

University of Goettingen, Institute for Theoretical Physics

FREEZE-IN: PROBLEMS AND OPPORTUNITIES

Francesco Costa

C. Cosme, FC, O. Lebedev, arXiv: 2306.13061

FC, L. Covi, to appear soon

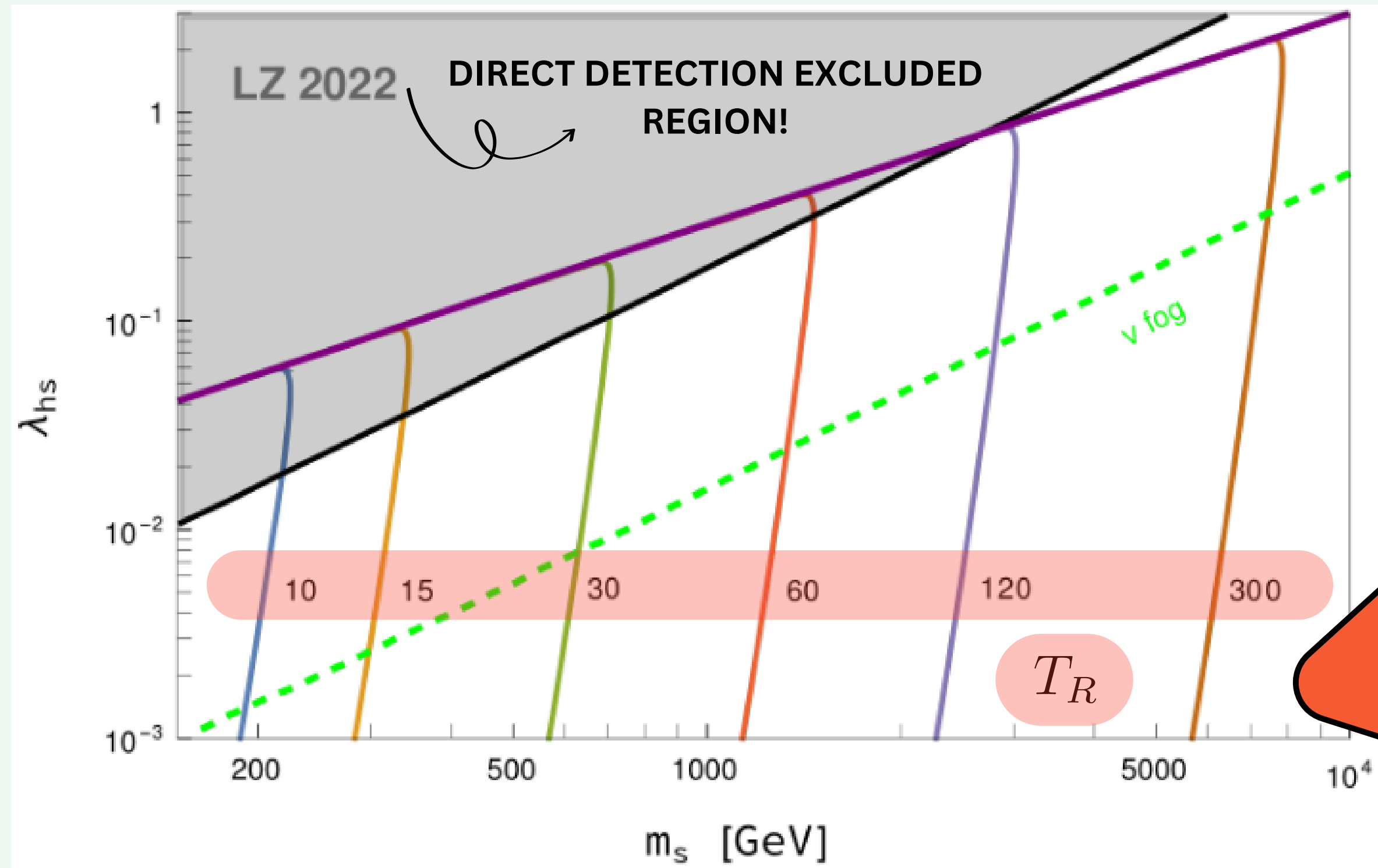


“Artistic” interpretation of
a FIMP dark matter

TeVPA 2023, Napoli

HIGGS PORTAL TO SCALAR DM

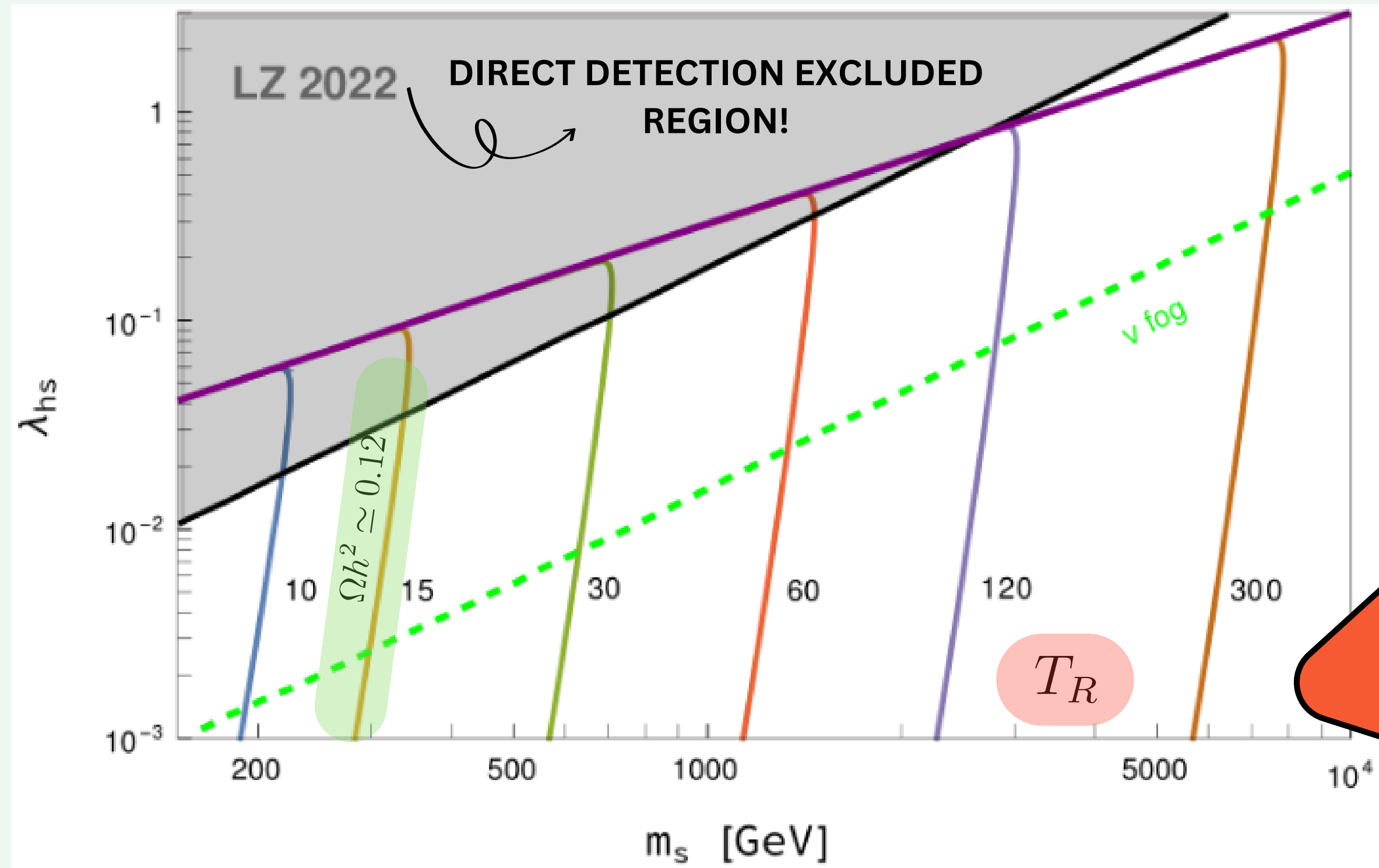
FREEZE-IN



! SPOILER ALERT

HIGGS PORTAL TO SCALAR DM

FREEZE-IN



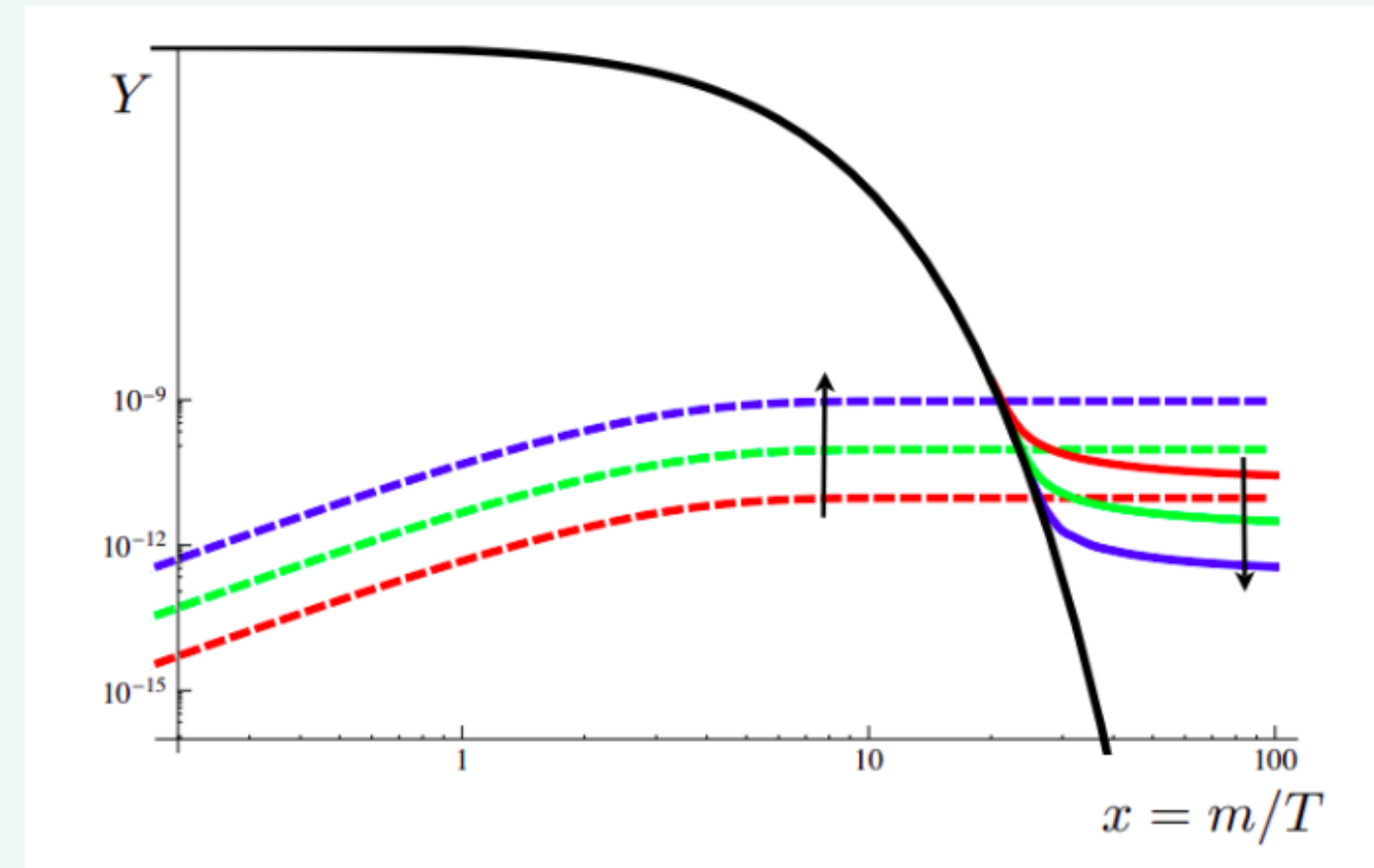
SPOILER ALERT

FREEZE-IN

$$\Gamma < H$$

- Out-of-equilibrium
- Dependence on the initial conditions
→ We assume a negligible initial abundance
- Very low couplings

