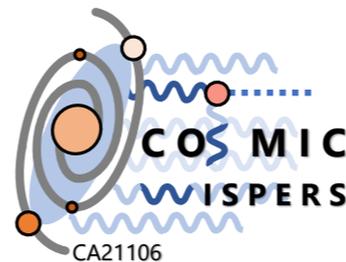


**WGII**  
**WISPs Dark Matter and Cosmology**  
**State of the art**

**Javier Redondo**  
**COST21106 kick off meeting**  
**LNf 23-24/02/2023**



**Dep. Theoretical Physics**  
**Universidad de Zaragoza**



**MAX-PLANCK-GESELLSCHAFT**  
**MPP Munich**

# Our Working group 2

*WG 2: WISPs Dark Matter and Cosmology.*

*... WISPs as dark matter candidates ...*

*... Production mechanisms ...*

*... Axion Thermal mass (lattice, ChiPT) ...*

*... Cosmic string decays ...*

*... Effects on Large and small-scale structure ...*

*... hot DM (lattice, ChiPT) ...*

*WISPs = Weakly-interacting\* slim/sub-eV Particles*

*\*not weak like electro-weak*

# WISPs as dark matter candidates

- WISPs are **natural candidates for CDM**

low mass, need to be feebly interacting, thermal populations subleading\*, **bosons\***..  
axions (QCD&ALP), pseudo Nambu-Goldstones, U(1) bosons, ... moduli, MCPs, sterile nu's..

- They need **non-thermal production mechanisms**

WISPs are/can be **sensitive to initial conditions** and **very early cosmology** (good and bad)  
(thermalisation erases effects of initial conditions in cases like WIMP DM)  
vacuum realignment, topological defects decay, vacuum fluctuations ...

- WISPy DM might have distinctive **effects at small cosmological scales**

**wave-effects, miniclusters**

- They are often **decaying DM**

low mass, feebly interacting nature makes **loooong lifetimes**  
some **opportunities for LM detection**

# Production mechanisms

## - Vacuum realignment

- 1 - *Initial conditions are not on the vacuum state*
- 2 - *WISPy potential drives the field to oscillate around it from times  $t \sim 1/\text{mass}$*
- 3 - *oscillations are coherent state of particles with EOS  $\langle w \rangle \sim 0$   
(if ICs are sufficiently homogeneous ... typically  $k \sim H$ )*

## 1 - ICs vary with cosmology model ...

*pre-inflation ( $\sim$  homogenous field)*

*stochastic axion (large vacuum fluctuations) [Graham 2016]*

*kinetic misalignment ( $\sim$  large field velocity)*

*hill-top ICs*

## 2 - well understood

*... in the linear regime (when fluctuations are small and linear)*

*not so in non-linear regimes (need some more numerical sims, resolution issues, axitons)*

## 3 - well understood

*except perhaps the issue of Sikivie's Bose-Einstein condensation and its effects on galactic scales\**

# Production mechanisms

## - Decay from topological defects

- *topological defects have dynamics on  $O(1/H)$  scales that produce  $k \sim H$  axions*
- *they require numerical simulations for precision*
- *theoretical models can be sometimes conflicting*

## - global cosmic strings

## - domain walls

## - other similar structures?

- *Monopoles*
- *Bubbles from phase transitions*
- *??*

## - Mostly studied in the case of the QCD axion

- *ALP generalisation is easy (some works already)*
- *Some other scalars like relaxions*
- *what about other WISPs? hidden photons, MCPs ... ? not much*
  
- *generalisation to non-standard cosmologies*

# Production mechanisms

## - Thermal production

- *can be naturally subleading*
- *can still produce hot-warm dark matter effects (suppression PS at high-k, etc...)*
- *Computationally easy in perturbative regimes*

## - Uncertainty from early Universe

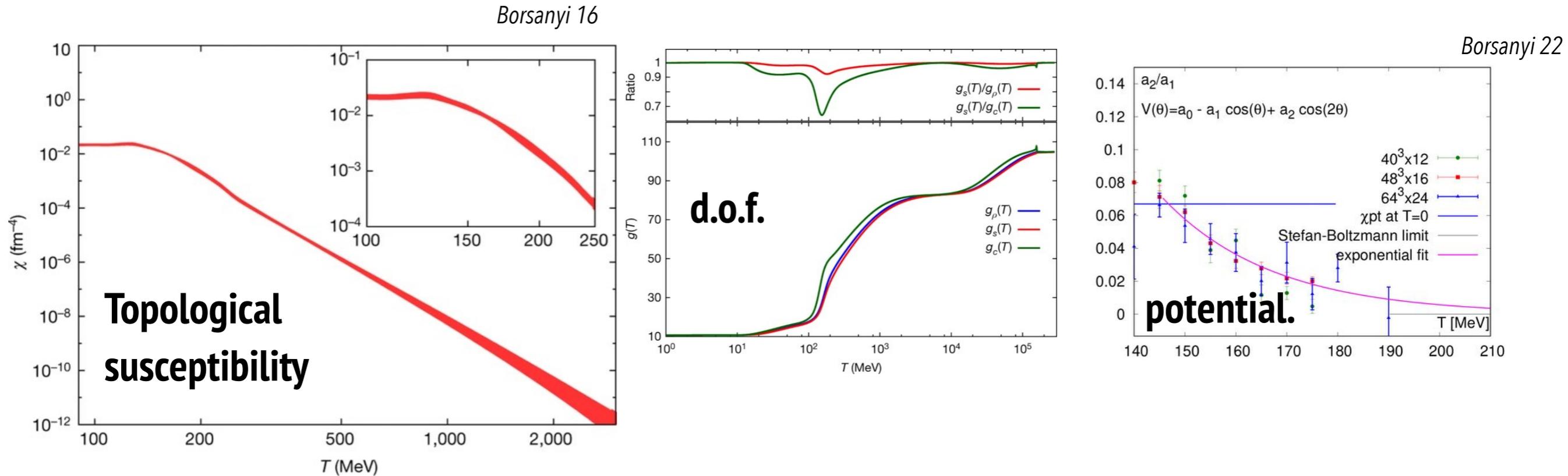
- *model dependency (more particles, d.o.f)*
- *entropy production?*
- *treat on a model basis*
- *CMB4 detection of  $N_{\text{eff}}$ , window to new d.o.f.*

## - Uncertainty from non-perturbative QCD

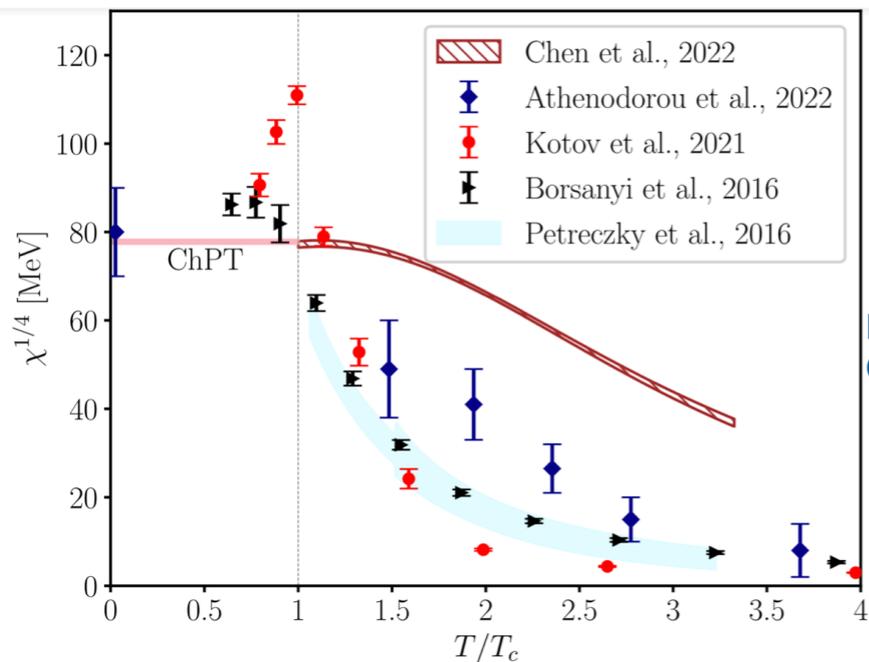
- *QCD axions in the  $\sim eV$  mass regime decouple during the QCD cross-over  $T \sim 150\text{MeV}$  where perturbative calculations are not reliable*
- *lattice QCD input could be useful*
- *region is borderline-excluded*

# Axion thermal mass

## - Lattice input for QCD axion cosmology



## - Different groups do not converge (topology at high T is extremely resource consuming)

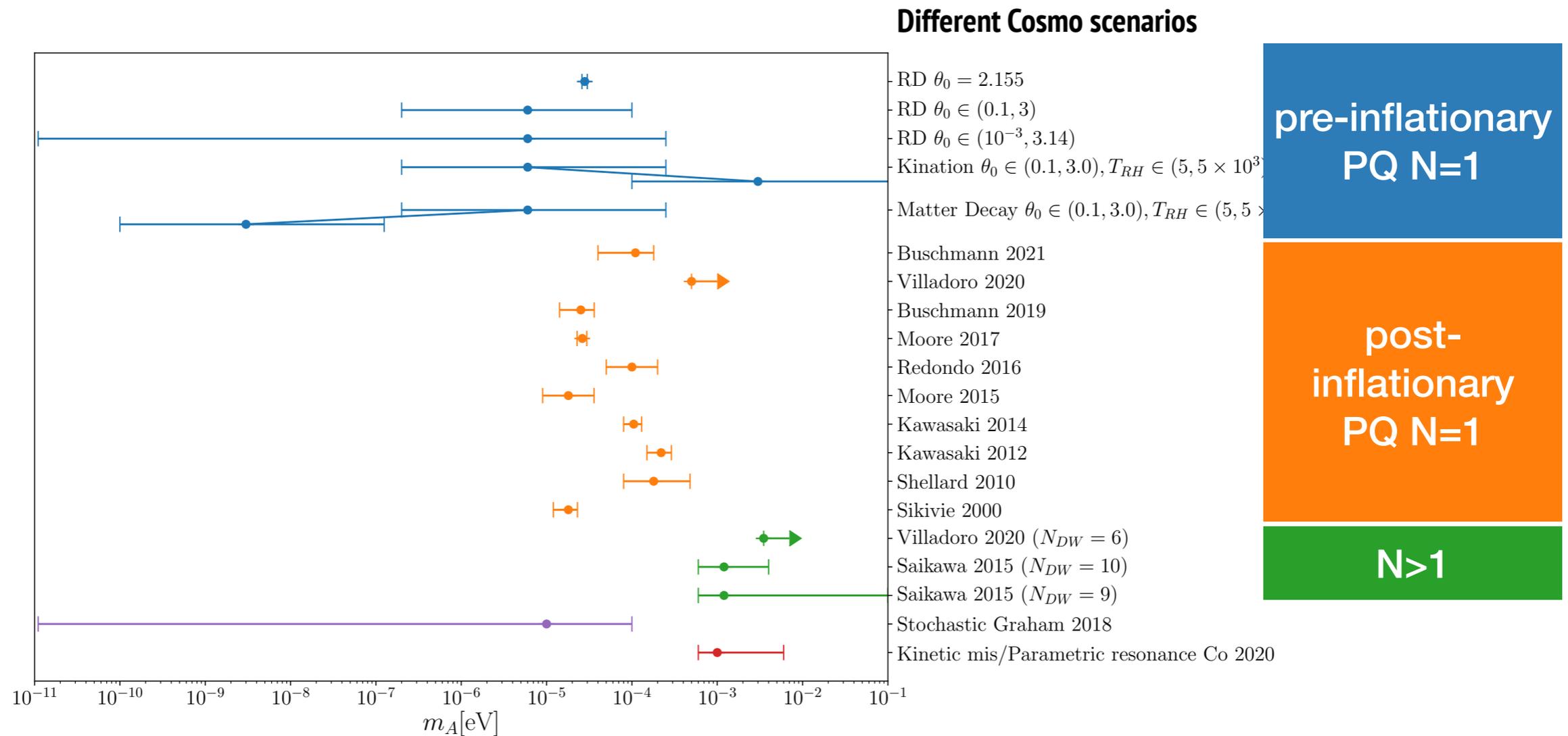


Plot by  
Claudio Bonanno

... Lattice issues: Results not entirely settled; extrapolation to high temperature regime may be subtle and needs further studies...

