Theory uncertainties affecting m_W measurements

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SWISS NATIONAL SCIENCE FOUNDATION

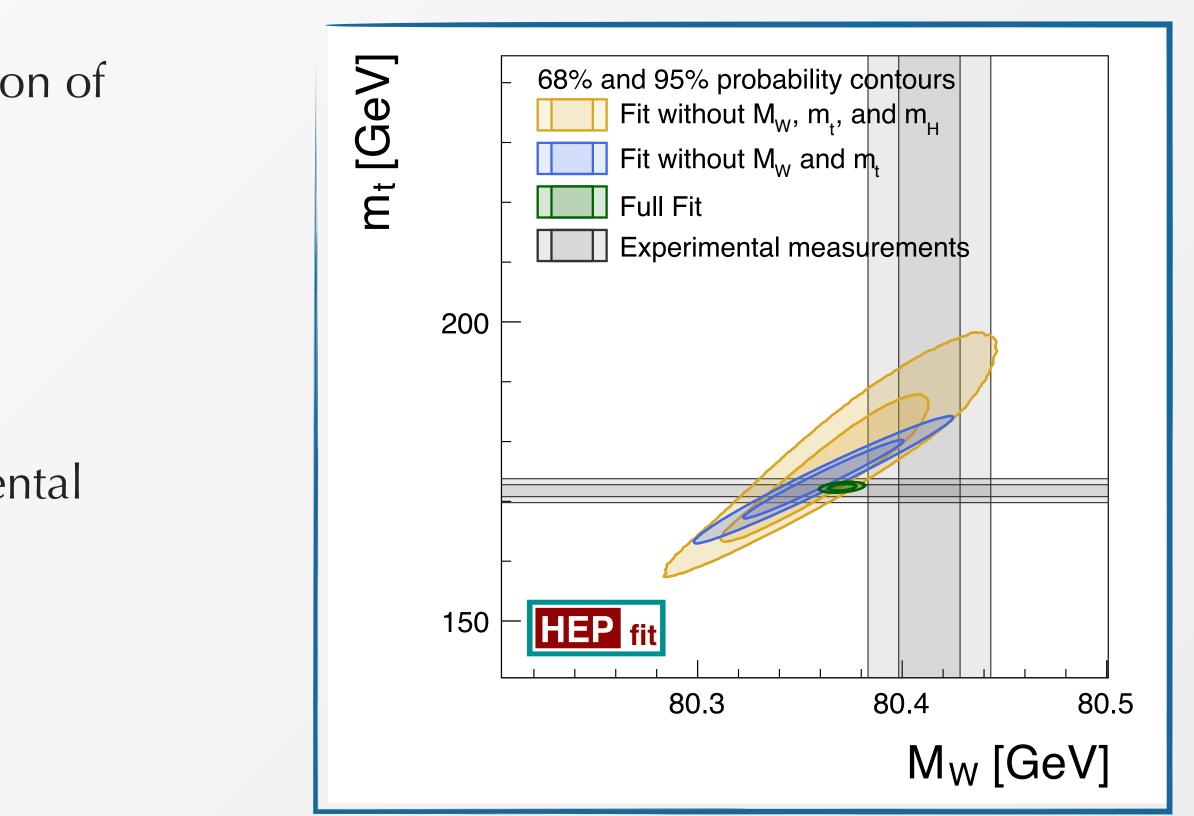
The discovery of the Higgs boson and the measurement of its mass allow for the prediction of the *W* mass with high precision

 $m_W = 80.350 \pm 8 \,\mathrm{GeV}$

Which is in a 2σ agreement with the experimental average (pre-CDF II)

 $m_W = 80.385 \pm 15 \,\mathrm{GeV}$

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[de Blas, Pierini, Reina, Silvestrini '22]





0.231

Full kinematics of **charged DY production** is not accessible at hadron colliders; in particular, the invariant mass of the neutrino-lepton pair cannot be reconstructed

Reconstruction possible in the transverse plane (requires precise measurement of the hadronic recoil) such as the lepton transverse momentum p_T^{ℓ} or the transverse mass $m_T = \sqrt{2p_T^{\ell}p_T^{\nu}(1 - \cos \Delta \phi_{\ell\nu})}$

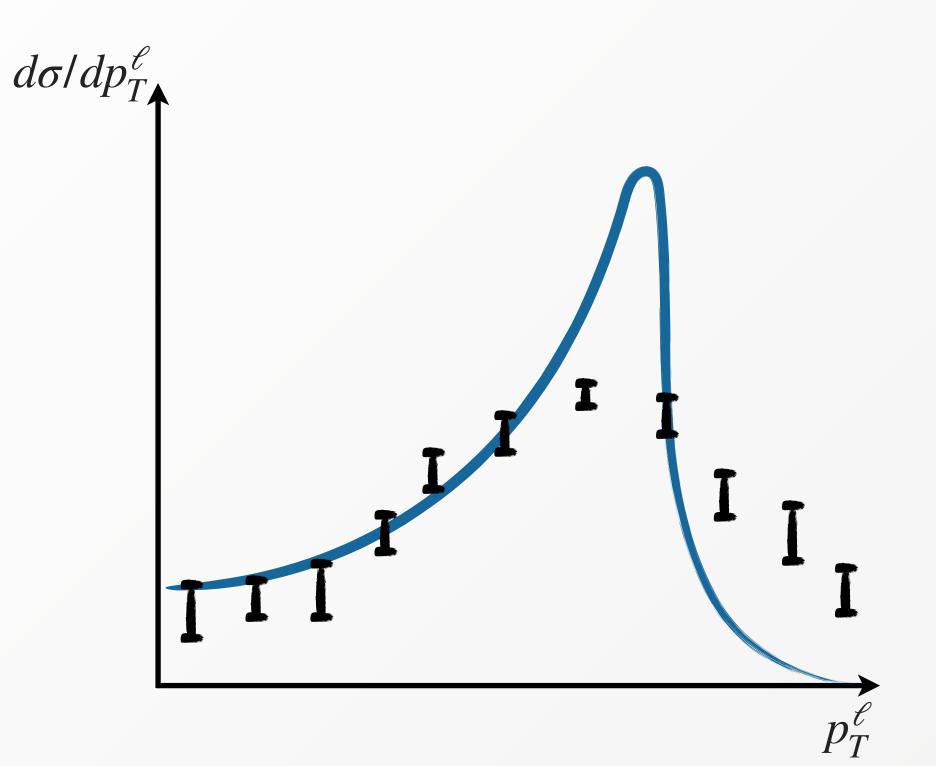
$$\frac{d\sigma}{d|p_T^{\ell}|^2} \sim \frac{1}{\sqrt{1 - 4\frac{|p_T^{\ell}|^2}{\hat{s}}}} \sim \frac{1}{\sqrt{1 - 4\frac{|p_T^{\ell}|^2}{m_W^2}}} \qquad \text{Jacobian peak at } p_T^{\ell} \sim m_W/2$$

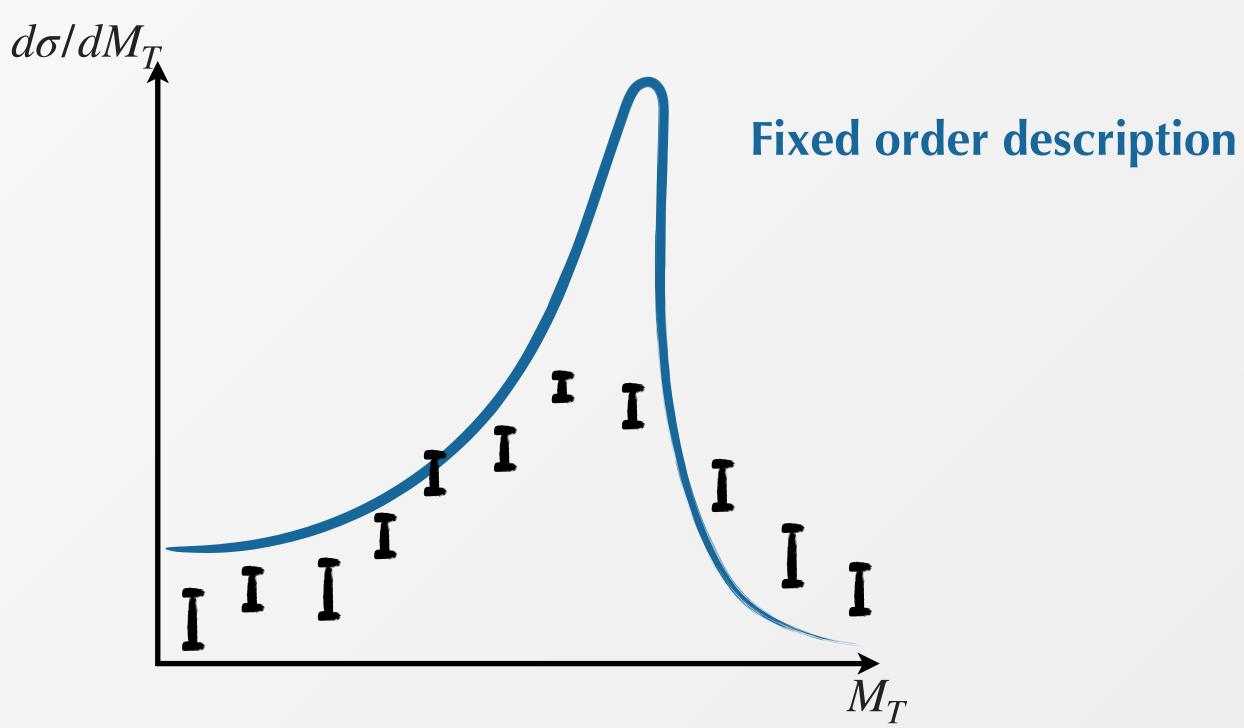
Enhanced sensitivity to m_W in both distributions at the $\mathcal{O}(10^{-3}) - \mathcal{O}(10^{-2})$ level.

Precise determinations of the W mass exploit observables with high sensitivity to small variations $\mathcal{O}(10^{-4})$ of m_W ,



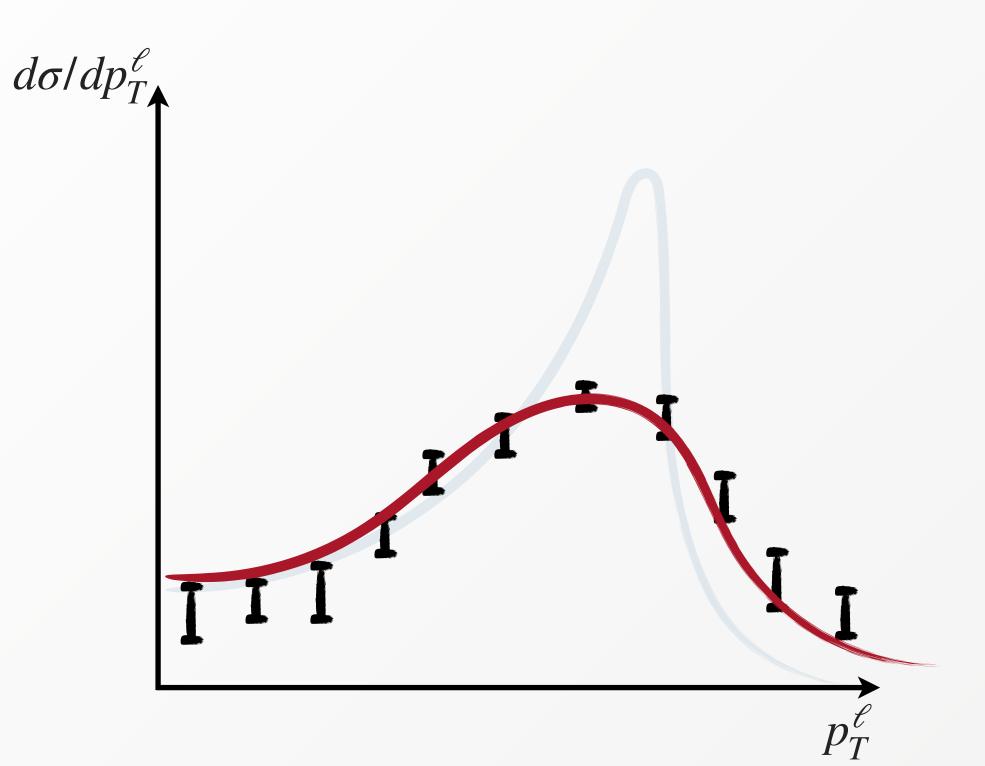
Different sensitivity to experimental uncertainties and quality of theoretical modelling





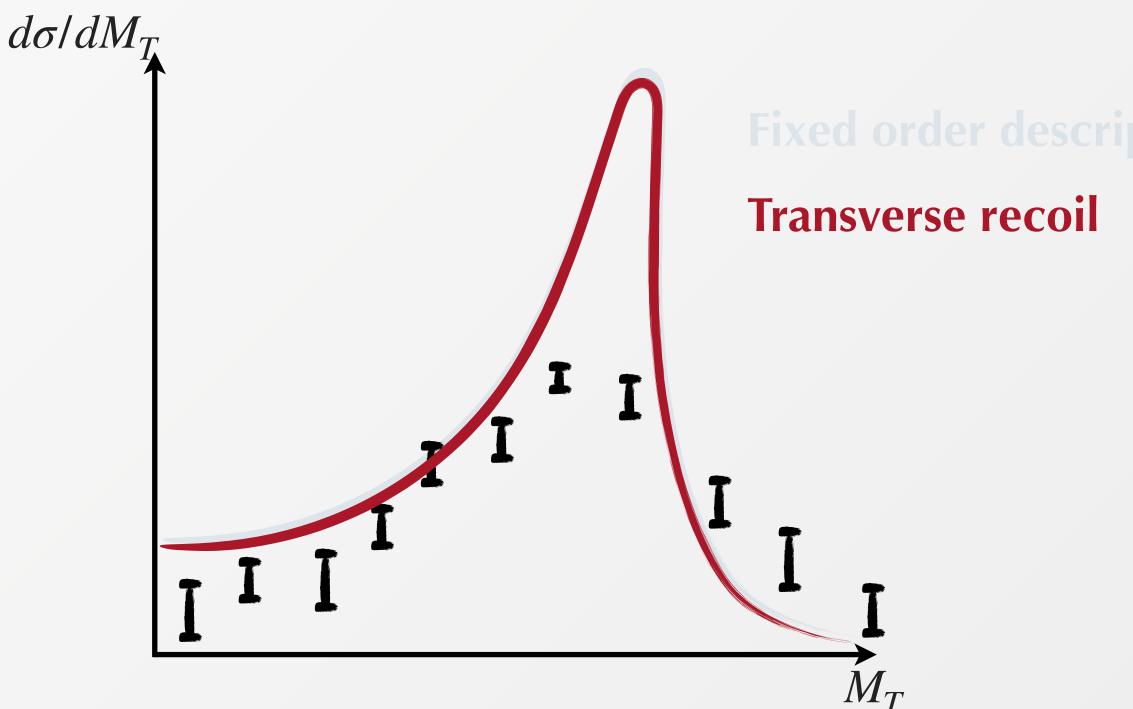


Different sensitivity to experimental uncertainties and quality of theoretical modelling

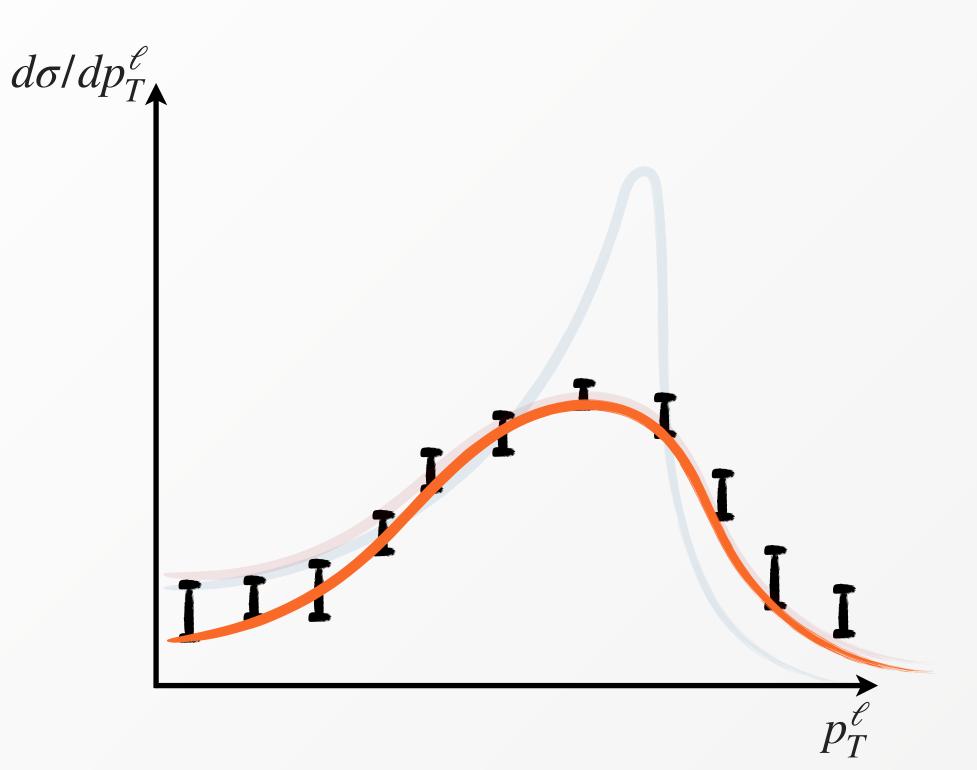


Description of the data requires:

Modelling of IS QCD + FS QED radiation

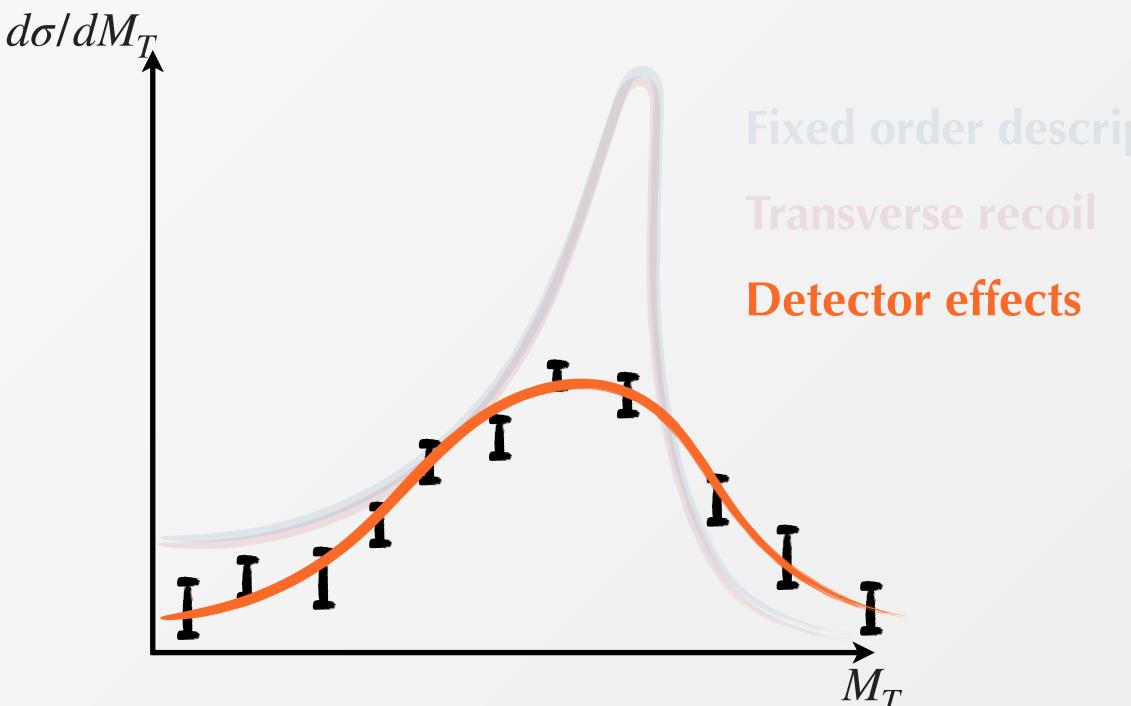


Different sensitivity to experimental uncertainties and quality of theoretical modelling



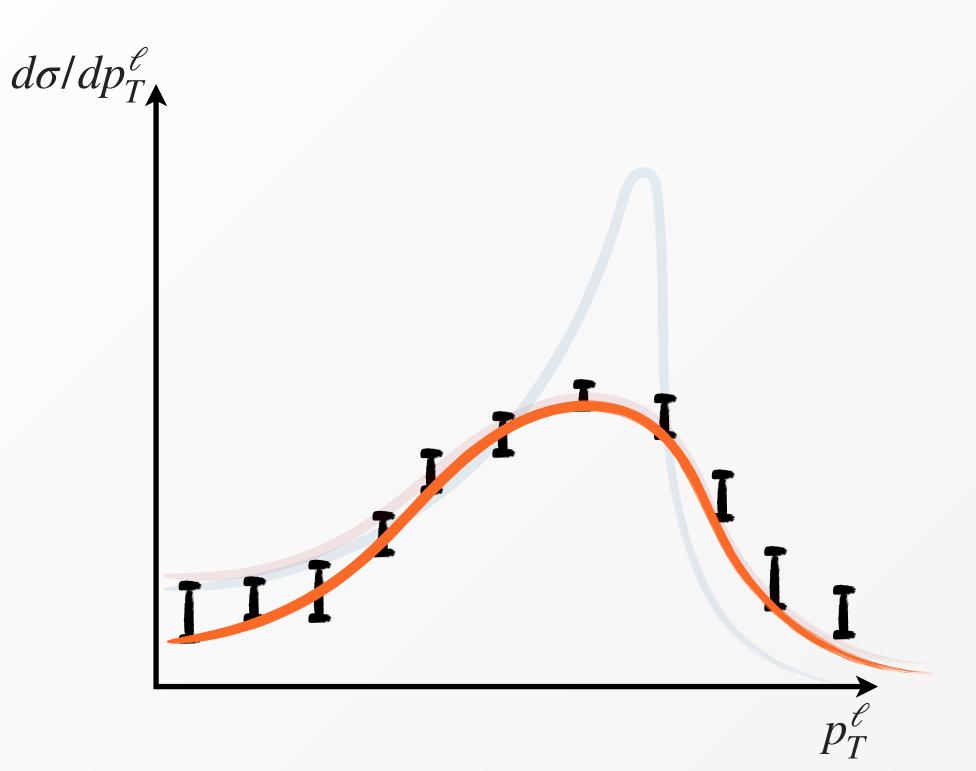
Description of the data requires:

- Modelling of **IS QCD + FS QED radiation**



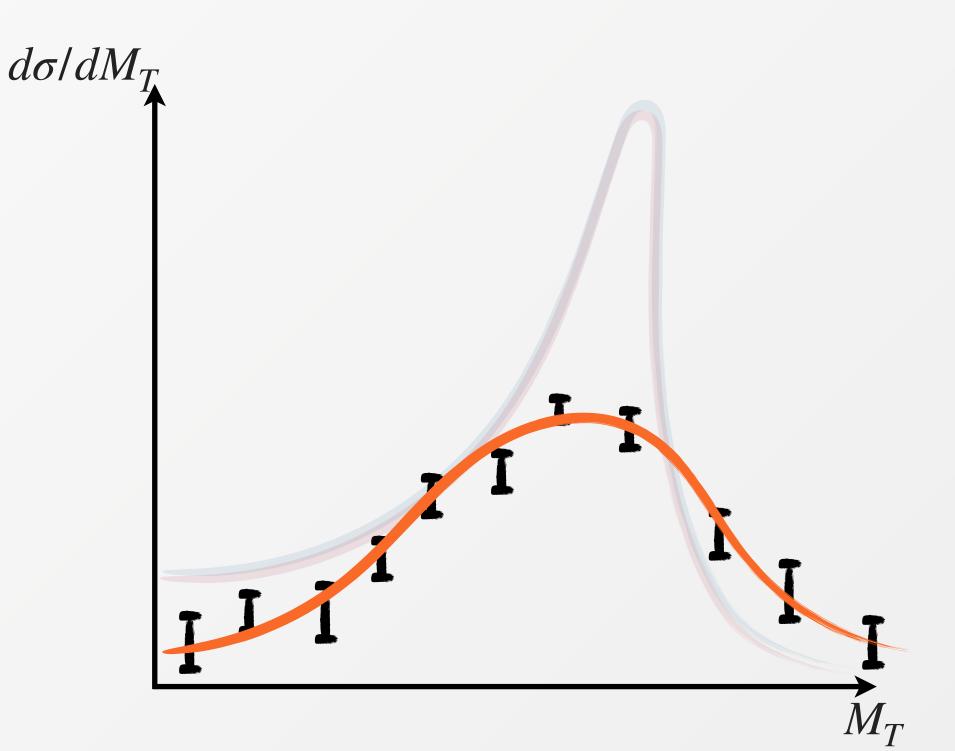
• Modelling of the smearing of the distributions due to the reconstruction of the neutrino in the transverse plane

