

# Theoretical activities supporting the experiments at LNS



**Danilo Gambacurta**

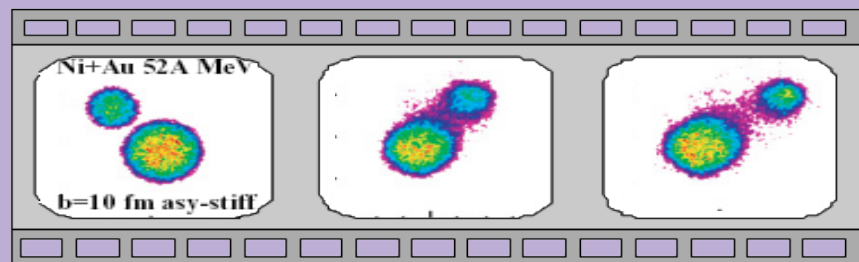
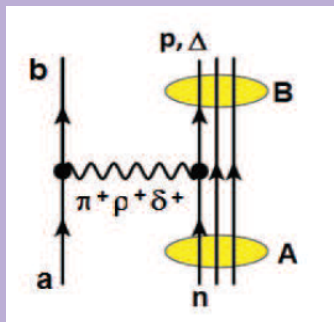
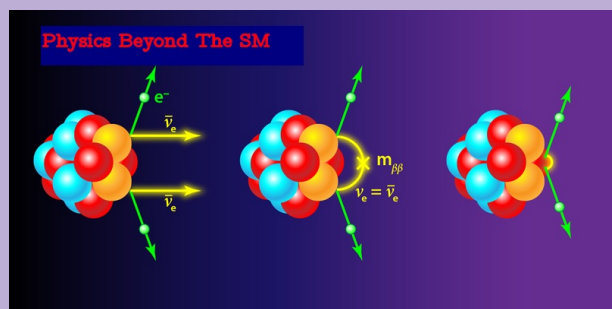
(On behalf of the LNS theoretical group)

Laboratori Nazionali del Sud (Catania)

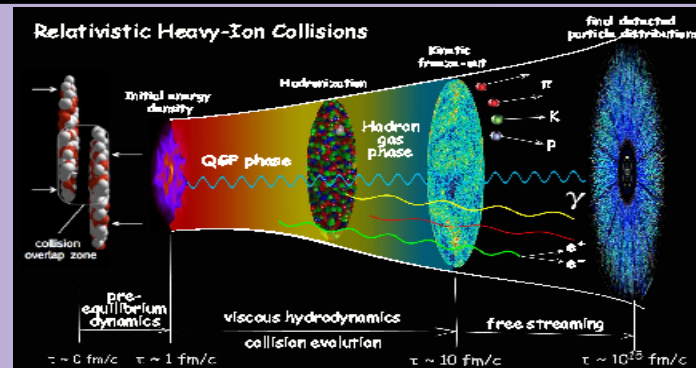
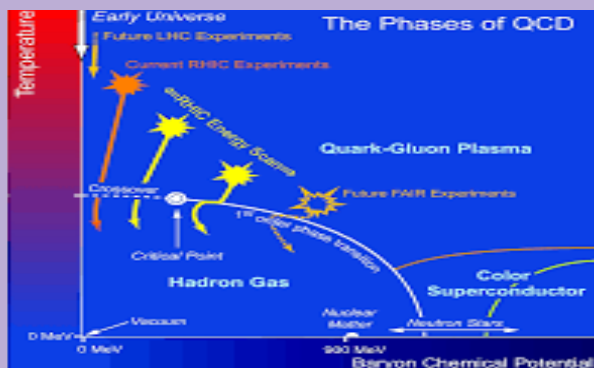
LNS Users Annual Meeting – 19.12.2022

# Research activities within the INFN "Specific Initiatives"

## MONSTRE: MODELing Nuclear STRUCTURE and REactions



## SIM: Strongly Interacting Matter at high density and temperature

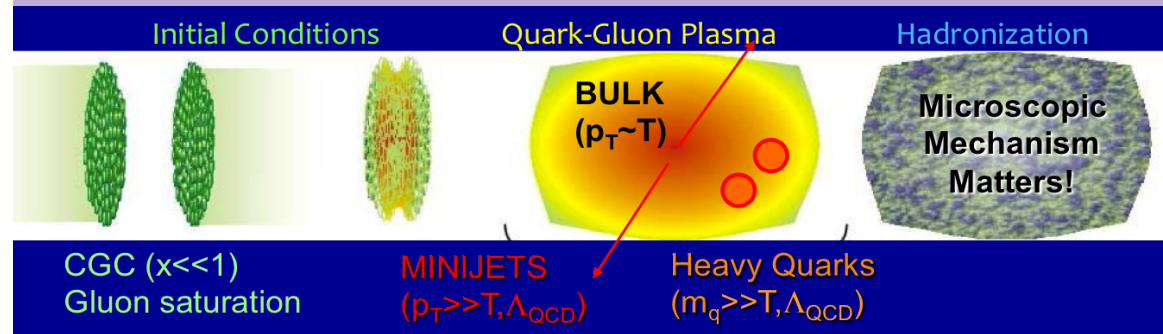
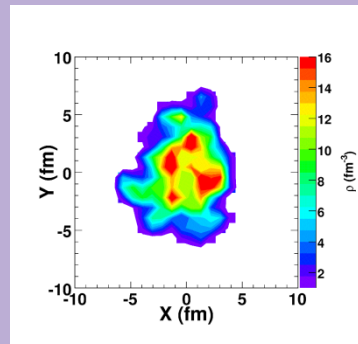
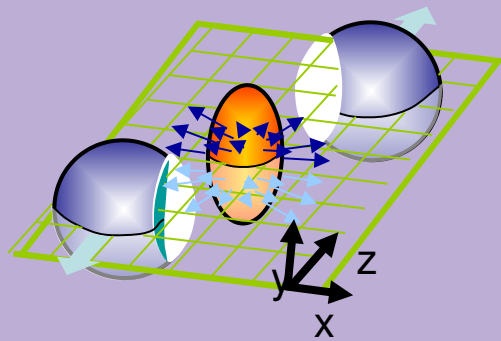


# SIM: Strongly Interacting Matter at high temperature and density

## Phenomenology of Quark Gluon Plasma with Transport Theories

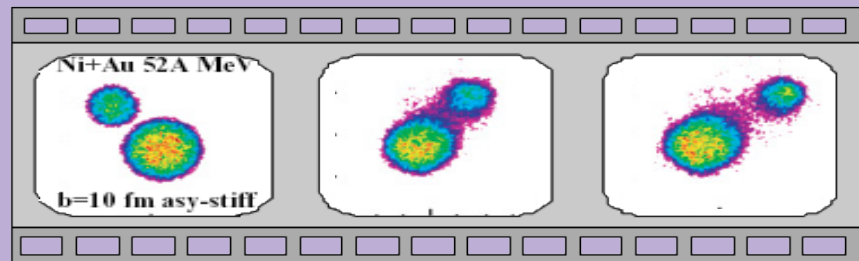
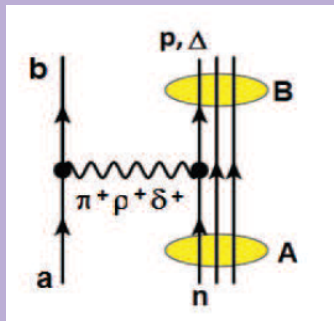
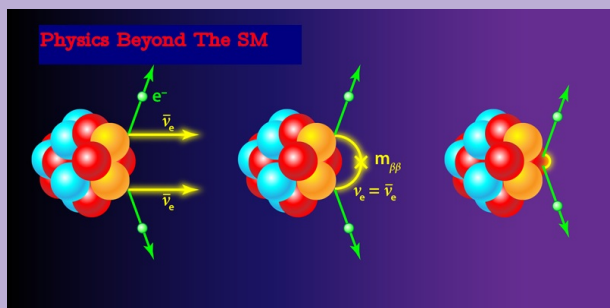
- ❖ Hadronization mechanisms
- ❖ Heavy quark dynamics: charm and bottom
- ❖ Non-equilibrium dynamics in AA, pA and pp collisions

