

## Fragmentation @ $e^+e^-$ colliders: Opportunities & Challenges

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Gunar.Schnell @ DESY.de



# single-hadron\*) (TMD) fragmentation functions

\*) complemented by rich world of di-hadron FFs

		quark pol.		
		U	L	T
hadron pol.	U	$D_1$		$H_1^\perp$
	L		$G_1$	$H_{1L}^\perp$
	T	$D_{1T}^\perp$	$G_{1T}^\perp$	$H_1 H_{1T}^\perp$

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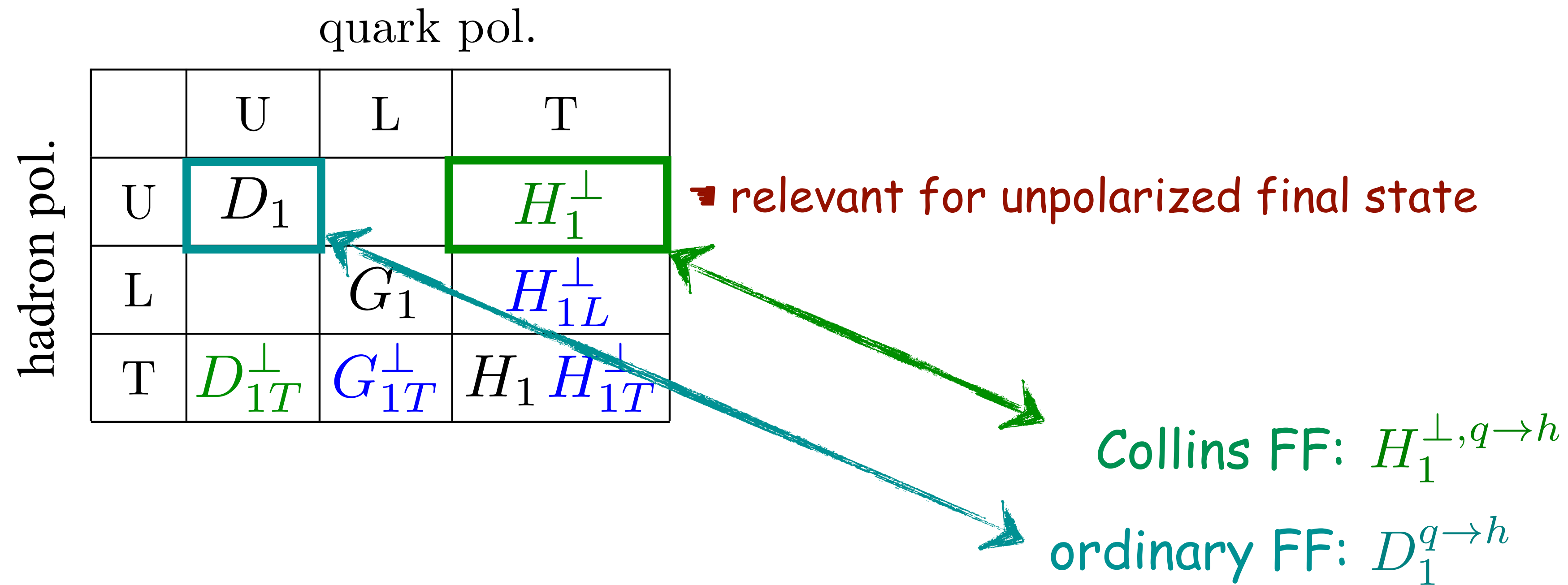
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relevant for unpolarized final state

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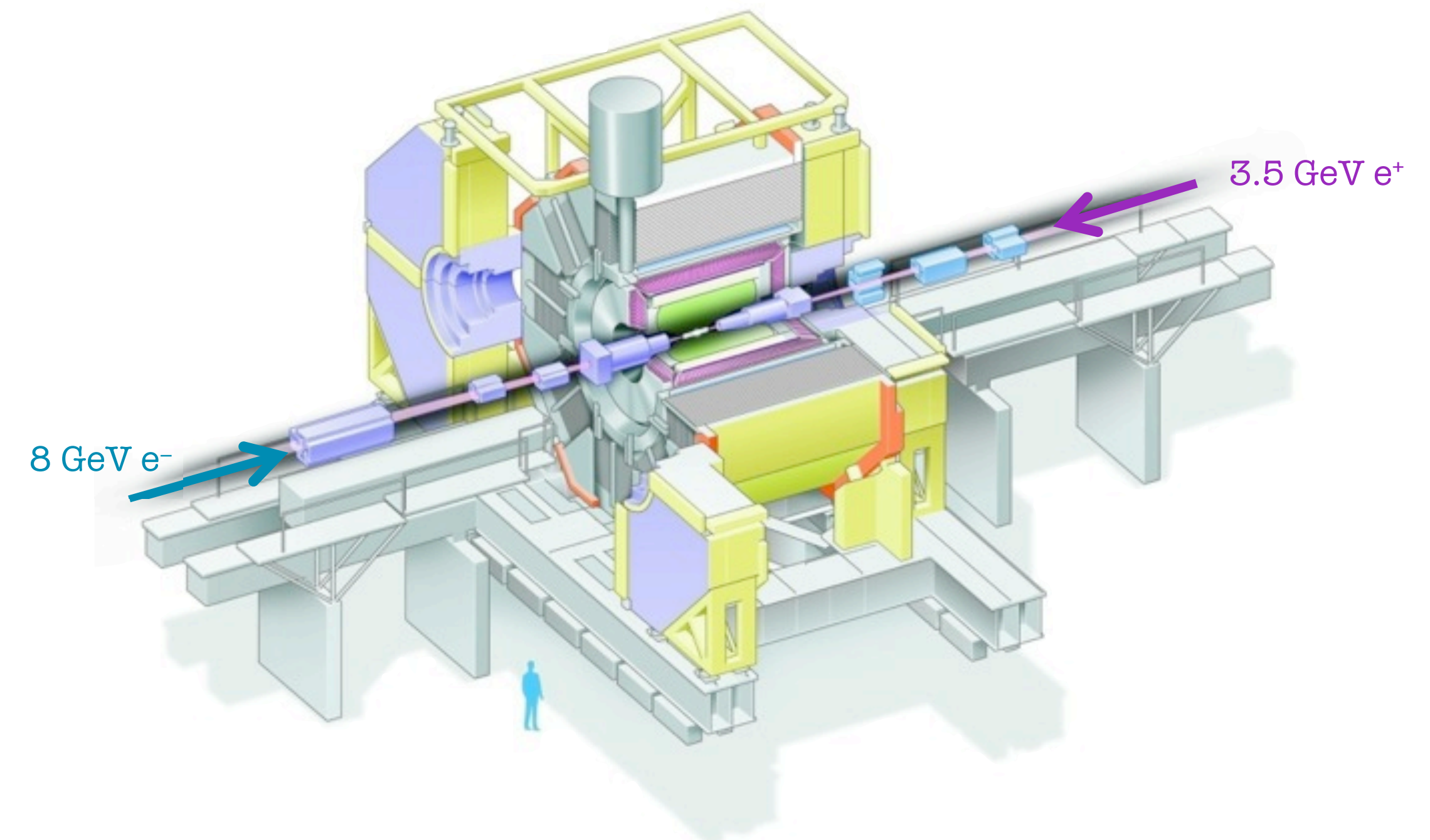
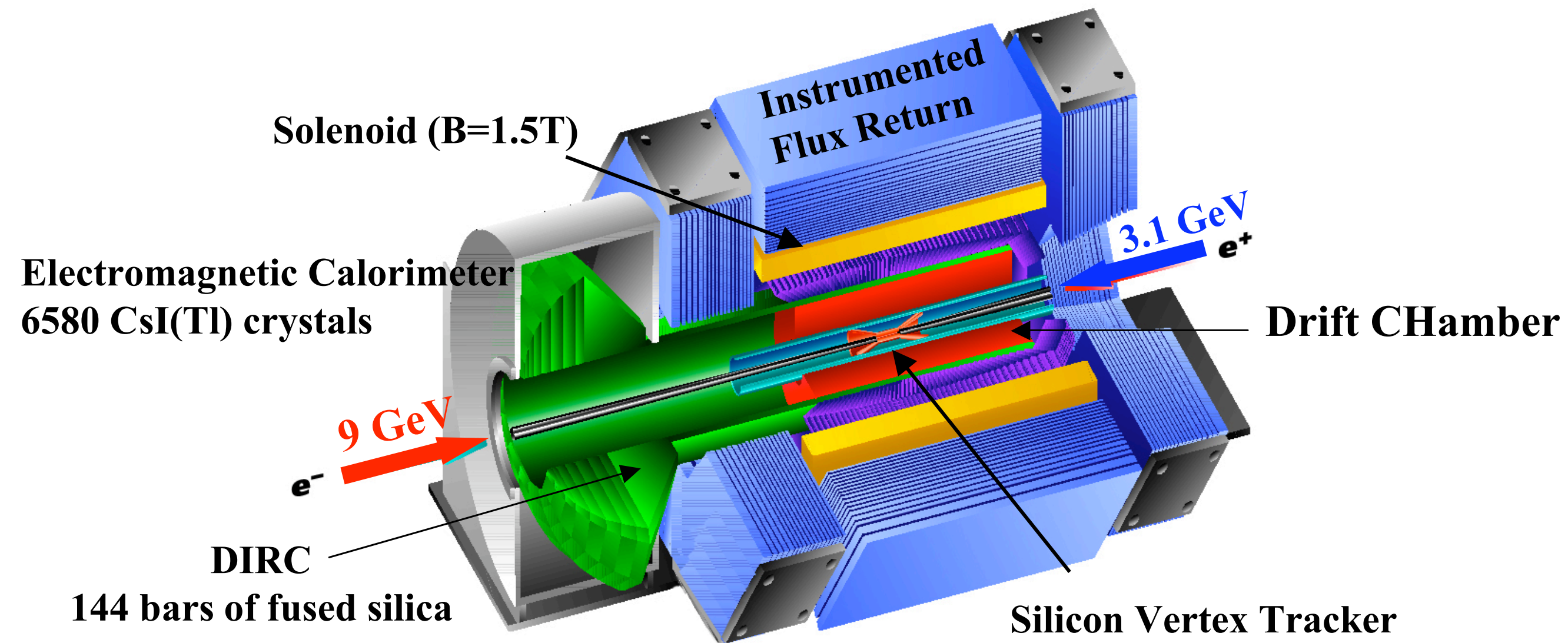
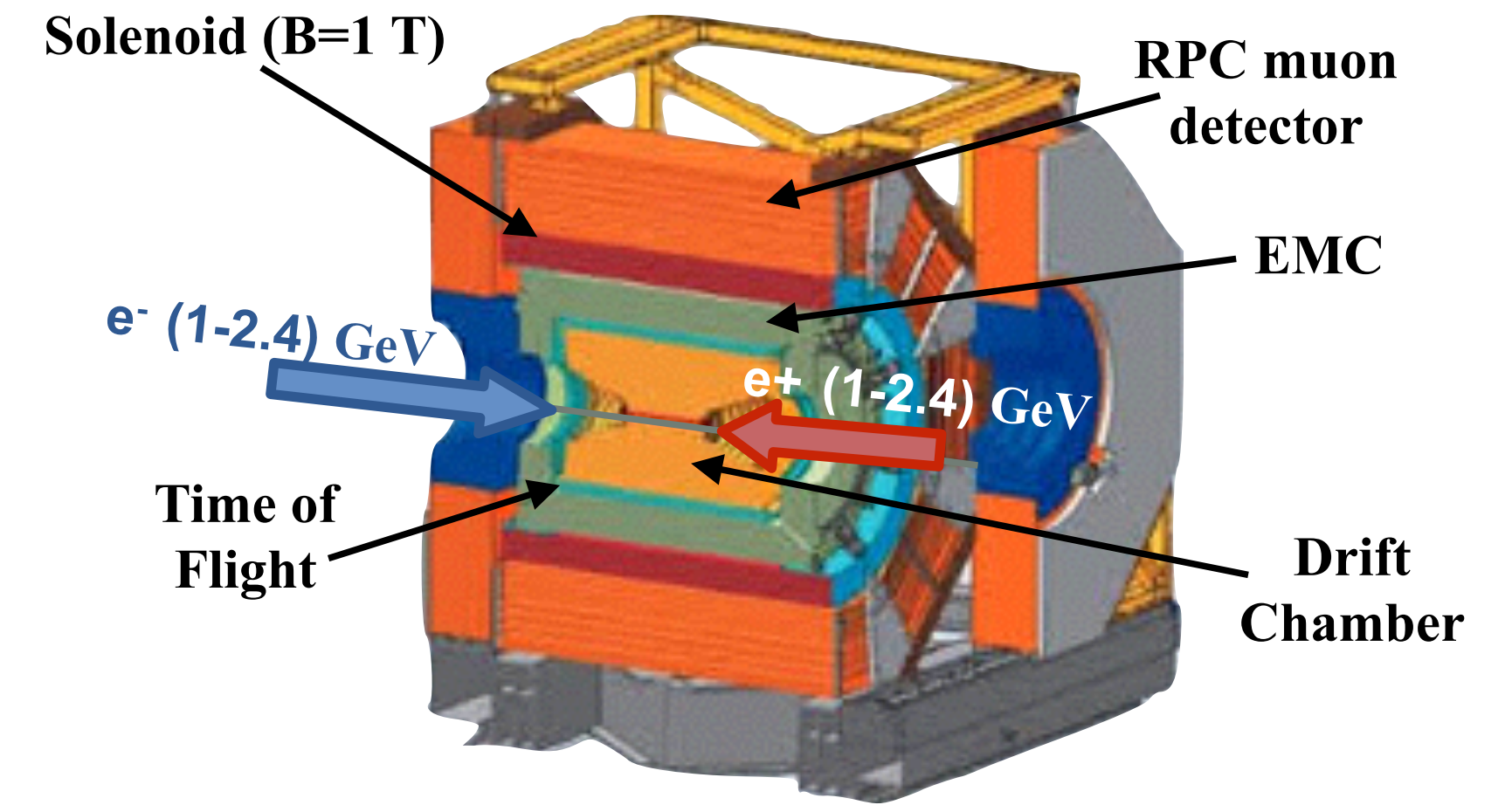
⇒ FFs act as quark flavor-tagger and polarimeter

FF ... fragmentation function



# $e^+e^-$ annihilation at BESIII, BaBar & Belle

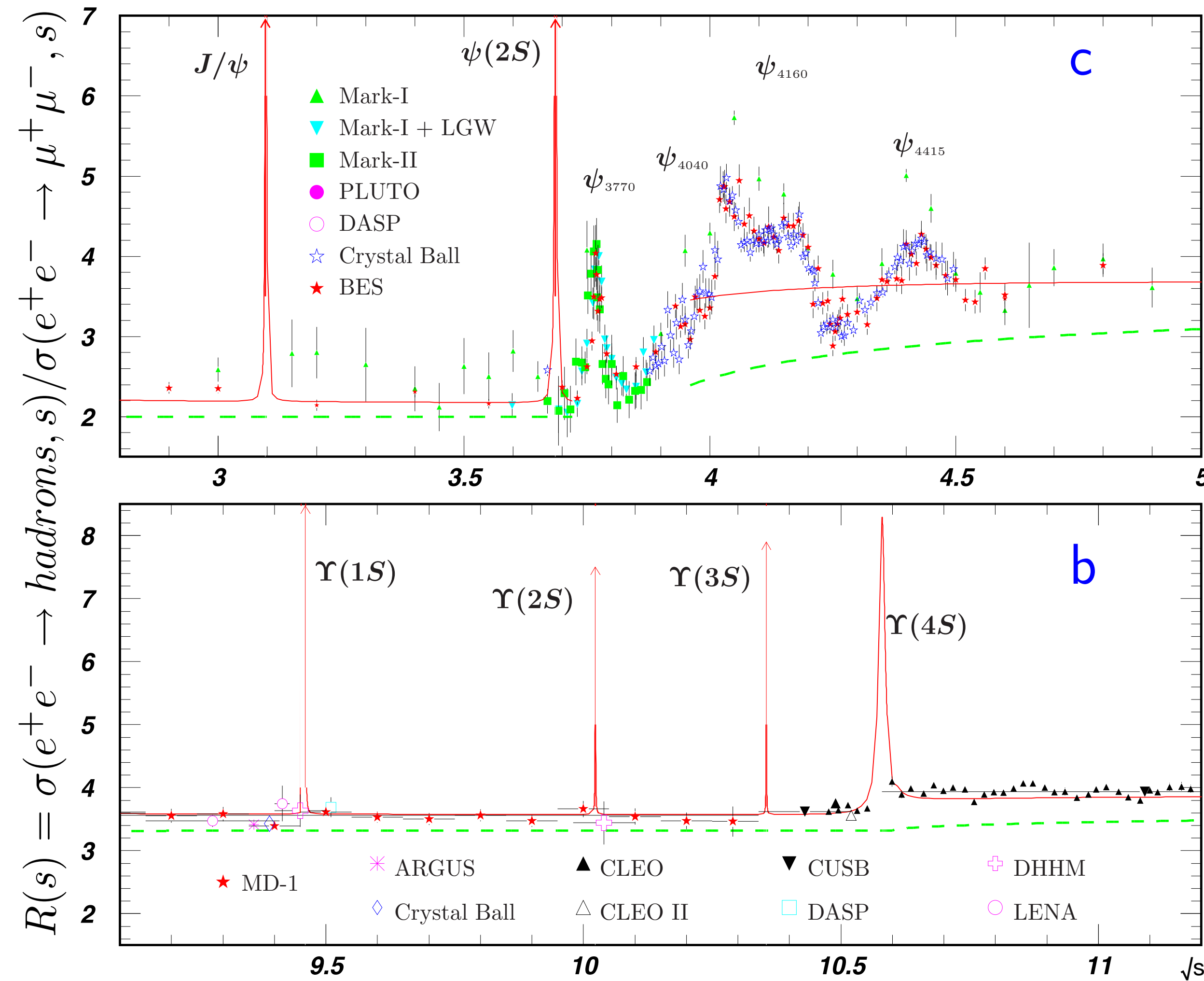
- BESIII: symmetric collider ( $E_e=1\dots 2.4$  GeV)
- BaBar/Belle: asymmetric beam-energy  $e^+e^-$  collider near/at  $\Upsilon(4S)$  resonance





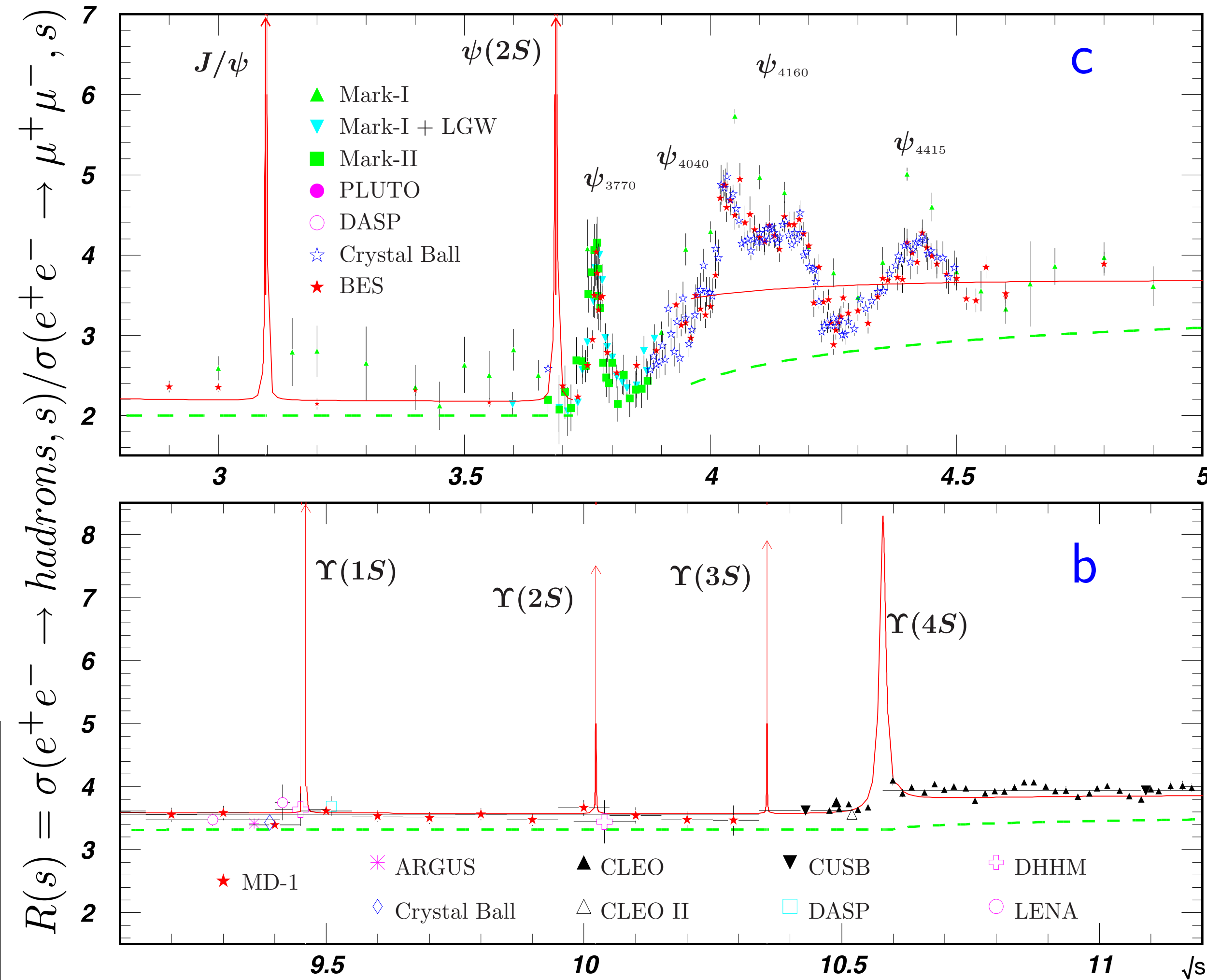
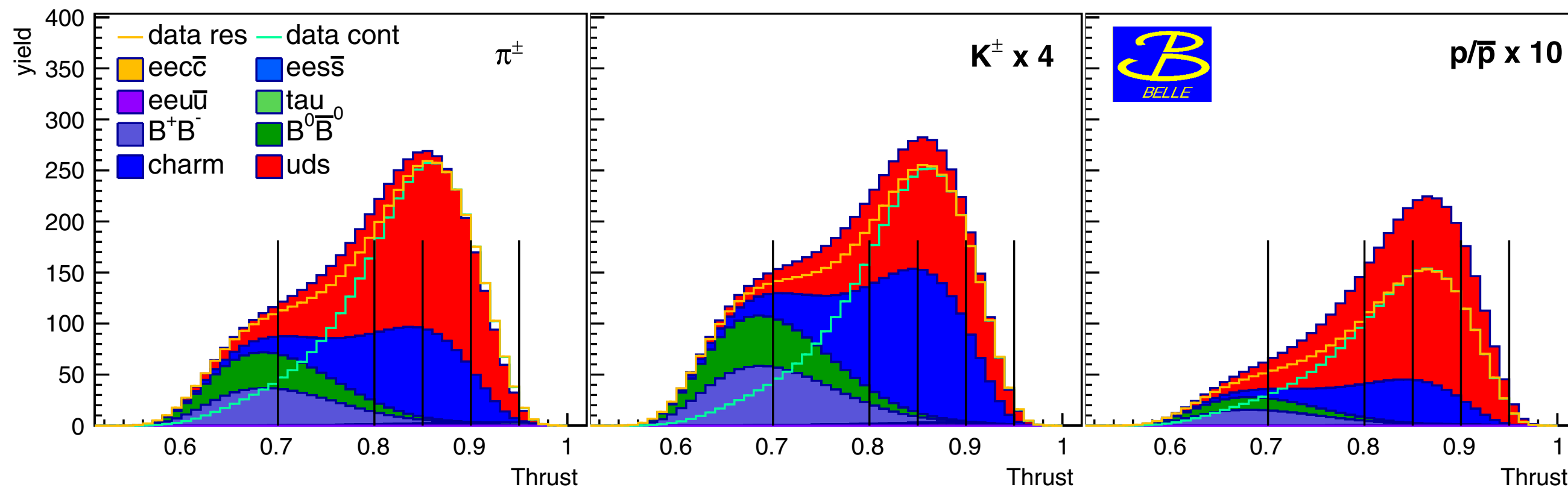
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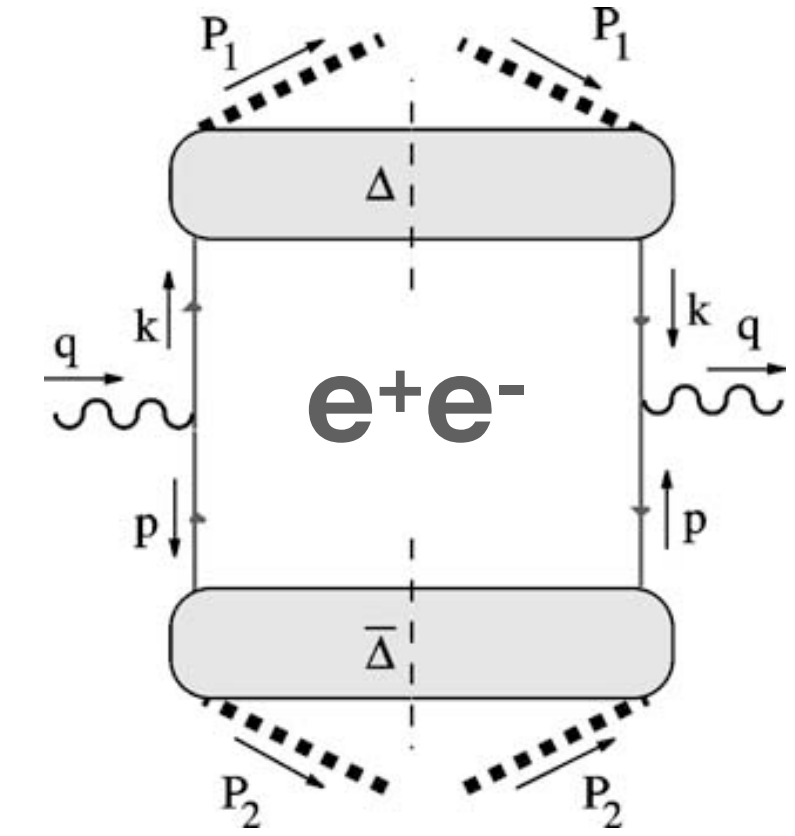
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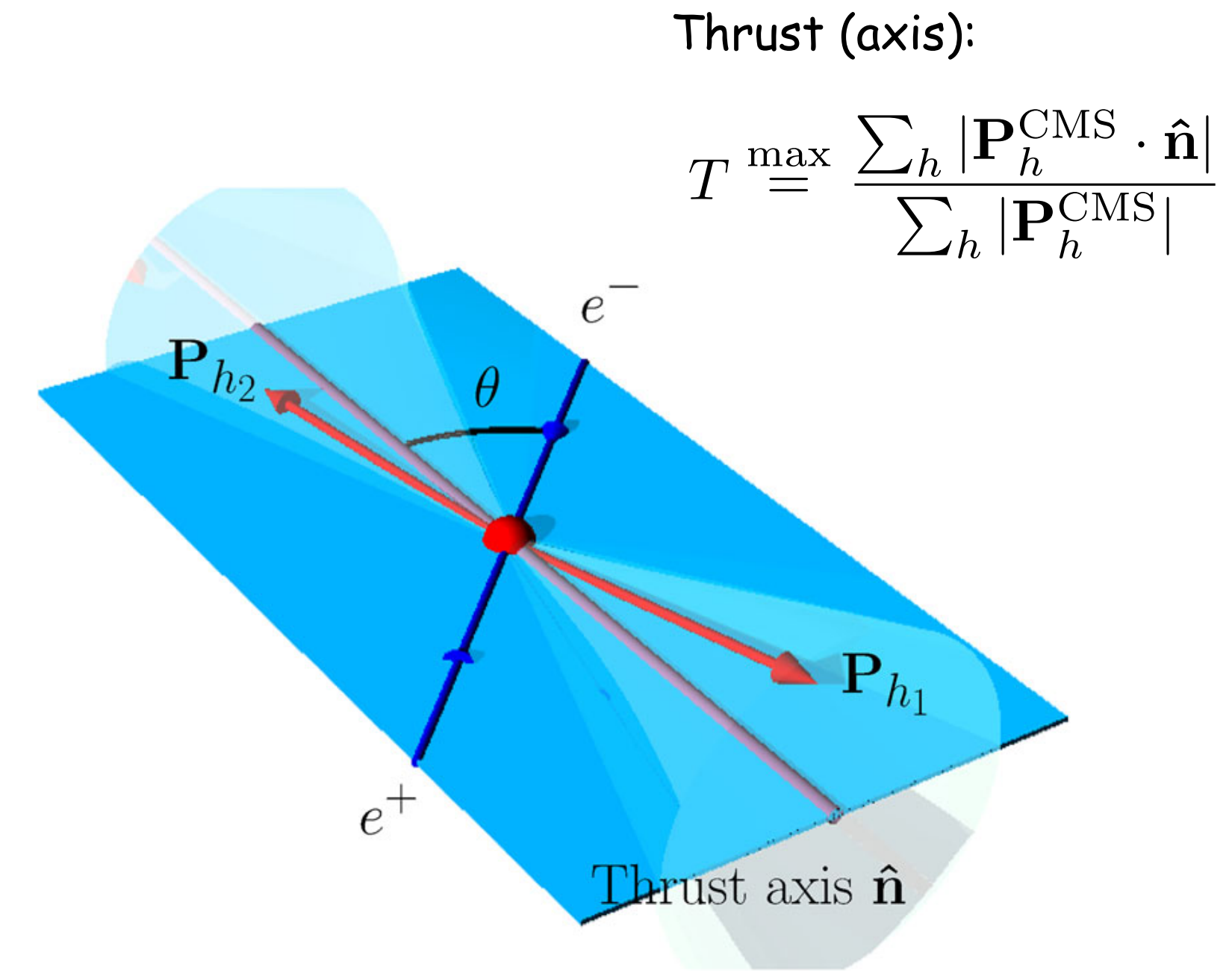
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- $D_1$  fragmentation function
- ( $D_{1T^\perp}$  spontaneous transv. polarization)



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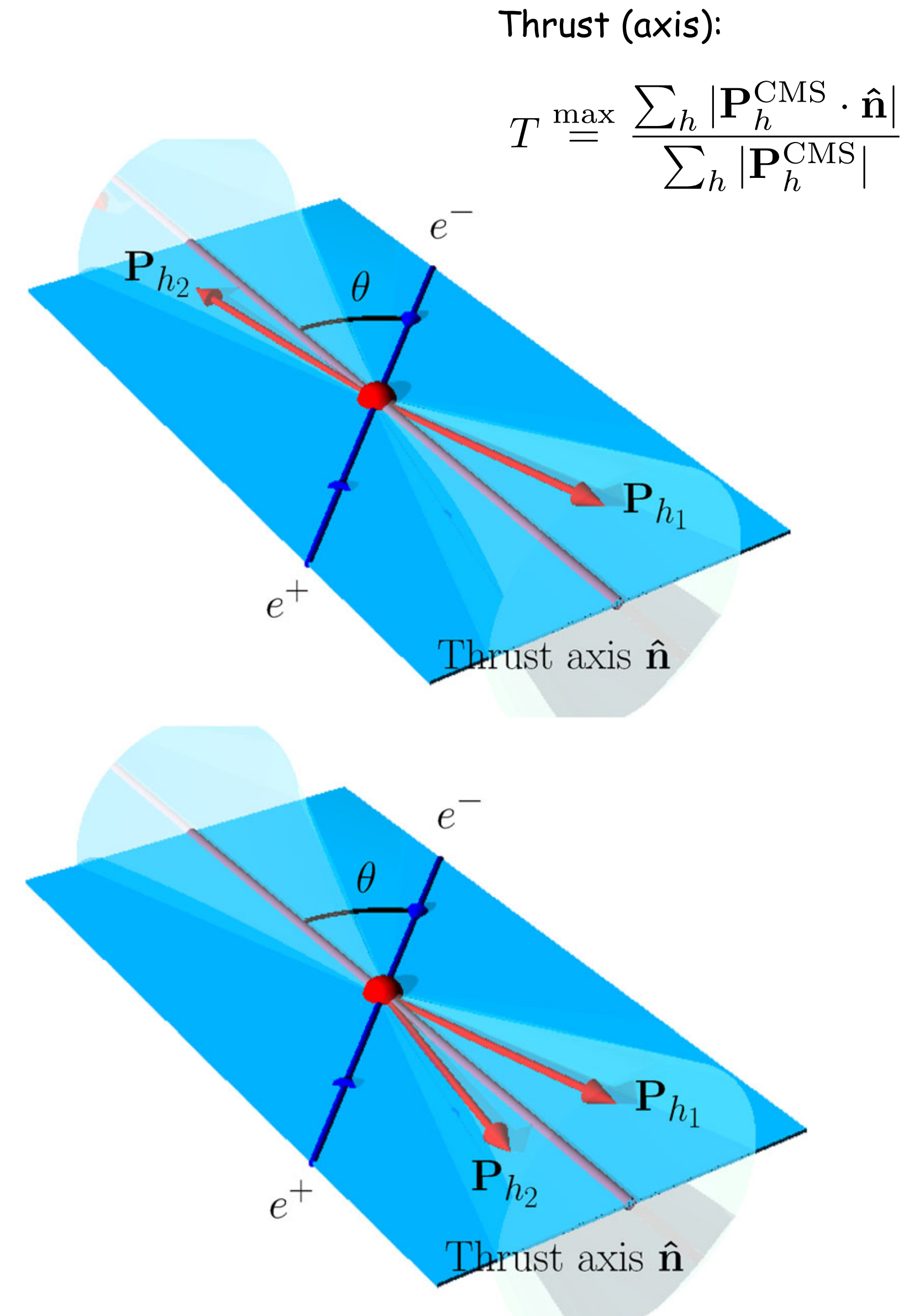
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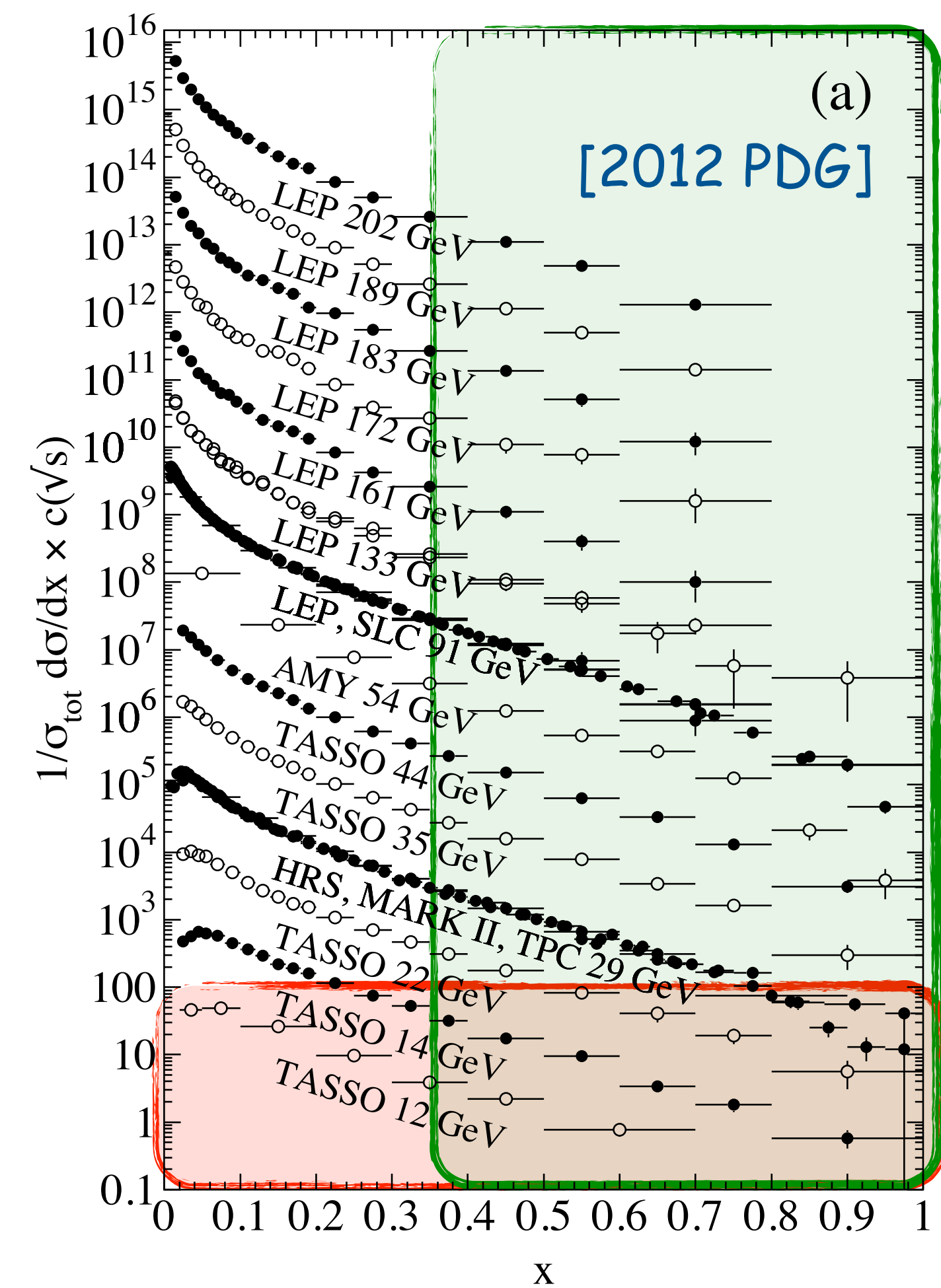
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  - di-hadron fragmentation



the collinear case

# single-hadron production

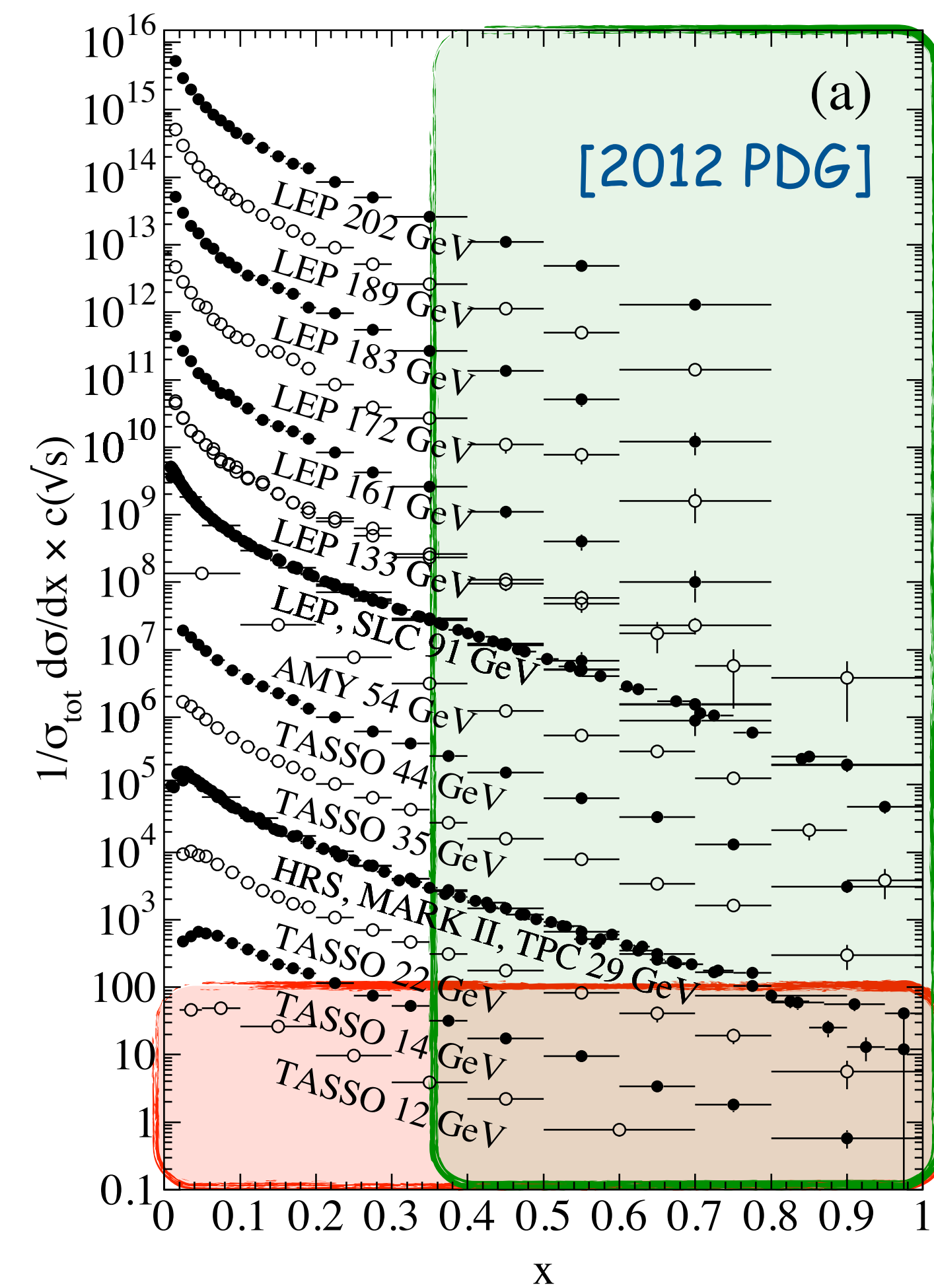
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- limits analysis of evolution and gluon fragmentation
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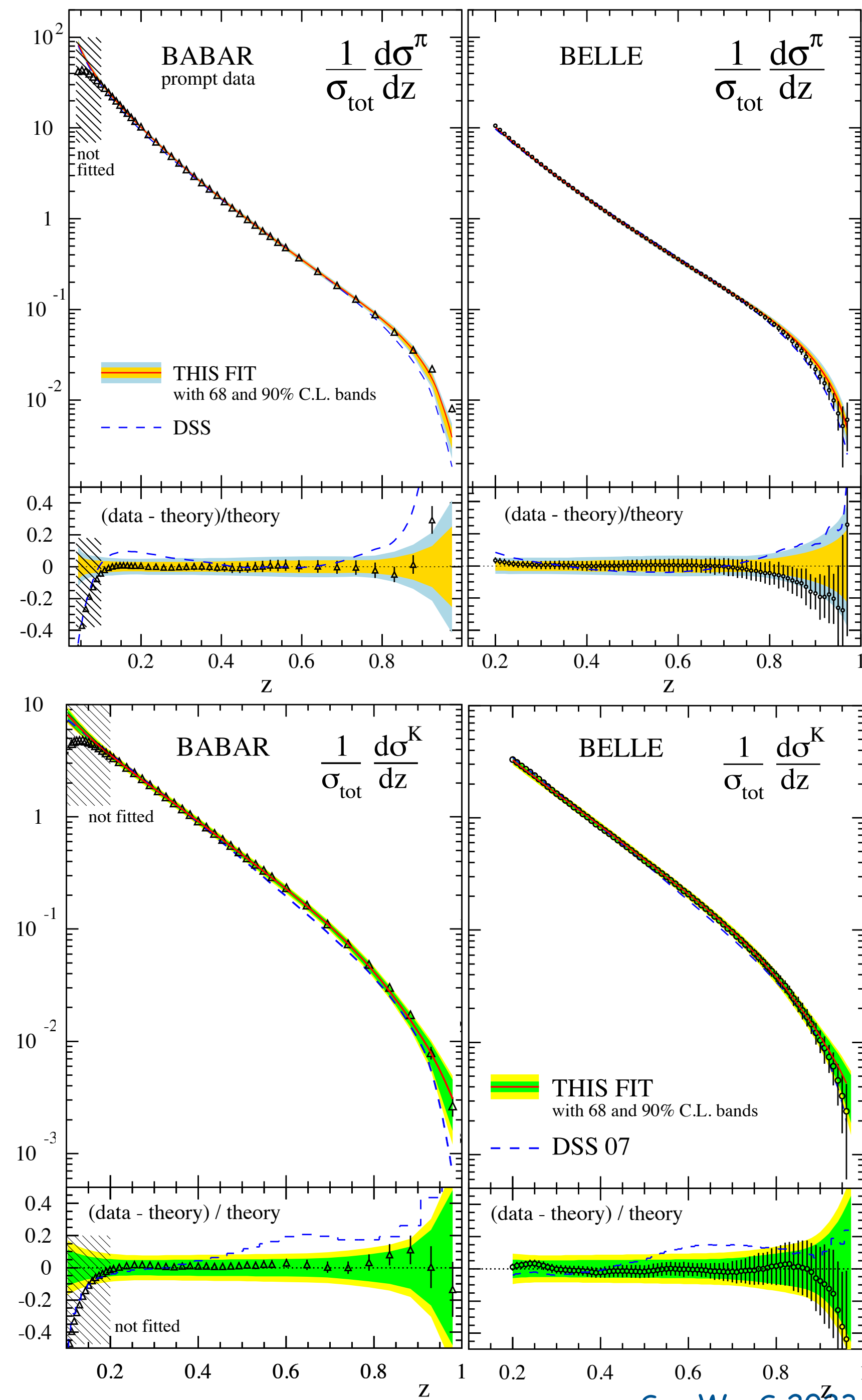
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- limits analysis of evolution and gluon fragmentation
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- by now also results from BaBar, Belle, and BESIII:
  - BaBar Collaboration, PRD 88 (2013) 032011:  $\pi^\pm$ ,  $K^\pm$ ,  $p+\bar{p}$
  - Belle Collaboration, PRL 111 (2013) 062002:  $\pi^\pm$ ,  $K^\pm$
  - Belle Collaboration, PRD 92 (2015) 092007 & 101 (2020) 092004:  $\pi^\pm$ ,  $K^\pm$ ,  $p+\bar{p}$
  - **NEW**: BESIII Collaboration, arXiv:2211.11253:  $\pi^0$ ,  $K_S^0$



