

# High energy neutrinos as probes of soft lepton number violation

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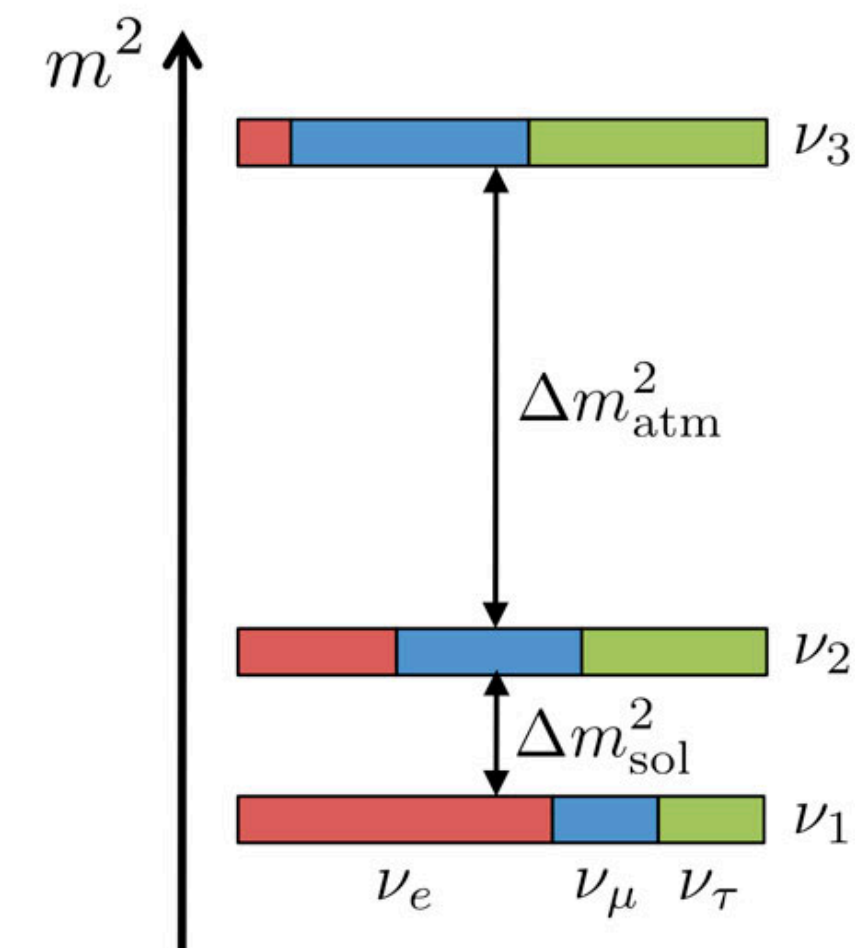
TeVPA 2023



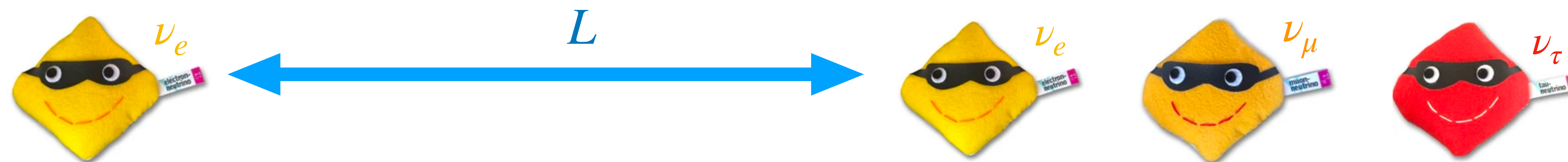
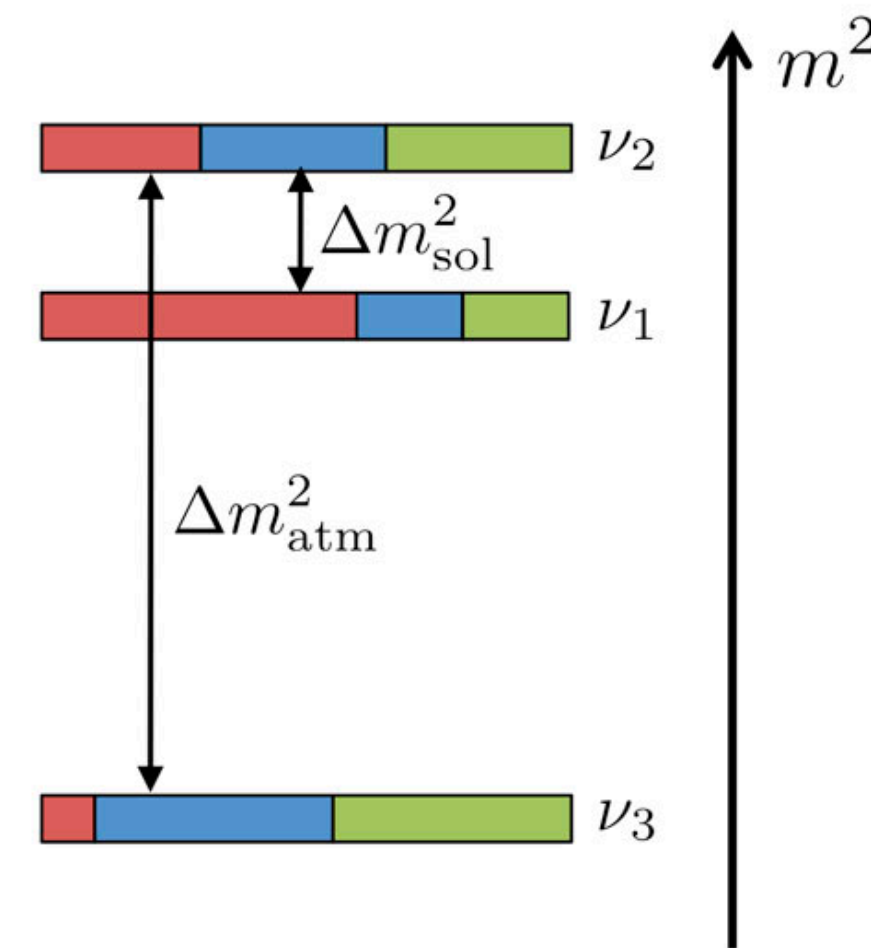
# Neutrino oscillations

- Neutrinos interact “weakly” with the rest, as well as with themselves.
- There are 3 active light neutrinos.
- Neutrinos are massive and can change flavor.

normal hierarchy (NH)



inverted hierarchy (IH)



$$P_{\nu_a \rightarrow \nu_b}(E) = \sin^2 2\theta \sin^2 \left( \frac{\Delta m^2 L}{4E} \right)$$

$$L_{\text{osc}} \propto \frac{E}{\Delta m^2}$$

# Lepton Number in the Standard Model

- Lepton number is a conserved symmetry in the SM classically. Violated by chiral anomalies.
- New physics leads to lepton-number violation. Might be related to origin of neutrino masses.
- Consider 1 active and 1 sterile neutrino. The Lagrangian,

$$\mathcal{L} = \bar{\nu}_L m_D \nu_R + \frac{1}{2} \bar{\nu}_L^c m_L \nu_L + \frac{1}{2} \bar{\nu}_R^c m_R \nu_R + \text{h.c.}$$



- The generic mass matrix  $\mathcal{M} = \begin{pmatrix} m_L & m_D \\ m_D & m_R \end{pmatrix}$



# Pseudo (Quasi)-Dirac neutrinos

Generic Majorana mass matrix  $\mathcal{M} = \begin{pmatrix} m_L & m_D \\ m_D & m_R \end{pmatrix}$ .

1. Dirac limit:  $m_{L,R} = 0$ .  
No lepton-number violation.
2. Majorana limit :  $m_{L,R} \gg m_D$ .  
Explicit lepton-number violation.
3. (Quasi) Pseudo-Dirac limit :  $m_{L,R} \ll m_D$ .  
Soft lepton-number violation.



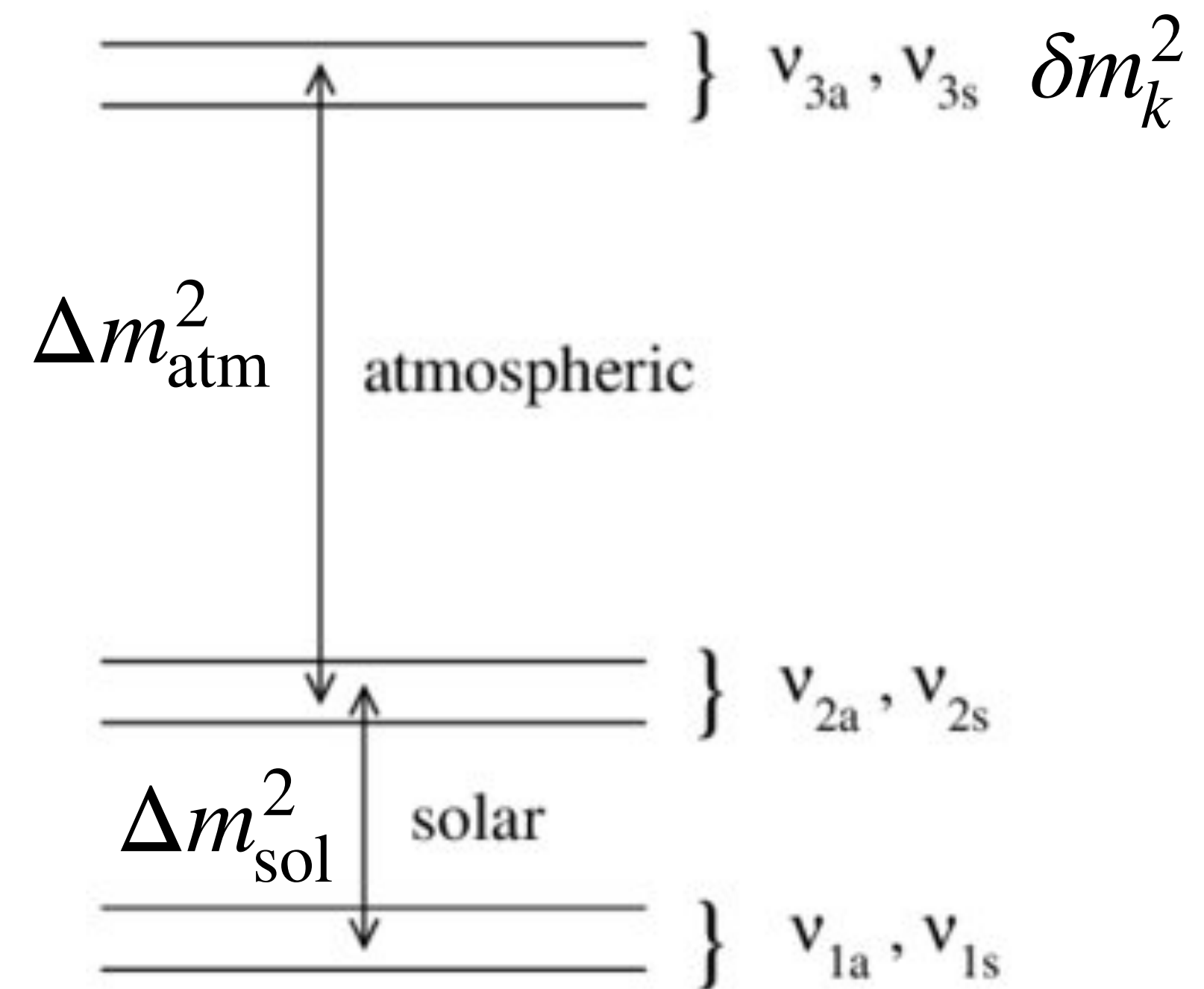


# Pseudo-Dirac neutrinos formalism

- 3 pairs of quasi-degenerate states, separated by  $\delta m_k^2$ , which is much smaller than the usual  $\Delta m_{\text{sol}}^2$  and  $\Delta m_{\text{atm}}^2$ .

$$m_{ks,ka}^2 \simeq m_k^2 \pm \delta m_k^2/2, \quad \text{where } \delta m^2 \sim m_D(m_L + m_R)$$

Kobayashi, Lim, PRD2001



- In the **P-D** limit, under certain approximations, mass matrix can be diagonalized by

$$\mathcal{V} = \begin{pmatrix} U_{\text{PMNS}} & 0 \\ 0 & U_R \end{pmatrix} \cdot \frac{1}{\sqrt{2}} \cdot \begin{pmatrix} 1_3 & i1_3 \\ \varphi & -i\varphi \end{pmatrix}$$

- Further generalizations considered with non-maximal mixings.

