

universität freiburg

# Boosting the production of sterile neutrino dark matter with self-interactions

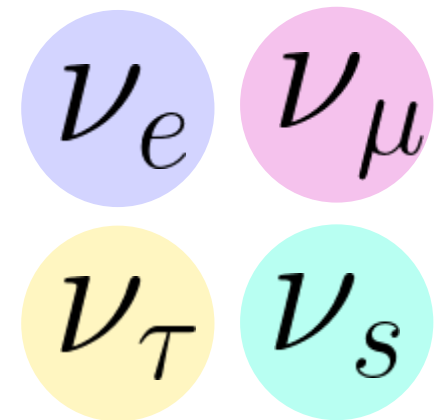
María Dias

Based on arXiv: 2307.15565

In collaboration with:  
Stefan Vogl  
TeVPA 2023, Napoli

# Sterile neutrinos as dark matter

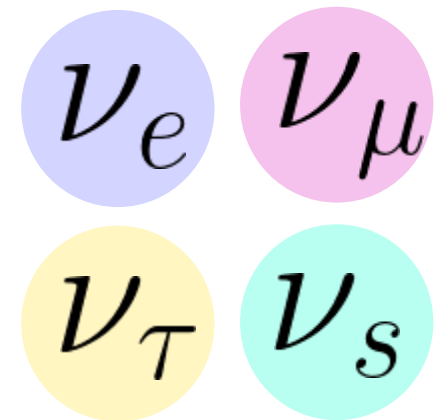
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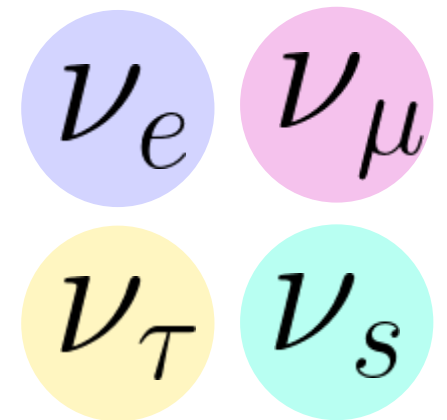


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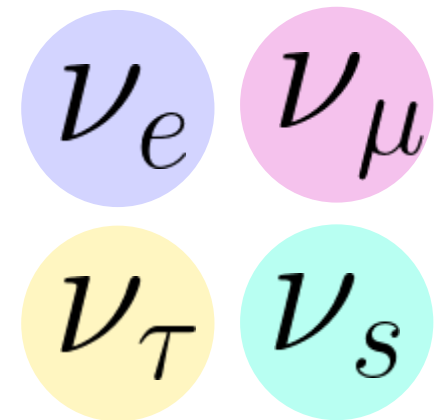
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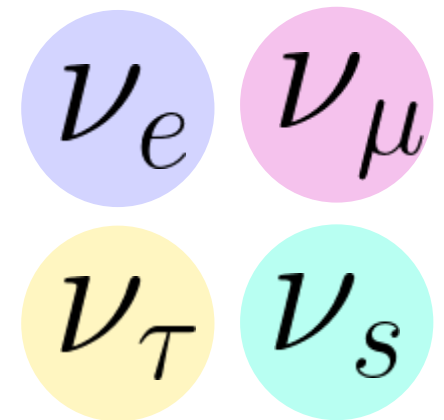
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Self-interactions

$$\mathcal{L}_{\text{int}} = y \bar{\nu}_s \nu_s \phi.$$

Johns and Fuller 1903.08296  
Bringmann et al. 2206.10630

# Production of sterile neutrinos

The evolution of the phase-space density of sterile neutrinos is given by the Boltzmann equation

$$\frac{\partial f_s}{\partial t} - H p \frac{\partial f_s}{\partial p} = \frac{\Gamma_t}{4} \left( \frac{\omega^2 \sin^2(2\theta)}{\omega^2 \sin^2(2\theta) + \frac{\Gamma_t^2}{4} + [\omega \cos(2\theta) - V_{\text{eff}}]^2} \right) [f_a - f_s] + \mathcal{C}_s$$

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Vacuum oscillation frequency  $\sim \frac{m_s^2}{2p}$

Active's distribution function



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↑ Sterile's distribution function  
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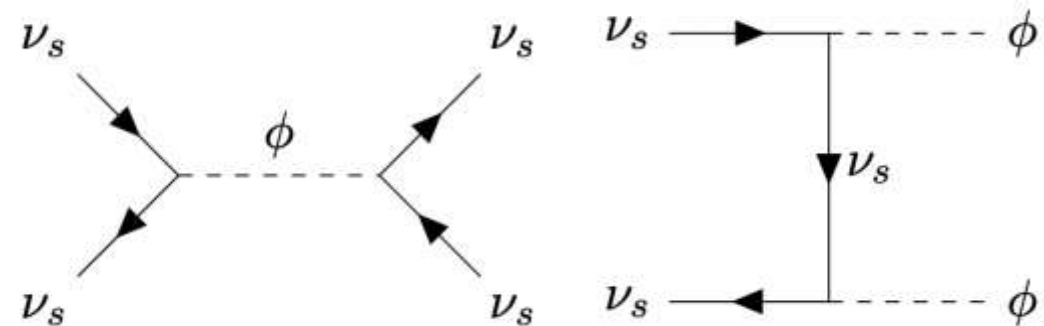
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↑ Active's distribution function  
↑ Sterile-sterile scattering processes

$$\Gamma_t = \Gamma_a + \Gamma_s$$



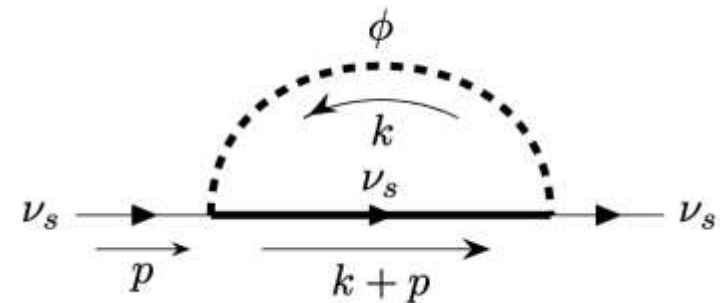
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Sterile's distribution function  $\frac{\partial f_s}{\partial t}$ 
Hubble's rate  $Hp$ 
Vacuum oscillation frequency  $\sim \frac{m_s^2}{2p}$   $\omega^2 \sin^2(2\theta)$ 
Vacuum mixing angle  $2\theta$ 
Total rate  $\frac{\Gamma_t^2}{4}$ 
Effective potential  $V_{\text{eff}}$ 
Active's distribution function  $f_a$ 
Sterile-sterile scattering processes  $\mathcal{C}_s$

$$V_{\text{eff}} = V_a - V_s$$



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Transition Probability

$$\langle P_m(\nu_a \leftrightarrow \nu_s) \rangle$$

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In-medium effective mixing angle

$$\sin^2(2\theta_m)$$

# Production regimes

What kind of behaviour can we expect from the system?

$$\frac{\partial f_s}{\partial t} - H_p \frac{\partial f_s}{\partial p} = \frac{\Gamma_t}{4} \left( \frac{\omega^2 \sin^2(2\theta)}{\omega^2 \sin^2(2\theta) + \frac{\Gamma_t^2}{4} + [\omega \cos(2\theta) - V_{\text{eff}}]^2} \right) [f_a - f_s] + \mathcal{C}_s$$

