

TMD DISTRIBUTIONS AT N4LLL



arXiv:2305.07473 [hep-ph] in collaboration with V. Moos, A. Vladimirov and

P. Zurita (Thanks for some slides)

And *JHEP* 10 (2022) 118 M. Bury et al.

<https://www.ucm.es/iparcos/>

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TMD FACTORIZATION

LP!

$$\frac{d\sigma}{dQ^2 dy dq_T^2} = \sigma_0 \sum_{f_1, f_2} \int \frac{d^2\mathbf{b}}{4\pi} e^{i(\mathbf{b}\cdot\mathbf{q}_T)} H_{f_1 f_2}(Q, Q) \{R[\mathbf{b}; (Q, Q^2)]\}^2 F_{f_1 \leftarrow h_1}(x_1, \mathbf{b}) F_{f_2 \leftarrow h_2}(x_2, \mathbf{b})$$

In recent years we have learnt a lot about this formula. For instance:

- Its range of applicability is provided by $\delta = \frac{q_T}{Q} \ll 1$, fixed- q_T , $\delta \sim 0.25$
- We have a non-perturbative evolution kernel (whose perturbative part is known at N3LO!!). We can work with different schemes (CSS, ζ -prescription, ..).
- We have a re-factorization of TMD at large transverse momentum in Wilson coefficients (now at N3LO!!) and PDF (now at NNLO!!)
- PDF are just part of a model

$$f_{1, f \leftarrow h}(x, b) = \sum_{f'} f_{NP}(x, b) \int_x^1 \frac{dy}{y} C_{f \leftarrow f'}(y, \mathbf{L}_{\mu_{\text{OPE}}}, a_s(\mu_{\text{OPE}})) f_{f \leftarrow h}(x/y, \mu_{\text{OPE}})$$

TMD FACTORIZATION

We can :

- Perform an extraction of TMD at N4LL (higher order than PDF..)
- Analyze the source of errors
- Be ready for NLP corrections

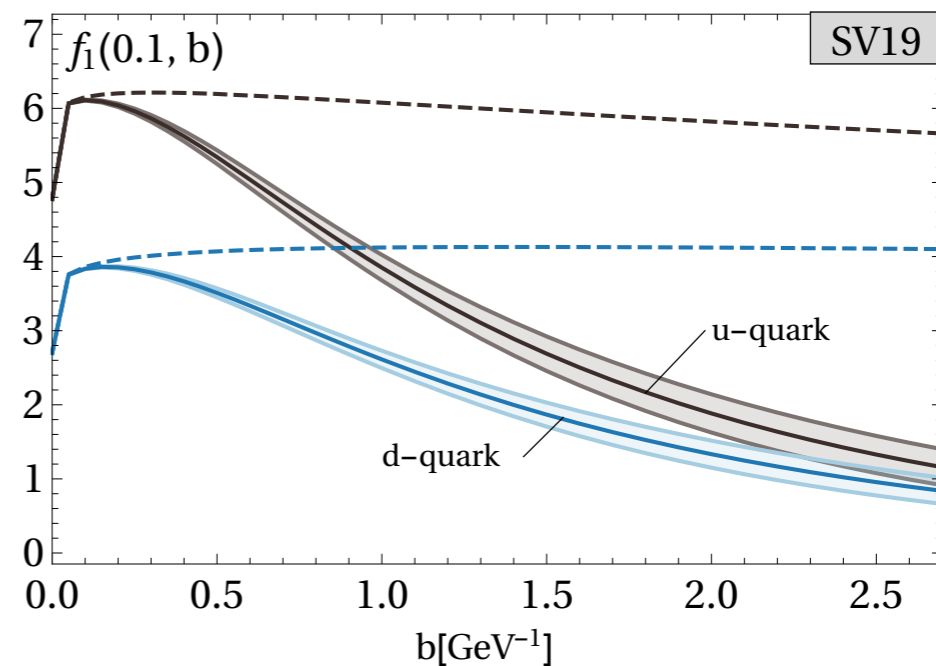
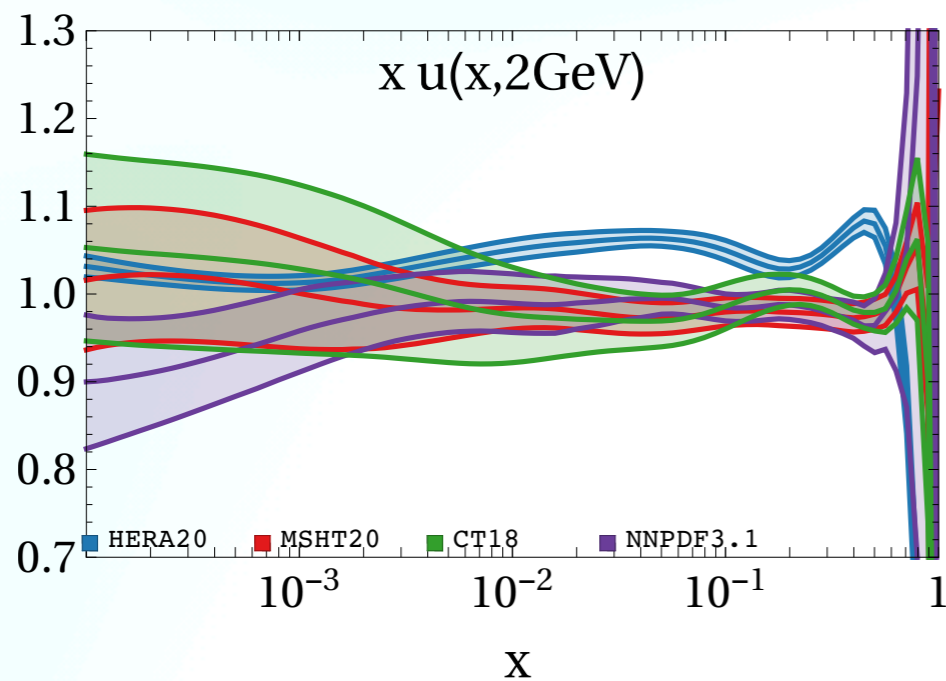
In this talk I will consider the first two points
We call the new Artemide code extraction

ART23

In SV19 we tried with several PDF sets

PDF set	χ^2_{DY}/N_{pt}
CT14	1,59
HERAPDF2.0	0,97
MMHT14	1,34
NNPDF3.1	1,14
PDF4LHC15	1,53

Also, in SV19, for $b \rightarrow 0$, the uncertainty bands $\rightarrow 0$.



THE PDF BIAS

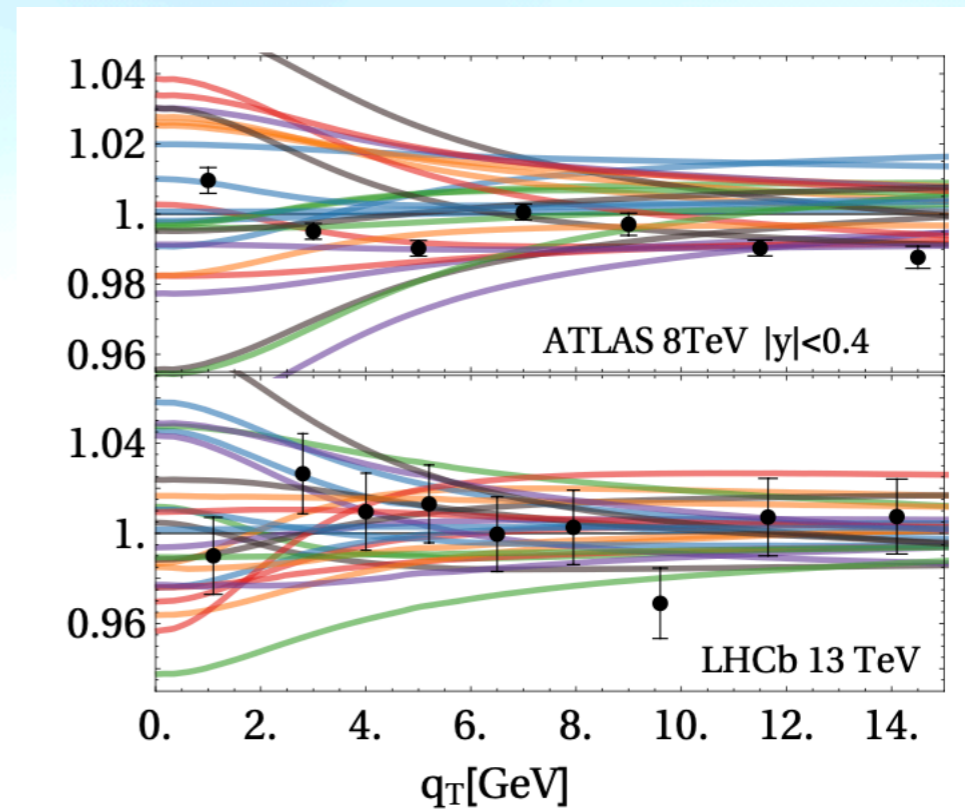
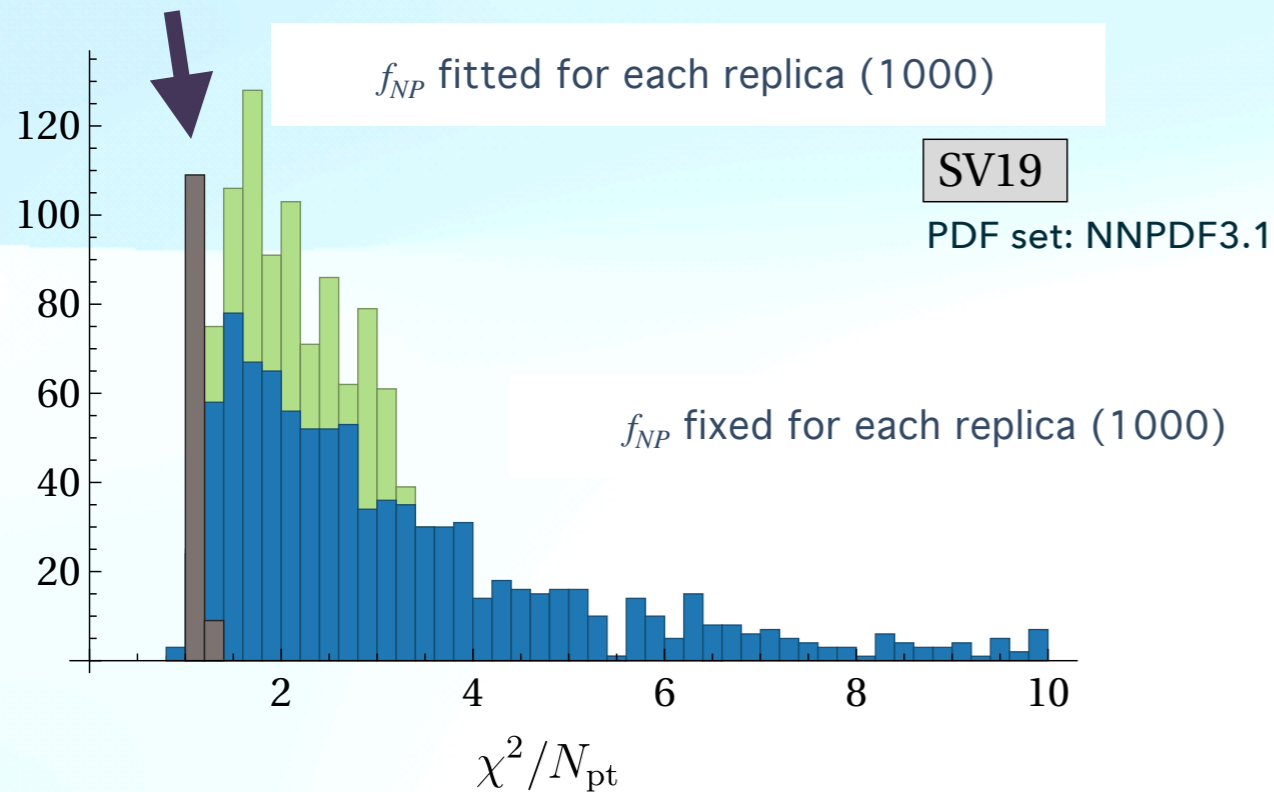
 So we have some questions to answer:

1. Can we get ***good TMD fits*** for different collinear PDFs?
2. Would they have sensible uncertainty bands?
3. Would they be consistent with each other?

FLAVOR INDEPENDENT f_{NP}

Most of replicas (64%) have $\chi^2/N > 2$.
Each replica has a peculiar shape

EXP error



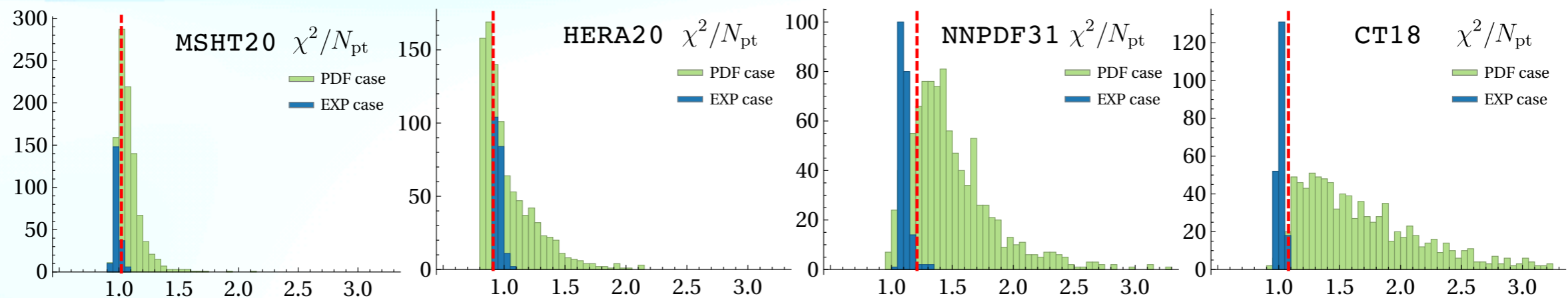
PDF UNCERTAINTIES AND FLAVOUR DEPENDENCE

M. Bury, F. Hautmann, S. Leal-Gomez, I. Scimemi, A. Vladimirov, PZ, **JHEP 10 (2022) 118**



Flavor separation make fits more PDF set independent and modeling simpler

$$f_{NP}^f(x, b) = \exp\left(-\frac{\lambda_1^f(1-x) + \lambda_2^f x}{\sqrt{1 + \lambda_0 x^2 b^2}} \mathbf{b}^2\right) \quad f = u, \bar{u}, d, \bar{d}, sea$$



ALL PDF DISTRIBUTIONS HAVE SIMILAR χ^2

THE SPREAD OF χ^2 OF PDF REPLICA IS HIGHLY REDUCED

FINAL χ^2 : MSHT20 (1.12), HERA20 (0.91), NNPDF31 (1.21), CT18 (1.08)

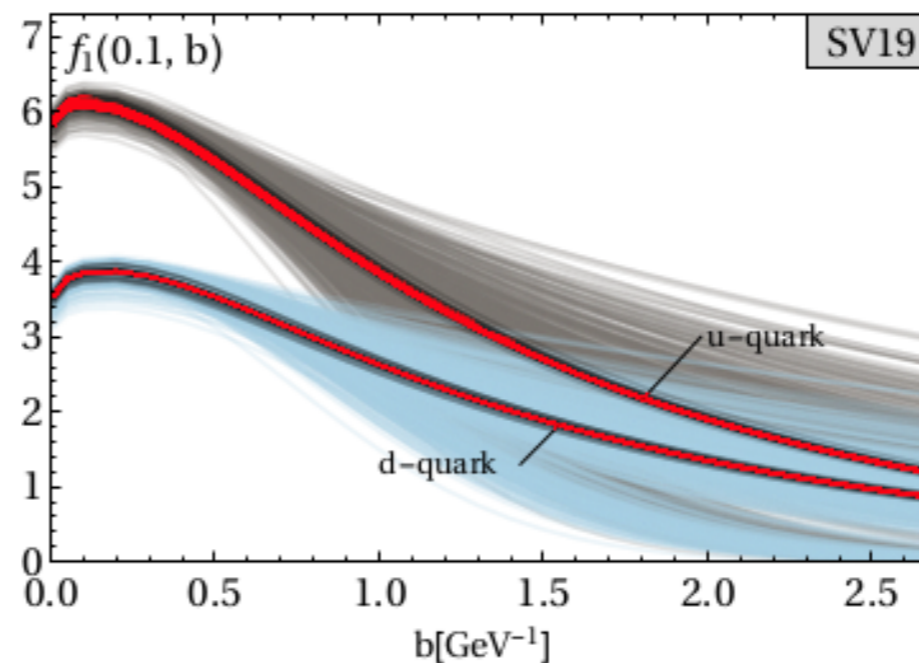
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📌 We include the PDF uncertainties while keeping f_{NP} fixed.

📌 We re-fit TMD, for each PDF replica.

📌 We get reasonable uncertainty bands.

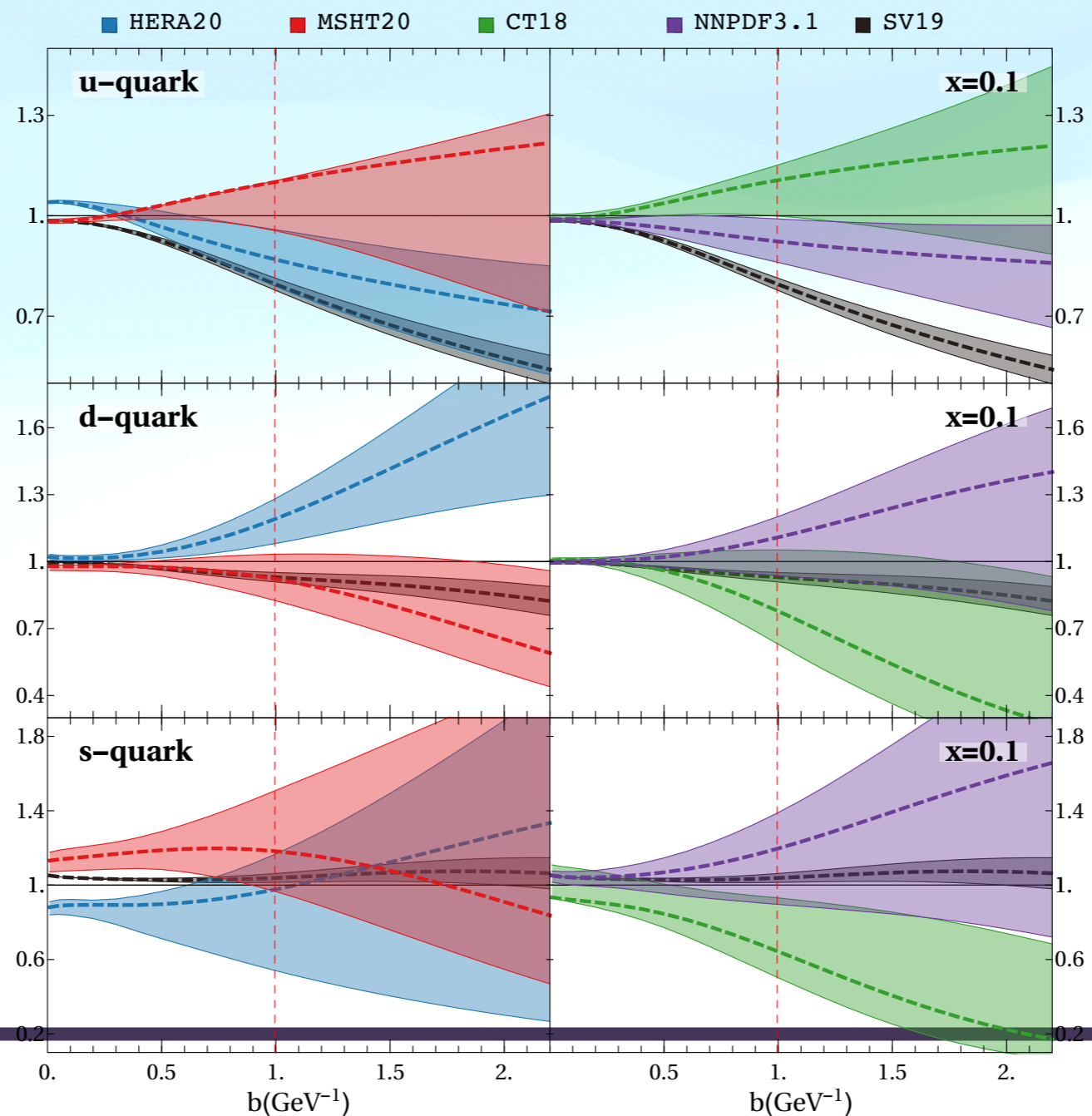


PDF UNCERTAINTIES AND FLAVOUR DEPENDENCE







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The TMD obtained from different sets agree reasonably





