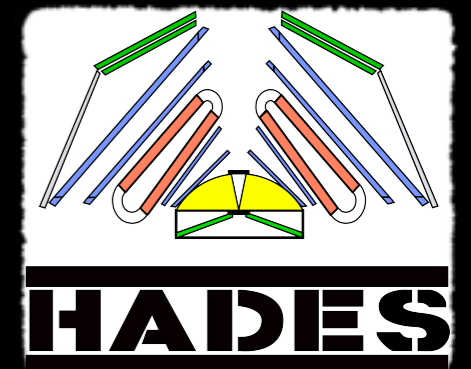




# Proton-proton and proton-cluster femtoscopy at the HADES experiment

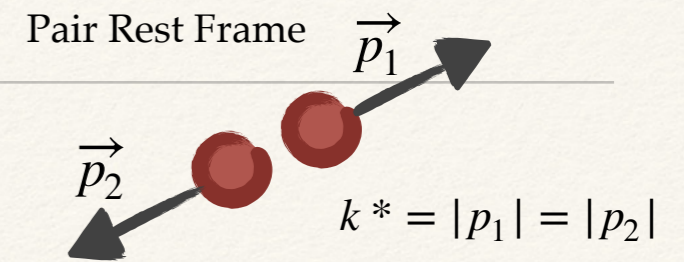
*Maria Stefaniak for HADES Collaboration*

1





# Femtoscscopy

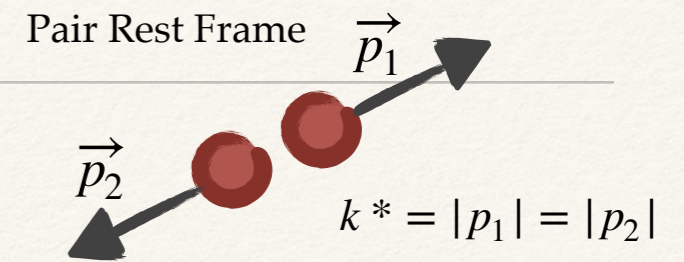


*Koonin-Pratt formula:*

$$C(k^*) = \int S(r^*) |\Psi(k^*, r^*)|^2 d^3 r^*$$

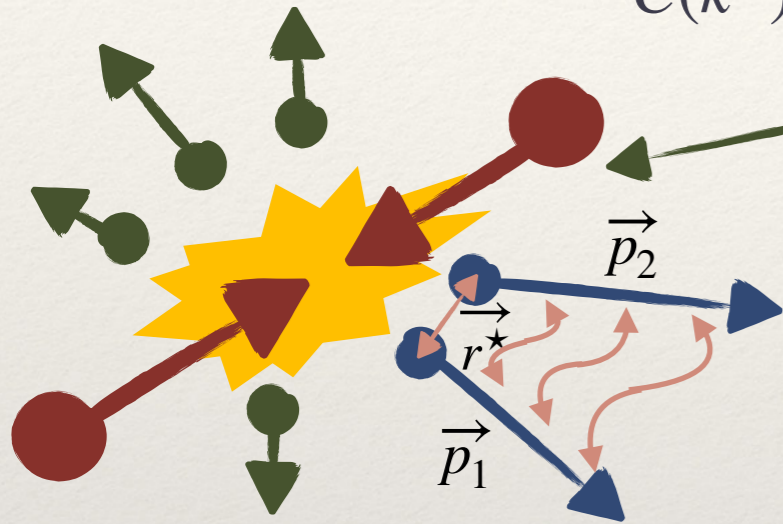


# Femtoscscopy



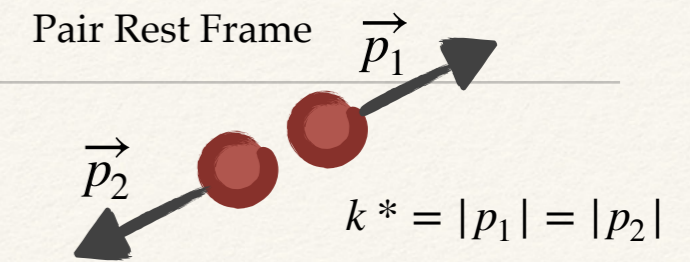
Koonin-Pratt formula:

$$C(k^*) = \int S(r^*) |\Psi(k^*, r^*)|^2 d^3 r^*$$



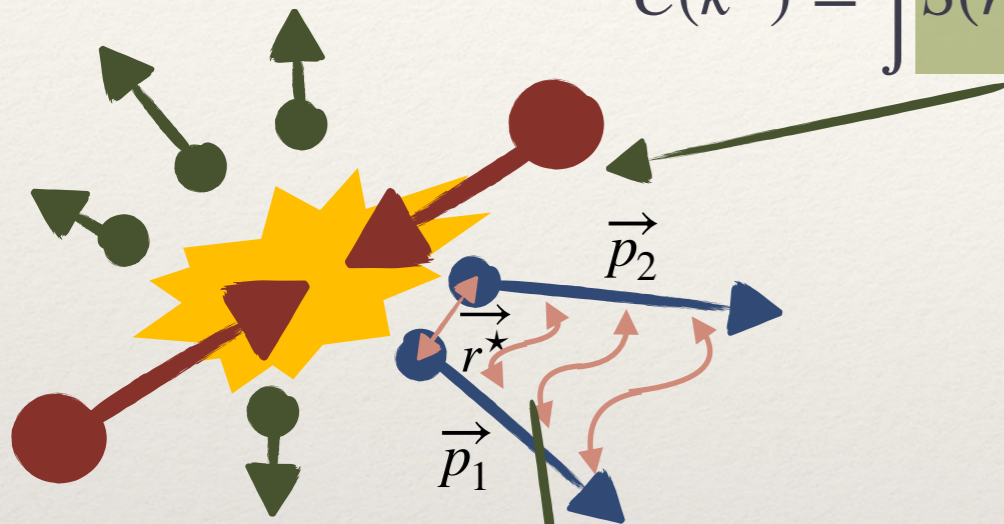


# Femtoscscopy

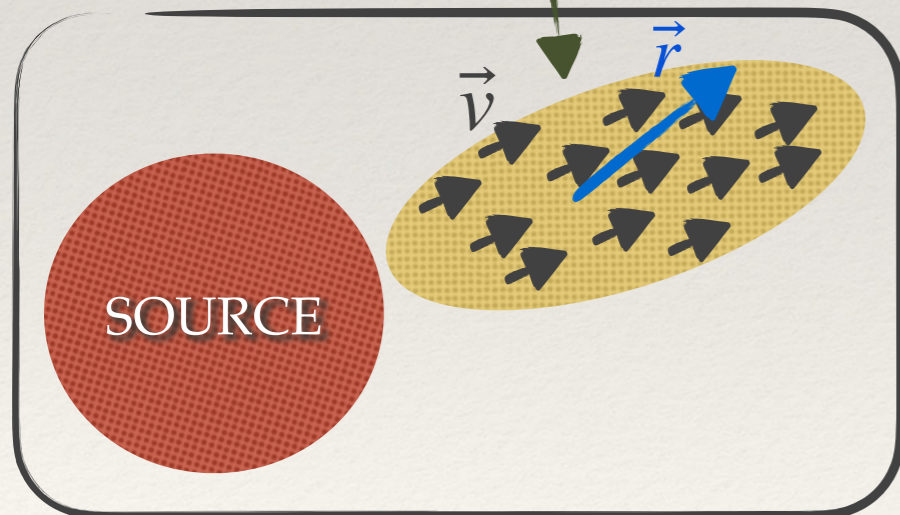


Koonin-Pratt formula:

