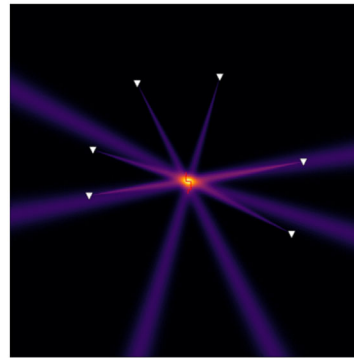
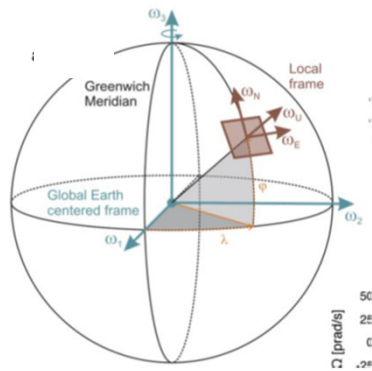


# Earth's Rock'n'Roll: Measuring rotational motions in Geodesy and Seismology



Heiner Igel<sup>1</sup>, Andreas Brotzner<sup>1</sup>, Felix Bernauer<sup>1</sup>, Sabrina Keil<sup>1</sup>, Chin-Jen Lin<sup>1,9</sup>, Frederic Guattari<sup>7</sup>, Fabian Lindner<sup>1,3</sup>, **Karl Ulrich Schreiber**<sup>2</sup>, Frank Vernon<sup>4</sup>, Joachim Wassermann<sup>1</sup>, Shihao Yuan<sup>1</sup> and others

- <sup>1</sup> LMU Munich, Germany
- <sup>2</sup> TU Munich, Germany
- <sup>3</sup> ETH Zurich, Switzerland

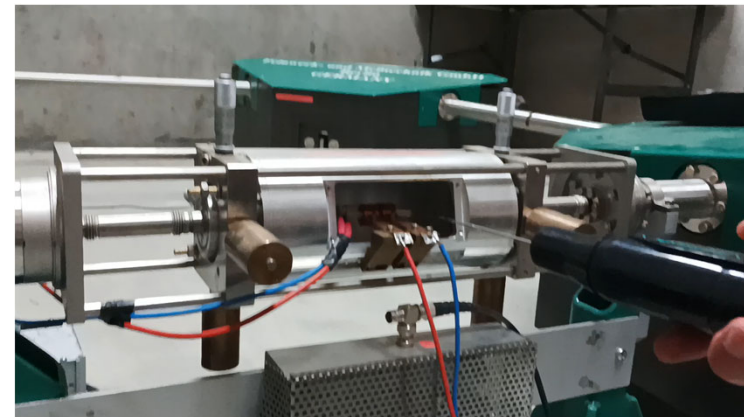
- <sup>4</sup> UCSD, La Jolla, CA
- <sup>5</sup> UC Santa Barbara, CA
- <sup>6</sup> University of Pisa, Italy

- <sup>7</sup> iXblue, St. Germain
- <sup>8</sup> University of Nantes
- <sup>9</sup> Academia Sinica, Taipei



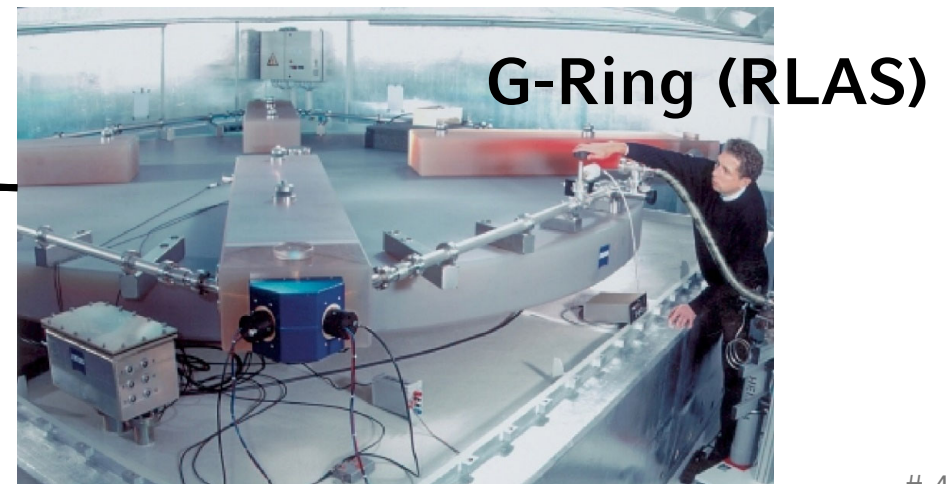
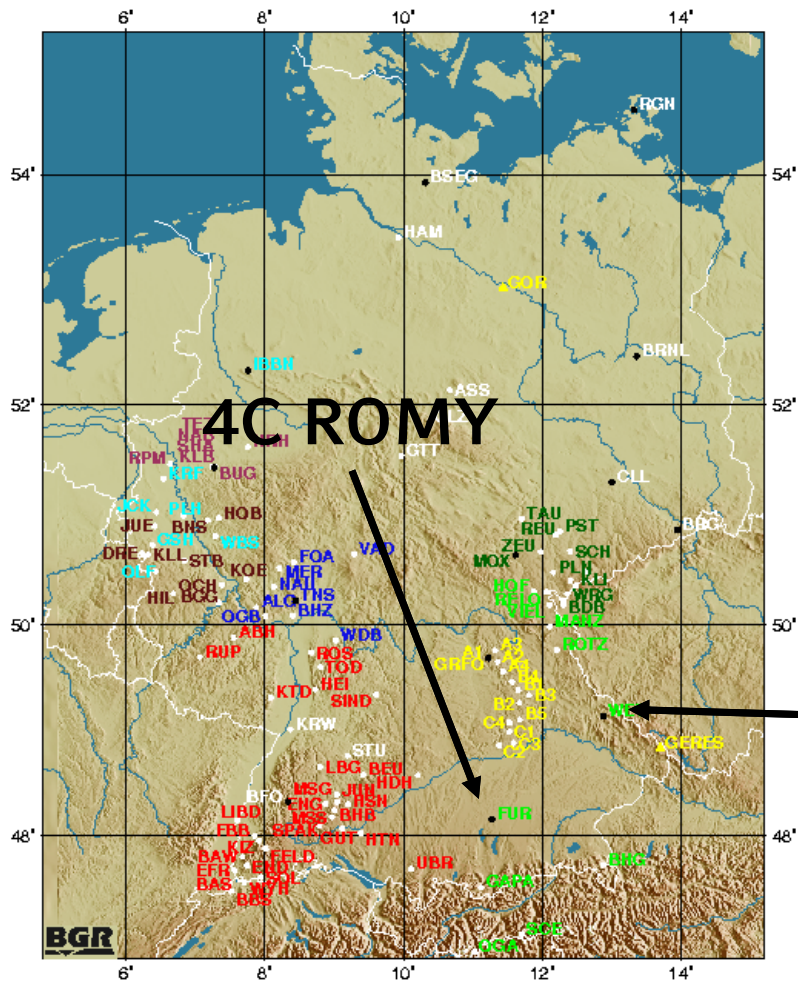
# Outline

- How do **ring lasers** measure Earth's rotation?
- How their **noise** sparked a new field in seismology (**rotational seismology**)
- A **portable** rotation sensor for seismology
- Rotational ground motions, **what are they good for?**
  - Structural inversion
  - Volcano seismology
  - Seismic source tracking
  - Seismic anisotropy and mantle flow
  - Planetary seismology
  - Ocean bottom seismology
  - Earthquake engineering
- Outlook

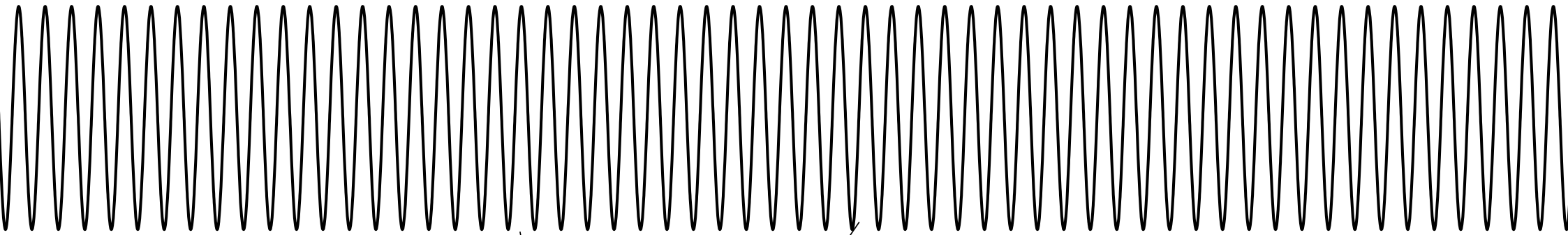


**How to observe Earth's**  
*(and local ground) rotations*  
*(without VLBI and satellites)?*

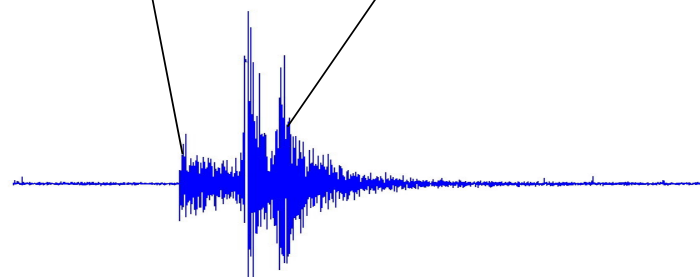
# Geodetic Observatory Wettzell, SE Germany



# „FM radio“ – Earth's rotation



Sagnac frequency sampled with 1-5kHz

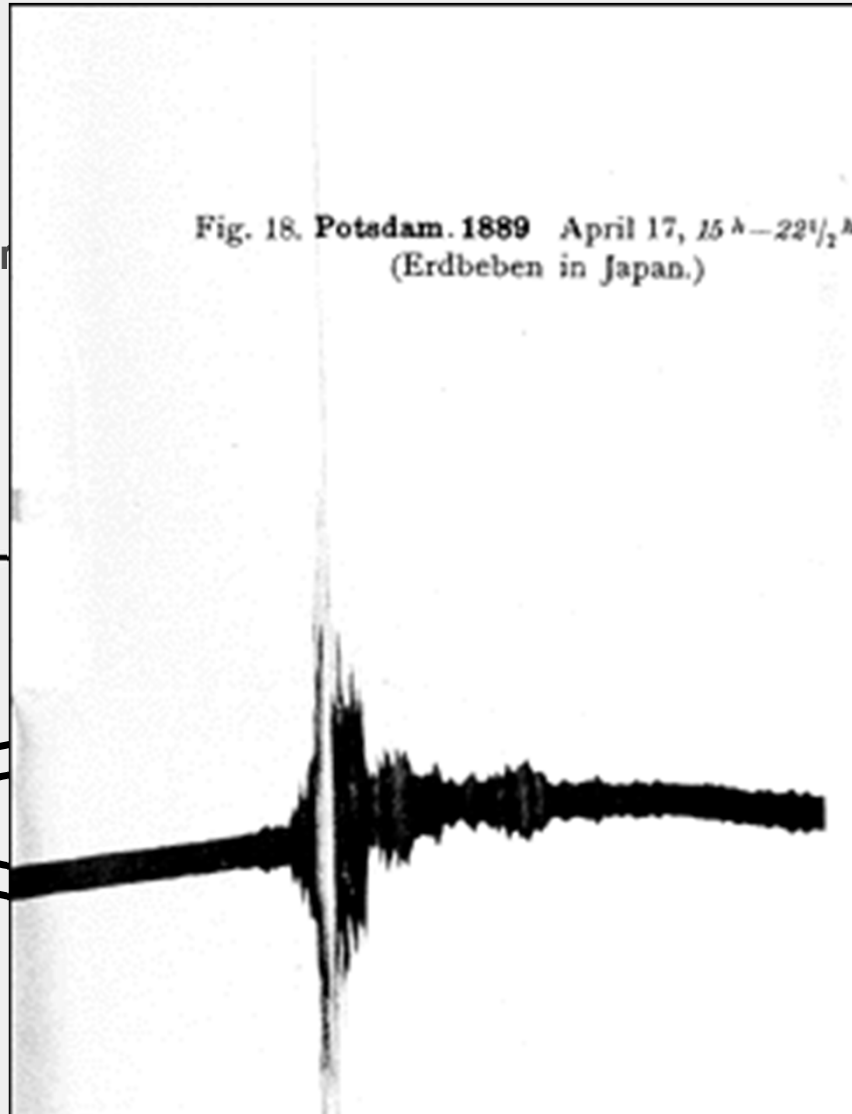


Rotation rate seismogram

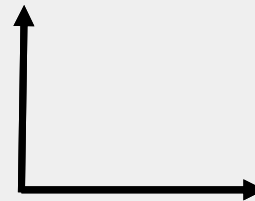
Tiny changes in the Sagnac frequencies are extracted to obtain the time series with rotation rate  
 $\Delta f \rightarrow \Omega$

