

Neutrino Portal to FIMP Dark Matter with an Early Matter Era

Catarina M. Cosme

in collaboration with
M. Dutra, T. Ma, Y. Wu, and L. Yang

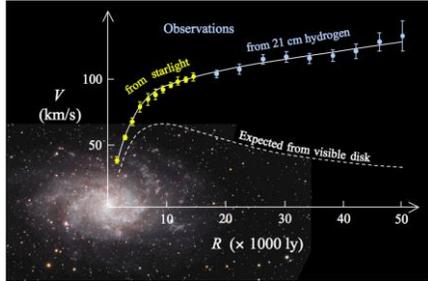
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TeV Particle Astrophysics, Archivio di Stato di Napoli, Italy, 12 September 2023

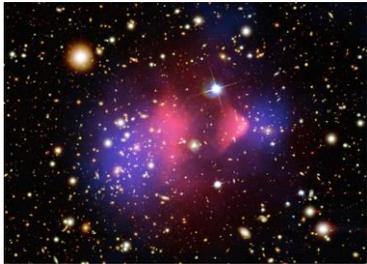


Introduction - Dark Matter (DM)

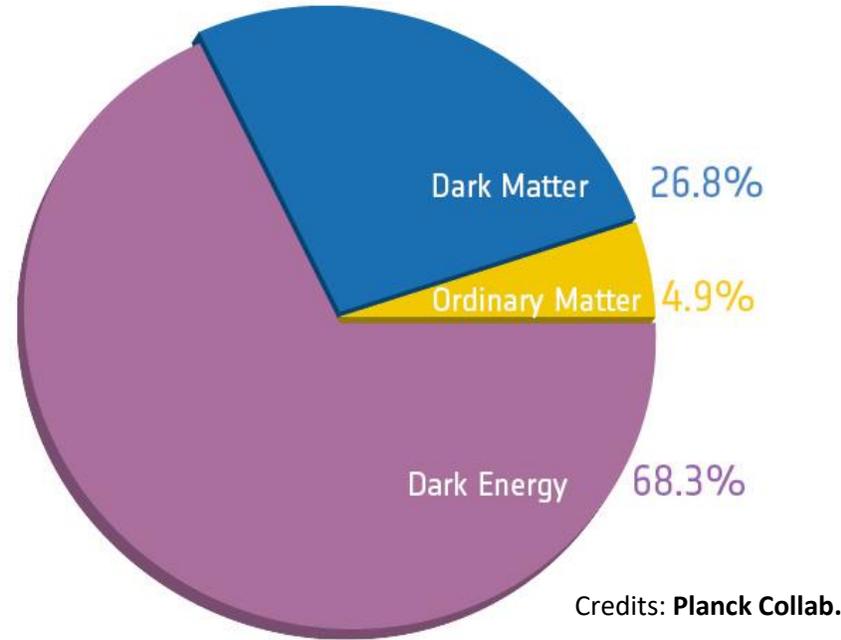
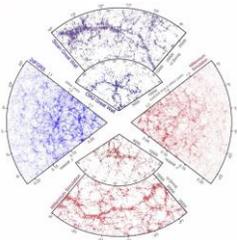
Galaxy Rotation Curves



Merging clusters (Bullet Cluster)



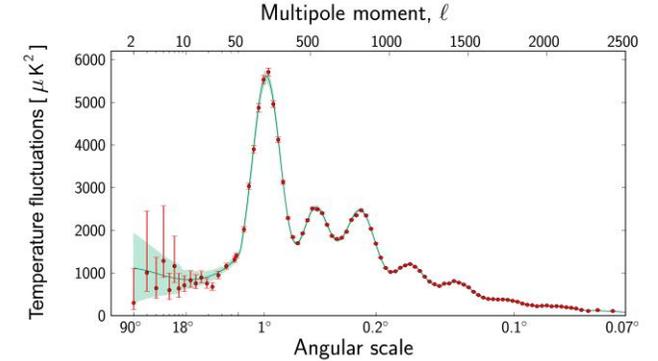
Structure formation



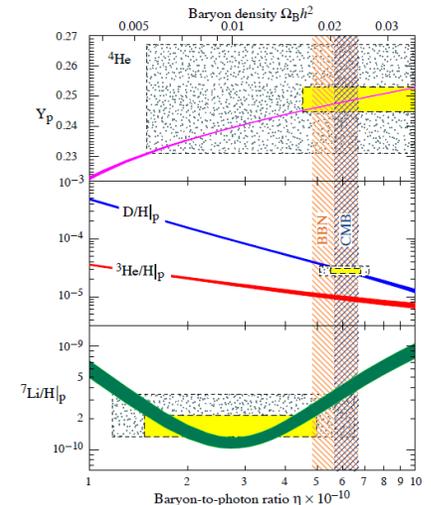
Properties of a DM candidate

- Stable or very long-lived (lifetime \geq age of the Universe);
- Cold (non-relativistic);
- Very small interaction with the electromagnetic field;
- It must have the observed abundance.

Cosmic Microwave Background (CMB)



Big Bang Nucleosynthesis (BBN)



Introduction - Dark Matter production mechanisms

Freeze-out

$$X\bar{X} \leftrightarrow SM$$

- Interactions **freeze-out** when: $\Gamma_X = n_X \langle \sigma v \rangle \lesssim H$;
- **WIMPs** – Weakly Interacting Massive Particles;
- $\Omega_{X,0} h^2 \sim \frac{1}{\lambda}$;
- But:
 - **no detection** so far;
 - Large parameter space **very constrained**
by experiments. [Arcadi et al. arXiv:1703.07364]

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vs

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$$\cancel{X\bar{X} \leftrightarrow SM}$$

Introduction - Dark Matter production mechanisms

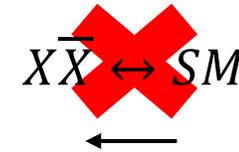
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Introduction - Dark Matter production mechanisms

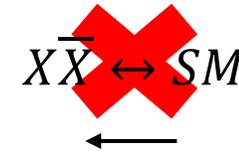
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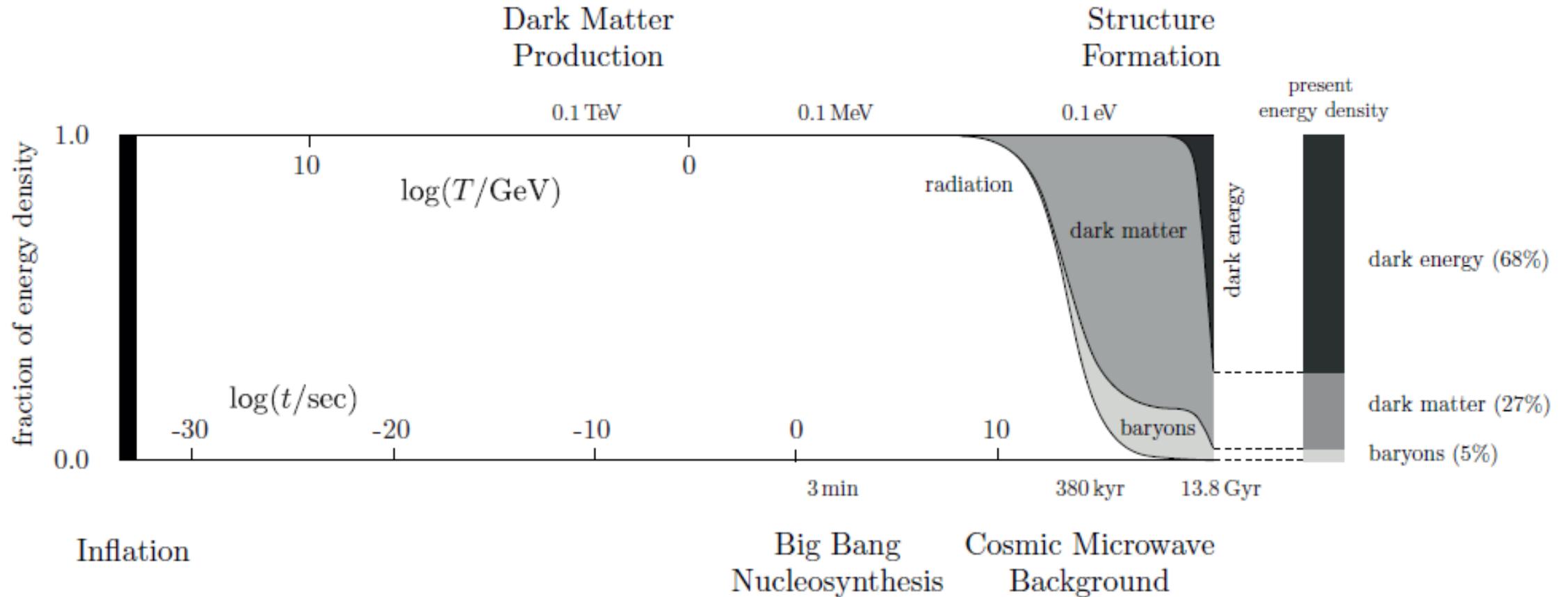
vs

Freeze-in



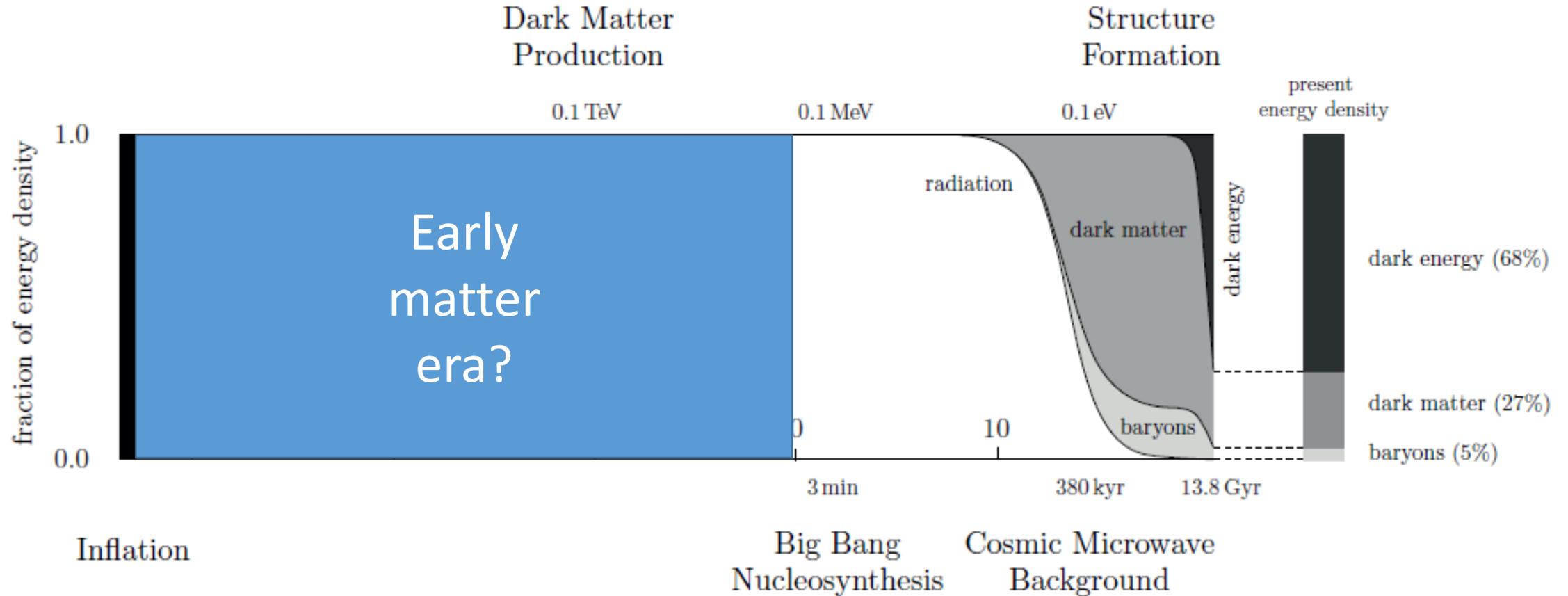
- $\Gamma_X < H$ **always**;
- **FIMPs** – Feebly Interacting Massive Particles;
- $\Omega_{X,0} h^2 \sim \lambda$;
- **Small couplings** to attain the **observed relic abundance**;
- Can evade stringent observational constraints;
- But: **hard to probe.**

Introduction – An early matter-dominated period



Credits: Daniel Baumann, *Cosmology, Part III Math Tripos*

Introduction – An early matter-dominated period



Introduction – An early matter-dominated period

Matter era: scalar field (inflaton candidates, meta-stable candidates, moduli fields...)

End of matter dominated period: **matter** component **decays** into Standard Model (SM) particles



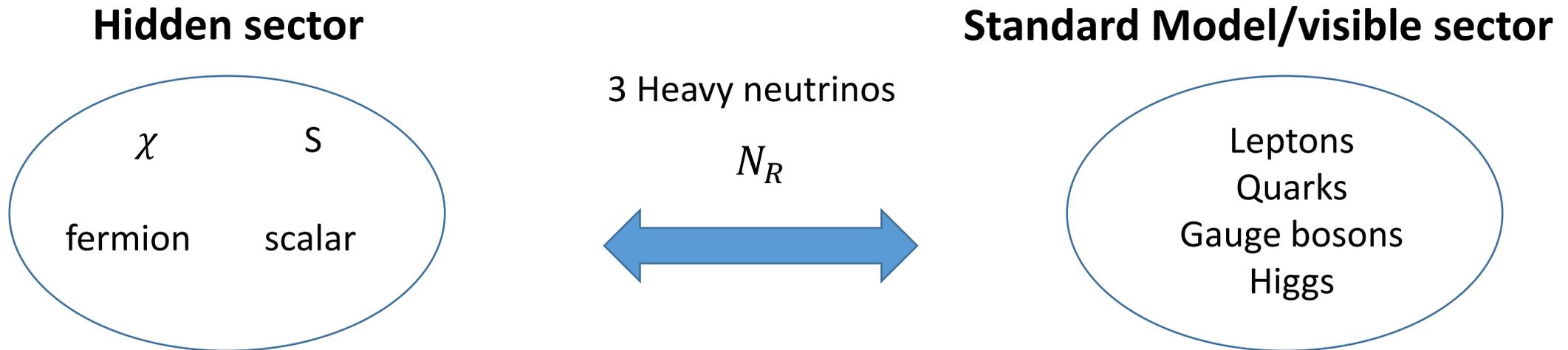
Dilution of **DM** number density



Freeze-in: **Couplings** to the visible sector **need to be larger** than usual freeze-in

DM production during a **non-standard expansion** may result to important
experimental and observational ramifications.

