



# **EuPRAXIA@SPARC\_LAB**

## **Start to end Simulations**

**C. Vaccarezza**  
**on behalf of WA1- Beam Physics & collaboration team**

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- **Recommendations from TDR-RC report Jun 2022**
- **WA1- S2E simulations activity results**
  - Basic Layout Start to end Simulation Results
    - Parameter list update
- **WA1- Main Topics-parallel studies:**
  - X-band cavity at Gun exit
  - Jitter studies
  - 1.2 GeV operation
  - Non linear regime WPs
  - Plasma Tline
- **Summary**

# From TDR Rev Comm Jun 2022

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## 2.4 Start to End Simulations

Good progress has been made since last meeting, on converging towards a solution for the beam line options before the plasma in optimizing the electron beam parameters of the drive and witness bunches for acceleration in plasma in the comb scheme.

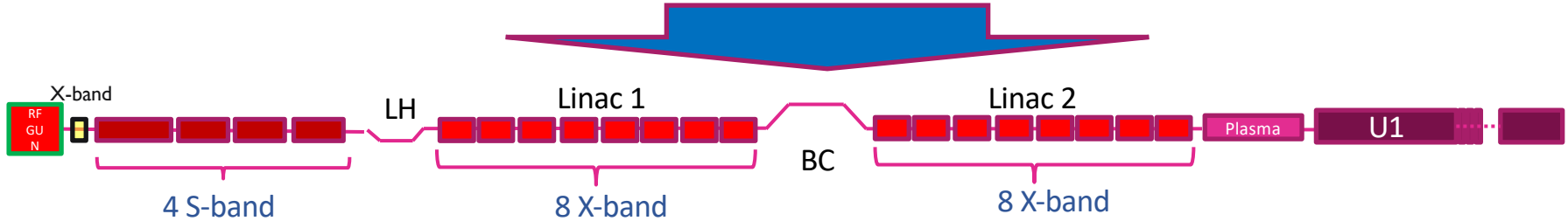
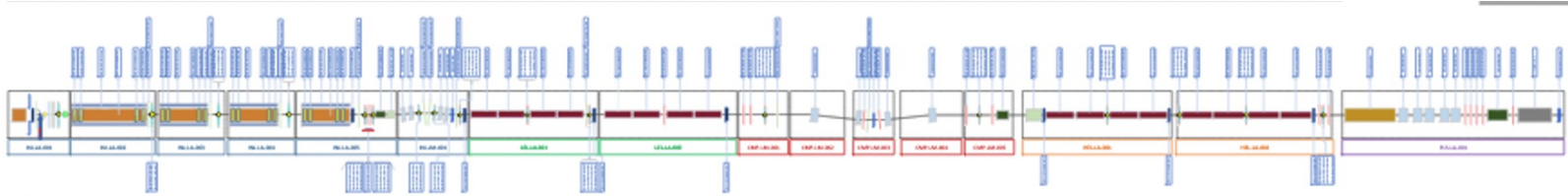
Two options are under consideration with different length/number of S-band structures in the injector: one using 4x2m, and another using 3+3x2m S-band structures have been studied for their suitability to insert an X-band linearizer after the gun. They were also compared with earlier injector layouts.

The first option offers a good solution for witness bunch charge up to 30 pC, whereas the second option looks better for higher charge of up to 50 pC. This latter solution does look promising and the RC endorses plans to study this option in more details. The planned tolerance and jitter studies will be important to make a final choice, as it may affect anticipated parameters of the driver/witness bunches at the entrance of the plasma.

The RC is pleased to see that more computing resources have been made available since the last meeting for optimization of injector with focus on controlling beam quality at the exit of the plasma and for parallelization of the Architect code for plasma simulations.

**The RC recommends finalizing the injector layout and continuing to progress on tolerance and jitter studies.**

# The Basic Layout



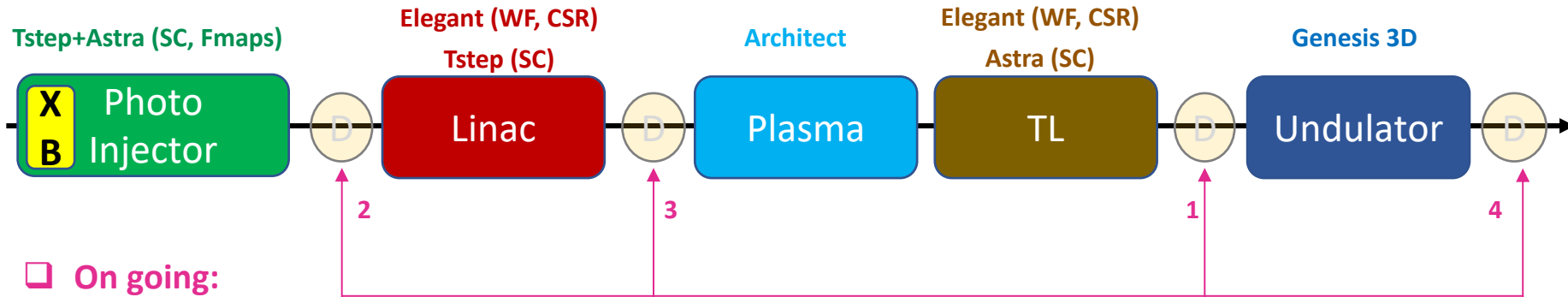
- Focused on Plasma acceleration operation scheme = WoP1
- Checked at each iteration for the High Charge Single Bunch boosted by an *All-RF* Linac up to 1 GeV = WoP2

# Start2End for the basic layout

## ❑ PhotoInjector Layout consolidation with 3m +3x2m S-band scheme:

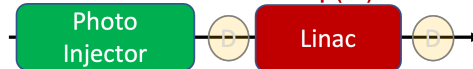
- Revision of nominal 30+200 pC WoP1 scheme for plasma acceleration: Photoinjector (no Xband)+ Linac + Plasma
- Transfer Line with CSR & SC for Undulator optics matching
- Undulator results

*done*

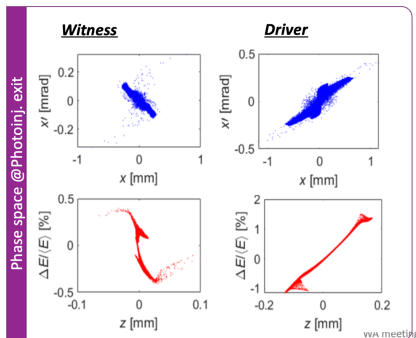


## ❑ On going:

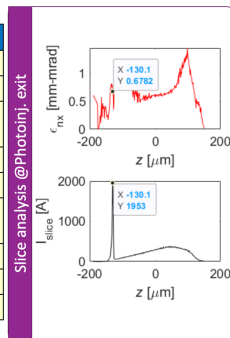
- Diagnostics feasibility/efficiency check w virtual measurements (priority order) to finalize the basic layout



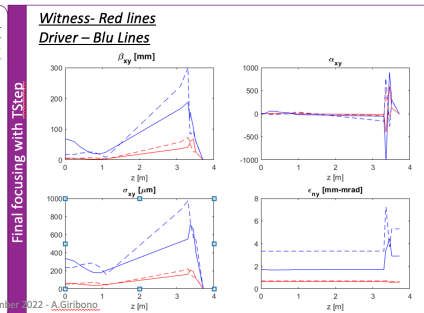
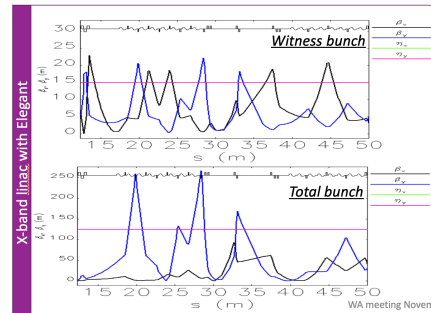
## Photoinjector