$$C(k^*) = \int S(r^*) |\Psi(k^*, r^*)|^2 d^3 r^*$$

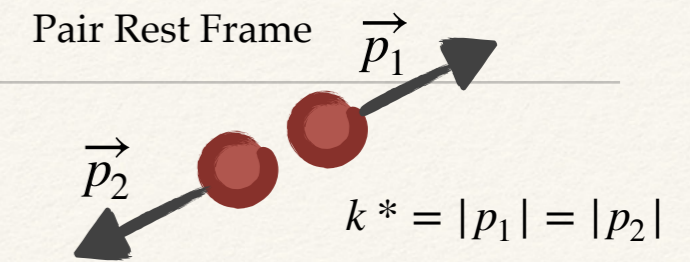


Measurements of phase space cloud



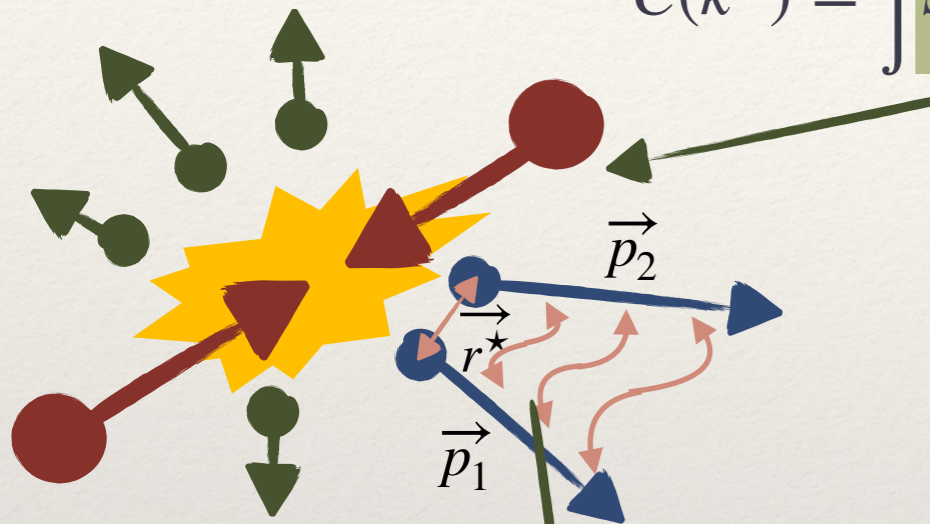


# Femtoscscopy



Koonin-Pratt formula:

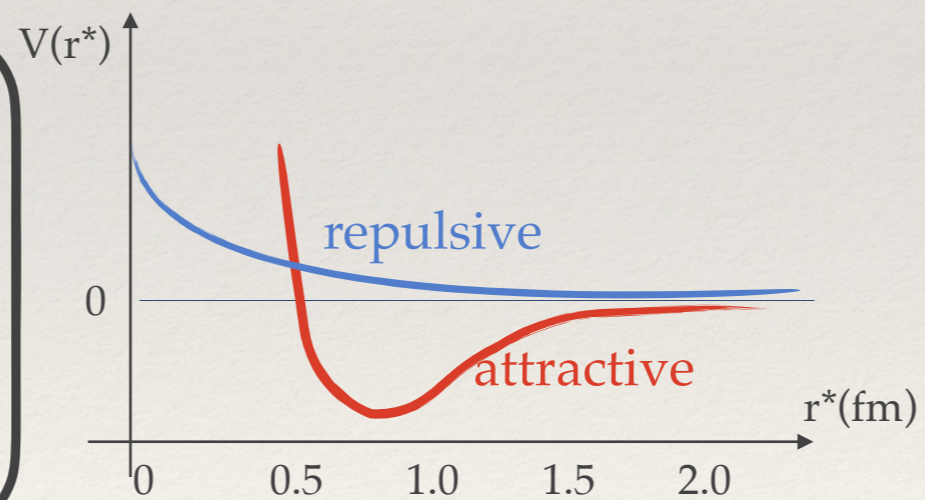
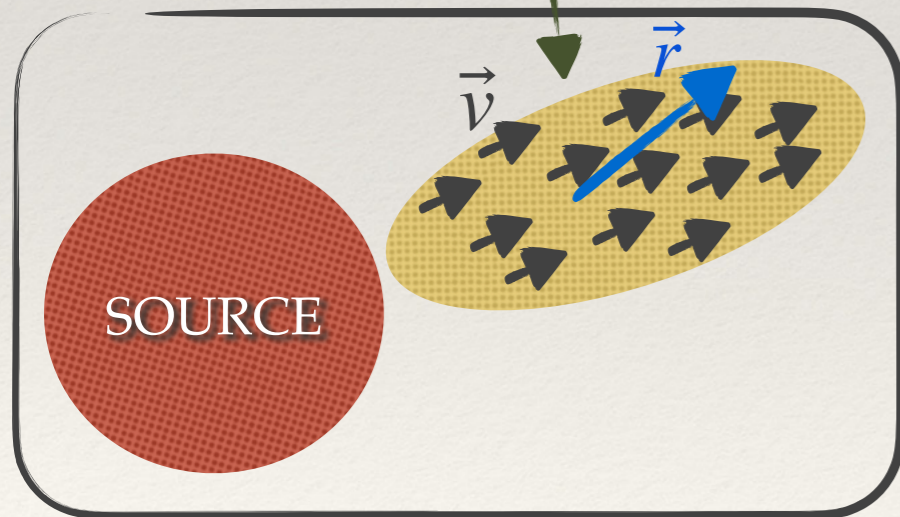
$$C(k^*) = \int S(r^*) |\Psi(k^*, r^*)|^2 d^3 r^*$$



Two-particle wave function

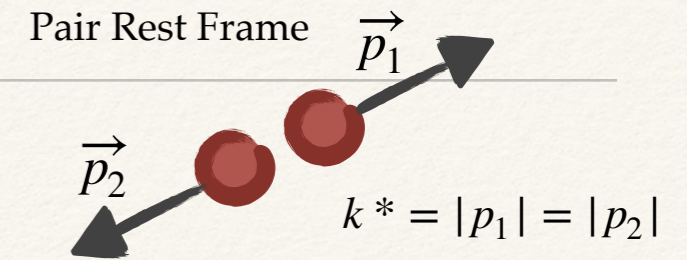
Schrödinger equation

Measurements of phase space cloud





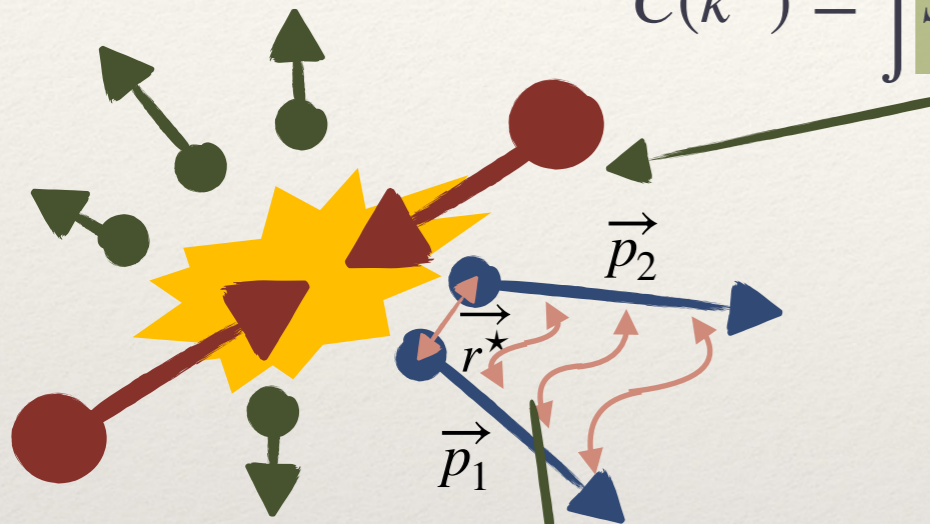
# Femtoscscopy



Koonin-Pratt formula:

$$C(k^*) = \int S(r^*) |\Psi(k^*, r^*)|^2 d^3 r^* = \frac{S_{\text{gnl}}(k^*)}{B_{\text{ckg}}(k^*)}$$

**In experiment:**  
 combination of all possible pairs in  
**Signal:** the same event  
**Background:** different events.

