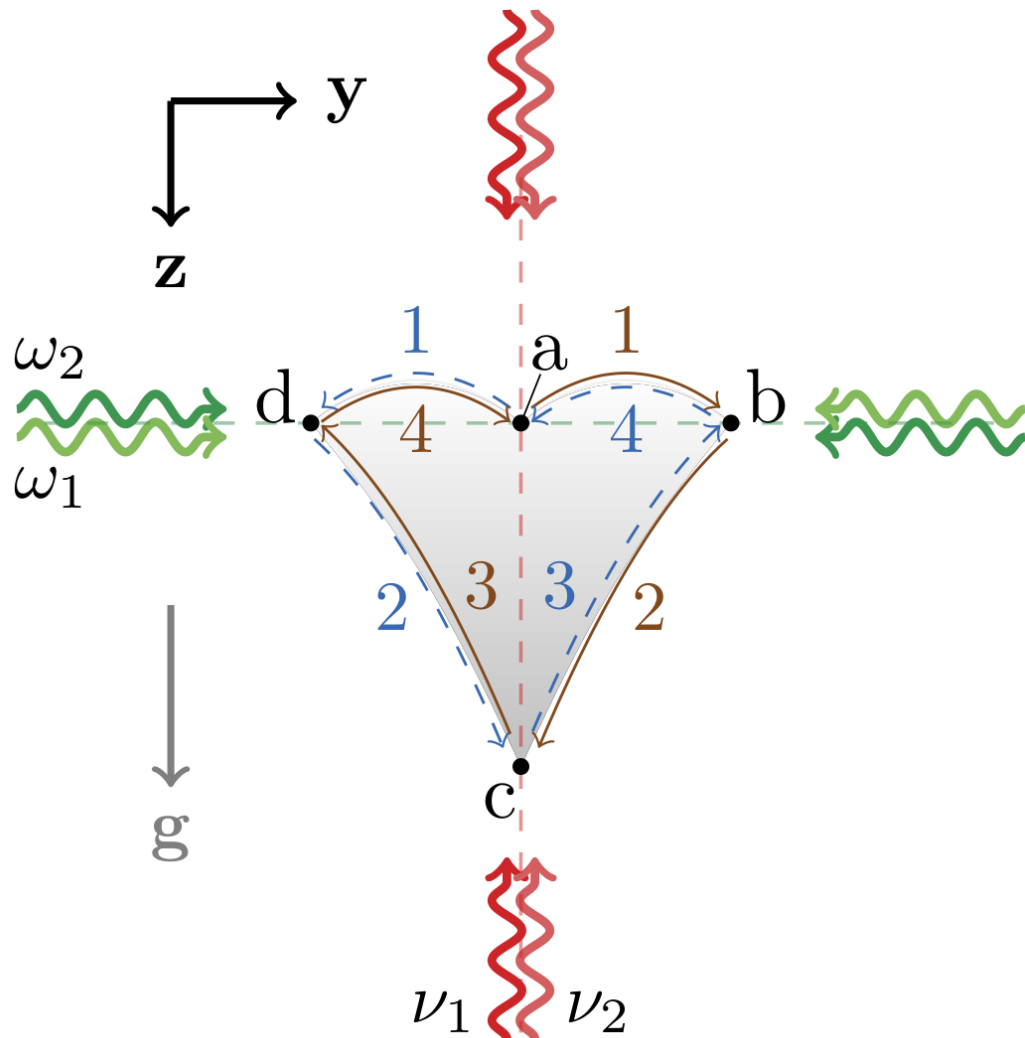
- Launch BEC (small initial momentum & low expansion rate)
- Horizontal beam splitter: two wave packets drifting apart (a)
- After time  $T$ , invert the movement of the atoms (b,d)
- After time  $2T$ , relaunch atoms and revert momentum (c)

