

Non-identical femtoscopy results from the STAR experiment

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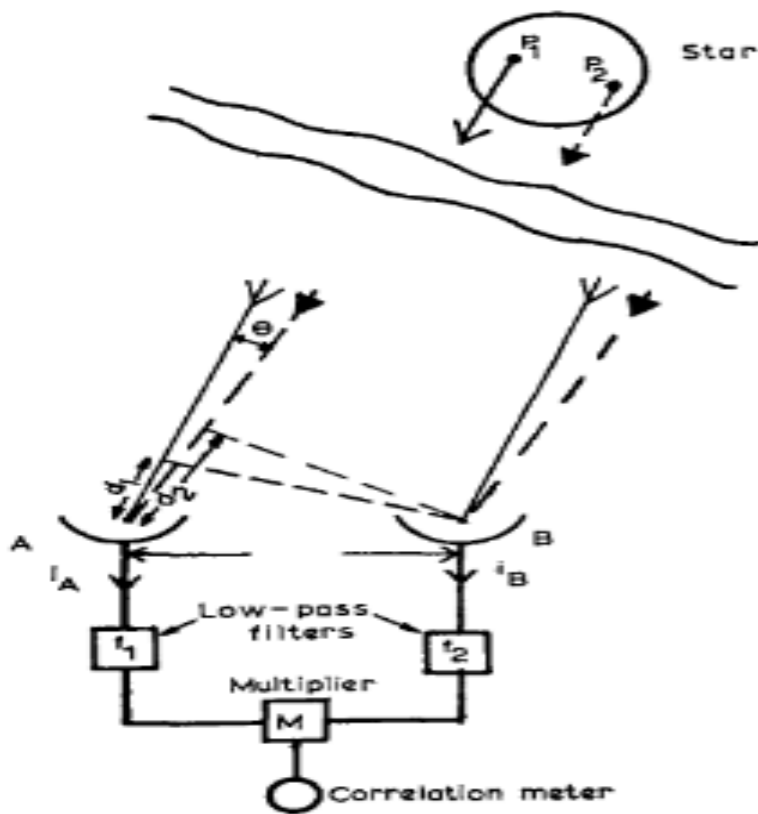


- Introduction to correlation femtoscopy
- STAR experiment at RHIC
- Experimental results on non-identical correlation
- Conclusion



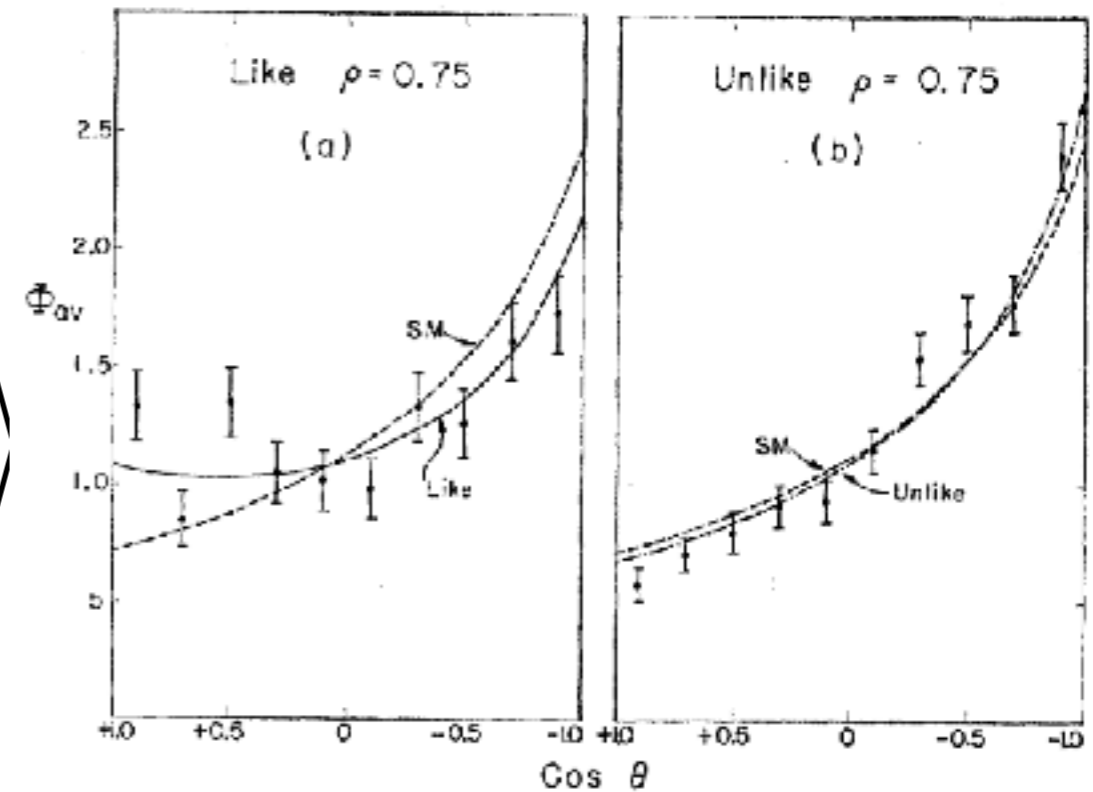
HBT and femtoscopy

Method to probe geometric and dynamic properties of the source



Angular Size
of Sirius

$\pi - \pi$
correlation



Goldhaber et al, Phys. Rev. 120, 300 (1960)

Hanbury Brown, R. Taylor & Francis, (1974)

Correlation femtoscopy

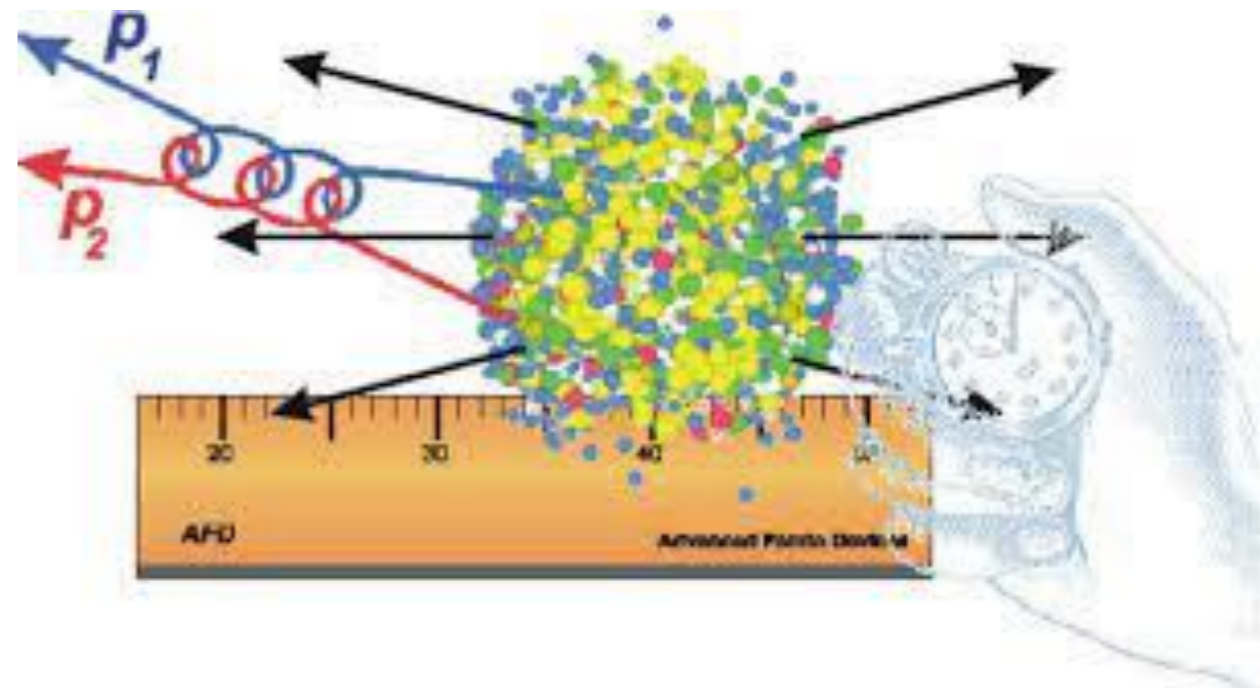
particle
correlations in
momentum space

particle emitting
source

Koonin-Pratt Equation:

$$C(k^*) = \int S(r^*) |\psi(k^*, r^*)|^2 d^3 r^*$$

$S(r^*)$ is the source function,
 $\psi(k^*, r^*)$ is two particle wave function,
 k^* and r^* are relative-momentum and
relative-separation.



from M. Lisa and S. Pratt

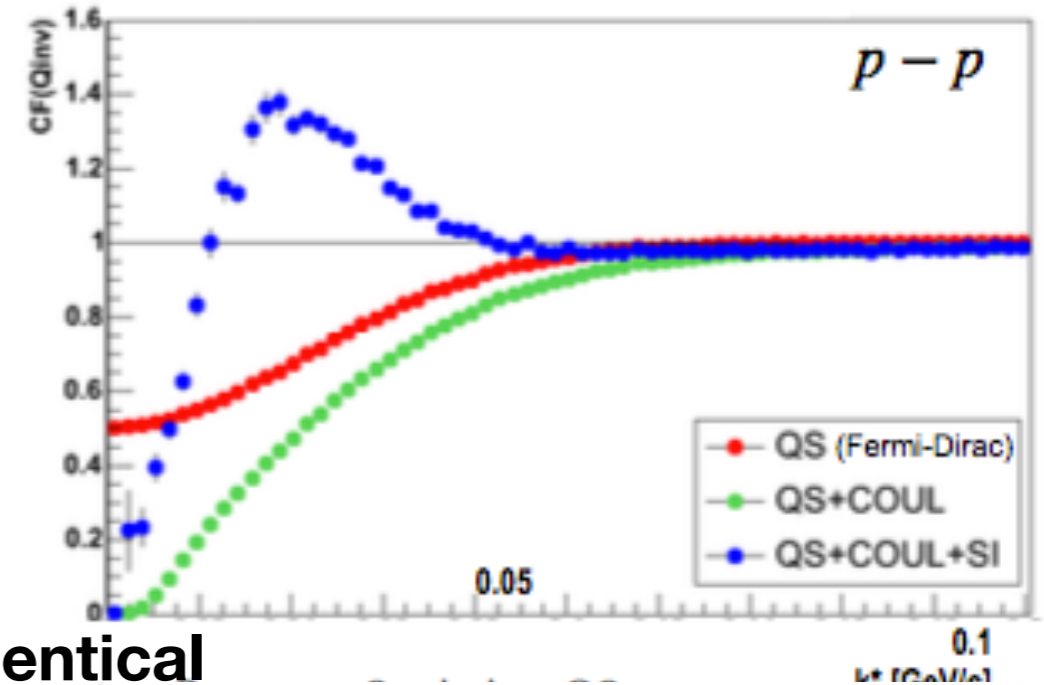
Steven E. Koonin, Phy Lett B 70, 43 (1977)
S. Pratt et al., Phys. Rev. C 42, 2646 (1990)