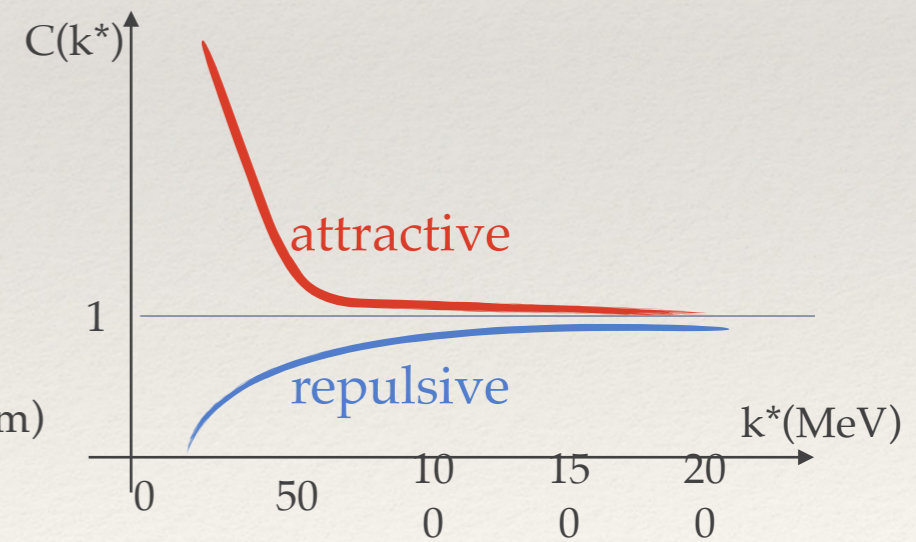
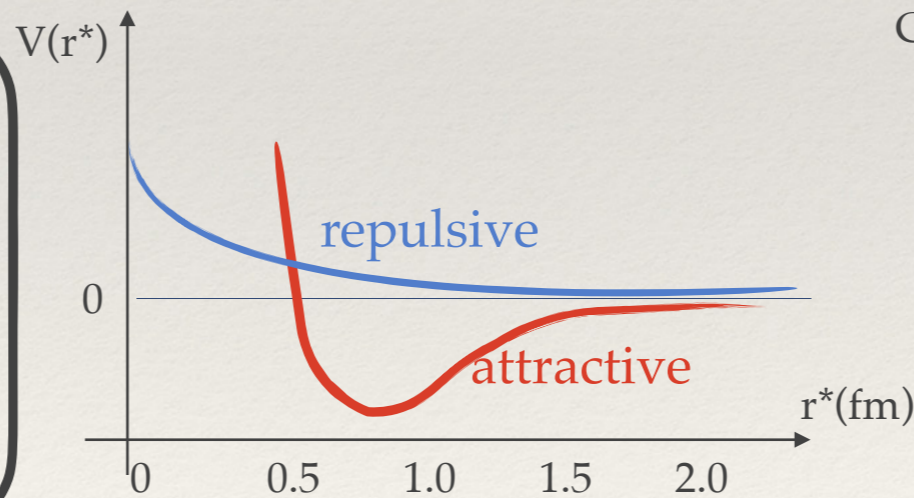
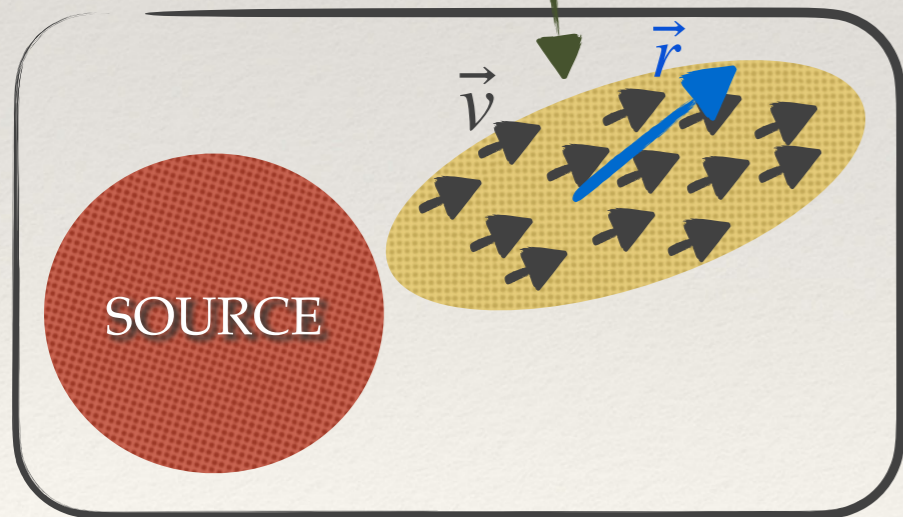


Two-particle wave function

Schrödinger equation

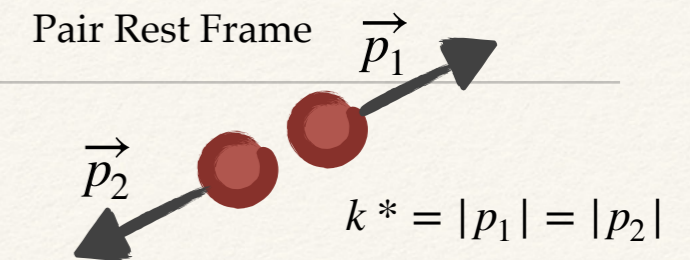
Correlation function

Measurements of phase space cloud





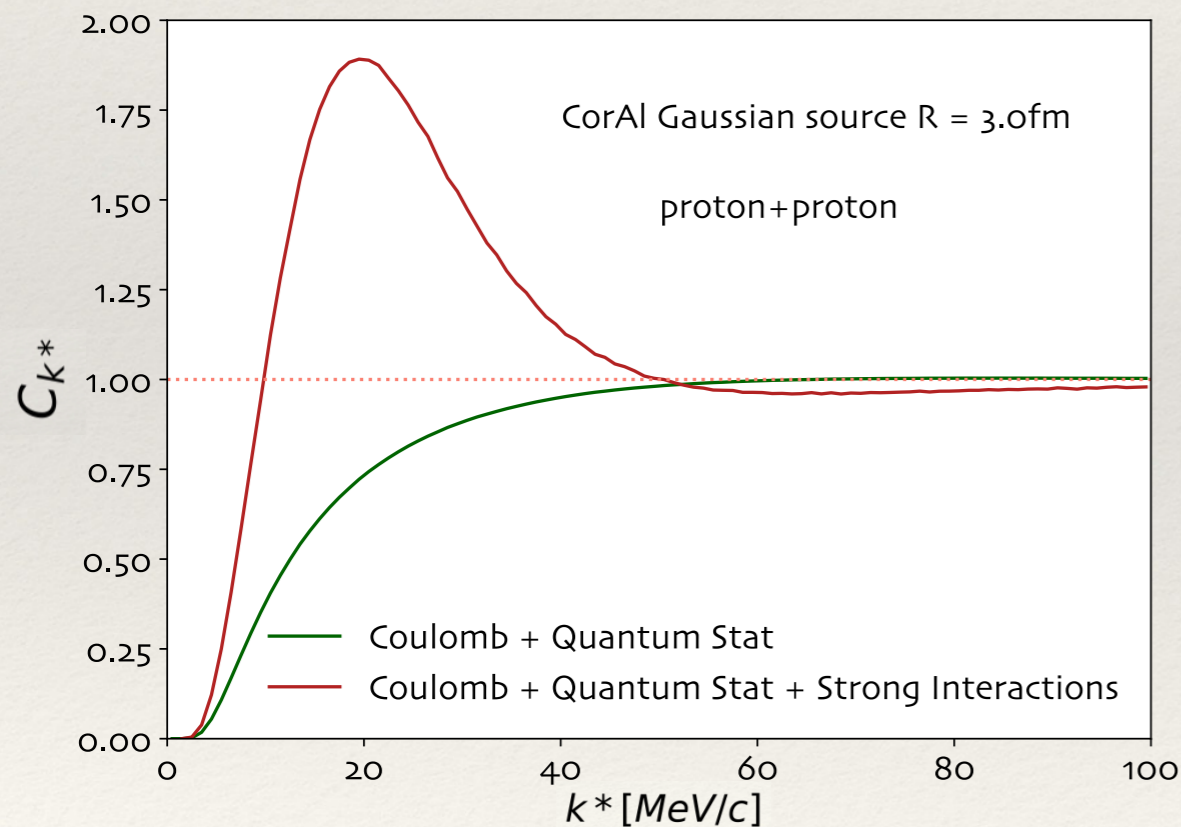
# Femtoscscopy



Koonin-Pratt formula:

$$C(k^*) = \int S(r^*) |\Psi(k^*, r^*)|^2 d^3 r^* = \frac{Sgnl(k^*)}{Bckg(k^*)}$$

Origin of the Correlation Function:



## 1. Coulomb:

- Attractive for opposite sign particles
- **Repulsive for same sign particles**

## 2. Quantum Statistic:

- Bosons: positive
- **Fermions: negative**

## 3. Strong Interactions:

- Can be both **attractive** or **repulsive**, depending on potentials



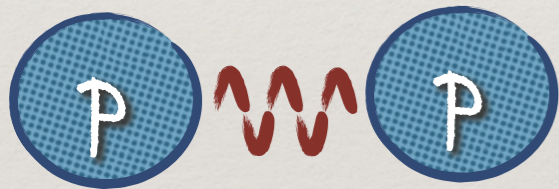
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# Measurements

---

Femtoscopic correlations of:

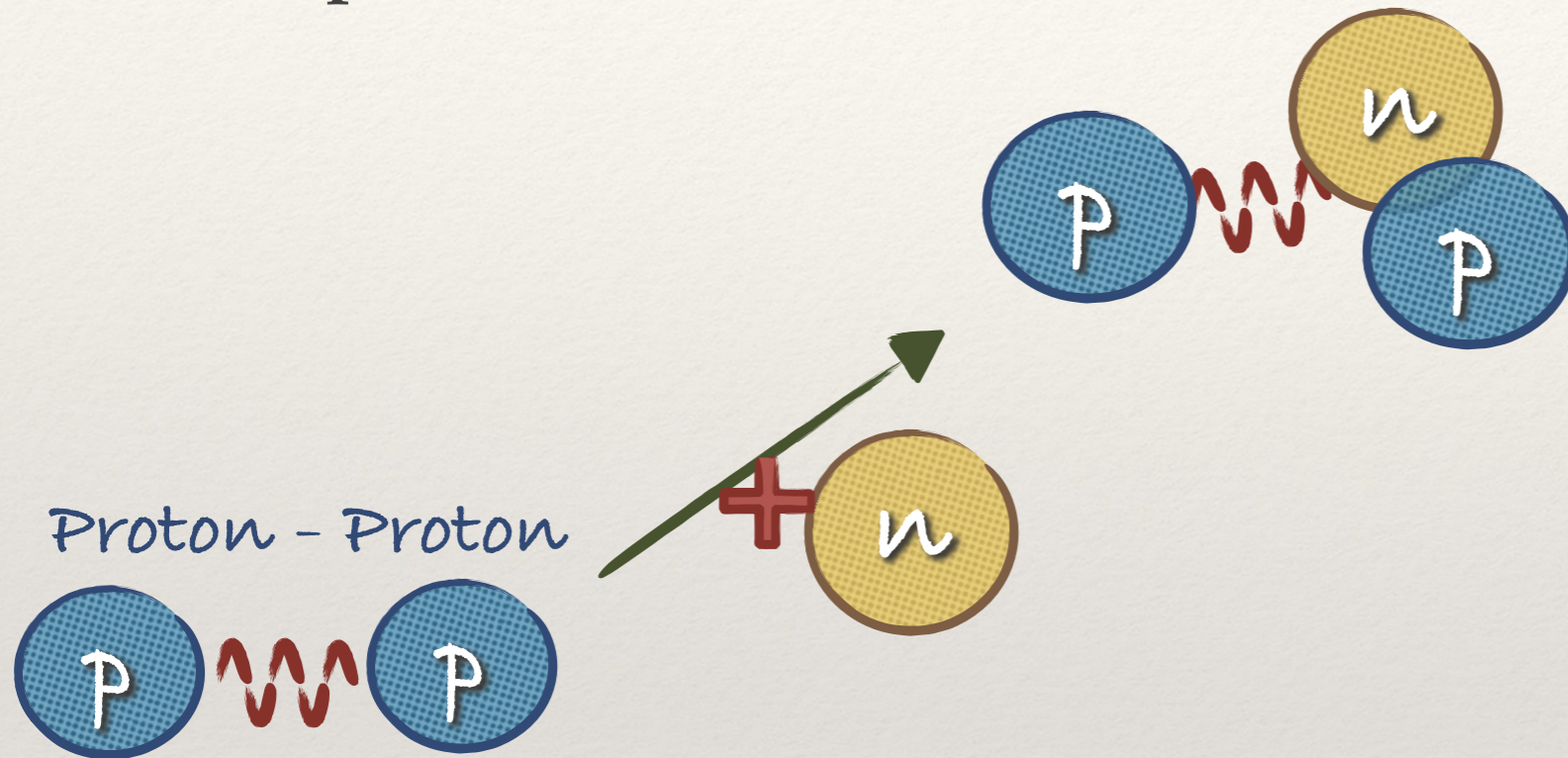
Proton - Proton





# Measurements

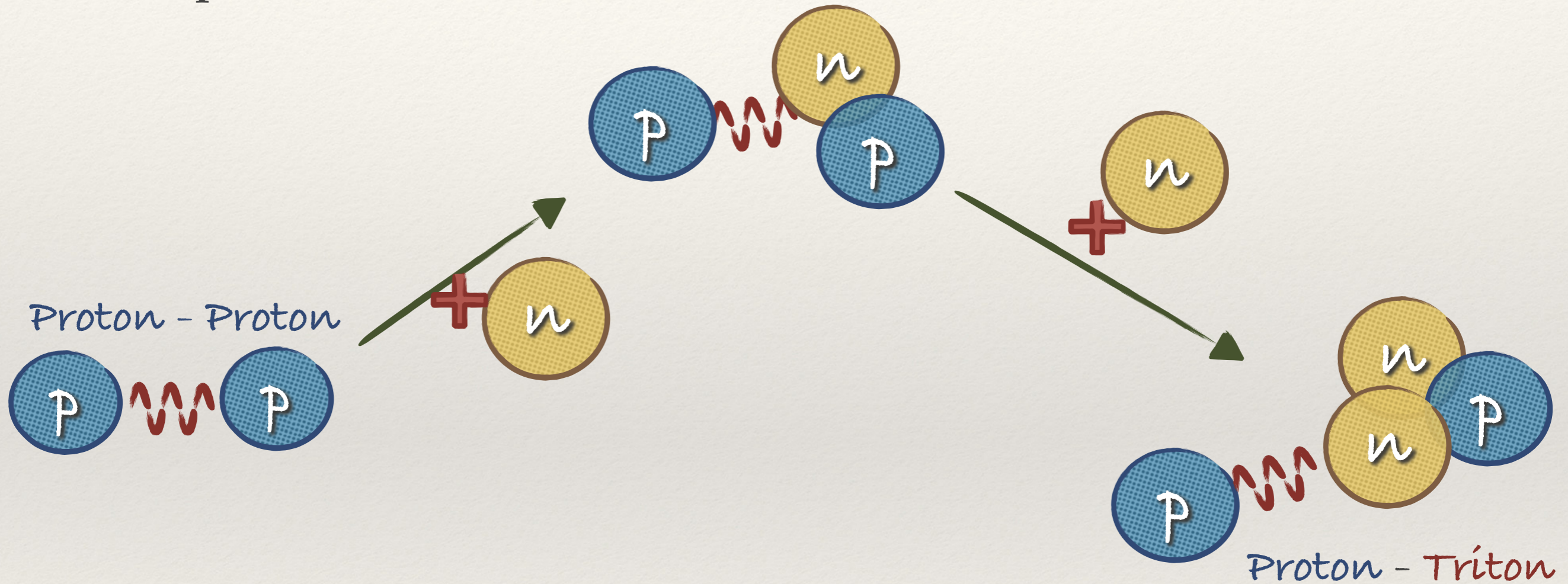
Femtoscopic correlations of: Proton - Deuteron





# Measurements

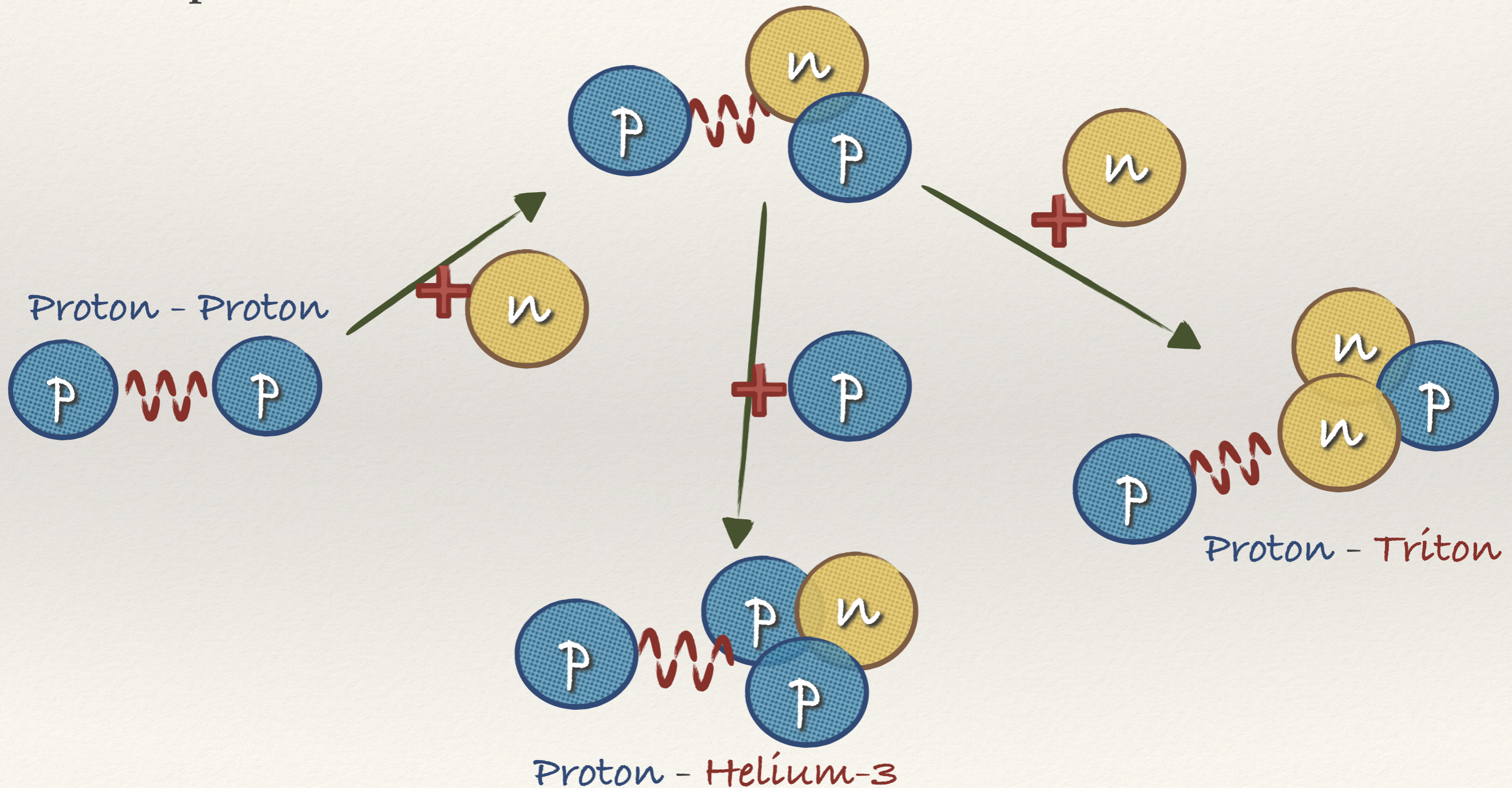
Femtoscopic correlations of: Proton - Deuteron