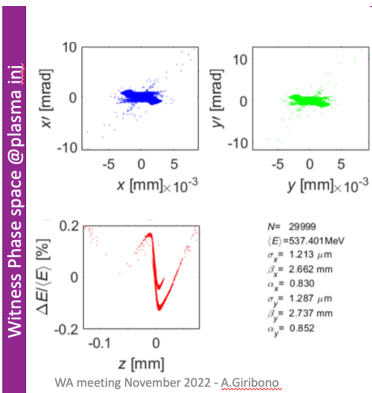
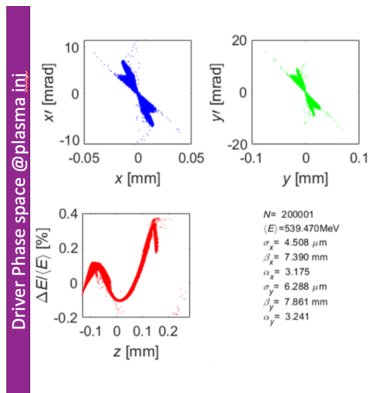
Beam parameters @ Photoinj. exit	Witness	Driver
E [MeV]	124.75	126.46
$\epsilon_{xy}$ [mm mrad]	0.70	1.52
$\sigma_{z-rms}$ [ $\mu$ m]	4.923	62.320
$\Delta E/E$ [%]	0.117	0.547
$\Delta t$ [ $\mu$ m]	151.5 (0.505)	
$\sigma_{x-rms}$ [ $\mu$ m]	118	127
$\beta_{xy}$ [mm]	6.127	2.609
$\alpha_{xy}$	2.475	-1.534



## Linac

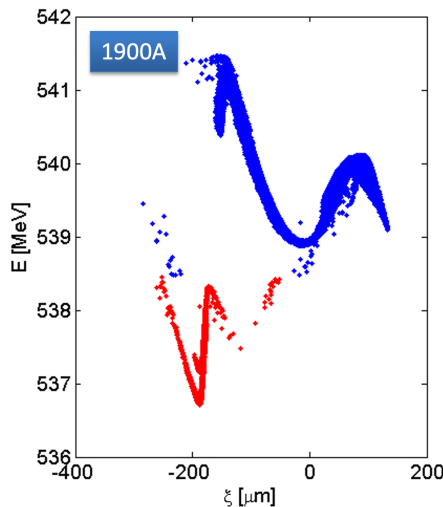


## Capillary entrance

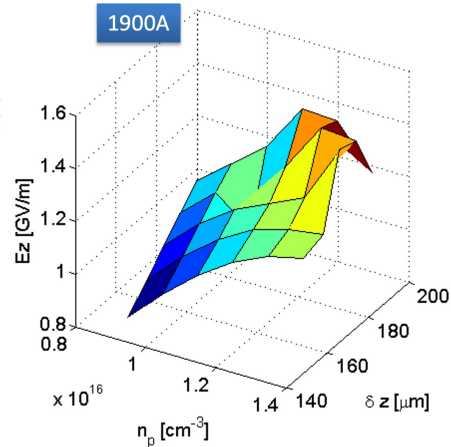
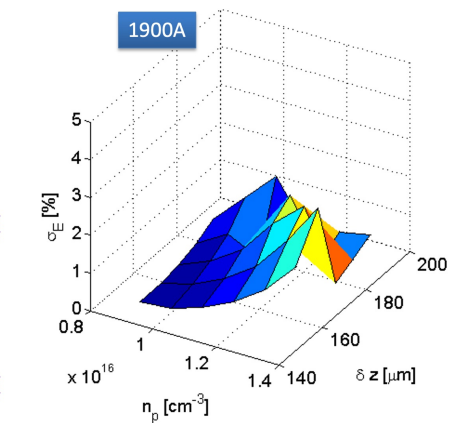
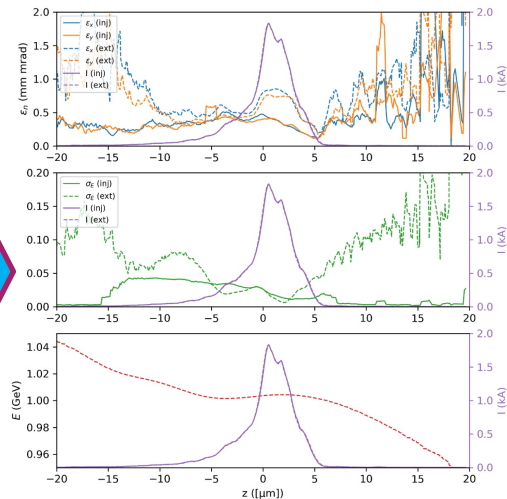


Beam parameters @ Plasma inj.	Witness	Driver
E [MeV]	537.6	539.5
$\epsilon_{xy}$ [mm mrad]	0.68-0.70	2.9-5.3
$\sigma_{z-rms}$ [ $\mu$ m]	5.460	59.620
$\Delta E/E$ [%]	0.057	0.095
$\Delta t$ [ $\mu$ m]	151 (0.505)	
$\sigma_{x-rms}$ [ $\mu$ m]	1.2-1.3	4.5-6.3
$\beta_{xy}$ [mm]	2.7-2.7	7.4-7.8
$\alpha_{xy}$	0.83-0.85	3.2-3.2

**30 + 200 pC**

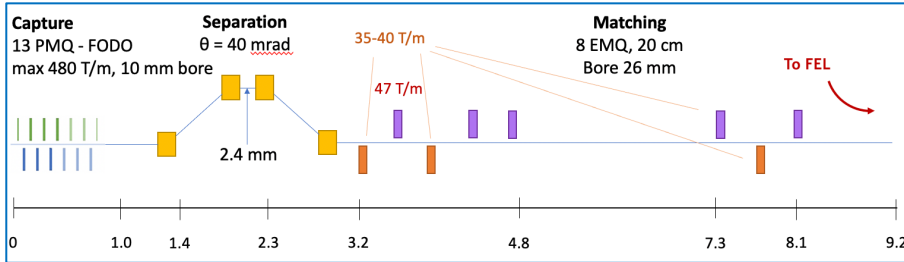


- $\Delta z = 158 \mu\text{m}$
- $n_p = 0.9 \cdot 10^{16} \text{ cm}^{-3}$
- $\sigma_E = 0.06\%$
- $E_Z = 0.9 \text{ GV/m}$  (including 1 cm injection ramp, so, actually, slightly higher)
- Slice energy spread, virtually untouched (or reduced)
- Slight emittance increase (to be improved with ramps)
- Accelerating length 0.56 m