Sources of correlation:

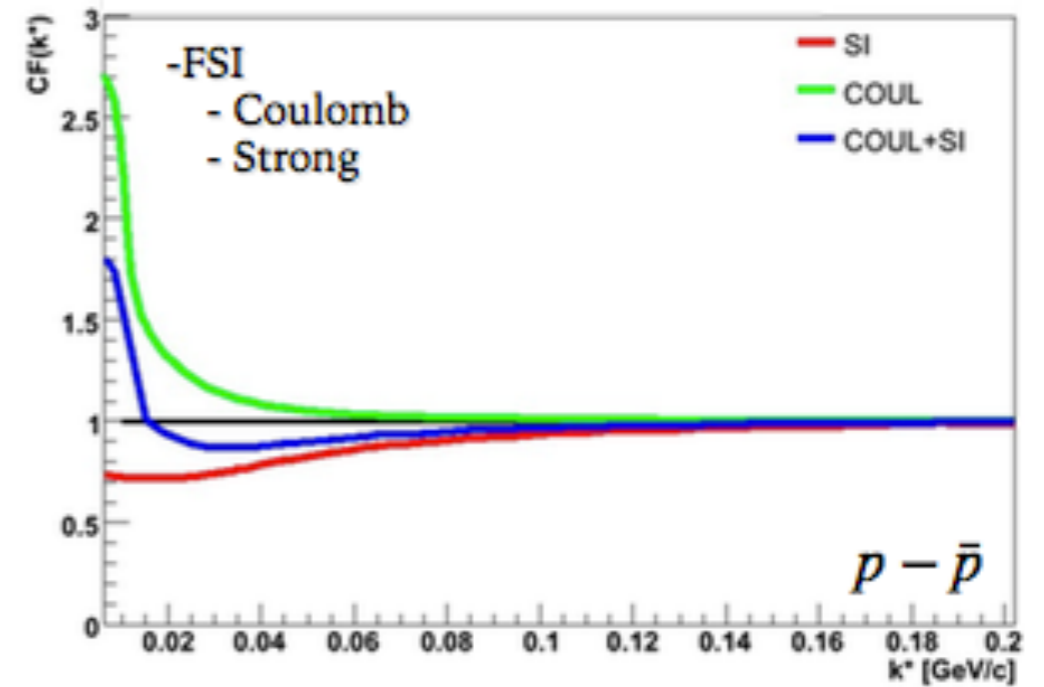
Quantum Statistics
Fermi-Dirac
Bose-Einstein

Final state interaction
Strong interactions
Coulomb interaction

Identical



Non-identical



H. Zbroszczyk, Ph.D. thesis

Correlation function

$$C(k^*) = \int S(r^*) |\psi(k^*, r^*)|^2 d^3 r^*$$

source function:
(traditional
femtoscscopy)
measures spatial
evolution of source

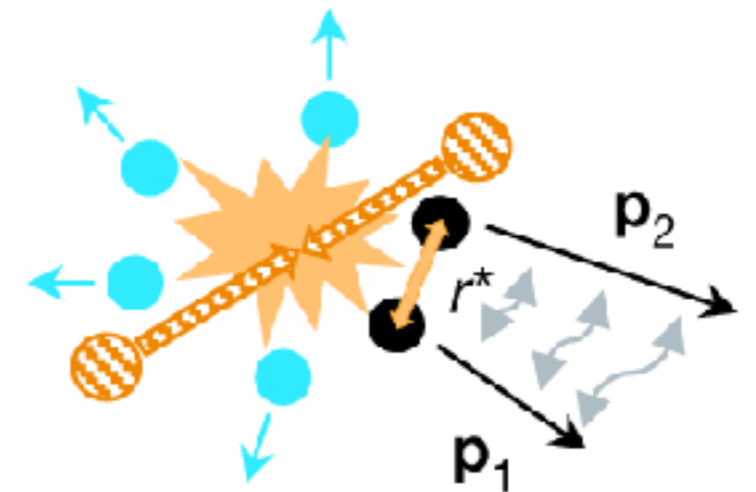
1. Gauss :
Standard approach

$$S(r) = \frac{1}{(4\pi r_0^2)^{3/2}} \exp\left(-\frac{r^2}{4r_0^2}\right)$$

$S(r)$: Source function
 r_0 is source radius

2. Levy :
anomalous diffusion/Jet
fragmentation

3. Exponential, Cauchy ..



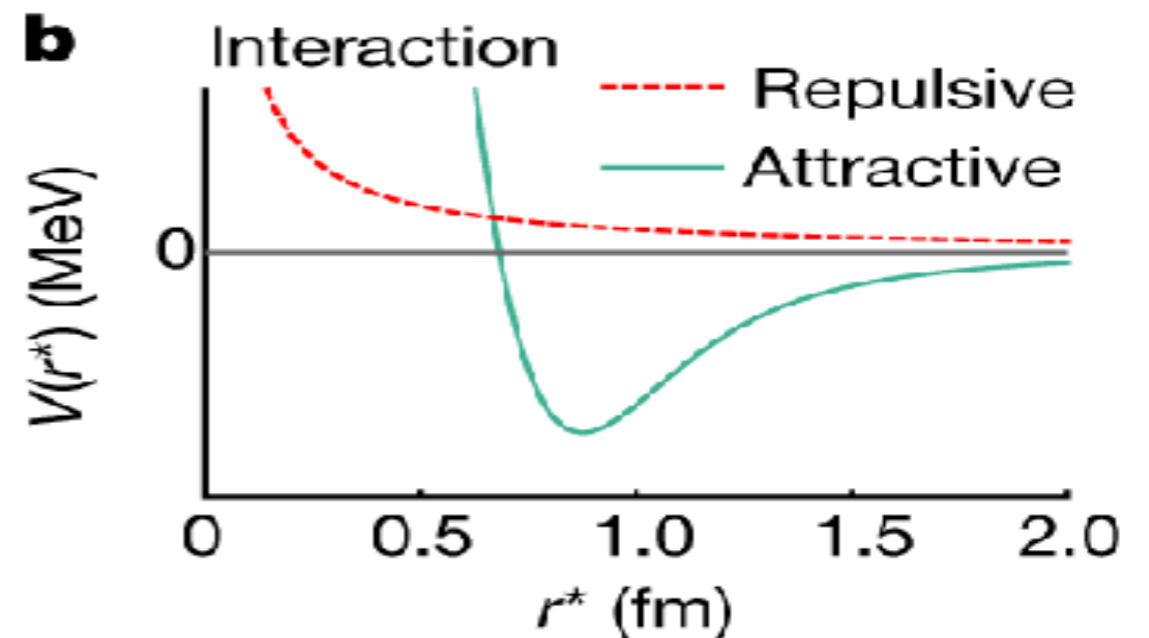
Emission source $S(r^*)$

Nature 588, 232-238 (2020)

Correlation function

$$C(k^*) = \int S(r^*) |\psi(k^*, r^*)|^2 d^3 r^*$$

Two particle wave function:
(non-traditional femtoscopy)
measures final state interactions



Schrödinger equation



Two-particle wavefunction

$$|\psi(\mathbf{k}^*, \mathbf{r}^*)|$$

Lednicky Approach:
 f_0 (scattering length), d_0 (effective radius)

Sov. Journ. Nucl. Phys. 35 (1982) 770

Nature 588, 232–238 (2020)

Lednicky Approach:

Assumptions:

- Independent emission
- Single particle source
- Source size is bigger than the range of interaction ($\sim 1\text{fm}$)
- s-wave component dominant in FSI description (for close relative velocities)

$$\Psi_{-\vec{k}^*}^{(+)}(\vec{r}^*) = \sqrt{A_C(\varepsilon)} \frac{1}{\sqrt{2}} \left[e^{-i\vec{k}^* \cdot \vec{r}^*} F(-i\varepsilon, 1, i\zeta^+) + f_C(\vec{k}^*) \frac{\tilde{G}(\rho, \varepsilon)}{r^*} \right],$$

A_C is Gamow factor

$$\zeta^\pm = k^* r^* (1 \pm \cos\theta^*)$$

$$\varepsilon = 1/(k^* a_c)$$

F is the confluent hypergeometric function

\tilde{G} is the combination of the regular and singular s-wave Coulomb functions

$f_c(k^*)$ is the strong-interaction scattering amplitude modified by the Coulomb component:

$$f_c^{-1}(k^*) = \frac{1}{f_0} + \frac{1}{2}d_0 k^{*2} - \frac{2}{a_c}h(k^* a_c) - ik^* a_c$$

Scattering parameters appears directly in Lednicky approach.
=> connection to strong interaction.

Sov. Journ. Nucl. Phys. 35 (1982) 770

Correlation function

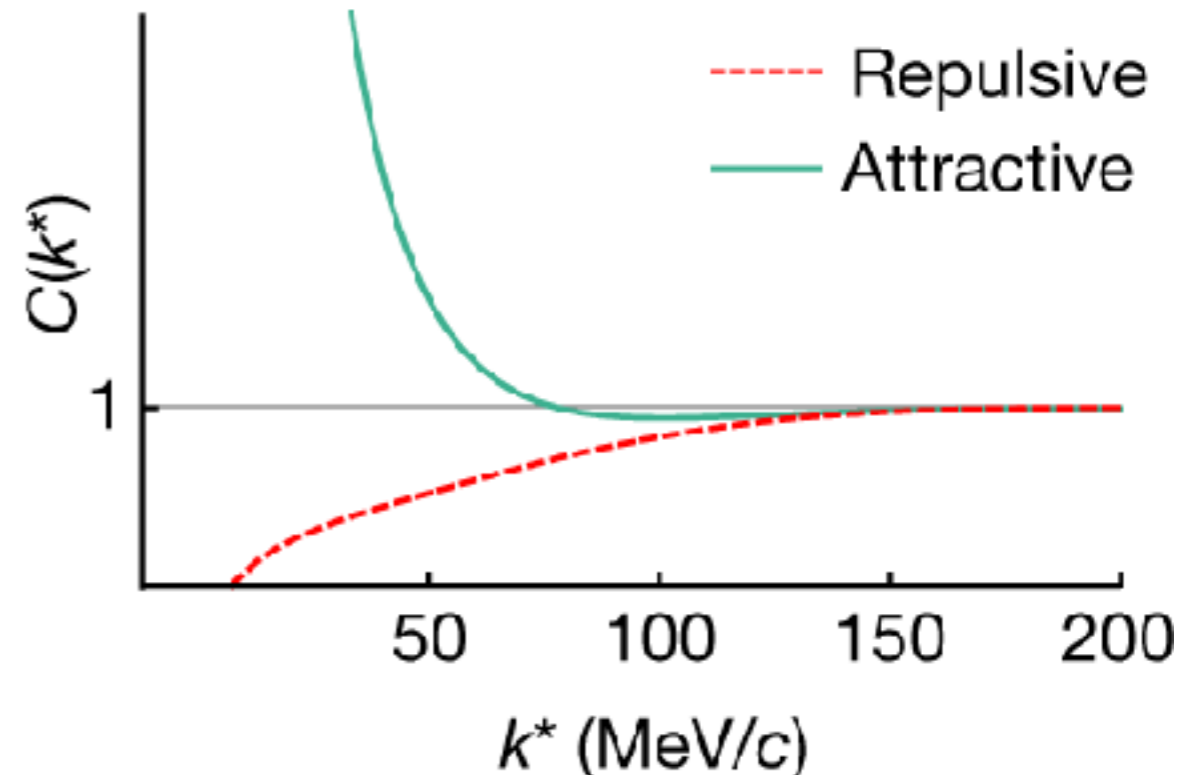
$$C(k^*) = \int S(r^*) |\psi(k^*, r^*)|^2 d^3 r^*$$

Correlation function:
measured experimentally

$C(k^*) = A(k^*)/B(k^*)$
 $A(k^*)$: same event distribution
 $B(k^*)$: mixed event distribution

$$k^* = |\vec{p}_1| = |\vec{p}_2|$$

Where \vec{p}_1 and \vec{p}_2 are three momentum of particles.