# ...One person's noise ...

Earth's *constant* rotation



rotation rate



time

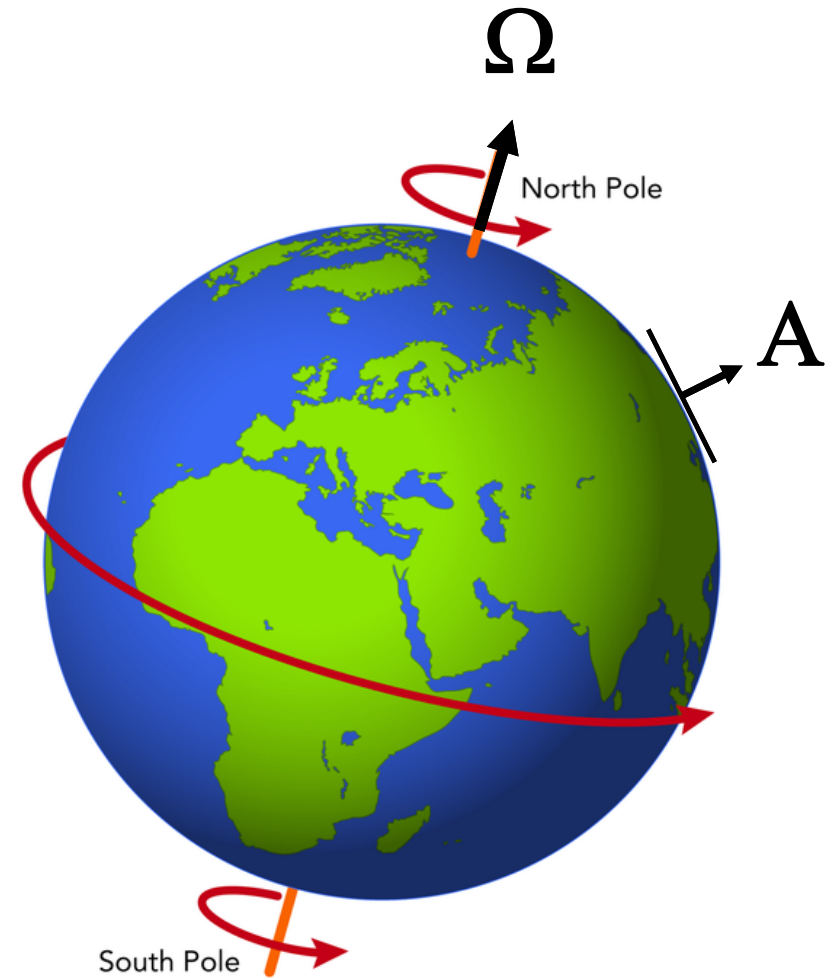
and local vertical axis after  
earthquake December 2004

# Sagnac Effect – Measuring Earth's rotation and more ...

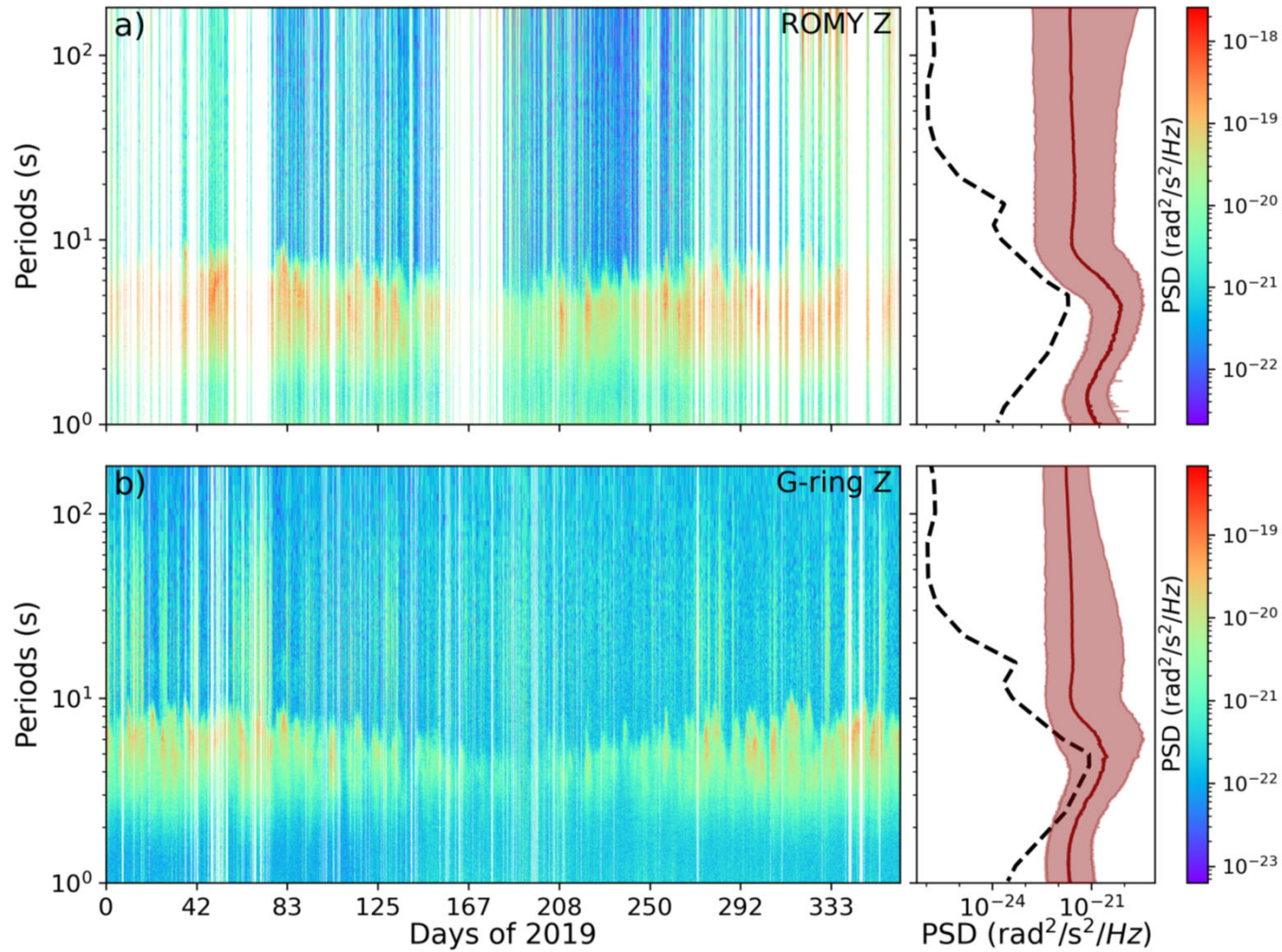
$$\Delta f_{Sagnac} = \frac{4\Omega \cdot A}{\lambda P}$$

- A surface of the ring laser (vector)
- $\Omega$  imposed rotation rate (Earth's rotation + earthquake +...)
- $\lambda$  laser wavelength (e.g. 632 nm, He-Ne)
- P perimeter (e.g. 4-36m)
- $\Delta f$  Sagnac frequency (e.g. 348,6 Hz sampled at 1000Hz)

G-ring WET (Since summer 2009) resolution down to **~0.07 prad/s**  
**ROMY resolution expected ~0.04 prad/s**



# Earth's Background Rotations



- Background noise for ROMY (top) and G-ring (bottom) in 2019
- Theoretical rotational low noise model for Earth (dashed line)

Brotzer et al., 2023 (SRL, submitted)

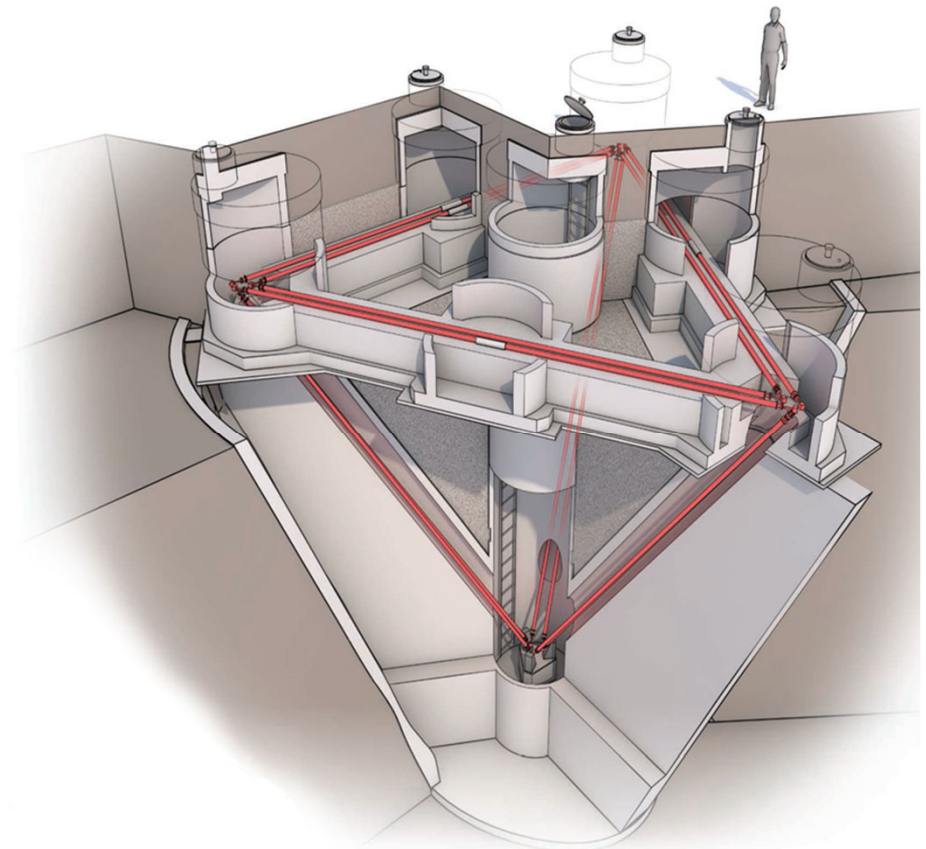
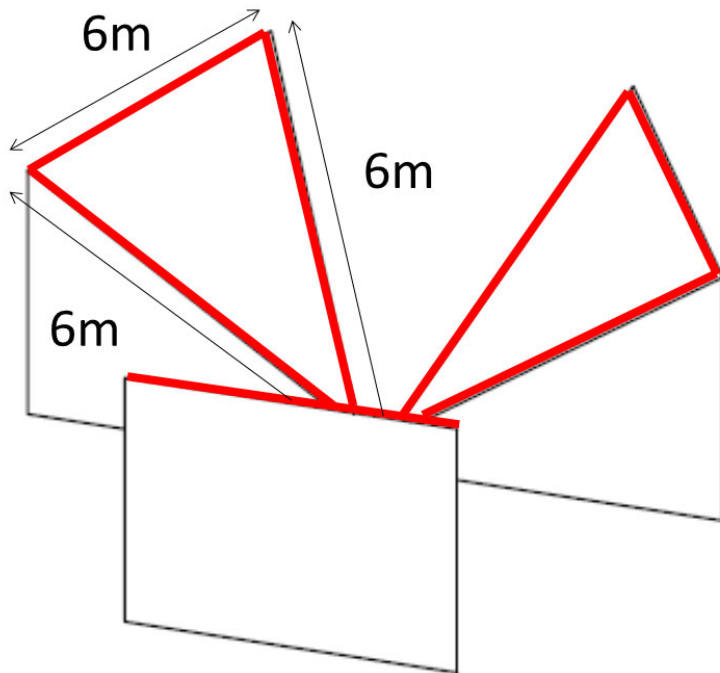


Measuring the complete  
rotation vector:

**The ROMY Ring Laser**

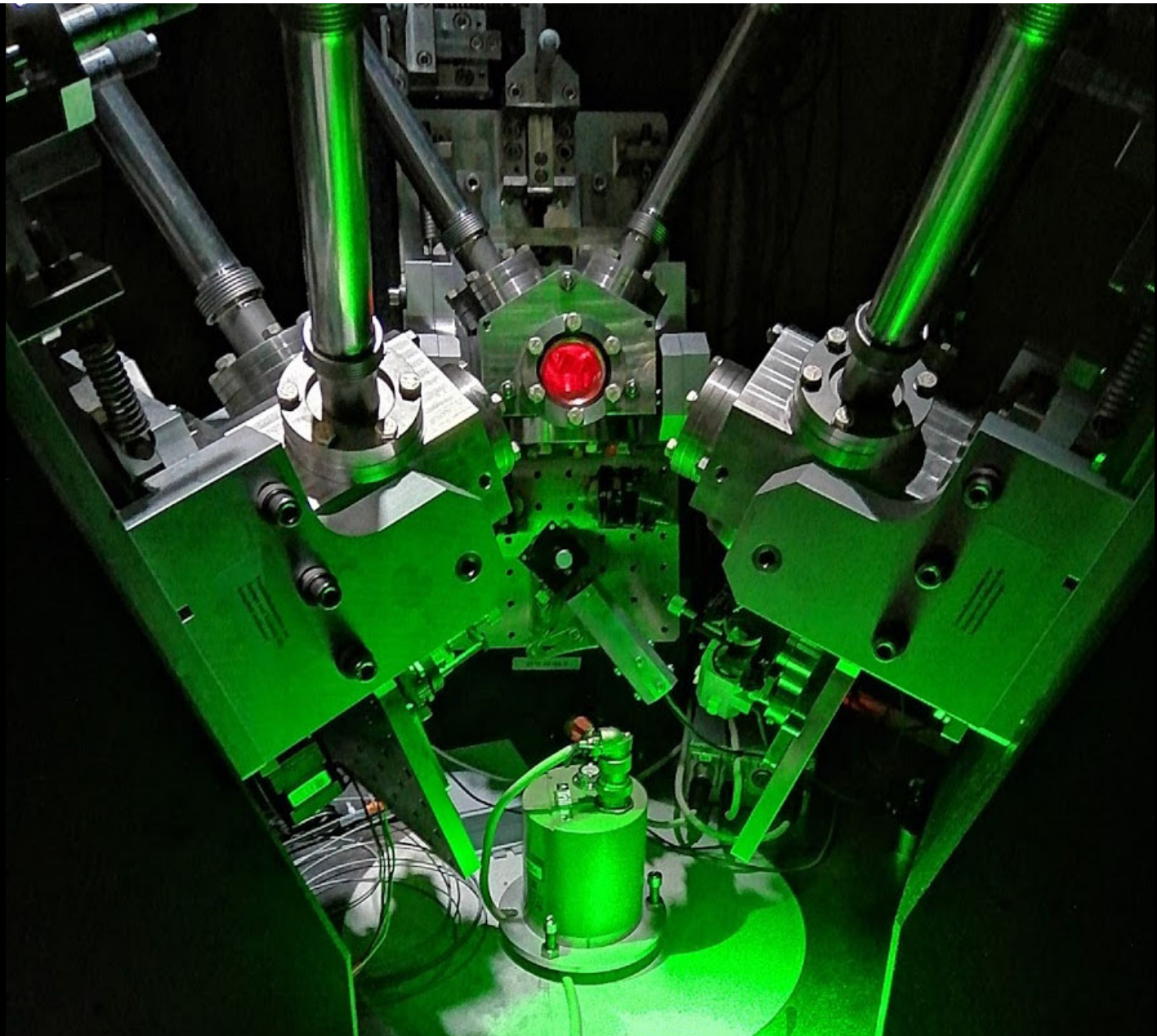
# The ERC ROMY Project

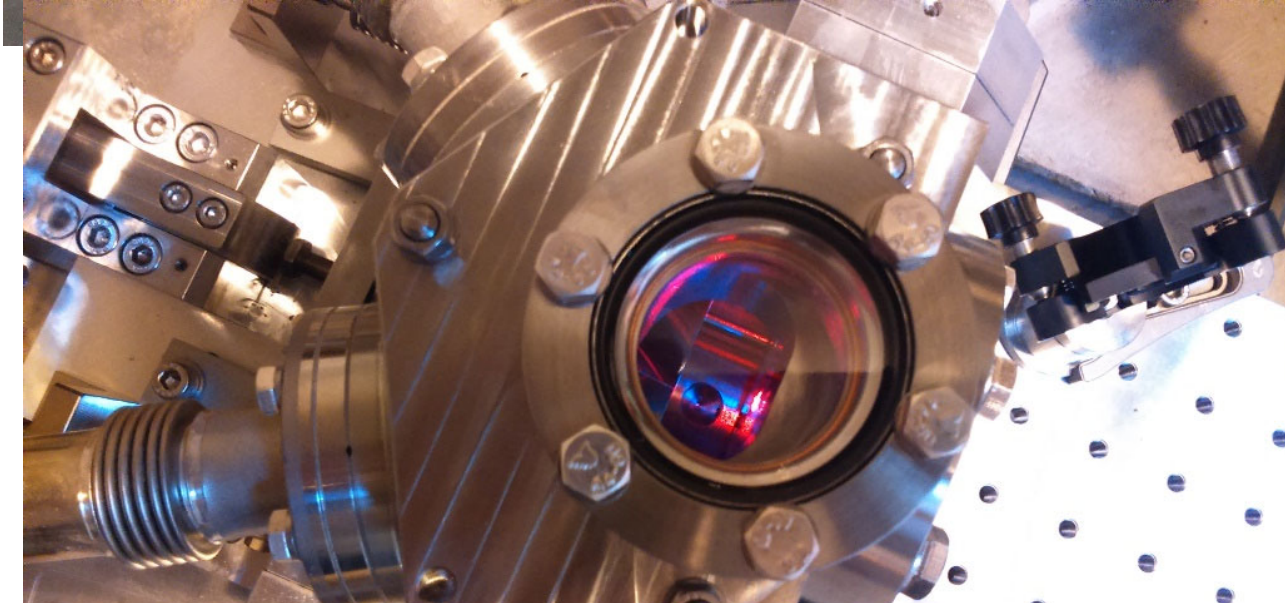
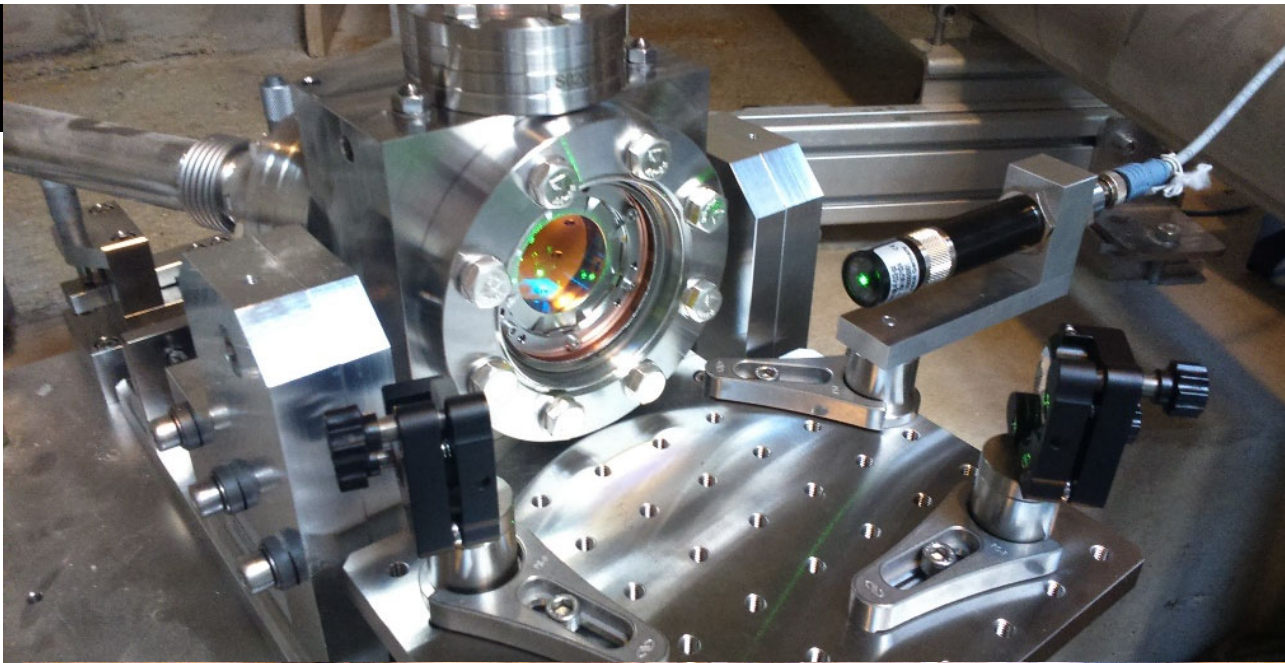
3-component planned -> finally 4 components (redundancy)



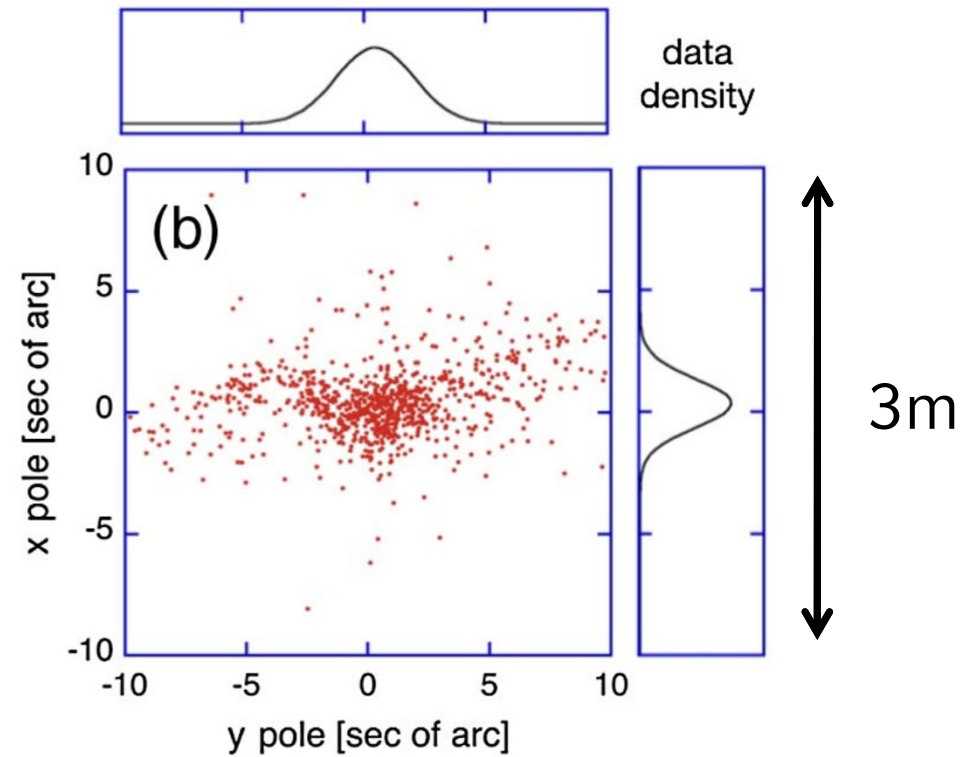
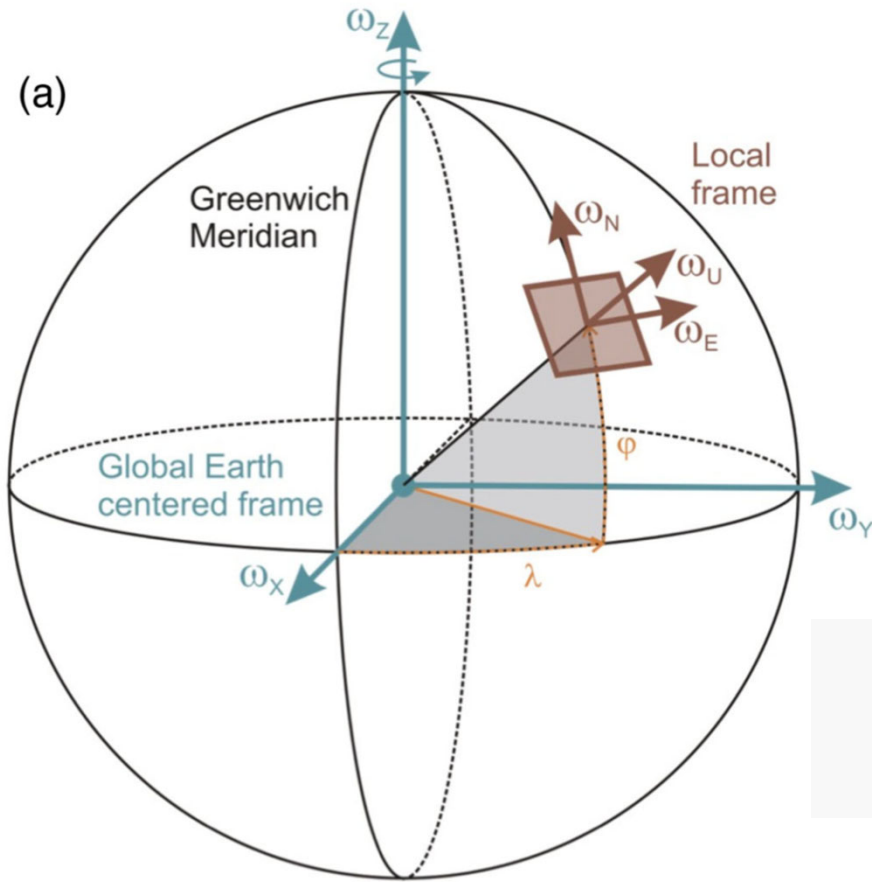
Hand, „Lord of the rings“, Science, 2017 (video on youtube) # 10



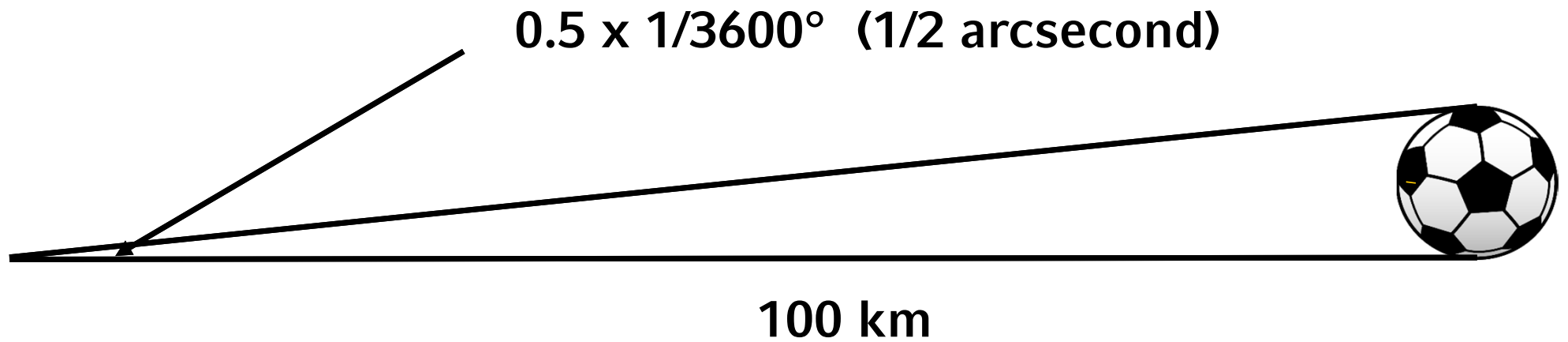




# Polar Motion – Rate change (world record, but ...)



# Angular Resolution



## Conclusions – Geodetic applications

- Most accurate **direct observation** of Earth's complete vector of rotation
- Stability over one week less than 0.1 asec of **polar motion** (3m)
- $4 \times 10^{-7}$  relative resolution of **Earth's rotation rate** (over one week)
- We observe **drifts** (settling of concrete structure?)
- Lasing difficult to **stabilize** due to proximity of resonance frequencies -> split mode (benefit and curse of ring laser size)
- Exact mixing of **isotopes** for two beam directions critical
- Efficient extraction of **Hydrogen** atoms crucial (getter)

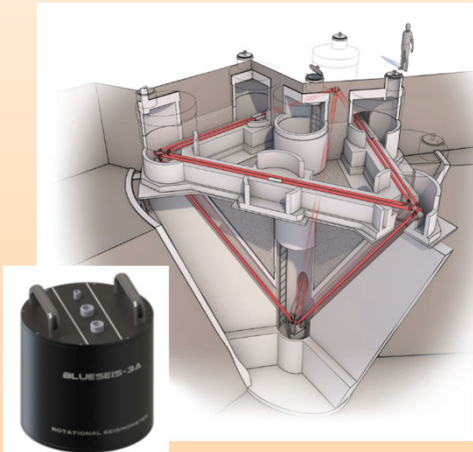
Future:

- **Geometry stabilization** for better long term stability and resolution



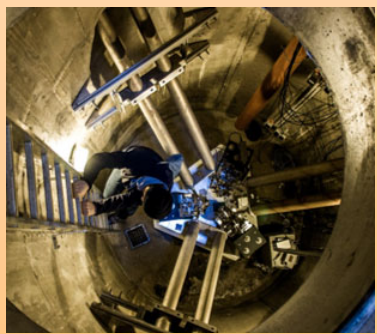
What about seismology?