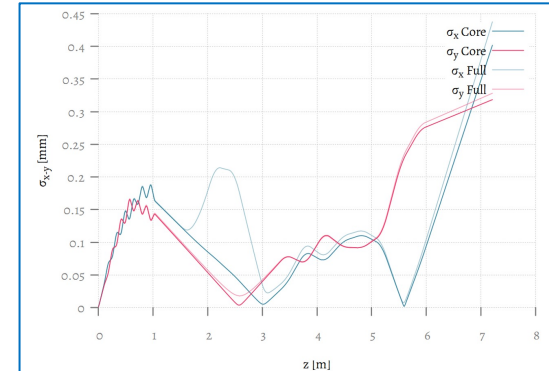




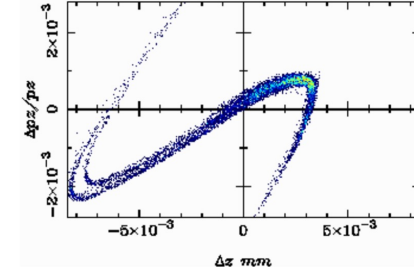
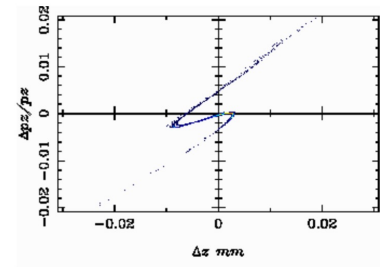
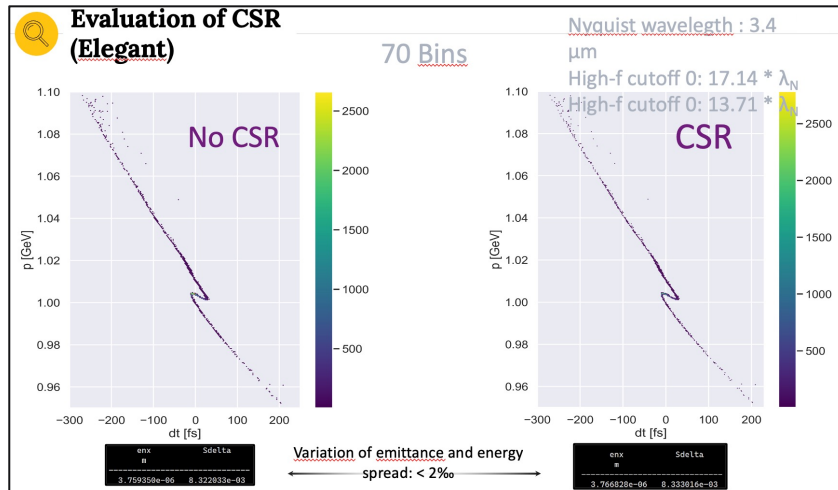
## Layout



## Transverse beam size evolution w Space Charge (Astra)



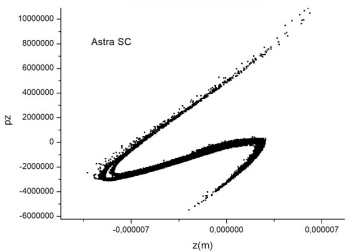
**Aperture**  
0.250 mm diameter (11% cut)  
8.35 MeV to 1.12 MeV



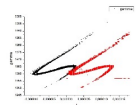
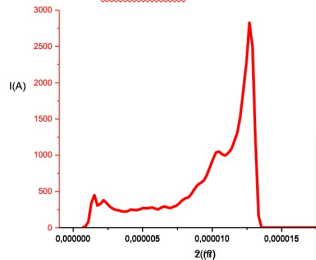


Beam from TL with space charge  $E=1\text{GeV}$ ,  $Q= 30 \text{ pC}$ .

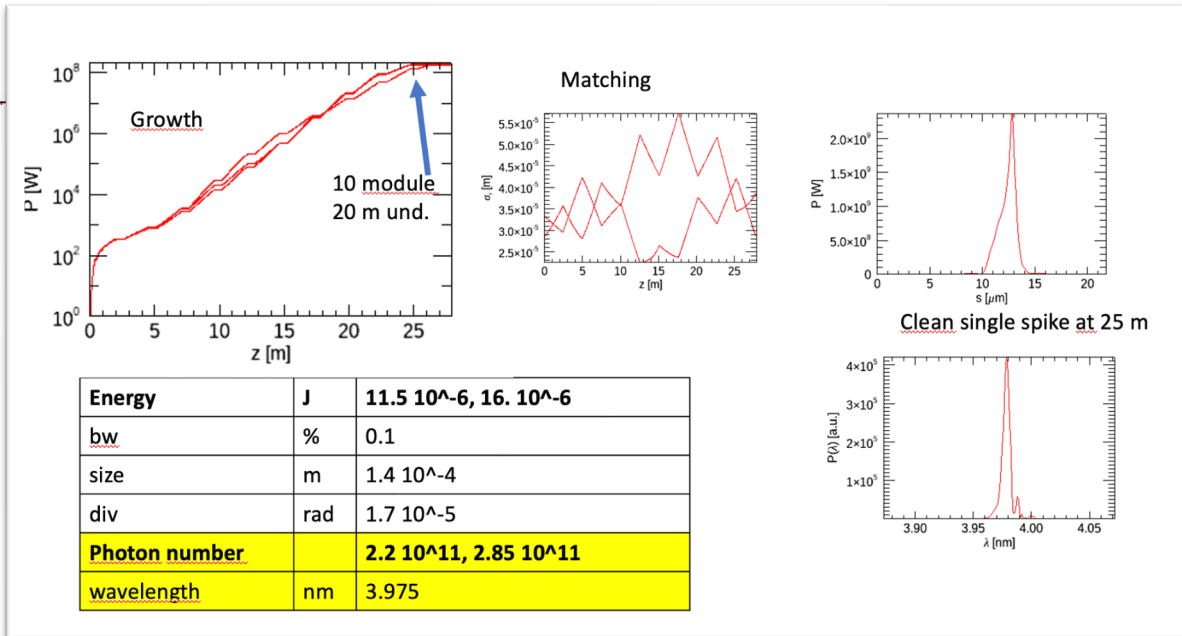
Phase space



Current

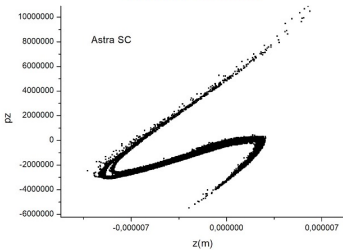


Comparison Astra(black)/Genesis 1.3 (red)

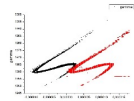
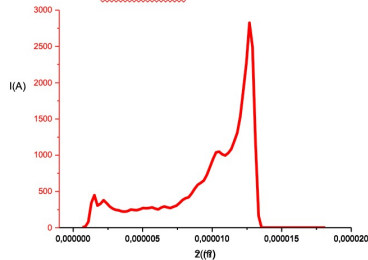


Beam from TL with space charge E=1GeV, Q= 30 pC.