Nature 588, 232–238 (2020)

How to quantify

Correlation function in spherical coordinates

$$C(\mathbf{q}) = \sum_{l,m} C_l^m(q) Y_l^m(\theta, \phi)$$

where harmonic components are:

$$C_l^m(q) = \int_{\Omega} C(q, \theta, \phi) Y_l^m(\theta, \phi) d\Omega$$

Ω - full solid angle

$Y_l^m(\theta, \phi)$ - spherical harmonic function

$q = |\mathbf{q}|$ - pair relative momentum

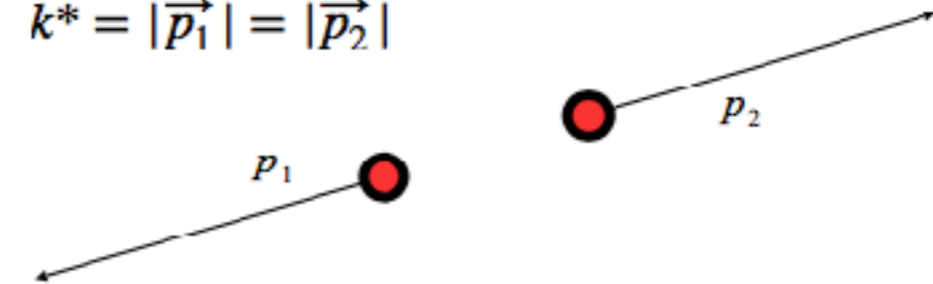
θ and ϕ - polar and azimuthal angle

C_0^0 :sensitive to size of the emitting source (shapes same as correlation function)

C_1^1 :sensitive to the spacetime emission asymmetry

Pair Rest Frame - **PRF**

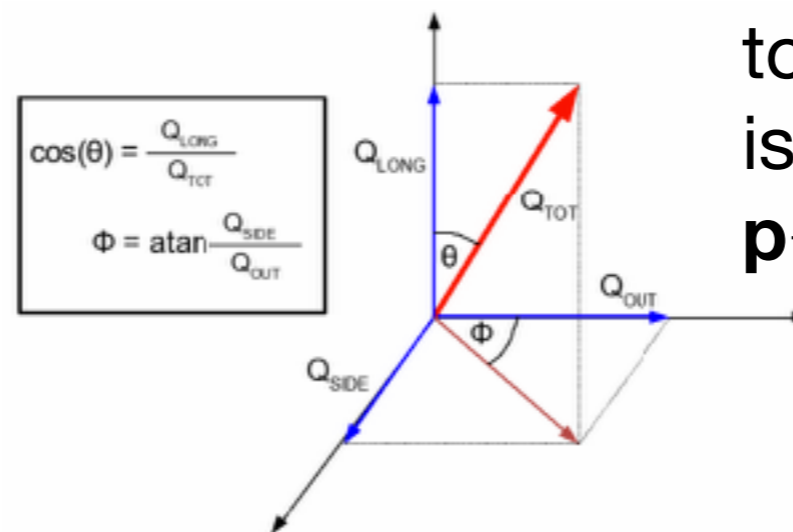
$$k^* = |\vec{p}_1| = |\vec{p}_2|$$



$$Q_{inv} = 2k^* \text{ if } m_1 = m_2$$

From Hanna Zbroszczyk

Pair Rest Frame (PRF):
total momentum of pair
is zero,
 $\mathbf{p}_1 + \mathbf{p}_2 = 0$



From Zbigniew Chajecki

P. Danielewicz and S. Pratt., Phys. Lett B618, 60 (2005) Phys. Rev. C75, 034907 (2007)
Z. Chajecki and M. Lisa Phys. Rev. C78, 064903 (2008)
Kisiel and D.A. Brown Phys. Rev. C80, 064911 (2009)
A. Kisiel Phys. Rev. C81, 064906 (2010)

Pion-Kaon system: asymmetry

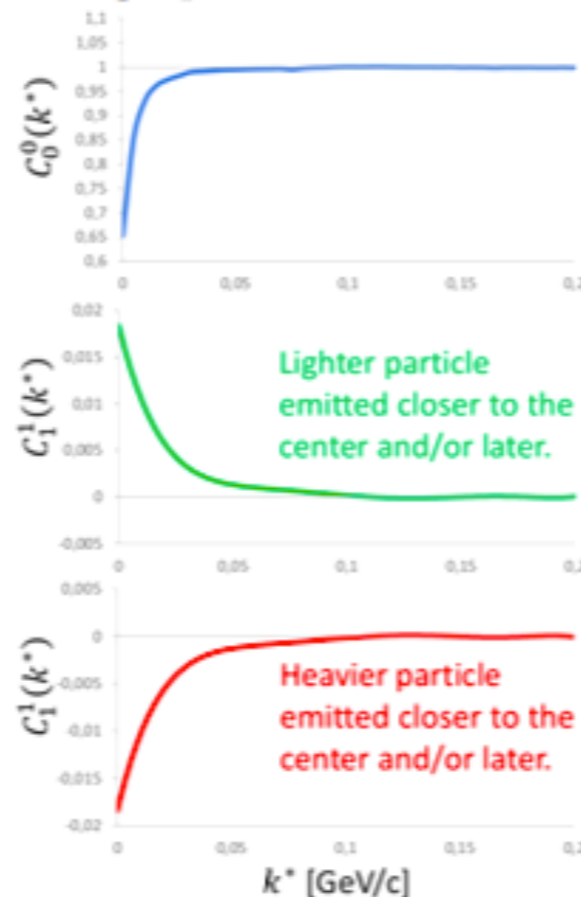
Time asymmetry:

particles are assumed to be emitted from the same positions; viz. kaon (anti-proton) is considered as emitted first, the pion (proton) second

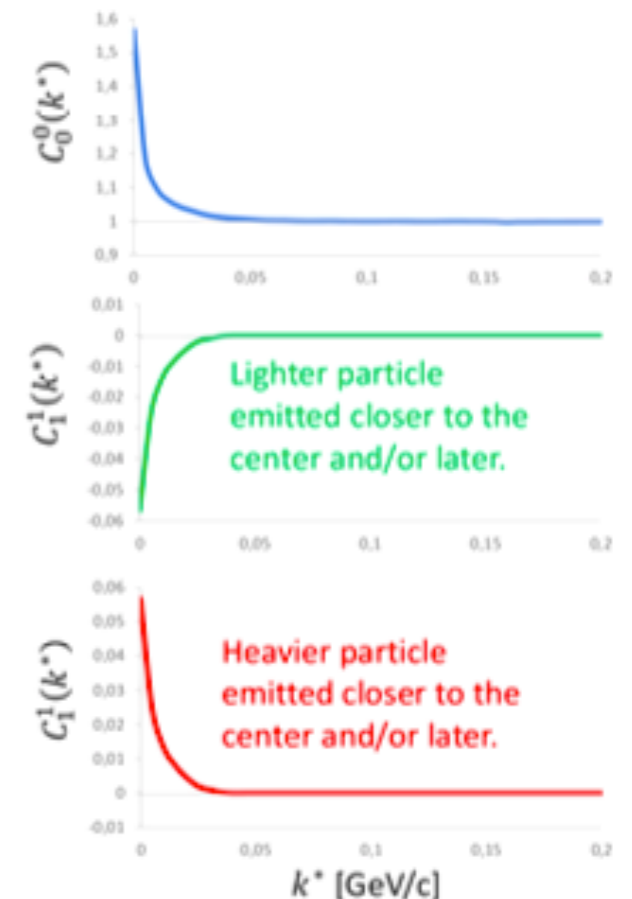
Spatial asymmetry:

particles are assumed to be emitted at the same time; viz. pion (proton) is assumed to be emitted closer (to the center of system) and kaon (anti-proton) is considered as emitted further from the system center

Like-sign particle combinations

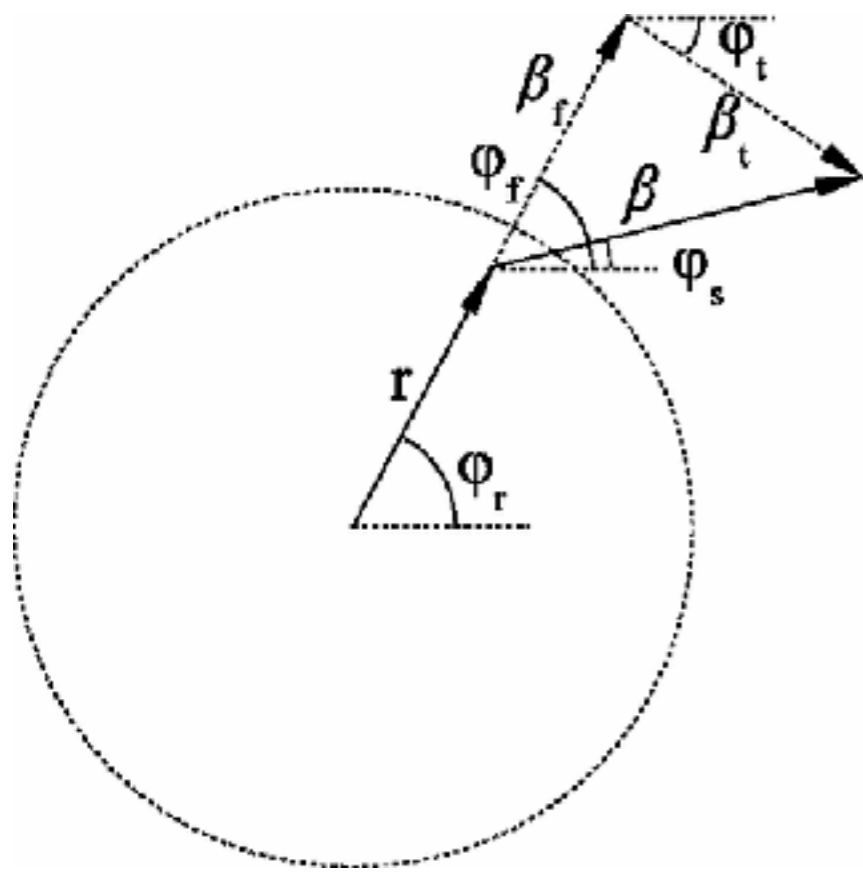


Unlike-sign particle combinations



Emission asymmetry arises in a system where both thermal and collective velocities exist and are comparable in magnitude
Lighter particles are emitted closer to the centre/later than heavier particles