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Talk by Paul Frederik  
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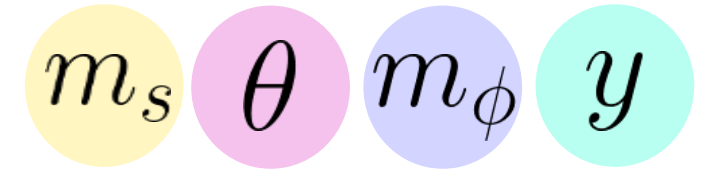


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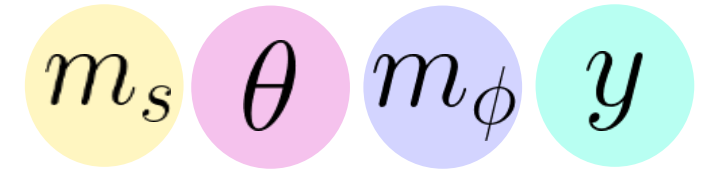
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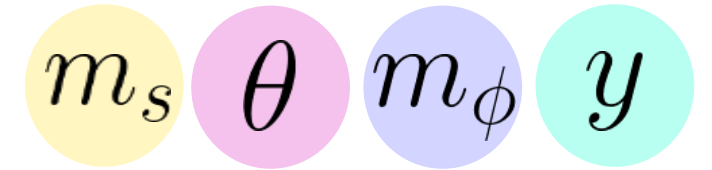
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- The mass of the sterile neutrinos
- The mixing angle

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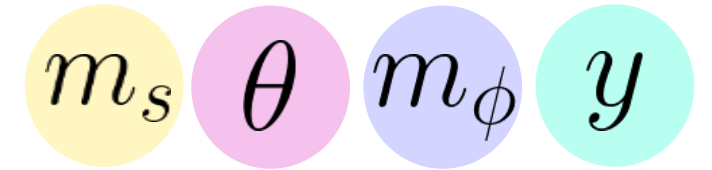
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- The mass of the sterile neutrinos
- The mixing angle
- The mass of the mediator



# Production regimes



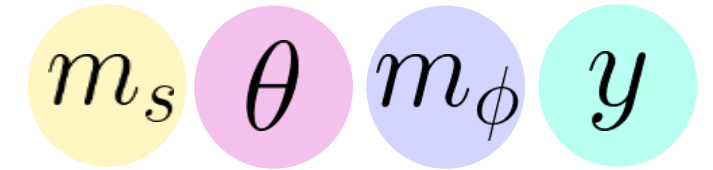
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- The mass of the sterile neutrinos
- The mixing angle
- The mass of the mediator
- The size of the Yukawa coupling


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- The mixing angle
- The mass of the mediator 
- The size of the Yukawa coupling

$$m_\phi \gg T$$

$$m_\phi \ll T$$

$$V_s < 0$$

$$V_s > 0$$

# Thermalization of the system

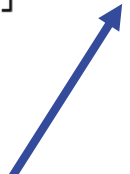
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$$\Gamma_{\nu_s \nu_s \leftrightarrow \phi \phi} f_s \left( 1 - \frac{f_s^2}{f_{\text{eq}}^2} \right)$$

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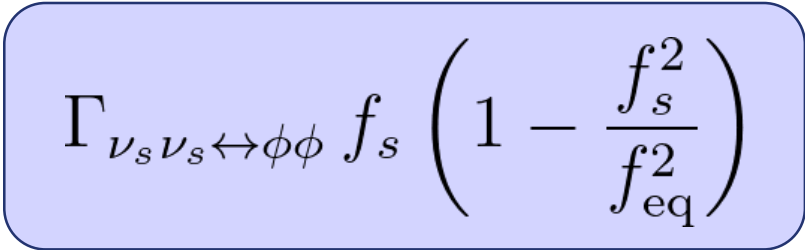
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$$\Gamma_{\nu_s \nu_s \leftrightarrow \phi \phi} f_s \left( 1 - \frac{f_s^2}{f_{\text{eq}}^2} \right)$$

The process stops itself



# Thermalization of the system

What role does the sterile collision term play?

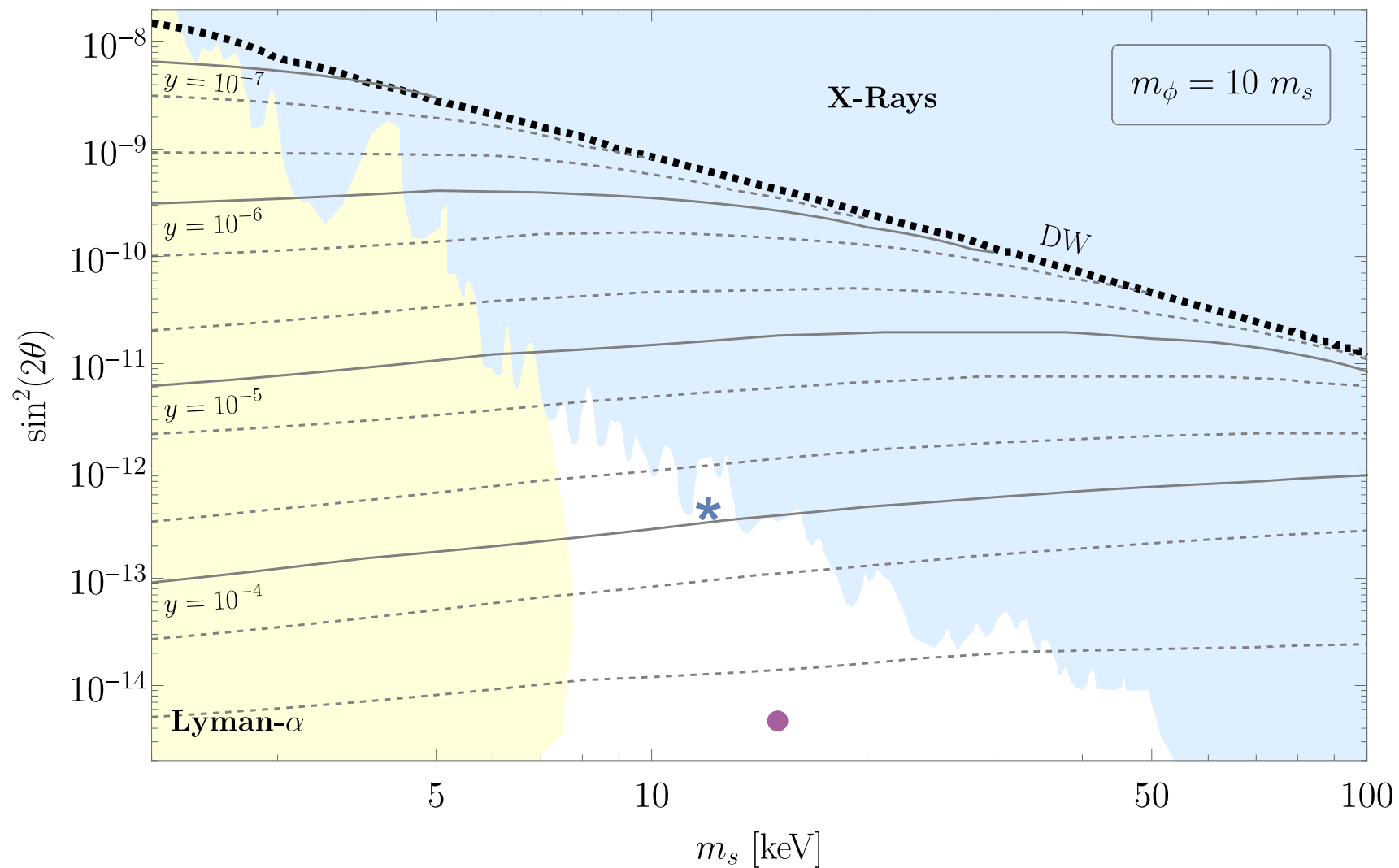
$$\frac{\partial f_s}{\partial t} - H p \frac{\partial f_s}{\partial p} = \frac{\Gamma_t}{4} \left( \frac{\omega^2 \sin^2(2\theta)}{\omega^2 \sin^2(2\theta) + \frac{\Gamma_t^2}{4} + [\omega \cos(2\theta) - V_{\text{eff}}]^2} \right) [f_a - f_s] + \mathcal{C}_s$$