Phase space

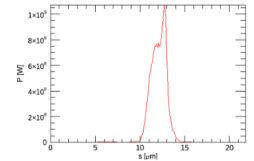
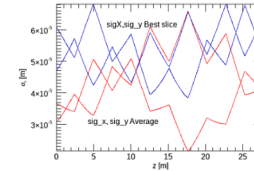
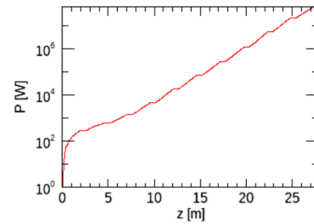


Current

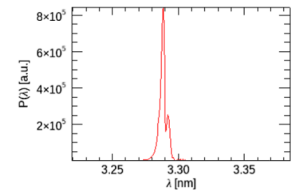


Comparison Astra(black)/Genesis 1.3 (red)

Same beam, undulator tuned at 3.3 nm



Energy	J	$6,6 \cdot 10^{-6}$
bw	%	0.1
size	m	$1.4 \cdot 10^{-4}$
div	rad	$1.7 \cdot 10^{-5}$
Photon number		$1.09 \cdot 10^{11}$
wavelength	nm	<b>3.3</b>



## Nominal FEL parameters from CDR

Parameter	Unit	PWFA	Full X-band
Radiation Wavelength	nm	3	
Photons per Pulse	$\times 10^{12}$	0.1	1
Photon Bandwidth	%	0.9	0.5
Undulator Area Length	m	30	
$\rho(1D/3D)$	$\times 10^{-3}$	1	2
Photon Brilliance per shot	$mm^2 mrad^2$ $bw(0.1\%)$	$1 \times 10^{27}$	

## FEL Parameters Nov 2022

Parameter	Unit	PWFA	Full X-band
Radiation Wavelength	nm	<b>3-4</b>	<b>4</b>
Photons per Pulse	$\times 10^{12}$	<b>0.1-0.25</b>	1
Photon Bandwidth	%	<b>0.1</b>	0.5
Undulator Area Length	m	30	
$\rho(1D/3D)$	$\times 10^{-3}$	<b>2</b>	2
Photon Brilliance per shot	$(s \text{ mm}^2 \text{ mrad}^2)$ $(bw(0.1\%))$	<b><math>1-2 \times 10^{28}</math></b>	$1 \times 10^{27}$

## Electron Beam parameters from CDR

Parameter	Unit	PWFA	Full X-band
Electron Energy	GeV	1	1
Bunch Charge	pC	30	200
Peak Current	kA	1-2	1-2
RMS Energy Spread	%	1.1	0.1
RMS Bunch Length	$\mu\text{m}$	6-4	24-20
RMS norm. Emittance	$\mu\text{m}$	1	1
Slice Energy Spread	%	0.03	0.02
Slice norm Emittance	mm-mrad	0.5	0.3

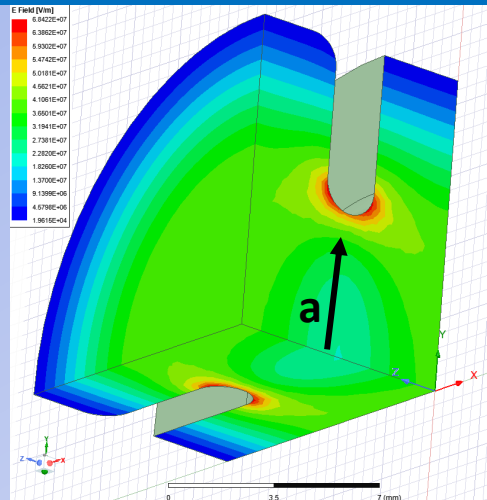
## Electron Beam Parameters Nov 22

Parameter	Unit	PWFA	Full X-band
Electron Energy	GeV	<b>1-1.2</b>	1
Bunch Charge	pC	<b>30-50</b>	<b>200-500</b>
Peak Current	kA	1-2	1-2
RMS Energy Spread	%	<b>0.1</b>	0.1
RMS Bunch Length	$\mu\text{m}$	6-3	24-20
RMS norm. Emittance	$\mu\text{m}$	1	1
Slice Energy Spread	%	$\leq 0.05$	$\leq 0.05$
Slice norm Emittance	mm-mrad	0.5	0.5

# **WA1-Main Topics parallel study**

## NEW Requirements from Beam dynamics:

- E-beam  $\Sigma_x=1.5-2$  mm  
→ cavity iris radius  $a=4$ mm
- Cavity Length = 10 cm
- $2\pi/3$  mode
- Accelerating Gradient  
TW option Eacc = 16.5 MV/m  
SW option Eacc = 16.3 MV/m

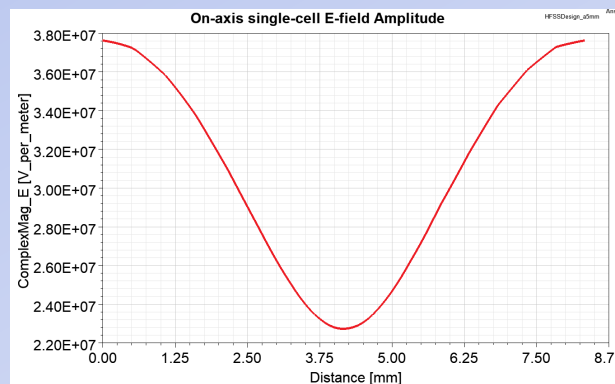


## RF design – first step

### Comparison

- TW structure, constant impedance
- SW structure

	a = 4 mm	TW	SW
f		11.9942 GHz	11.9942 GHz
Q		6600	8,600
Vg		3.6 %	-
r		85.3 MΩ/m	80 MΩ/m
Eacc		16.5 MV/m	16.3 MV/m
alpha		0.63 1/m	-
Lt		10 cm	10 cm
Coupling $\beta$		-	2
Fill time Tf		9.3 ns	-
Build up $\tau$		-	76 ns
Pin		3.2 MW	0.37 MW



NB: for higher gradients/powers  
no X-band recirculator for SW

# Xband Insertion: Driver 200 pC – Witness 30 pC improvements

**A. Bacci**  
**L. Faillace**

	Driver 200 pC			Witness 30 pC				Full Beam		
Older cases	$\sigma_x$	$\sigma_z$	$\epsilon_{n,x-y}$	$\sigma_x$	$\langle I \rangle$	$\sigma_z$	$\epsilon_{n,x-y}$	$\langle E \rangle$	$\Delta_z$	
	$\mu\text{m}$	$\mu\text{m}$	mm mrad	$\mu\text{m}$	kA	$\mu\text{m}$	mm mrad	MeV	$\mu\text{m}$	
A) WP 4 – 2222	218	55.0	1.54	522	1.00	2.6	0.43	102	150	
B) WP-X 3 TW – 2222	112	55.0	2.68	229	0.80	3.2	0.32	166	150	
C) WP-X 4 SW – 2222	106	55.0	2.78	220	0.77	3.3	0.34	167	149	
D) WP-X 5 SW – 3222	200	55.0	3.2	240	0.67	3.8	0.43	170	200	

Check Traffic light colors: green – Yellow – red

**This case: X-band + 3.0 m S-band + 4 x (2.0 m S-band) has been optimized to reach the referece  $\Delta z$  of 150  $\mu\text{m}$ :  
Further, we produced simulations also for  $\Delta z = 145 \mu\text{m}$  and  $140 \mu\text{m}$**

	Driver 200 pC			Witness 30 pC				Full Beam		
D) Improv. – 3222	$\sigma_x$	$\sigma_z$	$\epsilon_{n,x-y}$	$\sigma_x$	$\langle I \rangle$	$\sigma_z$	$\epsilon_{n,x-y}$	$\langle E \rangle$	$\Delta_z$	
	124	55.0	4.2	187	835	3.1	0.6	162	150	
	112	55.0	4.1	185	836	3.1	0.55	162	146	
	115	55.0	4.1	180	831	3.2	0.55	162	141	