The model – Neutrino portal to FIMP Dark Matter with an early matter era



+ extra scalar for the early matter era

- SM neutrinos mass: **Type-I seesaw** mechanism;

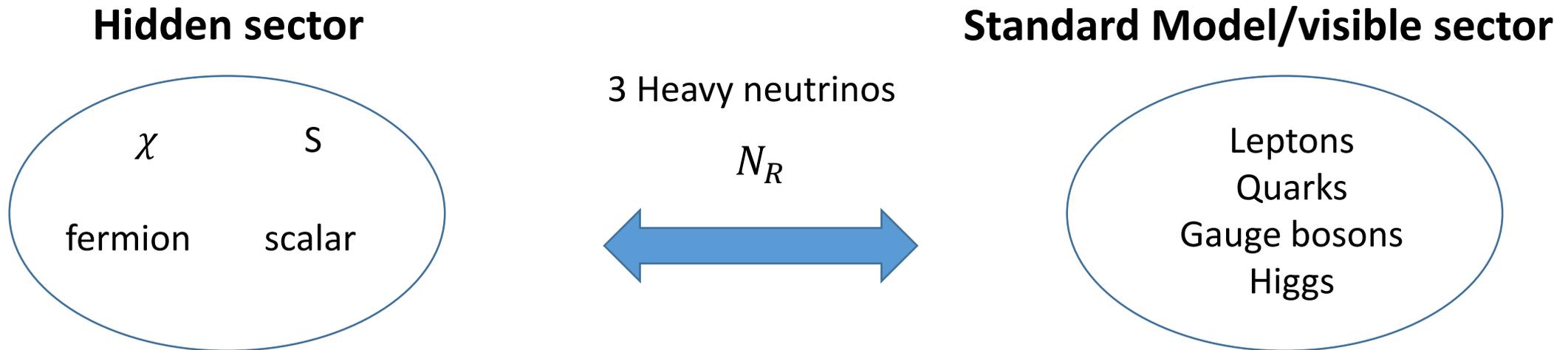
$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{hidden}} + \mathcal{L}_{\text{seesaw}} + \mathcal{L}_{\text{portal}}$$

$$\mathcal{L}_{\text{hidden}} = \bar{\chi}(i\partial - m_\chi)\chi + |\partial_\mu S|^2 - m_S^2 |S|^2 + V(S)$$

$$\mathcal{L}_{\text{portal}} = - \left(\lambda_\chi^i S \bar{\chi} (N_\ell^i)_R + h.c \right)$$

$$\mathcal{L}_{\text{seesaw}} = \frac{1}{2} \bar{N}_\ell^i (i\partial \delta^{ij} - m_N^{ij}) N_\ell^j - \left(\bar{L}_L^i Y_\nu^{ij} \tilde{H} (N_\ell^j)_R + h.c \right)$$

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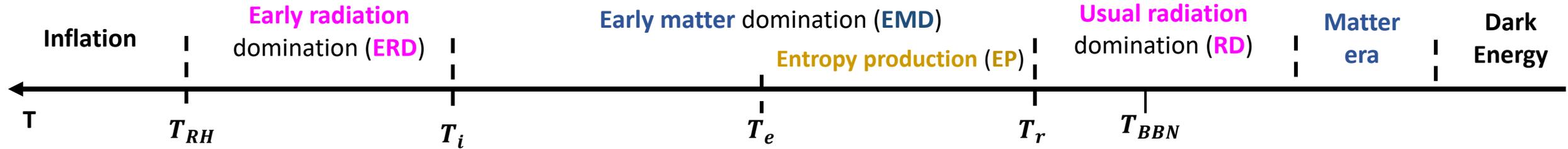
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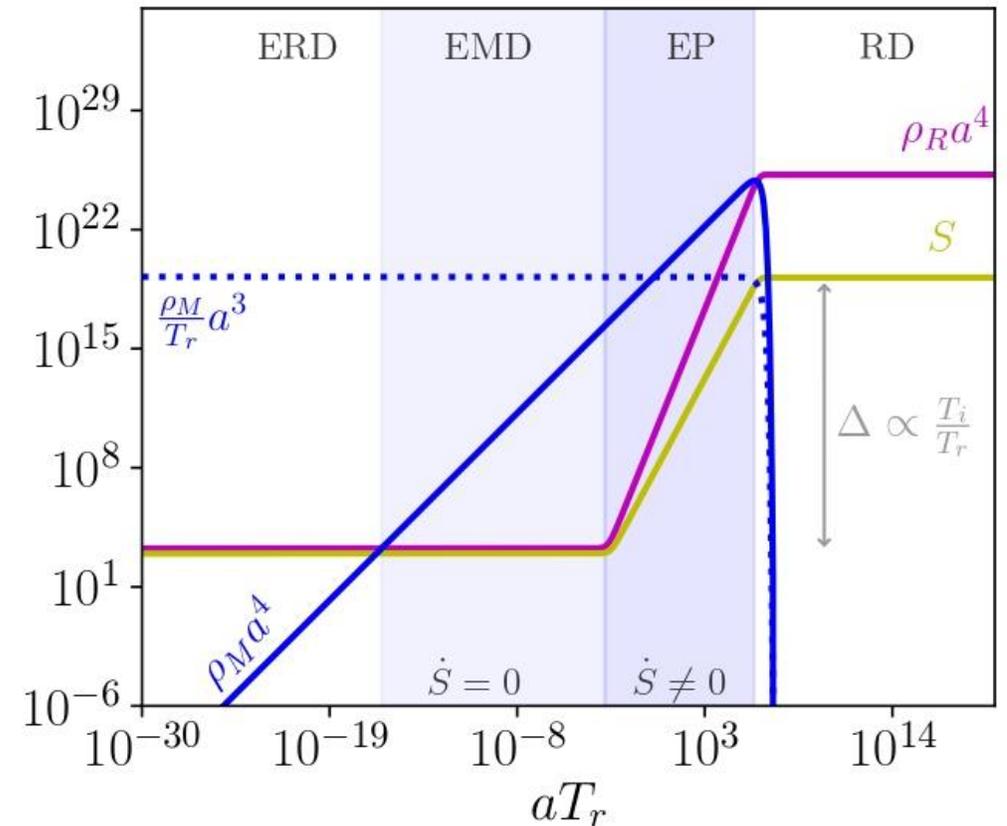
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Evolution of the Universe

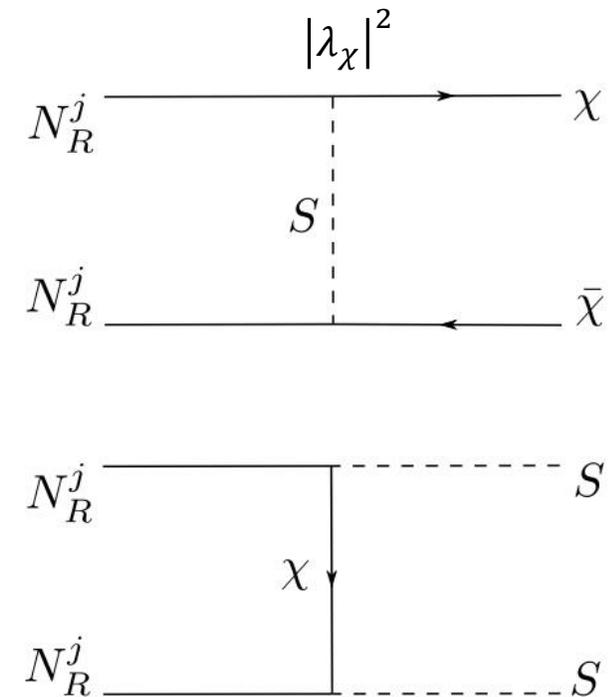
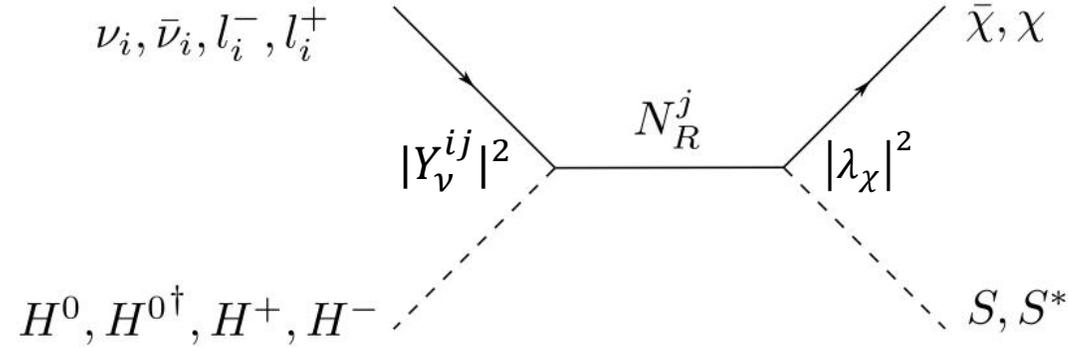
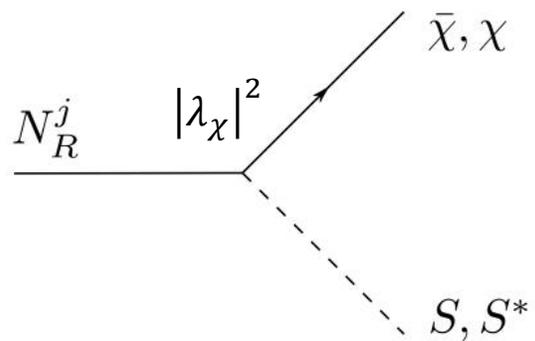


- $\rho_M \gg \rho_R, \rho_{DM}$ for some initial temperature T_i ;
- $H_{RD} = \frac{\pi}{\sqrt{90}} \sqrt{g_*} \frac{T^2}{M_{Pl}}$;
- $H_{EMD}(T) = H_{RD}(T_r) \sqrt{\Delta \frac{4g_s(T)}{3g_e(T_r)}} \left(\frac{T}{T_r}\right)^{\frac{3}{2}}$
 $\Delta \equiv$ Amount of **entropy production** during EMD;
 related with the duration of the EMD \Rightarrow **larger Δ** ,
longer EMD;
- $H_{EP}(T) = H_{RD}(T_r) \frac{g_e(T)}{g_e(T_r)} \left(\frac{T}{T_r}\right)^4$;



Dark matter production – Processes contributing to DM

Processes contributing to the Freeze-in production:



Dark matter production – Relic abundance

DM relic abundance

- DM production $\rightarrow \frac{n_{DM}}{s} \equiv Y_{DM}$ becomes constant;
- DM relic abundance:

$$\Omega_{DM,0} \equiv \frac{\rho_{DM,0}}{\rho_{c,0}} = \frac{m_{DM}}{3H_0^2 M_{Pl}^2} n_{DM} = \frac{m_{DM}}{3H_0^2 M_{Pl}^2} Y_{DM,0} s_0 \approx 0.26$$

$$Y_{DM,0} = Y_{ERD} + Y_{EMD} + Y_{EP} + Y_{RD}$$

- The yield Y_{DM} for some period is given by:

$$Y_{DM}(T_f) - Y_{DM}(T_i) = \int_{T_i}^{T_f} dT g_{*s} \frac{R_{DM}}{HTs}$$

Depends on the epoch

Has to take into account all the processes contributing to DM (depends on λ_χ, Y_ν^{ij})

$$R_2^{1 \rightarrow 23} \approx n_1 \Gamma_{1 \rightarrow 23}$$

$$R_3^{12 \rightarrow 34} \equiv n_1^{eq} n_2^{eq} \langle \sigma v \rangle_{12 \rightarrow 34}$$

Phenomenology – Indirect detection prospects

- **Indirect detection experiments:** Look for the product of the decay or annihilation of DM particles;
- In the case $m_{DM} > m_N$  **DM annihilates to N**  **N decays** into SM particles;
- Experiments like INTEGRAL/SPI, Fermi-LAT and H.E.S.S. place **stringent constraints** on the **dark matter annihilation cross-section** into **heavy neutrinos**.