# Implementation of the multi-loop geometry



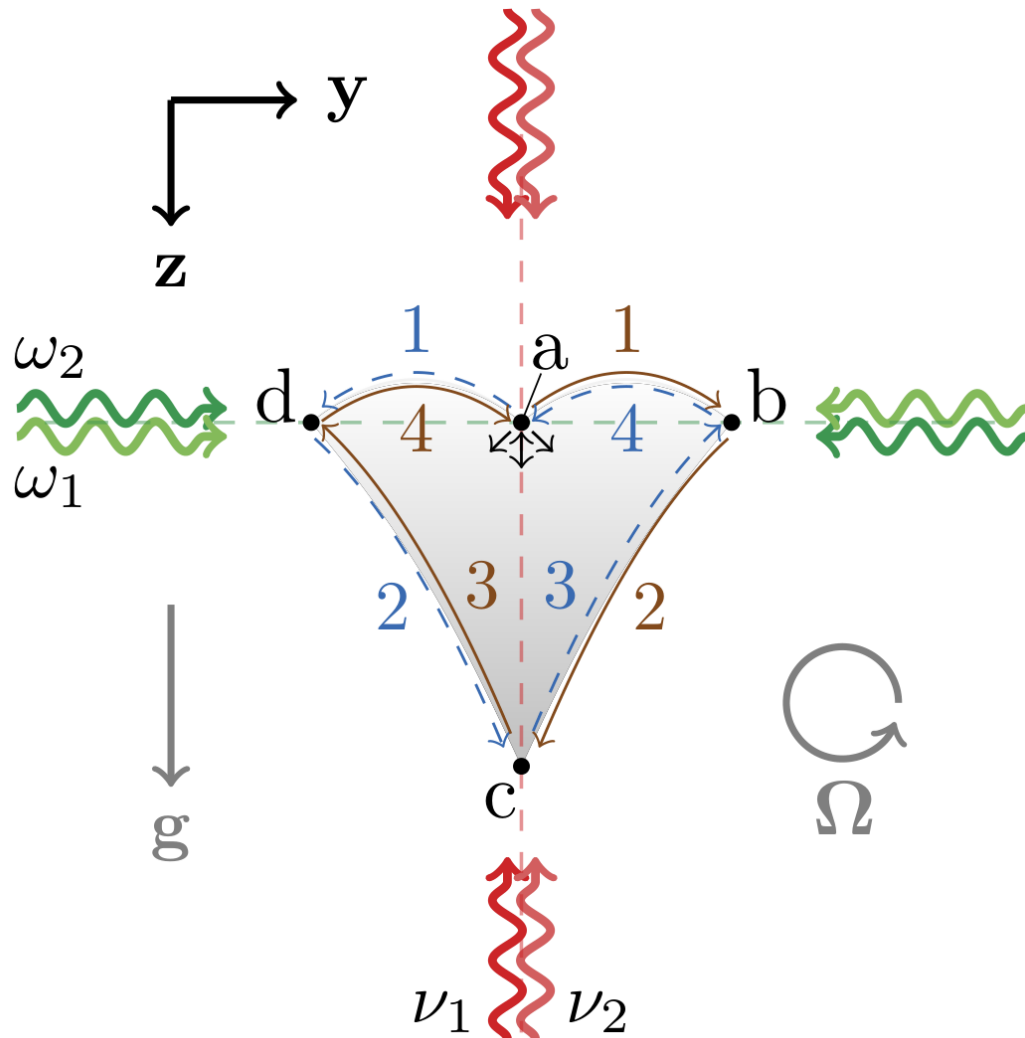
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- After time  $2T$ , relaunch atoms and revert momentum (c)
- After time  $3T$ , deflect atoms towards each other (b,d)

# Implementation of the multi-loop geometry



- Launch BEC (small initial momentum & low expansion rate)
- Horizontal beam splitter: two wave packets drifting apart (a)
- After time  $T$ , invert the movement of the atoms (b,d)
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- After time  $3T$ , deflect atoms towards each other (b,d)
- After time  $4T$ , atoms cross falling downwards (a)

