

Evolution of Resonant Self-interacting Dark Matter Halos

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Based on
AK and Hee Jung Kim, arXiv:2304.12621

June 23, 2023 @ Pollica Summer Workshop

Contents

Resonant self-interacting dark matter (SIDM)

- sharp velocity dependence of self-scattering cross section
- are resonant SIDM halos similar to constant SIDM halos?

Evolution of resonant SIDM halos

- isothermal region does not evolve monotonically from inside to outside unlike constant SIDM
- formation, development and thermalization of **density break**

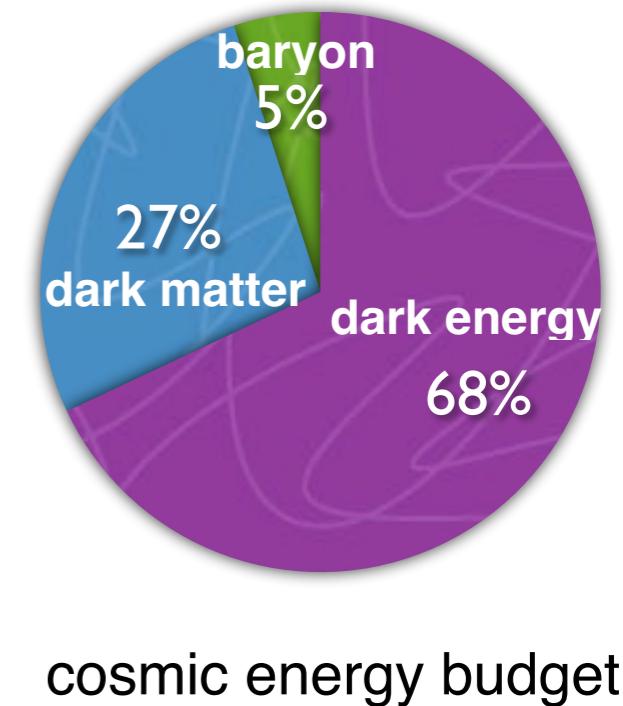
Possible imprints on observations

- density break in a certain mass range of halos
- change in stellar orbits by density break in the past

Dark matter

Dark matter

- evident from cosmological observations
 - cosmic microwave background (CMB)...
- essential to form galaxies in the Universe
- one of the biggest mysteries
 - astronomy, cosmology, particle physics...



Gravitational probes

- complementary to direct, indirect and collider searches
- how the star distribution changes w/ properties of dark matter
 - all known properties of dark matter are derived in this way (including its existence; SM neutrinos are too hot to form galaxies)

Dark matter

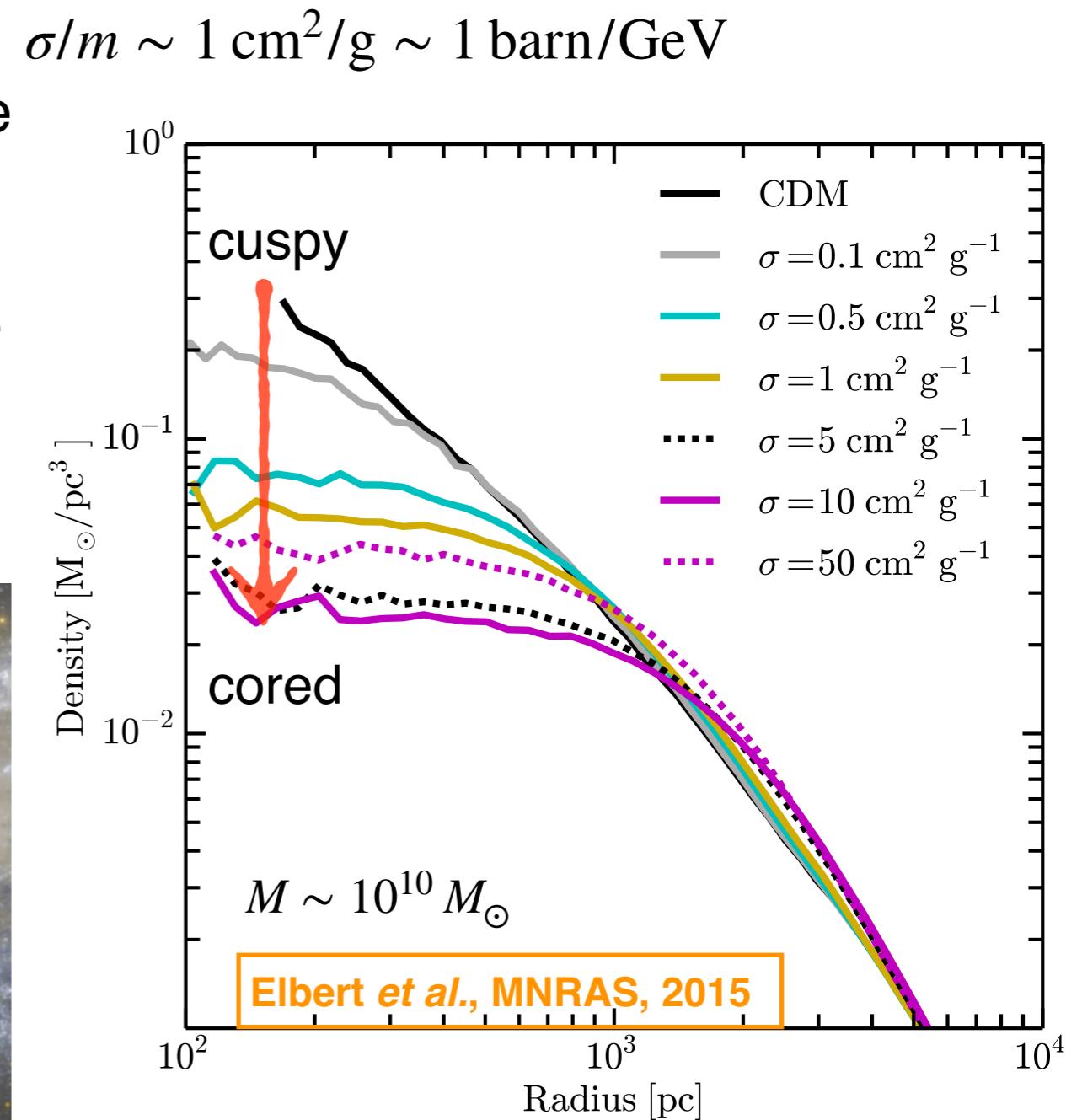
Self-interacting dark matter (SIDM)

- interactions **among** dark matter particles

- hard to probe in other searches

- dark matter density profile inside a halo turns from cuspy to cored

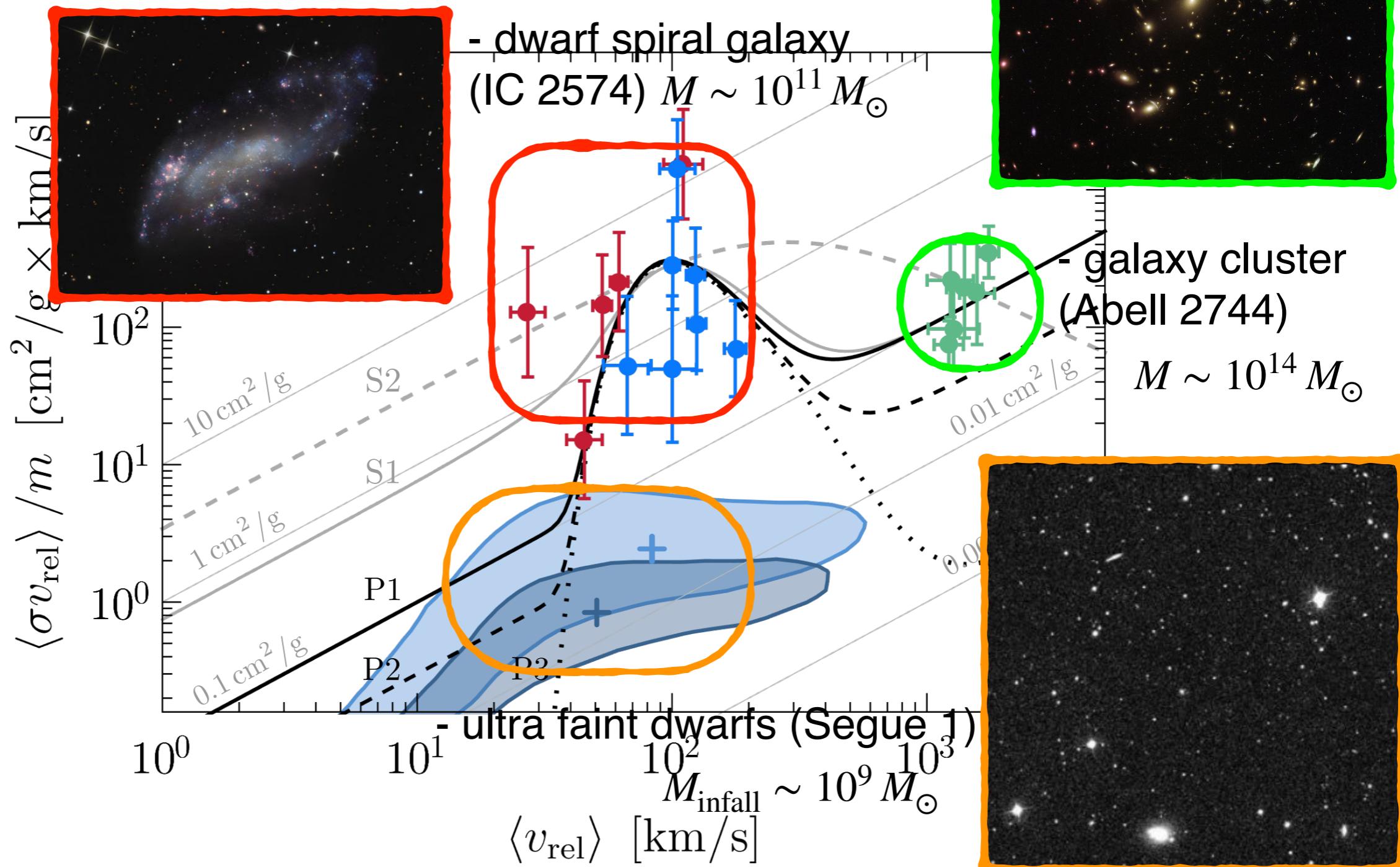
- cored profile “appear to” provide better fit to astronomical data



“Data” points

Overview

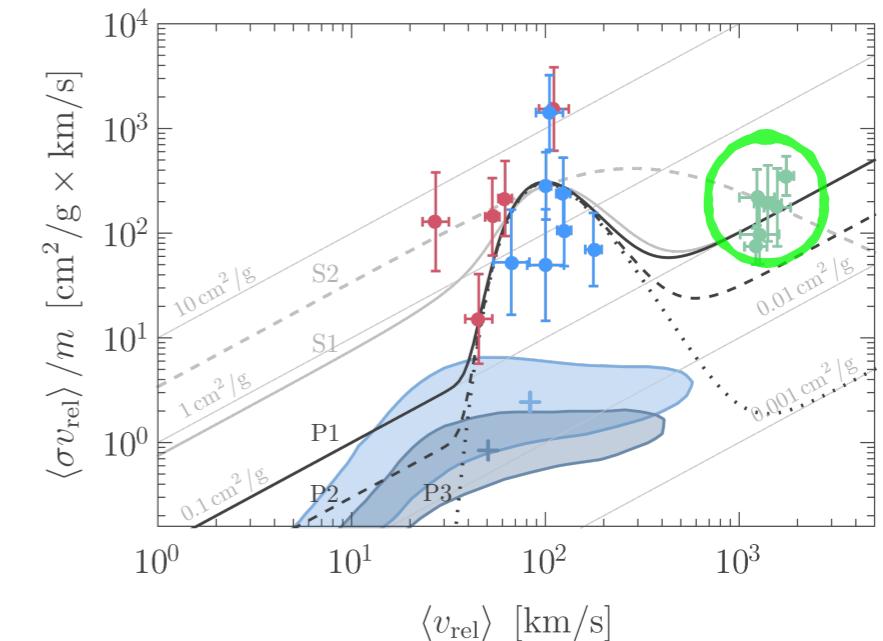
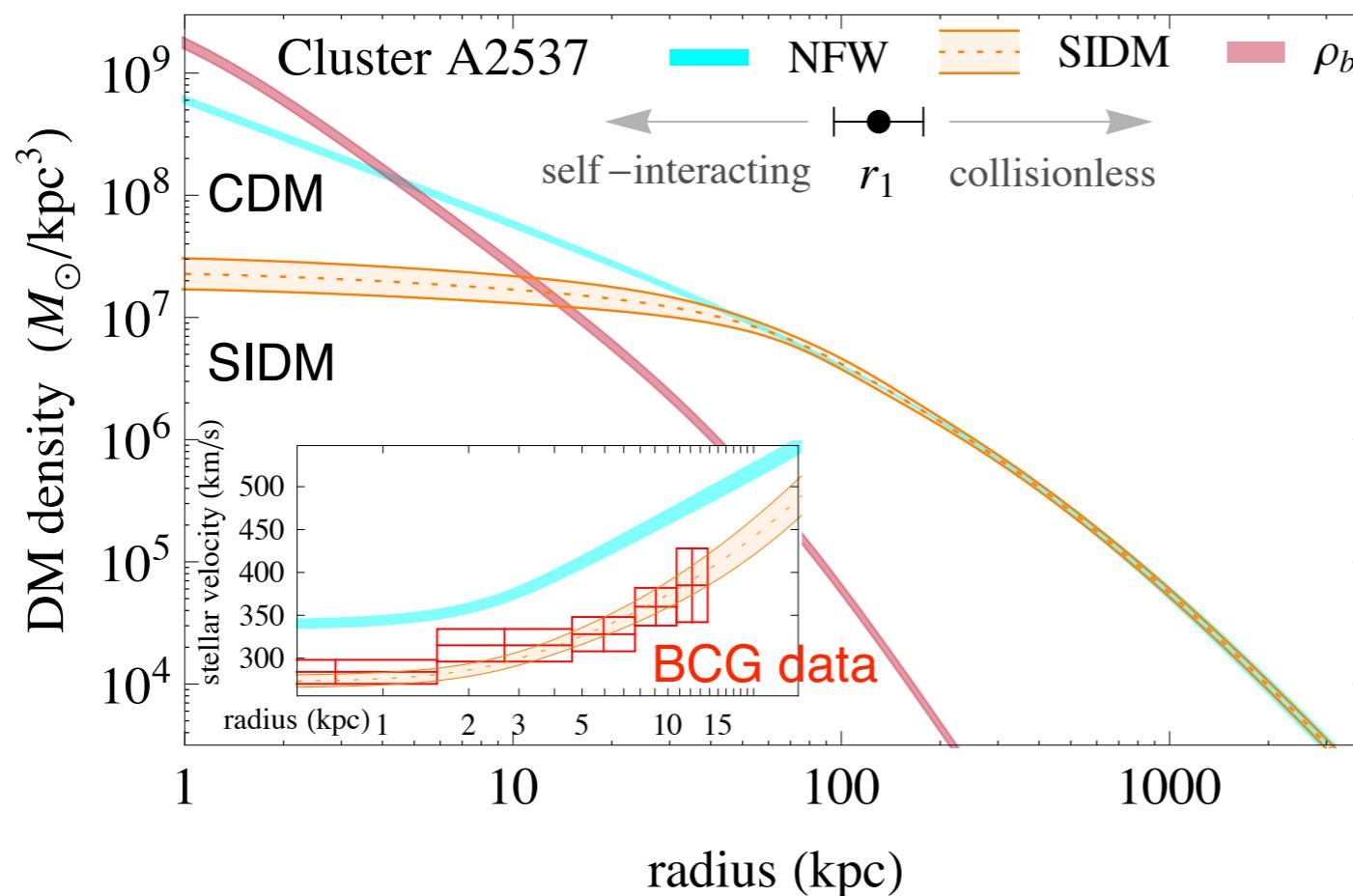
- cores in various-size halos may prefer sharp velocity dependence of self-scattering cross section



Data points

Galaxy clusters (GCs)