# Measurements

Femtoscopic correlations of: Proton - Deuteron





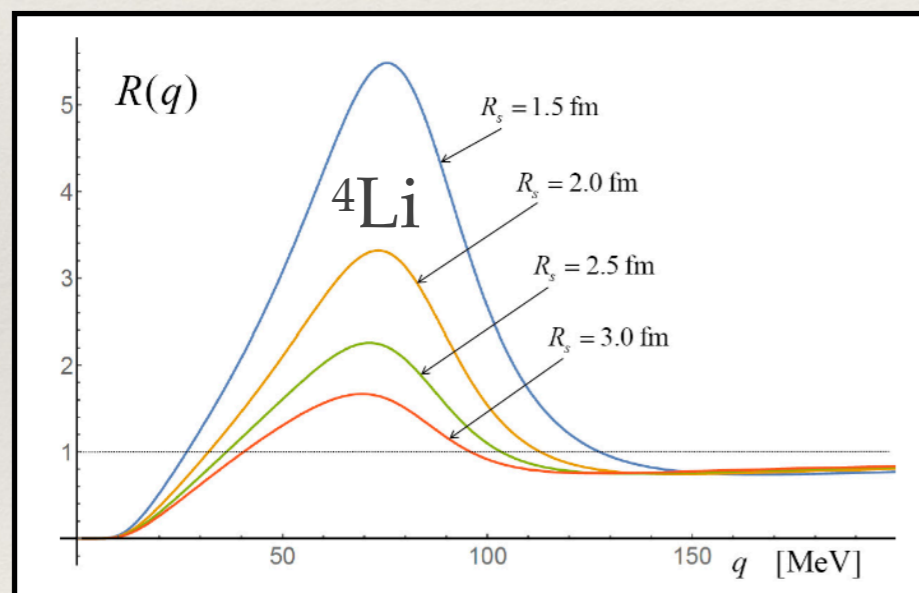
# Motivation

## 1. Studies of decaying nuclear state presence

Some of them impossible to see in traditional “mass invariant” distributions

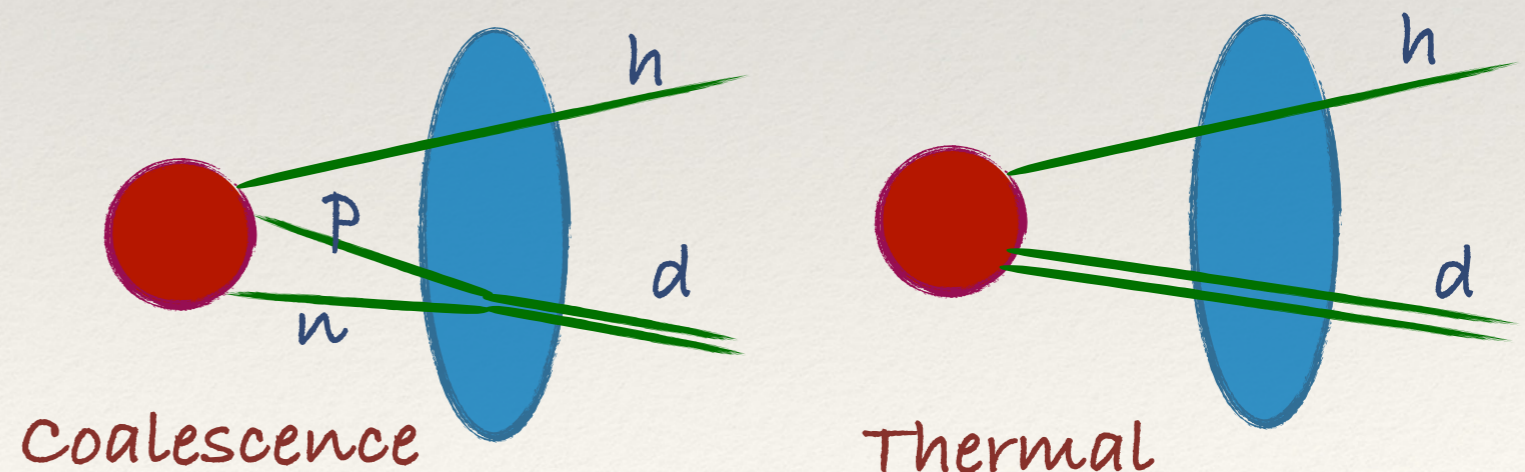
**Femtoscopic correlations provide the access to these studies**