ART23


-  **Flavor dependence.**
 -  **All the latest datasets!**
 -  **W-boson production!**
 -  **Increased perturbative accuracy! (N^4LL)**
 -  **Includes collinear PDF uncertainties!**
 -  **A full new fit to Drell-Yan data.**
-

ART23: DETAILS

Evolution:

 We use the ζ prescription (I.S., A. Vladimirov *JHEP* 08 (2018) 003)

 We use the integral form of the evolution kernel to introduce a scale dependence similar to CSS for direct comparison

$$\mathcal{D}(b, \mu) = \mathcal{D}_{\text{small-b}}(b^*, \mu^*) + \int_{\mu^*}^{\mu} \frac{d\mu'}{\mu'} \Gamma_{\text{cusp}}(\mu') + \mathcal{D}_{\text{NP}}(b) \quad b^*(b) = \frac{b}{\sqrt{1 + \frac{b^2}{B_{\text{NP}}^2}}} = \frac{2e^{-\gamma_E} b}{\mu^*}$$


 We discover that we are sensitive to log corrections to the NP

part of the evolution kernel

$$\mathcal{D}_{\text{NP}}(b) = bb^* \left[c_0 + c_1 \ln \left(\frac{b^*}{B_{\text{NP}}} \right) \right]$$


ART23: DETAILS

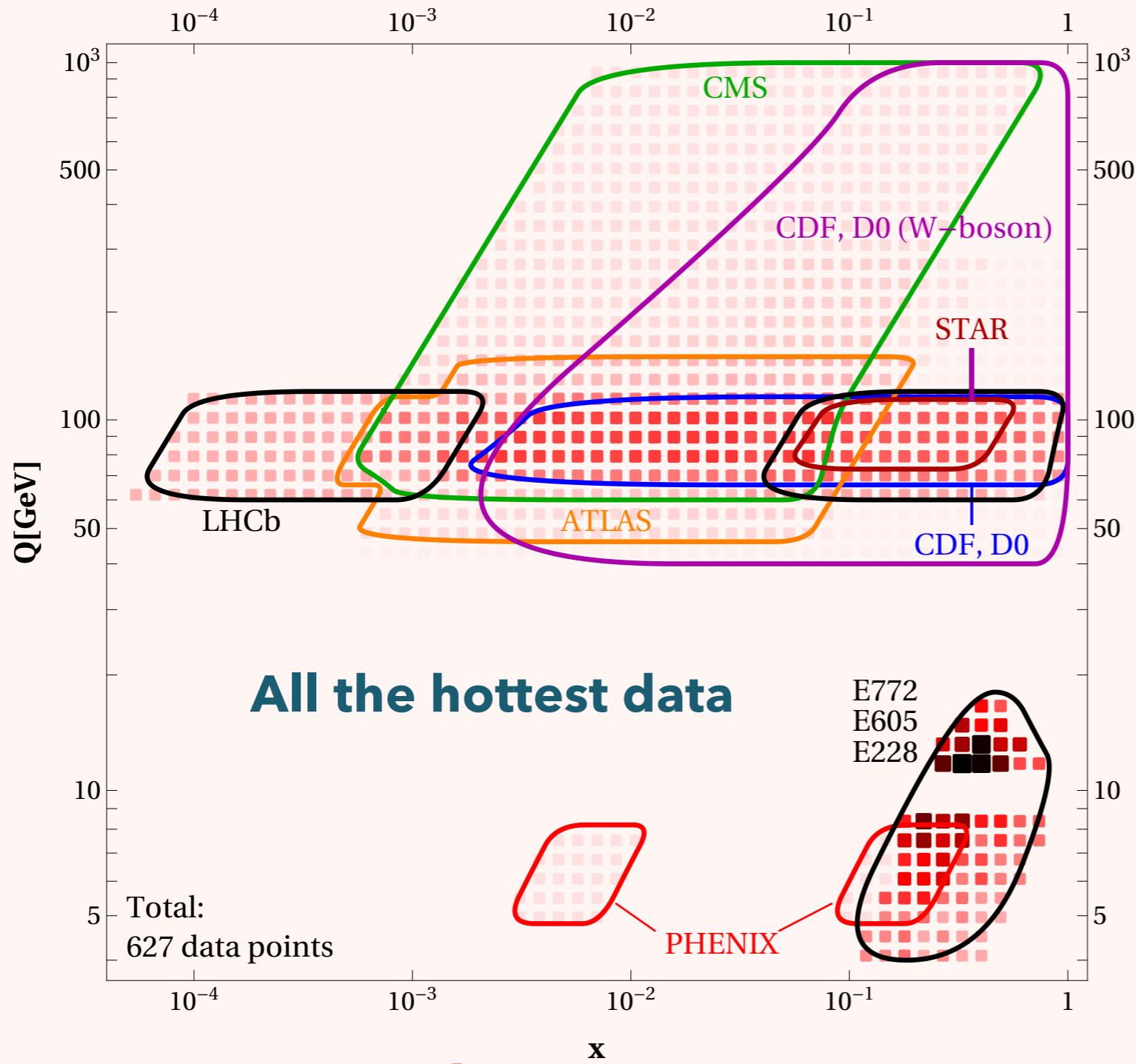
Simple Parameterization: $f_{NP}^f(x, b) = \frac{1}{\cosh\left(\left(\lambda_1^f(1-x) + \lambda_2^f x\right)b\right)}$

$f = u, \bar{u}, d, \bar{d}, sea$

In total, 13 parameters

Reference PDFs: MSHT20

ART23: DETAILS



627 data points

New in!

PHENIX: DY data at

$\sqrt{s} = 200$ **GeV**

STAR: Z/ γ -boson

production at

$\sqrt{s} = 510$ **GeV**

(preliminary).

CMS and LHCb: y -

differential Z-boson

production at $\sqrt{s} = 13$ TeV.

ATLAS: high precision

differential Z-boson cross-

section.

CMS: high-Q neutral-

boson production.

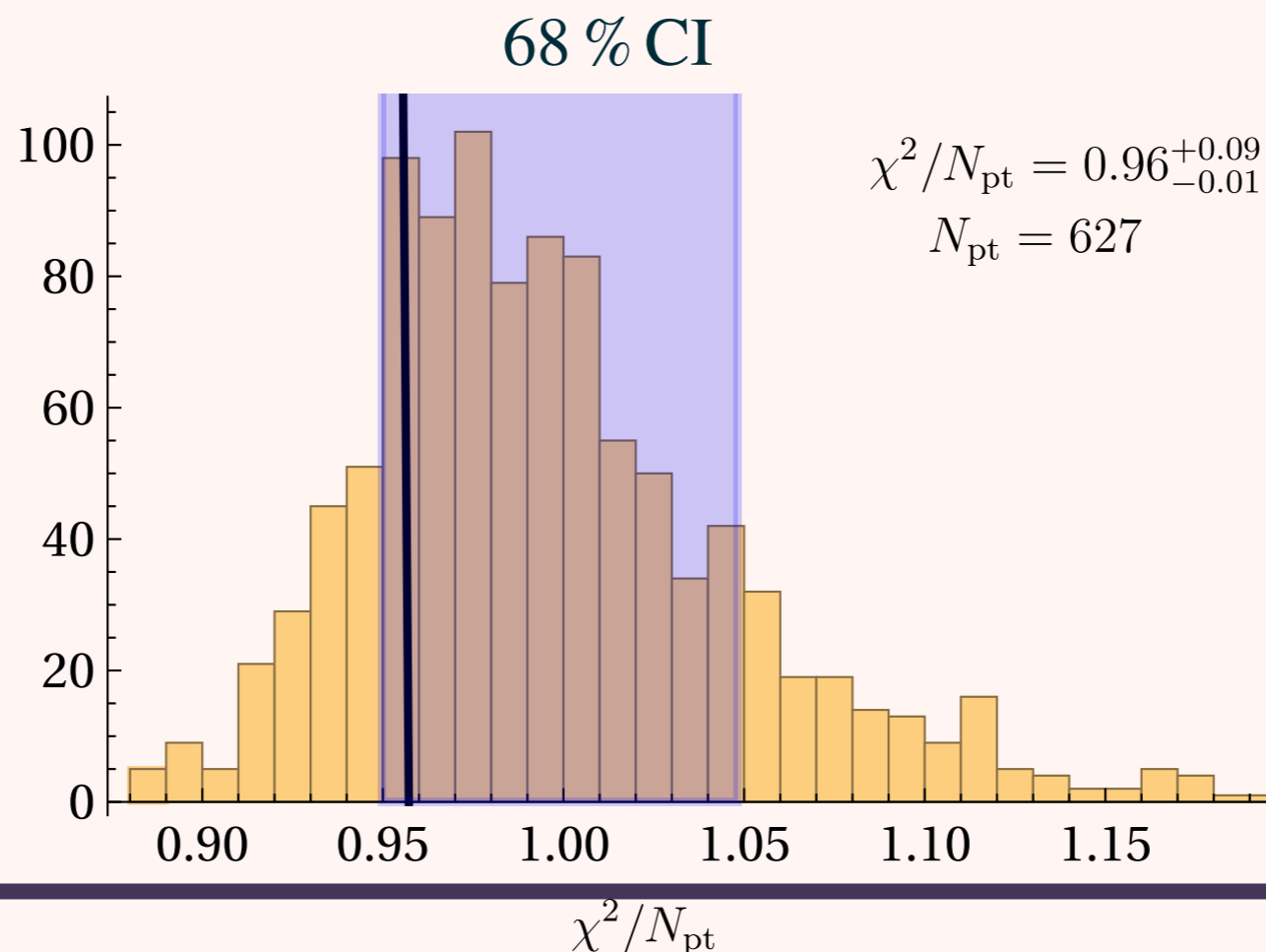
Tevatron: W-boson

production.