# ... seismic instrumentation for ground motion?



Many components  
Very sensitive  
Difficult installation

Single point



ROMY ring laser



Nodal arrays  
Low sensitivity  
„Cheap“

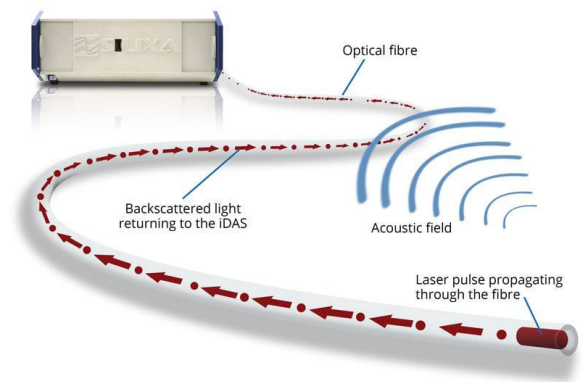
[myshake.berkeley.edu](http://myshake.berkeley.edu)

Billions of sensors



... any combination ...

But how?



*distributed acoustic sensing (DAS)*  
Graphics, silixa.com

# Complete ground motion - Translation, strain, rotation

$$\begin{aligned}\mathbf{u}(\mathbf{x} + \delta\mathbf{x}) &\approx \mathbf{u}(\mathbf{x}) + \mathbf{G} \delta\mathbf{x} \\ &= \mathbf{u}(\mathbf{x}) + \boldsymbol{\varepsilon} \delta\mathbf{x} + \boldsymbol{\Omega} \delta\mathbf{x} \\ &= \mathbf{u}(\mathbf{x}) + \boldsymbol{\varepsilon} \delta\mathbf{x} + \boldsymbol{\omega} \times \delta\mathbf{x}\end{aligned}$$



translation

$$\varepsilon_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$$

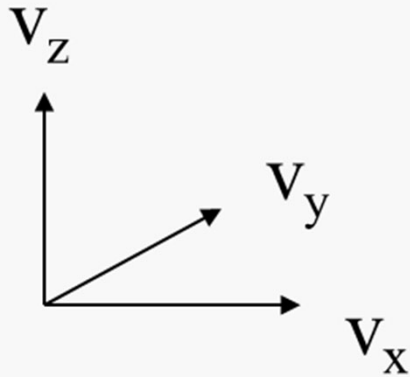
strain

$$\omega_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} - \frac{\partial u_j}{\partial x_i} \right)$$

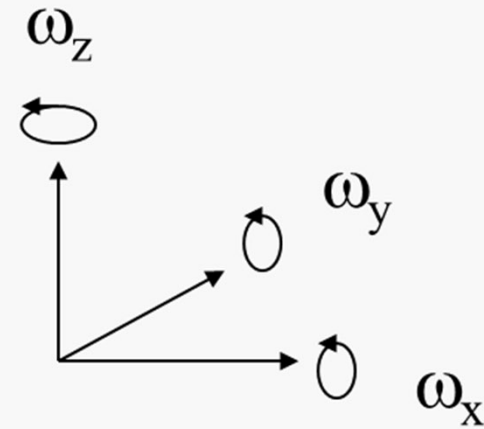
rotation

$$\boldsymbol{\omega} = \frac{1}{2} (\nabla \times \mathbf{u})$$

## 6 DoF seismic observations for seismology



Ground velocity  
***Seismometer***

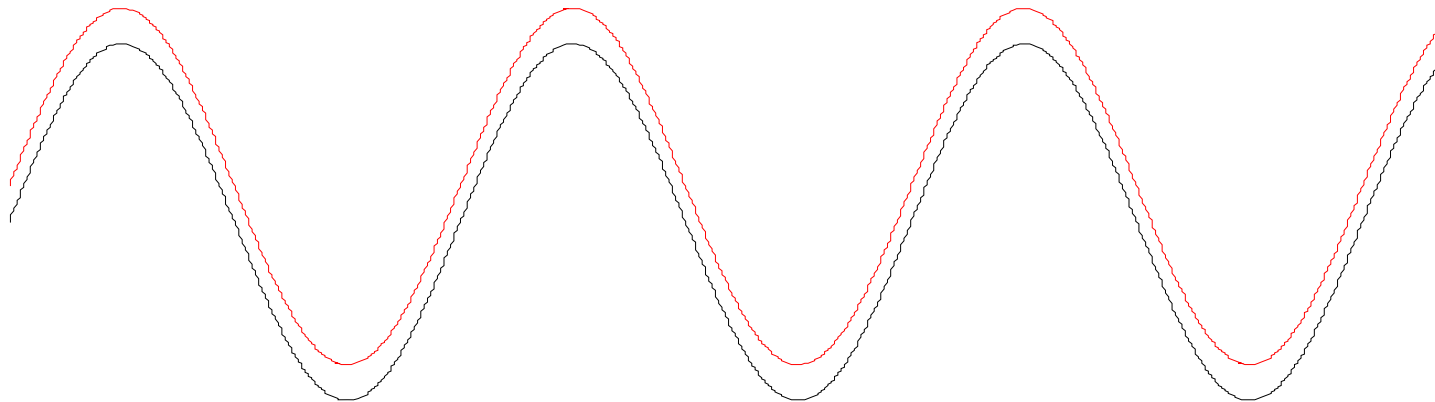


Rotation rate  
***Rotation sensor***

# Primer - Rotational Seismology

Plane transversely polarized (S or Love) wave propagating in x-direction with phase velocity  $c$

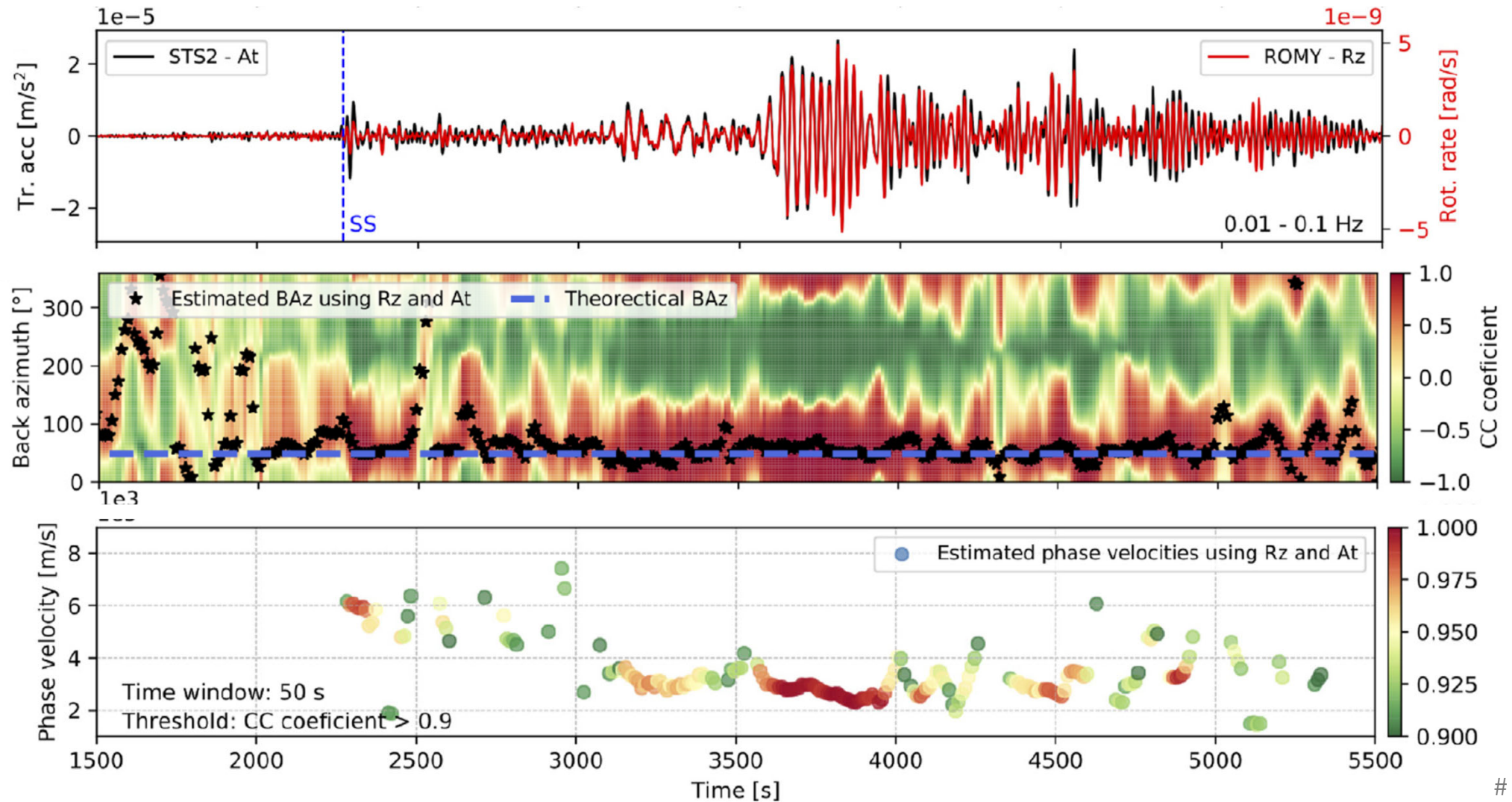
**rotation rate** – **transverse acceleration**



$$\frac{\ddot{u}_y(x, t)}{\Omega_z(x, t)} = -2c$$

Rotation rate and acceleration should be **in phase** and the amplitudes scaled by **two times the horizontal phase velocity**

# Real data – P.N.G. M7.6, 2019 (Igel et al., GJI, 2021)

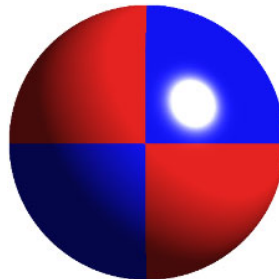
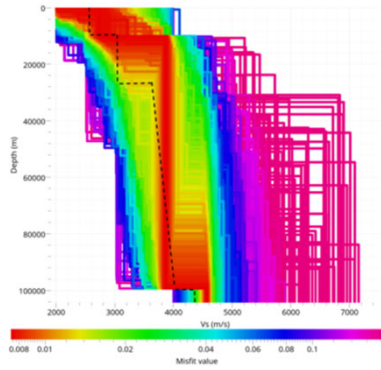
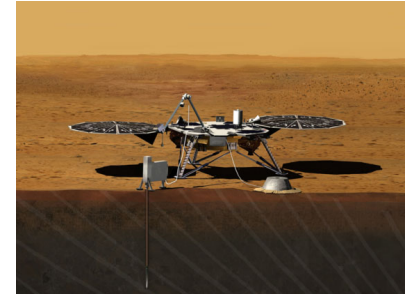
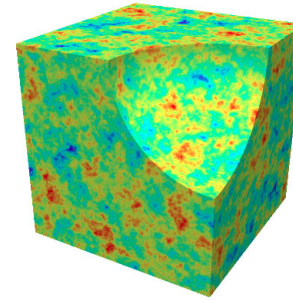
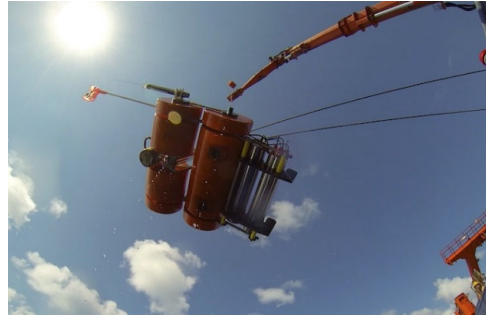


# Why 6+ DoF (same ideas apply to strain!)?

6+ DoF point observations provide wavefield information **similar to small-scale seismic arrays** (slowness, backazimuth, phase separation)

(e.g., Schlüter 1903; Sollberger et al., GJI, 2017; Sollberger et al., Sensors, 2020)

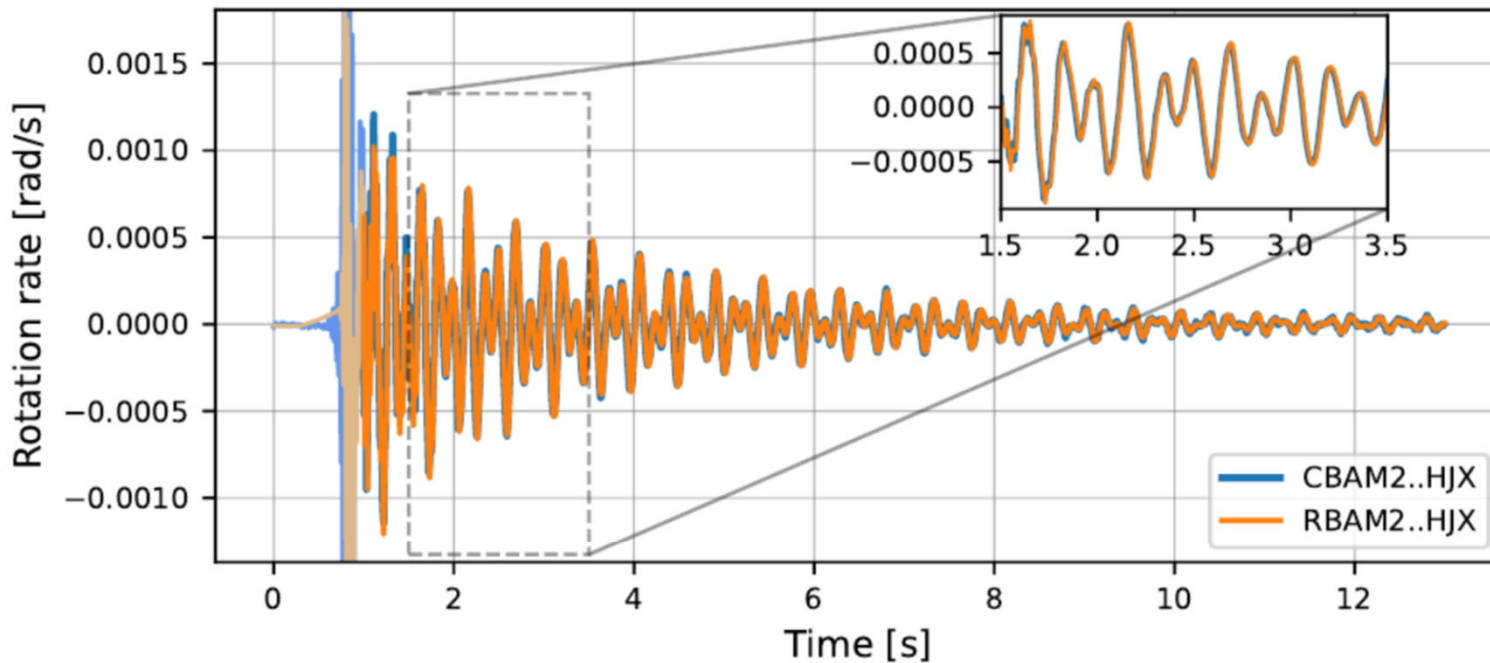
... wide range of applications ...





