## Challenges for the dark-matter and dark-energy models that point towards a new model

#### in

Dark Energy: from fundamental theories to observations (and back) [Sept 11-15, 2023] 12th Sept 2023

Frascati

Pavel Kroupa Helmholtz-Institut für Strahlungs- und Kernphysik (HISKP) University of Bonn

> Astronomisches Institut, Charles University in Prague

c/o Argelander-Institut für Astronomie University of Bonn

Pavel Kroupa: Bonn & Charles University, Prague

# Outline :

- I)The inflation + cold/warm dark-matter + dark-energy Newtonian/Einsteinian standard model of cosmology (LCDM)
- II) The inflation + cold/warm dark matter + dark-energy Milgromian nuHDM model of cosmology (the nuHDM model)
- III) The inflation + cold/warm dark-matter + dark energy Bohemian model of cosmology (the BMoC)



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= a model that has equations of motion and which can be put into the computer with star formation to compute the formation of galaxies.





Do the observed (real) E galaxies contain stellar populations with the predicted large spread of ages ?

No!



Eappen et al. 2022 :

(orange points are central galaxies



Do the observed (real) E galaxies contain stellar populations with the predicted large spread of ages ?

This is in  $>5\sigma$  tension with E galaxies that form in a LCDM model universe (Eappen et al. 2022).

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Does the LCDM produce mostly disk galaxies ? No !



#### Does the LCDM produce mostly disk galaxies ? No!

#### LCDM falsified with >13 sigma.





Figure 4. Comparison between the observed distribution of  $q_{sky}$  and that produced by different cosmological ACDM simulations for galaxies with  $10.0 < \log_{10}(M_*/M_{\odot}) \le 11.65$ . The observed  $q_{sky}$  distributions (black and gray points with error bars) have been weighted based on the stellar mass distribution of the TNG50-1 run (shown in Figure 2). Invisible error bars (Equation 8) are smaller than the data point symbol. The total  $\chi^2$  values between the observed and simulated distributions (Equation 7) and the corresponding levels of tension are reported in Table 3. The TNG50-1, TNG100-1, Illustris-1, EAGLE50, and EAGLE100 computations shown here use 882, 6424, 6842, 480, and 3613 subhalos, respectively.

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# Thus, the galaxy population elliptical galaxy In LCDM, stars in model elliptical galaxies have ages ranging from <1Gyr to 13Gyr</td> and most model galaxies are spheroidal (elliptical-like), due to the buildup through many mergers.

disagreement

*In the real Universe*, <u>elliptical galaxies make < 5%</u> in number which is nearly constant over half the lifetime of the Universe.

In the real Universe, most (>90 %) of all galaxies are extended thin disk galaxies.

LCDM thus predicts a completely wrong fraction of elliptical galaxies and the stellar ages in real elliptical galaxies are completely different (>12Gyr).

Both failures of LCDM are individually at  $> 5\sigma$  confidence

Delgado-Serrano et al. 2010 Eappen et al. 2022 Haslbauer et al. 2022

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elliptical galaxy disk galaxy disk galaxy

The merger-driven buildup of galaxies in LCDM is in  $\gg 5\sigma$  disagreement with the observed population of galaxies.



then what about dark matter?

Does it even exist?

How can we test for dark matter?



#### How can one test for the existence of dark matter?

By construction of the standard cold- or warm-dark matter models, the dark matter particle interacts only gravitationally with ordinary matter.

> Any finite interaction cross section with dark-matter particles and particles from the Standard Model of Particle Physics must be negligible :

#### **Otherwise :**

- galaxies would look different (e.g. E galaxies in galaxy clusters), Gnedin & Ostriker 2001

- pre-CMB structure formation would be incompatible with the CMB, and
- no trace of a dark matter particle has been found in any experiment despite a very large world-wide effort under, on, and above the ground.

How can one test for the existence of such a dark matter particle ?

#### The LCDM model predicts each galaxy to be in a massive very extended dark matter halo.

This is due to each galaxy growing through many mergers.

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For a galaxy with a mass M<sub>bar</sub> in stars + gas, LCDM predicts the properties of its dark matter halo.



For a given galaxy, its dark-matter halo is thus known (within a well specified range of properties)



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Given these properties, we can test if the observed *satellite galaxies* (e.g. around our Milky Way) comply with these in terms of their *ages, stellar masses, position and velocity vectors.* 

As the satellite galaxy orbits, it induces a wake of dark matter particles behind itself, and this leads to *Chandrasekhar dynamical friction*, the strength of which depends on the *total mass of the satellite galaxy.* 

They must have fallen-in -- so, are there infall solutions ?