ART23: DETAILS

📌 **Fitting procedure: construct simultaneous replicas of the **data** AND the **PDFs**. Then fit.**

📌 **The number of replicas needed to have a faithful representation of the TMDPDF distribution was deemed to be 1000.**



ART23: RESULTS

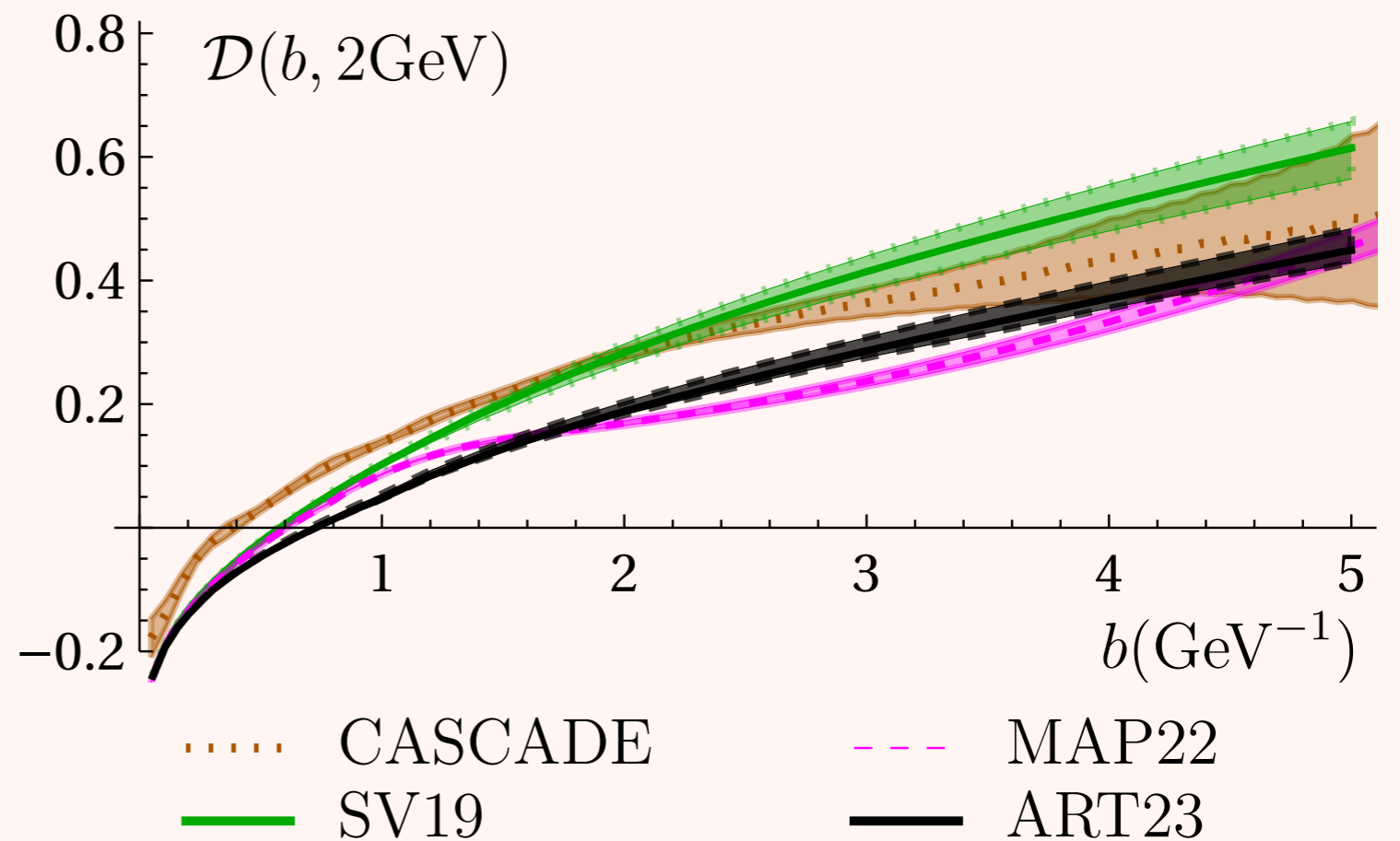
- overall improvement w.r.t. SV19. Specially for the LHC data. Higher precision plays a key role here.
- more realistic uncertainty bands than in SV19.

CS kernel close to the one from the global fit MAP22

$$B_{\text{NP}} = 1.56^{+0.13}_{-0.09} \text{ GeV}$$

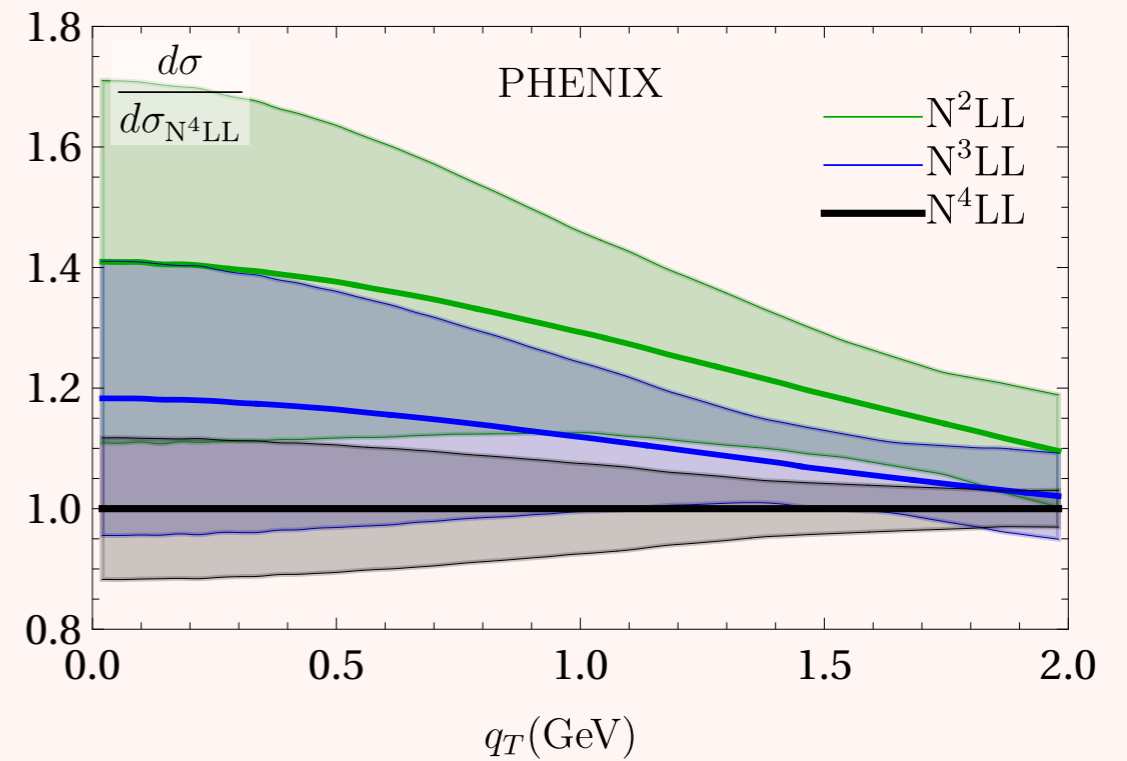
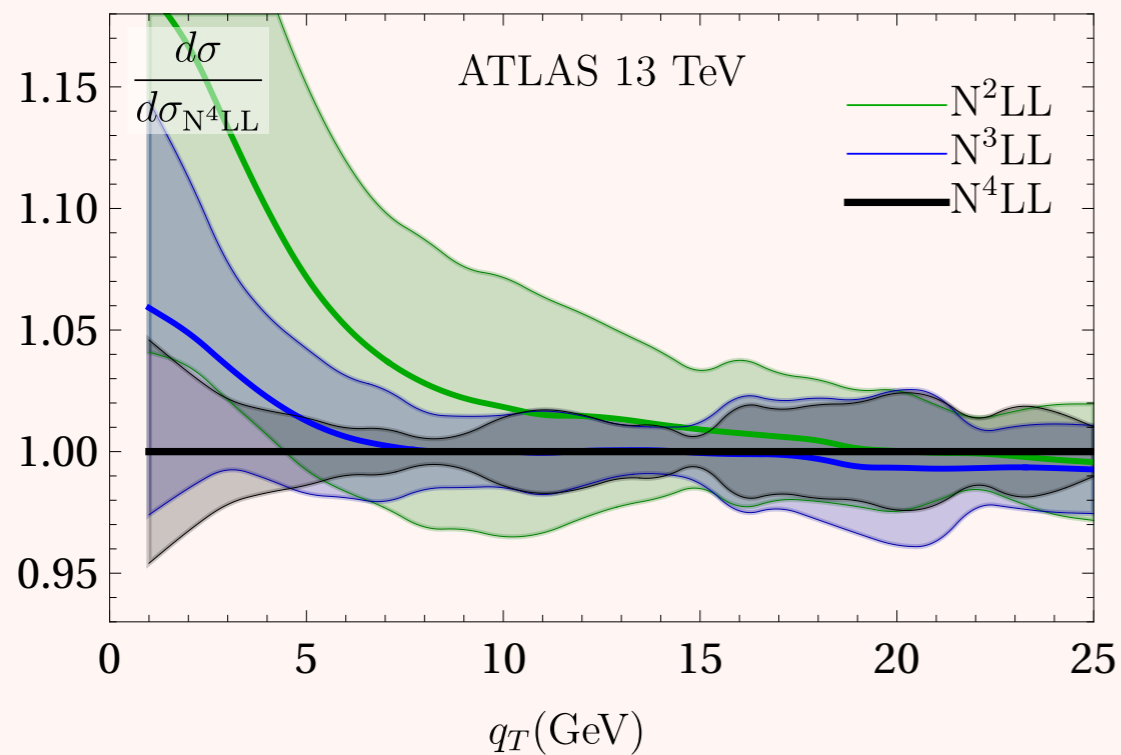
$$c_0 = 3.69^{+0.65}_{-0.61} \cdot 10^{-2}$$