- mass distribution in the outer region is determined by strong/weak gravitational lensing
 - stellar kinematics in the central region (brightest cluster galaxies) prefer cored SIDM profile



$$\sigma/m \sim 0.1 \text{ cm}^2/\text{g}$$

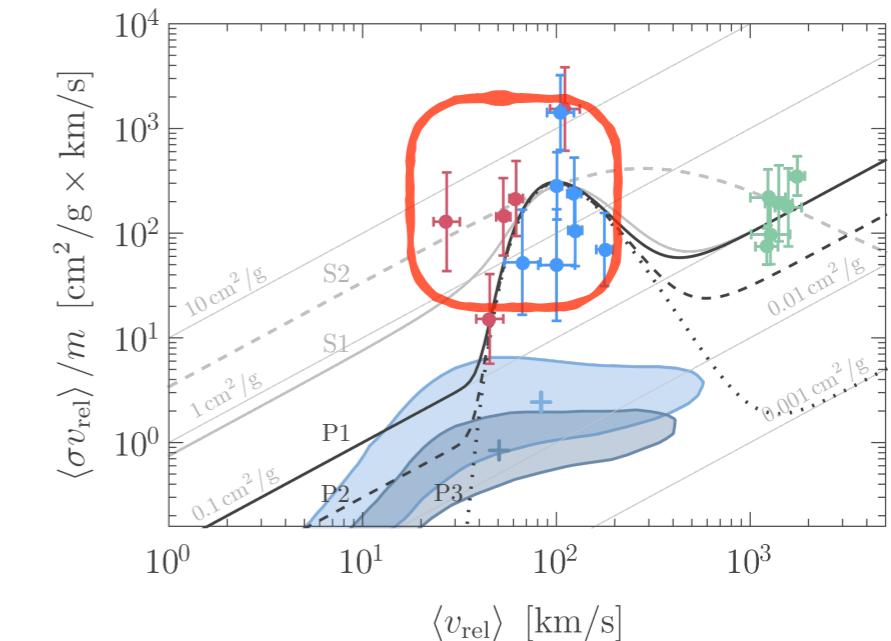
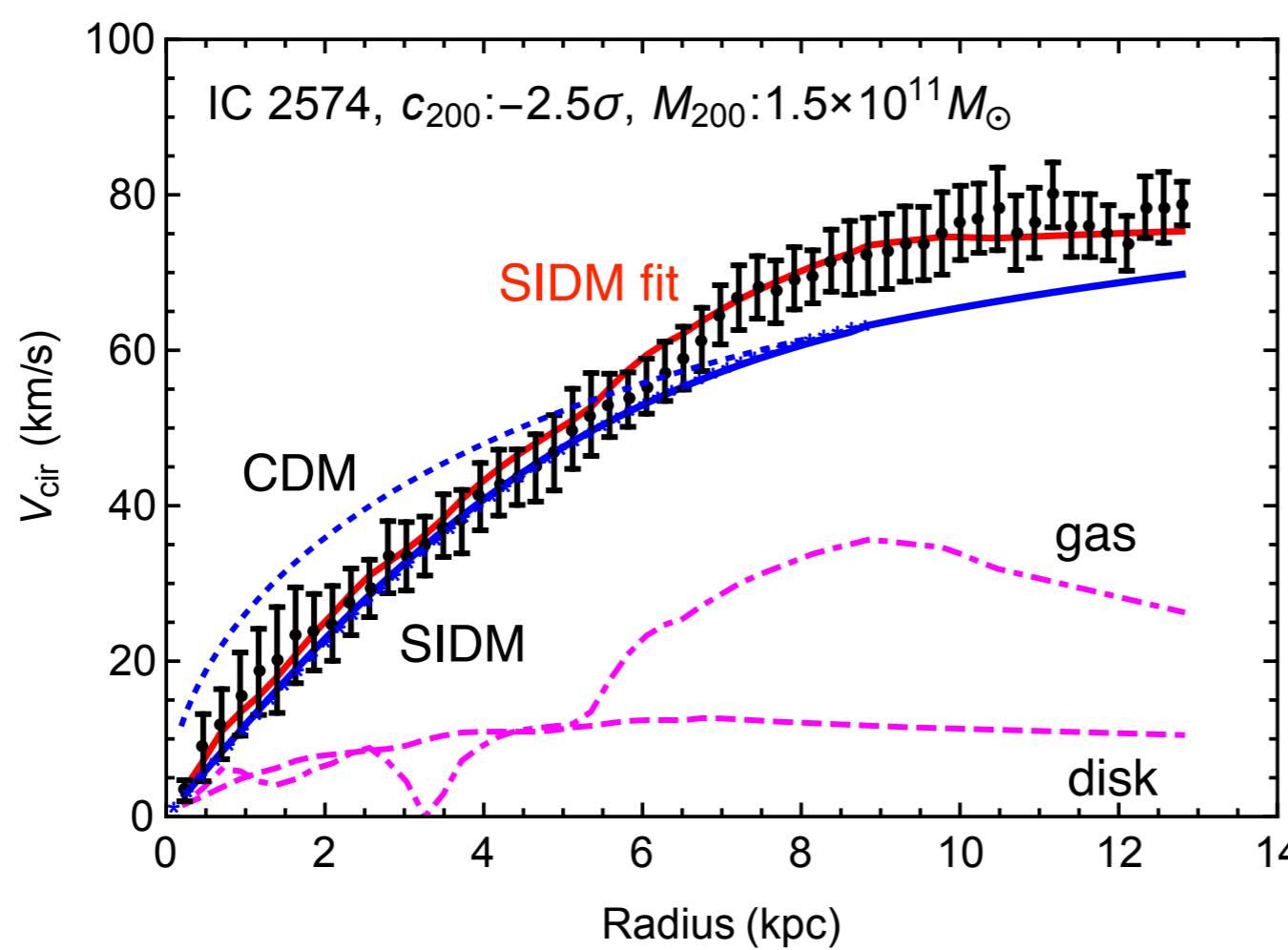
$$\langle v_{\text{rel}} \rangle \sim 10^3 \text{ km/s}$$

Kaplinghat, Tulin, and Yu, PRL, 2016

Data points

Dwarf spiral galaxies

- mass distribution is broadly determined by rotation curves
- rotation velocity in central region (of some galaxies) prefer cored SIDM profile



$$\sigma/m \sim 1 \text{ cm}^2/\text{g}$$

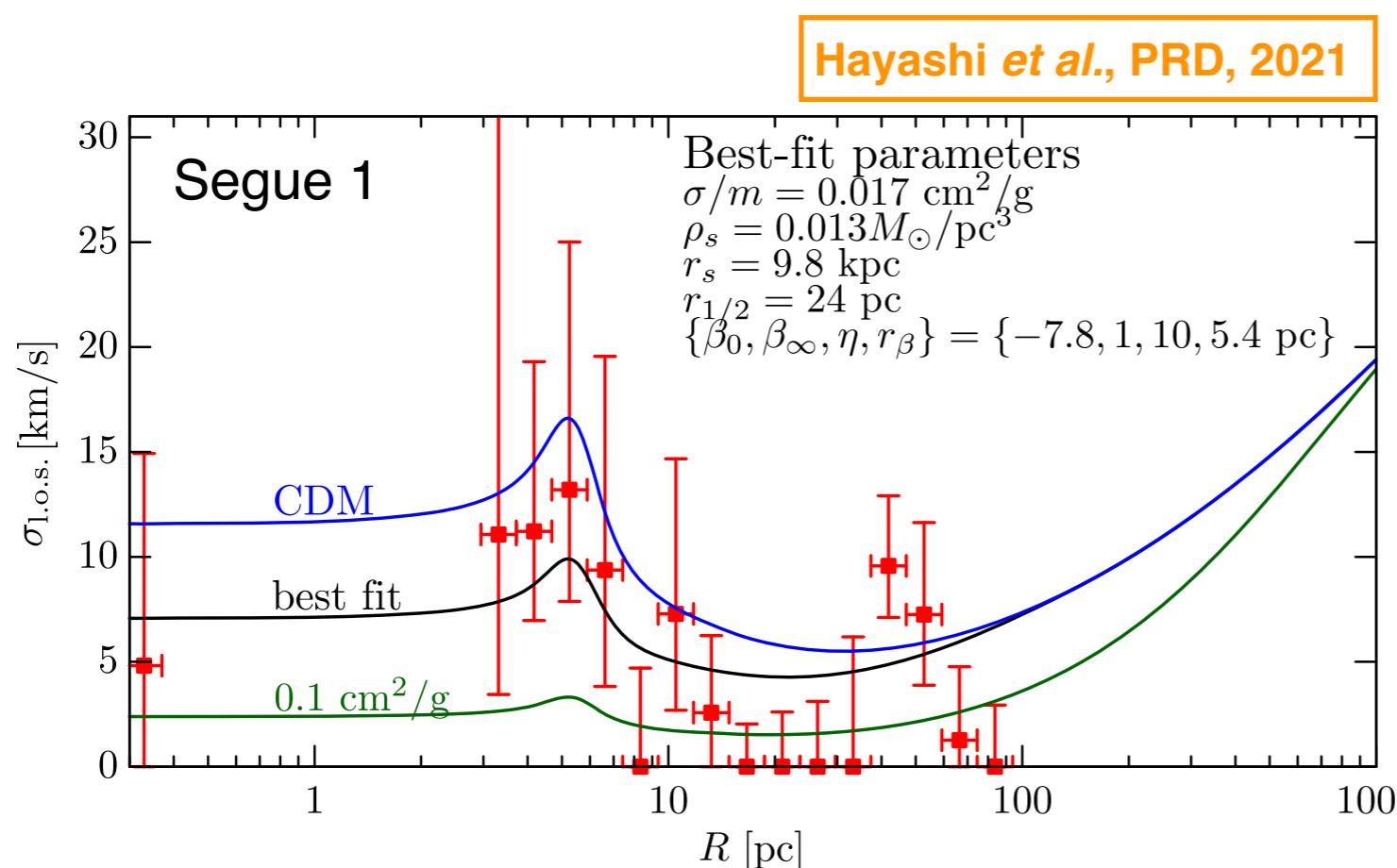
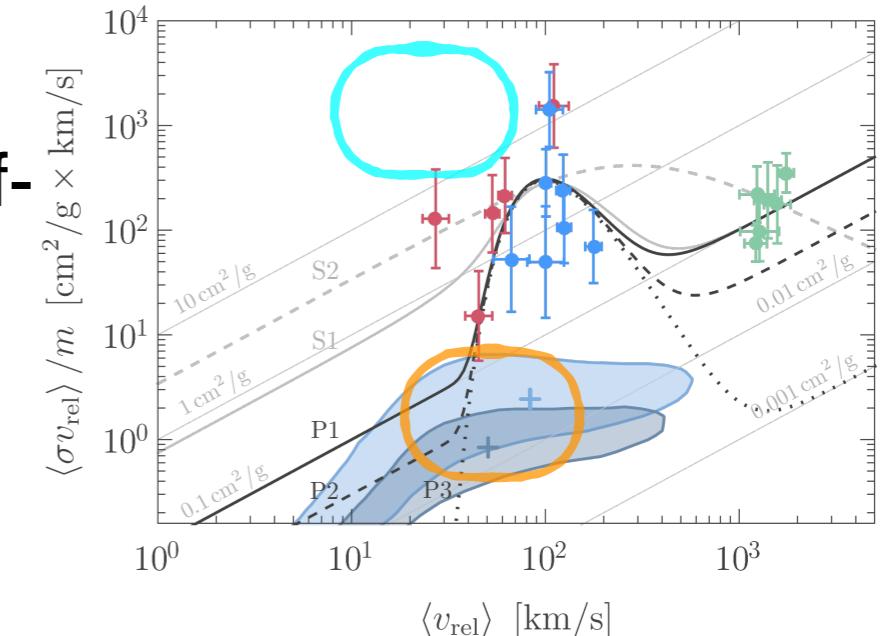
$$\langle v_{\text{rel}} \rangle \sim 10^2 \text{ km/s}$$

AK, Kaplinghat, Pace, and Yu, PRL, 2017

Data points

Ultra faint dwarf (UFD) galaxies

- mass distribution is determined by line-of-sight velocity dispersion (LOSVD) profile
- LOSVD in the central region (of some UFDs) prefer cuspy CDM profile



$$\sigma/m < 0.1 \text{ cm}^2/\text{g}$$

$$\langle v_{\text{rel}} \rangle \sim 30 \text{ km/s}$$

- gravothermal collapse?

Correa, MNRAS, 2021

Possible explanations

Resonant SIDM

Chu, Garcia-Cely, and Murayama, PRL, 2019

- resonance + constant offset

$$\frac{\sigma}{m} = \frac{4\pi S}{m^2 E(v_{\text{rel}})} \frac{\Gamma(v_{\text{rel}})^2/4}{[E(v_{\text{rel}}) - E(v_R)]^2 + \Gamma(v_{\text{rel}})^2/4} + \frac{\sigma_0}{m}$$

- thermal average

$$f(v_{\text{rel}}; \nu) = \frac{v_{\text{rel}}^2}{\sqrt{4\pi\nu^3}} \exp\left(-\frac{v_{\text{rel}}^2}{4\nu^2}\right)$$

$$\langle v_{\text{rel}} \rangle = (4/\sqrt{\pi})\nu$$

- s-wave benchmarks

- S1 and S2

$$\gamma = 10^{-4.5}, 10^{-1.1}$$

$$v_R = 120 \text{ km/s}, 5035 \text{ km/s}$$

$$m/S^{1/3} = 22 \text{ GeV}, 16 \text{ GeV}$$

$$\sigma_0/m = 0.1 \text{ cm}^2/\text{g}, \ll 0.1 \text{ cm}^2/\text{g}$$

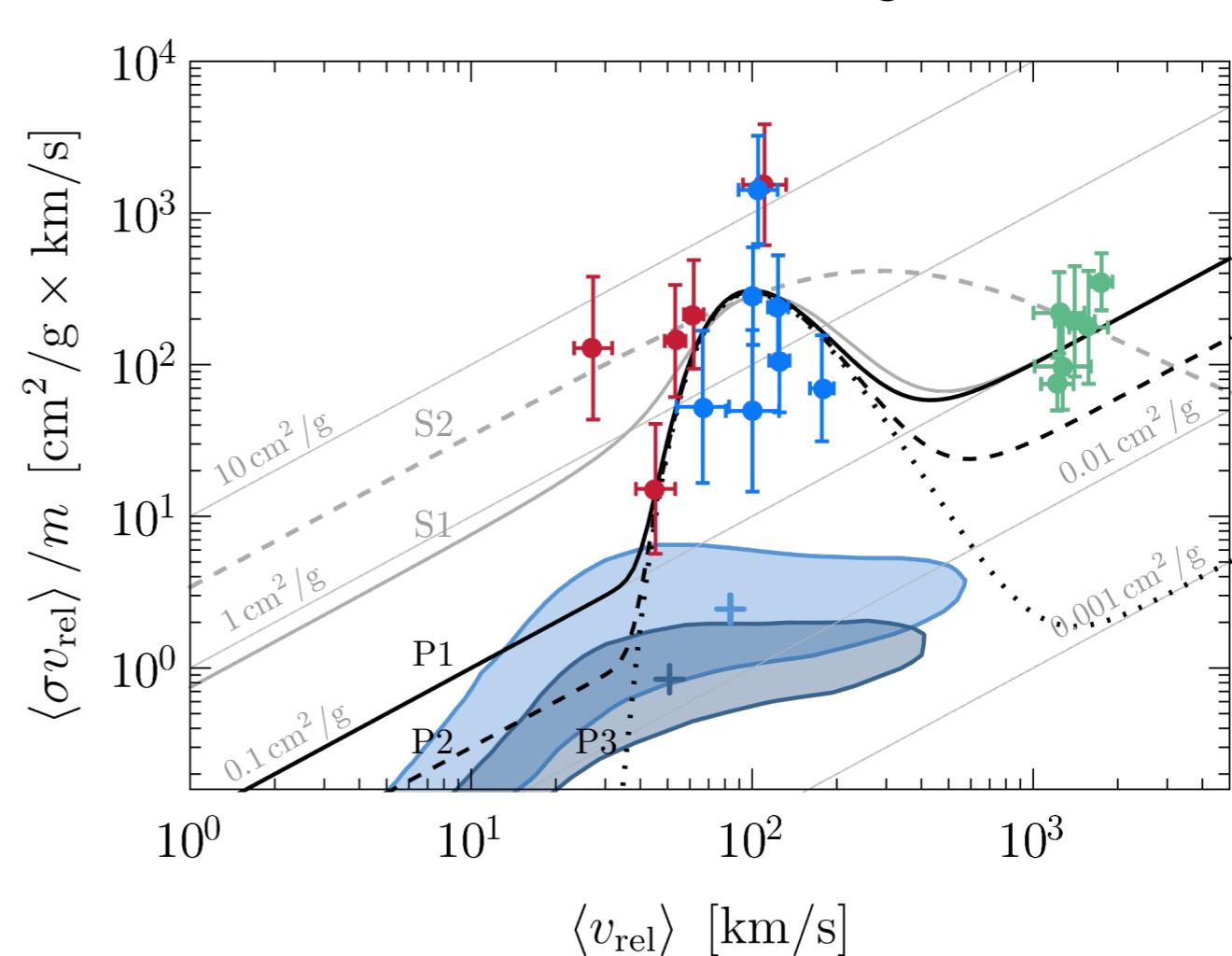
$$S = (2s_R + 1)/(2s_{\text{dm}} + 1)^2$$

$$E(v_{\text{rel}}) = (m/2)v_{\text{rel}}^2/2$$

$$E(v_R) = m_R - 2m$$

$$\Gamma(v_{\text{rel}}) = m_R \gamma^2 v_{\text{rel}}^{2\ell+1}$$

- running width



Possible explanation

Resonant SIDM

- s-wave benchmarks
 - S1 and S2 do not satisfy the UFD constraints
 - one need to take $\gamma \lesssim 10^{-7}(m/\text{GeV})^{3/2}[\nu_R/(100 \text{ km/s})]^2$ for s-wave