Phenomenology – Indirect detection prospects

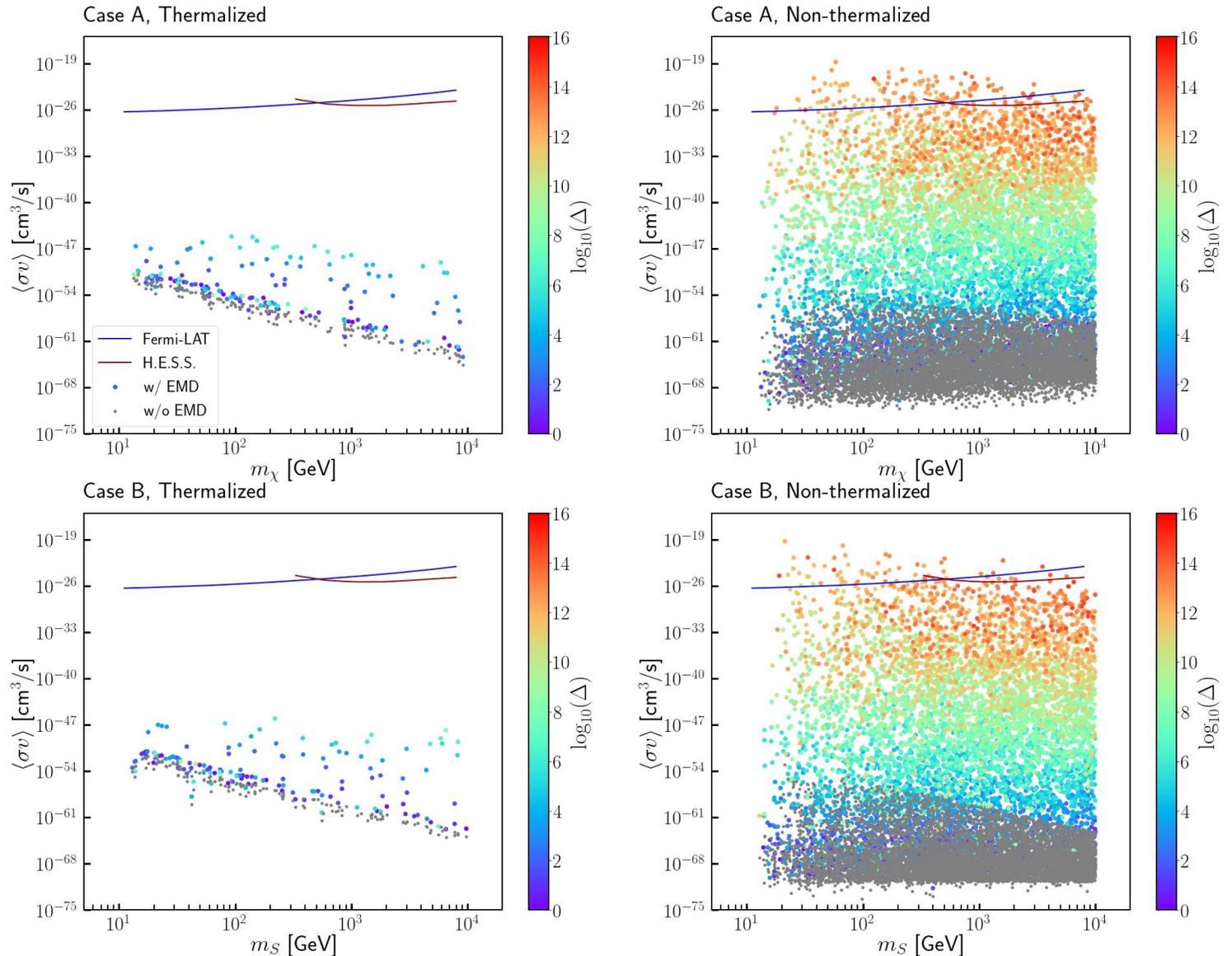
$$m_{DM} > m_N$$

Case A: χ is DM

Case B: S is DM

Parameters	Case A	Case B
m_χ	[1 GeV, 10^4 GeV]	[m_S , 10^6 GeV]
m_S	[m_χ , 10^6 GeV]	[1 GeV, 10^4 GeV]
m_N	[10 GeV, 10^6 GeV]	
T_i	[10^2 GeV, 5×10^{14} GeV]	
T_r	[4 MeV, T_i]	

$\langle\sigma v\rangle_{DM DM \rightarrow NN}$ bounds from [Campos et al. arXiv:1702.06145]



Conclusions

- We have studied the **DM neutrino portal via freeze-in in an early matter-era**;
- Discussed the **dynamics** of the Universe and DM throughout the **modified cosmic history**;
- Evaluated the **relevant constraints** of the model;
- If the **freeze-in** happens **during** an **early-matter** dominated epoch \Rightarrow **larger couplings** to SM;
- **Indirect detection: early-matter era enhances cross sections** relevant for indirect detection, can be **tested** with **current** experiments.

Thank you for your attention! / Grazie per l'attenzione!

Backup slides

Parameter Space

Parameters	Case A	Case B
m_χ	[1 GeV, 10^4 GeV]	$[m_S, 10^6$ GeV]
m_S	$[m_\chi, 10^6$ GeV]	[1 GeV, 10^4 GeV]
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T_r	[4 MeV, T_i]	

Table 1. The scan ranges for each input parameter in all cases. Note that Y_ν^{ij} is fully determined by m_N and $R = \mathbb{I}$, and λ_χ is chosen to give the observed dark matter relic density and is required to be less than 4π .

Parameter Space

in the interaction matrix Y_ν^{ij} , which is parameterized in the Casas-Ibarra scheme [64]:

$$Y_\nu = \frac{i\sqrt{2}}{v} U_{\text{PMNS}} m_\nu^{1/2} R m_N^{1/2}, \quad (2.6)$$

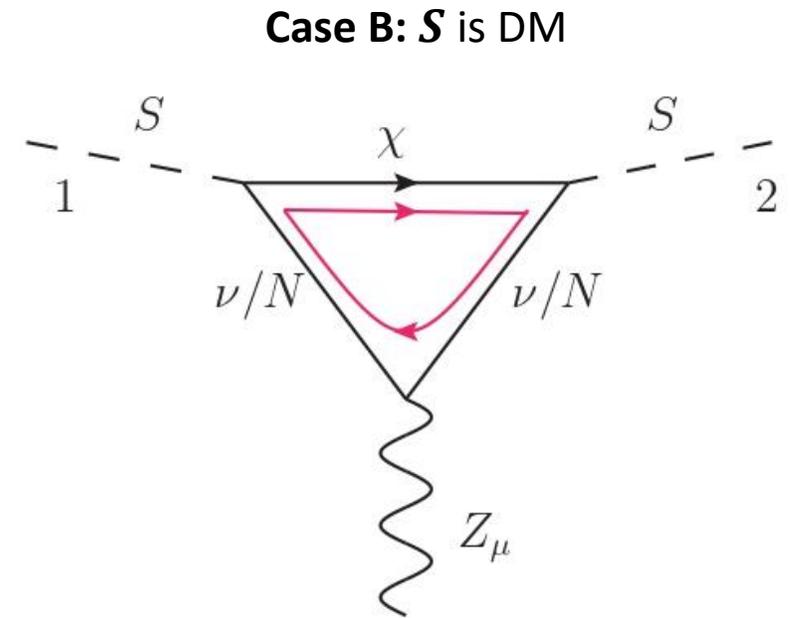
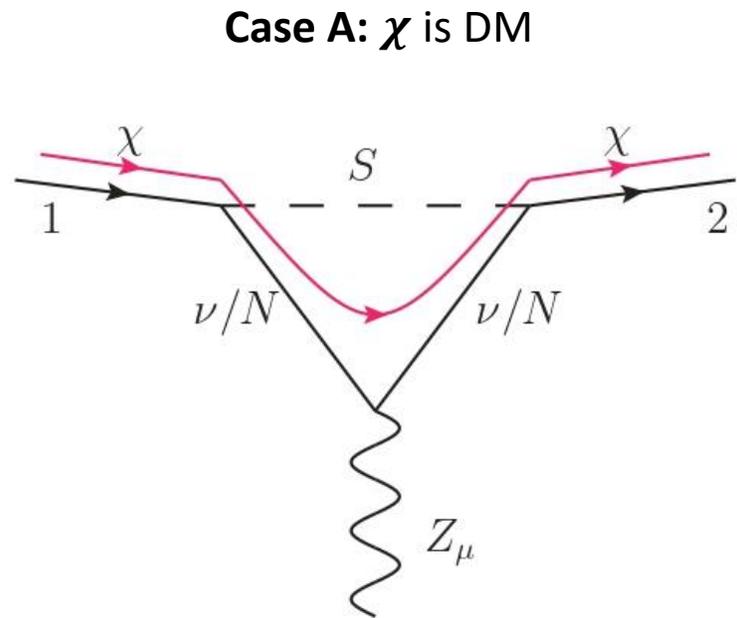
where U_{PMNS} is the PMNS matrix containing three mixing angles $(\theta_{12}, \theta_{23}, \theta_{13})$ and three phases $(\delta_{\text{CP}}, \alpha_1, \alpha_2)$ and is parametrized as

$$U_{\text{PMNS}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \cdot \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{\text{CP}}} & 0 & c_{13} \end{pmatrix} \cdot \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \cdot \mathcal{P} \quad (2.7)$$

where $c_{ij} \equiv \cos \theta_{ij}$ and $s_{ij} \equiv \sin \theta_{ij}$, and $\mathcal{P} = \text{diag}(e^{i\alpha_1}, e^{i\alpha_2}, 1)$. The value of these angles and phases are taken from the recent global fitting results [65]¹. $m_{\nu/N}^{1/2}$ represent the diagonal matrices with square root of the eigen-masses ($\sqrt{m_{\nu/N}^i}$) in the diagonal entries and R is an extra complex orthogonal matrix ($R^T R = \mathbb{I}$) parameterized by three complex angles.

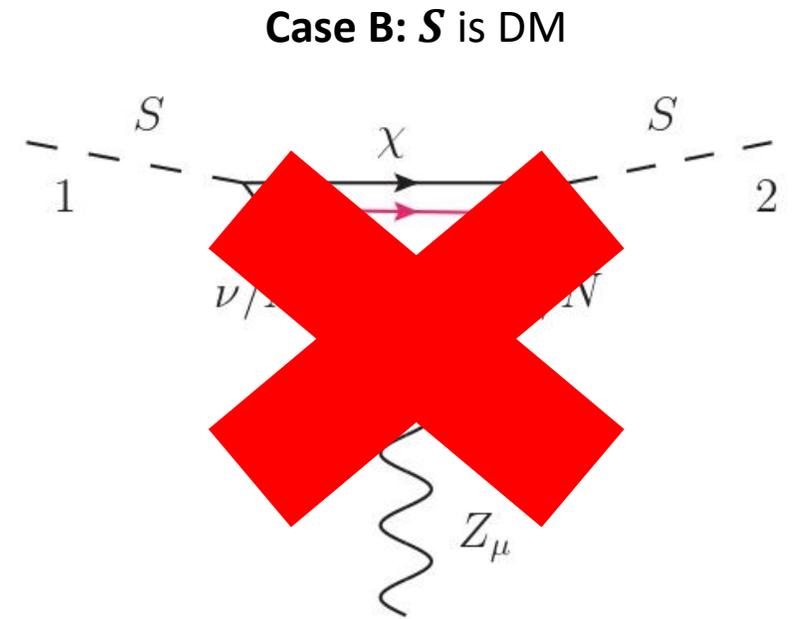
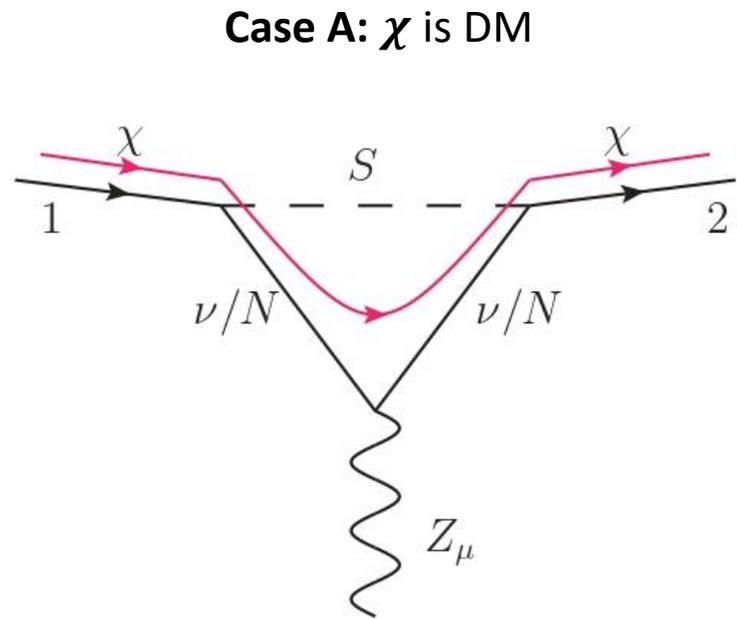
Phenomenology – Direct detection prospects

- **Direct detection experiments:** Scattering of DM with atomic nuclei in detectors; identify the deposited energies;
- Direct detection relevant vertices:



Phenomenology – Direct detection prospects

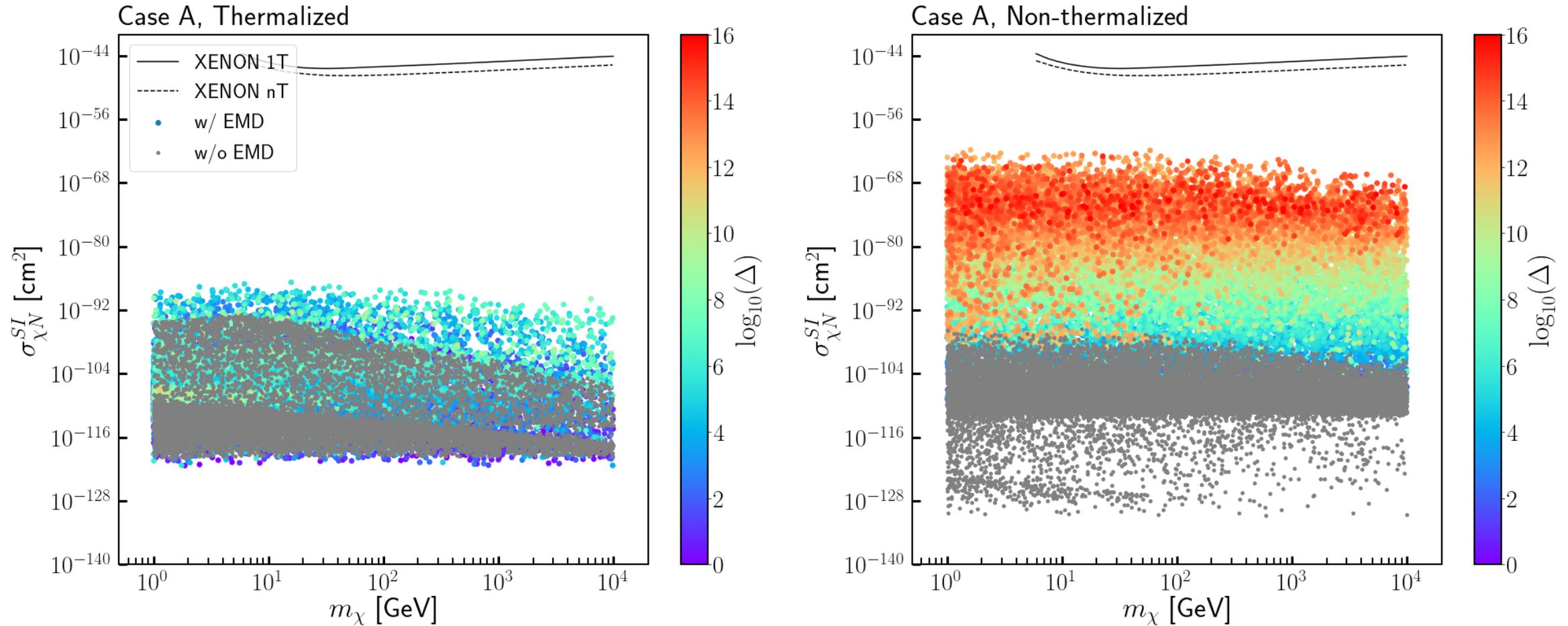
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Very suppressed – not consider this case for direct detection