$$c_1 = 5.82^{+0.64}_{-0.88} \cdot 10^{-2}$$



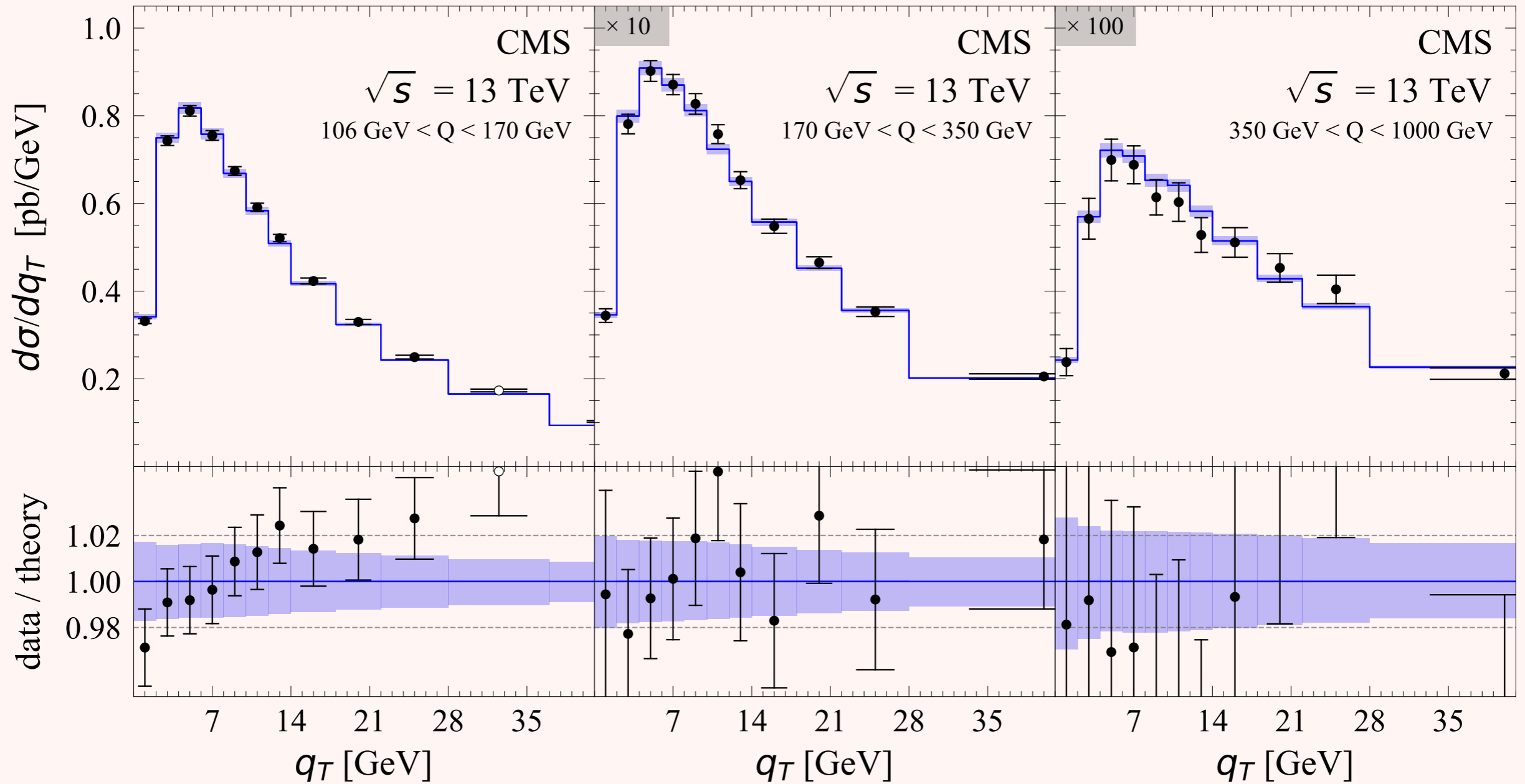
ART23: RESULTS

Scale variations $\left\{ \mu \rightarrow s_2\mu, \mu^* \rightarrow s_3\mu^*, \mu_{\text{OPE}} \rightarrow s_4 \frac{2e^{-\gamma_E}}{b} + 2\text{GeV} \right\}$.

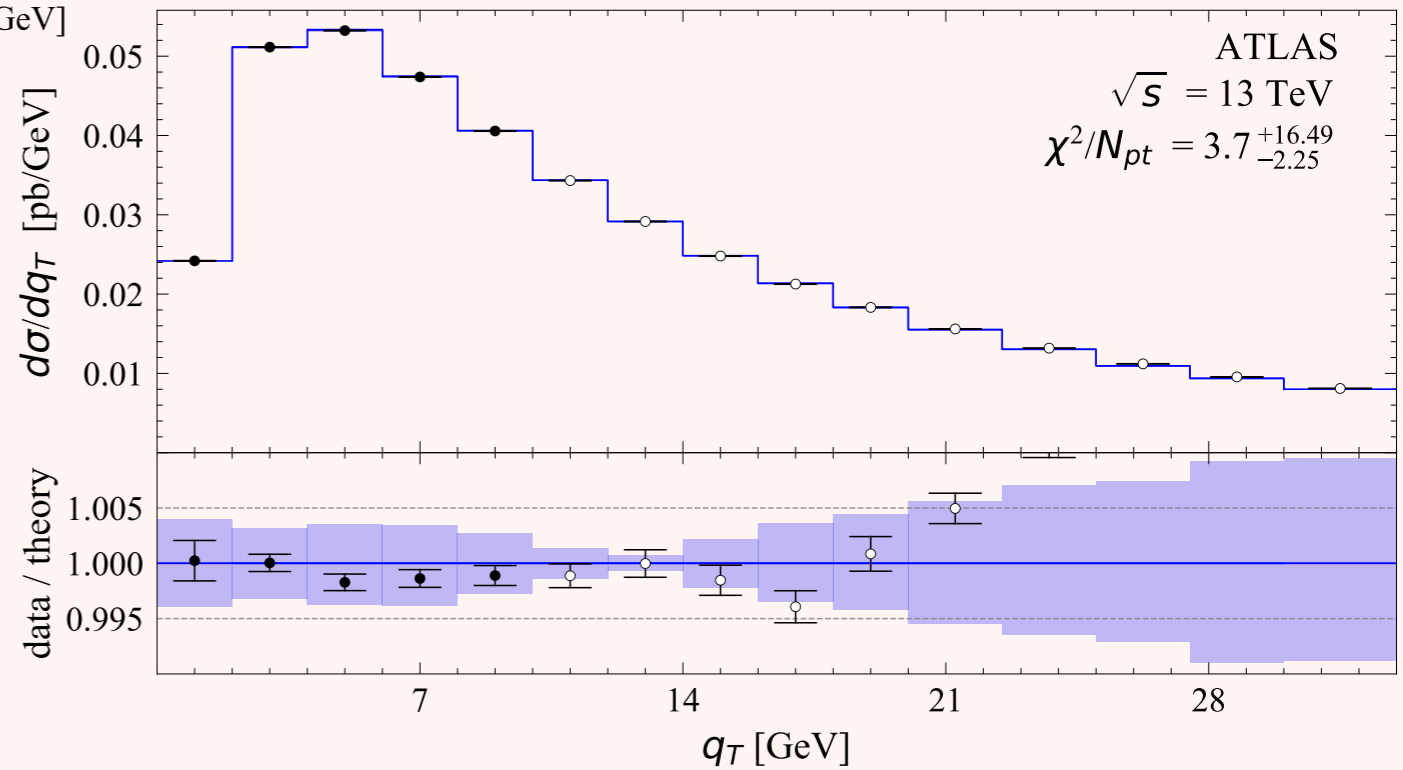
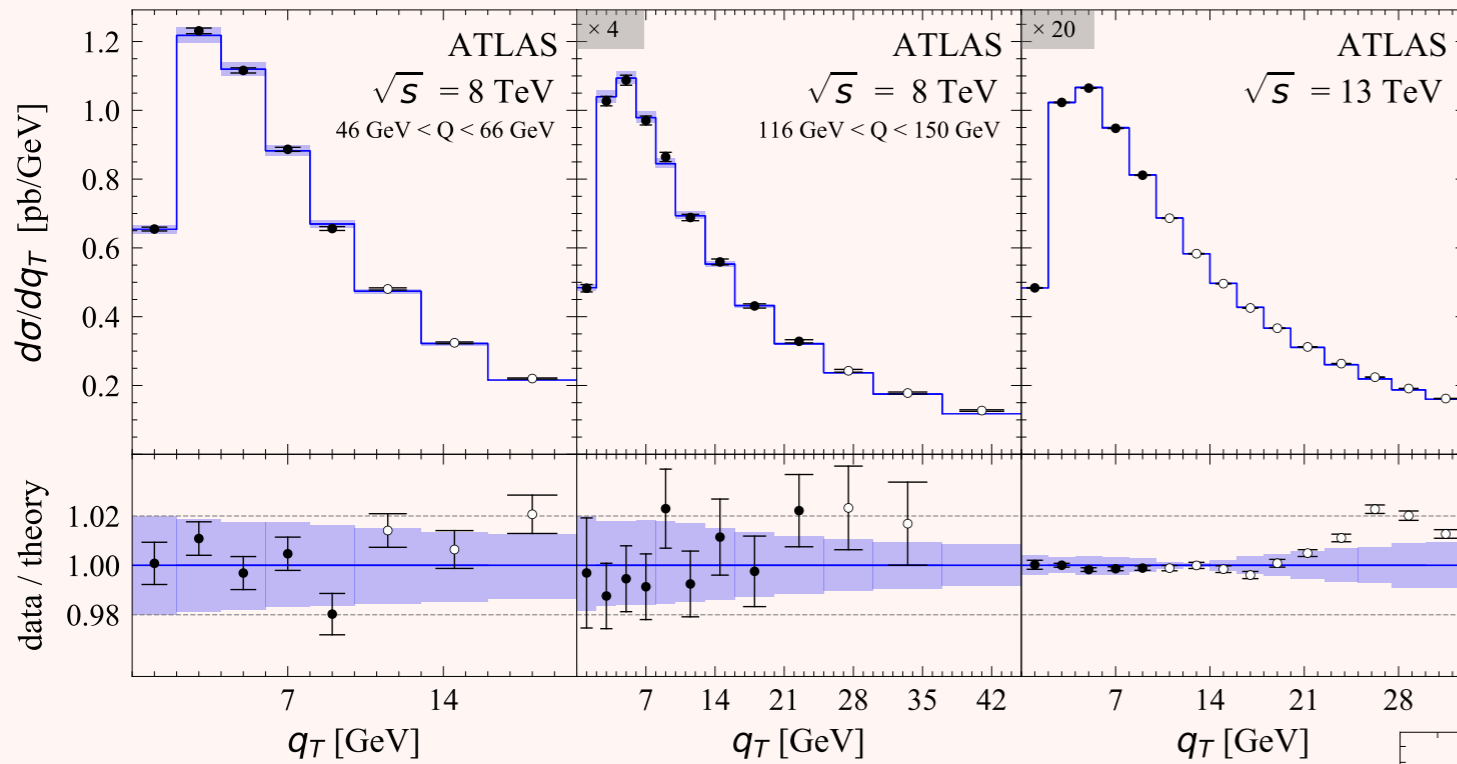