Anamiati, Fonseca, Hirsch, PRD2018

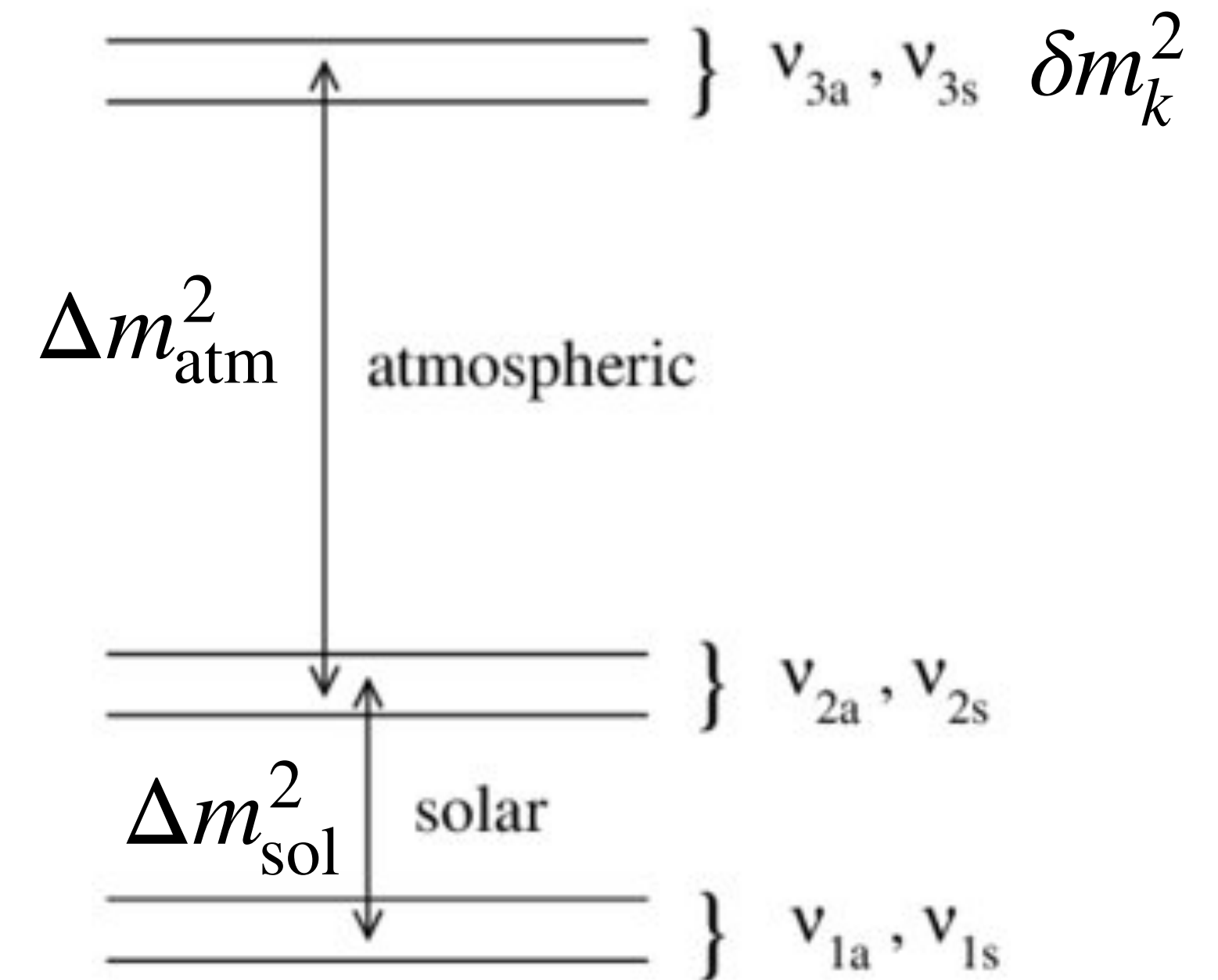
# Oscillations due to small $\delta m^2$

- $\delta m_k^2$  will lead to oscillations at very large distances,  $L \propto 1/\delta m^2$
- Flavor oscillation probability induced by  $\Delta m_{\text{sol}}^2$  and  $\Delta m_{\text{atm}}^2$  over a large distance gets averaged.

$$P(\bar{\nu}_\beta \rightarrow \bar{\nu}_\gamma) = P_{aa}(z, E) \left| U_{\beta k} \right|^2 \left| U_{\gamma k} \right|^2$$

- Survival probability

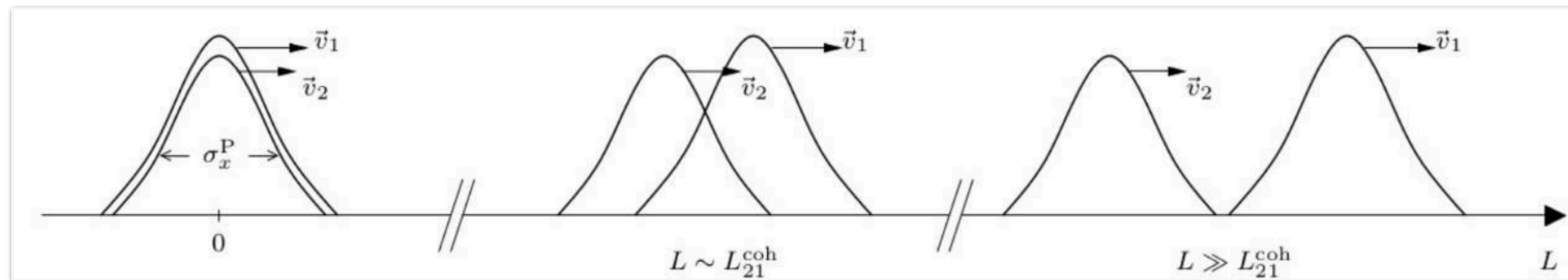
$$P_{aa}(z, E) = \frac{1}{2} \left( 1 + e^{-\left(\frac{L(z)}{L_{\text{coh}}}\right)^2} \cos \left( 2\pi \frac{L(z)}{L_{\text{osc}}} \right) \right)$$



# Oscillations due to small $\delta m^2$

- Survival probability  $P_{aa}(z, E) = \frac{1}{2} \left( 1 + e^{-\left(\frac{L(z)}{L_{\text{coh}}}\right)^2} \cos \left( 2\pi \frac{L(z)}{L_{\text{osc}}} \right) \right)$

- Wave-packet separation decoherence also becomes important. Decoherence important if  $L(z) > L_{\text{coh}}$ .



Giunti and Kim, Fundamentals of neutrino physics

$$L_{\text{osc}} = \frac{4\pi E_\nu}{\delta m^2}$$

$$L_{\text{coh}} = \frac{4\sqrt{2} E_\nu}{|\delta m^2|} (E_\nu \sigma_x)$$

Width of wavepacket

A smaller  $\sigma_x$  can cause decoherence.

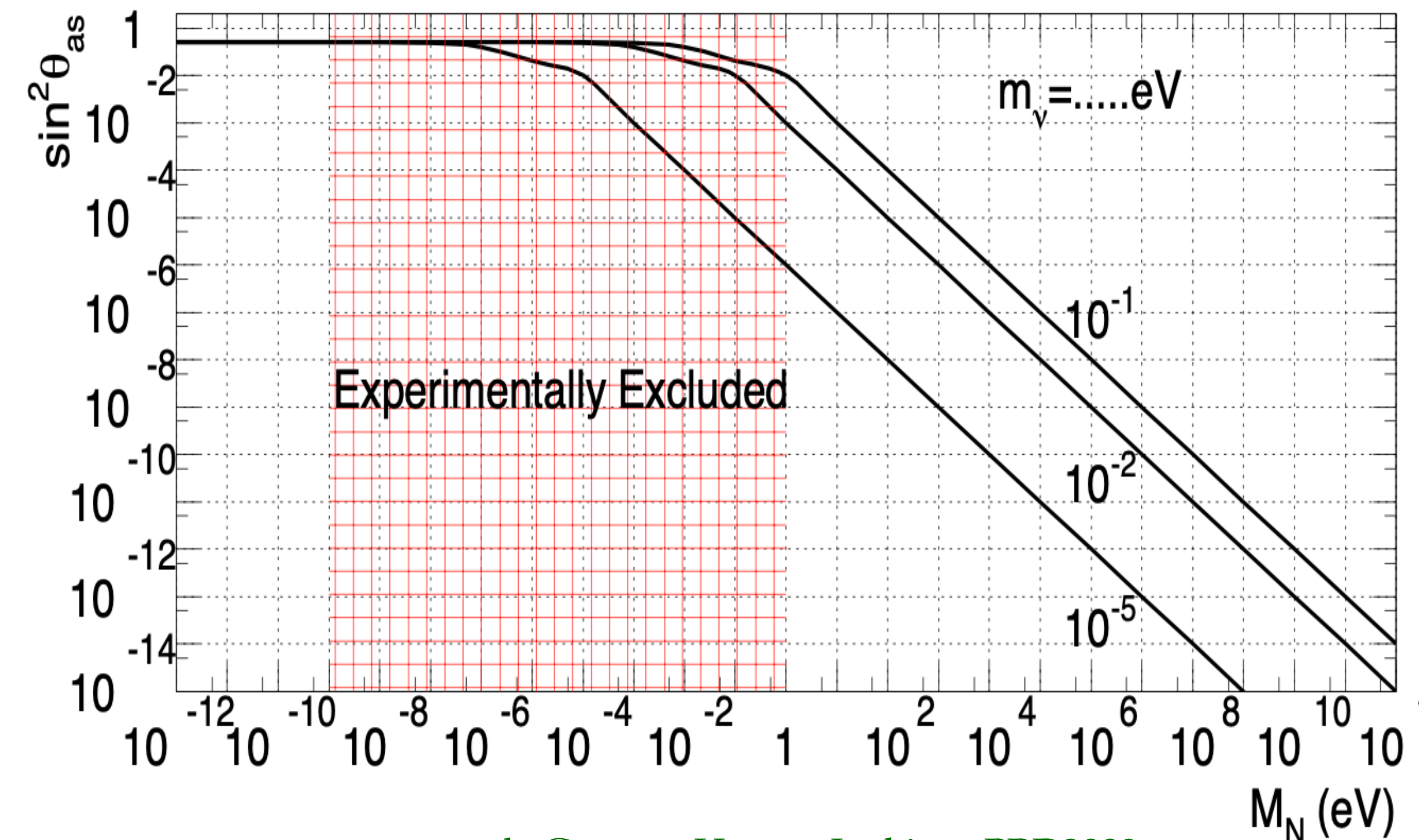
# Bounds from neutrino sources

Experiment	$\varepsilon_1^2$ [eV <sup>2</sup> ]	$\varepsilon_2^2$ [eV <sup>2</sup> ]	$\varepsilon_3^2$ [eV <sup>2</sup> ]
KamLAND	$7.7(3.4) \times 10^{-6}$	$1.7(1.0) \times 10^{-5}$	–
Solar + KamLAND	$1.7(1.3) \times 10^{-11}$	$1.7(1.5) \times 10^{-11}$	–
DayaBay + MINOS + T2K	–	$1.5(0.9) \times 10^{-4}$	$1.3(0.074) \times 10^{-3}$
Super-K + DayaBay + MINOS + T2K	–	$1.9(1.8) \times 10^{-5}$	$1.2(1.1) \times 10^{-5}$
JUNO	$1.7(0.07) \times 10^{-5}$	$2.3(0.09) \times 10^{-5}$	$6.0(2.2) \times 10^{-5}$

Table 1: 95 % upper limits on  $\varepsilon_i^2$  derived from different experimental data sets. Two numbers are given for each case; the first one is the limit obtained marginalizing over two standard oscillation parameters (see text), the second (in brackets) is the limit obtained for the best fit point value of the standard oscillation parameters. For a discussion see text.