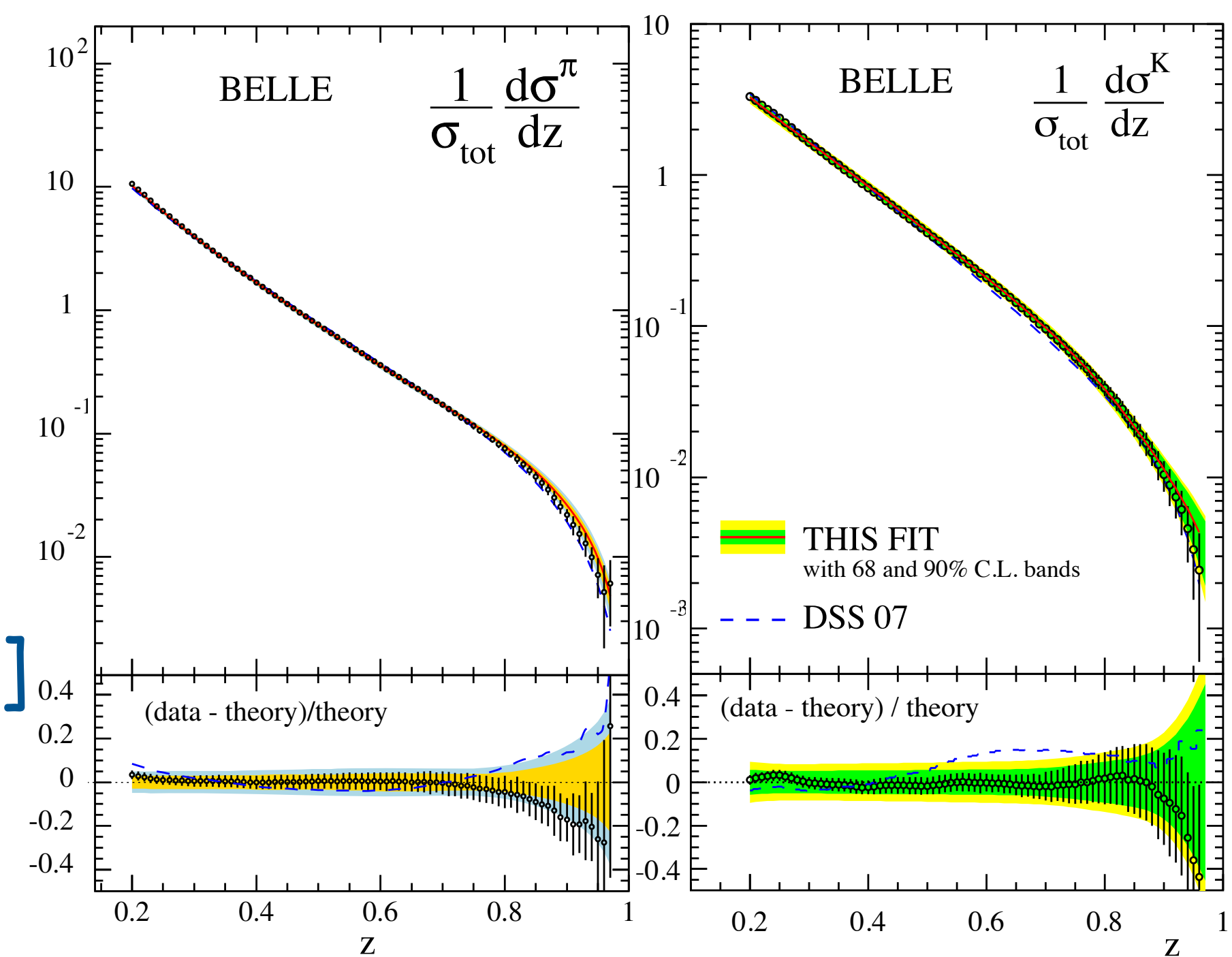
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- very precise data for charged pions and kaons
- Belle data available up to very large  $z$  ( $z < 0.98$ )
- included in 2015 DEHSS fits [e.g., PRD91 (2015) 014035]
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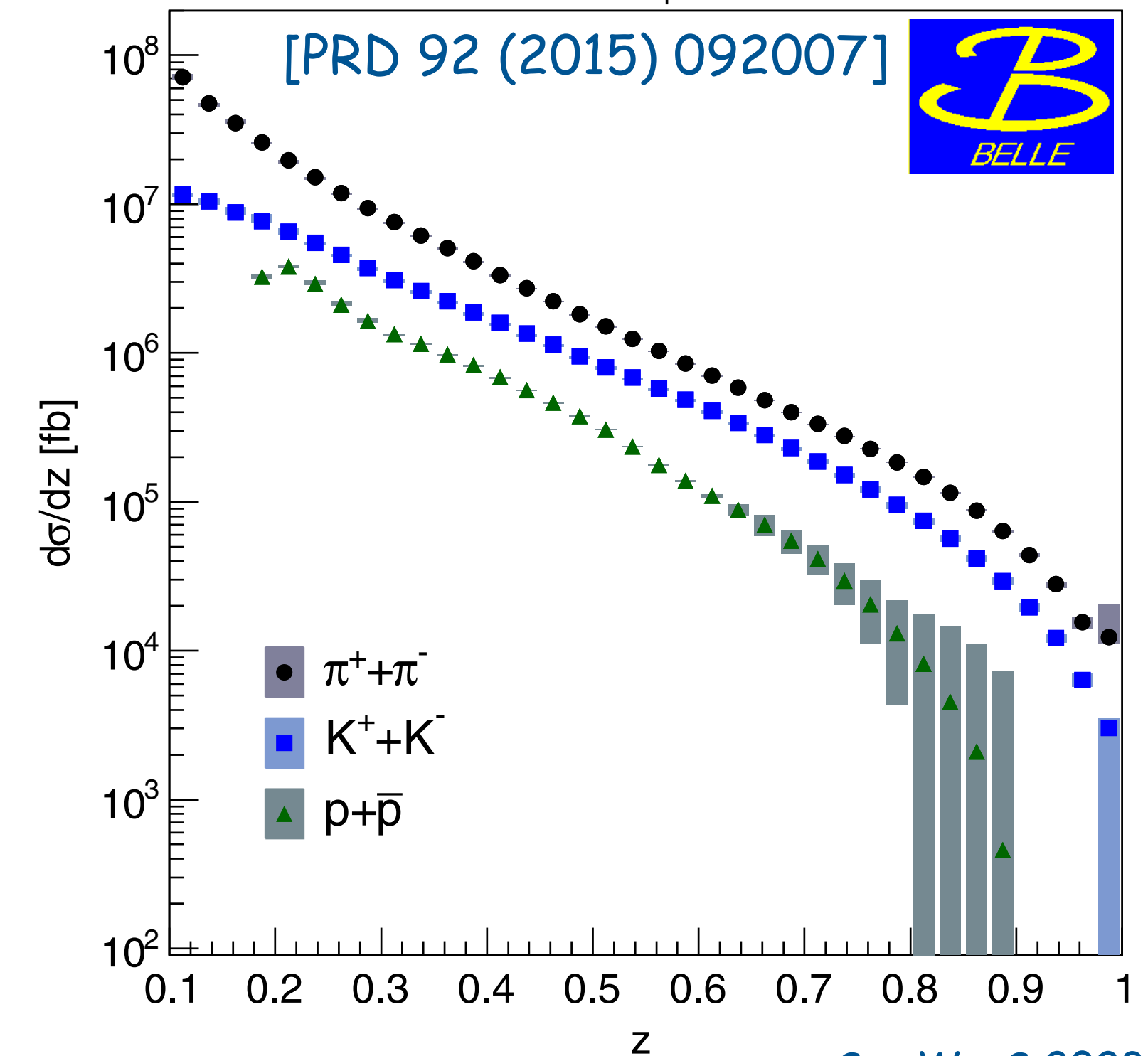
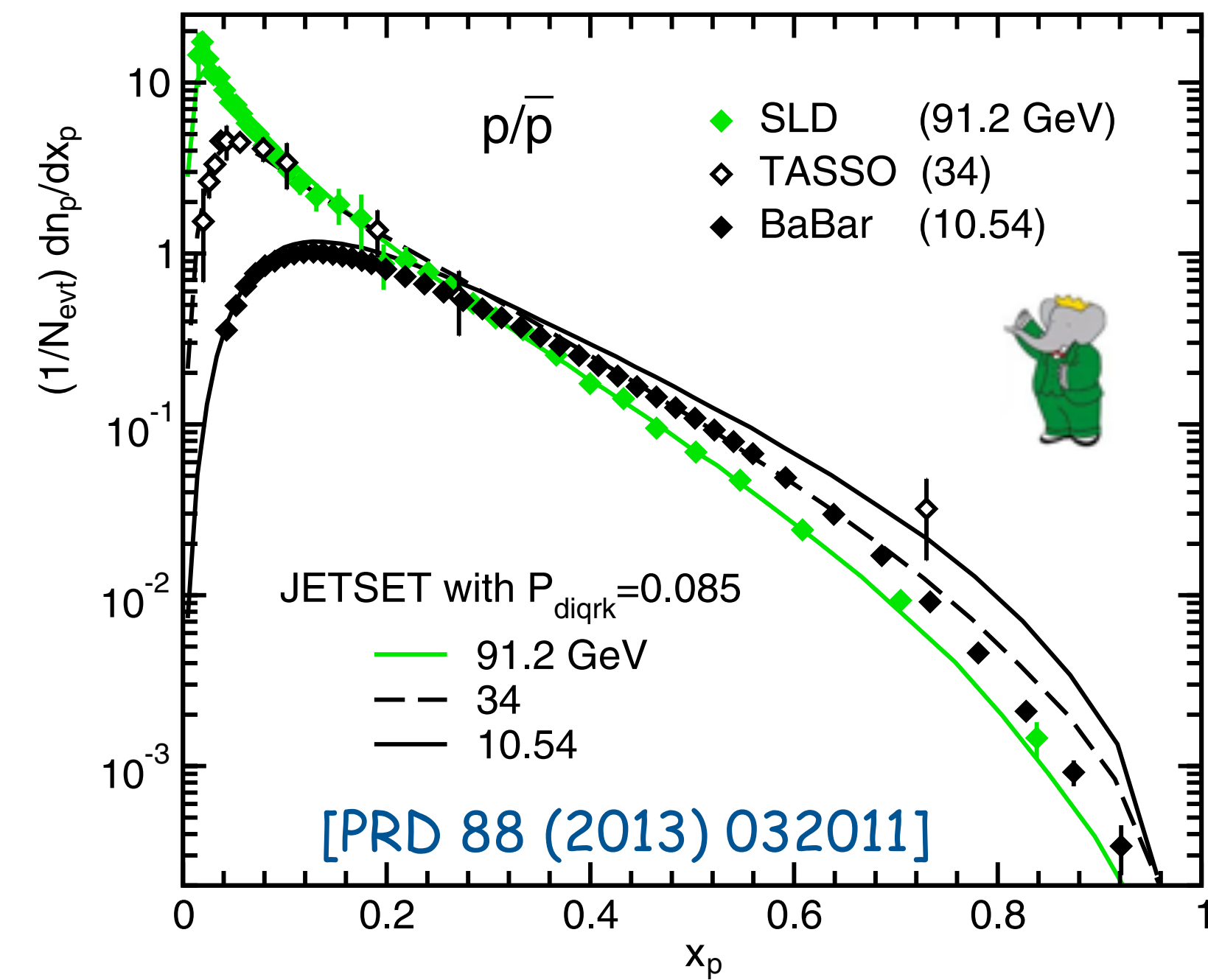
[EPJC 77 (2017) 516, NNFF1.0]

In the case of the BELLE experiment we multiply all data points by a factor  $1/c$ , with  $c = 0.65$  for charged pions and kaons [69] and with  $c$  a function of  $z$  for protons/antiprotons [53]. This correction is required in order to treat the BELLE data consistently with all the other SIA measurements included in NNFF1.0. The reason is that a kinematic cut on radiative photon events was applied to the BELLE data sample in the original analysis instead of unfolding the radiative QED effects. Specifically, the energy scales



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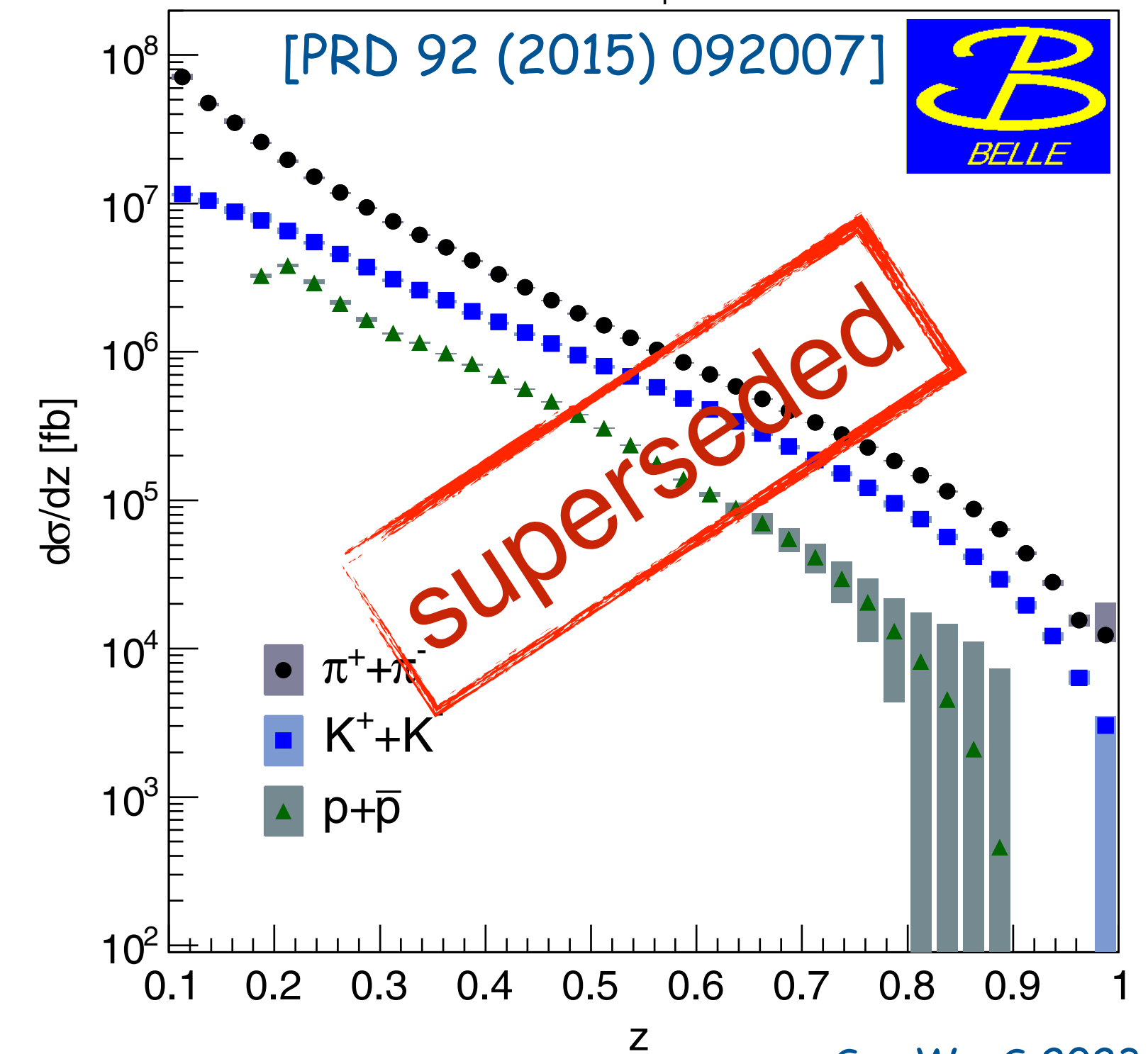
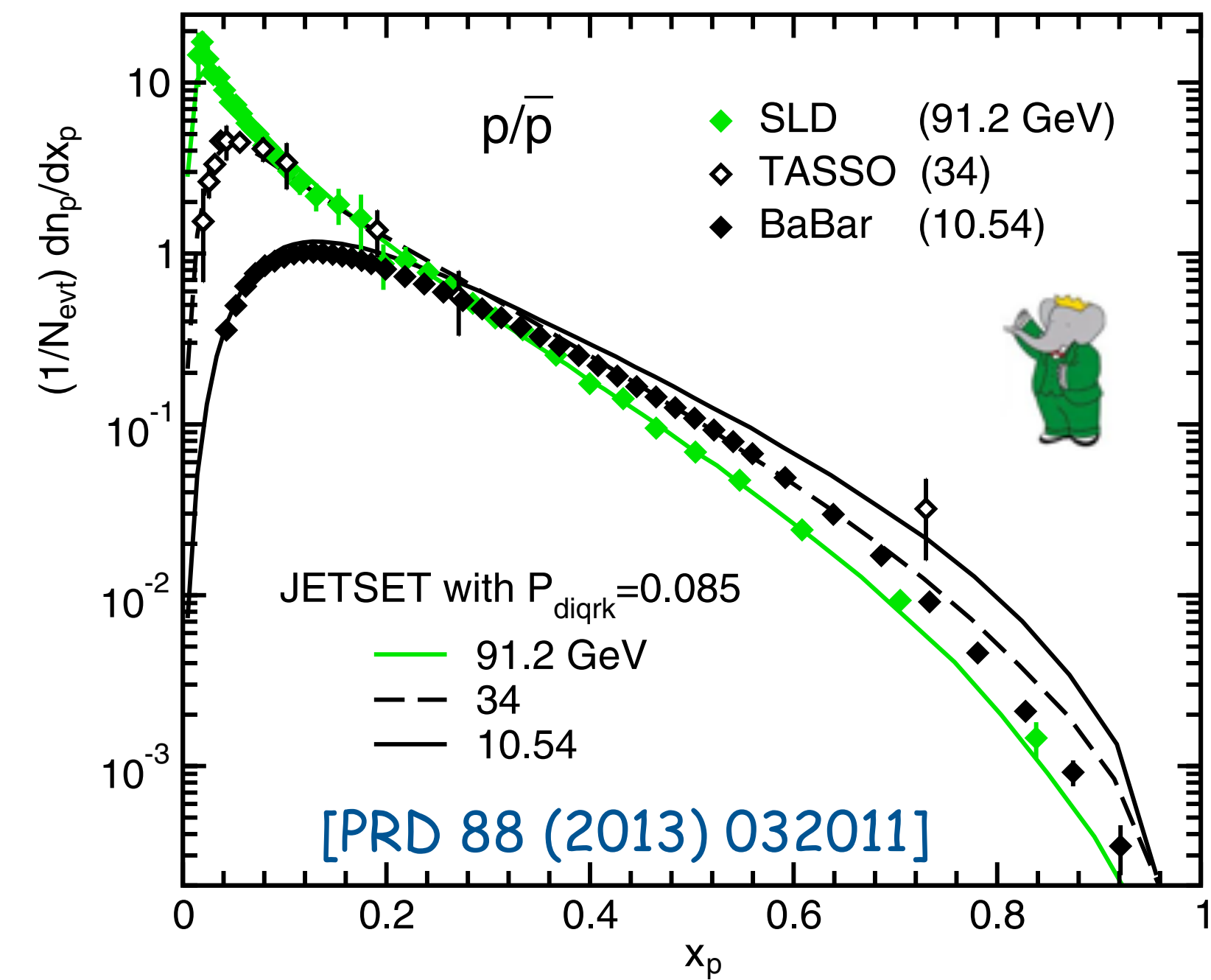
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- data available for (anti)protons
  - not (yet) included in DEHSS or MAPFF, but, e.g., in NNFF 1.0 [EPJC 77 (2017) 516]
  - similar  $z$  dependence as pions
  - about  $\sim 1/5$  of pion cross sections





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- Belle re-analysis presented in PRD 101 (2020) 092004



**interlude**  
about counting

- cross sections are basically count rates
- “how to count?” sounds like a simple question, but the devil is in the details
  - what to do with hadrons that have (somewhere!) an ISR photon
  - in general, how to deal with events that are assigned to “wrong” kinematic bin due to instrumental effects [e.g., measured and true momentum might differ]
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- hadron yields also undergo series of other corrections:
  - particle (mis)identification [e.g., not every identified pion was a pion]
  - non-qq processes [e.g., two-photon processes,  $\Upsilon \rightarrow BB, \dots$ ]
  - “ $4\pi$ ” correction [e.g., selection criteria and limited geometric acceptance]
  - “optional”: weak-decay removal [e.g., “prompt fragmentation”]



- what to do with hadrons that have (somewhere) an ISR photon
  - nothing! — leave it to phenomenology to deal with QED corrections
    - however, (uncorrected/corrected) yields are ISR & detector dependent
  - reject all events that have an isolated photon?
    - detectors almost never fully hermetic, many ISR photons travel down the beam pipe
    - still fully inclusive reaction?
  - use some Monte Carlo to estimate event fraction with an ISR photon that carries away more than  $x\%$  of total available energy (e.g., 0.5% as in earlier Belle analyses)
    - what is a reasonable choice for  $x$ ?
    - ISR treatment model dependent, indeed depends on annihilation cross section
  - use some Monte Carlo to estimate ratio of hadrons produced in absence of ISR vs. full QED+QCD simulation
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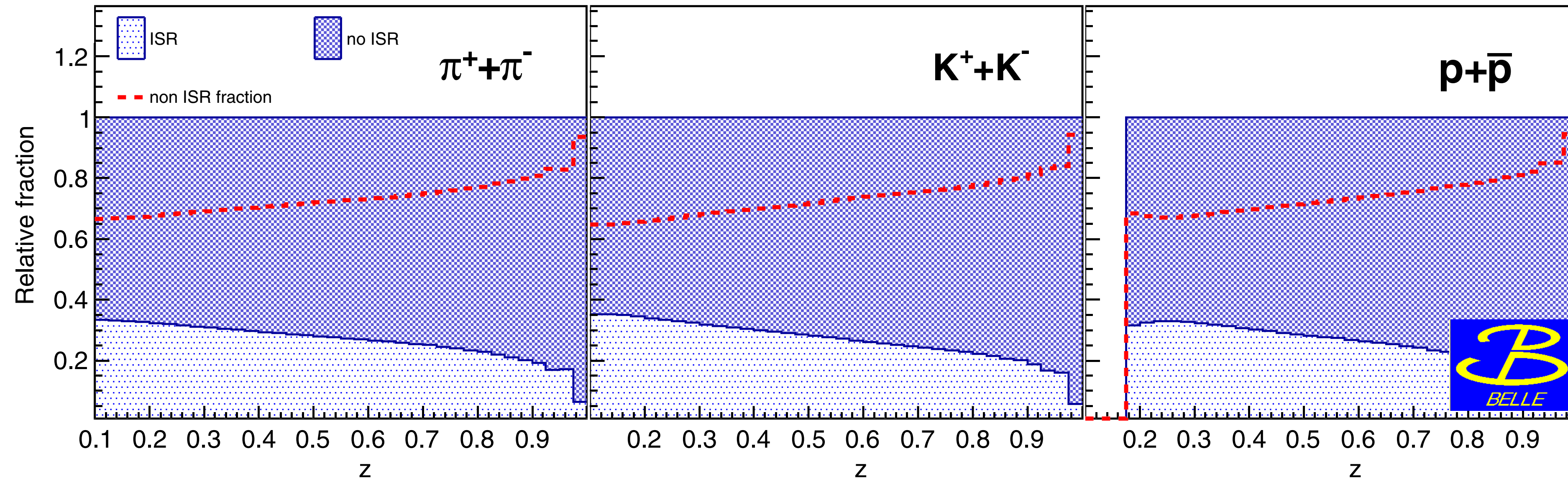
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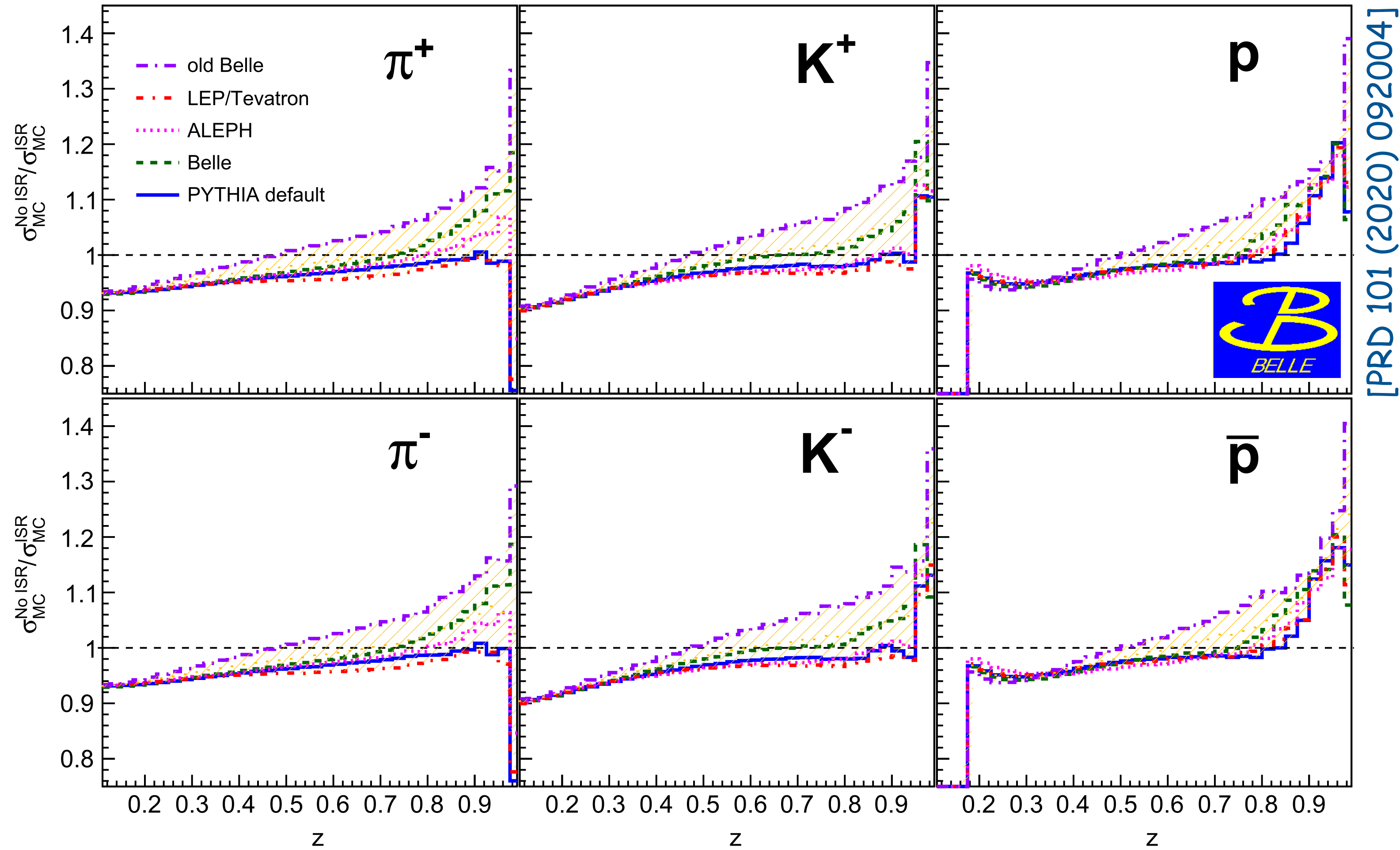
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# ISR corrections - PRD 92 (2015) 092007



- relative fractions of hadrons as a function of  $z$  originating from ISR or non-ISR events ( $\equiv$  energy loss less than 0.5%)
- large non-ISR fraction at large  $z$ , as otherwise not kinematically reachable (remember  $z = E_h / 0.5\sqrt{s_{\text{nominal}}}$ )
- keep only fraction of the events  $\rightarrow$  strictly speaking not single-inclusive annihilation
- currently used constant 0.65 correction to undo ISR correction is not a constant vs.  $z$

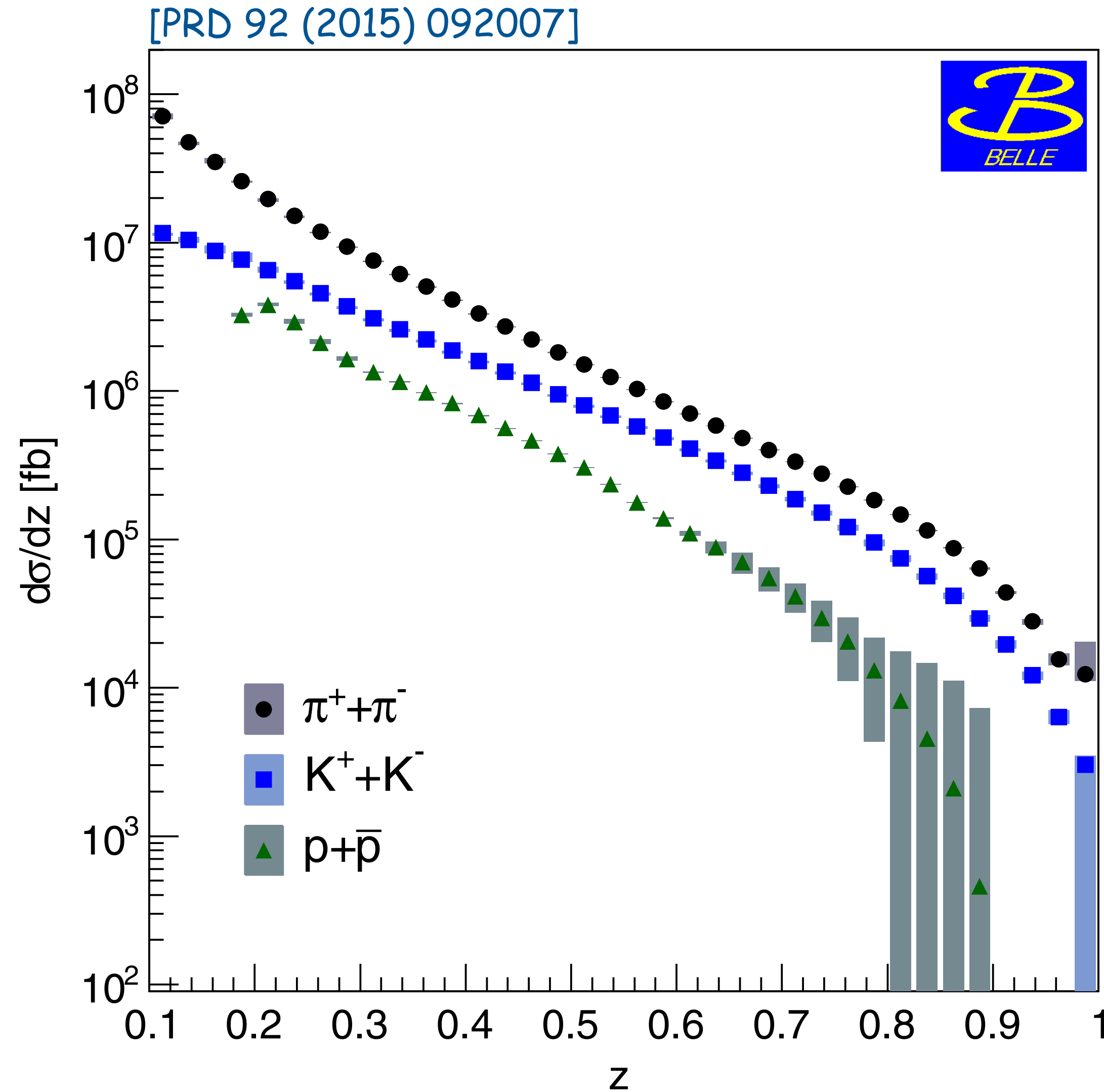
# ISR corrections - PRD 101 (2020) 092004



- non-ISR / ISR fractions based on PYTHIA switch MSTP(11)
- PYTHIA model dependence; absorbed in systematics by variation of tunes

# comparison old&new Belle single-hadron cross sections

● previous analysis

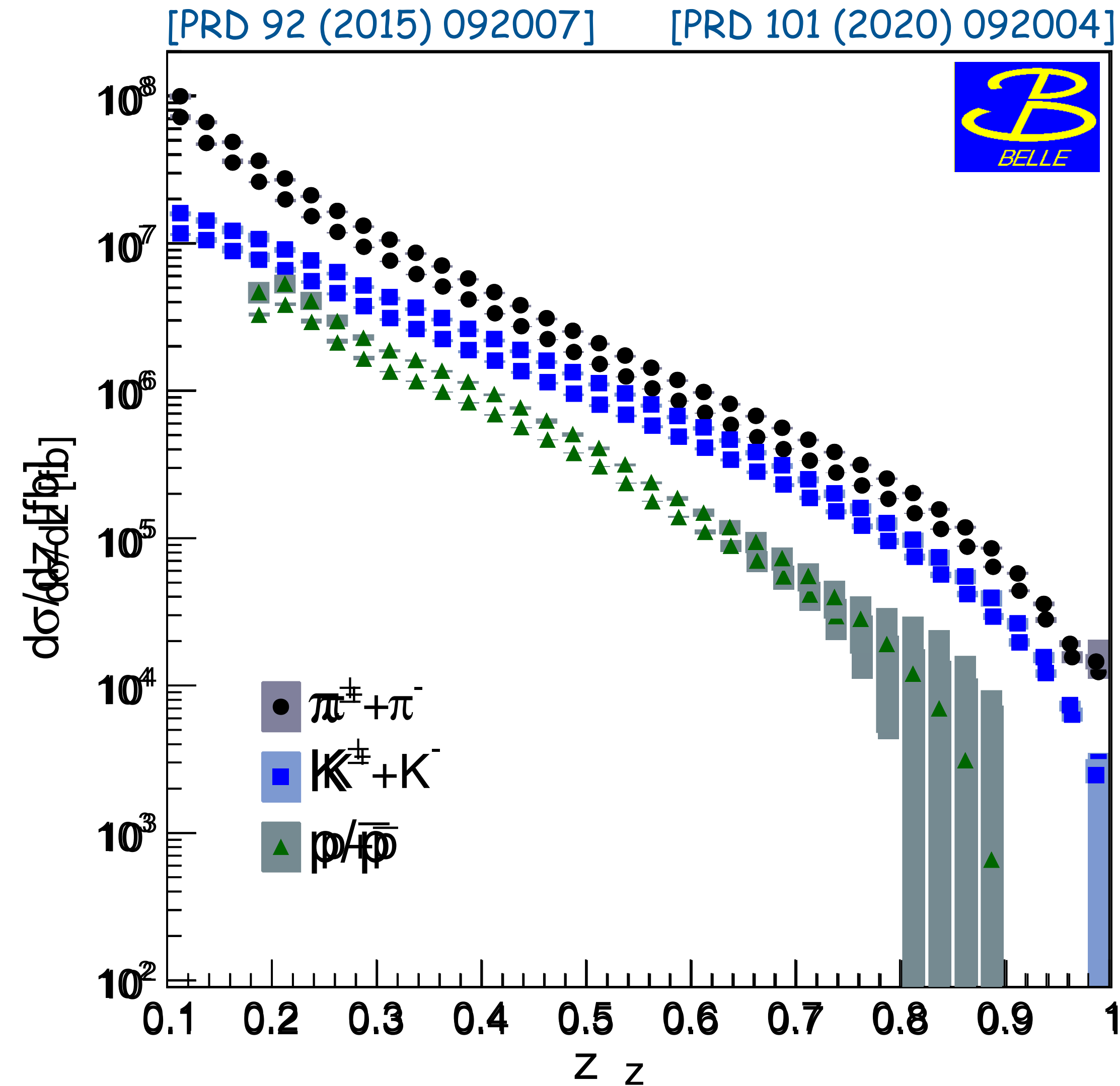




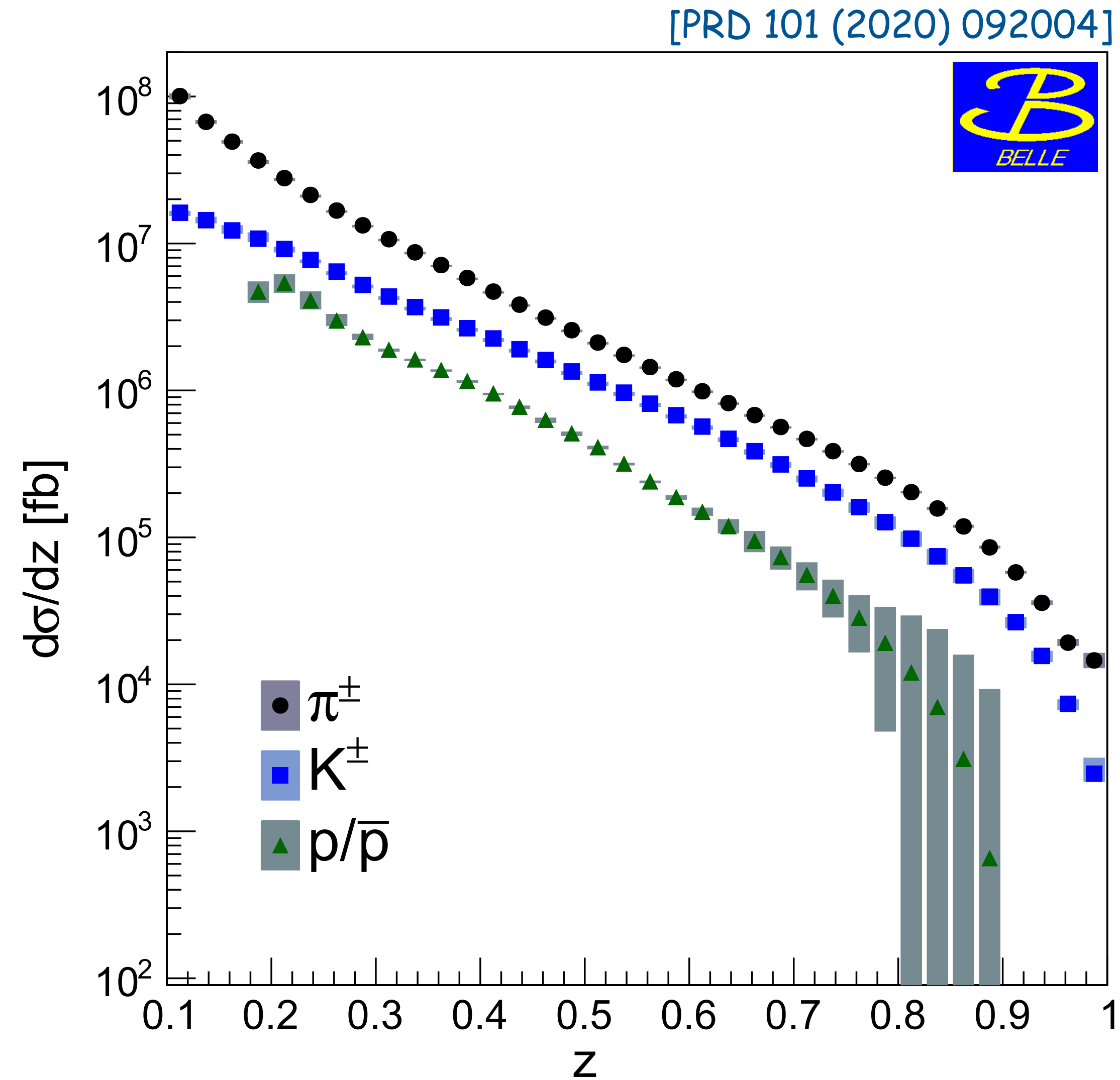
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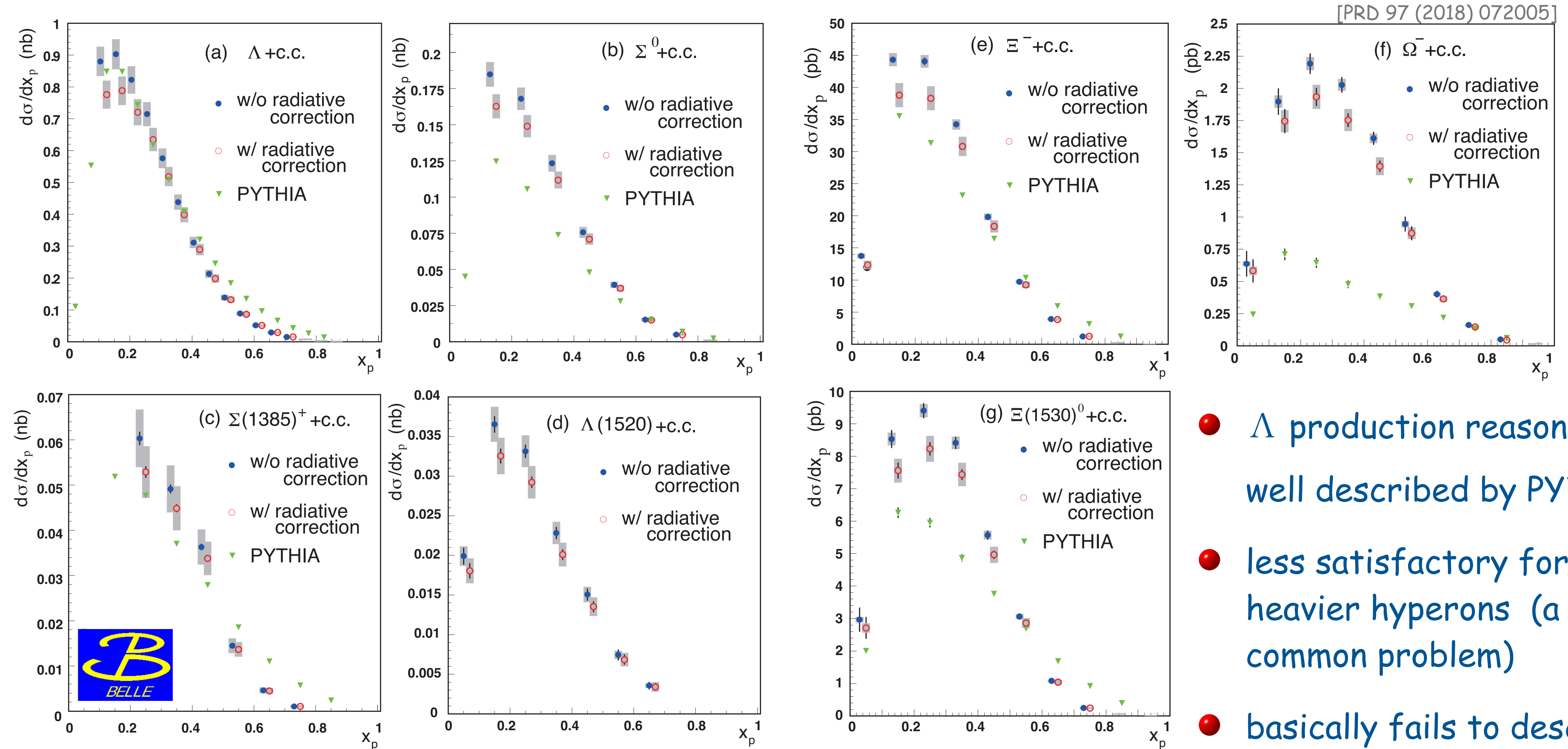


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# single-hadron production: hyperons



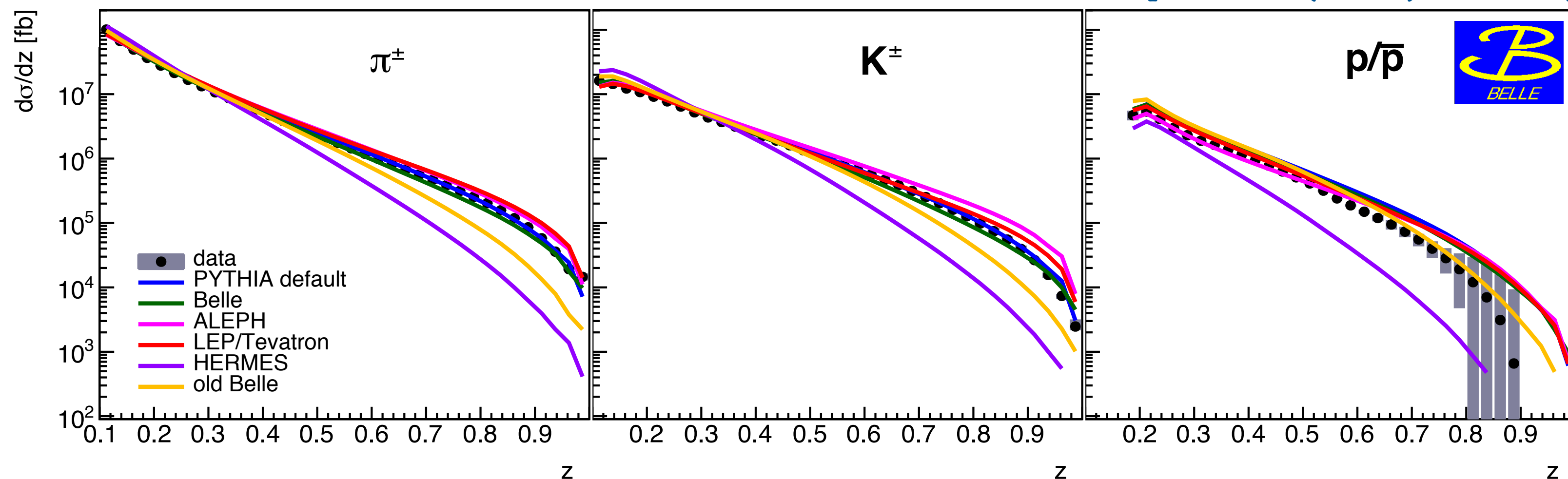
- $\Lambda$  production reasonably well described by PYTHIA
- less satisfactory for heavier hyperons (a quite common problem)
- basically fails to describe  $\Omega^-$  production



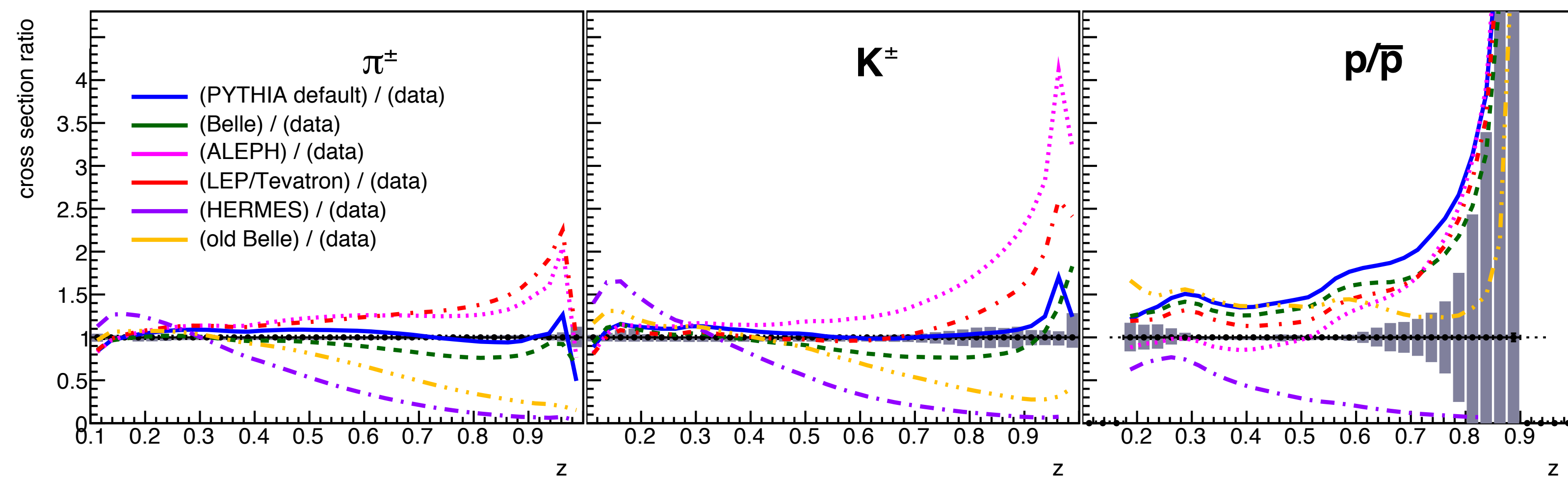
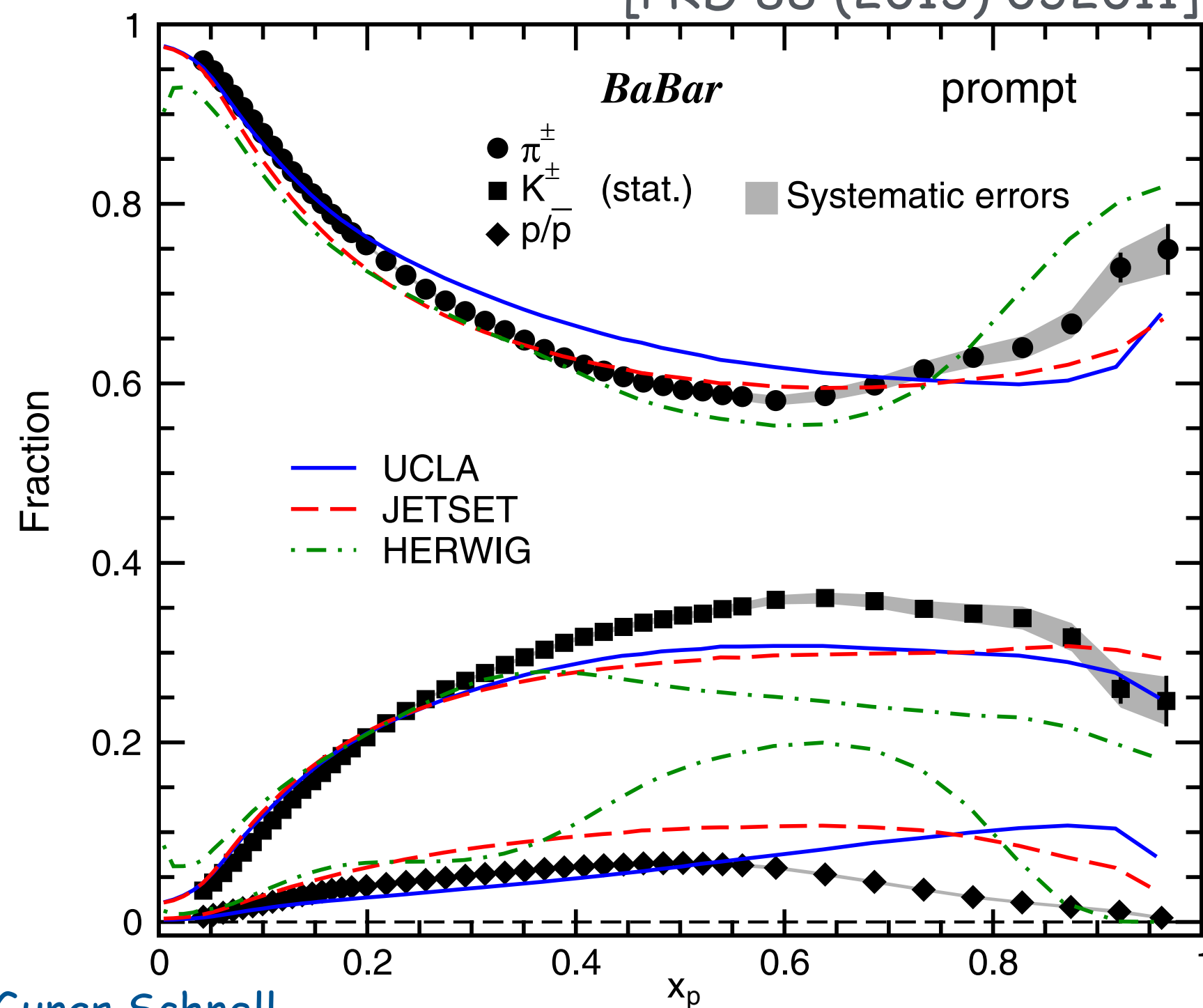
# single-hadron production: data-MC comparison