# Seismology needs a portable sensor!

SP2-vertical, 1.0 Hz - 40 Hz, cc = 0.9525



## IS-3A ROTATIONAL SEISMOMETER

HIGH-GRADE 3-COMPONENT SEISMOMETER FOR LAND APPLICATIONS

Recognizes the possibility to explore rotational ground motion. Recognized for its mastery of Fiber Optic Gyroscope (FOG), the **ixBlue** group stands as a high-grade applications such as inertial navigation, hydrography and satellite. Its 30 years' unchallenged expertise, **ixBlue** revolutionizes geosciences by product that seismology has always been looking for. **BlueSeis-3A** is today able answer to the rotational seismometer need: 3-axis, broadband, low-noise and flat passband solution with "geosciences-ready" interfaces including

### BENEFITS

OG) for

- Rotation as a new observable in seismology!
- Easy to deploy: no calibration, no tilt range limitation, insensitive to environmental conditions
- Heading provided by the system
- 2-in-1: "weak motion" low-noise + "strong motion" dynamic
- Plug and play interfaces

ography • Volcanology • Earthquake physics • Geophysical exploration

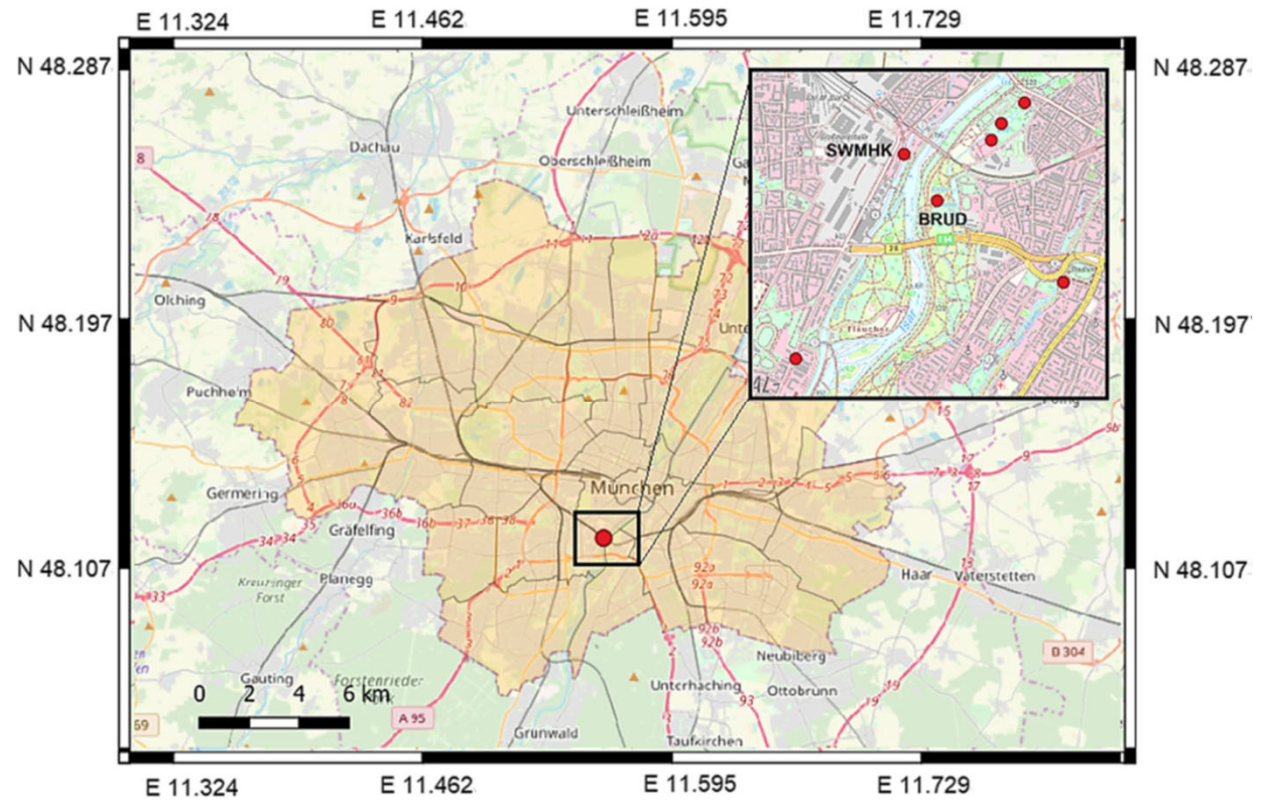


# Measuring site effects in an urban environment



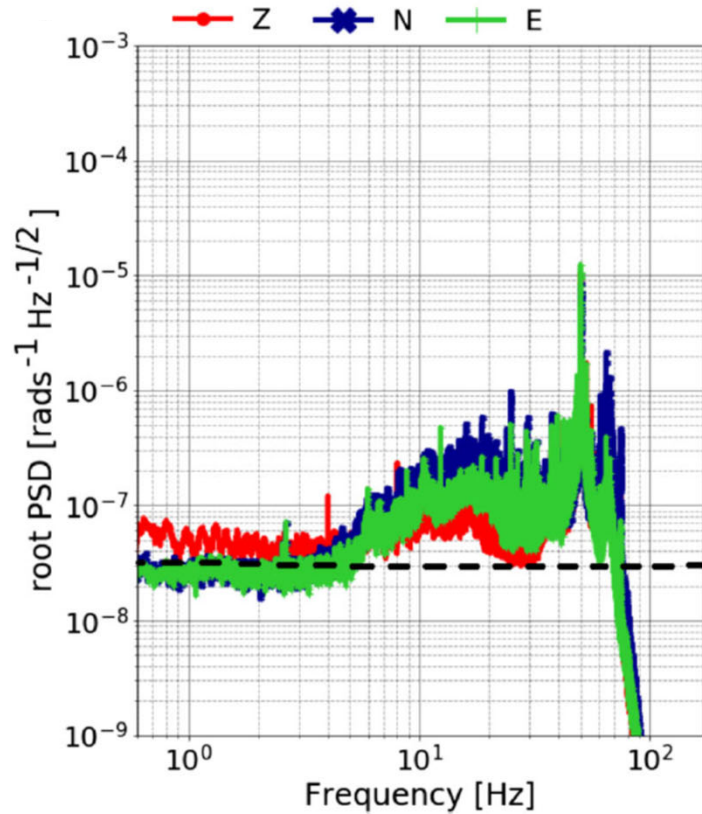
# Microzonation Downtown Munich

## Single-site seismic tomography

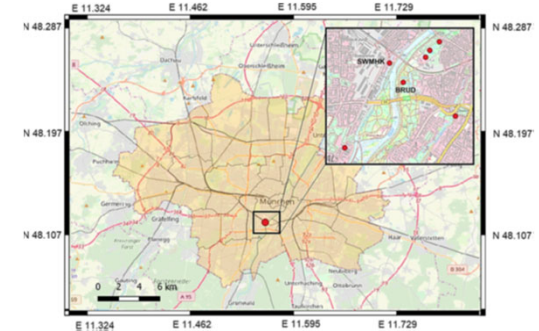
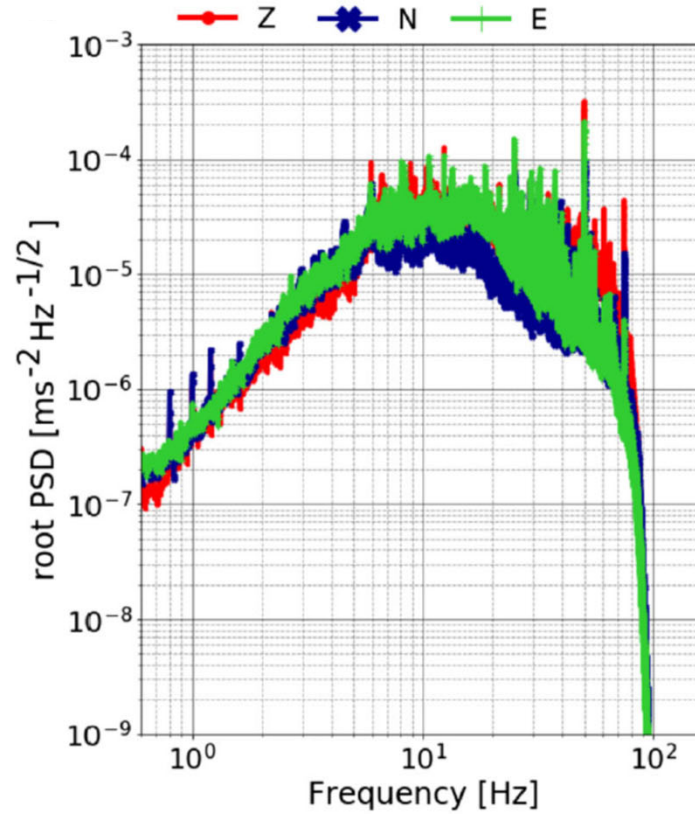