$$\lambda \sim \mathcal{O}(10^{-10})$$

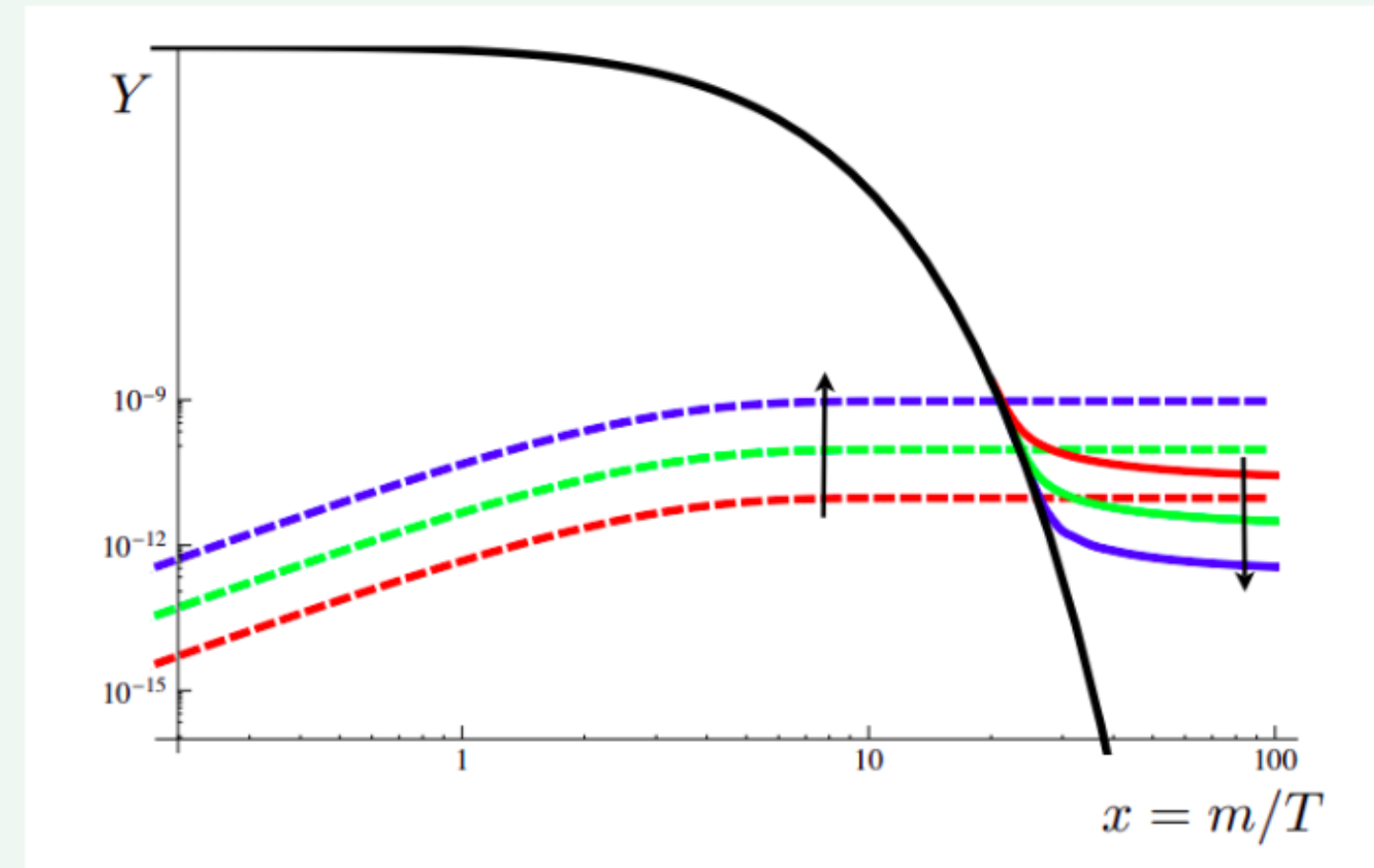


FREEZE-IN

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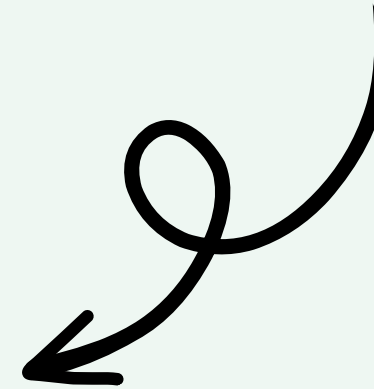
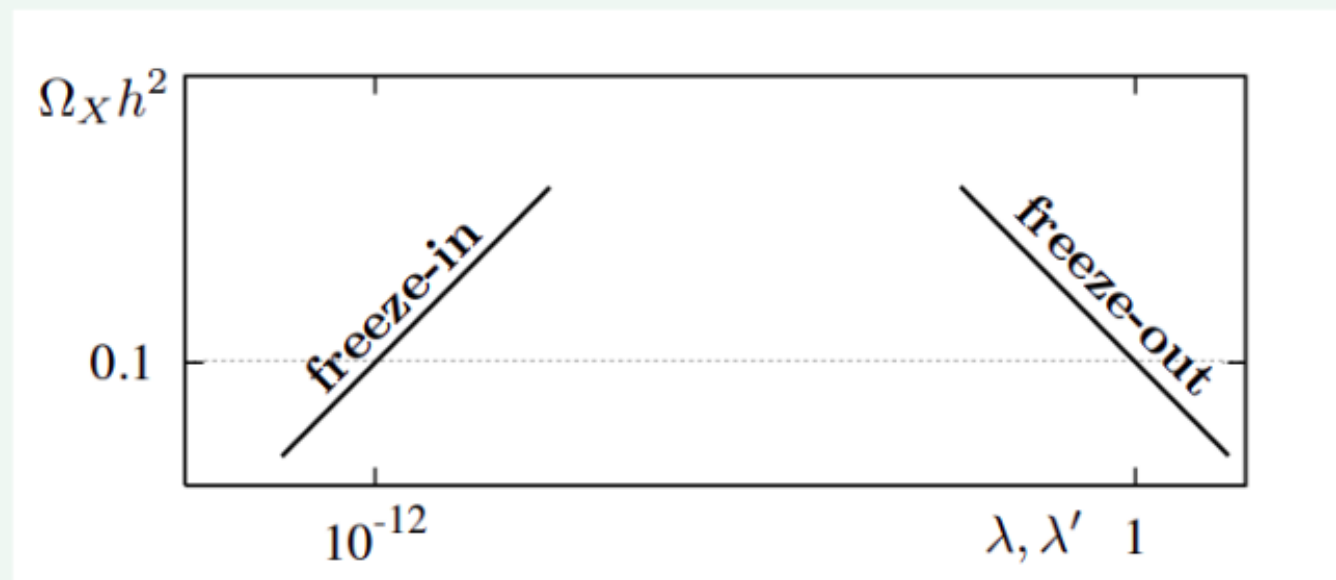
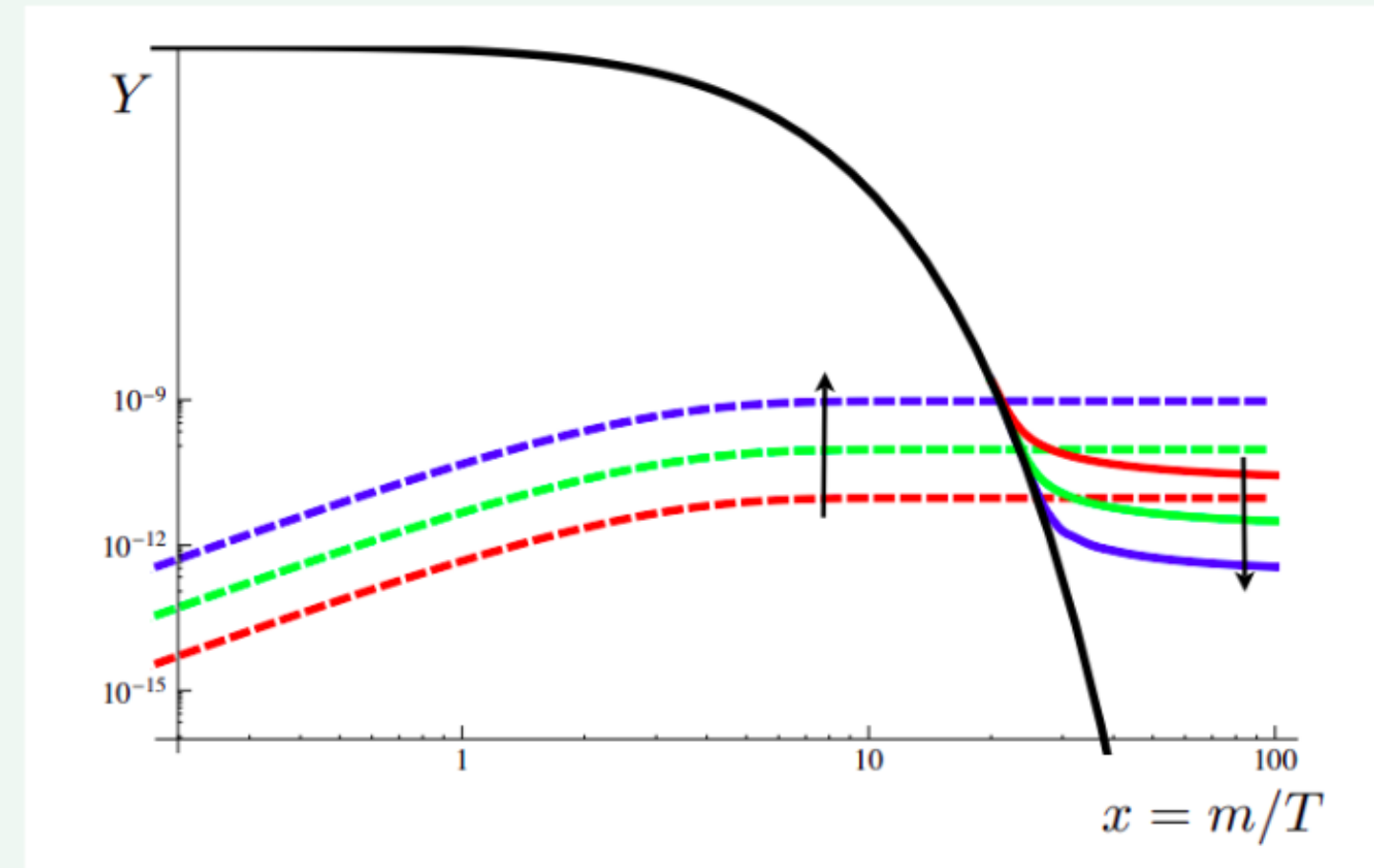
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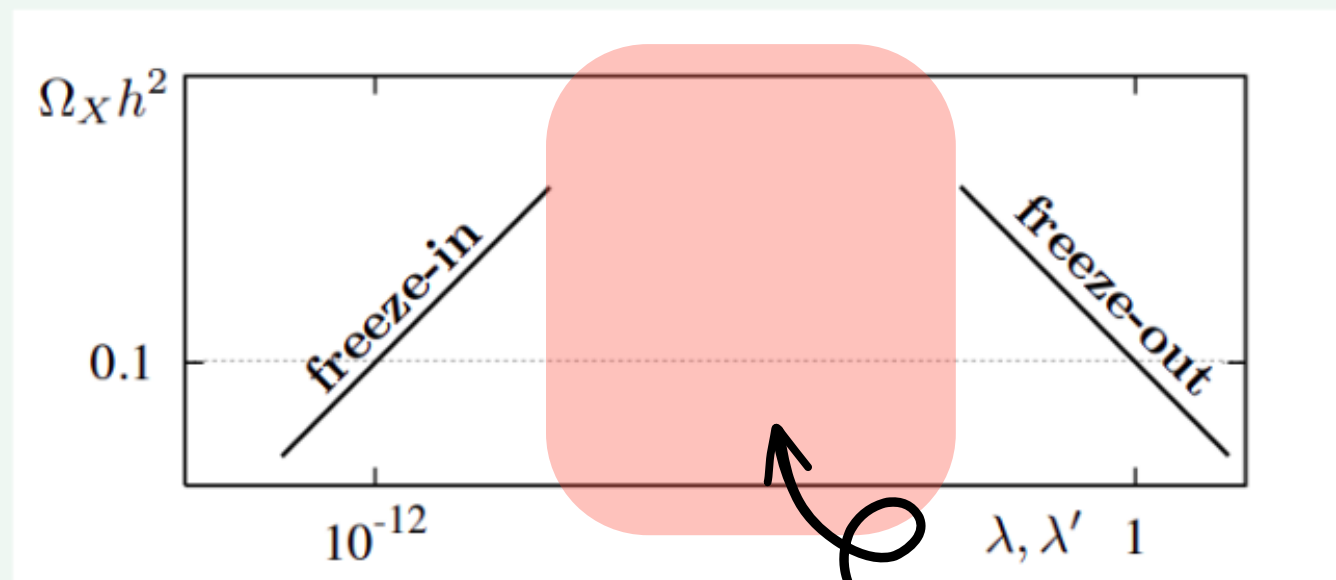
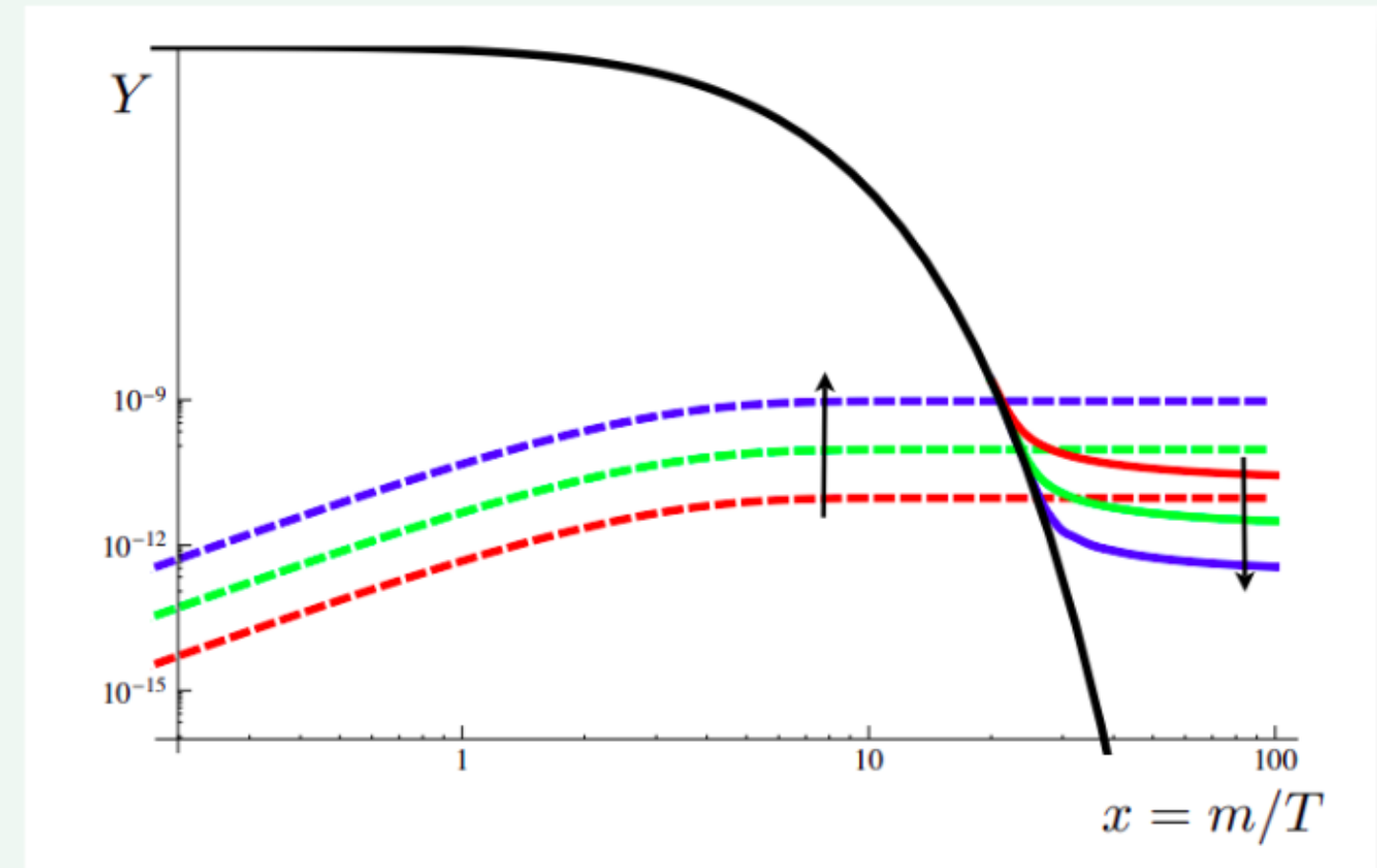
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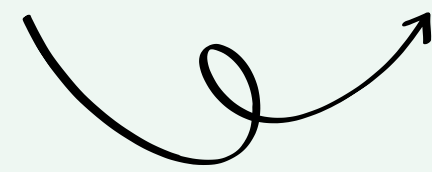