# Cosmic string decays (axion DM mass)

- Axion DM mass from theory could/should (not) guide the experiment

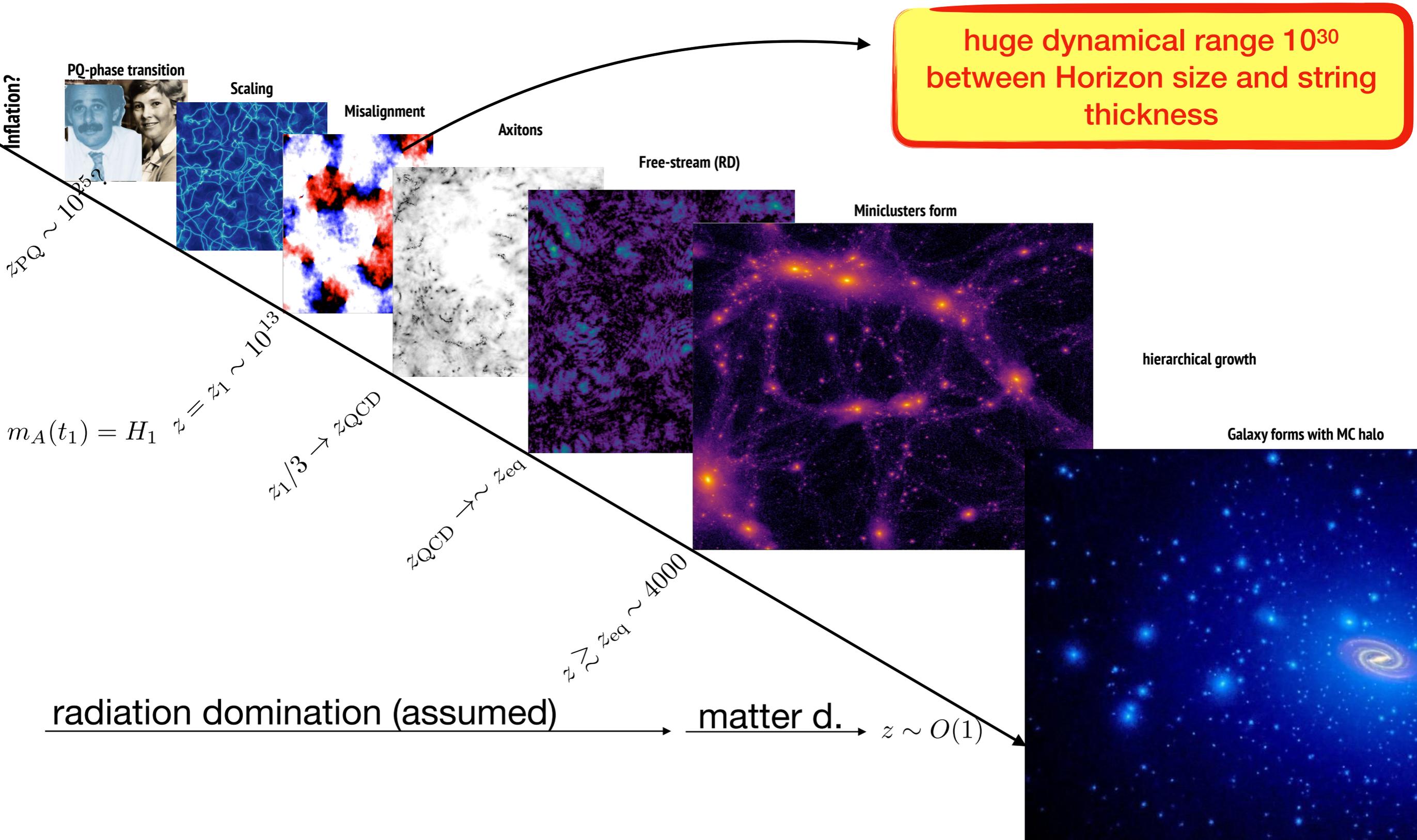


- post-inflationary PQ N=1 has no IC uncertainty (some model, and cosmology uncertainty)

the estimates of the axion DM mass disagree due to the different interpretation of numerical simulations

# post-inflationary scenario

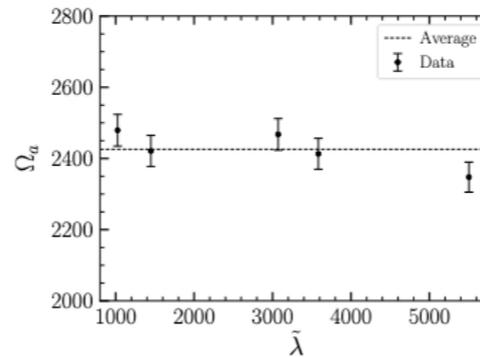
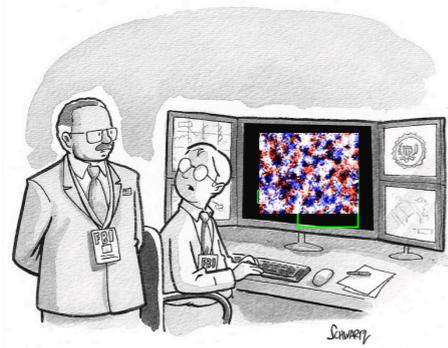
- ordered by time, scale factor, redshift, temperature



# how to tackle the large-dynamical range problem

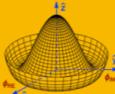
Two approaches:

**Direct simulation : 1) Simulate and 2) count the axions, extrapolate** *Moore, Redondo, Buschmann*



**Usual U(1) global string**

$$\mu = 2\pi \int r dr \left( \partial_r |\varphi|^2 + V(|\varphi|) + \frac{|\varphi|^2}{r^2} \right) \sim v^2 + \pi v^2 \log(vr_{\text{cut}})$$

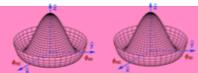


*Moore, Redondo, Buschmann*

- 1 extra degree of freedom
- unphysical DW destruction
- PRS trick (enhanced tension at early times)

**Moore tension string**

$$\mu \sim 2v^2 + \pi \frac{v^2}{q_1^2 + q_2^2} \log(vr_{\text{cut}})$$

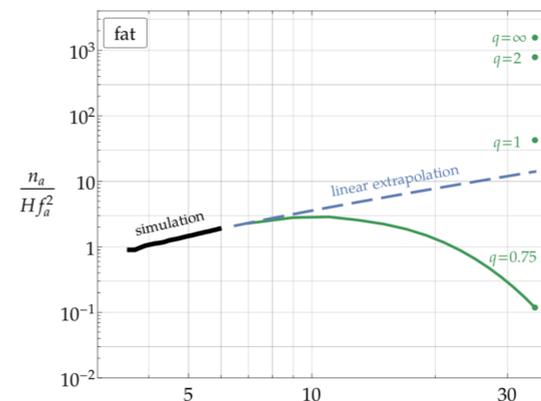
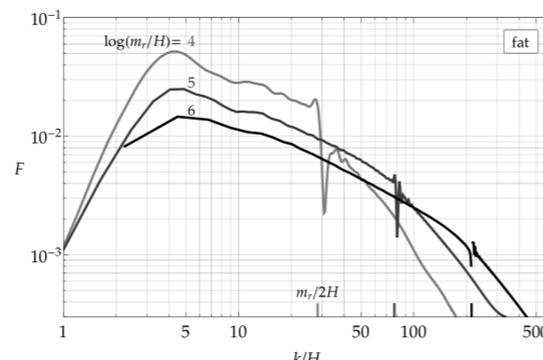
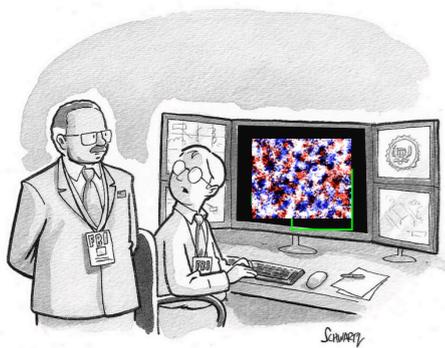


*Moore*

- 2+3 extra degrees of freedom (two higgs, 1 vector field)
- no unphysical DW destruction
- PRS trick (enhanced tension at early times)

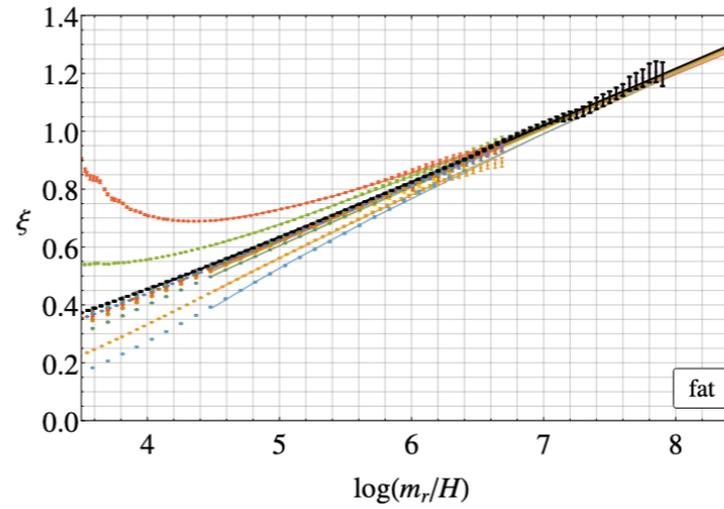
**In-Direct simulation : 1) Simulate to model axion emission from strings, 2) extrapolate the spectrum, 3) count the axions**

*Kawasaki, Gorghetto, Buschmann*



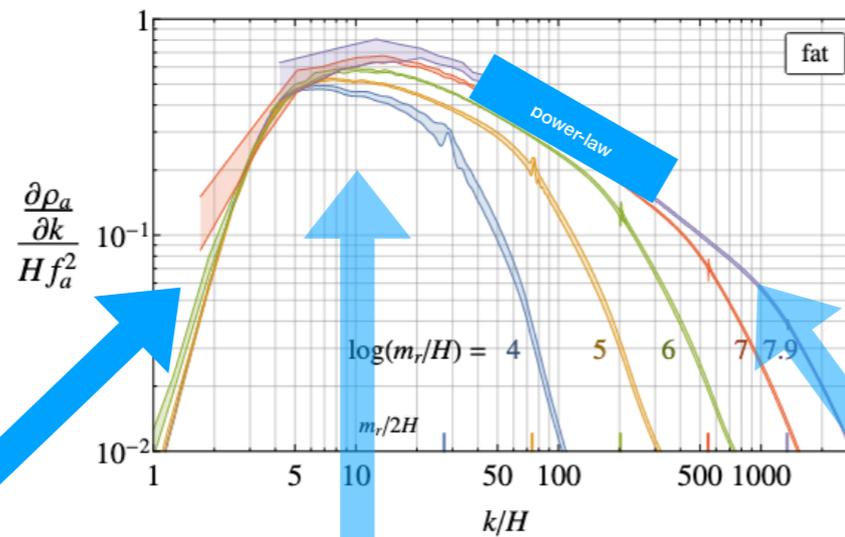
# Indirect method

- scaling solution (with log corrections!)  
(log corrections challenged)



Gorghetto, Redondo, Buschmann

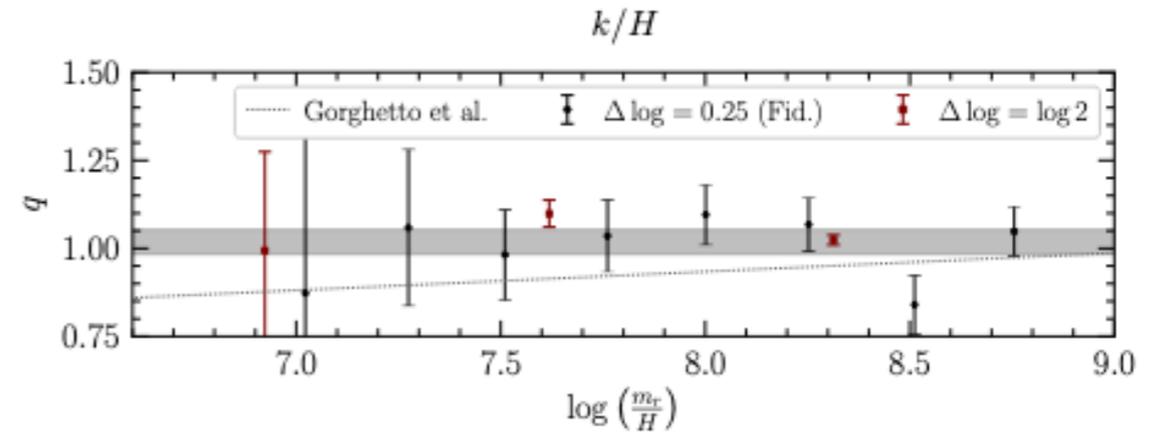
- axion spectrum .. power-law with UV and IR cut-offs (with log corrections\*)