Pion-Kaon system: asymmetry



In a hydrodynamical induced system :

$$\beta_{particle} = \beta_f + \beta_t$$

β_f : collective (flow) velocity
 β_t : thermal (random) velocity

component of mean emission point of a single particle parallel to the velocity

$$\langle x_{out} \rangle = \frac{\langle r \beta_f \rangle}{\langle \sqrt{\beta_t^2 + \beta_f^2} \rangle} = \frac{r_0 \beta_0 \beta}{\beta_0^2 + T/m_t}$$

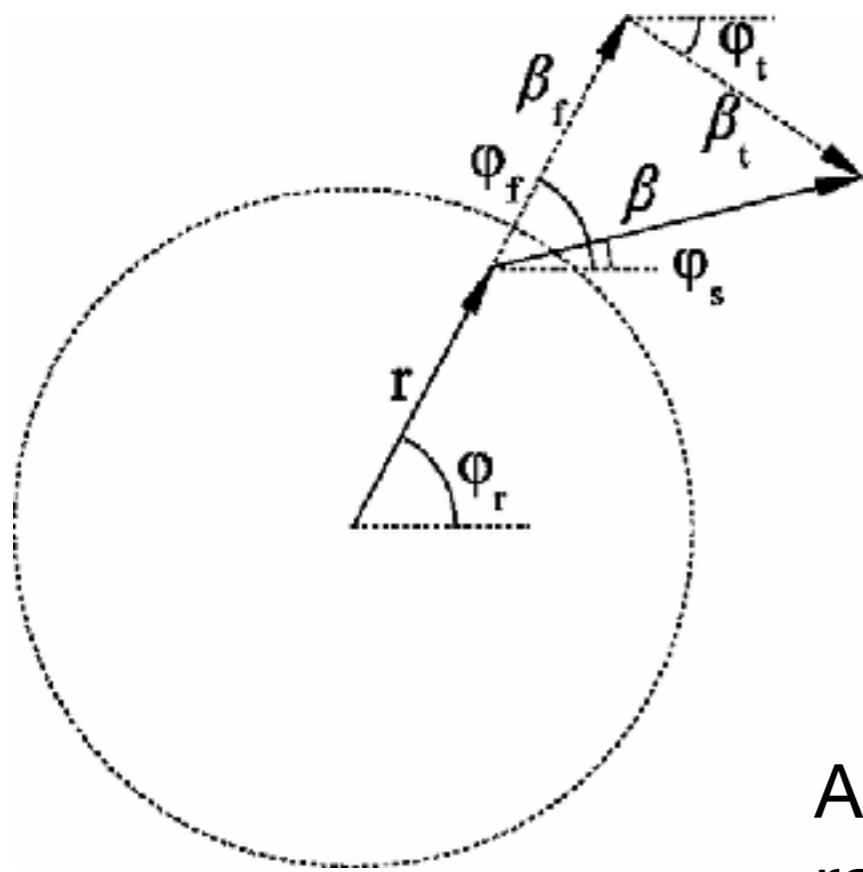
Adam Kisiel Phys. Rev. C 81,
064906 (2010)

For more details:

Talk by Adam Kisiel, 8/11/23

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Assuming Gaussian density profile,
 radius r_0 , linear transfer velocity profile $\beta_f = \beta_0/r_0$

$$S(r^*) = \exp \left(-\frac{(r_{out} - \mu_{out})^2}{\sigma_{out}^2} - \frac{r_{side}^2}{\sigma_{side}^2} - \frac{r_{long}^2}{\sigma_{long}^2} \right)$$

Adam Kisiel Phys. Rev. C 81,
 064906 (2010)

For more details:

Talk by Adam Kisiel, 8/11/23

$$\mu_{out}^{light,heavy} = \langle r_{out}^{light,heavy} \rangle = \langle x_{out}^{light} - x_{out}^{heavy} \rangle$$

Emission asymmetry arises in a system where both thermal and collective velocities exist and are comparable in magnitude

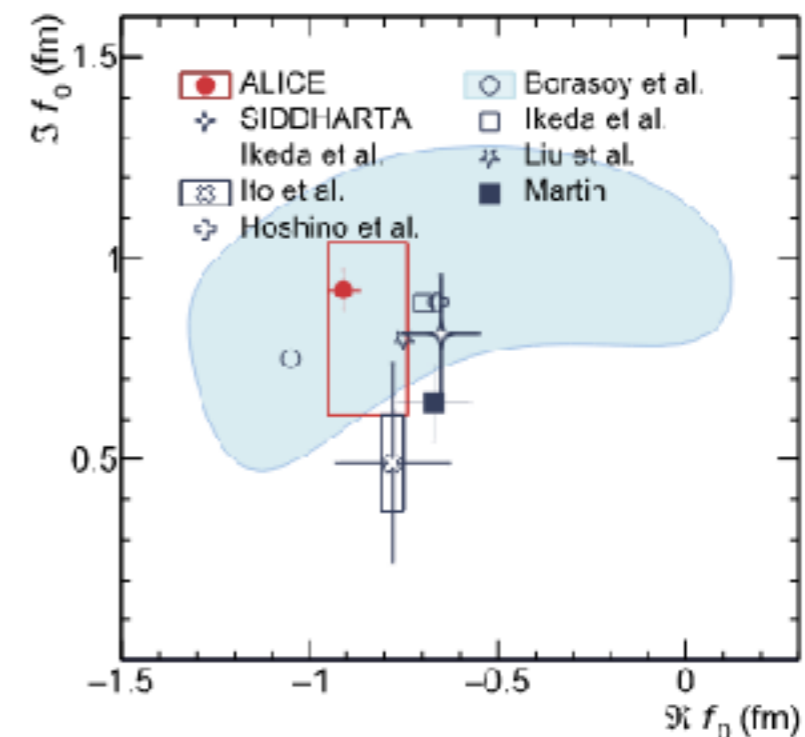
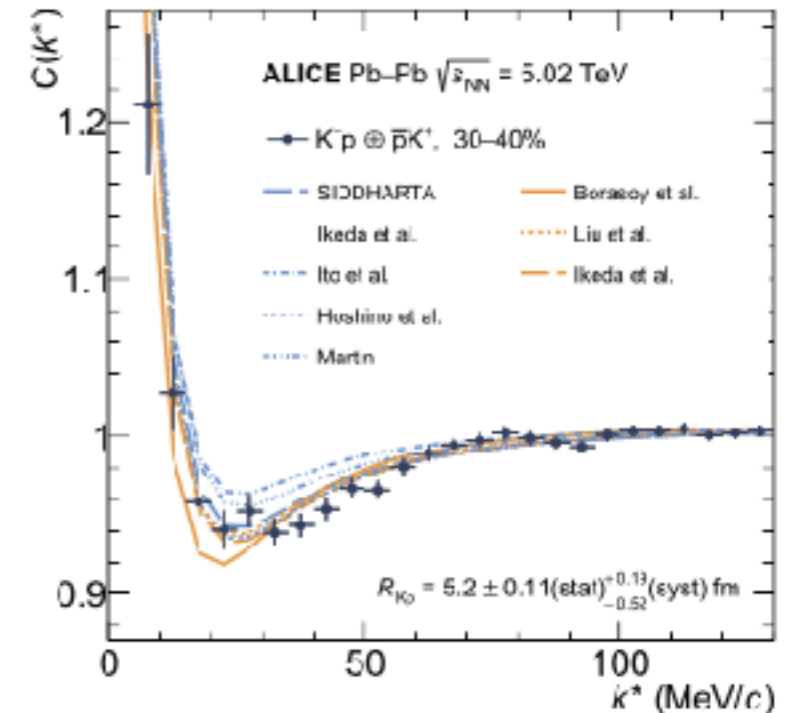
Lighter particles are emitted closer to the centre/later than heavier particles

Kaon-proton system: Strong interaction

- Kaons are less affected by the decay of resonances than pions
- Radius of particle emitting source - geometry of source
- Kaon-proton scattering parameters that describe the strong interaction
=>Scattering length f_0
=>effective range d_0