Different sensitivity to experimental uncertainties and quality of theoretical modelling



Mostly QCD + QED radiation

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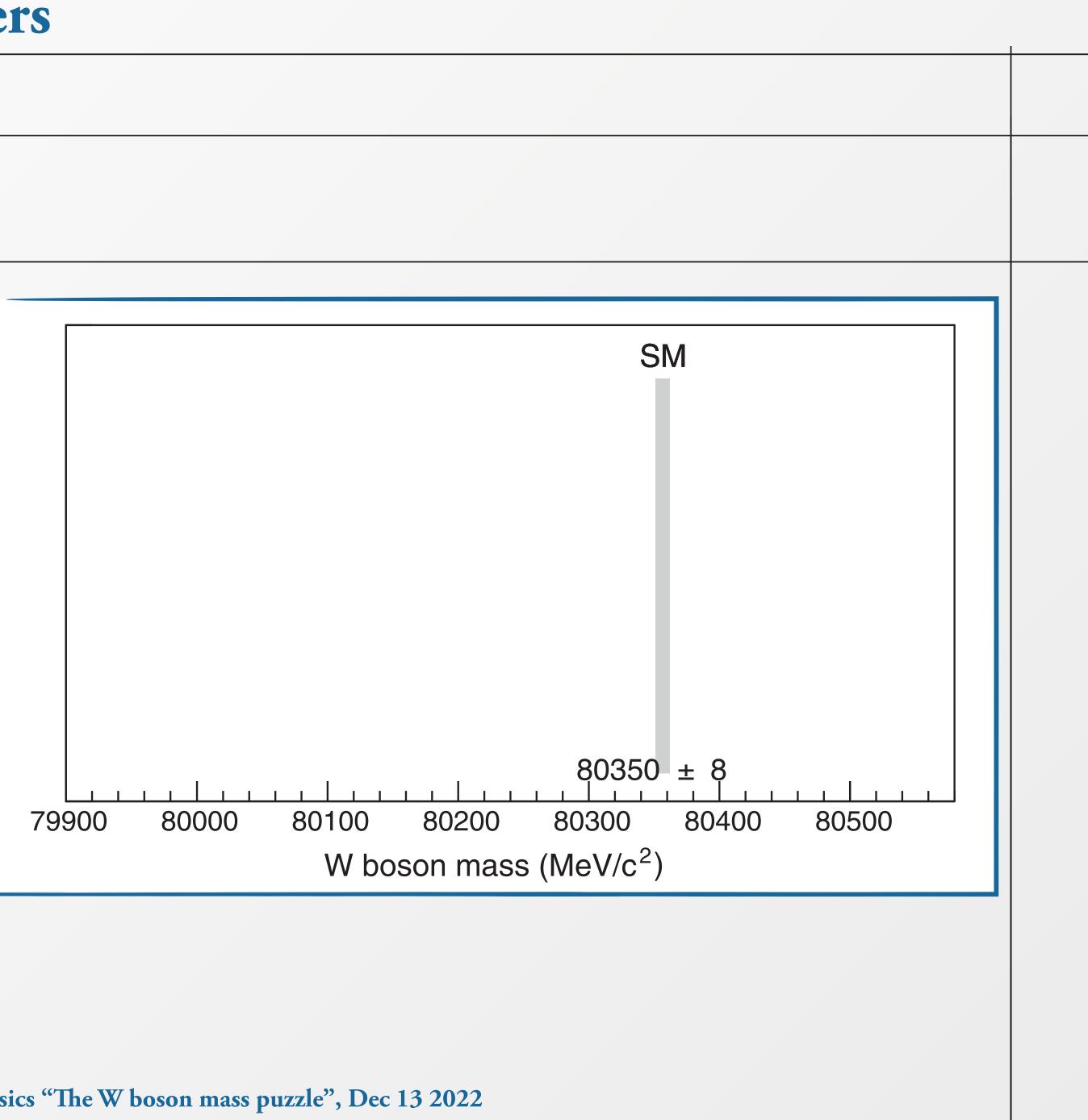


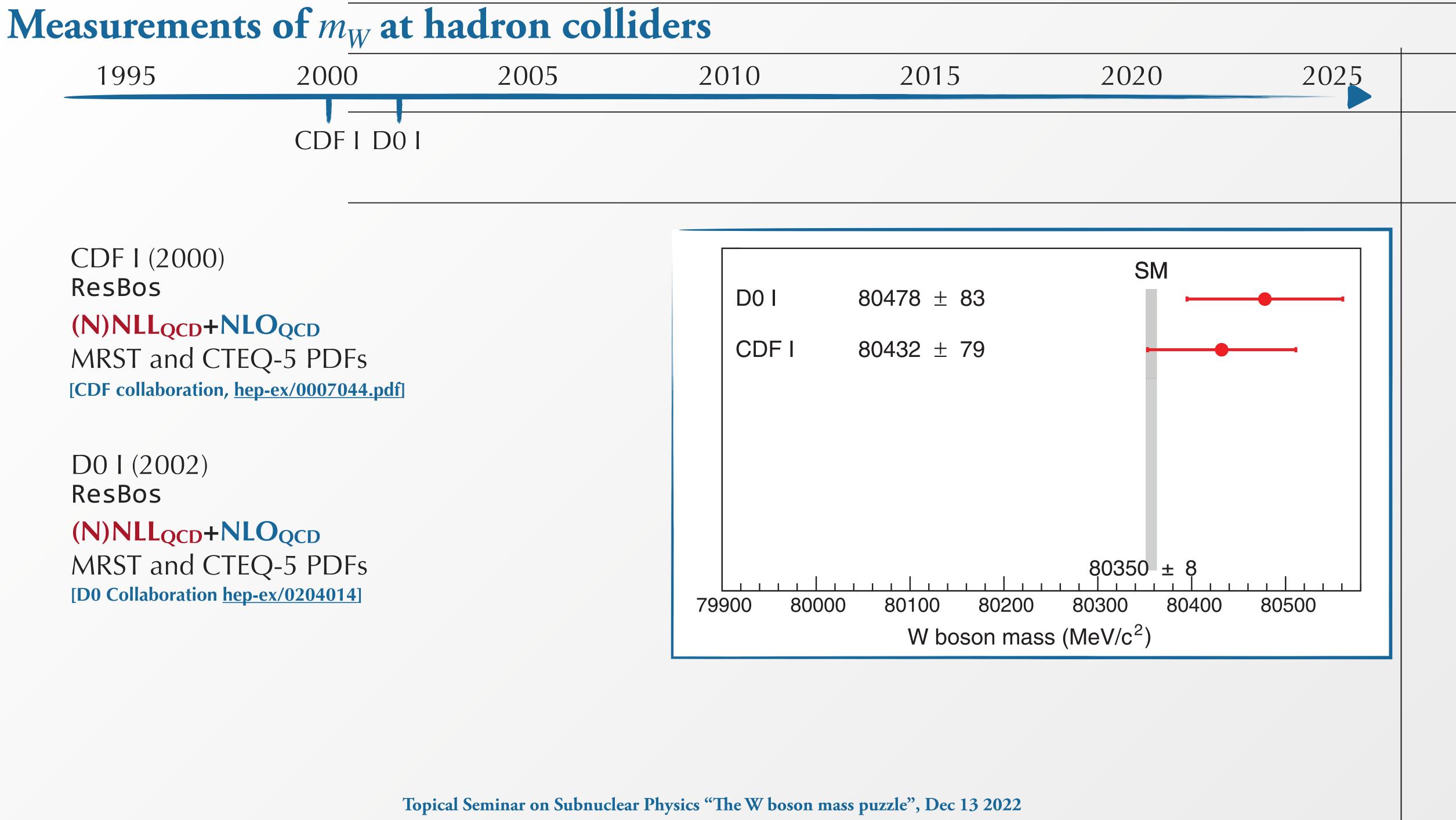
Mostly **detector effects**

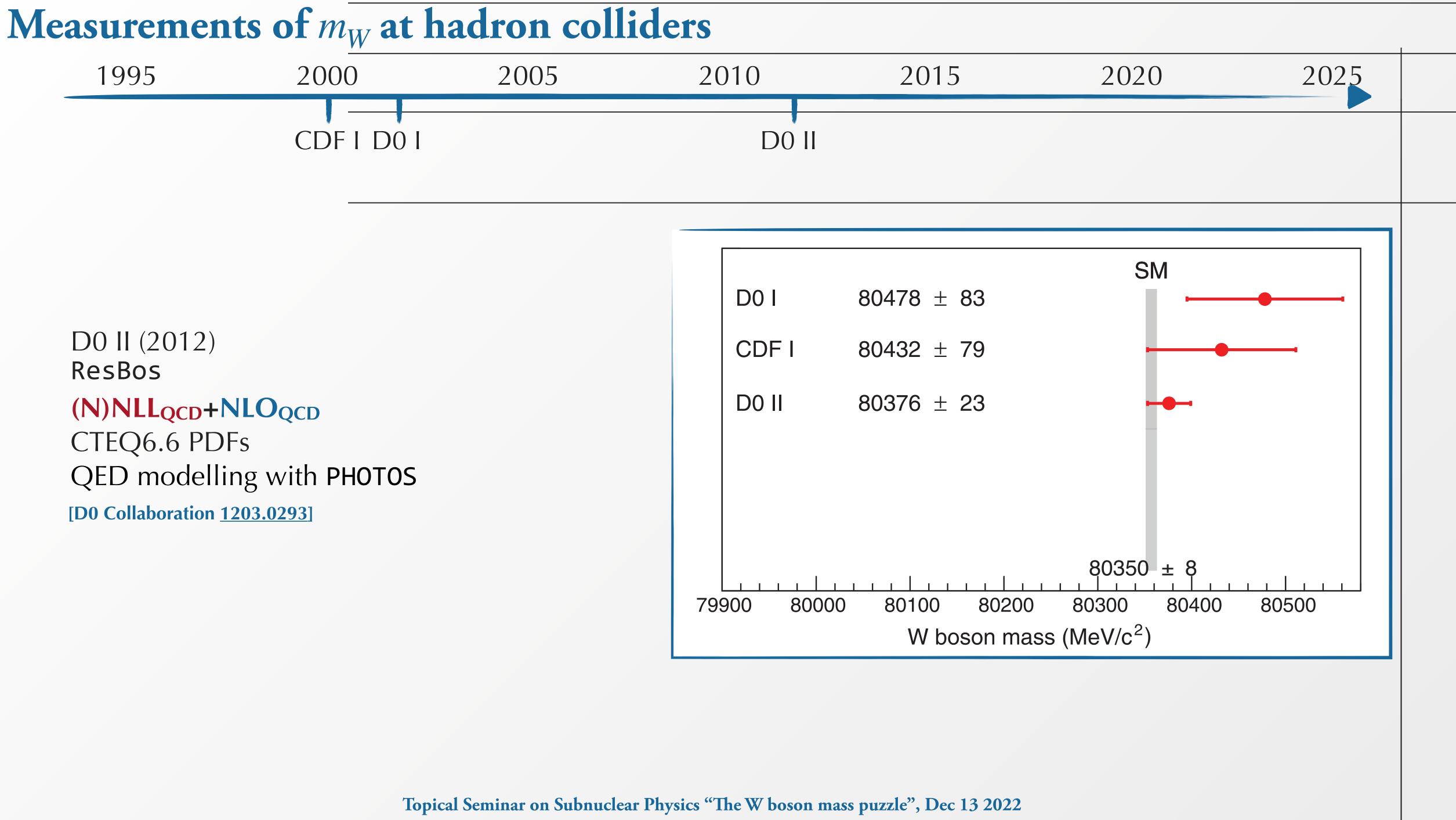
$$m_T = \sqrt{2p_T^{\ell} p_T^{\nu} (1 - \cos \Delta \phi_{\ell\nu})}$$

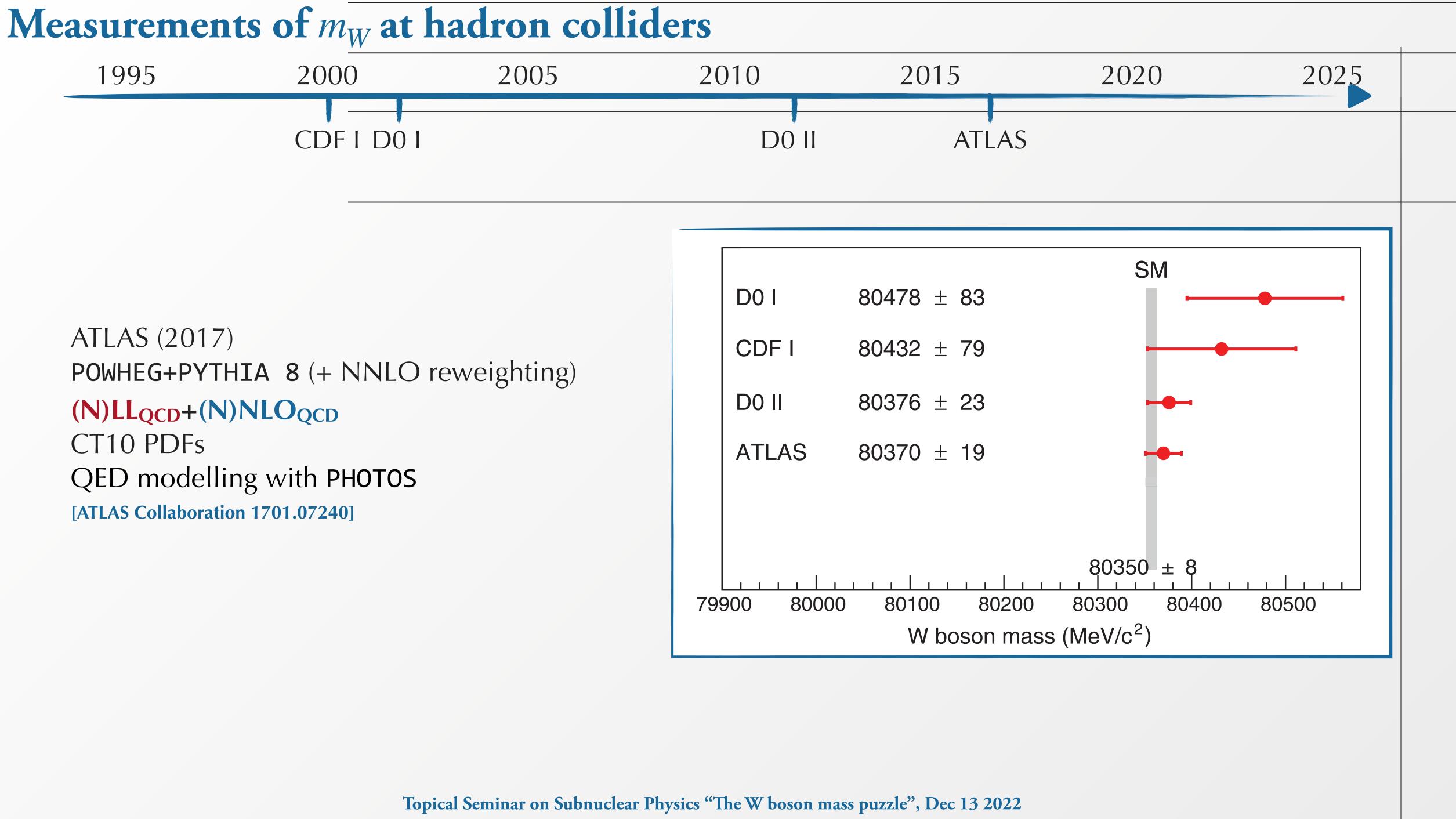
Requires precise determination of the neutrino transverse momentum: **challenging at the LHC** due to worse control of the hadronic recoil

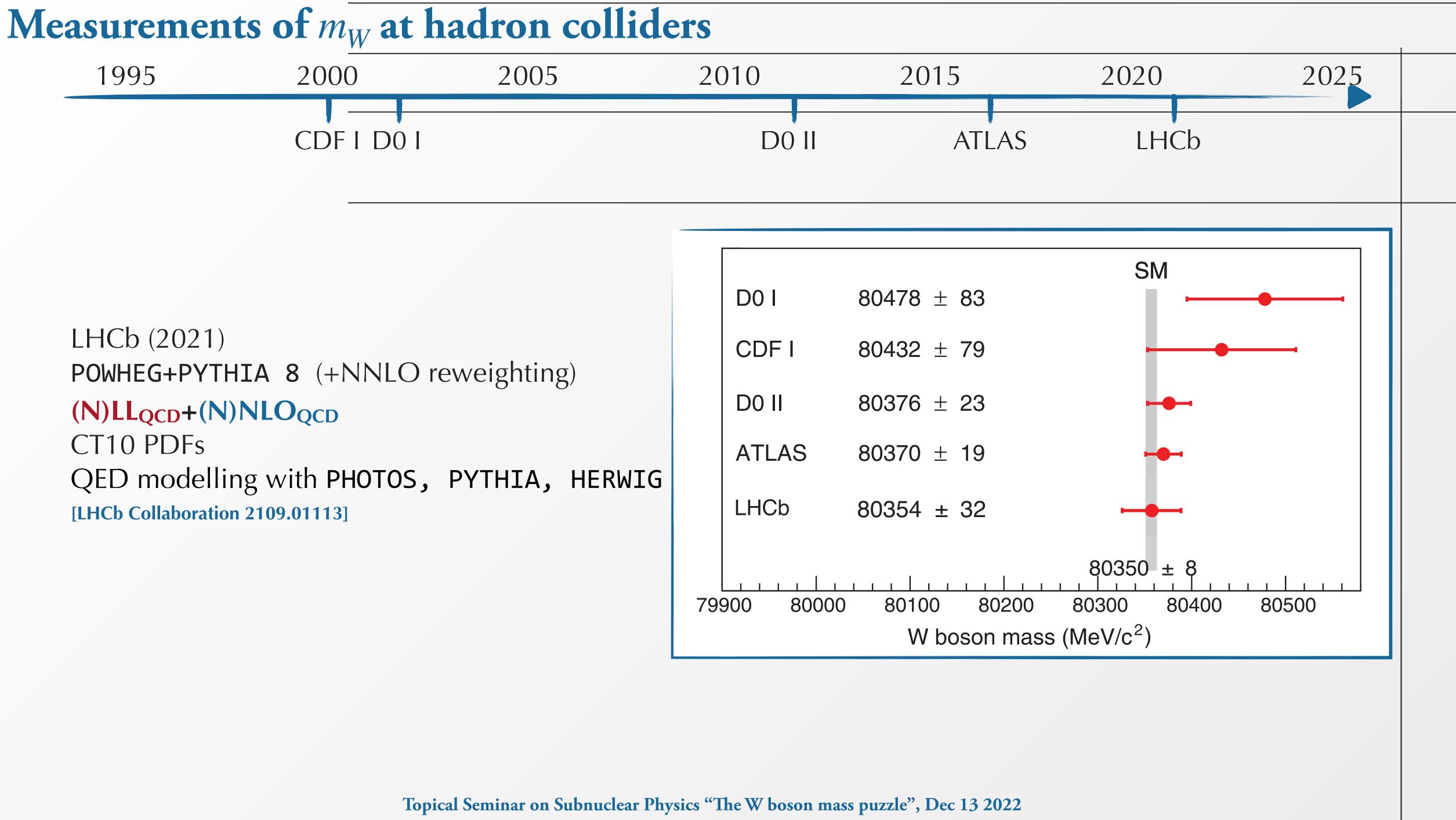
Measurements of m_W at hadron colliders

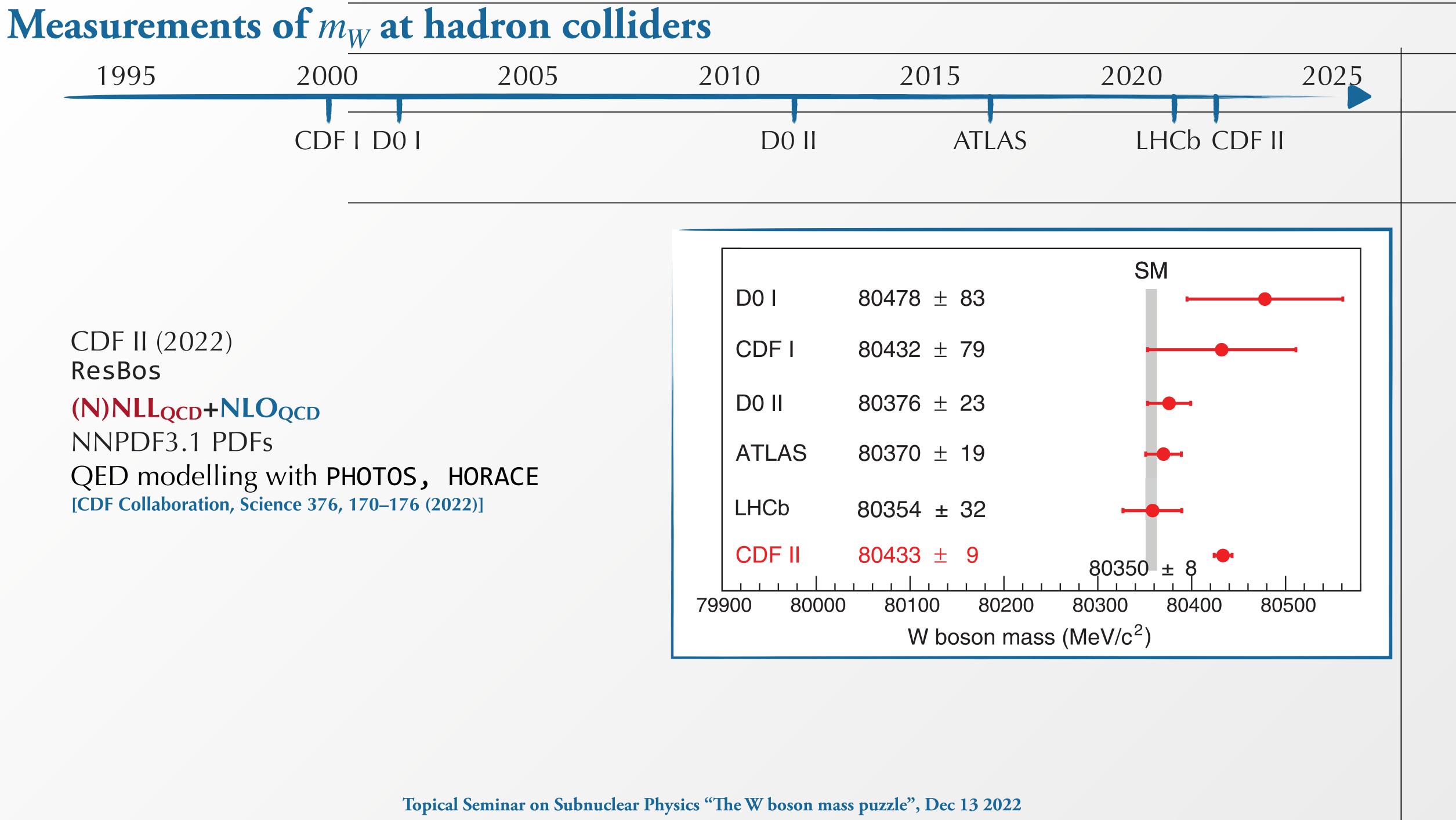








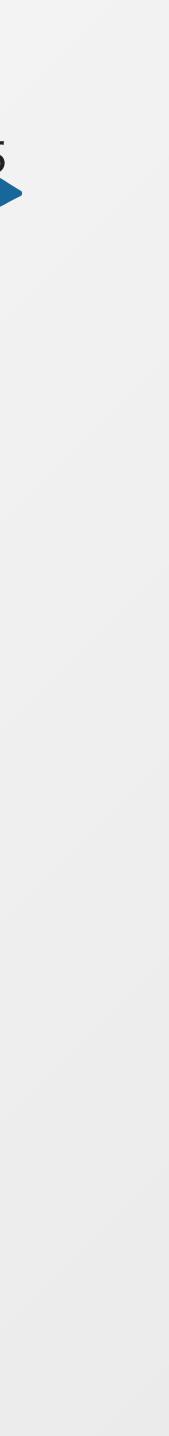




Mea

1995 20	00	2005		2010	2015	2020
CD	FIDOI			D0 II	ATLAS	LHCb CDF II
CDF II measurement		2				
extremely aggressive					Table 2. Uncertainties o M_W result.	on the combined
theory uncertainties, compared to CDF I re	• /	wnen				
	esuns				Source	Uncertainty (MeV)
compared to eDr m	esuns				Source Lepton energy scale	Uncertainty (MeV) 3.0
					Lepton energy scale Lepton energy resolution	3.0 1.2
Source of uncertainty		$W \rightarrow \mu \nu$	Common		Lepton energy scale Lepton energy resolution Recoil energy scale	3.0 1.2 1.2
Source of uncertainty		•	Common		Lepton energy scale Lepton energy resolution Recoil energy scale	3.0 1.2
Source of uncertainty Lepton scale		85	Common		Lepton energy scale Lepton energy resolution Recoil energy scale	3.0 1.2 1.2
		•	Common		Lepton energy scale Lepton energy resolution Recoil energy scale Recoil energy resolution	3.0 1.2 1.2
Source of uncertainty Lepton scale		85	Common 15		Lepton energy scale Lepton energy resolution Recoil energy scale Recoil energy resolution Lepton efficiency	3.0 1.2 1.2
Source of uncertainty Lepton scale Lepton resolution		85 20	Common 15 3		Lepton energy scale Lepton energy resolution Recoil energy scale Recoil energy resolution Lepton efficiency Lepton removal Backgrounds p_{T}^{Z} model	3.0 1.2 1.2 1.8 0.4 1.2 3.3 1.8
Source of uncertainty Lepton scale Lepton resolution PDFs P_T^W		85 20 15	Common 15 3		Lepton energy scale Lepton energy resolution Recoil energy scale Recoil energy resolution Lepton efficiency Lepton removal Backgrounds p_T^Z model p_T^W/p_T^Z model	3.0 1.2 1.2 1.8 0.4 1.2 3.3 1.8 1.8 1.3
Source of uncertainty Lepton scale Lepton resolution PDFs P_T^W Recoil	$W \rightarrow e \nu$ 75 25 15 15 37	85 20 15 20	Common 15 3		Lepton energy scale Lepton energy resolution Recoil energy scale Recoil energy resolution Lepton efficiency Lepton removal Backgrounds p_T^Z model p_T^W/p_T^Z model Parton distributions	3.0 1.2 1.2 1.8 0.4 1.2 3.3 1.8 1.8 1.3
Source of uncertainty Lepton scale Lepton resolution PDFs P_T^W Recoil Higher order QED		85 20 15 20 35 10	Common 15 3 5		Lepton energy scale Lepton energy resolution Recoil energy scale Recoil energy resolution Lepton efficiency Lepton removal Backgrounds p_T^Z model p_T^W/p_T^Z model Parton distributions QED radiation	3.0 1.2 1.2 1.8 0.4 1.2 3.3 1.8 1.8 1.3
Source of uncertainty Lepton scale Lepton resolution PDFs p_T^W Recoil	$W \rightarrow e \nu$ 75 25 15 15 37	85 20 15 20	Common 15 3 5		Lepton energy scale Lepton energy resolution Recoil energy scale Recoil energy resolution Lepton efficiency Lepton removal Backgrounds p_T^Z model p_T^W/p_T^Z model Parton distributions	$\begin{array}{c} 3.0\\ 1.2\\ 1.2\\ 1.8\\ 0.4\\ 1.2\\ 3.3\\ 1.8\\ 1.3\\ 3.9\\ 2.7\\ 6.4\end{array}$