# Microzonation Downtown Munich- City Noise

## Rotation Rate

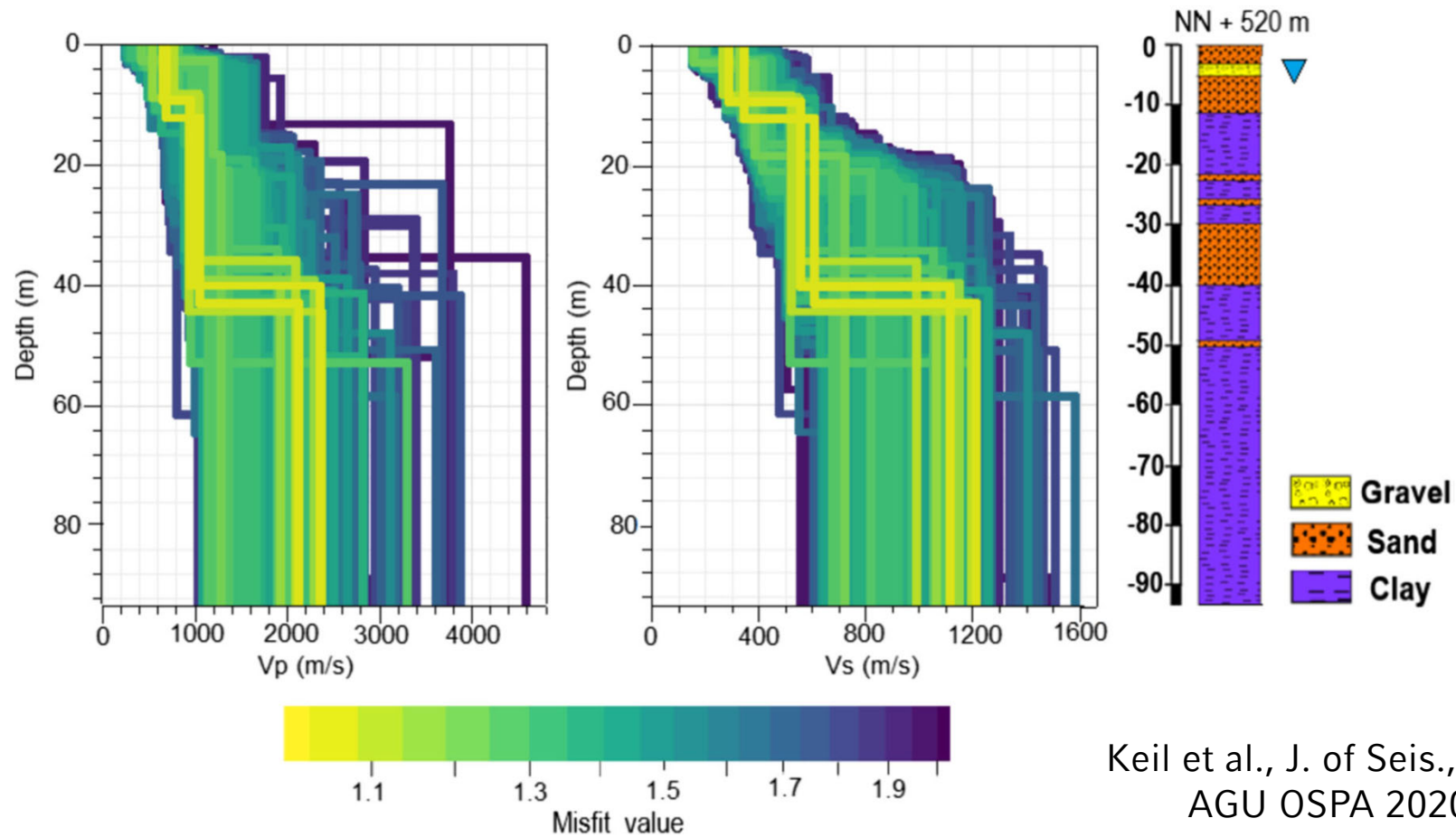


## Acceleration



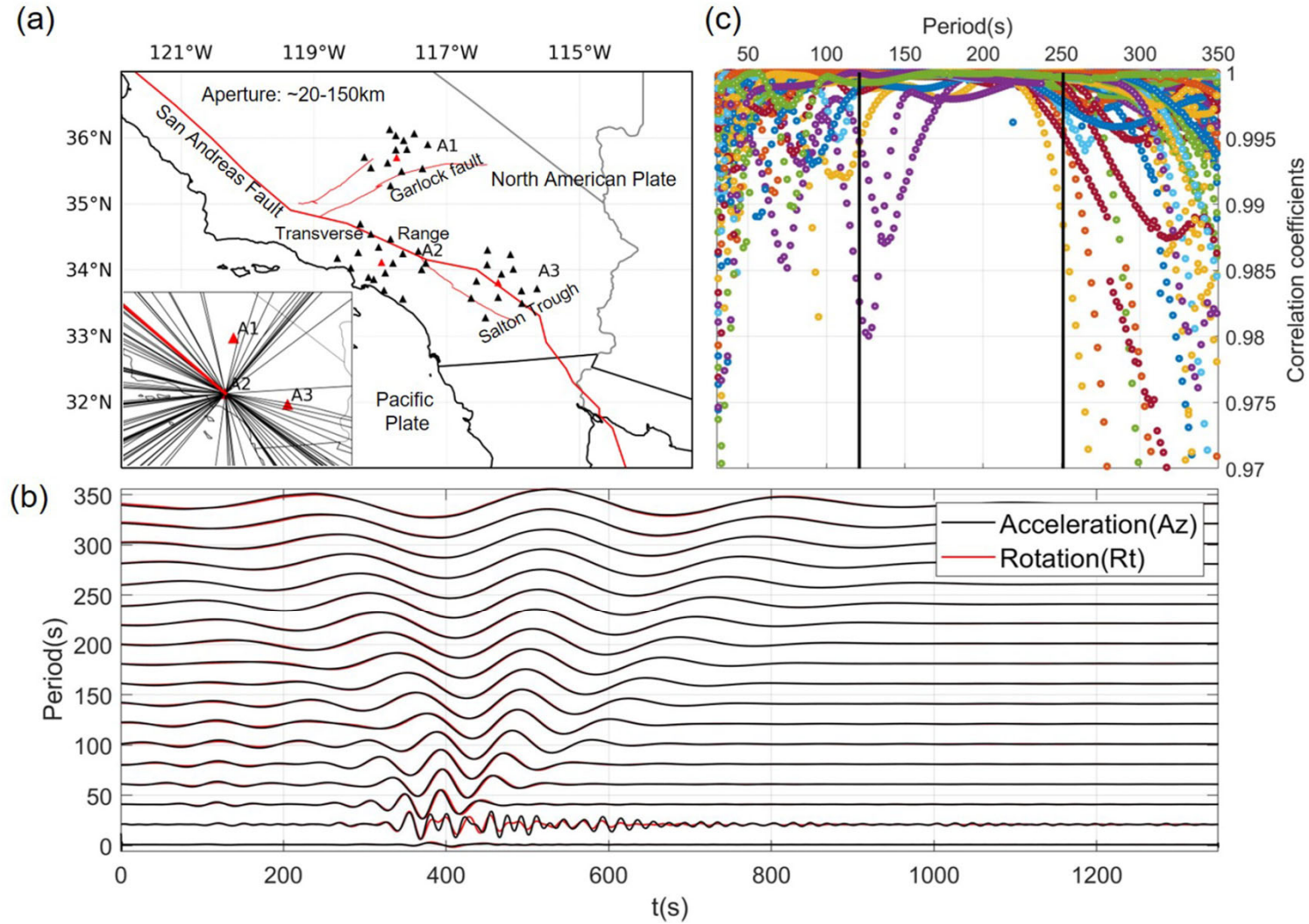
The spectral ratio leads to **phase velocities** -> (dispersion)

# Local 1D velocity – 6 DoF and H/V

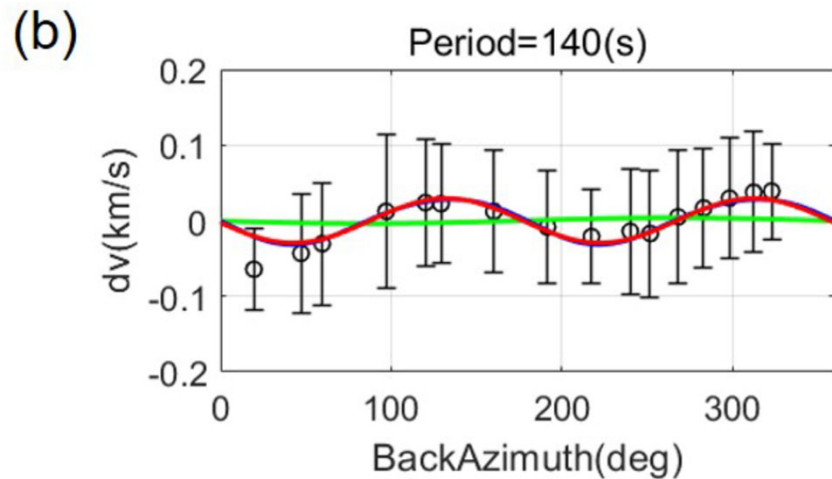
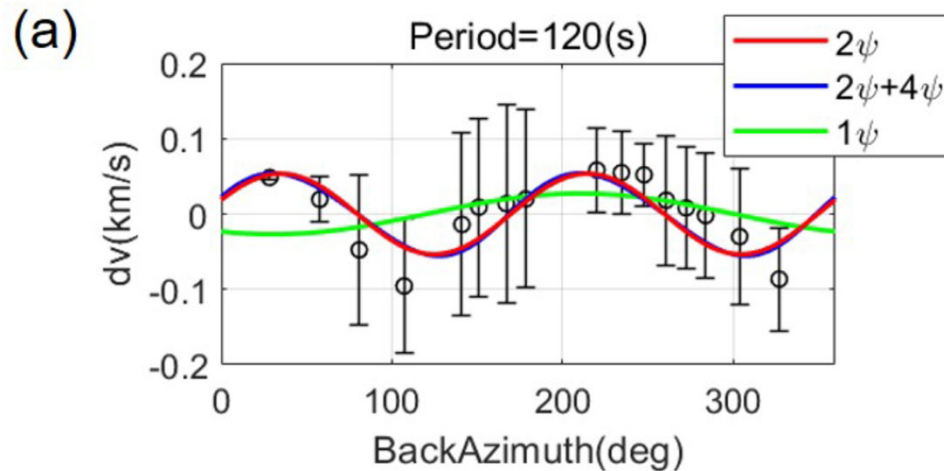


Keil et al., J. of Seis., 2020  
AGU OSPA 2020

# Anisotropy from rotations

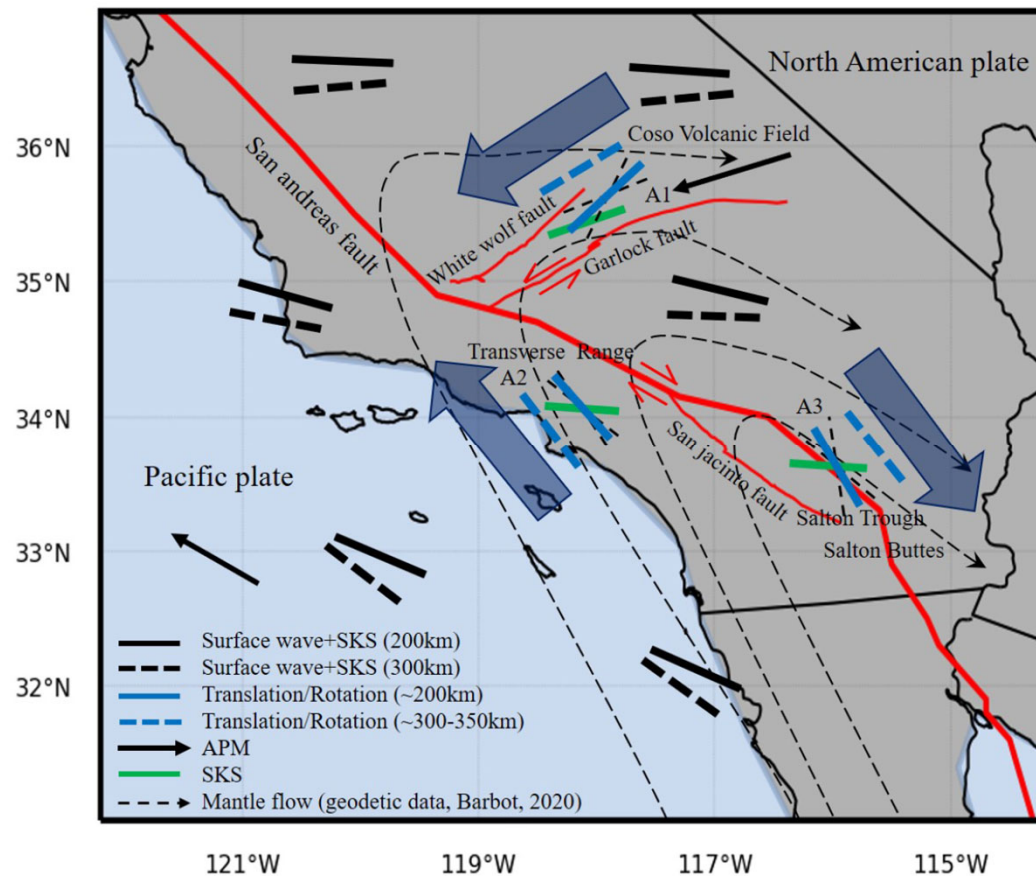


# Anisotropy from rotations



- Azimuthal variations of surface wave velocity from **point observations** of rotations and translations
- Clear evidence for azimuthal anisotropy (upper mantle tectonic flow)

# Anisotropy and mantle flow

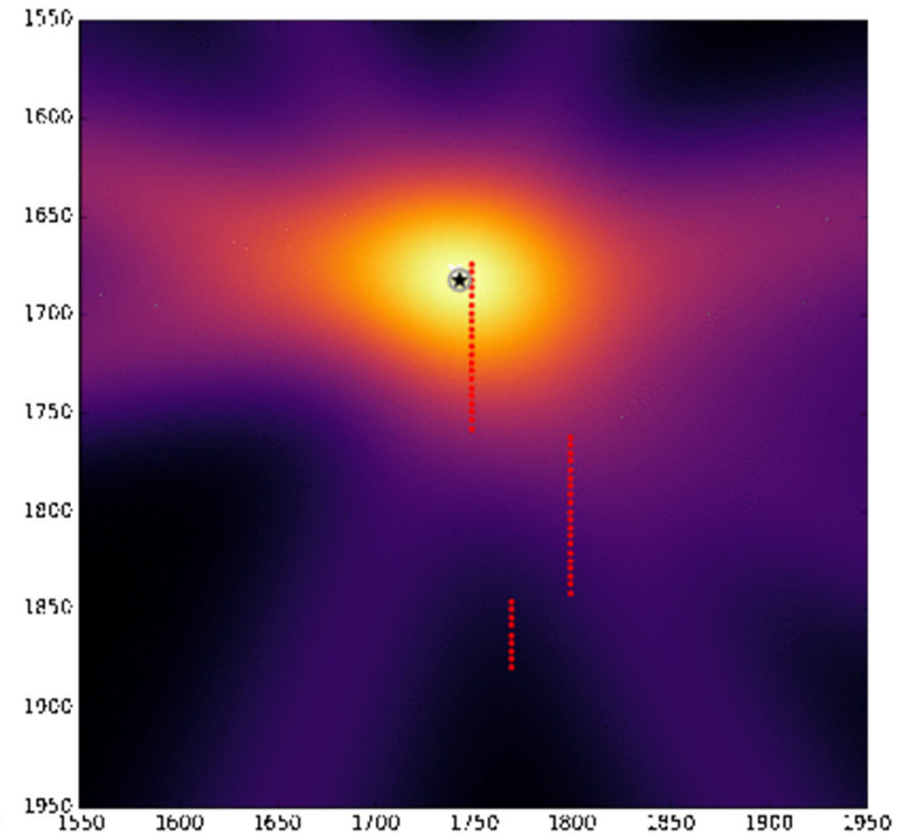
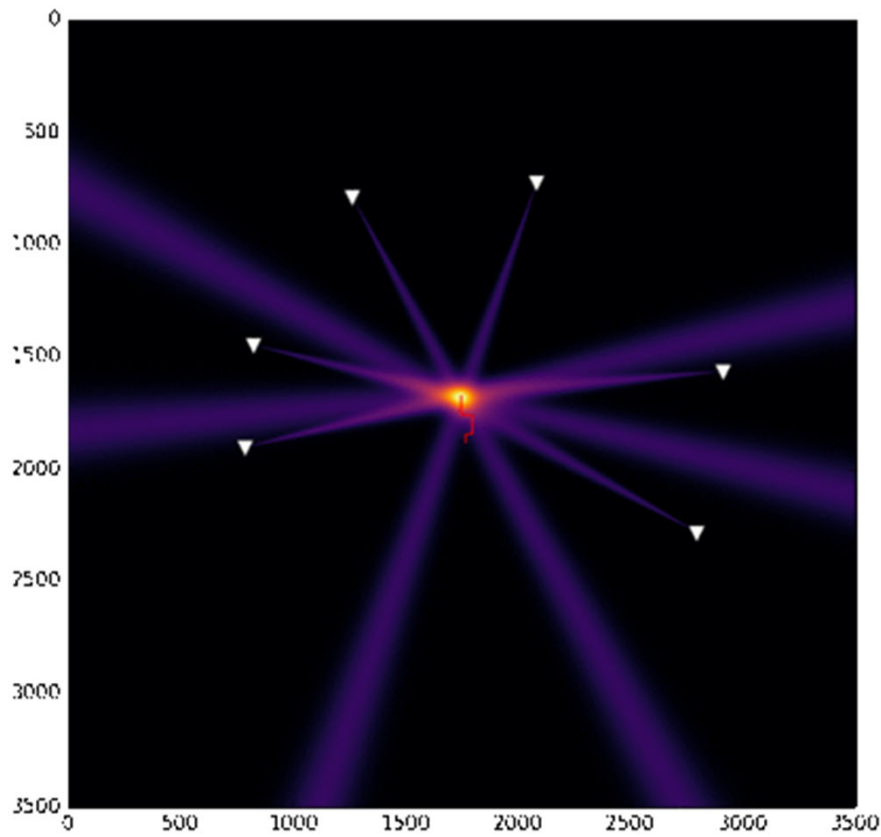