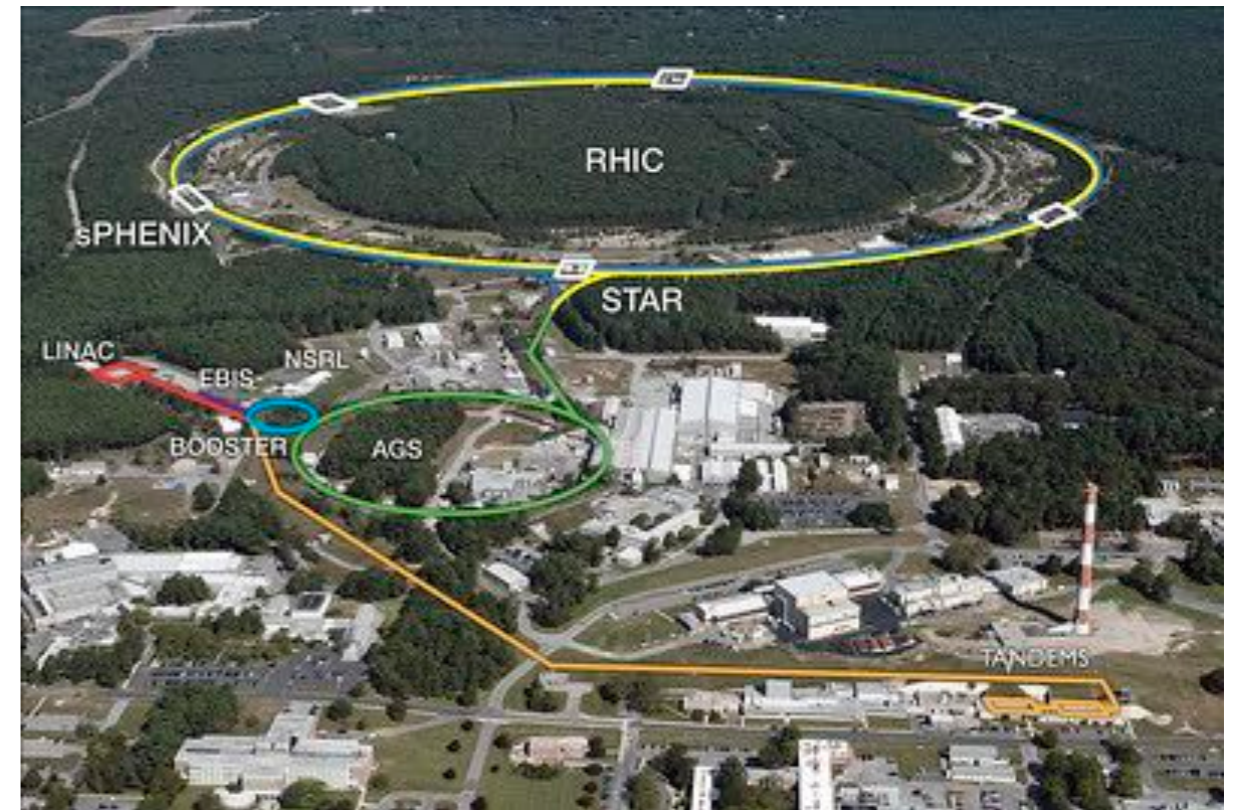
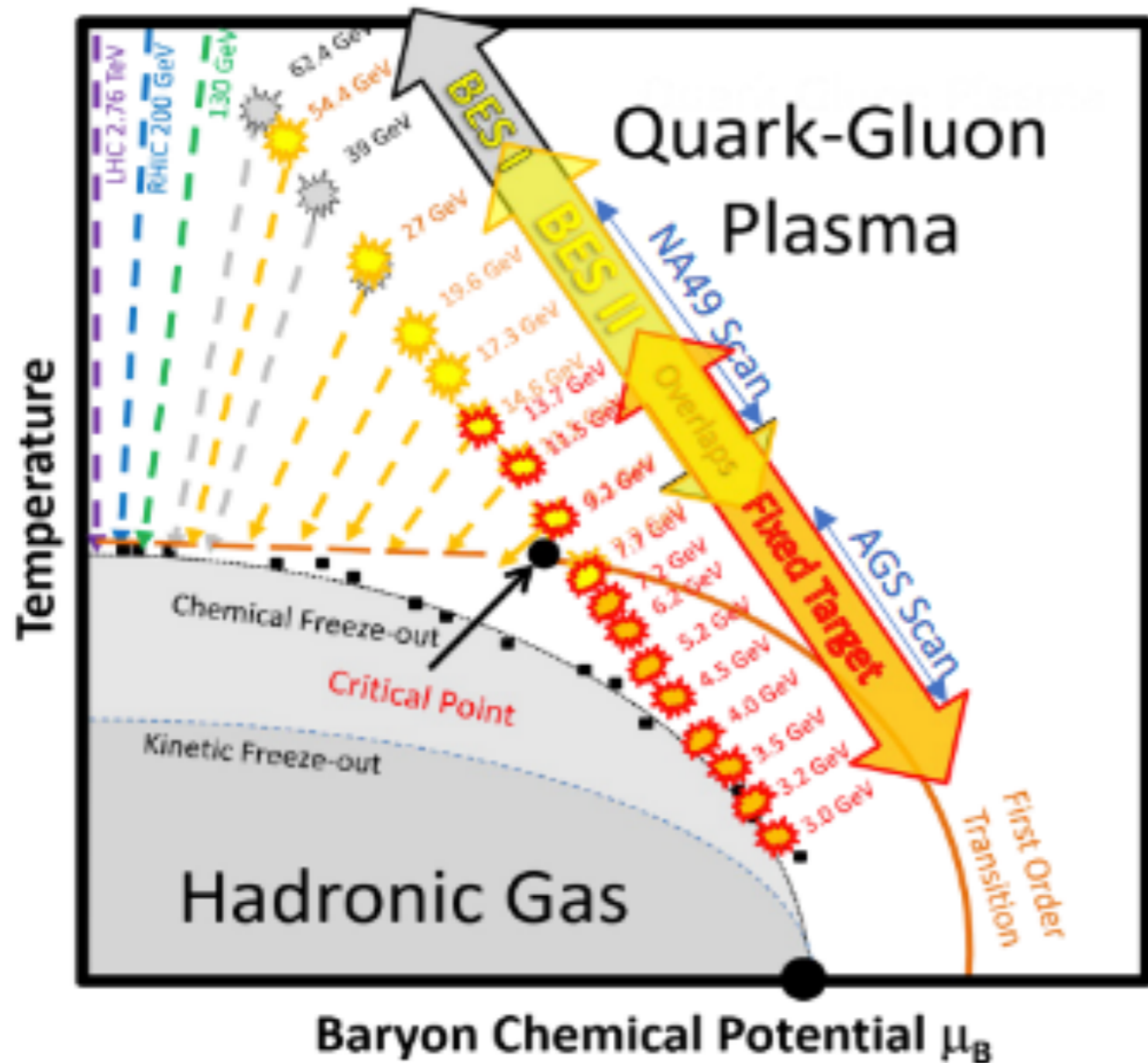
For more details:

Talk by Malgorzata Janik, 7/11/23



Kaon-proton, PbPb 5.02 TeV, ALICE Collaboration
Phy Let B 822 (2021) 136708

STAR experiment at RHIC

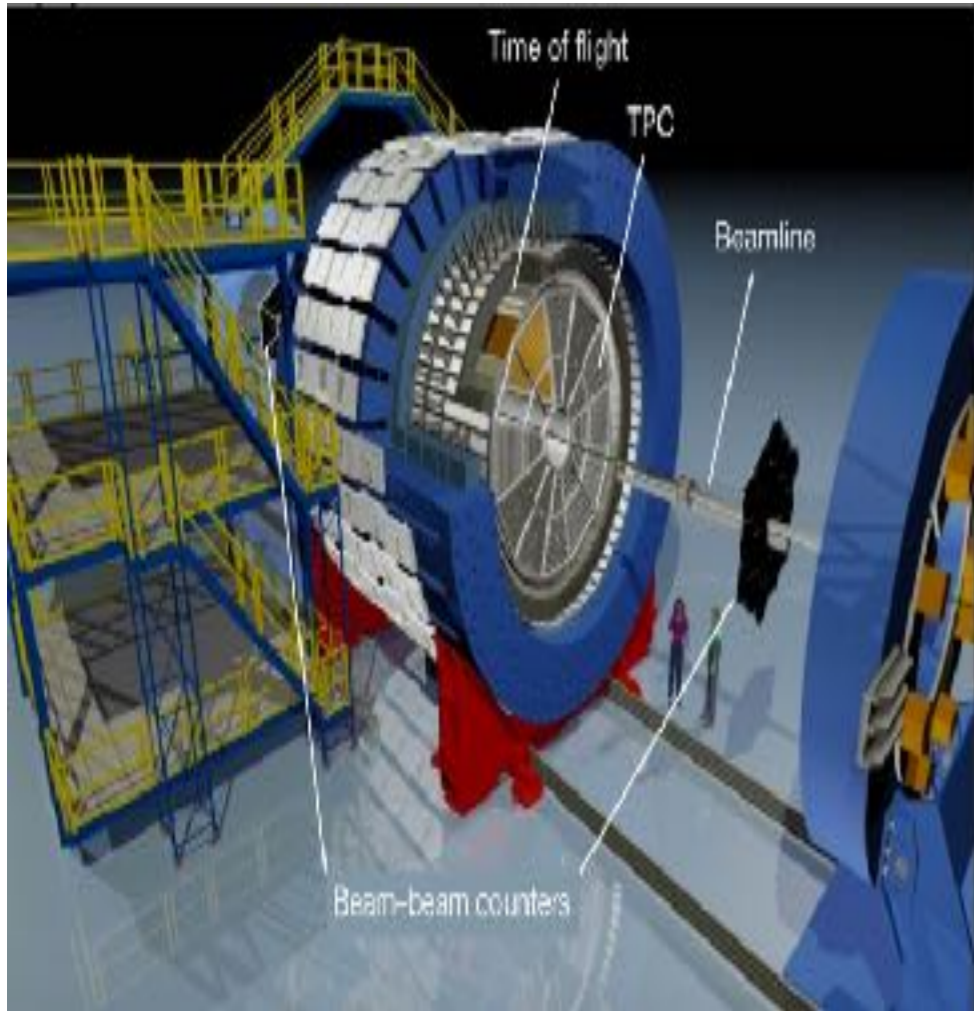


Energy:
 $\sqrt{s_{NN}} = 3- 200 \text{ GeV} (500 \text{ GeV for p+p})$

Systems:
 p+p, p+Al, p+Au, d+Au, $^3\text{He}+\text{Au}$, Cu+Cu, Cu+Au, Ru+Ru, Zr+Zr, Au+Au, U+U

<https://indico.cern.ch/event/1139644/contributions/5343956/>

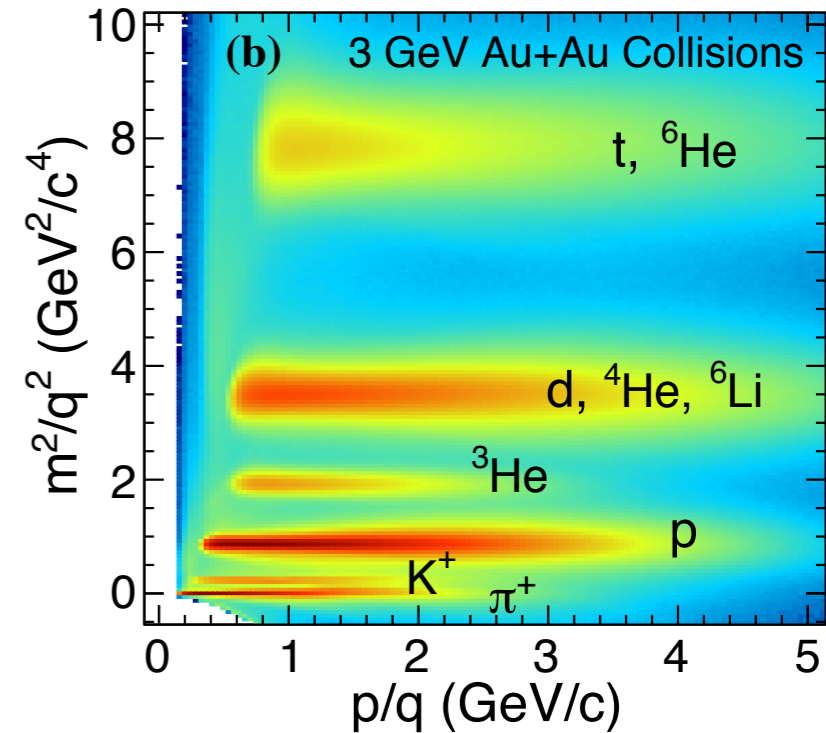
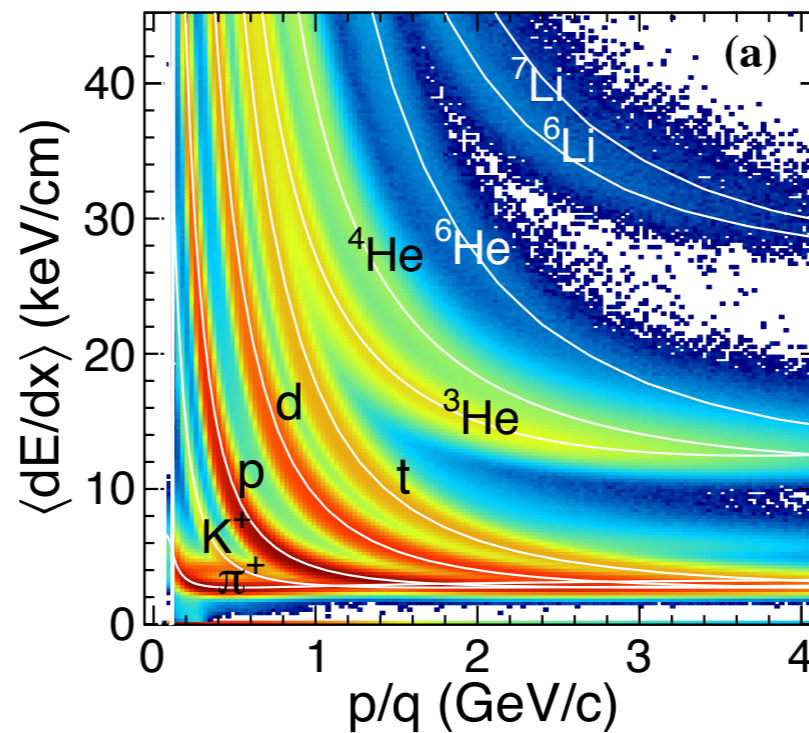
Particle Identification