[CDF collaboration, <u>hep-ex/0007044.pdf</u>]



2000

CDF I D0 I

CDF II measurement features extremely aggressive estimates for theory uncertainties, especially when compared to CDF I results

But also when compared to a more recent analysis with lower luminosity, as all the errors are reduced by a factor 2-3

> $p_T(W)$ model 5 Parton distributions 10 QED radiation 4

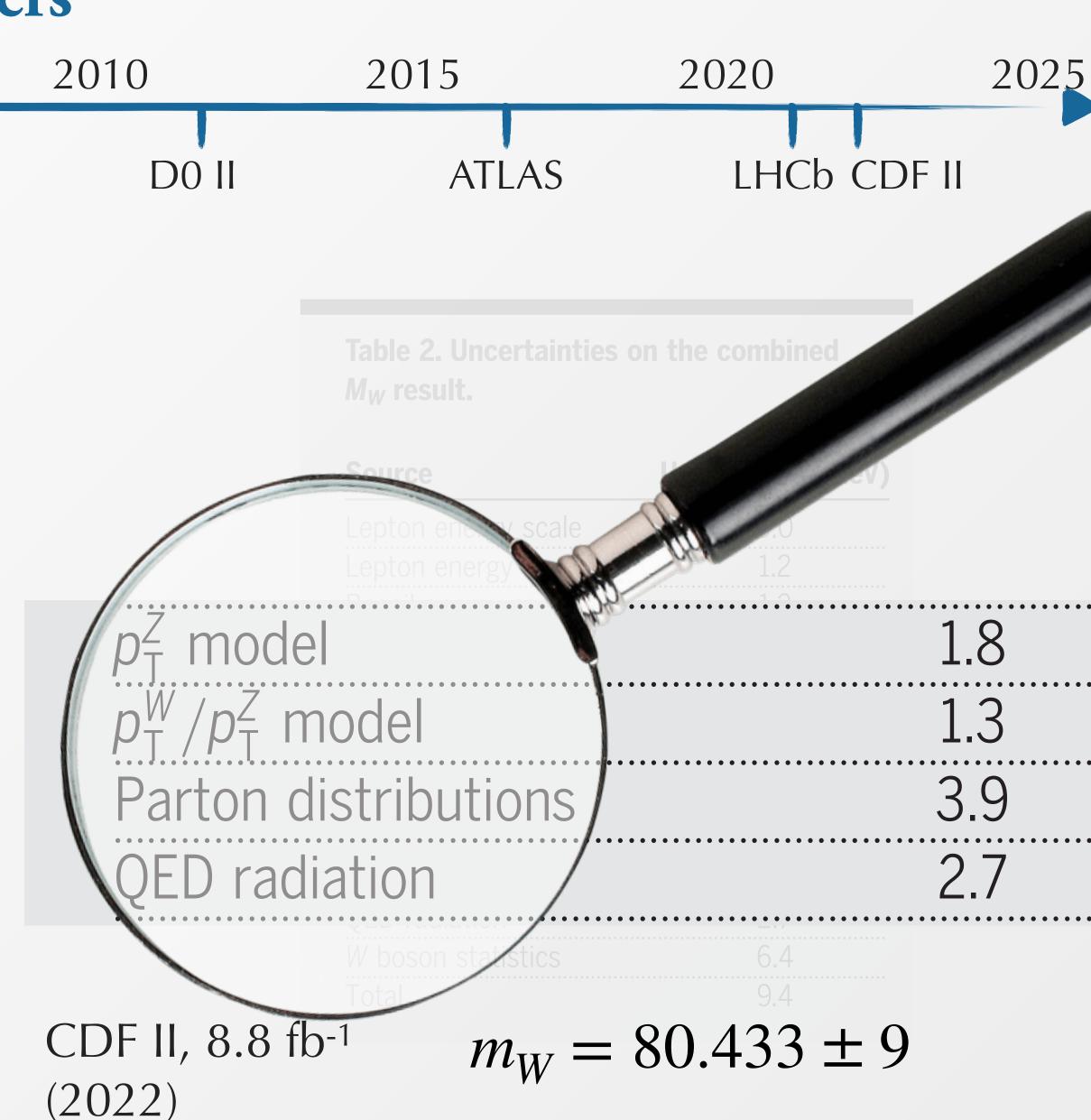
> > [CDF collaboration, 1203.0275]

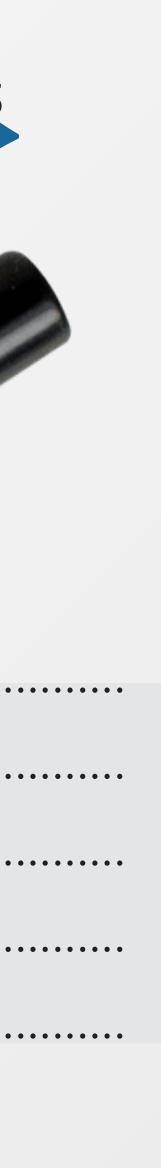
CDF II, 2.2 fb⁻¹ (2012)

1995

$$m_W = 80.387 \pm 19$$

2005





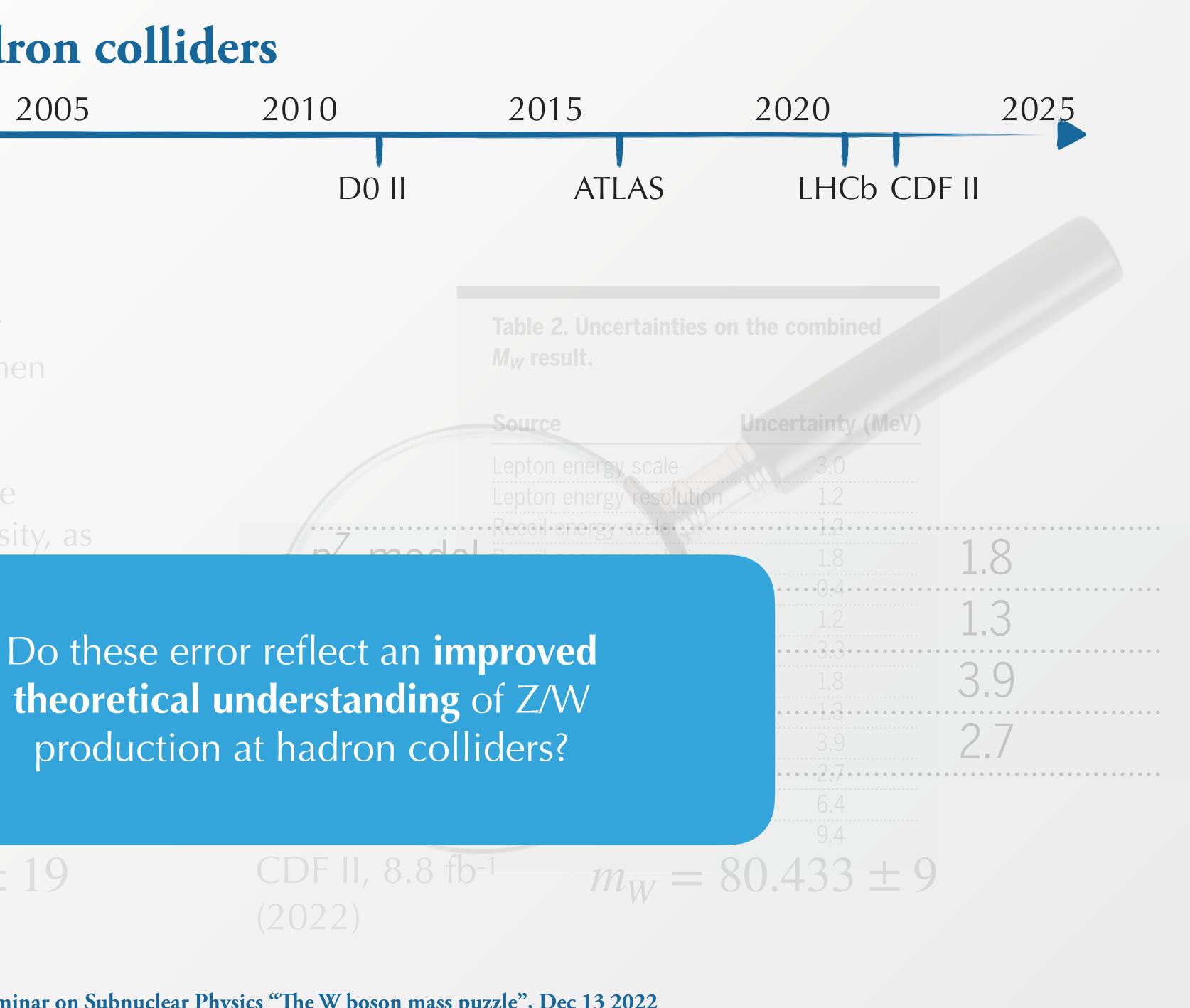
1995 2000 2005 CDF I D0 I

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CDF II, 2.2 fb⁻¹

 $m_W = 80.387 \pm 19$



1995 2000 2005 CDFID01

> CDF II, 2.2 fb⁻¹ (2012)

> > Not really: despite being published 10 years apart, the two analyses share most of the same underlying **theoretical model**

ResBos (N)NLLocd+NLOocd CTEQ6.6 NLO PDFs QED modelling with PHOTOS+HORACE

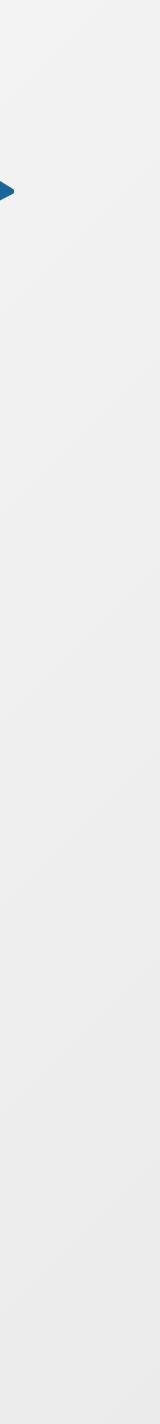
Reduction of the theoretical error obtained via additional **data constraint** and use of **more modern PDF sets**

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CDF II, 8.8 fb⁻¹ (2022)

ResBos (N)NLLQCD+NLOQCD NNPDF3.1 NNLO PDFs QED modelling with PHOTOS+HORACE



Theory uncertainties and m_W measurements

ResBos (N)NLLQCD+NLOQCD NNPDF3.1 NNLO PDFs QED modelling with PHOTOS+HORACE

Theory uncertainties and m_W measurements

ResBos (N)NLL_{QCD}+NLO_{QCD} NNPDF3.1 NNLO PDFs QED modelling with PHOTOS+HORACE

> *"Estimating theory uncertainties"* is more of an art than a science"

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Stefano Forte

NNPDF3.1 NNLO PDFs QED modelling with PHOTOS+HORACE

Uncertainties related to PDFs can have different origin:

- Uncertainty propagated from the statistical and systematic errors on the measurements used in their determination (canonical "**PDF uncertainty**")
- Theoretical uncertainties of the predictions used in PDF fits, such as missing higher order uncertainty: these are starting to be addressed only recently, and are typically not included in the nominal PDF uncertainty [Abdul Khalek, Ball, LR, et al, (NNPDF Coll.), 1905.04311] [J. McGowan, T. Cridge, L. Harland-Lang, R. Thorne (MSHT Coll.) 2207.04739]

encompasses the envelope of various PDF sets

- Comparisons between different groups used to assess sources of **methodological uncertainty** in the PDF extraction
- m_W measurements typically include the nominal PDF uncertainty and, more conservatively, they also assess that it

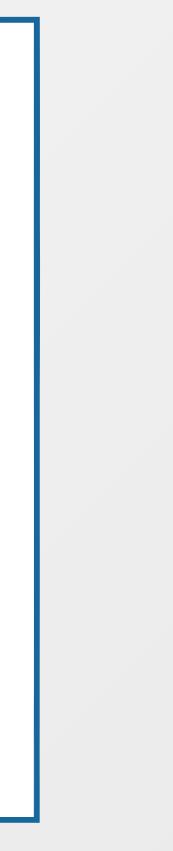
Numerous studies on the impact of PDF uncertainties have been performed at both colliders [Tevatron 0707.0085,0708.3642,0908.0766,1203.0275,1203.0293,1307.7627] [Bozzi, Citelli, Rojo, Vesterinen, Vicini 1104.2056, 1501.05587, 1508.06954] [ATLAS 1701.07240] [Kotwal PRD 98, 033008] [Manca, Cerri, Foppiani, Rolandi 1707.09344] [Bianchini, Rolandi 1902.03028] [Farry, Lupton, Pili, Vesterinen, 1902.04323] [Bagnaschi, Vicini 1910.04726] [Hussein, Isaacson, Huston 1905.00110] [Gao, Liu, Xie 2205.03942]

The relative size of PDFs uncertainties at the Tevatron and at the LHC is affected by the different centre-of-mass energy of the collision and the **different initial states**

PDFs uncertainties **not an obstacle at Tevatron**; they have long been considered a **limiting factor at the LHC** due to the smaller values of the partonic *x* probed (higher collider energy) and the larger contribution from the second quark generation

 $\sqrt{s} = 13 \text{ TeV}$ 1.20 1.15 1.10 1.05 $\mathcal{L}_{ar{S}\mathcal{C}}$ 1.00 0.95 0.90 0.85 NNPDF3.1 0.80 10^{1} 10^{2} 10^{3} M_{x}





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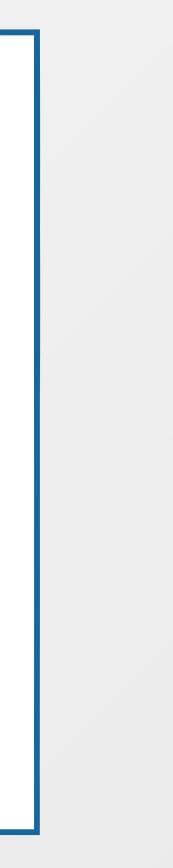
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Latest generation of NNPDF parton densities (large number of LHC datasets included, new machinelearning based methodology) achieves substantial **reduction** of PDF uncertainty

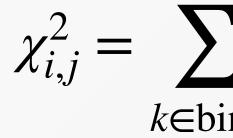
 $\sqrt{s} = 13 \text{ TeV}$ 1.20 1.15 1.10 1.05 ${\cal L}_{ar{S}{\cal C}}$ 1.00 0.95 0.90 0.85 NNPDF4.0 0.80 10^{1} 10^{2} 10^{3} M_{x}



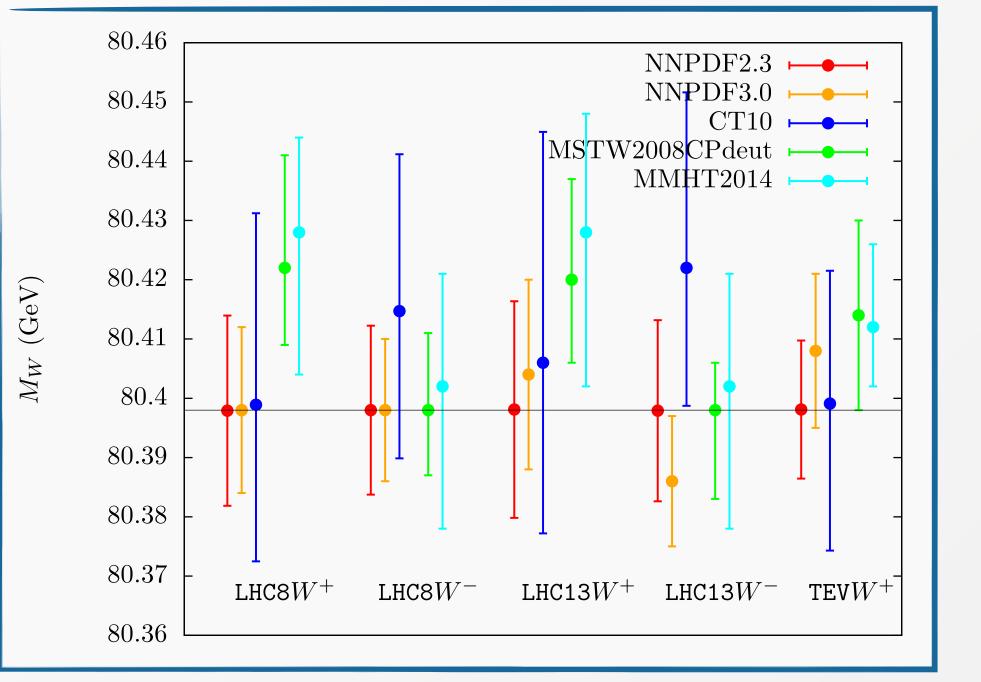


PDFs and their uncertainties: template fits

PDF-induced uncertainty typically computed by generating templates with a given PDF member *i* for various values of m_W , and subsequently fitting all other members *j* defining a proper figure of merit



Once the preferred value for m_W for each member has been determined by minimising the figure of merit, compute PDF-induced uncertainty



[Bozzi, Citelli, Vicini 1501.05587]

$$\frac{(T_k^j - D_k^i)^2}{\sigma_k^2}$$

PDF uncertainties with this strategy are **relatively** large at the LHC, with a resulting uncertainty larger than 10 MeV and considerably large spreads between different PDF sets

Cfr. ~ 4 MeV quoted by CDF II with NNLO PDFs

4 MeV also claimed by CDF II to be the shift between NNPDF3.1 NNLO and ~15 years old NLO CTEQ6.6 PDFs

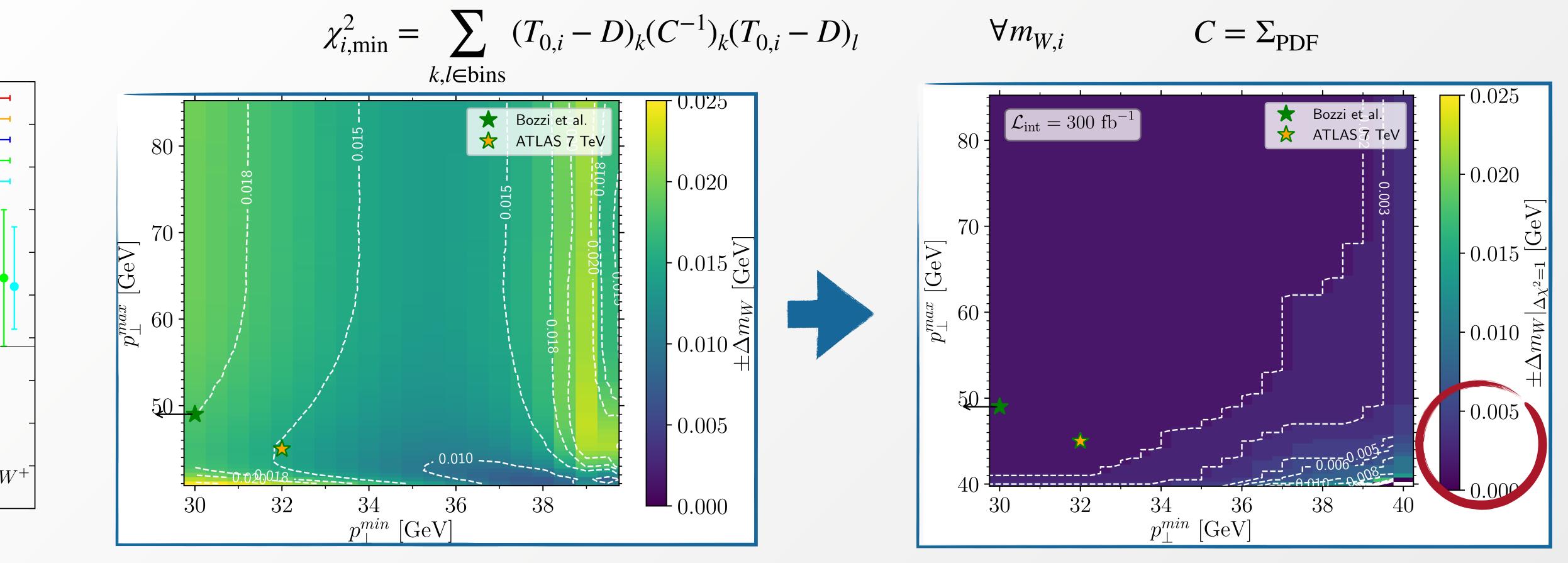


PDFs and their uncertainties: bin-by-bin correlations

This estimate does not take into account **bin-by-bin correlations** between PDF replicas

$$(\Sigma_{\rm PDF})_{ij} = \langle (\mathcal{T} - \langle \mathcal{T} \rangle_{\rm PDF})_i (\mathcal{T} - \langle \mathcal{T} \rangle_{\rm PDF})_j \rangle_{\rm PDFs}$$

Compute χ^2 taking into account bin-by-bin correlations introducing a covariance matrix in the definition