Γ_{cusp}	γ_V	β	$\mathcal{D}_{\text{small-b}}$	$C_{f \leftarrow f'}$	C_V	PDF
$a_s^5 (\Gamma_4)$	$a_s^4 (\gamma_4)$	$a_s^6 (\beta_4)$	$a_s^4 (d^{(4,0)})$	$a_s^3 (C_{f \leftarrow f'}^{[3]})$	a_s^4	NNLO

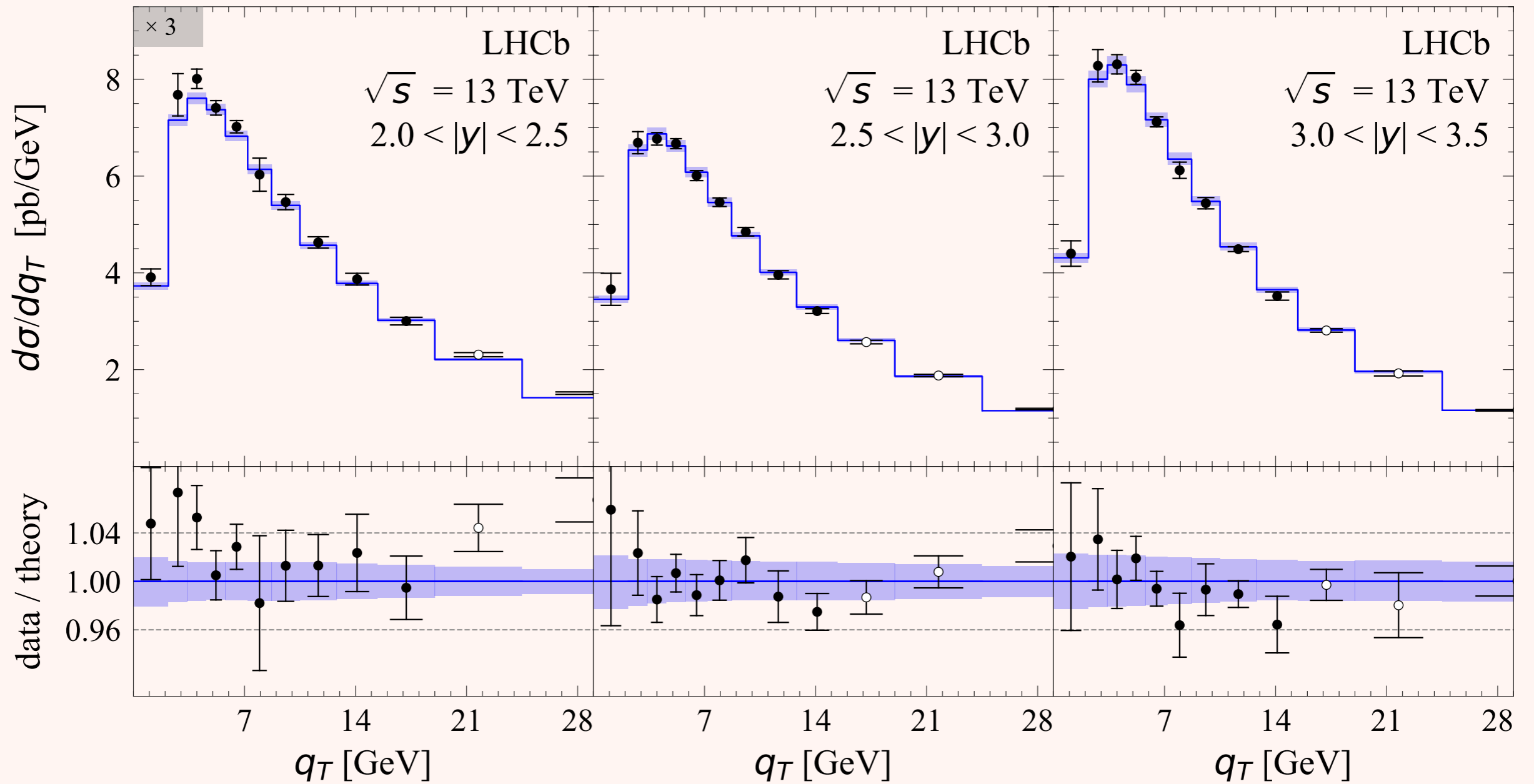
ART23: RESULTS



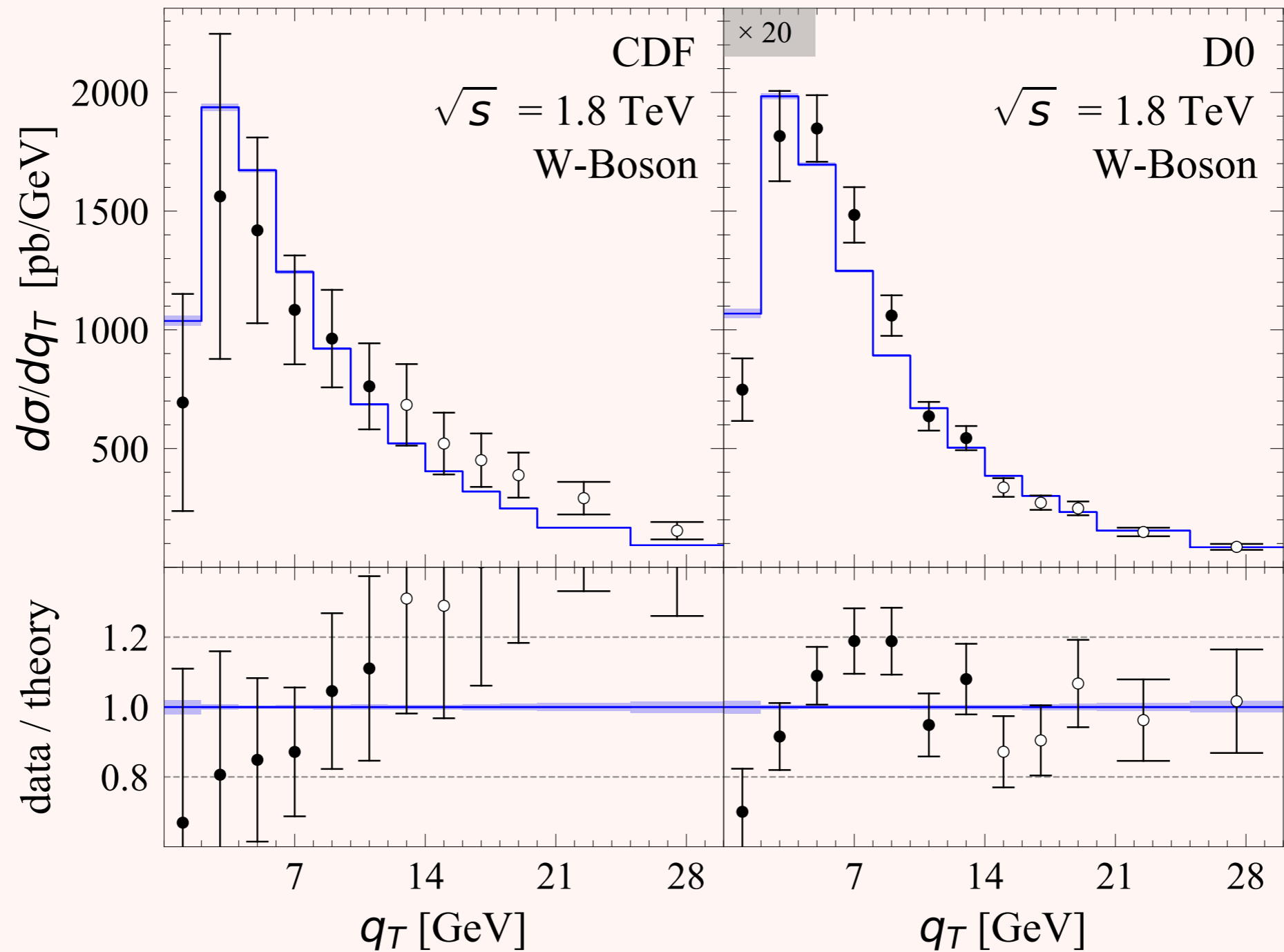
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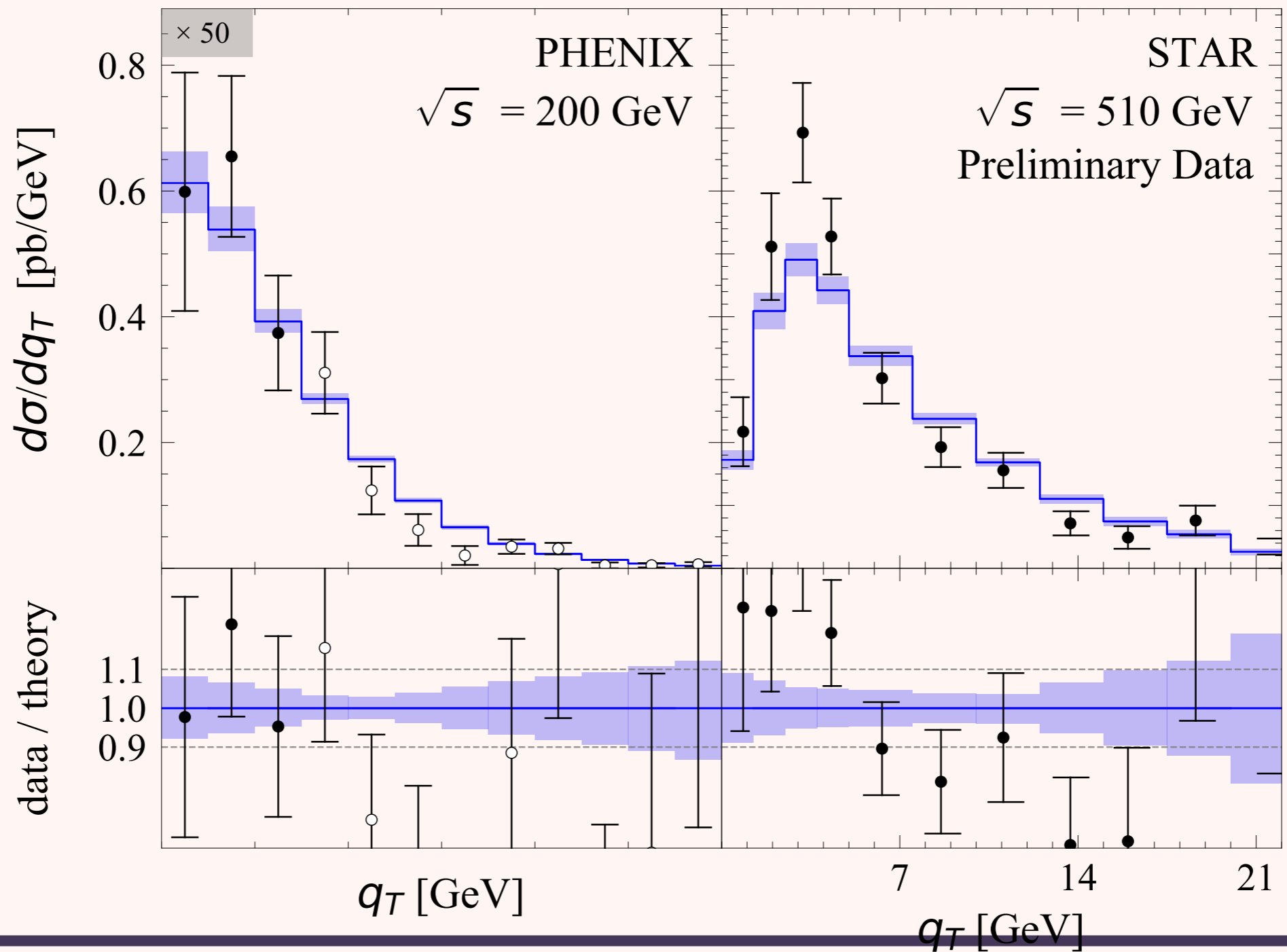
ART23: RESULTS