Bounds:

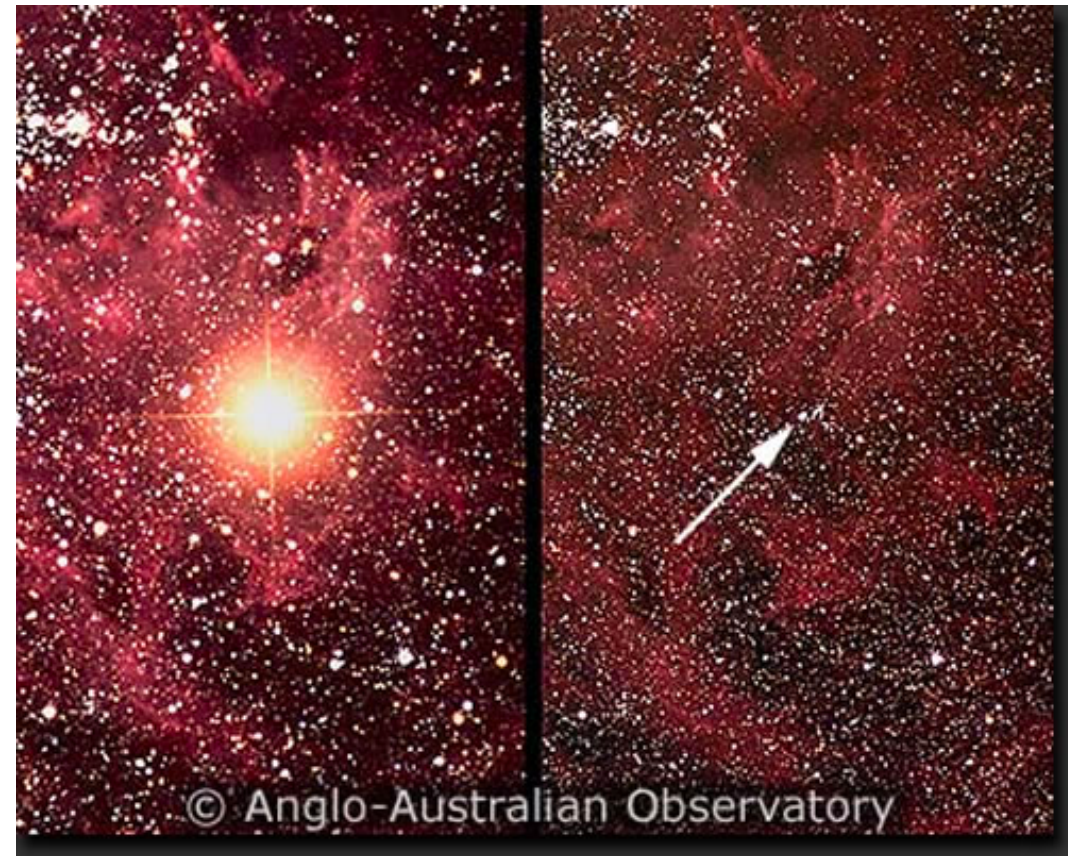
1. Solar neutrinos  $\delta m^2 < 10^{-12} \text{ eV}^2$
2. Atmospheric neutrinos  $\delta m^2 < 10^{-4} \text{ eV}^2$
3. High energy astrophysical neutrinos  
 $10^{-18} \text{ eV}^2 < \delta m^2 < 10^{-12} \text{ eV}^2$



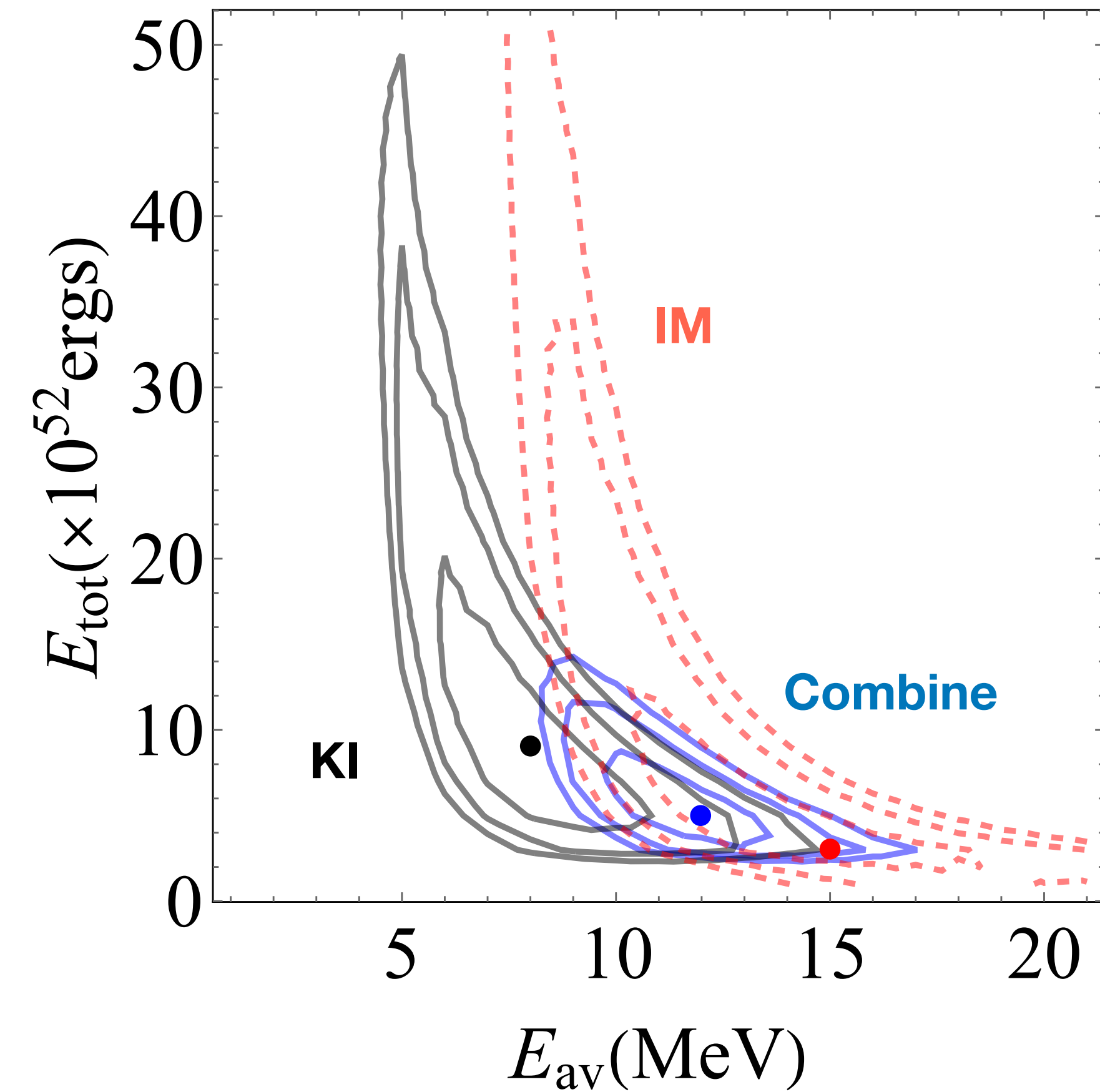
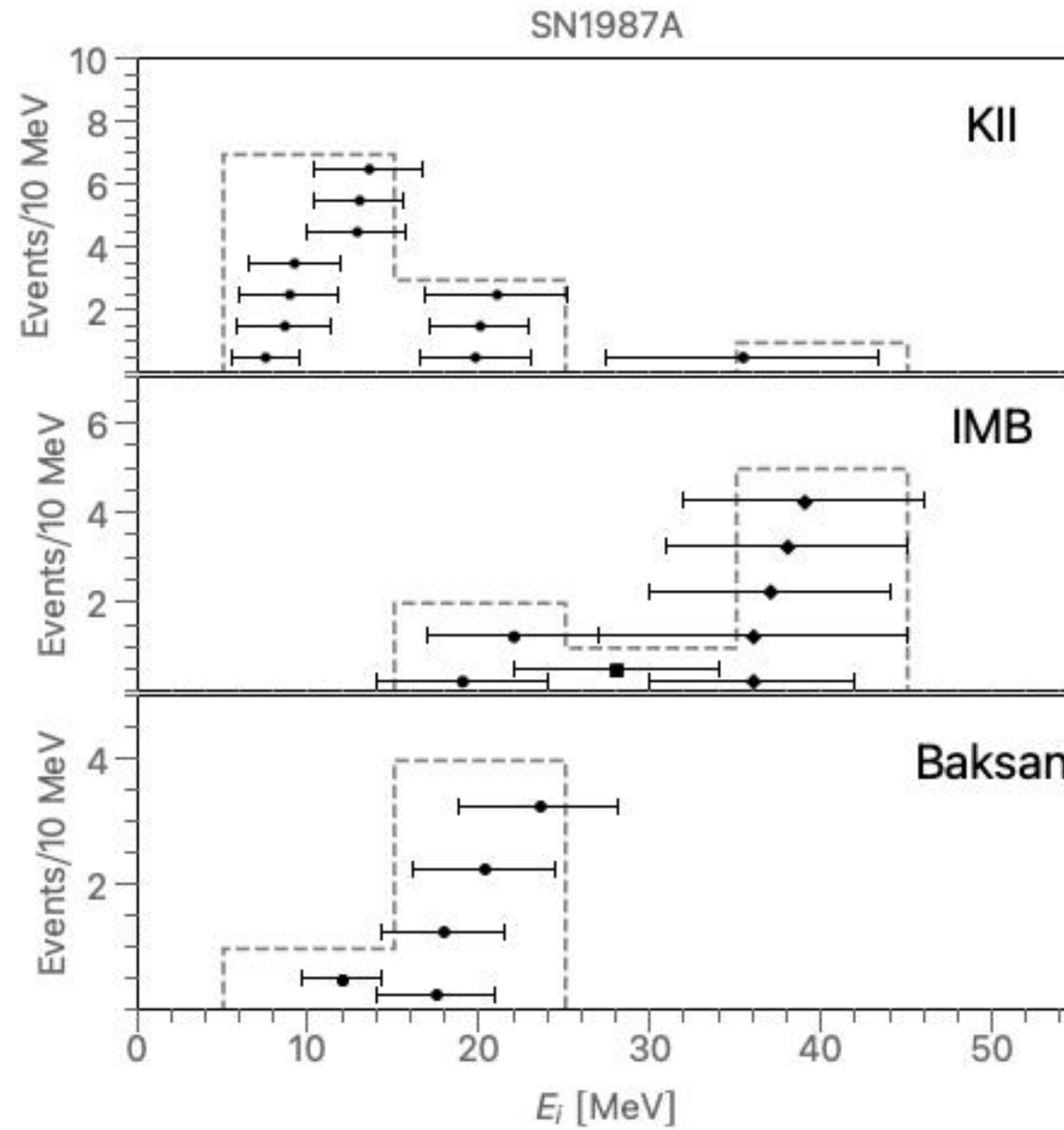


What other sources  
can we consider?