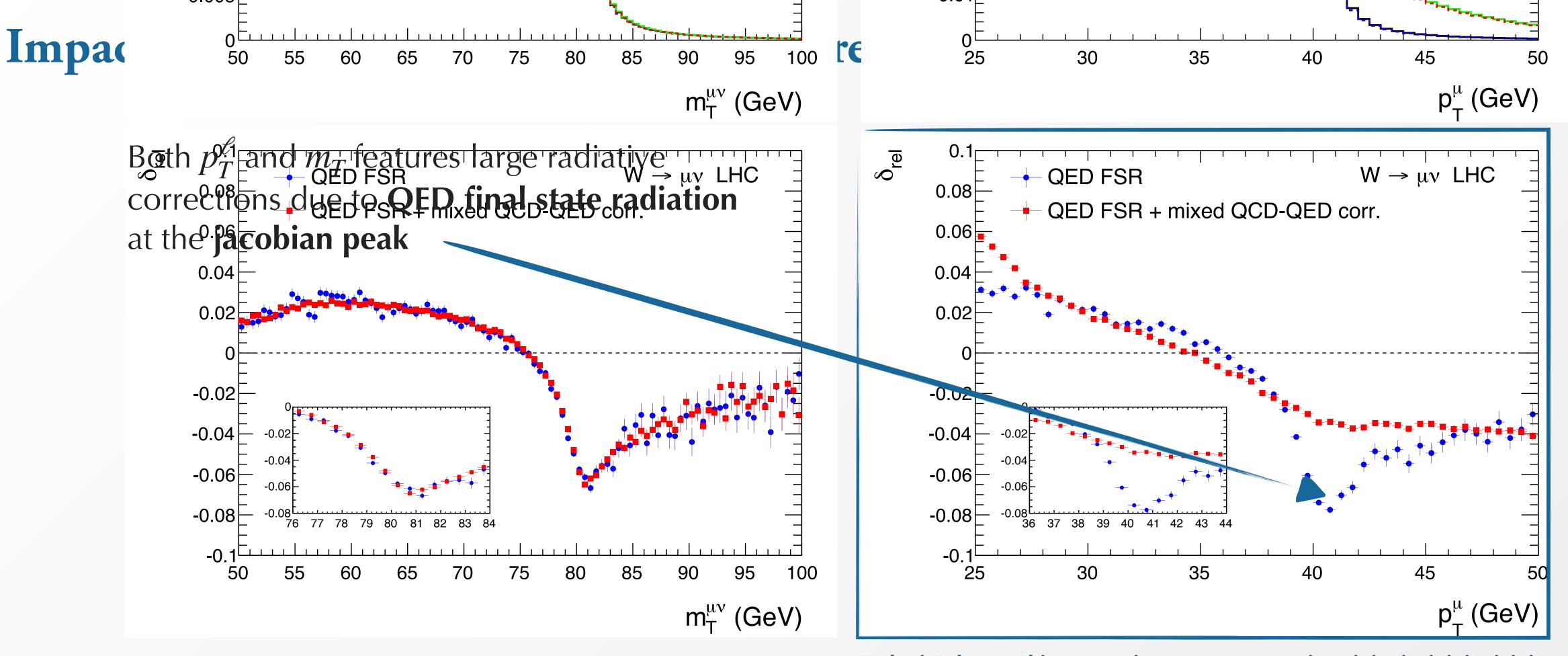
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Reduced sensitivity to the PDF uncertainty, if other source of errors are under control



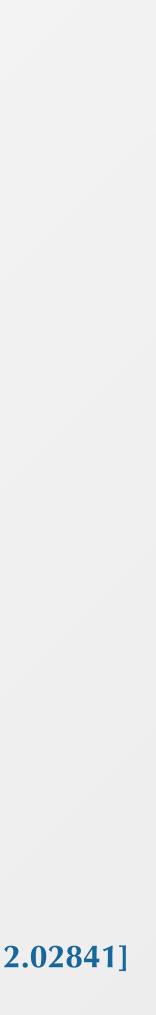
QED modelling and its uncertainty

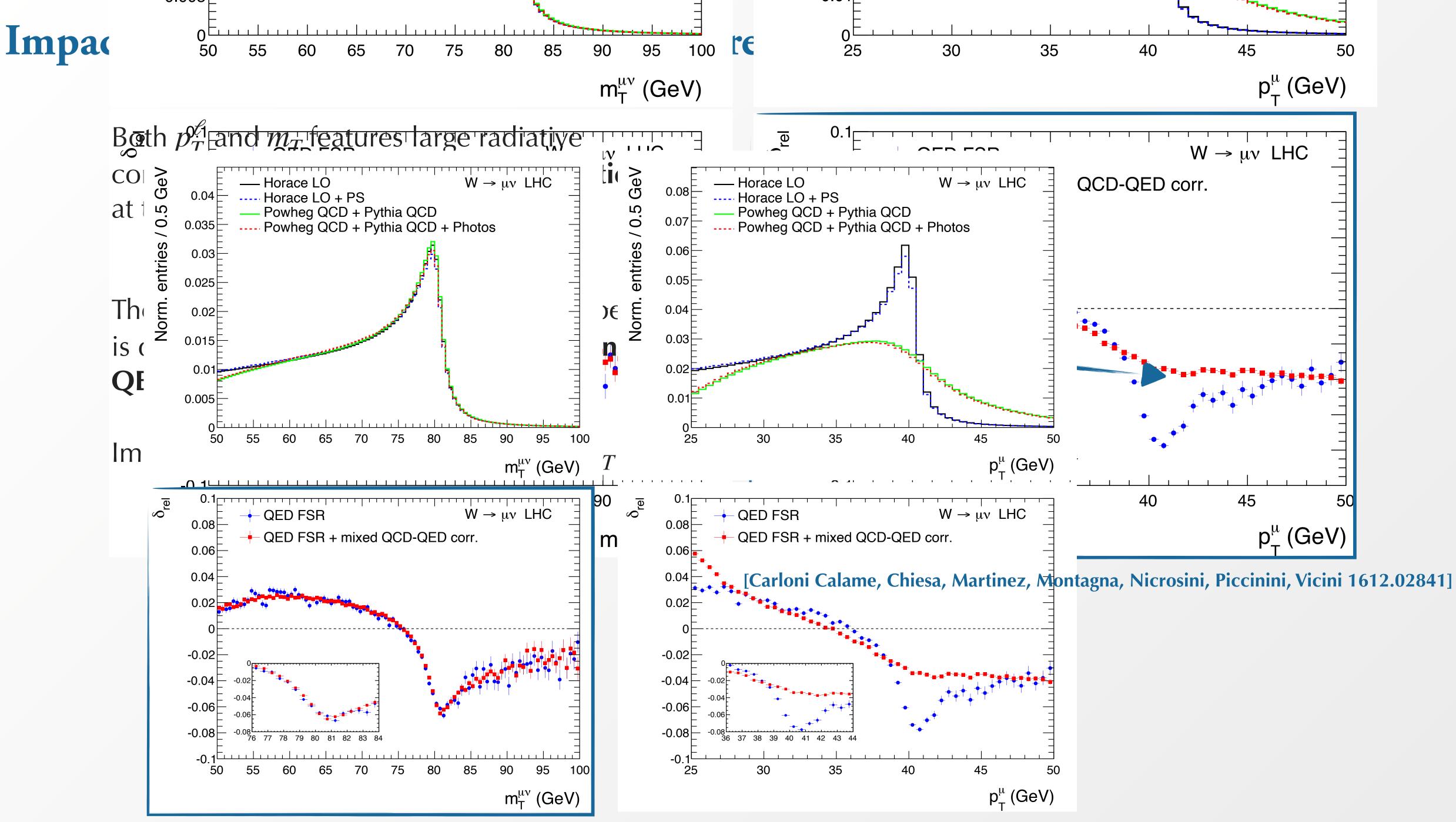
NNPDF3.1 NNLO PDFs QED modelling with PHOTOS+HORACE



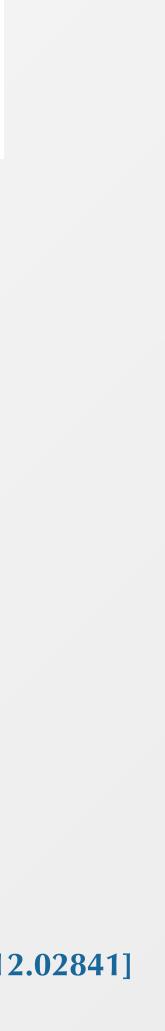
[Carloni Calame, Chiesa, Martinez, Montagna, Nicrosini, Piccinini, Vicini 1612.02841]

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Impact of EW and mixed QCD×EW corrections

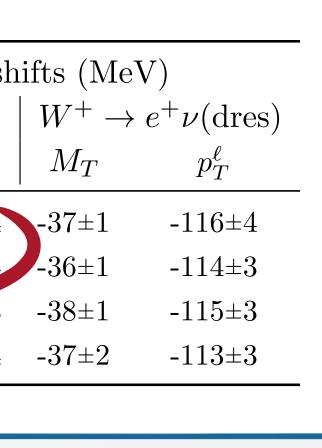
Largest shifts induced by **QED FSR**

Subleading EW effects induce few MeV shifts

	$p\bar{p} \rightarrow W^+, \sqrt{s} = 1.96 \text{ TeV}$	$M_W \mathrm{sh}^2$		
	Templates accuracy: NLO-QCD+QC	$W^+ \to \mu^+ \nu$		
	Pseudodata accuracy	QED FSR	M_T	p_T^ℓ
1	$NLO-QCD+(QCD+QED)_{PS}$	Рутніа	-91±1	-308±4 -282±4
2	$NLO-QCD+(QCD+QED)_{PS}$	Рнотоз	-83±1	-282±4
3	$\text{NLO-}(\text{QCD+EW})\text{-two-rad} + (\text{QCD+QED})_{\text{PS}}$	Pythia	-86 ± 1	-291±3
4	$\text{NLO-}(\text{QCD+EW})\text{-two-rad}+(\text{QCD+QED})_{\text{PS}}$	Рнотоз	-85 ± 1	-290 ± 4

[Carloni Calame, Chiesa, Martinez, Montagna, Nicrosini, Piccinini, Vicini 1612.02841]

	$pp \to W^+, \sqrt{s} = 14 \text{ TeV}$	M_W shifts (MeV)				
	Templates accuracy: LO		$W^+ \to \mu^+ \nu$		$W^+ \to e^+ \nu$	
	Pseudo–data accuracy	M_T	p_T^ℓ	M_T	p_T^ℓ	
1	HORACE only FSR-LL at $\mathcal{O}(\alpha)$	-94±1	-104 ± 1	-204 ± 1	-230 ± 2	
2	HORACE FSR-LL	-89 ± 1	-97 ± 1	-179 ± 1	-195 ± 1	
3	HORACE NLO-EW with QED shower	$-90{\pm}1$	$-94{\pm}1$	-177 ± 1	-190 ± 2	
4	HORACE FSR-LL $+$ Pairs	$-94{\pm}1$	-102 ± 1	-182 ± 2	-199 ± 1	
5	Рнотоs FSR-LL	-92 ± 1	-100 ± 2	-182±1	-199 ± 2	



Analyses do include the bulk of the QCDxQED corrections

The impact on the m_W shifts of the mixed QCDXQED corrections strongly depends on the underlying QCD model

Note: in this approach non-factorizable contributions are neglected







Impact of EW and mixed QCD×EW corrections

Largest shifts induced by QED FSR

Subleading EW effects induce few MeV shifts

 $p\bar{p} \rightarrow W^+, \sqrt{s} =$ Templates accuracy: NL(Pseudodata accuracy

- 1 NLO-QCD+ $(QCD+QED)_{PS}$
- 2 NLO-QCD+(QCD+QED)_{PS}
- 3 NLO-(QCD+EW)-two-rad+(Q
- 4 NLO-(QCD+EW)-two-rad+(Q

Do we have a precise understanding of **mixed QCD**×**EW** corrections?

[Carloni Calame, Chiesa, Martinez, Montagna, Nicrosini, Picc

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Templates accuracy: LO $W^+ \rightarrow \mu^+ \nu$ $W^+ \rightarrow e^+ \nu$ Pseudo-data accuracy M_T p_T^ℓ M_T p_T^ℓ 1HORACE only FSR-LL at $\mathcal{O}(\alpha)$ -94 ± 1 -104 ± 1 -204 ± 1 -230 2HORACE FSR-LL -89 ± 1 -97 ± 1 -179 ± 1 -195 3HORACE NLO-EW with QED shower -90 ± 1 -94 ± 1 -177 ± 1 -190 4HORACE FSR-LL + Pairs -94 ± 1 -102 ± 1 -182 ± 2 -199 5PHOTOS FSR-LL -92 ± 1 -100 ± 2 -182 ± 1 -199		$pp ightarrow W^+, \sqrt{s} = 14 { m TeV}$	M_W shifts (MeV)			
1 HORACE only FSR-LL at $\mathcal{O}(\alpha)$ -94 ± 1 -104 ± 1 -204 ± 1 -230 2 HORACE FSR-LL -89 ± 1 -97 ± 1 -179 ± 1 -195 3 HORACE NLO-EW with QED shower -90 ± 1 -94 ± 1 -177 ± 1 -190 4 HORACE FSR-LL + Pairs -94 ± 1 -102 ± 1 -182 ± 2 -199		Templates accuracy: LO	$W^+ ightarrow \mu^+ u$		$W^+ ightarrow e^+ u$	
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4 HORACE FSR-LL + Pairs -94±1 -102±1 -182±2 -199	2	HORACE FSR-LL	-89±1	-97±1	-179 ± 1	-195 ± 1
	3	HORACE NLO-EW with QED shower	-90±1	-94±1	-177 ± 1	-190 ± 2
5 Photos FSR-LL -92±1 -100±2 -182±1 -199	4	HORACE FSR-LL + Pairs	-94±1	-102±1	-182±2	-199±1
	5	Photos FSR-LL	-92±1	-100 ± 2	-182±1	-199 ± 2

Jude the bulk of the ections

e *m_W* shifts of the D corrections strongly nderlying QCD model

Note: in this approach non-factorizable contributions are neglected

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Progress in mixed QCD×EW corrections

Complete set of corrections to neutral and charged current Drell-Yan production recently obtained by two groups NNLO QCD-EW corrections to charged-current DY (2-loop contributions in pole approximation).

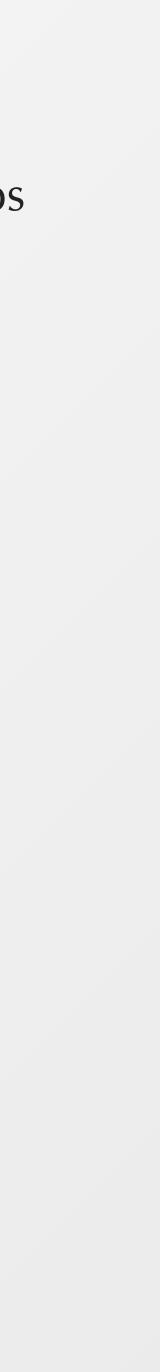
[Buonocore, Grazzini, Kallweit, Savoini, Tramontano 2102.12539]

exact NNLO QCD-EW corrections to neutral-current DY [Bonciani, Buonocore, Grazzini, Kallweit, Rana, Tramontano, Vicini, 2106.11953] [Armadillo, Bonciani, Devoto, Rana, Vicini 2201.01754] [Buccioni, Caola, Chawdhry, Devoto, Heller, von Manteuffel, Melnikov, Röntsch, Signorile-Signorile 2203.11237]

Impact of mixed $\mathcal{O}(\alpha_s \alpha)$ corrections estimated to be potentially relevant for $\mathcal{O}(10 \text{ MeV})$ extraction at the LHC [Behring, Buccioni, Caola, Delto, Jaquier, Melnikov, Röntsch 2103.02671]

Matching of such corrections to QCD and QED all-order resummation of high relevance for accurate and precise analysis of the p_T^{ℓ} distribution

Combination of QCD+QED resummation so far available only for on-shell Z production [Cieri, Ferrera, Sborlini '18]



QCD modelling and its uncertainty

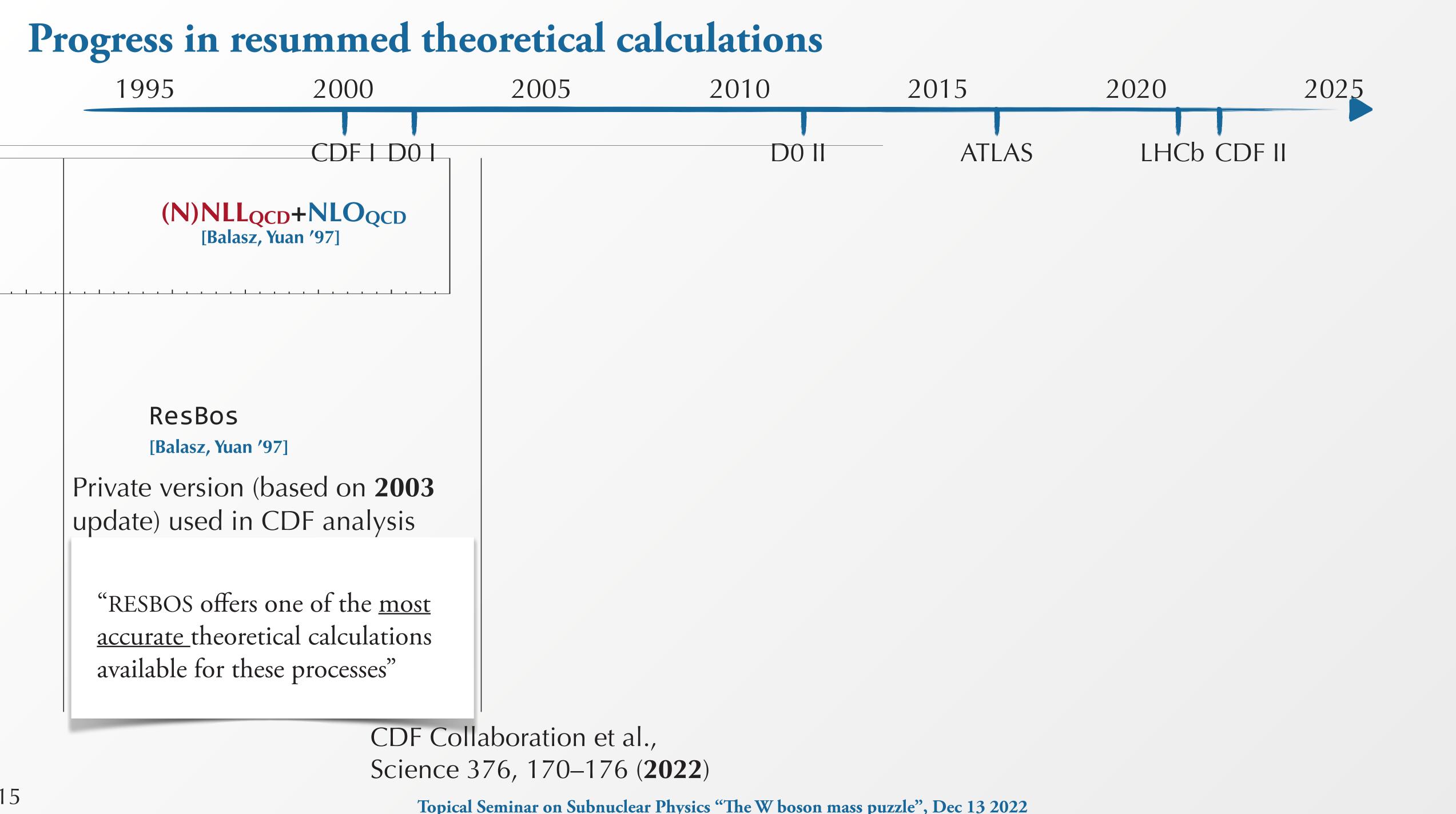
ResBos (N)NLL_{QCD}+NLO_{QCD} NNPDF3.1 NNLO PDFs QED modelling with PHOTOS+HORACE

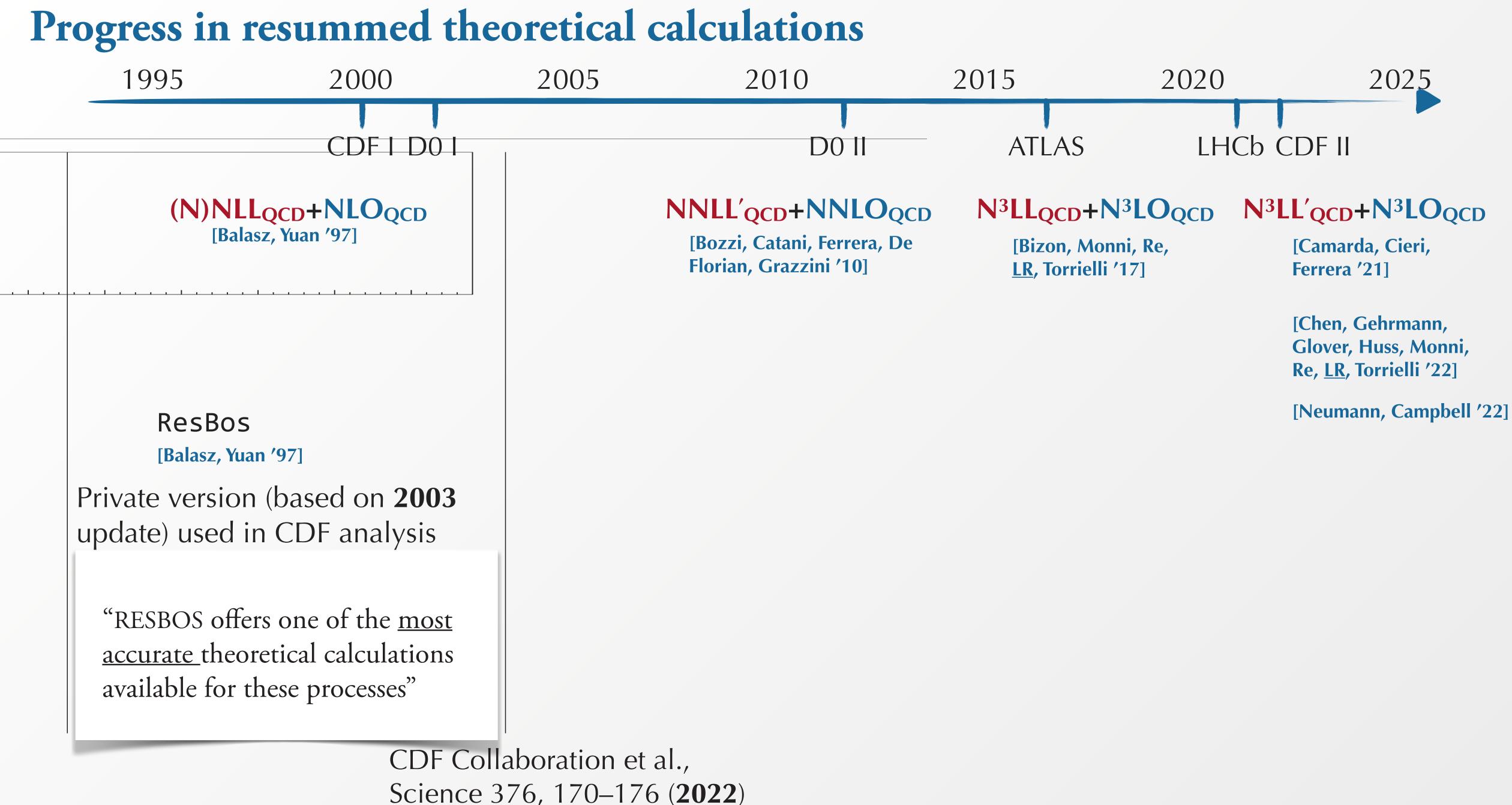
QCD modelling and its uncertainty

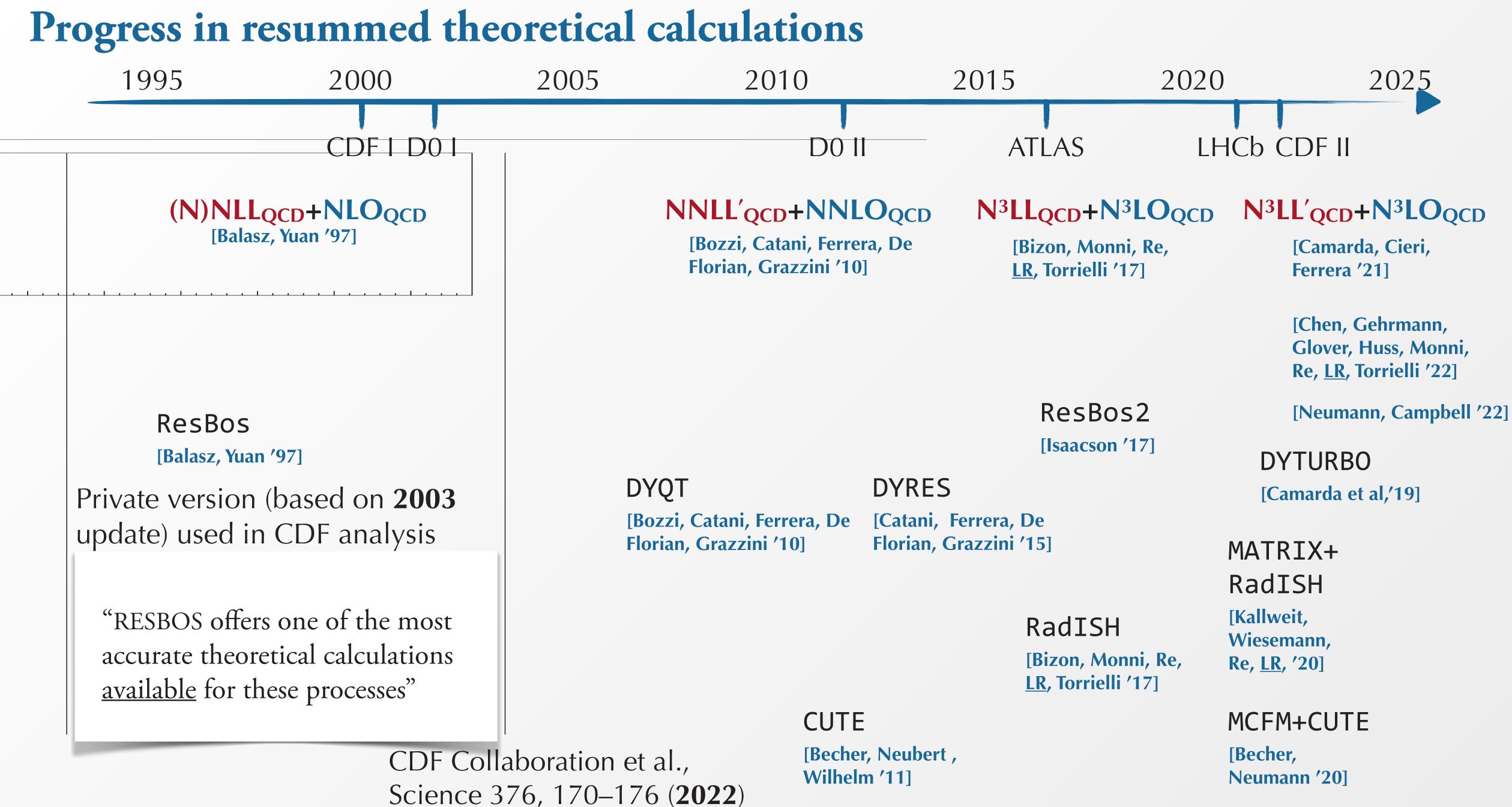
ResBos (N)NLLQCD+NLOQCD NPDF3.1 NNLO PDFs "RESBOS offers one of the most accurate theoretical calculations available for these processes" CDF Collaboration et al., Science 376, 170–176 (**2022**)

