



\*\*\*\* XVII SuperB Workshop and Kick Off Meeting \*\*\*\*

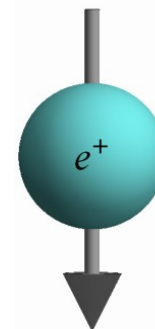
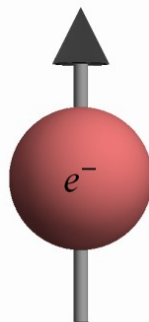
29/05-02/06 2011

La Biodola – Isola d'Elba – Italy

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# Time-dependent CP asymmetries in D (and B) decays

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# Outline

Motivations

The CKM matrix and the UT's

Time-dependent formalism (correlated mesons)

Analysis of CP eigenstates

$D^0 \rightarrow K^+ K^- , \pi^+ \pi^- , \rho^0 \rho^0$

Uncorrelated  $D^0$  mesons ( $\Upsilon(4S)$  and LHCb)

Conclusions

# Motivations (i)

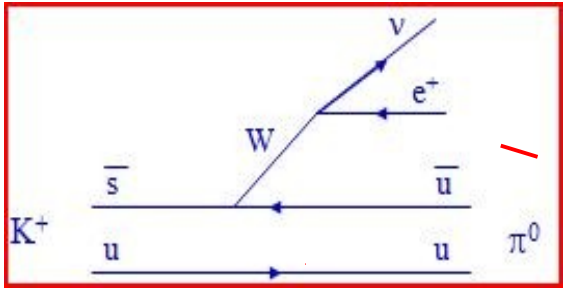
- Origin of CP violation is still one of the biggest questions in particle physics and cosmology today
- CP violation has not yet been observed in charm, and a time-dependent analysis has not been done yet
- Improvements in the precision and knowledge of the CKM unitarity triangle(s) is still possible
- SuperB will offer a unique environment to perform precision tests of the standard model

# CKM Matrix

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$c_{ij} = \cos \theta_{ij}; s_{ij} = \sin \theta_{ij}$ 
 $\delta = cp$  violating phase
 $s_{13} \ll s_{23} \ll s_{12} \ll 1$  (EXPERIMENTS)

**Wolfenstein parametrization**  
 expansion in terms of  $\sin \theta_c: V_{us} = 0.225 = \lambda \rightarrow V_{ud} = 1 - \frac{\lambda^2}{2} + O(\lambda^3)$



$$V_{CKM} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

CKM-M may be forced to be unitary to all order in  $\lambda$  !!

$$s_{12} = \lambda = \frac{|V_{us}|}{\sqrt{|V_{ud}|^2 + |V_{us}|^2}}; s_{23} = A\lambda^2 = \lambda \left| \frac{V_{cb}}{V_{us}} \right|;$$

$$s_{13} e^{i\delta} = V_{ub}^* = A\lambda^3(\rho + i\eta) = A\lambda^3(\bar{\rho} + i\bar{\eta}) \frac{\sqrt{1 - A^2\lambda^4}}{(\sqrt{1 - \lambda^2} \sqrt{1 - A^2\lambda^4(\bar{\rho} + i\bar{\eta})})}$$

# Buras parametrization: $\lambda^5$

*PDG standard parametrization with*

$$s_{12} = \lambda, \quad s_{13} \sin \delta_{13} = A \lambda^3 \eta, \quad \bar{\eta} = \eta \left[ 1 - \frac{\lambda^2}{2} + O(\lambda^4) \right]$$

$$s_{23} = A \lambda^2, \quad s_{13} \cos \delta_{13} = A \lambda^3 \rho, \quad \bar{\rho} = \rho \left[ 1 - \frac{\lambda^2}{2} + O(\lambda^4) \right]$$

$$V_{CKM} = \begin{pmatrix} 1 - \lambda^2/2 - \lambda^4/8 & \lambda & A \lambda^3 (\bar{\rho} - i\bar{\eta}) + A \lambda^5 (\bar{\rho} - i\bar{\eta})/2 \\ -\lambda + A^2 \lambda^5 [1 - 2(\bar{\rho} + i\bar{\eta})] & 1 - \lambda^2/2 - \lambda^4(1 + 4A^2)/8 & A \lambda^2 \\ A \lambda^3 [1 - (\bar{\rho} + i\bar{\eta})] & -A \lambda^2 + A \lambda^4 [1 - 2(\bar{\rho} + i\bar{\eta})]/2 & 1 - A^2 \lambda^4/2 \end{pmatrix} + O(\lambda^6)$$

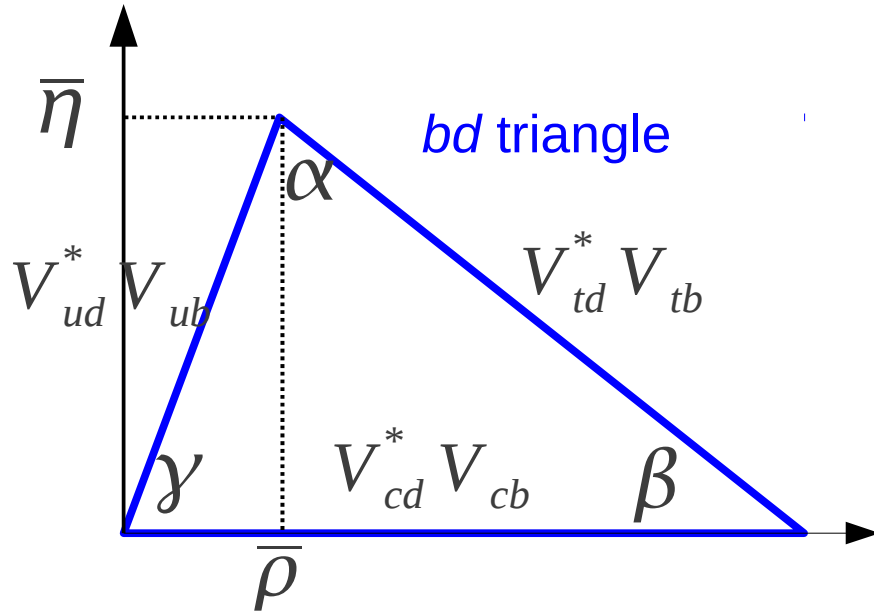
**TAB 1**

	UTFit	CKM Fitter
$\lambda$	$0.22545 \pm 0.00065$	$0.22543 \pm 0.00077$
$A$	$0.8095 \pm 0.0095$	$0.812^{+0.013}_{-0.027}$
$\rho$	$0.135 \pm 0.021$	-----
$\eta$	$0.367 \pm 0.013$	-----
$\bar{\rho}$	$0.132 \pm 0.020$	$0.144 \pm 0.025$
$\bar{\eta}$	$0.358 \pm 0.012$	$0.342 \pm 0.016$

Why do we express the matrix in terms of  $\bar{\rho} \bar{\eta}$ ?

# Unitarity triangles

Unitarity conditions of the CKM matrix are translated into 6 possible unitary triangles in the complex plane. We illustrate two here.



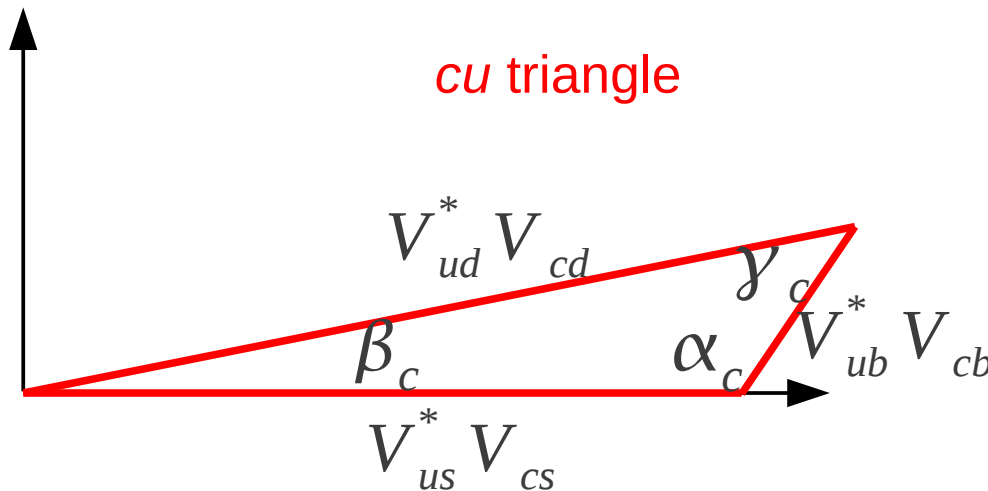
$$V_{ud}^* V_{ub} + V_{cd}^* V_{cb} + V_{td}^* V_{tb} = 0$$

$$\alpha = \arg\left[\frac{-V_{td}^* V_{tb}}{V_{ud}^* V_{ub}}\right] = (91.4 \pm 6.1)^\circ$$

$$\beta = \arg\left[\frac{-V_{cd}^* V_{cb}}{V_{td}^* V_{tb}}\right] = (21.1 \pm 0.9)^\circ$$

$$\gamma = \arg\left[\frac{-V_{ud}^* V_{ub}}{V_{cd}^* V_{cb}}\right] = (74 \pm 11)^\circ$$

FROM  
EXPERIMENTS



$$V_{ud}^* V_{cd} + V_{us}^* V_{cs} + V_{ub}^* V_{cb} = 0$$

$$\alpha_c = \arg\left[\frac{-V_{ub}^* V_{cb}}{V_{us}^* V_{cs}}\right] = (111.5 \pm 4.2)^\circ$$

$$\beta_c = \arg\left[\frac{-V_{ud}^* V_{cd}}{V_{us}^* V_{cs}}\right] = (0.0350 \pm 0.0001)^\circ$$

$$\gamma_c = \arg\left[\frac{-V_{ub}^* V_{cb}}{V_{ud}^* V_{cd}}\right] = (68.4 \pm 0.1)^\circ$$

AVERAGE  
OF VALUES  
IN TAB 1

# What we are doing

Bigi and Sanda ( hep-ph/9909479v2) pointed out that  $\beta_c$  is one of two other angles that should be measured ( the other is  $\beta_s$  ).

We explore the potential to study this (tri)angle for the first time.

It is unlikely we can measure  $\beta_c$  (<0.1 degrees) to high precision, but a larger value would signify new physics.

A TDCPV analysis can measure  $2\beta_c + \Phi_{MIX}$  . Current mixing phase average value is 10 degrees.

The mixing angle  $\Phi_{MIX}$  is intrinsically interesting, and can, otherwise, only be measured in time-dependent Dalitz plot analyses of D0 to self-conjugate final states.