Phenomenology – Direct detection prospects

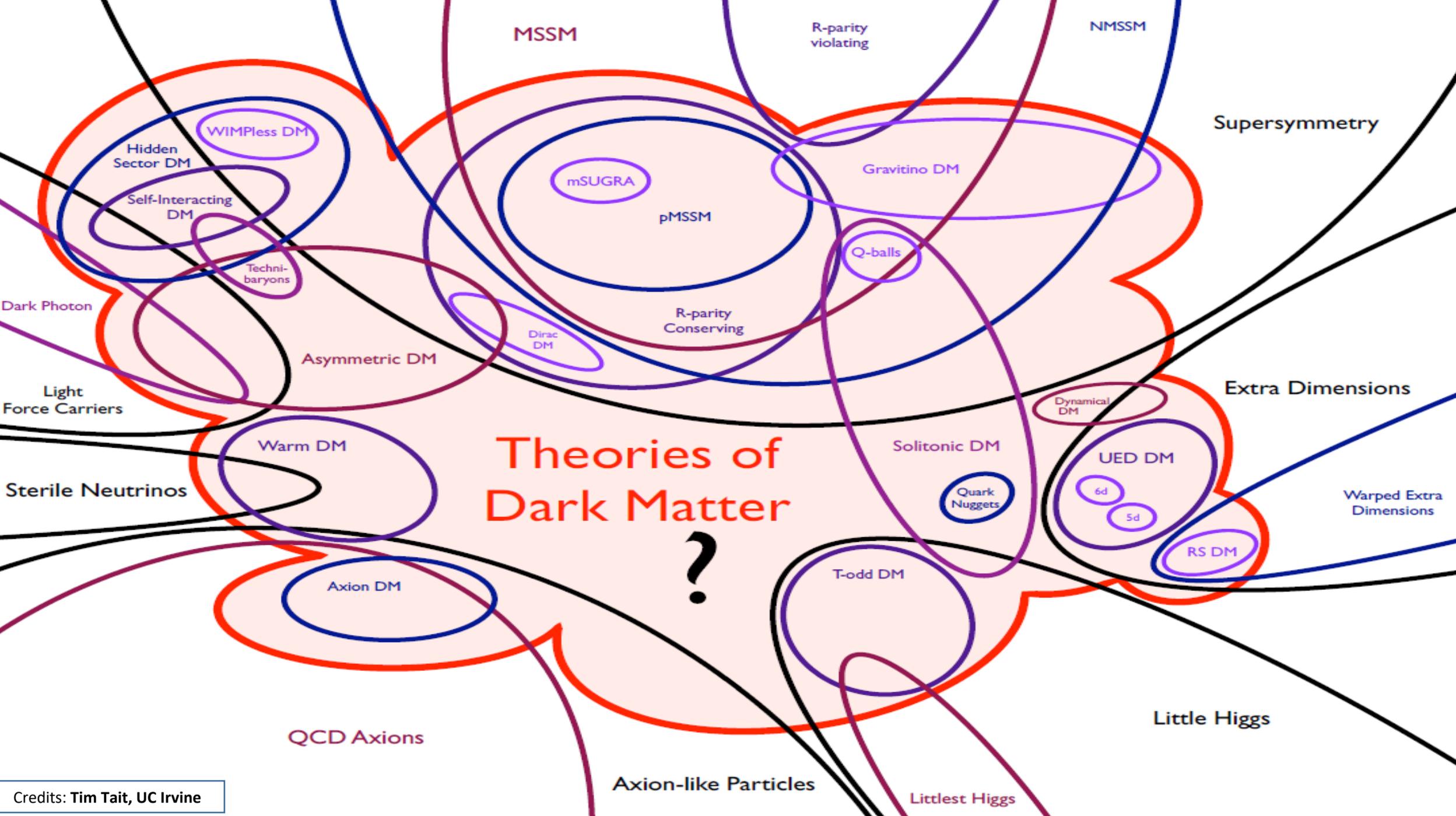
Direct detection experiments: Scattering of DM with atomic nuclei in detectors;



$\sigma_{\chi N}^{SI}$ - Spin Independent DM-nucleon scattering cross section

Case A: χ is DM

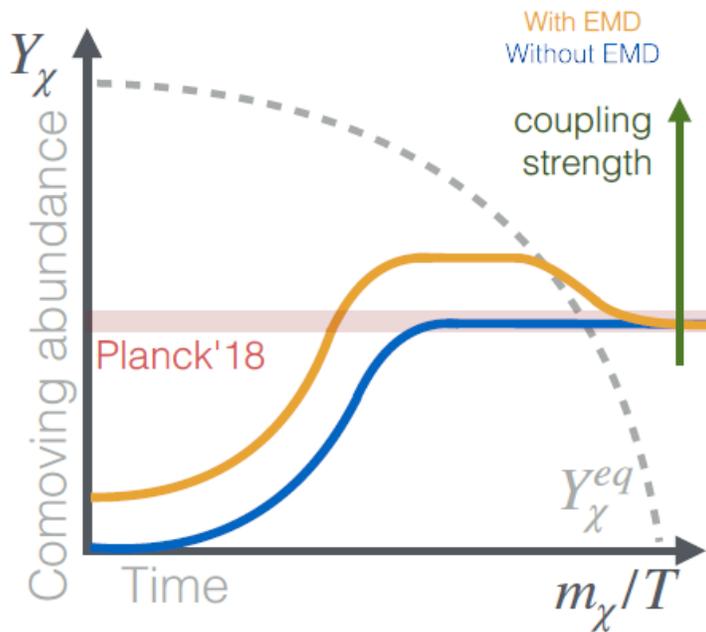
Theories of Dark Matter



Introduction – An early matter-dominated period

Matter era: scalar field (inflaton candidates, meta-stable candidates, moduli fields...)

End of matter dominated period: **matter** component **decays** into Standard Model (SM) particles;



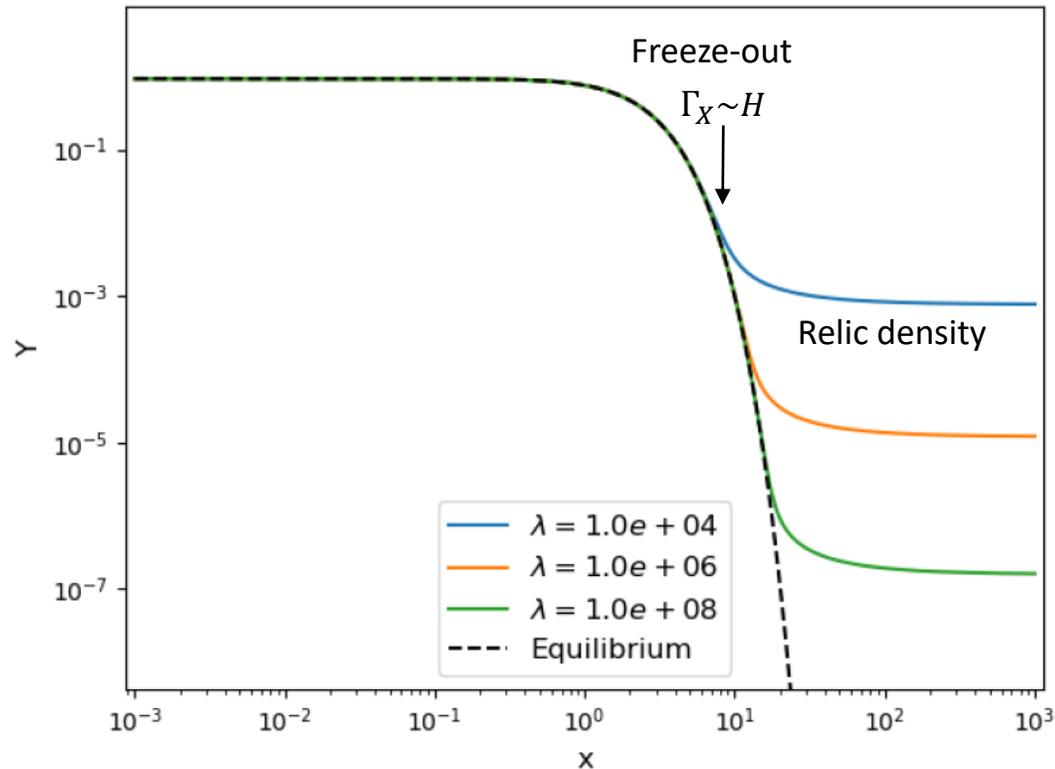
Dilution of DM number density

Freeze-in: **Couplings** to the visible sector **need to be larger** than usual freeze-in

DM production during a non-standard expansion may result to important **experimental and observational** ramifications.

Introduction - Dark Matter production mechanisms

Freeze-out mechanism (Weakly Interacting Massive Particles – WIMPs)



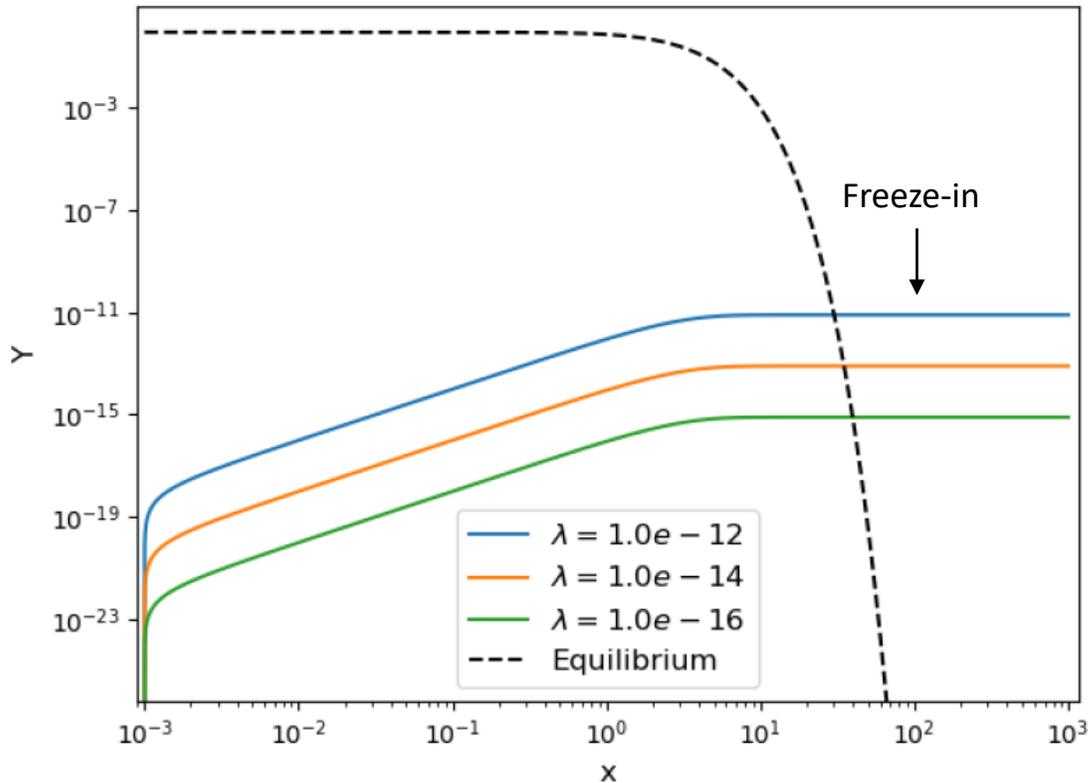
$$Y \equiv \frac{n_X}{s}, \quad x \equiv \frac{m}{T}$$

$$X\bar{X} \leftrightarrow SM$$

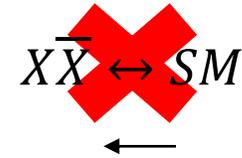
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Introduction - Dark Matter production mechanisms