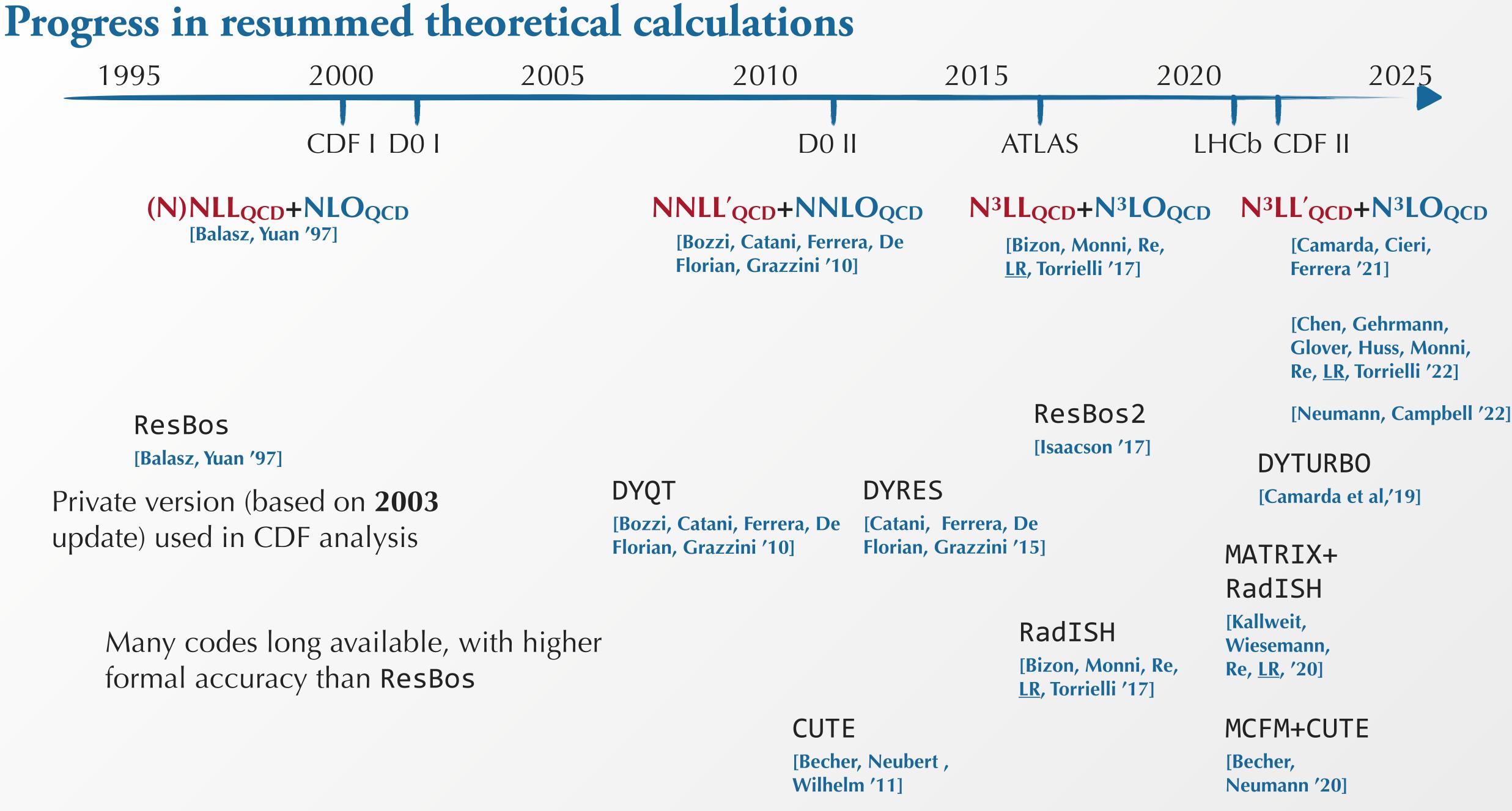
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modelling with PHOTOS+HORACE



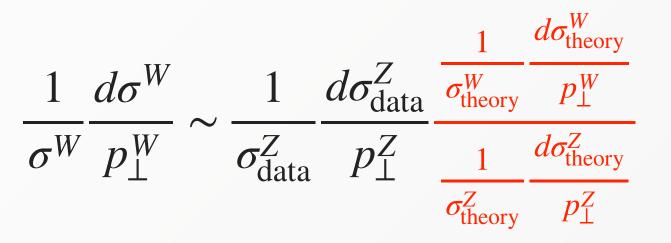






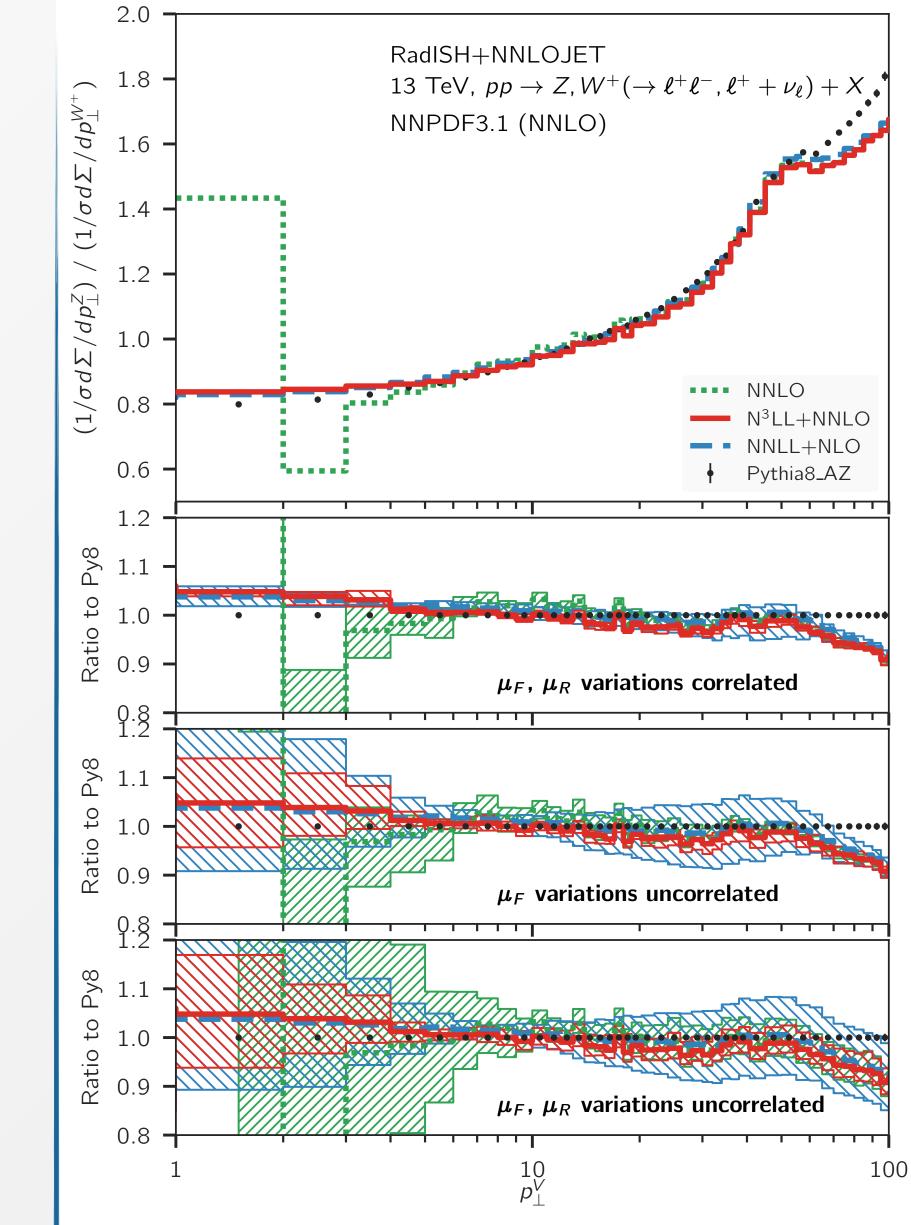


Possible to assess behaviour of the perturbative series at higher orders for crucial observables such as p_T^Z/p_T^W ratio

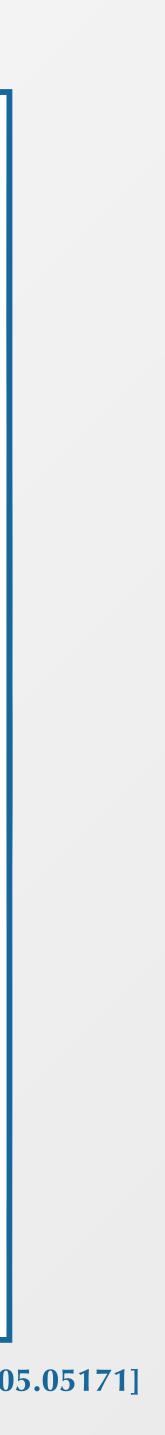


Stability of the ratio indicates high level of correlation between the two spectra

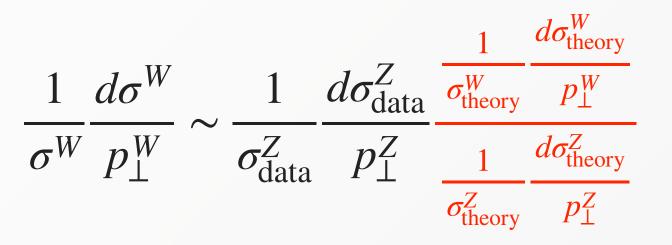
Comparison with tuned event generator such as PYTHIA* however indicates that full correlation might be too strong an assumption



[Bizon, de Ridder, Gehrmann, Glover, Huss, Chen, Monni, Re, <u>LR</u>, Walker, 1905.05171] Topical Seminar on Subnuclear Physics "The W boson mass puzzle", Dec 13 2022

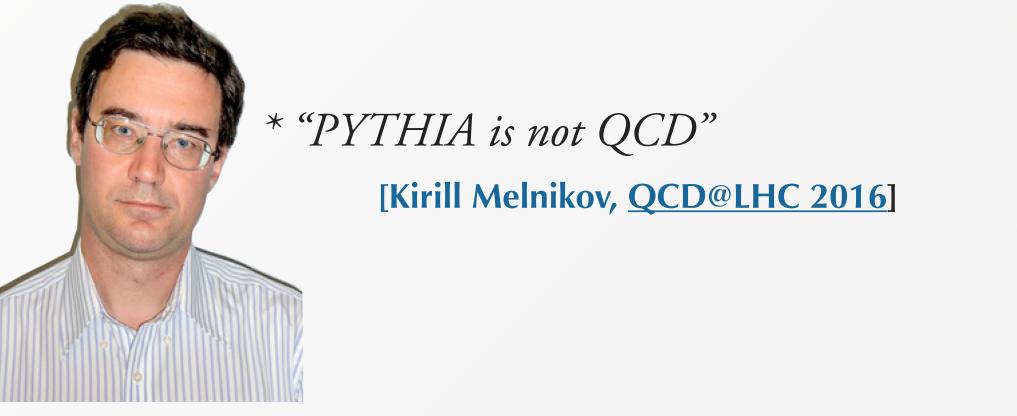


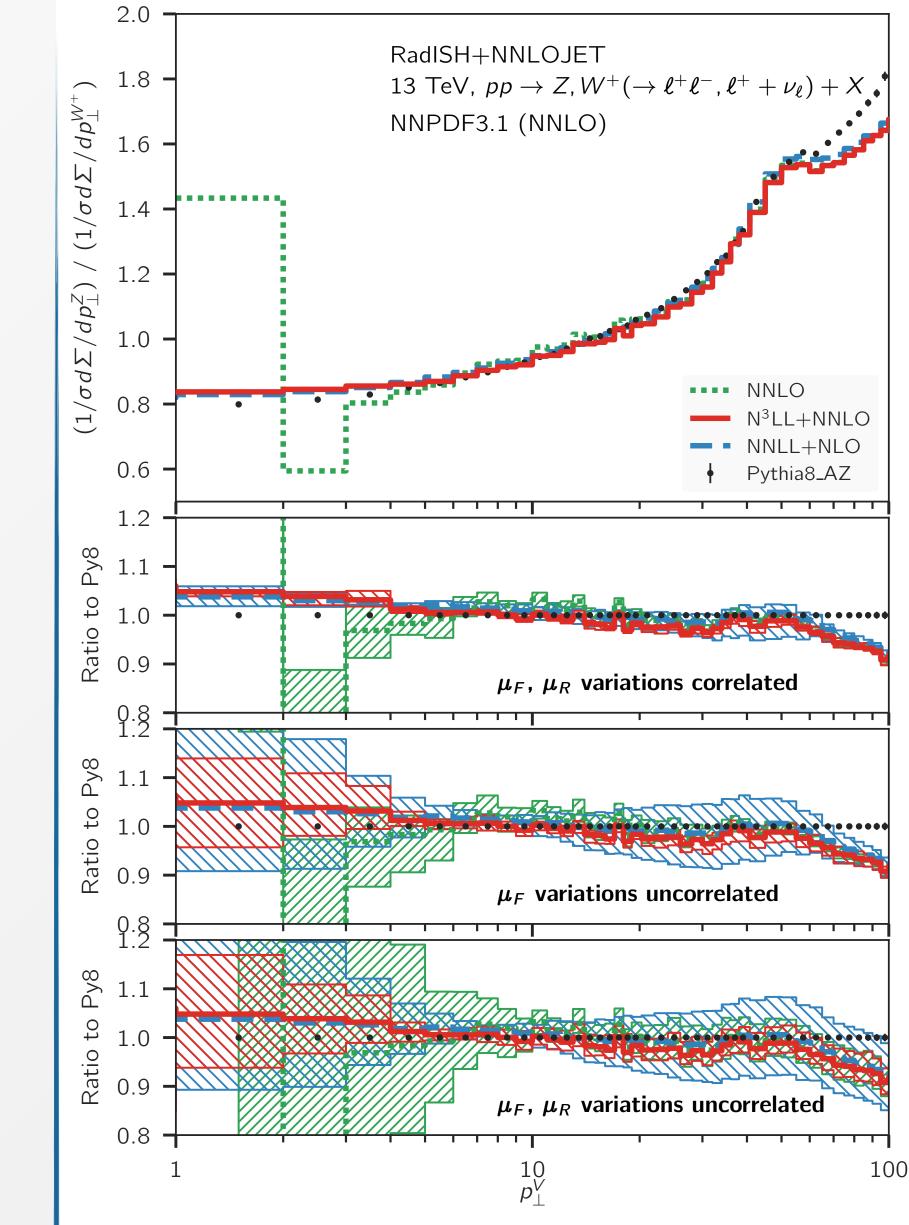
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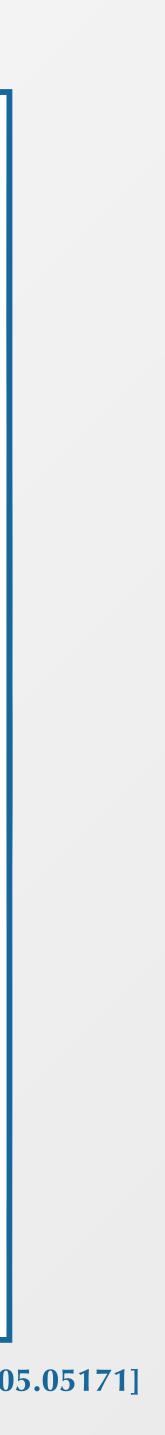
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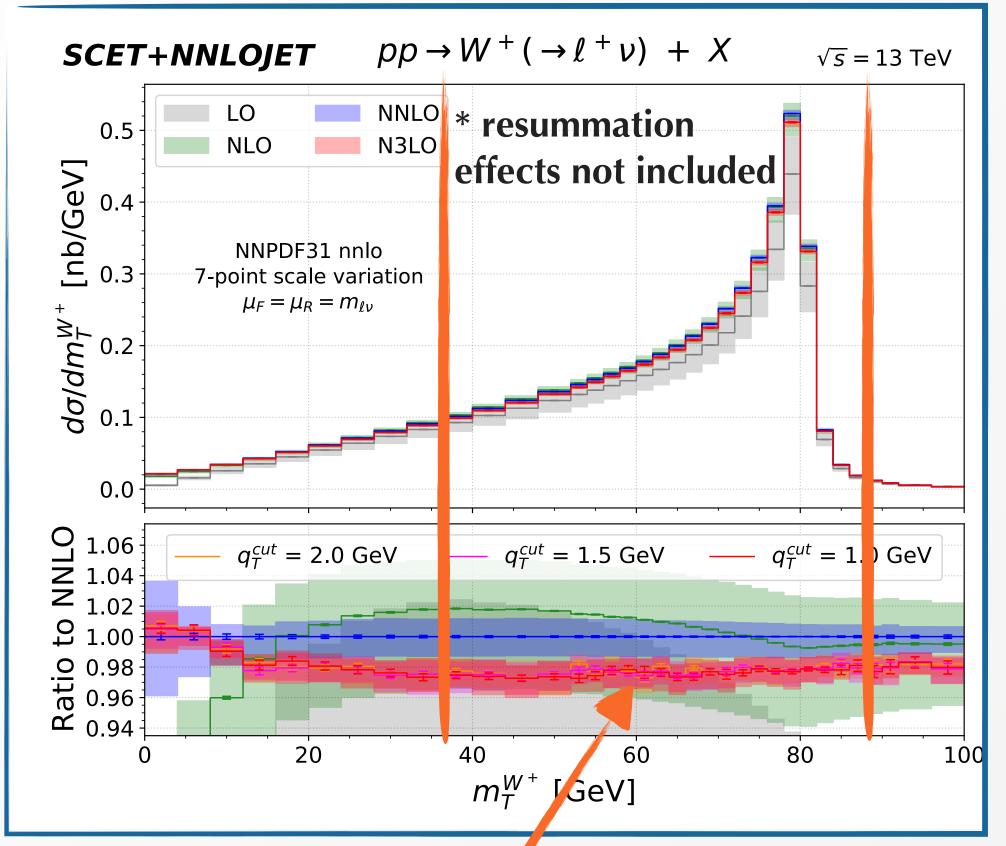




[Bizon, de Ridder, Gehrmann, Glover, Huss, Chen, Monni, Re, <u>LR</u>, Walker, 1905.05171] Topical Seminar on Subnuclear Physics "The W boson mass puzzle", Dec 13 2022