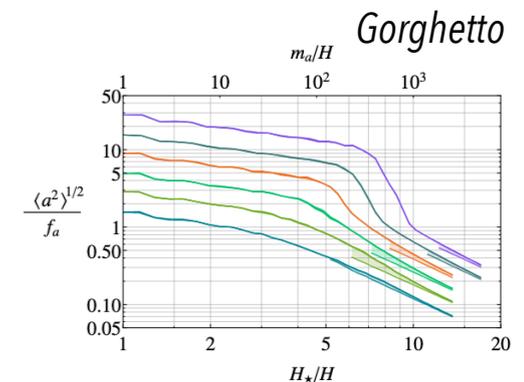
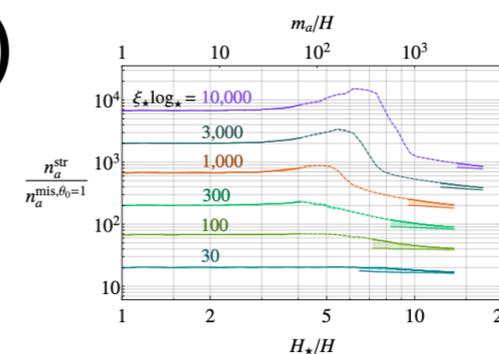
low-k cut-off

most of axions  $k \sim$  horizon

UV cut-off at radial mass



- Possible non-linear effects for large axion density ( $q \gg 1$ )



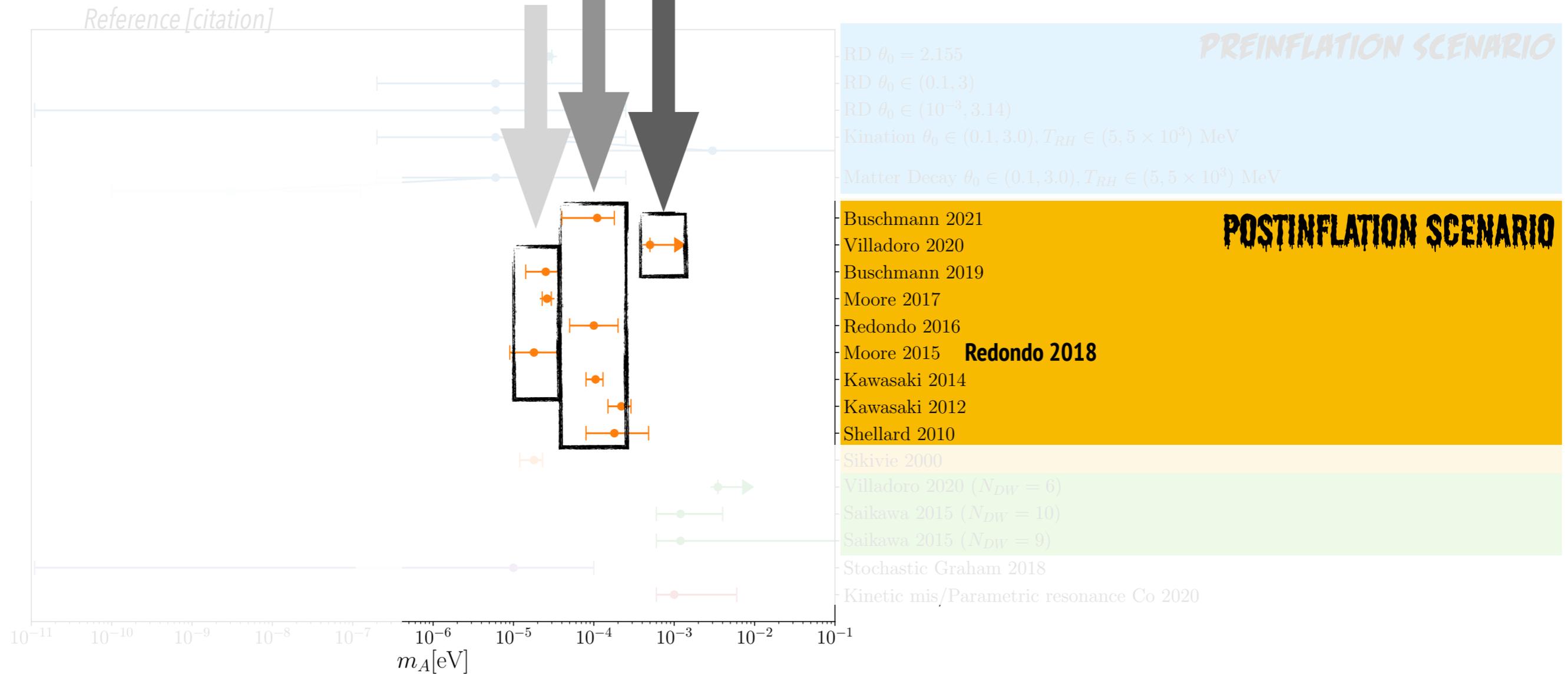
Gorghetto

# Results and controversies

Extrapolation  $\xi \sim 1, q \sim 1$  or  $\xi \sim 15, q < 1$

Direct simulations

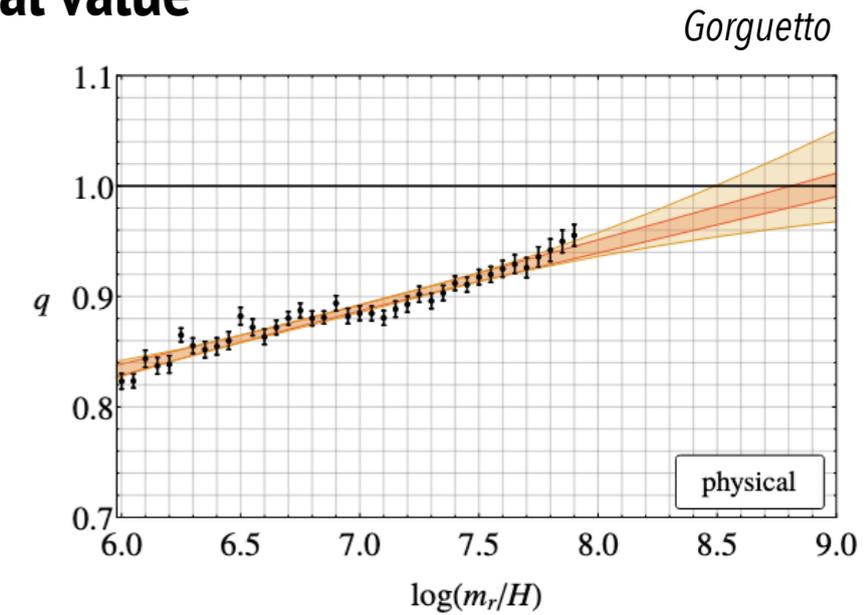
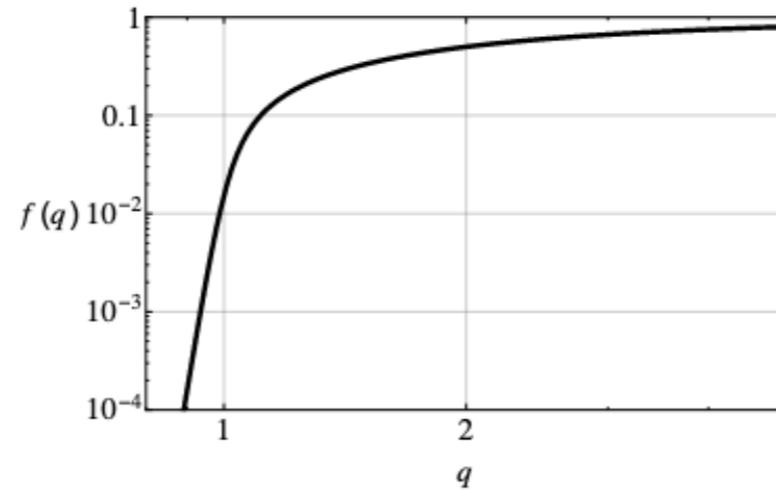
Extrapolation  $\xi \sim 10, q \sim 2$



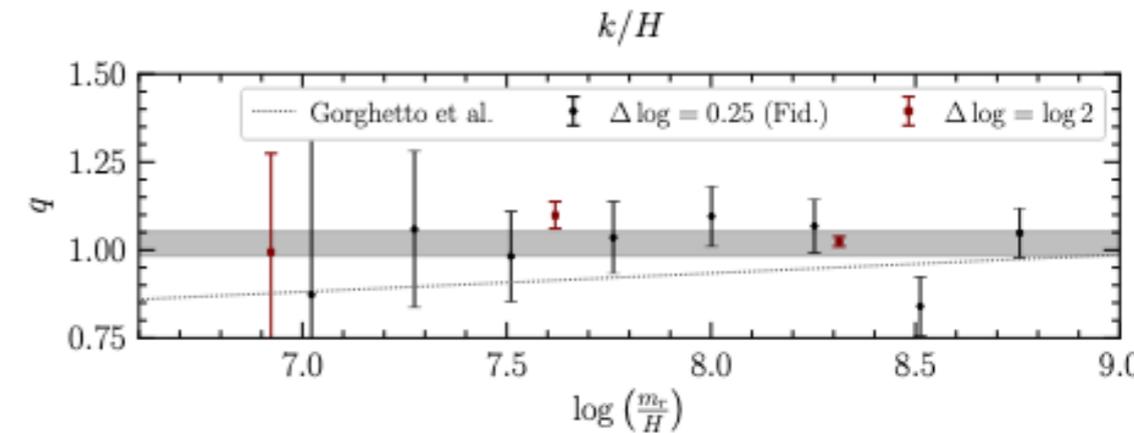
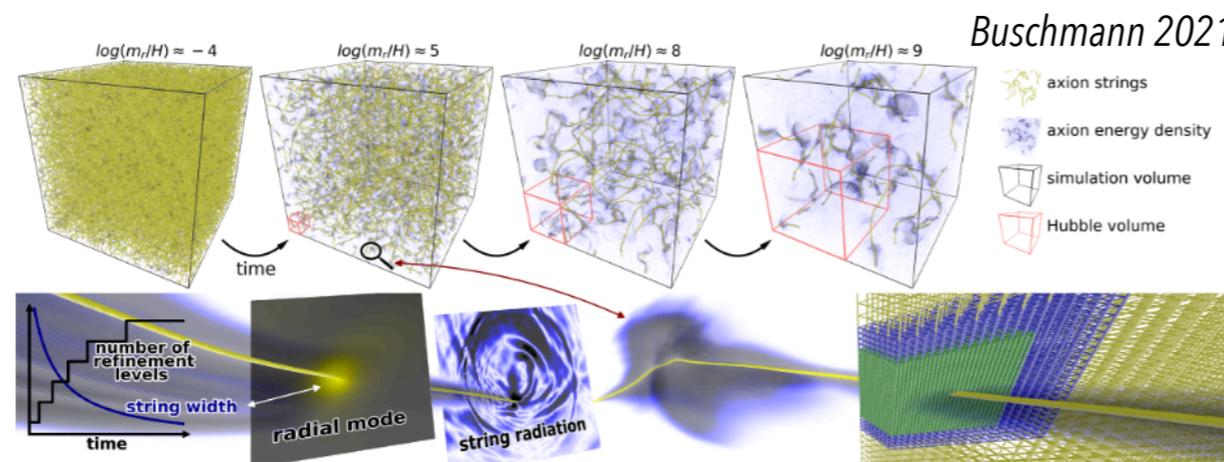
# Current plans ...

- Numerical simulations ( $4000^3$ ,  $1100^3$ ) reach almost the critical value

$$n_a(t) \approx \frac{8H\xi(t)\mu_{\text{eff}}(t)}{x_0} \times \begin{cases} 1 - 1/q & q > \\ \frac{1}{\log\left(\frac{m_r}{Hx_0}\right)} & q = \\ \frac{1-q}{q(2q-1)} \left[\frac{Hx_0}{m_r}\right]^{1-q} & \frac{1}{2} < q < \end{cases}$$



- AMR can give us a few extra factors of 2 to reach 9~10 (theoretically up to 12)

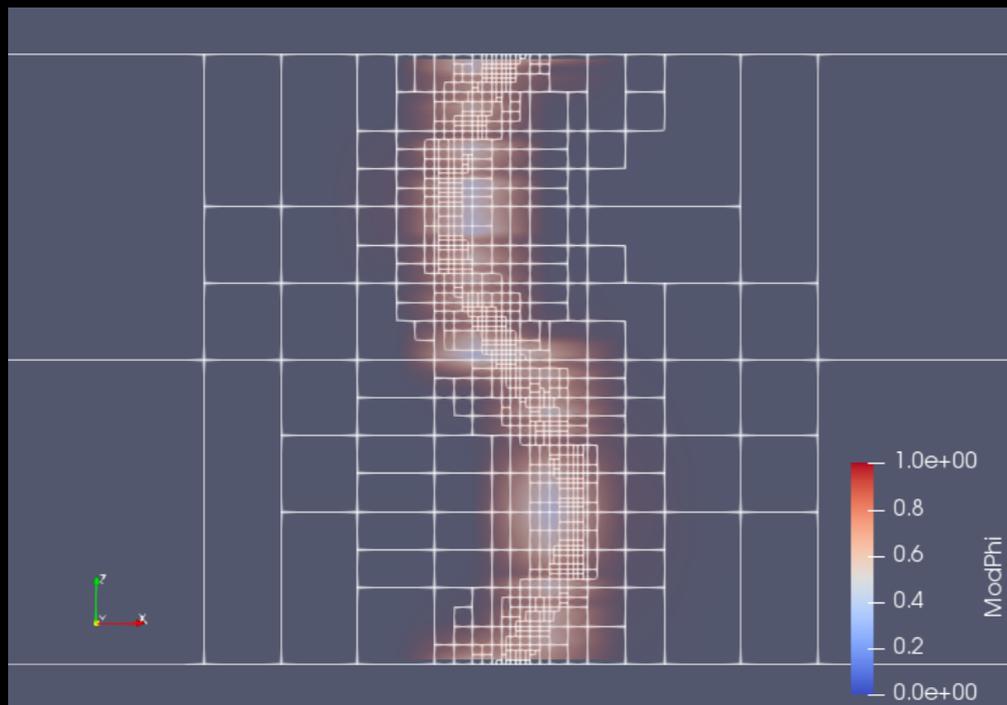


# Adaptive Mesh Refinement

## For strings...

### Fixed Grid

- $\Delta x$  fixed throughout the simulation
- For  $\delta \sim 1$  strings, must use at least  $\Delta x \sim 0.5$
- Computational resources typically limit to  $\sim 4096^3$  grid points,  $\ln(R/\delta) \sim 8$