- p-wave benchmarks

- P1, P2 and P3

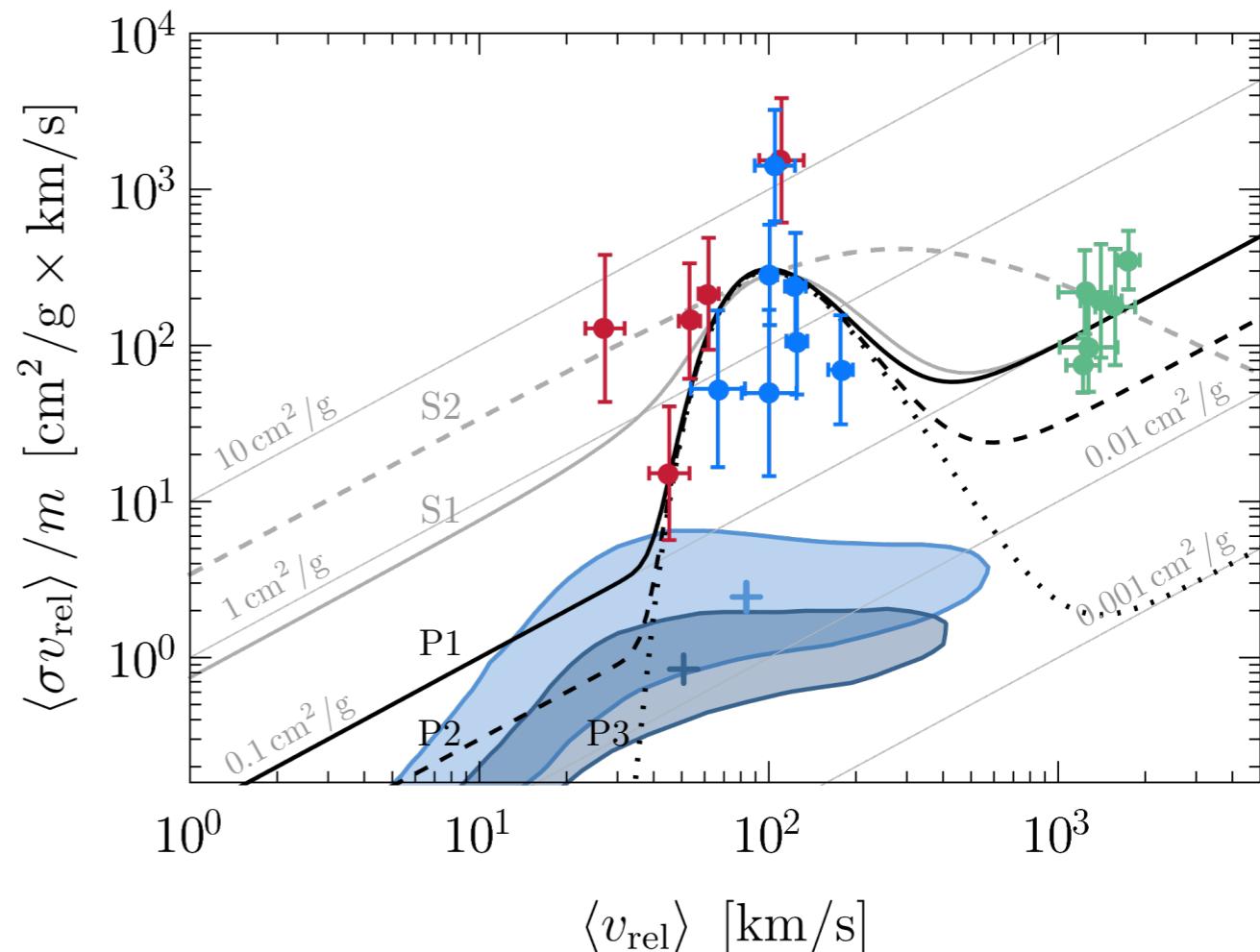
$$\gamma = 10^{-3} \quad \nu_R = 108 \text{ km/s}$$

$$m/S^{1/3} = 0.4 \text{ GeV}$$

$$\sigma_0/m = 0.1 \text{ cm}^2/\text{g}, 0.03 \text{ cm}^2/\text{g}$$

$$0.001 \text{ cm}^2/\text{g}$$

- consider P2 benchmark mainly in the following



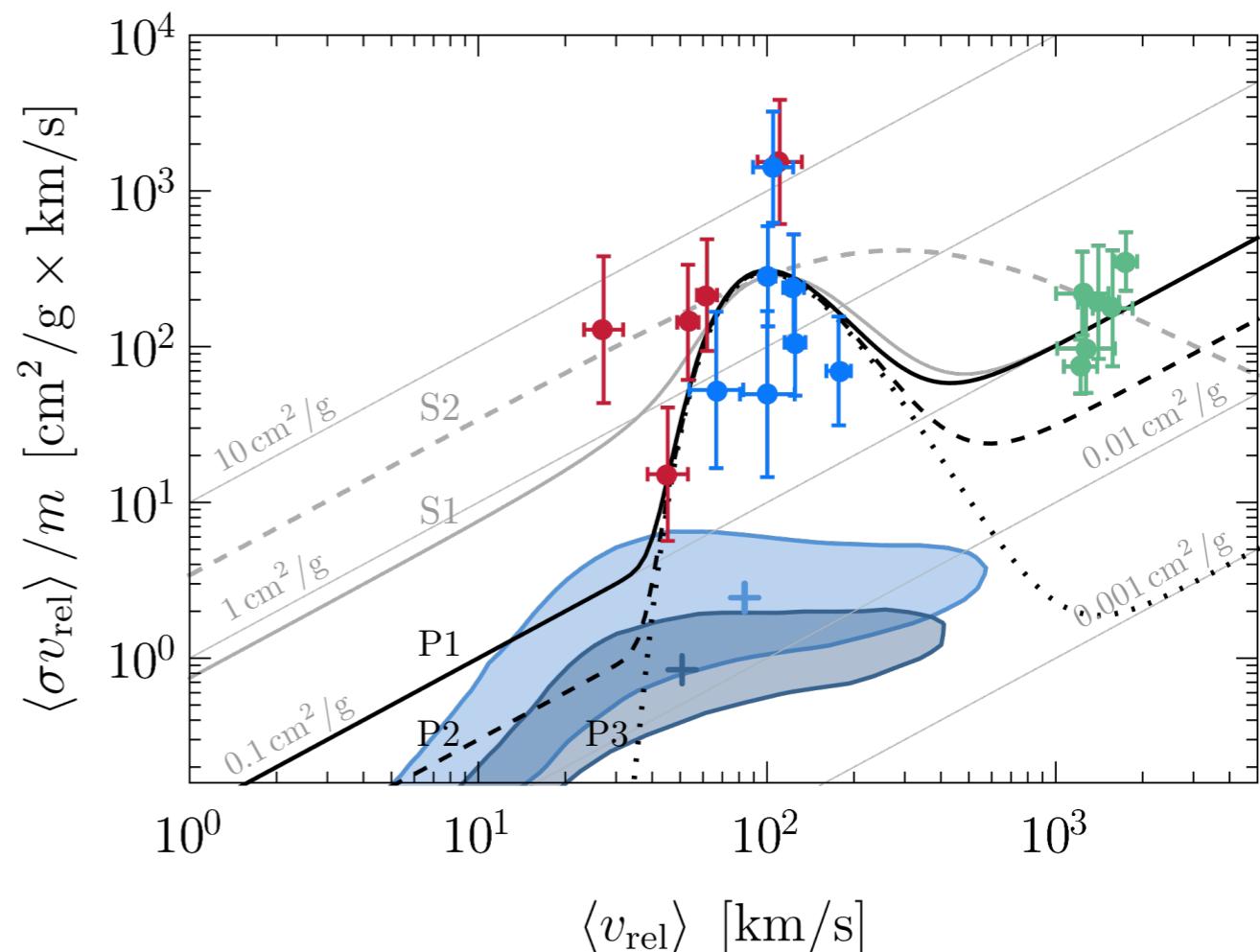
Resonant SIDM

Question

- data are obtained by r1-procedure
 - switching Navarro-Frenk-White (NFW) profile to isotherm profile inside r_1
 - assuming efficient heat conduction inside r_1
 - valid for constant SIDM
- Is a resonant SIDM halo similar to constant SIDM halo?**
 - mapping between resonant SIDM and constant SIDM

$$\rho_{\text{NFW}}(r_1) \frac{\langle \sigma v \rangle_{\text{NFW}}(r_1)}{m} t = 1$$

$$\rho_{\text{NFW}}(r) = \frac{\rho_s}{r/r_s(1+r/r_s)^2}$$



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Possible imprints on observations

- density break in a certain mass range of halos
- change in stellar orbits by density break in the past

Evolution of resonant SIDM halos

Gravothermal modeling of isolated halo

- assuming hydrostatic equilibrium in the course of evolution

$$\frac{\partial}{\partial r}(\rho v^2) = -\rho \frac{GM}{r^2} \quad \frac{\partial}{\partial r}M = 4\pi r^2 \rho$$

- self-scattering leads to heat conduction

$$\frac{D}{Dt} \ln \left(\frac{\nu^3}{\rho} \right) = -\frac{1}{4\pi r^2 \rho \nu^2} \frac{\partial L}{\partial r} = \frac{1}{3t_{\text{cond.}}} \quad \frac{L}{4\pi r^2} = -\kappa \frac{\partial T}{\partial r}$$

- heat conduction timescale

- naive interpolation between LMFP and SMFP regimes

$$\kappa^{-1} = \kappa_{\text{LMFP}}^{-1} + \kappa_{\text{SMFP}}^{-1}$$

- SMFP $\kappa_{\text{SMFP}} = \frac{3}{2} b \frac{\nu}{\sigma_0 K_5(\nu)}$

$$b = \frac{25\sqrt{\pi}}{32} \simeq 1.38 \quad K_p(\nu) = \frac{\langle \sigma v_{\text{rel}}^p \rangle}{\sigma_0 \langle v_{\text{rel}}^p \rangle}$$

Outmezguine et al., MNRAS, 2023

- LMFP $\kappa_{\text{LMFP}} = \frac{3C}{2\pi^{3/2}} \frac{\rho \nu^3 \sigma_0 K_1(\nu)}{G m^2}$

$$p = 3?$$

Outmezguine et al., MNRAS, 2023

- start with NFW profile

$$p = 5?$$

Yang et al., ApJ, 2023

- mean c-M relation

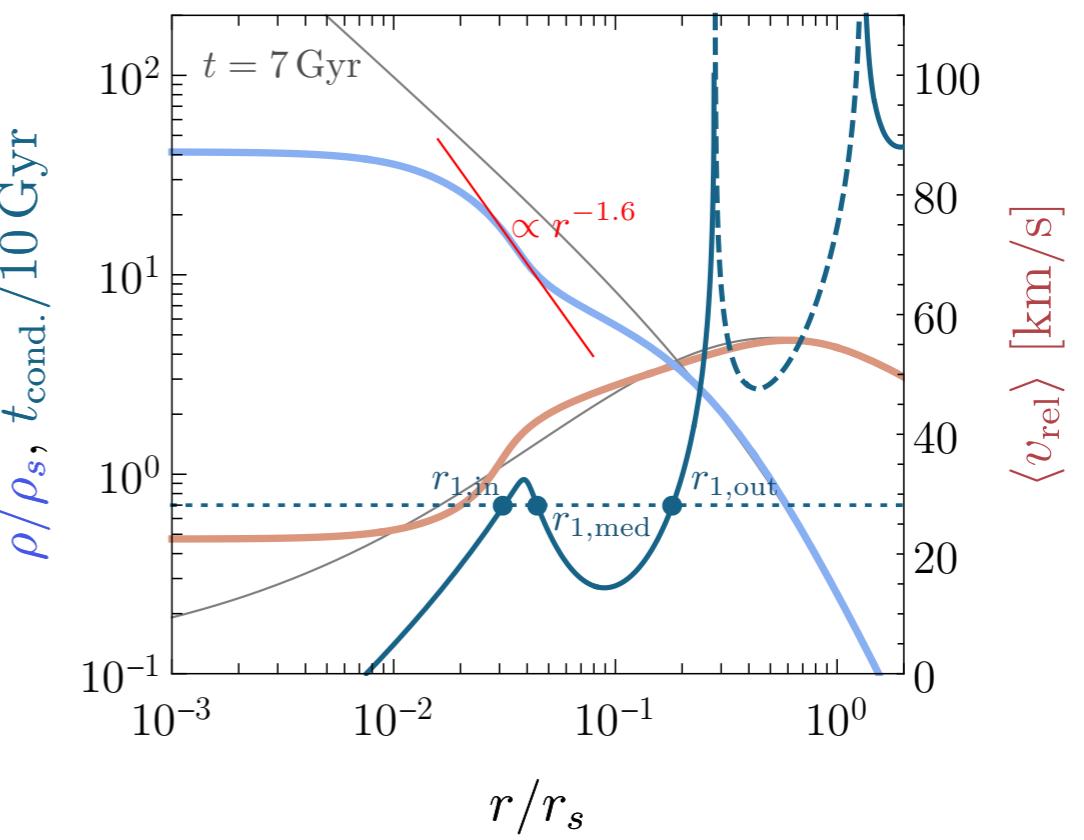
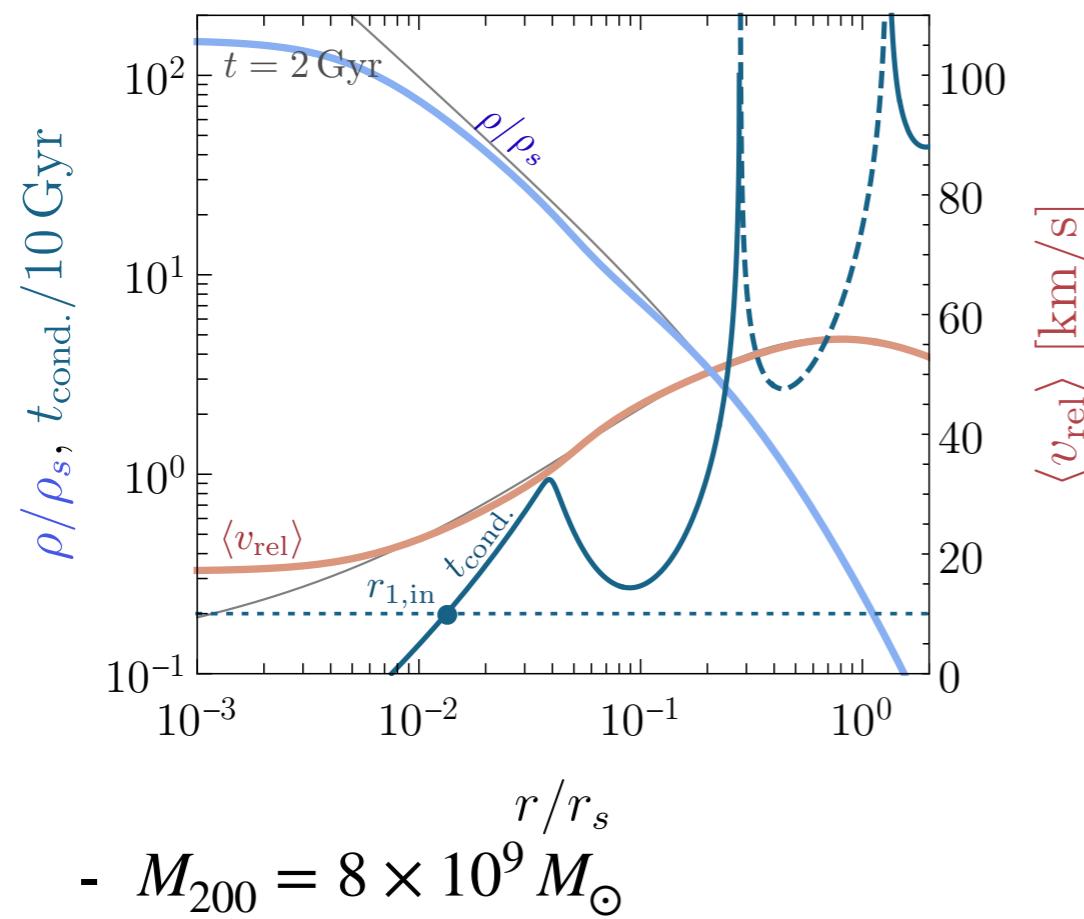
$$C \simeq 0.75$$