*S. Mrówczyński, S. Bazak: Eur. Phys. J. A 56, 193 (2020)*



p-3He with  ${}^4\text{Li}$  resonance + Coulomb

Possible validation of the production mechanism



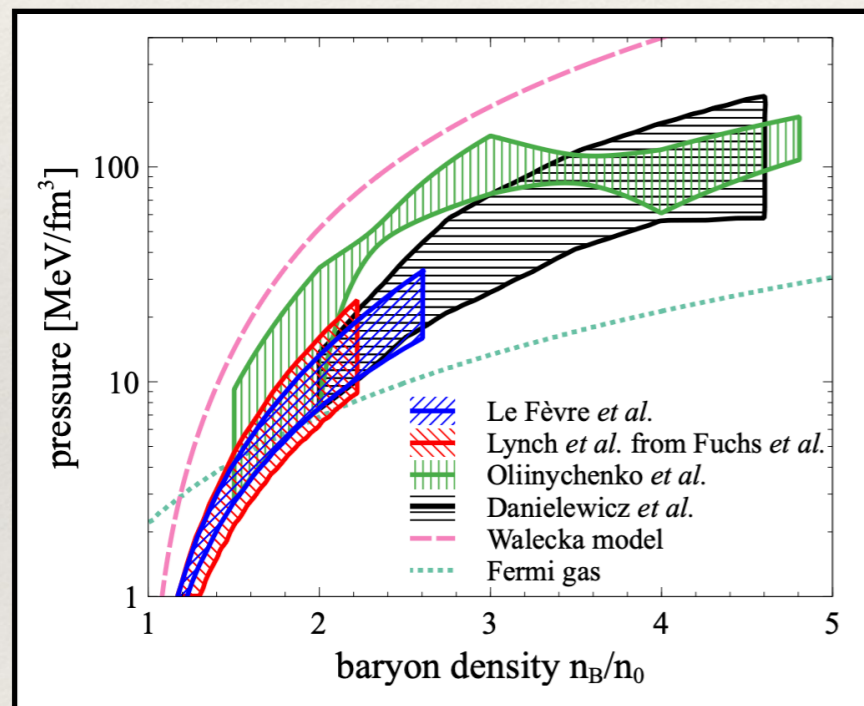


# Motivation

## 2. Sensitivity to EoS

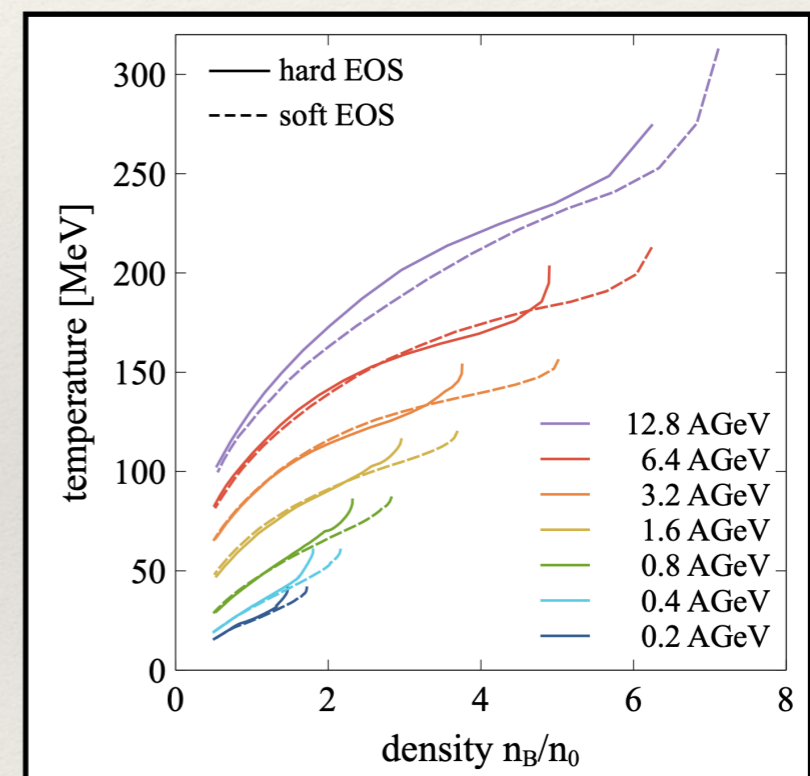
A. Sorensen, M. Stefaniak, et al: White Paper "Dense Nuclear Matter Equation of State from Heavy-Ion Collisions" arXiv:2301.13253

### Experimental constraints on the EoS searches



Selected constraints on the symmetric EOS obtained from comparisons of experimental data to hadronic transport simulations

### How to access different system's temperatures and densities



Prepared with UrQMD Skyrme potential, Temperature in the center of mass frame

Low baryon densities well explored, while in higher ones still huge uncertainty.

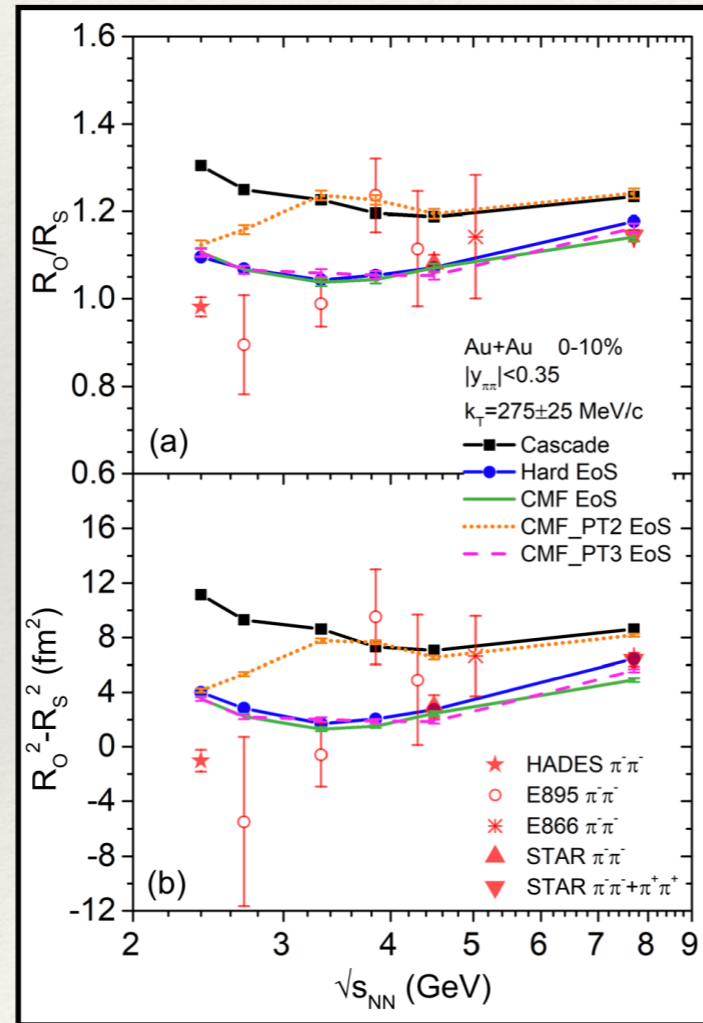
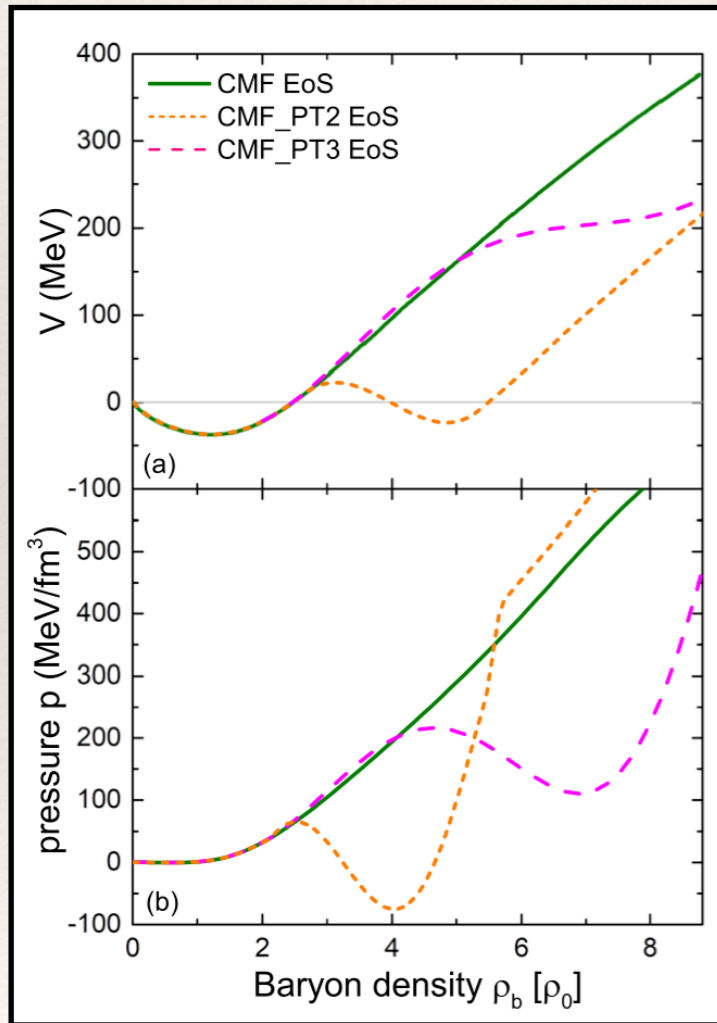