Ref. Prof. V. Greco

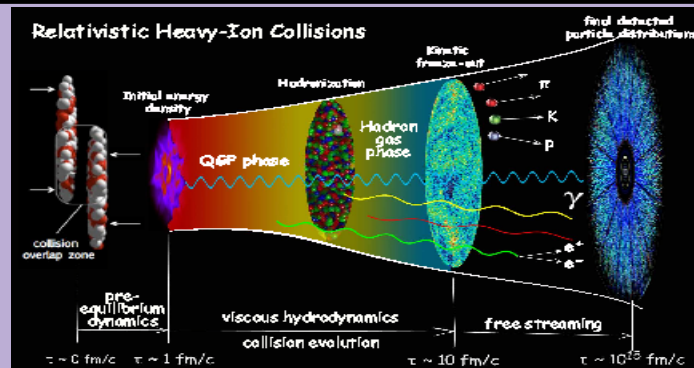


# Research activities within the INFN "Specific Initiatives"

## MONSTRE: MODELing Nuclear STRUCTURE and REactions



## SIM: Strongly Interacting Matter at high density and temperature



# Nuclear Structure Studies

## Theoretical Models and Techniques

- ✓ *Energy Density Functional(EDF) Framework (Skyrme-Gogny)*
- ✓ *HF, HF+BCS, HFB (ground state and low lying spectroscopy)*
- ✓ *RPA, QRPA, Second RPA, TDHF (nuclear response and excitations)*
- ✓ *Spherical and Deformed, also superfluid, systems can be studied*
- ✓ *Transport theories based on EDF*

## Main Physical Cases of Interest

- ✓ *Collective nuclear excitations, especially in neutron-rich and exotic nuclei (Giant Resonances, Pygmy Dipole Resonance, ...)*
- ✓ *EoS of asymmetric matter (symmetry energy, ...)*
- ✓ *Charge exchange excitations (Gamow-Teller, Fermi, etc,)*
- ✓ *Beta Decay (single and double, with or without neutrinos)*
- ✓ *Interdisciplinary aspects between nuclear and neutrino physics*
- ✓ *Proton – Neutron pairing in  $Z \sim N$  nuclei*

# Nuclear Reaction Studies

## Theoretical Models and Techniques

- ✓ *Semi-classical transport theories, incorporating many-body correlations*
- ✓ *DWBA and/or coupled channel calculations*
- ✓ *Formulation of scattering theory for double Charge Exchange (CE) Reactions*

## Main Physical Cases of Interest

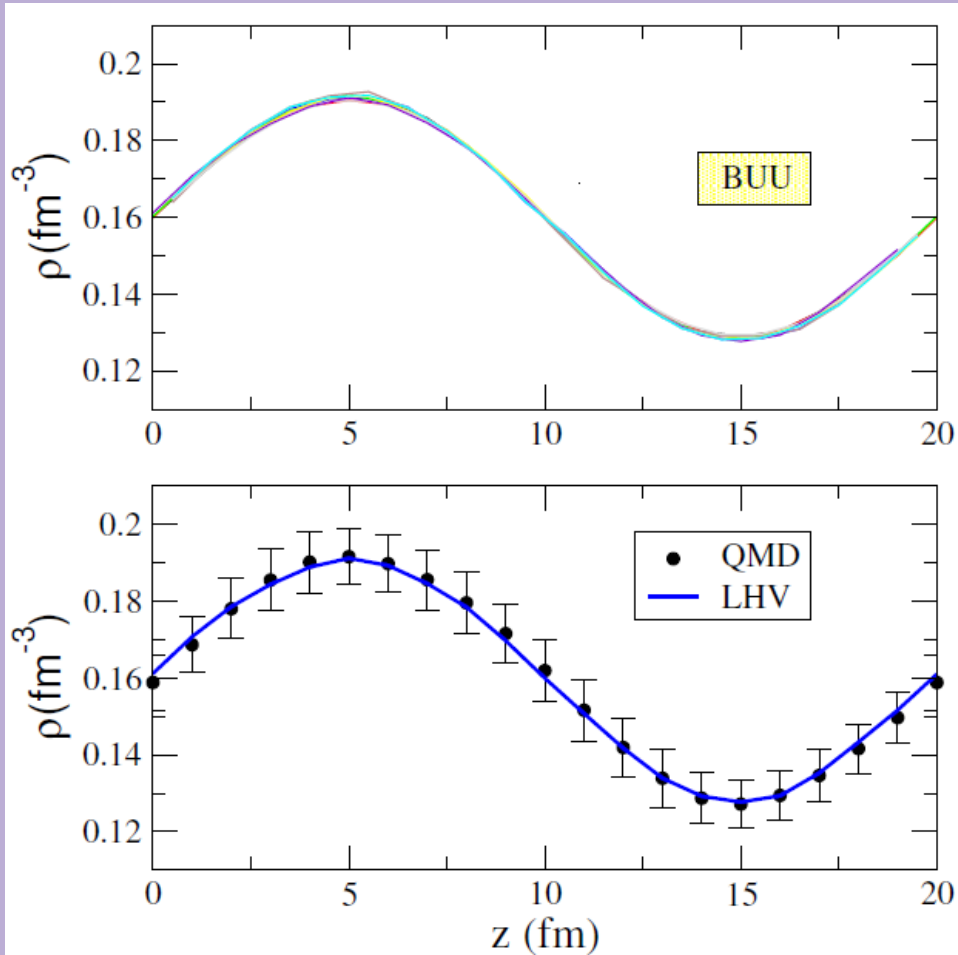
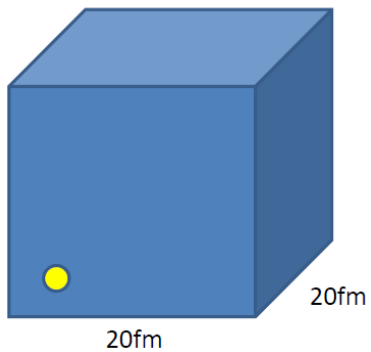
- ✓ *Nuclear reactions at Fermi/intermediate energies*
- ✓ *Direct reaction (transfer, charge exchange, probing spin-isospin channels)*
- ✓ *Fragmentation reactions, also for medical applications*
- ✓ *Impact of Eos on nuclear reactions*
- ✓ *Double Charge Excitations and the connection to double beta decay*
- ✓ *Reactions of astrophysics interest (light systems, cluster structures)*

**A (few) recent  
Applications  
and  
Studies**

# Reaction dynamics in semi-classical stochastic approaches

## Transport Model Evaluation Project

### Box simulations: test of mean-field dynamics



- Sinusoidal perturbation:  
 $\rho(z, t=t_0) = \rho_0 + a_p \sin(kz)$   
 $k = 2\pi/L, \quad L = 20 \text{ fm} \quad a_p = 0.2 \rho_0$
- Fermi sphere defined as a function of the local density

- ▣ Symmetric matter zero temperature
- Only mean-field potential
- No surface terms
- Compressibility  $K = 500 \text{ MeV}$