Koda and Shapiro, MNRAS, 2011

Evolution of resonant SIDM halos

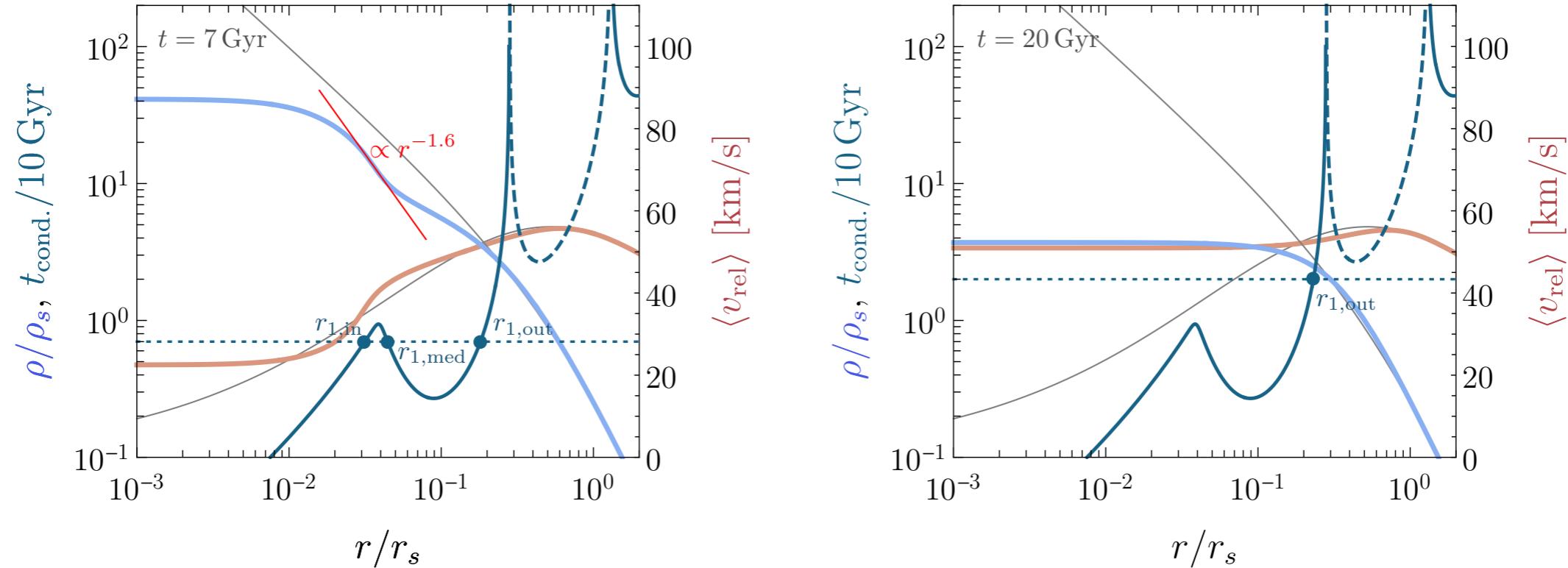
Formation of density break

- profile of heat conduction timescale has a sharp peak $r/r_s \simeq 0.1$
- three r_1 's appear for $t > t_{\text{break}}$ $t_{\text{cond.}}(r_1) = t$
- two isothermal regions appear $r < r_{1,\text{in}}$ $r_{1,\text{med}} < r < r_{1,\text{out}}$
- density break forms to connect the two isothermal regions



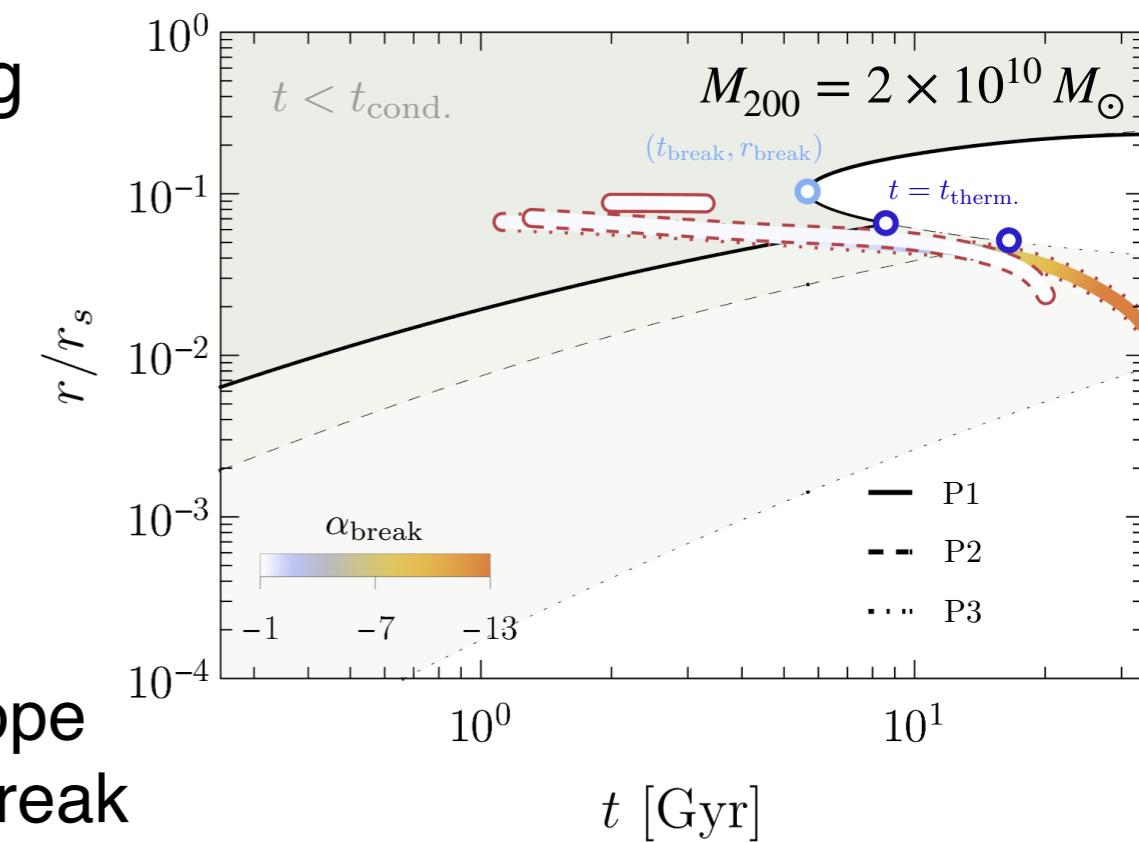
- $M_{200} = 8 \times 10^9 M_\odot$

Evolution of resonant SIDM halos



Development and thermalization of density break

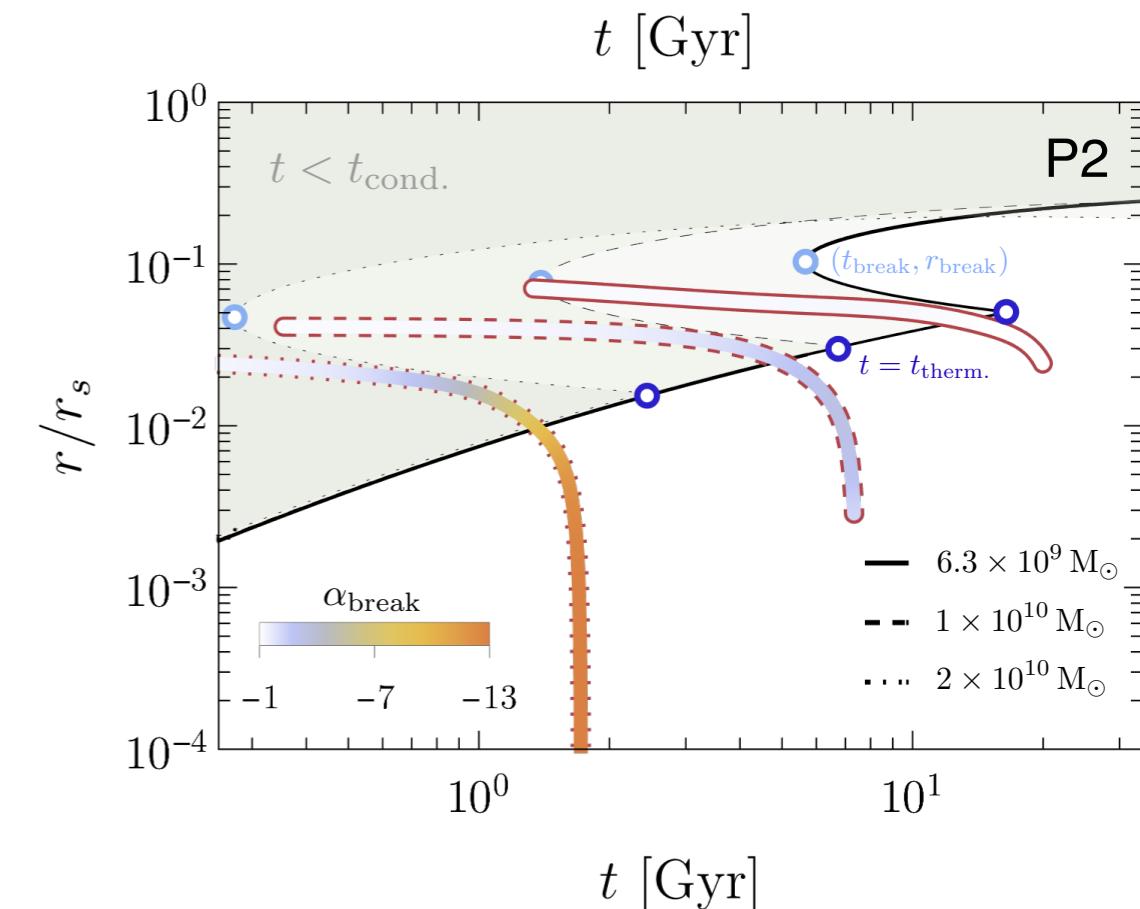
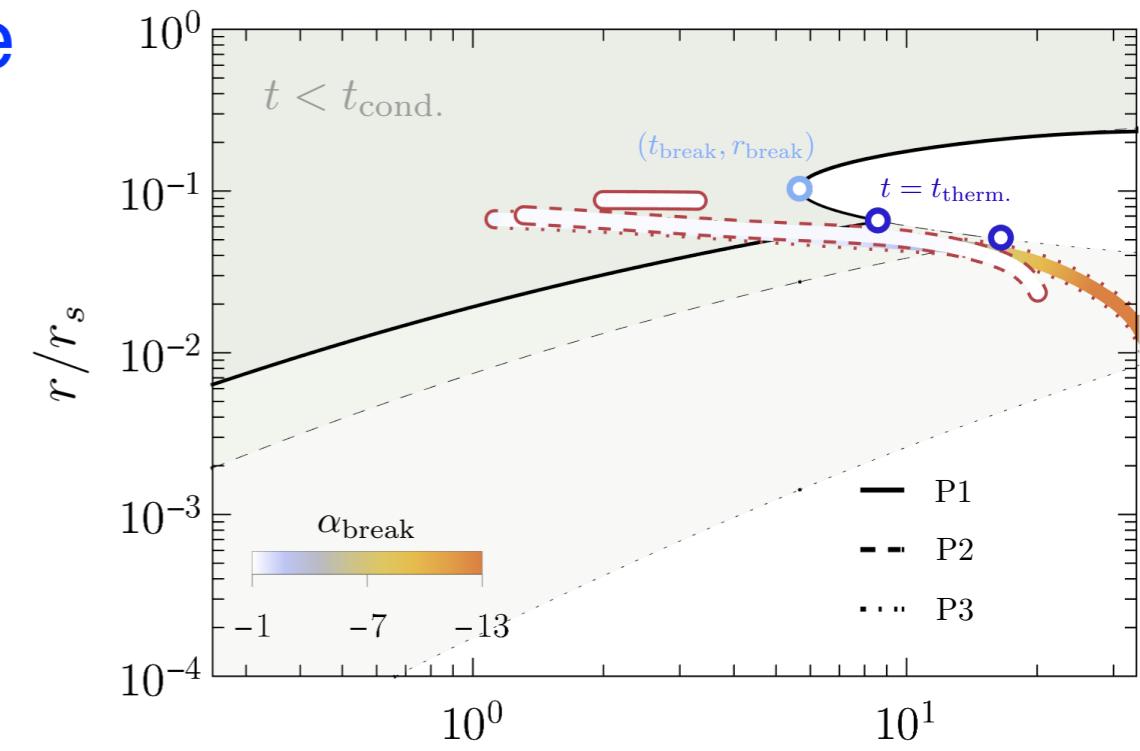
- propagates inwards, while expanding the outer isothermal region
- during propagation, slope of density break gets sharper
- reaches the inner isothermal region and is thermalized to disappear
 - position of steepest slope defines that of density break