# Time-dependent formalism (i)

Neutral meson systems exhibit mixing of mass eigenstates  $|P_{1,2}\rangle$  where:

$$i \frac{d}{dt} \begin{pmatrix} |P_1\rangle \\ |P_2\rangle \end{pmatrix} = \begin{pmatrix} M_{11} - \frac{i}{2} \Gamma_{11} & M_{12} - \frac{i}{2} \Gamma_{12} \\ M_{12}^* - \frac{i}{2} \Gamma_{12}^* & M_{22} - \frac{i}{2} \Gamma_{22} \end{pmatrix} \begin{pmatrix} |P^0\rangle \\ |\bar{P}^0\rangle \end{pmatrix} = H_{eff} \begin{pmatrix} |P^0\rangle \\ |\bar{P}^0\rangle \end{pmatrix}$$

$$|P_{1,2}\rangle = p |P^0\rangle \pm q |\bar{P}^0\rangle \quad \begin{matrix} \nearrow q^2 + p^2 = 1 \text{ normalize the wavefunction} \\ \searrow \frac{q}{p} = \sqrt{\frac{m_{12}^* - i\Gamma_{12}^*/2}{M_{12} - i\Gamma_{12}/2}} \end{matrix}$$

$$H_{eff} = M - \frac{i}{2} \Gamma \quad \begin{matrix} \nearrow M_{11} = M_{22}, \Gamma_{11} = \Gamma_{22} \leftarrow \text{CPT INVARIANCE} \\ \rightarrow M_{11} = M_{22}, \Gamma_{11} = \Gamma_{22}, \Im\left[\frac{\Gamma_{12}}{M_{12}}\right] = 0 \leftarrow \text{CP INVARIANCE} \\ \searrow \Im\left[\frac{\Gamma_{12}}{M_{12}}\right] = 0 \leftarrow \text{T INVARIANCE} \end{matrix}$$

$$\frac{d}{dt} \langle \Psi(t) | \Psi(t) \rangle = - \langle \Psi(t) | \Gamma | \Psi(t) \rangle$$



# Time-dependent formalism (ii)

The time-dependence of decays of  $P^0$  ( $\bar{P}^0$ ) to final state  $|f\rangle$  are:

$$\Gamma(P^0 \rightarrow f) \propto e^{-\Gamma_1 |\Delta t|} \left[ \frac{h_+}{2} + \frac{\Re(\lambda_f)}{1 + |\lambda_f|^2} h_- + e^{[\Delta\Gamma|\Delta t|/2]} \left( \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \cos \Delta M \Delta t - \frac{2 \Im(\lambda_f)}{1 + |\lambda_f|^2} \sin \Delta M \Delta t \right) \right]$$

$$\bar{\Gamma}(\bar{P}^0 \rightarrow f) \propto e^{-\Gamma_1 |\Delta t|} \left[ \frac{h_+}{2} + \frac{\Re(\lambda_f)}{1 + |\lambda_f|^2} h_- - e^{[\Delta\Gamma|\Delta t|/2]} \left( \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \cos \Delta M \Delta t - \frac{2 \Im(\lambda_f)}{1 + |\lambda_f|^2} \sin \Delta M \Delta t \right) \right]$$

where:  $h_{+-} = 1 \pm e^{\Delta\Gamma|\Delta t|}$ ,  $\lambda_f = \frac{q}{p} \frac{\bar{A}}{A}$   **$\lambda_f$  very important!**

We now obtain the time-dependent CP asymmetry

$$A(\Delta t) = \frac{\bar{\Gamma}(\Delta t) - \Gamma(\Delta t)}{\bar{\Gamma}(\Delta t) + \Gamma(\Delta t)} = 2 e^{\Delta\Gamma|\Delta t|/2} \frac{(|\lambda_f|^2 - 1) \cos \Delta M \Delta t + 2 \Im(\lambda_f) \sin \Delta M \Delta t}{(1 + |\lambda_f|^2) h_+ + 2 h_- \Re(\lambda_f)}$$

But real life differs.. (due to mis-tag probability)

# Mistag and Dilution

Non-trivial mis-tag probabilities from mis-reconstruction, wrongly associated slow pions, background, mixing of D meson used for tagging (small effect).

Mis-tag probability:  $\omega$  ( $\bar{\omega}$  for the anti-particle)

Dilution:  $D=1-2\omega$

If one defines:  $\Delta\omega=\omega-\bar{\omega}$

→ the dilution becomes:  $D+\Delta\omega=1-2\omega+\Delta\omega$

One can account for mis-tag probabilities by considering the **physical decay rate** as function of  $\Delta t$  (correlated pairs):

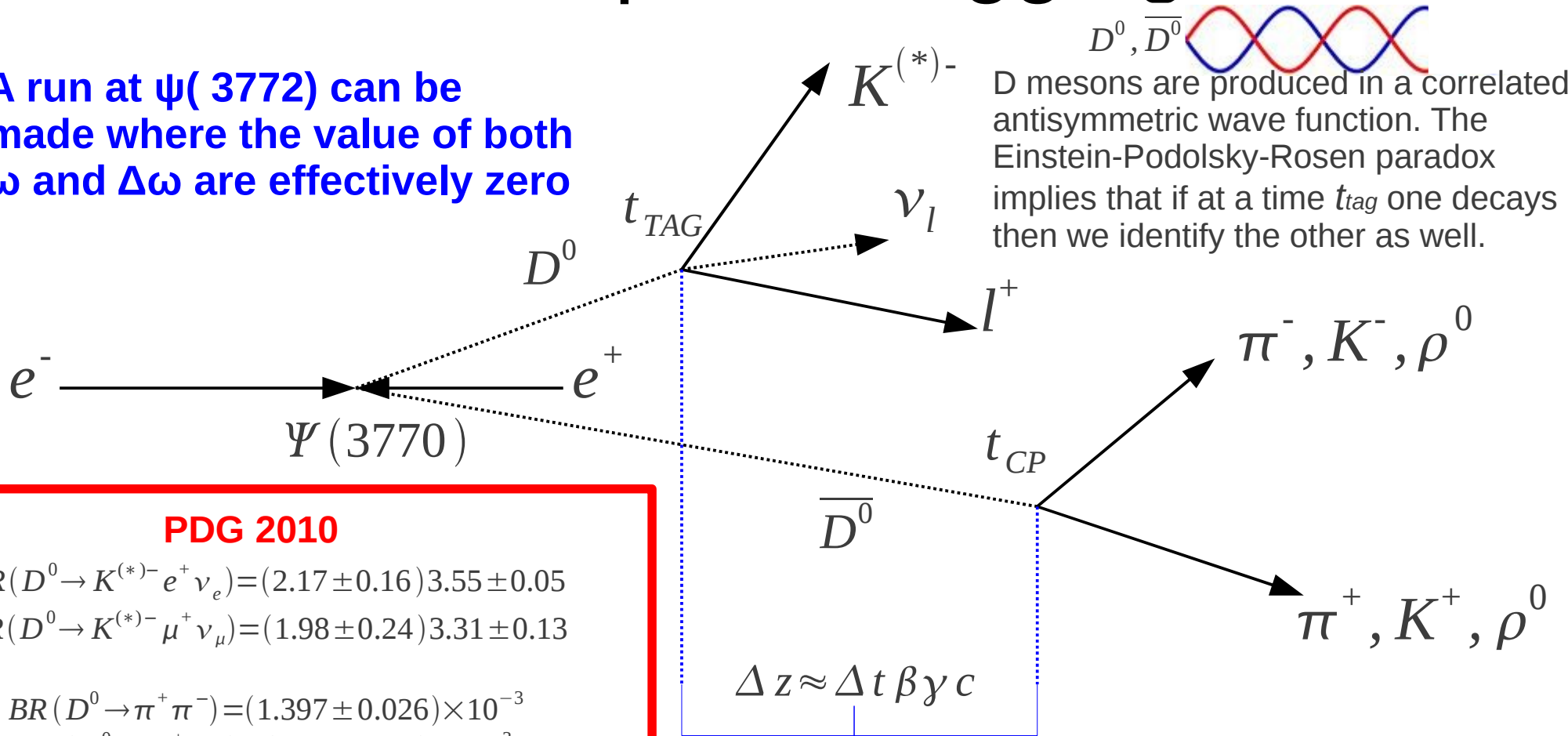
$$\Gamma^{Phys}(\Delta t) = (1 - \bar{\omega})\Gamma(\Delta t) + \omega\bar{\Gamma}(\Delta t)$$

$$\bar{\Gamma}^{Phys}(\Delta t) = \bar{\omega}\Gamma(\Delta t) + (1 - \omega)\bar{\Gamma}(\Delta t)$$

$$A^{Phys}(\Delta t) = \frac{\bar{\Gamma}^{Phys}(\Delta t) - \Gamma^{Phys}(\Delta t)}{\bar{\Gamma}^{Phys}(\Delta t) + \Gamma^{Phys}(\Delta t)} = -\Delta\omega + \frac{(D + \Delta\omega)e^{\Delta\Gamma|\Delta t|/2}(|\lambda_f|^2 - 1)\cos\Delta M\Delta t + 2\Im(\lambda_f)\sin\Delta M\Delta t}{(1 + |\lambda_f|^2)h_+/2 + h_-\Re(\lambda_f)}$$

# Semi-leptonic tagging

A run at  $\psi(3772)$  can be made where the value of both  $\omega$  and  $\Delta\omega$  are effectively zero



At time  $t_{TAG}$  the decays  $D \rightarrow K^{-(+) } l^{-(+) } \nu_l$  account for 11% of all  $D$  decays and unambiguously assigns the flavour:  $D^0$  is associated to a  $l^+$ ,  $\bar{D}^0$  is associated to a  $l^-$

Assuming PDG values for BR and CLEO\_c efficiency for double tagging we expect with semi-leptonic tag  $\sim 158000$  for  $D^0 \rightarrow \pi^+ \pi^-$

# Analysis of CP eigenstates (i)

When exploring CP violation, ignoring long distance effects, the parameter  $\lambda$  may be written as:

$$\lambda_f = \left| \frac{q}{p} \right| e^{i\phi_{MIX}} \left| \frac{\bar{A}}{A} \right| e^{i\phi_{CP}}$$

$\phi_{MIX}$  : phase of  $D^0 \bar{D}^0$  mixing  
 $\phi_{CP}$  : overall phase of  $D^0 \rightarrow f_{CP}$  (eigenstate)

$$A = |T| e^{i(\phi_T + \delta_T)} + |CS| e^{i(\phi_{CS} + \delta_{CS})} + |W| e^{i(\phi_W + \delta_W)} + \sum_{q=d,s,b} |P_q| e^{i(\phi_q + \delta_q)}$$