#### Simulations:

200 runs for QMD-like codes

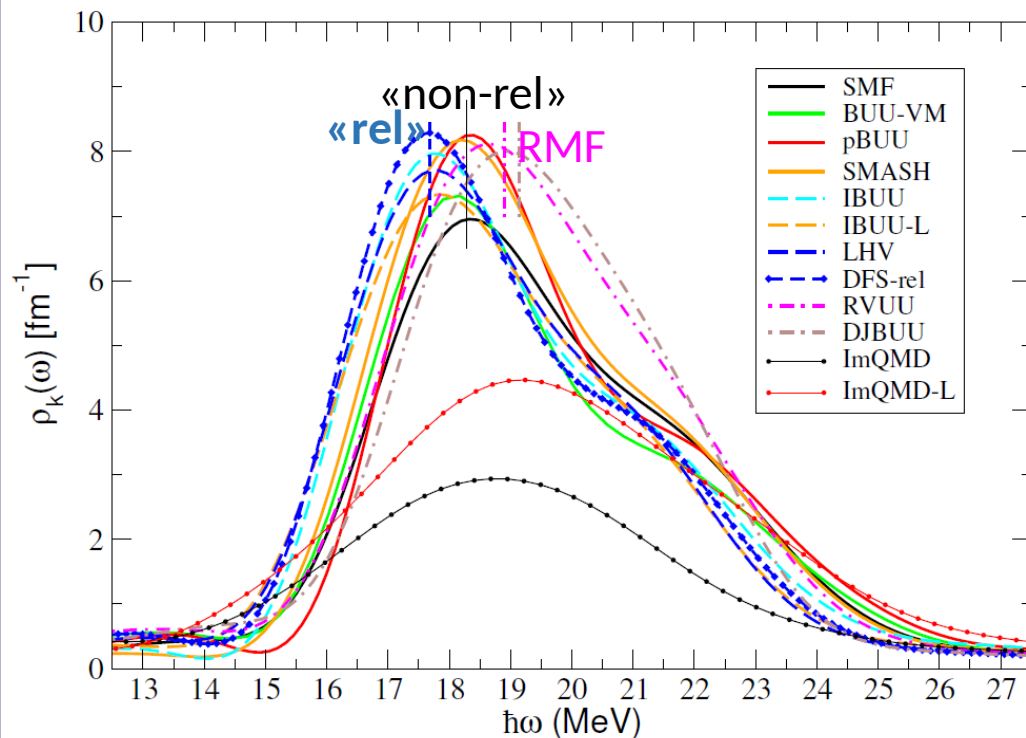
10 runs for BUU-like codes, with  $N_{\text{TP}} = 100$



# Results of all codes

Response function:

$$\rho_k(\omega) = \int_{t_{in}}^{t_{fin}} dt \rho_k(t) \cos(\omega(t - t_{in}))$$

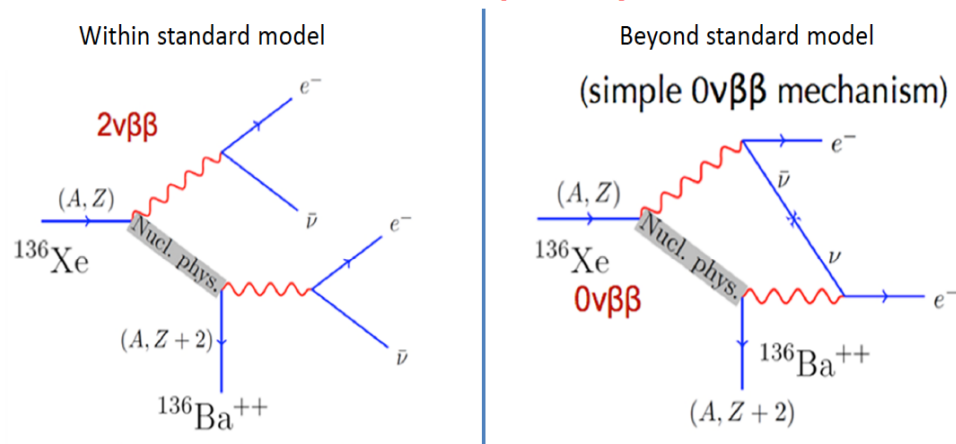


- Differences between **BUU** codes are compatible with different treatment of kinematics and/or mean-field
- **QMD** codes:
  - frequency affected by less repulsive many-body term (can be cured with Lattice method)
  - large damping effects

# Theoretical part of NUMEN project (Resp. M. Colonna)

For *single charge exchange (SCE)* Nuclear Reactions are a well tested approach to probe single  $\beta$  decay... MAGNEX at LNS allow to access *double charge exchange (DCE)*

## Double $\beta$ -decay



$$1/T_{1/2}^{0\nu}(0^+ \rightarrow 0^+) = G_{0\nu} \left| M^{\beta\beta 0\nu} \right|^2 \left( \frac{\langle m_\nu \rangle}{m_e} \right)^2$$

**Nuclear Matrix Element (NME)!**

$$\left| M_\varepsilon^{\beta\beta 0\nu} \right|^2 = \left| \langle \Psi_f | \hat{O}_\varepsilon^{\beta\beta 0\nu} | \Psi_i \rangle \right|^2$$

$$T_{\beta\alpha}^{(z)} = \langle \chi_\beta^{(-)} | (b | V_{res} G_c V_{res} | a) | \chi_\alpha^{(+)} \rangle =$$

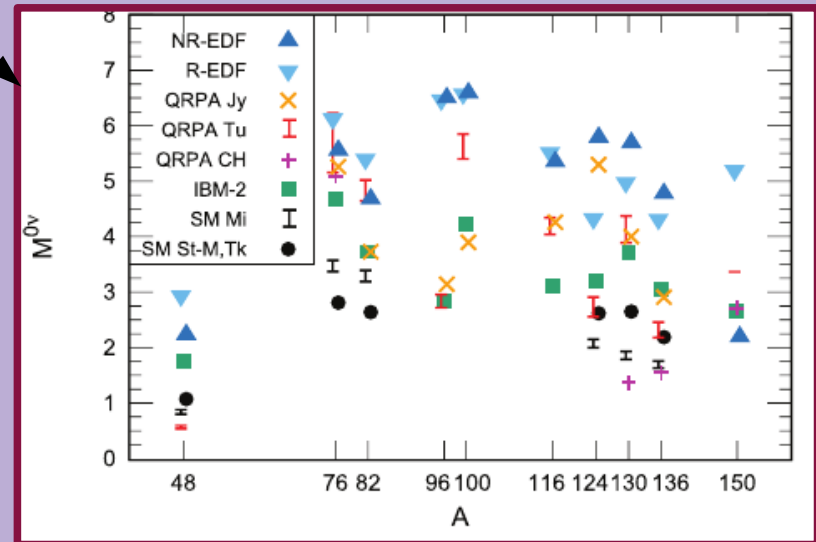
**Double**

$$= \sum_c \int \frac{d^3k}{(2\pi)^3} \langle \chi_\beta^{(-)} | (b | V_{res} | c) | \chi_\gamma^{(+)} \rangle \cdot \frac{1}{\varepsilon_\alpha - \varepsilon_\beta + i\eta}$$

**Single**

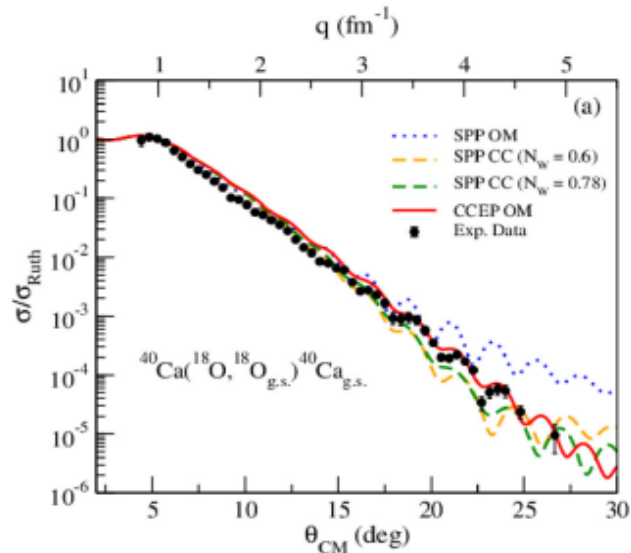
$$\cdot \langle \tilde{\chi}_\gamma^{(+)} | (c | V_{res} | a) | \chi_\alpha^{(+)} \rangle \quad \text{Single}$$

- ① Modellizzazione meccanismo di reazione per **SCE / DCE** fattorizzazione anche in AA
- ② Doppio scambio come convoluzione di 2 processi singoli => link with Double-beta decay
- ③ *Modelli struttura nucleare per meccanismi SCE/DCE*