$\sqrt{s_{NN}}$	7.7	11.5	39 (0-10%)	39 (10-30%)	39 (30-70%)
#Events (in mln)	0.24	1.3	11.7	25.7	45.4

TPC - ionization energy loss

From TOF - mass²



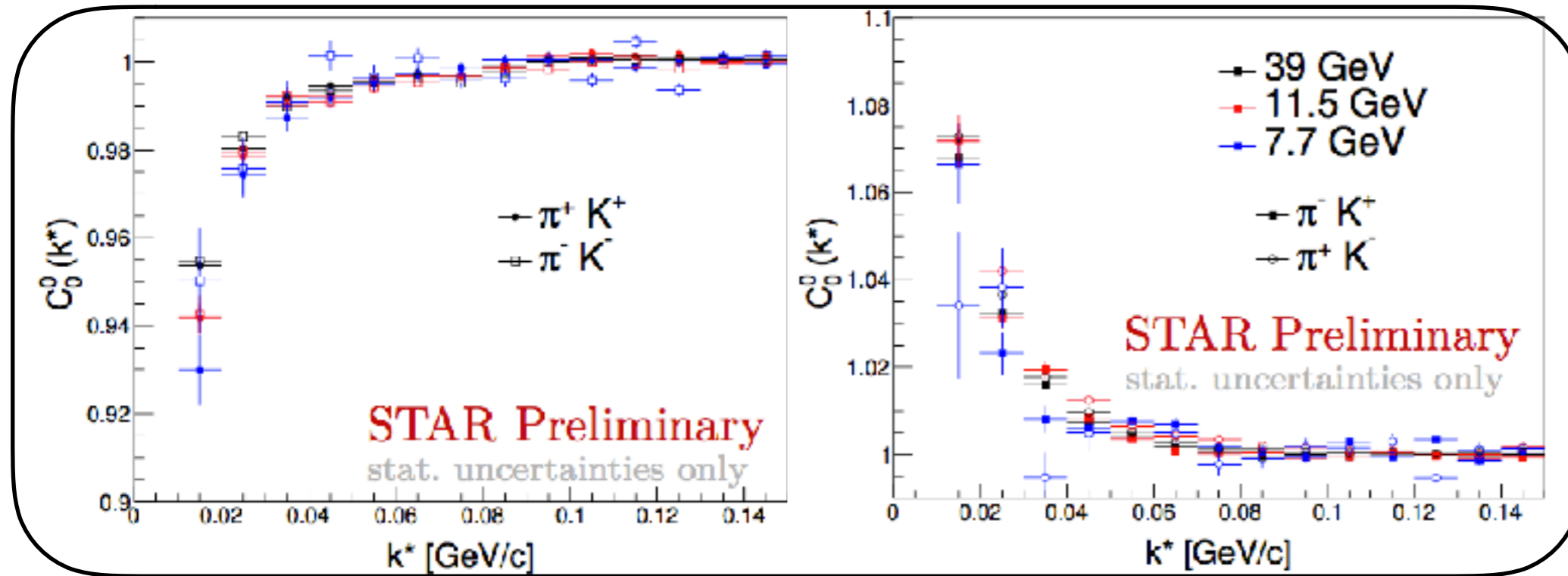
STAR collaboration

Phys. Lett. B 827 (2022) 136941

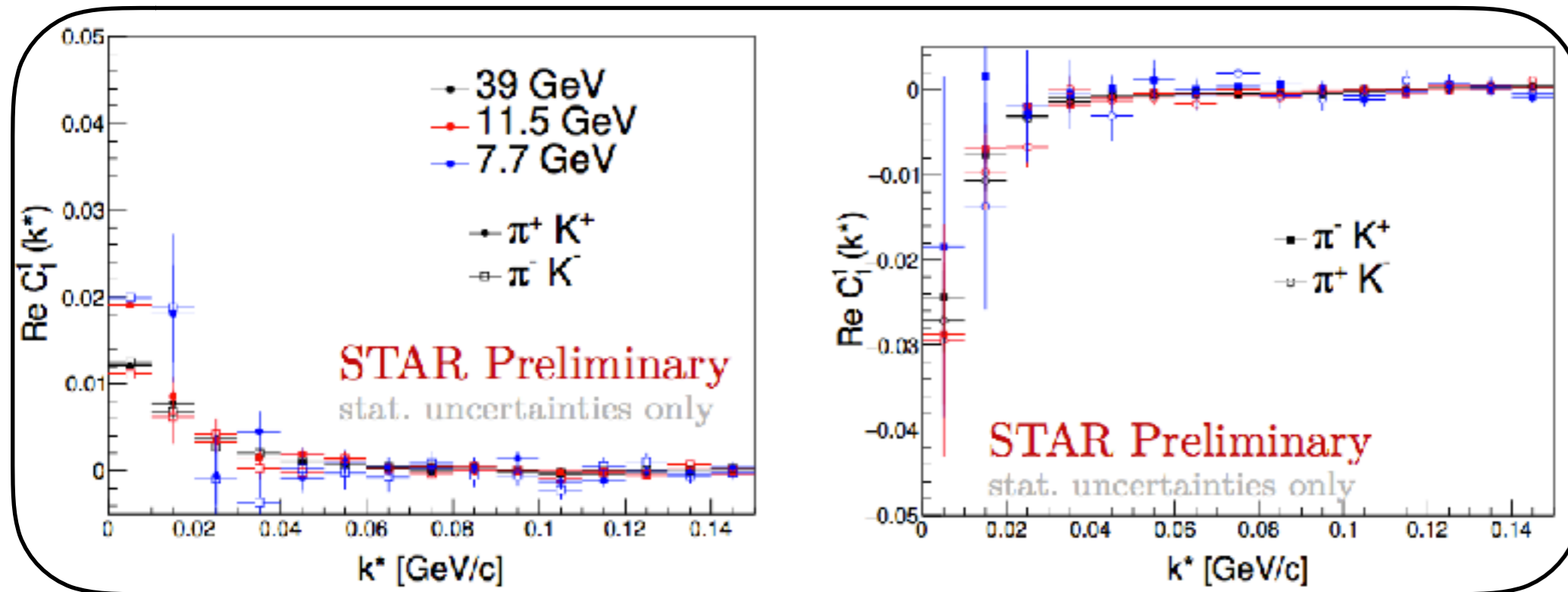
<https://doi.org/10.1038/nature23004>

Large acceptance: $|\eta| < 1.8$, $0 < \phi < 2\pi$
Excellent particle identification capabilities (Time Of Flight and Time Projection Chamber)

Collision energy dependence

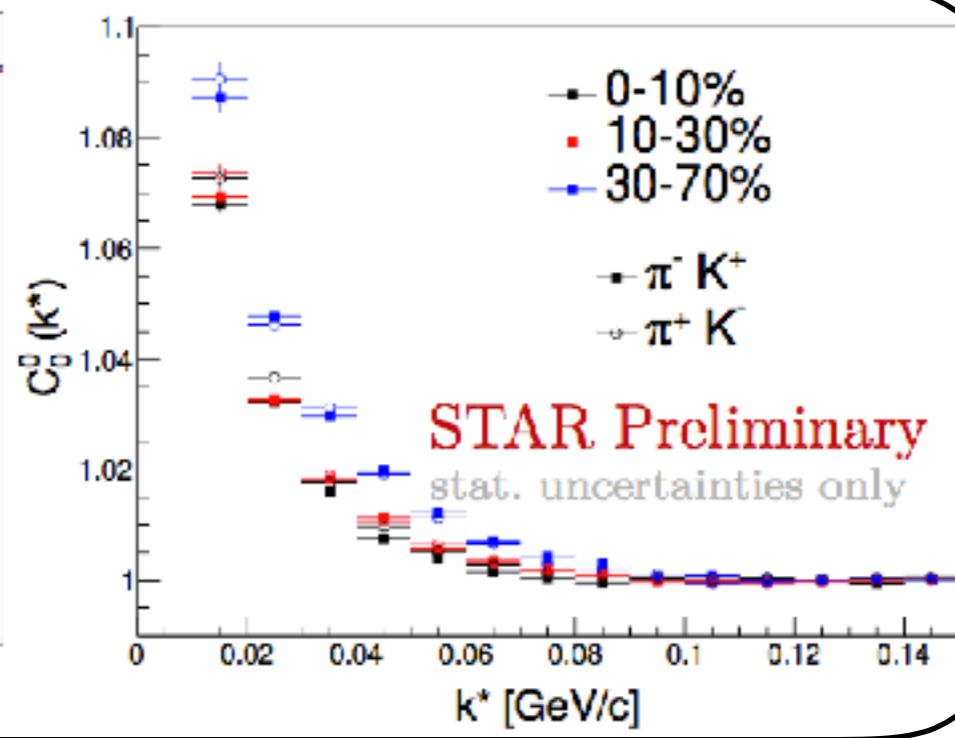
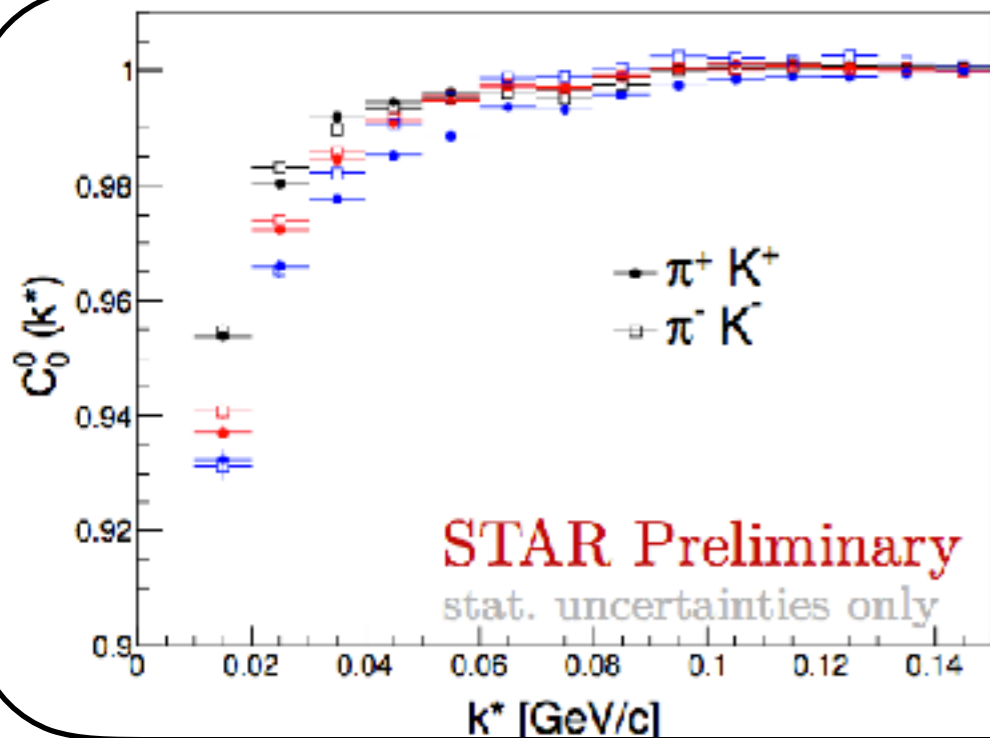