Evolution of resonant SIDM halos

Benchmark / halo-size dependence

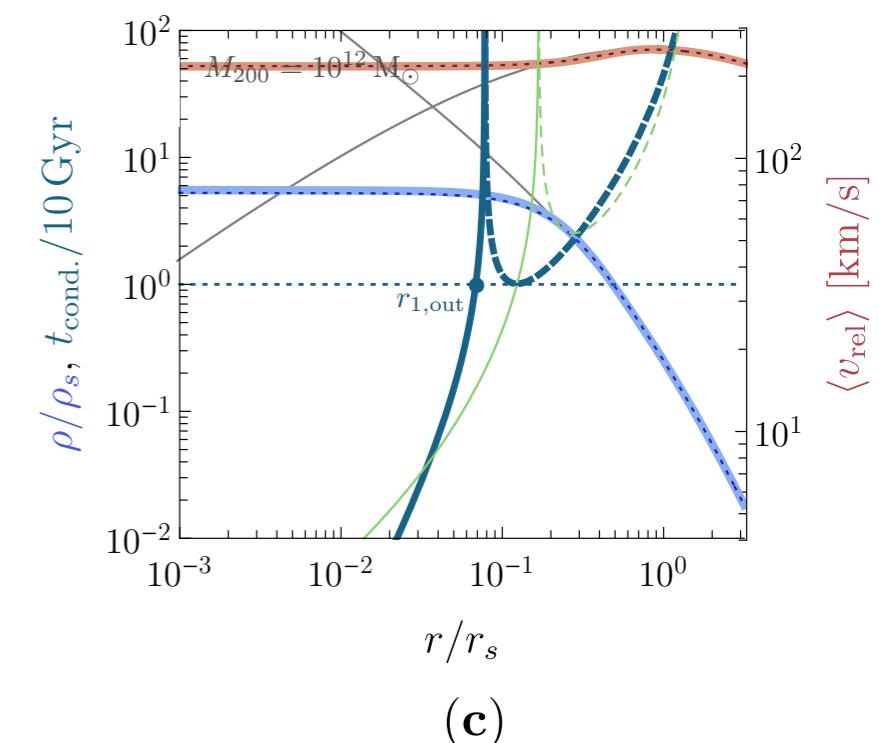
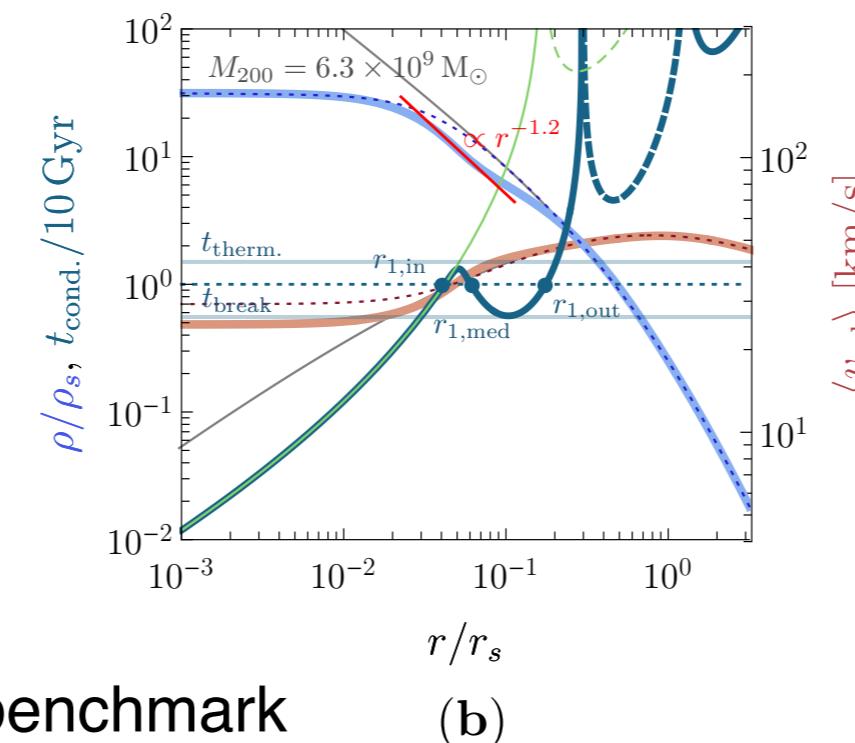
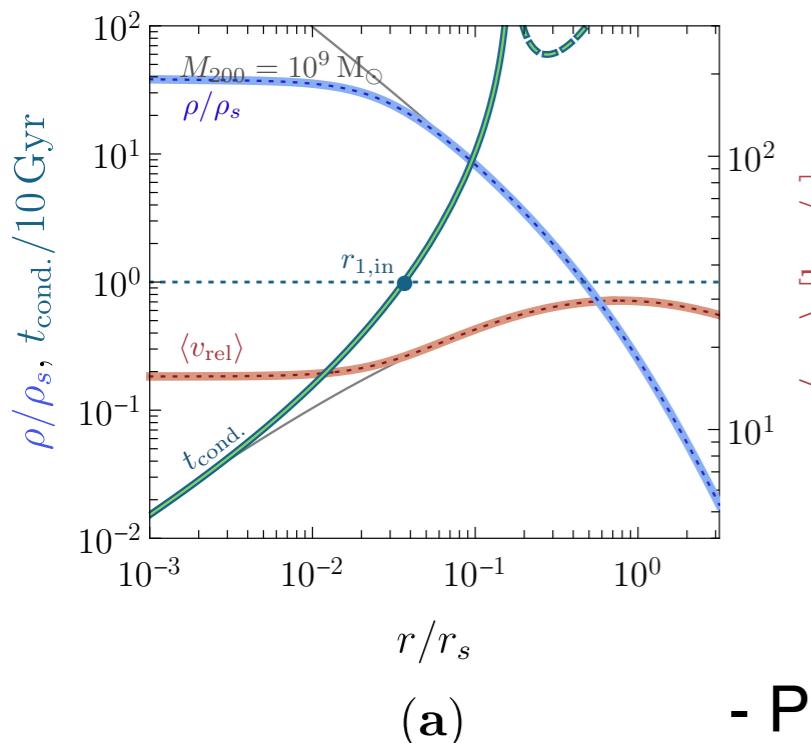
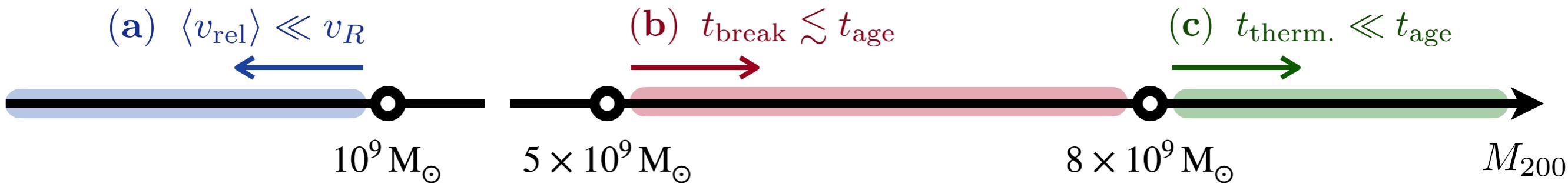
- density break propagates longer till thermalization and develops further, for larger separation between $r_{1,\text{in}}$ and $r_{1,\text{med}}$ at $t = t_{\text{break}}$
- smaller offset cross section (P3)
 - smaller $r_{1,\text{in}}$ $t = t_{\text{break}}$
 - larger halos
 - earlier formation (smaller t_{break})



Resonant SIDM halos at present

Halo dependence

- no resonant scattering in too small halos (a)
- density break develops at present in a certain mass range (b)
- density break developed and is already thermalized in larger halos (c)

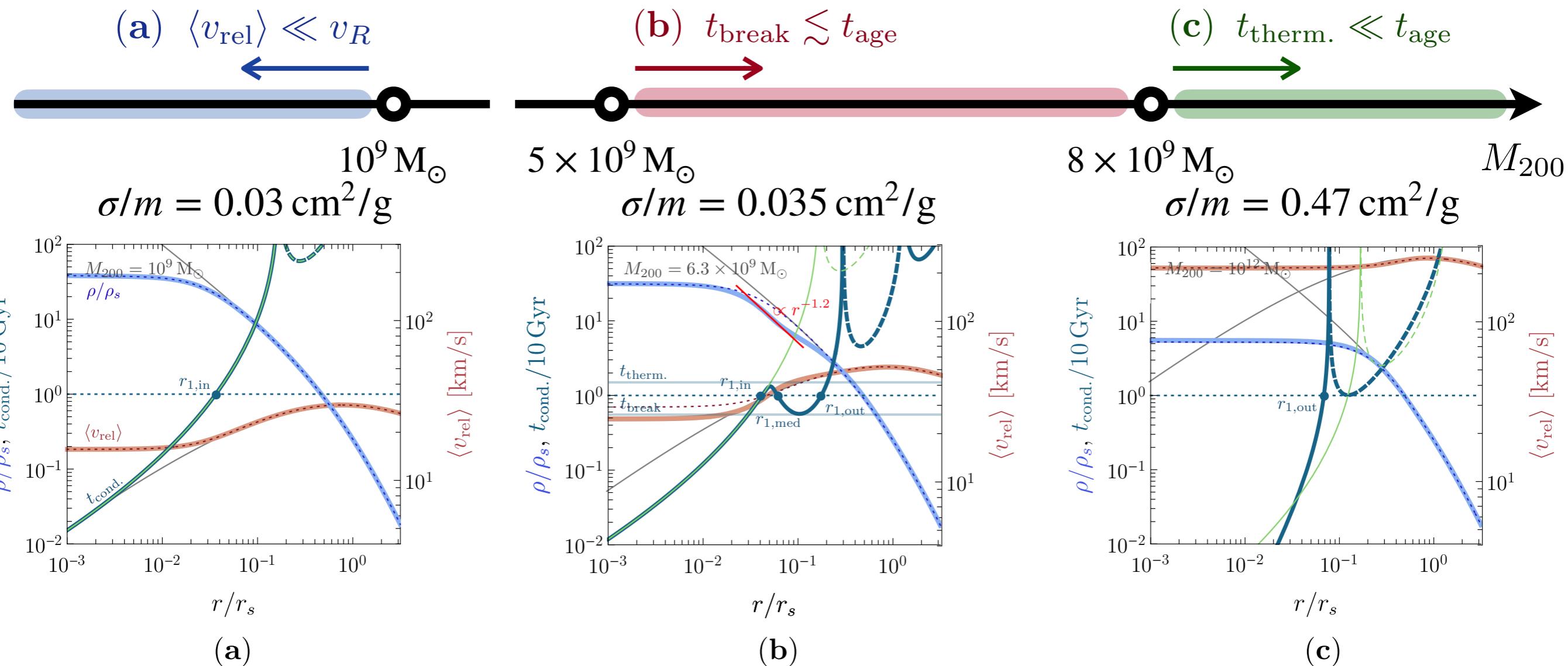


- P2 benchmark

Resonant SIDM halos at present

Similarity to constant SIDM halos

- one can find an identical constant SIDM halo except for a certain mass range (b)
- systematic mapping?



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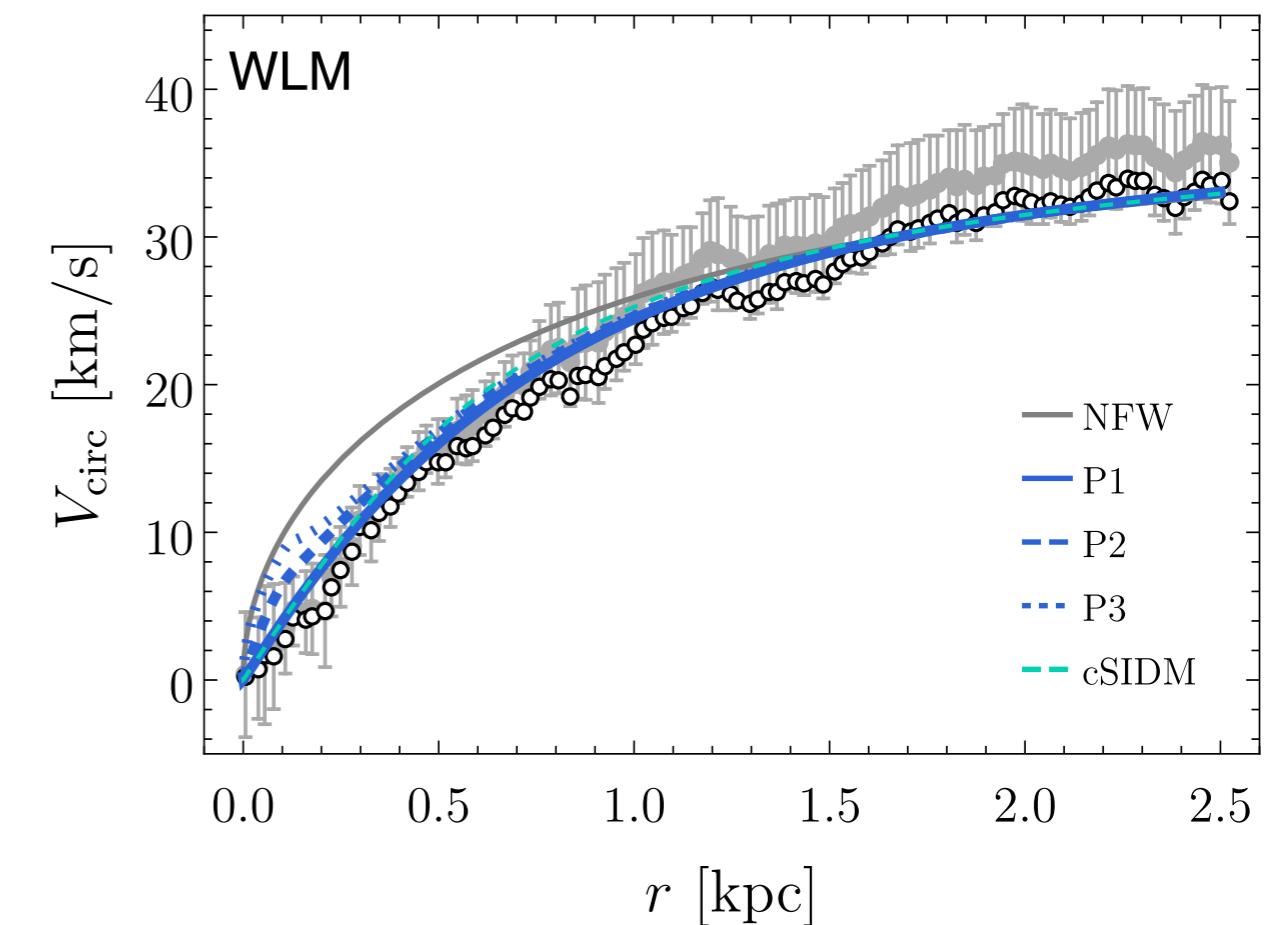
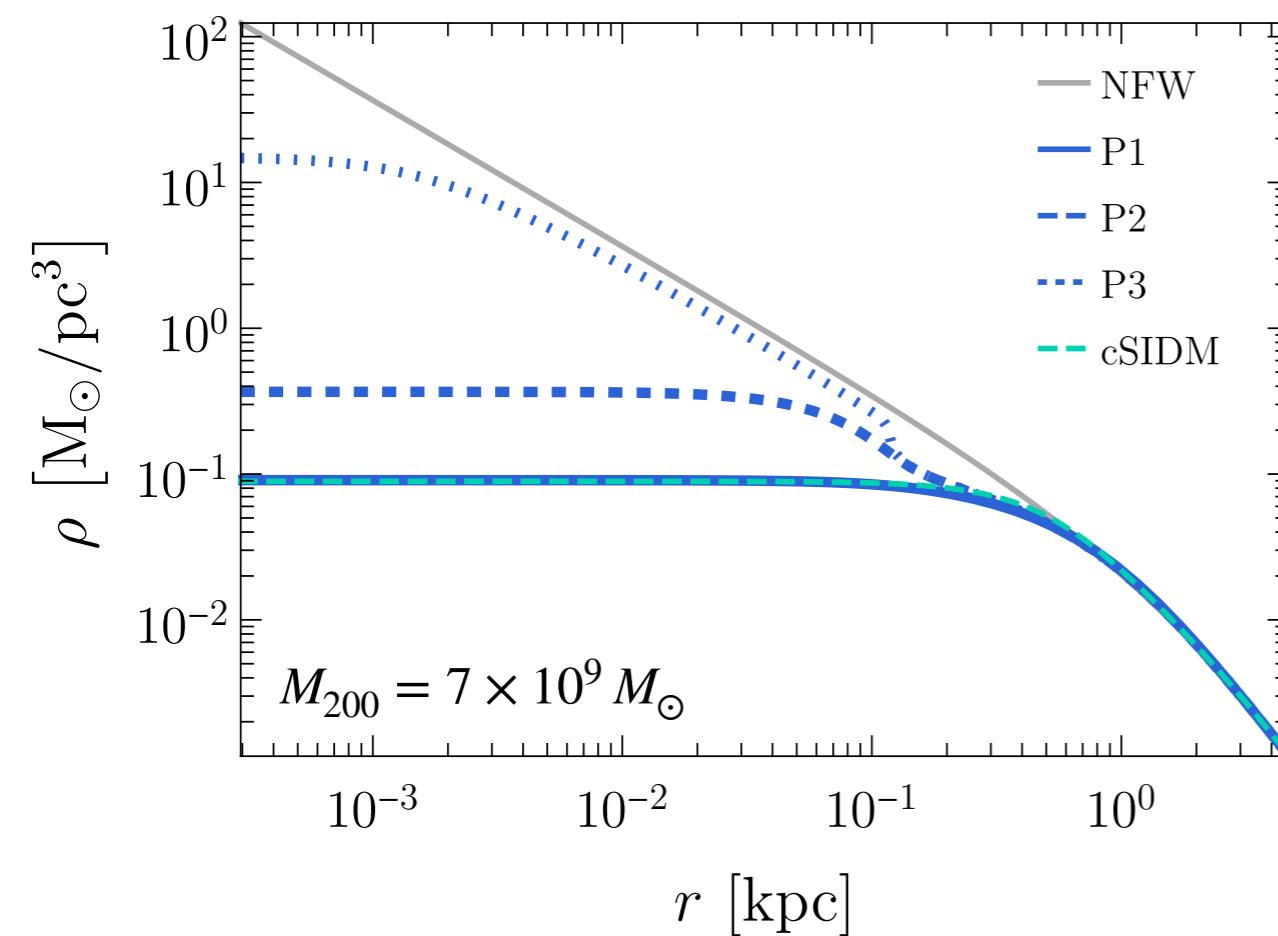
Possible imprints on observations