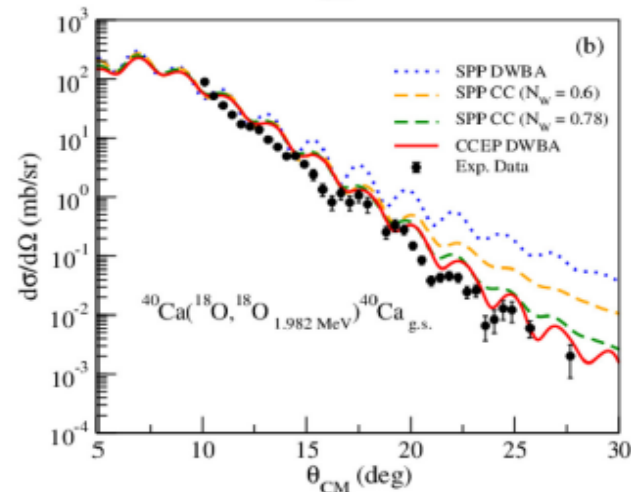


# $^{40}\text{Ca}(^{18}\text{O}, ^{18}\text{F})^{40}\text{K}$

## A Constrained Analysis of the $^{40}\text{Ca}(^{18}\text{O}, ^{18}\text{F})^{40}\text{K}$ Direct Charge Exchange Reaction Mechanism at 275 MeV, M. Cavallaro et al. *Frontiers in Astron. And Space Sci.* 8, 659815 (2021)

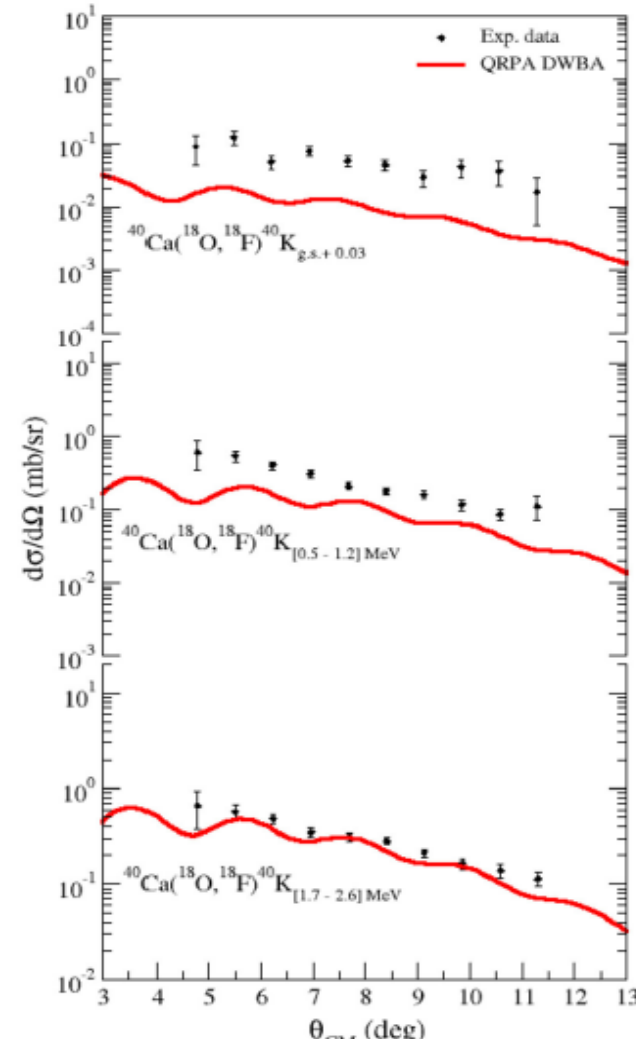


elastic



inelastic

good agreement

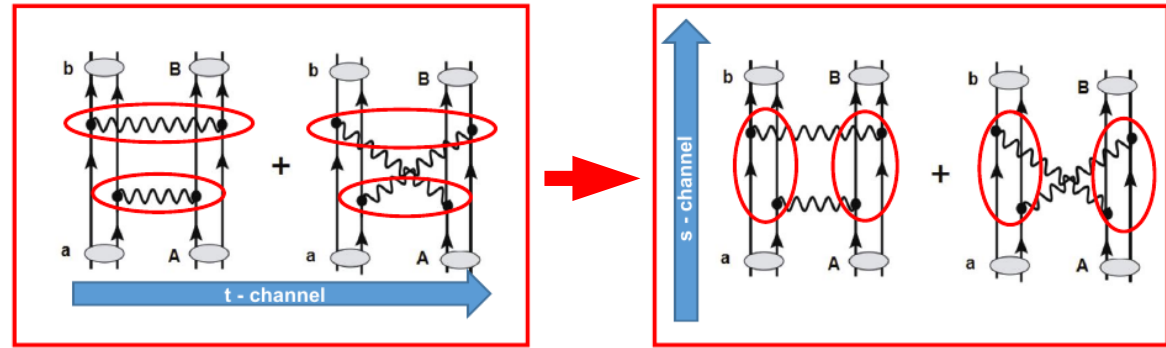


SCE

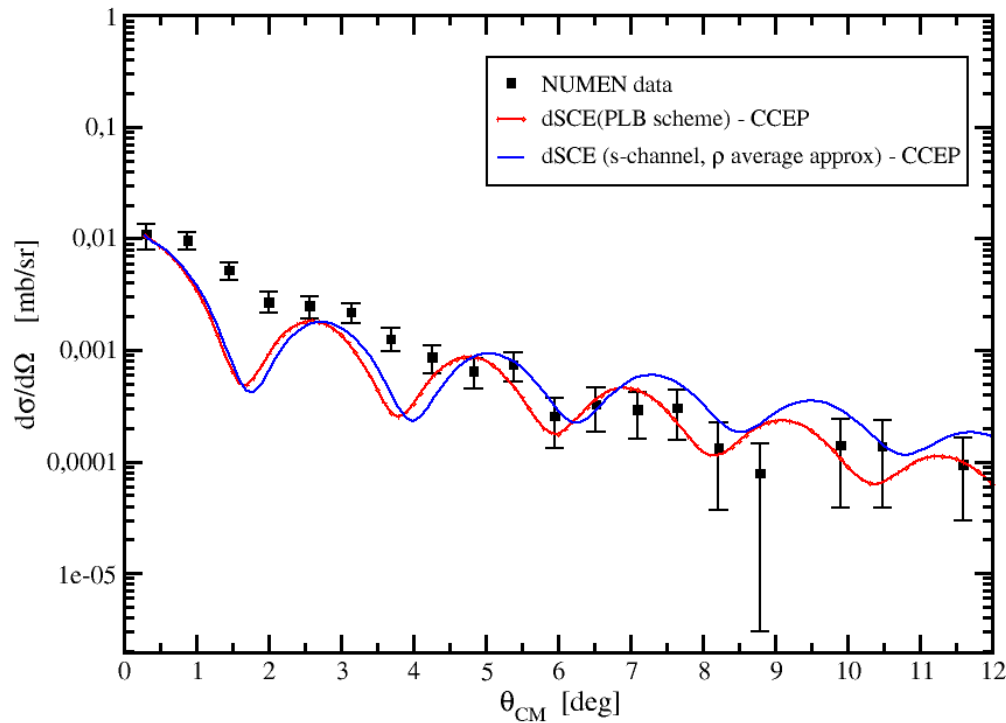
# ➤ DSCE Cross Section - $^{40}\text{Ca}(^{18}\text{O}, ^{18}\text{Ne}_{\text{g.s.}})^{40}\text{Ar}_{\text{g.s.}}$

*H. Lenske, J.I. Bellone, M. Colonna, D. Gambacurta, Universe 7 (2021) 4, 98*

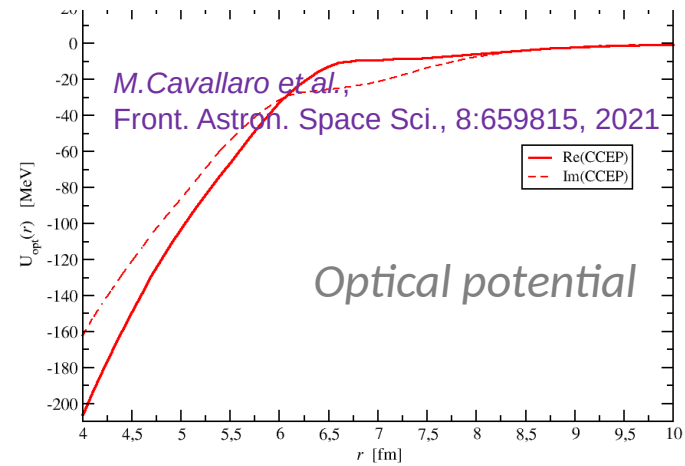
*J.I. Bellone et al., PLB 807 (2020) 135528*