- pion and(?) kaon data reasonably well described by Jetset
- protons difficult to reproduce, especially at large  $z$
- MC overshoots data

[PRD 101 (2020) 092004]



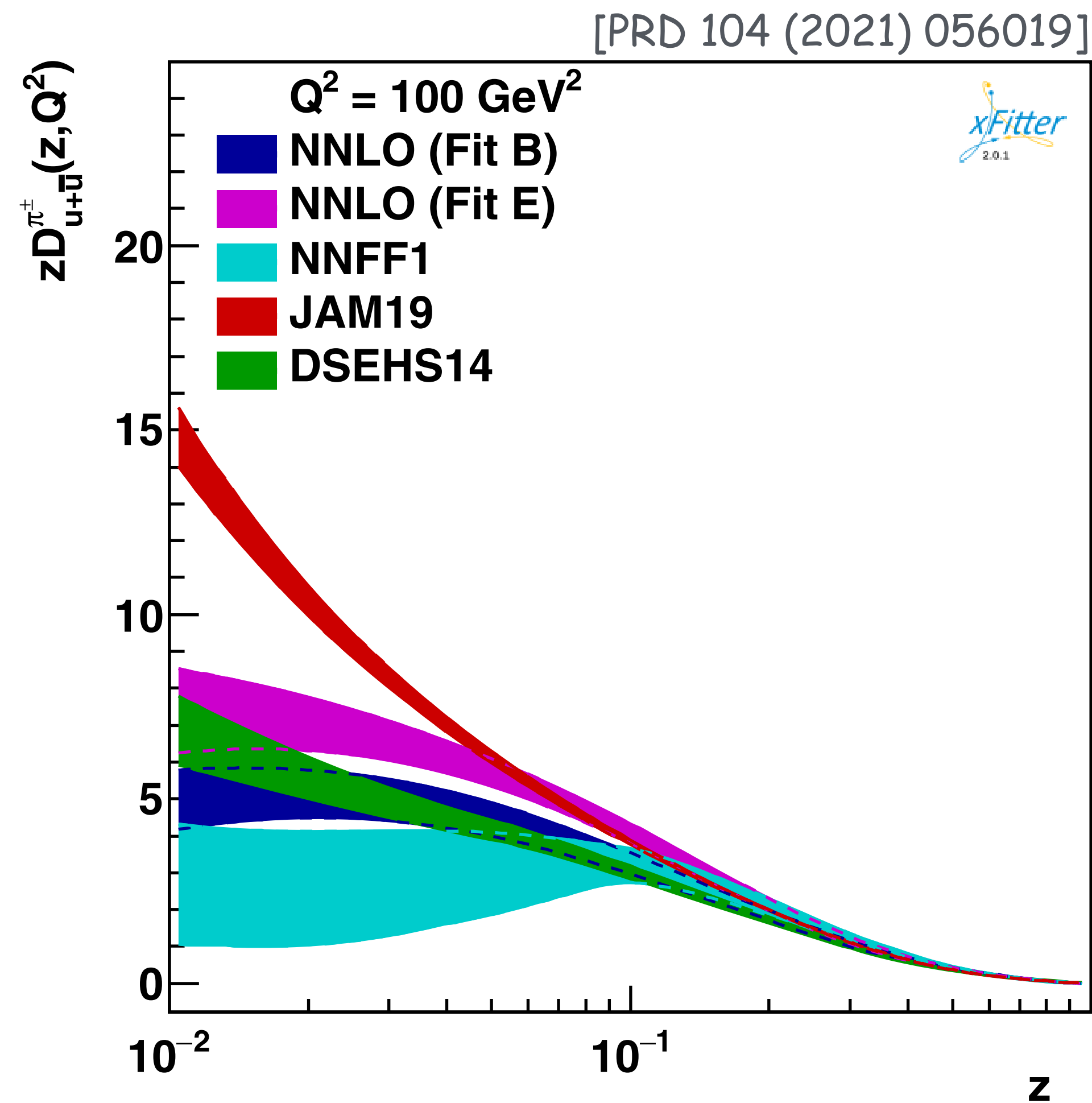
[PRD 88 (2013) 032011]



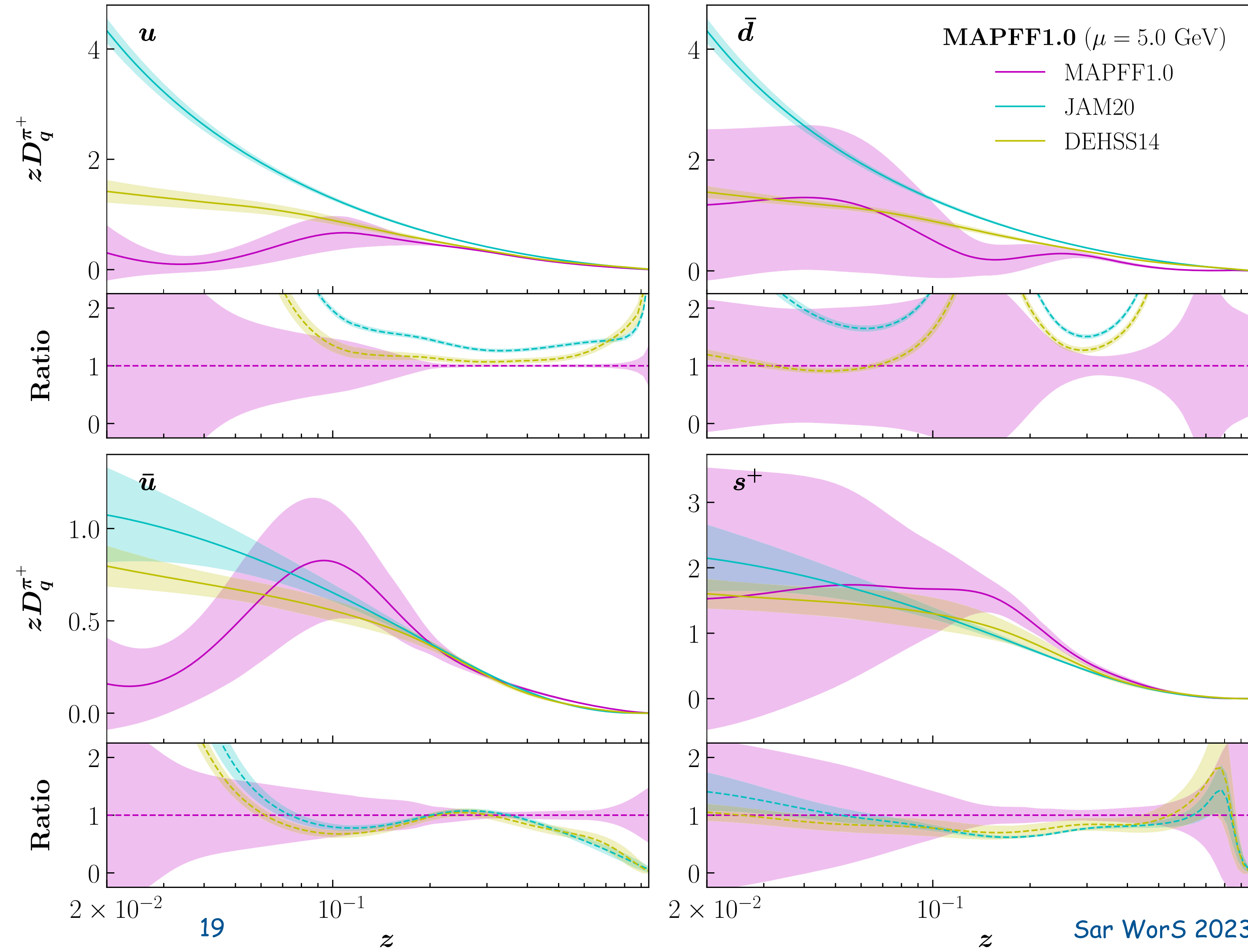
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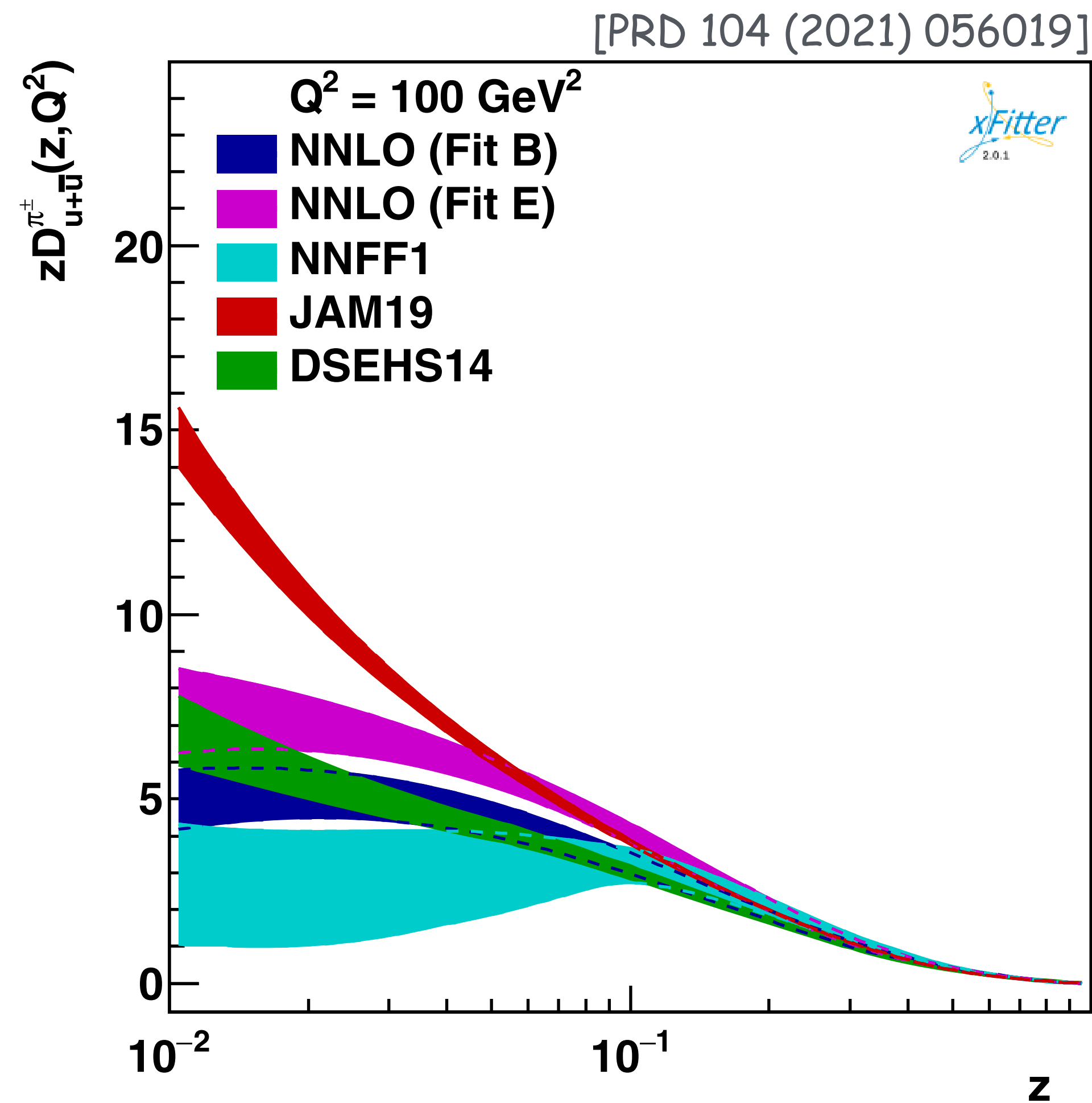


[PRD 104 (2021) 034007]



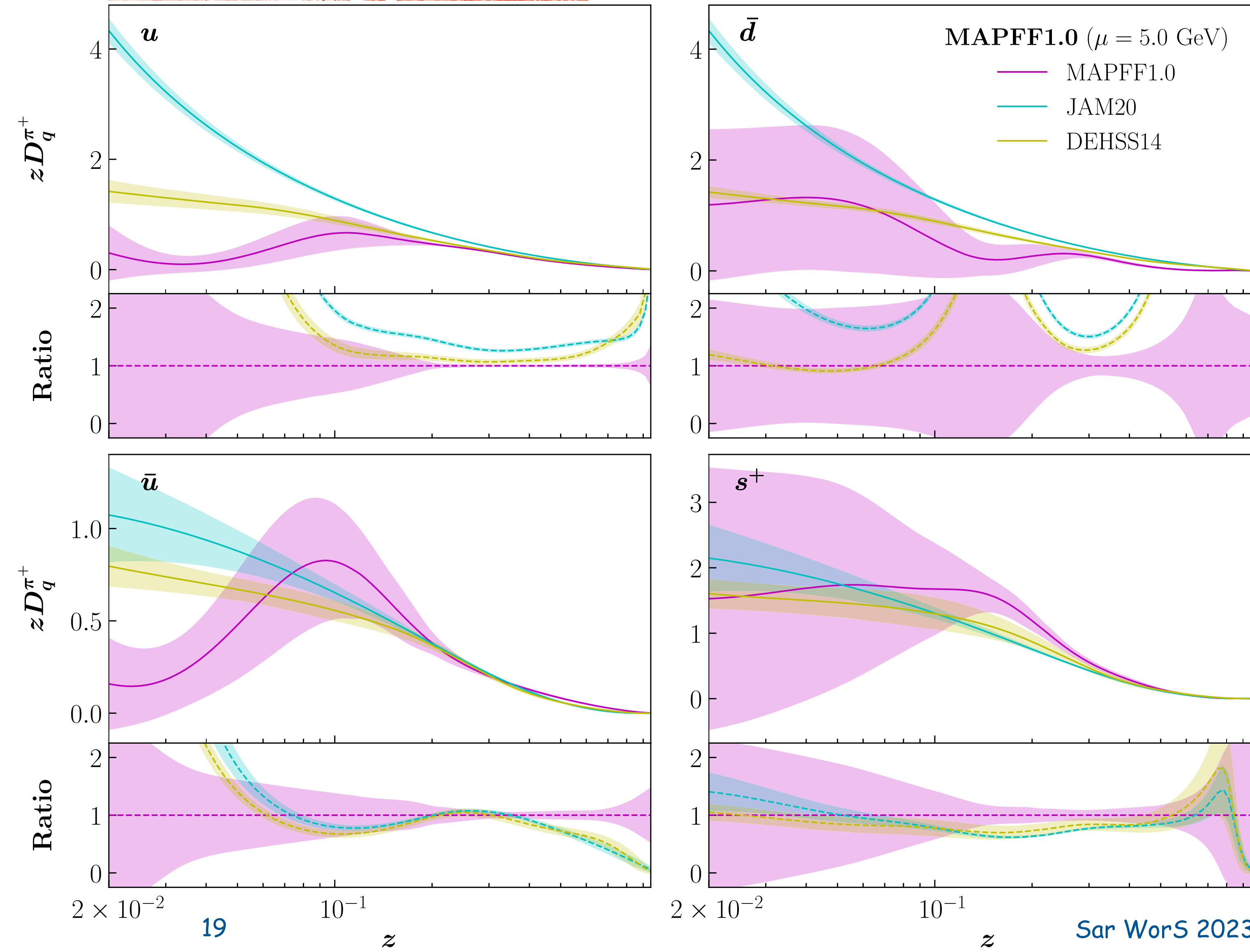
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👉 talk by Emanuele

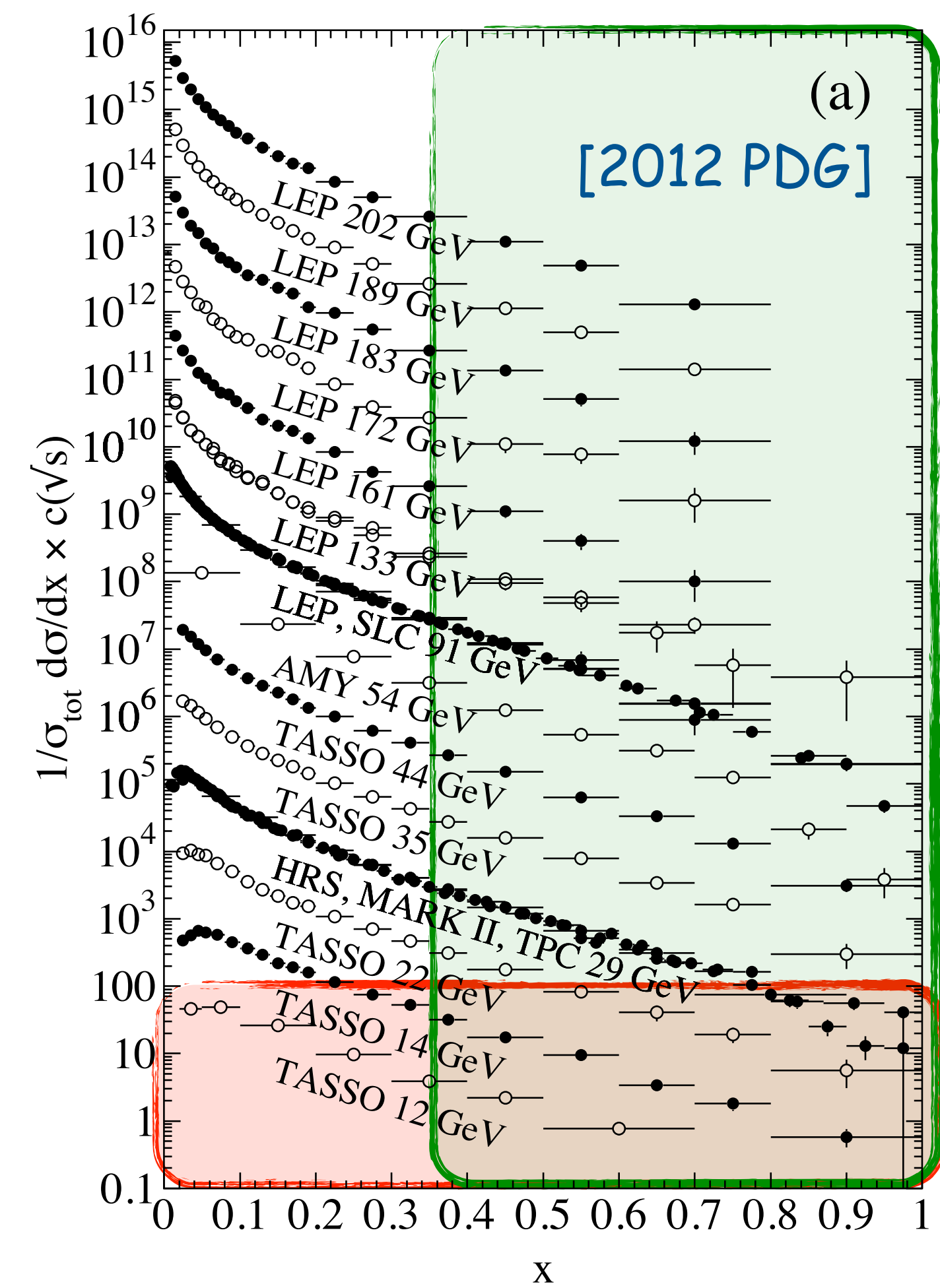
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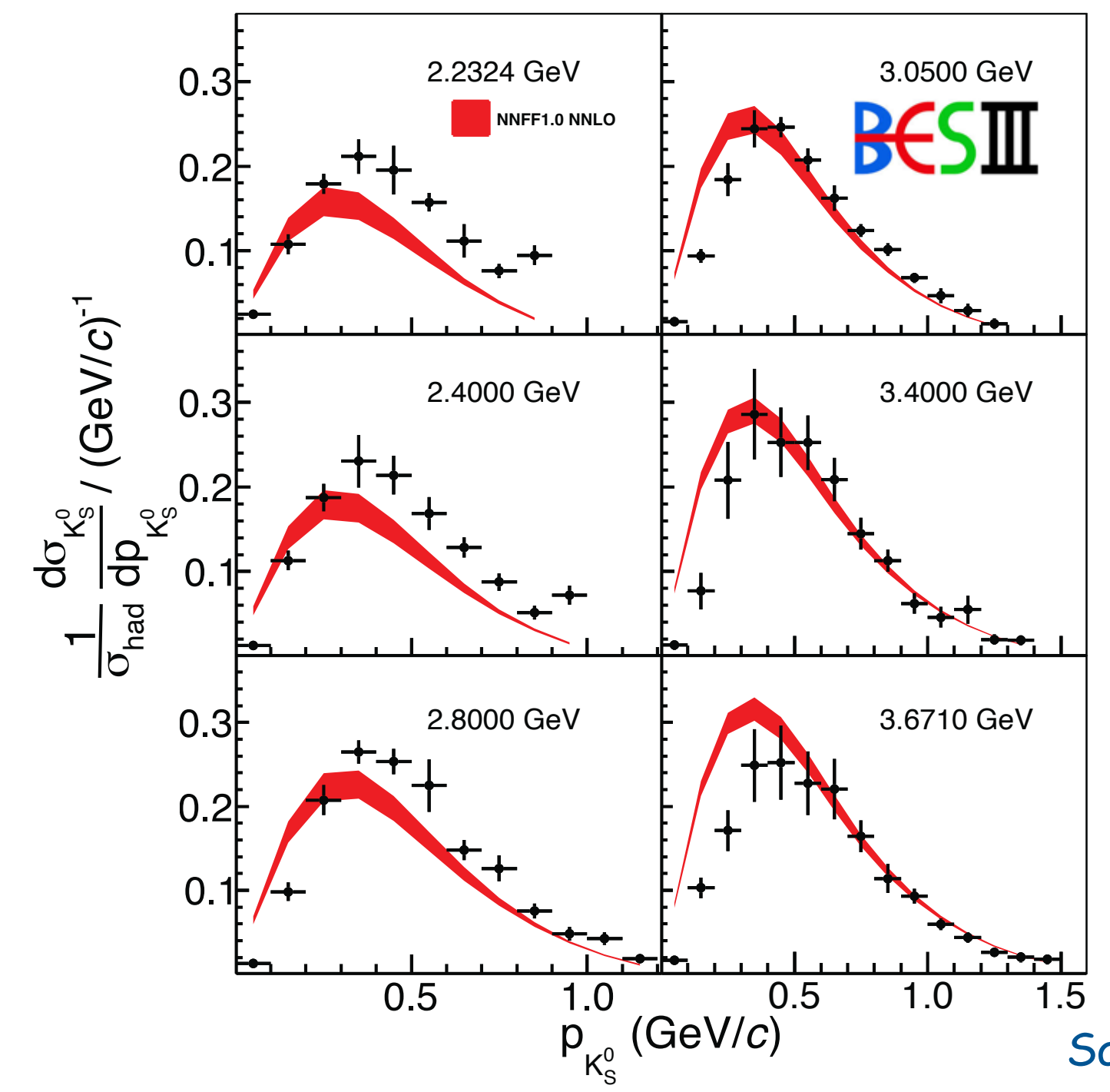
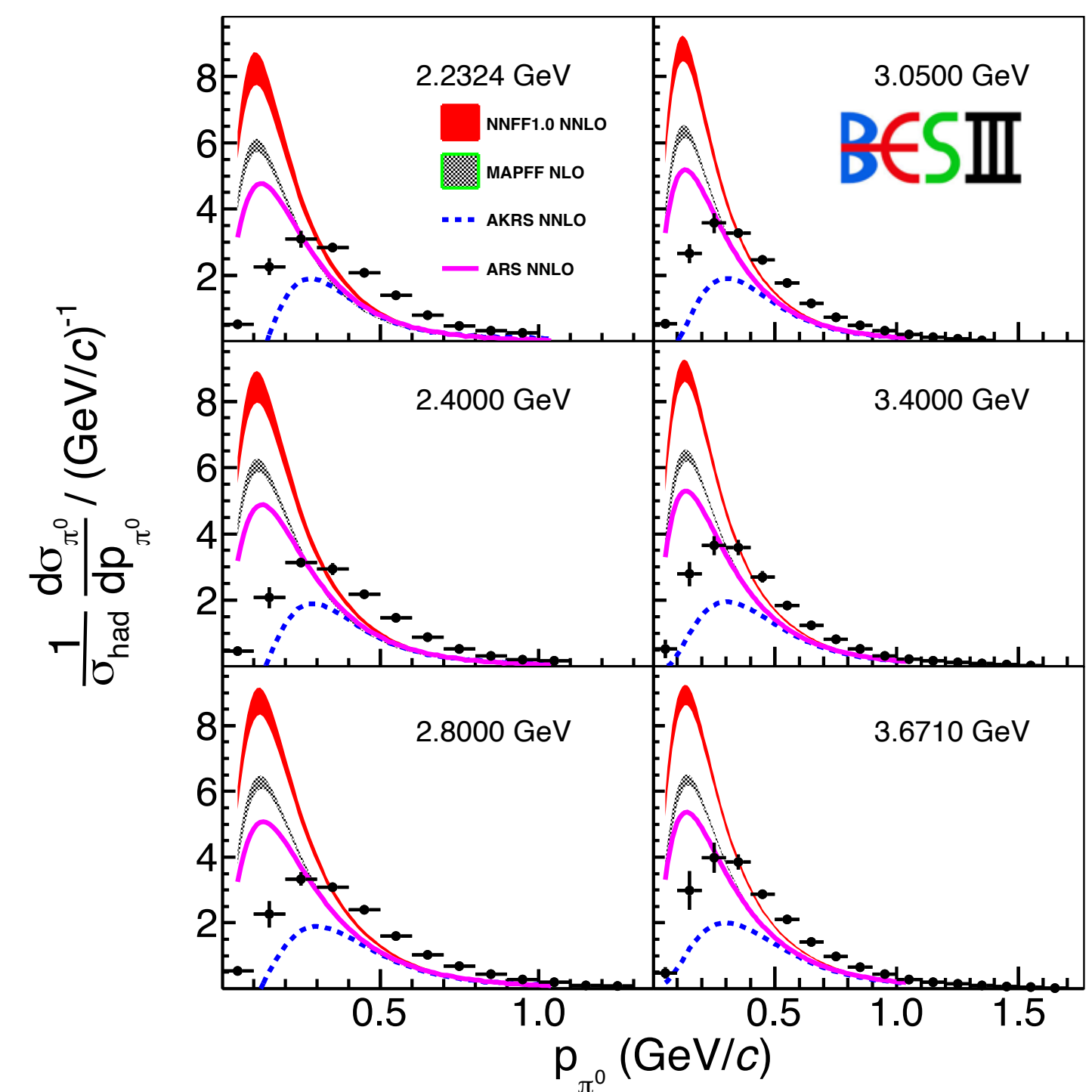
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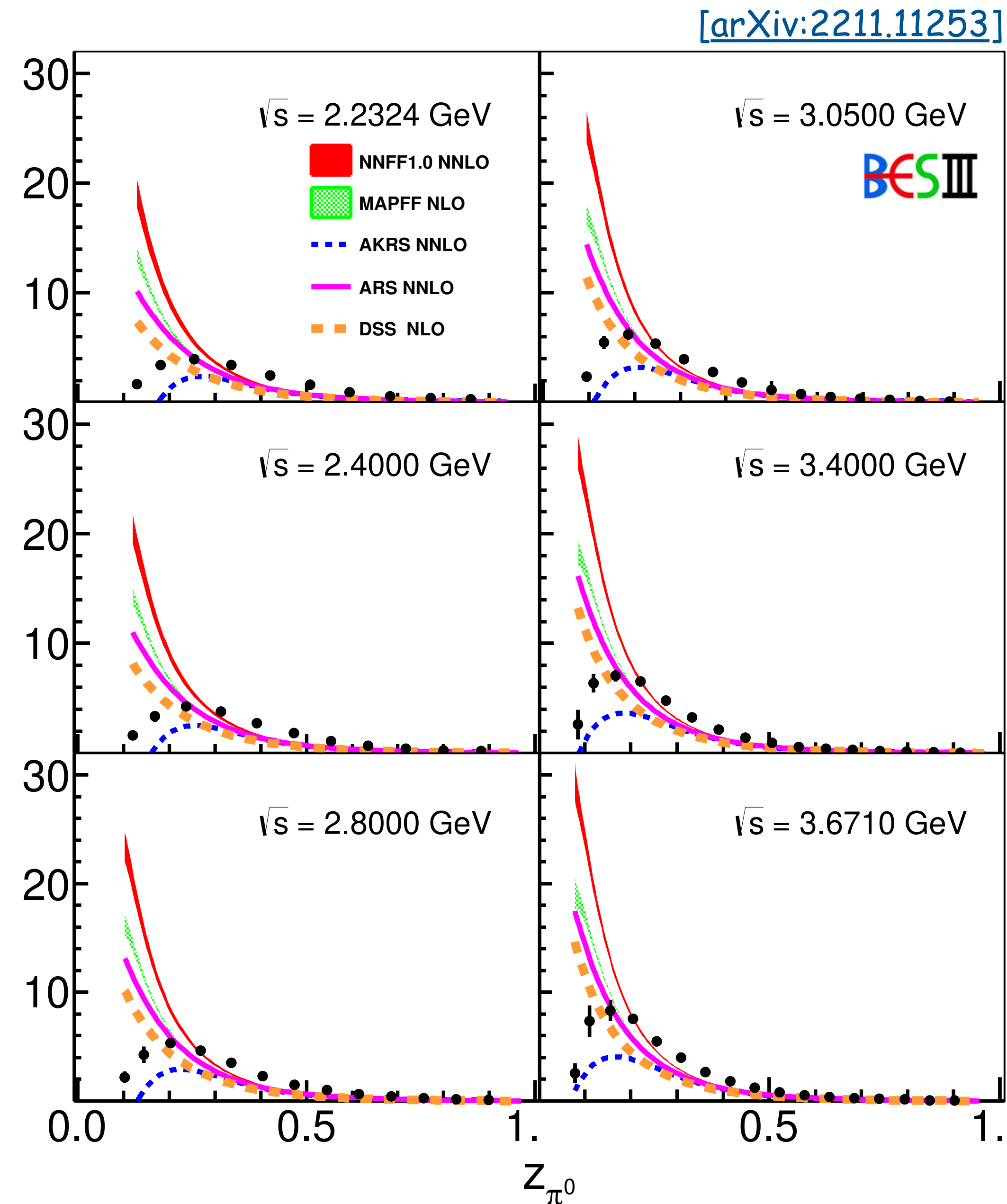
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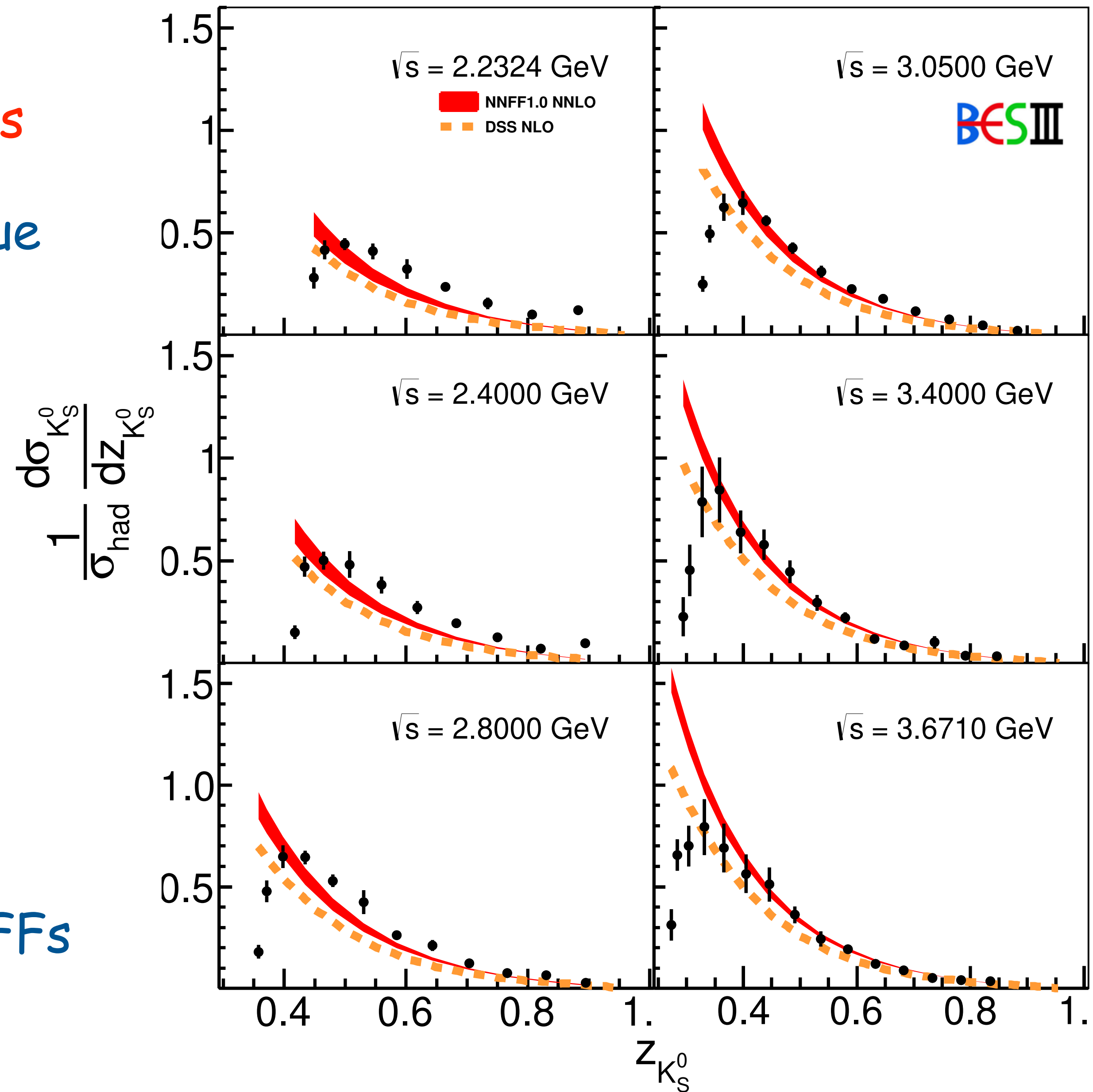
$$\frac{1}{\sigma_{\text{had}}} \frac{d\sigma_{\pi^0}}{dz_{\pi^0}}$$



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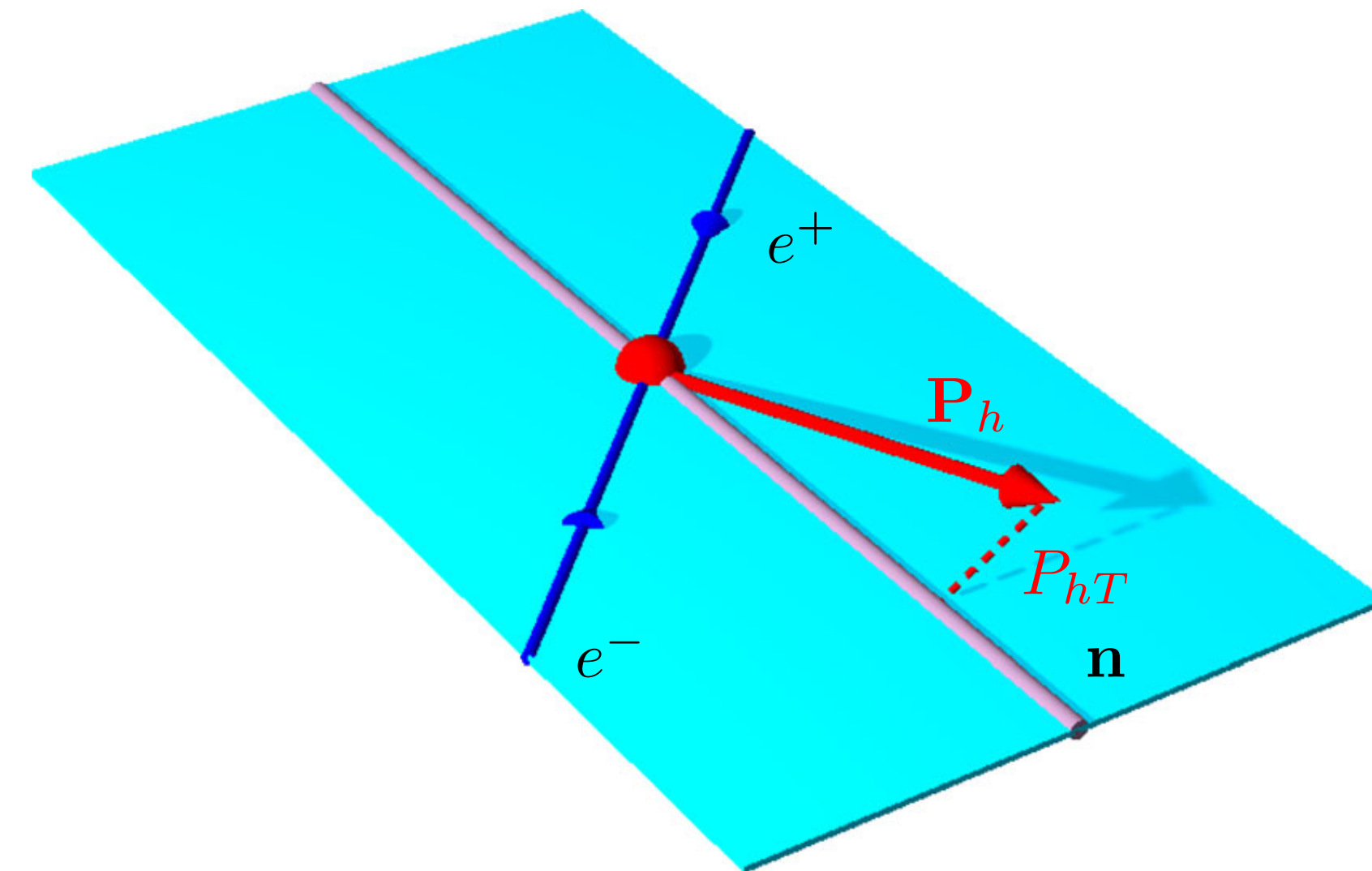
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- somewhat surprising for neutral pions as easily related to charge-pion FFs
- neutral-kaon FF relation to charged-kaon FFs more involved  
(here: simply charge average as for pions)



# inclusive hadrons - transverse momentum

- quasi-inclusive hadron production gives access to transverse momentum in fragmentation
- transverse momentum measured with respect to thrust axis  $\mathbf{n}$
- involves sum over all final-state particles in event
- event selection and hadron distributions dependent on thrust value  $T$  required
  - low thrust  $\rightarrow$  more spherical
  - high thrust  $\rightarrow$  highly collimated



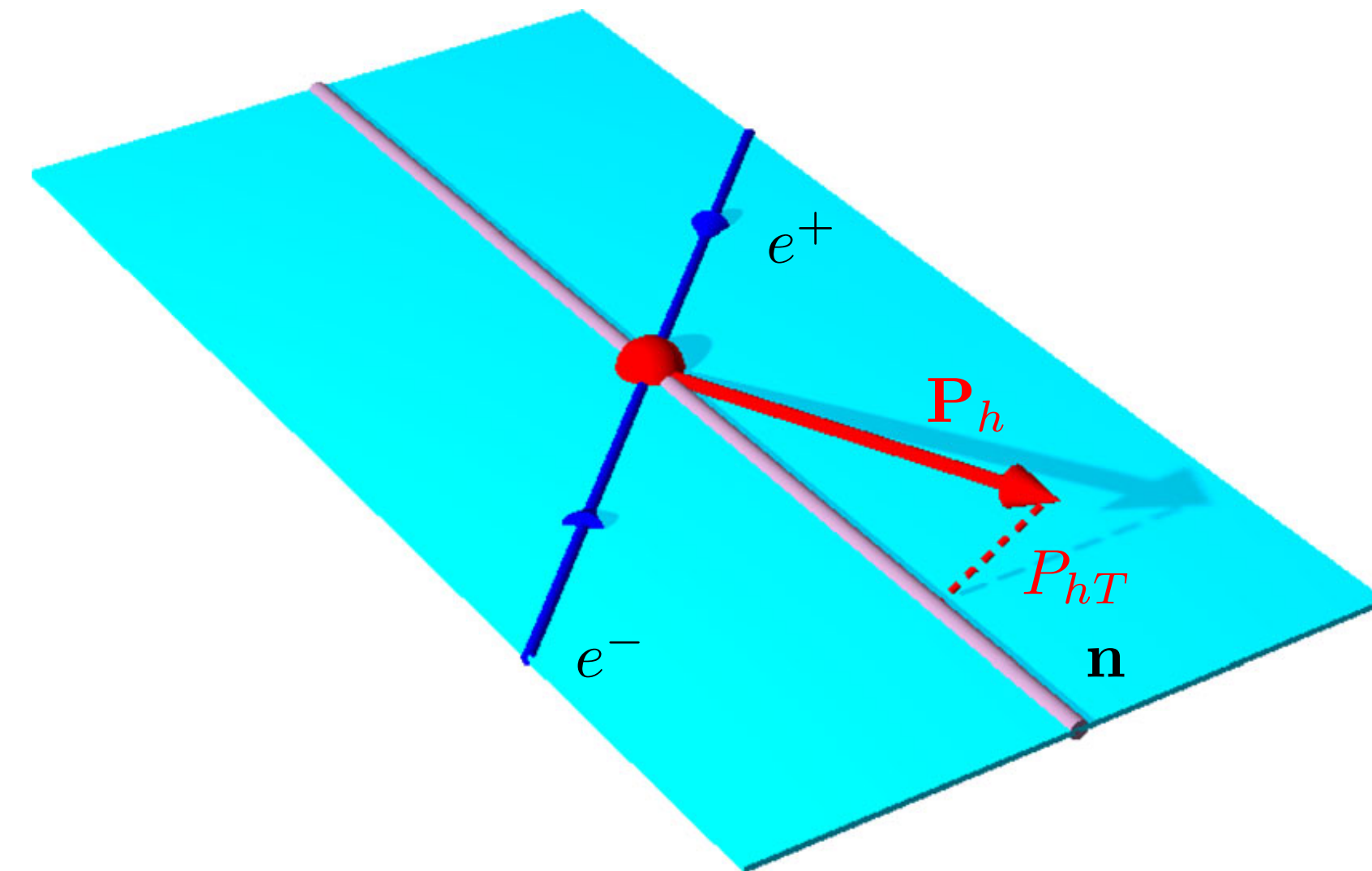
$$T \stackrel{\text{max}}{=} \frac{\sum_h |\mathbf{P}_h^{\text{CMS}} \cdot \hat{\mathbf{n}}|}{\sum_h |\mathbf{P}_h^{\text{CMS}}|}$$

👉 talks by Andrea & Mariaelena



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- transverse momentum measured with respect to thrust axis  $\mathbf{n}$
- analysis performed differential in  $z$  &  $P_{hT}$ , in various slices in thrust  $T$  ( $\Rightarrow$  18x20x6 bins)
- correction steps similar as for  $P_{hT}$ -integrated cross sections
- Gaussian fits to transverse-momentum distribution provided for all hadrons in  $(z, T)$ -bins

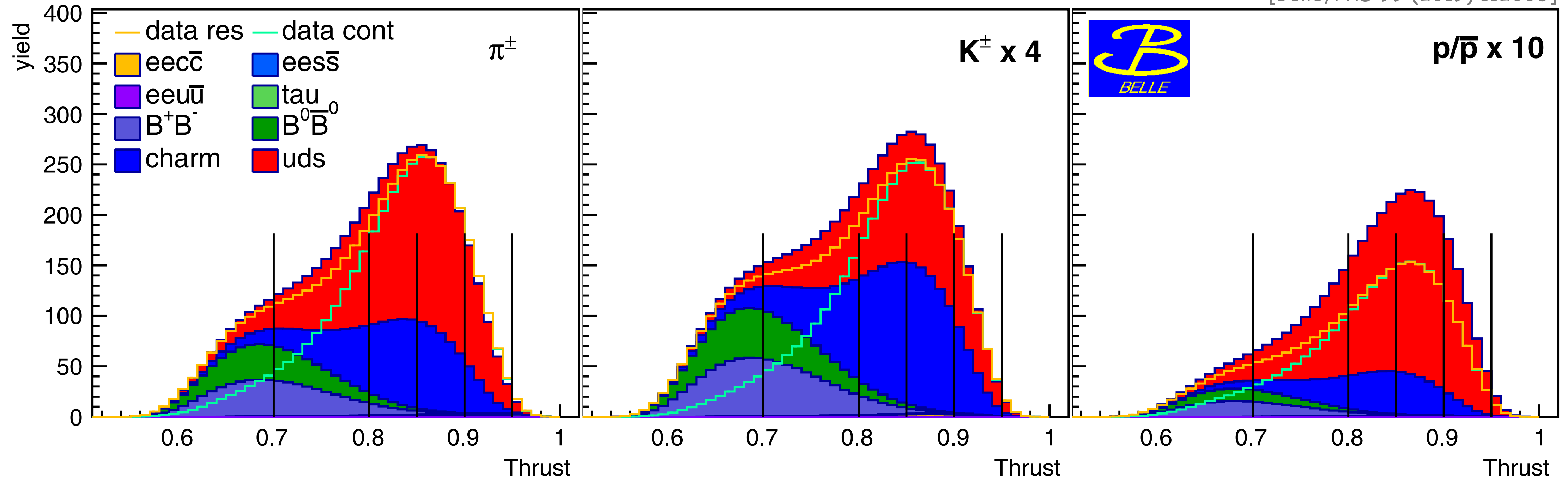


$$T \stackrel{\text{max}}{=} \frac{\sum_h |\mathbf{P}_h^{\text{CMS}} \cdot \hat{\mathbf{n}}|}{\sum_h |\mathbf{P}_h^{\text{CMS}}|}$$