# 1. SN1987A



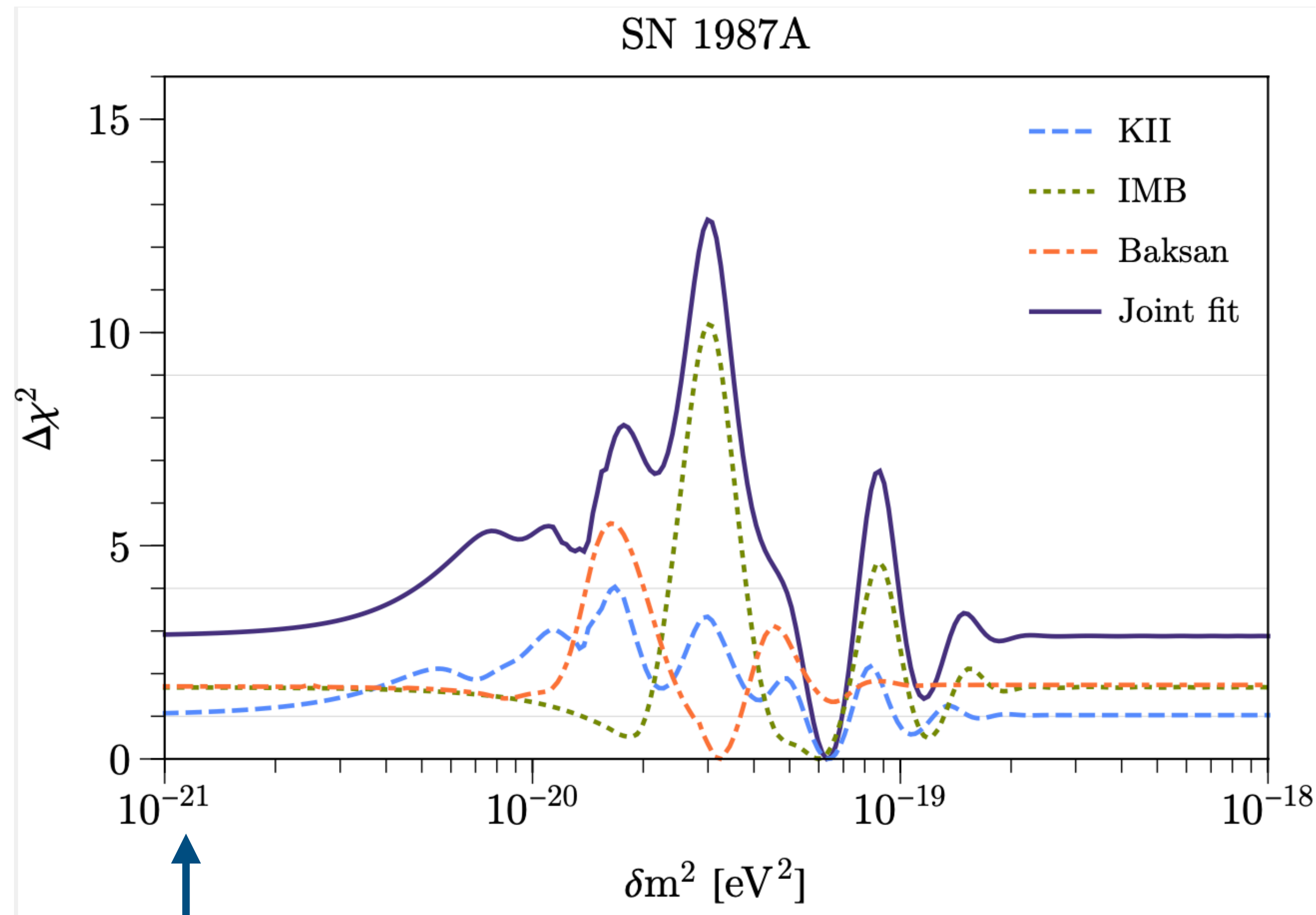
Large Magellanic Cloud  
50 kpc away



Slight tension between  
IMB and KII data?

$$d\mathcal{N}_{\bar{\nu}}(E_{\nu}) = \frac{E_{\text{tot}}}{\langle E_{\bar{\nu}} \rangle} \frac{(1 + \alpha)^{1+\alpha}}{\Gamma(1 + \alpha)} \left( \frac{E_{\nu}}{\langle E_{\bar{\nu}} \rangle} \right)^{\alpha} e^{-(1+\alpha)\frac{E_{\nu}}{\langle E_{\bar{\nu}} \rangle}},$$

# 1. SN1987A



- Slight preference for the PD possibility,  $\Delta\chi^2 \sim 3$
- Exclude  $\delta m^2 \sim [2.5, 3.] \times 10^{-20} \text{eV}^2$  with  $\Delta\chi^2 > 9$

Martinez-Soler, Perez-Gonzalez, MS, (PRD 2021)

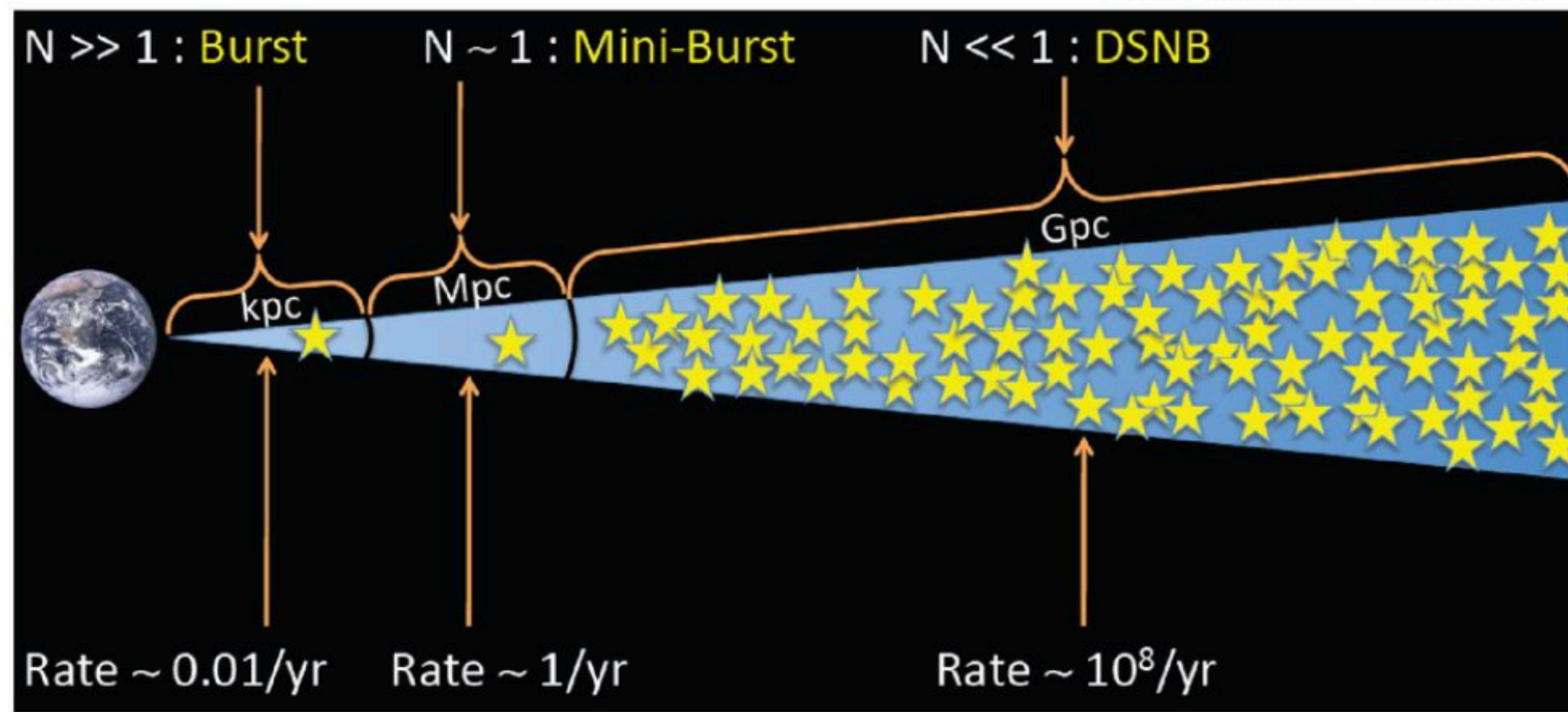
No Oscillations

$$L_{\text{osc}} = \frac{4\pi E_\nu}{\delta m^2} \sim 20 \text{ kpc} \left( \frac{E_\nu}{25 \text{ MeV}} \right) \left( \frac{10^{-19} \text{ eV}^2}{\delta m^2} \right)$$