The following processes, as we will see, are tree dominated

$$D^0 \rightarrow K^+ K^-, \pi^+ \pi^-, K^+ K^- K^0, K^0 \pi^+ \pi^-$$

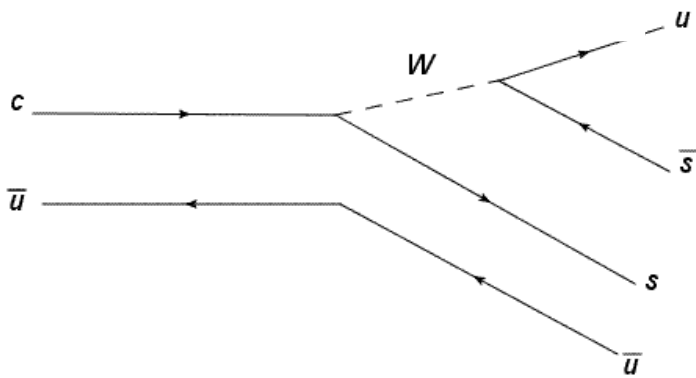
Assuming negligible the contribution due to P/CS/W amplitudes, then:

$$\lambda_f = \left| \frac{q}{p} \right| e^{i\phi_{MIX}} e^{+2i\phi_T^W}$$

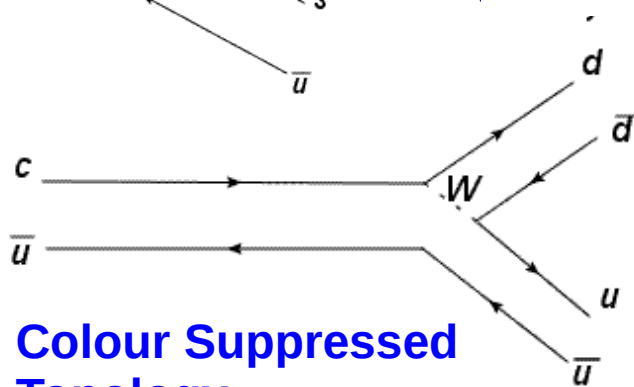
# Analysis of CP eigenstates (ii)

$$A = |T| e^{i(\phi_T + \delta_T)} + |CS| e^{i(\phi_{CS} + \delta_{CS})} + |W| e^{i(\phi_W + \delta_W)} + \sum_{q=d,s,b} |P_q| e^{i(\phi_q + \delta_q)}$$

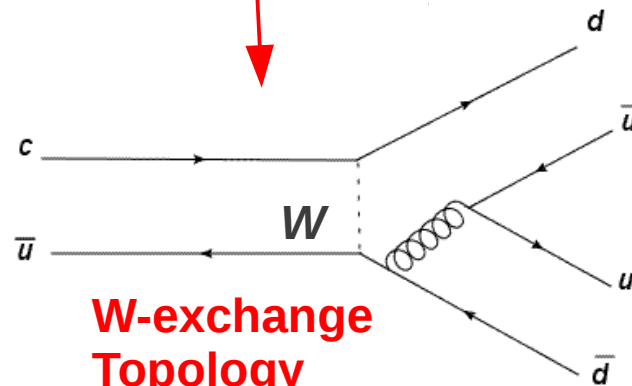
Tree  
Topology



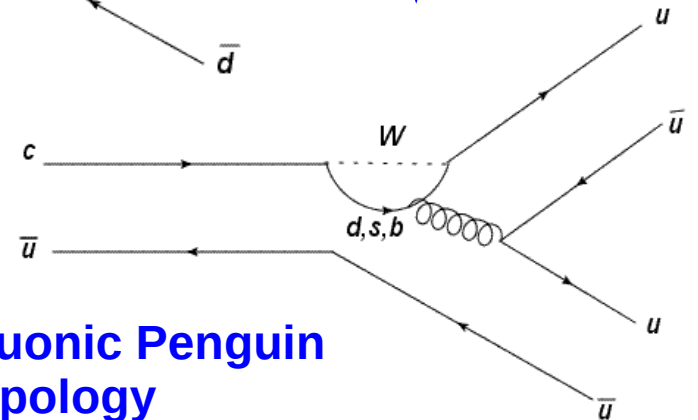
Colour Suppressed  
Topology



W-exchange  
Topology



Gluonic Penguin  
Topology



# Analysis of CP eigenstates (iii)

mode	$\eta_{CP}$	$T$	$CS$	$P_q$	$W_{EX}$
$D^0 \rightarrow K^+ K^-$	+1	$V_{cs} V_{us}^*$		$V_{cq} V_{uq}^*$	
$D^0 \rightarrow K_S^0 K_S^0$	+1				$V_{cs} V_{us}^* + V_{cd} V_{cd}^*$
$D^0 \rightarrow \pi^+ \pi^-$	+1	$V_{cd} V_{ud}^*$		$V_{cq} V_{uq}^*$	$V_{cd} V_{ud}^*$
$D^0 \rightarrow \pi^0 \pi^0$	+1		$V_{cd} V_{ud}^*$	$V_{cq} V_{uq}^*$	$V_{cd} V_{ud}^*$
$D^0 \rightarrow \rho^+ \rho^-$	+1	$V_{cd} V_{ud}^*$		$V_{cq} V_{uq}^*$	$V_{cd} V_{ud}^*$
$D^0 \rightarrow \rho^0 \rho^0$	+1		$V_{cd} V_{ud}^*$	$V_{cq} V_{uq}^*$	$V_{cd} V_{ud}^*$
$D^0 \rightarrow \phi \pi^0$	+1		$V_{cs} V_{us}^*$	$V_{cq} V_{uq}^*$	
$D^0 \rightarrow \phi \rho^0$	+1		$V_{cs} V_{us}^*$	$V_{cq} V_{uq}^*$	
$D^0 \rightarrow f^0(980) \pi^0$	-1		$V_{cs} V_{us}^* + V_{cd} V_{ud}^*$	$V_{cq} V_{uq}^*$	
$D^0 \rightarrow \rho^0 \pi^0$	+1		$V_{cd} V_{ud}^*$	$V_{cq} V_{uq}^*$	$V_{cd} V_{ud}^*$
$D^0 \rightarrow a^0 \pi^0$	-1		$V_{cd} V_{ud}^*$	$V_{cq} V_{uq}^*$	$V_{cd} V_{ud}^*$
$D^0 \rightarrow K_S^0 K_S^0 K_S^0$	+1				$V_{cs} V_{ud}^* + V_{cd} V_{us}^*$
$D^0 \rightarrow K_L^0 K_S^0 K_S^0$	-1				$V_{cs} V_{ud}^* + V_{cd} V_{us}^*$
$D^0 \rightarrow K_L^0 K_L^0 K_S^0$	+1				$V_{cs} V_{ud}^* + V_{cd} V_{us}^*$
$D^0 \rightarrow K_L^0 K_L^0 K_L^0$	-1				$V_{cs} V_{ud}^* + V_{cd} V_{us}^*$

# Analysis of CP eigenstates (iv)

Amplitude to order  $\lambda^6$ :

REAL  $\rightarrow V_{cs} V_{us}^* = \lambda - \frac{\lambda^3}{2} - \left( \frac{1}{8} + \frac{A^2}{2} \right) \lambda^5,$

COMPLEX  $\rightarrow V_{cd} V_{ud}^* = -\lambda + \frac{\lambda^3}{2} + \frac{\lambda^5}{8} + \frac{A^2 \lambda^5}{2} [1 - 2(\bar{\rho} + i\bar{\eta})]$

$\rightarrow V_{cb} V_{ub}^* = A^2 \lambda^5 (\bar{\rho} + i\bar{\eta}),$

REAL  $\rightarrow V_{cd} V_{cd}^* = \lambda^2 - \lambda^6 A^2 [1 - 2\bar{\rho}],$

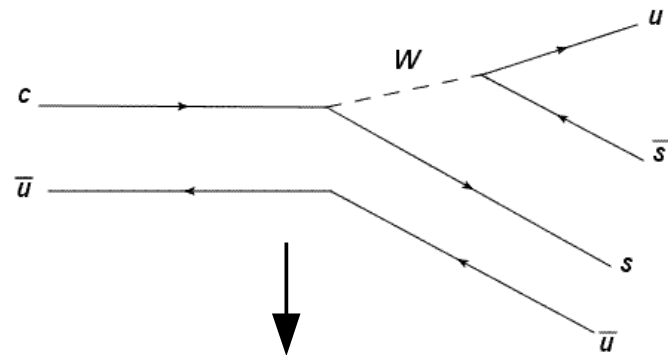
$\rightarrow V_{cs} V_{ud}^* = 1 - \lambda^2 - \frac{A^2 \lambda^4}{2} + A^2 \lambda^6 \left[ \frac{1}{2} - \bar{\rho} - i\bar{\eta} \right]$

COMPLEX  $\rightarrow V_{cd} V_{us}^* = -\lambda^2 + \frac{A^2 \lambda^6}{2} [1 - 2(\bar{\rho} + i\bar{\eta})].$

$V_{cb} V_{ub}^*$  large phase :  $V_{ub} \rightarrow \gamma_c = \gamma$   
 $V_{cd} V_{ud}^*$  and  $V_{cd} V_{us}^*$  small phase :  $V_{cd} \rightarrow \beta_c$   
 $V_{cs} V_{ud}^*$  small phase entering at  $O(\lambda^6)$

# $D^0 \rightarrow K^+ K^-$

Tree topology

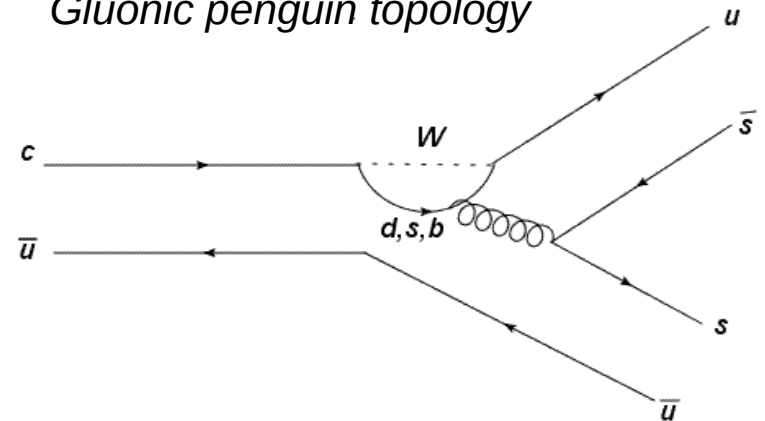


$$V_{cs} V_{us}^*$$

$$V_{cs} V_{us}^* = \lambda - \frac{\lambda^3}{2} - \left( \frac{1}{8} + \frac{A^2}{2} \right) \lambda^5$$