# thrust distribution: process contributions

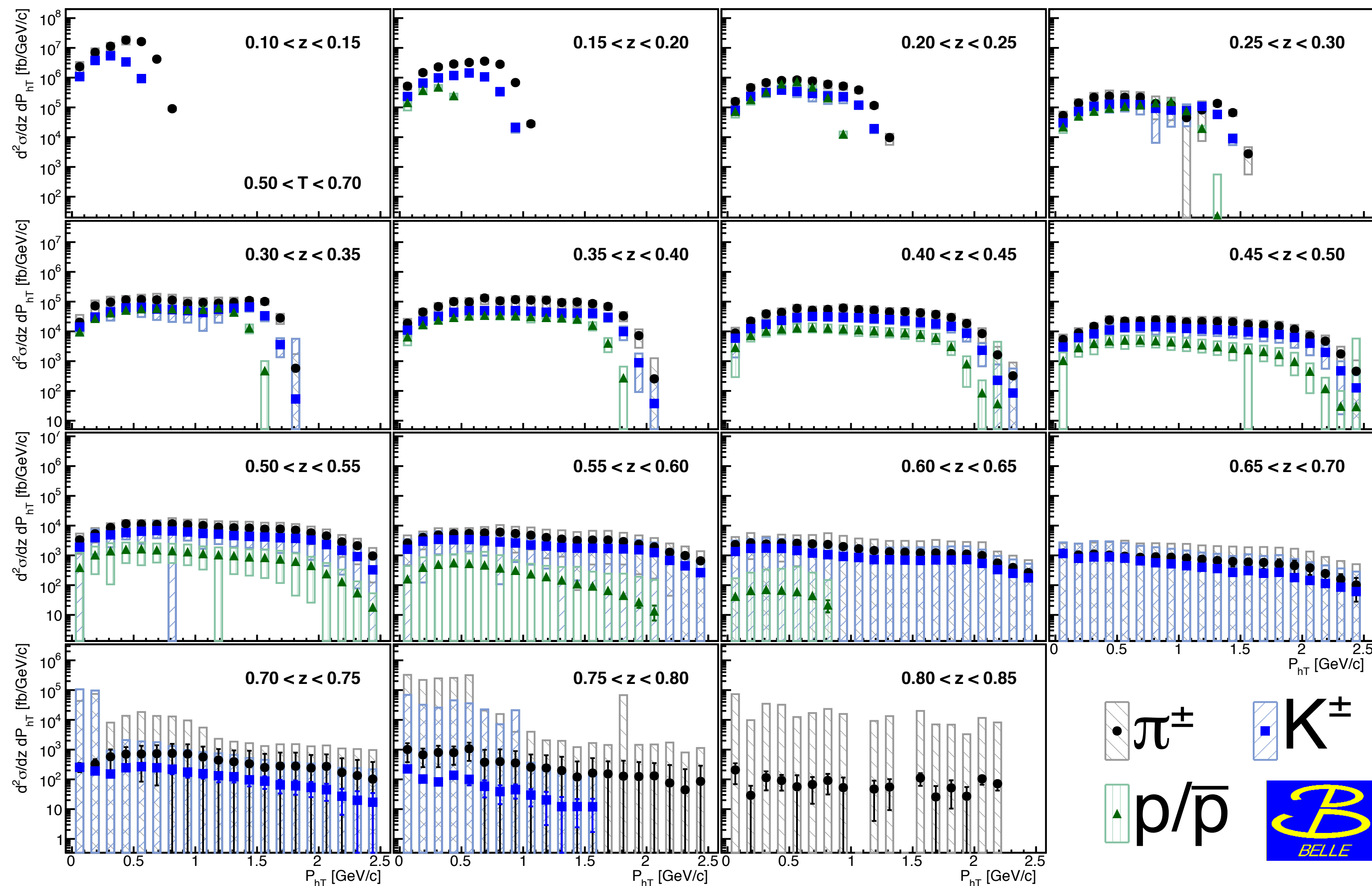
[Belle, PRD 99 (2019) 112006]



- large contribution from BB at lower thrust
- large thrust dominated by uds and charm fragmentation  
(at very large  $T$  significant  $\tau$  contribution for pions, not visible here)
- will concentrate mainly on  $0.85 < T < 0.9$  bin, though others available as well

# transverse-momentum distributions

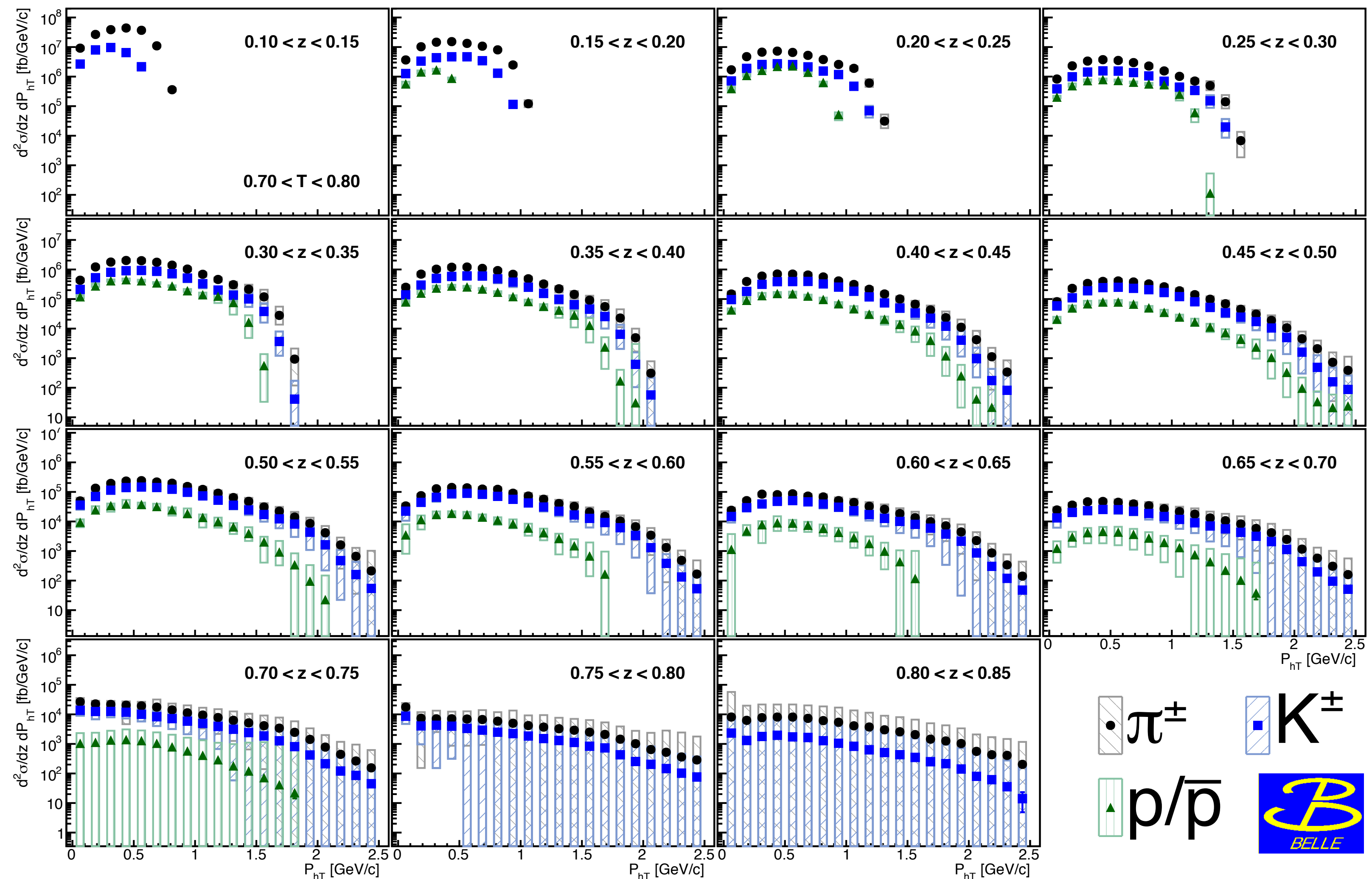
- lowest T bin -> rather spherical events
- transverse momenta almost uniformly distributed in medium-z bins
- faster drop for heavier hadrons



[PRD 99 (2019) 112006]

# transverse-momentum distributions

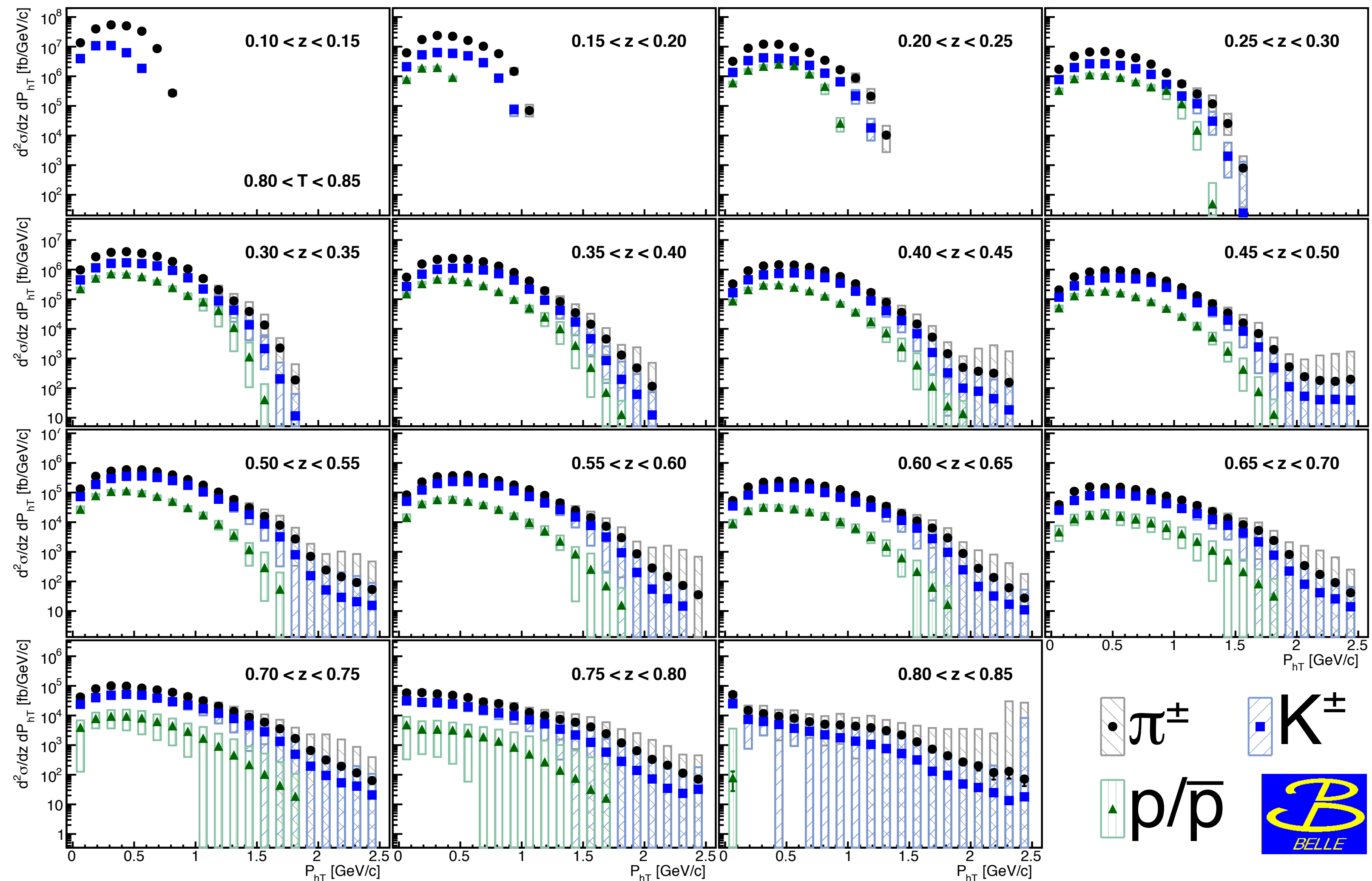
- $0.7 < T < 0.8$  -> particles already more collimated
- transverse momenta more Gaussian distributed
- large- $z$  region with large uncertainties



[PRD 99 (2019) 112006]

# transverse-momentum distributions

- $0.8 < T < 0.85$
- transverse momenta mostly Gaussian distributed
- possible deviations for large- $P_{hT}$  tails [but also larger uncertainties]

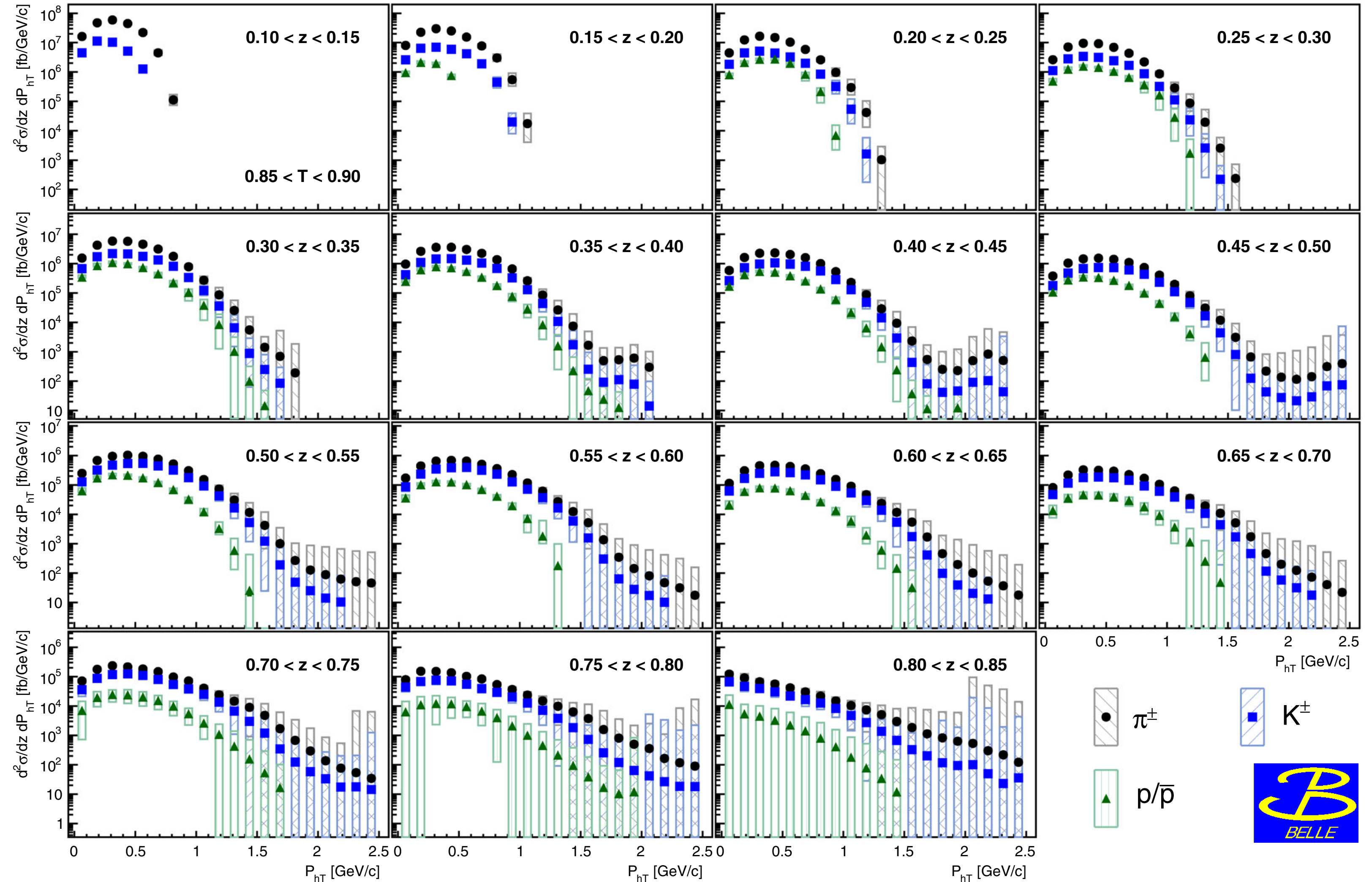


[PRD 99 (2019) 112006]



# transverse-momentum distributions

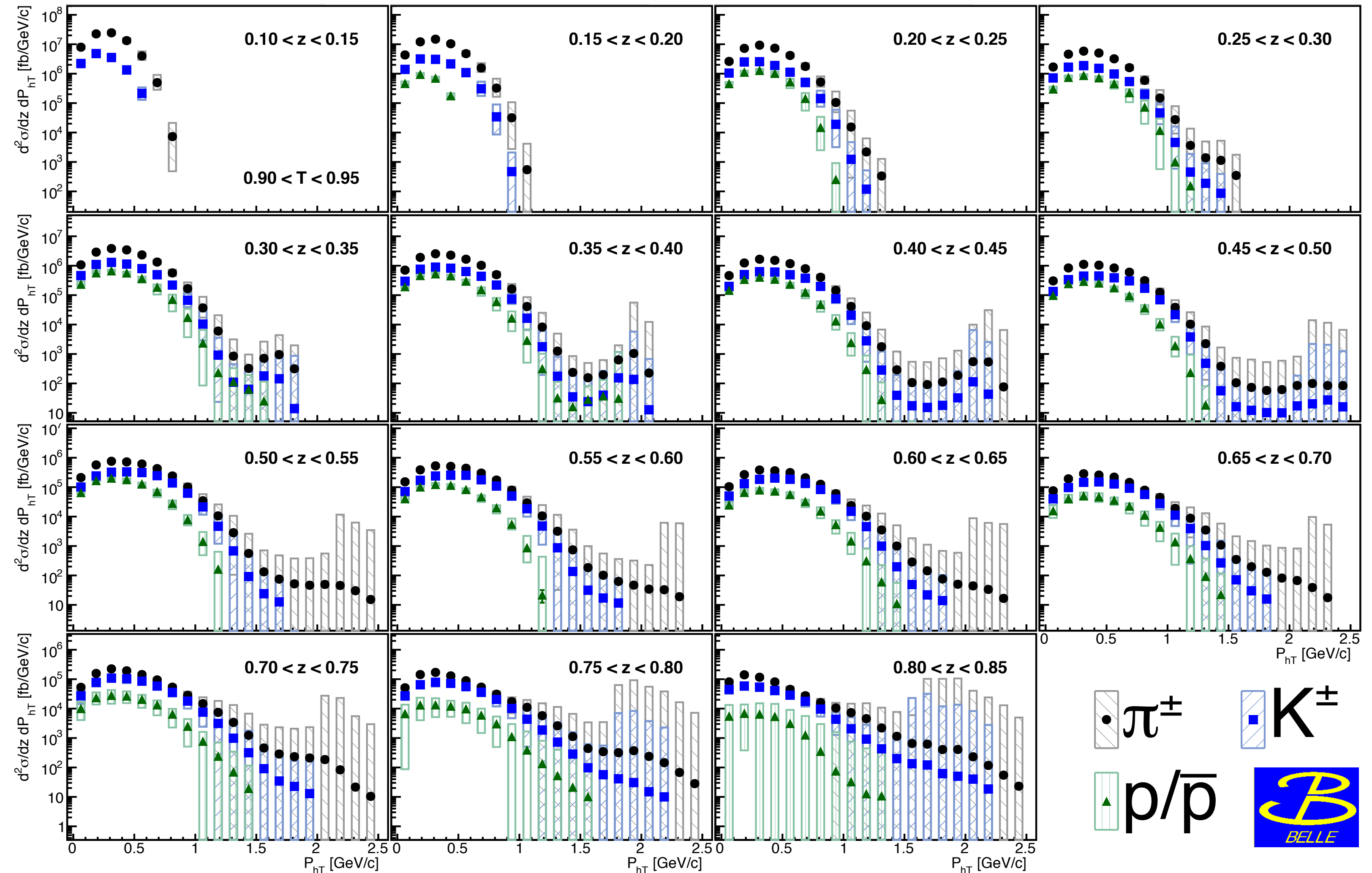
- $0.85 < T < 0.9$
- transverse momenta mostly Gaussian distributed; widths narrowing
- possible deviations for large- $P_{hT}$  tails [but also larger uncertainties]



[PRD 99 (2019) 112006]

# transverse-momentum distributions

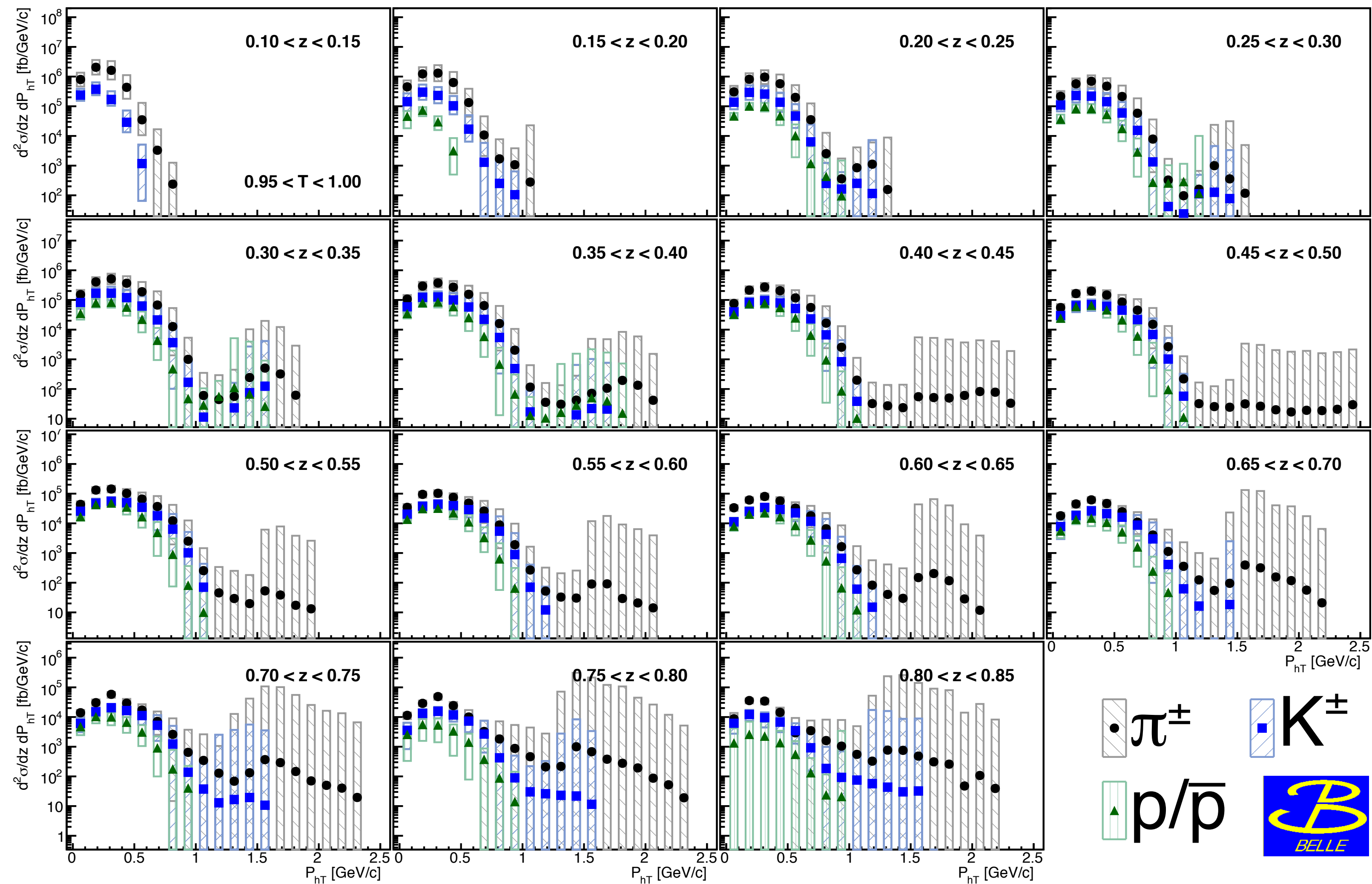
- $0.9 < T < 0.95$
- transverse momenta mostly Gaussian distributed; widths even narrower
- possible deviations for large- $P_{hT}$  tails [but also larger uncertainties]





# transverse-momentum distributions

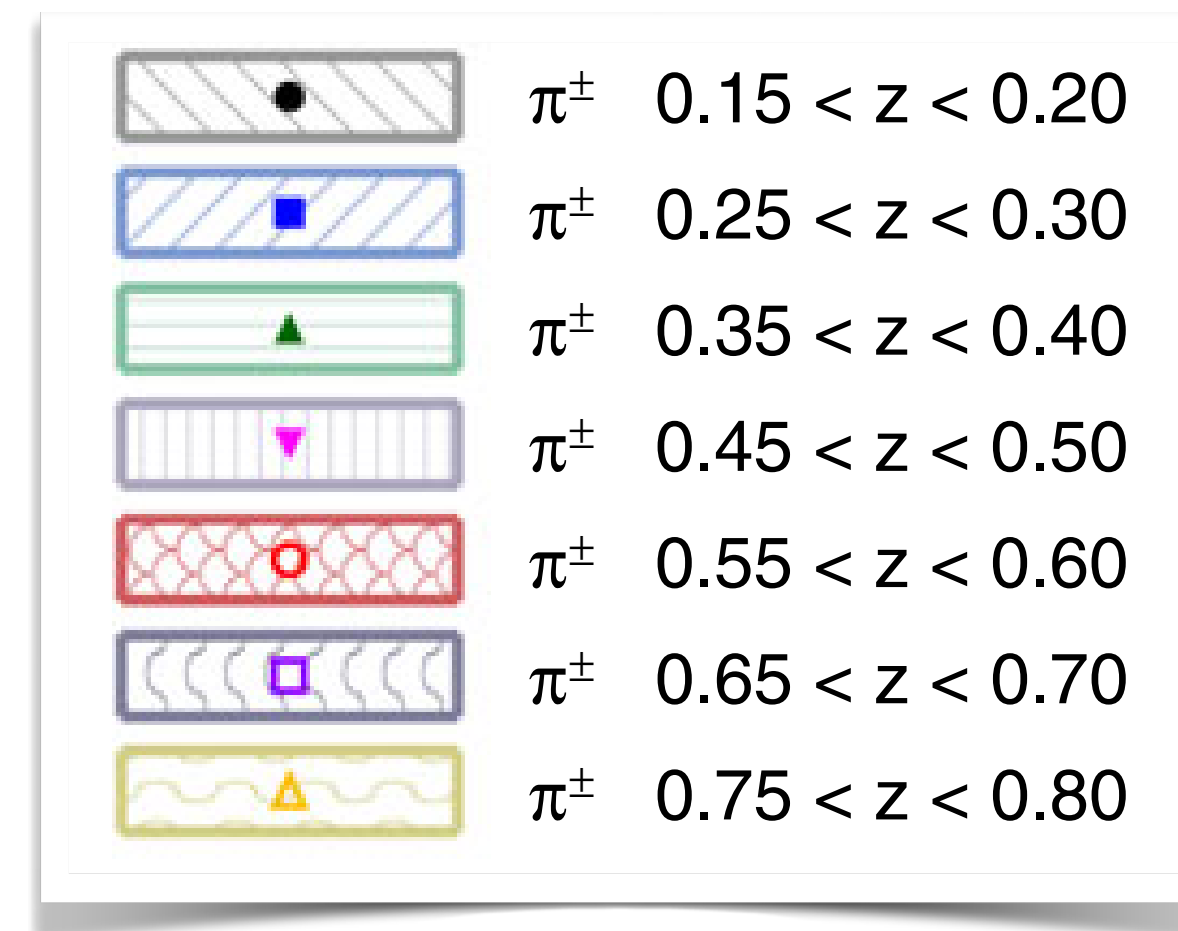
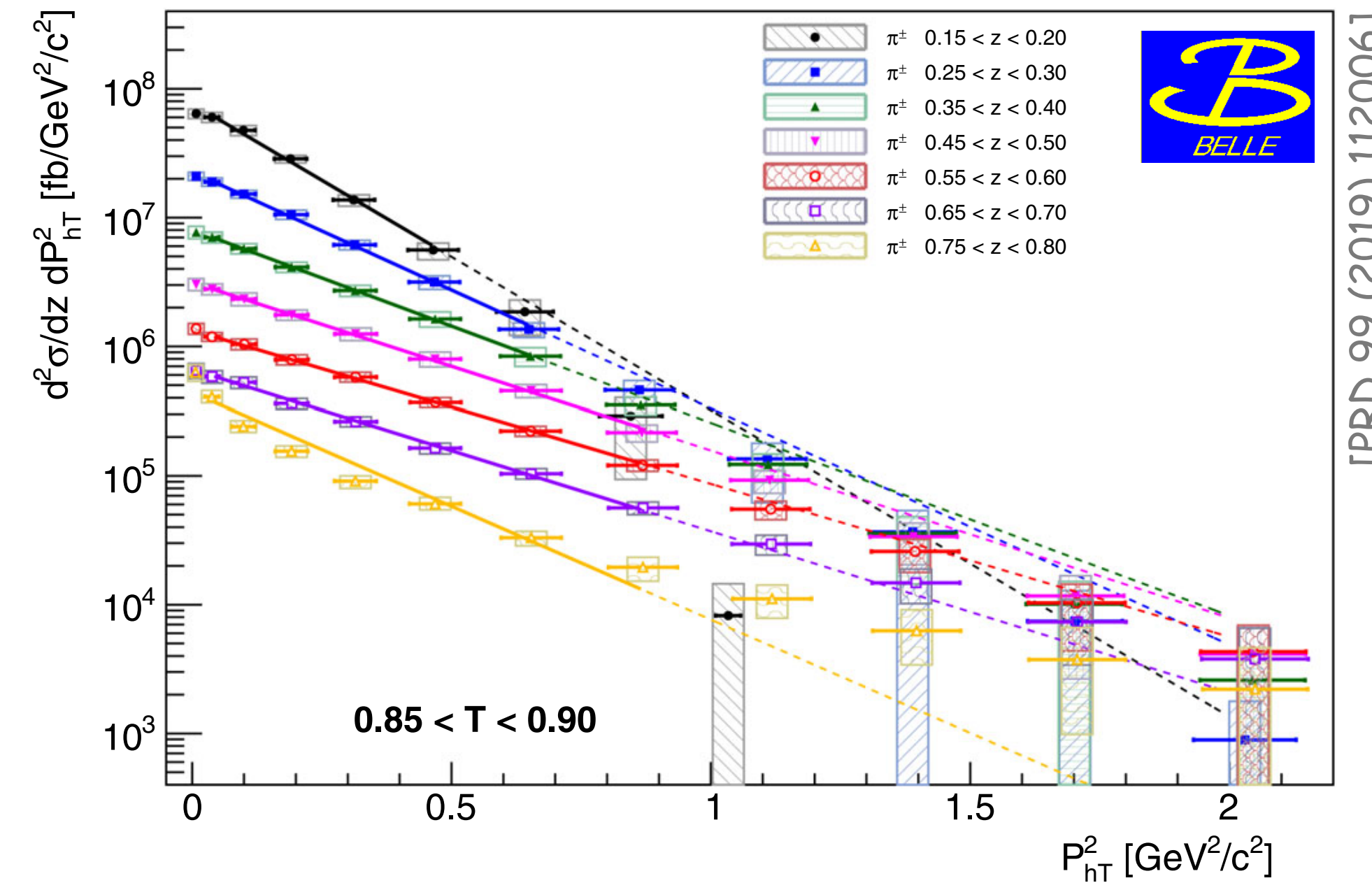
- $0.95 < T < 1.0$
- transverse momenta mostly Gaussian distributed
- widths very narrow as particles now very collimated



[PRD 99 (2019) 112006]

# transverse-momentum: Gaussian widths

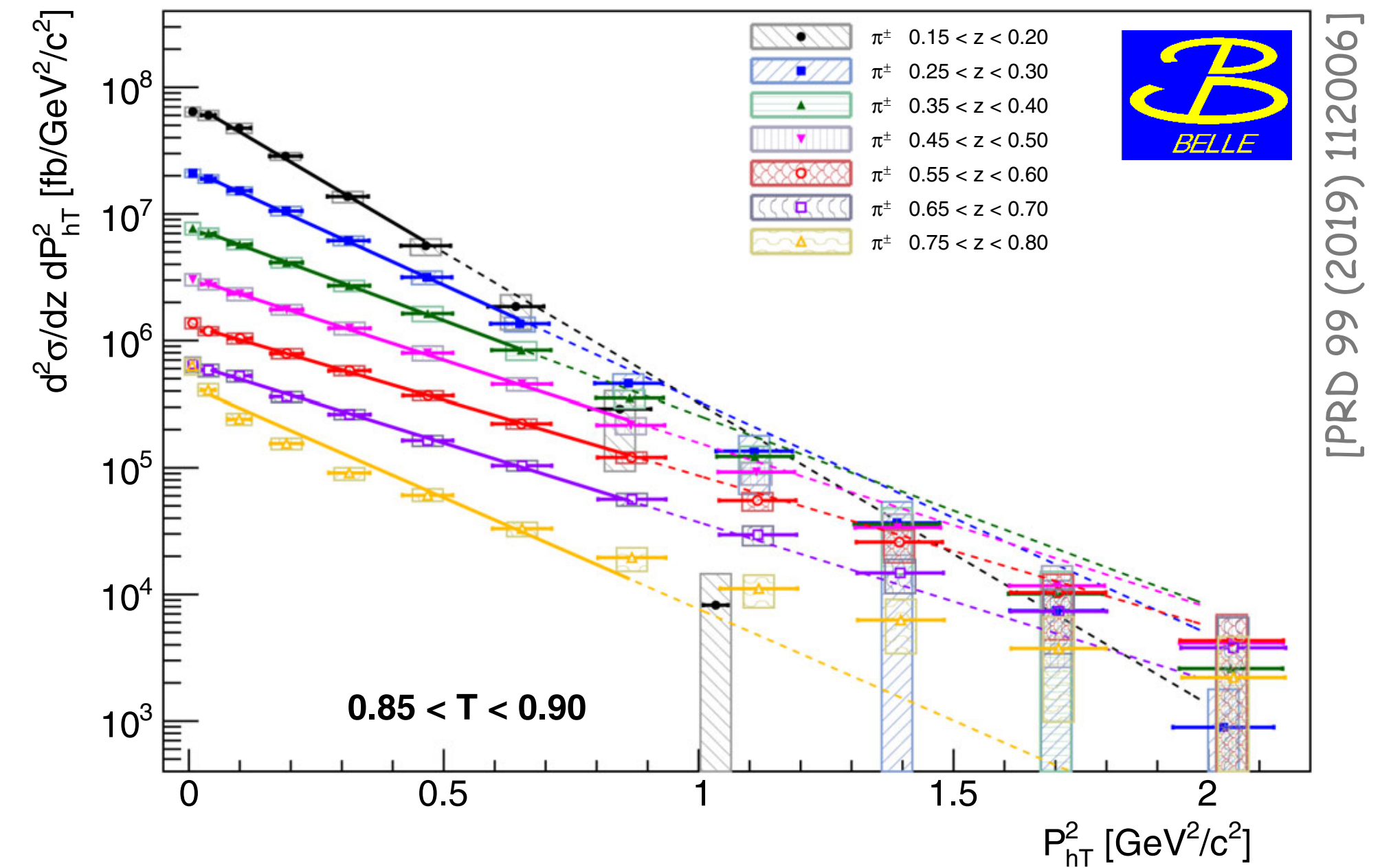
- $0.85 < T < 0.90$
- fit Gauss to low- $P_{hT}$  data
- mostly well described with possible exception at high  $z$
- deviation from Gauss at large  $P_{hT}$
- clear increase of width with  $z$  for low values of  $z$



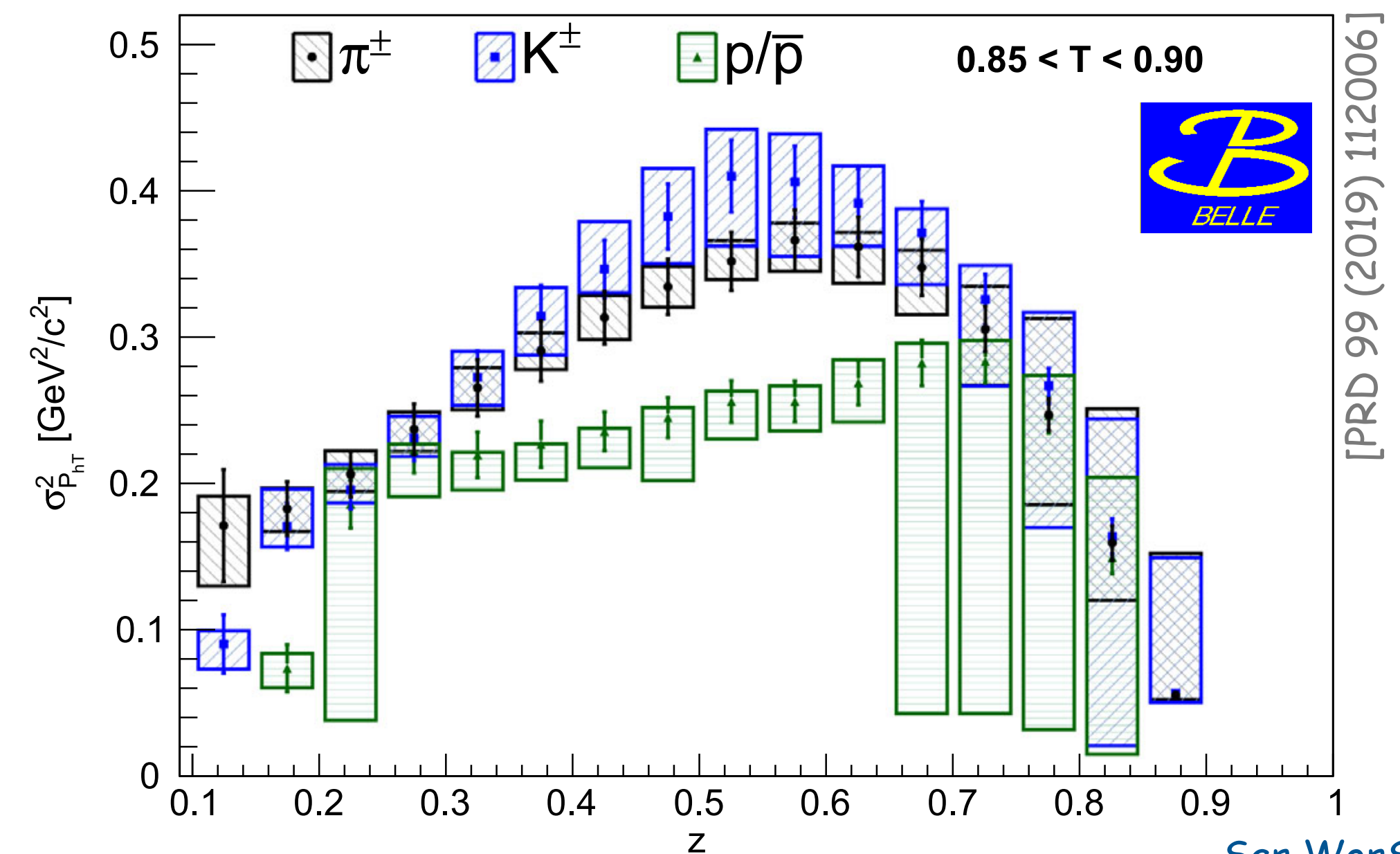


# transverse-momentum: Gaussian widths

- $0.85 < T < 0.90$ 
  - fit Gauss to low- $P_{hT}$  data
  - mostly well described with possible exception at high  $z$
  - deviation from Gauss at large  $P_{hT}$
  - clear increase of width with  $z$  for low values of  $z$
- Gaussian widths as function of  $z$ 
  - general increase with  $z$  with turnover at larger values of  $z$  for mesons
  - protons with smaller width and a more linear rise with  $z$



[PRD 99 (2019) 112006]

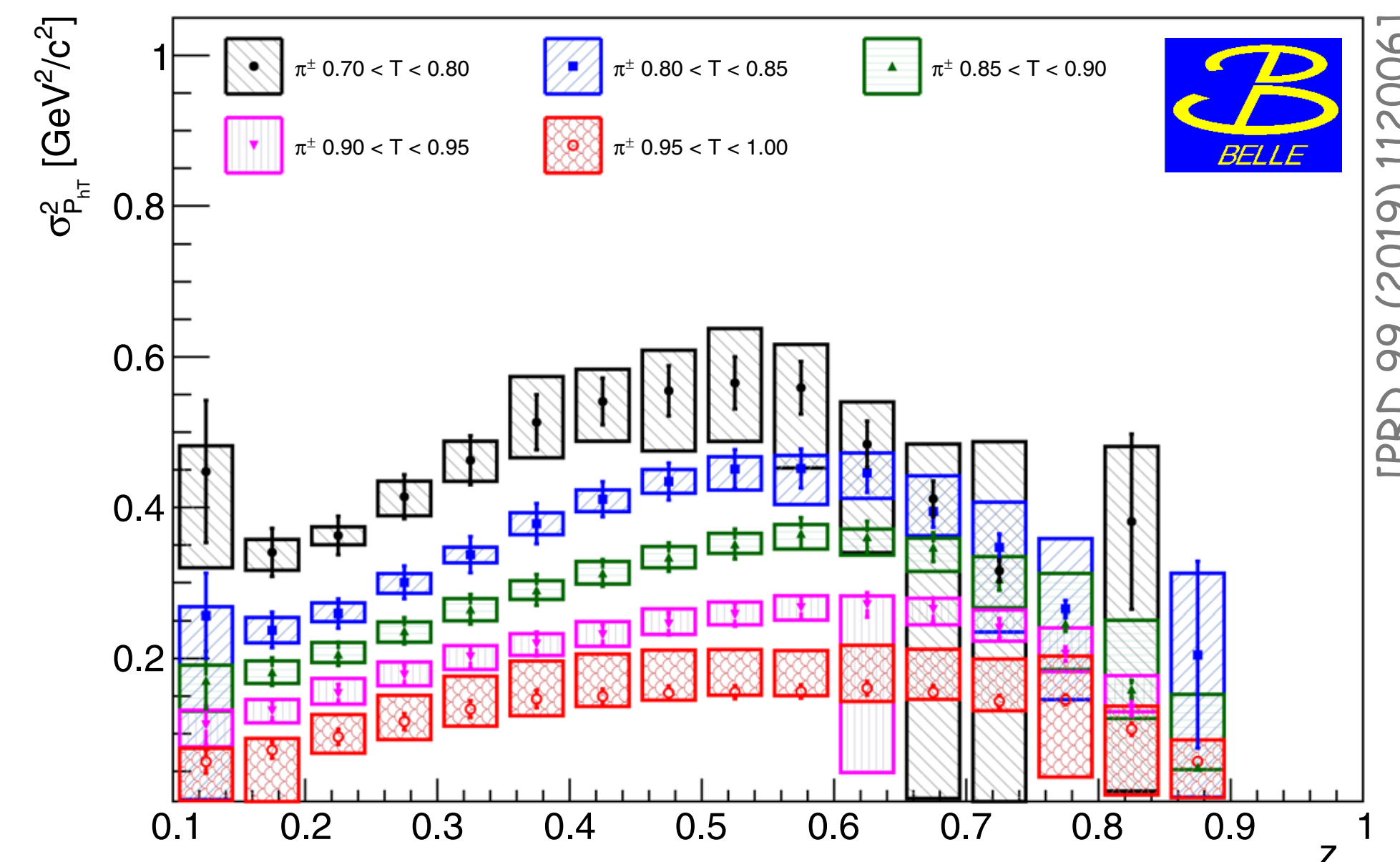
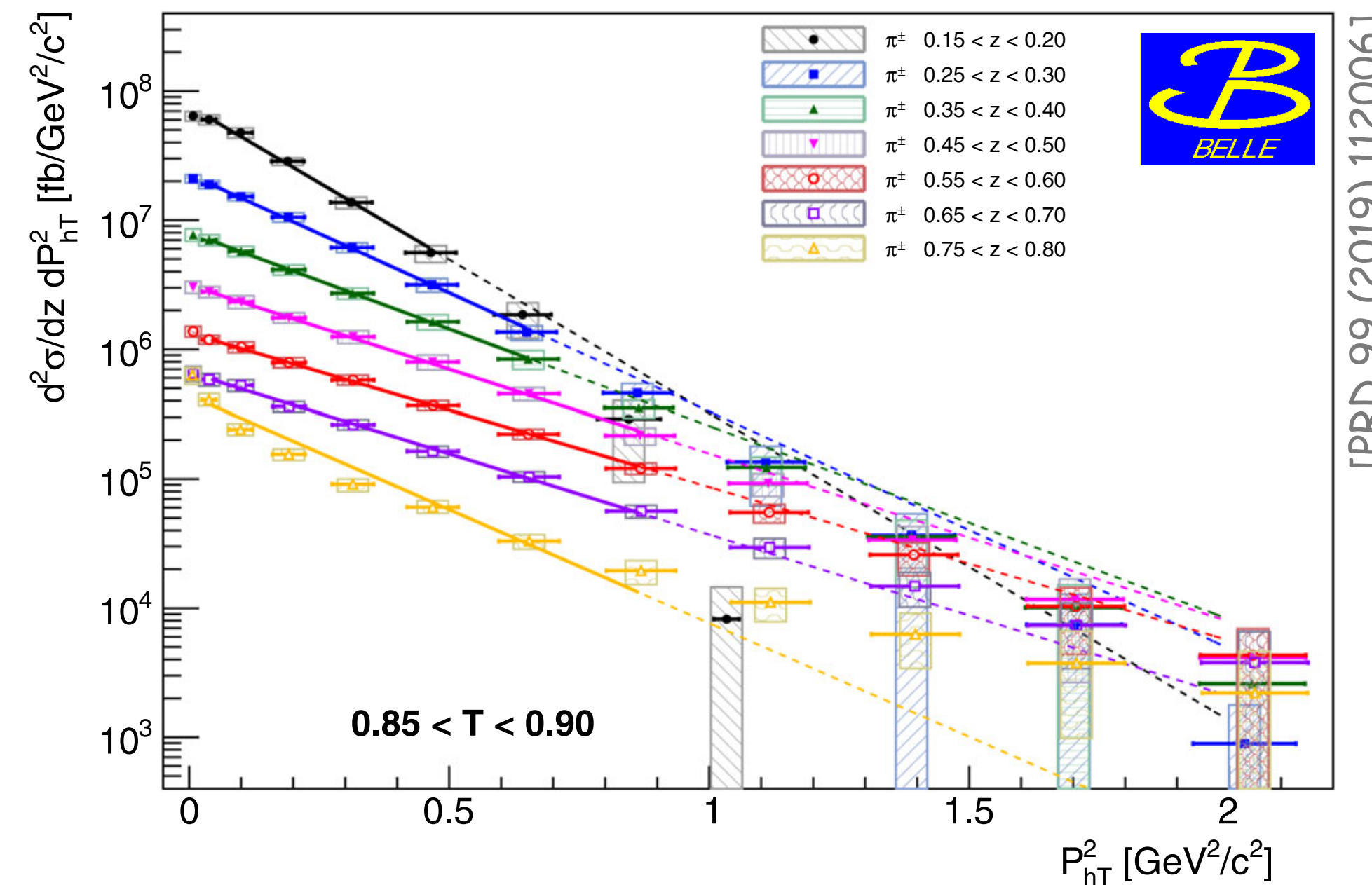


[PRD 99 (2019) 112006]