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- change in stellar orbits by density break in the past

Density breaks at present

Rotation curve

- P1 benchmark halo is identical to constant SIDM halo $\sigma/m = 0.33 \text{ cm}^2/\text{g}$
- P3 benchmark halo has a circular velocity profile transiting from constant SIDM to NFW around 0.1 kpc
 - may be a distinctive signature if observed by any chance



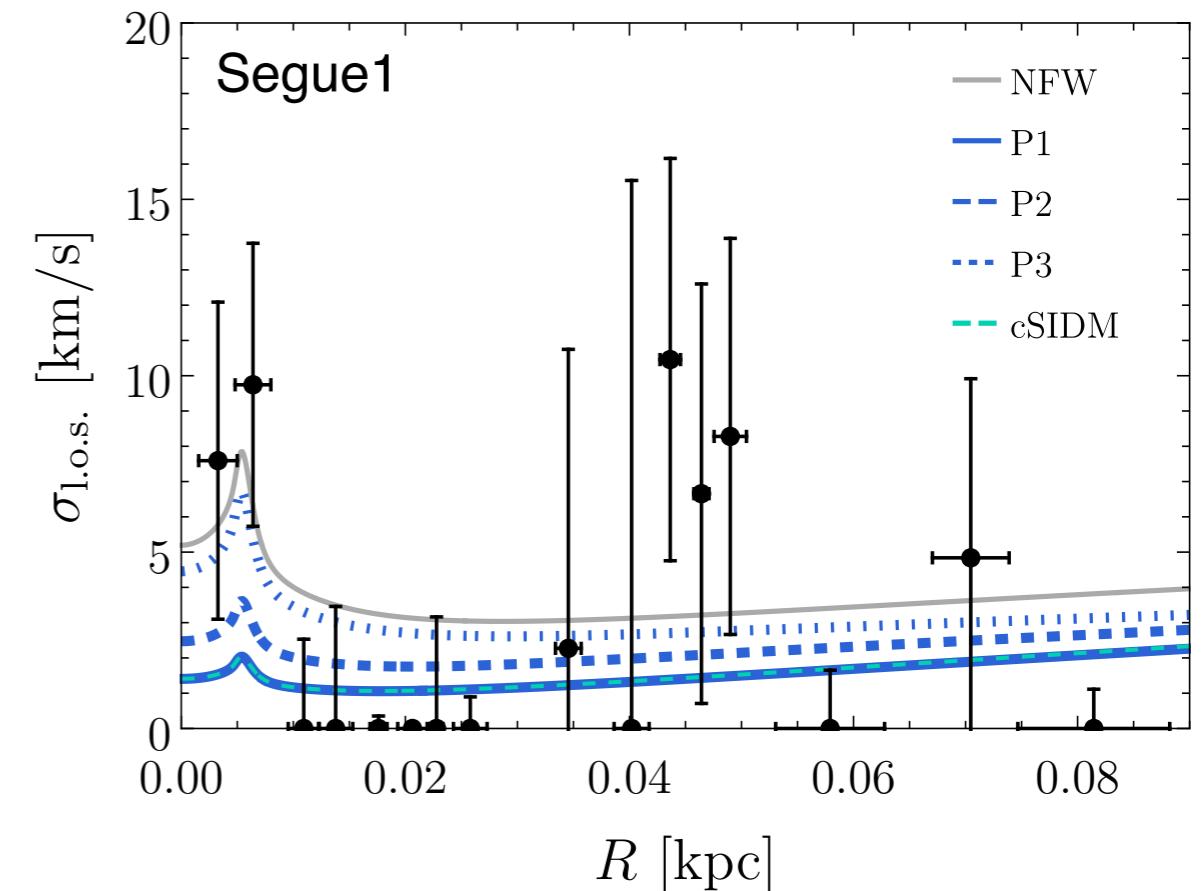
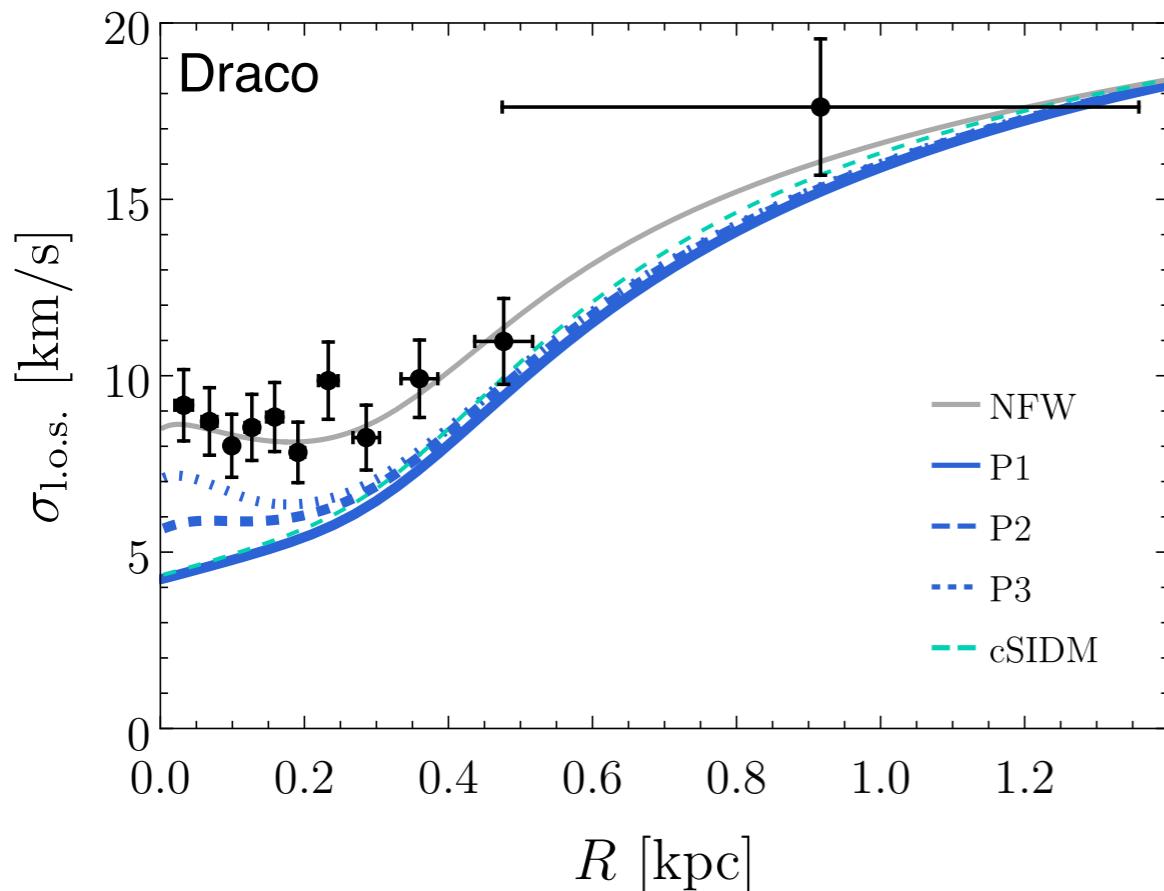
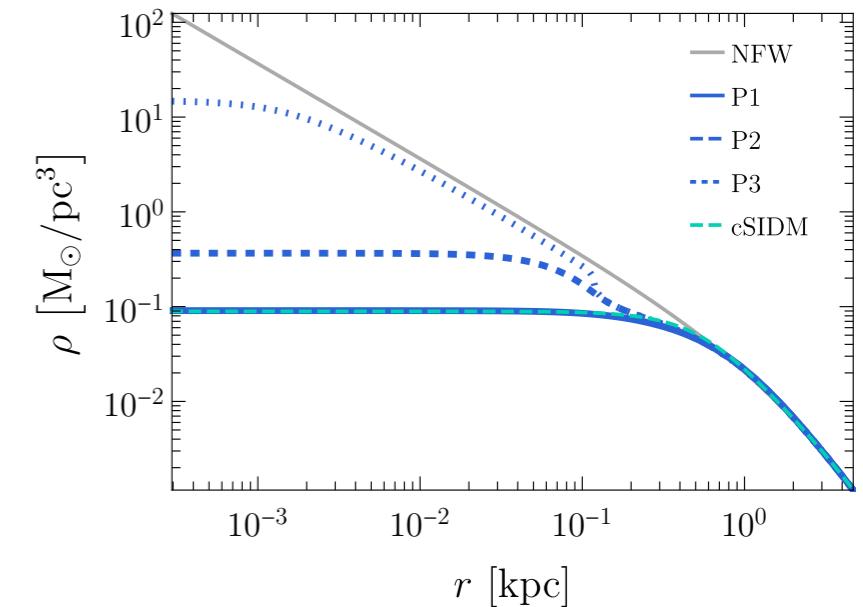
Density breaks at present

LOSVD profile of MW satellites

- stellar kinematic parameters are fixed to best fit values for NFW profile

Hayashi *et al.*, PRD, 2021

- P3 benchmark halo shows a transition from constant SIDM to NFW around 0.1 kpc
 - may fit the data better than constant SIDM



Density breaks in the past

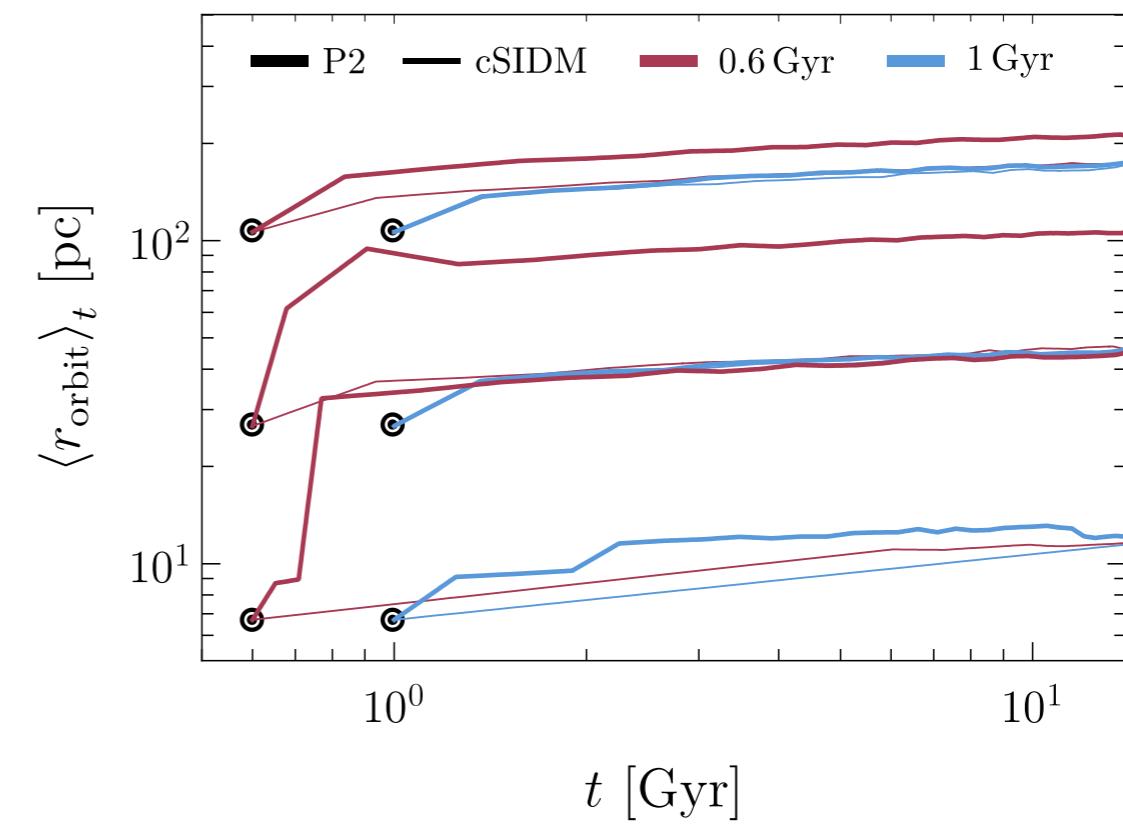
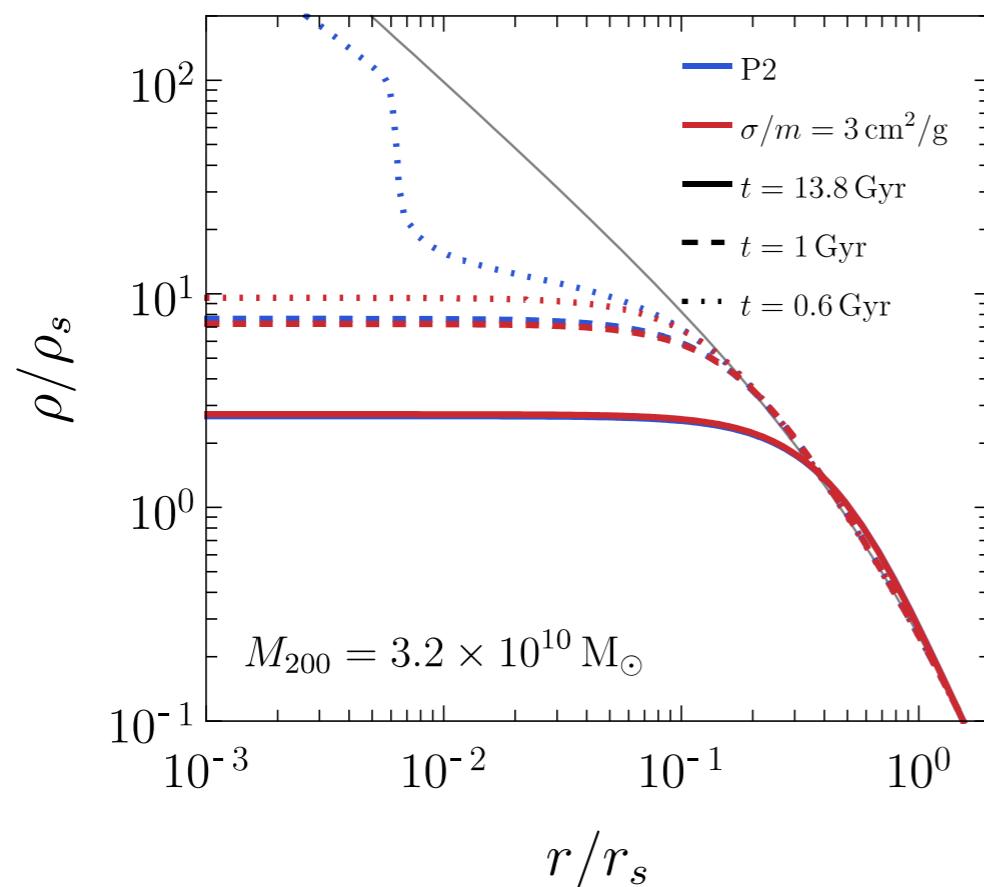
Change in mean stellar orbits