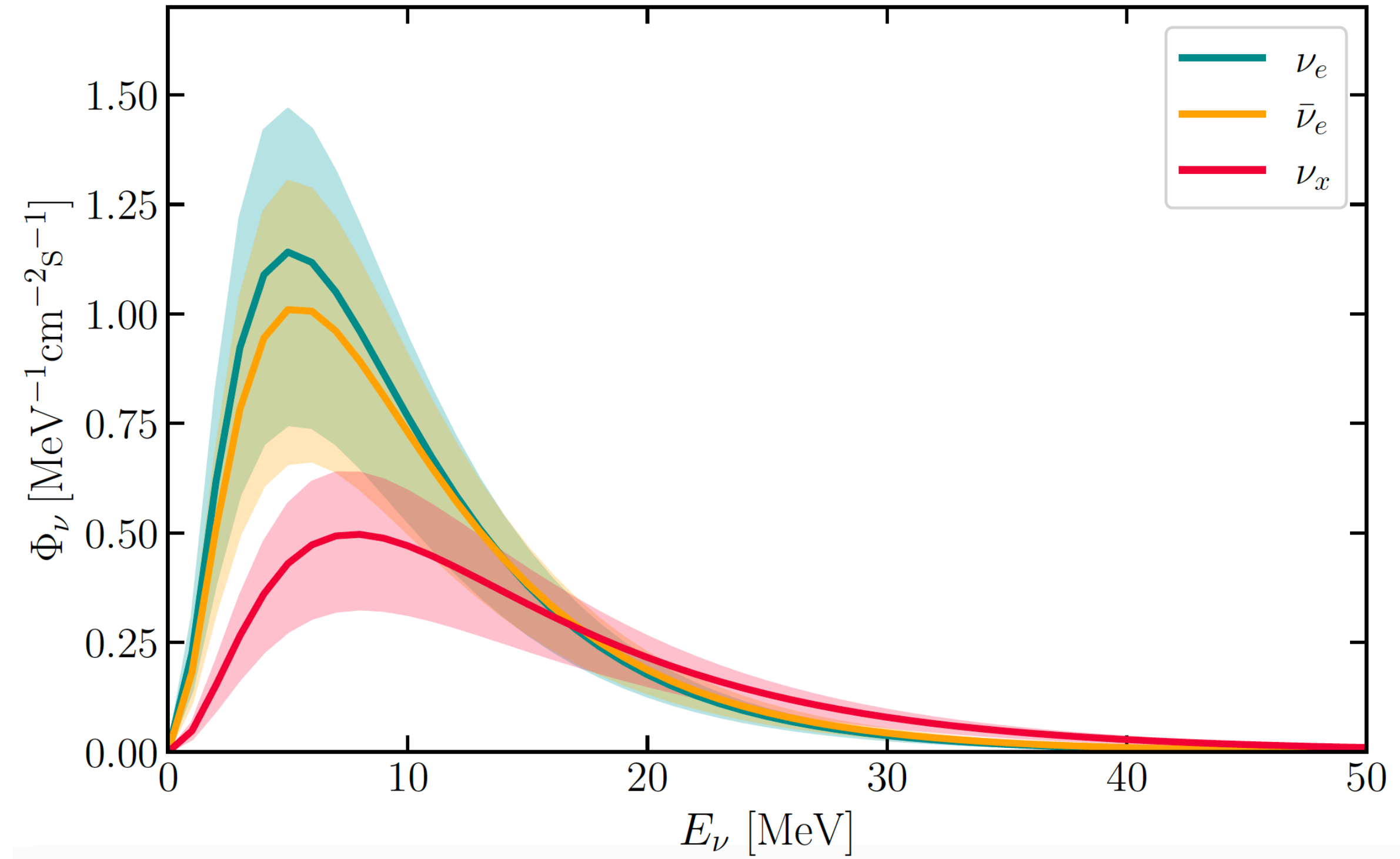


# 2. DSNB

John Beacom, TAUP2011



DSNB=Diffuse Supernova Neutrino Background

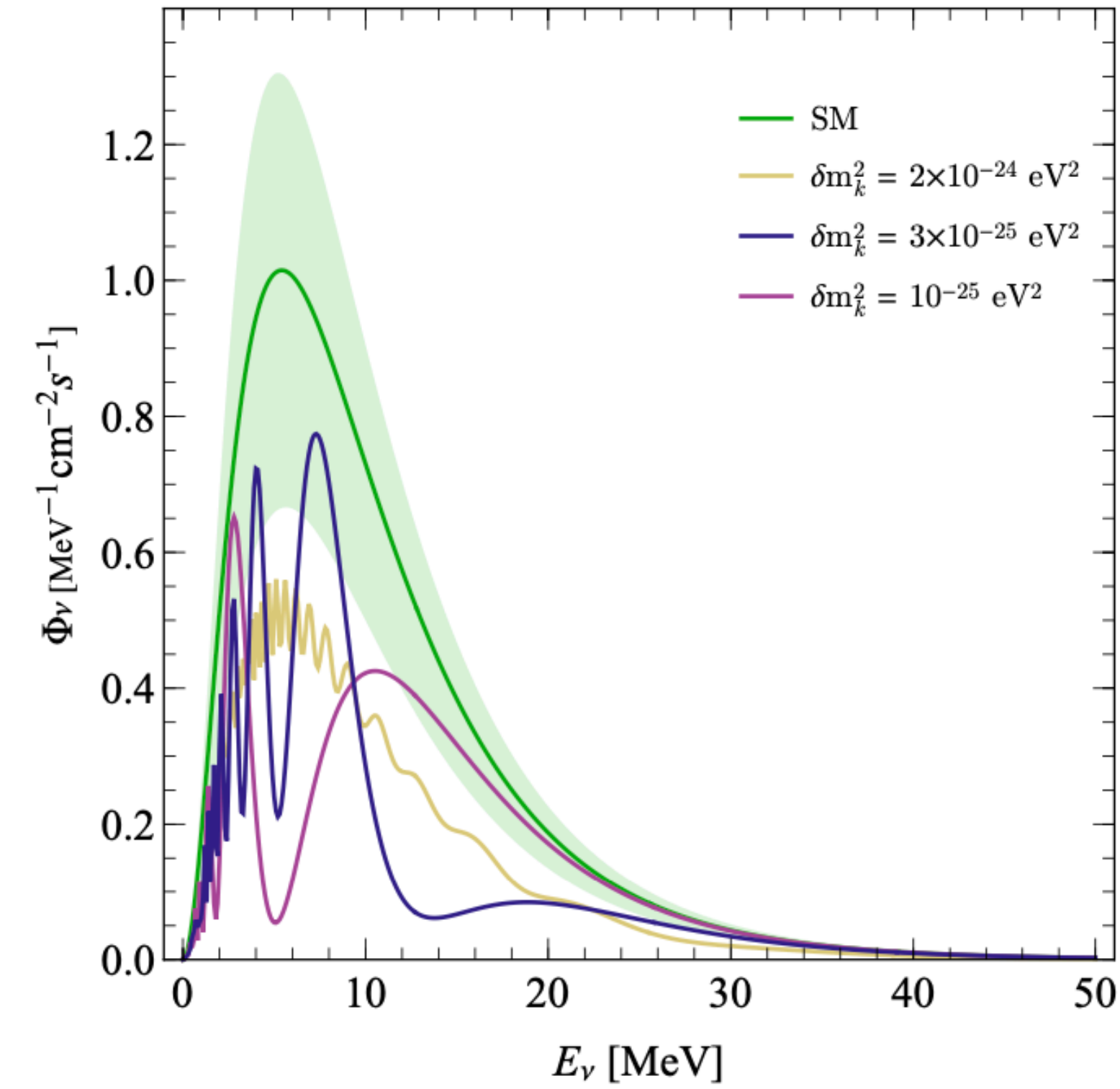


Neutrinos from Gpc distance

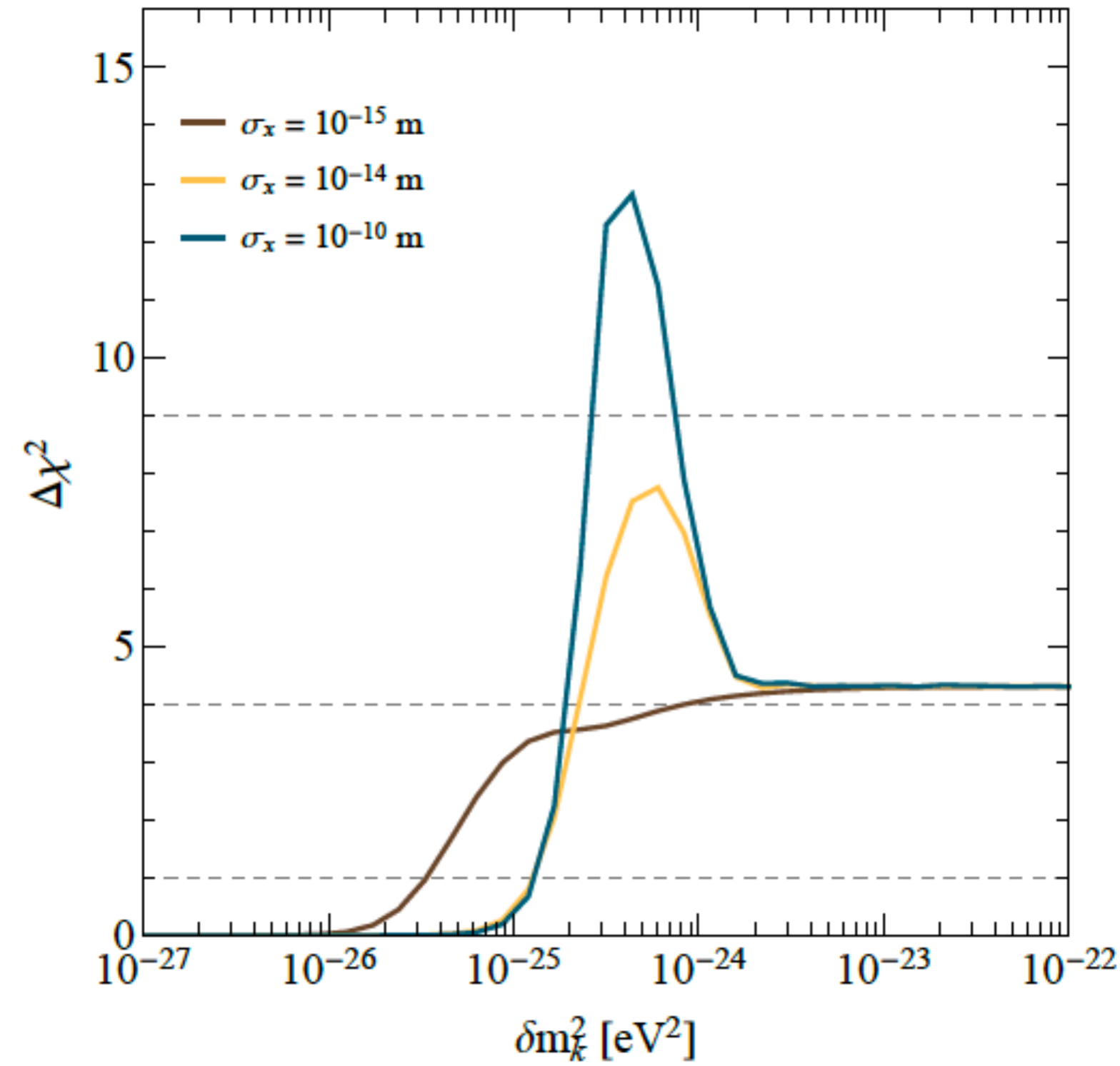
$$L_{\text{osc}} = \sim 16 \text{ Gpc} \left( \frac{E_\nu}{20 \text{ MeV}} \right) \left( \frac{10^{-25} \text{ eV}^2}{\delta m^2} \right)$$

# 2. DSNB

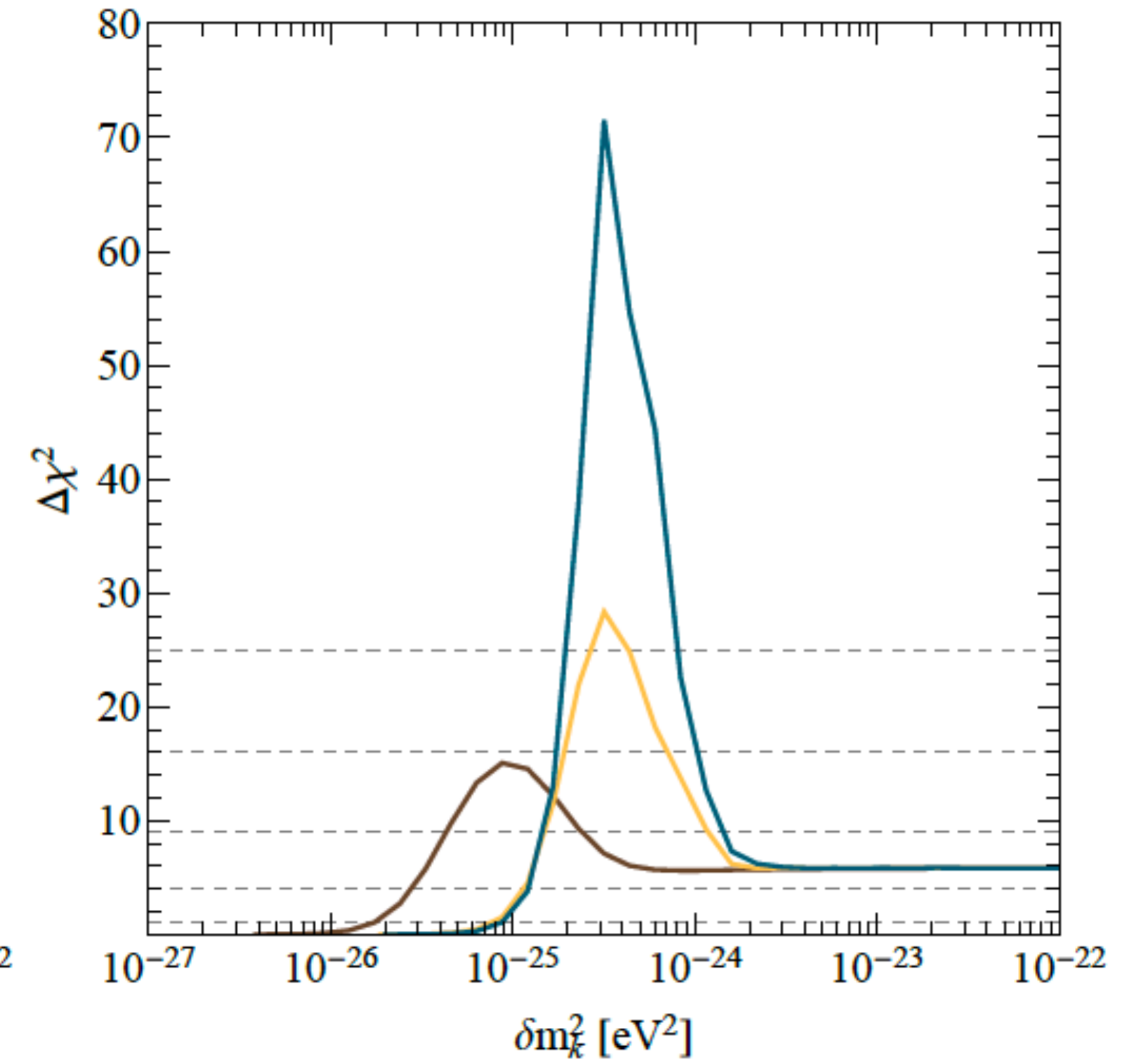
$\bar{\nu}_1$  DSNB Flux –  $\sigma_x = 10^{-10} \text{m}$



Pseudo-Dirac neutrinos – SK



Pseudo-Dirac neutrinos – HK



$$L_{\text{osc}} = \sim 16 \text{ Gpc} \left( \frac{E_\nu}{20 \text{ MeV}} \right) \left( \frac{10^{-25} \text{ eV}^2}{\delta m^2} \right)$$

de Gouvea, Martinez-Soler, Perez-Gonzalez, MS (PRD 2020)

DSNB sensitive to  $\delta m^2 \sim \mathcal{O}(10^{-25} \text{ eV}^2)$  with a high significance.