# Implementation of the multi-loop geometry

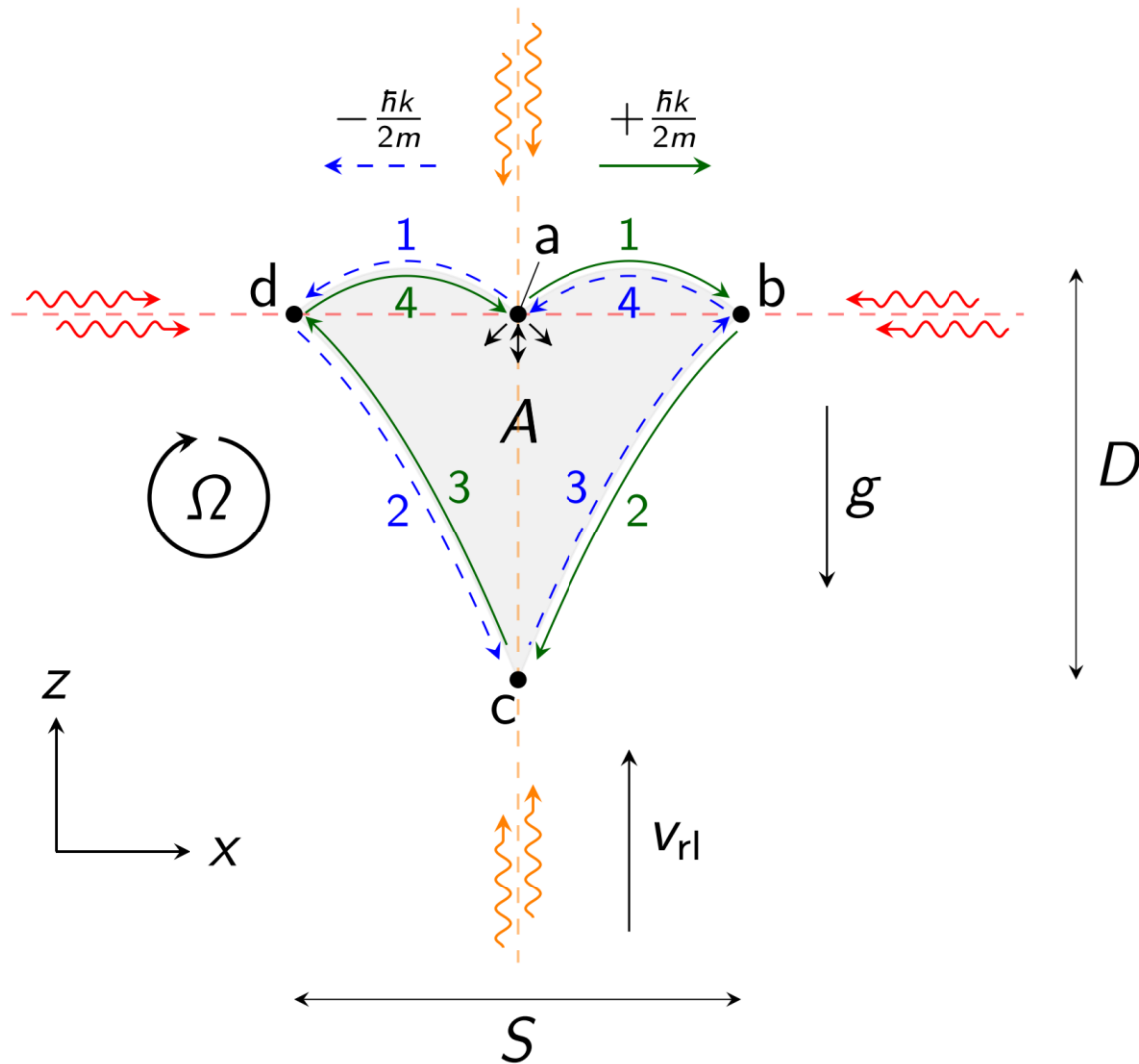


- Launch BEC (small initial momentum & low expansion rate)
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- After time  $4T$ , atoms cross falling downwards (a)

Two options:

1. Repeat sequence  $\rightarrow$  form another  $2n$  loop
2. Close interferometer and read out phase

# Multi-loop geometry



Single (~butterfly / double loop) or multiple round trips

Relaunch velocity:  $v_{rl} = |\mathbf{v}_{rl}| = 3gT$

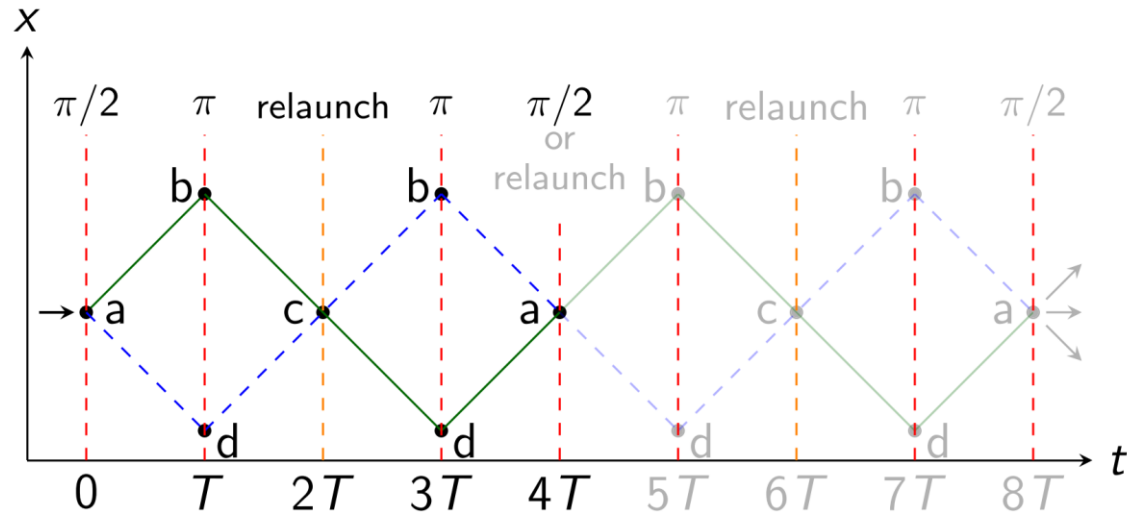
Enclosed area:  $A = n \cdot 2 \frac{\hbar k}{m} g T^3$

Phase shift:  $\Delta\phi_{Sagnac} = n \cdot (\mathbf{k} \times \mathbf{g}) \Omega T^3$

Wavevector  $\mathbf{k}$ , gravitational acceleration  $\mathbf{g}$ , rotation  $\Omega$ , atomic mass  $m$ , number of round trips  $n$



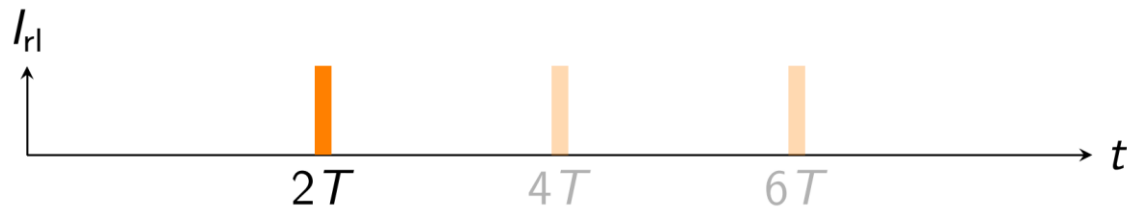
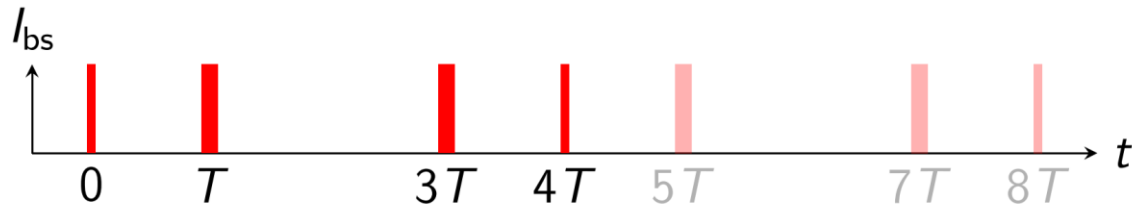
# Pulse timings



## Single round trip – 2 loops:

- 4 beam splitting pulses:  $\pi/2 - \pi - \pi - \pi/2$
- Pulse separation:  $T - 2T - T$
- Relaunch at  $2T$
- Recombination at  $4T$

Extension to multi-loop operation by relaunch instead of recombination



Beam splitter intensity  $I_{bs}$ , relaunch pulse intensity  $I_{rl}$  (not to scale)