### AMR

- Enables increase  $\ln(R/\delta)$  with fixed (limited) resources
- E.g. equivalent  $\ln(R/\delta) \sim 8$  simulation ran on **32x fewer processors AND multiple 10x faster using AMR**

$\mathcal{O}(\text{days}) \rightarrow \mathcal{O}(\text{hours})$

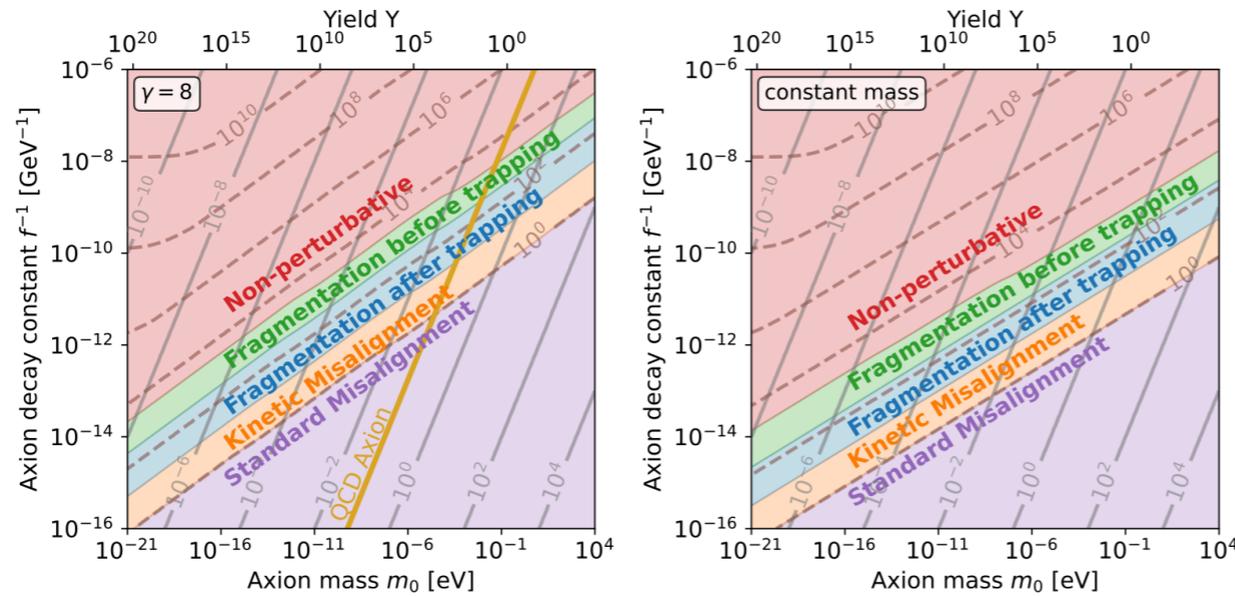
- Should comfortably achieve  $\ln(R/\delta) \sim 10$  or higher with same resources
- Equivalent fixed grid would need fixed grid of *at least*  $> 65000^3$  for same box size

**Bonus: potential for even further speedups with GPU support**

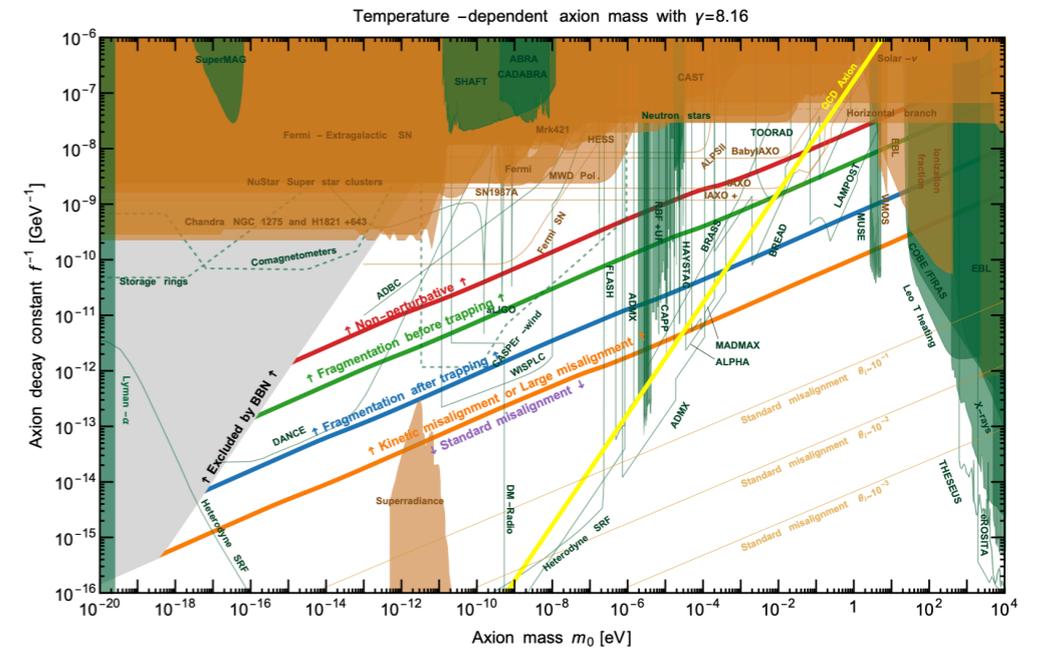
# Simulations for "pre-inflation" non-linear scenarios

Use our very powerful codes for these rare non-linear scenarios

## kinetic misalignment

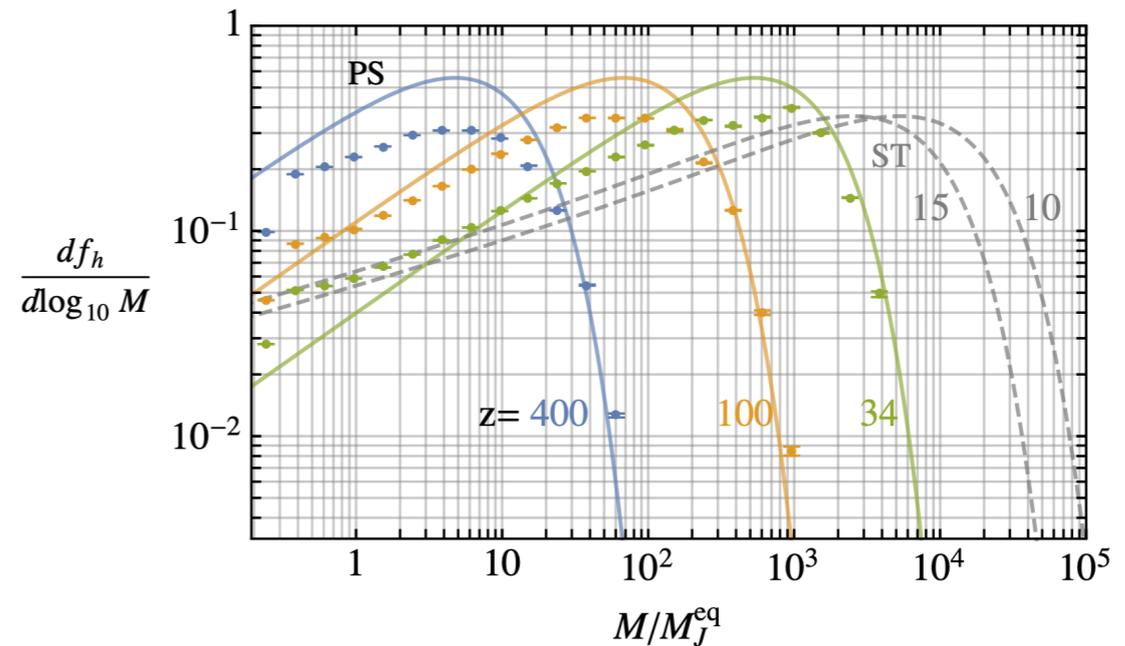
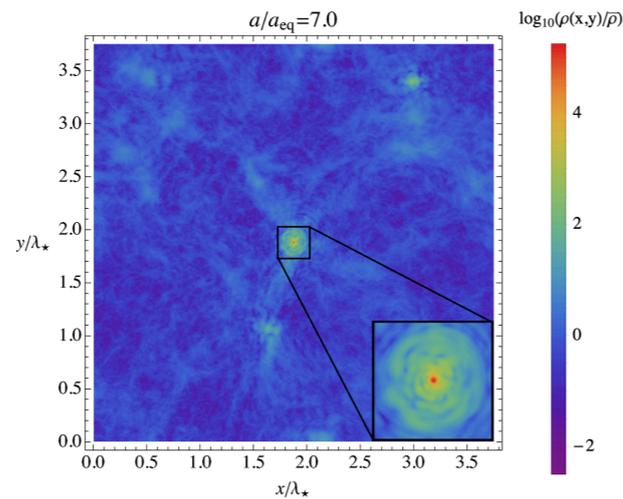


Eröncel 22



theta~pi ?

## dark photons (and stars) Gorghetto 22



NDW > 1 Saikawa 15, Gorghetto 21, 22

# Small structure

**Axion minihalos and axion stars (same for dark photons)**

**Seeds in early Universe:**

**Gravitational collapse around  $z_{\text{eq}}$**

**Hierarchical growth**

**Survival in the galaxy**

**DM field in the galaxy (voids?) see talk of Giovanni Pierobon**

**Microlensing**

**Collisions with compacts, radio signals**

# Small structure

## Axion minihalos and axion stars (same for dark photons)

### Seeds in early Universe:

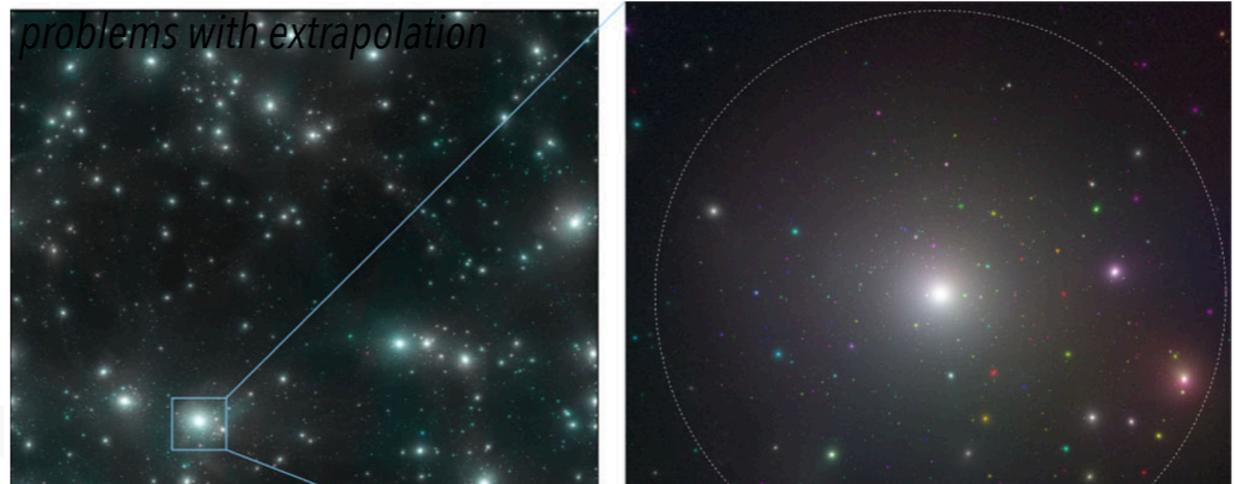
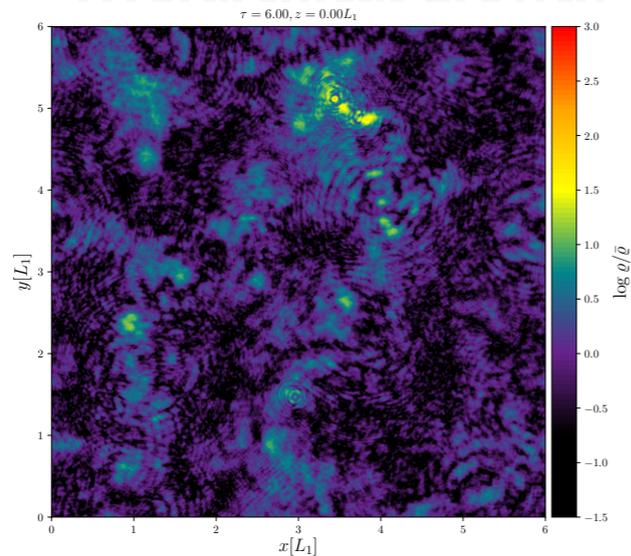
Redondo 18, Buschmann 19, Gorghetto 22