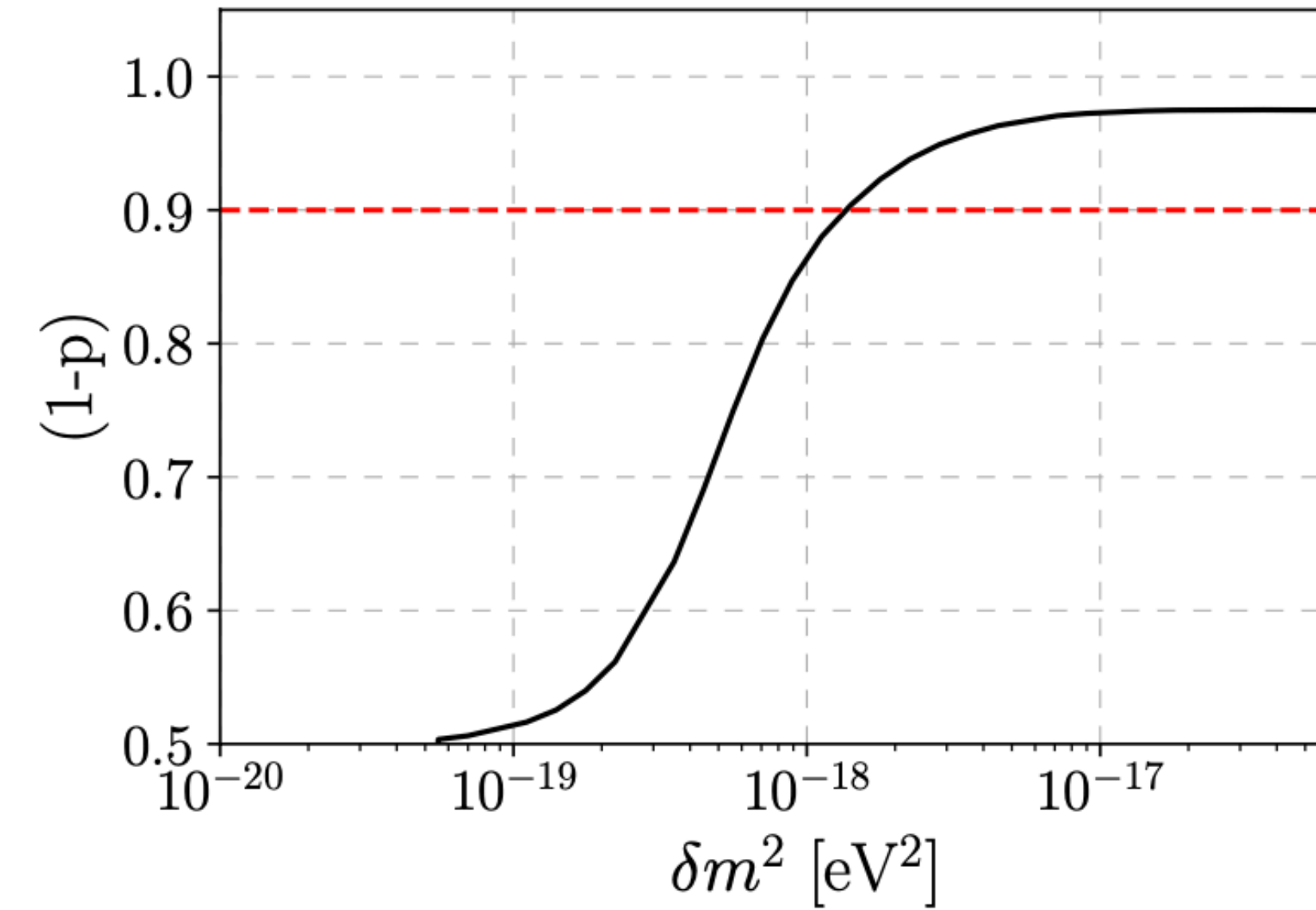
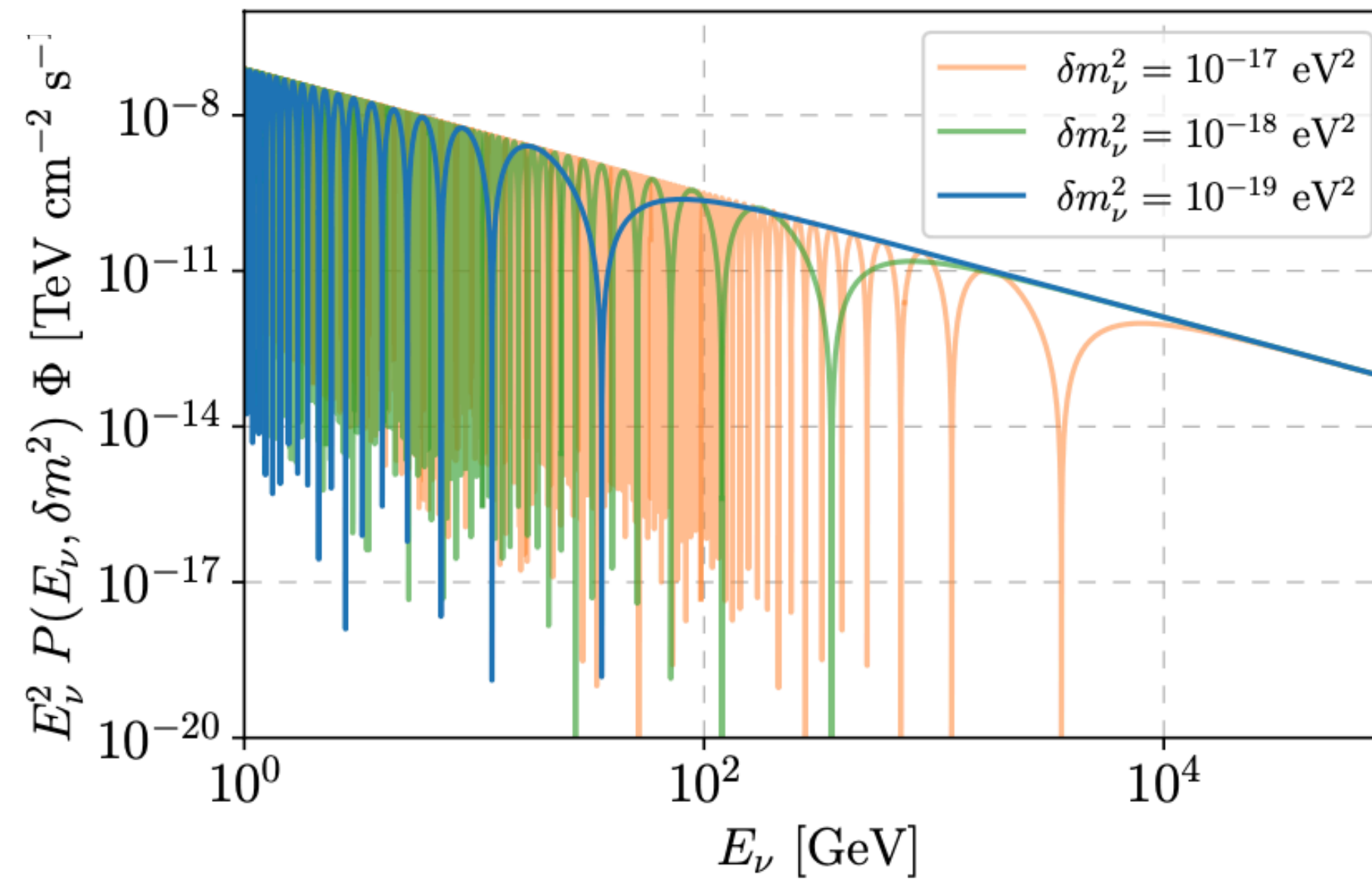


# 3. NGC 1068

## NEUTRINO ASTROPHYSICS

### Evidence for neutrino emission from the nearby active galaxy NGC 1068

IceCube Collaboration\*†



Rink, MS (2023)

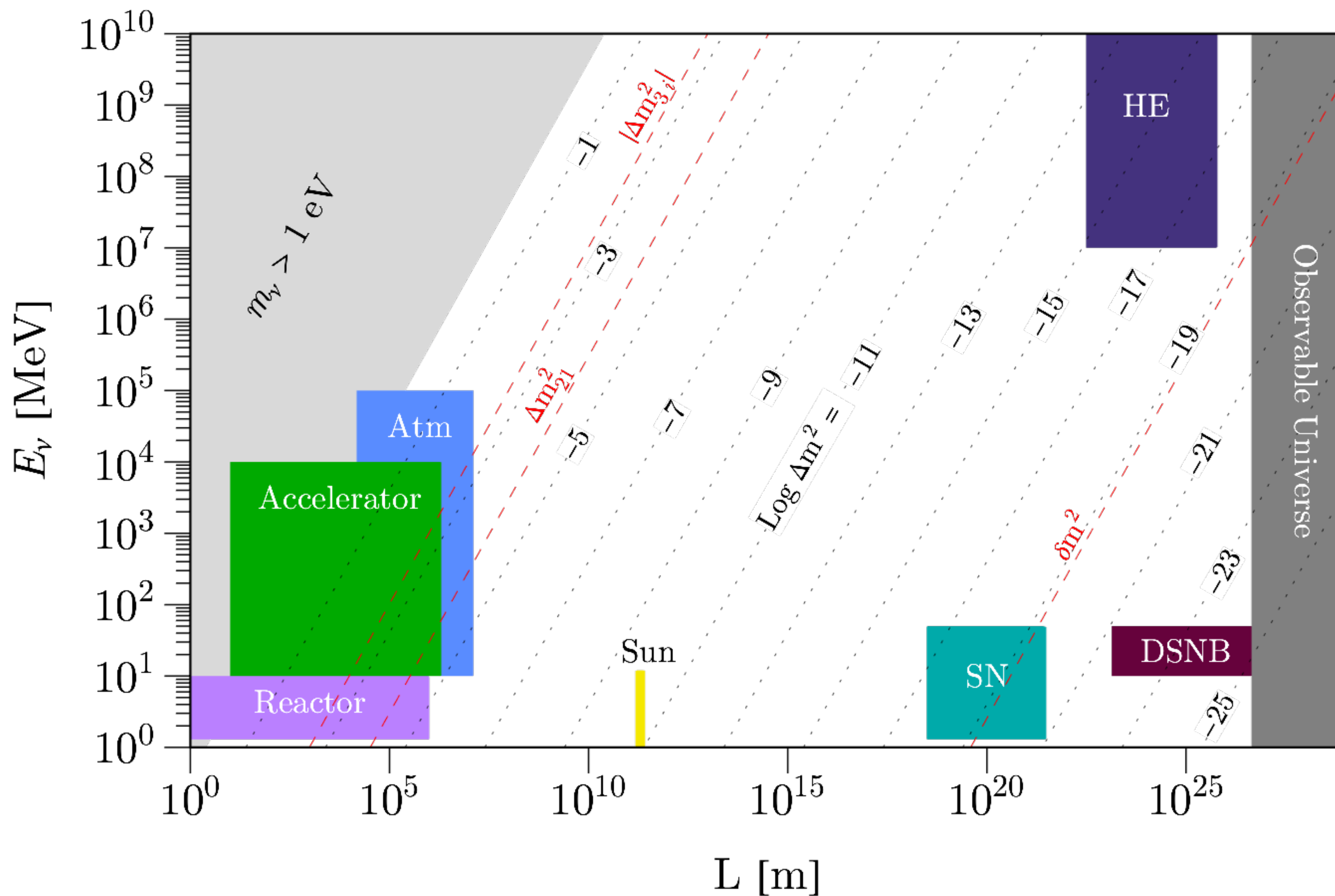
$$L_{\text{osc}} = \sim 15 \text{ Mpc} \left( \frac{E_\nu}{1 \text{ TeV}} \right) \left( \frac{10^{-18} \text{ eV}^2}{\delta m^2} \right)$$

TeV neutrinos from Gpc sensitive to  $\delta m^2 \sim \mathcal{O}(10^{-18} \text{ eV}^2)$



# Final thoughts

Neutrinos from far-away sources are strong probes of soft lepton-number violation.