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#### The problem :

In the LCDM model, the observed satellite galaxies *must have* fallen-in.

That is, they must have come in from a large distance and get "stuck" (through dynamical friction) in the dark matter halo of the Milky Way

> So, are there infall solutions for the observed satellite galaxies of the Milky Way ?

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## LCDM predicts a new phenomenon :

If there is dark matter, then there must be Chandrasekhar dynamical friction.



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# Thus, if there is dark matter, then there must be Chandrasekhar dynamical friction.

The situation:



## **Prediction of new phenomenon :**

Thus, essentially:



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## Prediction of new phenomenon :

Thus, essentially:



# Newtonian plus dark matter calculations of the encounter of two disk galaxies



Wetzstein, Naab & Burkert 2007

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Chandrasekhar dynamical friction is very well understood.

e.g. Binney & Tremaine 1987 - textbook

## Chandrasekhar dynamical friction :

Orbits of satellite galaxies



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## **Chandrasekhar dynamical friction :**

 $M_{\rm DMhalo} < 5 \times 10^9 M_{\odot}$   $4_{\rm incompatible} M_{\rm DMhalo} > 10^{10} M_{\odot}$ 

Orbits of satellite galaxies









https://doi.org/10.1093/mnrasl/slac030

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#### The synchronized dance of the magellanic clouds' star formation history

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#### P. Massana<sup>(0)</sup>,<sup>1,2</sup>\* T. Ruiz-Lara<sup>(0)</sup>,<sup>3</sup>\* N. E. D. Noël,<sup>1</sup> C. Gallart,<sup>4,5</sup> D. L. Nidever,<sup>6</sup> Y. Choi<sup>(0)</sup>,<sup>7</sup>

J. D. Sakowska<sup>©</sup>,<sup>1</sup> G. Besla,<sup>8</sup> K. A. G. Olsen,<sup>9</sup> M. Monelli<sup>©</sup>,<sup>4,5</sup> A. Dorta,<sup>4</sup> G. S. Stringfellow<sup>©</sup>,<sup>10</sup> S. Cassisi,<sup>11,12</sup> E. J. Bernard,<sup>13</sup> D. Zaritsky<sup>©</sup>,<sup>8</sup> M.-R. L. Cioni<sup>©</sup>,<sup>14</sup> A. Monachesi<sup>©</sup>,<sup>15,16</sup> R. P. van der Marel<sup>7,17</sup> T. L. L. de Boer<sup>18</sup> and A. R. Walker<sup>19</sup>

#### ABSTRACT

We use the SMASH survey to obtain unprecedented deep photometry reaching down to the oldest main-sequence turn-offs in the colour-magnitude diagrams (CMDs) of the Small Magellanic Cloud (SMC) and quantitatively derive its star formation history (SFH) using CMD fitting techniques. We identify five distinctive peaks of star formation in the last 3.5 Gyr, at  $\sim$ 3,  $\sim$ 2,  $\sim$ 1.1,  $\sim$ 0.45 Gyr ago, and one presently. We compare these to the SFH of the Large Magellanic Cloud (LMC), finding unequivocal synchronicity, with both galaxies displaying similar periods of enhanced star formation over the past  $\sim$ 3.5 Gyr. The parallelism between their SFHs indicates that tidal interactions between the MCs have recurrently played an important role in their evolution for at least the last  $\sim$ 3.5 Gyr, tidally truncating the SMC and shaping the LMC's spiral arm. We show, for the first time, an SMC–LMC correlated SFH at recent times in which enhancements of star formation are localized in the northern spiral arm of the LMC, and globally across the SMC. These novel findings should be used to constrain not only the orbital history of the MCs but also how star formation should be treated in simulations.



Figure 2. Comparison of the global SFRs for the SMC (this work) and the LMC (Ruiz-Lara et al. 2020b). Vertical dashed lines link the peaks at 0.45, 1.1, 2, and 3 Gyr ago in the SMC to those of the LMC. The horizontal bars in the top panel show the width of the SFH enhancement. Uncertainties in the SFHs (shaded regions) were calculated as in Hidalgo et al. (2011) and Rusakov et al. (2021).

The LMC and SMC have peaks in the SFRs at very similar times because of their orbits about each other.

This constrains the number of close encounters the SMC had with the LMC

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The LMC and SMC have dark-matter halos according to the LCDM model and are integrated backwards in time (i.e. "the friction leads to an acceleration) assuming their observed position and velocity vectors (Gaia data).