- $\mathcal{C}_s$  tries to drive the system towards equilibrium
- The process  $\nu_s \nu_s \leftrightarrow \phi \phi$  essentially results in  $2\nu_s \rightarrow 4\nu_s$  upon the decay of  $\phi$
- The system will cool down

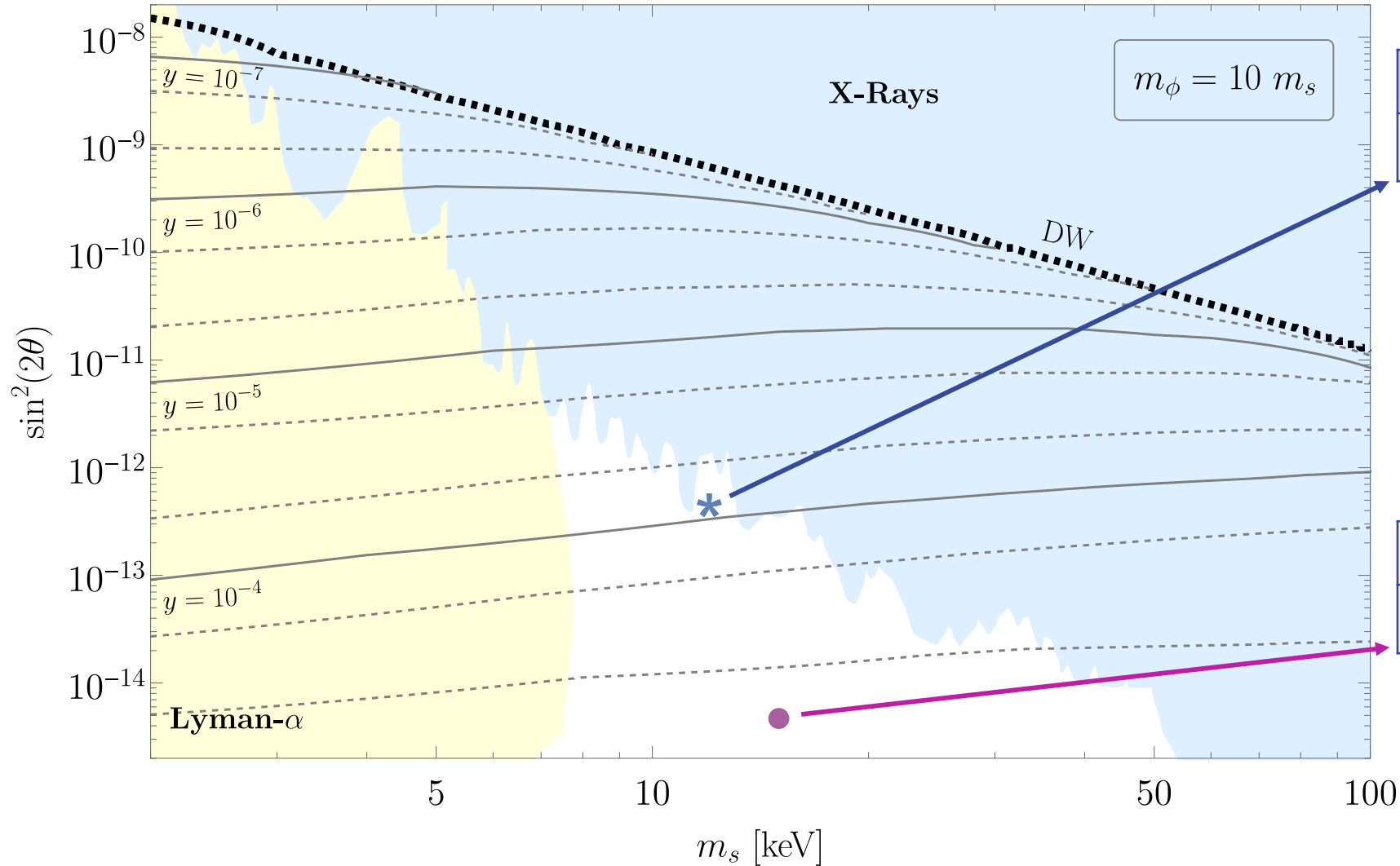
$$\Gamma_{\nu_s \nu_s \leftrightarrow \phi \phi} f_s \left( 1 - \frac{f_s^2}{f_{\text{eq}}^2} \right)$$

Only important for low and intermediate mediator masses

# The parameter space



# The parameter space



$m_s$	$\sin^2(2\theta)$
12 keV	$5 \times 10^{-13}$

$m_s$	$\sin^2(2\theta)$
15 keV	$4.68 \times 10^{-15}$

# One heavy-mediator benchmark



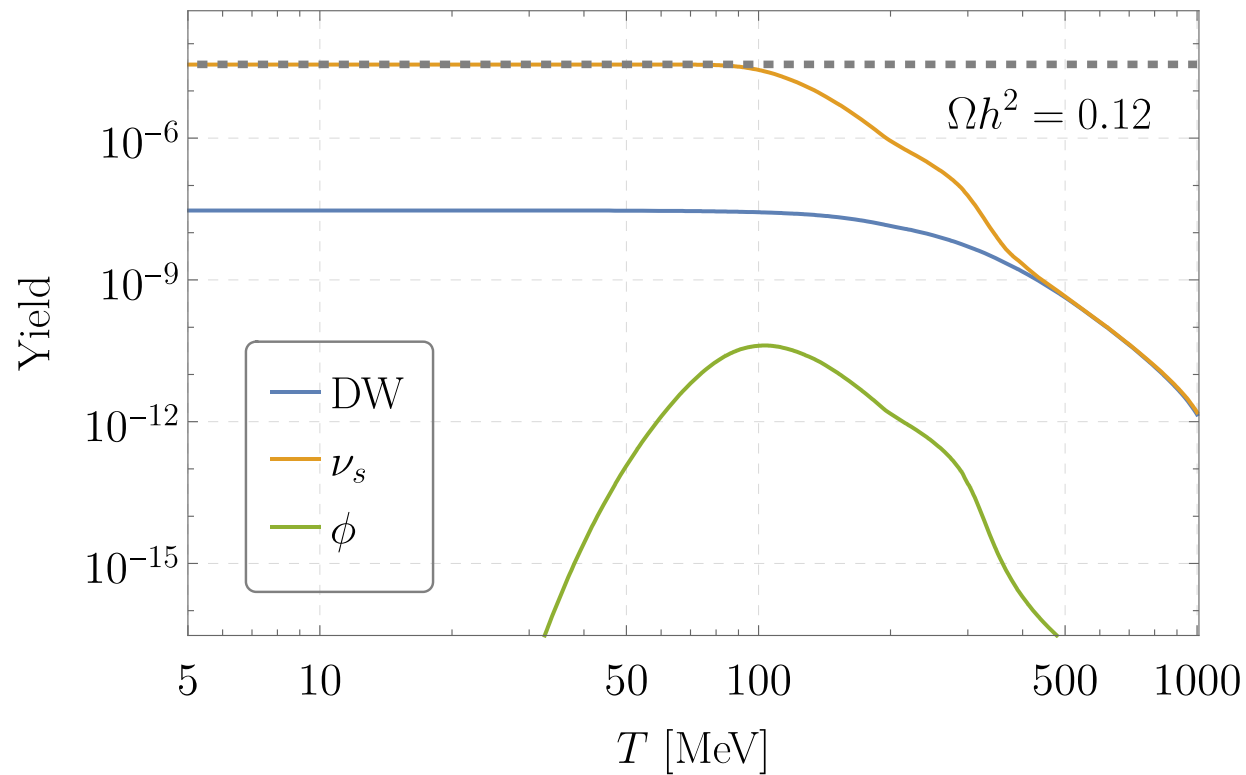
$m_s$	$m_\phi$	$y$	$\sin^2(2\theta)$
12 keV	1.5 GeV	$6.92 \times 10^{-2}$	$5 \times 10^{-13}$