Visible energy dependence

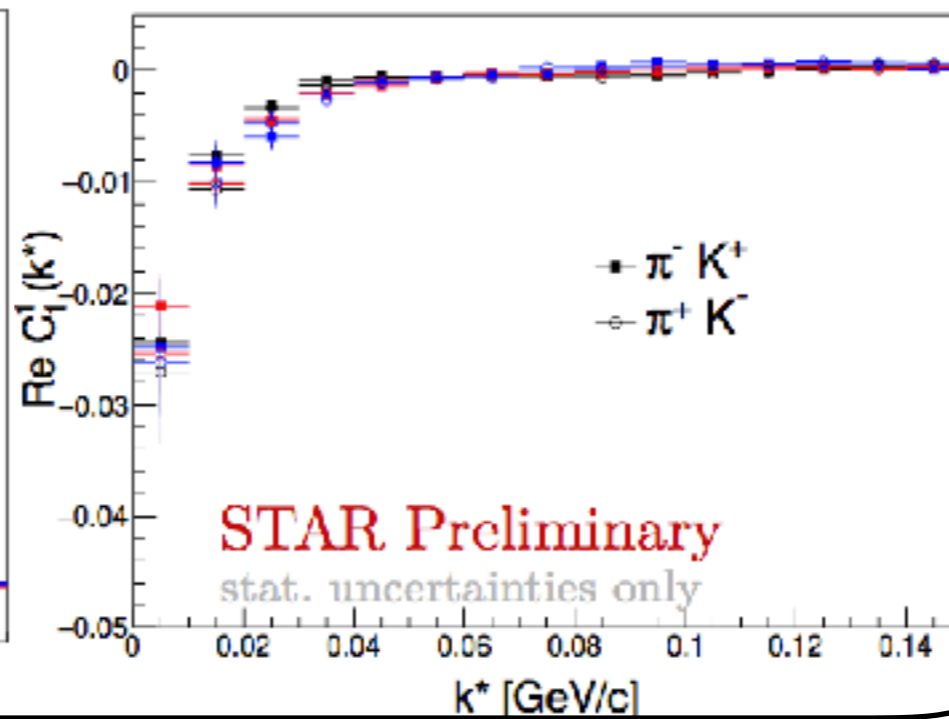
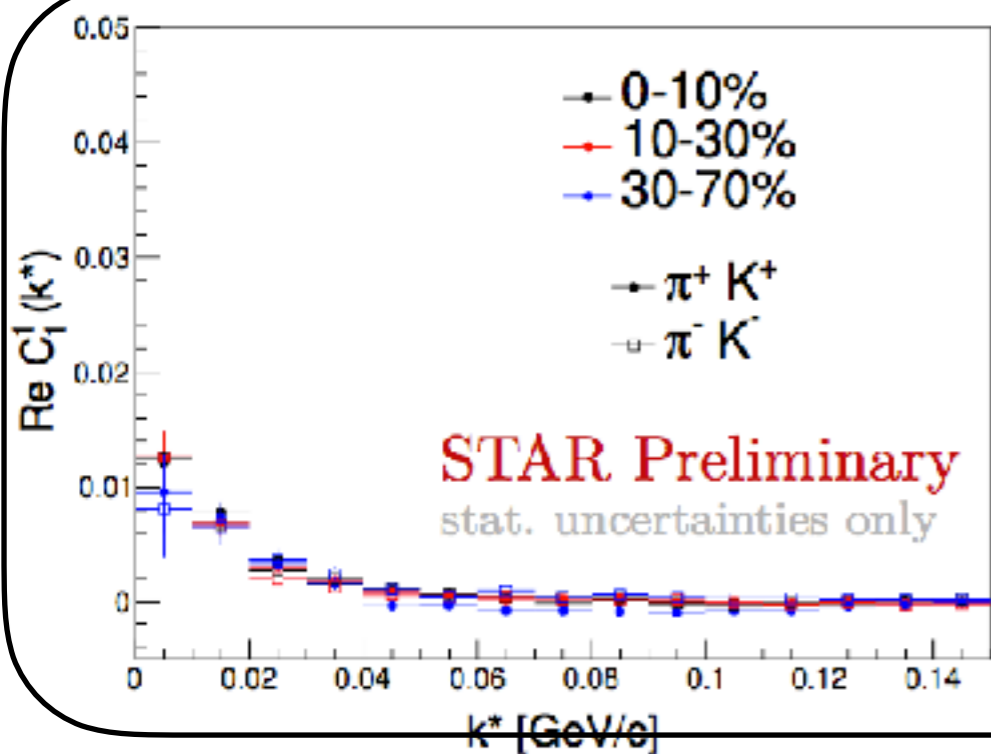


<Zero: signal of emission asymmetry

Centrality dependence

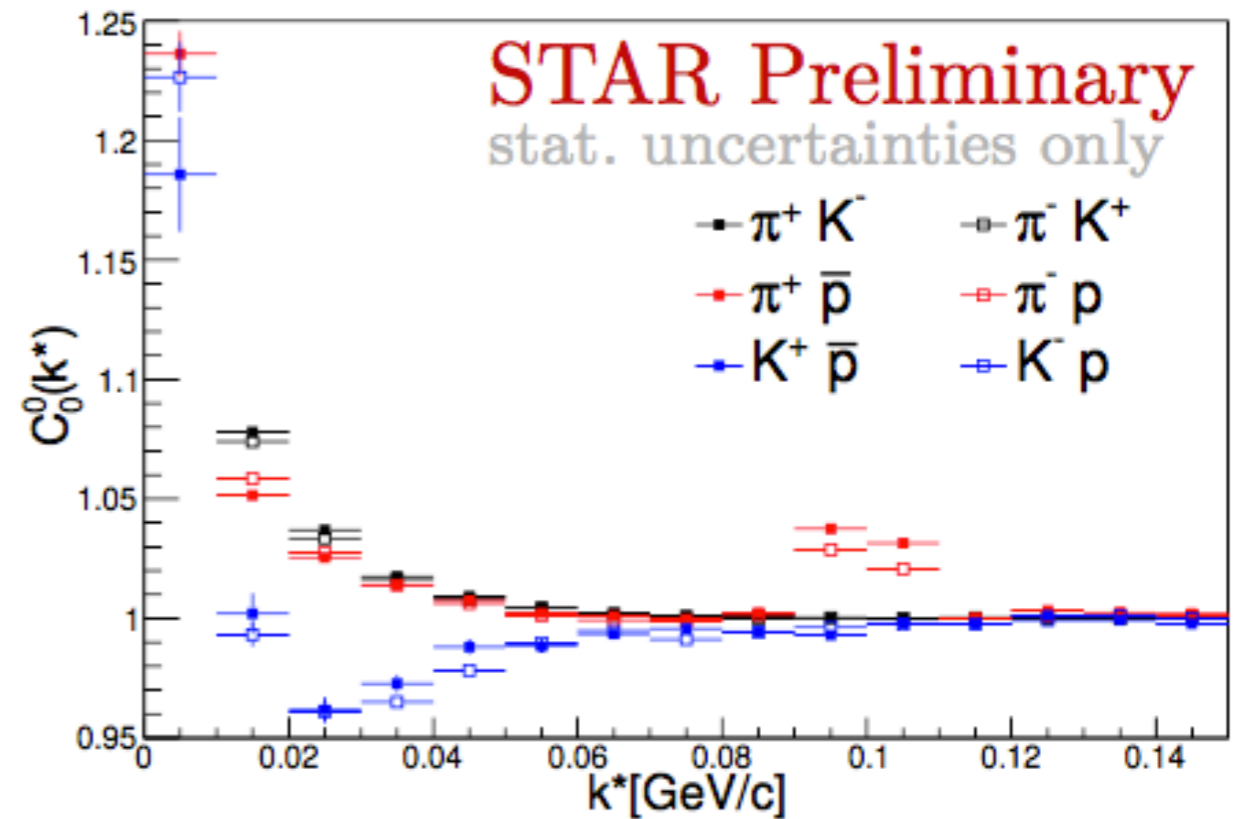
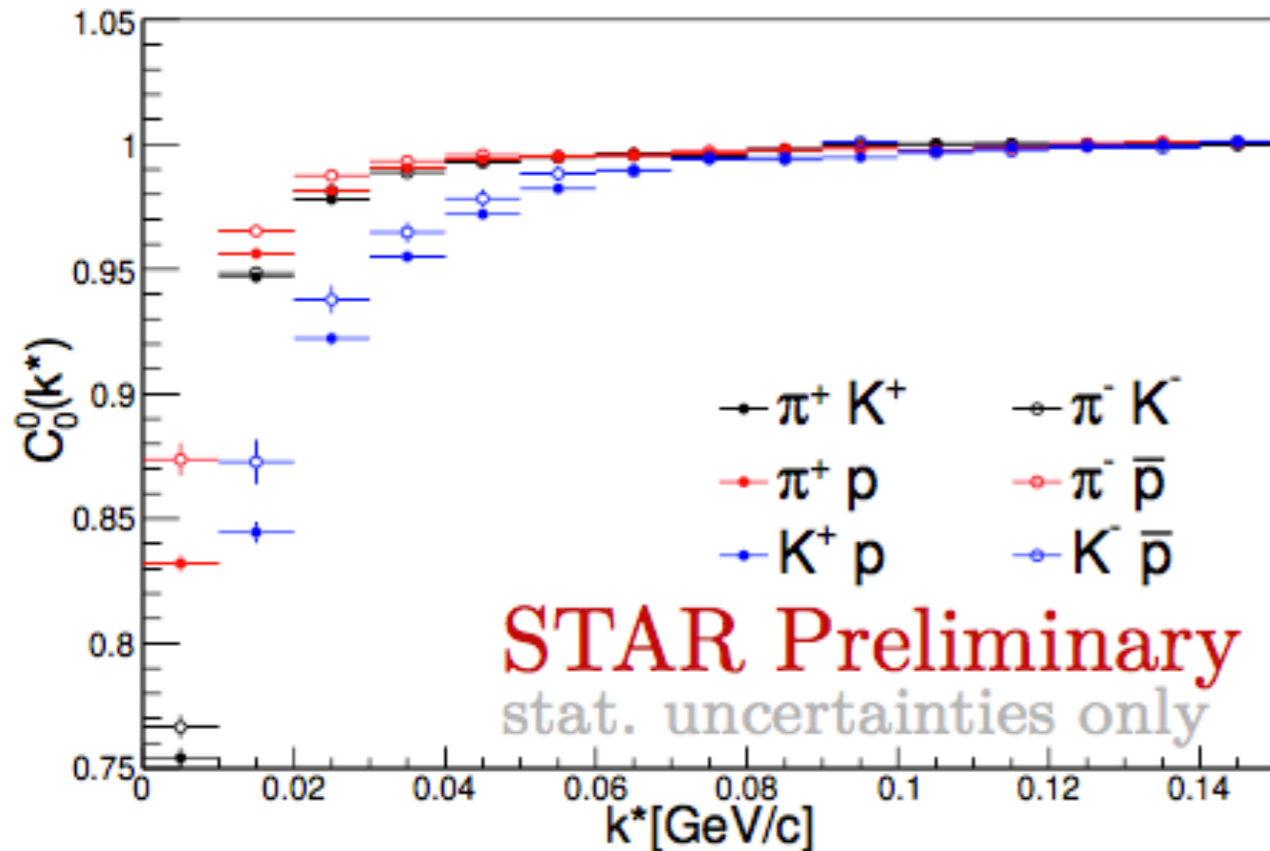