### Gravitational collapse around $z_{eq}$

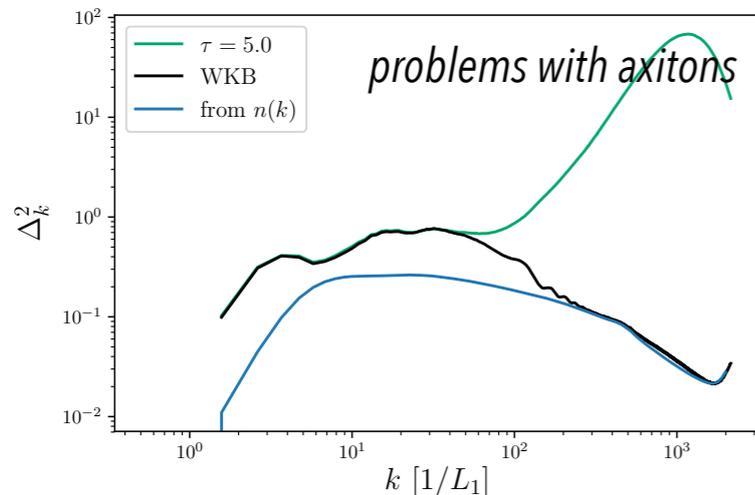
Simulations with Strings, other needed, problems with extrapolation

large scales are trustable, convert to N-body and simulate gravity

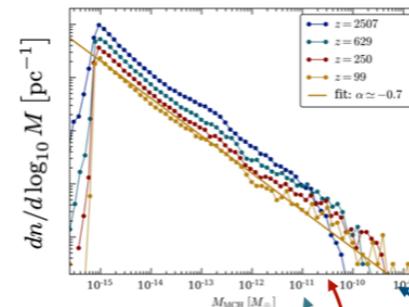
Eggemeier 20



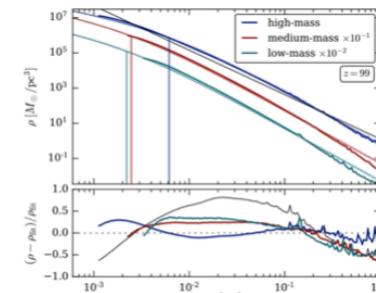
- Large simulation ( $N=1024^3$  particles) in a Large box ( $L=24 L_1$ ) simulated with jaxions in a  $8192^3$  grid
- Periodic boundaries, volume effects when smallest scale becomes non-linear



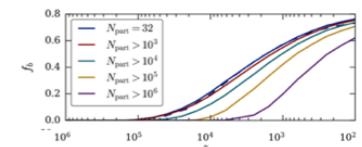
problems with axitons



- Loads of low-M MCs
- Spherical collapse with  $\Phi = \langle \delta \rangle \sim 1$  at  $z \sim z_{eq} \Phi$
- Typical MC  $\Phi \sim 1 \rightarrow M_0 \sim 10^{-11} M_\odot$
- Clusters of miniclusters  $\Phi < 1$



- NFW reasonable fit
- better than  $r^{-9/4}$  (accretion)
- concentration  $\sim M$  not well resolved for small M



- Nearly 80% of axions bound in MCs!!
- Tidal disruption with galaxy stars can lower the number
- Most axions in Massive MCs
- Mean MC has low mass

# Small structure

## Axion minihalos and axion stars (same for dark photons)

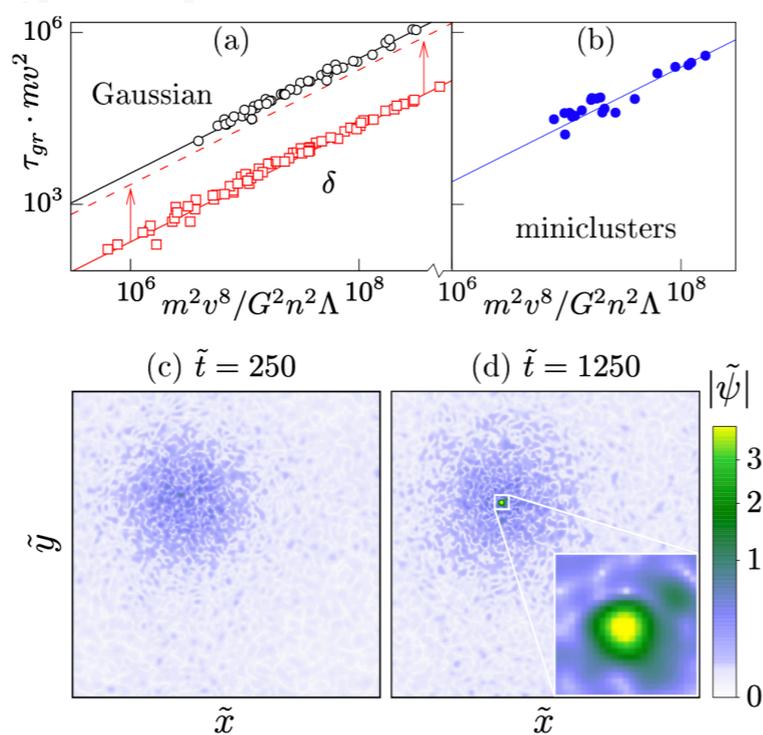
Seeds in early Universe:

Redondo 18, Buschmann 19, Gorghetto 22

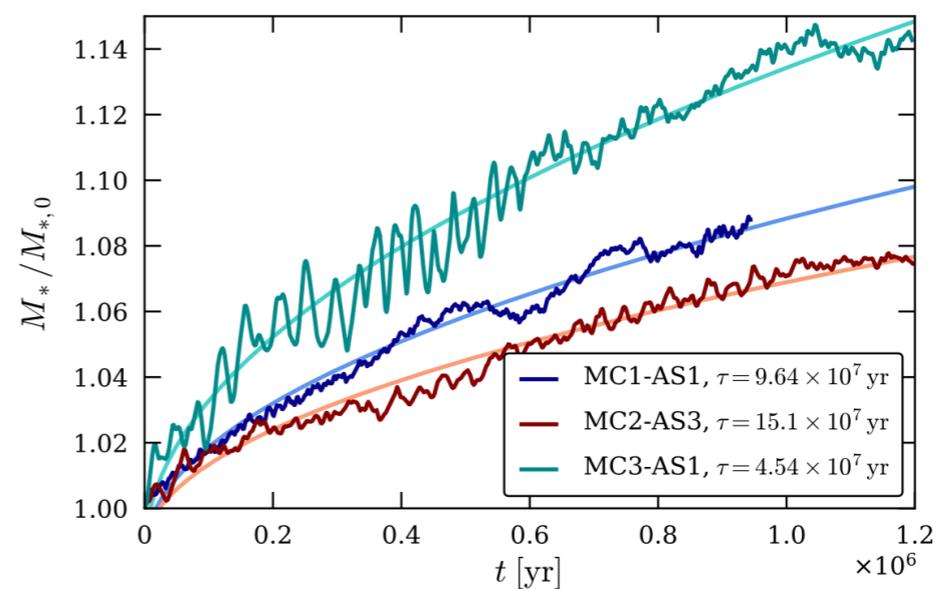
Gravitational collapse around  $z_{eq}$

Formation and Growth of axion stars in MCs

Levkov 18



Eggemeier 19



# Small structure

## Axion minihalos and axion stars (same for dark photons)

Seeds in early Universe:

Gravitational collapse around  $z_{\text{eq}}$

**Hyerarchical growth** *partially addressed, not so complicated*

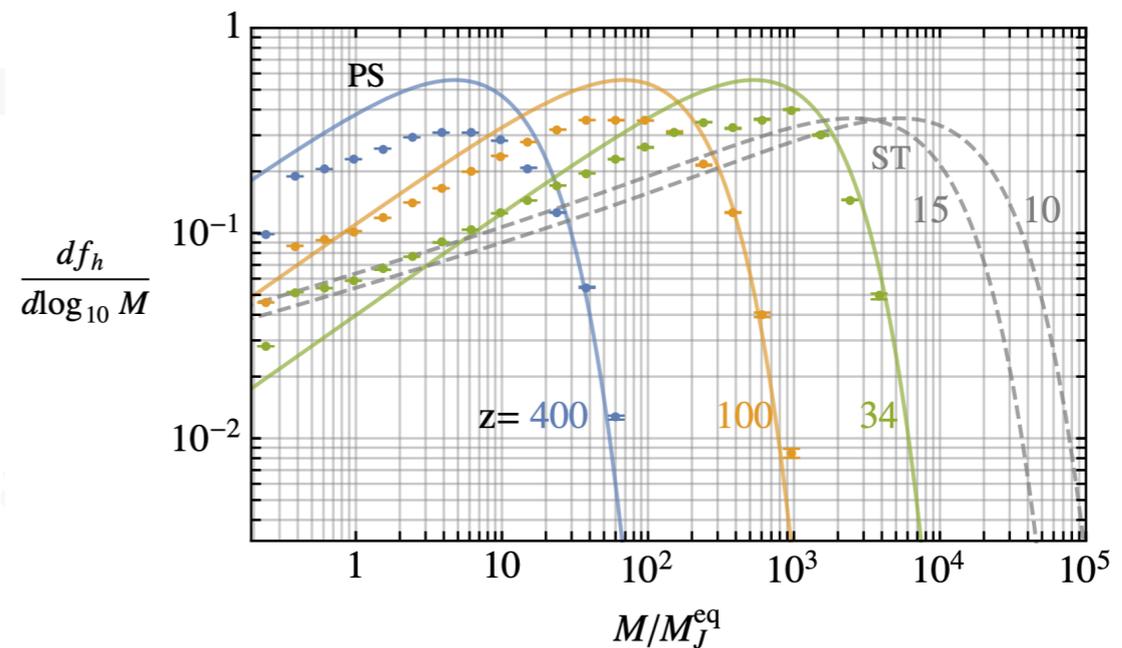
*Eggemeier 20, Gorghetto 22*

Survival in the galaxy

DM field in the galaxy (voids?) see 1

Microlensing

Collisions with compacts, radio sign



# Small structure

## Axion minihalos and axion stars (same for dark photons)

Seeds in early Universe:

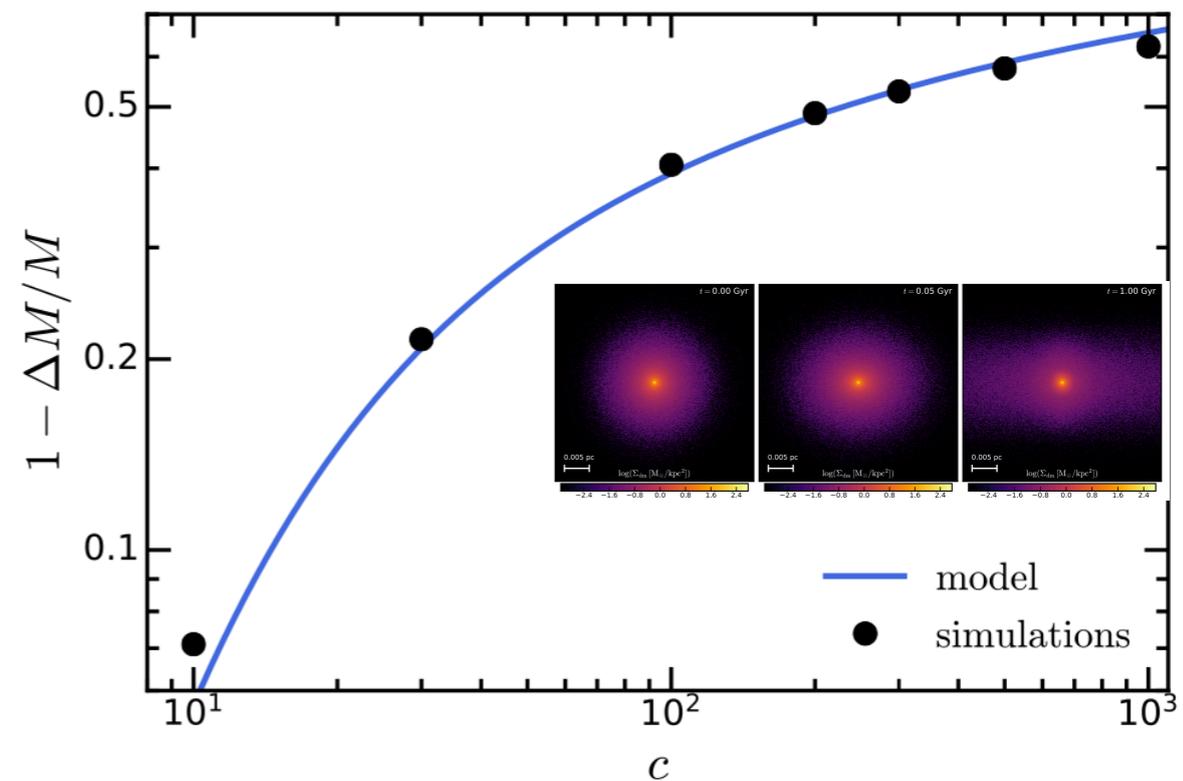
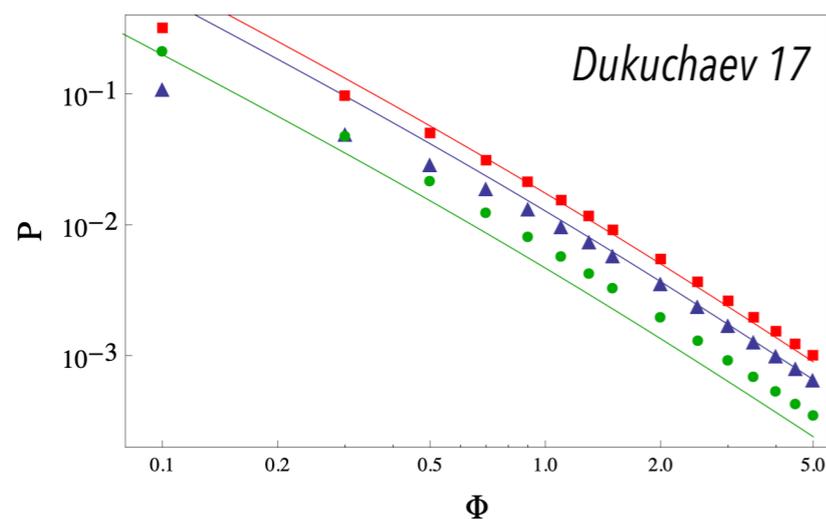
Gravitational collapse around  $z_{eq}$

Hierarchical growth

## Survival in the galaxy

*Dukuchaev 17, Kavanagh 21, Dandoy 22, Zurek 22*

Theoretical, montecarlo, numerical simulations, but not (much) feedback from Early Universe SIM-motivated properties (HMF, density profiles\*, etc..)



# Small structure

## Axion minihalos and axion stars (same for dark photons)

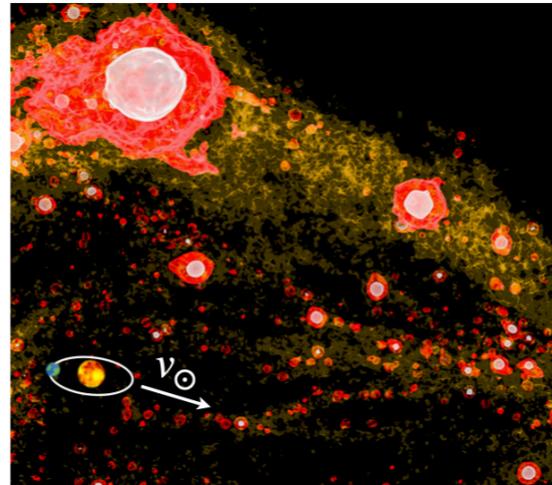
Seeds in early Universe:

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Survival in the galaxy

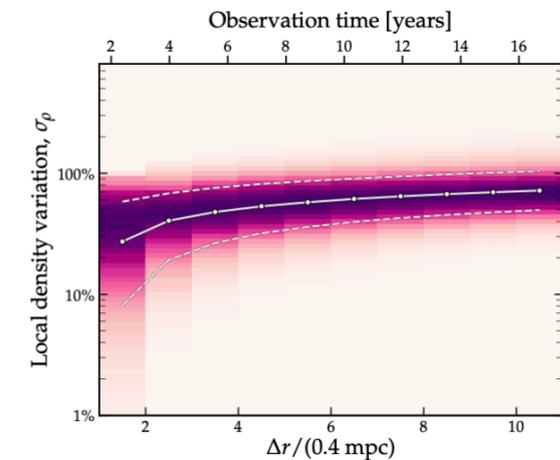
Volume rendering



$v_{\odot} \sim 220$  km/s

*Eggemeier, O'Hare, GP, Redondo, Wong, 2022*

$\mathcal{O}(10^5)$  trajectories  $\sigma_{\rho}(r) = \frac{1}{\langle \rho(r) \rangle_{\text{traj}}} \sqrt{\frac{1}{n_r} \sum_{i=1}^{n_r} (\rho(r_i) - \langle \rho(r) \rangle_{\text{traj}})^2}$



Expected variation of 20–30% for an observing time of  $\mathcal{O}(1)$  year

Almost 100% on even longer timescales

## DM field in the galaxy (voids?) see talk of Giovanni Pierobon

Relevant question for Direct Dark matter, first steps

Microlensing

Collisions with compacts, radio signals

# Small structure

## Axion minihalos and axion stars (same for dark photons)

Seeds in early Universe:

Gravitational collapse at

Hierarchical growth

Survival in the galaxy

DM field in the galaxy (voids?) see talk of

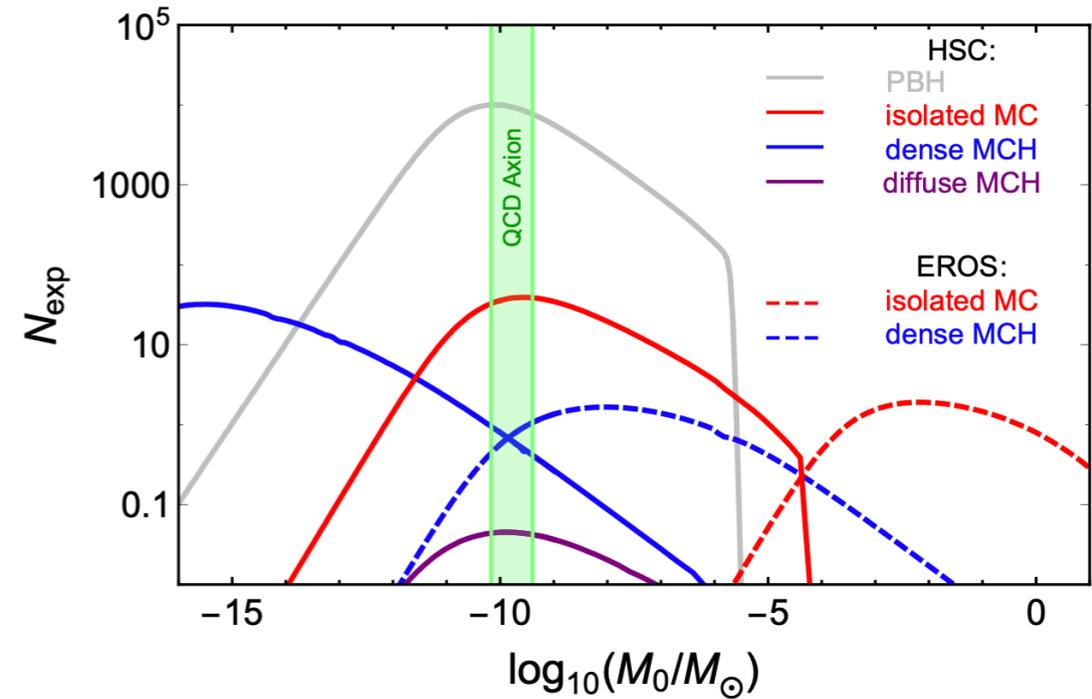
### Microlensing

Collisions with compacts, radio signals

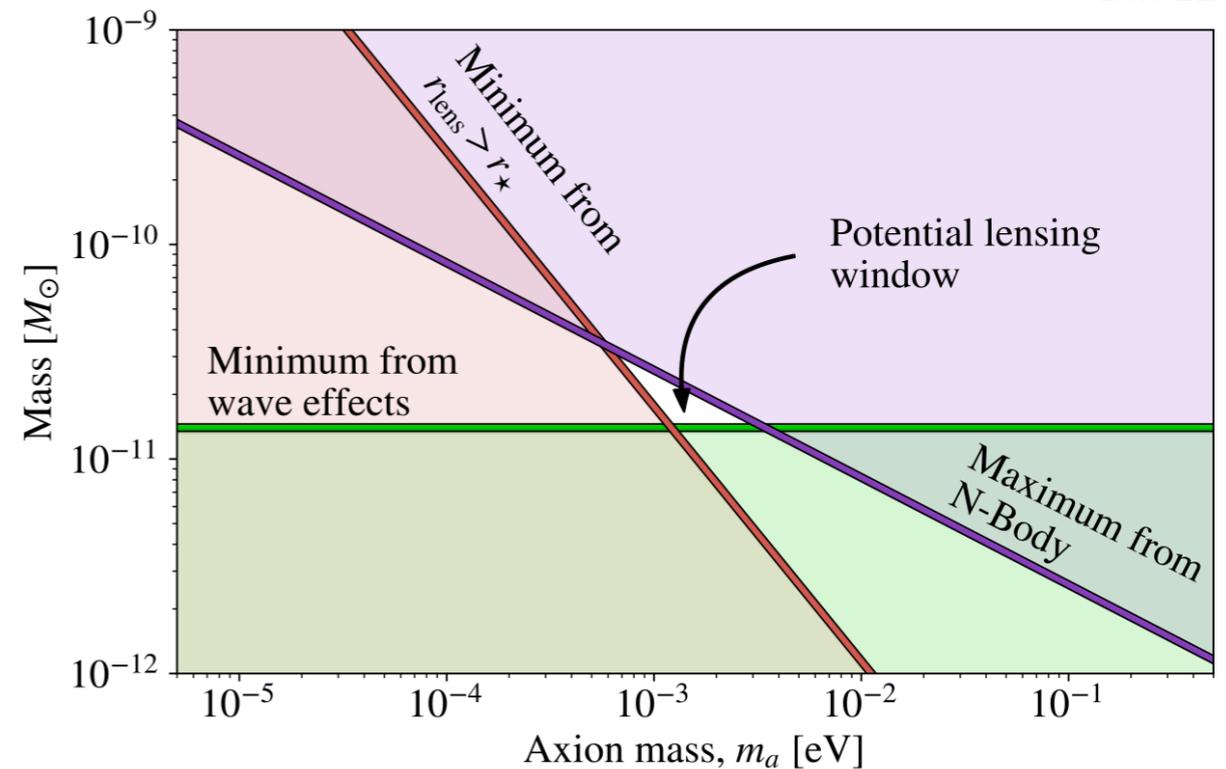
Theory expectations based on  
O(1) analytical properties  
were very optimistic

Expectations based on  
analytical properties from numerical  
simulations make it much harder  
BUT STILL the num. sims. are not FINAL