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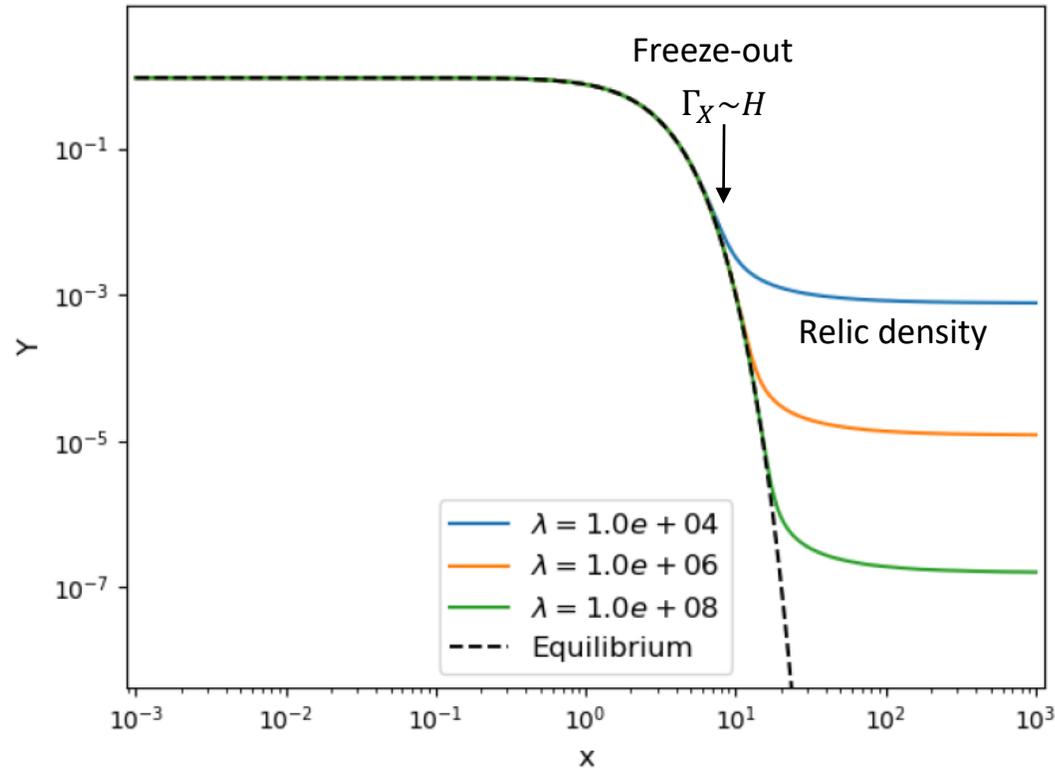
$$Y \equiv \frac{n_X}{s}, \quad x \equiv \frac{m}{T}$$



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- **Small couplings** to attain the **observed relic abundance**;
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Introduction - Dark Matter production mechanisms

Freeze-out mechanism (Weakly Interacting Massive Particles – WIMPs)



Credits: Taylor Gray, Carleton U.

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Dark Matter (DM) **evolution**:

$$\frac{dn_X}{dt} + 3Hn_X = -\langle\sigma v\rangle \left(n_X^2 - (n_X^{eq})^2 \right)$$

Interactions **freeze-out** when:

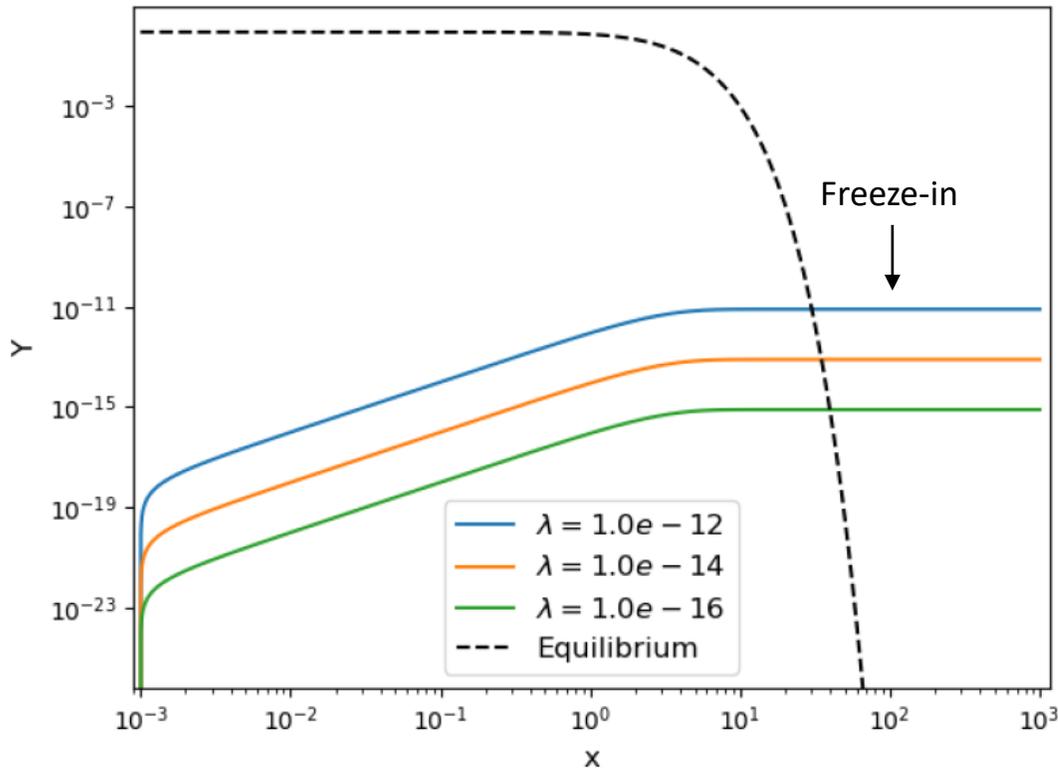
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Present DM **abundance**:

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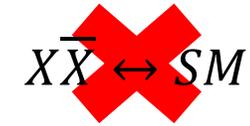
Introduction - Dark Matter production mechanisms

Freeze-in mechanism - Feebly Interacting Massive Particles (FIMPs)



Credits: Taylor Gray, Carleton U.

$$Y \equiv \frac{n_X}{s}, \quad x \equiv \frac{m}{T}$$



DM evolution:

$$\frac{dn_X}{dt} + 3Hn_X = 2\Gamma_{\sigma \rightarrow XX} \frac{K_1(m_\sigma/T)}{K_2(m_\sigma/T)} n_\sigma^{eq}$$

Interactions rate:

$$\Gamma_X < H \text{ always}$$

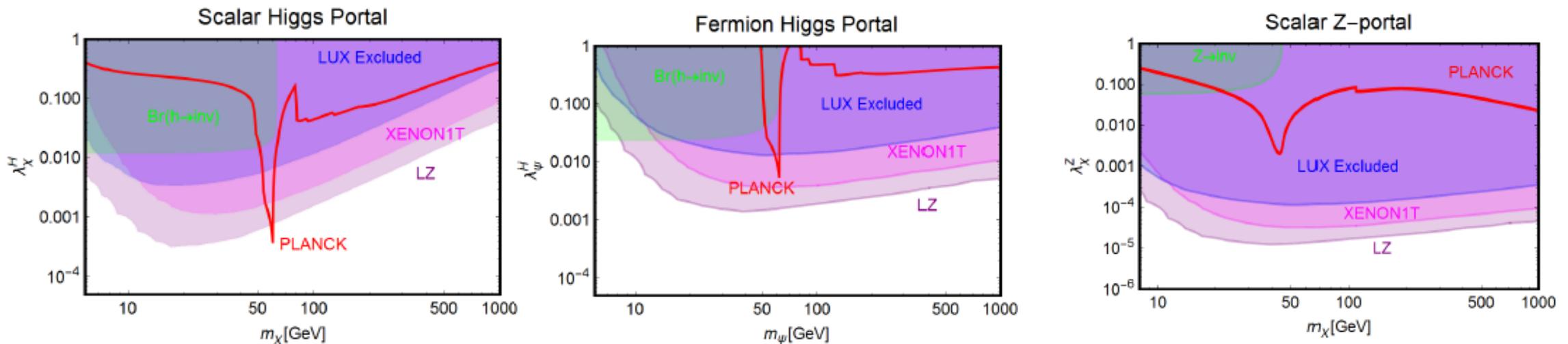
Present DM abundance:

$$\Omega_X h^2 \sim \Gamma_{\sigma \rightarrow XX} \sim \lambda$$

Introduction - Dark Matter production mechanisms

Freeze-out mechanism

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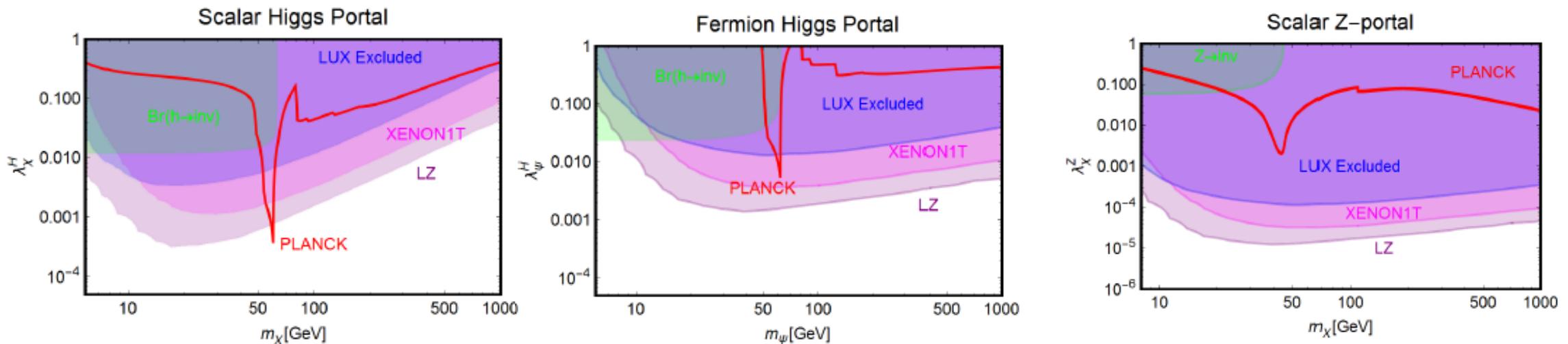


Credits: Arcadi et. al, arXiv:1703.07364

Introduction - Dark Matter production mechanisms

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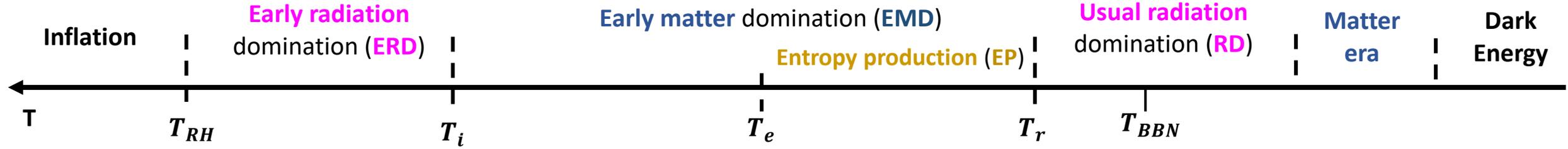
Credits: Arcadi et. al, arXiv:1703.07364

“The waning of the WIMP?”

The model – Neutrino portal to FIMP Dark Matter with an early matter era

- **Why** neutrino portal? Neutrinos are another intriguing piece of the cosmic puzzle;
- **Freeze-in** + **Non-standard cosmologies** + **Higgs portal**: Bernal, **CC**, Tenkanen arXiv: 1803.08064; Bernal, **CC**, Tenkanen, Vaskonen arXiv: 1806.11122; Hardy arXiv: 1804.06783;
- **Freeze-out** + **Neutrino portal**: Blennow et al, arXiv: 1903.00006;
- **Freeze-out** + **Non-standard cosmologies** (including **early-matter era**): Drees, F. Hajkarim arXiv:1711.05007; D’Eramo, Fernandez, and Profumo arXiv: 1703.04793; Hamdan and Unwin arXiv: 1710.03758;
- **Freeze-in** + **Neutrino portal**: Becker arXiv: 1806.08579; Chianese, King arXiv: 1806.10606; Chianese, Fu, King arXiv: 1910.12916;
- **Freeze-in** + **Early-matter era** + **Neutrino portal**: this work.

Evolution of the Universe

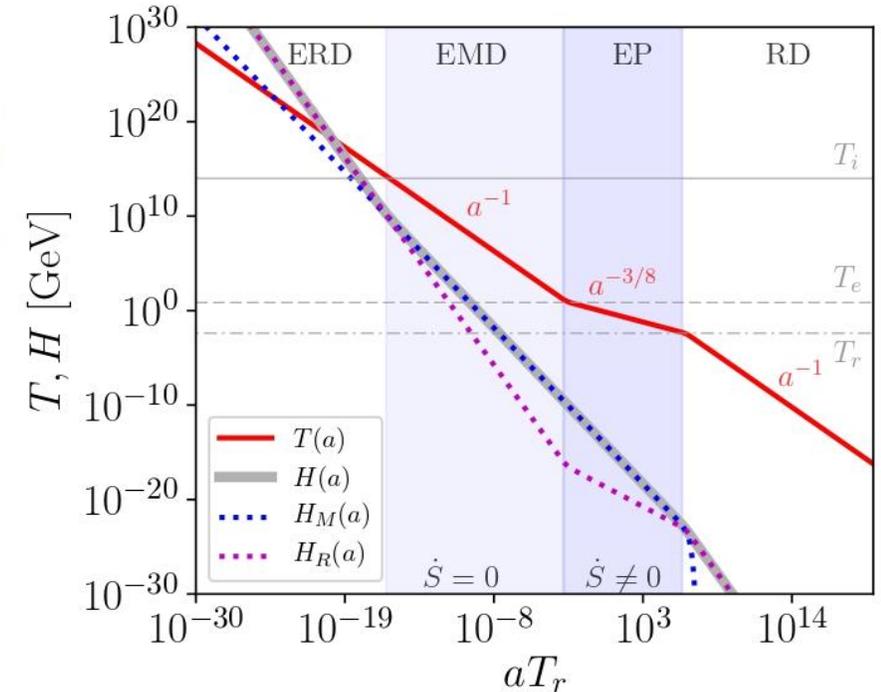
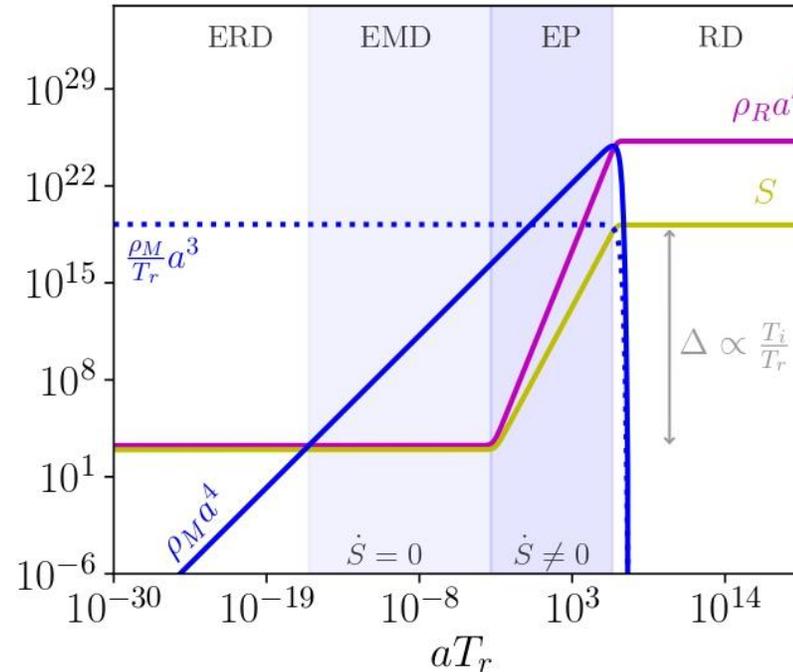