- Azimuthal variations of surface wave velocity from **point observations** of rotations and translations
- Clear evidence for azimuthal anisotropy (upper mantle tectonic flow)
- Fast velocity directions compatible with GPS observations

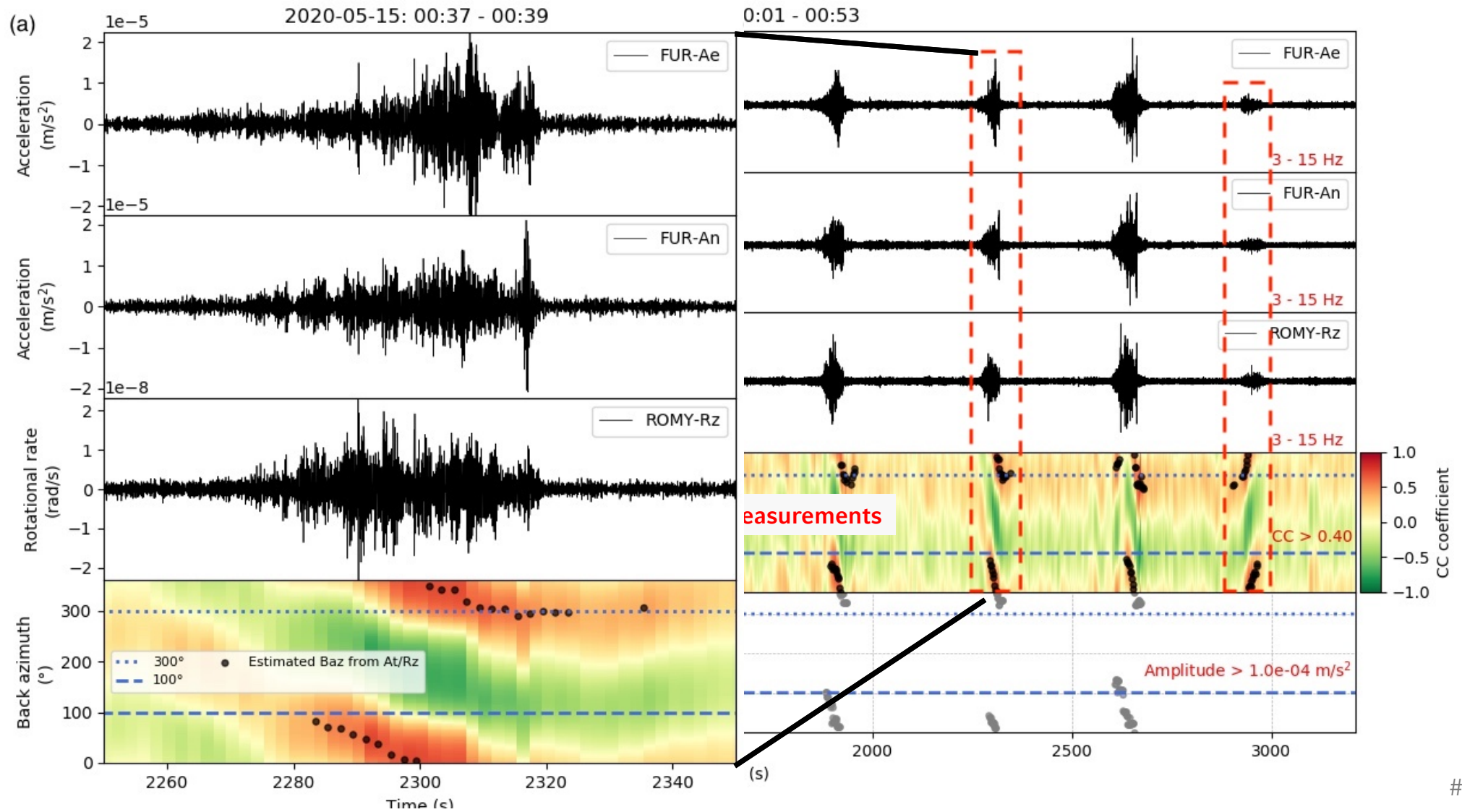
Tang et al. (to be submitted)



# Tracking seismic sources

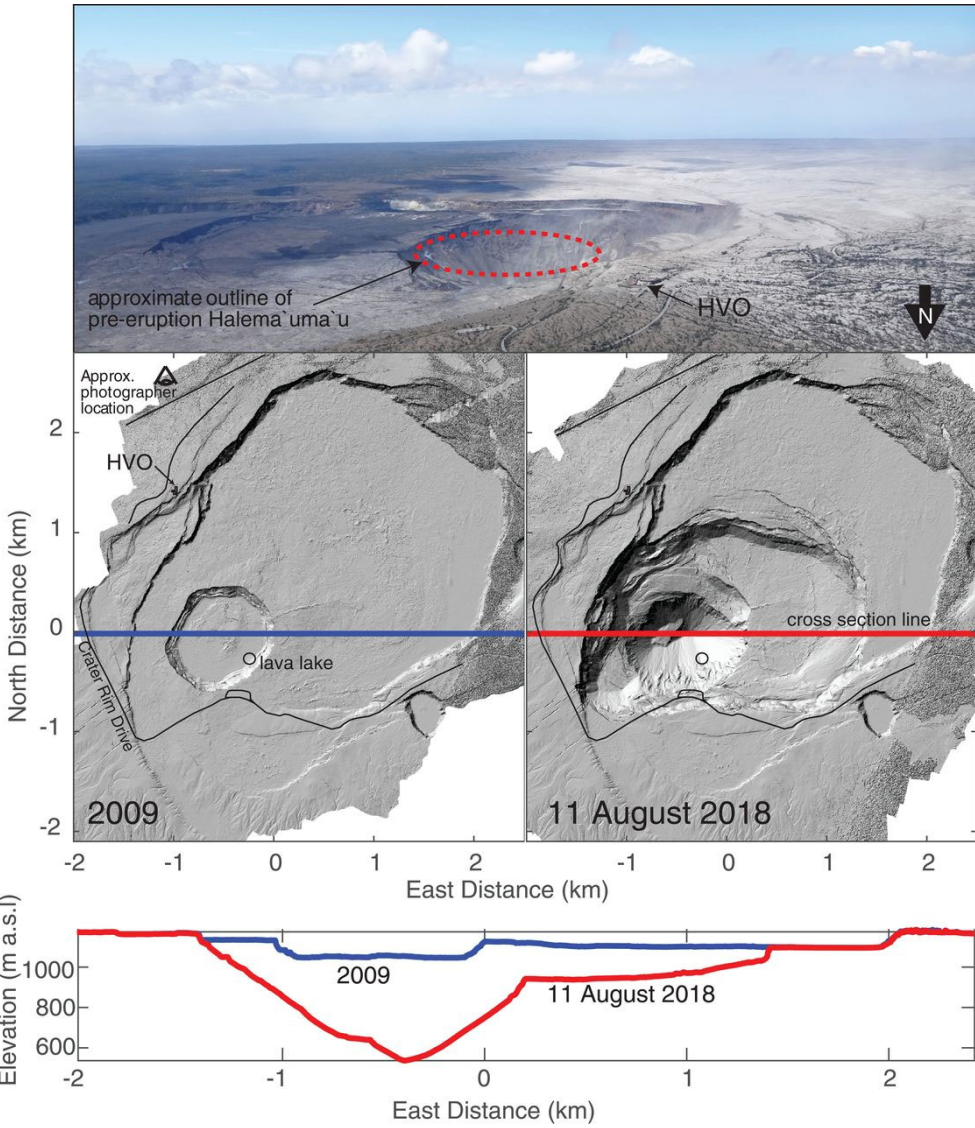


# Singe-station speed control (Yuan et al., JGR, 2021)

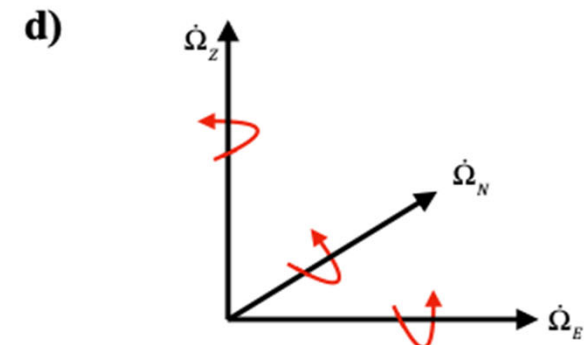
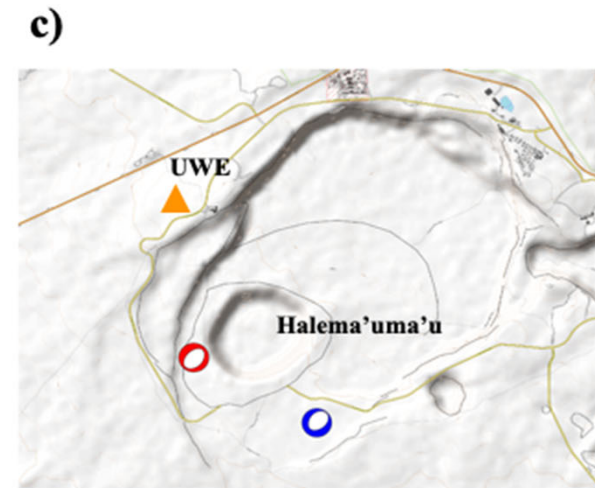
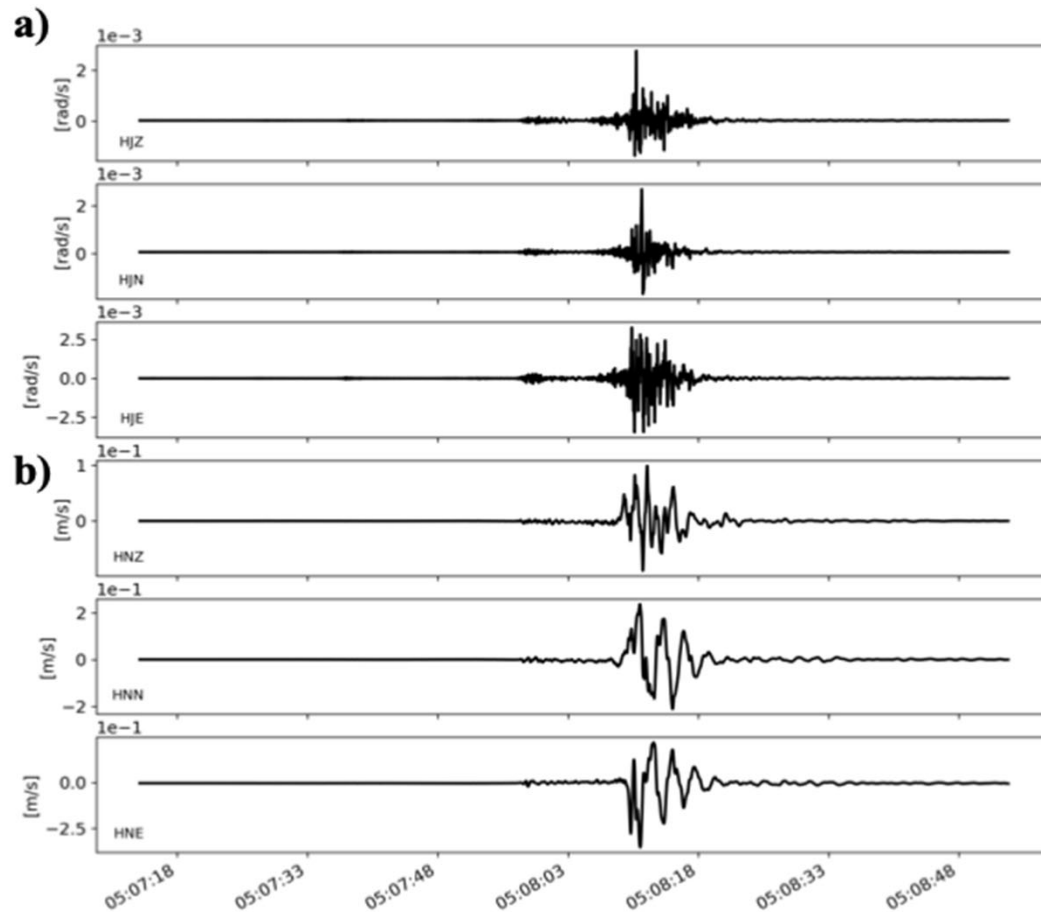