# transverse-momentum: Gaussian widths

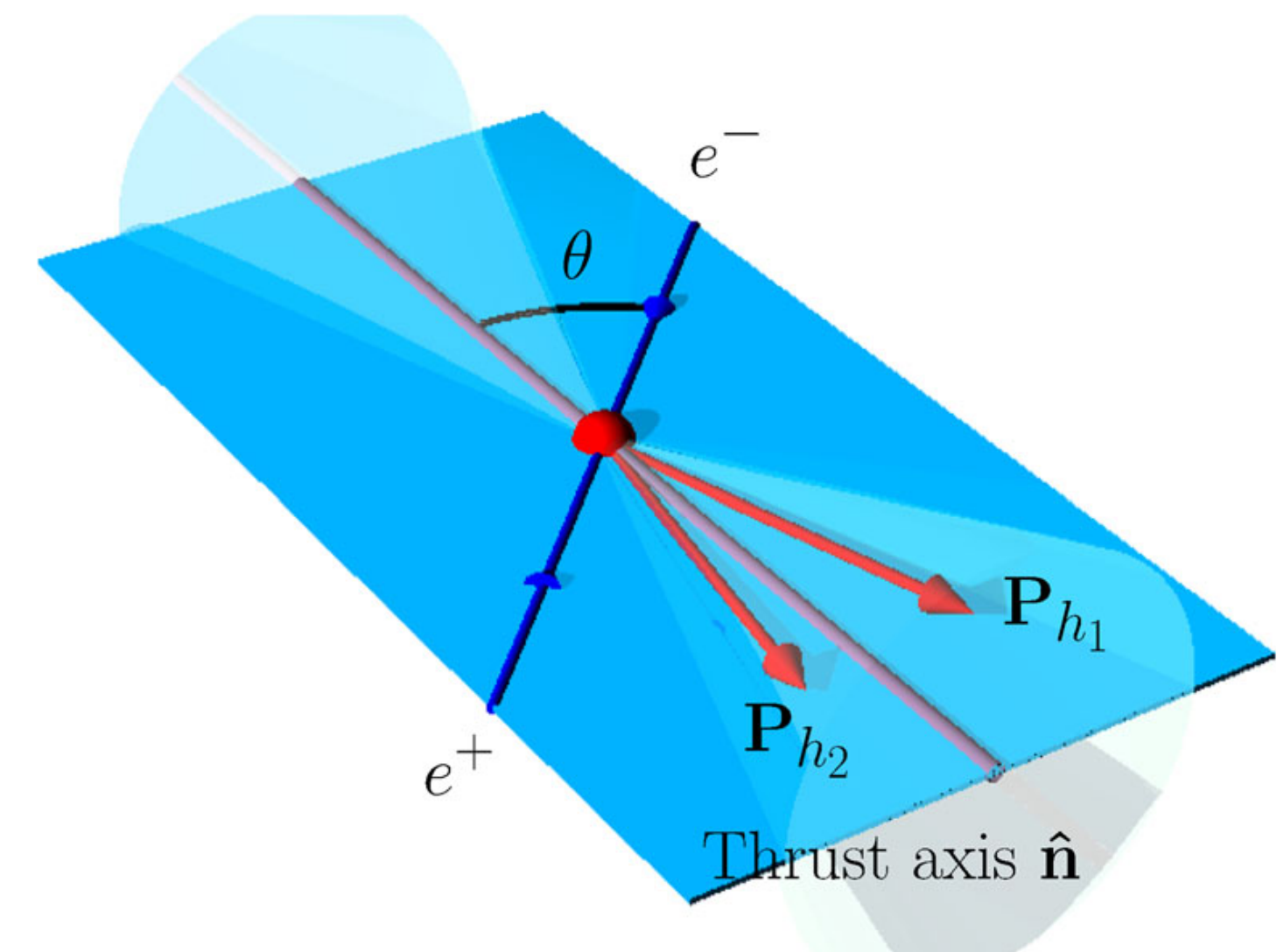
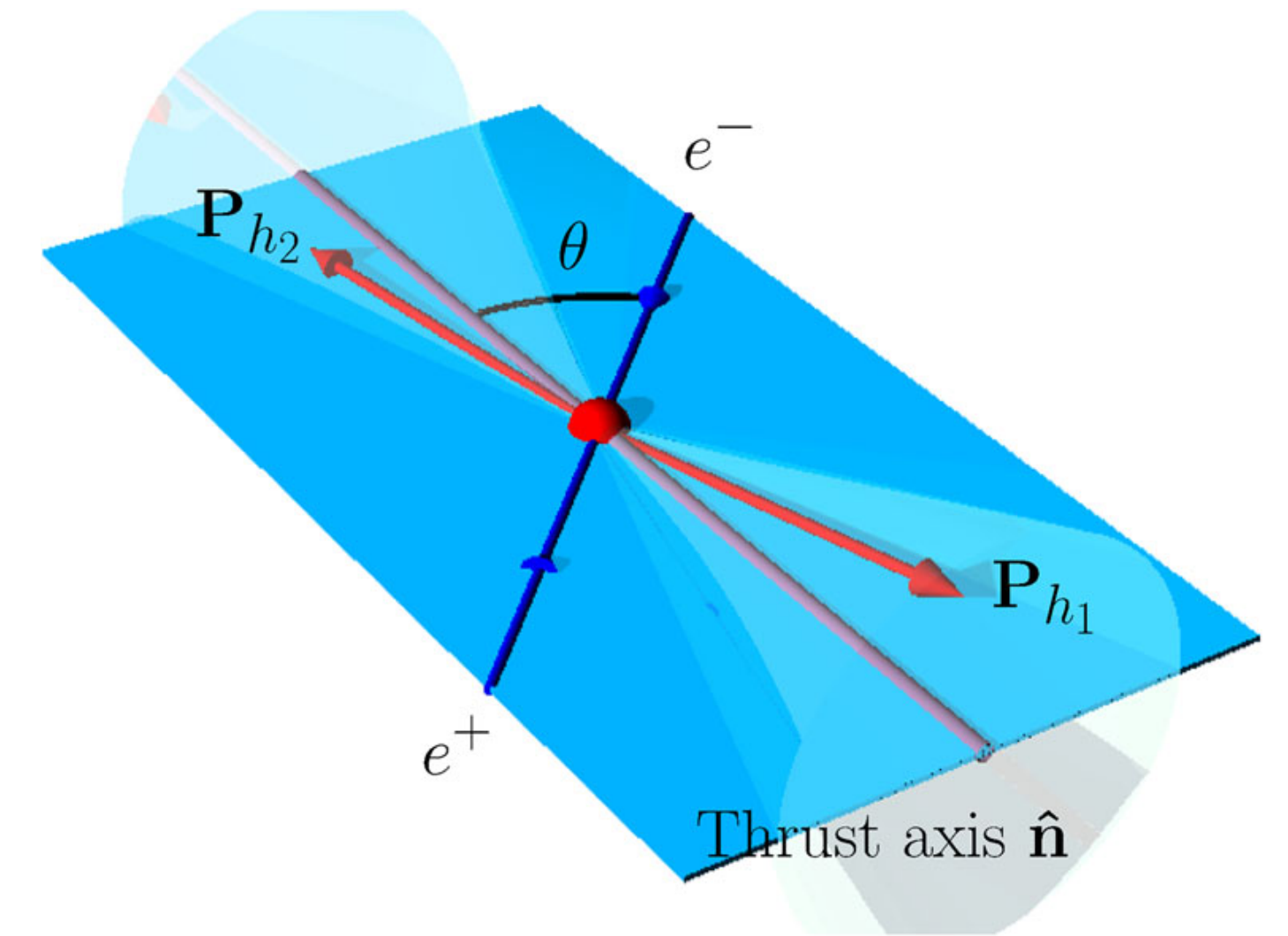
- $0.85 < T < 0.90$ 
  - fit Gauss to low- $P_{hT}$  data
  - mostly well described with possible exception at high  $z$
  - deviation from Gauss at large  $P_{hT}$
  - clear increase of width with  $z$  for low values of  $z$
- Gaussian widths depend on  $z$  and  $T$ 
  - general increase with  $z$  with turnover at larger values of  $z$
  - clear decrease of widths with increase of  $T$ 
    - particles more and more collimated





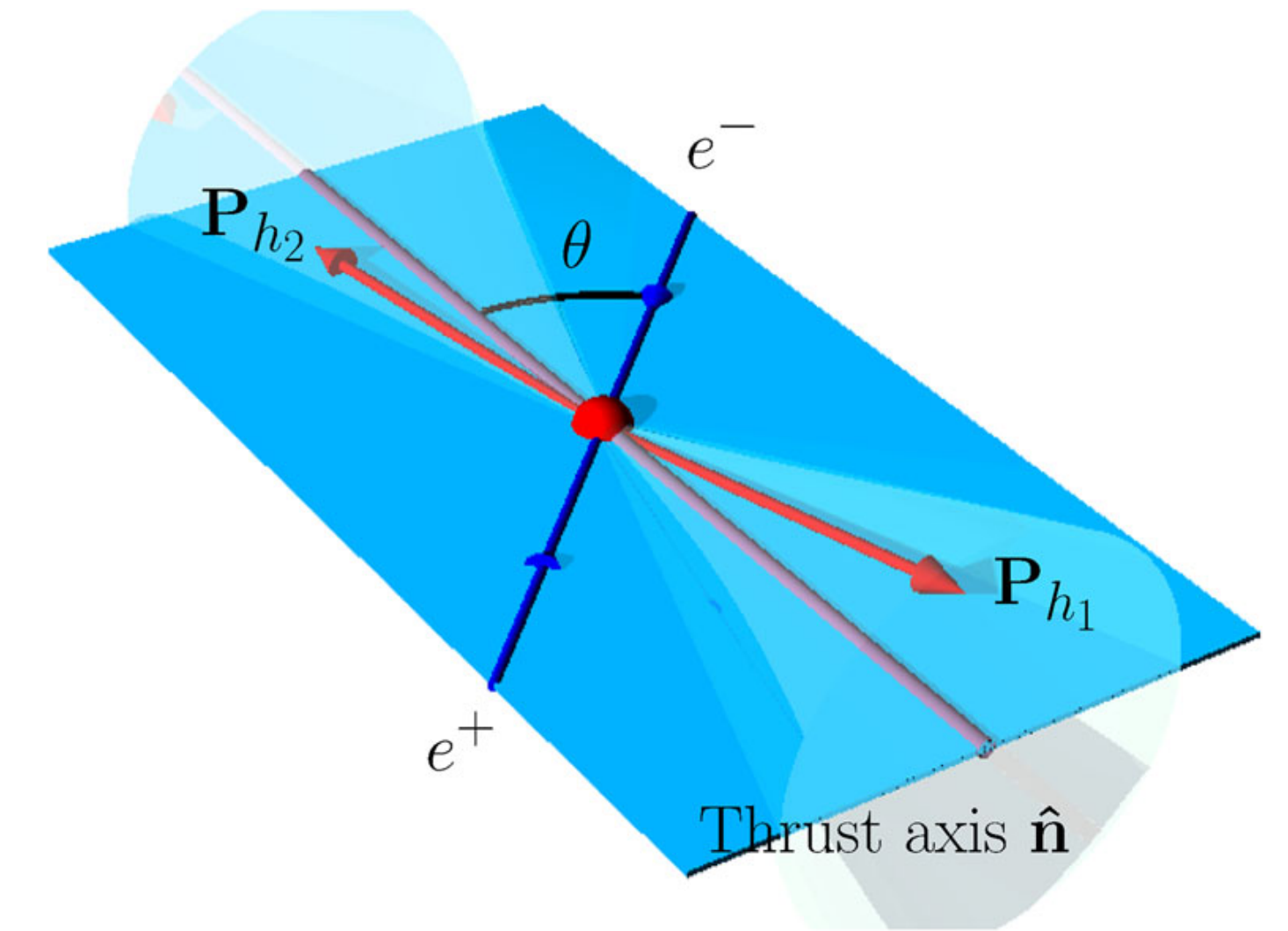
# hadron-pair production

- single-hadron production has low discriminating power for parton flavor
- can use 2<sup>nd</sup> hadron in opposite hemisphere to “tag” flavor, transverse momentum, as well as polarization
- mainly sensitive to product of single-hadron FFs
- if hadrons in same hemisphere: **dihadron fragmentation**
  - a la de Florian & Vanni [Phys. Lett. B 578 (2004) 139]
  - a la Collins, Heppelmann & Ladinsky [NPB 420 (1994) 565]; Boer, Jacobs & Radici [PRD 67 (2003) 094003]
- raises question of defining hemispheres
  - common choices: separation by plane normal to i) thrust axis or to ii) one of the two hadrons (back-to-back case)
  - alternatively, via relevant kinematic variables



# hadron-pair production

- single-hadron production has low discriminating power for parton flavor
- can use 2<sup>nd</sup> hadron in opposite hemisphere to “tag” flavor, transverse momentum, as well as polarization
- mainly sensitive to product of single-hadron FFs
- various definitions for scaling variable



- traditional  $z$  (“std”):

$$z_i = \frac{2P_i \cdot q}{q^2} \quad (i = 1, 2)$$

- Altarelli et al. (“AEMP”):

[Nucl. Phys. B160 (1979) 301]

$$z_1 = \frac{2P_1 \cdot q}{q^2} \quad z_2 = \frac{P_1 \cdot P_2}{P_1 \cdot q}$$

- Mulders & van Hulse (“MVH”):

[PRD 100 (2019) 034011]

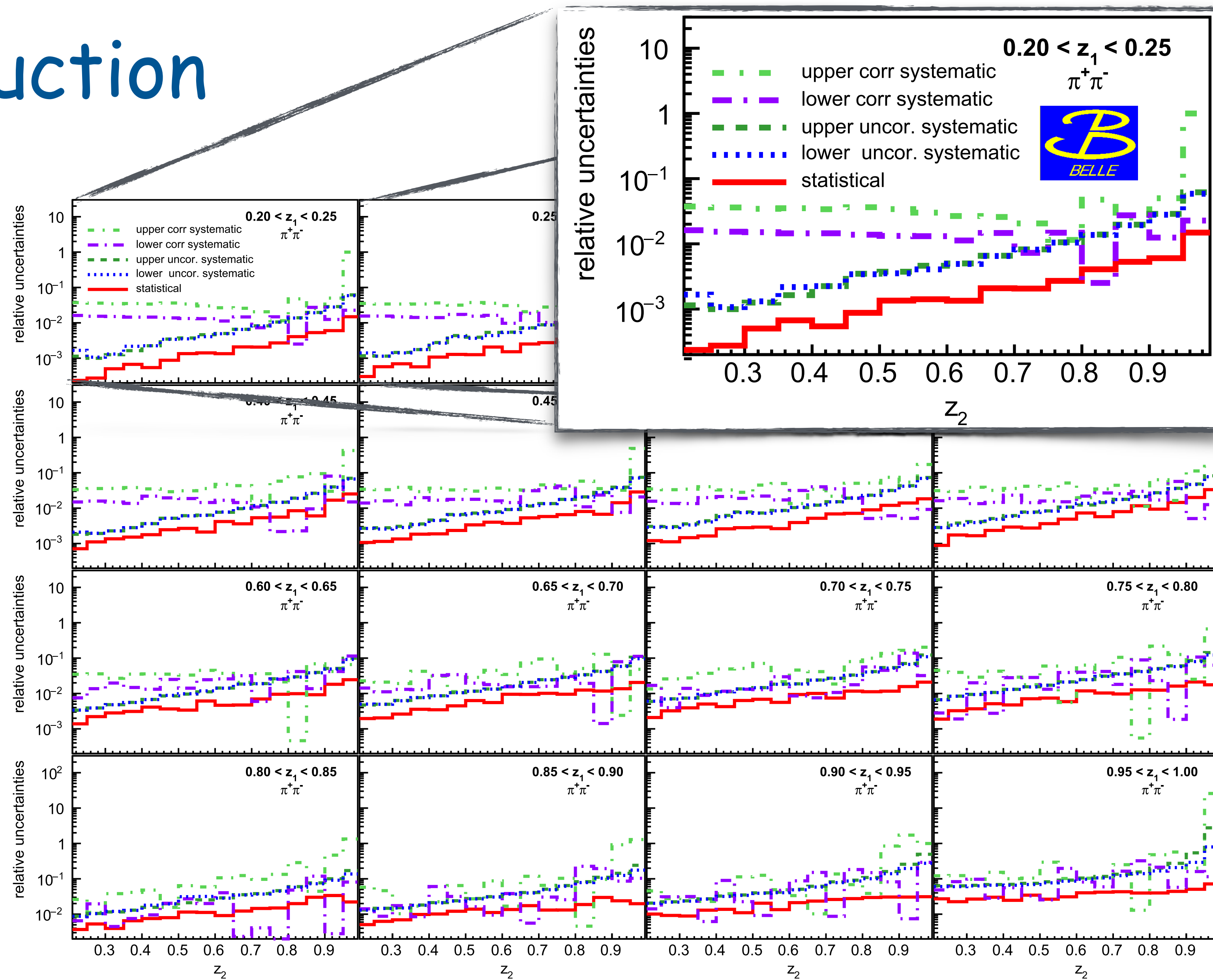
$$z_1 = \left( P_1 \cdot P_2 - \frac{M_{h_1}^2 M_{h_2}^2}{P_1 \cdot P_2} \right) \frac{1}{P_2 \cdot q - M_{h_2}^2 \frac{P_1 \cdot q}{P_1 \cdot P_2}}$$

👉 talk by Charlotte



# light-meson pair production

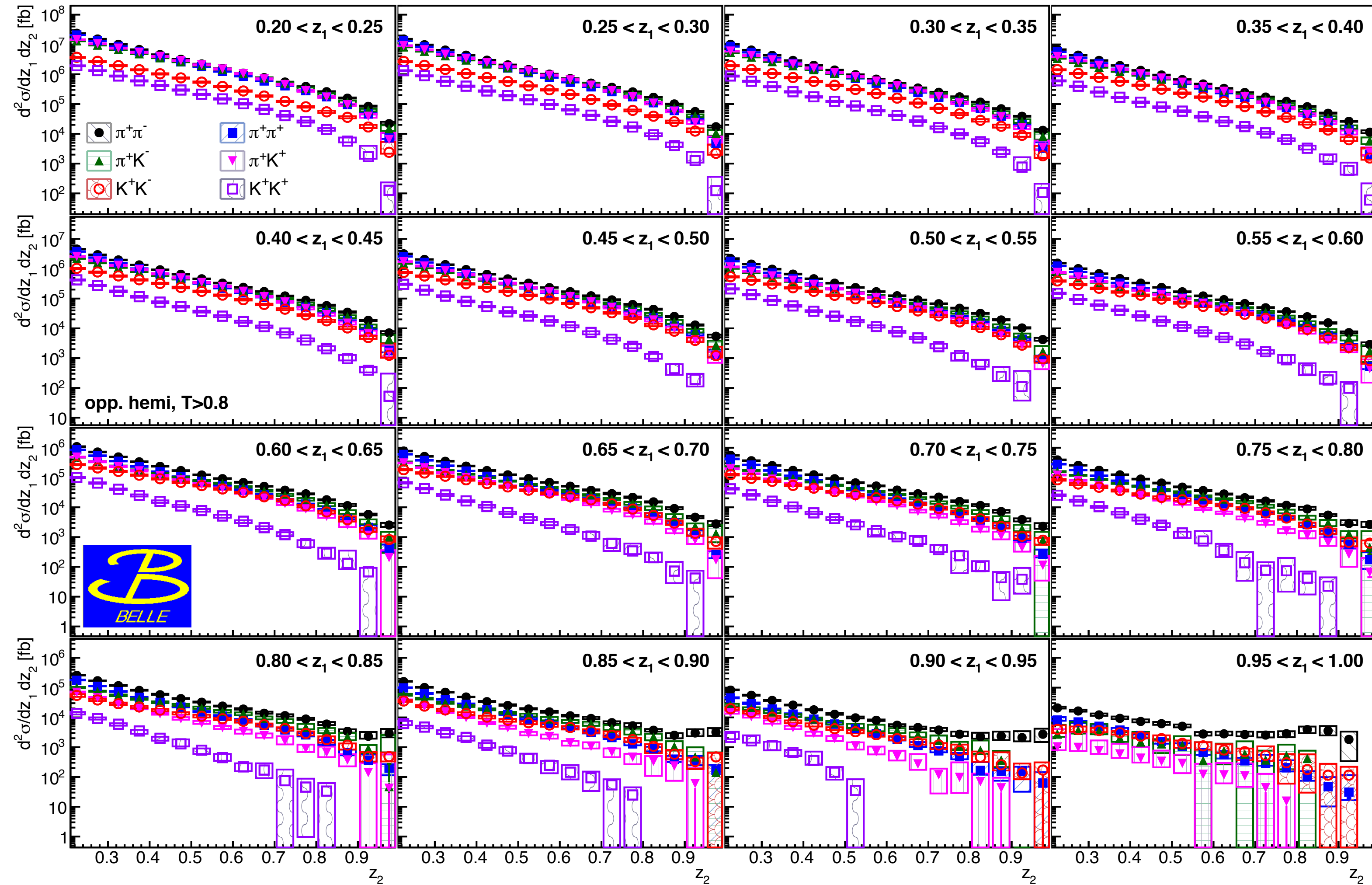
- systematics-dominated over entire kinematic range
- strongly asymmetric systematics
- main contribution from Monte Carlo tune dependence



# light-meson pair production

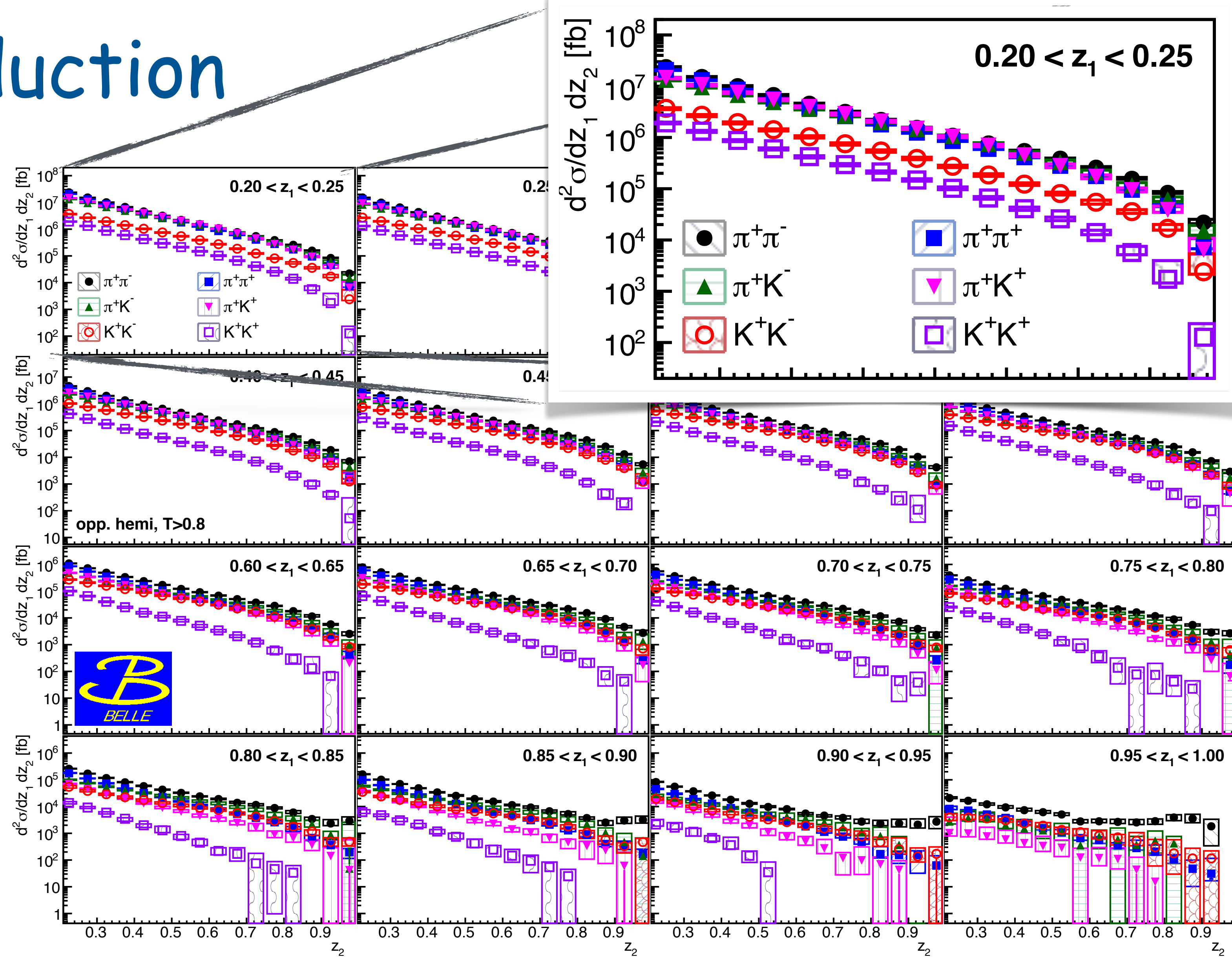
[PRD 101 (2020) 092004]

- systematics-dominated over entire kinematic range
- clear flavor dependence
- suppression of kaons
- suppression of like-sign pairs
- more pronounced at large  $z$  (stronger flavor sensitivity)



# light-meson pair production

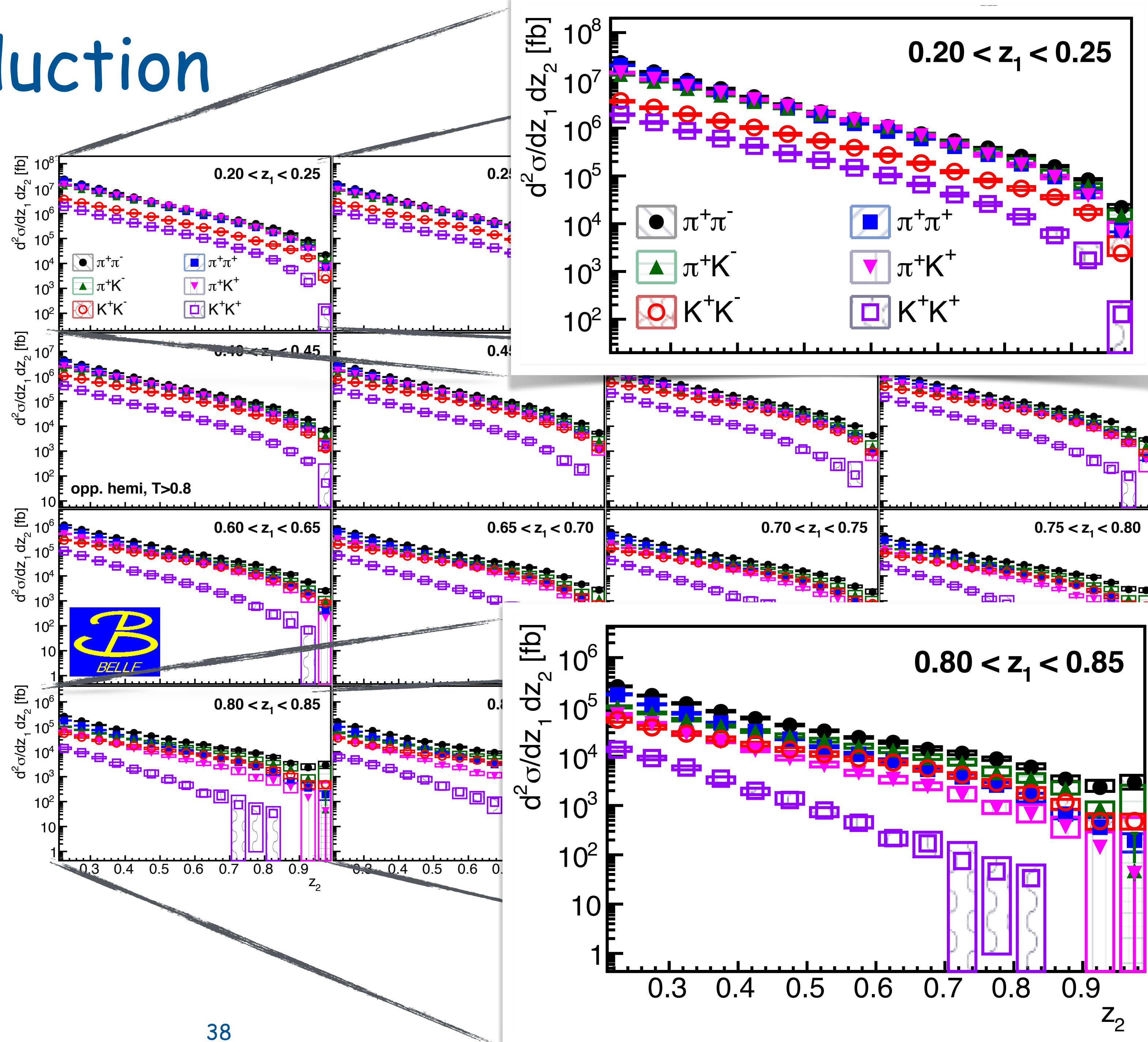
- systematics-dominated over entire kinematic range
- clear flavor dependence
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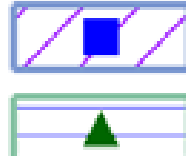
# light-meson pair production


- systematics-dominated over entire kinematic range
- clear flavor dependence
- suppression of kaons
- suppression of like-sign pairs
- more pronounced at large  $z$  (stronger flavor sensitivity)





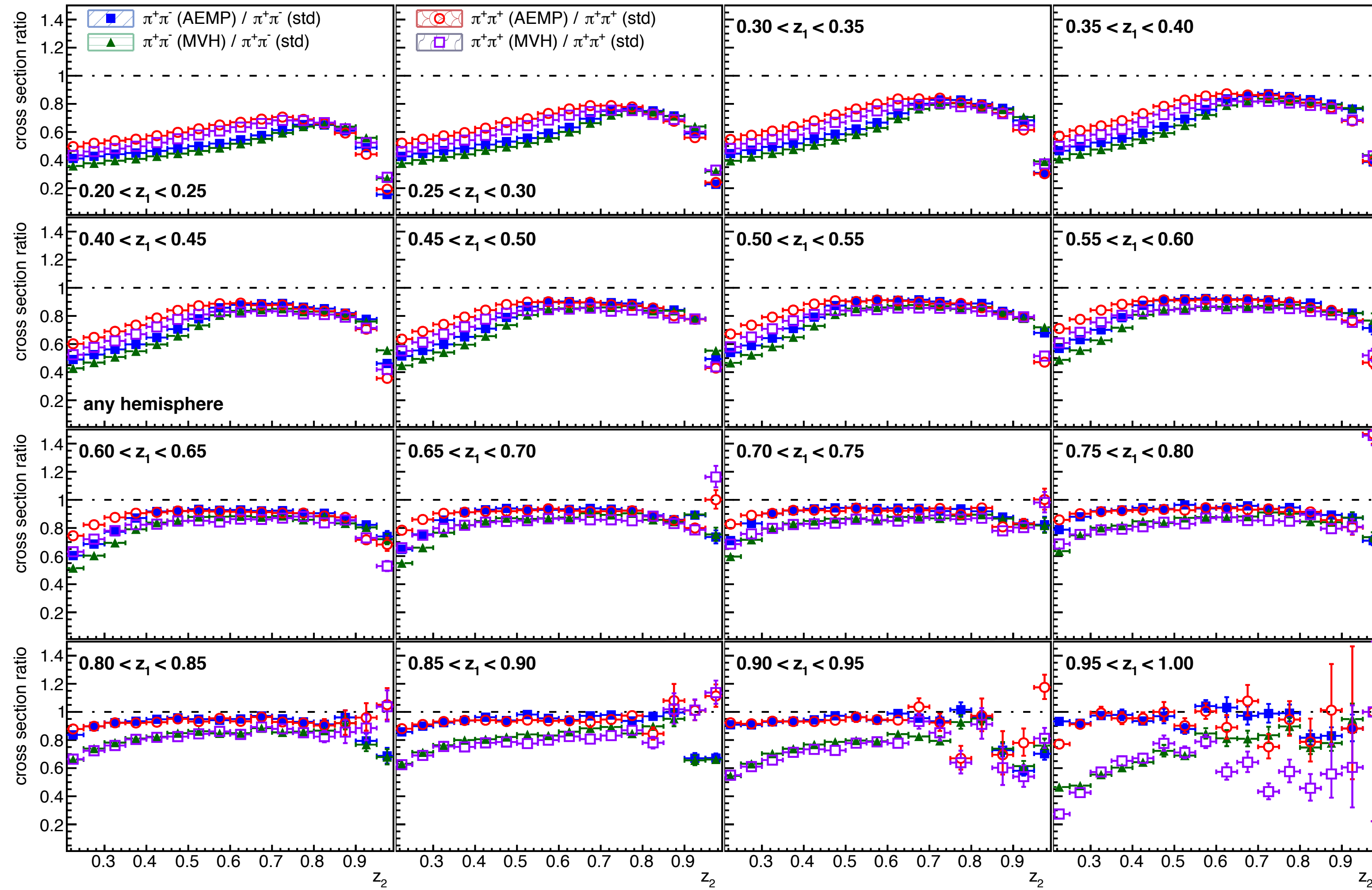
# light-meson pair production


 $\pi^+\pi^-$  (AEMP) /  $\pi^+\pi^-$  (std)  
 $\pi^+\pi^-$  (MVH) /  $\pi^+\pi^-$  (std)


 $\pi^+\pi^+$  (AEMP) /  $\pi^+\pi^+$  (std)  
 $\pi^+\pi^+$  (MVH) /  $\pi^+\pi^+$  (std)



- systematics-dominated over entire kinematic range
- clear flavor dependence
- suppression of kaons
- suppression of like-sign pairs
- more pronounced at large  $z$  (stronger flavor sensitivity)
- suppression (especially low  $z$ ) for alternative fractional-energy definitions, more so for MVH

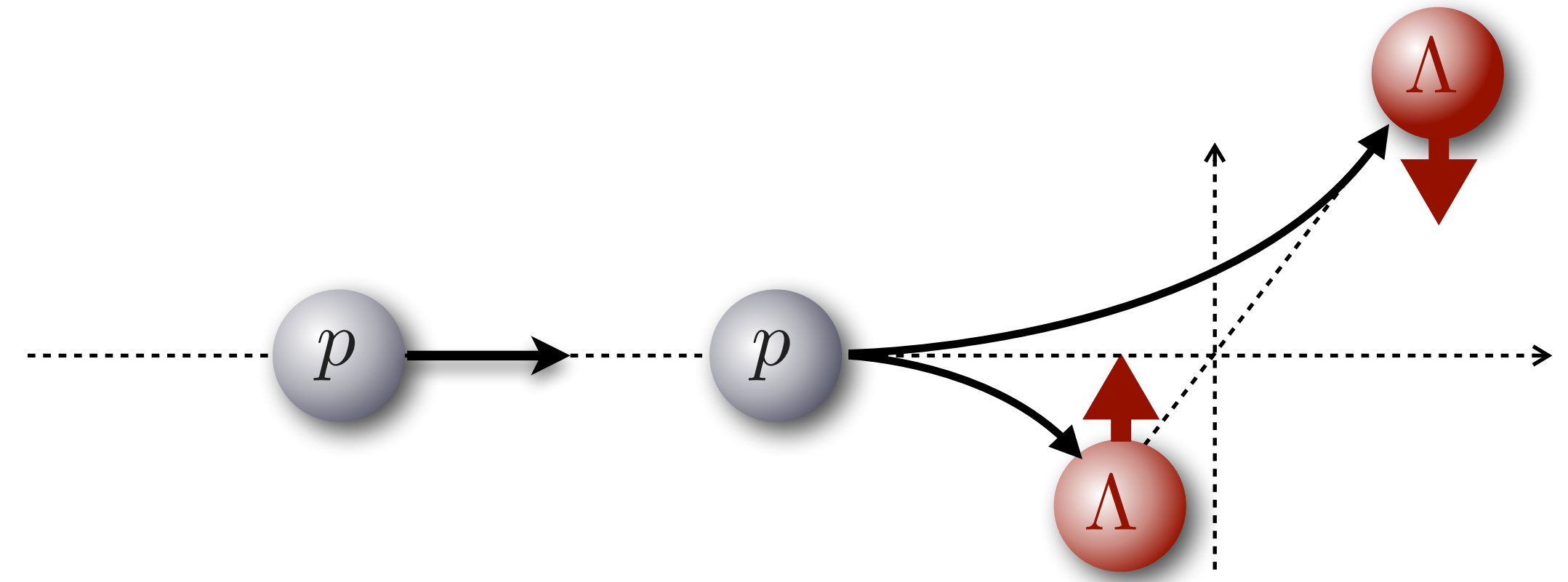
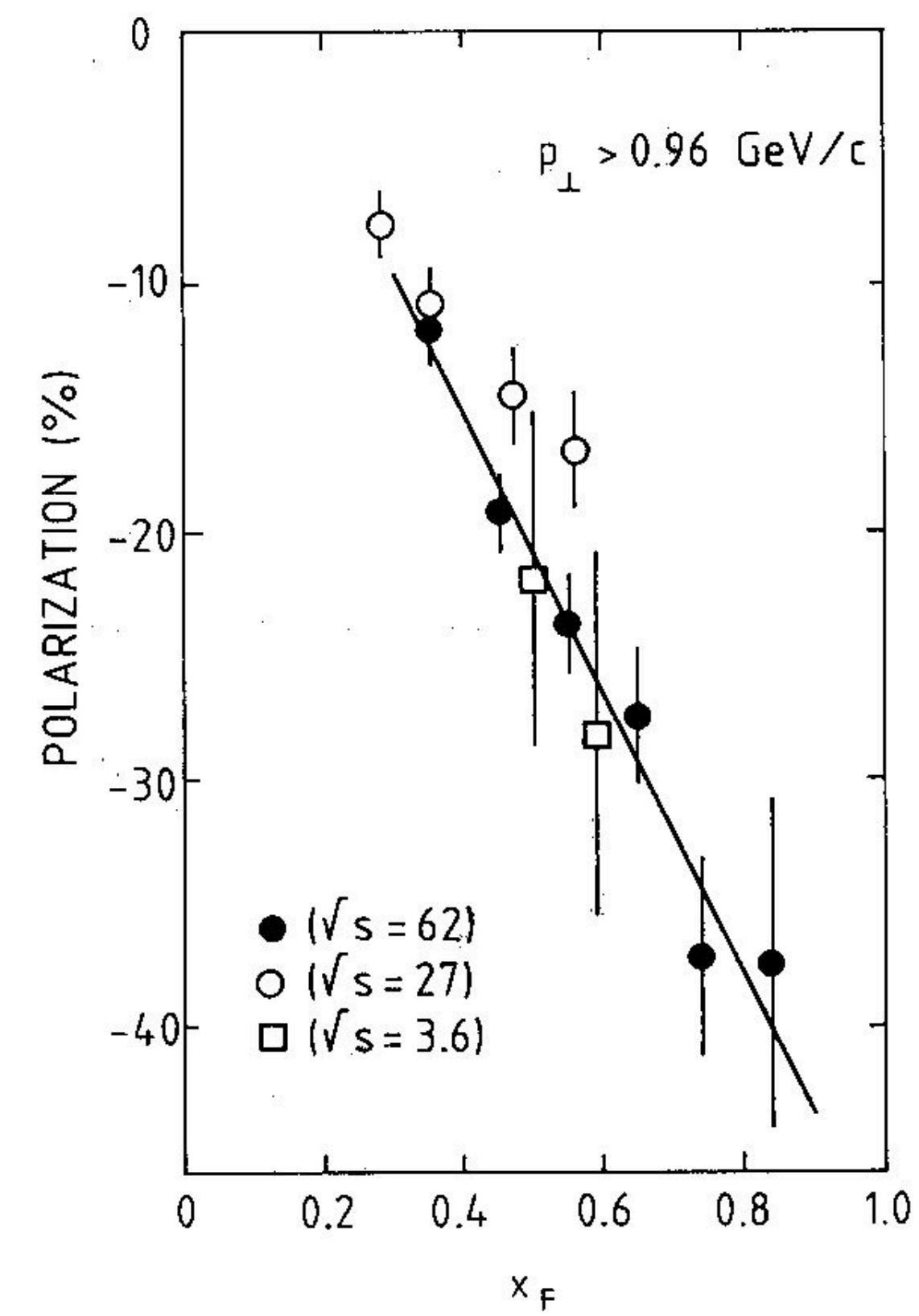


👉 talk by Charlotte

[PRD 101 (2020) 092004]

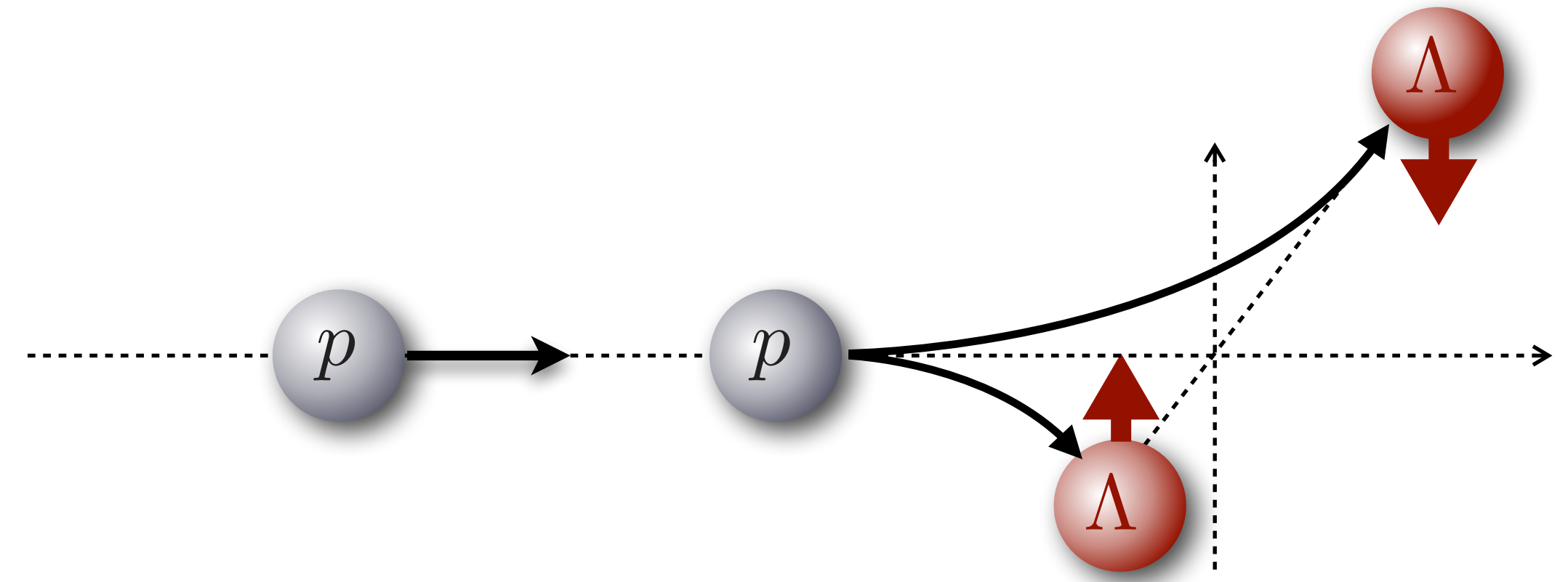
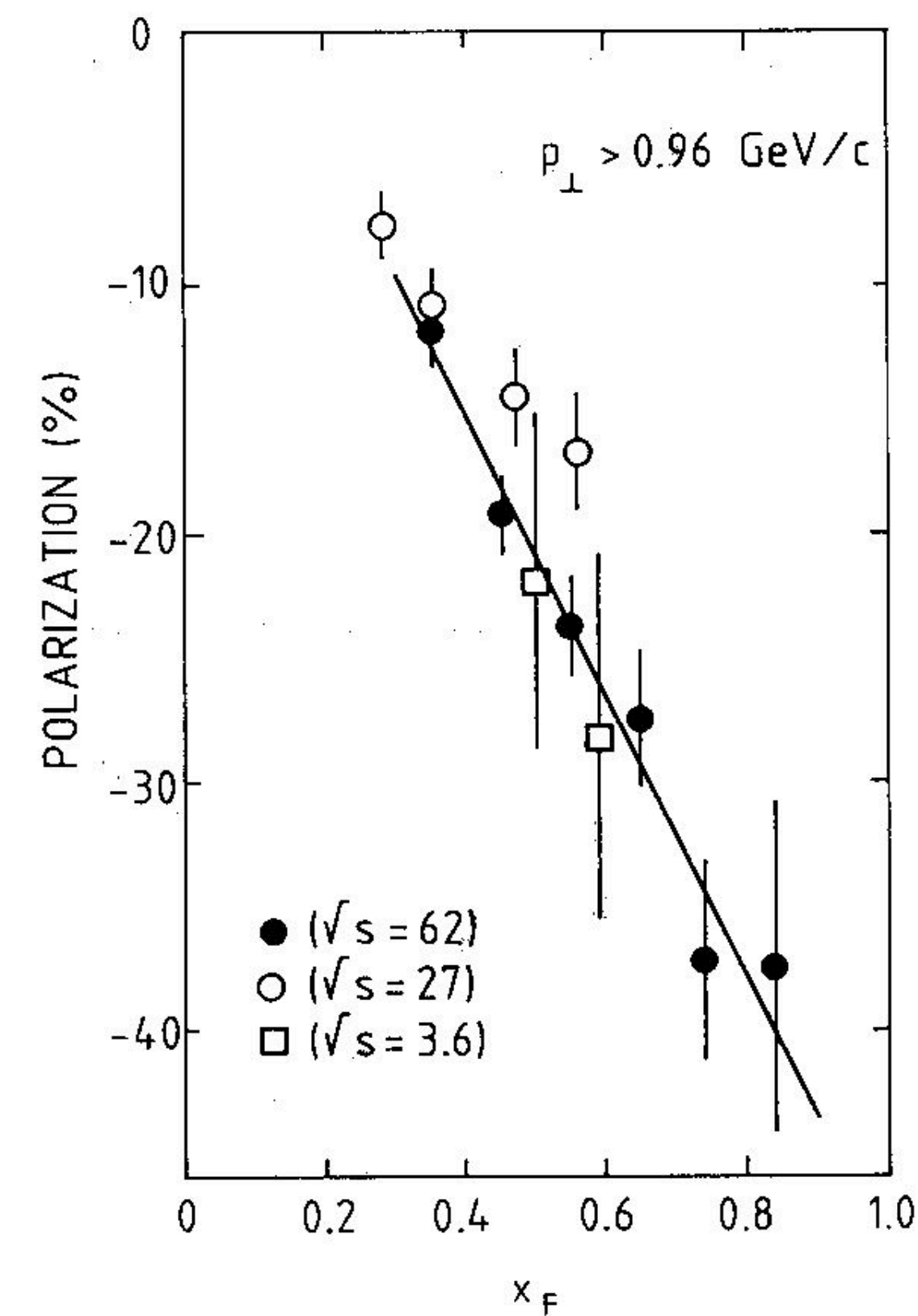
polarization effects  
despite unpolarized initial state