Overproduction

GRAVITATIONAL PARTICLE PRODUCTION

INFLATON OSCILLATING AT THE END OF INFLATION

OSCILLATION OF THE SCALE FACTOR



with s is a feebly interacting particle

GRAVITATIONAL PARTICLE PRODUCTION

INFLATON OSCILLATING AT THE END OF INFLATION

with s is a feebly interacting particle

OSCILLATION OF THE SCALE FACTOR

$$\langle a(t) \rangle = a_0 \left(\frac{t}{t_0} \right)^{\frac{n+2}{3n}}$$

OSCILLATING BACKGROUND METRIC

GRAVITATIONAL PARTICLE PRODUCTION

INFLATON OSCILLATING AT THE END OF INFLATION

with s is a feebly interacting particle

OSCILLATION OF THE SCALE FACTOR

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PARTICLE PRODUCTION

OSCILLATING BACKGROUND METRIC



GRAVITATIONAL PARTICLE PRODUCTION

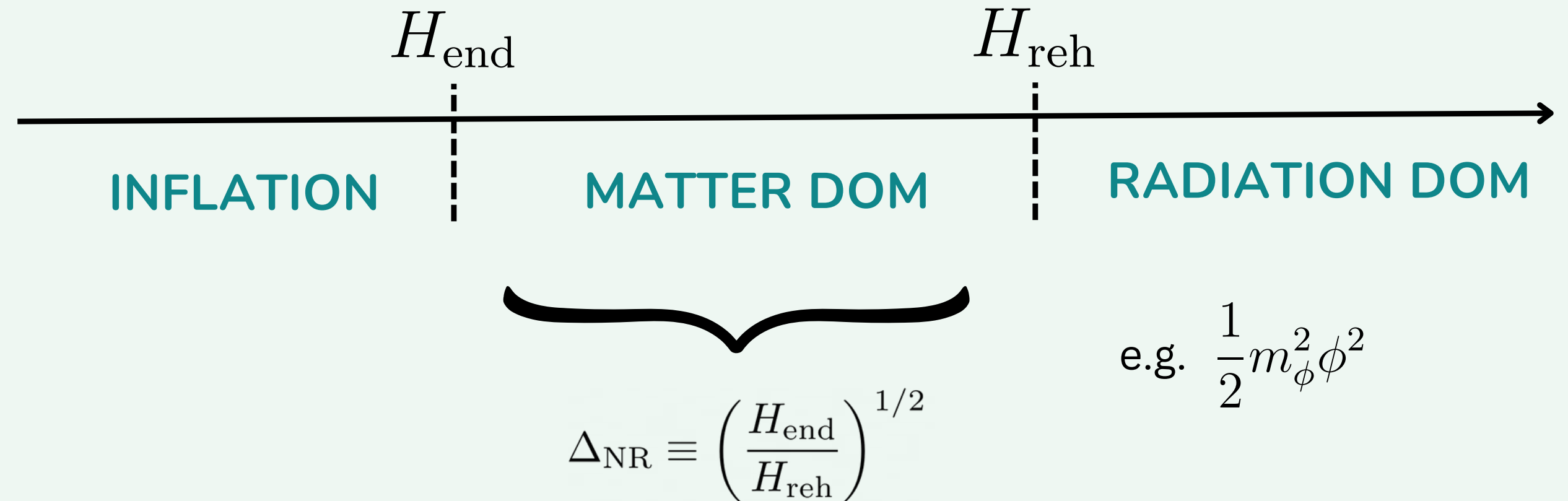
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PRODUCTION DURING
INFLATON OSCILLATION

GRAVITATIONAL PARTICLE PRODUCTION

s is a feebly interacting particle

PRODUCTION DURING
INFLATON OSCILLATION



GRAVITATIONAL PARTICLE PRODUCTION

s is a feebly interacting particle

PRODUCTION DURING INFLATON OSCILLATION



$$\Omega_s h^2 \lesssim 0.1$$

$$\Delta_{\text{NR}} \gtrsim 10^6 \left(\frac{H_{\text{end}}}{M_{\text{Pl}}} \right)^{3/2} \left(\frac{m_s}{\text{GeV}} \right)$$

$$\Delta_{\text{NR}} \equiv \left(\frac{H_{\text{end}}}{H_{\text{reh}}} \right)^{1/2}$$

e.g. $\frac{1}{2} m_\phi^2 \phi^2$

Lower bound on the length matter dominated epoch in order to avoid overproduction of DM

DURING INFLATION

O. Lebedev, 2210.02293
Y. Ema, R. Jinno, K. Mukaida, K. Nakayama, 1502.02475

$$\Delta_{\text{NR}} \gtrsim 10^7 \lambda_s^{-3/4} \left(\frac{H_{\text{end}}}{M_{\text{Pl}}} \right)^{3/2} \left(\frac{m_s}{\text{GeV}} \right) \quad \leftarrow \quad \lambda_s \text{ is the self-coupling}$$

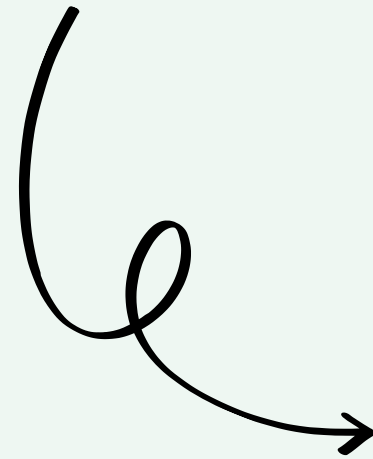
INFLATON OSCILLATION

$$\Delta_{\text{NR}} \gtrsim 10^6 \left(\frac{H_{\text{end}}}{M_{\text{Pl}}} \right)^{3/2} \left(\frac{m_s}{\text{GeV}} \right)$$

QUANTUM GRAVITY

$$C \frac{\phi^4 s^2}{M_{\text{Pl}}^2} \quad \rightarrow \quad \Delta_{\text{NR}} \gtrsim 10^{17} C^2 \frac{m_s}{\text{GeV}}$$

**LONG MATTER DOMINATED
EPOCH**

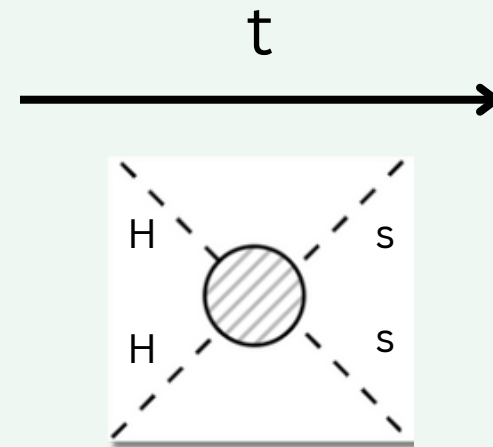


**LOW REHEATING
TEMPERATURE**

WHAT HAPPENS AT LOW TR?

Higgs portal

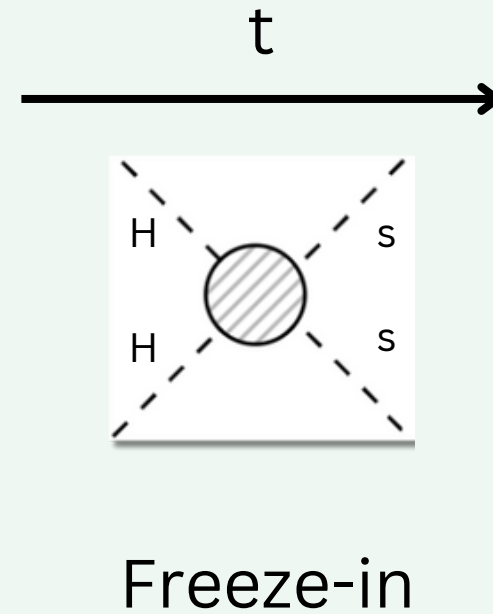
$$\mathcal{L} \supset \frac{1}{2} \lambda_{hs} s^2 H^\dagger H$$



WHAT HAPPENS AT LOW TR?