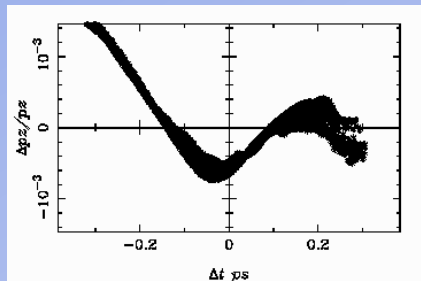
To NOTE: the beam parameters are very close but with different distance between Driver and Witness

# Xband Insertion: High Charge Single Bunch

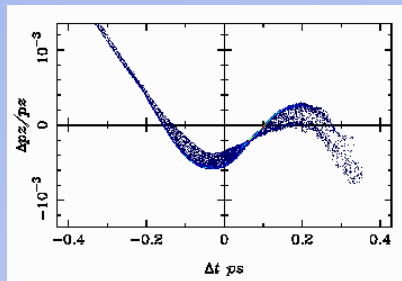
A. Bacci  
L. Faillace

Example: Long Phase space analysis

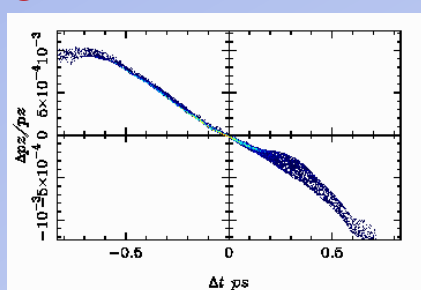
A



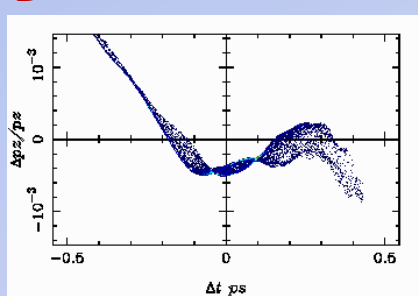
B



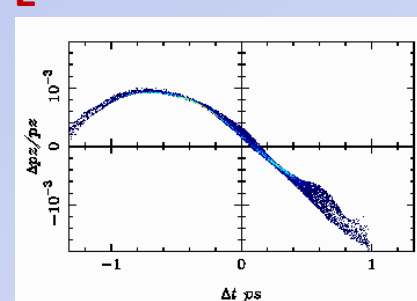
C



D



E

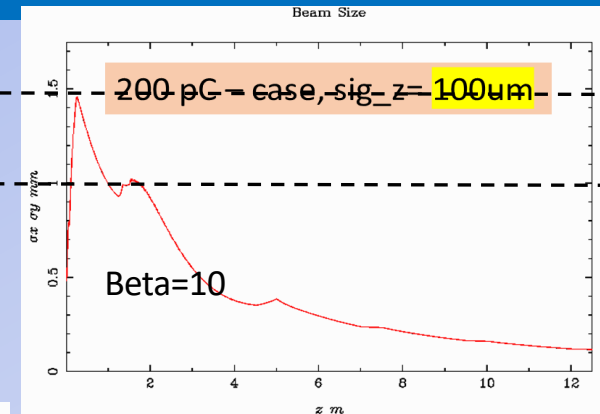
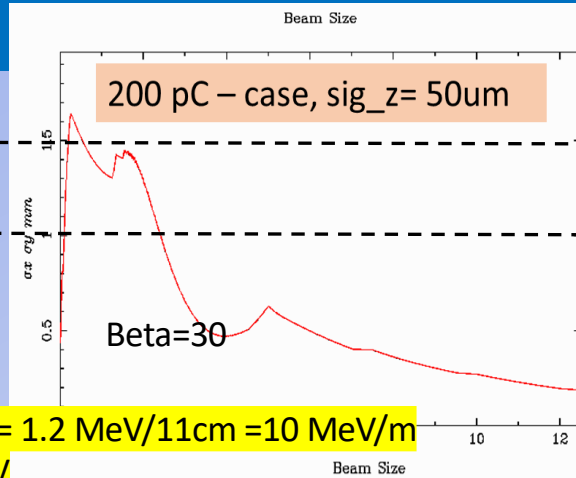
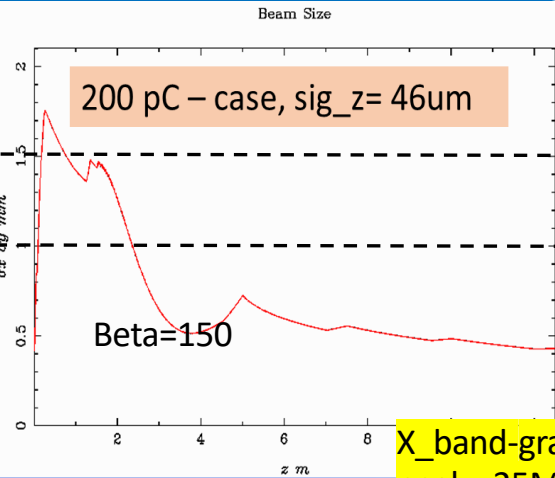


Parameter		A	B	C	D	E
Charge	(pC)	200	200	200	300	500
Current	(A)	600	500	210	550	400
$\sigma_z$	( $\mu\text{m}$ )	46	50	100	65	150
$\varepsilon_{nx,y}$ slice	( $\mu\text{rad}$ )	0.5	0.5	0.5	0.5	0.8
$\Delta_E$ slice	(keV)	20	20	8	10	20

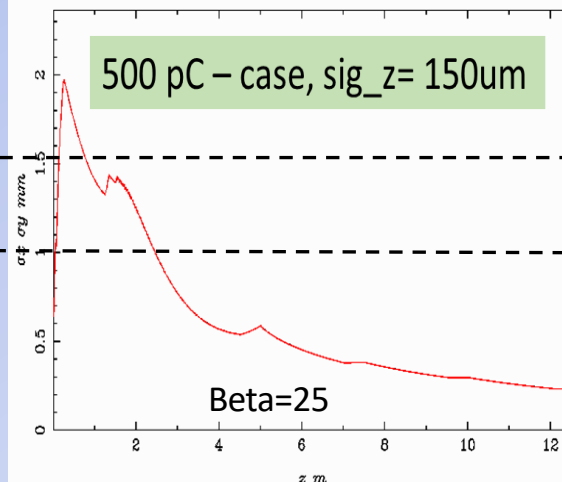
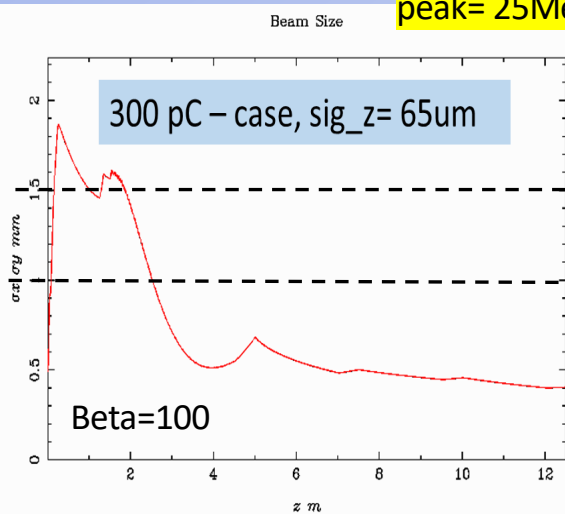