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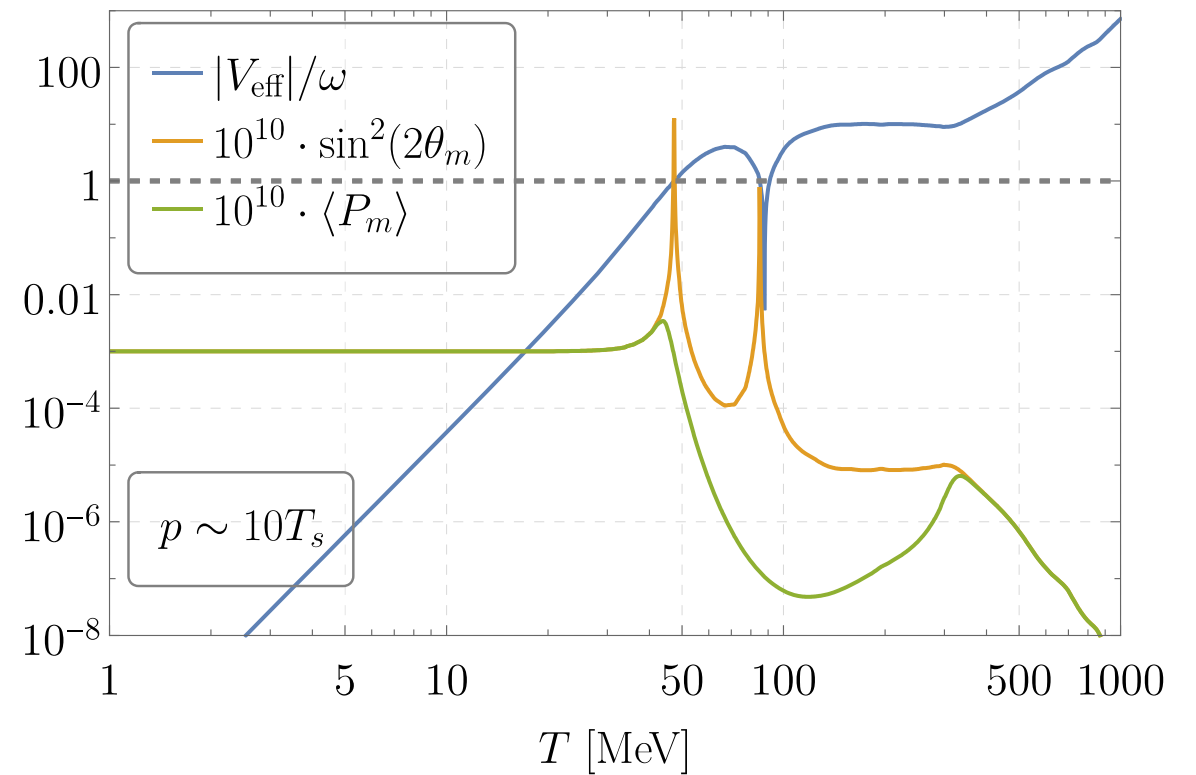
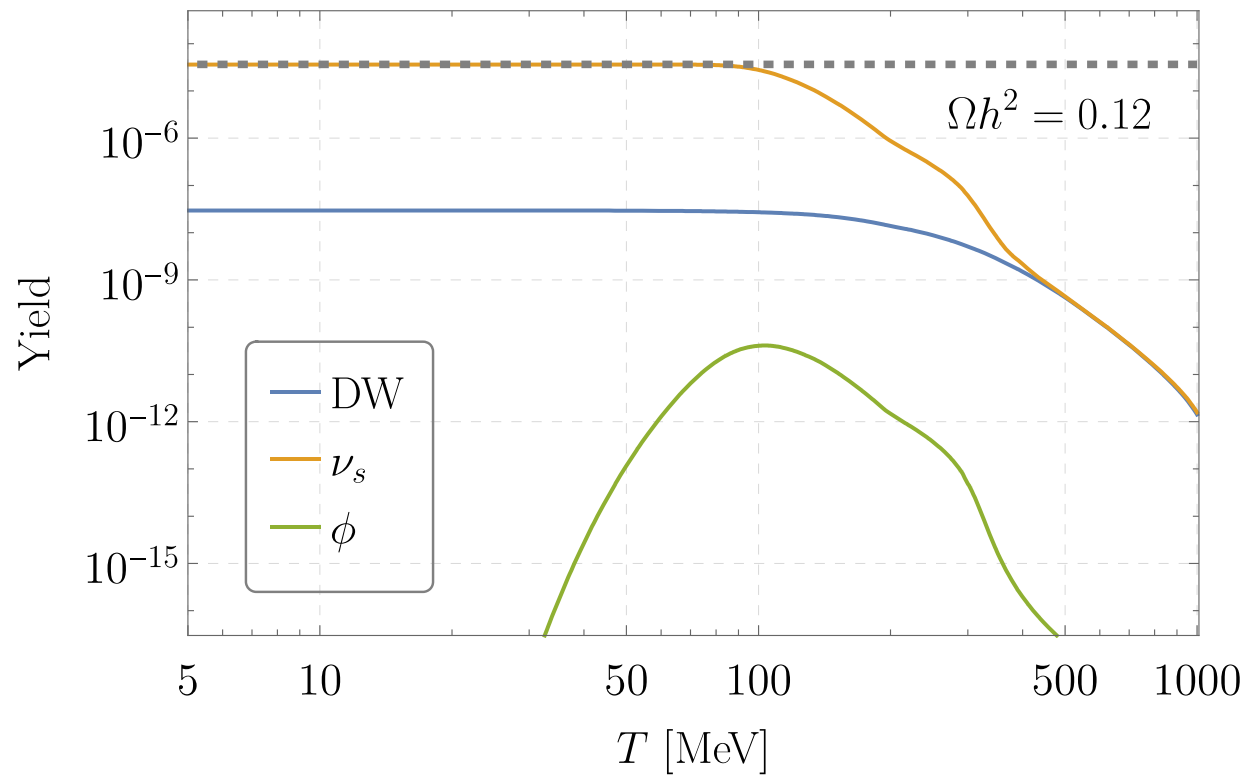
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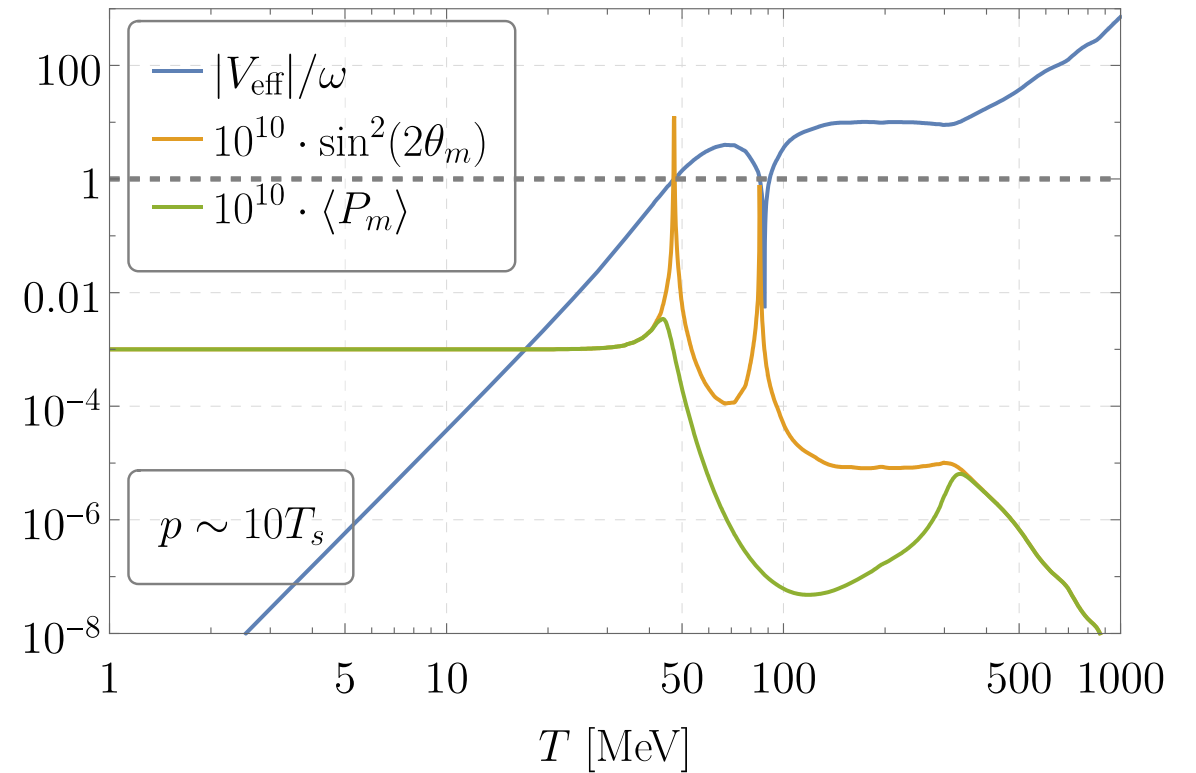