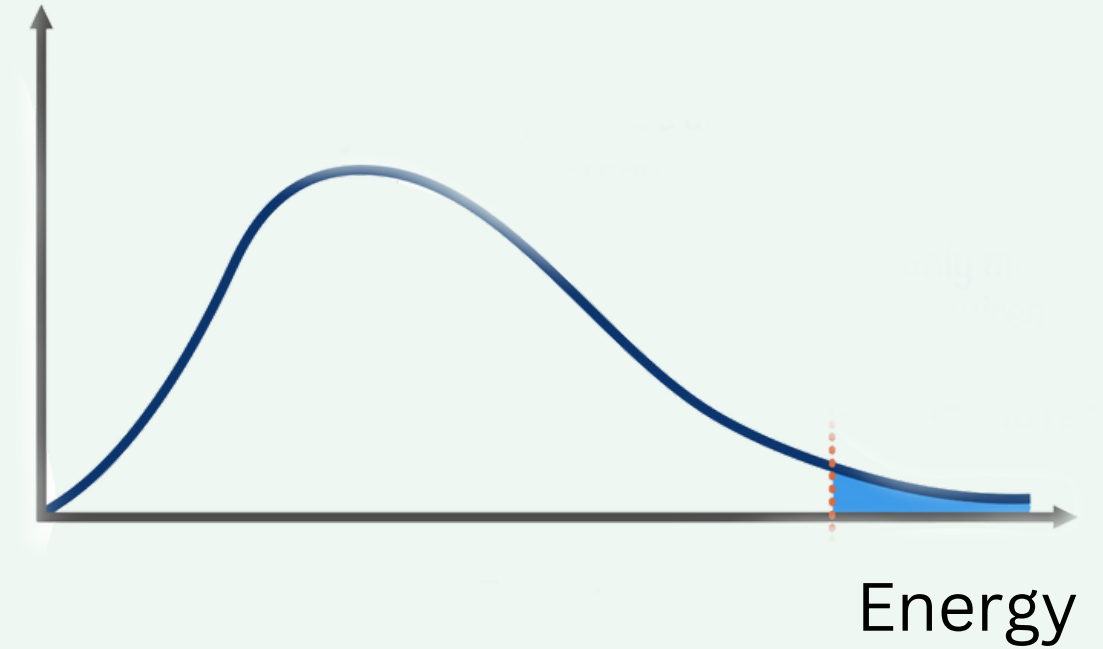
Higgs portal

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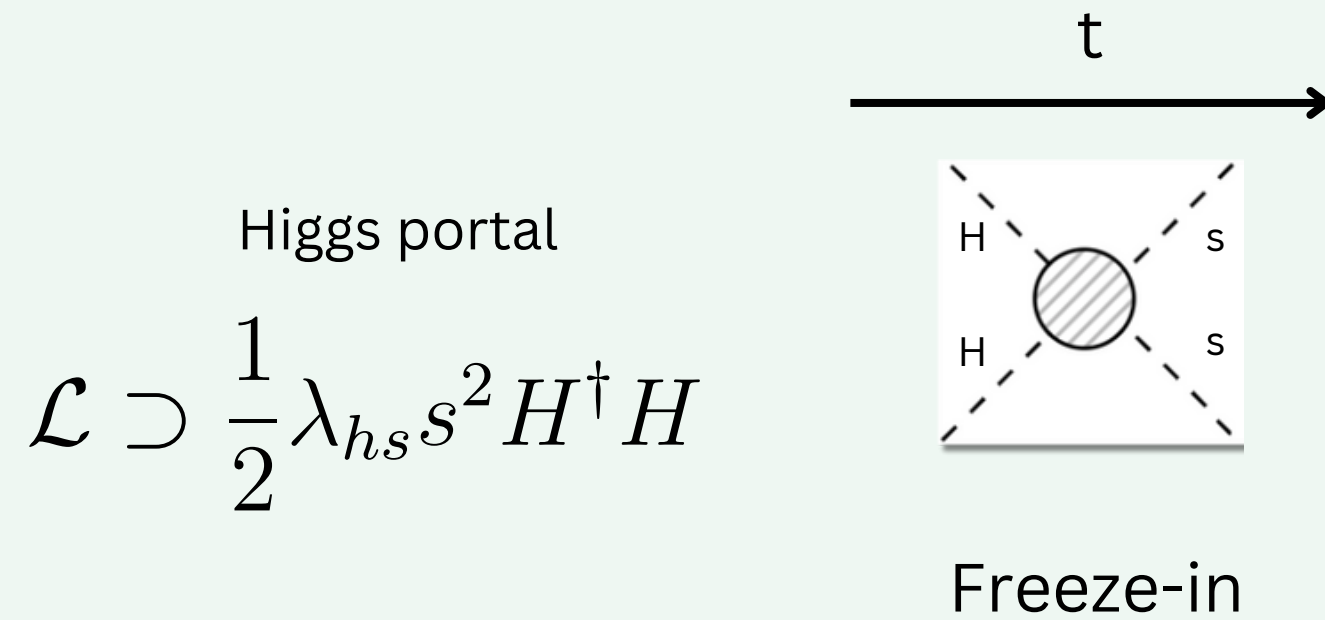
$$m_H < m_s \quad \& \quad T_R < m_s$$

of H particles

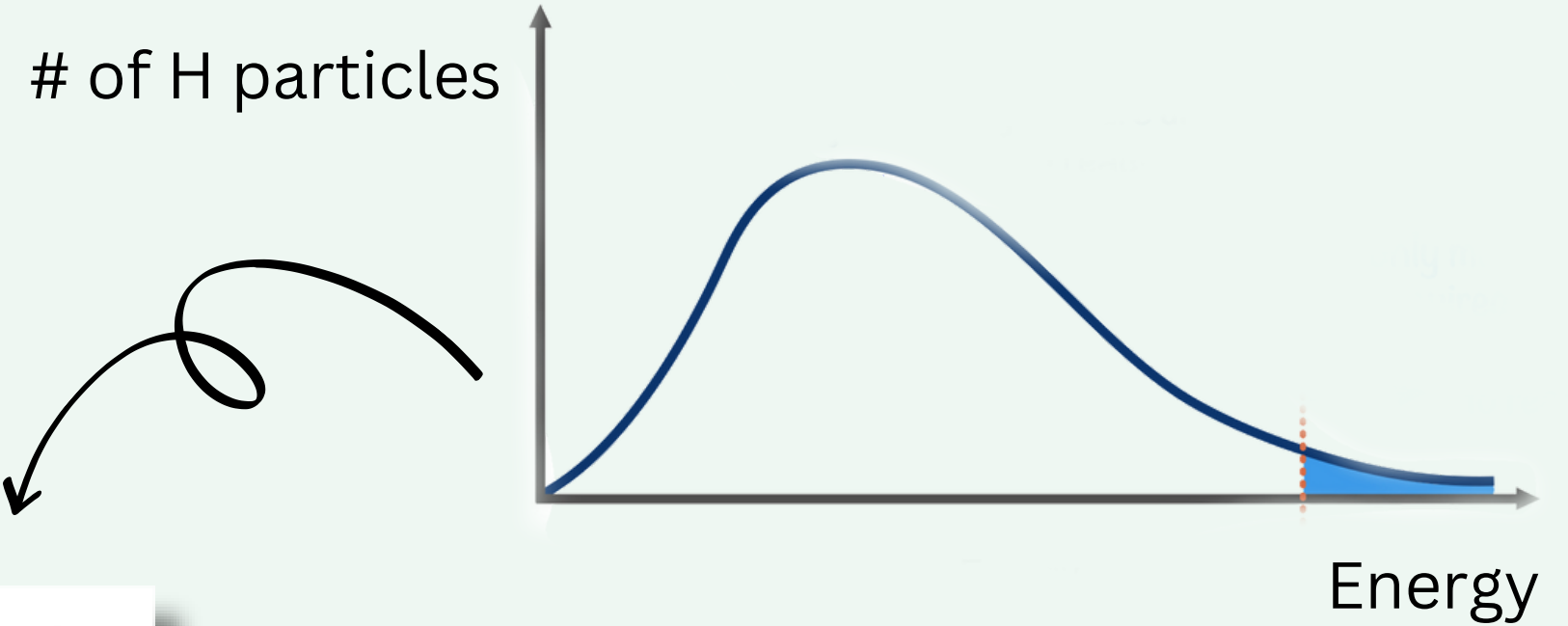


Boltzmann distribution

WHAT HAPPENS AT LOW TR?



$$m_H < m_s \quad \& \quad T_R < m_s$$

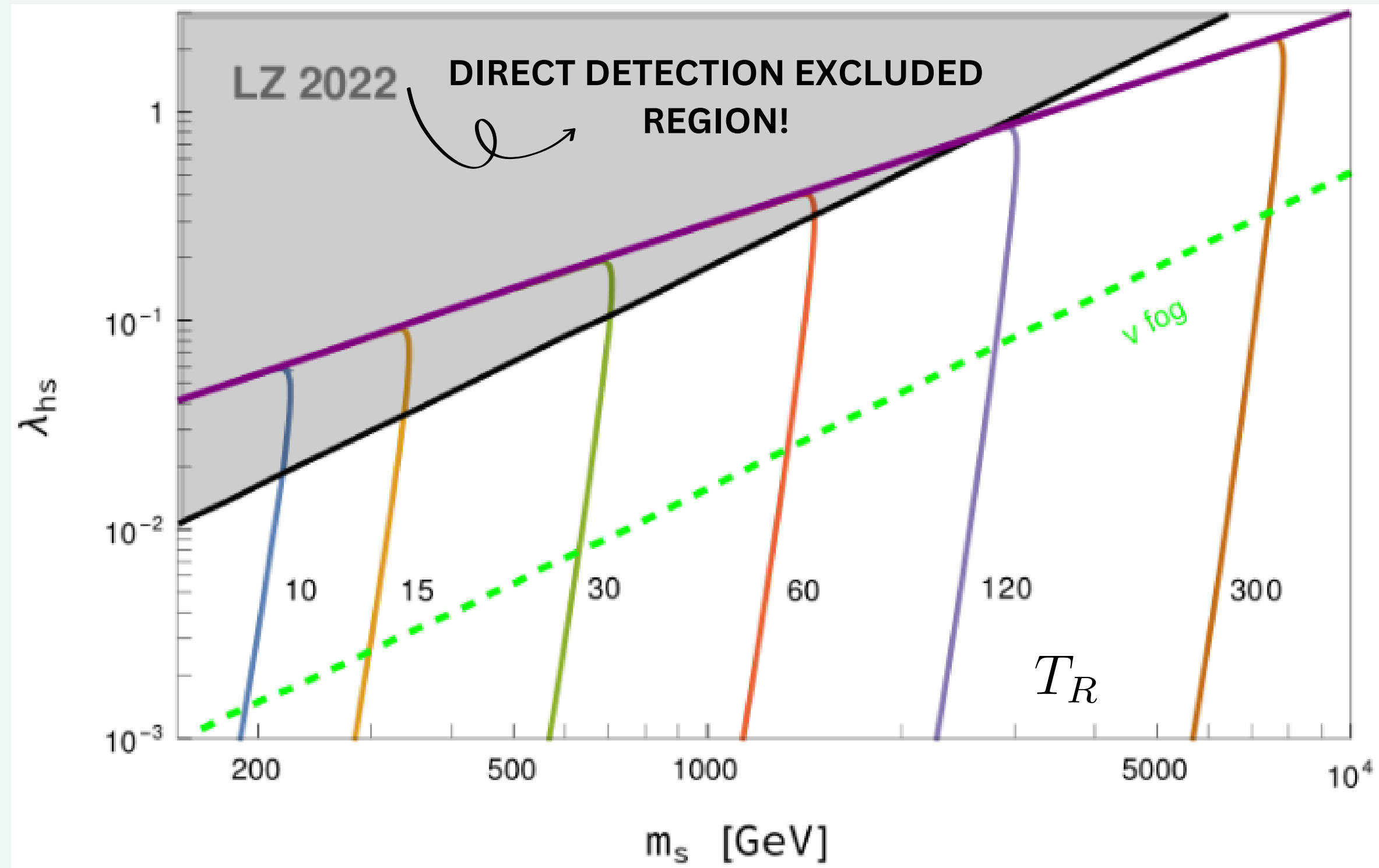


Boltzmann distribution

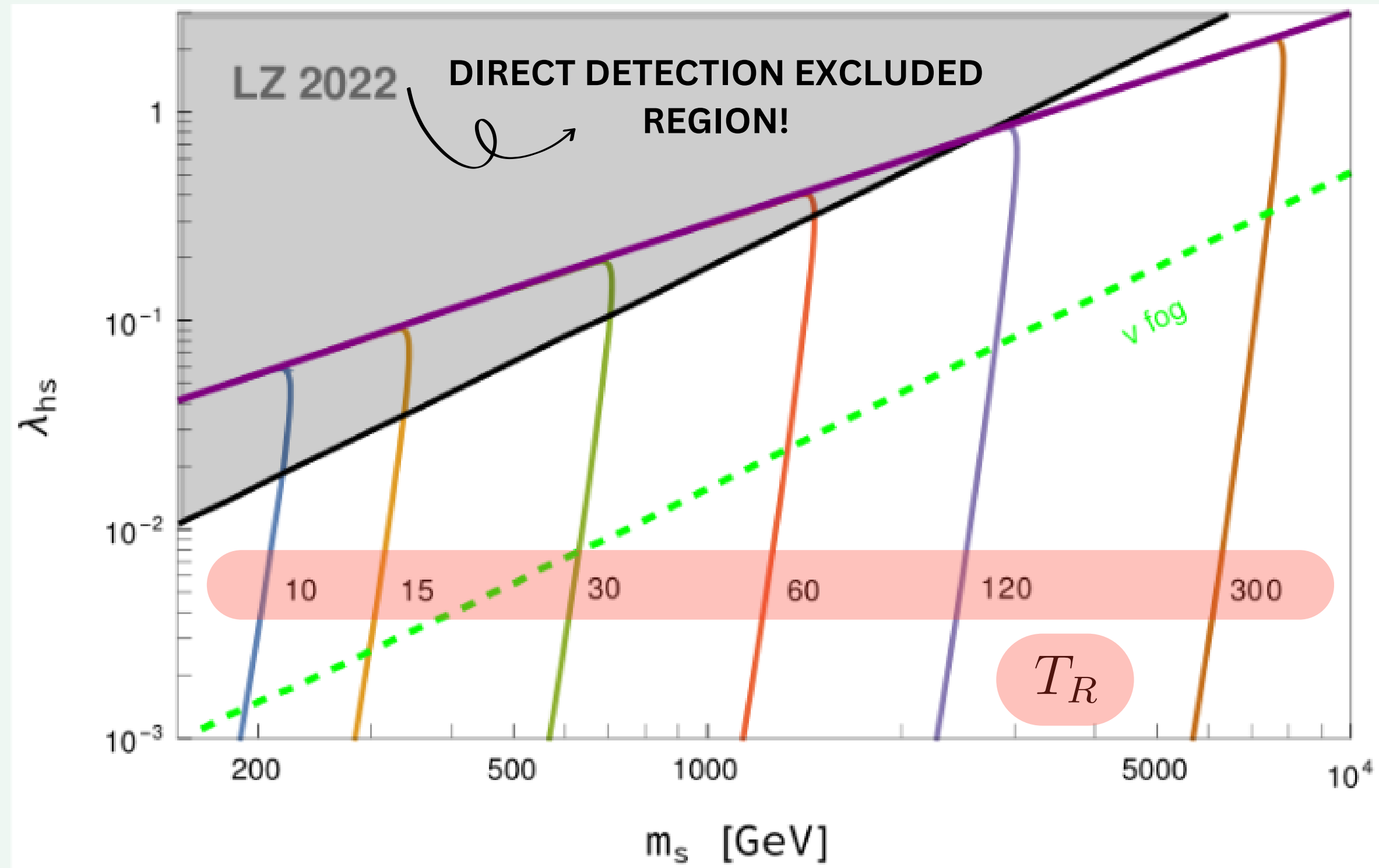
$$\Gamma(h_i h_i \rightarrow ss) \simeq \frac{\lambda_{hs}^2 T^3 m_s}{2^7 \pi^4} e^{-2m_s/T}$$