# Xband Insertion: High Charge Single Bunch

A. Bacci  
L. Faillace



X\_band-grad= 1.2 MeV/11cm =10 MeV/m  
peak= 25MeV



No particle losses  
from PIC  
simulations

Now the Comb & SB beams are  
ready to be tracked through the  
Linac and in the undulator to  
optimize the X-band correction

## First step: benchmark w SPARC\_LAB observation

- Photoinjector sensitivity studies are on going in order to test the robustness of the reference working point, especially with regards to the compression phase stability, as needed to ensure a  $\mu$ -scale bunch length.
- At first, the study is being focused on the RF phase jitters, in the range  $\pm 0.1$  degree for EuPRAXIA (worst case,  $\pm 0.03$  degree seems nevertheless feasible), that are strictly connected with the RF compression scheme efficiency.
- In the meanwhile, experimental activities are ongoing at the SPARC\_LAB test facility, even if considering higher RF phase jitter errors ( $\pm 1$  degree) due to the current accelerator technology, so to benchmark the beam dynamics simulations made for EUPRAXIA@SPARC\_LAB with the experimental results.

- The experimental activity performed at SPARC\_LAB has regarded three working point, f1-f2-f3 described in Table, relying on the velocity bunching scheme each with a different compression factor.
- Simulations have been performed with the TStep code

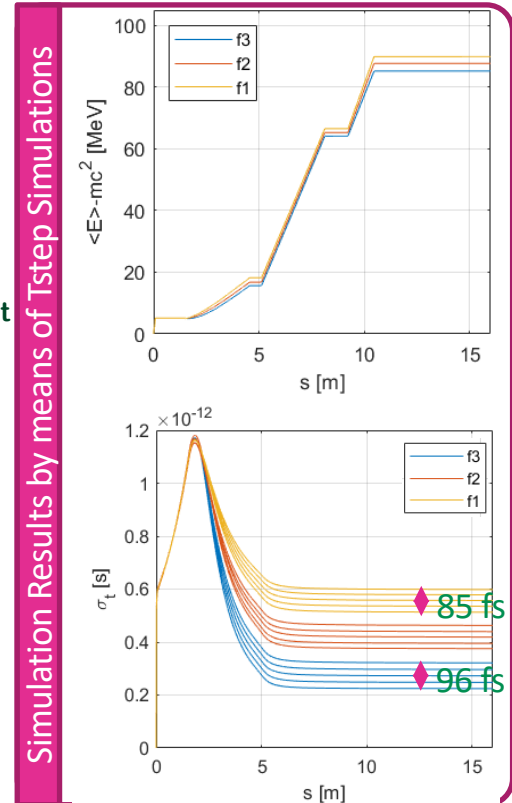
WP	RF phase (deg)	Energy (MeV)		Energy Spread (keV)		$\sigma_z$ (rms - $\mu\text{m}$ )	
		Exp	Sim	Exp	Sim	Exp	Sim
f1	-84.16	90.44	90.45	240	218.0	170.7	166
f2	-87.16	88.33	88.23	200	192.0	123.8	125.5
f3	-90.16	85.95	85.76	130	130.2	83	81.7

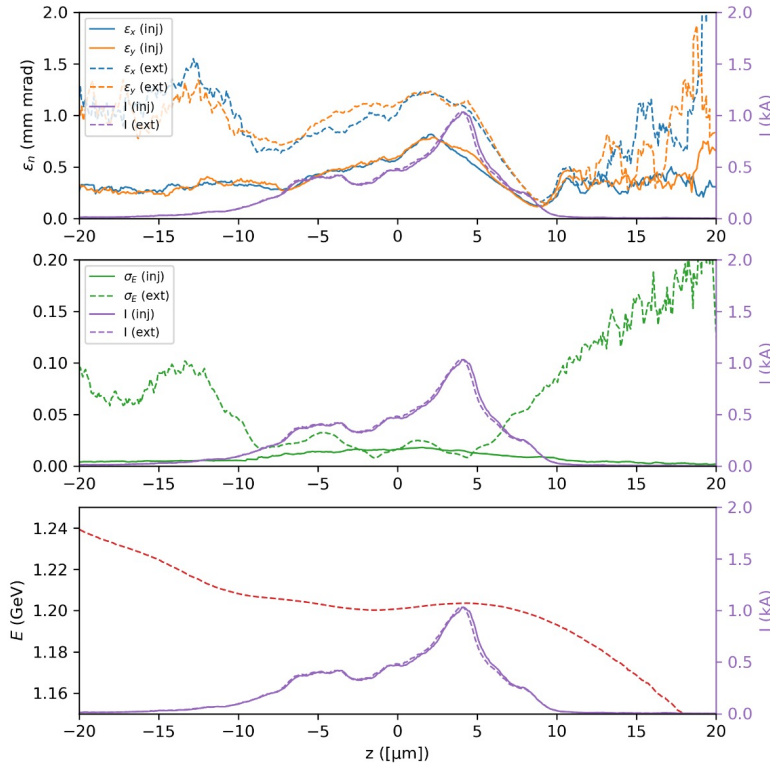
- The results are in terms of coefficient of arrival time jitter (ATJ) defined as

$$\Delta t_{\text{linac}} \approx \sum_{i=1}^4 c_i \Delta t_i.$$

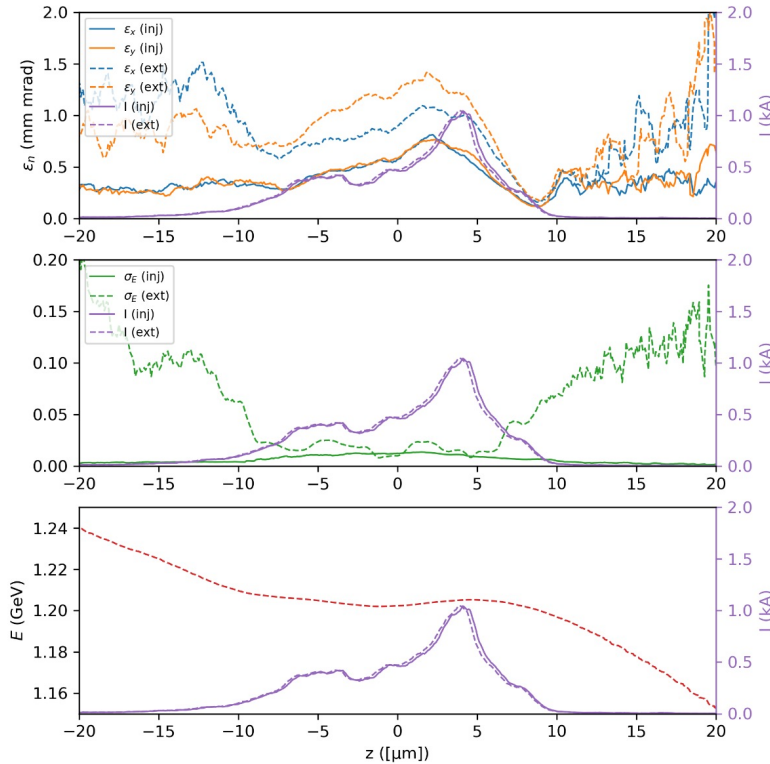
- Experimental results show that, as expected by theory and simulations, at the maximum explored compression phase:
  - the main contribution to the time arrival jitter comes from the phase jitter of the first accelerating structure, with  $\pm 1$  degree phase error translating in  $\approx \pm 1$  ps  
 → EUPRAXIA@SPARC\_LAB worst case  $\Delta\Phi=0.1$ deg: driver and witness are expected to temporally jitter together of  $\pm 0.1$  ps. The jitter between them, due to the fact that they enter the S1 with different compression phase that is linked to slightly different  $c_i$ , is under evaluation
  - $\pm 1$  degree phase error on S1 results in  $\pm 17\%$  error on the final beam length  
 → EUPRAXIA@SPARC\_LAB worst case  $\Delta\Phi=0.1$ deg: expected witness length  $6\pm 0.1$   $\mu\text{m}$ , expected driver length  $60\pm 1$   $\mu\text{m}$