# Caldera collaps: Strong ground motions

# Before - After

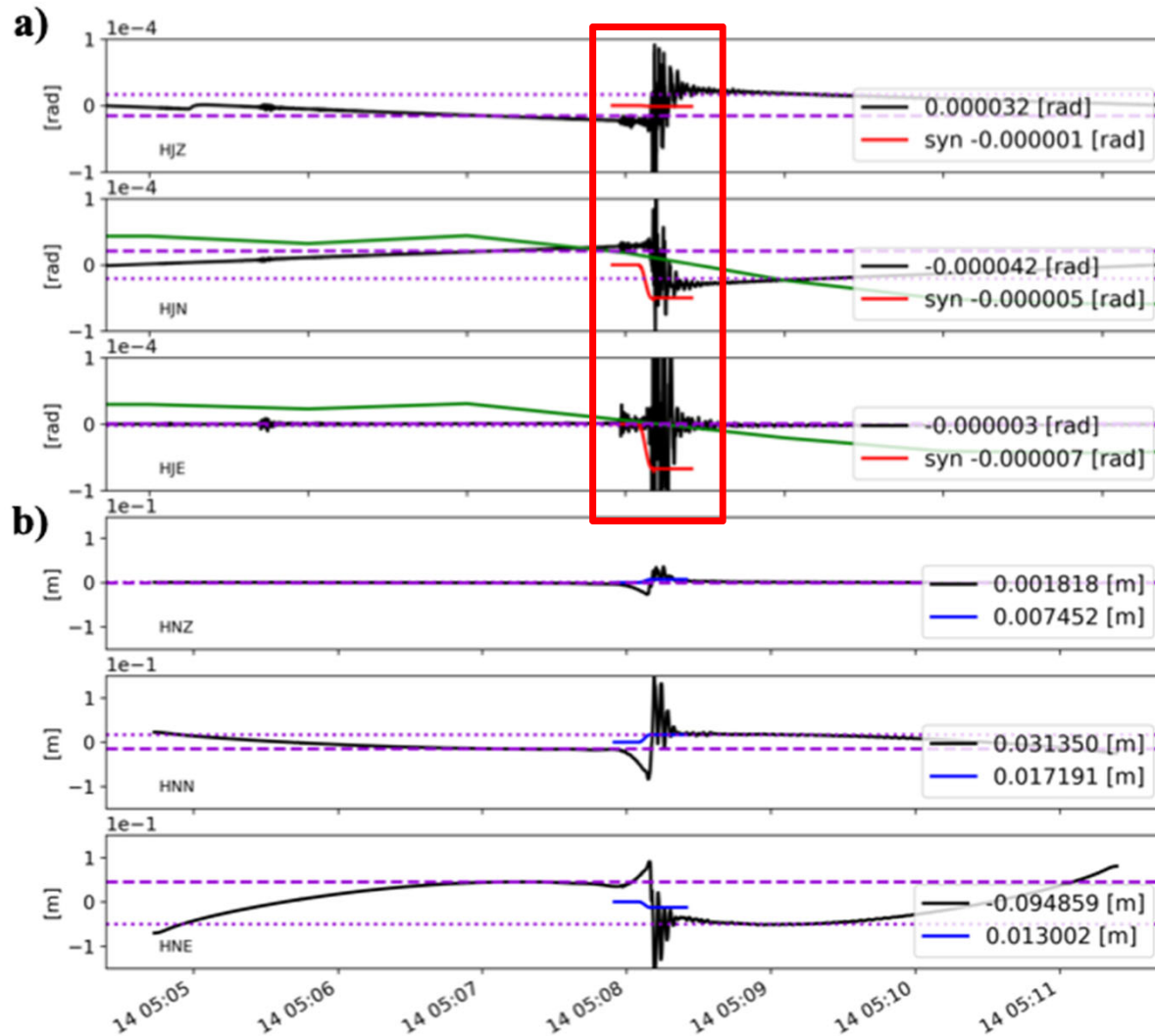


# 6 DoF Observations Hawaii



(Wassermann et al., GRL, 2020)

# Static Rotation Observations



First dynamic observation of **static rotation changes** with blueSeis

- Additional constraints on caldera collapse
- Tilt correction for displacement sensors

(Wassermann et al., GRL, 2020)

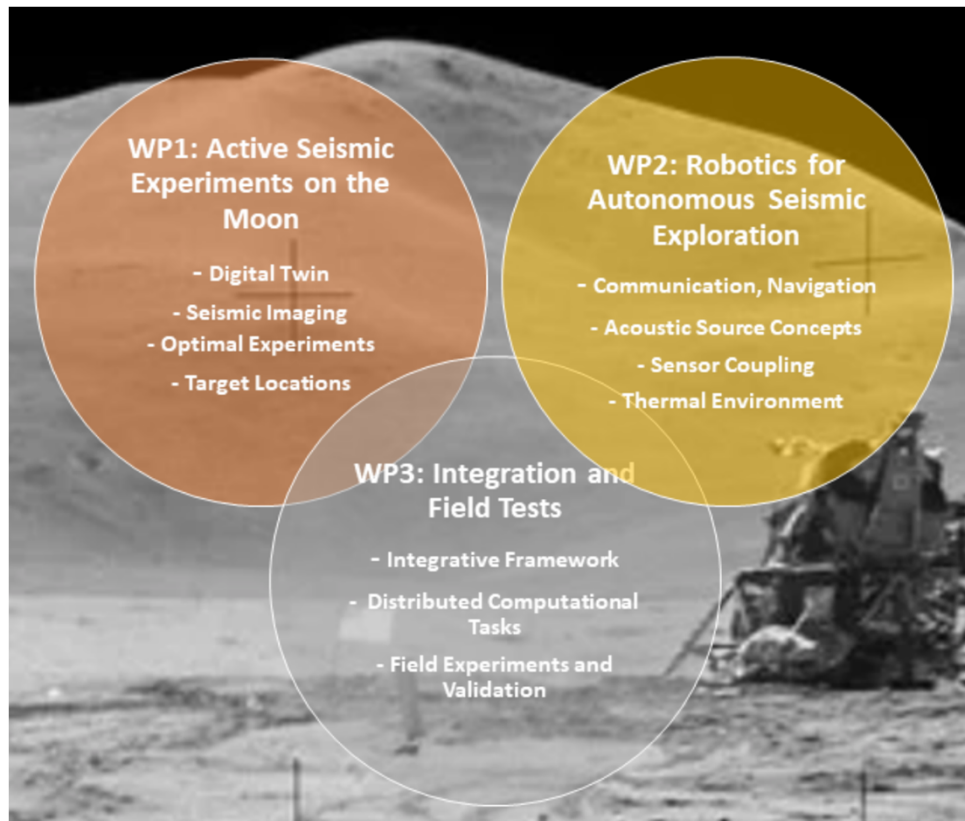
# Not shown here ...

- 6C allows **correcting tilt contamination** (OBS, strong ground motion) – Lindner et al. (2016), Bernauer et al. (2020a)
- 6C allows new ways of **seismic tomography without travel times** - Fichtner et al. (2009), Bernauer et al. (2012)
- 6C is interesting for **planetary seismology**, prototype in development – Bernauer et al. (2020b)
- 6C is interesting for **structural health monitoring** – GIOTTO project, see youtube movie (<https://youtu.be/szYqnmuEoNw>)
- 6C has benefits when inverting for **moment tensors** – Donner et al. (2018,2020)
- 6C has benefits for **finite-source inversion** – Bernauer et al. (2014), Reinwald et al. (2016)

# Outlook

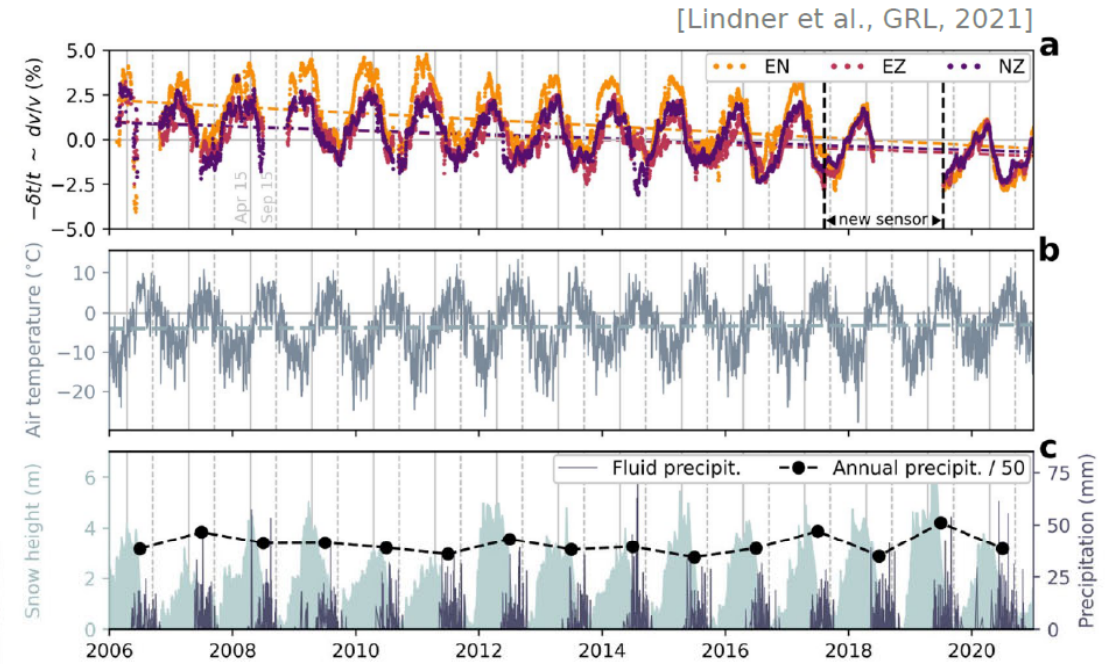
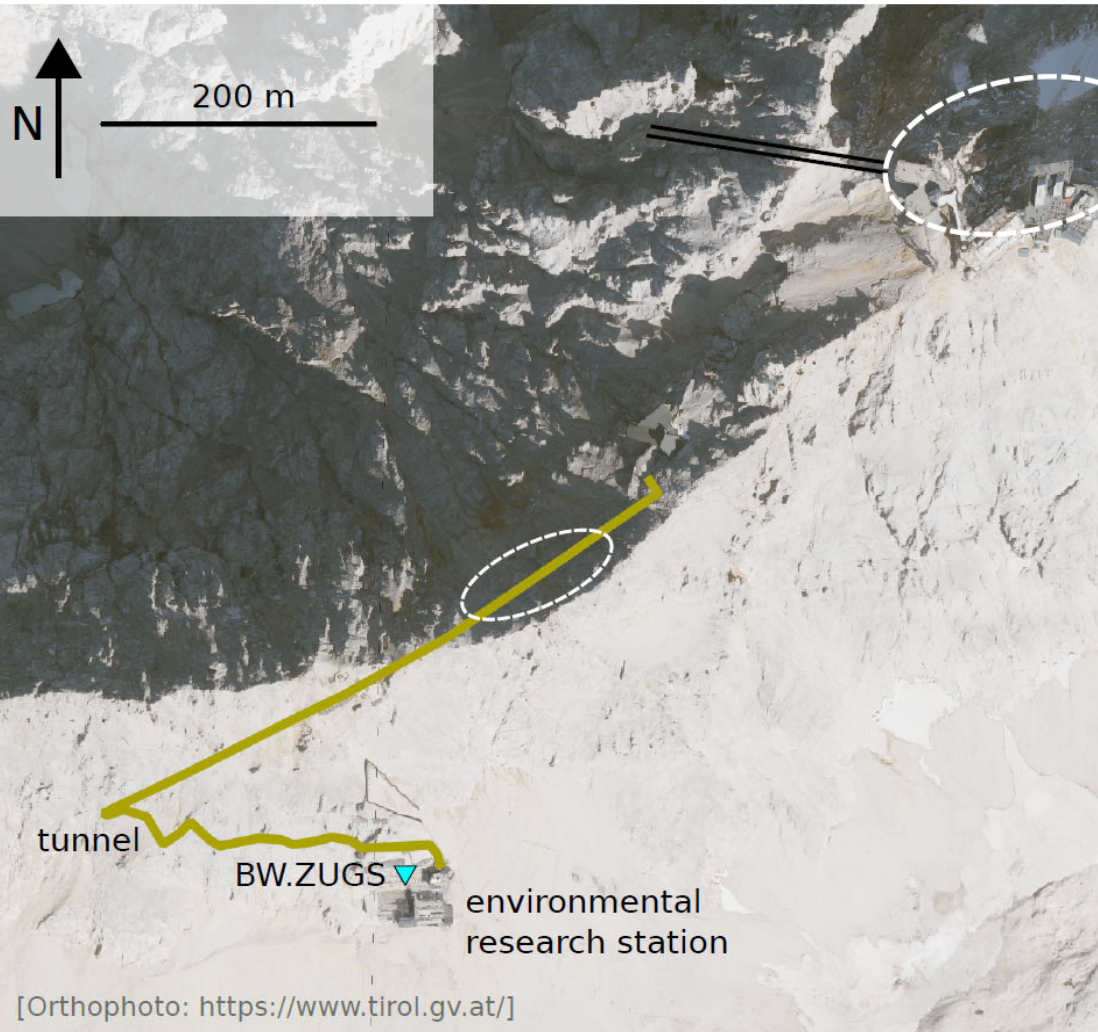


# Robotic seismic networks



- **Wave propagation in strongly scattering media**
- **Coda wave interferometry**
- **Near surface imaging**
- **Gradient observations (rotations, strain)**
- **Characteristic wavefields for target objects**
  - ice-bearing rocks
  - Cavities
- **Robotic concepts**
  - Navigation
  - Distributed computing
  - Tomography
  - Mobility

# Monitoring permafrost change – Mt Zugspitze, Germany



(Substantially) **increased sensitivity of gradient observations** (strain, rotations) w.r.t. near-receiver structure!

# Conclusions

- **Ring lasers** deliver most accurate rotation sensing for geodesy and seismology
- **Fibre-optic gyros** are the most promising rotation sensing instruments for 6C broadband seismology (but ...)
- Seismology now has a **portable broadband rotation sensor** (blueSeis-3A family)
- **Field studies** are only now beginning
- The most promising application domains are:
  - Microzonation (in cities)
  - Volcano monitoring
  - Ocean-bottom seismology
  - Earthquake physics (source studies)
  - Earthquake engineering (building vibrations)
  - Environmental seismology (permafrost, groundwater)
  - Planetary seismology (active seismics, lander interaction)

**Interested?** Check out:

- [www.rotational-seismology.org](http://www.rotational-seismology.org)
- [www.romy-erc.eu](http://www.romy-erc.eu)
- [https://www.mdpi.com/journal/sensors/special\\_issues/Rotatin\\_Rate\\_Sensors](https://www.mdpi.com/journal/sensors/special_issues/Rotatin_Rate_Sensors)



Thank you for your attention!