The rate of production is Boltzmann suppressed

HIGGS PORTAL TO SCALAR DM

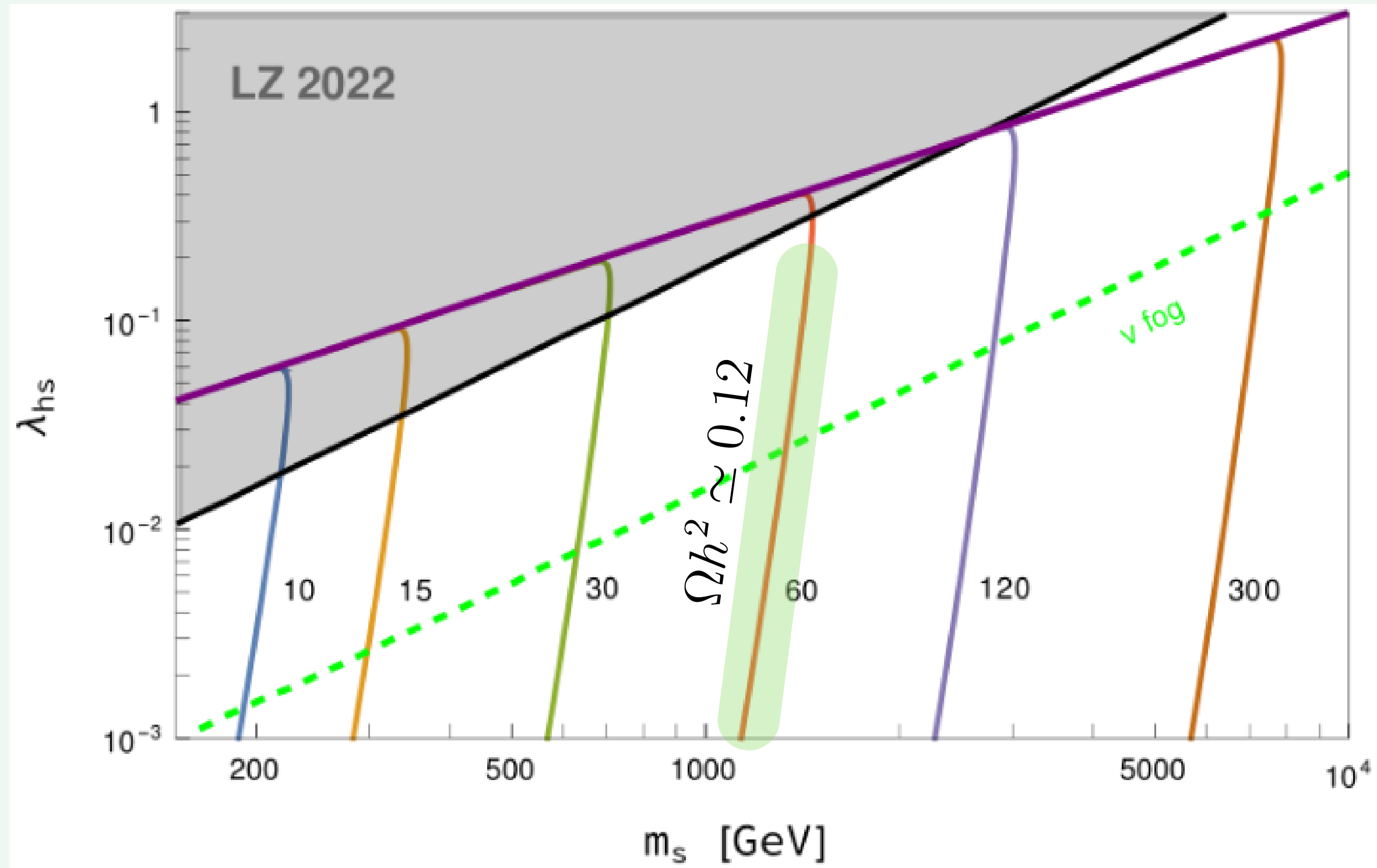


HIGGS PORTAL TO SCALAR DM



HIGGS PORTAL TO SCALAR DM

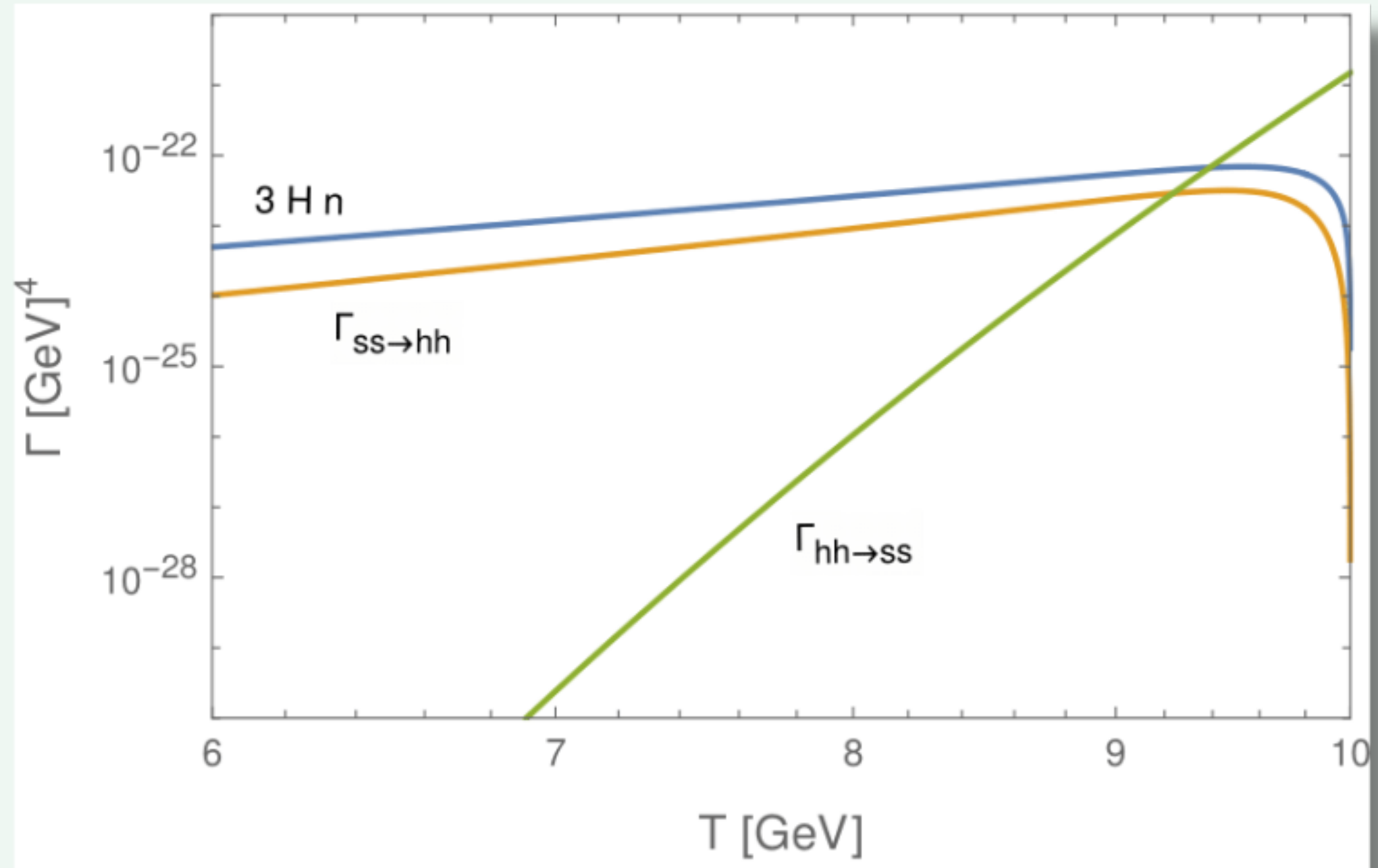
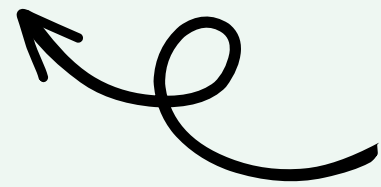
FREEZE-IN



FREEZE-IN REGIME

Boltzmann equation

$$\dot{n} + 3Hn = \Gamma(h_i h_i \rightarrow ss) - \Gamma(ss \rightarrow h_i h_i)$$

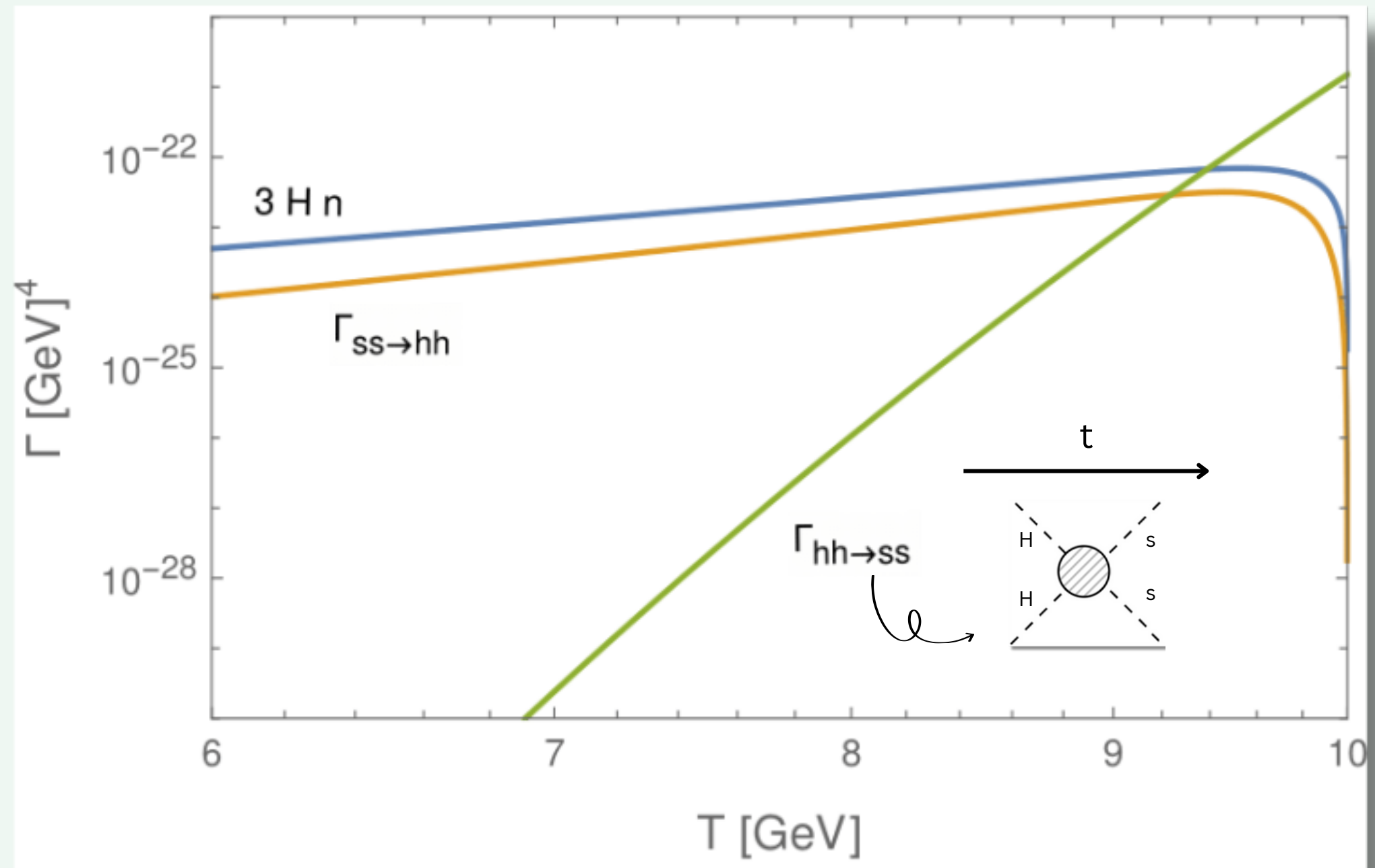
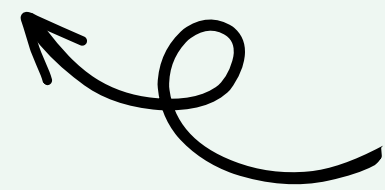