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- $H_{RD} = \frac{\pi}{\sqrt{90}} \sqrt{g_*} \frac{T^2}{M_{Pl}}$;

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- $H_{EP}(T) = H_{RD}(T_r) \frac{g_e(T)}{g_e(T_r)} \left(\frac{T}{T_r}\right)^4$;



$\Delta \sim \frac{T_i}{T_r} \equiv$ Amount of **entropy production** during EMD; related with the **duration of the EMD** \Rightarrow larger Δ , longer EMD

Evolution of the Universe

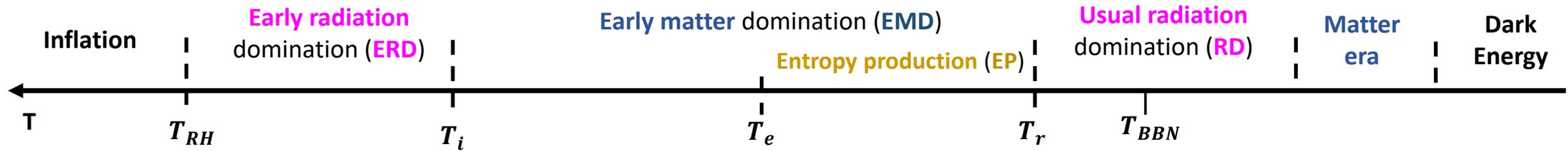
$$\rho_M \gg \rho_R, \rho_{DM} \text{ for some initial temperature } T_i$$

- Hubble parameter: $H(t) = \sqrt{\rho_{tot}}/(\sqrt{3}M_P)$, with $\rho_{tot}(t) = \rho_R(t) + \rho_M(t)$;
- Solve:

$$\begin{cases} \dot{\rho}_M + 3H(t)\rho_M = -\rho_M\Gamma_M \\ \dot{\rho}_R + 4H(t)\rho_R = B_R\rho_M\Gamma_M \end{cases}$$

- The thermal history of the Universe has **4** important **periods**:
 - **Early radiation** domination (ERD);
 - **Early matter** domination (EMD);
 - **Entropy production** (EP);
 - **Usual radiation** domination (RD);

Evolution of the Universe



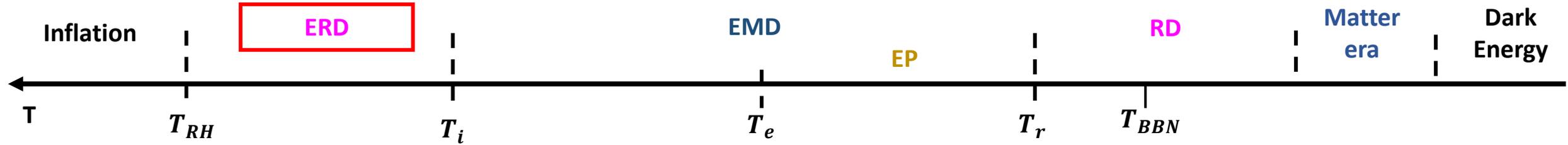
T_{RH} - Inflationary reheating temperature;

T_i - Beginning of the early matter-era;

T_e - End of the isentropic early matter-era \Rightarrow entropy production starts;

T_r - Decay of the matter component; usual radiation takes place; $T_r \gtrsim T_{BBN} \sim 4 \text{ MeV}$

Evolution of the Universe



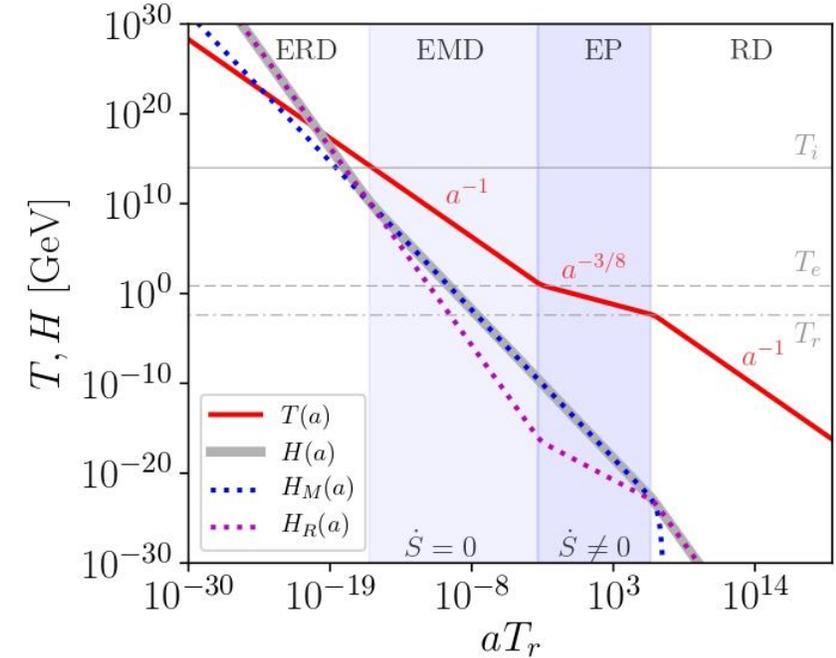
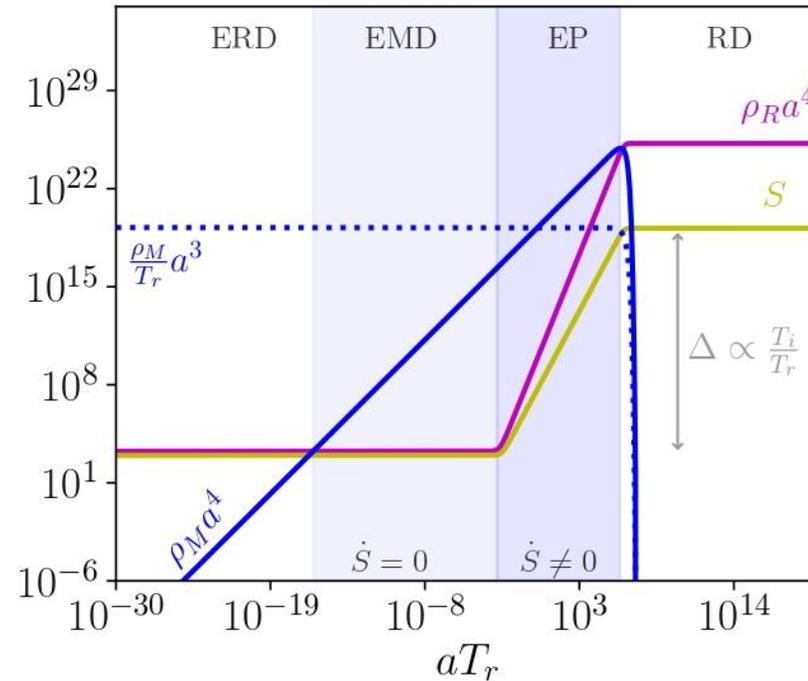
ERD:

- M is not dominant yet;**

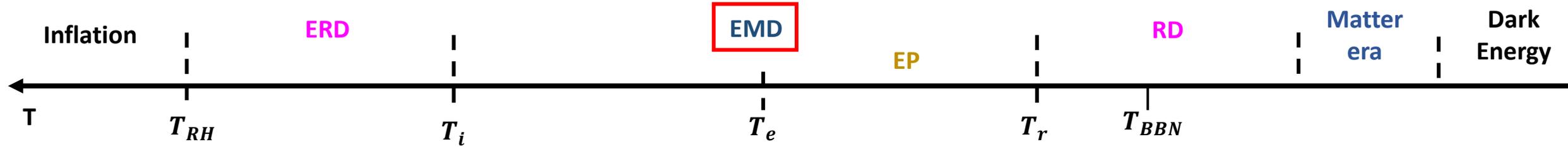
$$H_{RD} = \frac{\pi}{\sqrt{90}} \sqrt{g_*} \frac{T^2}{M_{Pl}}$$

- Continuity of $H(T)$:**

$$H_{RD}(T_i) = H_{EMD}(T_i)$$



Evolution of the Universe

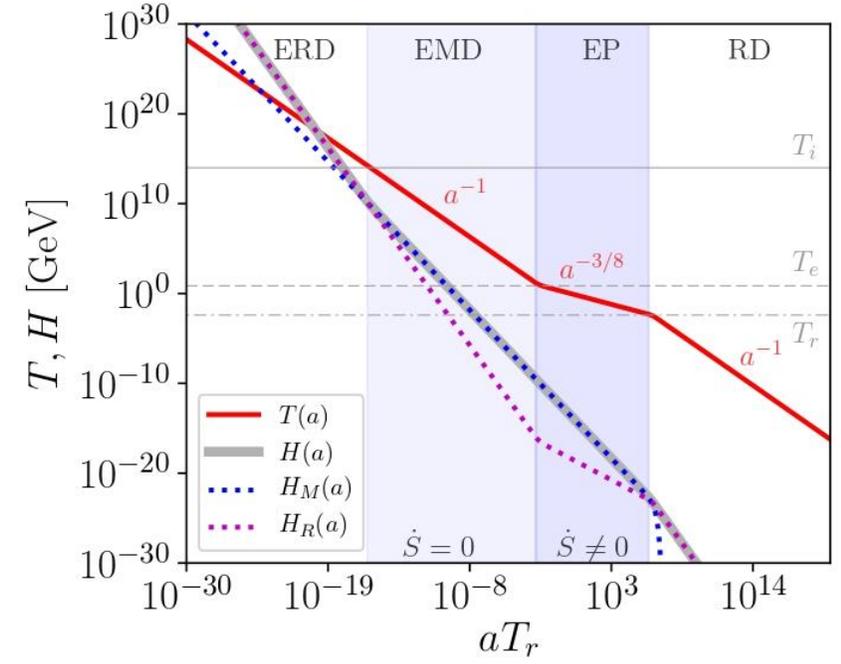
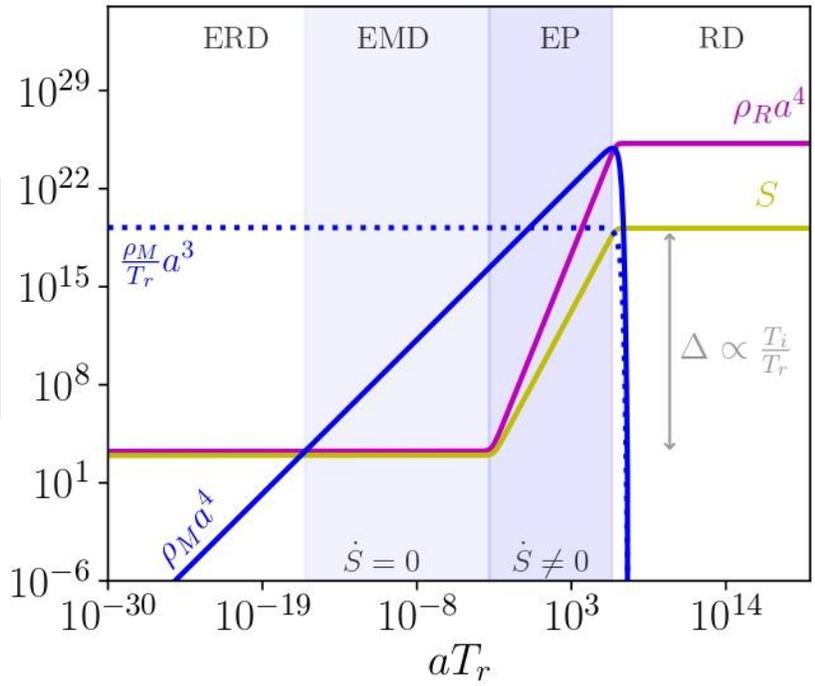


EMD:

- Until T_e , entropy s is **constant**.

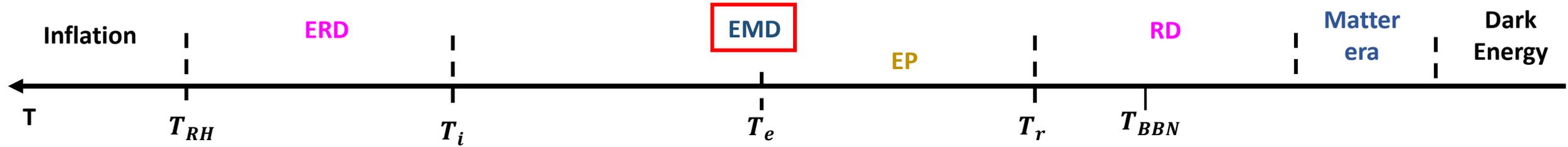
$$H_{EMD}(T) = H_{RD}(T_r) \sqrt{\Delta \frac{4g_s(T)}{3g_e(T_r)} \left(\frac{T}{T_r}\right)^{\frac{3}{2}}}$$

- $T > T_r$: $H_{EMD}(T) > H_{RD}(T) \Rightarrow$ **Faster** expansion of the Universe.