**Real**

Gluonic penguin topology



$$V_{cd} V_{ud}^* + V_{cs} V_{us}^* + V_{cb} V_{ub}^*$$

**Real**

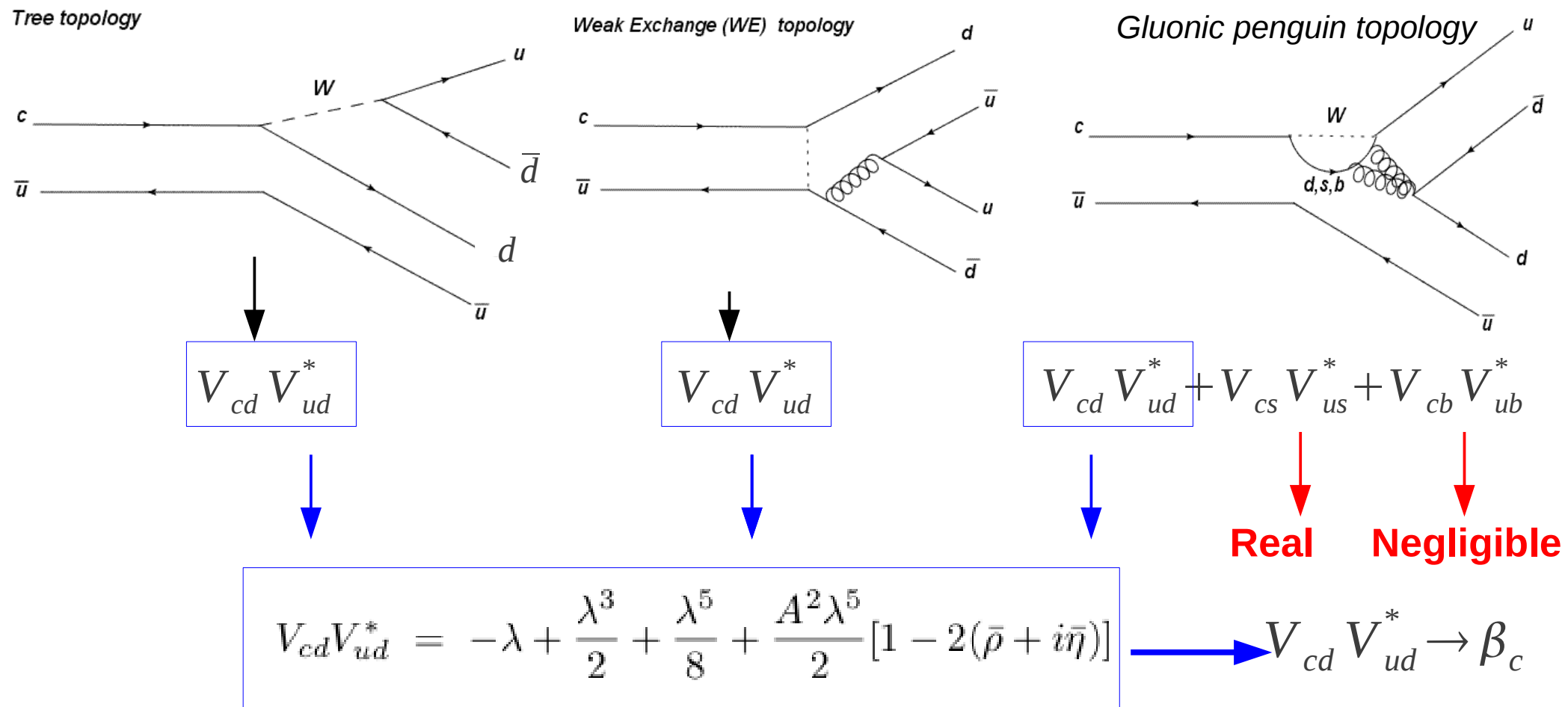
**Negligible**

$$V_{cd} V_{ud}^* = -\lambda + \frac{\lambda^3}{2} + \frac{\lambda^5}{8} + \frac{A^2 \lambda^5}{2} [1 - 2(\bar{\rho} + i\bar{\eta})]$$

- To first order one would expect to measure an asymmetry consistent with zero:
- **cross check of detector reconstruction and calibration**
  - **ideal mode to use when searching for new physics (NP)**



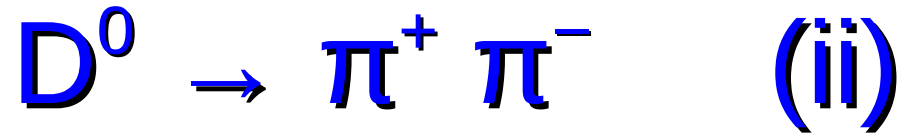
# $D^0 \rightarrow \pi^+ \pi^-$ (i)



Penguin topologies are DCS loops while the Tree amplitude is CS

→ Penguin contribution could in principle be ignored, but..

→ A complete theoretical analysis is necessary if one wants to extract the weak phase and disentangle the  $c \rightarrow s \rightarrow u$  penguin



hep-ph/9909479

## On the Other Five Unitarity Triangles

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There are two Isospin amplitude contributing to the process  $D^0 \rightarrow \pi^+ \pi^-$  and the situation is almost the same with respect to the process where  $B^0 \rightarrow \pi \pi$ .

$$A(\Delta t) = \frac{\bar{\Gamma}(\Delta t) - \Gamma(\Delta t)}{\bar{\Gamma}(\Delta t) + \Gamma(\Delta t)} = 2 e^{\Delta\Gamma t/2} \frac{(|\lambda_f|^2 - 1) \cos \Delta M \Delta t + 2 \Im(\lambda_f) \sin \Delta M \Delta t}{(1 + |\lambda_f|^2)(1 + e^{\Delta\Gamma \Delta t}) + 2 \Re(\lambda_f)(1 - e^{\Delta\Gamma \Delta t})}$$

when  $\Delta\Gamma = 0 \rightarrow A(\Delta t) = -C \cos \Delta M \Delta t + S \sin \Delta M \Delta t$

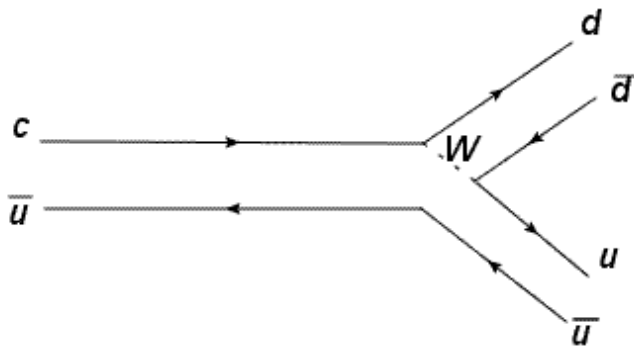
The difference between the process  $D^0 \rightarrow \pi^+ \pi^-$  and the process where  $B^0 \rightarrow \pi \pi$  is that  $\Delta\Gamma \neq 0$ . The effect is that instead of measuring S and C, one measure directly the real and imaginary part of  $\lambda_f$ :

$$\lambda_f = \frac{q}{p} \frac{\bar{A}}{A}$$

If one wants relate precisely the weak phase to the observed CP asymmetry, to constrain the penguin pollution it becomes necessary to measure  $D^0 \rightarrow \pi^+ \pi^-$ ,  $D^+ \rightarrow \pi^+ \pi^0$ ,  $D^0 \rightarrow \pi^0 \pi^0$   
**This will require an  $e^+e^-$  environment**

$$D^0 \rightarrow \rho^0 \rho^0$$

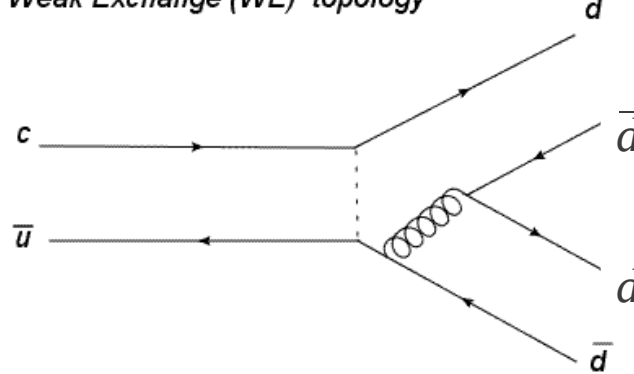
Color Suppressed (CS) Tree topology



$$V_{cd} V_{ud}^*$$



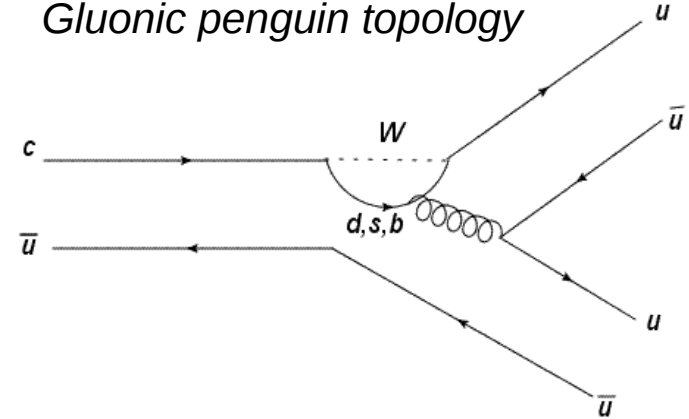
Weak Exchange (WE) topology



$$V_{cd} V_{ud}^*$$



Gluonic penguin topology



$$V_{cd} V_{ud}^* + V_{cs} V_{us}^* + V_{cb} V_{ub}^*$$

**Real**

**Negligible**

$$V_{cd} V_{ud}^* = -\lambda + \frac{\lambda^3}{2} + \frac{\lambda^5}{8} + \frac{A^2 \lambda^5}{2} [1 - 2(\bar{\rho} + i\bar{\eta})]$$

Similar situation as in  $D^0 \rightarrow \pi^+ \pi^-$

# Simulated performance of TDCPV at $\psi(3770)$

- $\Psi(3770)$  channel:

$$D_{\text{tag}} \rightarrow K^- e^+ \nu_e$$

$$D^0 \rightarrow \pi^+ \pi^-$$

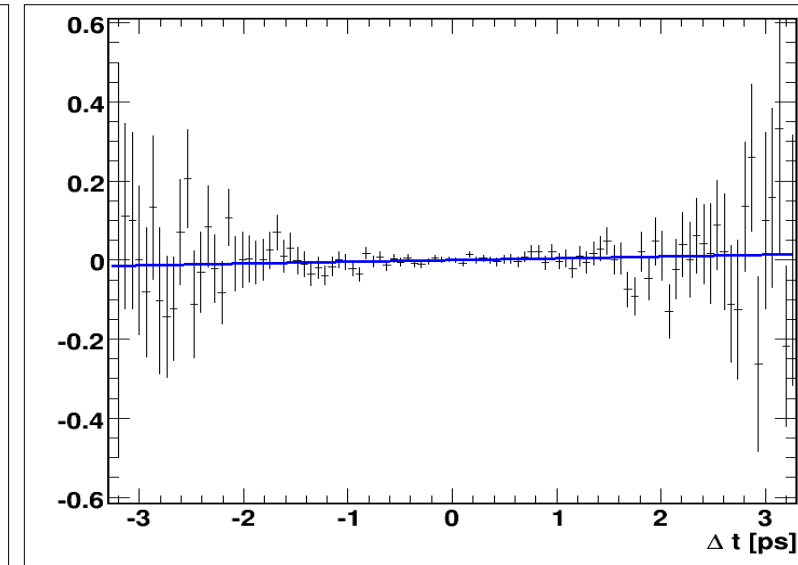
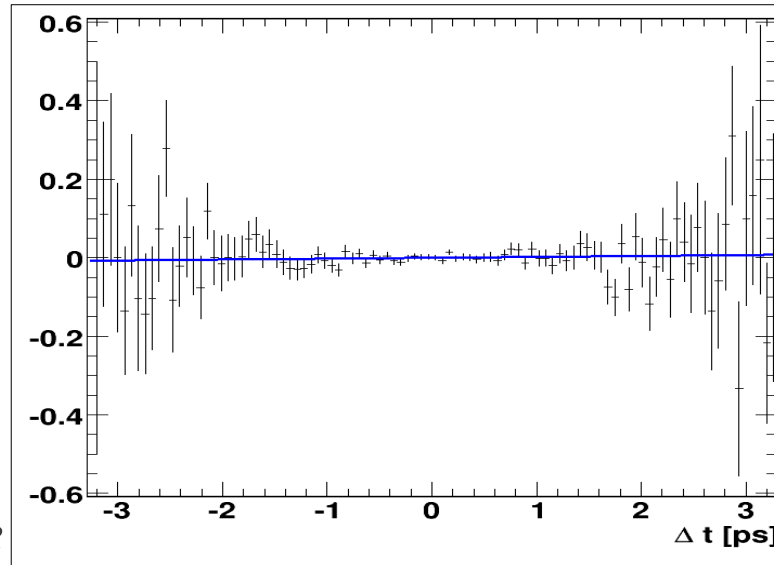
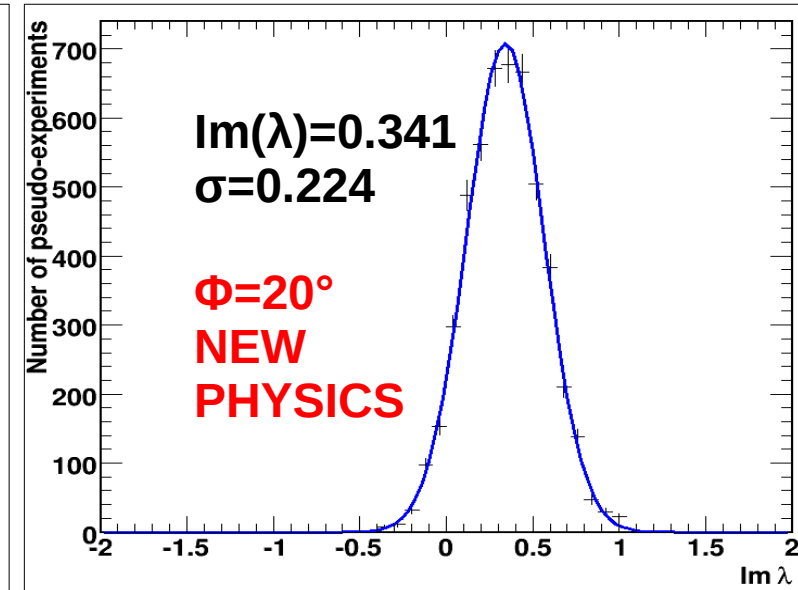
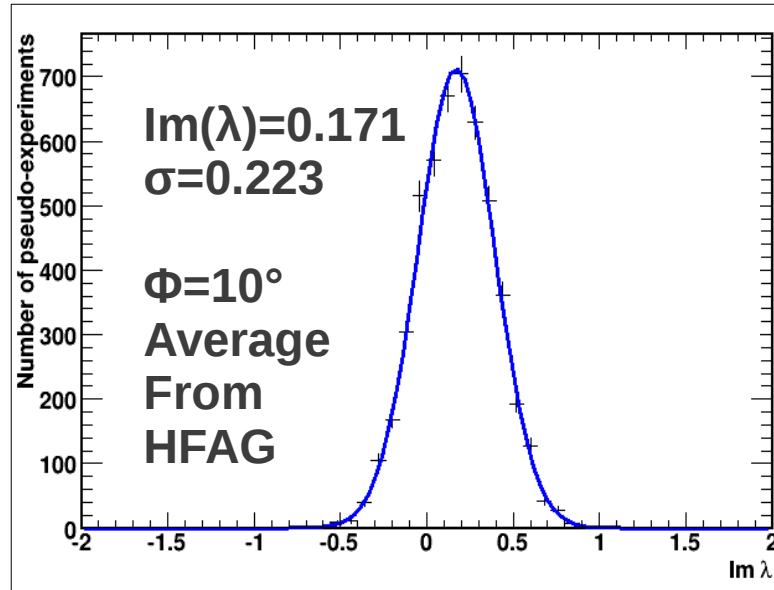
- SuperB 3 months at 3770:  $500 \text{ fb}^{-1}$

- Estimated yields from  $CLEO_c$  results:

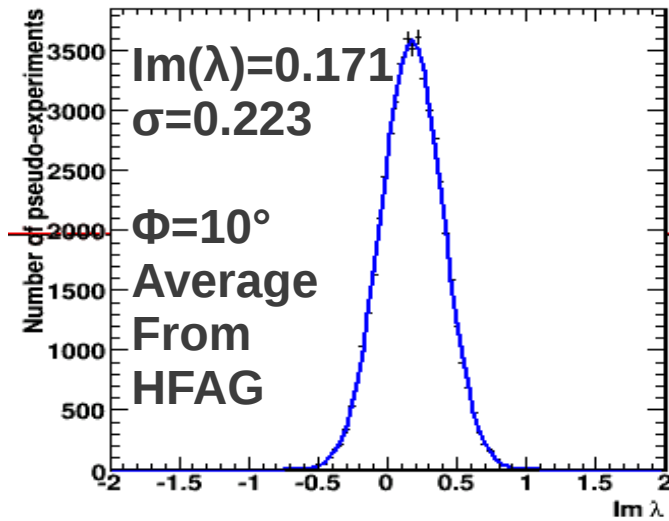
$$158000 D^0 \rightarrow \pi^+ \pi^-$$

- Adding  $D_{\text{tag}} \rightarrow K^* e^+ \nu_e$  double the statistics

- More tagging modes plus 6 months run at the  $\Psi(3770)$  means 6 times larger data sample



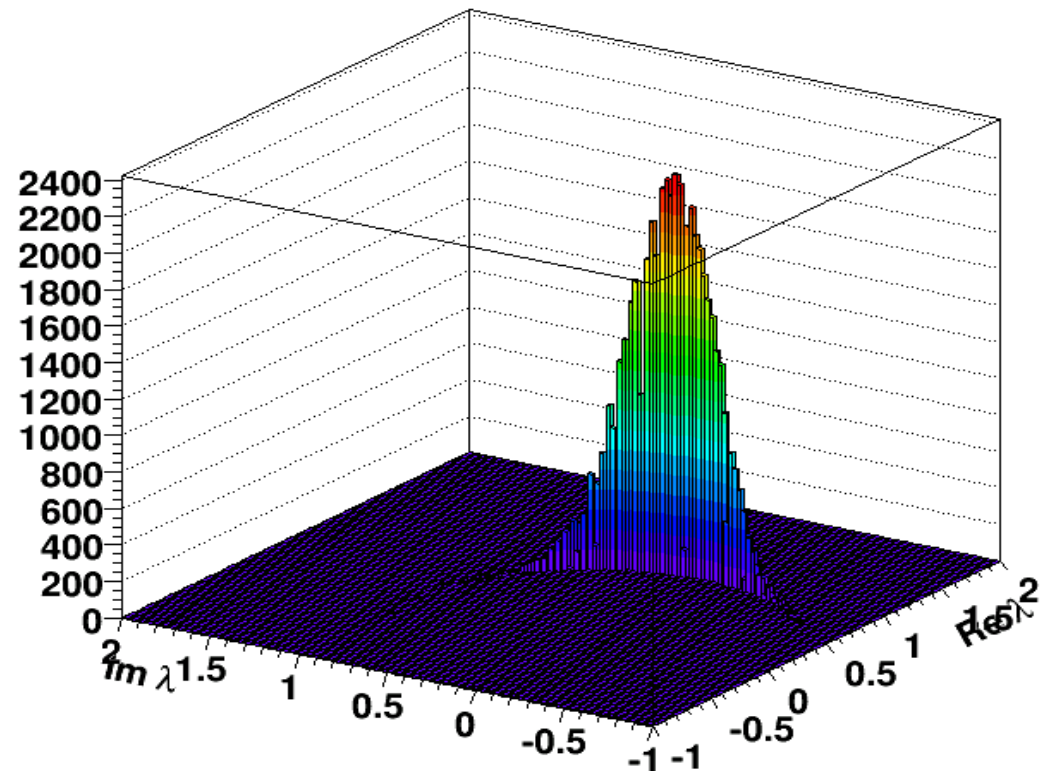
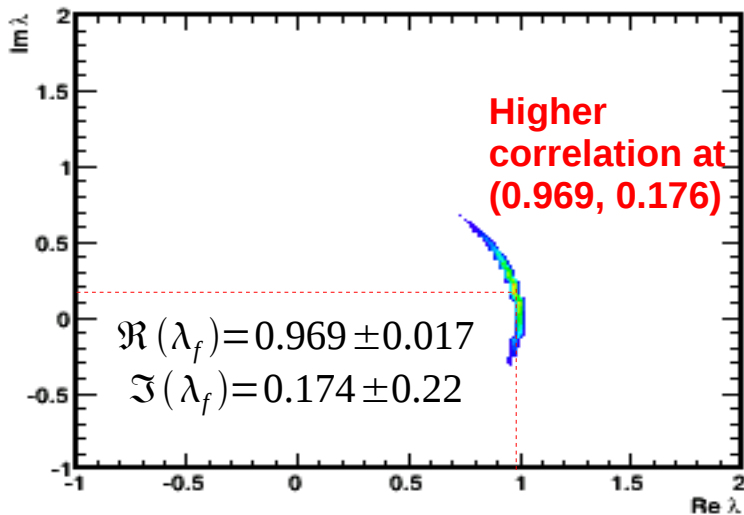
# Im( $\lambda$ ) vs. Re( $\lambda$ )