# polarizing fragmentation

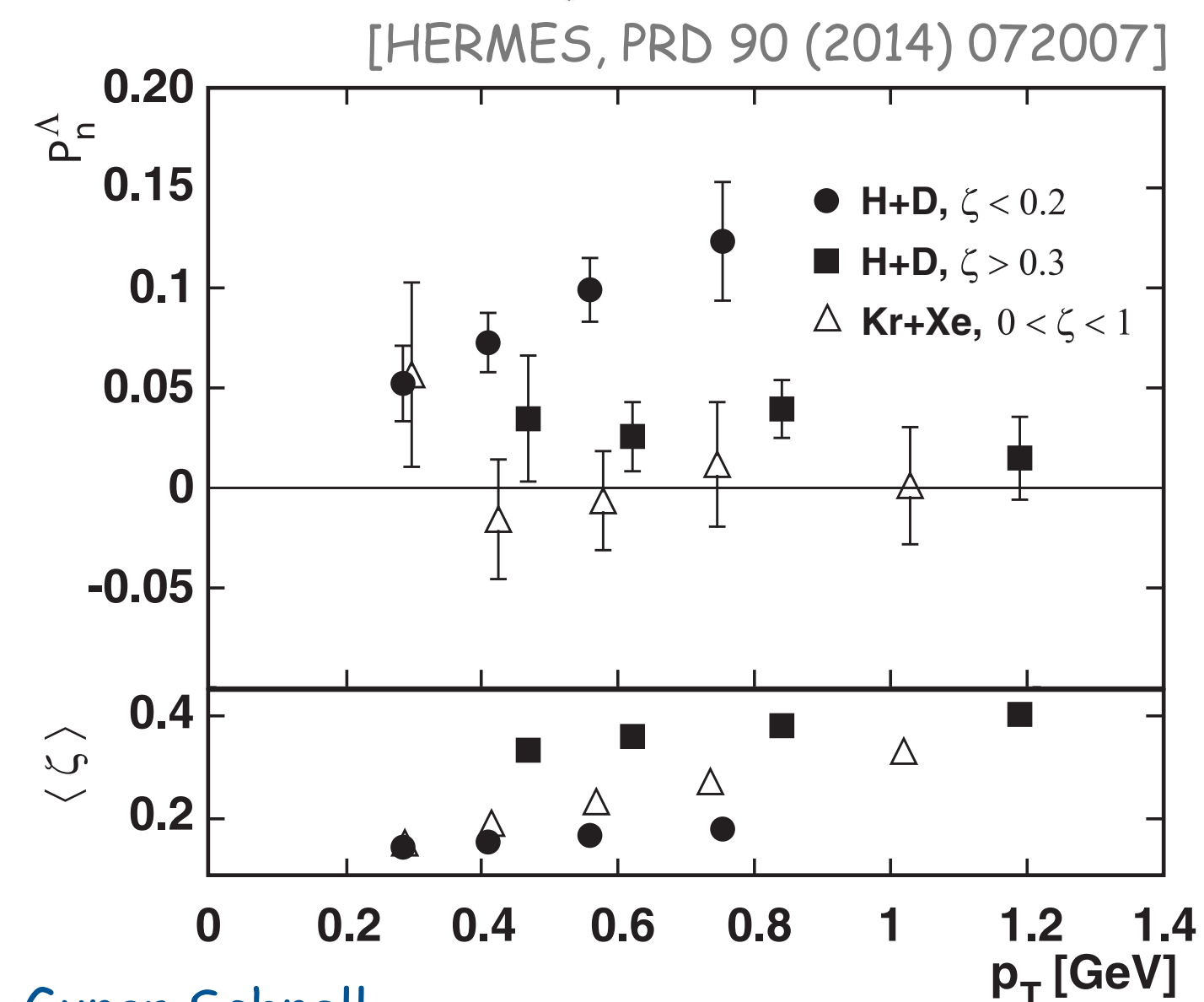


- large hyperon polarization in unpolarized hadron collision observed

# polarizing fragmentation

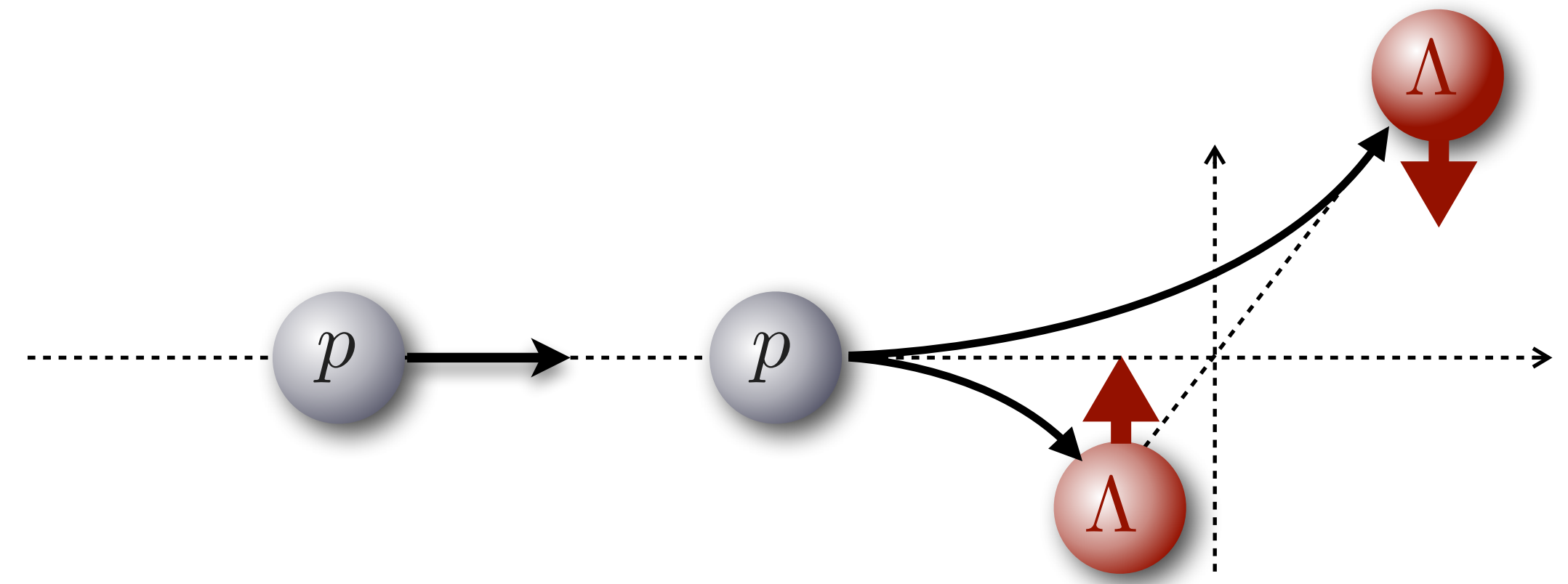
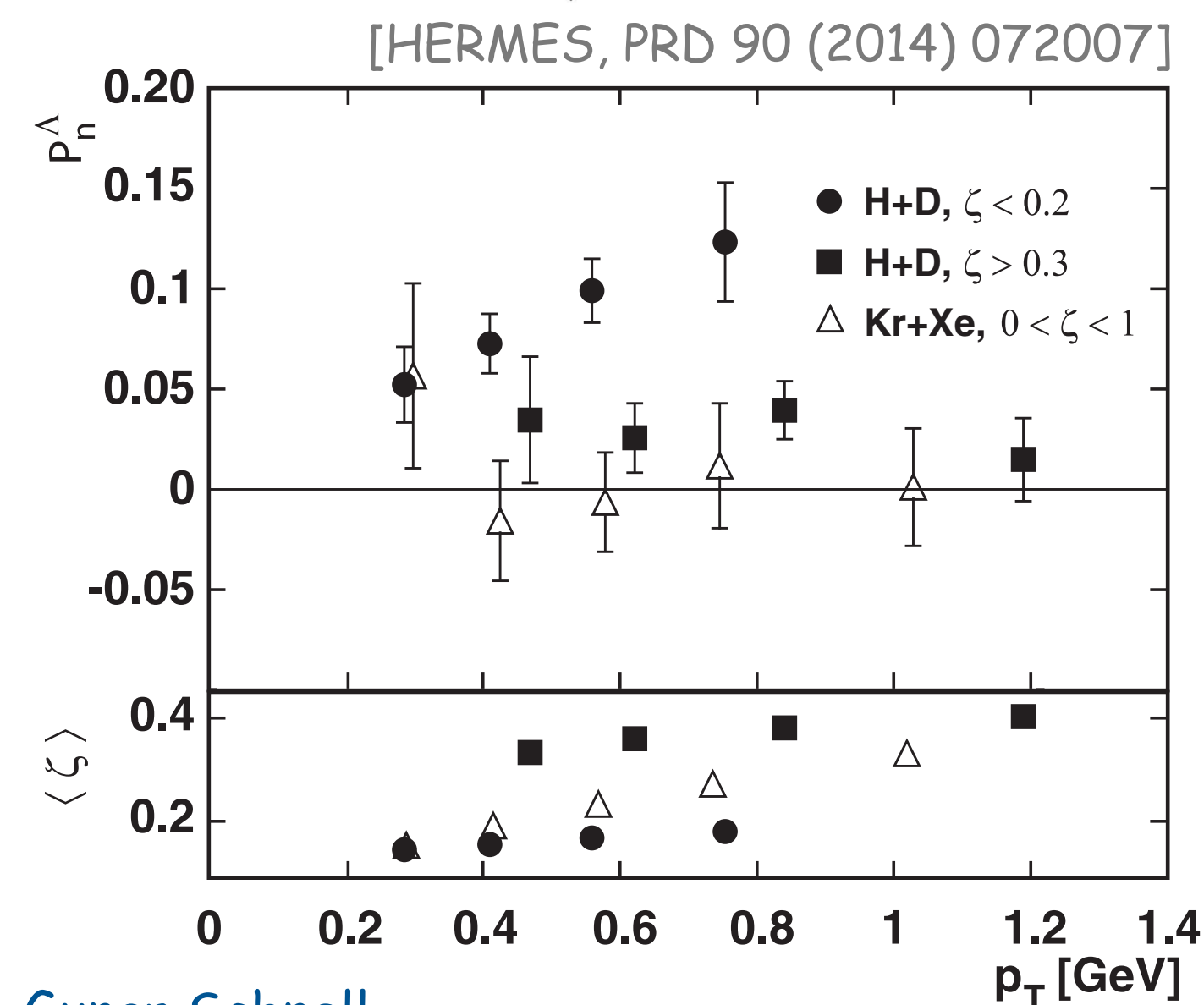
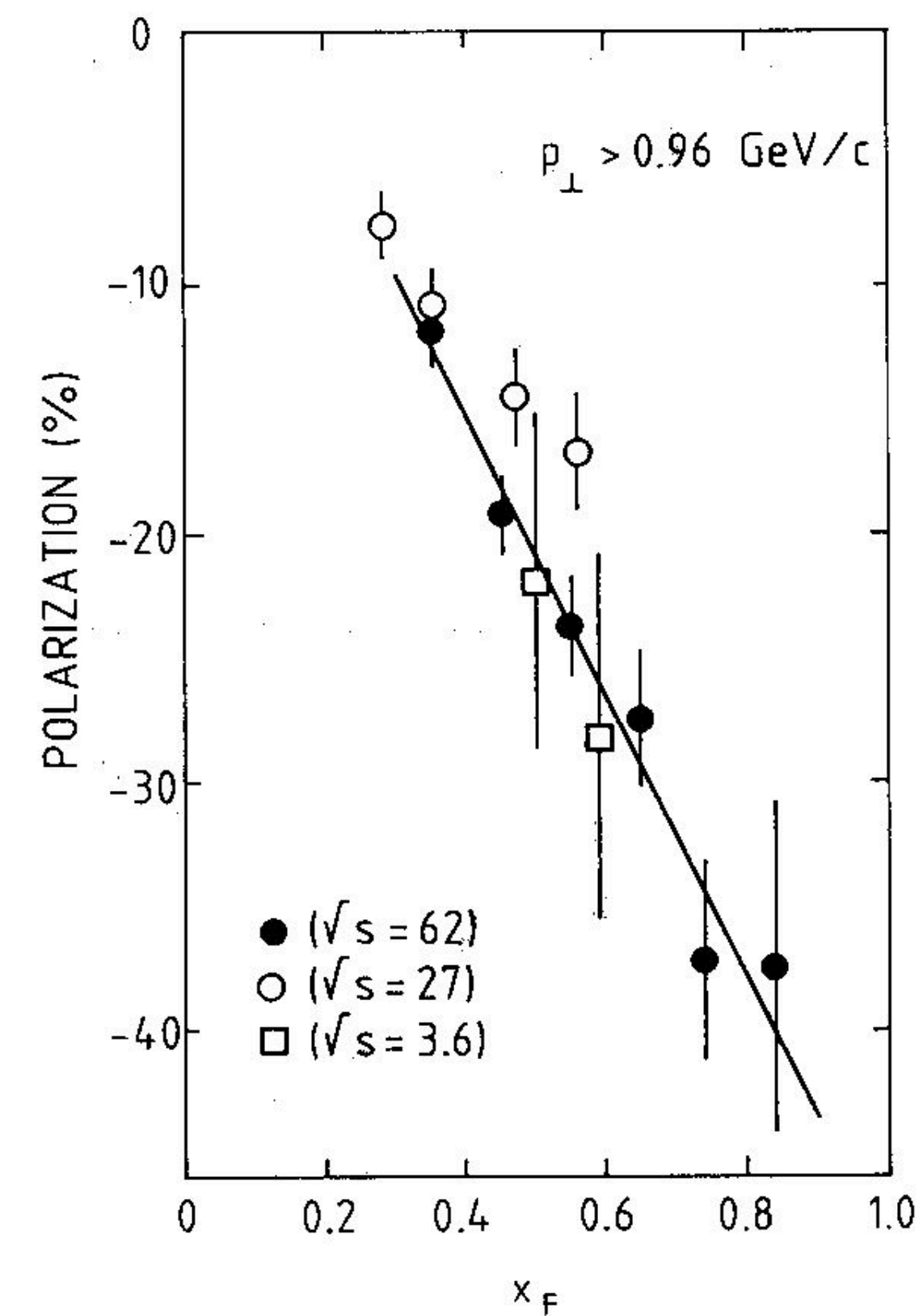


- large hyperon polarization in unpolarized hadron collision observed
- ... as well as in inclusive lepto-production

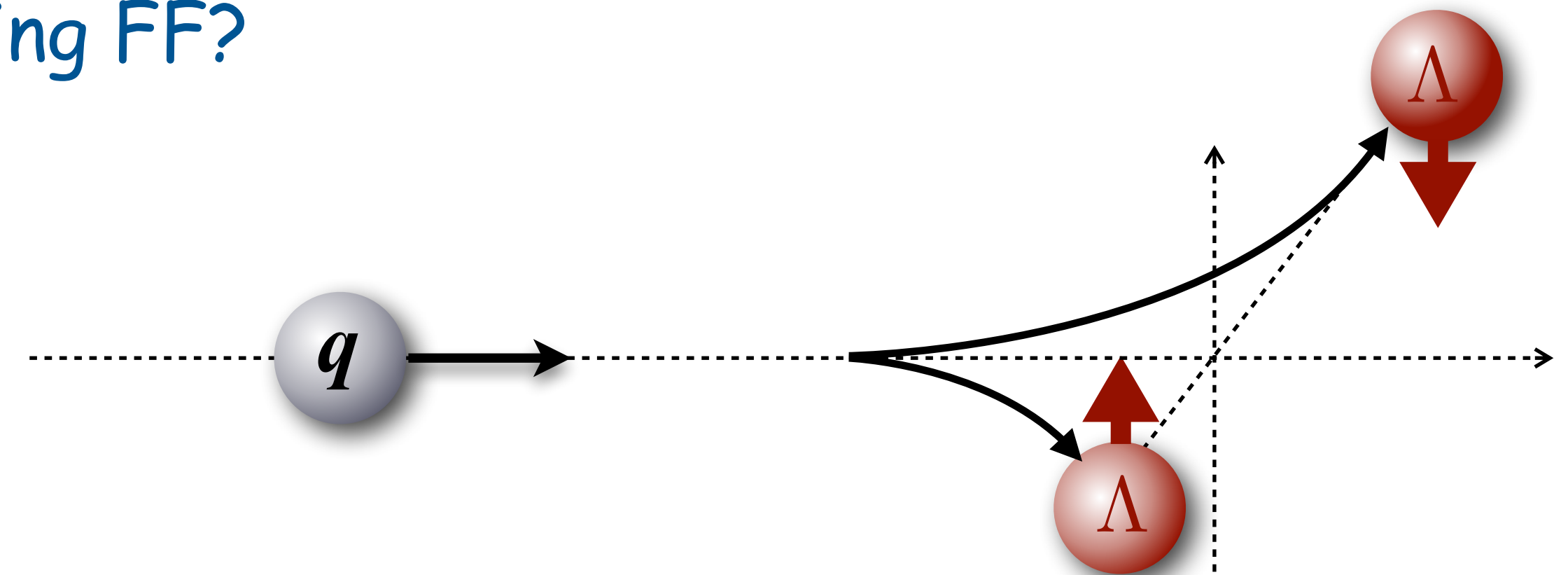




# polarizing fragmentation

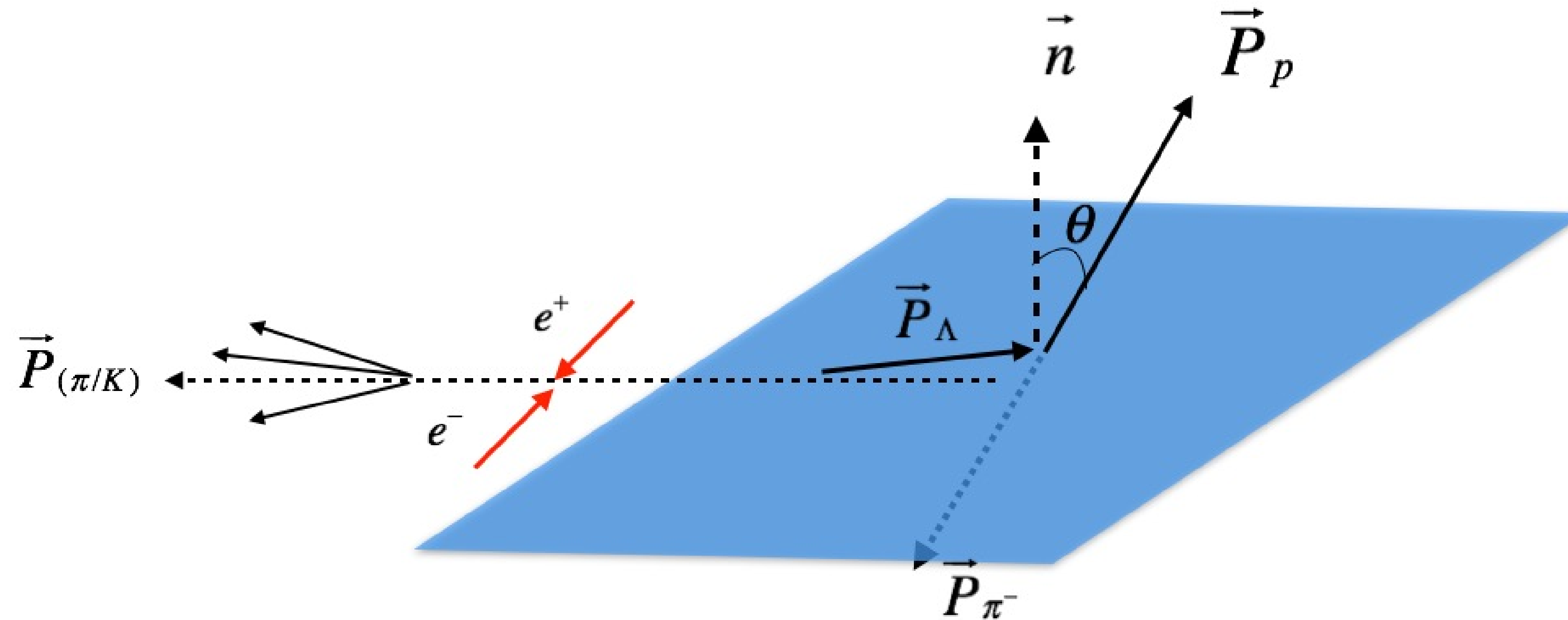


- large hyperon polarization in unpolarized hadron collision observed
- ... as well as in inclusive lepto-production
- caused by polarizing FF?



# polarizing fragmentation function

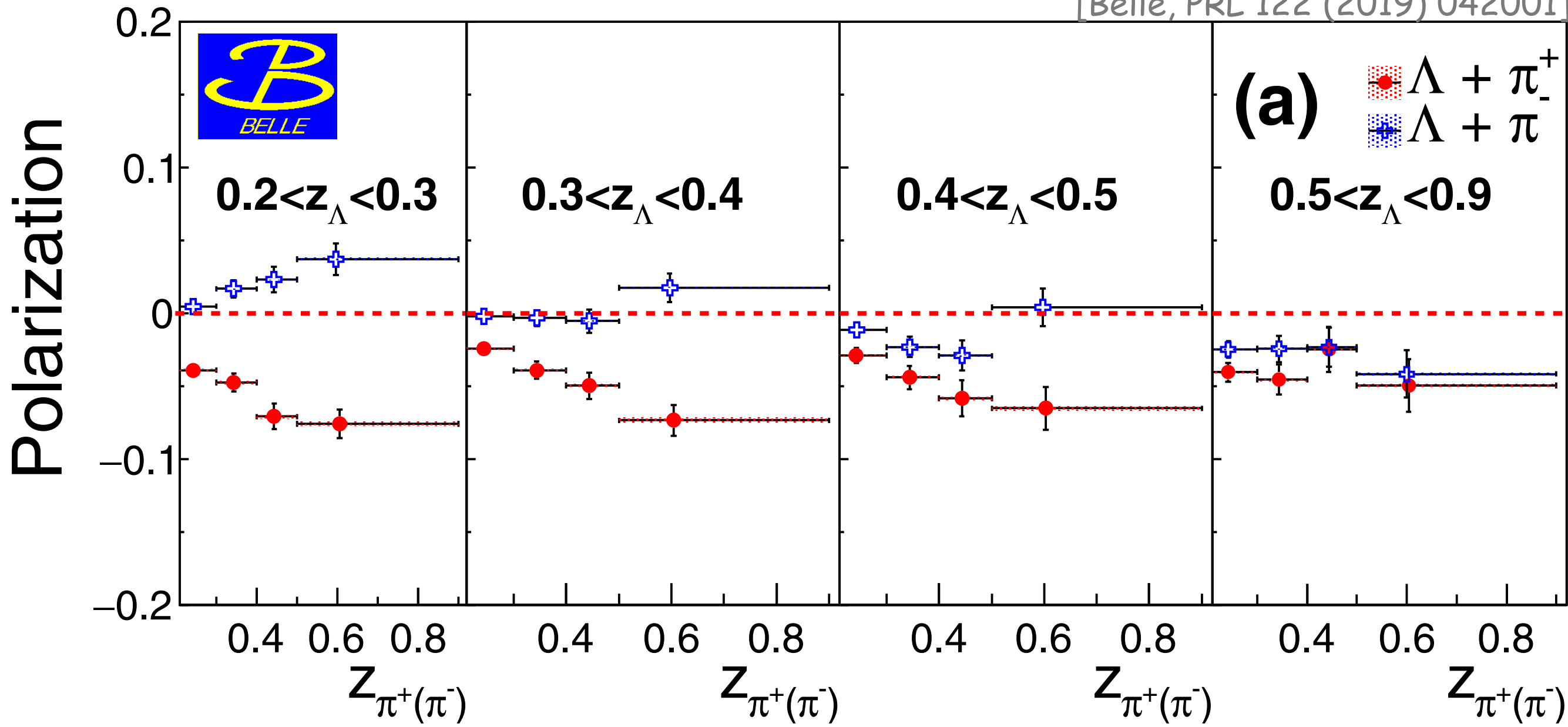
- polarization measured normal to production plane, i.e.  $\propto (\vec{P}_q \times P_\Lambda)$



- reference axis to define transverse momentum:
  - "hadron frame" - use momentum direction of "back-to-back" hadron
  - "thrust frame" - use thrust axis
- exploit self-analyzing weak decay of  $\Lambda$  to determine polarization

# polarizing fragmentation function

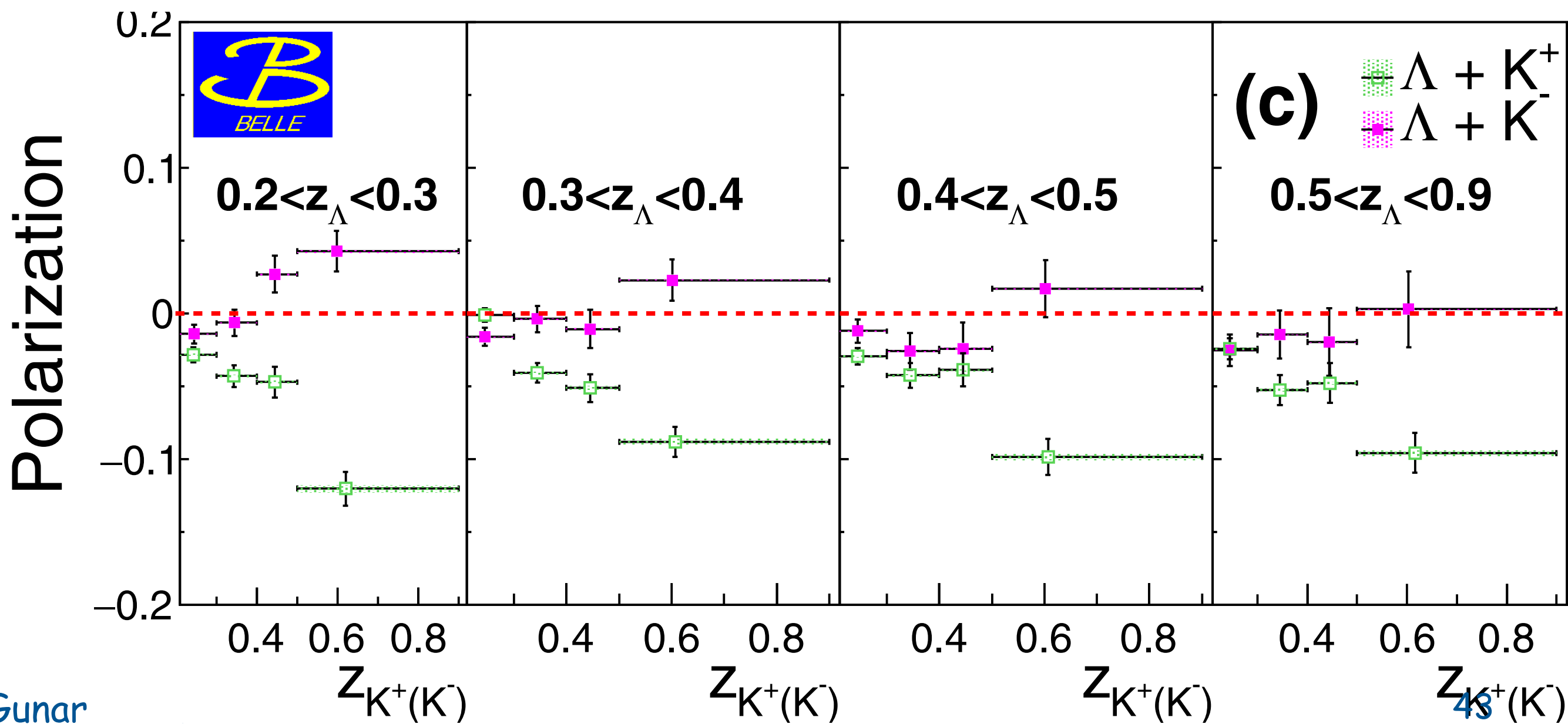
[Belle, PRL 122 (2019) 042001]



- flavor tagging through hadrons in opposite hemisphere:

- large- $z_h$  hadrons tag quark flavor more efficiently

- ➔ enlarges differences between oppositely charged hadrons

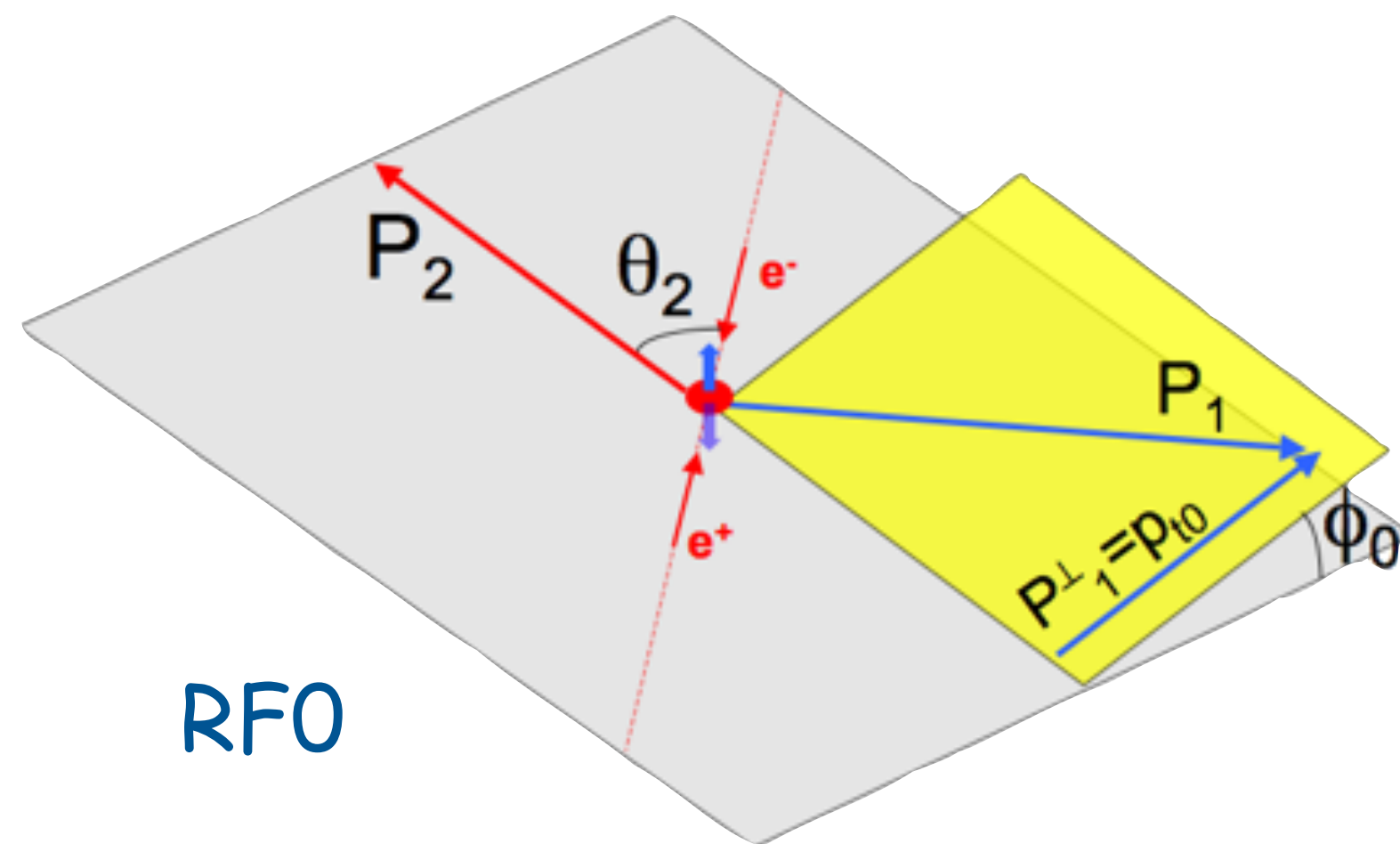


👉 talk by Marco

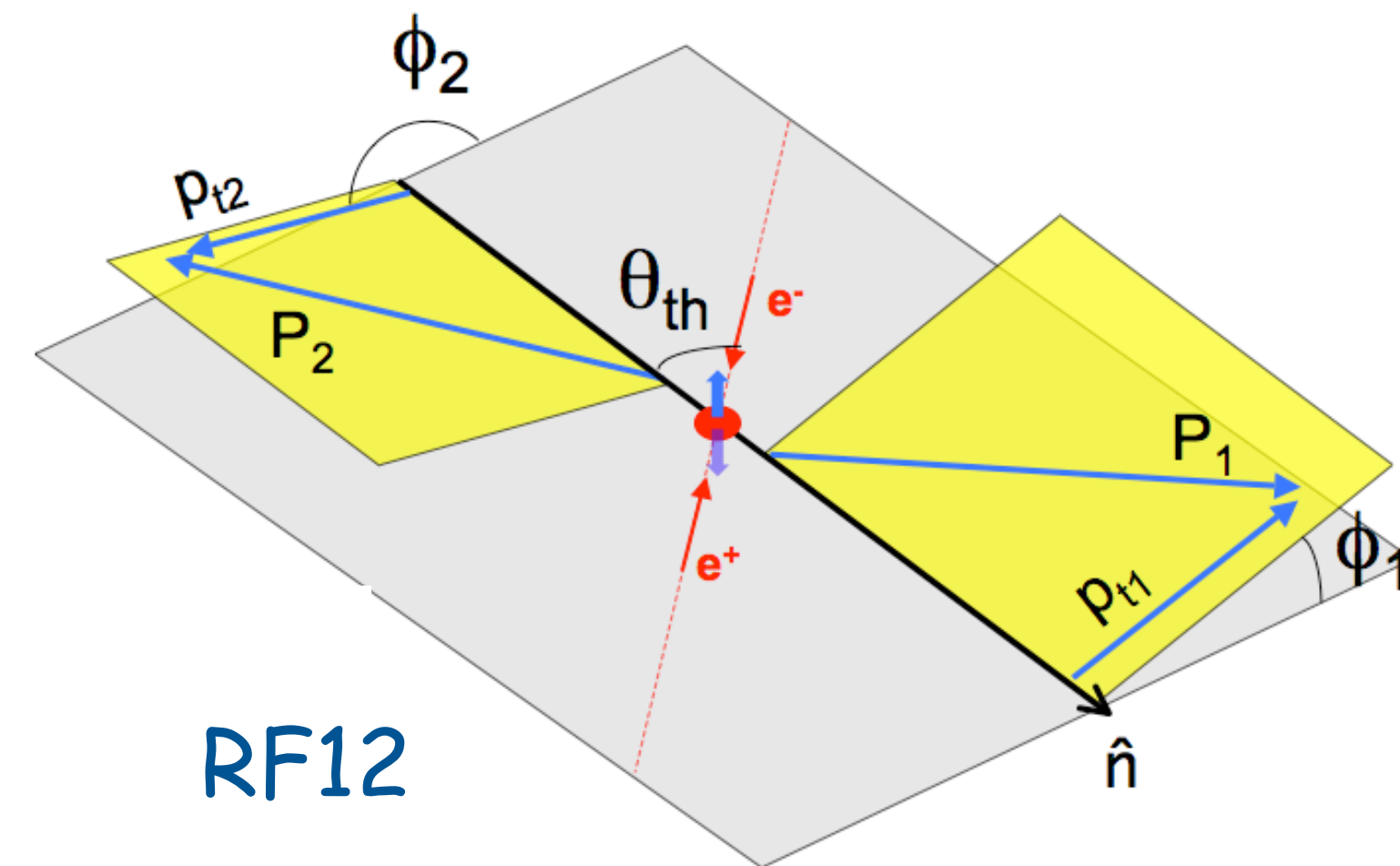
$$z_h = \frac{E_h}{\sqrt{s}/2}$$

# hadron pairs: angular correlations

- angular correlations between nearly back-to-back hadrons used to tag transverse quark polarization -> Collins fragmentation functions
- RF0: one hadron as reference axis ->  $\cos(2\phi_0)$  modulation
- RF12: thrust (or similar) axis ->  $\cos(\phi_1+\phi_2)$  modulation



RF0



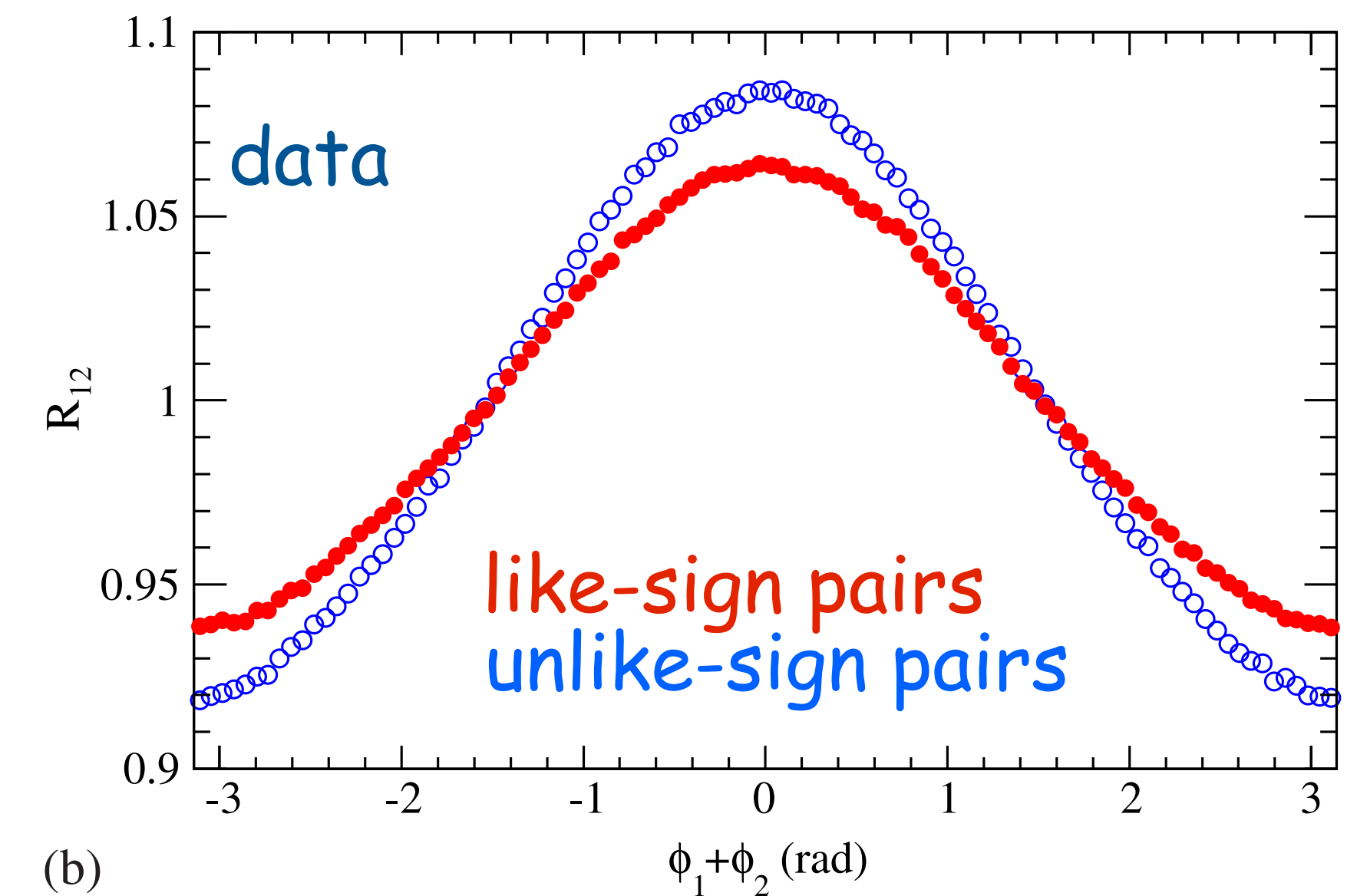
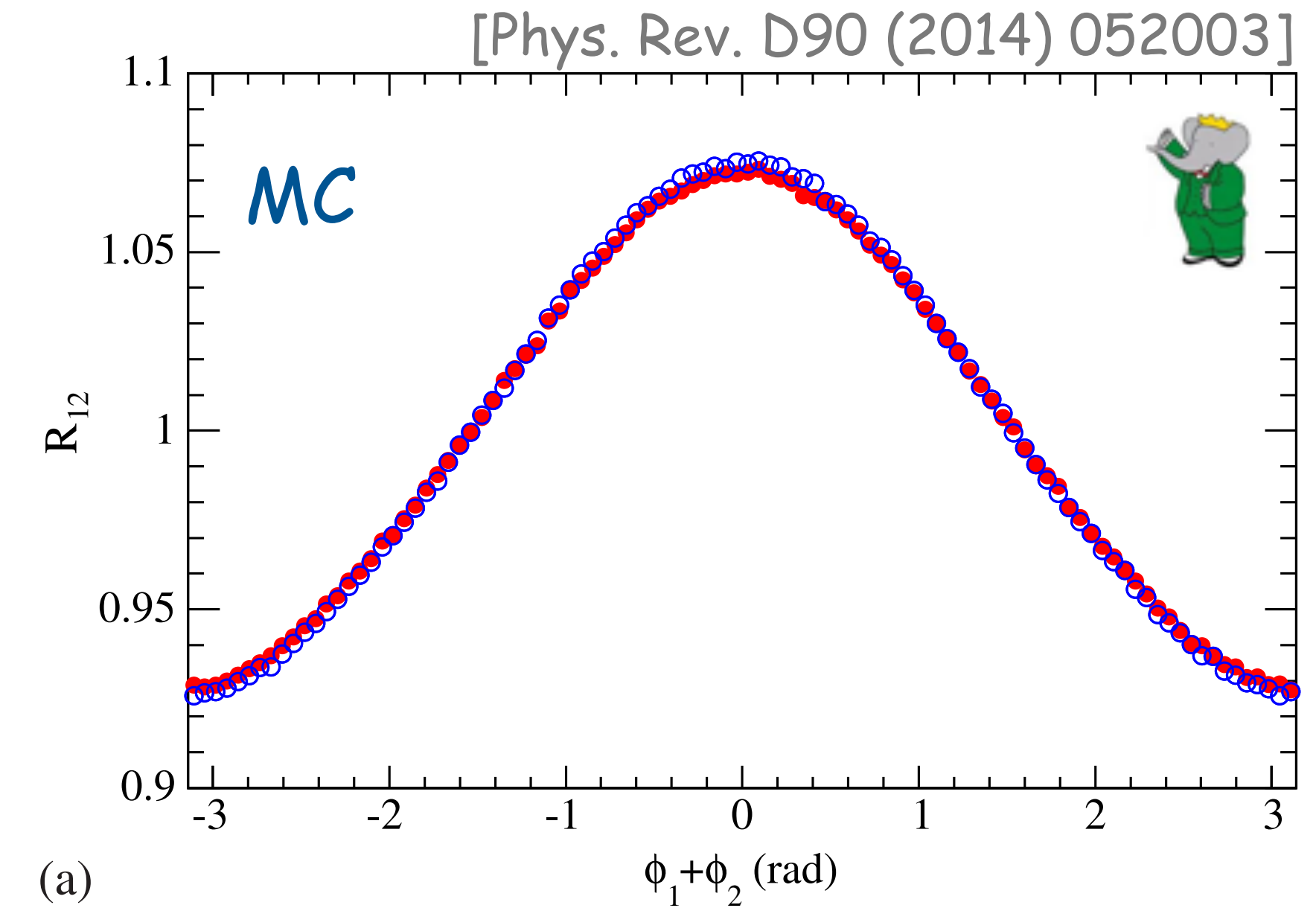
RF12

- RF0 and RF12: different convolutions over transverse momenta
- debatable: MC used to "correct" thrust axis to  $q\bar{q}$  axis



# hadron pairs: angular correlations

- challenge: large modulations even without Collins effect (e.g., in PYTHIA MC)

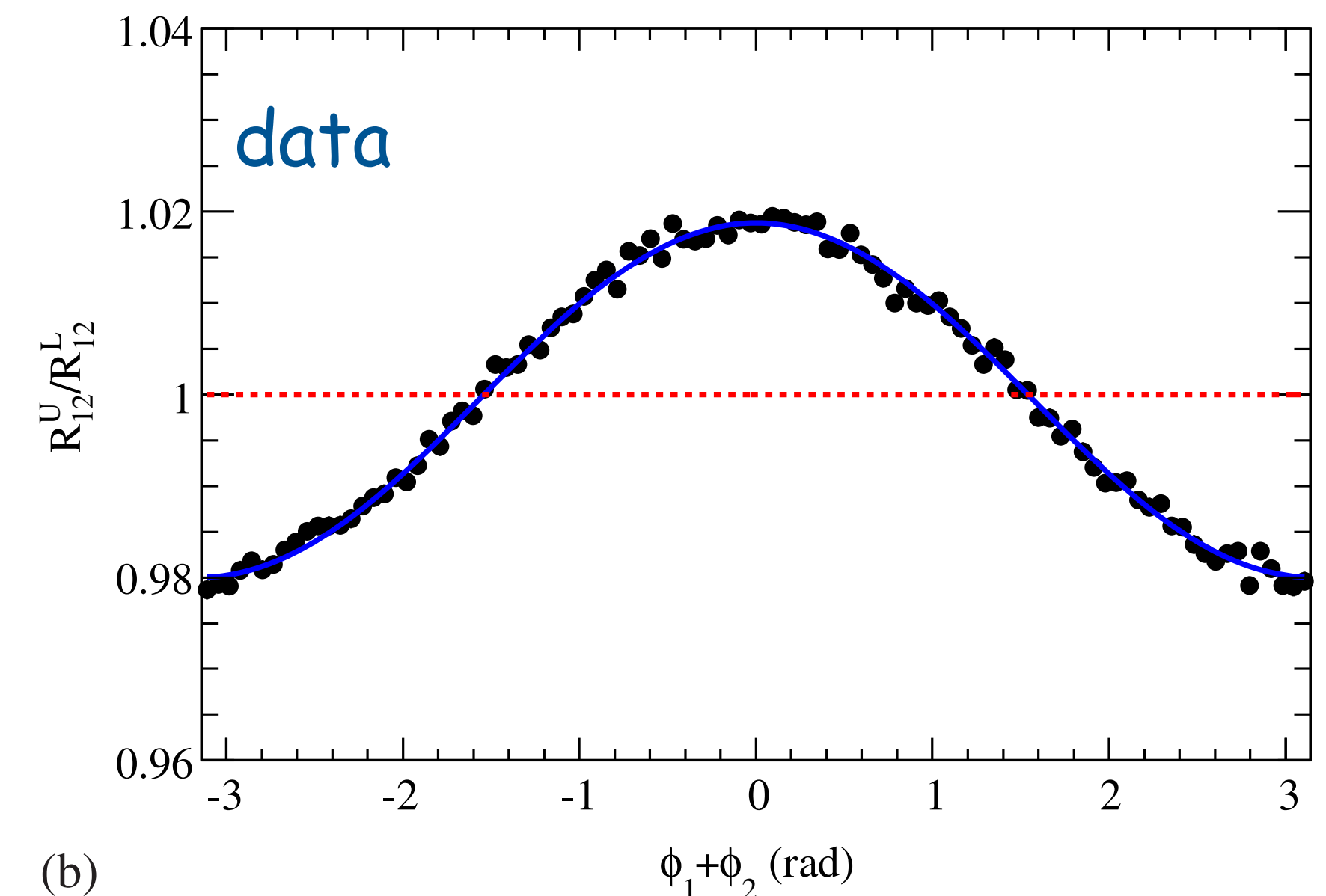
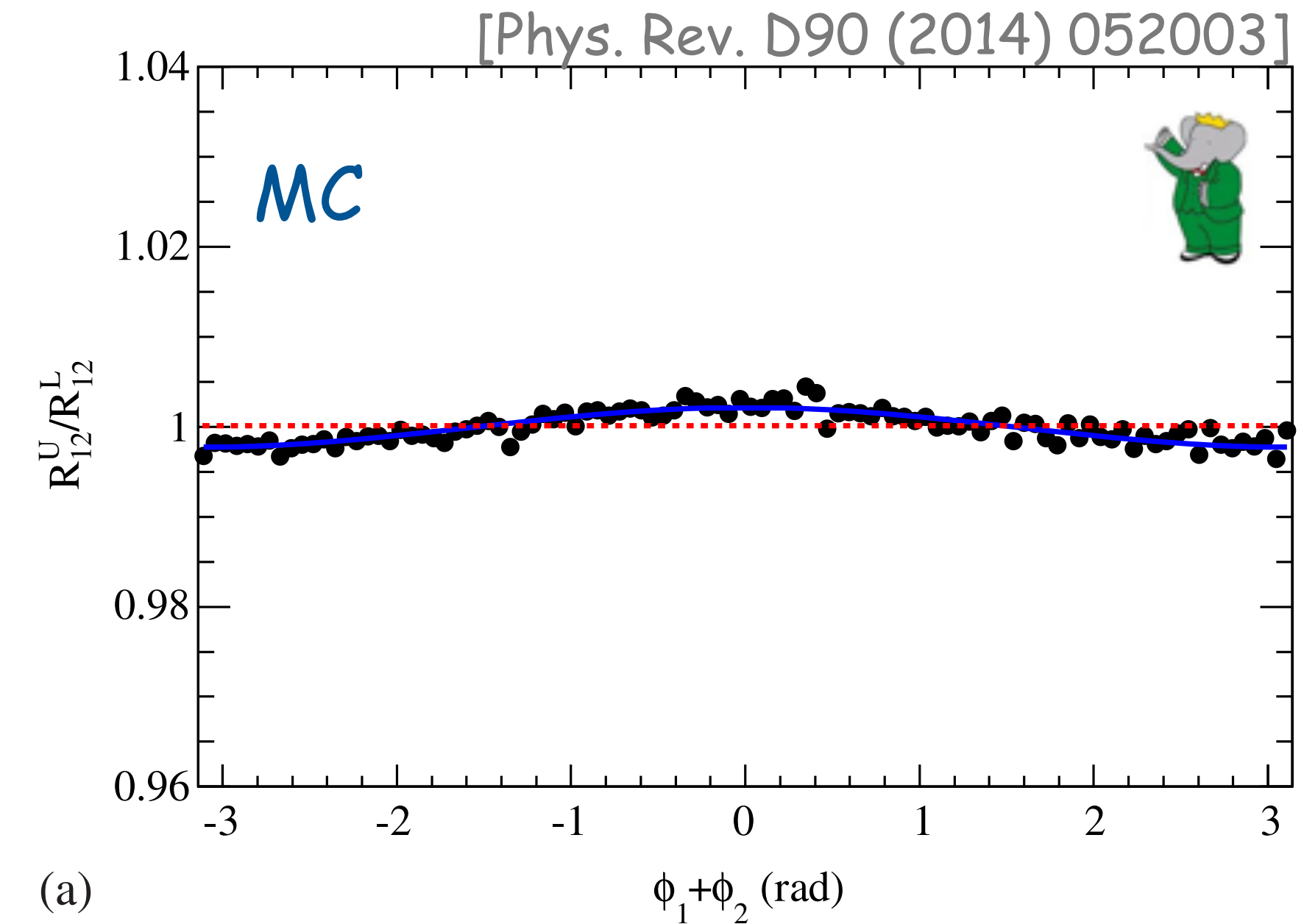