$\Delta \equiv$ Amount of **entropy production** during EMD; related with the duration of the EMD \Rightarrow **larger Δ , longer EMD**;

Evolution of the Universe



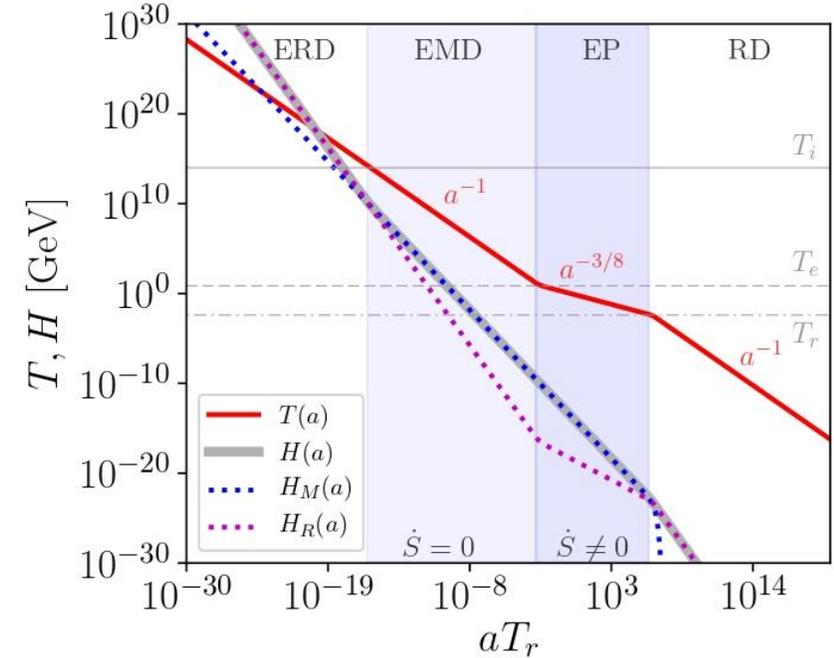
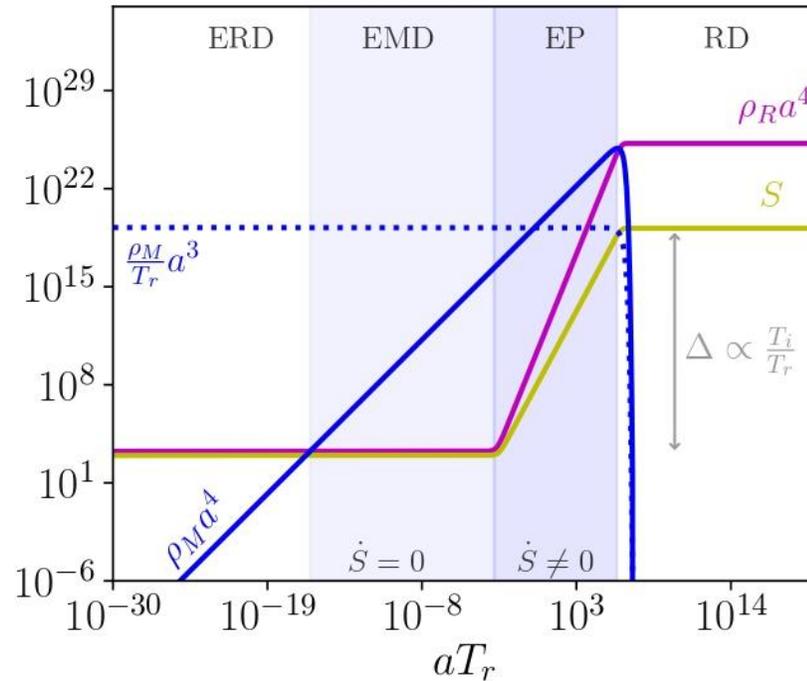
EMD:

$$\Delta = \frac{3 g_e(T_i) T_i}{4 g_s(T_i) T_r}$$

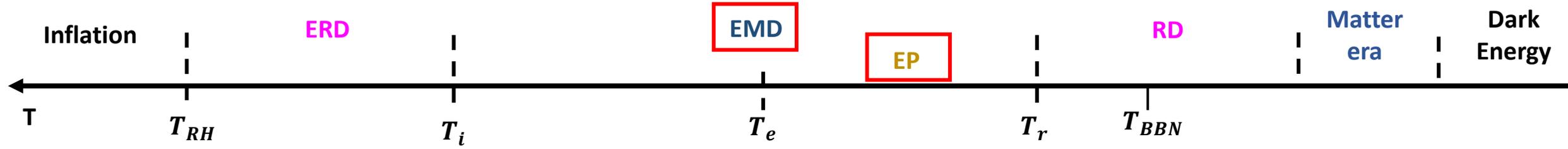
$$\frac{T_e}{T_r} = \left(\Delta \frac{4 g_s(T_e) g_e(T_r)}{3 g_e^2(T_e)} \right)^{\frac{1}{5}}$$



- T_e is fixed by T_i and T_r ;
- T_i and T_r parametrize the early matter era.



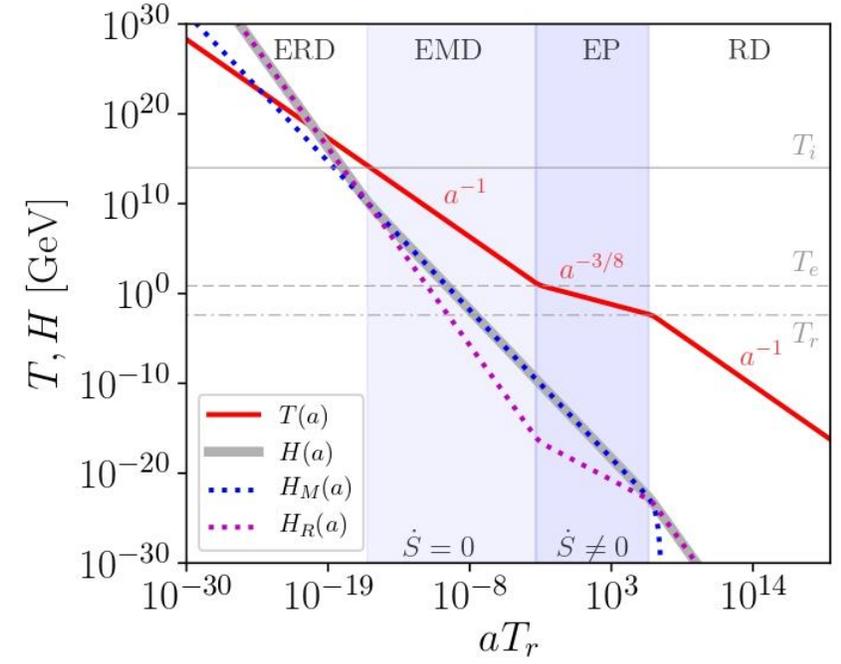
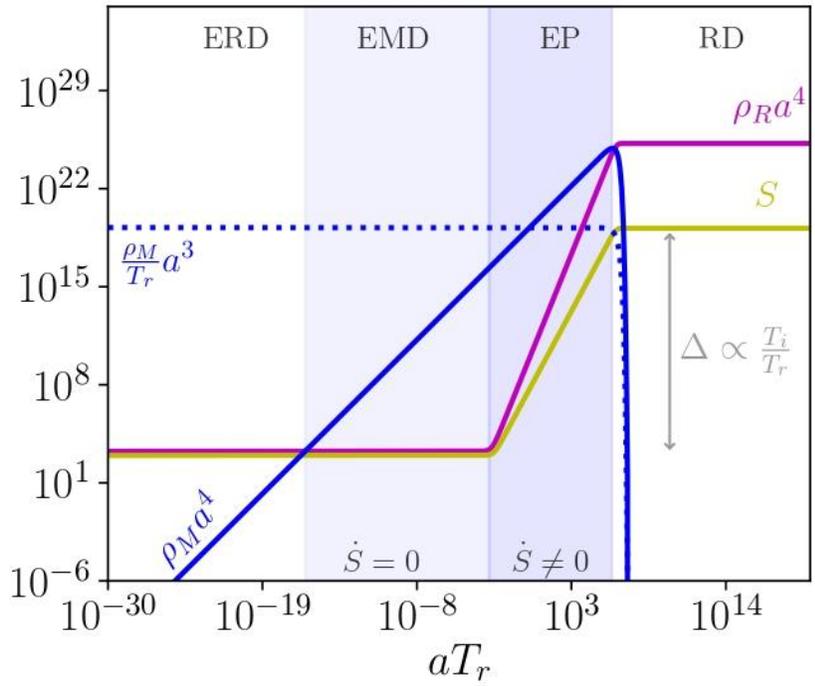
Evolution of the Universe



EP:

- **M decays** (not instantaneously) only into the visible sector \Rightarrow **DM dilution**;
- Entropy is not conserved: Entropy production $\Rightarrow T \sim a^{-3/8}$

$$H_{EP}(T) = H_{RD}(T_r) \frac{g_e(T)}{g_e(T_r)} \left(\frac{T}{T_r} \right)^4$$



Dark matter production - Constraints

Freeze-in conditions: $\Gamma_{decays}, \Gamma_{s-channels}, \Gamma_{t-channels} \ll H(T)$

Can we have the feeling of **how the early matter era is affecting our model?**

- Case: $\frac{\Gamma_{NR \rightarrow \bar{\chi} S}}{H(T)} \ll 1$

Recall: $\Delta \sim \frac{T_i}{T_r}$

$$\lambda_\chi \ll \left(\frac{10^3 \text{ GeV}}{m_N} \right)^{\frac{1}{2}} \left(\frac{g_e(100 \text{ GeV})}{103.5} \right)^{\frac{1}{4}} \frac{0.01}{(1 - \epsilon^2)} \times \begin{cases} 2.5 \times 10^{-8} \frac{T}{100 \text{ GeV}}, & \text{for } \Delta = 1 \\ 1.5 \times 10^{-4} \left(\frac{T}{100 \text{ GeV}} \right)^{\frac{3}{4}} \left(\frac{T_r}{4 \text{ MeV}} \right)^{\frac{1}{4}} \left(\frac{\Delta}{2 \times 10^{16}} \right)^{\frac{1}{4}}, & \text{for } \Delta = 2 \times 10^{16} \end{cases}$$

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Longer EMD allows out-of-equilibrium processes with **larger couplings**

Heavy neutrinos thermalization

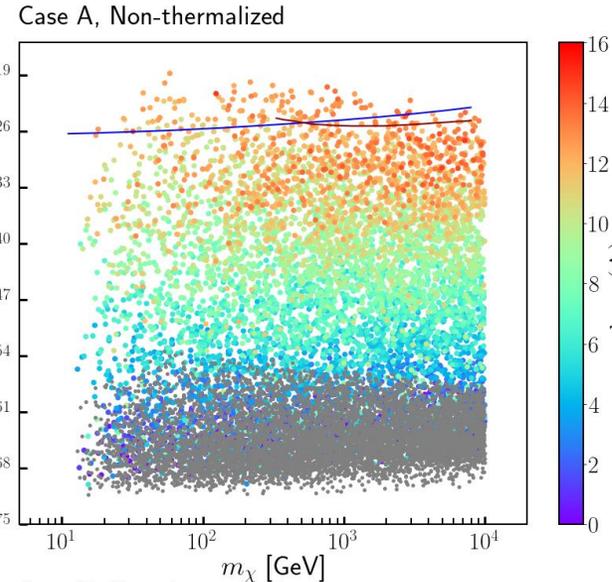
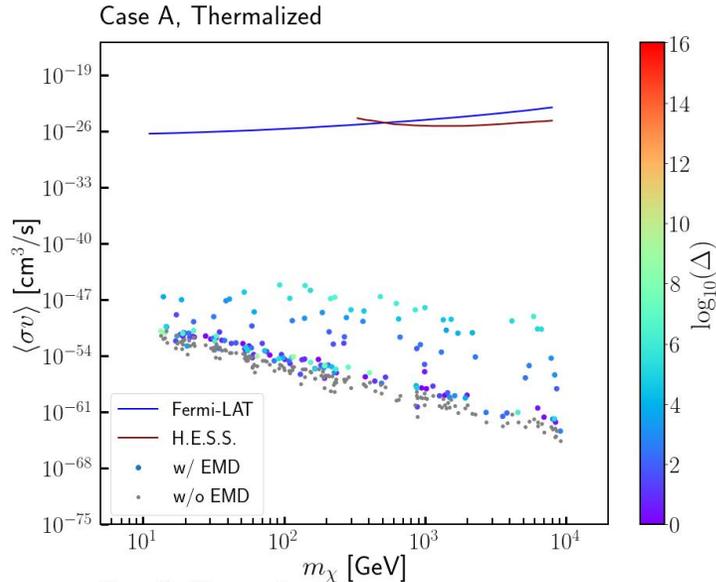
- Chemical equilibrium between **N** and **SM** driven by decays and inverse decays: $N \leftrightarrow Hl$ or $H \leftrightarrow Nl$;
- Heavy neutrinos **thermalized** with the SM when $\Gamma_{decays} > H$;

Thermalized heavy neutrinos: **all processes** (s-channels, t-channels, decays) are relevant for
DM production

Non-thermalized heavy neutrinos: neutrinos not abundant enough to decay and annihilate via
t-channel into FIMPs \Rightarrow only **s-channel** contributes for **DM production**.