#### Other applications of Chandrasekhar dynamical friction:

The bars of galaxies are too long Existence of dark matter halos falsified with  $> 5\sigma$  confidence Roshan, Ghafourian et al. 2021



The observed configuration of

no dark matter halos





The homogeneity (1 in 10-5) of the cosmic microwave background radiation (CMB) ==> smoothness at z=1100



In LCDM, the galaxy dark matter halos and galaxy groups are spheroidal and the model universe is very smooth (isotropic and homogeneous on scales > 100Mpc)

How spheroidal are real groups and how homogeneous and isotropic is the real Universe?

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## **Observed** :

A) The crystal-like Pawlowski et al. (2013) structure of the Local Group of Galaxies ( $\approx 3 \text{ Mpc}$  / the *PKJ structure*)

## Structure of and correlations in Local group

Frighteningly symmetric structure of the Local Group

Looking along the line between Milky Way and Andromeda Everything we know about the Local Group today :

Pawlowski, Kroupa & Jerjen (2013): "The discovery of symmetric structures in the Local Group"

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- B) The Keenan-Barger-Cowie (2013,  $\approx 600 \text{ Mpc}$ ) void (the *KBC void*)

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## **KBC** void and Hubble Tension

#### The Cosmological Scale

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Haslbauer, Banik & Kroupa 2020:

The under-density is evident in

optical galaxy surveys

Maddox+1990; Zucca+1997

near-infrared galaxy surveys

Keenan, Barger & Cowie'13 (KBC)

#### X-ray cluster surveys

Böhringer+2015; Böhringer, Chan, Collins 2020; Migkas+21

## CMB dipole indicating large-scale bulk flows as expected for such a void (radio observations)

Rubart & Schwarz 2013; Rubart, Bacon & Schwarz 2014; Javanmardi+ 2015; Secrest+ 2020

#### Additionally :

Strong evidence for highly significant over- and under-densities in galaxy-cluster data

Migkas & Reiprich (2018); Migkas et al. (2021)

4.9 sigma exclusion of cosmological principle based on distribution of 10<sup>6</sup> quasars Secrest+... Sarkar et al. (2021)



Figure 1. The KBC void: the actual density of normal matter divided by the mean cosmological density is plotted in dependence of the distance from the position of the Sun (which is in the Local Group of galaxies). The grey area indicates the density fluctuations allowed by the ACDM model. Taken from fig. 1 in Kroupa (2015).



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- C) The Haslbauer et al. (2023;  $\approx 5 \text{ Gpc}$ ) void (the *HKJ giga-void*)

#### Assume the $\approx 500$ galaxies in our 11Mpc neighbourhood are representative of all galaxies in the Universe. (cf: the stars in the Solar neighbourhood are representative of all stars in the Milky Way and in the Universe)

The 11 Mpc galaxies have nearly constant star formation histories. (*i.e.* present-day SFR  $\approx$  average SFR)

The maximum in the observed cosmic star-formation rate density near  $z \approx 1.8$ 

thus implies a massive matter-overdensity about 5 Gpc away



The real Universe is thus highly orderly structured on Mpc scales and highly inhomogeneous on all larger scales, up the the horizon (CMB hemispherical anisotropy) Schwarz et al. 2016



## Many tests made. All independent.

#### **E.g.**: (there are more tests)

#### I) Mutually independent tests for the existence of dark matter particles :

- The orbits of the Large and Small Magellanic Clouds Oehm+ 2023
- The lengths of galactic bars Roshan+ 2021
- The backsplash NGC3109 group of galaxies (at distance of a Mpc) Pawlowski&McGaugh 2018; Banik+2021
- The M81 group of galaxies (at distance of 3.6 Mpc) Oehm+ 2017
- No dark matter in dwarf galaxies in Fornax galaxy cluster Asencio+2022

II) Tests for the matter-distribution predicted by the dark matter models:

- Disks of Satellites around 6 nearby galaxies Kroupa+ 2005; Pawlowski+; Asencio+ 2022
- The 3d structure of the Local Group of galaxies (within one Mpc) Pawlowski+ 2013
- The KBC void (within one Gpc) Haslbauer+ 2020
- The Hubble Tension (within one Gpc) Haslbauer+ 2020
- The Lilly-Madau plot (5 Gpc scale) Haslbauer+ 2023
- The over-massive El Gordo galaxy cluster (8 Gyr away) Asencio+ 2021
- Bulk flows on cosmological scales Migkas+ 2021; Secrest +2022
- CMB anomalies (hemispherical power and temp. difference, lack of correlation on large angular scales, cold spot). Schwarz+ 2016