Fairbairn 17



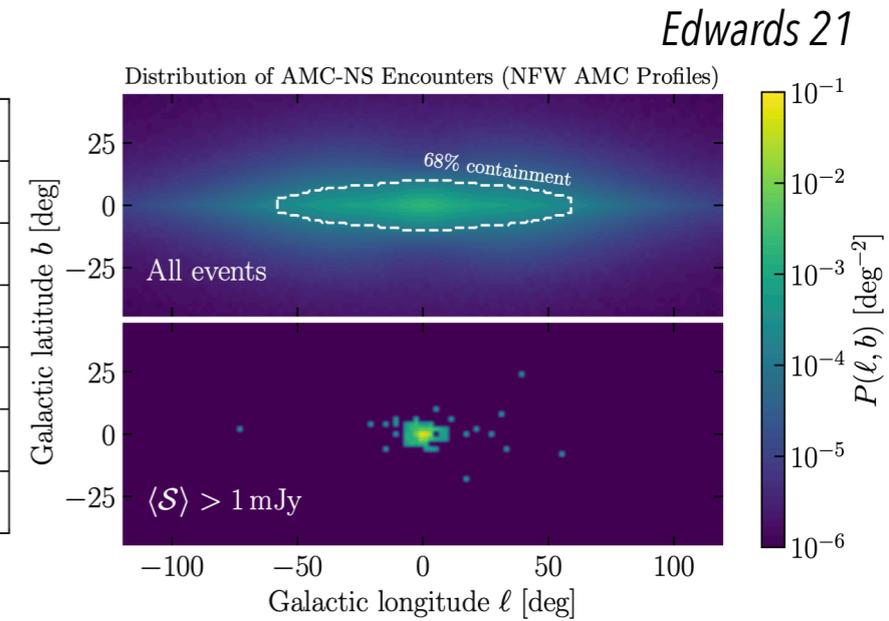
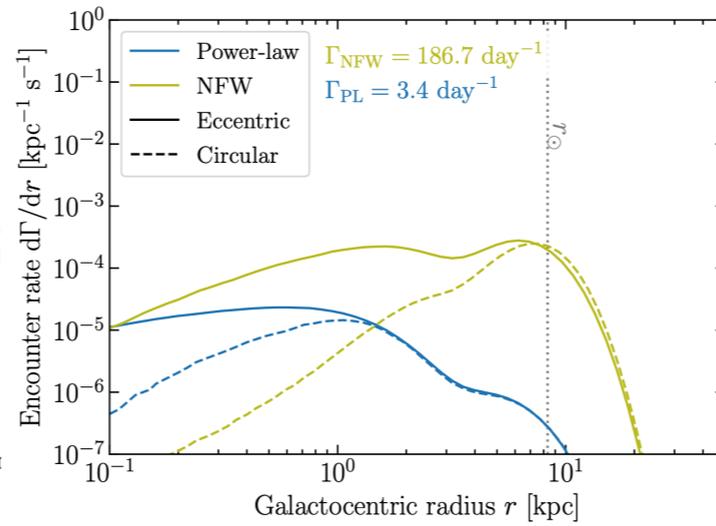
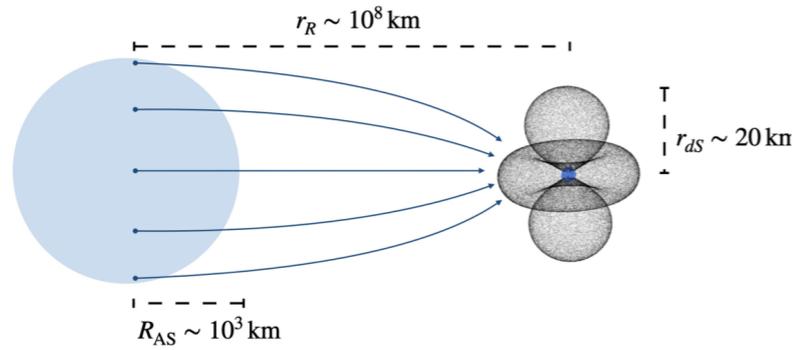
Ellis 22



# Small structure

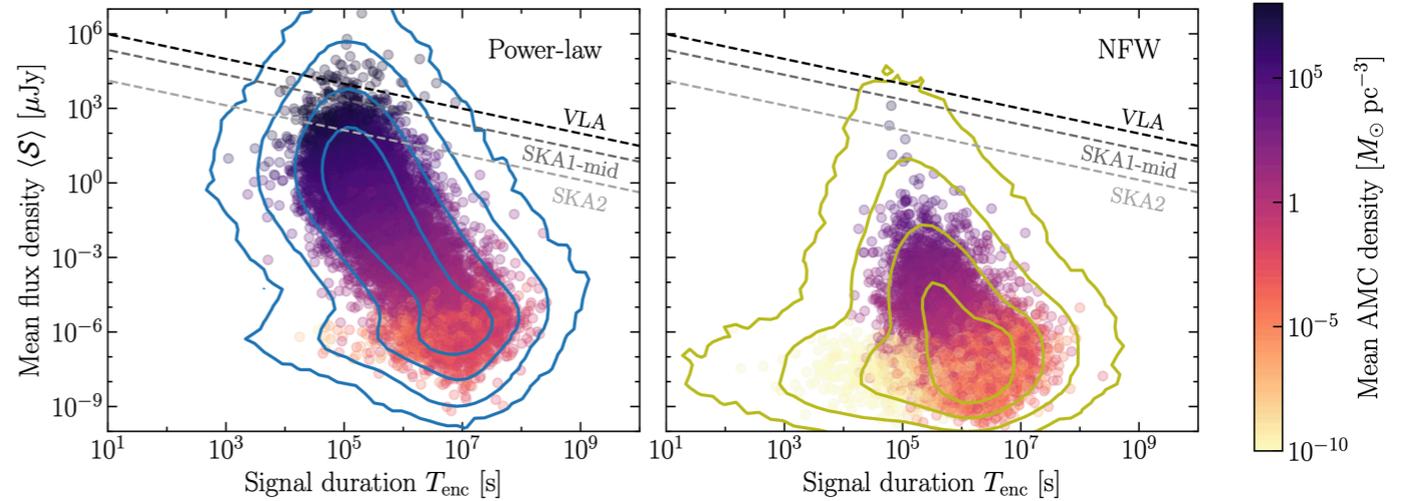
## Axion minihalos and axion stars (same for dark photons)

Seeds in early Universe:  
transient radio signals from  
MCs, axion stars in the B-field  
of neutron-stars  
Gravitational collapse around



DM field in the galaxy (voids?)

Microlensing



Collisions with compacts, radio signals

More recent assesment Witte 22

# Small structure

## Axion minihalos and axion stars (same for dark photons)

Seeds in early Universe

Gravitational collapse

Hierarchical growth

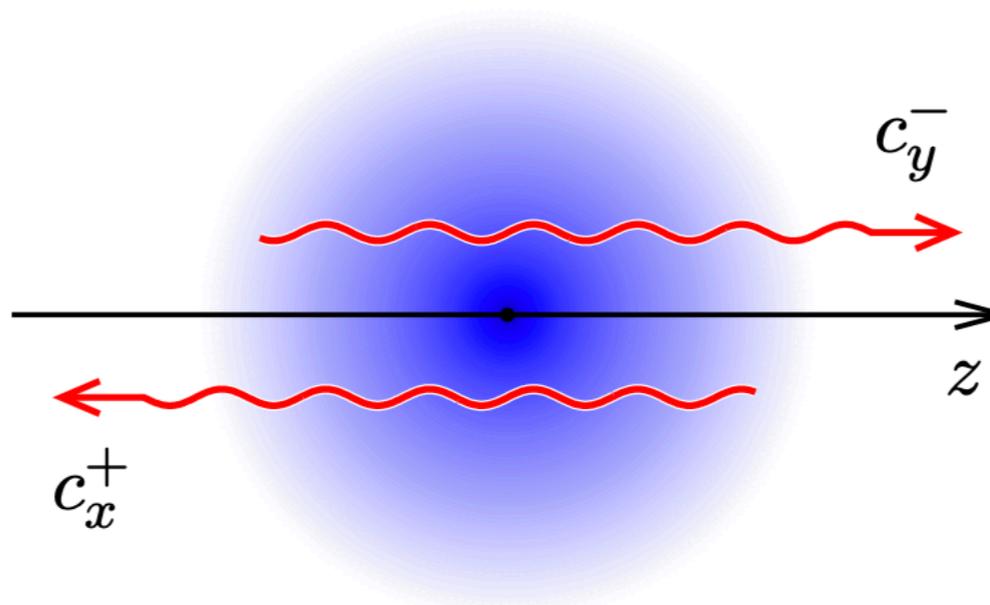
Survival in the galaxy

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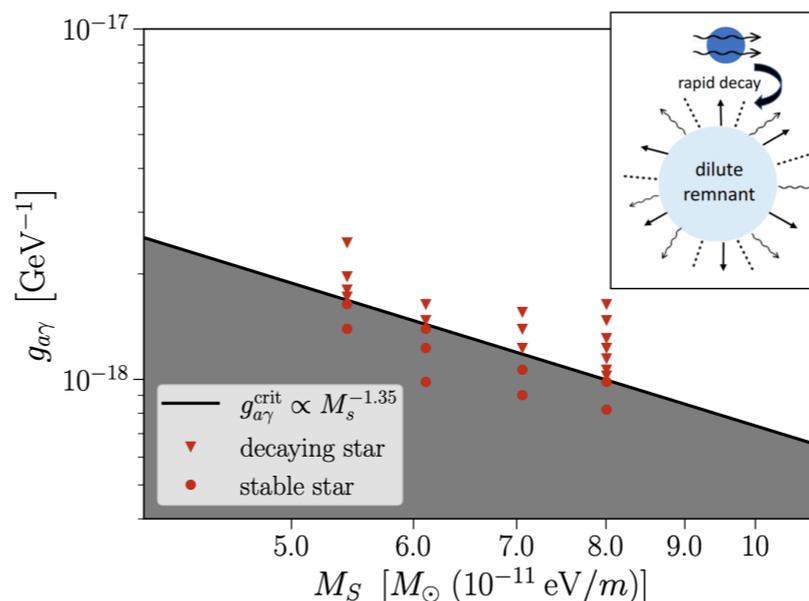
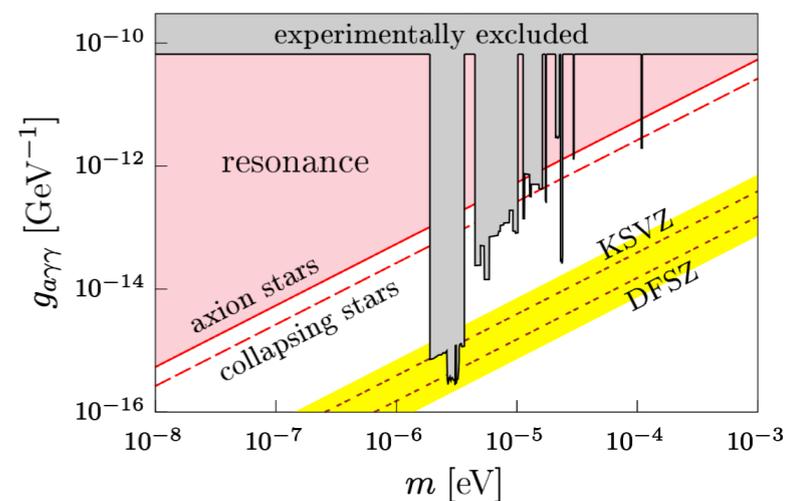
Microlensing