Phenomenology – Indirect detection prospects

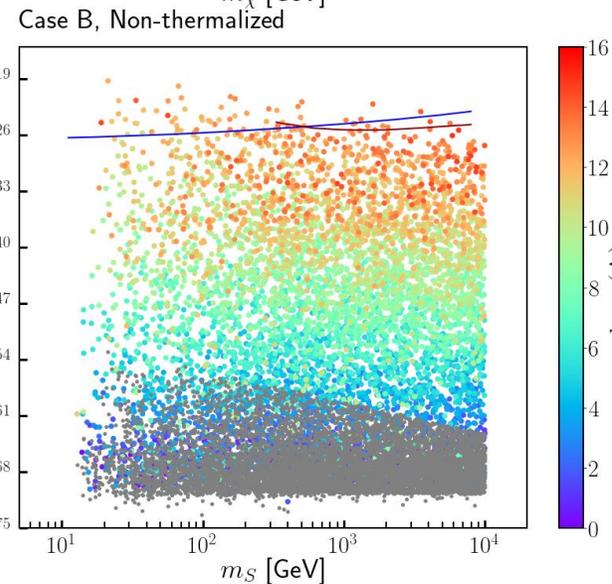
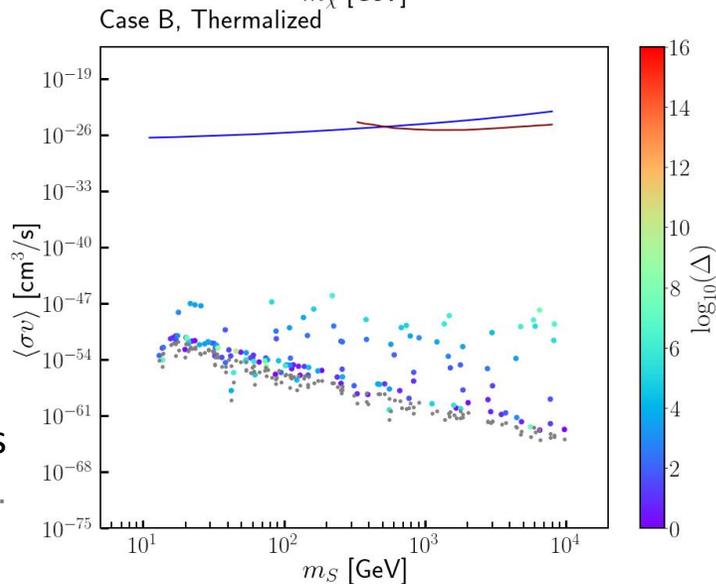
Case A: χ is DM



$m_{DM} > m_N$

$$\sigma_{\bar{\chi}\chi \rightarrow NNv} \Big|_{v \approx 0} = \frac{|\lambda_\chi|^4}{16\pi} \sqrt{1 - \frac{m_N^2}{m_\chi^2}} \frac{2m_\chi^2 - m_N^2}{(m_\chi^2 + m_S^2 - m_N^2)^2}$$

Case B: S is DM



$\langle\sigma v\rangle_{DMDM \rightarrow NN}$ bounds
from [Campos et al.
arXiv:1702.06145]

$$\sigma_{S^* S \rightarrow NNv} \Big|_{v \approx 0} = \frac{|\lambda_\chi|^4}{8\pi} \left(1 - \frac{m_N^2}{m_S^2}\right)^{3/2} \frac{m_N^2}{(m_\chi^2 + m_S^2 - m_N^2)^2}$$

The model – Neutrino portal dark matter via Freeze-in in an early matter era

Type-I seesaw mechanism

- Explain the smallness of the neutrino masses;
- Introduce 3 heavy neutrinos (one for each generation), not predicted by SM.
- New Yukawa coupling: $\overline{L}_L^i Y_\nu^{ij} \tilde{H} (N_\ell^j)_R \longrightarrow$ contributes to the SM neutrinos mass;
- m_N is not constrained by any gauge symmetry \longrightarrow can be arbitrarily large (order of GUT scale);

The model – Neutrino portal dark matter via Freeze-in in an early matter era

Type-I seesaw mechanism

$$M_\nu = \begin{pmatrix} 0 & M_D \\ M_D^T & m_N \end{pmatrix} \xrightarrow{\text{Diagonalizing}} M_\nu = -M_D^T m_N^{-1} M_D$$

Yukawa coupling:

$$Y_\nu \sim \frac{\sqrt{m_\nu m_N}}{v} \longrightarrow \text{Completely defined if we fix } m_N$$

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Also:

$$m_\nu \sim \frac{Y_\nu^2 v^2}{m_N} \quad \text{“Seesaw”}$$



Phenomenology – Direct detection prospects

Focusing on the spin-independent (SI) DM-nucleus scattering cross section, we have:

$$\begin{aligned}\sigma_0^{SI} &= \frac{\mu_{\chi N}^2 |g_{Z\chi\chi}|^2}{4\pi m_Z^4} \left[Z(g_d^V + 2g_u^V) + (A - Z)(g_u^V + 2g_d^V) \right]^2 \\ &= \frac{\mu_{\chi N}^2}{\mu_{\chi p}^2} A^2 \sigma_{\chi N}^{SI},\end{aligned}\quad g_{Z\chi\chi} = -\frac{g\lambda_\chi^2}{32\pi c_W} \sum_{ij} (V^\dagger V)_{ij} (2m_N^2 C_0(m_\chi^2, 0^-, m_\chi^2, m_S^2, m_N^2, m_N^2) - m_N^2 C_0(m_\chi^2, 0^-, m_\chi^2, m_S^2, m_N^2, 0) + 4C_{00}(m_\chi^2, 0^-, m_\chi^2, m_S^2, m_N^2, 0) - 2C_{00}(m_\chi^2, 0^-, m_\chi^2, m_S^2, m_N^2, m_N^2) - 2C_{00}(m_\chi^2, 0^-, m_\chi^2, m_S^2, 0, 0)),$$

where σ_0^{SI} is the SI DM-nucleus scattering cross section, $\sigma_{\chi N}^{SI}$ is the SI DM-nucleon scattering cross section, which is usually used to compare experimental results with different target isotopes, $\mu_{\chi N}$ is the reduced mass between DM and the nucleus (mass number A , charge number Z), $\mu_{\chi p}$ is the reduced mass between DM and the nucleon, i.e. $\mu_{\chi N} = \frac{m_\chi m_N}{m_\chi + m_N}$ and $\mu_{\chi p} = \frac{m_\chi m_p}{m_\chi + m_p}$ and g_q^V are the corresponding vector current couplings of the quarks with Z-boson:

$$g_u^V = \frac{g}{c_W} \left(\frac{1}{2} - \frac{4}{3} s_W^2 \right), \quad g_d^V = \frac{g}{c_W} \left(-\frac{1}{2} + \frac{2}{3} s_W^2 \right). \quad (6.3)$$

Heavy neutrinos thermalization

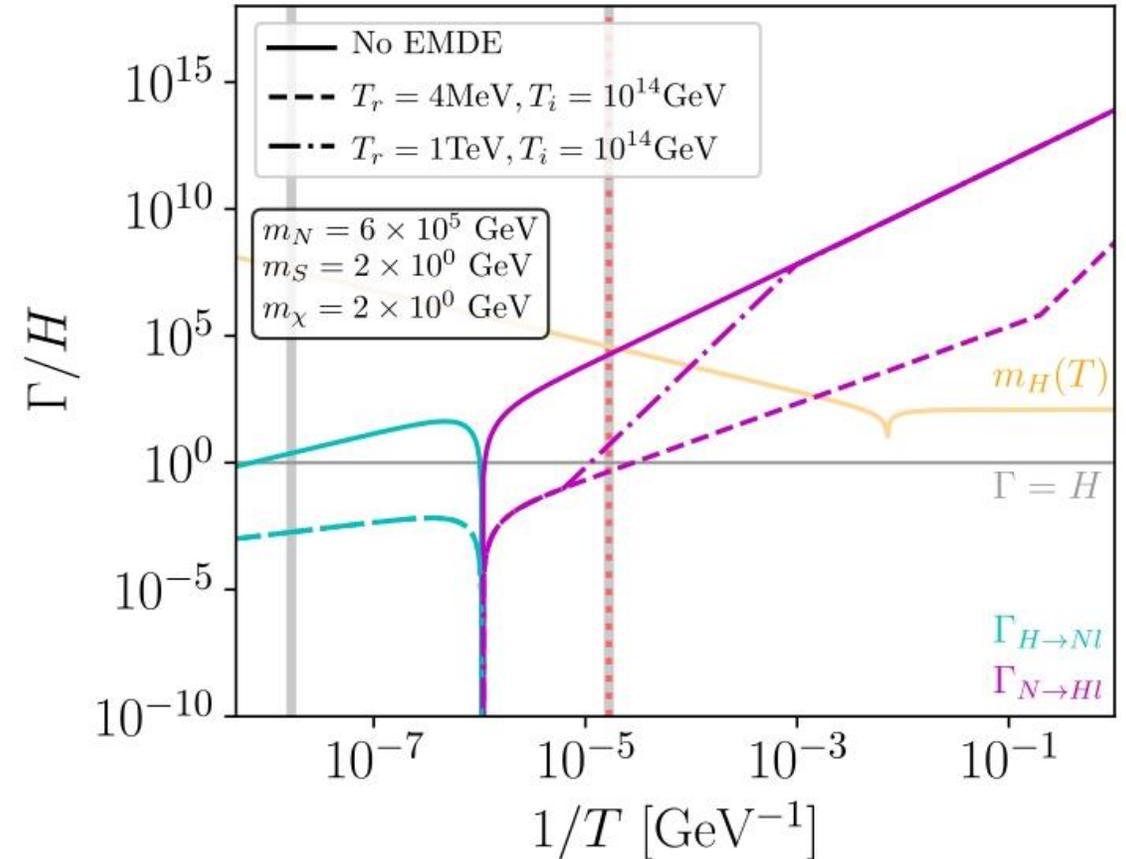
- Heavy neutrinos **thermalized** when $\Gamma > H$;
- **DM freeze-in** occurs between the **grey** vertical lines;

Heavy N case (with $m_N \gg m_S, m_\chi$)

- **Large Yukawa coupling** \Rightarrow **N** easily thermalizes with the cosmic bath;



Long EMDE \Rightarrow no thermalization.



Heavy neutrinos thermalization

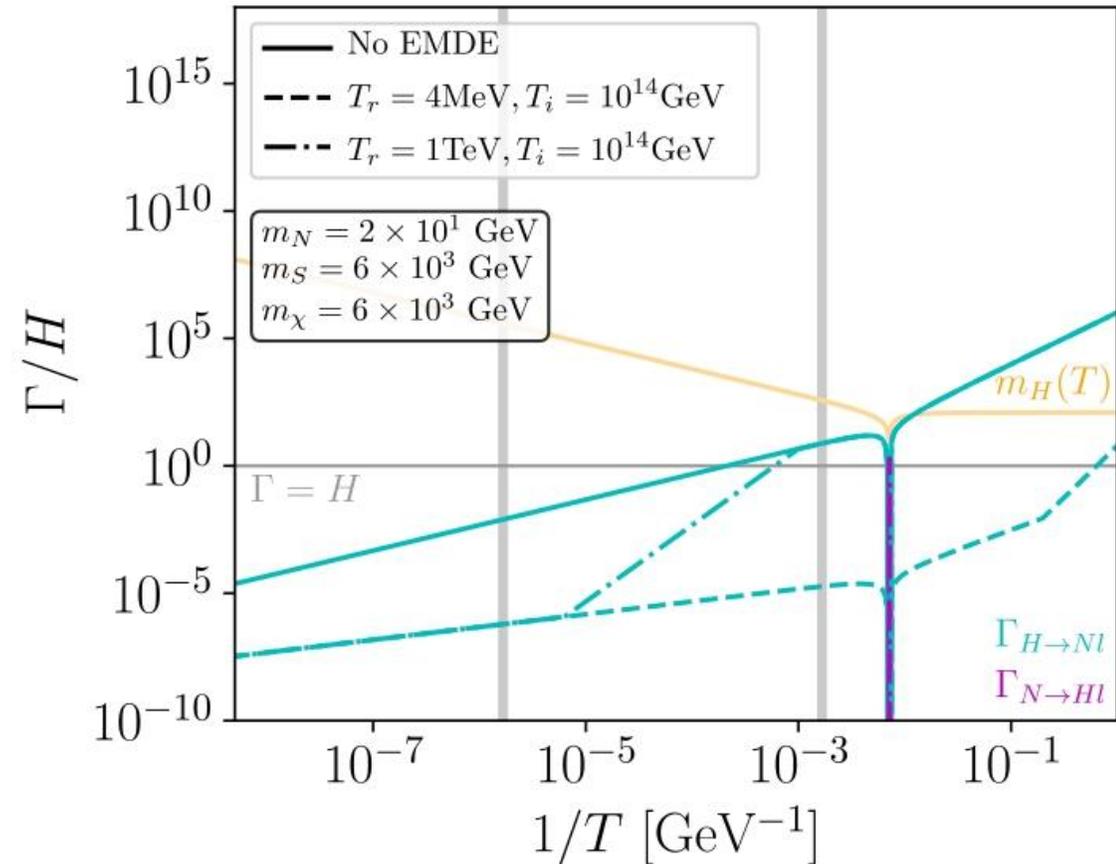
- Heavy neutrinos **thermalized** when $\Gamma > H$;
- **DM freeze-in** occurs between the **grey** vertical lines;

Light N case (with $m_N < m_S, m_\chi$)

- **Freeze-in** occurs at $T \gg m_N \Rightarrow$ decay widths suppressed by Yukawa couplings



Heavy neutrino is **never thermalized**.



Heavy neutrinos thermalization

- Heavy neutrinos **thermalized** when $\Gamma > H$;
- **DM freeze-in** occurs between the **grey** vertical lines;

Light N case (with $m_N > m_S, m_\chi$)

- **Long EMDE** difficults thermalization;



- Heavy neutrino is **thermalized** only for **short EMDE**.