**Thank you!**

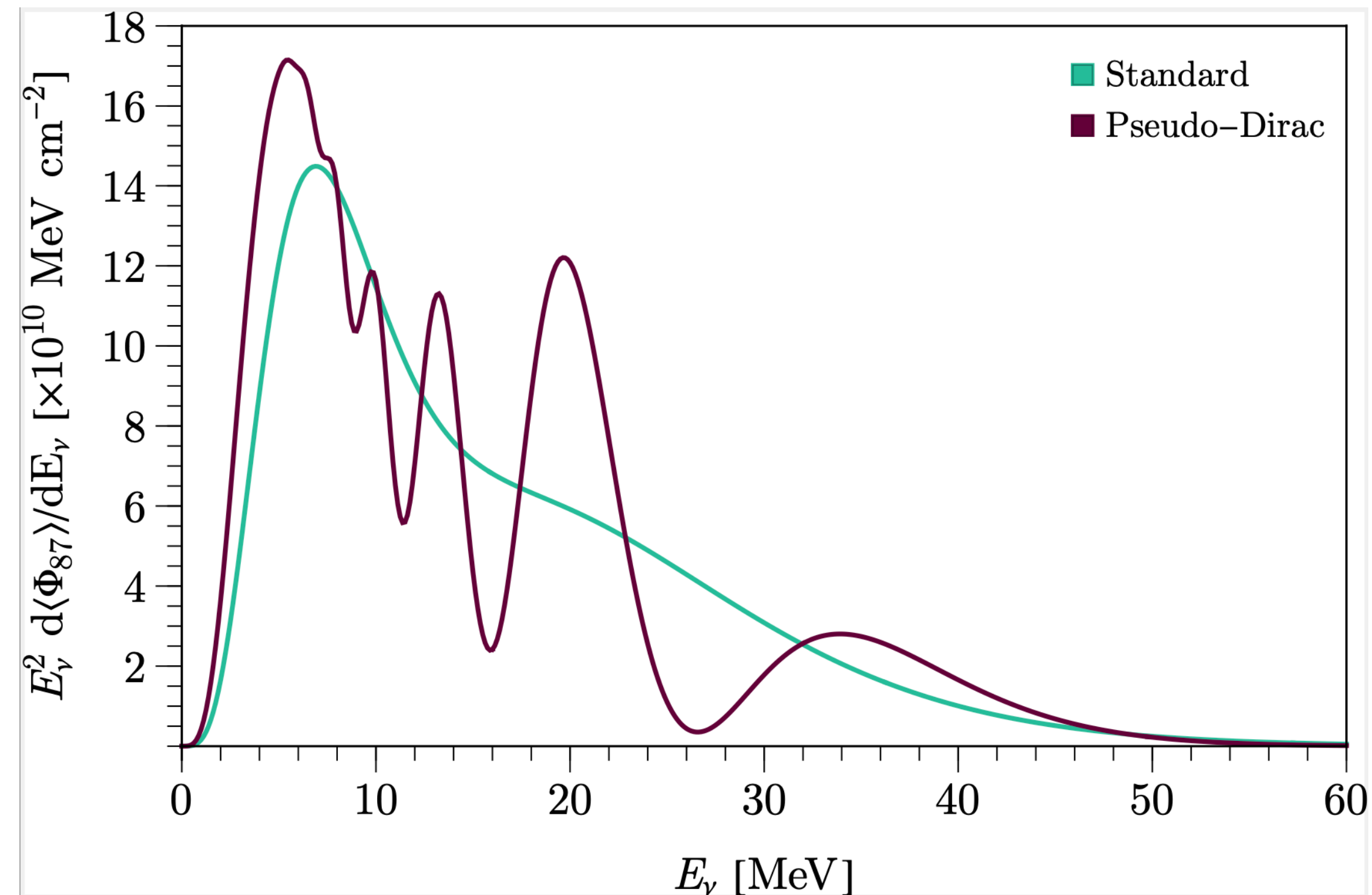
# SN flux, processed by PD probability

$$L_{\text{osc}} = \frac{4\pi E_\nu}{\delta m^2} \sim 20 \text{ kpc} \left( \frac{E_\nu}{25 \text{ MeV}} \right) \left( \frac{10^{-19} \text{ eV}^2}{\delta m^2} \right)$$

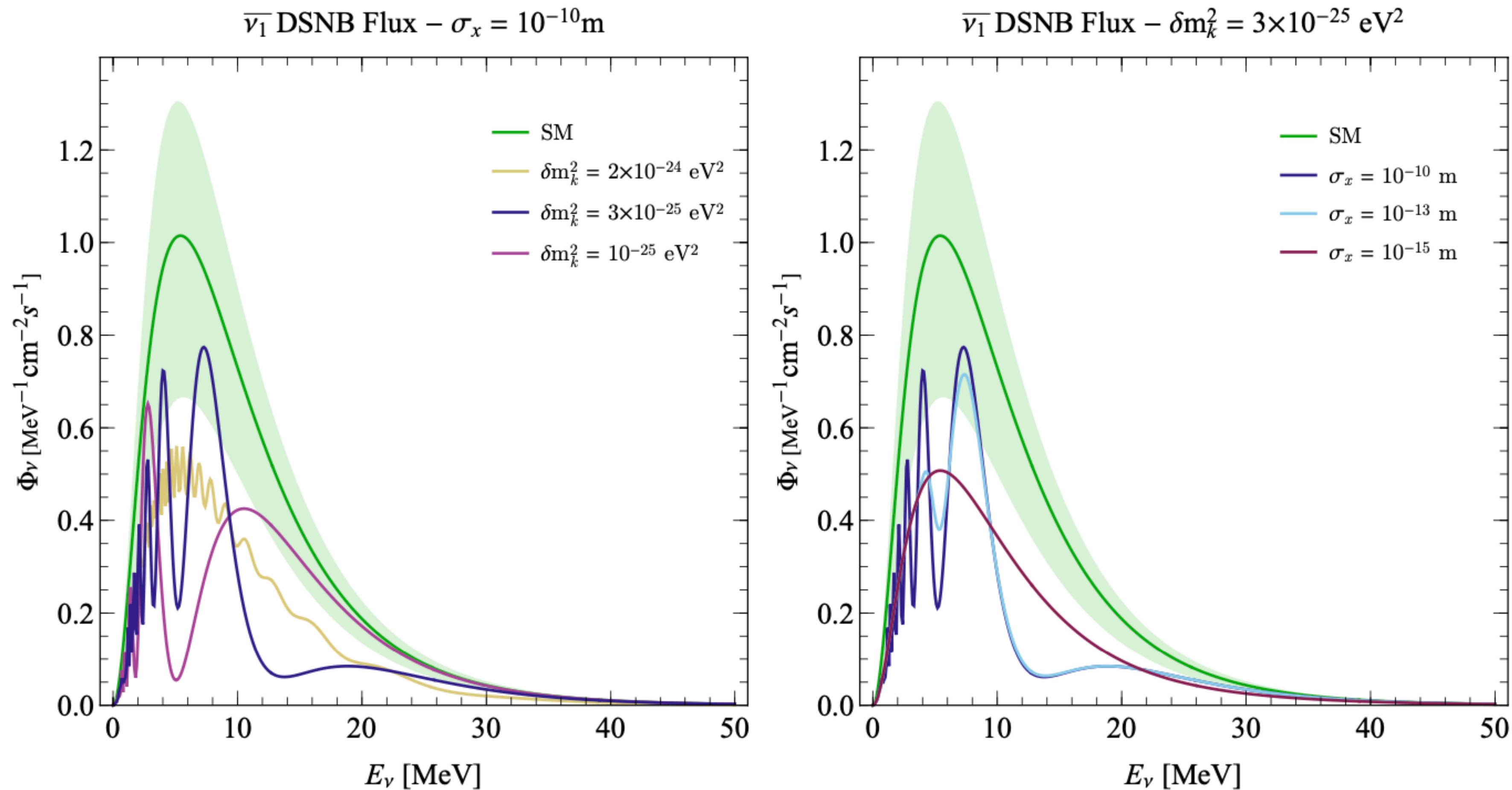
$$L_{\text{coh}} = \frac{4\sqrt{2}E_\nu}{|\delta m^2|} (E_\nu \sigma_x) \sim 114 \text{ kpc} \left( \frac{E_\nu}{25 \text{ MeV}} \right)^2 \left( \frac{10^{-19} \text{ eV}^2}{\delta m^2} \right) \left( \frac{\sigma_x}{10^{-13} \text{ m}} \right),$$