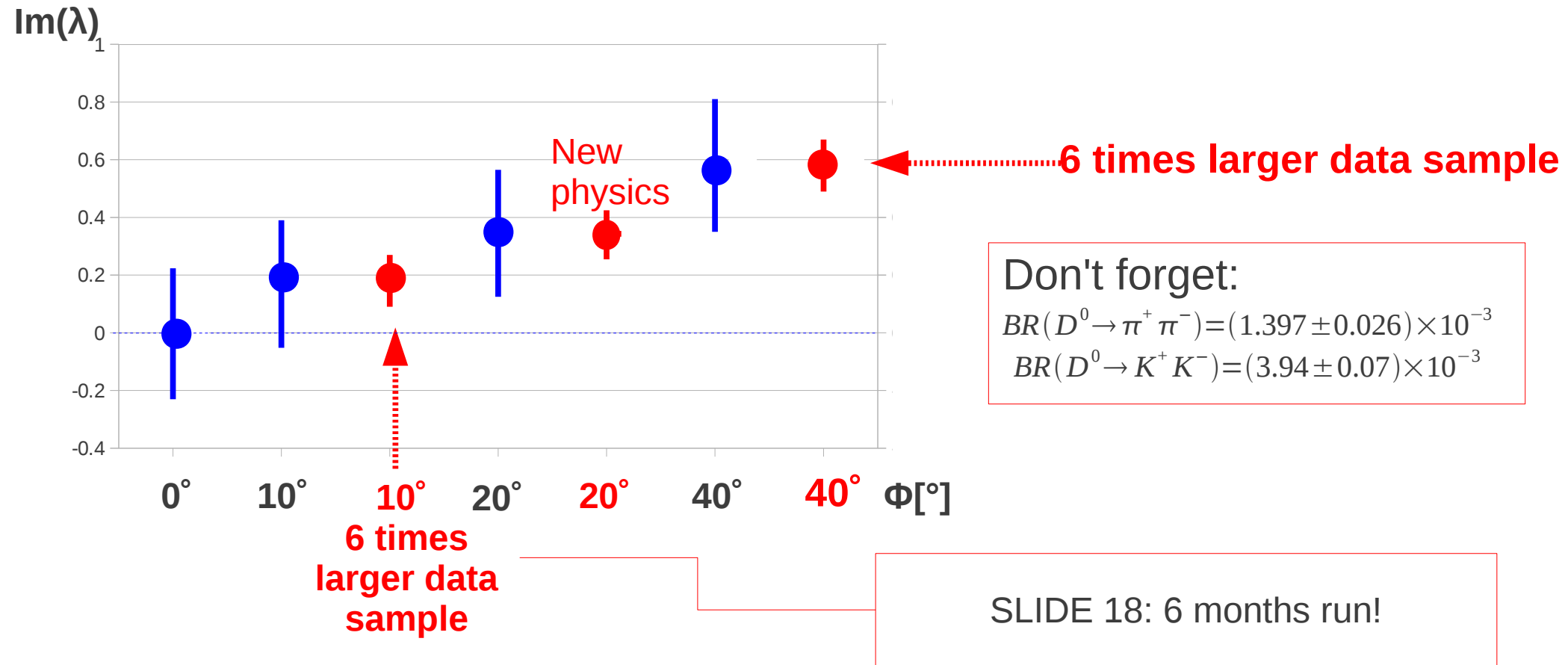
160000  $D^0 \rightarrow \pi^+ \pi^-$  equivalent to  $0.5 \text{ ab}^{-1}$   
 We run 50000 pseudo-experiments  
 We expect :

$$\Re(\lambda_f) = 0.985$$

$$\Im(\lambda_f) = 0.174$$



# Imaginary part of $\lambda$ vs $\Phi$ : CP-violation



As already seen, the value of  $\lambda$  is strictly dependent on the value of the phase  $\Phi$ . The red dots show that a longer run or more tagging modes at  $\Psi(3770)$  would provide an higher precision (smaller error) for this measurement.

- The precision does NOT depend on the value of the phase  $\Phi$ .

# Uncorrelated $D^0$ mesons

$$A(t) = \frac{\bar{\Gamma}(t) - \Gamma(t)}{\bar{\Gamma}(t) + \Gamma(t)} = 2e^{\Delta\Gamma t/2} \frac{(|\lambda_f|^2 - 1)\cos\Delta M t + 2\Im(\lambda_f)\sin\Delta M t}{(1 + |\lambda_f|^2)(1 + e^{\Delta\Gamma t}) + 2\Re(\lambda_f)(1 - e^{\Delta\Gamma t})}$$

Mistag probability and dilution become important

$$A^{Phys}(t) = \frac{\bar{\Gamma}^{Phys}(t) - \Gamma^{Phys}(t)}{\bar{\Gamma}^{Phys}(t) + \Gamma^{Phys}(t)} = +\Delta\omega + \frac{(D - \Delta\omega)e^{\Delta\Gamma t/2}(|\lambda_f|^2 - 1)\cos\Delta M t + 2\Im(\lambda_f)\sin\Delta M t}{(1 + |\lambda_f|^2)h_+/2 + h_- \Re(\lambda_f)}$$

The flavour tagging is accomplished by identifying a “slow” pion in the

processes (CP and CP conjugated):

$$D^{*+} \rightarrow D^0 \pi^+$$

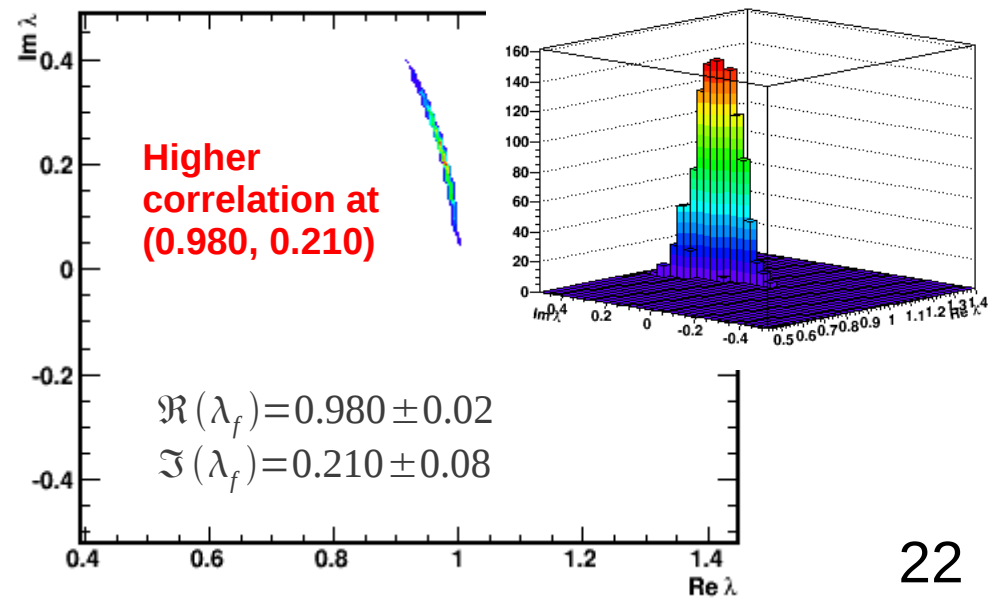
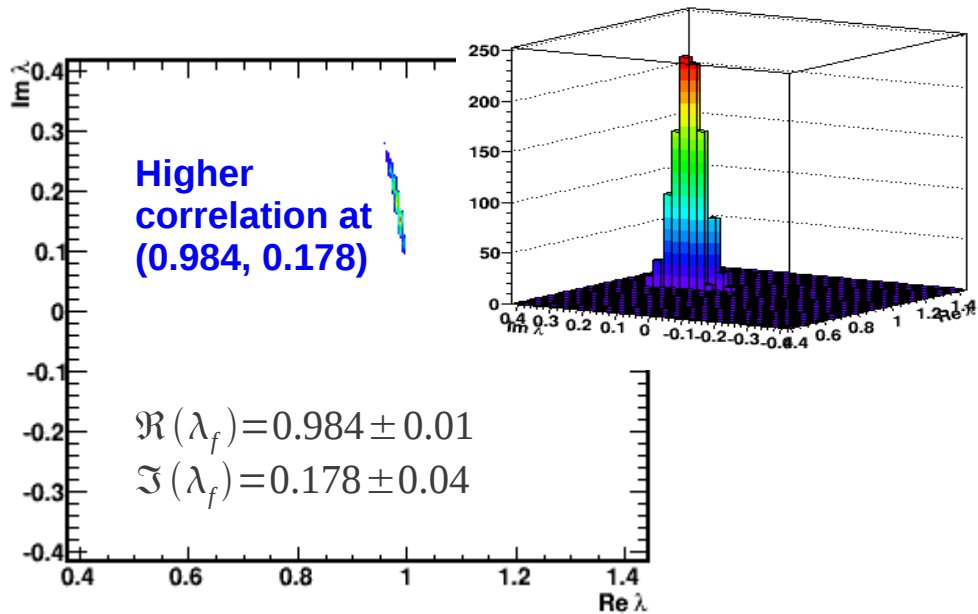
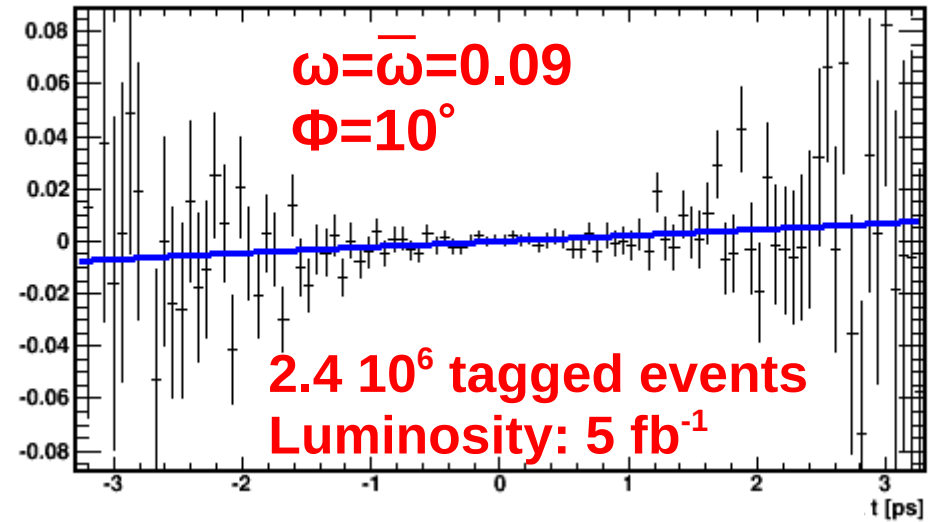
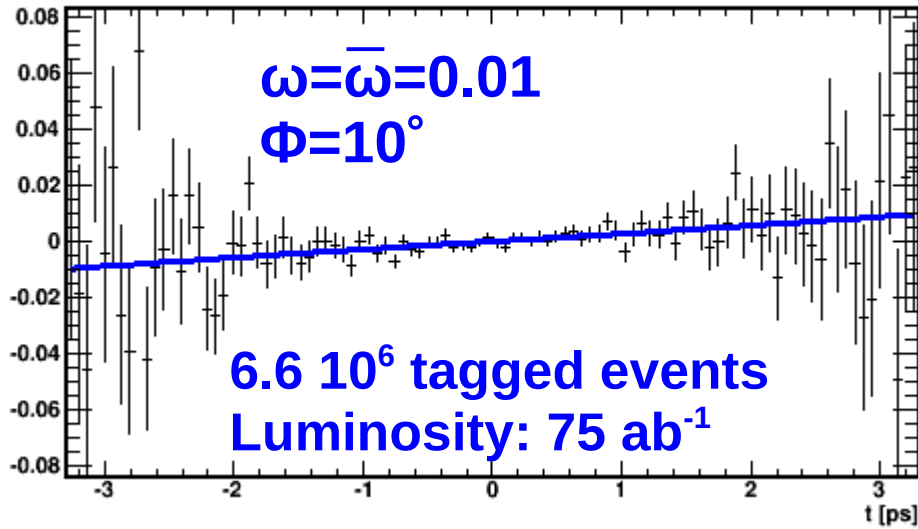
$$D^{*-} \rightarrow \bar{D}^0 \pi^-$$