# Motivation

## 2. Sensitivity to EoS

*P. Li, J. Steinheimer, et al: Sci. China-Phys. Mech. Astron. 66, 232011 (2023)*

*S.Pratt: Phys. Rev. D33:1314,1986*



**Pion femtoscopy  
with UrQMD**

EoS sensitivity by pion  
femtoscopia decreases for lower  
net baryon densities

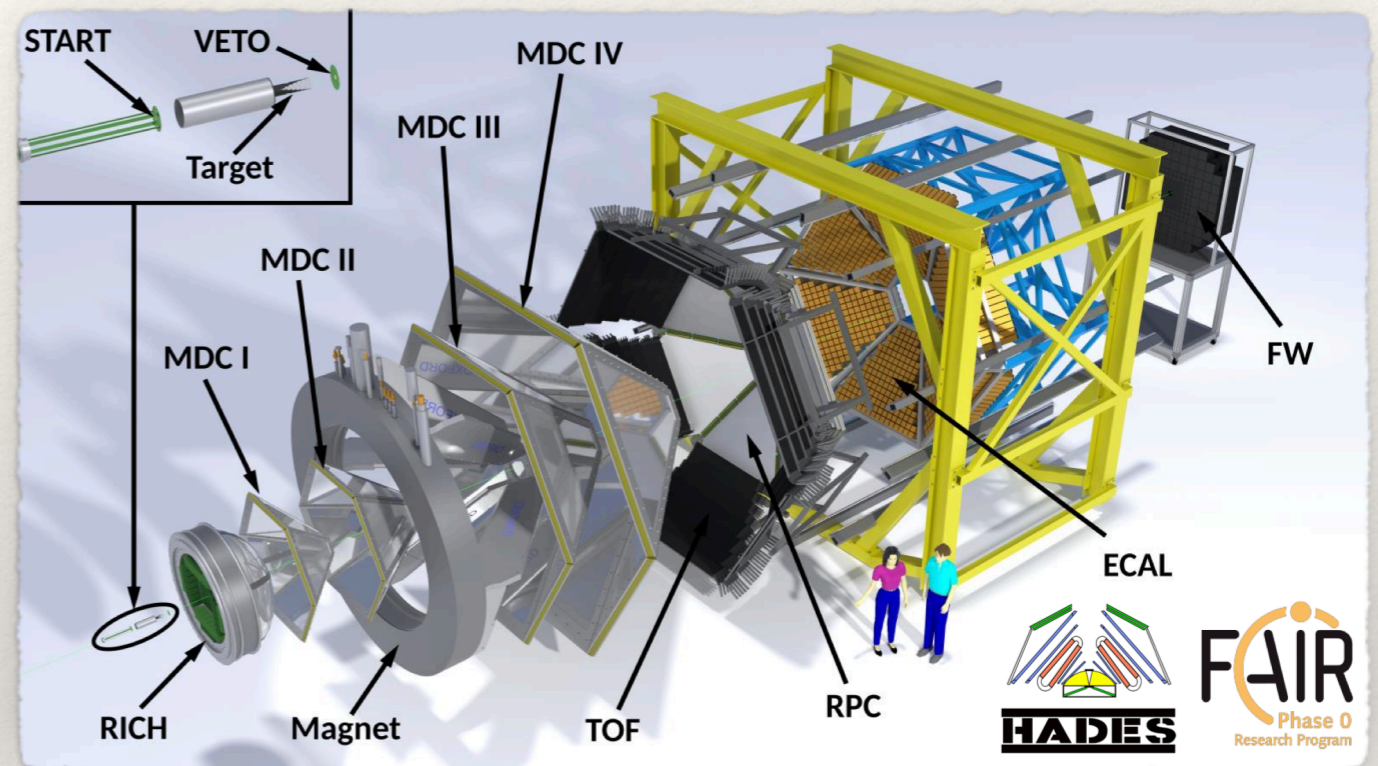
CMF PT2 EoS: phase transition at low baryon densities  
CMF PT3 EoS: phase transition at higher baryon densities



# HADES Experiment

## High Acceptance Di-Electron Spectrometer

- Fixed target experiment at SIS18 (GSI, Germany)
- Low mass Mini-Drift-Chambers used for tracking
- Time of flight walls RPC and TOF
- Almost full azimuthal angle and polar angles between  $18^\circ$  and  $85^\circ$  covered

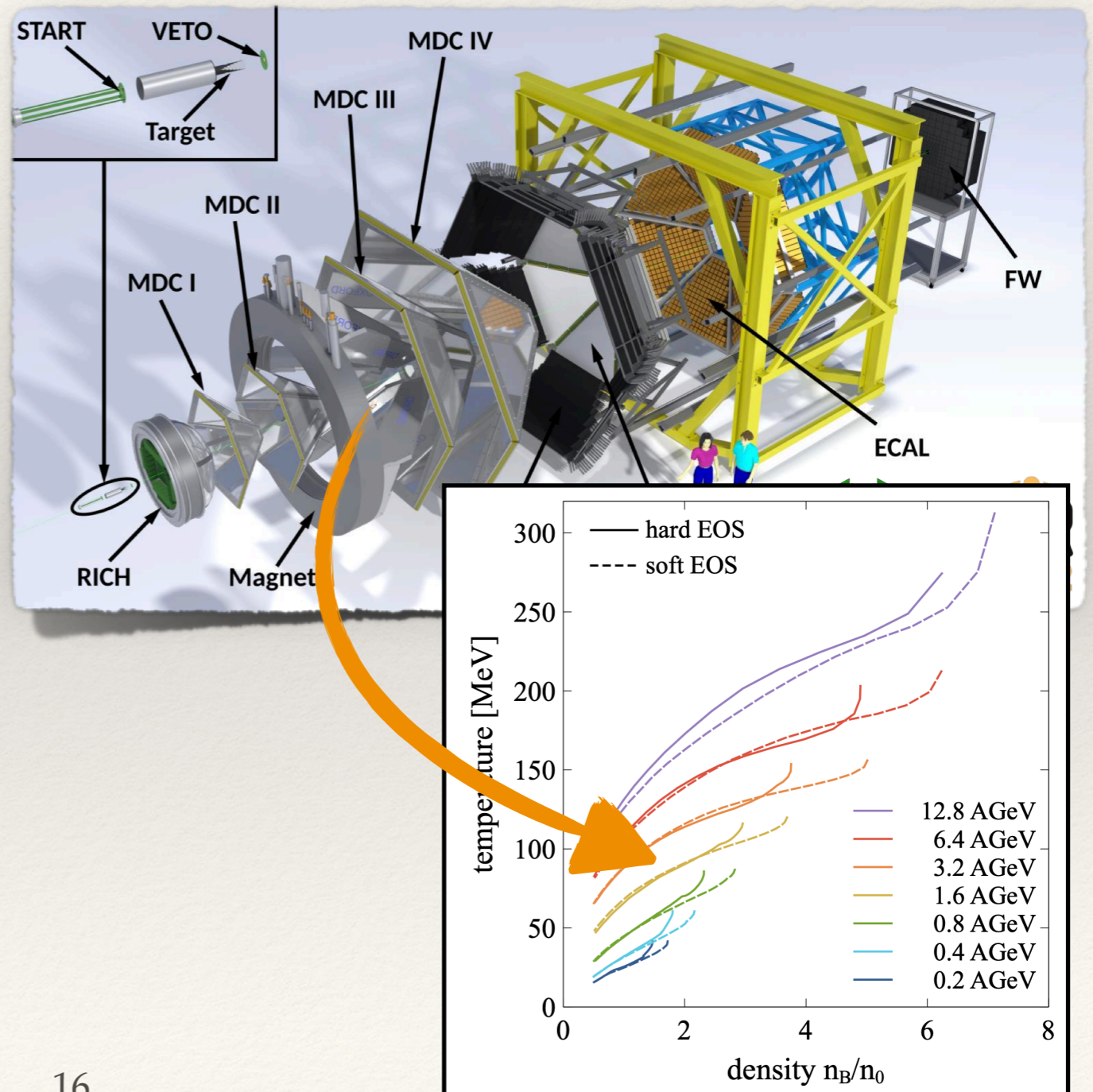




# HADES Experiment

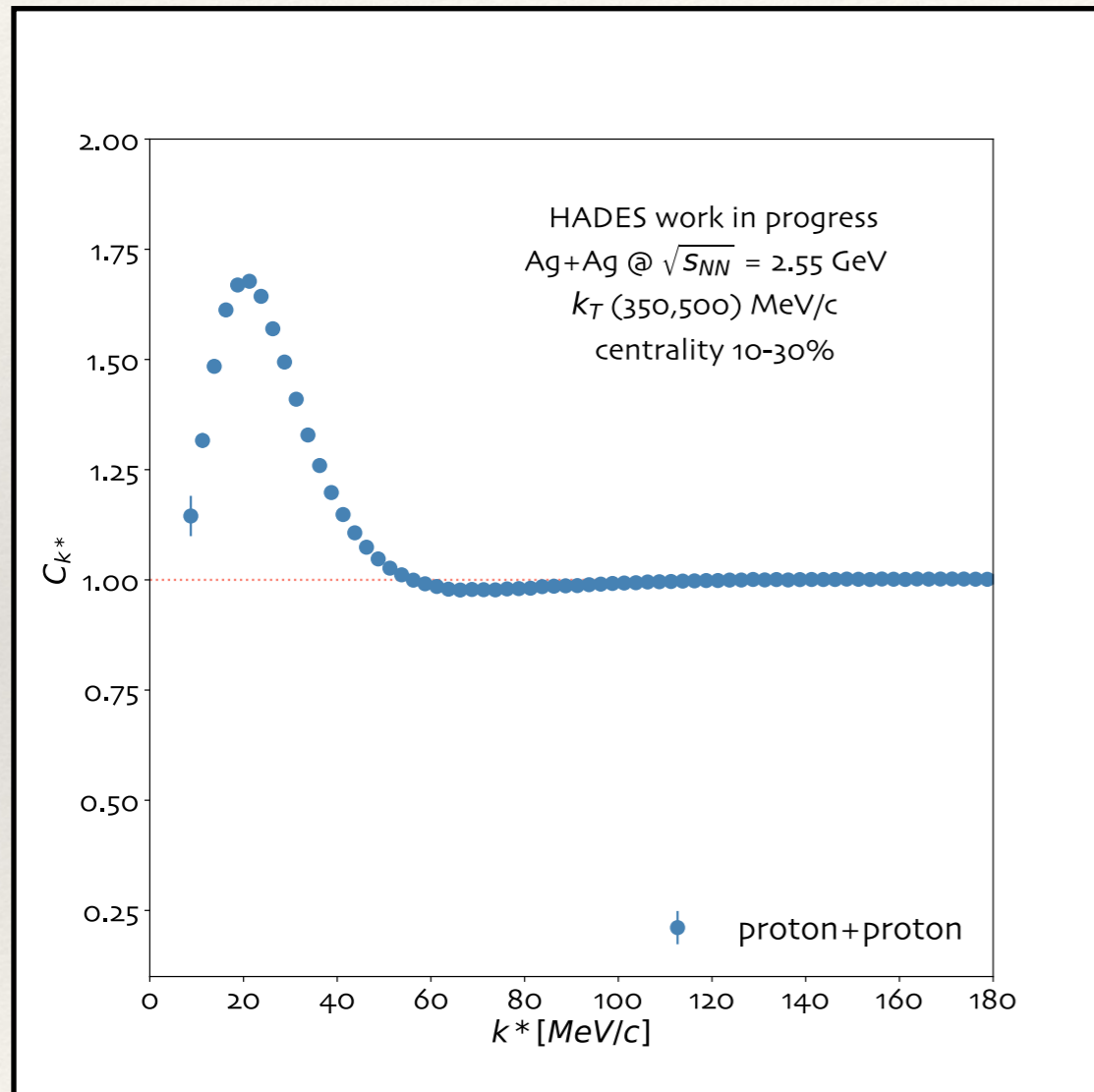
## High Acceptance Di-Electron Spectrometer