# hadron pairs: angular correlations

- challenge: large modulations even without Collins effect (e.g., in PYTHIA MC)
- construct double ratio of normalized-yield distributions  $R_{12}$ , e.g. unlike-/like-sign:

$$\begin{aligned} \frac{R_{12}^U}{R_{12}^L} &\simeq \frac{1 + \left\langle \frac{\sin^2 \theta_{\text{th}}}{1 + \cos^2 \theta_{\text{th}}} \right\rangle G^U \cos(\phi_1 + \phi_2)}{1 + \left\langle \frac{\sin^2 \theta_{\text{th}}}{1 + \cos^2 \theta_{\text{th}}} \right\rangle G^L \cos(\phi_1 + \phi_2)} \\ &\simeq 1 + \left\langle \frac{\sin^2 \theta_{\text{th}}}{1 + \cos^2 \theta_{\text{th}}} \right\rangle \{G^U - G^L\} \cos(\phi_1 + \phi_2) \end{aligned}$$

- suppresses flavor-independent sources of modulations
- $G^{U/L}$ : specific combinations of FFs
- remaining MC asymmetries  $\Rightarrow$  systematics

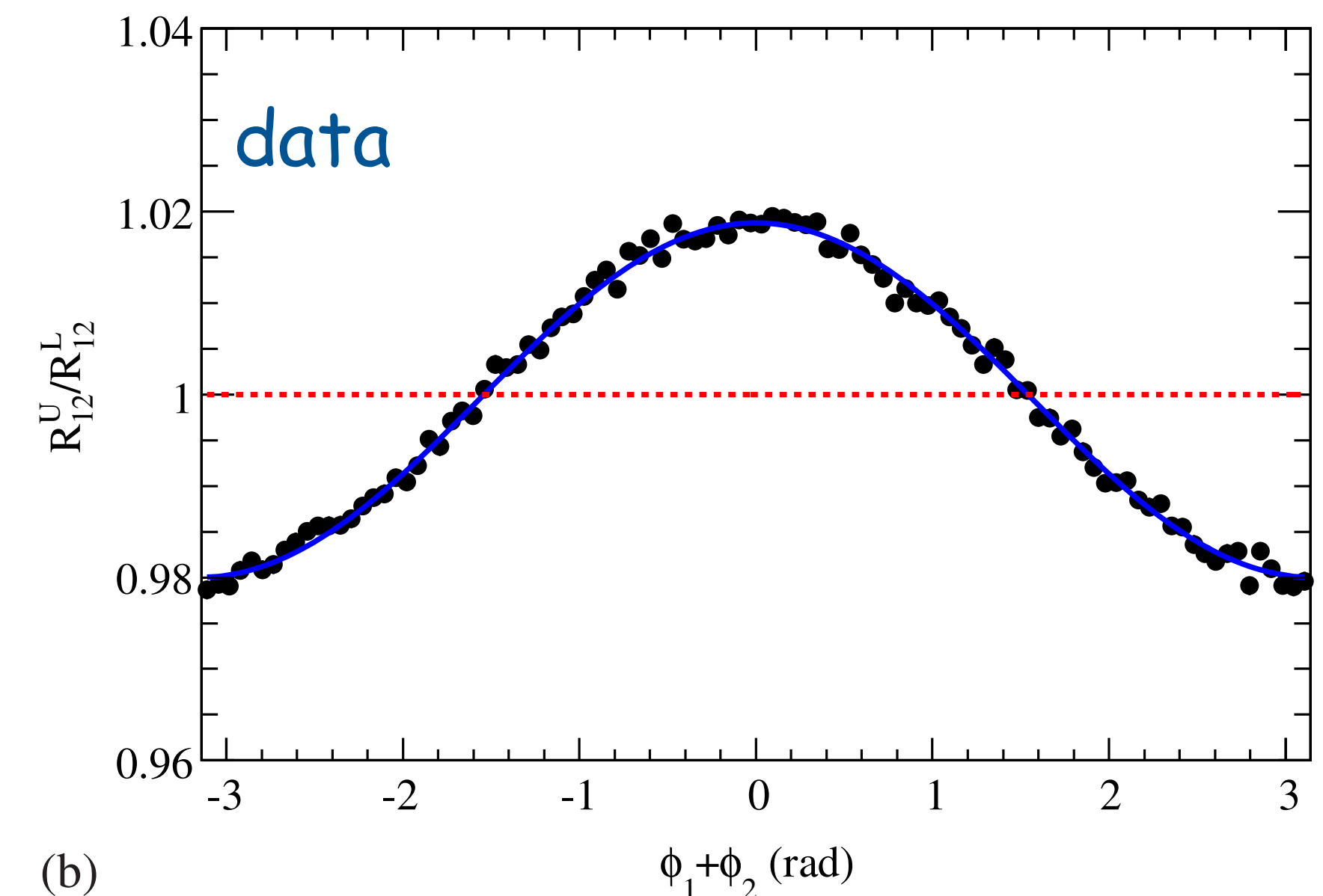
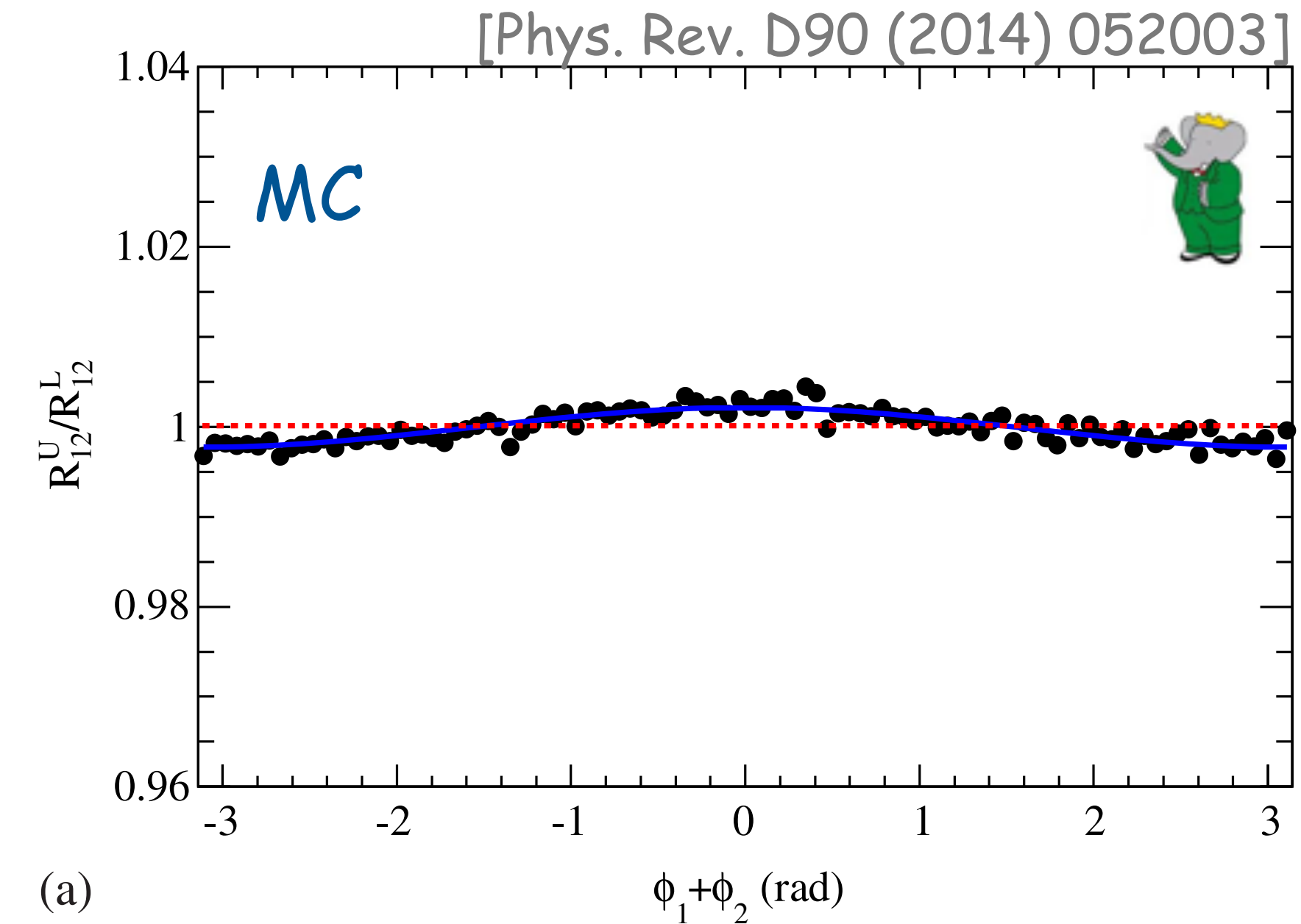


# hadron pairs: angular correlations

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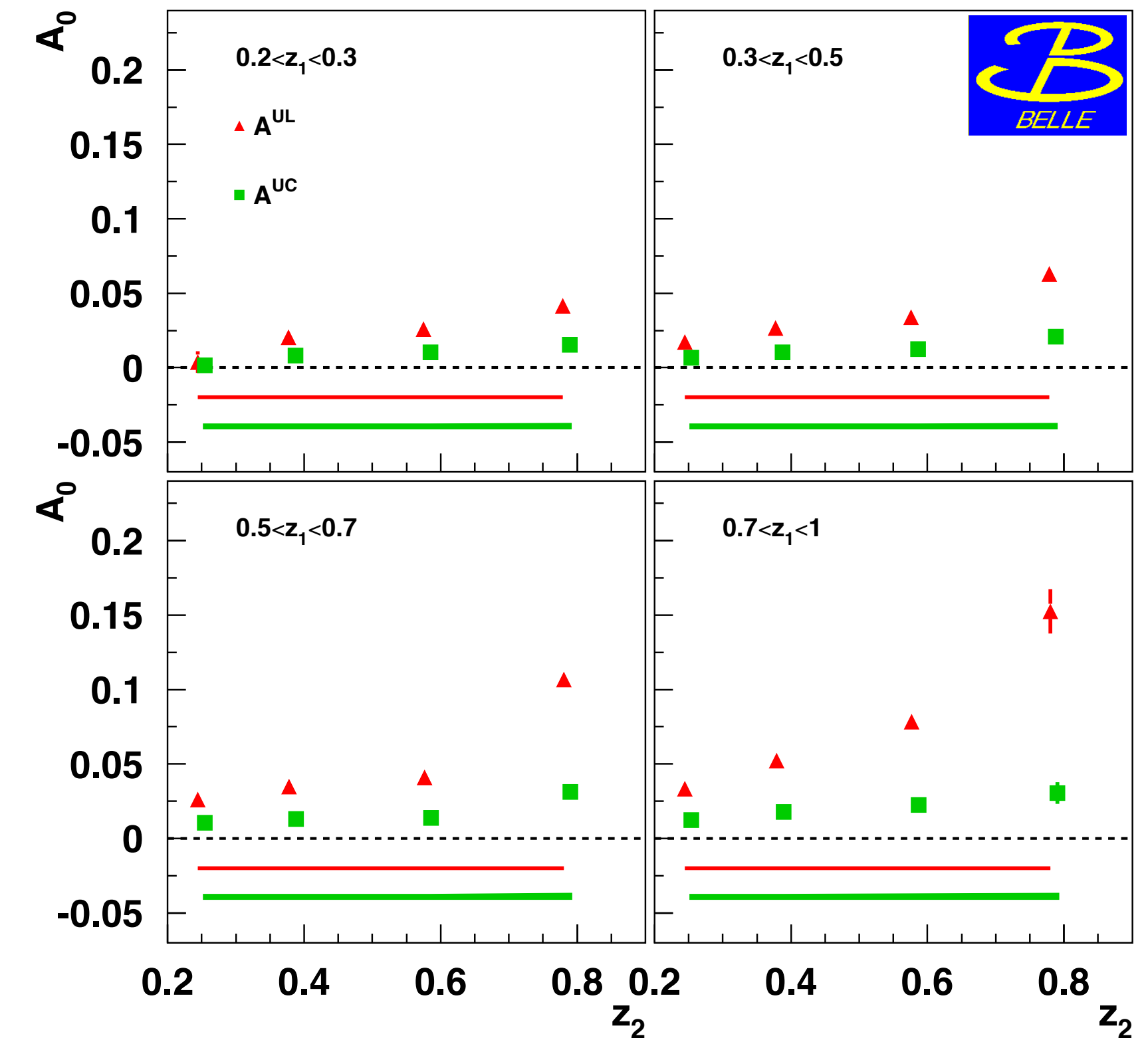
$$\begin{aligned} \frac{R_{12}^U}{R_{12}^L} &\simeq \frac{1 + \left\langle \frac{\sin^2 \theta_{\text{th}}}{1 + \cos^2 \theta_{\text{th}}} \right\rangle G^U \cos(\phi_1 + \phi_2)}{1 + \left\langle \frac{\sin^2 \theta_{\text{th}}}{1 + \cos^2 \theta_{\text{th}}} \right\rangle G^L \cos(\phi_1 + \phi_2)} \\ &\simeq 1 + \left\langle \frac{\sin^2 \theta_{\text{th}}}{1 + \cos^2 \theta_{\text{th}}} \right\rangle \{G^U - G^L\} \cos(\phi_1 + \phi_2) \end{aligned}$$

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# Collins asymmetries (RF0)

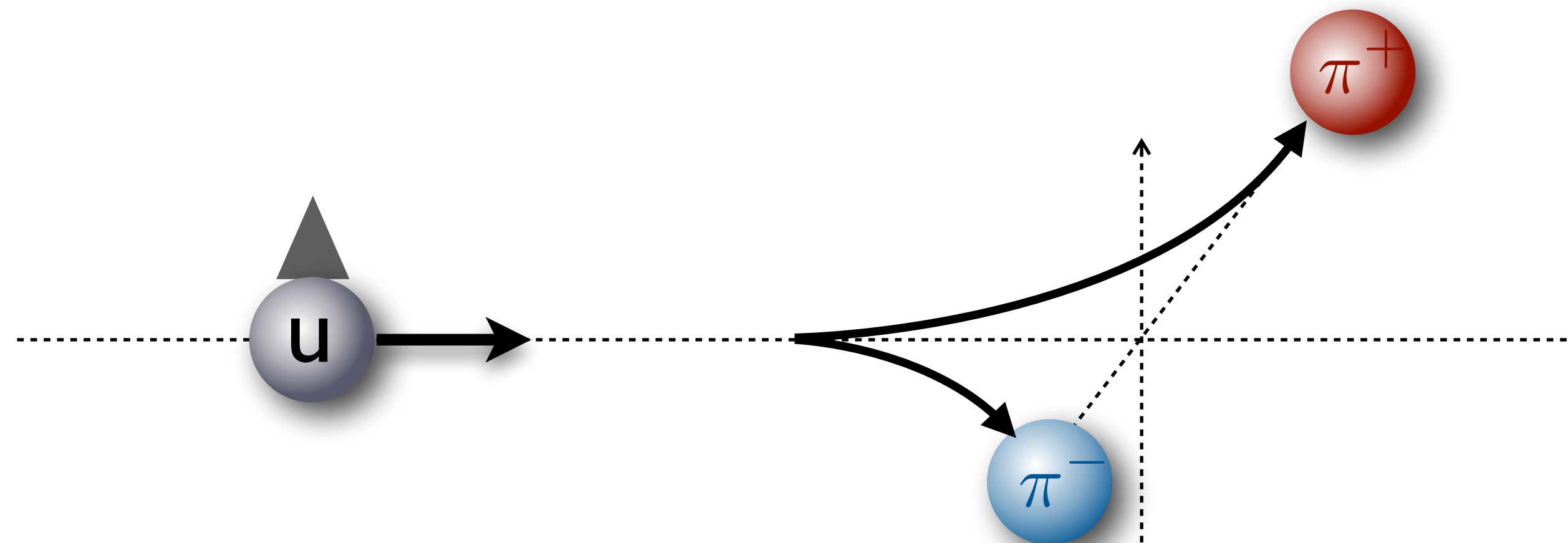
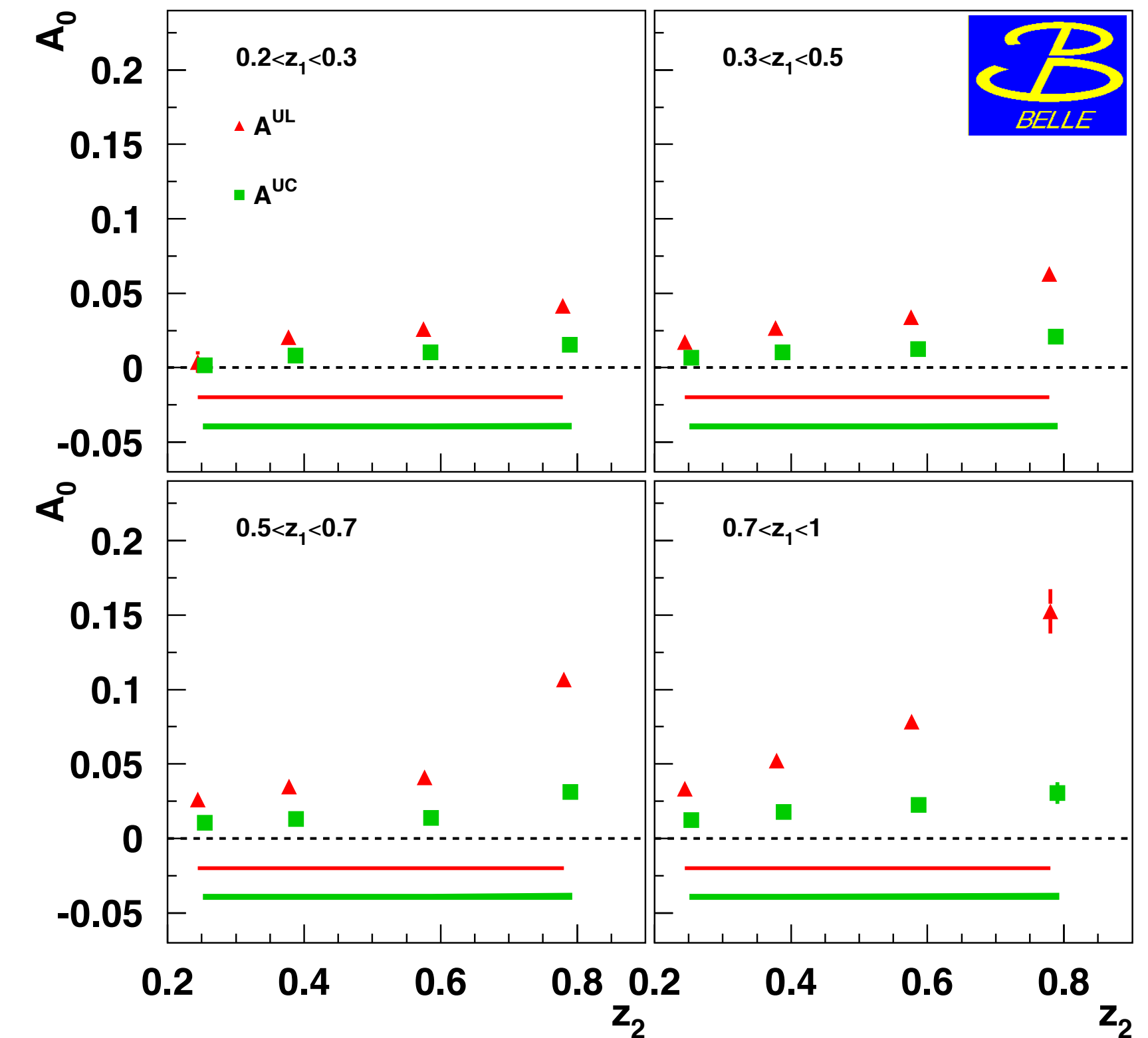
- first measurement of Collins asymmetries by Belle [PRL 96 (2006) 232002, PRD 78 (2008) 032011, PRD 86 (2012) 039905(E)]
- significant asymmetries rising with  $z$
- used for first transversity and Collins FF extractions

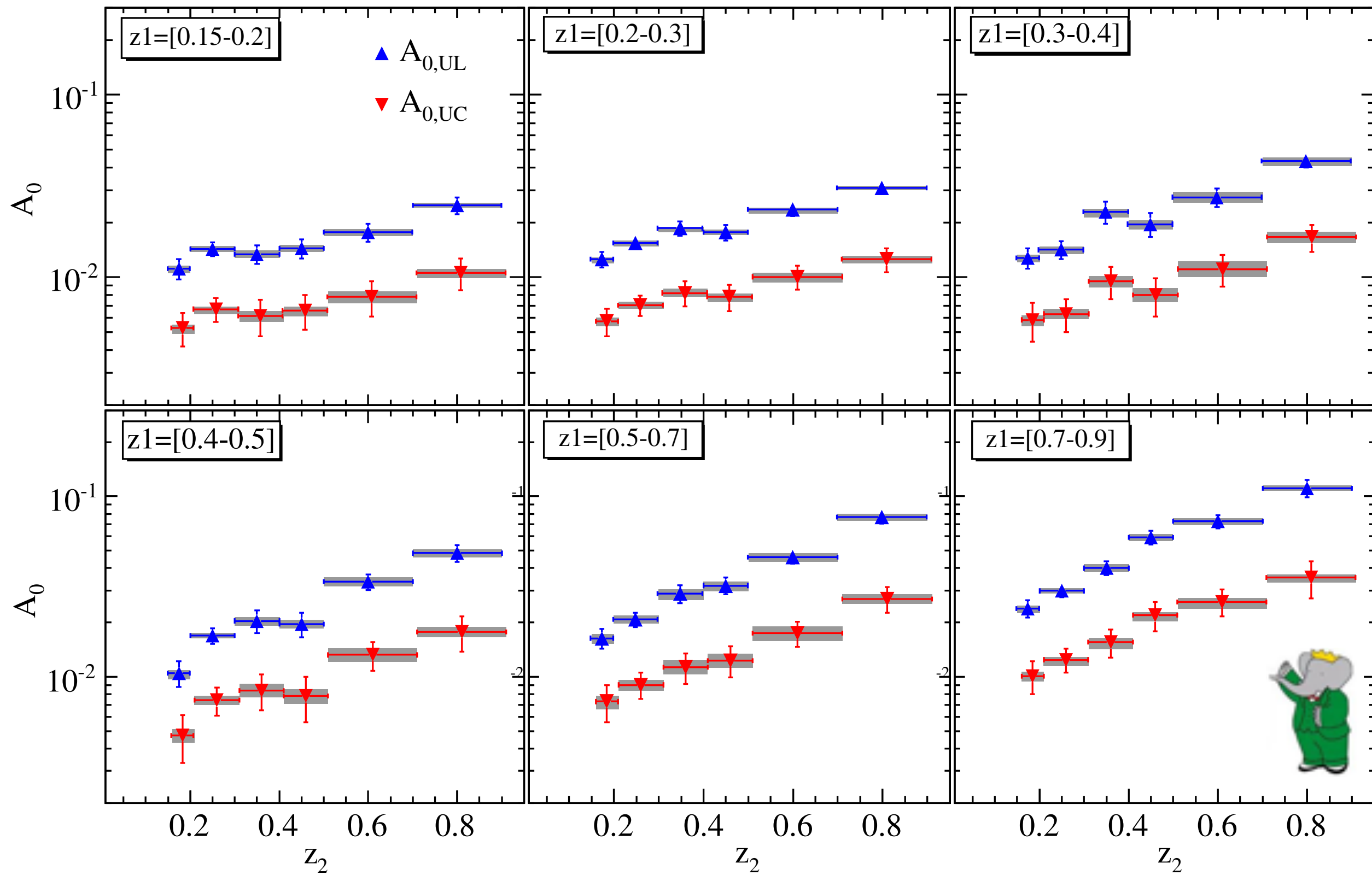




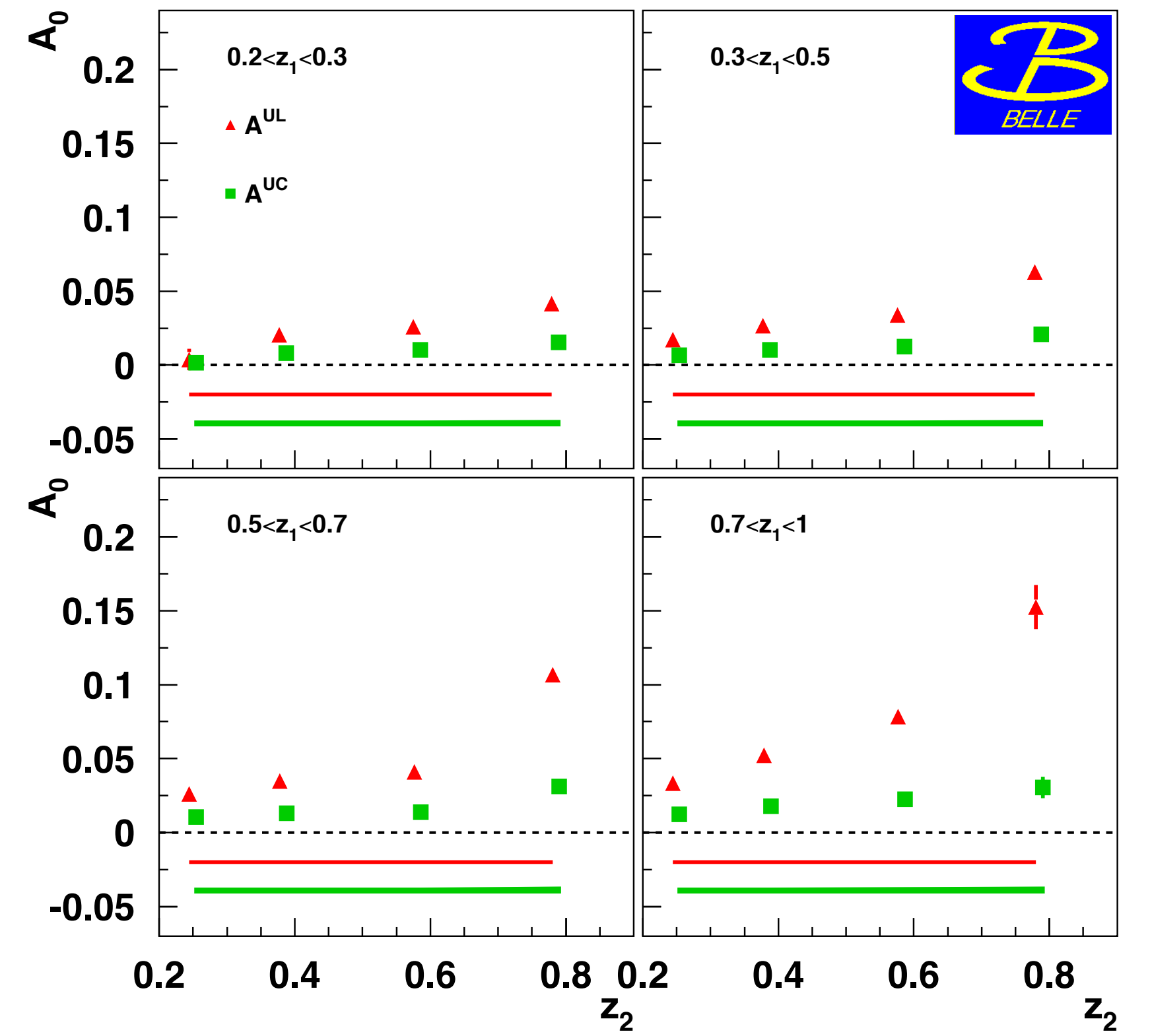
# Collins asymmetries (RF0)

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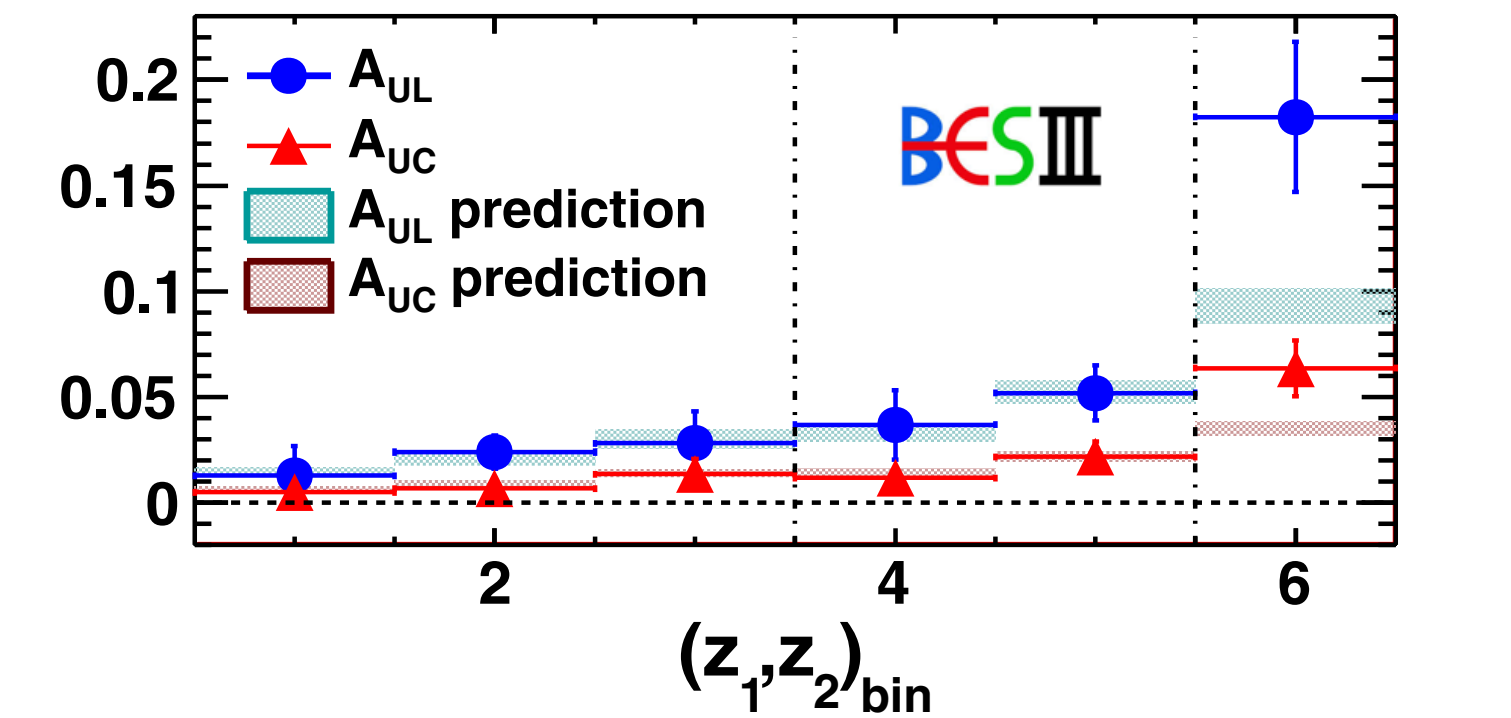
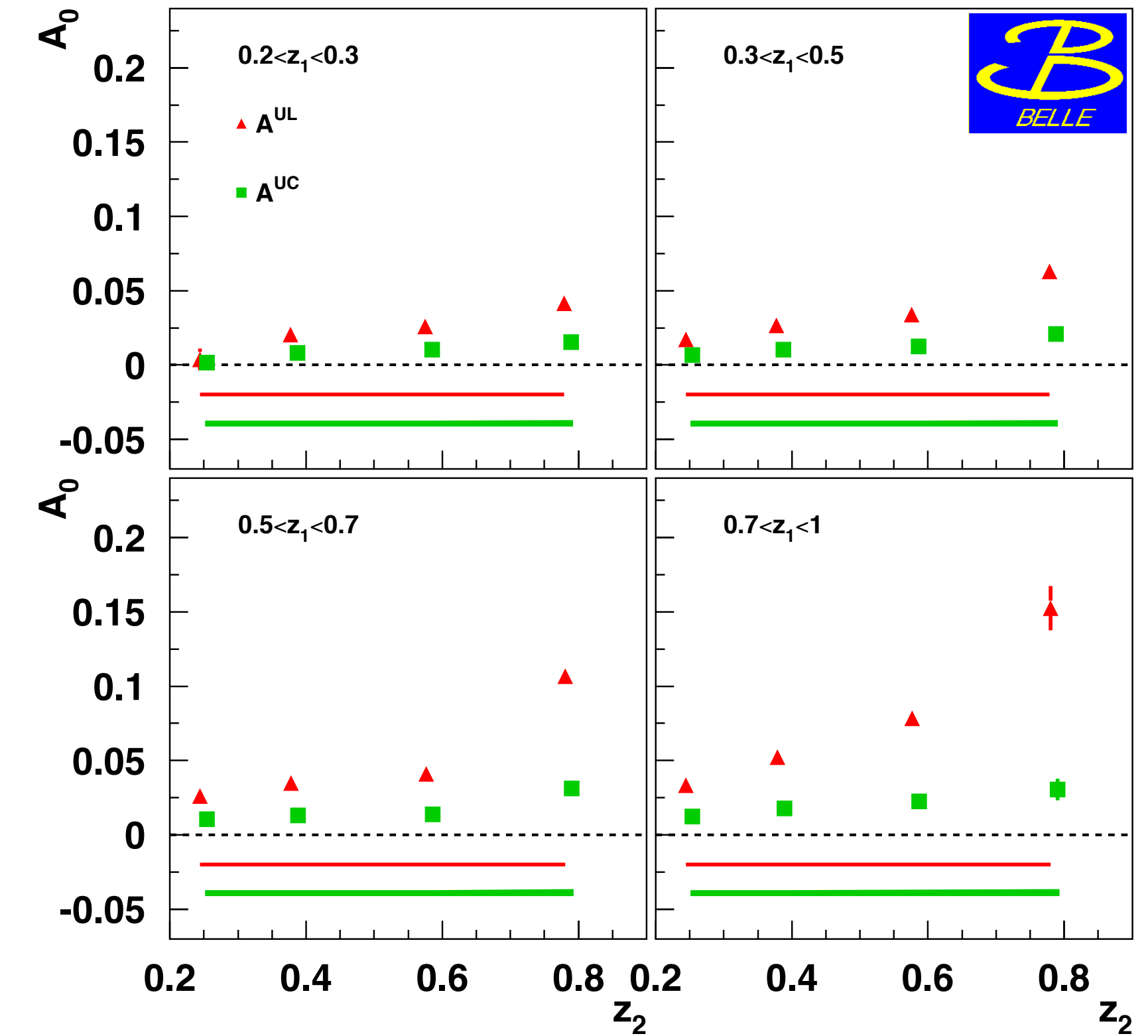
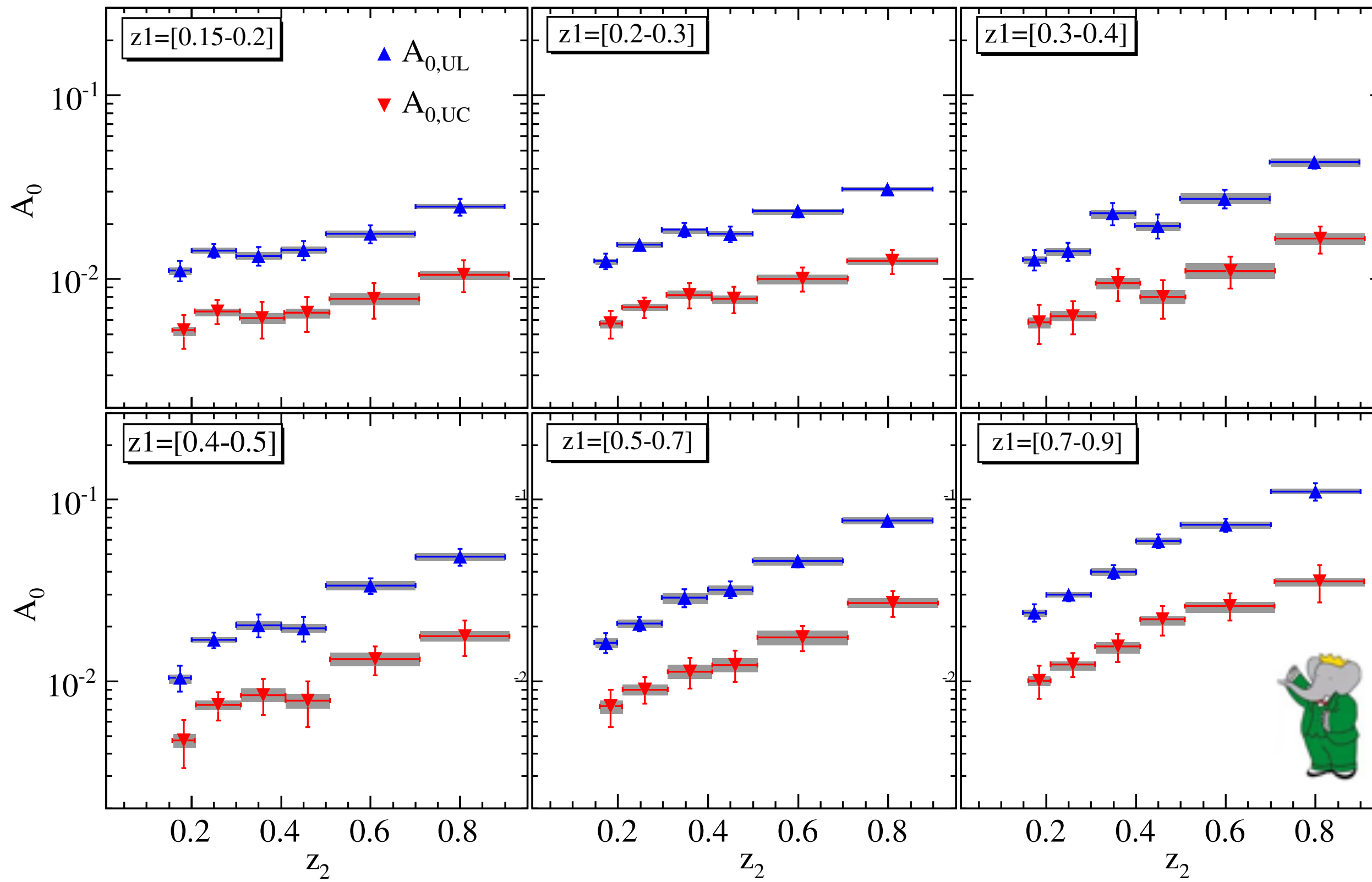
# Collins asymmetries (RF0)



- BaBar results [PRD 90 (2014) 052003] consistent with Belle

# Collins asymmetries (RFO)

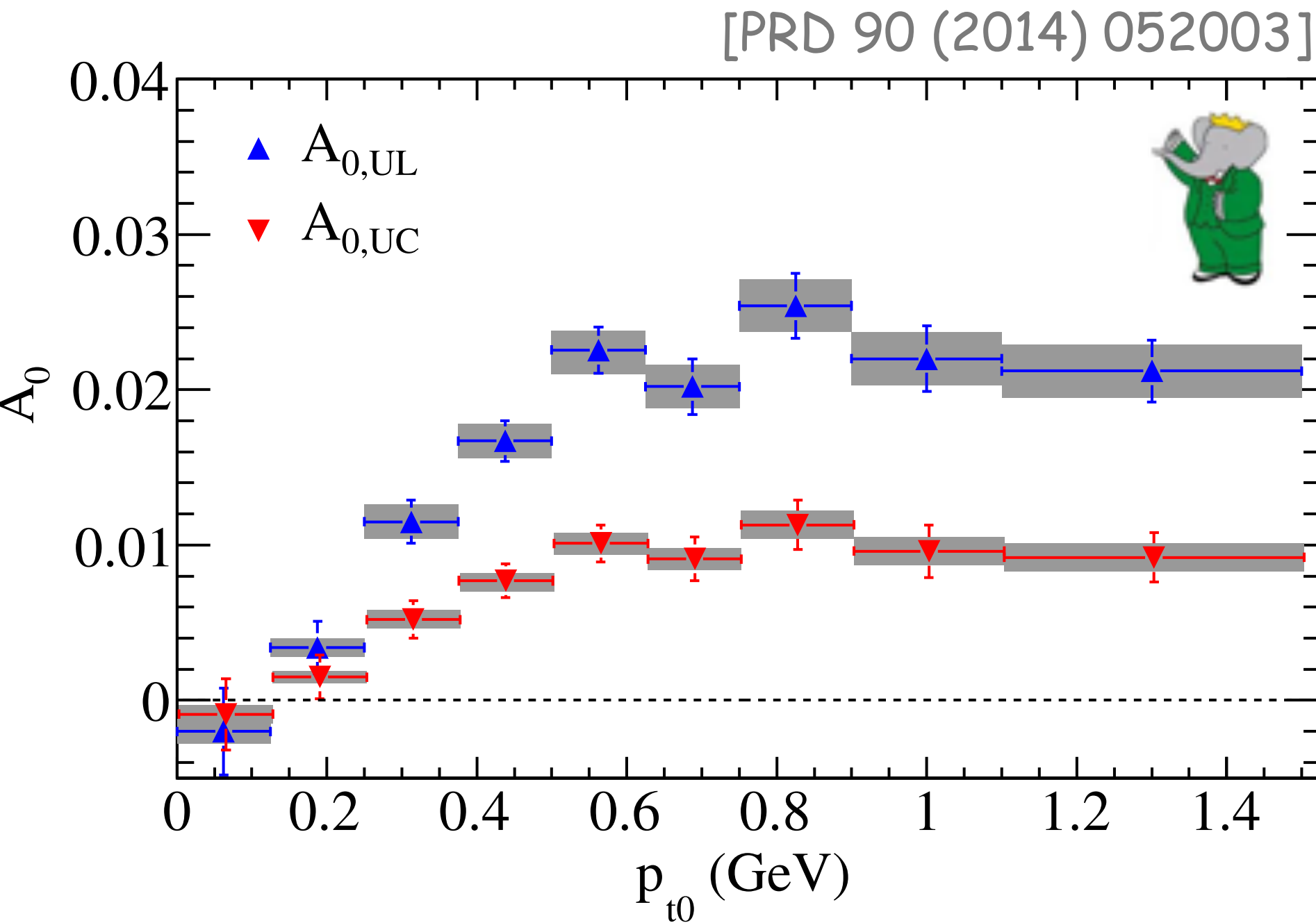
[Phys. Rev. D90 (2014) 052003]



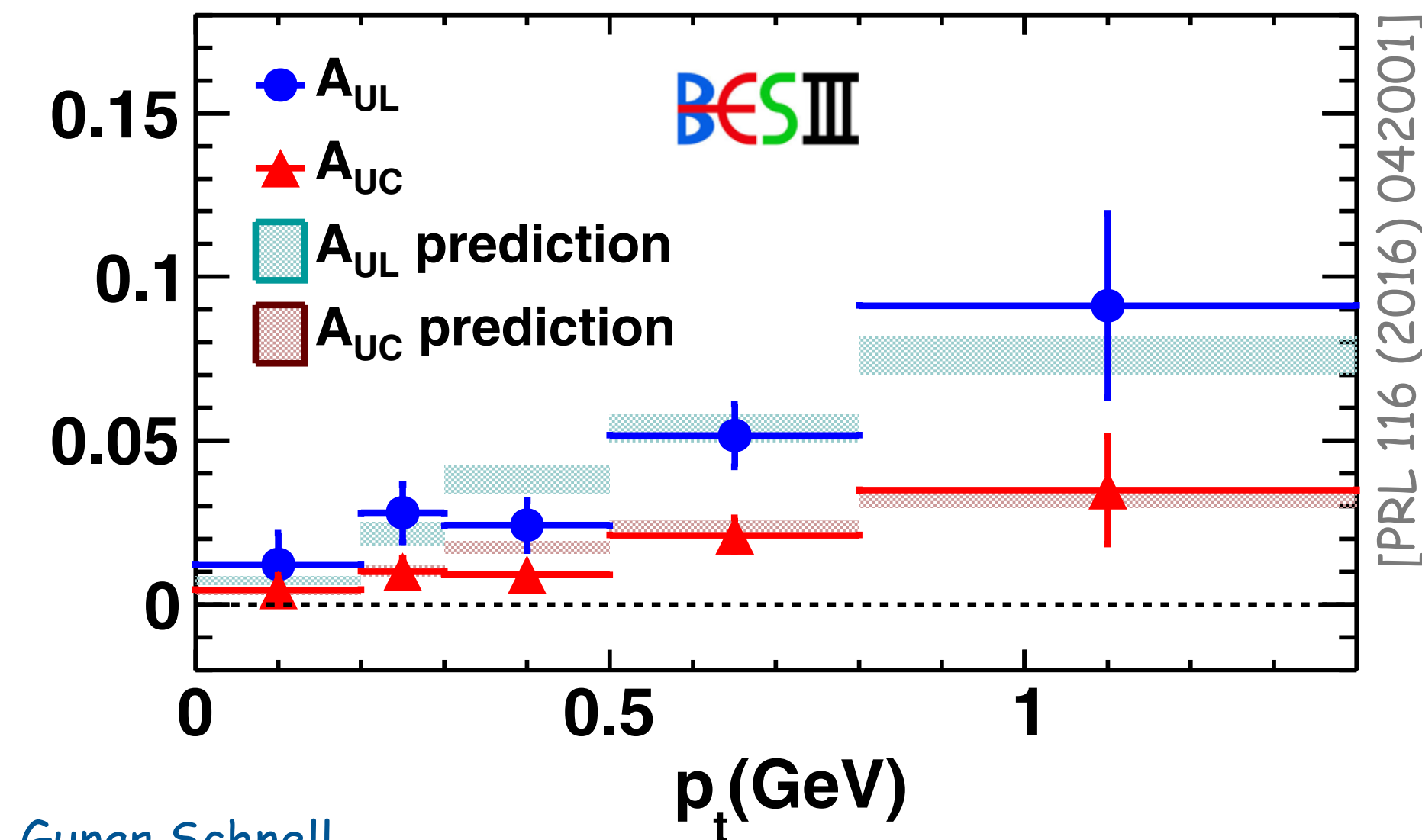
- BaBar results [PRD 90 (2014) 052003] consistent with Belle
- BESIII [PRL 116 (2016) 042001] (at smaller  $s$ ) consistent with TMD evolution [Kang et al., PRD 93 (2016) 014009]