Based mostly on Chandrasekhar dynamical friction and dynamical dissipation

> Based on the predicted stochastic merger histories and large-scale homogeneity of matter distribution



Figure 8: The SMoC-Confidence Graph: the cumulative loss in confidence that the Standard Model of Cosmology (SMoC) is a valid description of nature. The numbers 1-20 are based on a previous review (Kroupa, 2012, [6]), where an original form of the current plot appeared. Black squares (1, 2, and 5, representing inflation, dark matter, and dark energy, respectively) are treated in the SMoC as "new physics", so they are not assigned a loss of confidence. Upward blue triangles indicate failures, still current, already recognized in [6], while downward blue triangles (T1–T8) represent newly identified tensions where the loss of confidence was computed formally, as presented in Section 2.2. From the same section come the possible tensions (pT1–pT5), shown with red circles. Wherever the loss of confidence was not computed formally, we assign a drop in confidence by 50%. The inset graph zooms into the falsifications up to 2012.



#### **Reminder :**

For understanding galaxies it is of paramount importance to know which law of gravitation is valid.

Newton derived Newtonian gravitation (1648) as an empirical law based only on Solar system data (discovery of Uranus : 1781, Neptune : 1846).

It is the non-relativistic limit of Einsteinian general relativity (EGR).

But: EGR was developed prior to 1916 based on the constraint that EGR must comply to Newtonian gravitation in the non-relativistic limit.

Galaxies were not understood in 1917:

- The Shapley-Curtis debate on the nature of spiral nebulae took place in 1920.

- The motion of matter in them -- the flat rotation curve -- was measured in the late 1930s (Andromeda).

By assuming Newtonian/Einsteinian gravitation to be valid beyond the Solar System,

physicists thus

extrapolated an empirical law by many orders of magnitude in spatial, mass and acceleration scale to a regime where independent tests are not available.

E.g. in Solar system we can test the law of gravitation with independent tests.

Nearly all existing theoretical work on the formation and evolution of galaxies is today based on this extrapolation.

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Gravitational theory, as today implemented in all computer simulations of galaxies and cosmology is Newtonian, *based on the belief,* that this empirical law remains valid despite an extrapolation in scale by many orders of magnitude from the Solar system to galaxies and beyond.

> Should one expect an empirical law to hold over an extrapolation of orders of magnitude ?



How to proceed?

# A clue is provided by the *radial--acceleration* data in galaxies

## **Disc galaxies**



Balance between gravitation and centrifugal force

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Balance between gravitation and centrifugal force

According to Newton :  $g_{
m N} = G \, {M_{
m baryons} \over r^2}$ 





#### **Disc galaxies**



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g = observed acceleration from rotation curve  $g_{\rm N} =$  expected acceleration from observed matter distribution







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 $\overrightarrow{\nabla} \cdot \overrightarrow{\nabla} \Phi = 4\pi G \rho$ The standard Poisson equation: This can be re-written in terms of the *p*-Laplace operator,  $\Delta_p u := \nabla \cdot (|\nabla u|^{p-2} \nabla u)$ , as  $\left(\frac{|\overrightarrow{\nabla \Phi}|}{a_o}\right)^{p-2} \overrightarrow{\nabla} \Phi = 4\pi G \rho$  $\overrightarrow{\nabla}$ . p=2standard Poisson equation above Newtonian gravitation p=3non-standard Poisson equation -8 Jan Pflamm-Altenburg which gravitational dynamics ?  $\vec{\nabla} \cdot \left( \frac{|\vec{\nabla} \vec{\Phi}|}{a_o} \vec{\nabla} \Phi \right) = 4\pi G \rho$ a<sub>0</sub>=1.2 10<sup>-10</sup> m/s<sup>2</sup> -9 -10 Sufficiently far from  $\rho$  can assume spherical log<sub>10</sub>(a<sub>kin.</sub>) symmetry - integrate using divergence theorem -11  $\left(\frac{\partial \Phi}{\partial r}\right)^2 = \frac{a_0 G M(< r)}{r^2}$ p=2 -12 Lelli et. al 2017  $a_{p=3} = \sqrt{a_0 a_{p=2}}$ -13 , -13 -12 -11 -10 -9 -8  $a_{\rm kin} = g (\text{from above})^{\log_{10}(g_{\rm bary})}$  $g_{\text{bary}} = g_{\text{N}} = \text{from above}$ 

Remember the standard Poisson equation:  $\nabla \cdot \nabla \Phi = 4\pi G \rho$ This can be re-written in terms of the *p*-Laplace operator,  $\Delta_p u := \nabla \cdot (|\nabla u|^{p-2} \nabla u)$ , as



Is there a Lagrangían formulatíon ?