$^{40}\text{Ca}(^{18}\text{O}, ^{18}\text{Ne})^{40}\text{Ar}$  at  $E_{\text{lab}} = 275$  MeV

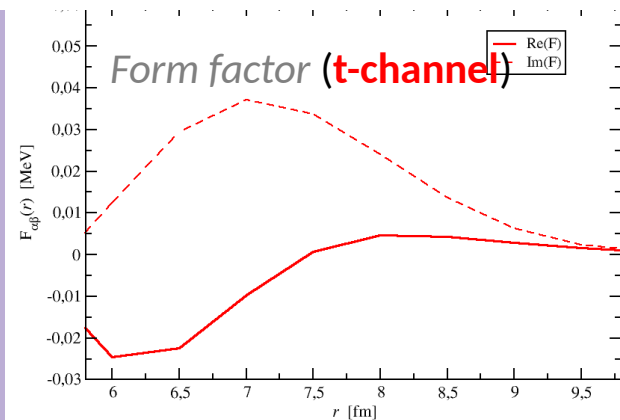


**s-channel (approx)**



*M. Cavallaro et al., Front. Astron. Space Sci., 8:659815, 2021*

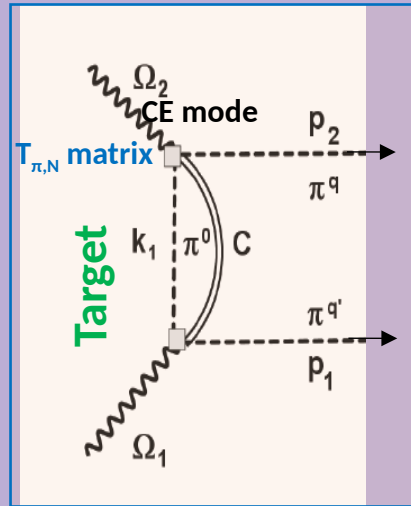
*Optical potential*



*Form factor (t-channel)*

# DCE reactions by double meson exchange: MDCE

- Analogies with  $0\nu\beta\beta$  matrix elements
  - Majorana-like DCE (MDCE)

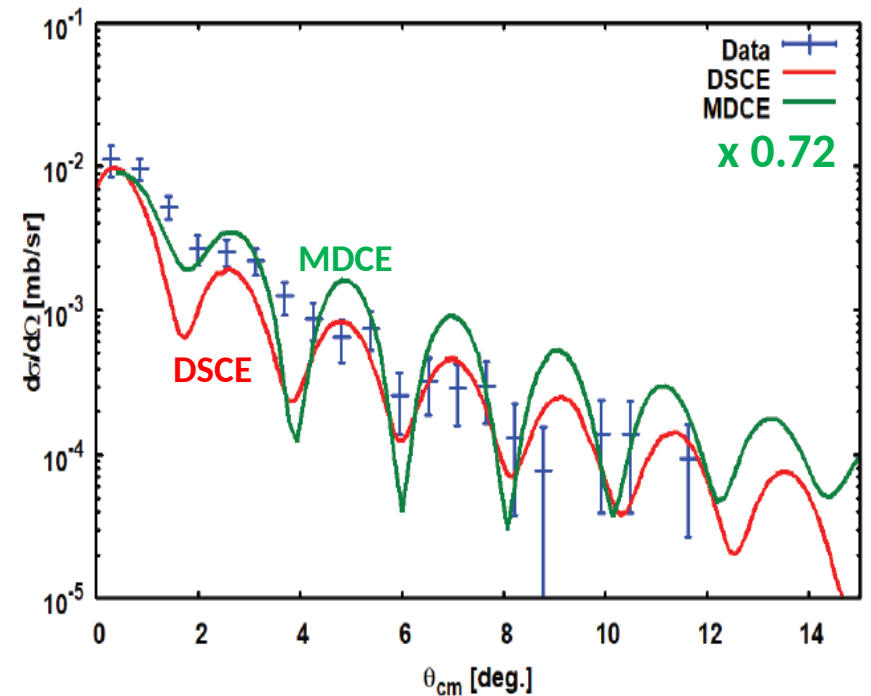
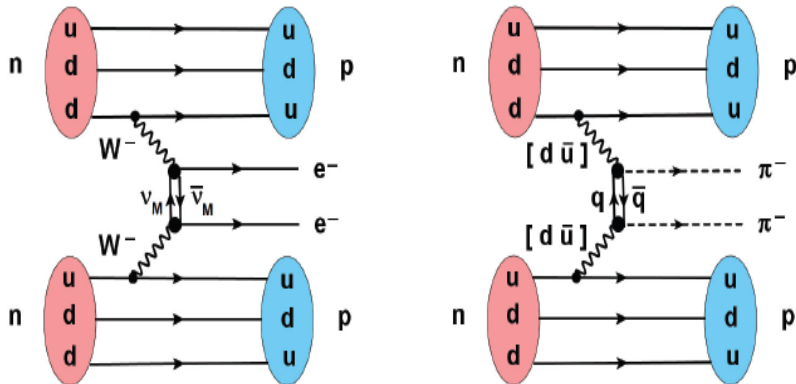


*H. Lenske et al., Progr. in Part. and Nucl. Phys.*  
 109 (2019) 103716  
*F. Cappuzzello, H.Lenske et al., PPNP* (2022),  
 submitted

- **MDCE** differential cross section  
 (diagonal  $s$ -wave and  $p$ -wave  $T_{\pi,N}$  contributions in NMEs)

$0\nu\beta\beta$

MDCE



$^{40}\text{Ca}(^{18}\text{O}, ^{18}\text{Ne}_{g.s.})^{40}\text{Ar}_{g.s.}$  @ 15 MeV/u

# DWBA reaction calculations for light systems for astrophysics studies

## Goal

Study the influence of ground-state (“static”) structure on the reaction dynamics in a fully quantum framework.

- Explicit evaluation of the cross-section in terms of the properties and interactions of reactants.
- No adjusting on reaction experimental data.

Study of  ${}^6\text{Li} + p \rightarrow \alpha + {}^3\text{He}$  transfer, focus on  ${}^6\text{Li}$  structure.

- Two-cluster models:  $|{}^6\text{Li} \text{ } \langle \text{red blue} \rangle = |\alpha d \text{ } \langle \text{red blue} \rangle$

Process dominated by quantum tunnelling of the Coulomb barrier.

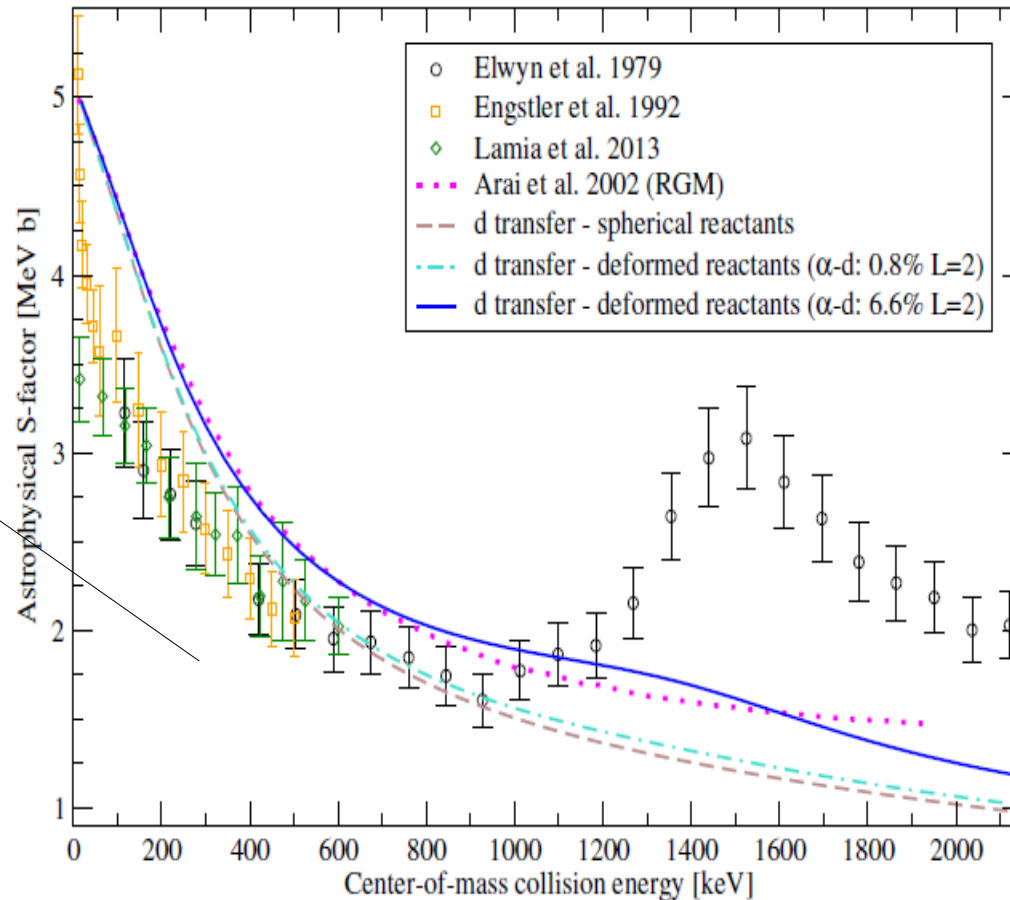
Astrophysical  $S$ -factor:

$$S(E) = E e^{2\pi\eta(E)} \sigma(E) \quad , \quad \eta(E) = \alpha_e Z_1 Z_2 \sqrt{\frac{\mu c^2}{2E}}$$

( $\sigma$  angle-integrated cross-section,  $E$  center-of-mass collision energy,  $Z_i$  reactants charge number,  $\alpha_e$  fine-structure constant,  $\mu$  reactants reduced mass,  $c$  speed of light).

# ${}^6\text{Li} + p \rightarrow {}^3\text{He} + \alpha$ : deuteron transfer

${}^6\text{Li} + p \rightarrow {}^3\text{He} + \alpha$





Models usually underestimate  
The low-energy  
part which  
Is important for  
astrophysical  
studies


Brown dashed line: point-like d transfer,  $\alpha$ -d motion in  $L = 0$   
Blue solid line: point-like d transfer, 6.6% of  $L = 2$  in  $\alpha$ -d motion




**Proton-neutron pairing and binding energies of nuclei close to the  $N = Z$  line**

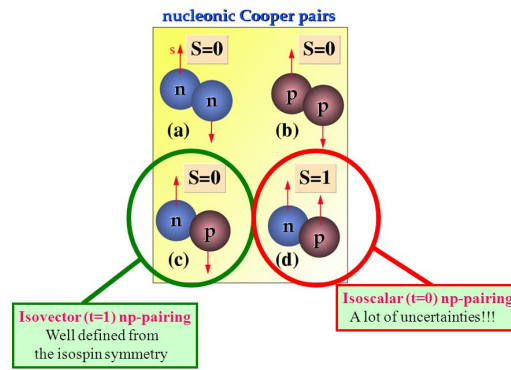
D. Negrea  and N. Sandulescu 

National Institute of Physics and Nuclear Engineering, 077125 Măgurele, Romania

D. Gambacurta 

INFN-LNS, Laboratori Nazionali del Sud, 95123 Catania, Italy

 (Received 1 November 2021; accepted 18 February 2022; published 23 March 2022)



- pp and nn pairing is well understood (BCS)
- p-n pairing not clear and very much studied both th. and exp.

- BCS description fails!!!
- We developed a new approach to treat all the pairing channels consistently
- Quartet Condensate Model (QCM) preserves particle and isospin symmetries
- Skyrme HF plus QCM calculations along all the nuclear chart  $20 < A < 100$ , including deformation
- Better agreement with data than HF plus BCS

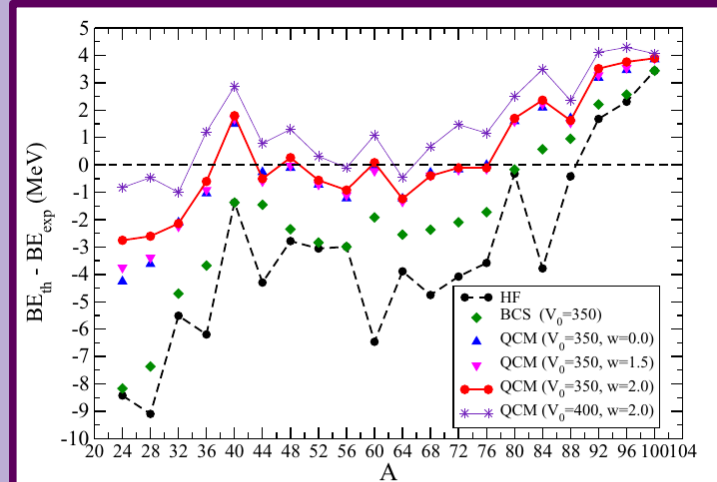
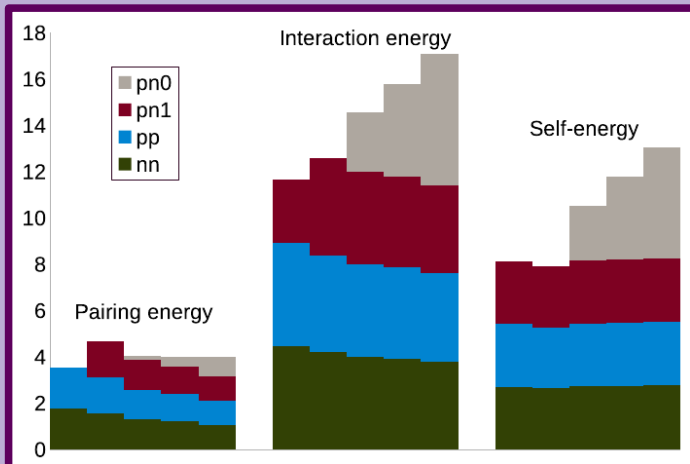


FIG. 1. Binding-energy residuals, in MeV, for even-even  $N = Z$  nuclei as a function of  $A = N + Z$ . The results correspond to the pairing forces and the approximations indicated in the figure.

- Isovector and isoscalar p-n pairing coexist but the isoscalar one is typically much weaker
- Next step: QCM in pair or alpha transfer



# Gamow-Teller Strength in $^{48}\text{Ca}$ and $^{78}\text{Ni}$ with the Charge-Exchange Subtracted Second Random-Phase Approximation