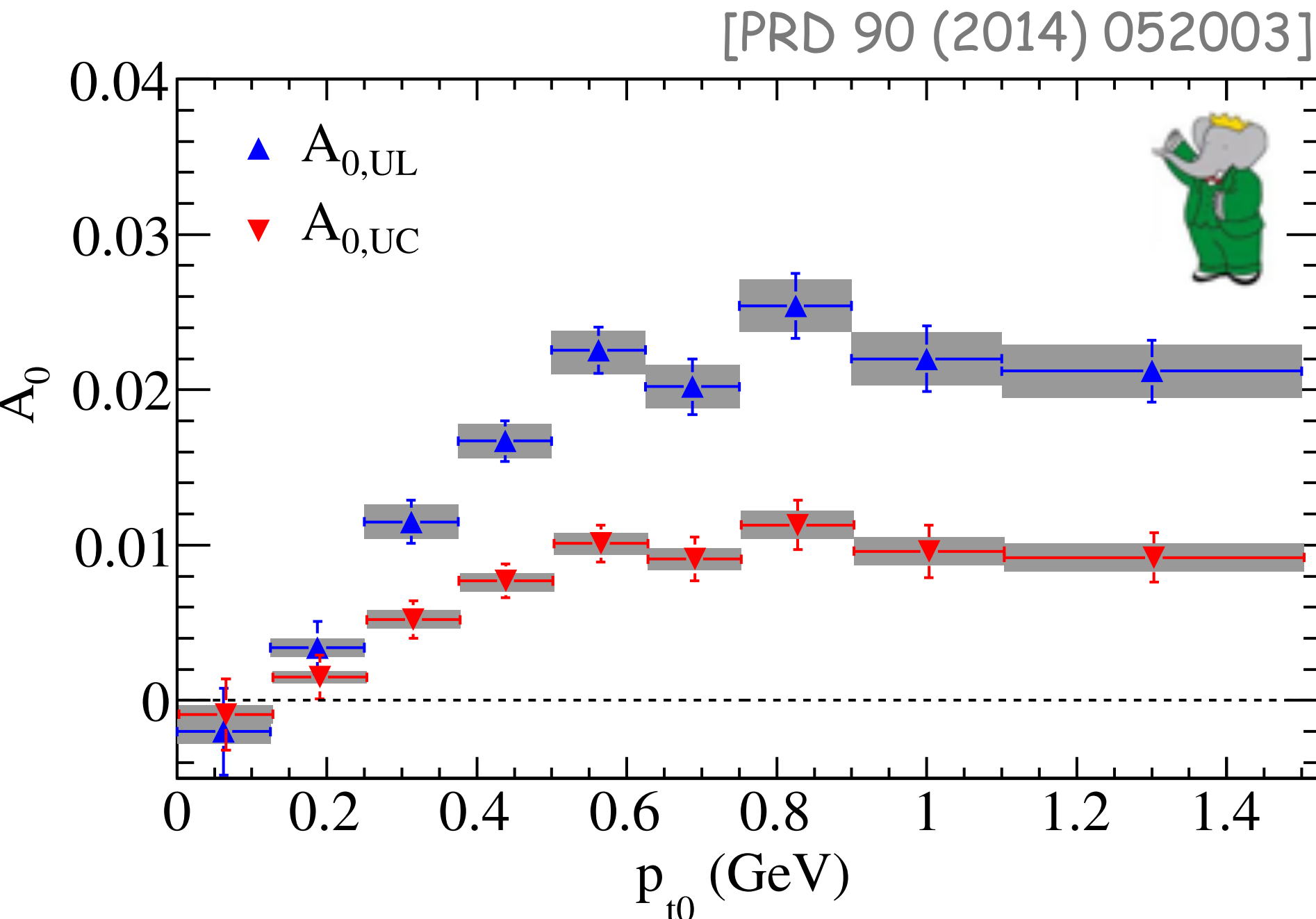
# Collins asymmetries - going further



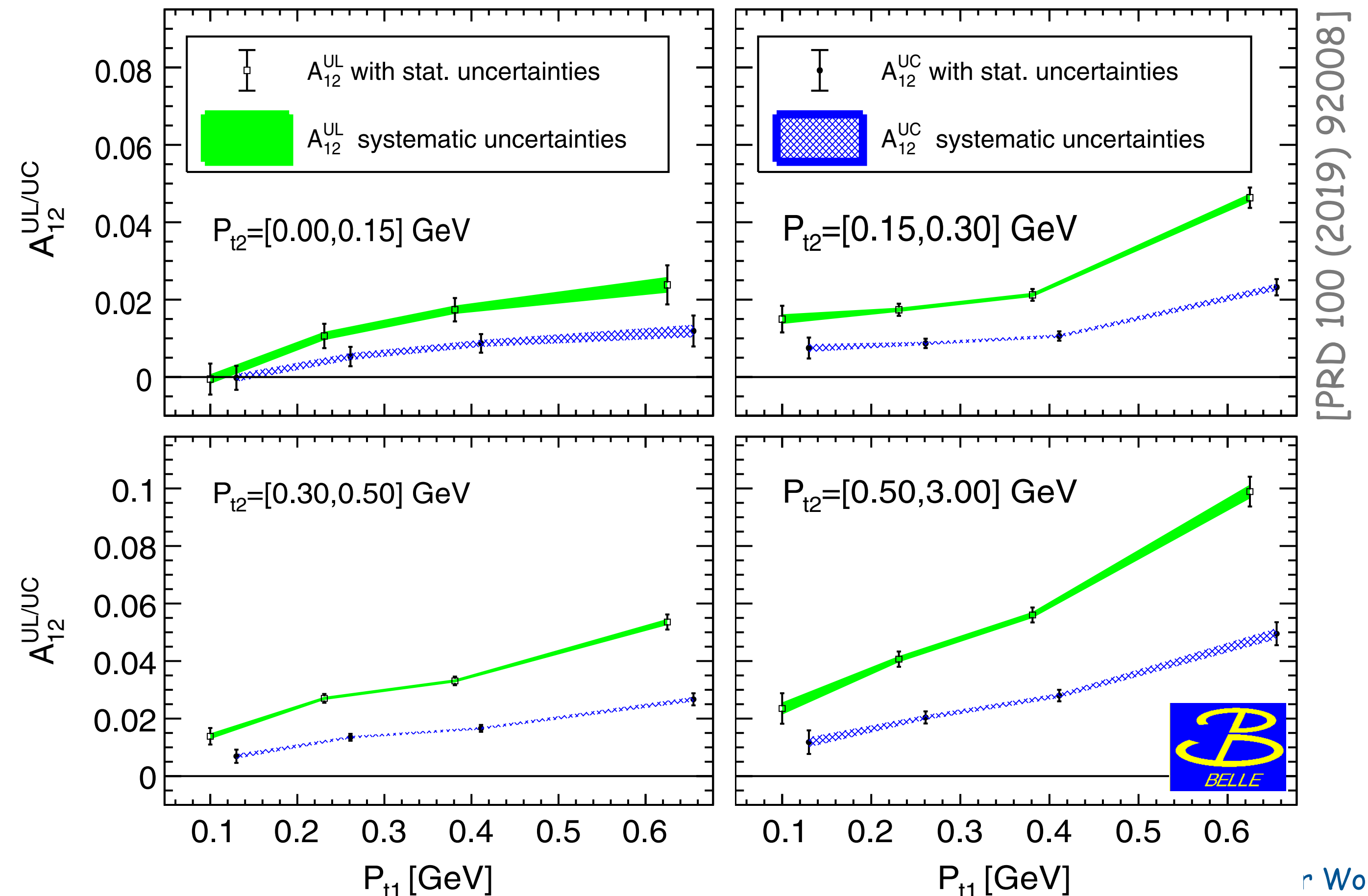
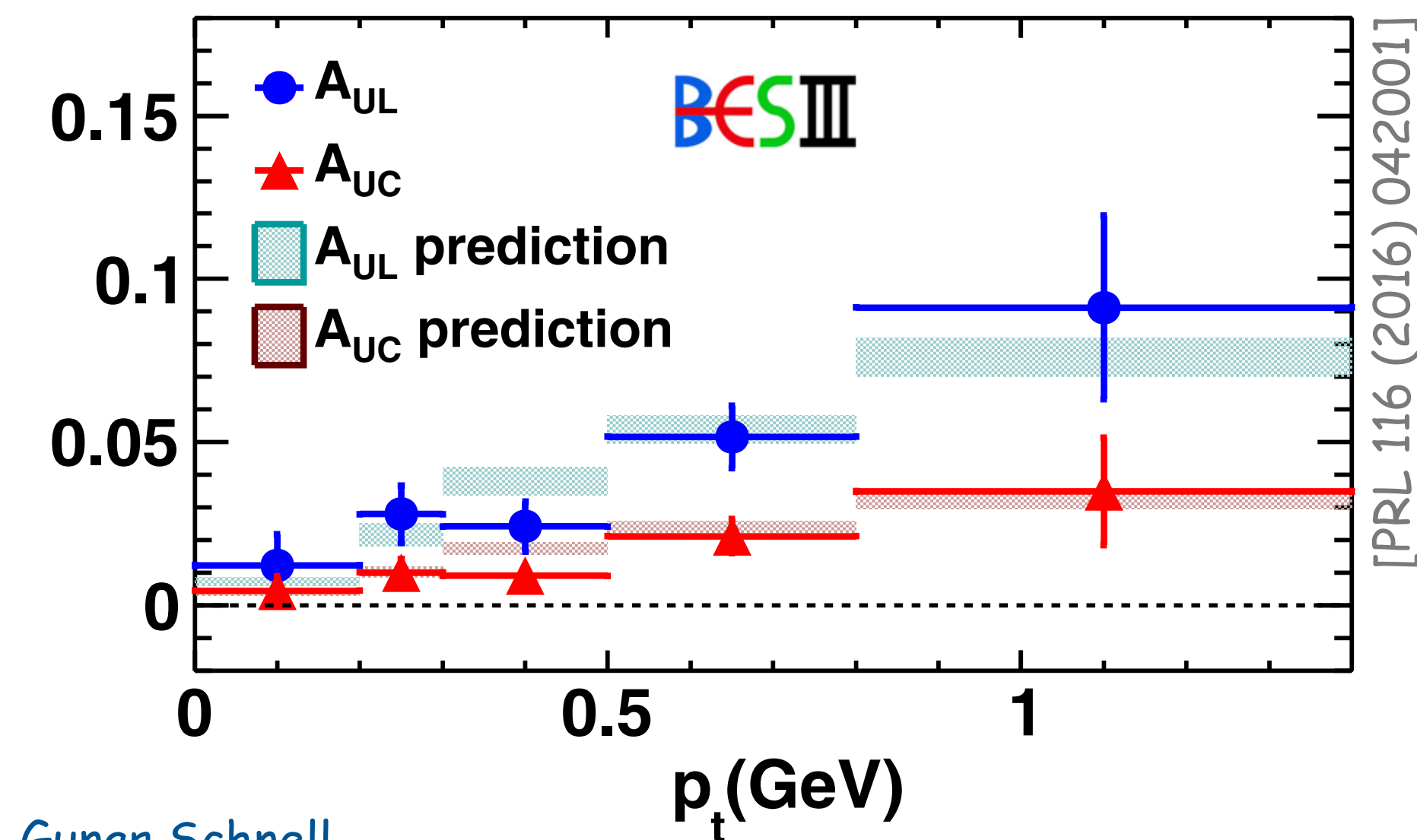
- $p_T$  dependence for charged pions from BaBar & BESIII
- typical rise with  $p_T$ ; turnover around 0.8 GeV



# Collins asymmetries - going further



- $p_T$  dependence for charged pions from BaBar & BESIII
- typical rise with  $p_T$ ; turnover around 0.8 GeV
- ... now also from Belle in R12 frame:



# Collins asymmetries - going further

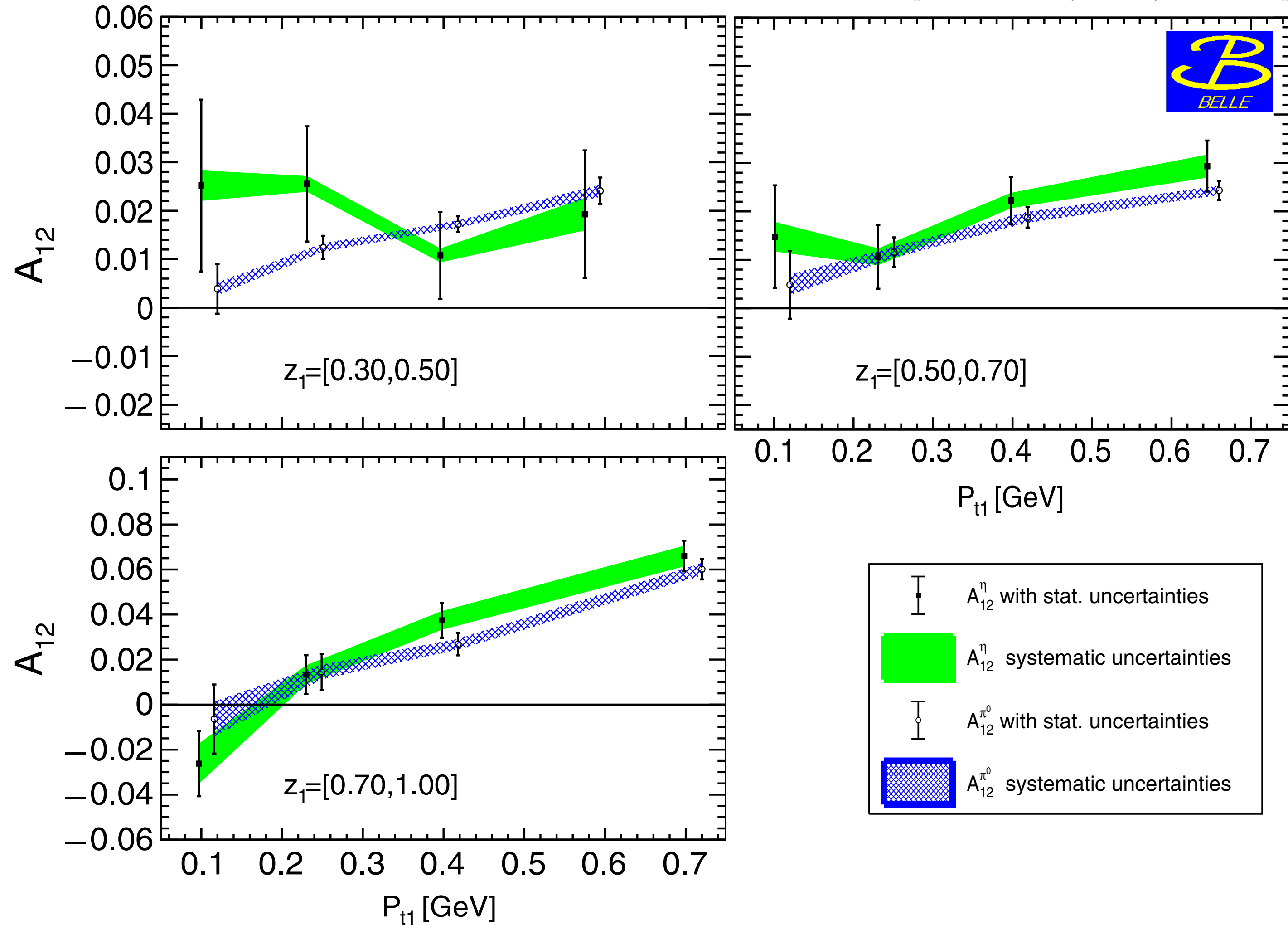
- ... as well as for neutral pion and eta

$$R_{12}^{\pi^0} = \frac{R_{12}^{0\pm}}{R_{12}^L} = \frac{\pi^0\pi^+ + \pi^0\pi^-}{\pi^+\pi^+ + \pi^-\pi^-}$$

$$R_{12}^{\eta} = \frac{R_{12}^{\eta\pm}}{R_{12}^L} = \frac{\eta\pi^+ + \eta\pi^-}{\pi^+\pi^+ + \pi^-\pi^-}$$

- no significant differences observed

[PRD 100 (2019) 92008]





# Collins asymmetries - going further

$$R_{12}^{\pi^0} = \frac{R_{12}^{0\pm}}{R_{12}^L} \approx 1 + \cos(\phi_{12}) \frac{\sin^2(\theta)}{1 + \cos^2(\theta)}$$

$$\times \left\{ \frac{5(H_1^{\perp, fav} + H_1^{\perp, dis}) \otimes (H_1^{\perp, fav} + H_1^{\perp, dis}) + 4H_{1, s \rightarrow \pi}^{\perp, dis} \otimes H_{1, s \rightarrow \pi}^{\perp, dis}}{5(D_1^{fav} + D_1^{dis}) \otimes (D_1^{fav} + D_1^{dis}) + 4D_{1, s \rightarrow \pi}^{dis} \otimes D_{1, s \rightarrow \pi}^{dis}} \right.$$

$$\left. - \frac{5(H_1^{\perp, fav} \otimes H_1^{\perp, dis} + H_1^{\perp, dis} \otimes H_1^{\perp, fav}) + 2H_{1, s \rightarrow \pi}^{\perp, dis} H_{1, s \rightarrow \pi}^{\perp, dis}}{5(D_1^{fav} \otimes D_1^{dis} + D_1^{dis} \otimes D_1^{fav}) + 2D_{1, s \rightarrow \pi}^{dis} \otimes D_{1, s \rightarrow \pi}^{dis}} \right\}.$$

isospin  
=  $A_{12}^{UL} - A_{12}^{UC}$

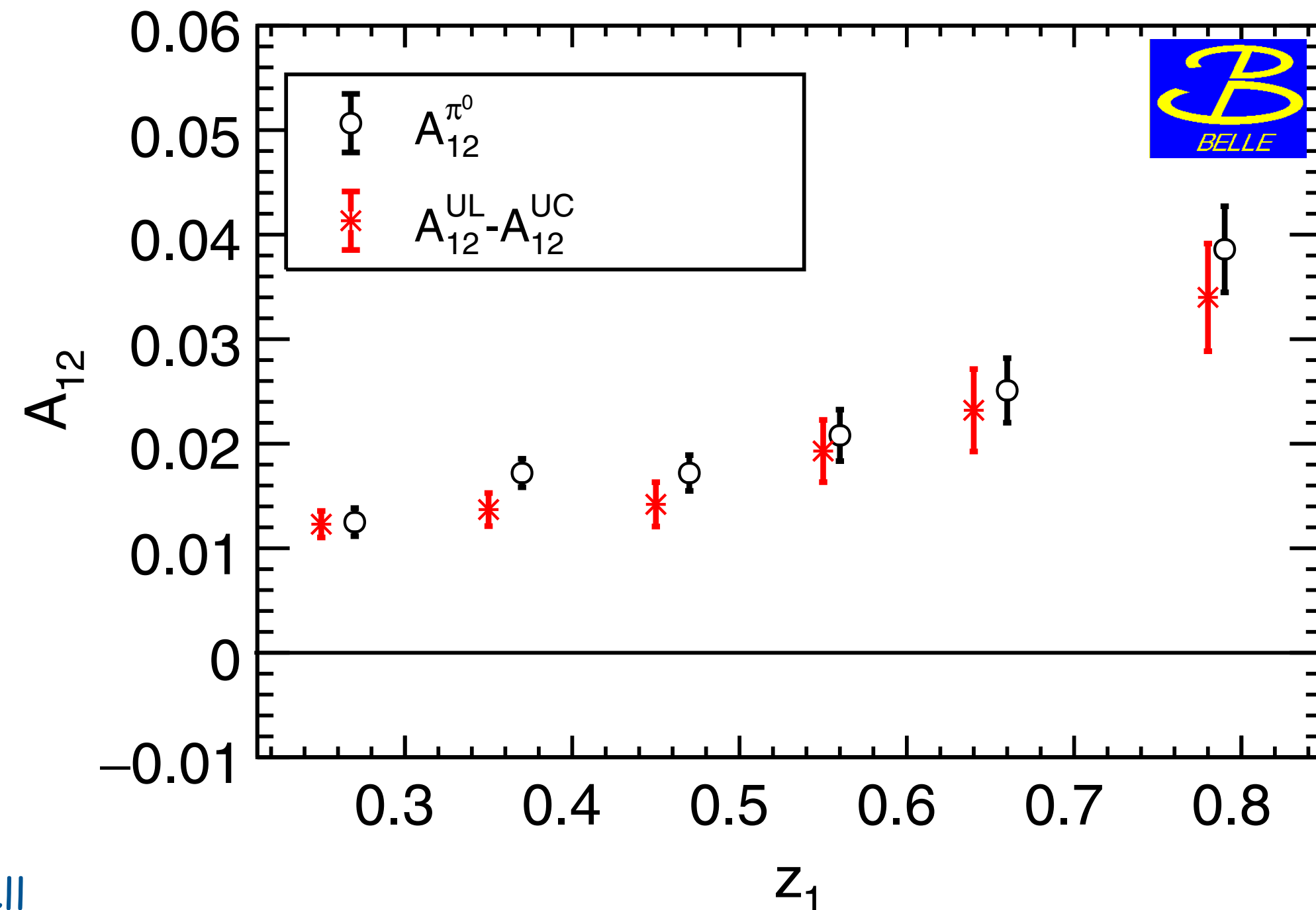
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isospin  
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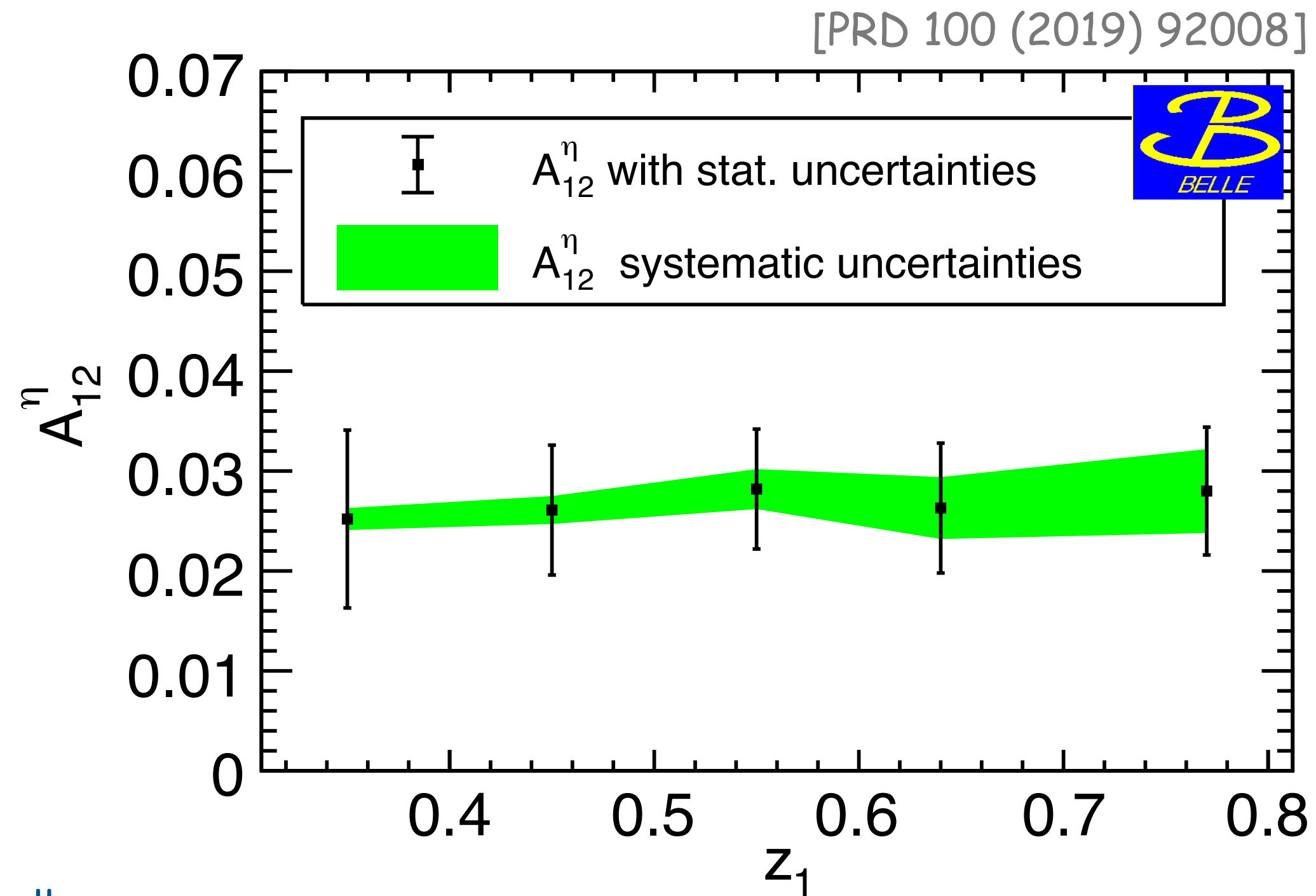
- consistency between neutral and charged pions
- typical rise with  $z$  also seen for neutral pions

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} isospin  $\underline{=}$   $A_{12}^{UL} - A_{12}^{UC}$



- consistency between neutral and charged pions
- typical rise with  $z$  also seen for neutral pions
- ... while basically flat for eta



# Collins asymmetries - going further

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- non-zero  $\pi^0$  or  $\eta$  results **not** direct sign of non-zero  $\pi^0$  or  $\eta$  Collins FFs

# Collins asymmetries - going further

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- non-zero  $\pi^0$  or  $\eta$  results **not** direct sign of non-zero  $\pi^0$  or  $\eta$  Collins FFs
- double ratio dominated by terms involving charged-pion yields

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 contribution from  $\pi^0$  or  $\eta$   
 contribution from charged pions

- non-zero  $\pi^0$  or  $\eta$  results **not** direct sign of non-zero  $\pi^0$  or  $\eta$  Collins FFs
- double ratio dominated by terms involving charged-pion yields
- only numerator of first term related to  $\pi^0$  or  $\eta$





# Collins asymmetries - going further

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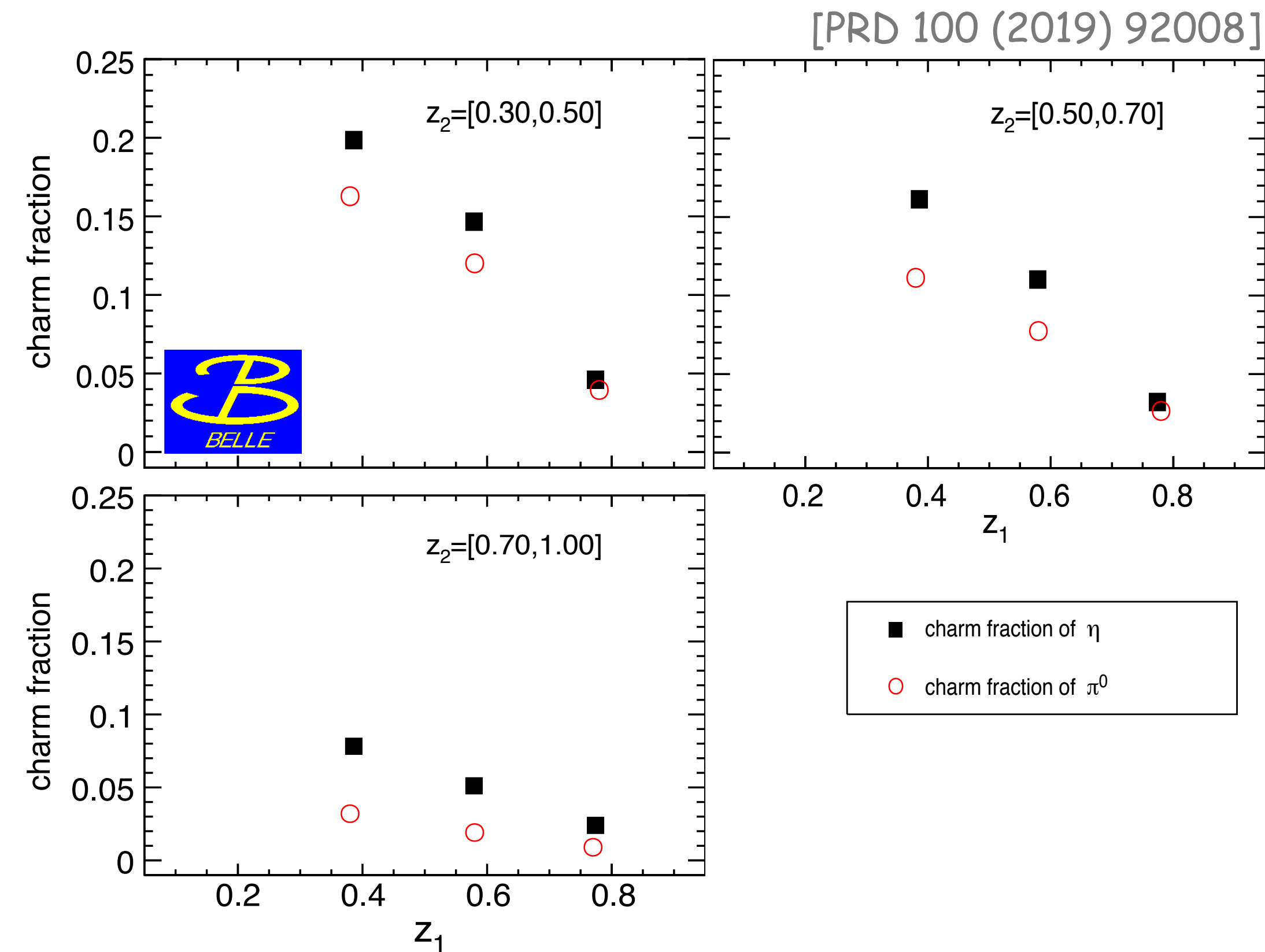
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- double ratio dominated by terms involving charged-pion yields
- only numerator of first term related to  $\pi^0$  or  $\eta$
- non-zero results could, in principle, arise entirely from charged-pion Collins FFs

# Collins asymmetries - going further

- qualitative changes in 2019 Belle analysis w.r.t. previous Belle analyses:
  - no correction to  $q\bar{q}$  axis;
    - ⇒ rather to thrust axis, which is observable
  - upper limit on opening angle imposed
  - no correction for charm contribution;
    - ⇒ provide charm fraction

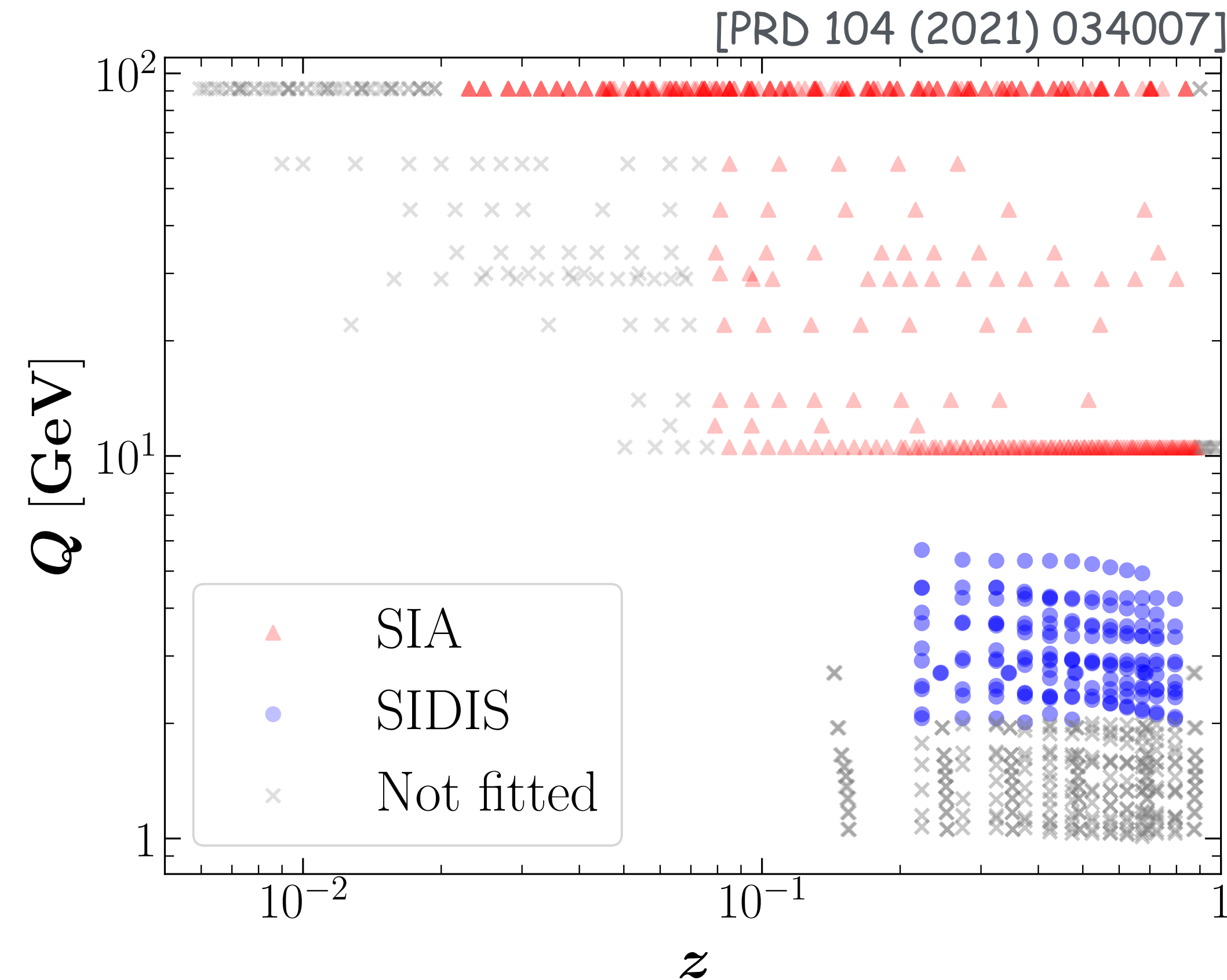


# the future

- several analyses still in the pipeline, e.g.,
  - $k_T$ -dependent  $D_1$  FFs (back-to-back hadrons)  
(Belle, BESIII & possibly BaBar) 
  - Collins asymmetries:
    - pion update w/ increased statistics (BESIII)
    - kaon & pion-kaon pairs;  $k_T$  dependence of Collins asymmetries (Belle, BESIII)
    - Collins asymmetries w/o double ratios (BaBar)
  - single-hadron production
    - short-lived mesons and resonances (Belle)
    - charged pions and kaon at lower  $s$  (BESIII)

# the future

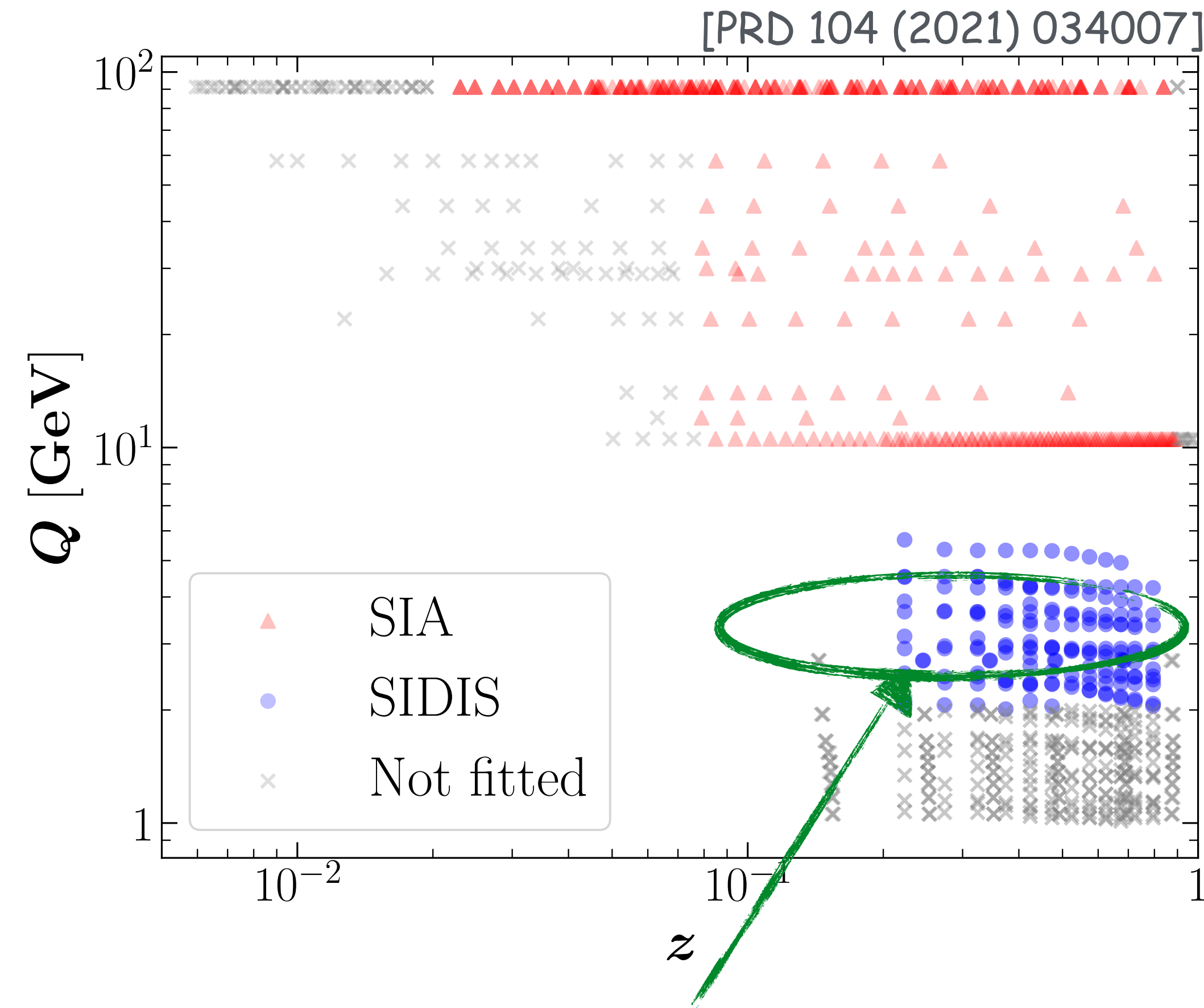
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    - charged pions and kaon at lower  $s$  (BESIII)  $\sim 62\text{pb}^{-1}$  @3.52 GeV used for Collins asym's

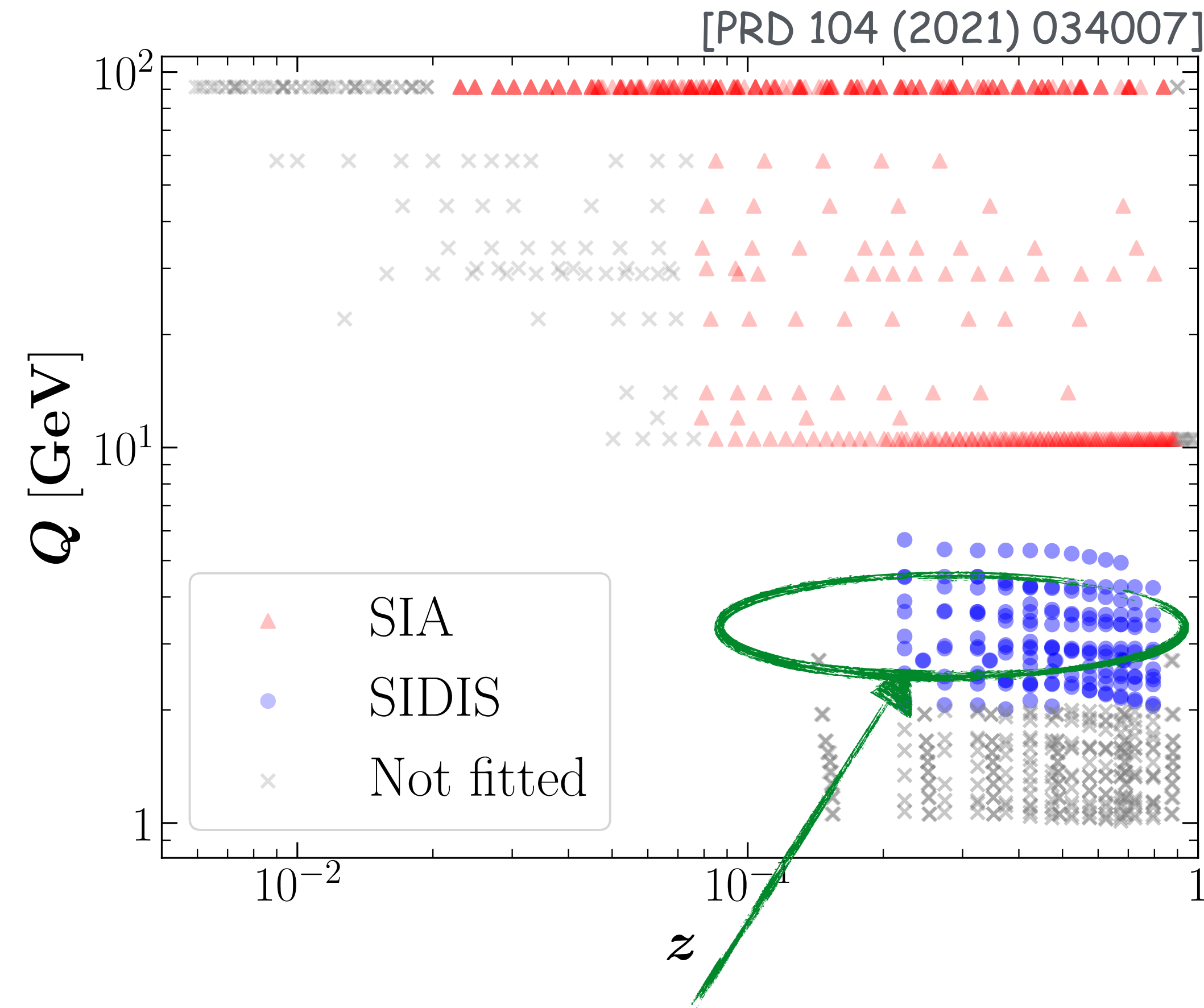


BESIII region

aim at  $250\text{pb}^{-1}$  data set

# the future

- several analyses still in the pipeline, e.g.,
  - $k_T$ -dependent  $D_1$  FFs (back-to-back hadrons) (Belle, BESIII & possibly BaBar) 👉 Charlotte
  - Collins asymmetries:
    - pion update w/ increased statistics (BESIII)
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    - Collins asymmetries w/o double ratios (BaBar)
  - single-hadron production
    - short-lived mesons and resonances (Belle)
    - charged pions and kaon at lower  $s$  (BESIII)
- new data from Belle II



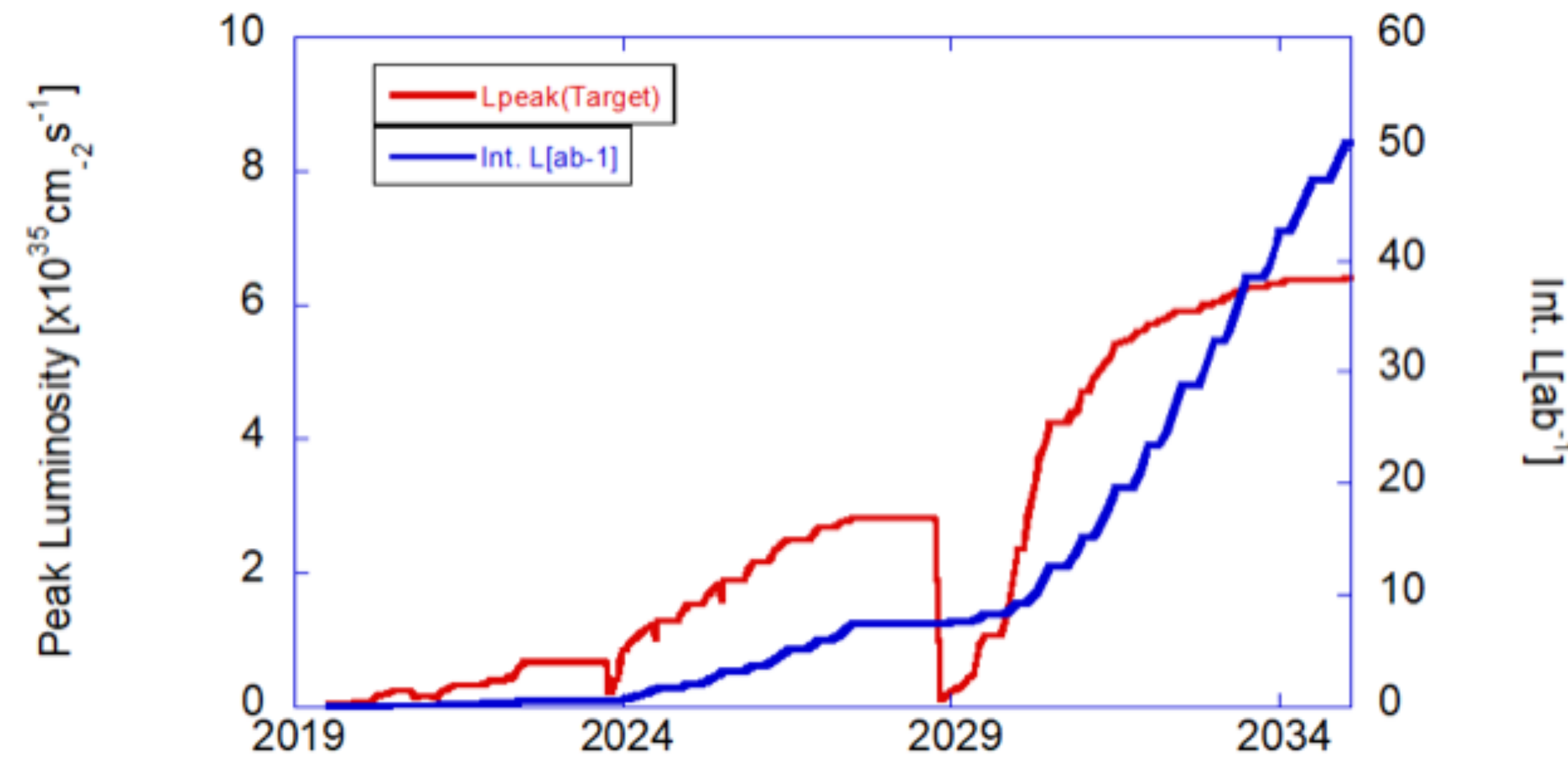
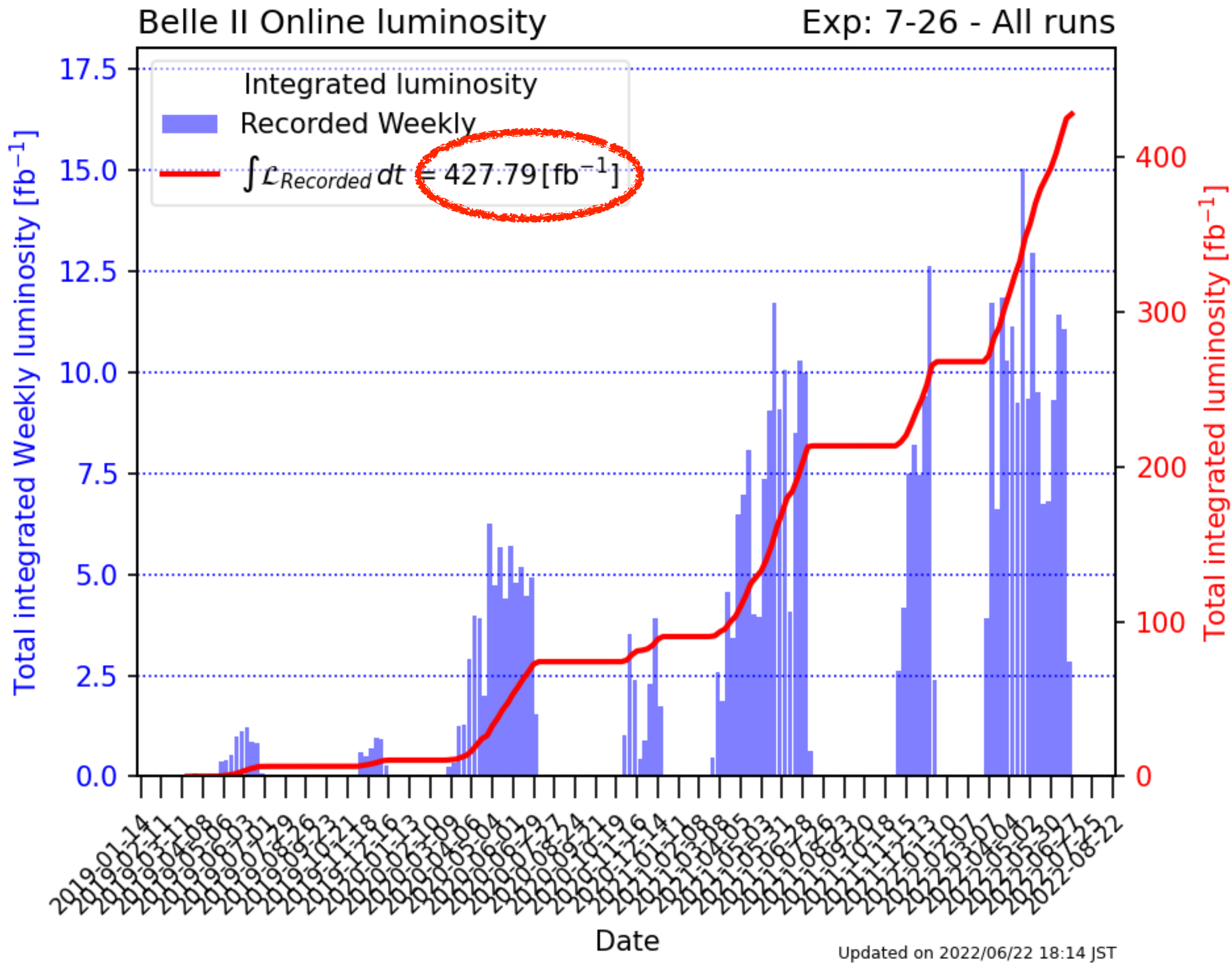
BESIII region

$\sim 62 \text{ pb}^{-1}$  @ 3.52 GeV used for Collins asym's

aim at  $250 \text{ pb}^{-1}$  data set



# the future



→ similar data sample as at 1<sup>st</sup>-gener. B-factories by 2024?