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→  $\omega \cos(2\theta) - V_a + V_s \approx 0$

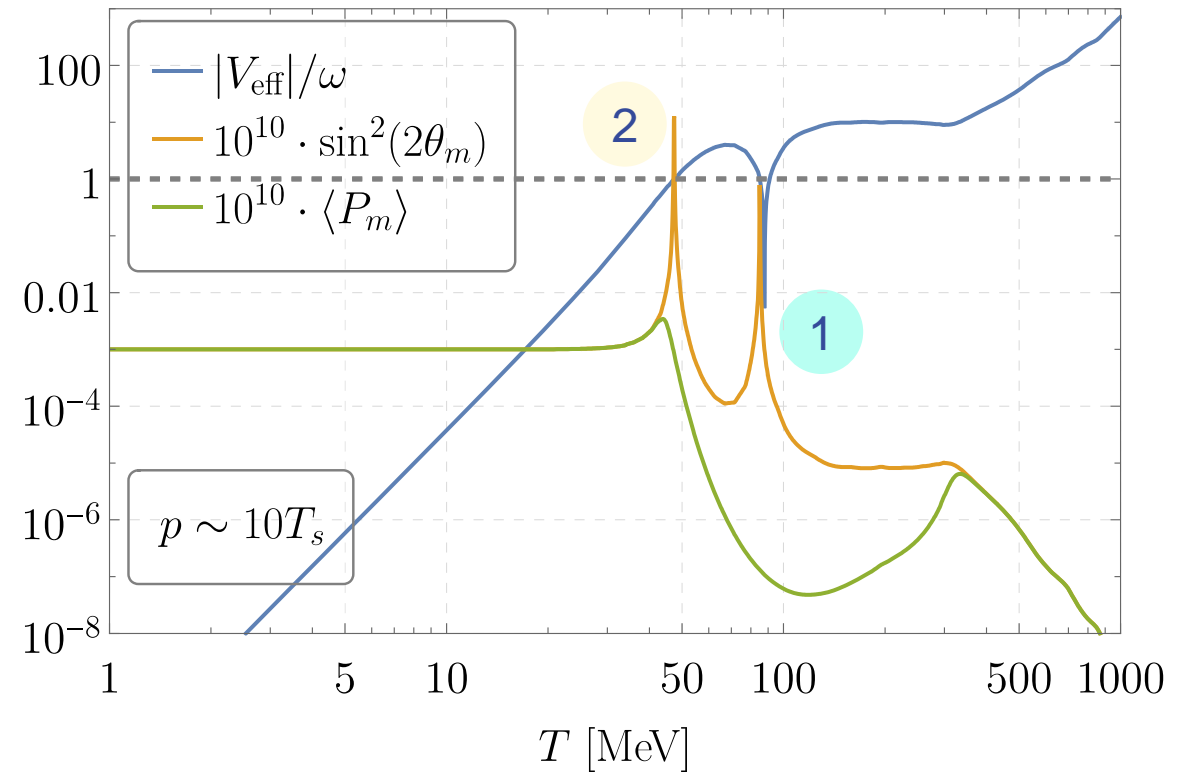


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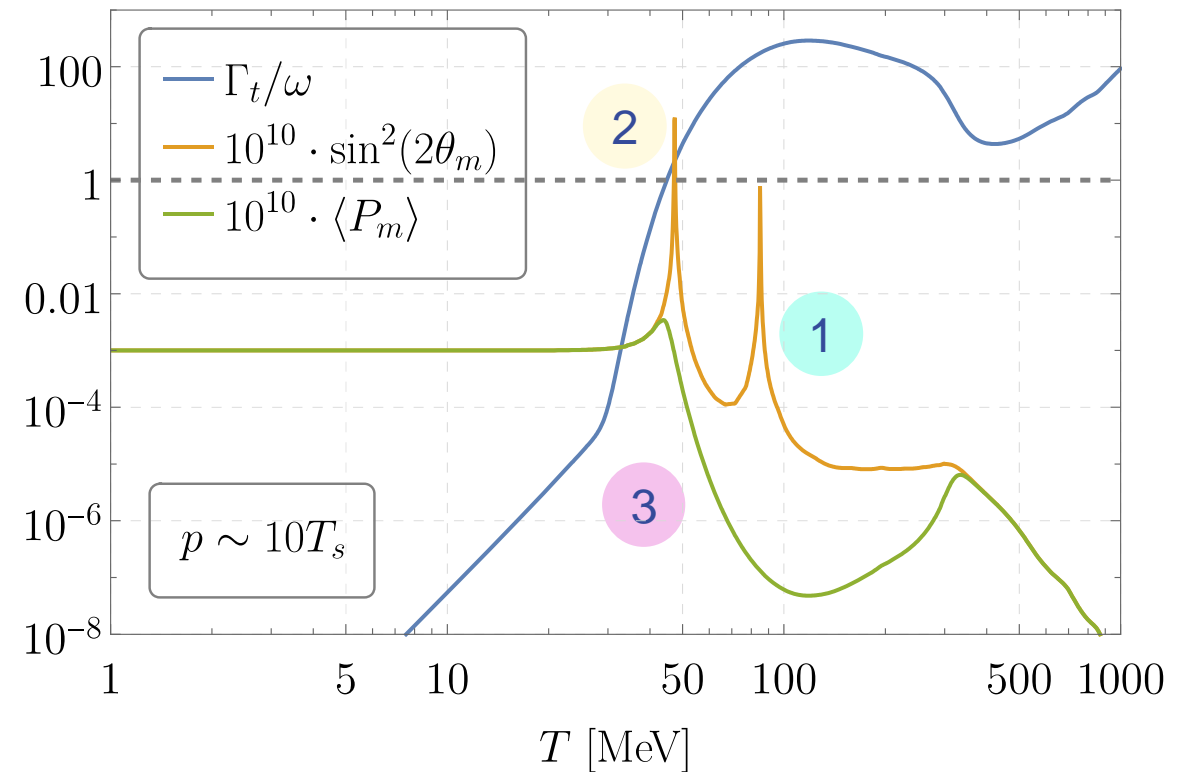


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➔  $\omega \cos(2\theta) - V_a + V_s \approx 0$

3 The resonances are regulated by quantum damping