←
TIME

FREEZE-IN REGIME

Boltzmann equation

$$\dot{n} + 3Hn = \Gamma(h_i h_i \rightarrow ss) - \Gamma(ss \rightarrow h_i h_i)$$

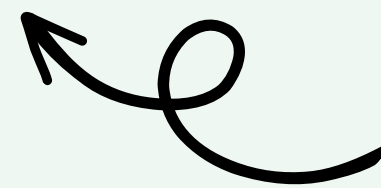


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TIME

FREEZE-IN REGIME

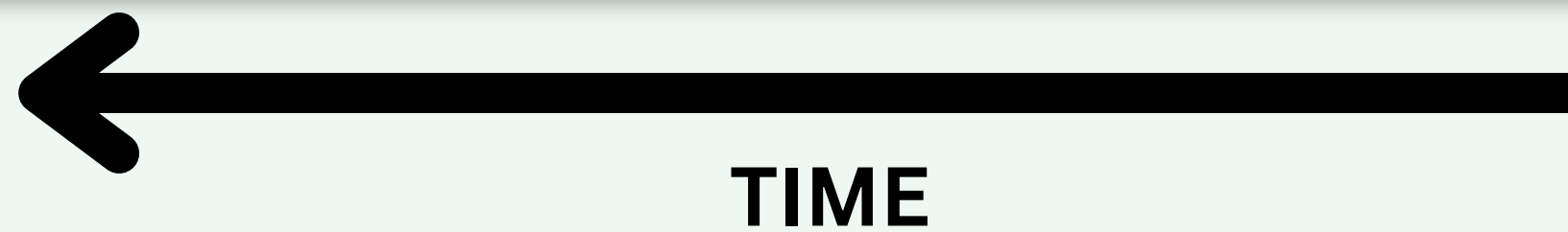
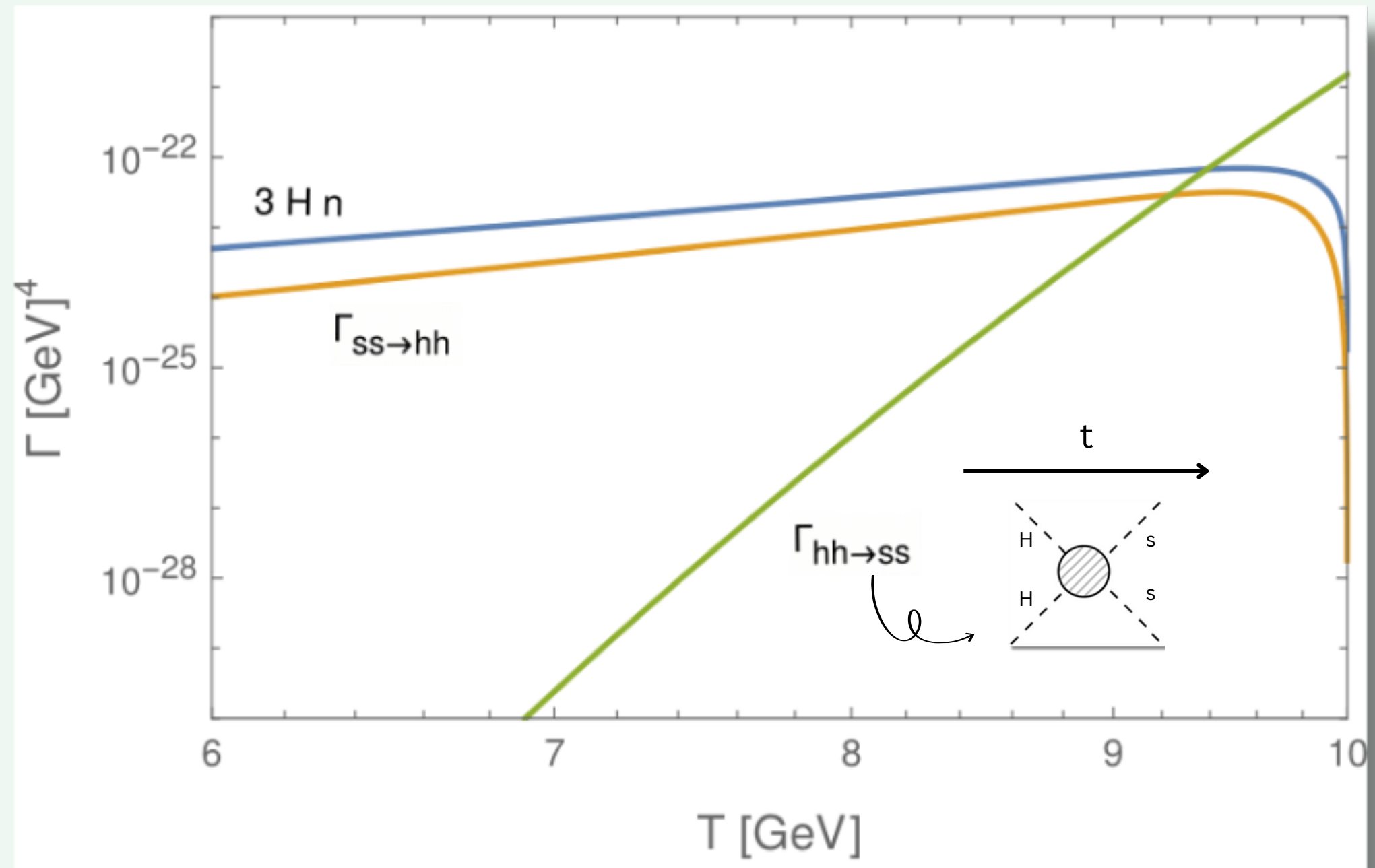
Boltzmann equation

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But

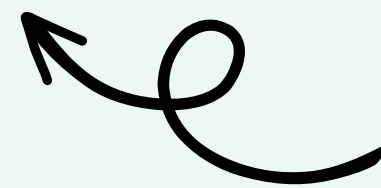
$$\Gamma > 3Hn$$



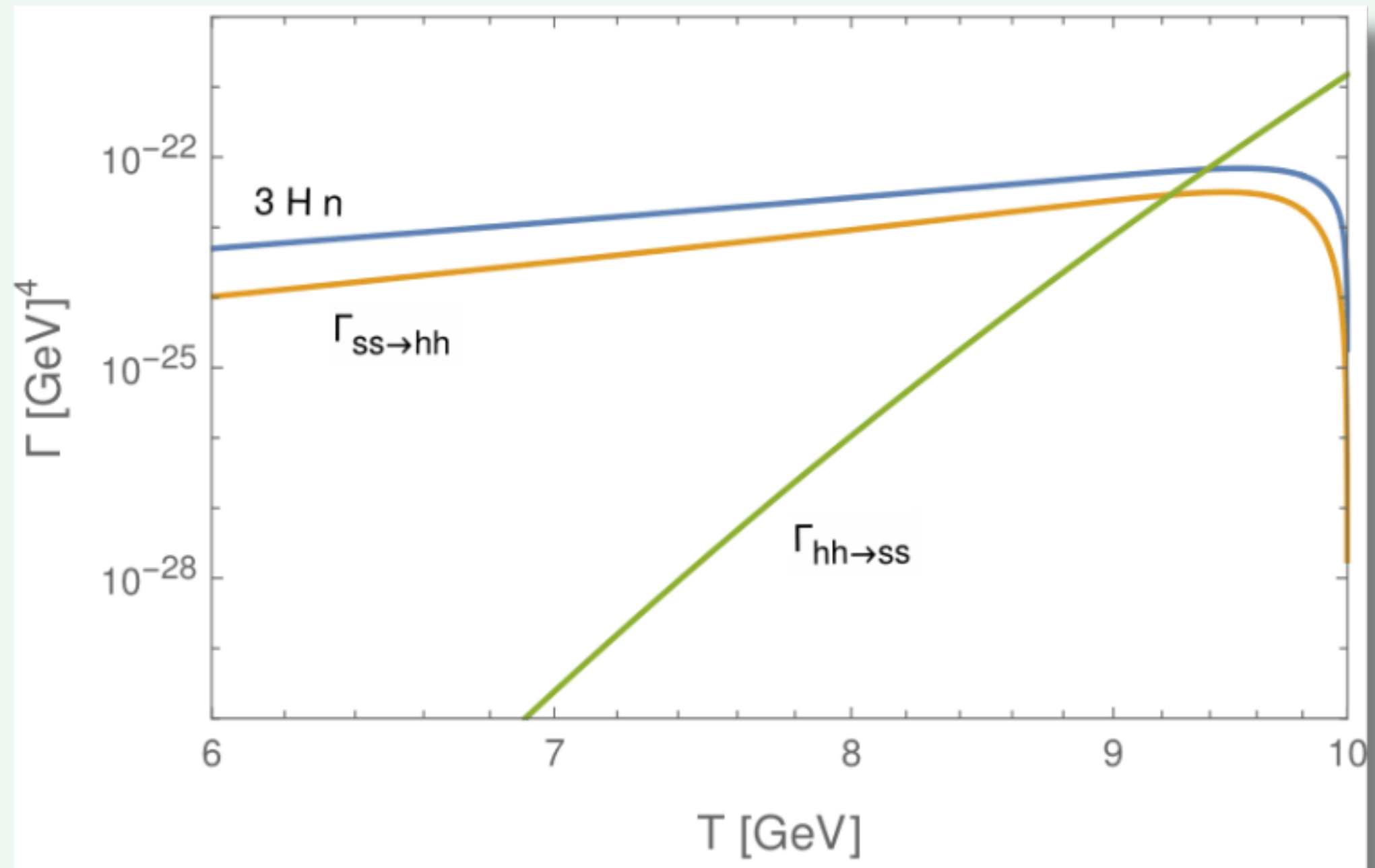
FREEZE-IN REGIME

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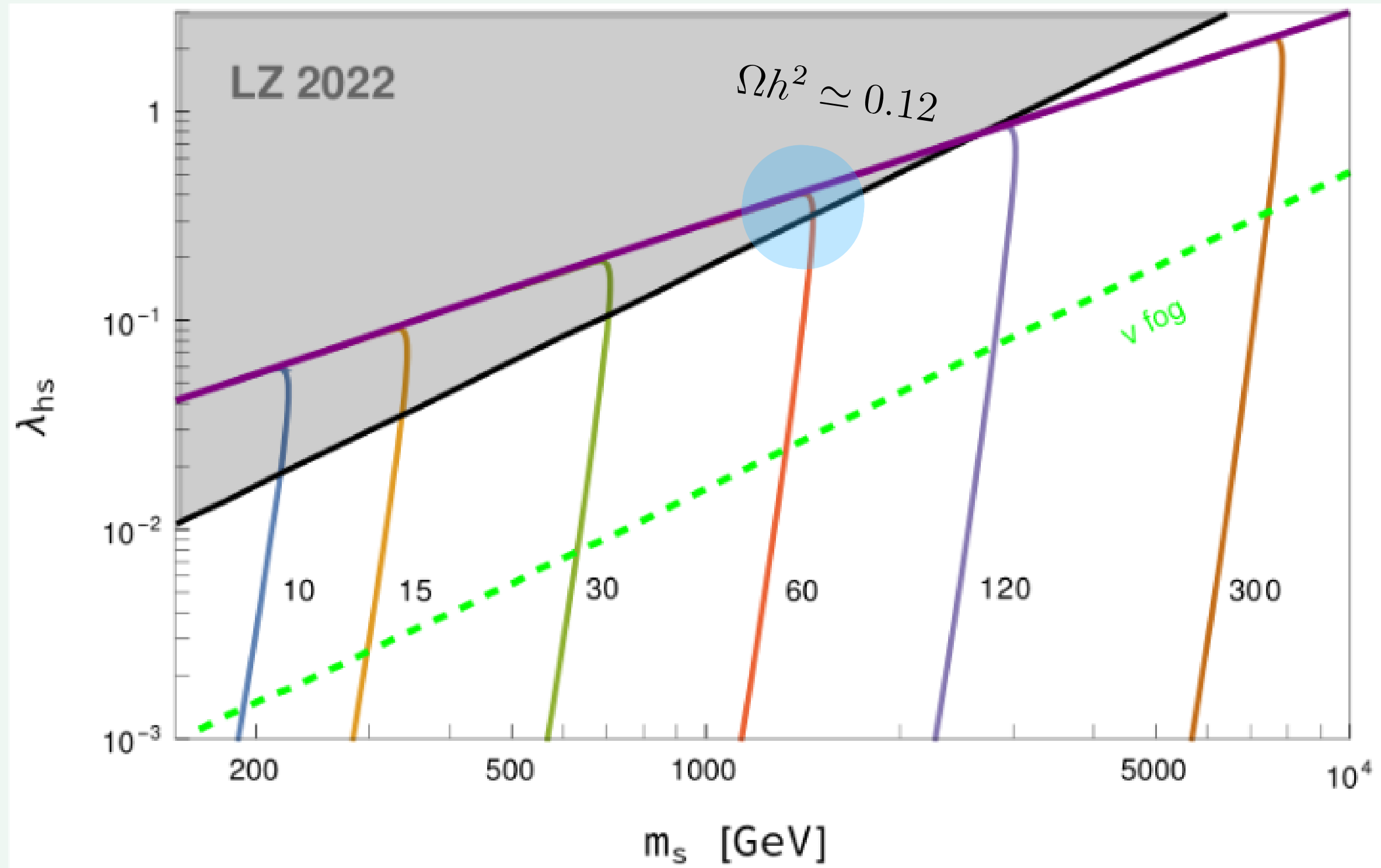
$\Gamma(h_i h_i \rightarrow ss) > 3Hn \not\Rightarrow$ Thermalisation
 $\Gamma(h_i h_i \rightarrow ss) = \Gamma(ss \rightarrow h_i h_i) \Rightarrow$ Thermalisation