- energy in orbit distribution function is updated by the average change of potential at every orbital period
- orbits of stars are different depending on which they form before or after the development of density break

$$p(r, t; E, j) \propto \frac{1}{\sqrt{E(t) - V(r, t; j)}}$$

$$\langle \Delta E \rangle_t = \langle \Delta V \rangle_t$$

Pontzen and Governato, MNRAS, 2012



Summary

Resonant SIDM

- realizes sharp velocity dependence inferred by cores in various-size halos

Resonant SIDM halos

- **density break** forms, develops and is thermalized
 - should be confirmed by cosmological simulations (e.g., mergers, tidal stripping...)
- except for a certain mass range, one can find an identical constant SIDM halo
 - not clear how to find systematically

Possible imprints

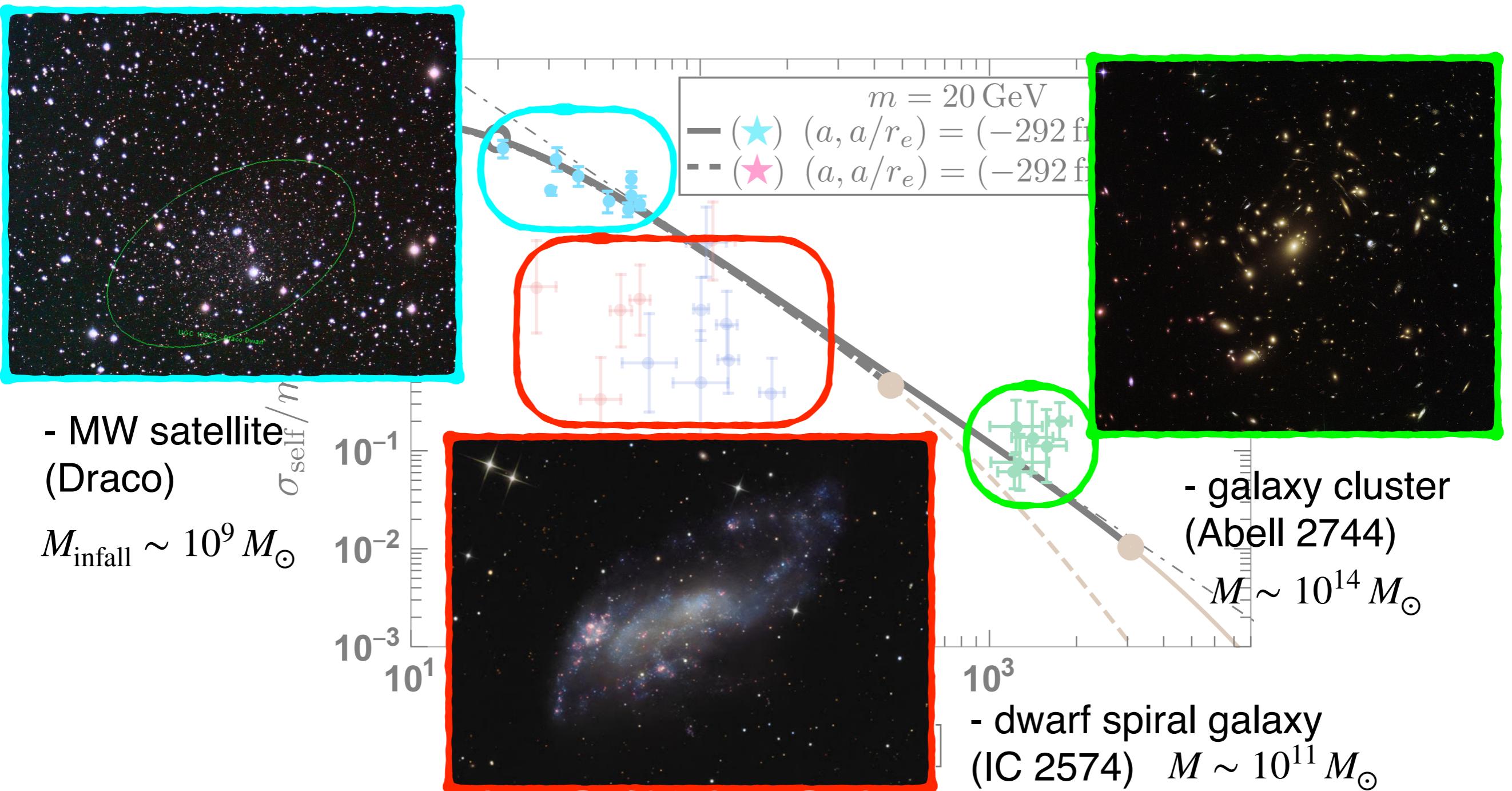
- density break at present may be seen in rotation curves and LOSVD profiles
- density break in the past differentiates orbits of stars forming before and after density break
 - should be studied further

Thank you

Data points

Overview

- cores in various-size halos



Another possible explanation

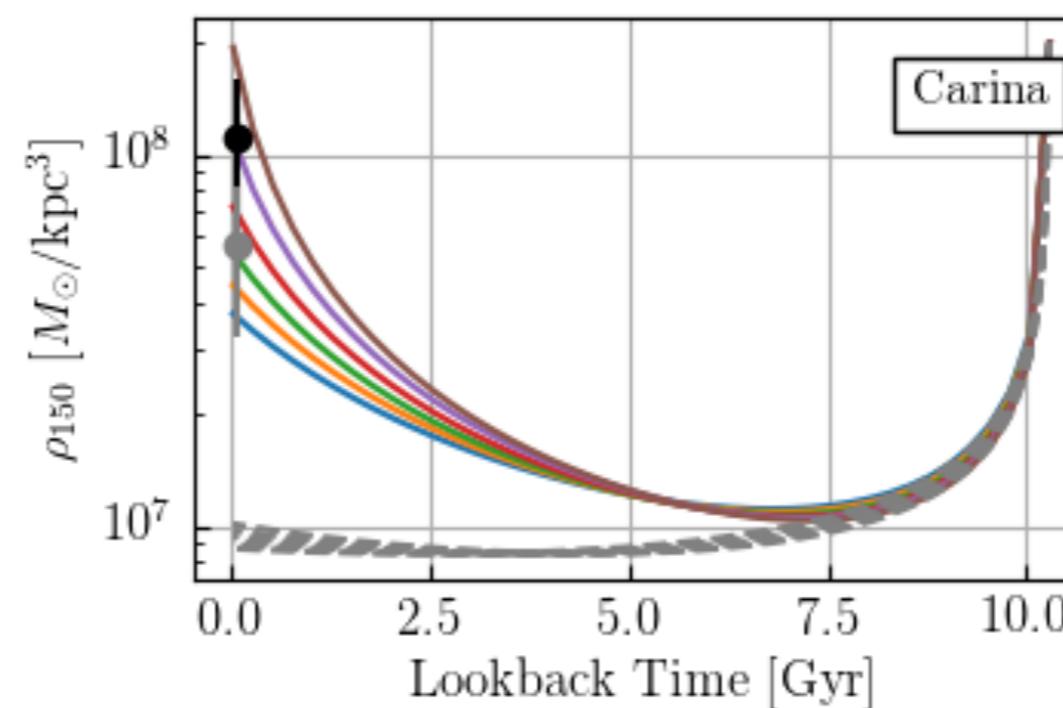
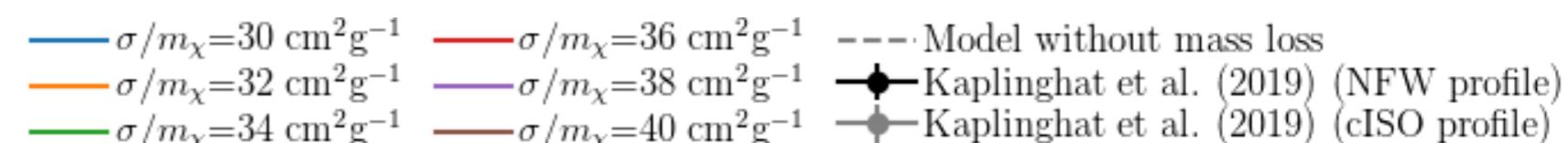
Gravothermal collapse

- another possibility is to take as a large cross section as $\sigma_{\text{self}}/m \sim 40 \text{ cm}^2/\text{g}$

$$\langle v_{\text{rel}} \rangle \sim 30 \text{ km/s}$$

- first core expands and central density gets lower

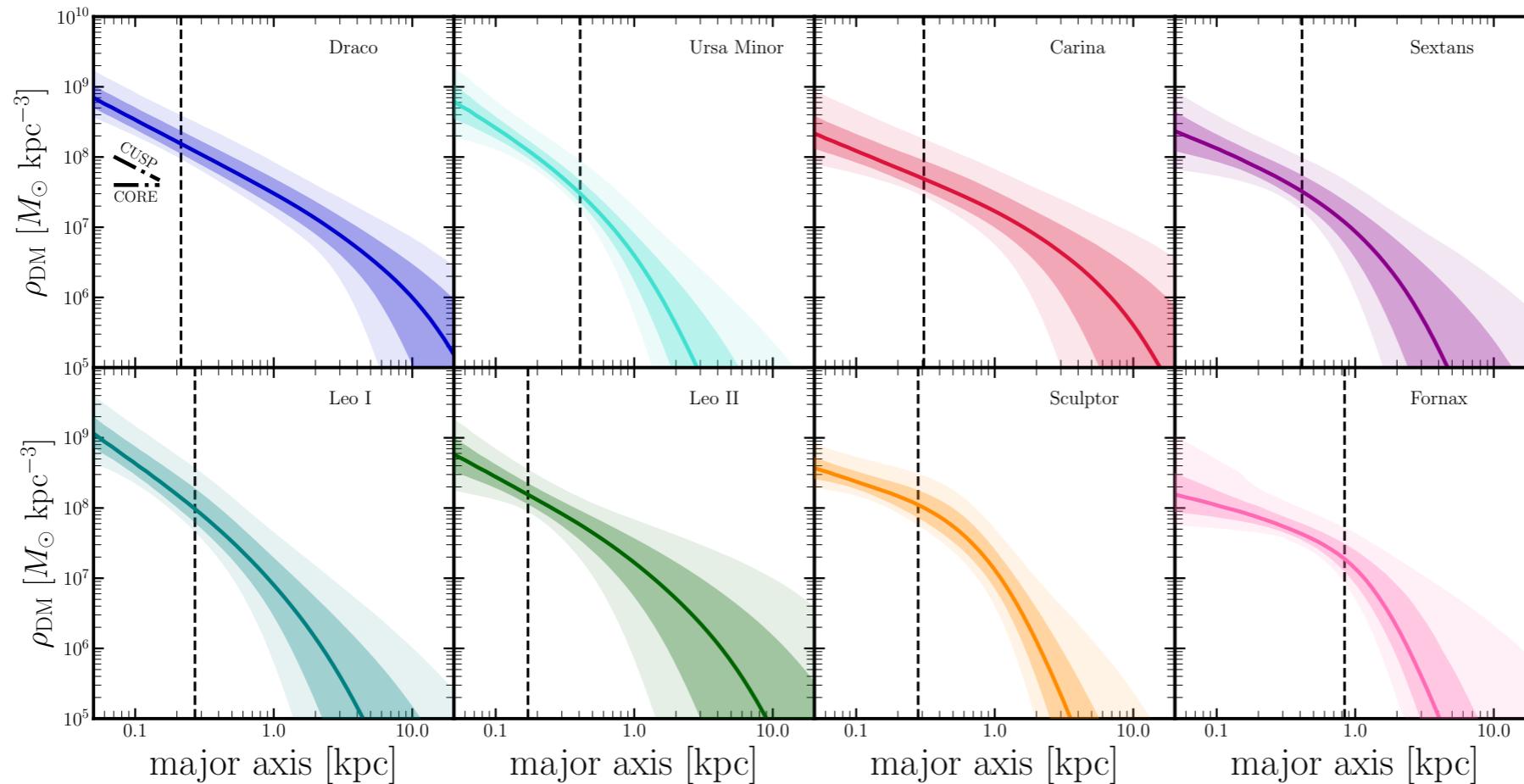
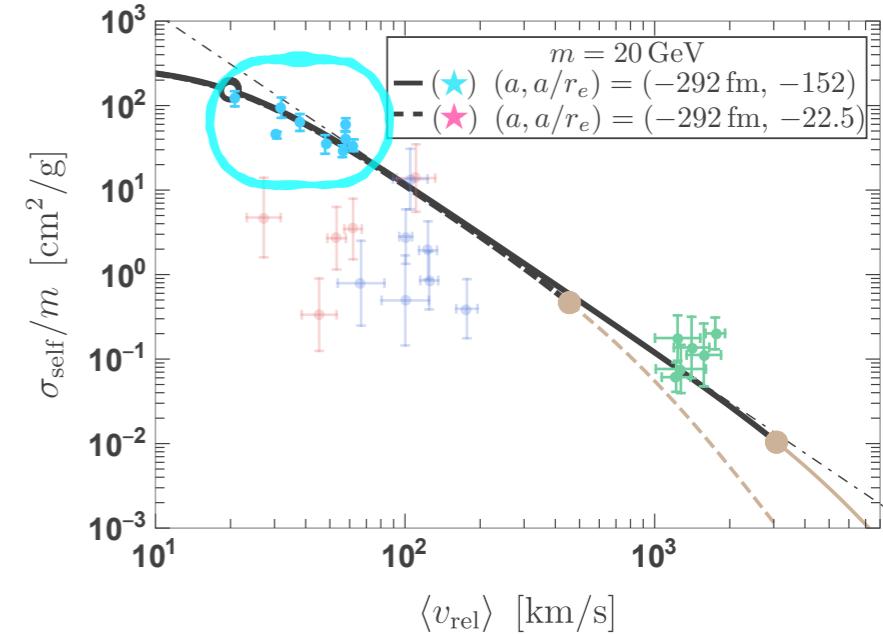
- then core shrinks and central density gets higher



Data points

Classical dwarfs

- mass distribution is determined by stellar kinematics
- stellar kinematics in the central region (of some satellites) prefer cuspy CDM profile



Hayashi, Chiba, and Ishiyama, ApJ, 2020

Data points

Classical dwarfs

- one possibility is to take as a tiny cross section as $\sigma_{\text{self}}/m \simeq 0.01 \text{ cm}^2/\text{g}$

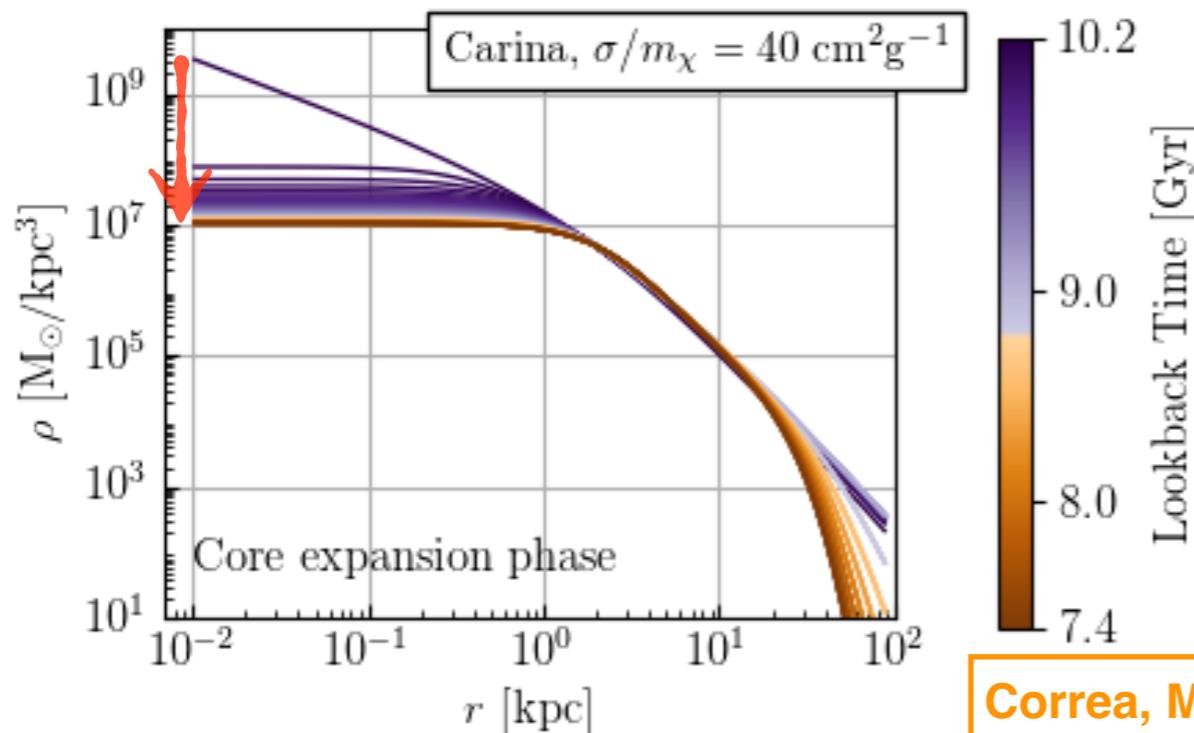
$$\langle v_{\text{rel}} \rangle \sim 30 \text{ km/s}$$

- resonance?