# Anticipated sensitivities



Sensor features	$N$	$k\left(\frac{2\pi}{780\text{nm}}\right)$	$T$ (ms)	$n$	$C$	$A$ (m <sup>2</sup> )	$t_c$ (s)	$S$ (m)	$D$ (m)	Sensitivity $\left(\frac{\text{rad/s}}{\sqrt{\text{Hz}}}\right)$
1: Multi loop	$10^5$	<b>40</b>	10	10	1	$4.6 \times 10^{-5}$	1.6	$2.4 \times 10^{-3}$	$2.8 \times 10^{-3}$	$3.2 \times 10^{-8}$
1: Four pulse	$10^5$	<b>350</b>	10	–	1	$4 \times 10^{-5}$	1.24	$2.1 \times 10^{-2}$	$5 \times 10^{-3}$	$3.2 \times 10^{-8}$
2: Multi loop	$4 \times 10^5$	20	250	10	1	$3.6 \times 10^{-1}$	<b>11.8</b>	$3 \times 10^{-2}$	0.7	$5.5 \times 10^{-12}$
2: Four pulse	$4 \times 10^5$	28	189	–	1	$2.1 \times 10^{-2}$	<b>2.8</b>	$3.1 \times 10^{-2}$	0.7	$4.2 \times 10^{-11}$
Compact	$5.9 \times 10^4$	40	10	6	0.53	$2.8 \times 10^{-5}$	1.44	$2.4 \times 10^{-3}$	$2.8 \times 10^{-3}$	$1.2 \times 10^{-7}$
High sensitivity	$2.9 \times 10^5$	20	250	4	0.66	$1.4 \times 10^{-1}$	5.8	$3 \times 10^{-2}$	0.7	$1.7 \times 10^{-11}$

Drop distance:  $D = (3T/2)^2 \cdot g/2$

Maximum trajectory separation:  $S = \hbar kT/m$

Quantum projection noise limit:  $\sigma_{\Omega}(t) = \frac{1}{C\sqrt{N} \cdot n \cdot (4kgT^3)} \sqrt{\frac{t_{prep} + n \cdot 4T + t_{det}}{t}}$

Double-loop dependent contrast:  $C(n) = C(1)^n$

Loss factor:  $l^{n-1}$  with  $l = 0.9$  for  $2n$  loops

Contrast  $C$ , number of atoms  $N$  (modified by losses), averaging time  $t$ , preparation time  $t_{prep}$ , detection time  $t_{det}$

[Table and results from: Schubert et al., Sci. Rep. 11, 16121 (2021), CC BY 4.0]

# Error terms due to relaunch and other couplings



	$\alpha_{\delta\tau}$ (rad)	$\alpha_{\Gamma}$	$\beta$	$v_{x0}$ ( $\mu\text{m/s}$ )	$v_{y0}$	$v_{z0}$	$y_0$ ( $\mu\text{m}$ )	$z_0$	$\delta g$ ( $\text{m/s}^2$ )	$\delta\Gamma$ ( $1/\text{s}^2$ )
Compact	$1.3 \times 10^{-4}$	$< 0.1$	$9.4 \times 10^{-5}$	200 *	250 †	250 †	100 ‡	100 ‡	$5.6 \times 10^{-4}$	$7.2 \times 10^{-2}$
High sensitivity	$6 \times 10^{-6}$	$2.5 \times 10^{-6}$	$6.6 \times 10^{-9}$	26 *	10 †	10 †	100 ‡	100 ‡	$5.4 \times 10^{-8}$	$1.1 \times 10^{-8}$

## Assumptions:

- Phase errors  $10n$  times below the quantum projection noise limit ( $\sim 1/\sqrt{N}$ ); †velocity acceptance; ‡position w.r.t. beam
- $\Gamma_x = \Gamma_y = 0.5\Gamma_z = 1.5 \cdot 10^{-6} \text{ s}^{-2}$ ,  $\Omega_x = \Omega_y = \Omega_z = 7.27 \cdot 10^{-5} \text{ rad/s}$ , \*gradient compensation to  $0.1\Gamma$