TIME

HIGGS PORTAL TO SCALAR DM

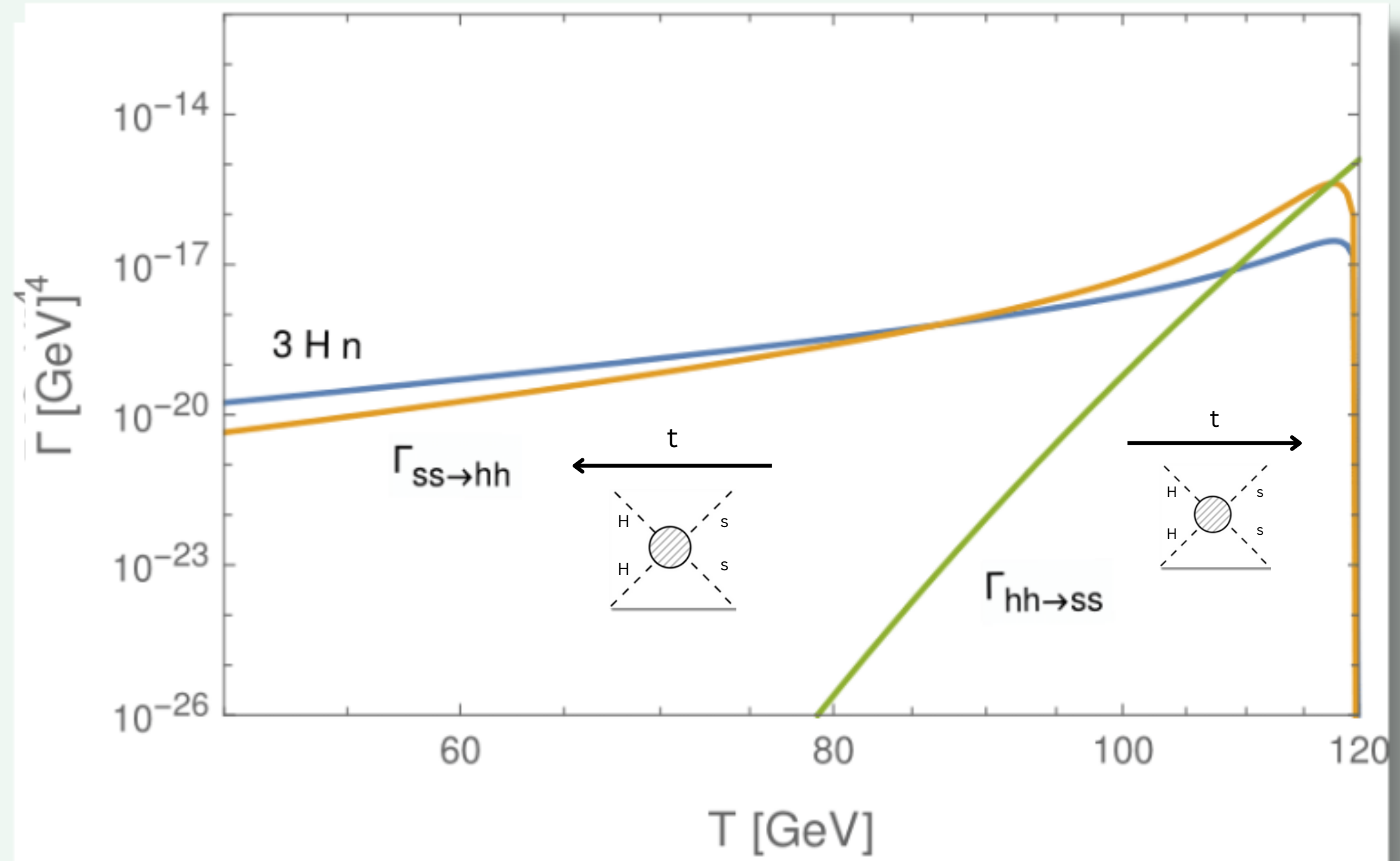
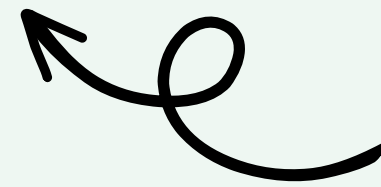
BACKREACTION



ANNIHILATION BECOMES IMPORTANT

Boltzmann equation

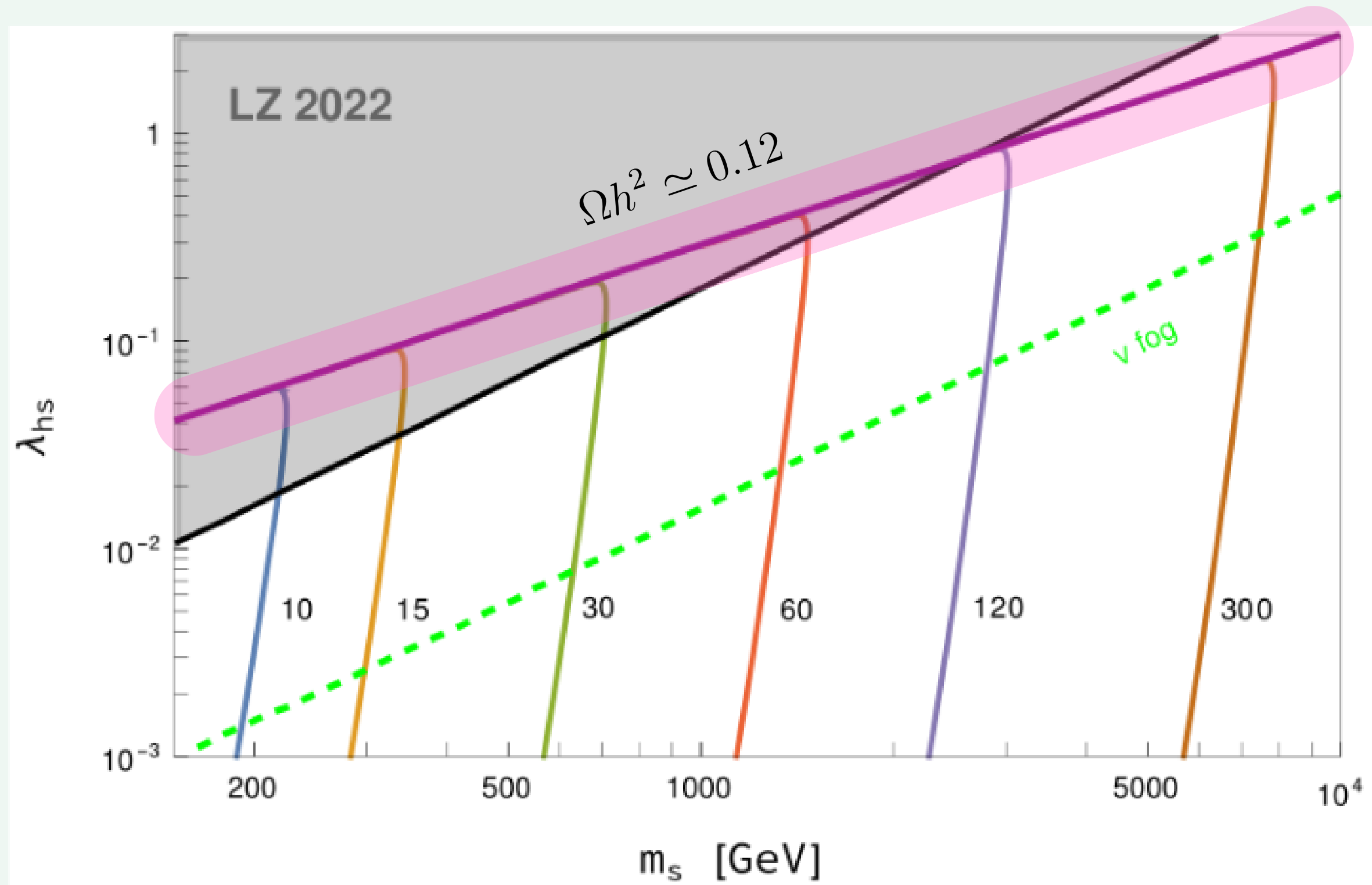
$$\dot{n} + 3Hn = \Gamma(h_i h_i \rightarrow ss) - \Gamma(ss \rightarrow h_i h_i)$$



←
TIME

HIGGS PORTAL TO SCALAR DM

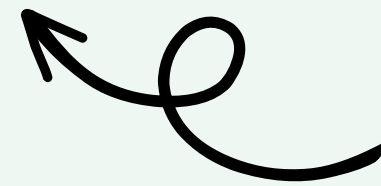
FREEZE-OUT



FREEZE-OUT REGIME

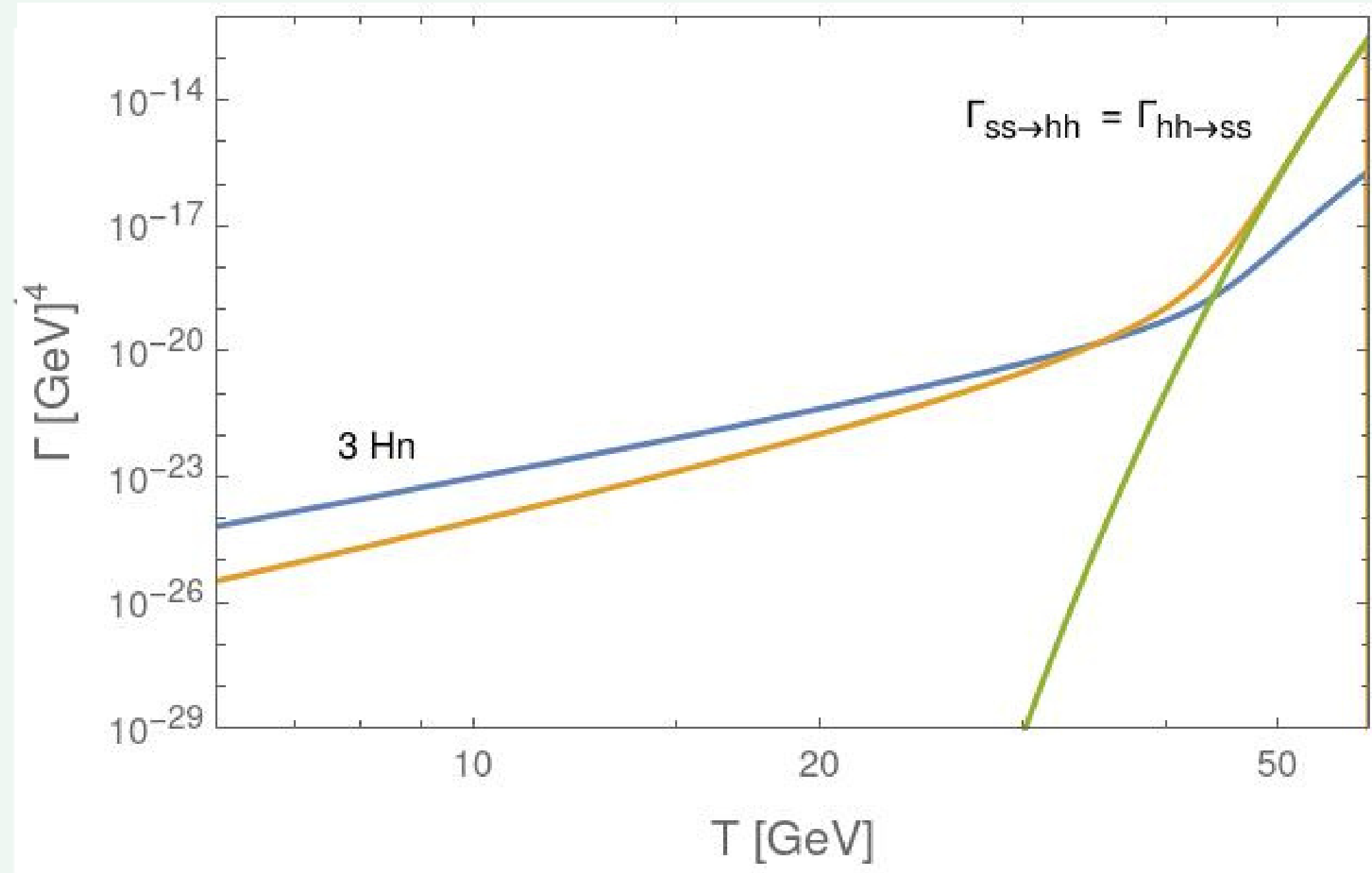
Boltzmann equation

$$\dot{n} + 3Hn = \Gamma(h_i h_i \rightarrow ss) - \Gamma(ss \rightarrow h_i h_i)$$