D. Gambacurta<sup>1</sup>, M. Grasso<sup>2</sup>, and J. Engel<sup>3</sup>

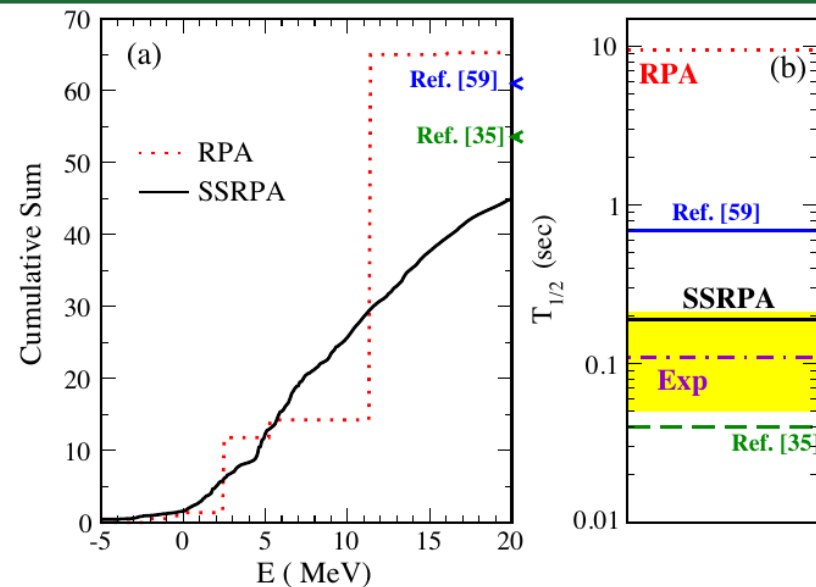
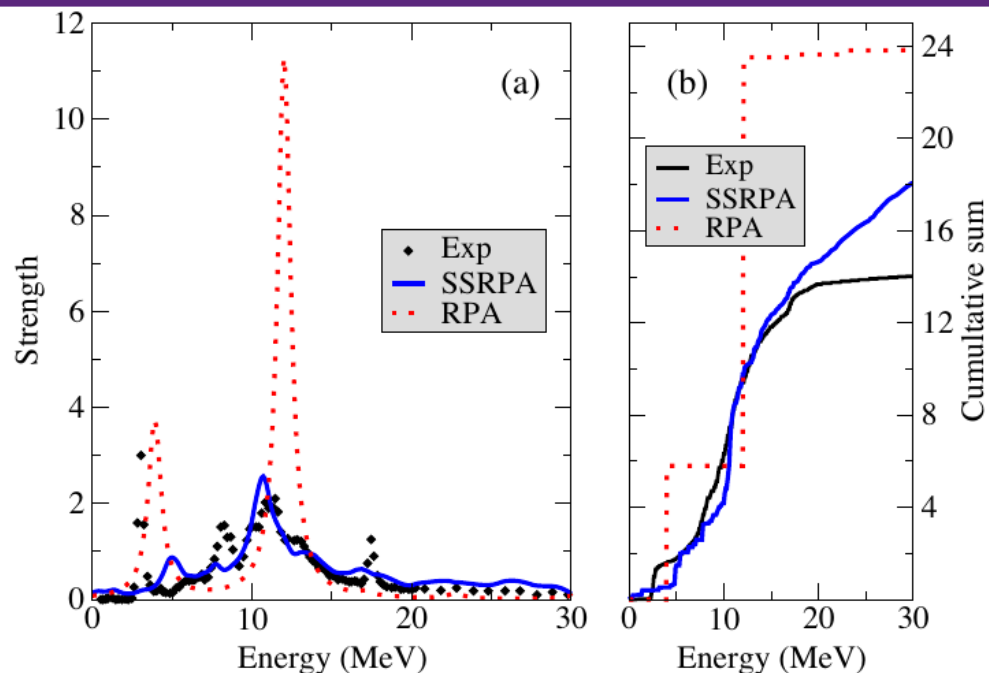


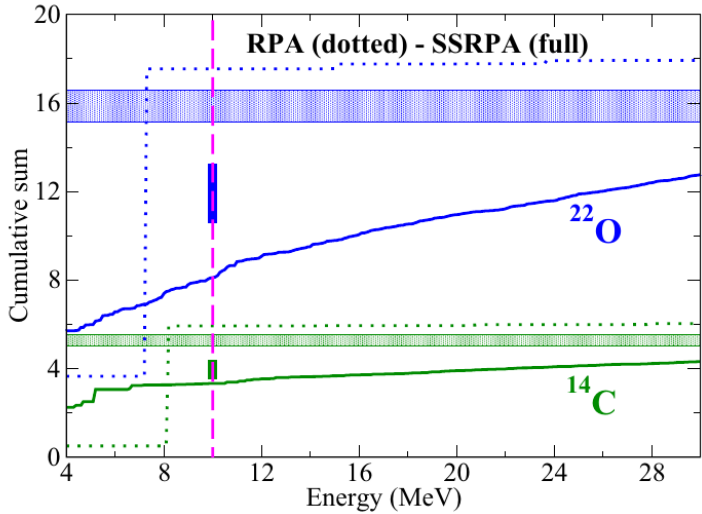
FIG. 4. (a) Cumulative sum for different models (see legend and text) for the nucleus  $^{78}\text{Ni}$ ; (b)  $\beta$ -decay half-life for  $^{78}\text{Ni}$  predicted by SSRPA, compared with predictions of other models and the experimental value [58]. The yellow band represents the experimental uncertainty.

- Extension to treat **Charge Exchange Excitations**
- **Open problem:** Models need quenching factor ( $\sim 0.7$ ) to reproduce data
- First application where **2p2h configurations** are introduced (together with 1p1h)
- Agreement with data **without *ad hoc*** quenching factor

**Quenching of Gamow-Teller strengths and two-particle-two-hole configurations**

Danilo Gambacurta<sup>1</sup> and Marcella Grasso<sup>2</sup>  
<sup>1</sup>INFN-LNS, Laboratori Nazionali del Sud, 95123 Catania, Italy  
<sup>2</sup>Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay, France

Comparison with *Ab initio* results including two body currents



Calculations for heavy nuclei: 90Zr and 132Sn

Quality of approximated schemes for future studies

- Implications for NME in **neutrino-less double-β decay** and **NUMEN project**

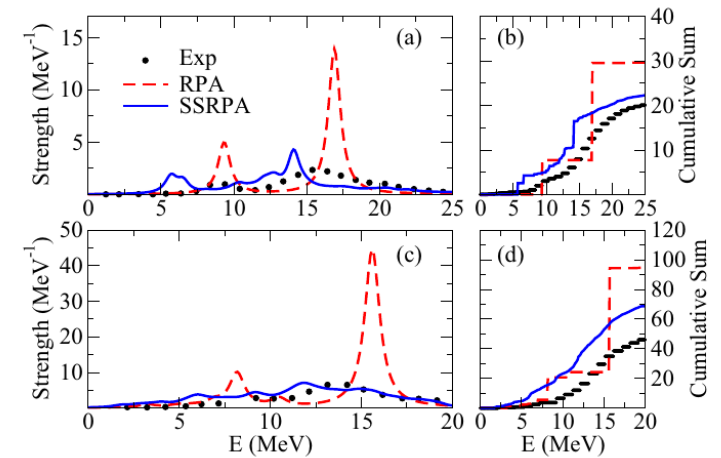


FIG. 6. (a)  $GT^-$  SSRPA and RPA folded spectra obtained with the Skyrme interaction SGII for the nucleus  $^{90}\text{Zr}$ . The experimental results Ref. [28] are also shown. (b) Strengths of panel (a) integrated up to 25 MeV. (c) Same as in (a) but for the nucleus  $^{132}\text{Sn}$ . The experimental results are extracted from Ref. [29]. (d) Strengths of panel (c) integrated up to 20 MeV.

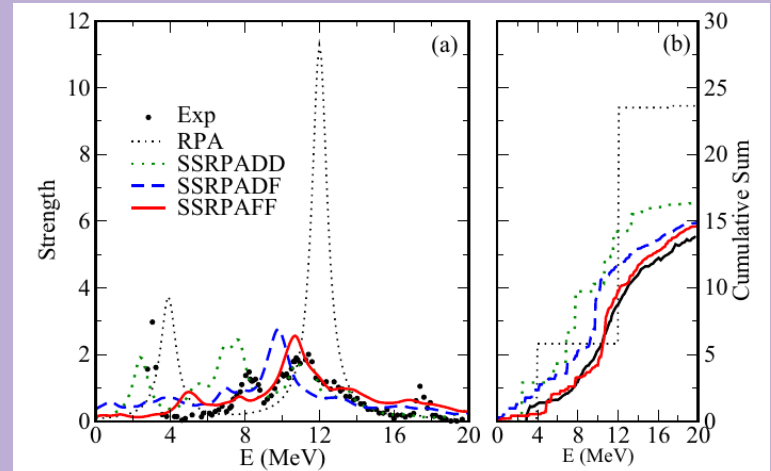


FIG. 1. (a)  $GT^-$  strengths obtained with the Skyrme interaction SGII for the nucleus  $^{48}\text{Ca}$  in  $\text{MeV}^{-1}$ . Experimental data are extracted from Ref. [7]. RPA and all SSRPA strengths are obtained by folding with a Lorentzian having a width of 1 MeV. (b) Cumulative sum of the strength up to the excitation energy of 20 MeV. See text for more details.