$$\frac{\partial f_s}{\partial t} - Hp \frac{\partial f_s}{\partial p} \sim \frac{\omega^2 \sin^2(2\theta)}{\Gamma_t} [f_a - f_s] + \mathcal{C}_s$$



# A benchmark with partial thermalization

$m_s$	$m_\phi$	$y$	$\sin^2(2\theta)$
15 keV	150 keV	$7.5 \times 10^{-4}$	$4.68 \times 10^{-15}$



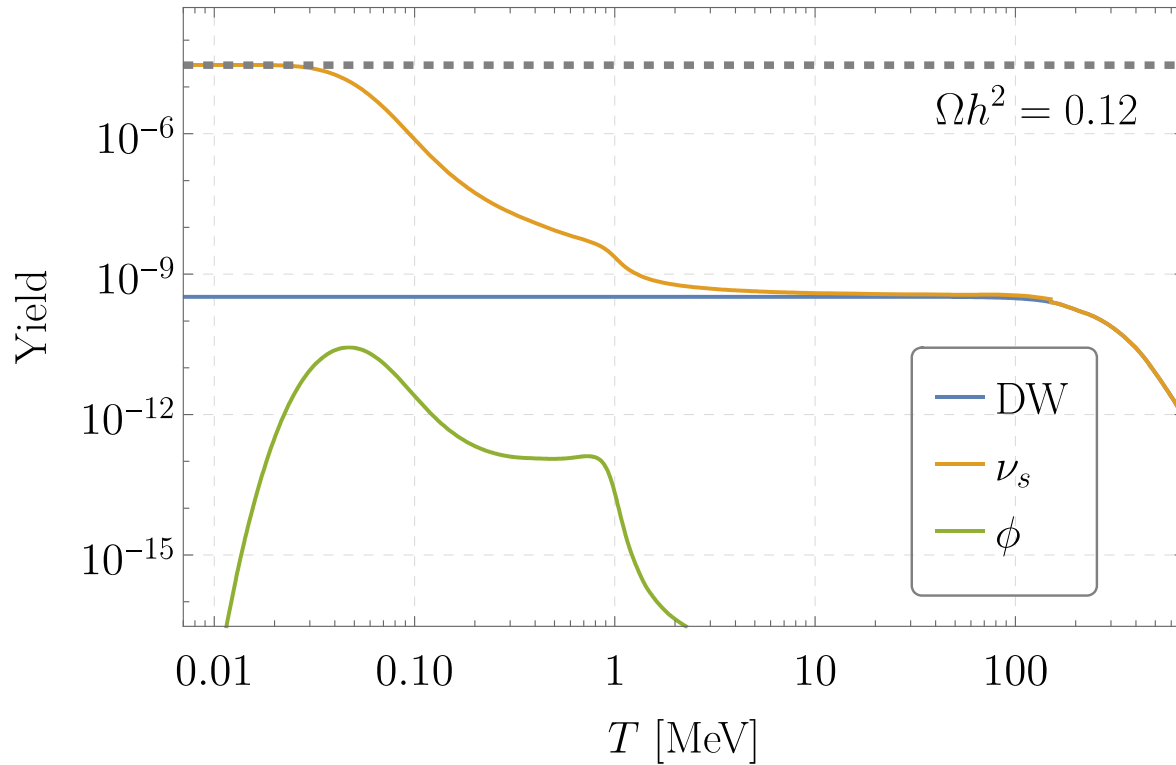
For lighter mediator masses, we expect the # changing processes to be important