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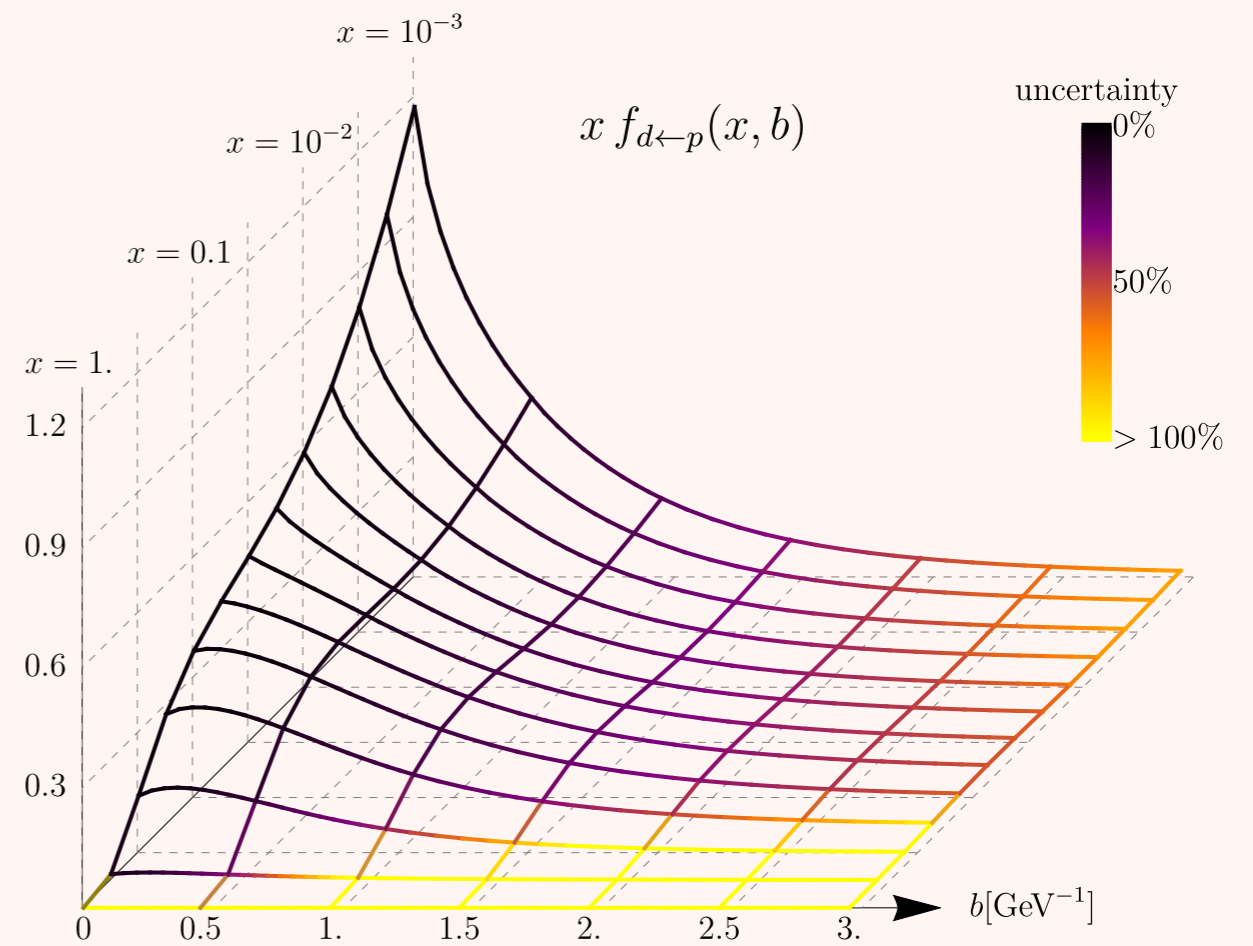
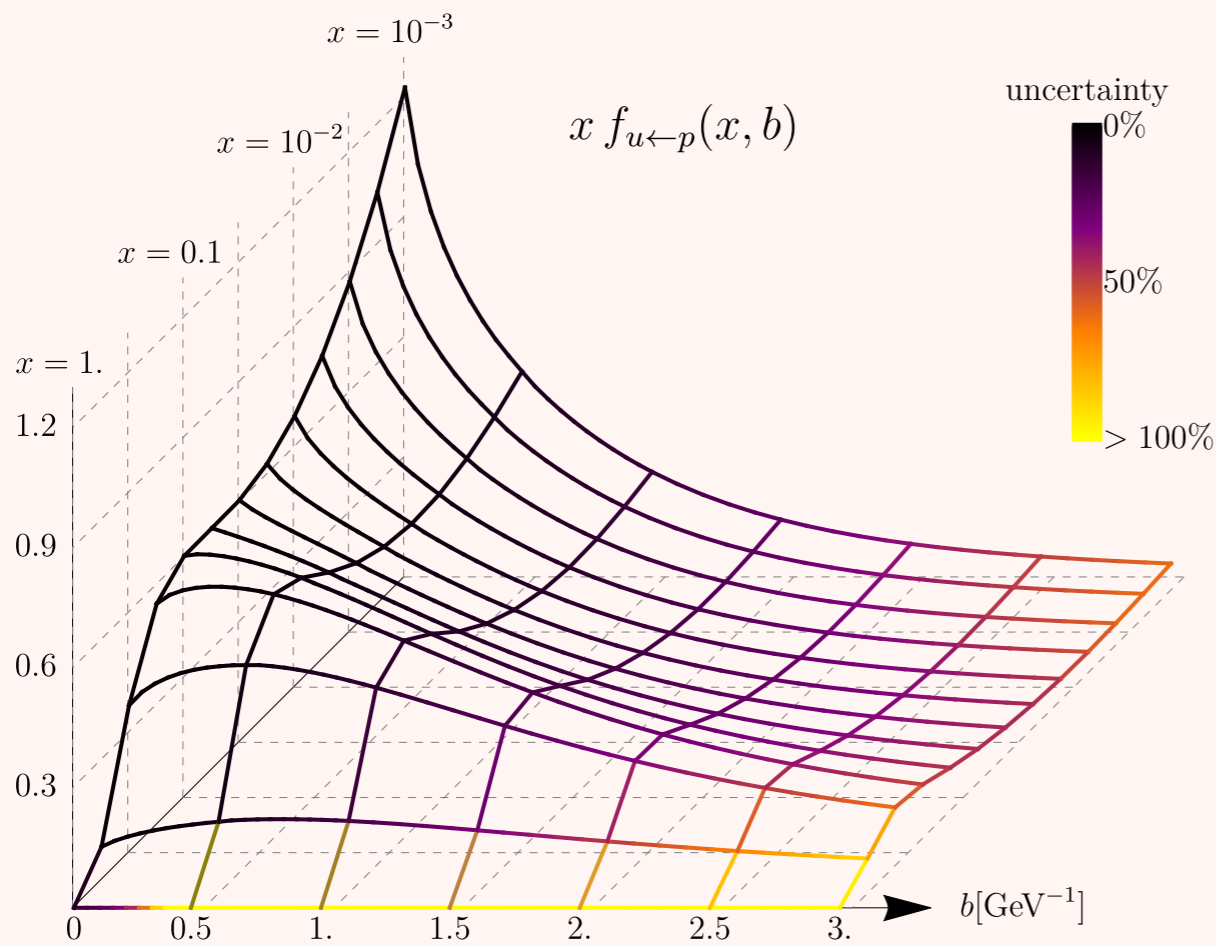