## Error terms due to imperfect pointing of the relaunch vector $\mathbf{v}_{rl}$ :

- Relaunch tilt  $\alpha$  and timing error  $\delta\tau$ :  $\Delta\phi_{\alpha,\tau} = -k v_{rl} \alpha \delta\tau = -3kgT\alpha\delta\tau$
- Relaunch tilt  $\alpha$  and gravity gradient  $\Gamma$ :  $\Delta\phi_{\alpha,\Gamma} = \mathbf{k}\Gamma\mathbf{v}_{rl}T^3 = 3k\alpha\Gamma_x gT^4$
- Relaunch tilt  $\beta$  and rotation  $\Omega$ :  $\Delta\phi_{\beta,\Omega} = 2(\mathbf{k} \times \mathbf{v}_{rl})\mathbf{\Omega}T^2 = 6k\beta g\Omega_z T^3$

## Dominant error terms depending on starting position $(x_0, y_0, z_0)$ / velocity $\mathbf{v}$ and others:

- Velocity  $v_x$ :  $\Delta\phi_{vx} = 4kT^3 (\Gamma_x + 3(\Omega_y^2 + \Omega_z^2)) v_x$
- Velocity  $v_y$ :  $\Delta\phi_{vy} = -4kT^3 (3\Omega_x\Omega_y + 4T(\Gamma_x + \Gamma_y)\Omega_z) v_y$
- Velocity  $v_z$ :  $\Delta\phi_{vz} = -4kT^3 (3\Omega_x\Omega_z + 4T(\Gamma_z + \Gamma_x)\Omega_y) v_z$
- Position  $y_0$ :  $\Delta\phi_{y0} = 8kT^3\Gamma_y\Omega_z y_0$
- Position  $z_0$ :  $\Delta\phi_{z0} = -8kT^3\Gamma_z\Omega_y z_0$
- Others:  $\Delta\phi_{\Gamma_x} = 18kT^5\Omega_y\Gamma_x$ ,  $\Delta\phi_{\Gamma_z} = 18kT^5\Omega_y\Gamma_z$

## Multi-loop rotation sensor:

- Compact sensor:  $1.2 \cdot 10^{-7} \text{ (rad/s)/}\sqrt{\text{Hz}}$  within a volume of  $20 \text{ mm}^3$
- Highly sensitive setup:  $1.7 \cdot 10^{-11} \text{ (rad/s)/}\sqrt{\text{Hz}}$  within a meter-sized vacuum vessel
- Compatible with implementing tilt & gravity measurements in the same setup
- Detection of multiple rotation axes by adding perpendicular horizontal beam splitter

# Summary & conclusion



## Features & status:

- Atom interferometry: a tool for absolute, long-term stable rotation (and acceleration) measurements
- Demonstrated instability: 30 nrad/s in 1 s, 0.1 nrad/s after averaging
- Systematic uncertainty: few 100 nrad/s; systematic error limited by wave front distortions

## Pathways for improvement:

- Ultracold atoms / BEC + DKC
- Lattice (re)launch
- Large momentum transfer (e.g. twin-lattice atom interferometer)
- Multi-loop schemes – up to  $1.7 \cdot 10^{-11} \text{ (rad/s)/}\sqrt{\text{Hz}}$  within a meter-sized vacuum vessel

A satellite with two large solar panel arrays is shown in orbit above the Earth. The satellite is gold-colored with various instruments and antennas. The solar panels are silver and rectangular. The Earth below shows green landmasses, blue oceans, and white clouds. The curvature of the Earth is visible on the right side of the image.

**THANK YOU**

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# Summary & conclusion



## Features & status:

- Atom interferometry: a tool for absolute, long-term stable rotation (and acceleration) measurements
- Demonstrated instability: 30 nrad/s in 1 s, 0.1 nrad/s after averaging
- Systematic uncertainty: few 100 nrad/s; systematic error limited by wave front distortions

## Pathways for improvement:

- Ultracold atoms / BEC + DKC
- Lattice (re)launch
- Large momentum transfer (e.g. twin-lattice atom interferometer)
- Multi-loop schemes – up to  $1.7 \cdot 10^{-11} \text{ (rad/s)/}\sqrt{\text{Hz}}$  within a meter-sized vacuum vessel

See poster by M. Gersemann

Positions available!