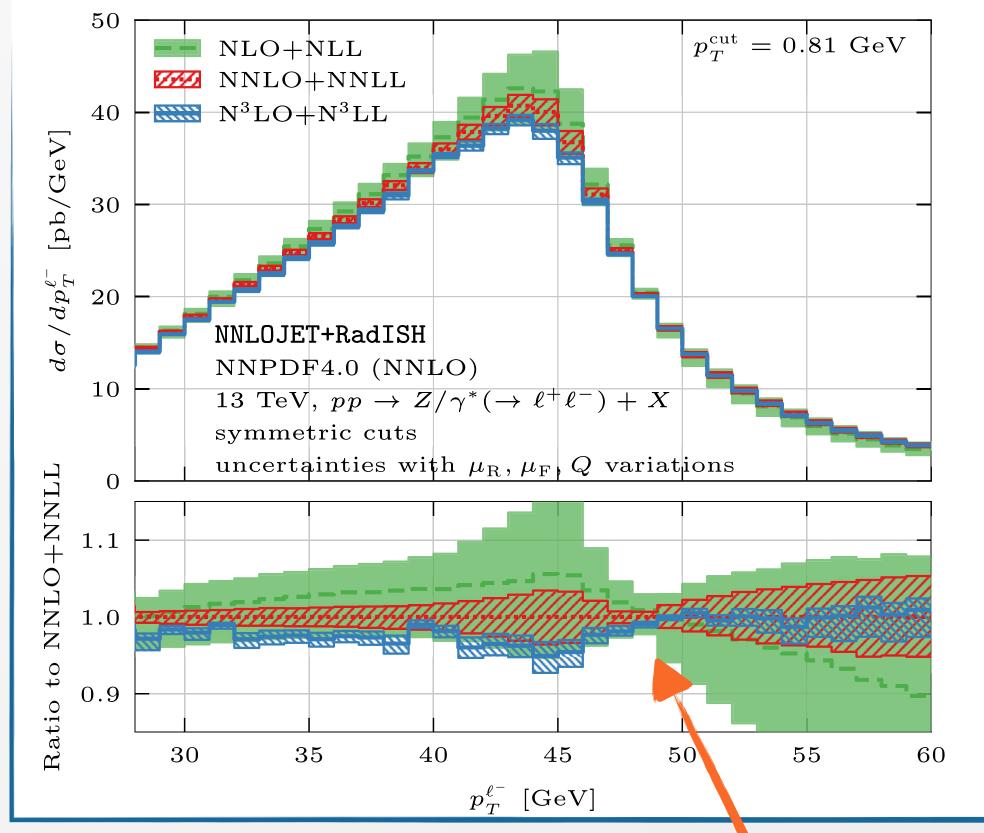


Shape of differential spectra is affected by higher order predictions



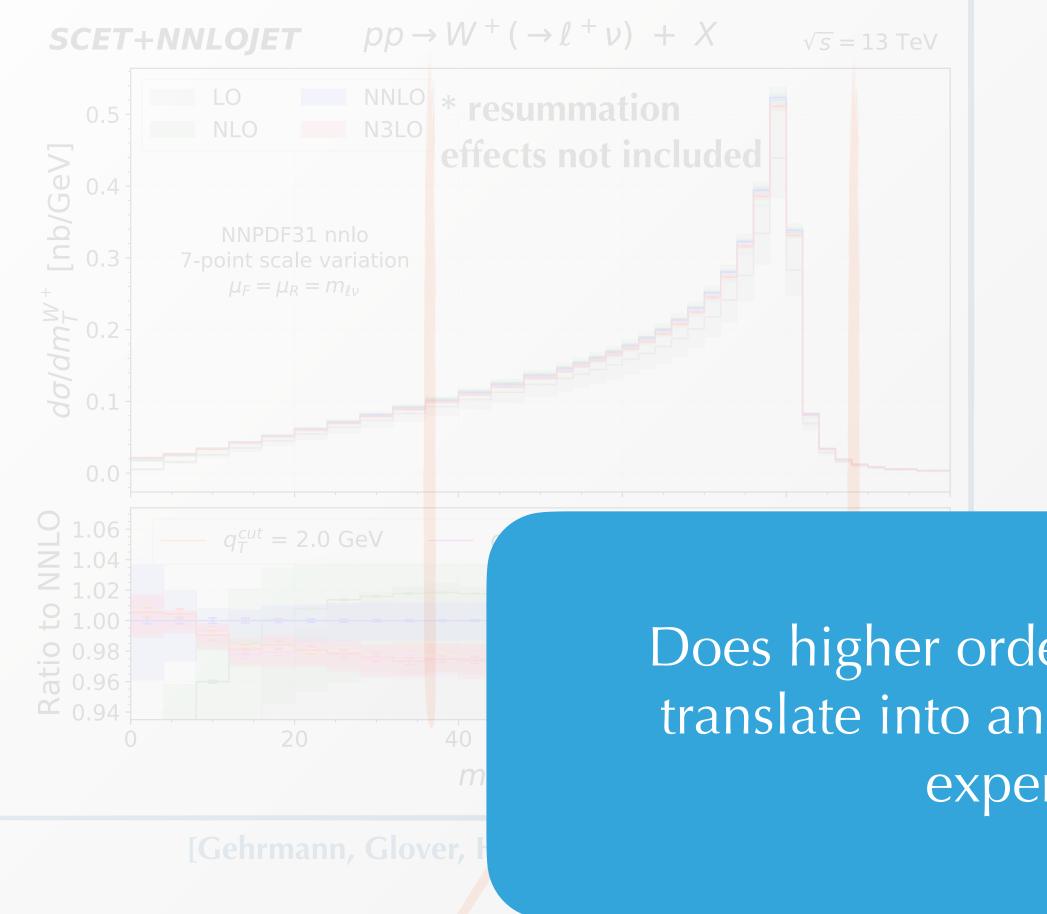
[Gehrmann, Glover, Huss, Chen, Yang, Zhu 2205.11426]

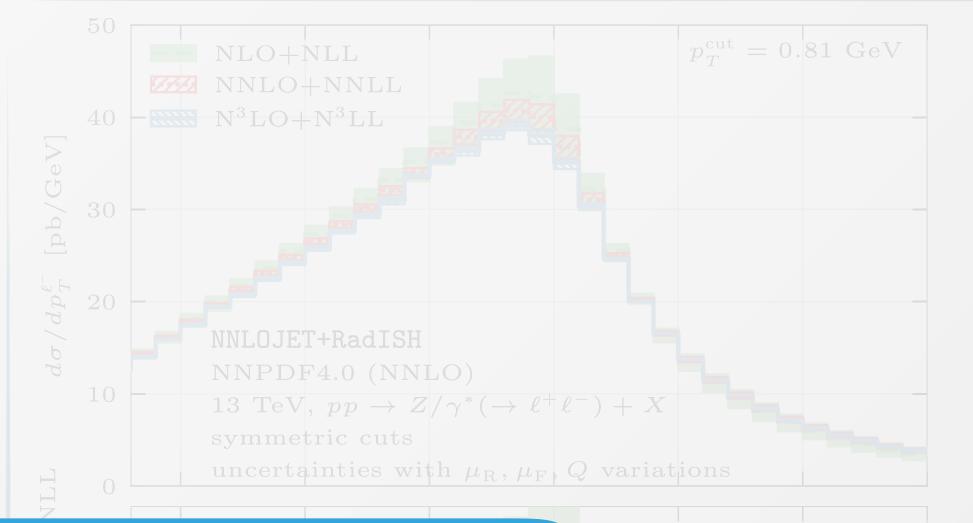
Impact of N³LO_{QCD} corrections relatively flat in the fit window for m_T



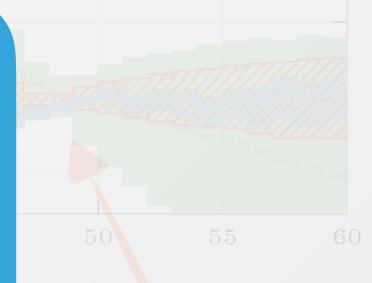
[Gehrmann, Glover, Huss, Chen, Monni, Re, LR, Torrivelli, 2203.01565]

N³LL'_{QCD}+N³LO_{QCD} modifies the shape after the Jacobian peak for p_T^{ℓ}

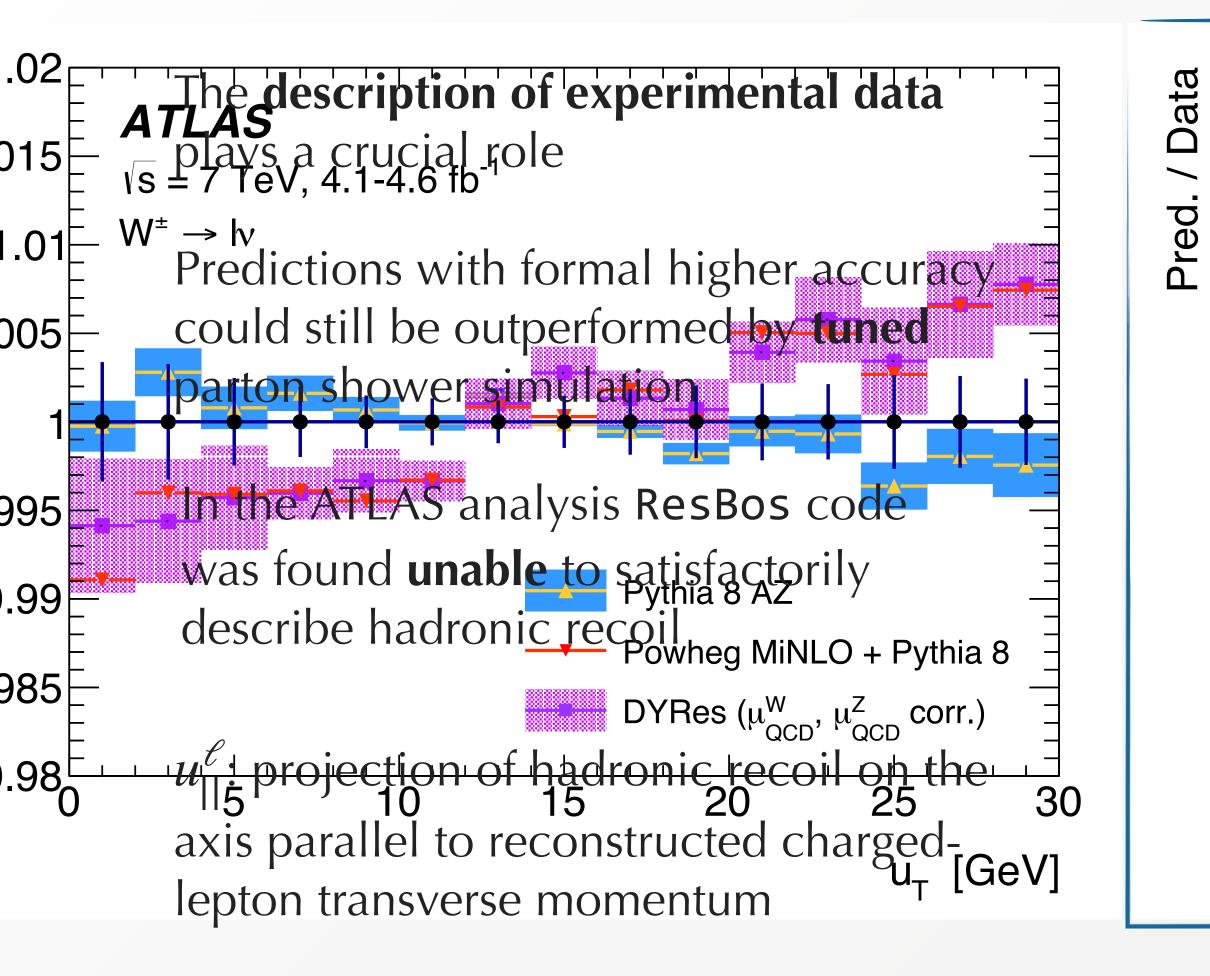


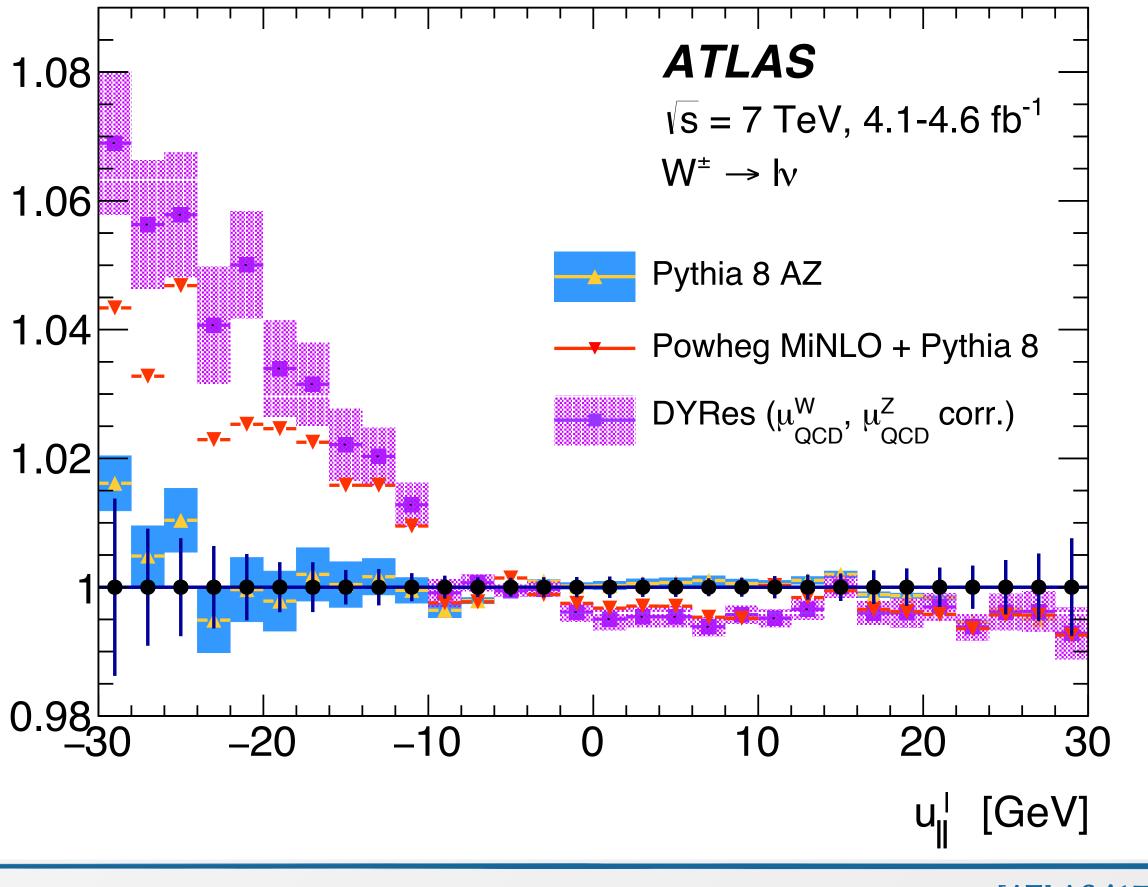


Does higher order accuracy automatically translate into an improved description of experimental data?



after the Jacobian peak for p_T^{t}





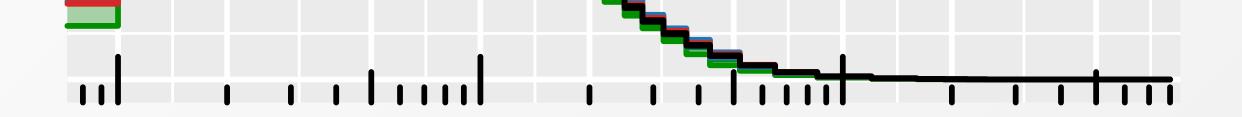
[ATLAS '17]

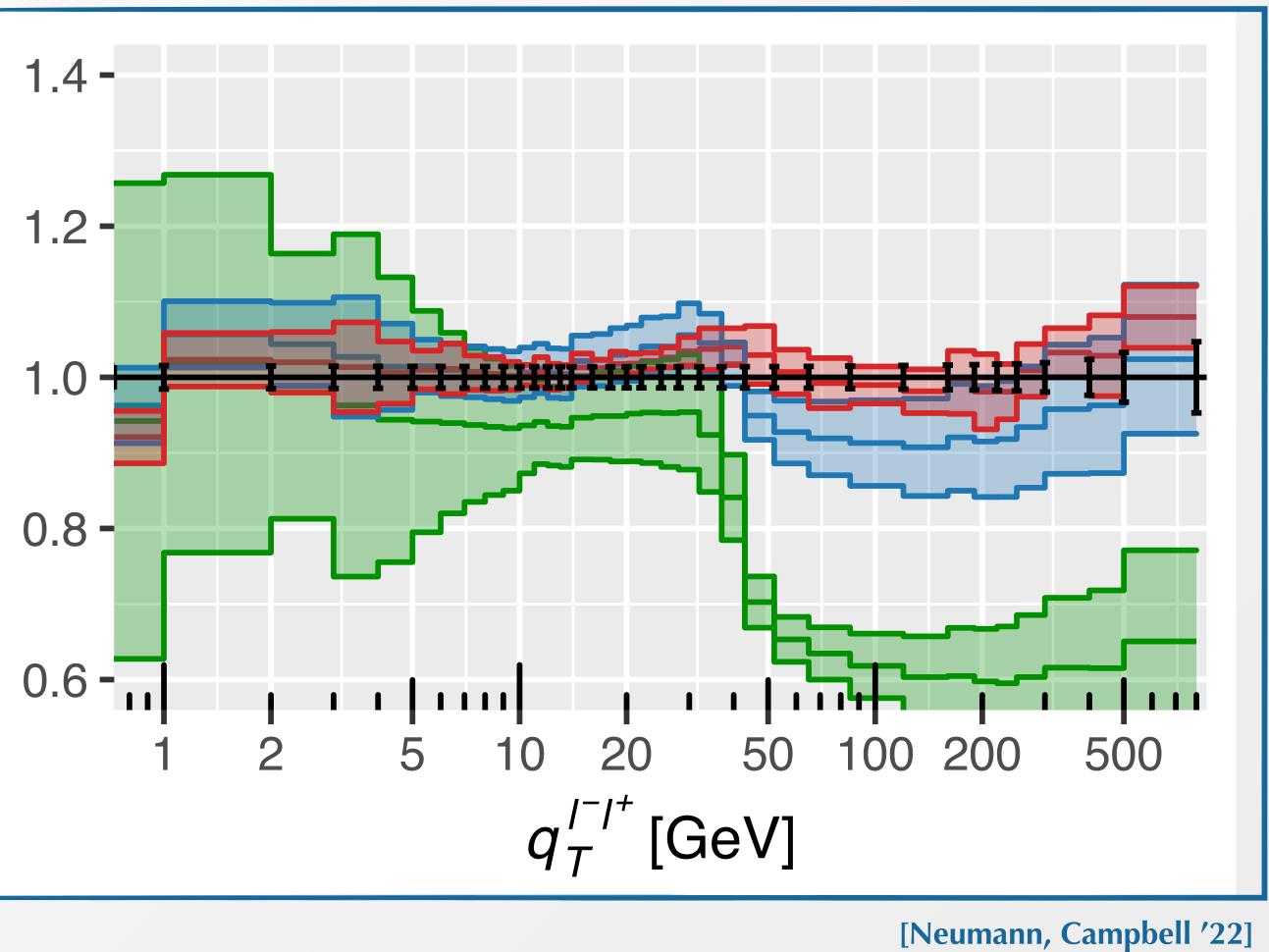
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The theoretical progress made in the the past 5 years has **significantly improved** the description of the experimental data, pinning down the theoretical uncertainties to the **few** percent level in the description of differential spectra

blue curve: NNLL'_{QCD}+NNLO_{QCD}

red curve: N³LL'_{QCD}+N³LO_{QCD}

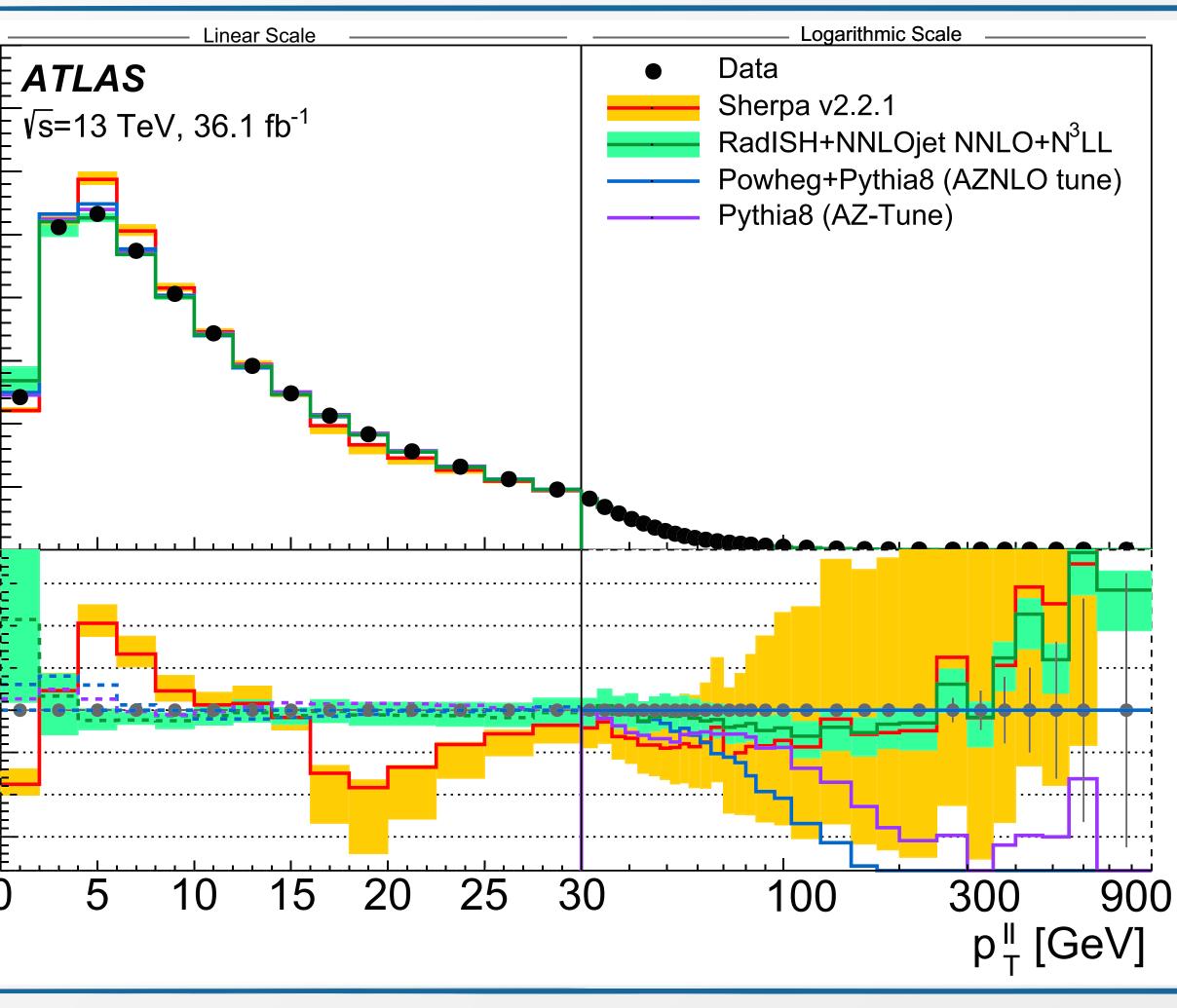




Theoretical predictions now are capable of describing the data **precisely** across a wide range of scales

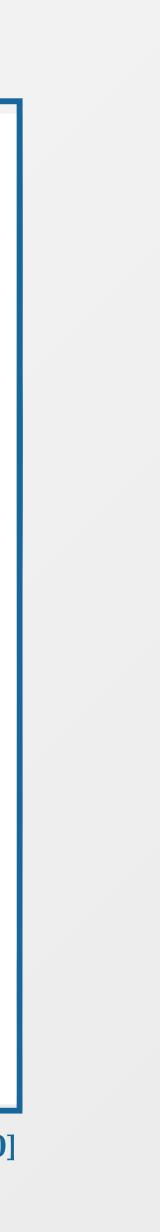
green curve: N³LL_{QCD}+N³LO_{QCD}

0.08 > 0.07 90.06 0.05 0.04 1/σ 0.03 0.02 0.01⊱ Data 1.15 .05 MC 0.95 0.9 0.85 0



[ATLAS '20]

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Theoretical predictions now are capable of describing the data **precisely** across a wide range of scales

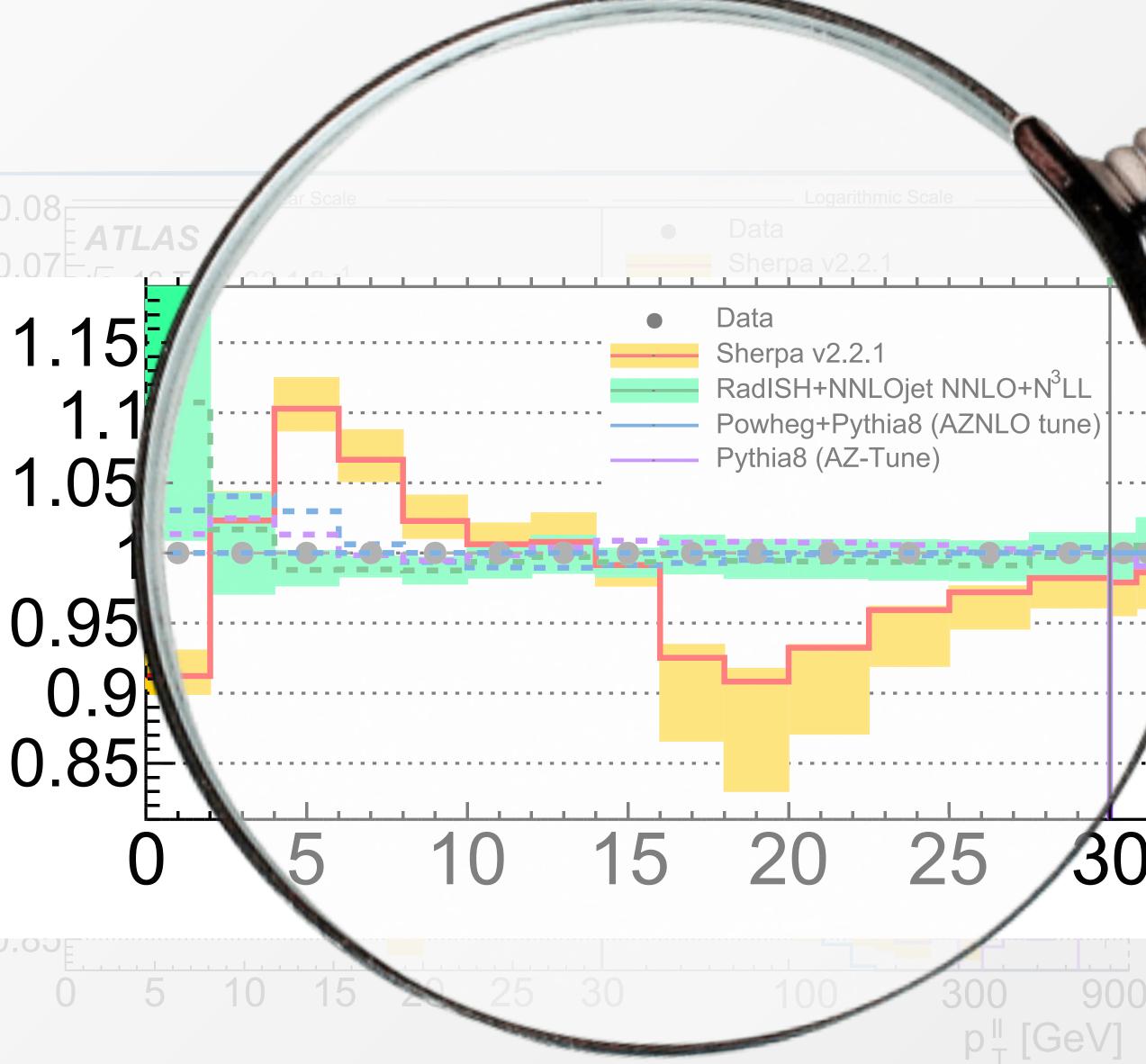
green curve: N³LL_{QCD}+N³LO_{QCD}

And are on par, if not better, than parton showers predictions that have been **tuned to experimental data**