WP	RF phase (deg)	$c_1$ (laser)		$c_2$ (RF gun)		$c_3$ (S1-S2)		$\sum_{i=1}^4 c_i$	
		Meas.	Sim.	Meas.	Sim.	Meas.	Sim.	Meas.	Sim.
f1	-84.16	0.12±0.05	0.13	0.02±0.04	-0.01	0.86±0.06	0.80	1.00±0.15	0.92
f2	-87.16	0.04±0.06	0.06	0.04±0.05	-0.03	1.00±0.07	0.97	1.08±0.18	0.99
f3	-90.16	-0.16±0.05	-0.12	-0.03±0.08	-0.05	1.14±0.06	1.08	0.95±0.19	0.91





- $\Delta z = 148 \mu\text{m}$
- $n_p = 1.1 \cdot 10^{16} \text{ cm}^{-3}$
- $\sigma_E = 0.1\%$
- $E_z = 0.95 \text{ GV/m}$  (including 1 cm injection ramp, so, actually, slightly higher)
- Slice energy spread, virtually untouched
- Slight emittance increase (to be improved with ramps)
- **Accelerating length 0.7 m**

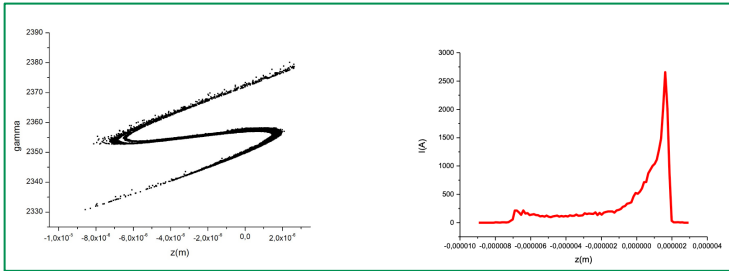


- $\Delta z = 174 \mu\text{m}$
- $n_p = 0.9 \cdot 10^{16} \text{ cm}^{-3}$
- $\sigma_E = 0.09\%$
- $E_z = 0.92 \text{ GV/m}$  (including 1 cm injection ramp, so, actually, slightly higher)
- Slice energy spread, virtually untouched (or reduced)
- Slight emittance increase (to be improved with ramps)
- Accelerating length 0.55 m

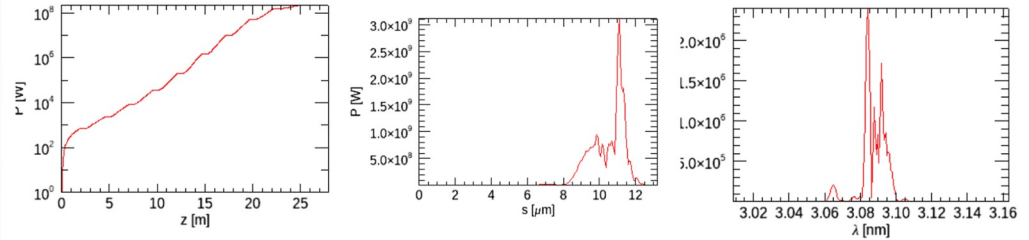
# «Exercise» for the undulator: (from plasma exit only - no TL)

V. Petrillo

Beam from plasma exit (80 cm capillary) E=1.2 GeV



## Undulator tuned at 3. nm

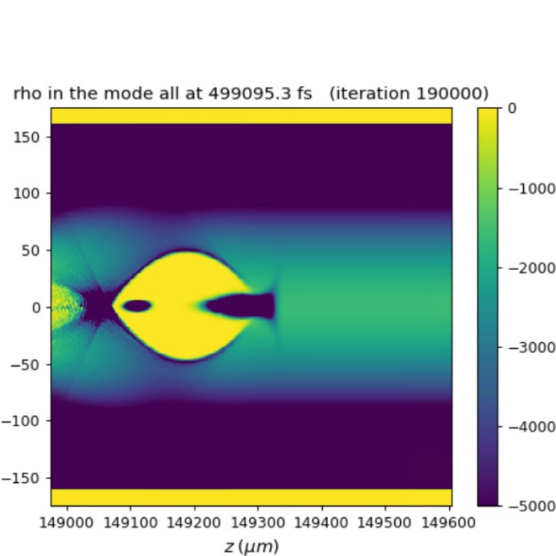


<u>Energy</u>	J	<b>10. 10<sup>-6</sup></b>
<u>bw</u>	%	0.25
<u>size</u>	m	8 10 <sup>-5</sup>
<u>div</u>	rad	1.3 10 <sup>-5</sup>
<u>Photon number</u>		<b>1.5 10<sup>11</sup></b>
<u>wavelength</u>	nm	<b>3.</b>

## Undulator tuned at 2.5 nm

<u>Energy</u>	J	<b>3.6 10<sup>-6</sup></b>
<u>bw</u>	%	0.26
<u>size</u>	m	7.5 10 <sup>-5</sup>
<u>div</u>	rad	1.15 10 <sup>-5</sup>
<u>Photon number</u>		<b>0.45 10<sup>11</sup></b>
<u>wavelength</u>	nm	<b>2.52</b>

In order to correctly simulate Working Points where the  $Q$  value exceeds 0.5, we are starting to employ the quasi-3D pic codes FBPIC [1] and Smilei [2]. With these codes, phenomena like hose instability can also be simulated.



FBPIC documentation

View page source

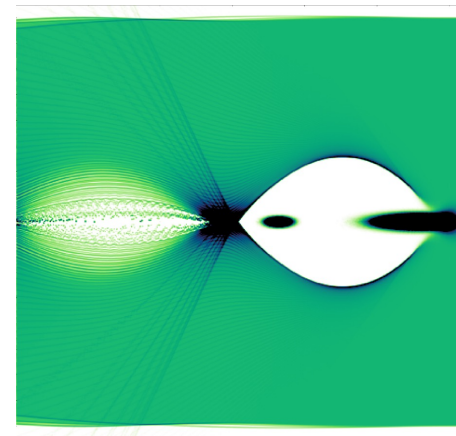
### FBPIC documentation

FBPIC (Fourier Bessel Particle-In-Cell) is a Particle-In-Cell (PIC) code for relativistic plasma physics. It is especially well-suited for physical simulations of laser-wakefield acceleration and plasma-wakefield acceleration.

The distinctive feature of FBPIC, compared to most other PIC codes, is to use a spectral cylindrical representation. This makes the code both fast and accurate, for situations with close-to-cylindrical symmetry. For a brief overview of the algorithm, its advantages and limitations, see the section Overview of the code.