Collisions with compacts, radio

Parametric resonance



Levkov 21

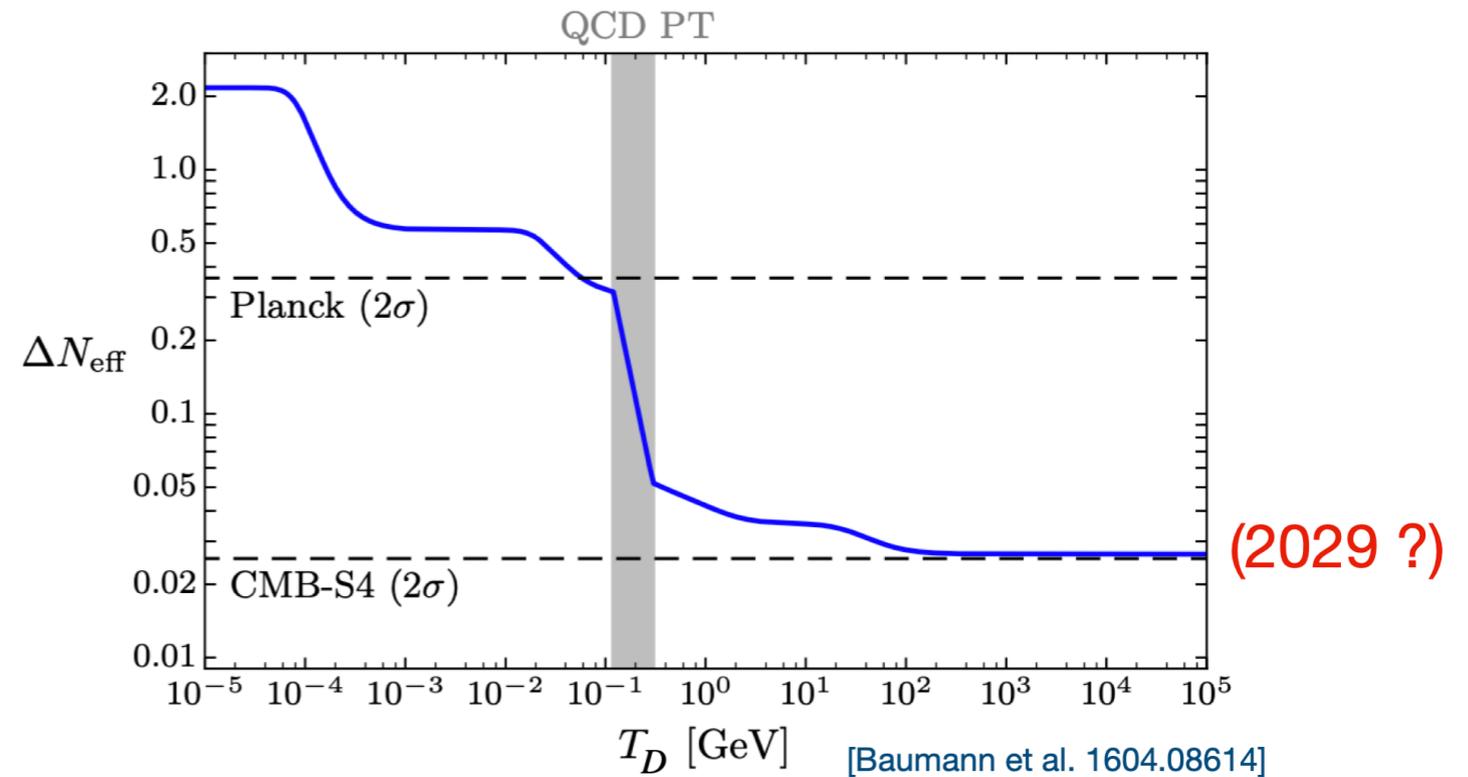


Jukko 23

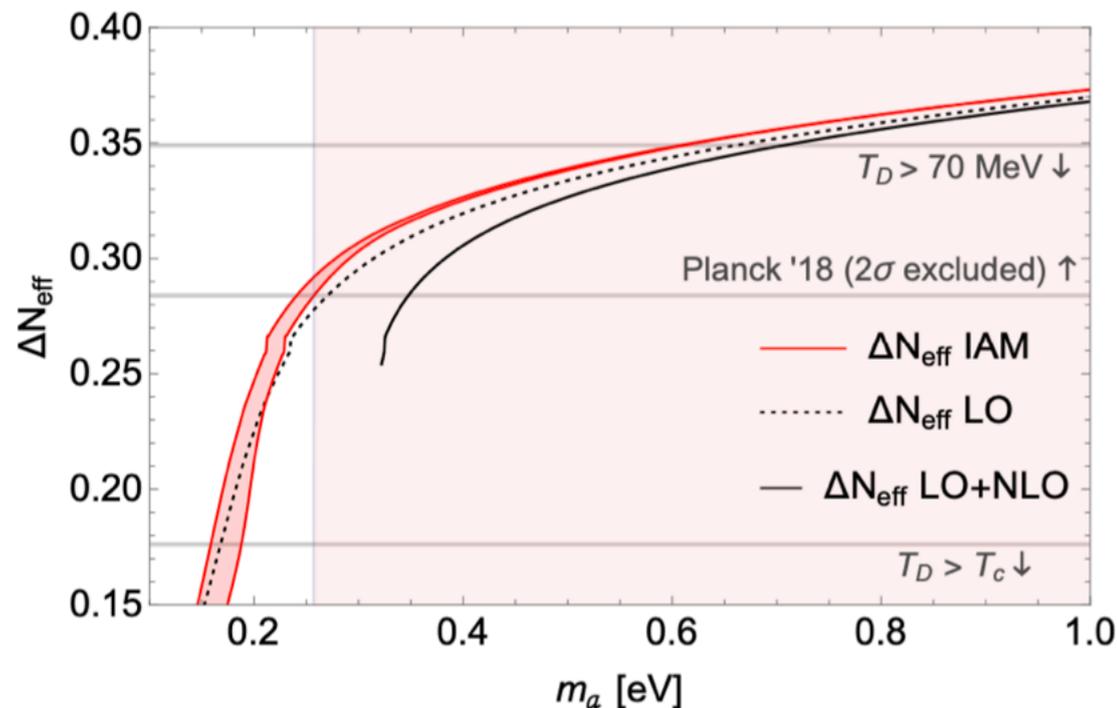
## Radio emission from axion stars

# hot DM

- CMB data can pinpoint dark radiation levels to  $N_{\text{eff}} \sim$  thermal axions decoupled above EWPT



- Calculations of decoupling around QCD PT were not reliable (LO CHPT) improved by Unitarisation



◆ LO and NLO ChPT reliable up to  $T_D = 70$  MeV

◆ IAM valid up to  $T_c \simeq 155$  MeV, gives a bound  $m_a \leq 0.26$  eV

Additional corrections needed for future sensitivities, K's,  $f_0(880)$ , thermal effects

# Large scale structure

- ``Large" mass WISPs

  - Strings outside the horizon (preinflation)** *Kaplan*

  - warm DM suppression of PS**

  - ...

- Ultra-light WISPs

  - Ly-alpha**

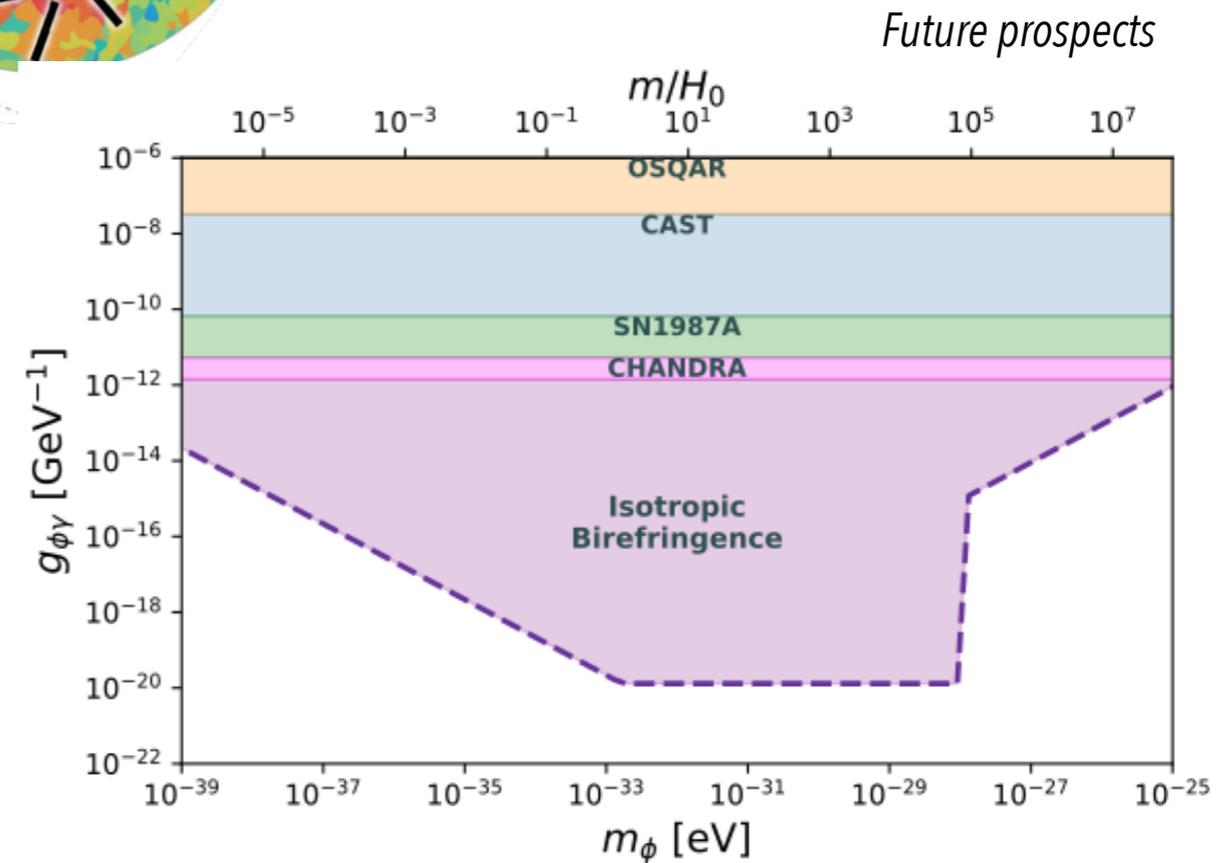
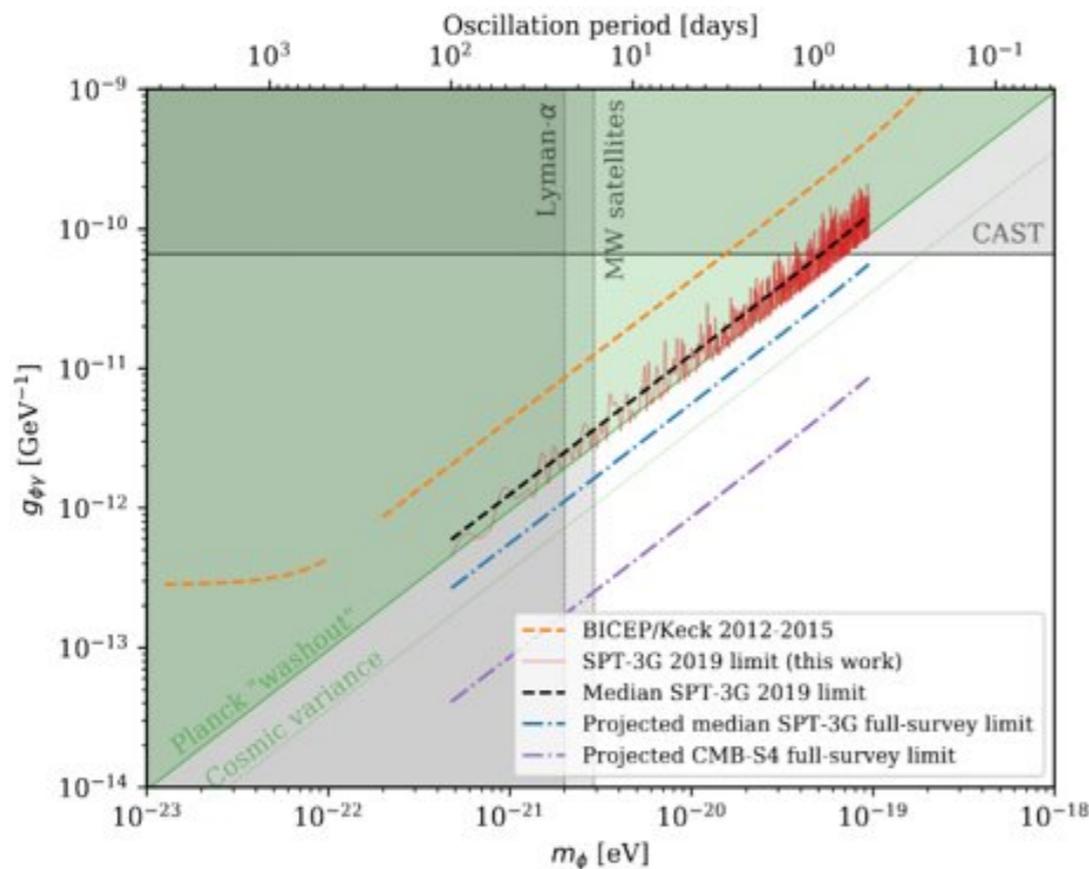
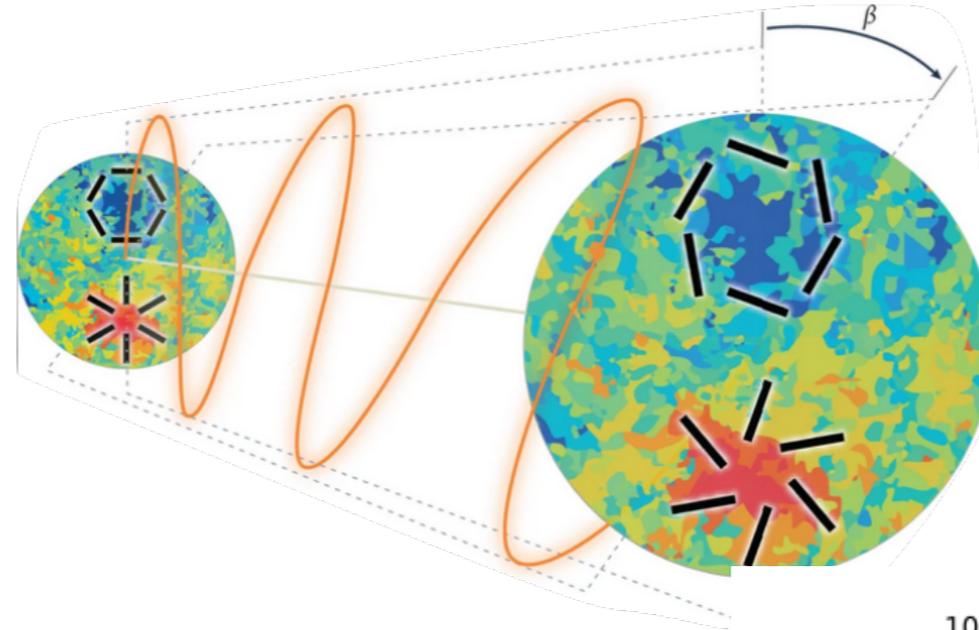
  - Power spectrum**

  - ...

# Cosmic birefringence

## ALP DM coupled to photons with extremely low mass rotates polarisation of CMB

See talk of P. Diego



What to expect in the near future:

- High-precision CMB polarisation data is on the way (SPT-3G, BICEP3, SO, LiteBIRD)
- Improved artificial calibrators are being deployed [exciting results coming soon from BICEP3!]
- Better understanding of Galactic dust EB

# Conclusions

- **Extremely exciting prospects and opportunities**
- **I have been quite biased (the art is broader than this meagre statement)**
- **QCD axion is somehow nicely covered by up-to-date studies but other WISPs much less**