# A benchmark with partial thermalization

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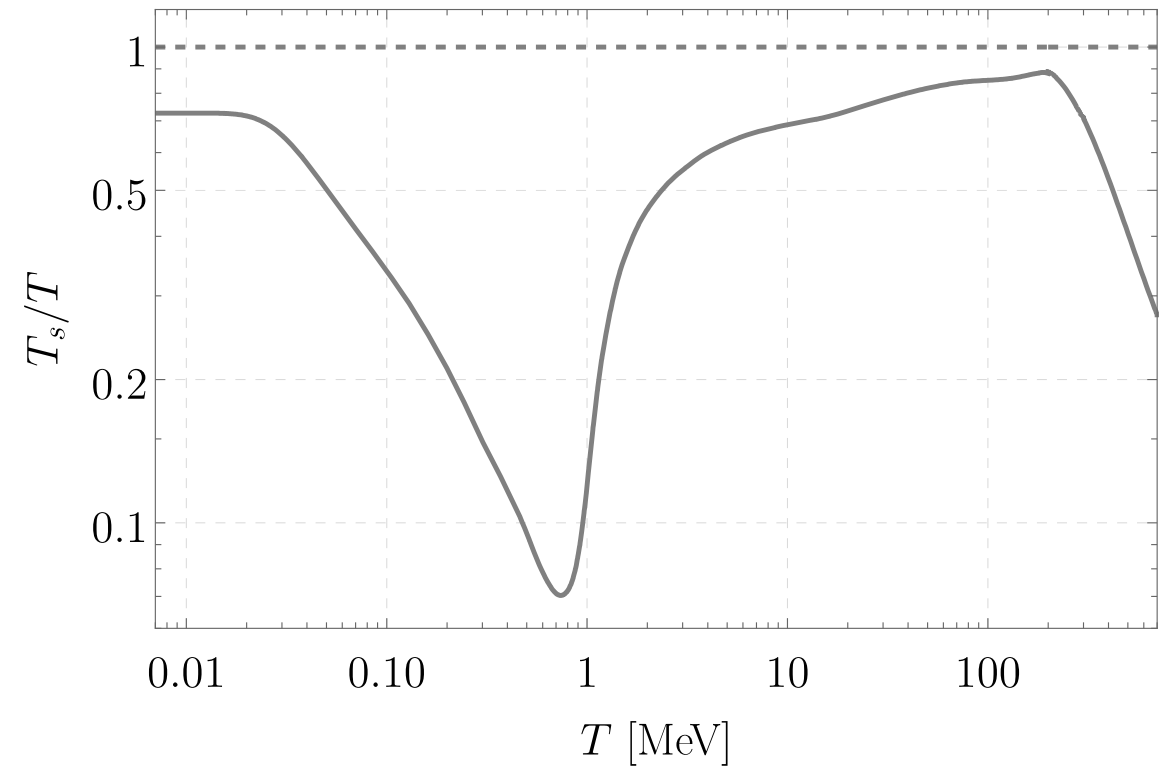
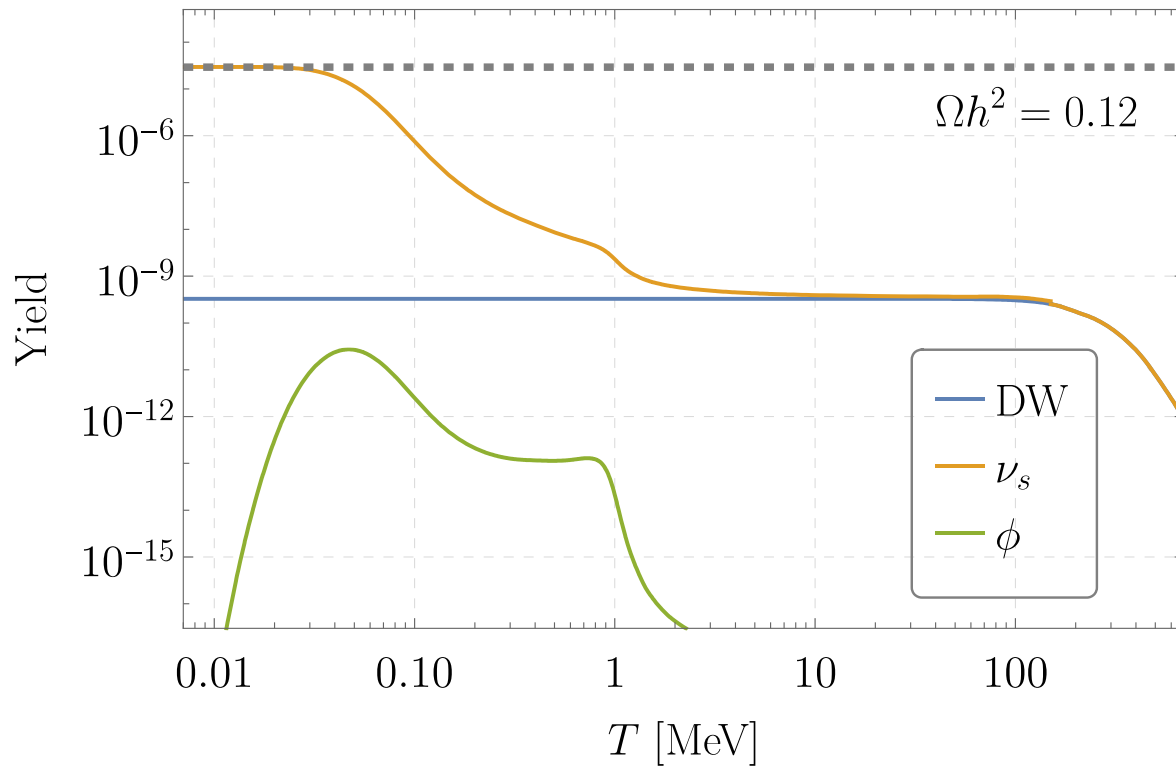
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# Overview of production regimes

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- Simplified Boltzmann equation
- Initial DW production

Bringmann et al. 2206.10630

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$$m_\phi \gtrsim 3 \text{ GeV}$$

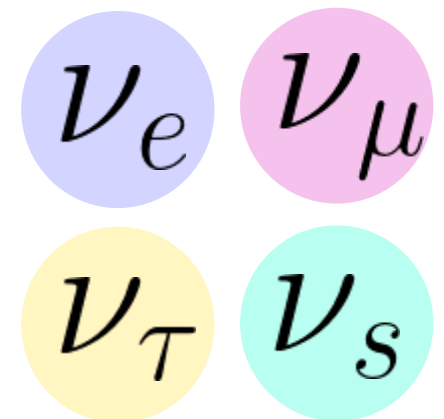
- Non-regulated resonances
- Runaway production

Johns and Fuller 1903.08296



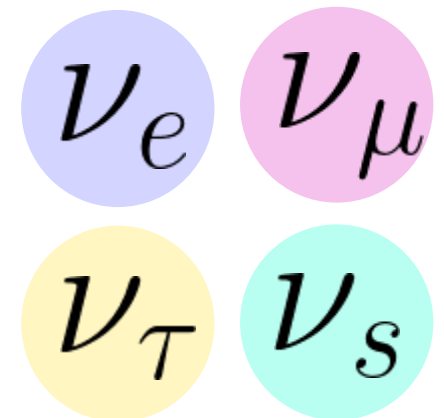
# Conclusions

- Sterile neutrinos are attractive BSM candidates



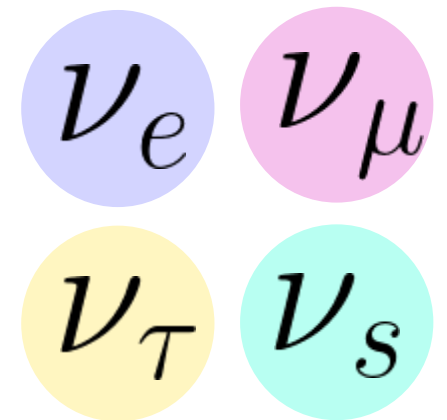
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# Conclusions

- Sterile neutrinos are attractive BSM candidates
- The canonical DW mechanism is mostly excluded
- Self-interactions among the sterile neutrinos can open new portions of parameter space



**Thank you for your attention**



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# Backup



# The rates



The rates are computed in the following way

$$\Gamma_{\nu_s \nu_s \leftrightarrow k k} = \frac{1}{2E_1} \int d\Pi_2 d\Pi_3 d\Pi_4 (2\pi)^4 \delta^4(p_i - p_f) |\mathcal{M}|_{\nu_s \nu_s \leftrightarrow k k}^2 f_s$$

The nine integrals can usually be reduced to two integrals that must be solved numerically

$$\Gamma_{\nu_s \nu_s \leftrightarrow \nu_s \nu_s} = \begin{cases} \frac{3y^4 T_s^2}{2\pi^3 p} e^{\frac{\mu}{T_s}} + \frac{y^2 T_s m_\phi^2}{2\pi p^2} e^{-\frac{m_\phi^2}{4pT_s} + \frac{\mu}{T_s}} & pT_s > \frac{3m_\phi^2}{2\sqrt{10}} \\ \frac{20y^4 p T_s^4}{3\pi^3 m_\phi^4} e^{\frac{\mu}{T_s}} + \frac{y^2 T_s m_\phi^2}{2\pi p^2} e^{-\frac{m_\phi^2}{4pT_s} + \frac{\mu}{T_s}} & pT_s \leq \frac{3m_\phi^2}{2\sqrt{10}} \end{cases}$$