## For fields :



AQUAL-MoND (Bekenstein & Milgrom 1984)

$$\mathcal{L} = \rho \Phi + \frac{a_0^2}{8\pi G} F\left(\nabla \Phi^2 / a_0^2\right)$$

from Jan Pflamm-Altenburg

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New universal law of gravitation



## **Conclusions :**

The many independent tests on few-pc to Gpc scales unambiguously show the dark-matter-based models to not be relevant for the Universe.

There is no dark matter.

Gravitation is compellingly Milgromian (and not Newtonian/Einsteinian).

The *nuHDM Milgromian cosmological model* that assumes inflation, sterile neutrinos as a hot-dark matter component, the CMB as the boundary condition and dark energy, appears to not describe the Universe.

A Milgromian cosmological model that avoids inflation, dark matter, dark energy appears to be very promising -- the Bohemian Model of Cosmology --

BMoC : laws of physics the same everywhere, but cosmological principle does not apply.

More on the details at another opportunity.

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# The END



#### *Milgromian Dynamics* from quantum mechanical processes in the vacuum

#### Kroupa et al. (2010), Appendix A (see Milgrom 1999):

"... an accelerated observer in a de Sitter universe (curved with a positive cosmological constant  $\Lambda$ ) sees a non-linear combination of the Unruh (1975) vacuum radiation and of the Gibbons & Hawking (1977) radiation due to the cosmological horizon in the presence of a positive  $\Lambda$ . Milgrom (1999) then defines inertia as a force driving such an observer back to equilibrium as regards the vacuum radiation (i.e. experiencing only the Gibbons-Hawking radiation seen by a non-accelerated observer). Observers experiencing a very small acceleration would thus see an Unruh radiation with a low temperature close to the Gibbons-Hawking one, meaning that the inertial resistance defined by the difference between the two radiation temperatures would be smaller than in Newtonian dynamics, and thus the corresponding acceleration would be larger. This is given by the formula of Milgrom (1983) with a well-defined transition-function  $\mu(x)$ , and  $a_0 = c (\Lambda/3)^{1/2}$ . Unfortunately, no covariant version (if at all possible) of this approach has been developed yet."

Loosely speaking (and speculating):

In curved space-time around a particle (itself composed of fluctuations in the vacuum), the side that is more curved ("distorted, squashed-up") exerts a smaller pressure on the particle, than the other, less-"squashed" side, because a less-squashed side can sustain more vibrational modes (larger spatial volume). In non-curved space, the pressure from the vacuum is symmetrically smaller.

(i.e. essentially the Cassimir effect)

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Can MOND cosmology account for the CMB?



**Figure 1.** The CMB angular power spectrum for our cosmological model (blue line), compared with the  $\Lambda$ CDM model (red line). The data points come from *WMAP* 7 year (black), Atacama Cosmology Telescope (ACT) (turquoise) and ACBAR (green).

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## The relativistic-MOND model of cosmology also accounts for the CMB



Skordis & Zlosnik (Phys. Rev. Letters, 2021)

FIG. 1. The CMB temperature (T)  $C_{\ell}^{TT}$  and *E*-mode polarization  $C_{\ell}^{EE}$  angular power spectra for  $\Lambda$ CDM and this theory for a collection of functions and parameter values. The  $\Lambda$ CDM parameters are angular acoustic scale  $100\theta_s = 1.04171$ , DM density  $\Omega_c h^2 = 0.1202$ , baryon density  $\Omega_b h^2 = 0.02235$ , reionization optical depth  $\tau = 0.049$ , helium fraction  $Y_{\text{He}} = 0.2422$ , primordial scalar amplitude  $10^9 A_s = 2.078$ , and spectral index  $n_s = 0.963$ , while the MOND curves deviate from these within  $\sim \{0.07, 0.33, 3.98, 14.29, 1.57, 0.58, 2.60\}\%$ . MOND models have  $\lambda_s = \infty$ , and their other parameters are shown in the  $C_{\ell}^{TT}$ panel, with  $Q_0$  and  $Z_0$  in  $Mpc^{-1}$ . The "Higgs-like" function parameters are incompatible with a MOND limit.