R · Pa

N.B. : RadISH+NNLOJET predictions do not include any non-perturbative modelling at low q_T

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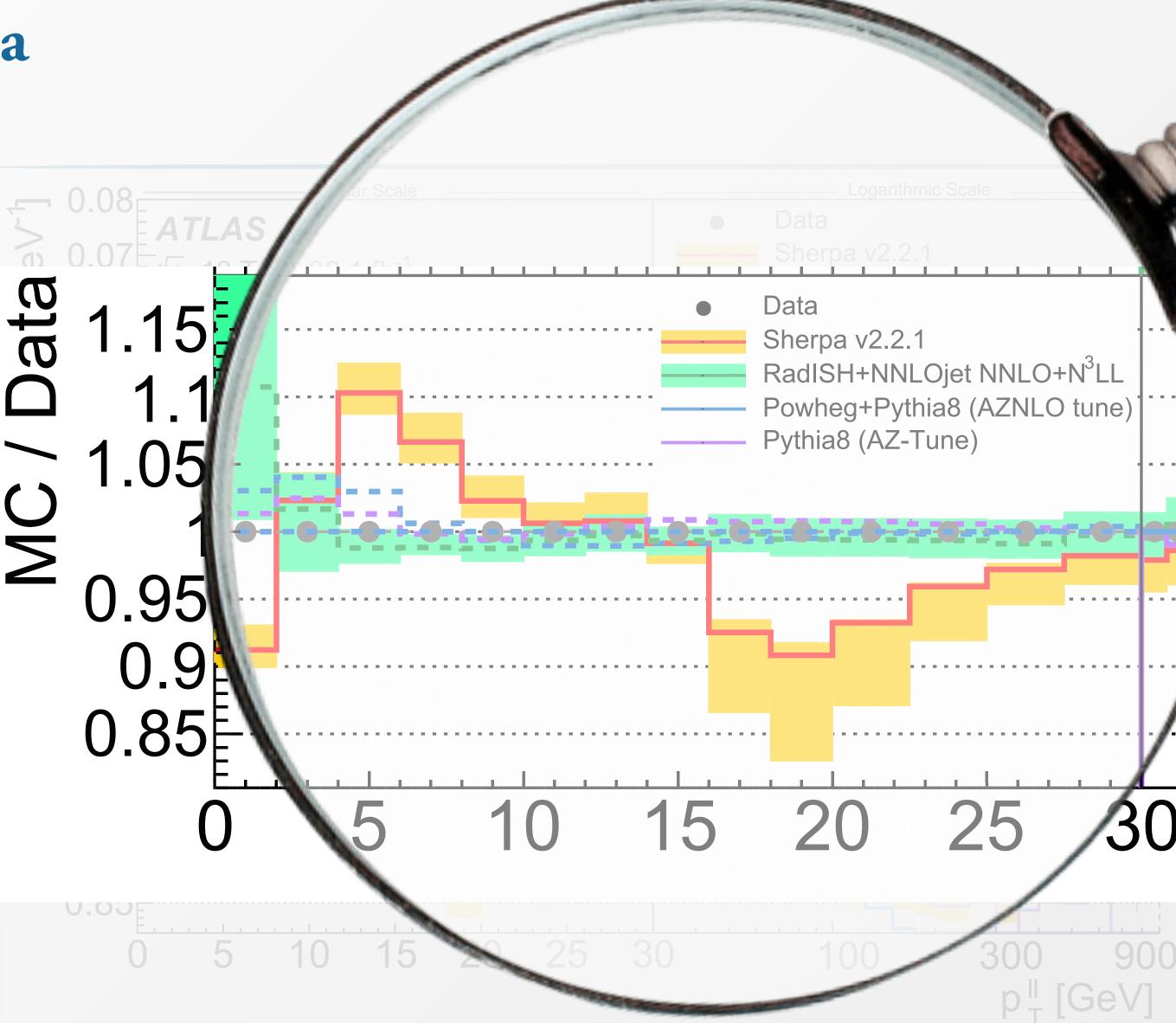
ATLAS '20

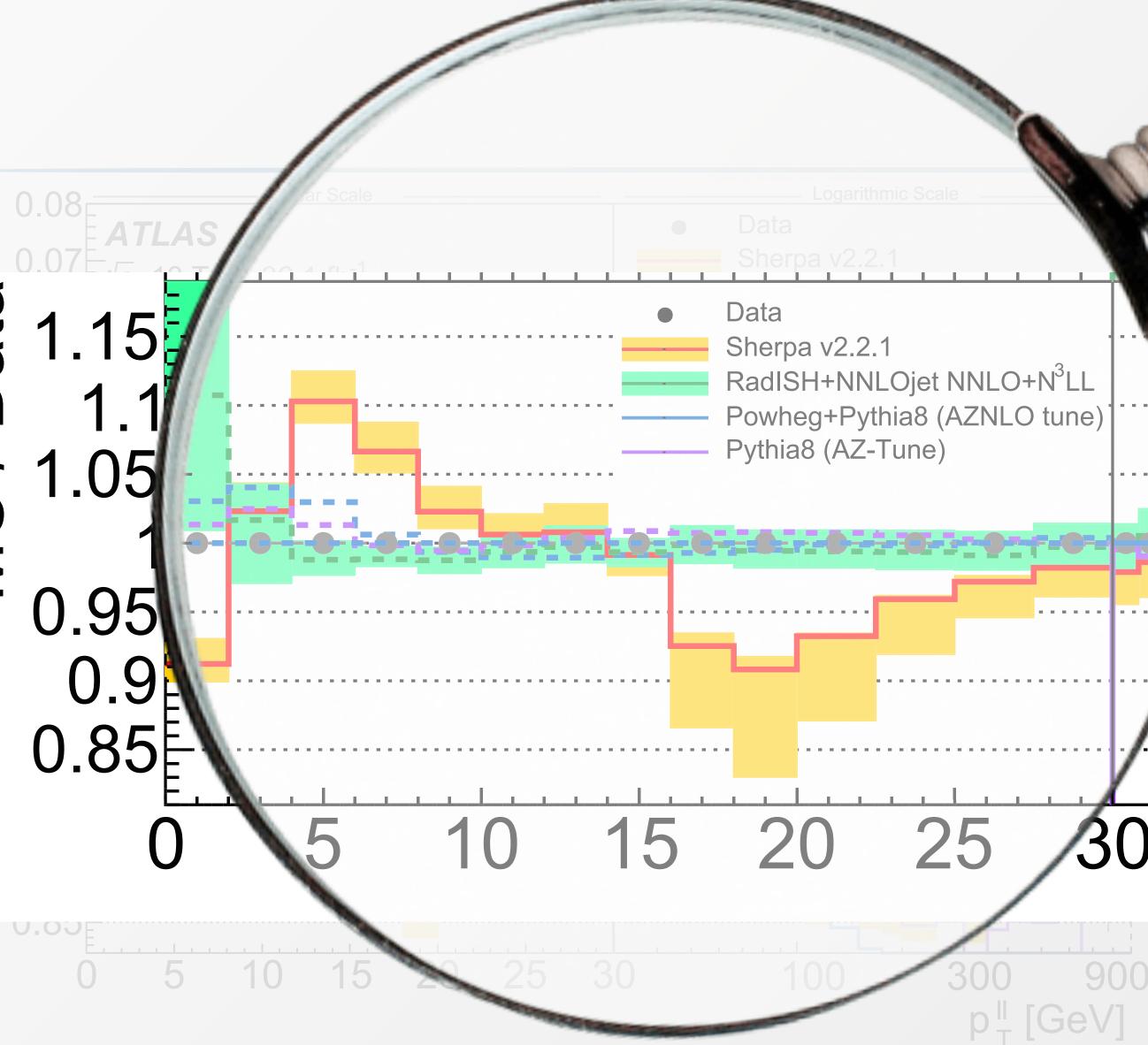


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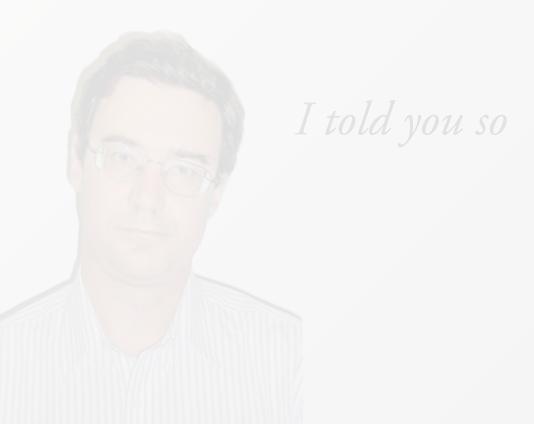


I told you so



capable of describing the data **precisely**

predictions that have been tuned to experimental data

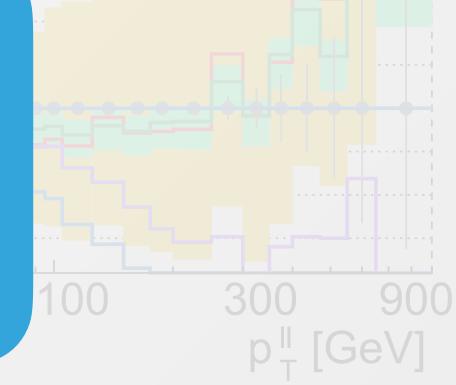


What is the impact of **higher-order** predictions on the extraction of m_W?

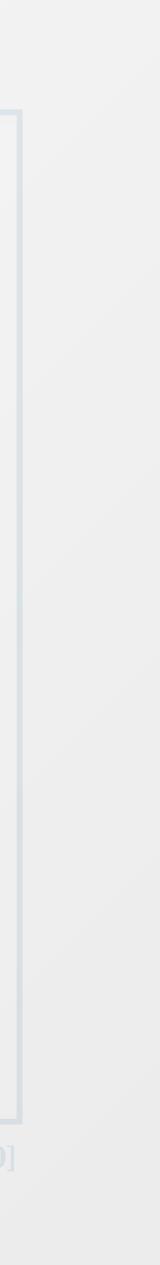
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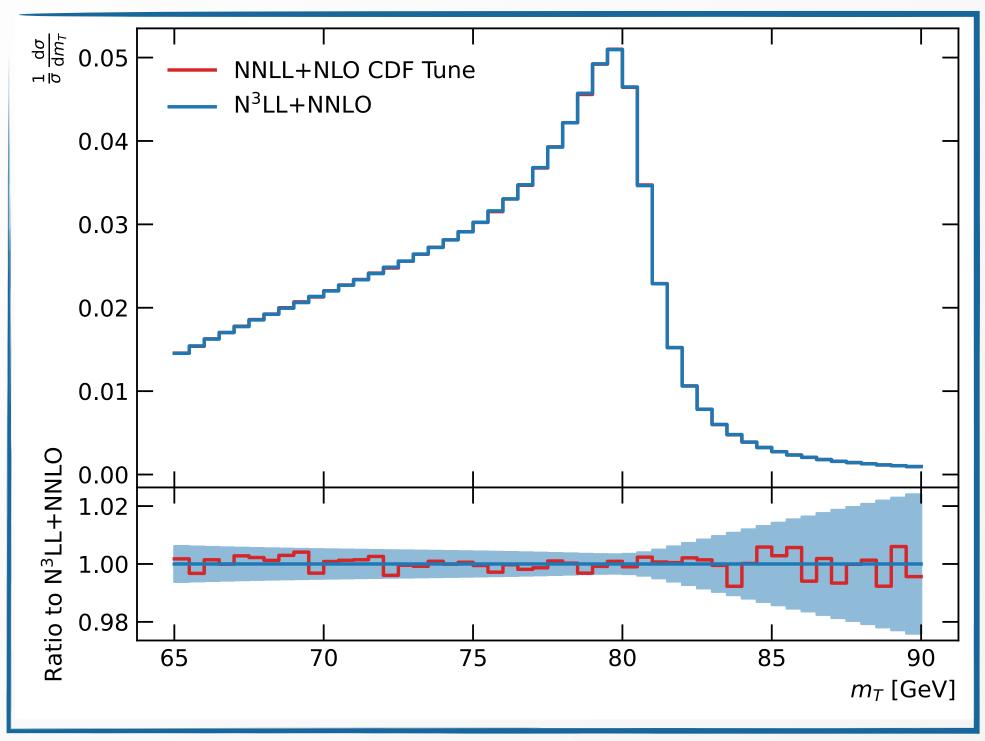


N.B.: RadISH+NNLOJET predictions do not



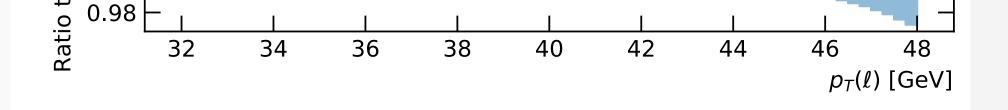
Higher order effects and tuning

Impact of MHOU estimated comparing ResBos2 (N³LL_{QCD}+(N)NLO_{QCD}) to ResBos ((N)NLL_{QCD}+(N)LO_{QCD}) [Isaacson, Fu, Yuan 2205.02788] [CERN-LPCC-2022-06]



another tool necessary to confirm these estimates

Although it is not realistic to assume that each analysis could be performed multiple times with different tools, the impact of varying the underlying QCD model should be assessed, see e.g. recent LHCb analysis



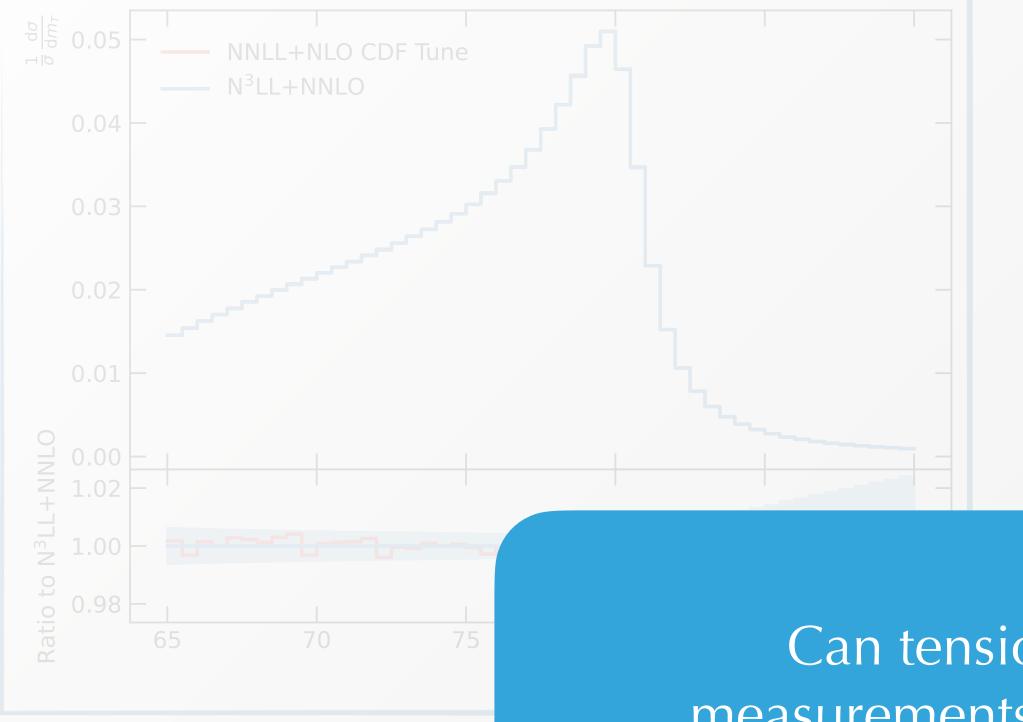
1. ResBos first tuned to reproduce ResBos2 for Z pT ^a² operedictions computed for W NULL + NLO CDE Tune distribution and compared to ResBos2 results Shift_estimated to be $\mathcal{O}(10 \text{ MeV})$ towards the SM results Is **a** MeV to be interpreted just as a shift or as estimate for the **theory uncertainty**? 1 - 2 MeV) uncertainty quoted in GDF II Iszit legitimate to allow for variations of parameters of the perturbative component (such as α_1) to describe data? $p_T(v)$ [GeV]

Is this estimate stable upon variations of the underlying resummation formalism? Independent analysis with





Higher order effects and tuning



Is this estimate stable up another tool necessary t

the impact of varying the underlying QCD model should be assessed, see e.g. recent LHCb analysis

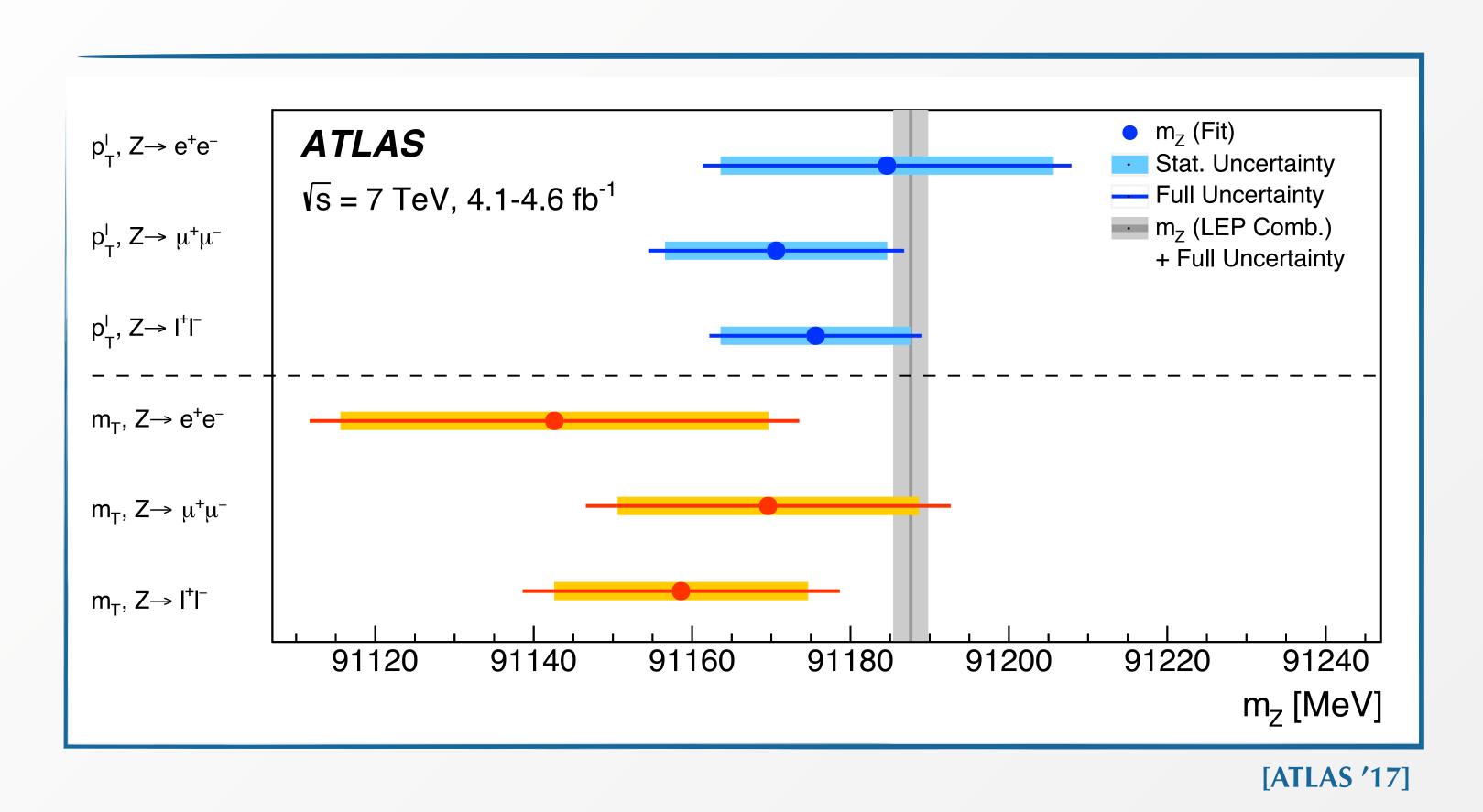
- 1. ResBos first tuned to reproduce ResBos2 for Z pT

- Is 10 MeV to be interpreted just as a shift or as estimate for the **theory uncertainty**?

Cfr. O(1 - 2 MeV) uncertainty quoted in CDF II

Can tension with SM and other measurements be explained entirely by missing higher order effects?