**SuperB at  $\Upsilon(4S)$  and LHCb**

$D^*$  from  $e^+e^- \rightarrow c\bar{c}$  can be separated from those coming from B's by applying a momentum cut. Clean environment. More easier to separate prompt  $D^*$  from B cascade than LHCb

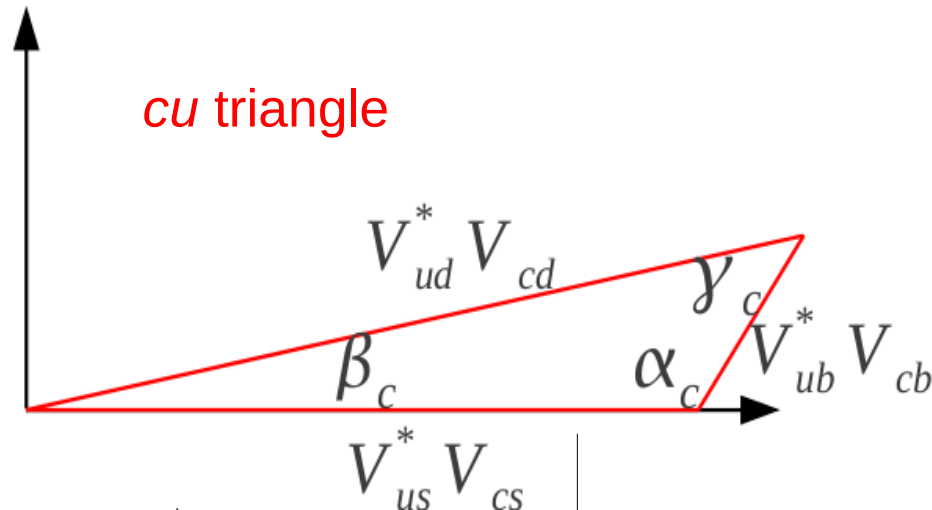
$D^*$  mesons are secondary particles produced in the primary decay of a B meson. High background level to keep under control. Trigger efficiency.

# Uncorrelated mesons: SuperB vs. LHCb





# Constraint on the $cu$ triangle

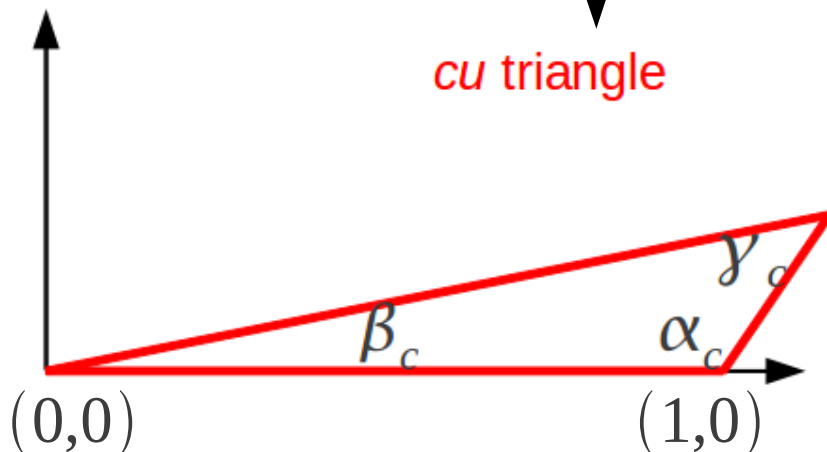


It is possible to constrain the apex of the  $cu$  triangle in two ways:

- 1) by constraining two internal angles
- 2) by measuring the sides

Normalizing the baseline to 1, so dividing by  $V_{us}^* V_{cs}$

$\gamma_c = (68.4 \pm 0.1)^\circ$  from *CKM prediction*  
 + any measurement of  $\beta_c \rightarrow$  constraint on the apex of the triangle



$$X + iY = 1 + \frac{A^2 \lambda^5 (\bar{\rho} + i\bar{\eta})}{\lambda - \lambda^3/2 - \lambda^5 (1/8 + A^2/2)}$$

Using existing constraints on Wolfenstein parameters, we find:

$$X = 1.00025$$

$$Y = 0.00062$$

# Conclusions

We are exploring time-dependent CP asymmetries in charm and we defined a measurement for the  $\beta_c$  angle in the charm UT.

After defining the tagging for charm, we have studied a number of possible final states.

Using the developed formalism we simulated pseudo-experiments assuming SuperB luminosity and we have shown that a possible measurement for TDCP asymmetries will be reasonable.

We simulated pseudo-experiments and applied the formalism for uncorrelated mesons for both SuperB and LHCb and we compared the obtained results. We highlight that a precision measurement of any time-dependent effect will require a detailed understanding of the background.

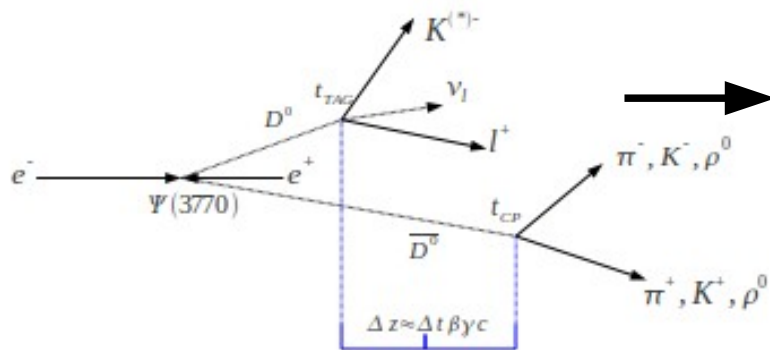
We define a test of the standard model by constraining the apex of the  $cu$  triangle

A larger run at charm threshold would provide a more precise measurement of  $\beta_c$

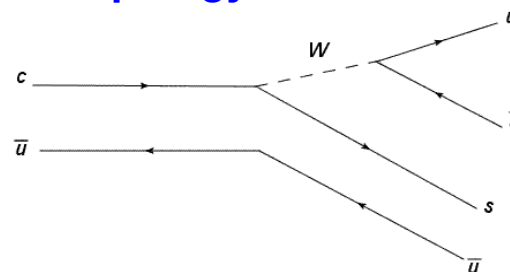
# Conclusions: pictures

$$A^{Phys}(\Delta t) = \frac{\overline{\Gamma^{Phys}}(\Delta t) - \Gamma^{Phys}(\Delta t)}{\overline{\Gamma^{Phys}}(\Delta t) + \Gamma^{Phys}(\Delta t)} = -\Delta\omega + \frac{(D + \Delta\omega)e^{\Delta\Gamma|\Delta t|/2} (|\lambda_f|^2 - 1) \cos \Delta M \Delta t + 2\Im(\lambda_f) \sin \Delta M \Delta t}{(1 + |\lambda_f|^2)h_+/2 + h_- \Re(\lambda_f)}$$

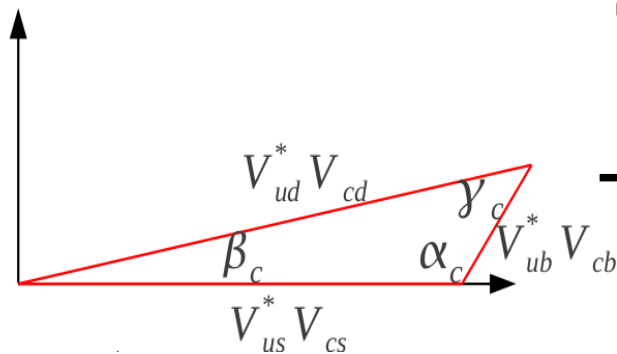
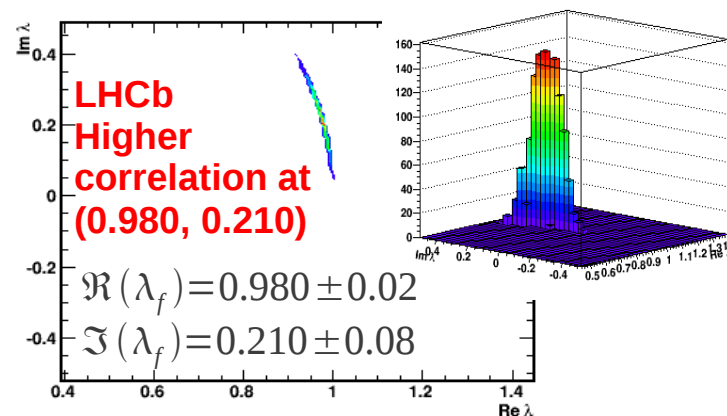
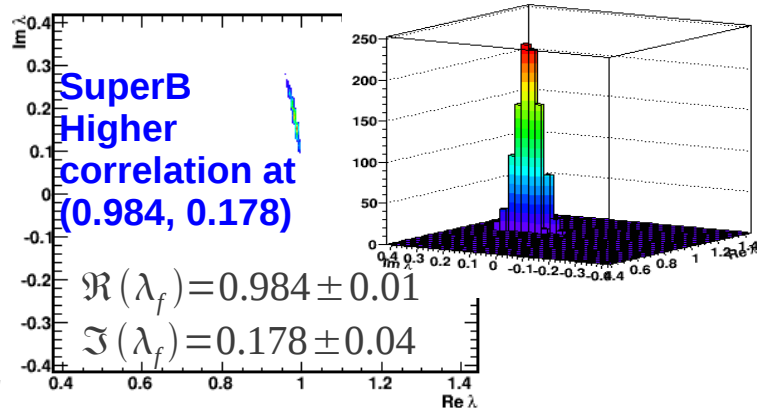
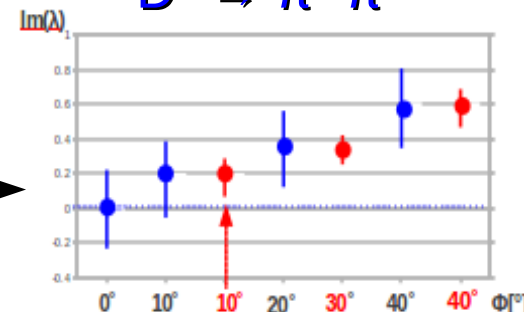
## Semi-leptonic tagging