In addition, FBPIC implements several useful features for laser-plasma acceleration, including:

- Moving window
- Calculation of space-charge fields at the beginning of the simulation
- Intrinsic mitigation of Numerical Cherenkov Radiation (NCR) from relativistic bunches
- Field ionization module (ADK model)
- Support for boosted-frame simulations (see Running boosted-frame simulations)



Smilei

Overview Understand Use

Units  
PIC algorithms  
Parallelization & optimization  
Physics modules  
Advanced numerical techniques

# Smilei

v4.7

Smilei is a Particle-In-Cell code for plasma simulation. Open-source, collaborative, user-friendly and designed for high performance on super-computers, it is applied to a wide range of physics studies: from relativistic laser-plasma interaction to astrophysics.

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The WP under consideration has  $q_W = 50$  pC,  $q_D = 500$  pC and  $Q > 2$  (depending on driver transverse size). The goal is to generate accelerating fields well in excess of 1 GV/m.

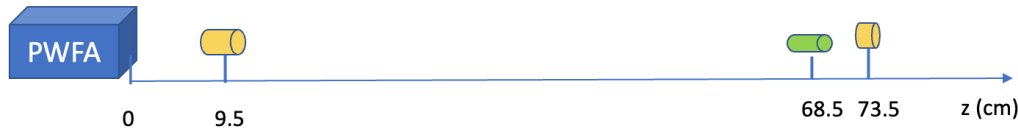
[1] <https://fbpic.github.io>

[2] <https://smileipic.github.io/Smilei/index.html#>

## Low current configuration : lens-collimator-lens

A new beam line was designed to test the line at lower currents close to those currently reachable

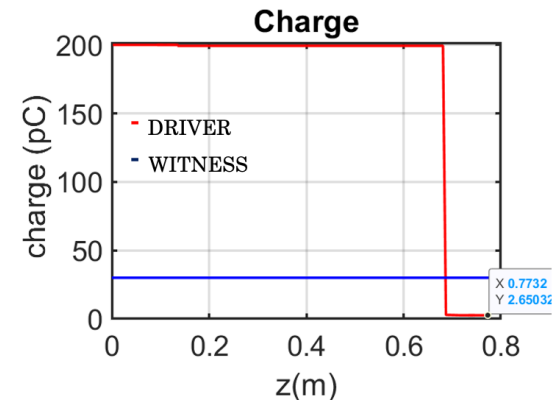
- Simulations have been performed by means of GPT for beam dynamics and a Matlab-based code for the plasma lens



- Witness macro particles 29934
- Diver macro particles 293730

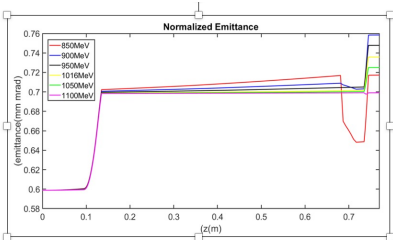
	$l$ (cm)	$d$ (cm)	$I$ (kA)	$r$ ( $\mu\text{m}$ )
lens1	4.0	9.5	0.85	500
lens2	1.0	73.5	0.80	500
coll	3.0	68.5	-	150

- ✓ transfer line of 74.5cm
- ✓ No change in bunch charge
- ✓ Energy spread remains about constant
- ✓ 1.3% driver charge at 74,5 cm

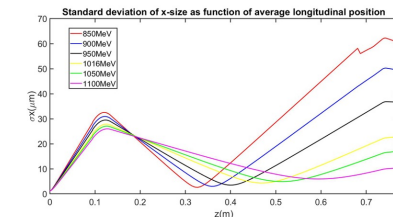
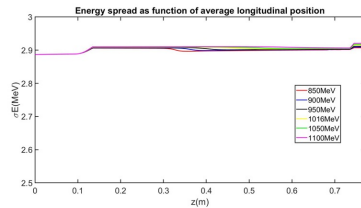




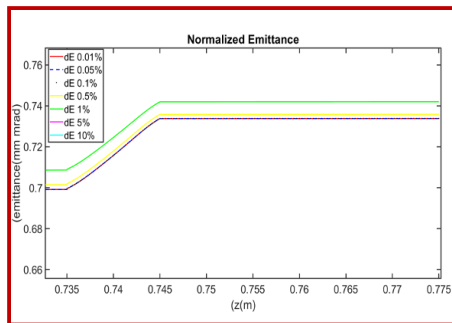
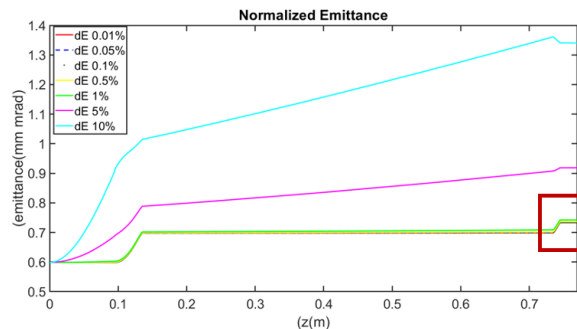
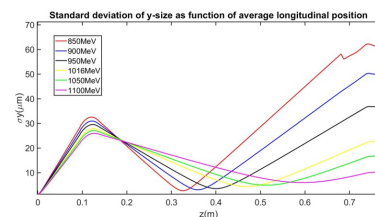
## Energy variation from 850 MeV to 1100MeV



- 850MeV charge reduced of 5.7%
- 900MeV charge reduced of 0.4%



- Energy spread remains about constant for each run
- The trend of sigma x (y) is preserved



- On going: Architect code to verify the emittance growth inside active plasma lenses
- Next: - Geant 4 simulations to include electromagnetic processes (Production of gamma rays, Bremsstrahlung, Multiple scattering,...).  
- Parametric studies with different beam configurations.

- No change in bunch charge
- Energy spread remains about constant for each run
- The trend of sigma x (y) is preserved

# Summary

## TD-RC Recommendations

This latter solution (3m + 3x2m S-band) does look promising and the RC endorses plans to study this option in more details..

The planned tolerance and jitter studies will be important to make a final choice, as it may affect anticipated parameters of the driver/witness bunches at the entrance of the plasma..

## Actions completed/non

The PhotoInjector Layout has been consolidated with the 3m +3x2m S-band scheme

The study has started with the benchmark of the simulation code/procedure with experimental results from SPARC\_LAB, to provide the most realistic predictions for EuPRAXIA at SPARC\_LAB. **The work now has to be completed**

### In particular:

- **Now we have to address the capture& matching Tline after the plasma to not loose the beam quality and optimize the undulator performance,**
  - **The X-band at the gun exit could help reducing the twisting of the long phase space of the plasma accelerated beam after the HE separation chicane**
  - **A dogleg with  $R_{56} < 5E-4$  will be studied**

# Next steps & Conclusions/MS

- ❑ Check of the diagnostics & beam measurements before and after the plasma
- ❑ Finalize plasma focusing w ramps
- ❑ Rise number of photons at undulator exit  
⇒ comparison with the “all\_RF” beam of same charge (the 50+230 pC beam is ready to be simulated in plasma)
- ❑ Finalize spectrometers & dumpers
- ❑ Finalize 2<sup>nd</sup> transfer line to ARIA undulator

## Reasonable milestones:

- **May 2023:** Stability & jitter sensitivity studies plus virtual measurements
- **June 2023:** First results on laser heater parameters w MBI studies for «all RF» beam



**Thanks for your  
attention**

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