Controlling systematics

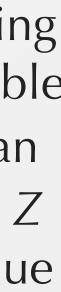


Robust check of many underlying systematics (although not sensible to modelling of p_T^Z/p_T^W ratio) can be performed by extracting the *Z* mass using template fit technique

"Quia vidisti me, credidisti; beati, qui non viderunt et crediderunt"

Johannes 20, 29

[because thou hast seen me, thou hast believed: blessed are they that have not seen, and yet have believed]



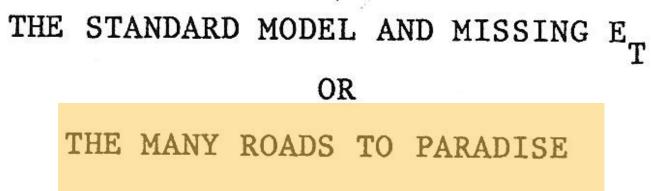


CERN - Geneva

cuts. We are thus able to sum the contributions of MANY SMALL sources which were absent in previous studies and which can, in the sum, yield a sizeable result. These are the "many roads" of the title. [This concern, that many small numbers can yield a large sum, was colourfully voiced at the meeting by G. Altarelli who described his vision of a mixture of small effects -- the Altarelli cocktail -- leading to the observed signal.] Before proceeding to the

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Ś



Stephen D. Ellis[#]

Template fits on shapes and their limitations

Template fit strategy relies on **tuning** of the model parameters, both perturbative and non-perturbative (strong coupling, non-perturbative component, intrinsic k_T) to fit p_T^Z

Program	χ^2/ndf	$lpha_s$	
DYTURBO	208.1/13	0.1180	$g = 0.523 \pm 0.047 \mathrm{GeV}^2$
POWHEGPythia	30.3/12	0.1248 ± 0.0004	$k_{\rm T}^{\rm intr} = 1.470 \pm 0.130 { m GeV}$
POWHEGHERWIG	55.6/12	0.1361 ± 0.0001	$k_{\rm T}^{\rm intr} = 0.802 \pm 0.053 { m GeV}$
HERWIG	41.8/12	0.1352 ± 0.0002	$k_{\rm T}^{\rm intr} = 0.753 \pm 0.052 {\rm GeV}$
Pythia, CT09MCS	69.0/12	0.1287 ± 0.0004	$k_{\rm T}^{\rm intr} = 2.113 \pm 0.032 {\rm GeV}$
Pythia, NNPDF31	62.1/12	0.1289 ± 0.0004	$k_{\rm T}^{\rm intr} = 2.109 \pm 0.032 {\rm GeV}$

Value of χ^2 lowered considerably after the fit, where good description of the data can be achieved

Result of the fit (default model of LHCb requires $\alpha_s \sim 0.130$) begs the question whether the QCD modelling has anything to do with perturbative QCD

Theory errors cannot be accommodated easily in the fitting procedure unless one uses a probabilistic definition of the theory uncertainty (which requires to go beyond canonical scale variation)

[LHCb '21]

[Cacciari, Houdeau 1105.5152] [Bonvini 2006.16293]

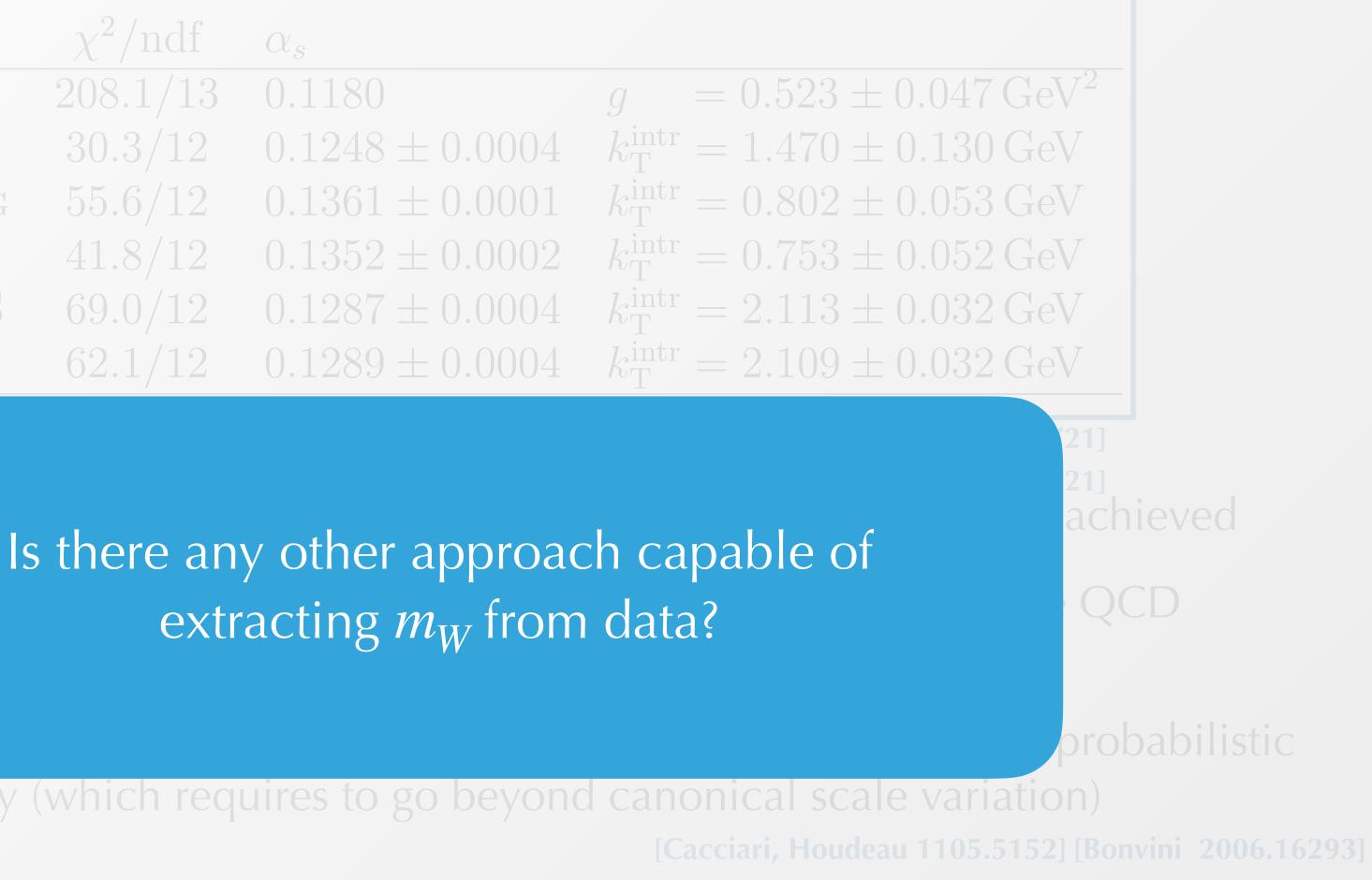
Template fits on shapes and their limitations

Template fit strategy relies on tuning of the model parameters, both perturbative and non-perturbative

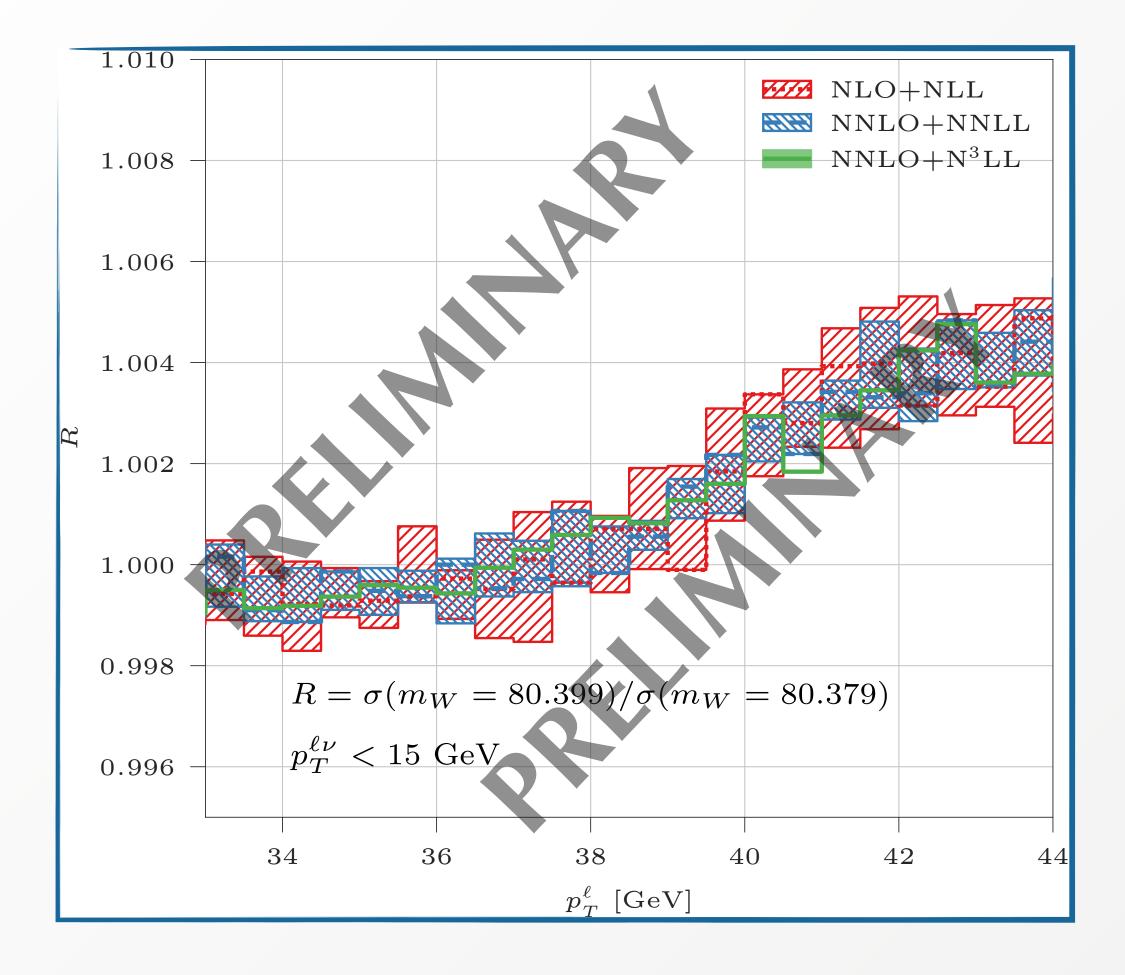
Program	χ^2/ndf	$lpha_s$
DYTURBO	208.1/13	0.11
POWHEGPYTHIA	30.3/12	0.12
POWHEGHERWIG	55.6/12	0.13
HERWIG	41.8/12	0.13
Pythia, CT09MCS	69.0/12	0.12
Pythia, NNPDF31	62.1/12	0.12

Value of χ^2 lowered con

Theory errors cannot be definition of the theory uncertainty (which requires to go beyond canonical scale variation)



The p_T^{ℓ} spectrum and its sensitivity to m_W



Sensitivity on m_W of the bins of the p_T^{ℓ} distribution can be quantified by means of the covariance matrix with respect to m_W variations

$$C_{ij} = \langle \sigma_i \sigma_j \rangle - \langle \sigma_i \rangle \langle \sigma_j \rangle$$

The eigenvalues of this matrix express sensitivity on m_W on linear combinations of bins of the distribution

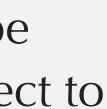
Large hierarchy between the first eigenvalue and the others, suggesting that the majority of the sensitivity is captured by the largest eigenvalue

Coefficients **changes sign** around $p_T^{\ell} \simeq 37$ GeV

Motivates definition of a scalar variable sensitive to *m*_W

$$\mathscr{A}(p_{T,\min}^{\ell}, p_{T,\min}^{\ell}, p_{T,\max}^{\ell}) = \frac{\sigma(p_{T,\min}^{\ell}, p_{T,\min}^{\ell}) - \sigma(p_{T,\min}^{\ell}, p_{T,\max}^{\ell})}{\sigma(p_{T,\min}^{\ell}, p_{T,\min}^{\ell}) + \sigma(p_{T,\min}^{\ell}, p_{T,\max}^{\ell})}$$

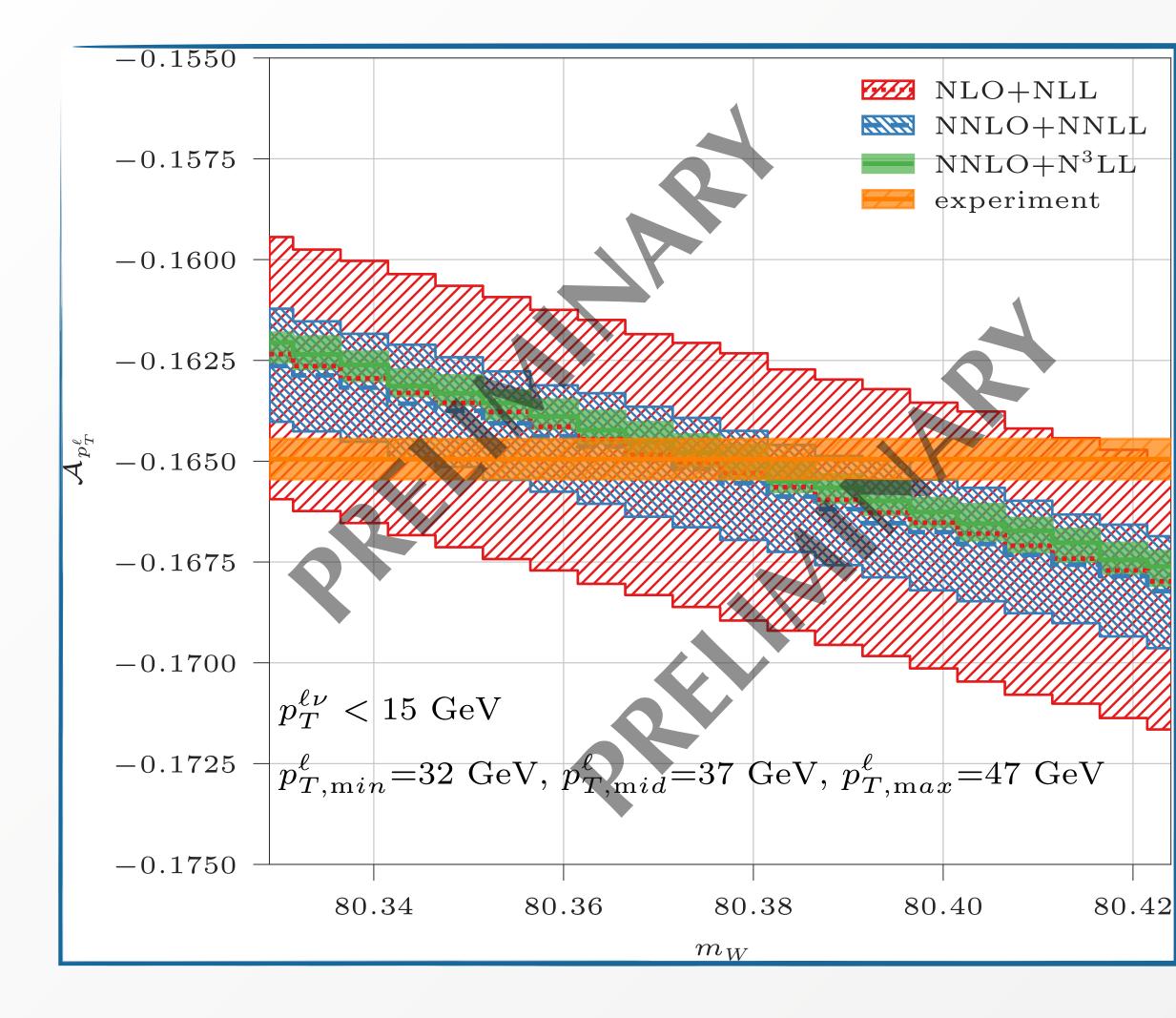








A scalar observable sensitive to m_W



$$\mathscr{A}(p_{T,\min}^{\ell}, p_{T,\min}^{\ell}, p_{T,\max}^{\ell}) = \frac{\sigma(p_{T,\min}^{\ell}, p_{T,\min}^{\ell}) - \sigma(p_{T,\min}^{\ell}, p_{T,\min}^{\ell})}{\sigma(p_{T,\min}^{\ell}, p_{T,\min}^{\ell}) + \sigma(p_{T,\min}^{\ell}, p_{T,\min}^{\ell})}$$

Sensitivity on m_W expressed by the slope of the asymmetry

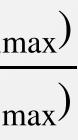
Large size of the two intervals reduces the statistical error and improves the quality of the detector effects unfolding

Perturbative convergence of the observable can be studied for different intervals $[p_{T,\min}^{\ell}; p_{T,\min}^{\ell}; p_{T,\min}^{\ell}; p_{T,\max}^{\ell}]$

Missing higher order uncertainty can be estimated by means of scale variations

Extraction can rely only on the information of the charged-current Drell-Yan process











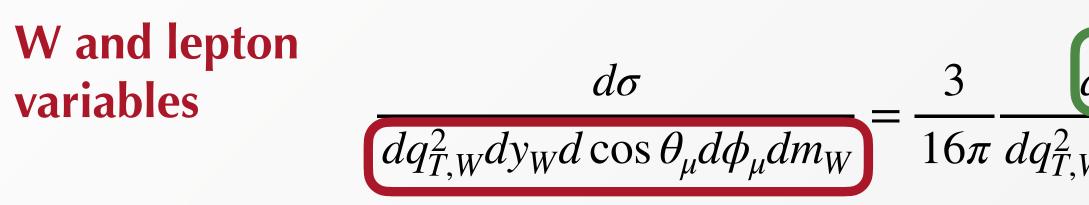
Data-driven approach to m_W extraction

A theory-agnostic extraction of m_W

[E. Manca, PhD Thesis 2016; V. Bertacchi, Tesi di Perfezionamento 2021]

Exploit statistics collected by CMS during Run II at the LHC to extract the value of m_W simultaneously with q_T^W , y_W and polarization spectra to obtain a statistically-dominated measurement of m_W

Decoupling of the (unknown) production physics from the (known) decay physics



1. Decompose inclusive $\eta^{\mu} \times p_{T}^{\mu}$ distribution in bins 2. Fit $\eta^{\mu} \times p_{T}^{\mu}$ distribution measured on data 3. Unfolding from the sole lepton kinematics to the underling boson kinematics

unpolarised cross section

$$\frac{d\sigma^{U+L}}{W^{d}W^{d}M_{W}}\left[(1+\cos^{2}\theta_{\mu})+\sum_{i=0}^{7}A_{i}P_{i}(\cos\theta_{\mu},\phi_{\mu})\right]$$
angular coefficients

s of
$$m_{W'}$$
, $Y_{W'}$, q_T^W for each P_i

Conclusion

- Huge progress in the last few years in precise PDF determination, higher-order QCD resummation and mixed QCD and QED corrections
- PDF uncertainty is not a substantial limitation for a precise extraction of m_W
- obtain **reliable estimates** of the theoretical uncertainties
- For such a delicate measurement, complementary approaches to extract m_W and determine its uncertainty should be used to avoid possible biases
- Shape of the p_T^{ℓ} distribution and presence of the Jacobian peak motivates the definition of a scalar performed on shapes
- Data-driven approach provides a valid alternative to extract m_W with a statistical-dominated error

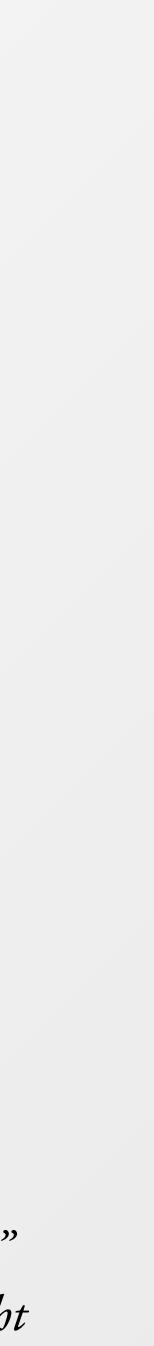
"The aim of science is not to open a door to infinite wisdom, but to set a limit to infinite error" Bertold Brecht

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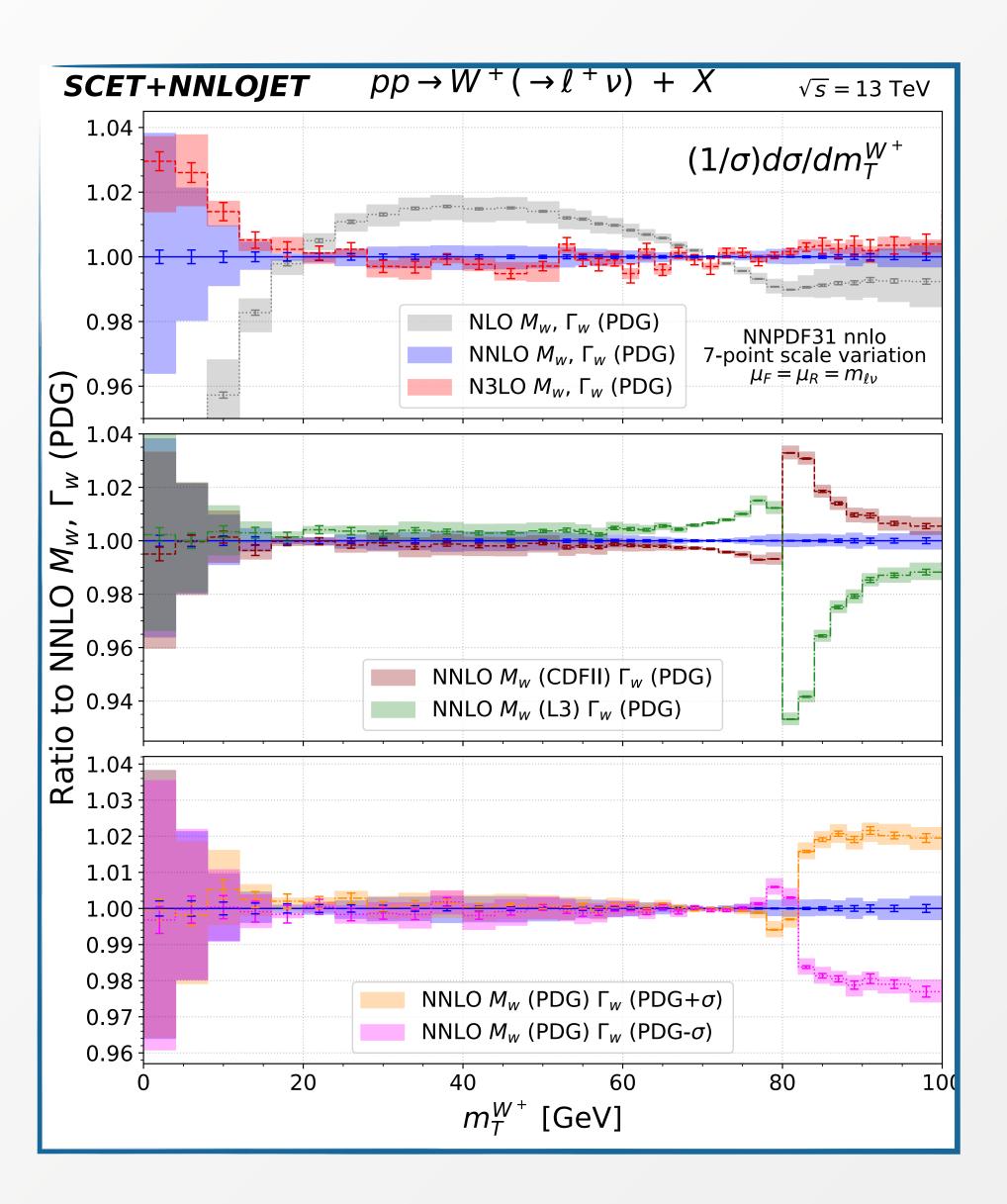
• Extraction of *m_W* mass at hadron colliders requires accurate knowledge of QCD and QED radiation

• Future measurement of m_W should exploit the huge amount of theoretical work in the last 5+ years to

observable which **maximises the sensitivity** on m_W and overcomes some limitations of templates fits





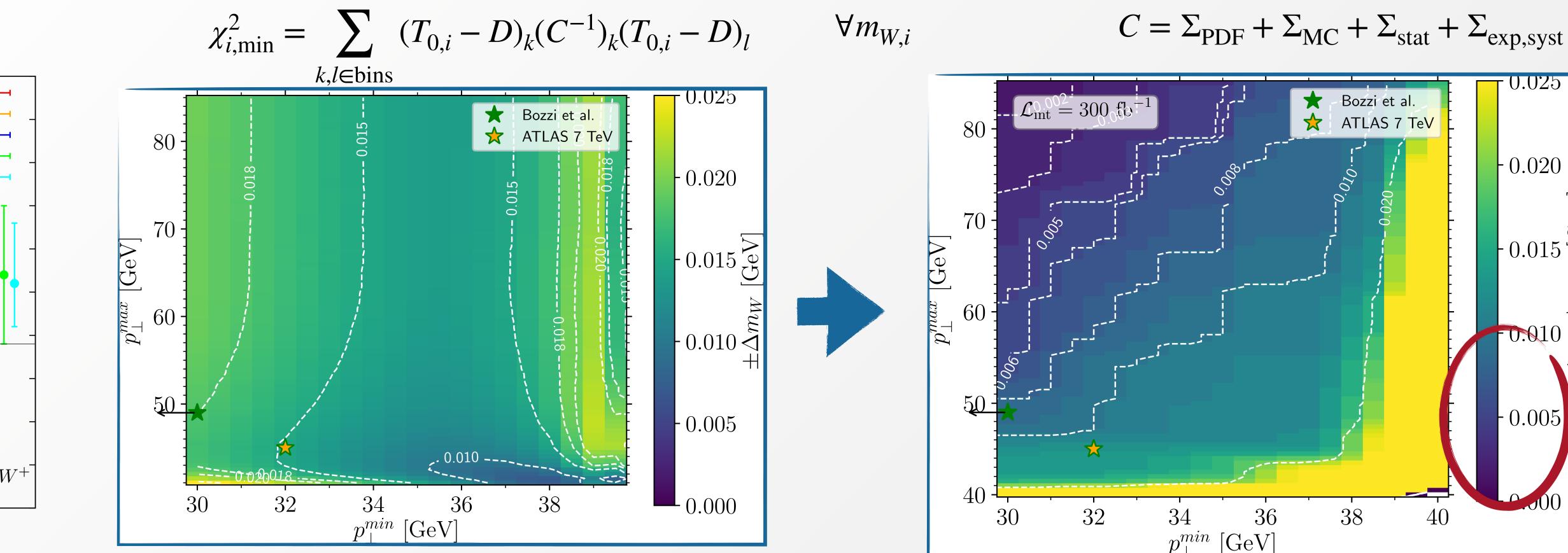


PDFs and their uncertainties: bin-by-bin correlations

This estimate does not take into account **bin-by-bin correlations** between PDF replicas

$$(\Sigma_{\rm PDF})_{ij} = \langle (\mathcal{T} - \langle \mathcal{T} \rangle_{\rm PDF})_i (\mathcal{T} - \langle \mathcal{T} \rangle_{\rm PDF})_j \rangle_{\rm PDFs}$$

Compute χ^2 taking into account bin-by-bin correlations introducing a covariance matrix in the definition



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Reduced sensitivity to the PDF uncertainty, if other source of errors are under control