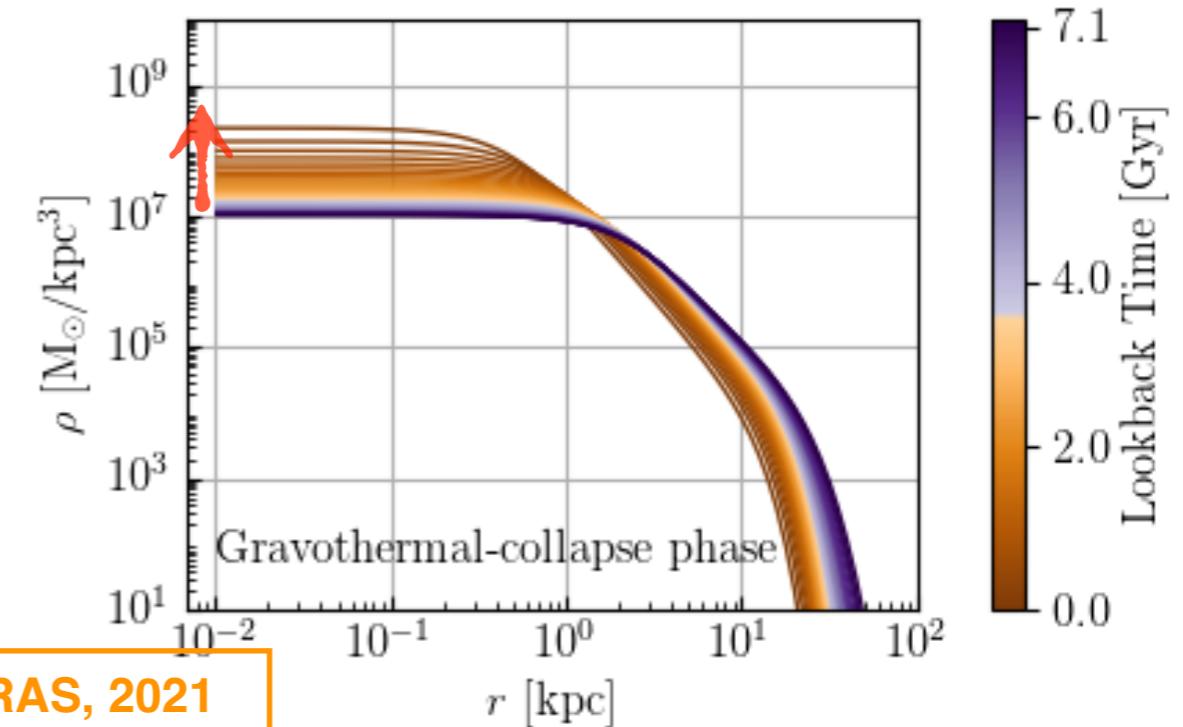
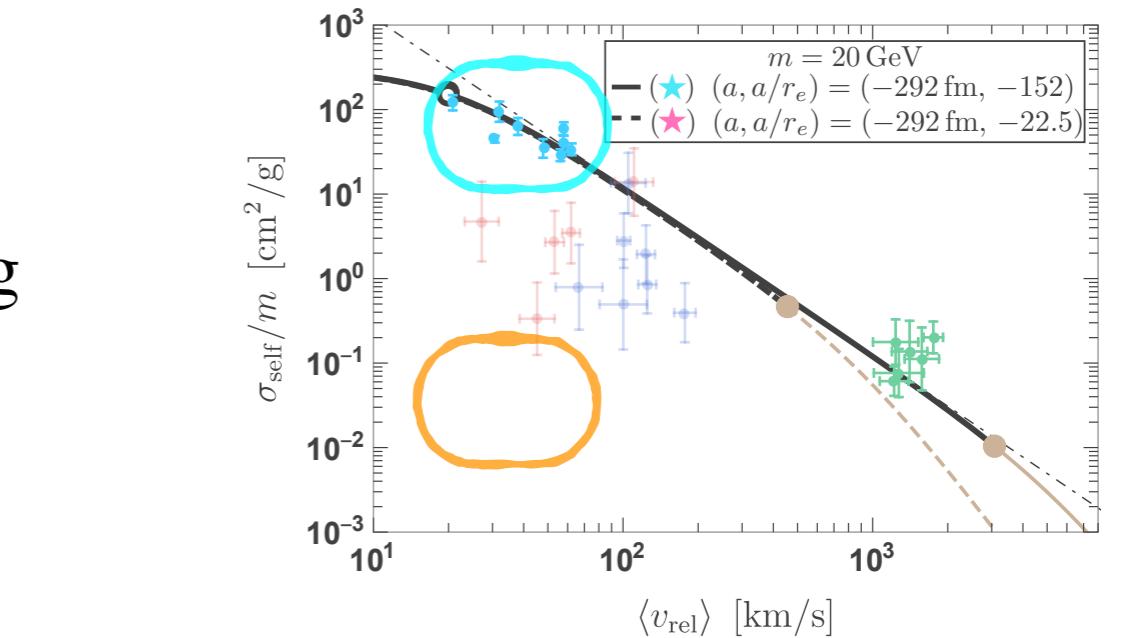
Chu, Garcia-Cely, and Murayama, PRL, 2019

- another possibility is to take as a large cross section as $\sigma_{\text{self}}/m \sim 40 \text{ cm}^2/\text{g}$ $\langle v_{\text{rel}} \rangle \sim 30 \text{ km/s}$

- gravothermal collapse



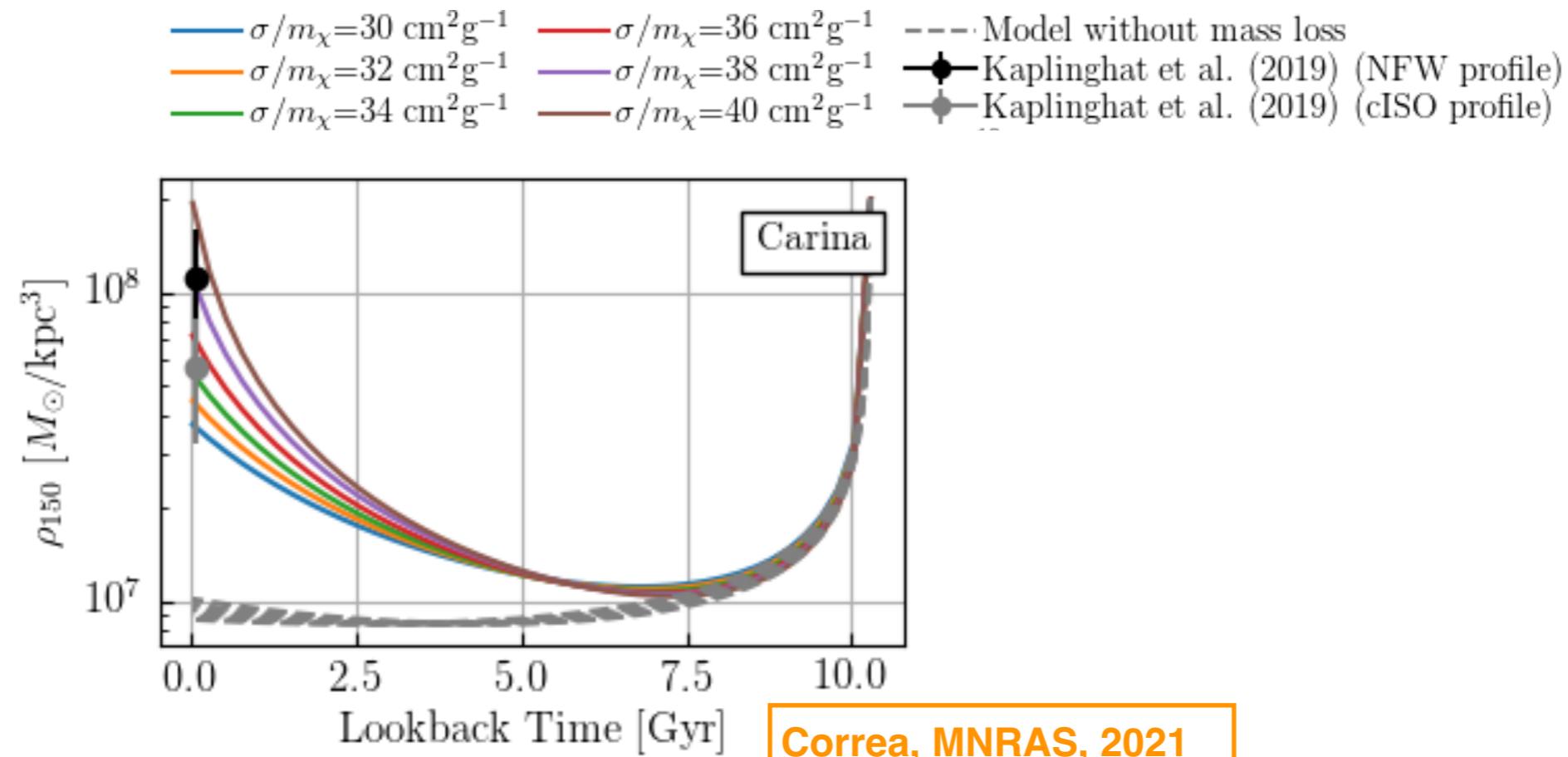
Correa, MNRAS, 2021



Data points

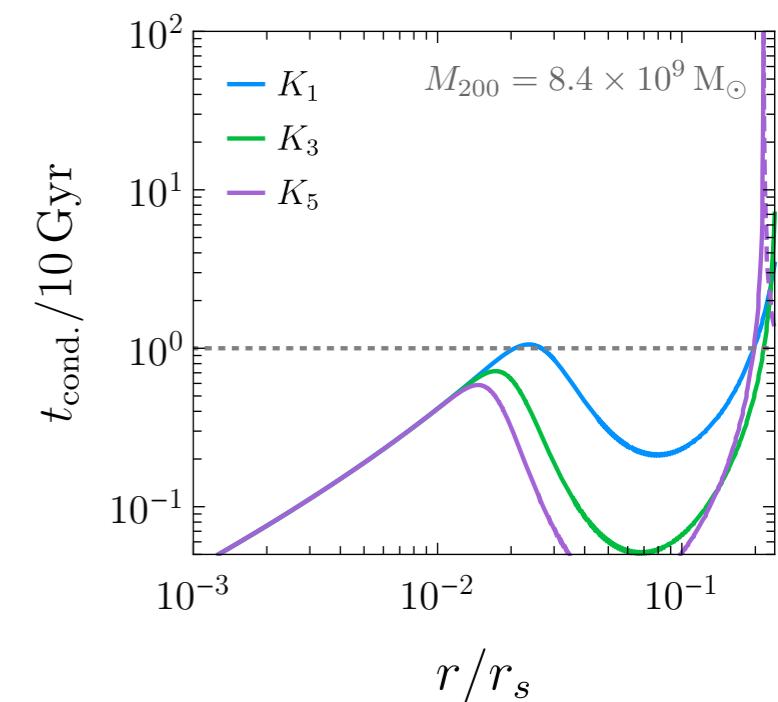
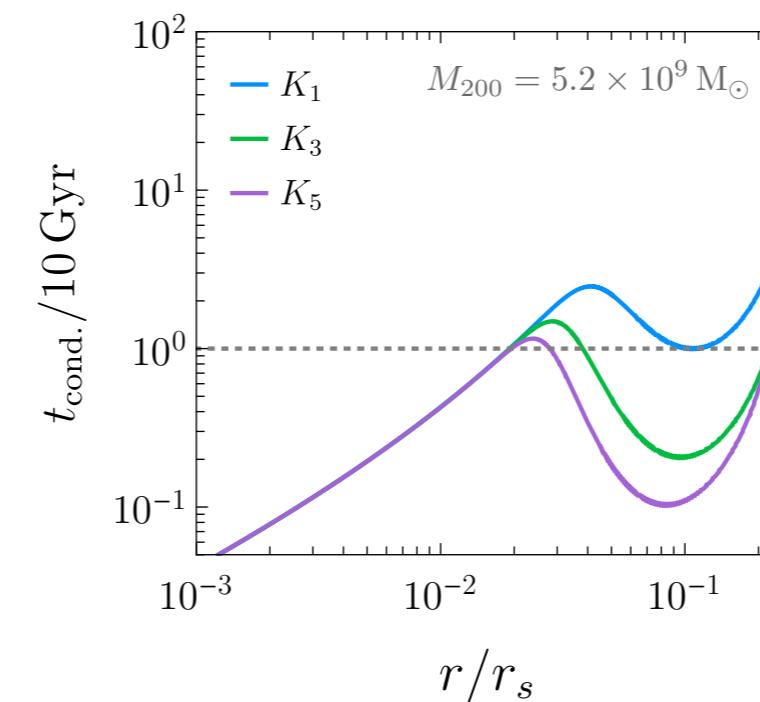
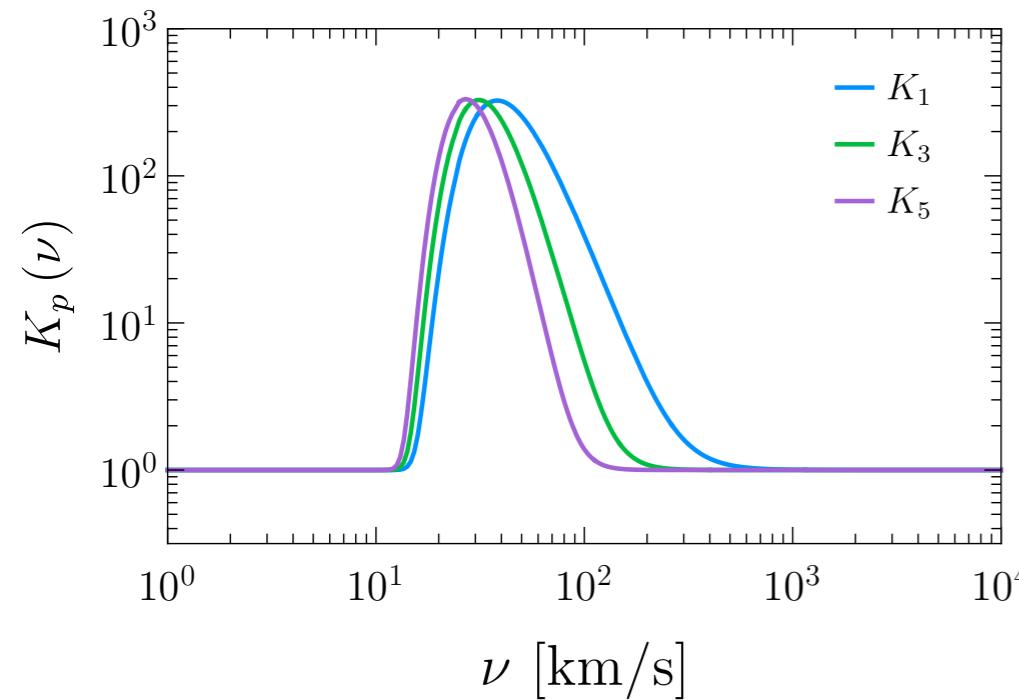
Classical dwarfs

- gravothermal collapse
 - core shrinks and central density gets higher
 - central density at present is very sensitive to the cross section



Gravothermal modeling

Dependence on distribution averaging



Evolution of resonant SIDM halos

Formation and thermalization time