# The potential



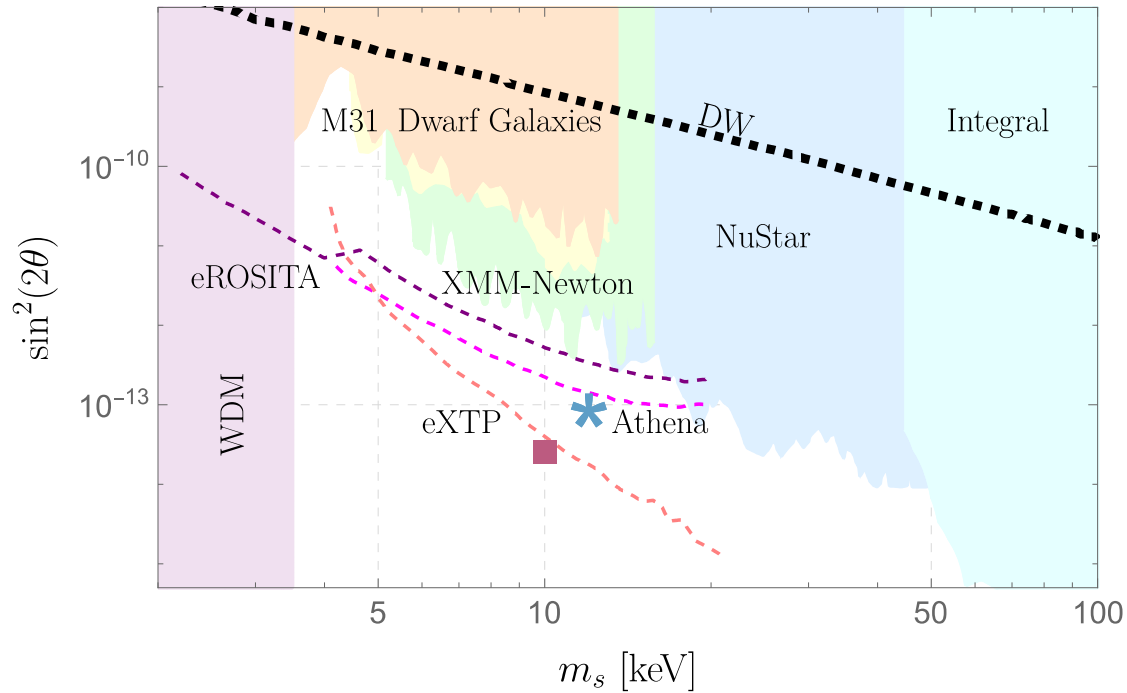
The potential modifies the dispersion relation of the SN

$$E = |\mathbf{p}| + \frac{m^2}{2|\mathbf{p}|} + V_{\text{eff}}$$

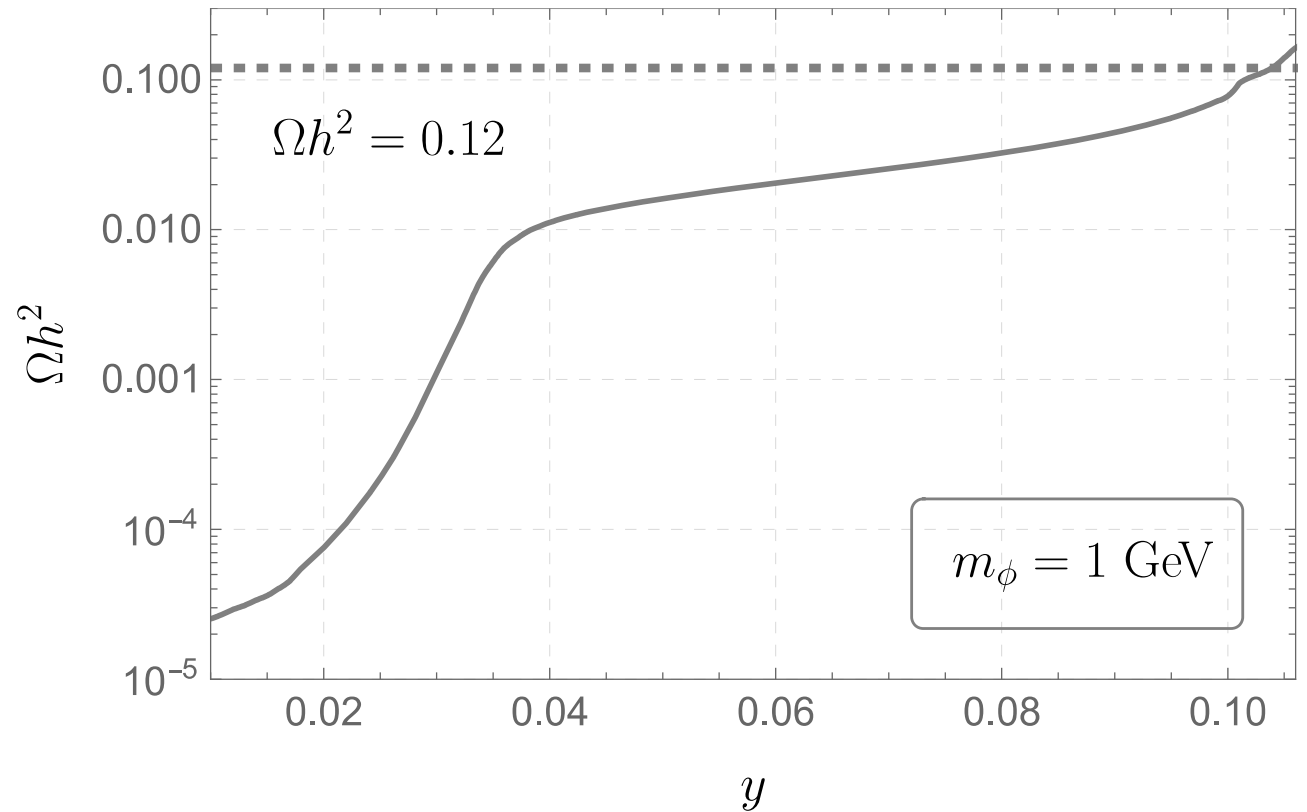
In the limiting cases the potential takes the form

$$V_s(p) = \begin{cases} \frac{y^2 T_s^2}{2\pi^2 p} e^{\frac{\mu_s}{T_s}} & T_s \gg m_\phi \\ -\frac{16y^2 p T_s^4}{\pi^2 m_\phi^4} e^{\frac{\mu_s}{T_s}} & T_s \ll m_\phi \end{cases}$$

# The parameter space



$m_s$	$\sin^2(2\theta)$
12 keV	$1 \times 10^{-13}$



➔ A heavy mediator implies a relatively large Yukawa



# Observational constraints

## X-ray searches

- The easiest observable decay for the SN is a one-loop process.

$$\Gamma_{\text{decay}} \sim \left[ \frac{\sin^2(2\theta)}{10^{-7}} \right] \left( \frac{m_s}{1 \text{ keV}} \right)^5$$



For keV sterile neutrinos, the resultant photon is in the X-ray band

- There are several searches for this type of decay

## Structure formation

- Sterile neutrinos are warm dark matter candidates.
- Structure will be smeared on scales below the free-streaming length of neutrinos.