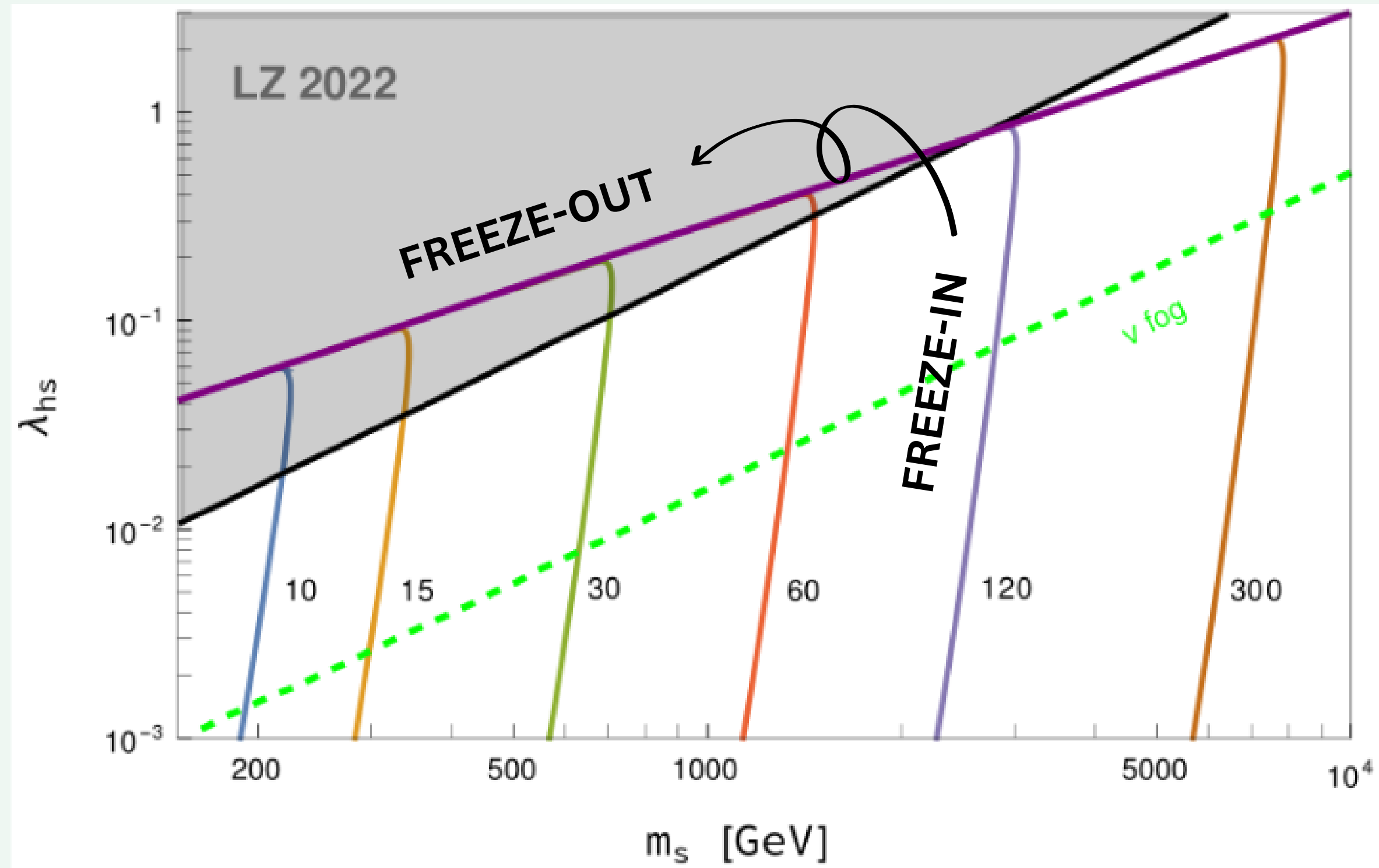
Freeze-out

$$\Gamma(h_i h_i \rightarrow ss) = \Gamma(ss \rightarrow h_i h_i)$$



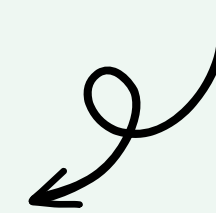
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HIGGS PORTAL TO SCALAR DM



TAKE HOME MESSAGE

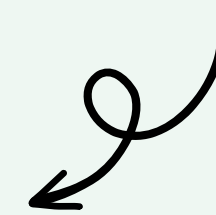
EARLY UNIVERSE EFFICIENT
GRAVITATIONAL PRODUCTION
OF FEEBLY COUPLED PARTICLES



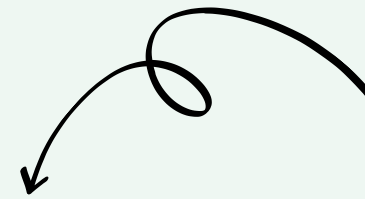
NEED FOR A "LONG" MATTER DOMINATED
EPOCH AND THEREFORE **LOW REHEATING**
TEMPERATURE TO AVOID OVERPRODUCTION

TAKE HOME MESSAGE

EARLY UNIVERSE EFFICIENT
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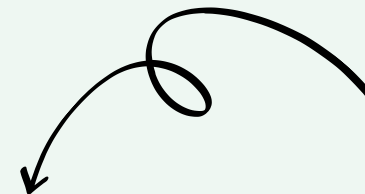
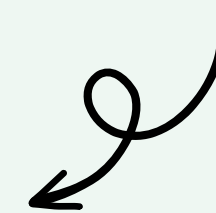
NEED FOR A "LONG" MATTER DOMINATED
EPOCH AND THEREFORE **LOW REHEATING
TEMPERATURE** TO AVOID OVERPRODUCTION



- **BOLTZMANN SUPPRESSED PRODUCTION RATE AND POSSIBLE DIRECT DETECTION SIGNATURES**
- **NO OVERPRODUCTION GAP BETWEEN FREEZE-OUT AND FREEZE-IN AT LOW REHEATING TEMPERATURES**

TAKE HOME MESSAGE

EARLY UNIVERSE EFFICIENT
GRAVITATIONAL PRODUCTION
OF FEEBLY COUPLED PARTICLES



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NEED FOR A "LONG" MATTER DOMINATED EPOCH AND THEREFORE **LOW REHEATING TEMPERATURE** TO AVOID OVERPRODUCTION



THANK YOU

Francesco Costa

Institute for Theoretical Physics,
University of Goettingen



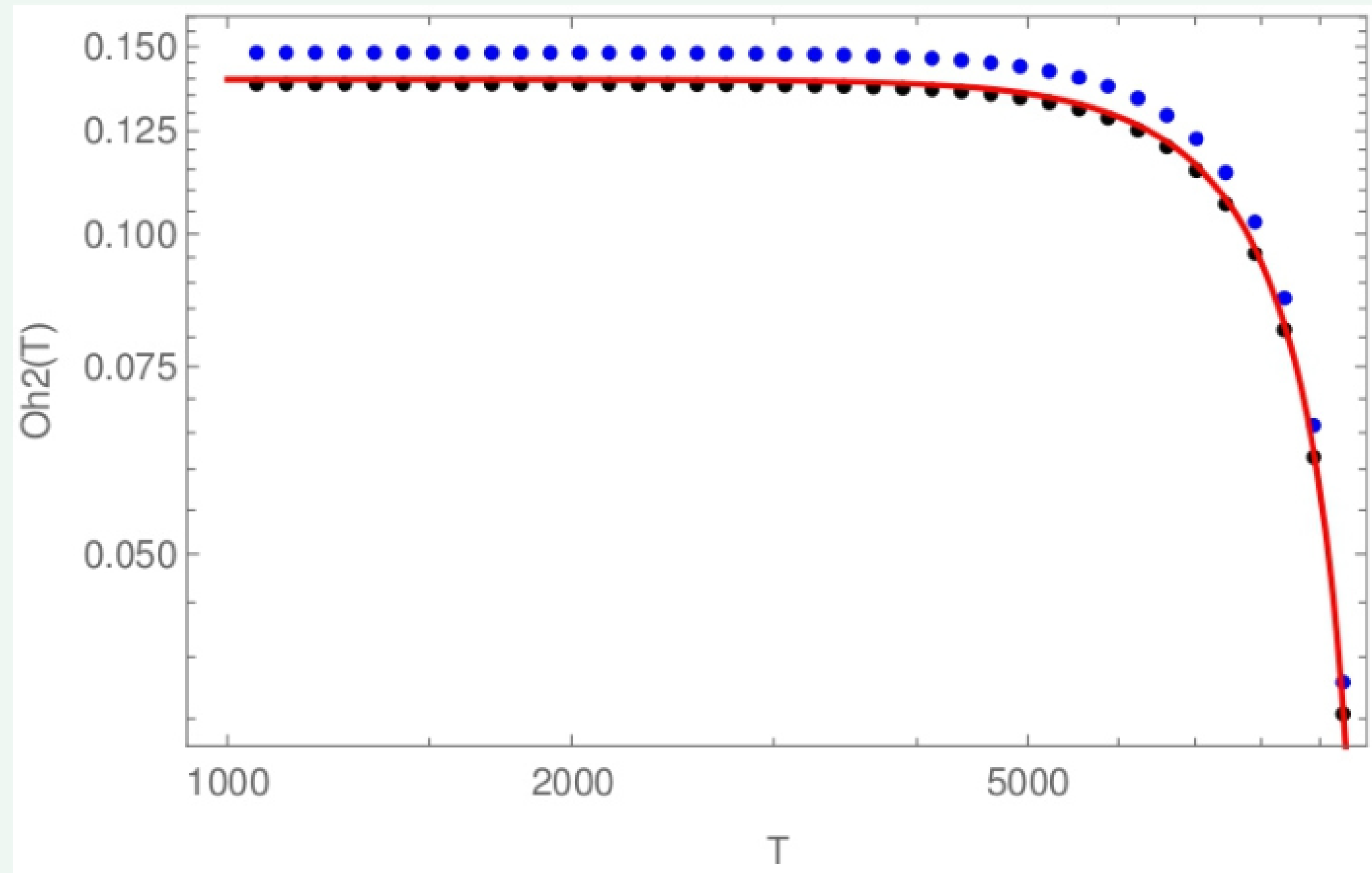
This project has received funding/support from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 860881-HIDDeN

BACK-UP

Non-instantaneous
reheating

$$m_\psi Y = 4 \times m_\psi Y_{inst}$$

Relativistic effect



BOLTZMANN SUPPRESSION

Scalar potential

$$V(s) = \frac{1}{2} \lambda_{hs} s^2 H^\dagger H + \frac{1}{2} m_s^2 s^2$$

Boltzmann equation

$$\dot{n} + 3Hn = \Gamma(h_i h_i \rightarrow ss) - \Gamma(ss \rightarrow h_i h_i)$$

Freeze-in rate

$$\Gamma(h_i h_i \rightarrow ss) = \langle \sigma(h_i h_i \rightarrow ss) v_r \rangle n_h^2 = \frac{2\pi^2 T}{(2\pi)^6} \int_{4m_s^2}^{\infty} d s \sigma(s - 4m_h^2) \sqrt{s} K_1(\sqrt{s}/T)$$

$$\Gamma(h_i h_i \rightarrow ss) \simeq \frac{\lambda_{hs}^2 T^3 m_s}{2^7 \pi^4} e^{-2m_s/T}$$

$$\lambda_{hs} \simeq 3 \times 10^{-11} e^{m_s/T_R} \sqrt{\frac{T_R}{m_s}}$$

$$m_H < m_s \quad \& \quad T_R < m_s$$