ART23: RESULTS

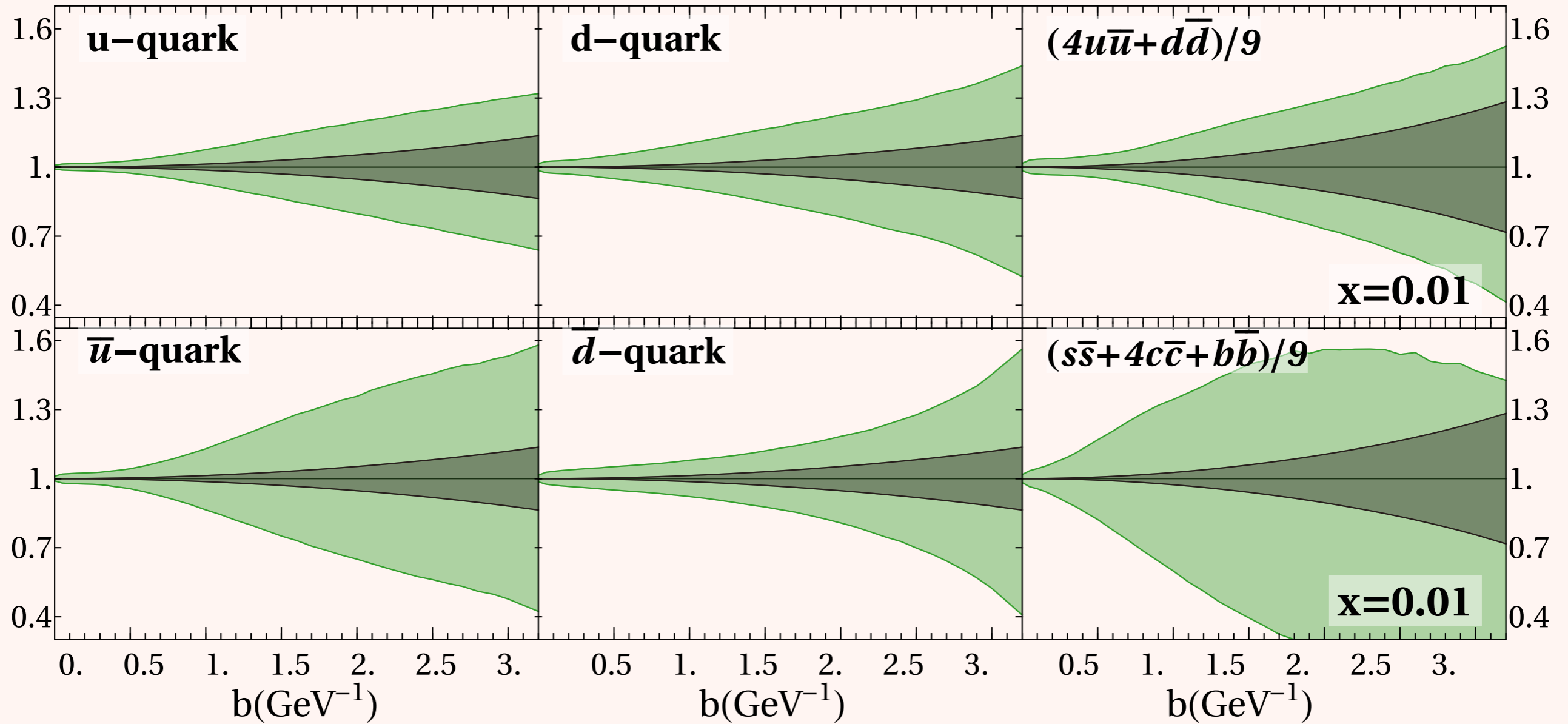


ART23: RESULTS

$$\begin{aligned}\lambda_1^u &= 0.87^{+0.10}_{-0.10}, & \lambda_2^u &= 0.91^{+0.33}_{-0.29}, \\ \lambda_1^d &= 0.99^{+0.09}_{-0.12}, & \lambda_2^d &= 6.06^{+1.36}_{-1.34}, \\ \lambda_1^{\bar{u}} &= 0.35^{+0.23}_{-0.22}, & \lambda_2^{\bar{u}} &= 46.6^{+7.9}_{-8.1}, \\ \lambda_1^{\bar{d}} &= 0.12^{+0.13}_{-0.11}, & \lambda_2^{\bar{d}} &= 1.53^{+0.54}_{-0.17}, \\ \lambda_1^{sea} &= 1.32^{+0.23}_{-0.24}, & \lambda_2^{sea} &= 0.46^{+0.13}_{-0.45},\end{aligned}$$








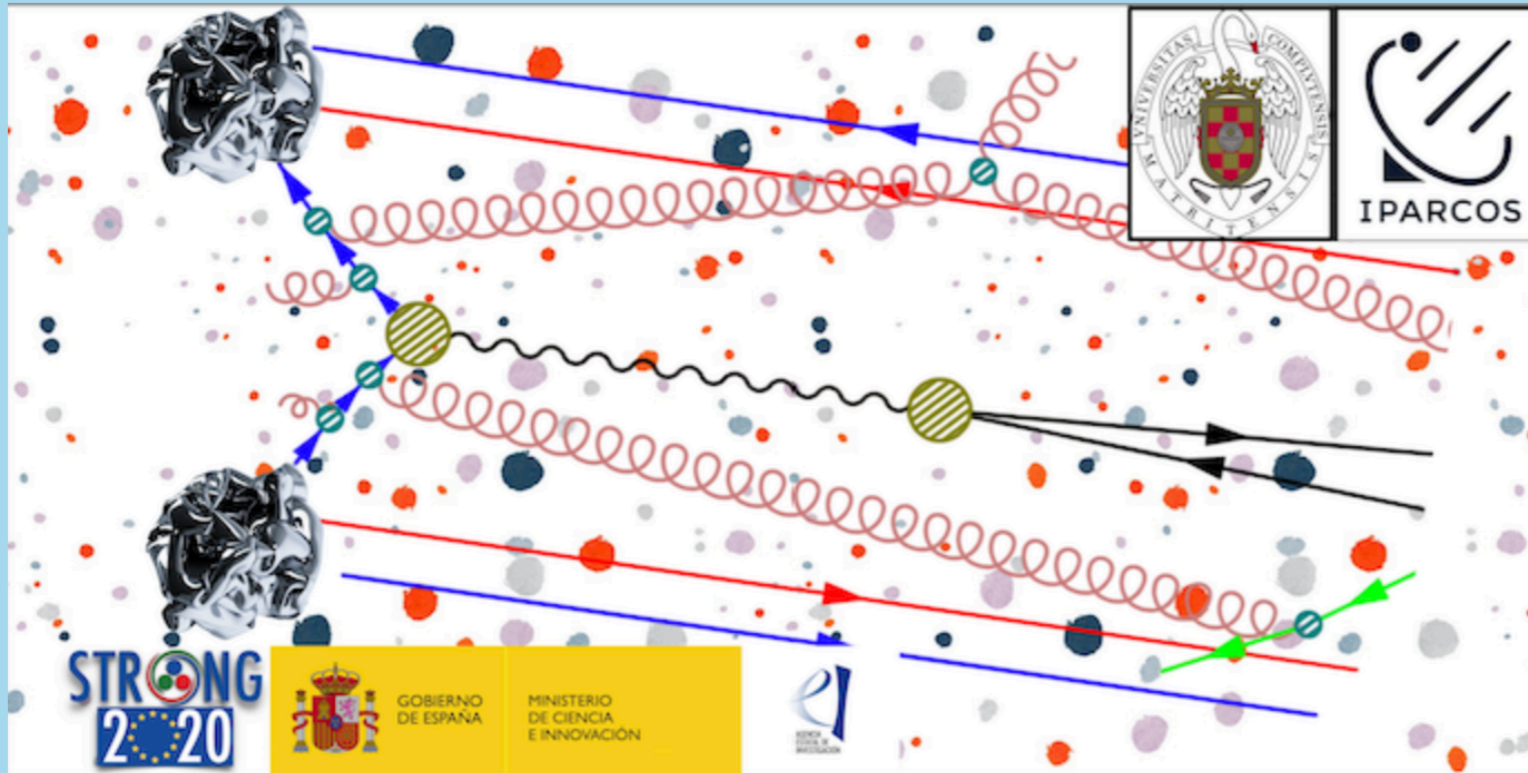
ART23: RESULTS



green: ART23
grey: SV19

SUMMARY

-  **We have performed a novel TMDPDF extraction: *ART23*.**
 -  **We used all the newest measurements and also W-boson production data, finding a good description.**
 -  **For the first time, the PDF uncertainties are systematically included. And we have realistic uncertainty bands.**
 -  **The flavor dependence in the NP ansatz is crucial to reduce the PDF bias.**
 -  **The global fit (including SIDIS data) is ... closer**
-



Resummation, Evolution, Factorization 2023 (REF2023)

23-27 octubre 2023
Facultad de Físicas
Europe/Madrid timezone

<https://indico.fis.ucm.es/event/19/>

BACK-UP

NNPDF3.1: COMPARISON