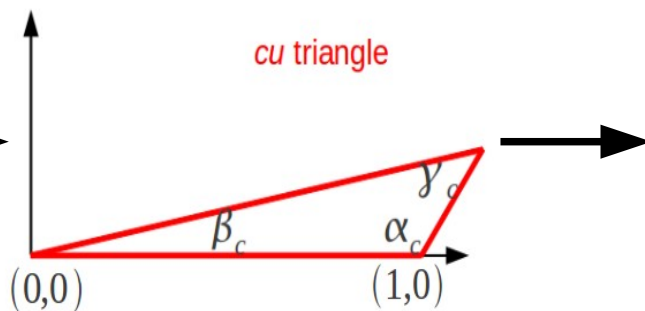
## Tree Topology



## D<sup>0</sup> → π<sup>+</sup> π<sup>-</sup>



## cu triangle



$$X + iY = 1 + \frac{A^2 \lambda^5 (\bar{\rho} + i\bar{\eta})}{\lambda - \lambda^3/2 - \lambda^5(1/8 + A^2/2)}$$

$X = 1.00025$   
 $Y = 0.00062$

# $B_d$ mesons (i)

All the time-dependent CP asymmetry measurements made on the assumption that  $\Delta\Gamma=0$ . **What if  $\Delta\Gamma\neq 0$ ?**

$$A(\Delta t) = \frac{\bar{\Gamma}(\Delta t) - \Gamma(\Delta t)}{\bar{\Gamma}(\Delta t) + \Gamma(\Delta t)} = 2e^{\Delta\Gamma\Delta t/2} \frac{(|\lambda_f|^2 - 1)\cos\Delta M\Delta t + 2\Im(\lambda_f)\sin\Delta M\Delta t}{(1+|\lambda_f|^2)(1+e^{\Delta\Gamma\Delta t}) + 2\Re(\lambda_f)(1-e^{\Delta\Gamma\Delta t})}$$

when  $\Delta\Gamma=0 \rightarrow A(\Delta t) = -C\cos\Delta M\Delta t + S\sin\Delta M\Delta t$

Example distributions:  $B^0$

$$\tau = 1.525 \times 10^{-12} \text{ s}$$

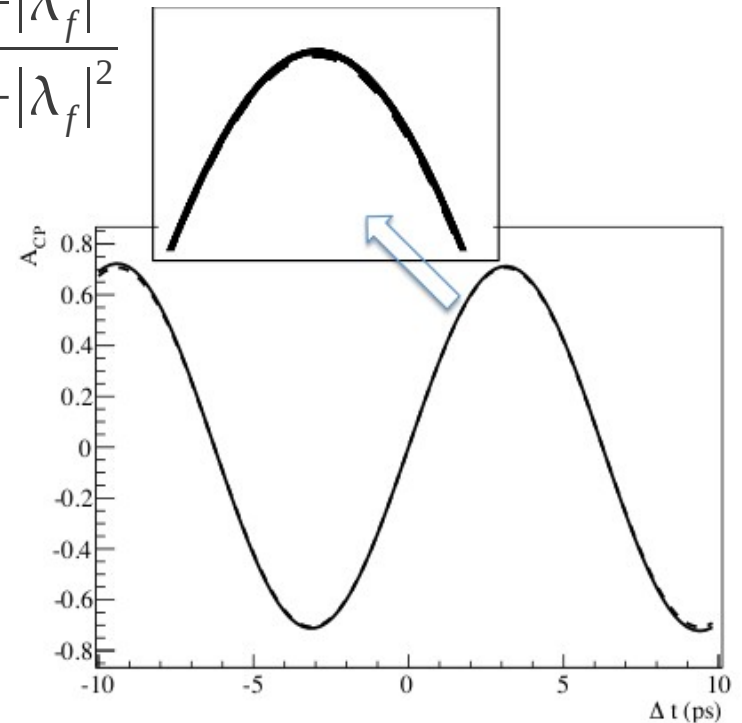
$$\Gamma = 1/\tau = 0.656 \times 10^{12} / \text{s}$$

$$\Delta m = 0.507 \times 10^{12} / \text{s}$$

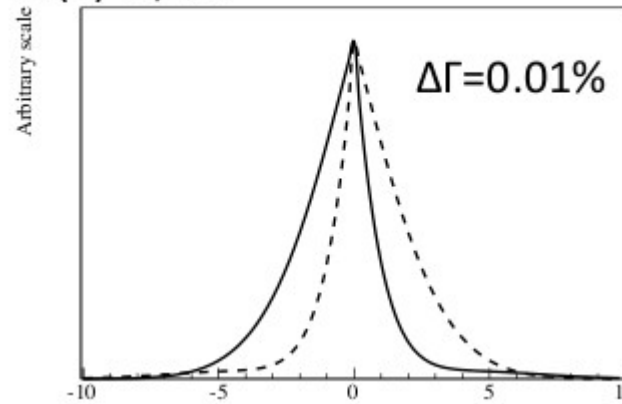
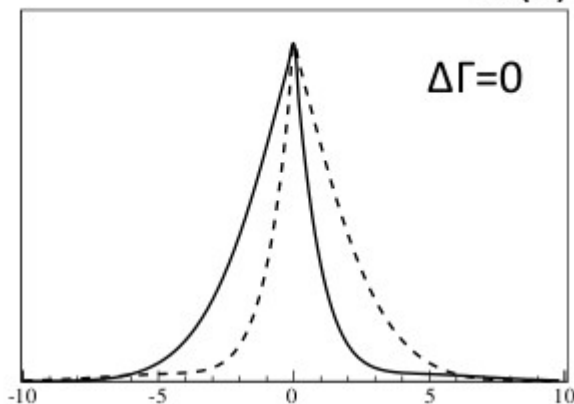
$$\Delta\Gamma \leq 6.56 \times 10^9 / \text{s}$$

$$(\Delta\Gamma/\Gamma = 0.01 [\pm 0.037])$$

$$S = \frac{2\Im(\lambda_f)}{1+|\lambda_f|^2}, \quad C = \frac{1-|\lambda_f|^2}{1+|\lambda_f|^2}$$



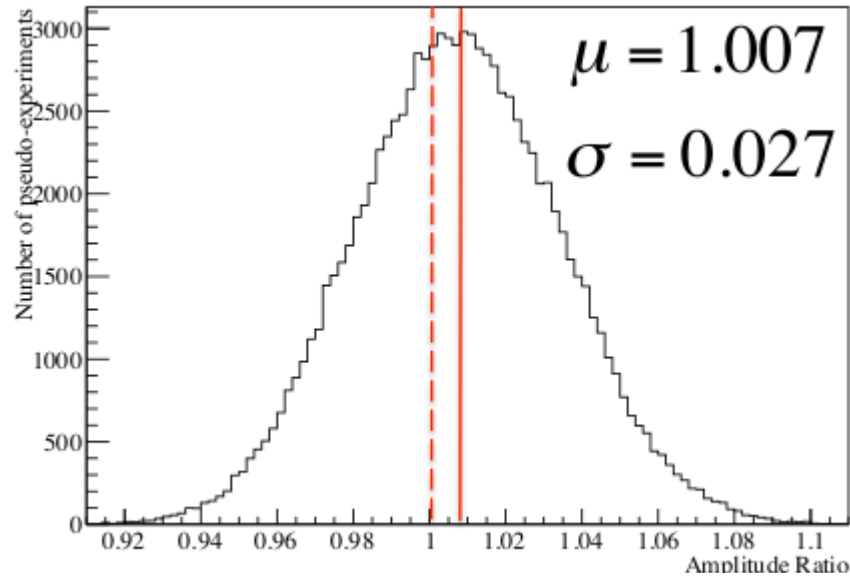
$$\text{Re}(\lambda) = \text{Im}(\lambda) = 1/\sqrt{2}$$



# $B_d$ mesons (ii)

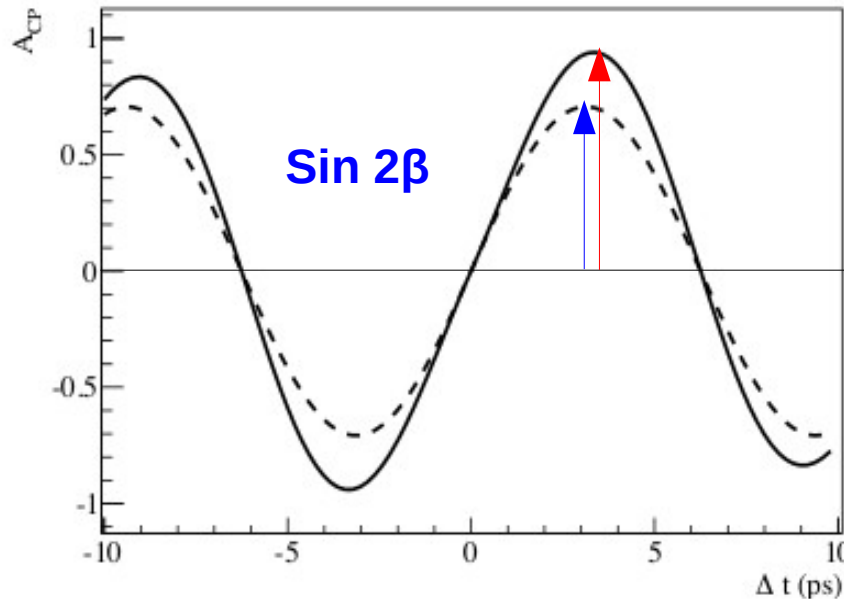
## Example distributions: $B^0$

$\tau = 1.525 \times 10^{-12} \text{ s}$   
 $\Gamma = 1/\tau = 0.656 \times 10^{12} \text{ /s}$   
 $\Delta m = 0.507 \times 10^{12} \text{ /s}$   
 $\Delta\Gamma \leq 6.56 \times 10^9 \text{ /s}$   
 $(\Delta\Gamma/\Gamma = 0.01 [\pm 0.037])$



Without better experimental determination, current measurements are at the level where we should be taking into account a possible non-zero  $\Delta\Gamma/\Gamma$ .

An extreme case:  $\Delta\Gamma/\Gamma = 0.50$



Positive  $\Delta\Gamma/\Gamma$  leads to an enhancement of the amplitude, a negative  $\Delta\Gamma/\Gamma$  leads to a decrease.

Dashed line is  $\Delta\Gamma=0$ .

# $B_s$ mesons

Oscillation in  $B_s$  decays are extremely fast: SuperB will not be able to perform a time-dependent CP asymmetry analysis

With a large sample of events at  $Y(5S)$  the distribution of events as function of  $\Delta t$  would contain information on  $Im(\lambda)$  and  $Re(\lambda)$

→ **informations on CPV related to TD measurements from hadron collider**

→ **particularly relevant for final states including neutral particles, such as  $B_s^0 \rightarrow \eta' \Phi$ , challenging measurement at hadron collider**

$$B_s \rightarrow \rho K_S^0, D_s^{+(-)} K^{-(+)}; B_s \rightarrow D \Phi$$

**LHCb can do these measurements well, since they have good time resolution**  
SuperB can probably measure asymmetries for  $\Delta t < 0$  vs.  $\Delta t > 0$

$B_s \rightarrow \pi^0 K_S^0$  The presence of the neutral pion and lack of informations to constrain the primary vertex: **excellent candidate for SuperB**

Thank you for your attention...  
...and...