Thank you

## ***Nuclear Structure: Main Physical Cases of Interest***

- ✓ ***Collective nuclear excitations, especially in neutron-rich and exotic nuclei (Giant Resonances, Pygmy Dipole Resonance, ...)***
- ✓ ***EoS of asymmetric matter (symmetry energy, ...)***
- ✓ ***Charge exchange excitations (Gamow-Teller, Fermi, etc,)***
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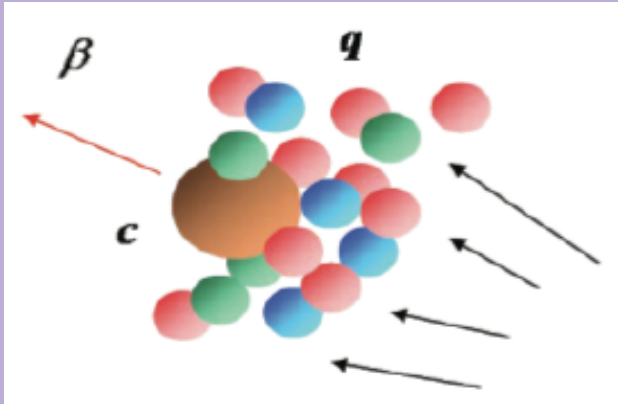
## ***Nuclear Reactions: Main Physical Cases of Interest***

- ✓ ***Nuclear reactions at Fermi/intermediate energies***
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- ✓ ***Fragmentation reactions, also for medical applications***
- ✓ ***Impact of EoS on nuclear reactions***
- ✓ ***Double Charge Excitations and the connection to double beta decay***
- ✓ ***Reactions of astrophysics interest (light systems, cluster structures)***

## Gruppo IV - LNS

- Stefano Burrello Ricercatore INFN (dal 1.11.2022 )
- Colonna Maria Dirigente di Ricerca [20% in CS3]
- Gambacurta Danilo Primo ricercatore Ricercatore [20% in CS3]
- Greco Vincenzo Professore Ordinario (Inc. Ric.) [10% in CS2]
- Salvatore Plumari Prof. Associato, UniCT
- Vincenzo Minissale Assegnista di Ricerca
- Jessica Bellone Assegnista di Ricerca NURE
- Simone Perrotta Assegnista di Ricerca
- Maria Lucia Sambataro Assegnista di Ricerca UnicT
  
- Angelo Asta Dottorando II anno
  
- Adriele Arena Laureando (laurea 15 Luglio 2022)
- Vincenzo Nugara Laureando (Ottobre 2022)

# An elephant in the liquid: Heavy Charm Quark



QGP composto al 99% da g e q=u,d,s,  $m_q \approx 10 \text{ MeV}$

+ qualche Charm Quarks:  $M_c \approx 1400 \text{ MeV}$

→ Poorly dragged & long thermalization time (!?)

$$\tau_{C,therm} \approx O(10^2) \gg \tau_{QGP} \gg \tau_{q,therm} \approx O(1) \text{ fm/c}$$

Moto Browniano

$$\frac{\partial f_{c,b}}{\partial t} = \underbrace{\Gamma}_{\text{Drag}} \frac{\partial (pf_{c,b})}{\partial p} + \underbrace{D}_p \frac{\partial^2 f_{c,b}}{\partial p^2}$$

Drag

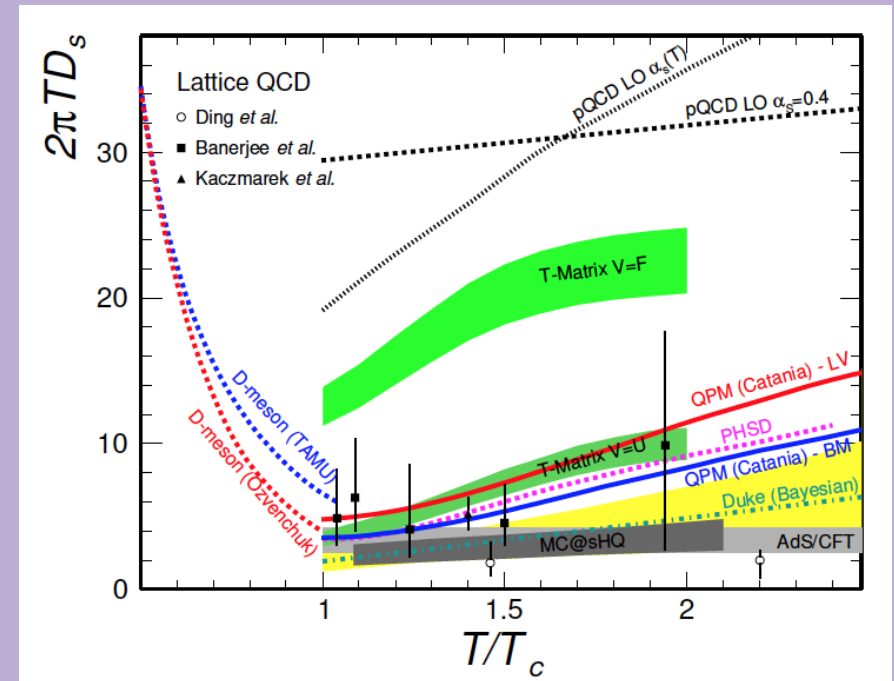
Diffusion

Tempo di termalizzazione  
e coefficiente Diffusione

$$\tau_{th} = \frac{M}{2\pi T^2} (2\pi T D_s) \cong 1.8 \frac{2\pi T D_s}{(T/T_c)^2} \text{ fm/c}$$

$$\Gamma_{coll} \approx D_s^{-1} \approx 0.5-1 \text{ GeV} \approx M_{q,g}(T)$$

barely quasi-particle states



**Not a model fit to IQCD data!**  
**Phenomenology  $\approx$  lattice QCD**

# Strong fields in relativistic nuclear collisions

## ✓ HUGE ANGULAR MOMENTUM GENERATING A STRONG VORTICITY



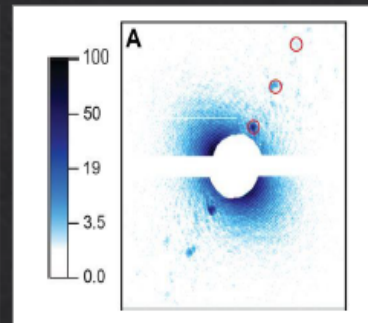
tornado cores

$\sim 10^{-1} \text{ s}^{-1}$



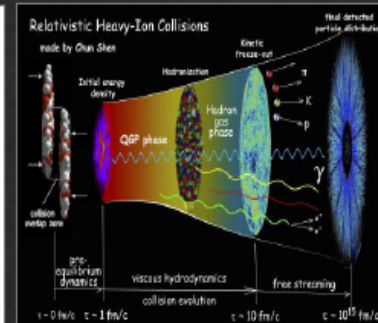
Jupiter's spot

$\sim 10^{-4} \text{ s}^{-1}$



He nanodroplets

$\sim 10^7 \text{ s}^{-1}$

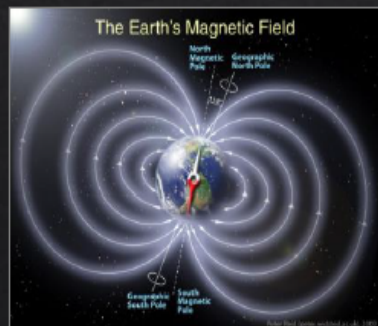


urHICs

$\sim 10^{22} - 10^{23} \text{ s}^{-1}$

vorticity  
 $\omega$

## ✓ INTENSE ELECTROMAGNETIC FIELDS (EMF)



Earth's field

$\sim 1 \text{ G}$



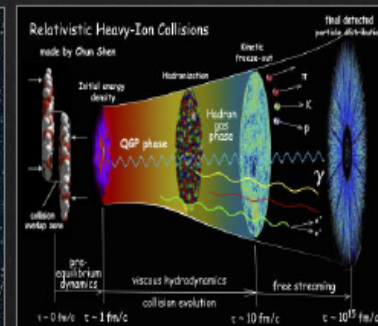
laboratory

$\sim 10^6 \text{ G}$



magnetars

$\sim 10^{14} - 10^{15} \text{ G}$



urHICs

$\sim 10^{18} - 10^{19} \text{ G}$

magnetic  
field  
 $B$