Visible centrality dependence



<Zero:
signal of
emission
asymmetry

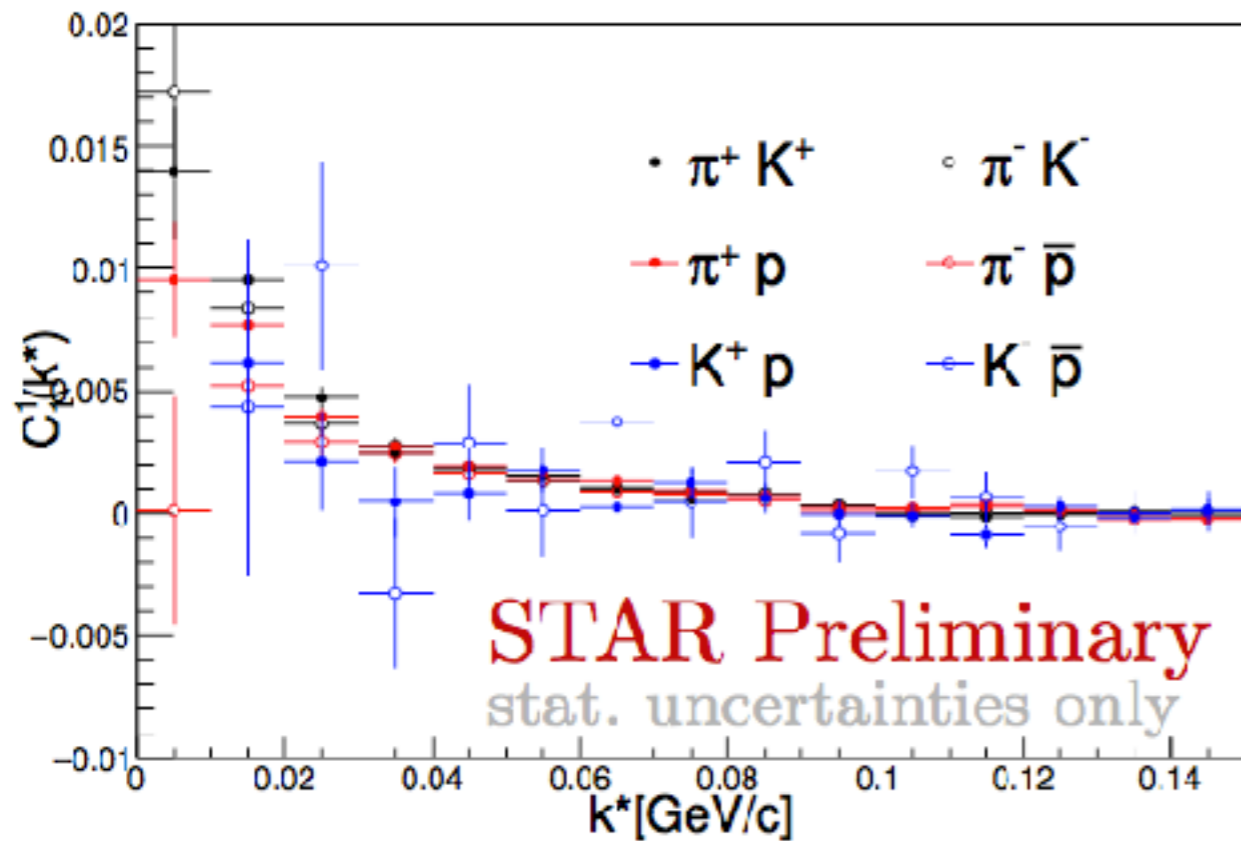
System dependence



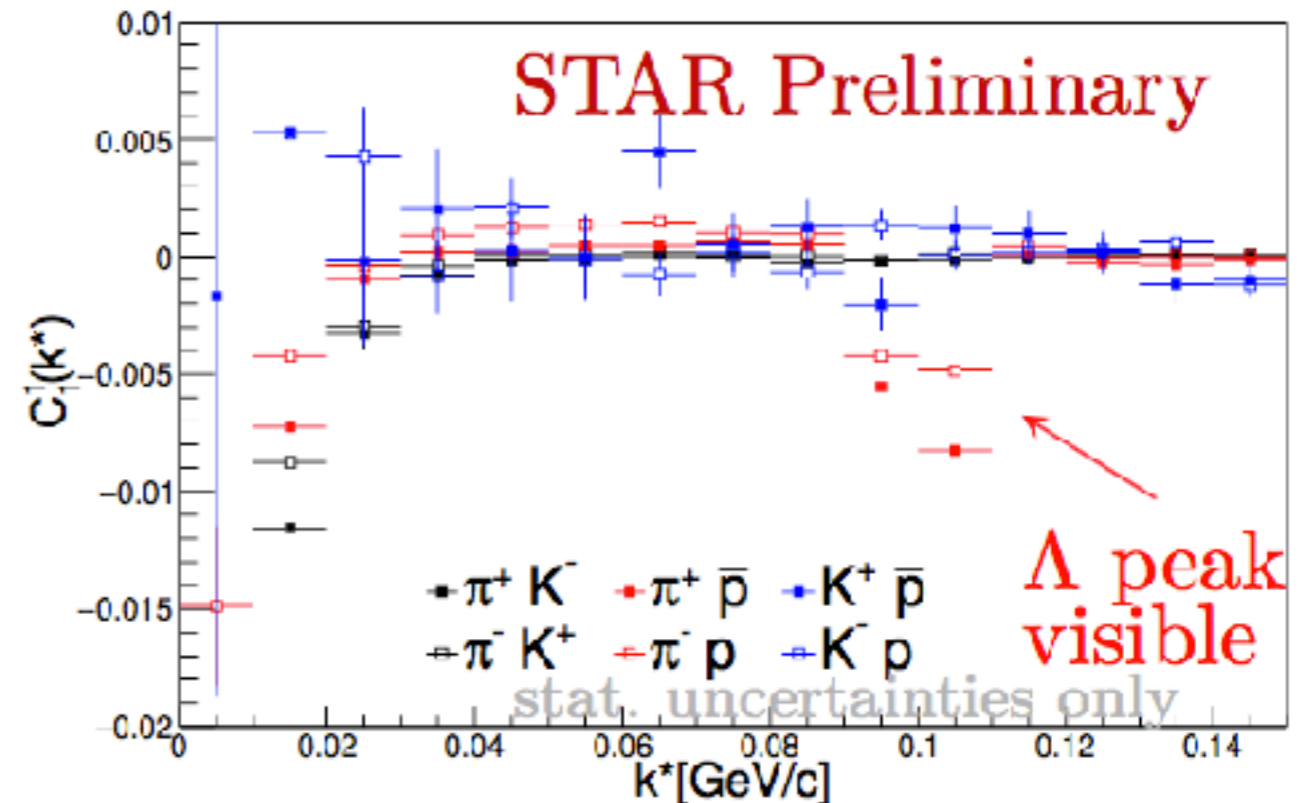
- Clear system dependence.
- Correlation function dominated by Coulomb interaction.
- Kaon-proton \rightarrow strongest correlation.

- $\Lambda(1116)$ peak visible in pion-proton.
- Kaon-proton pairs have significant strong interaction.

System dependence



Visible signal of emission asymmetry



Expected ordering of particles ->
sensitive to collective effects

Conclusion

Geometry:

Visible centrality, system and energy dependence of source size at BES energies.

Dynamics:

Clear signal of emission asymmetry for pion-kaon systems
=>collectivity effects

Lighter particles are emitted closer to the center and/or later

 Interactions:

A. Repulsive strong interaction appears below unity in the region of k^*
 $\sim 10-50$ MeV/c for Kaon-proton pair.

B. Like Sign correlation function:

Like sign pairs are dominated by Coulomb.

Kaon-proton \rightarrow strongest correlation.

C. Unlike sign correlation function:

$\Lambda(1116)$ peak visible in pion-proton.

Kaon-proton correlation function sensitive to strong interaction.

Outlook

- Exploring kaon-proton interaction
- Parameter of strong interaction - to be extracted

Thank you !