Oscillations due to  $\delta m^2$

Decoherence due to  $\delta m^2$  and  $\sigma_x$



# DSNB: Oscillations due to pseudo-Dirac nature

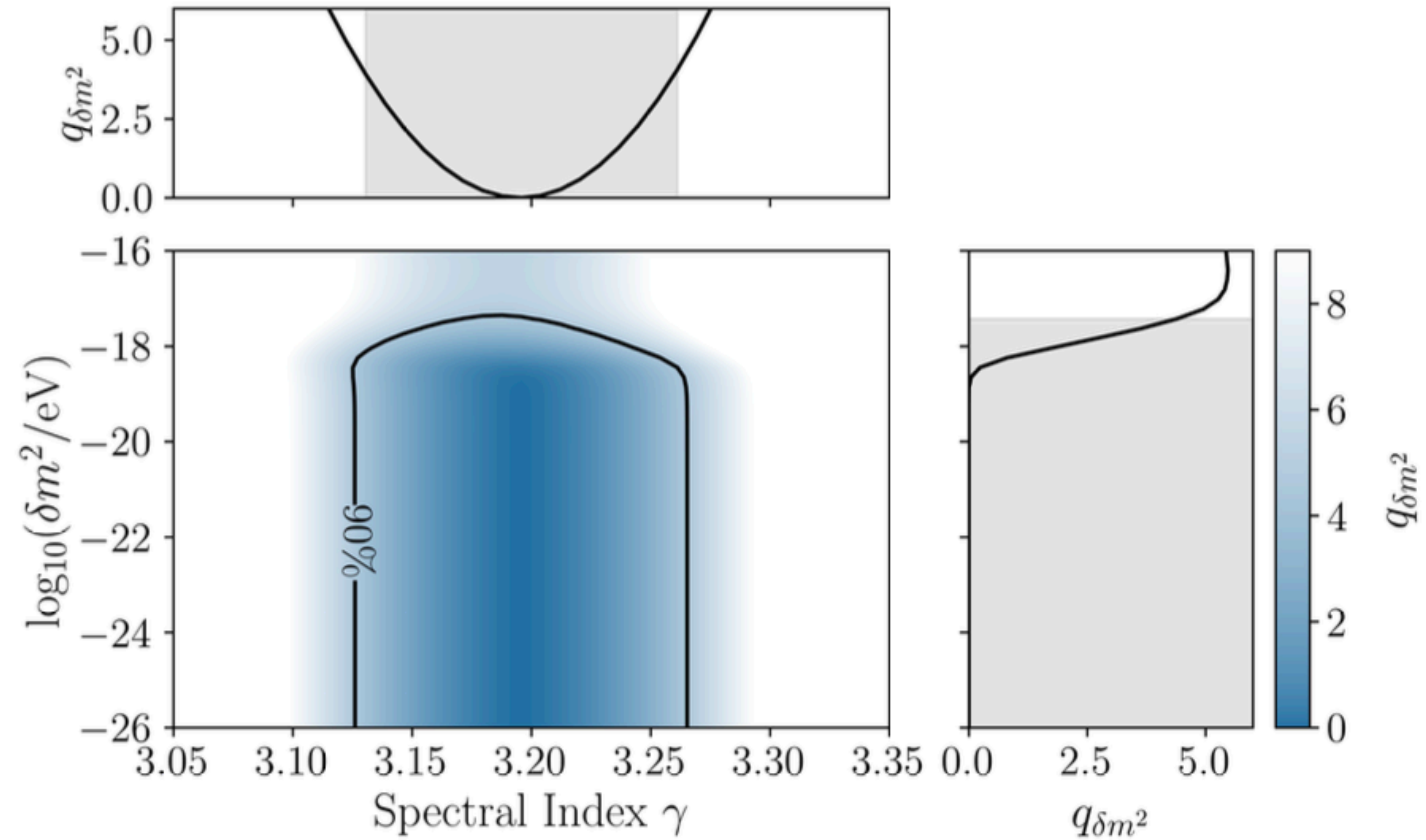
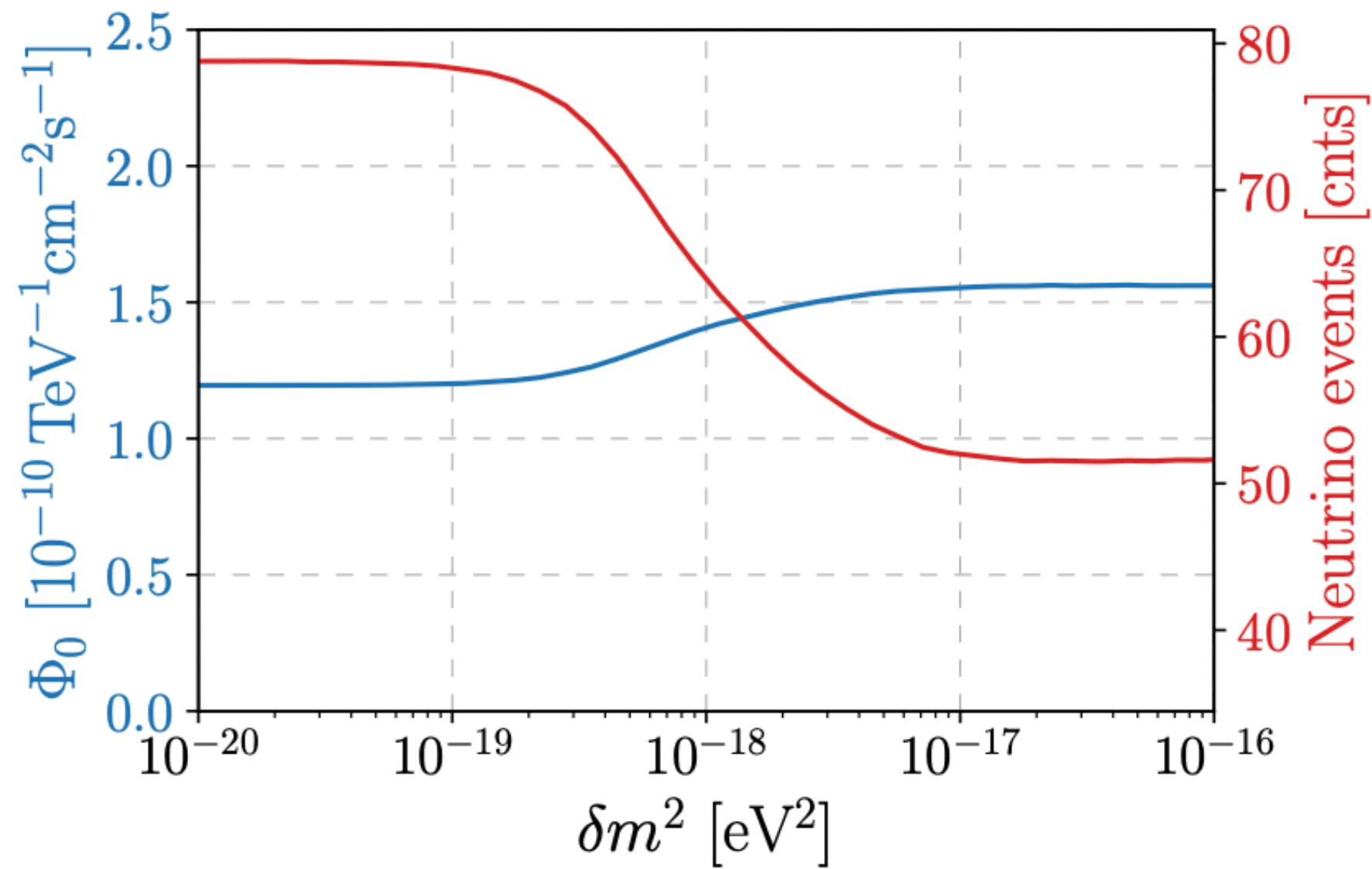
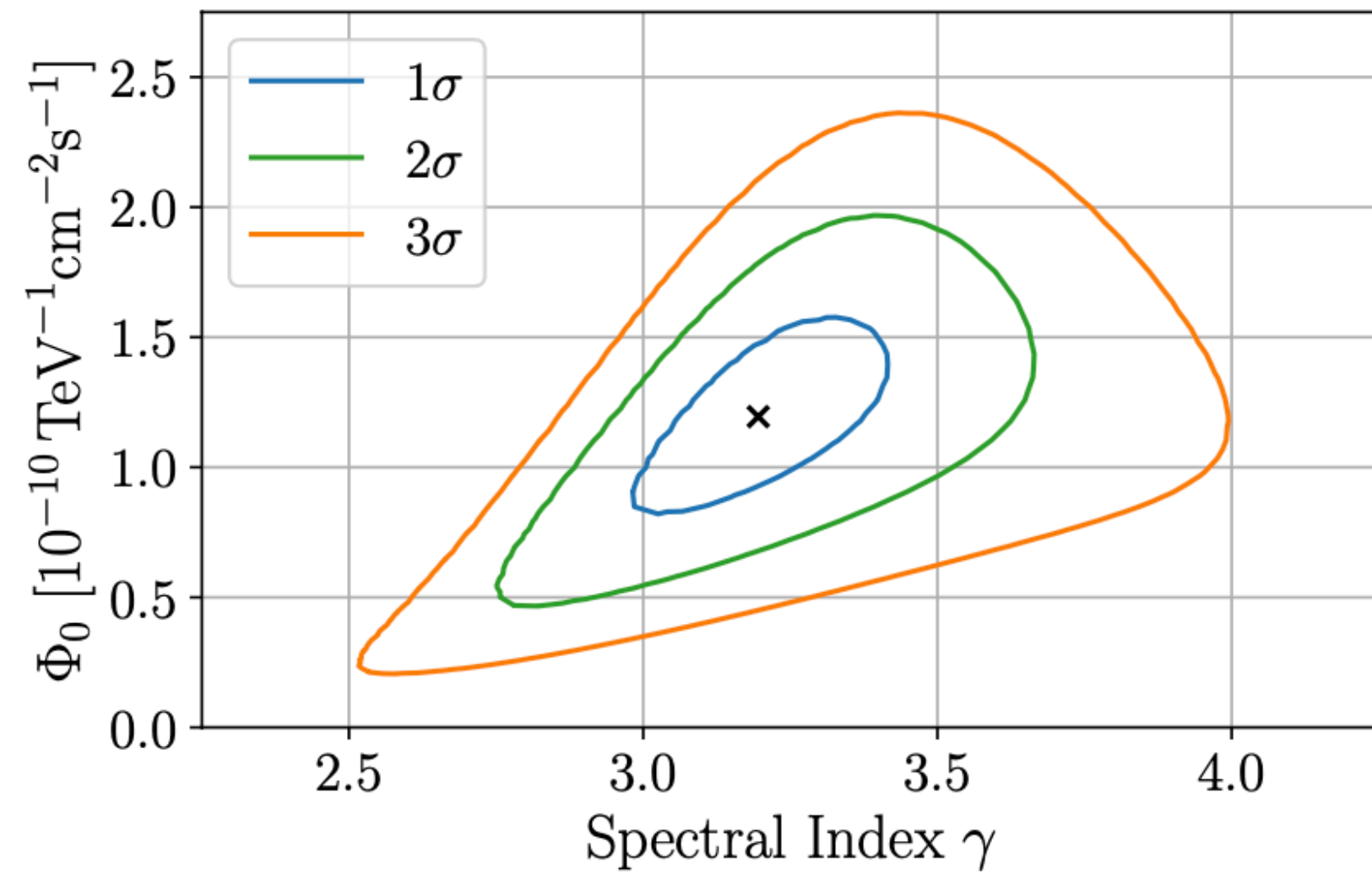


Increasing  $\delta m^2$  reduces  $L_{\text{osc}}$  and  $L_{\text{coh}}$ , and causes more oscillations

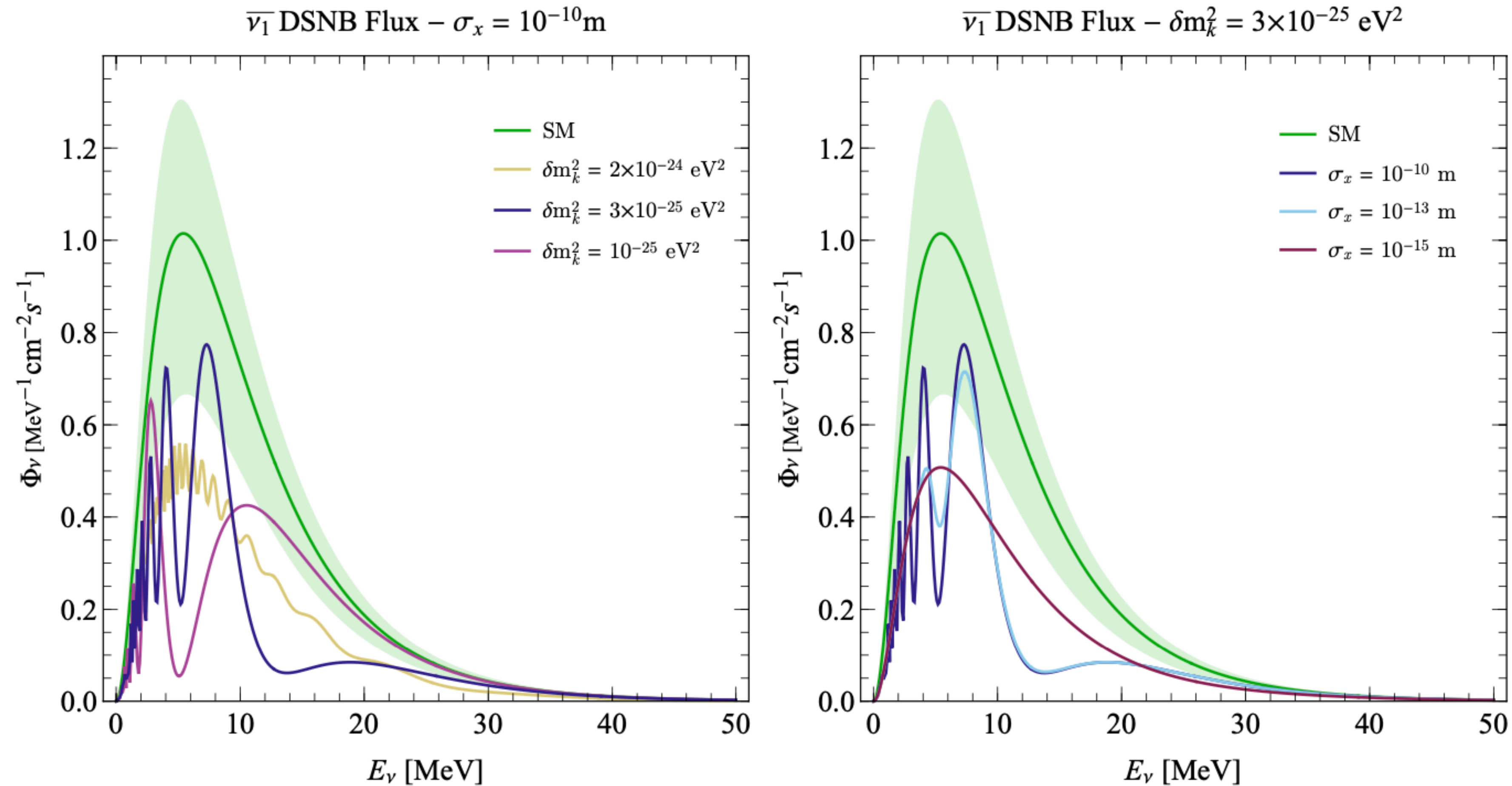
Decreasing  $\sigma_x$  reduces  $L_{\text{coh}}$ , and causes more decoherence



# Icecube: Oscillations due to pseudo-Dirac nature



# Oscillations due to pseudo-Dirac nature



Increasing  $\delta m^2$  reduces  $L_{\text{osc}}$  and  $L_{\text{coh}}$ , and causes more oscillations

Decreasing  $\sigma_x$  reduces  $L_{\text{coh}}$ , and causes more decoherence