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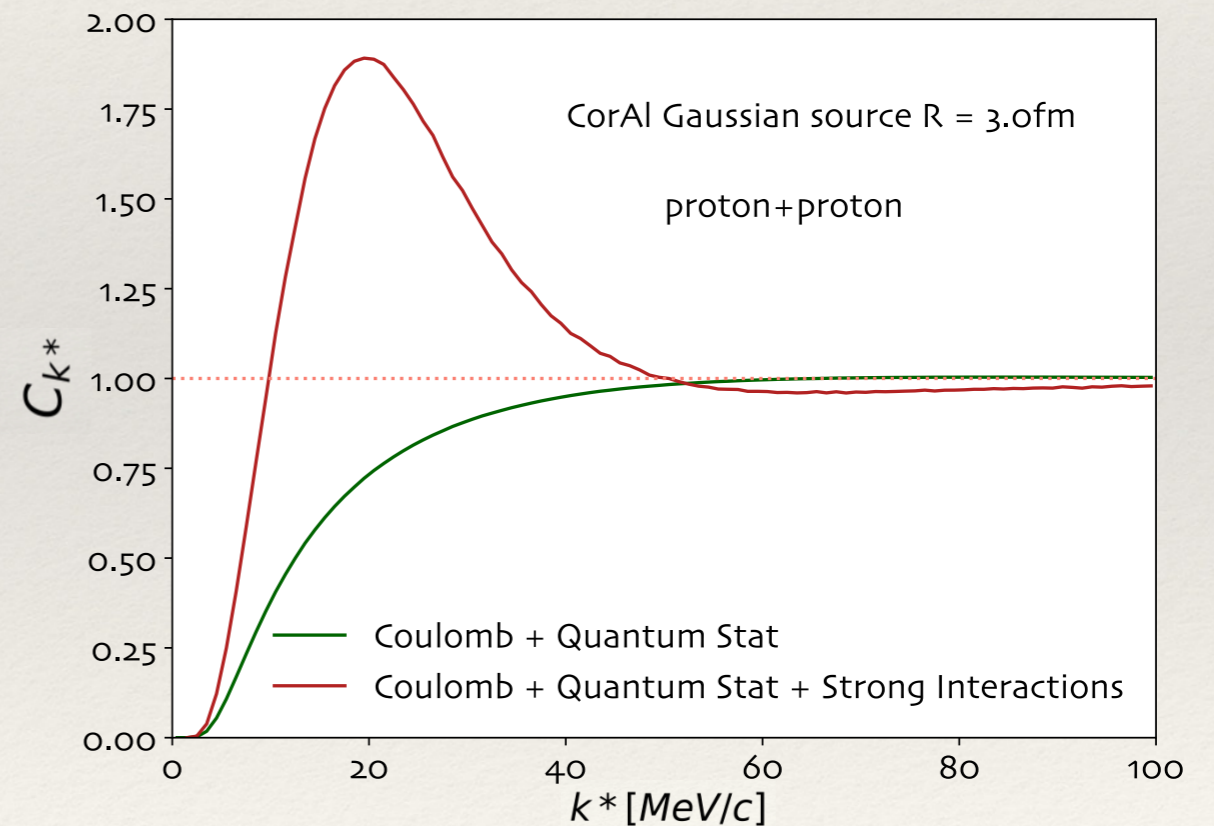




# Proton - cluster

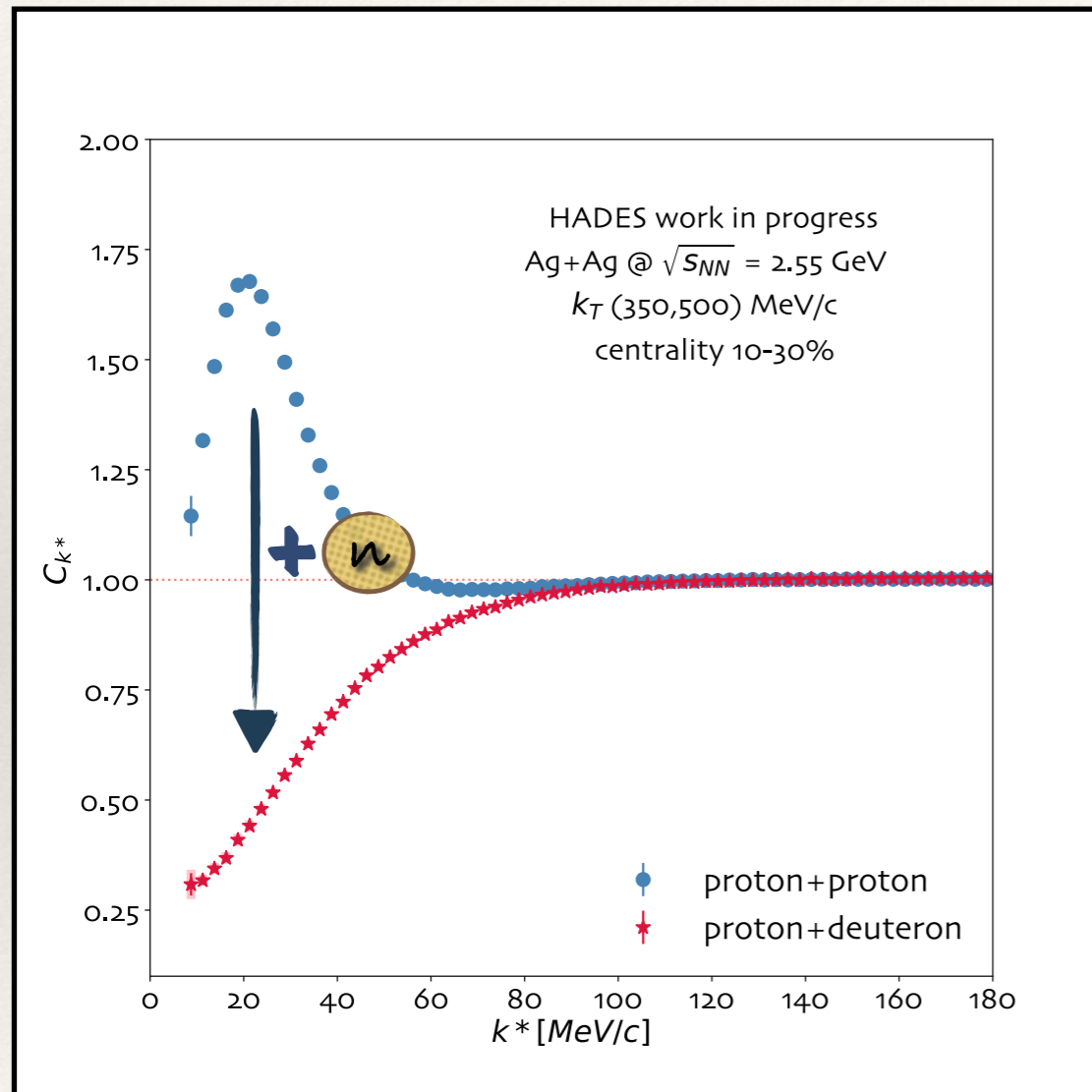


- Positive correlation originating from Strong Interactions
- Negative caused by Coulomb and Quantum Statistics



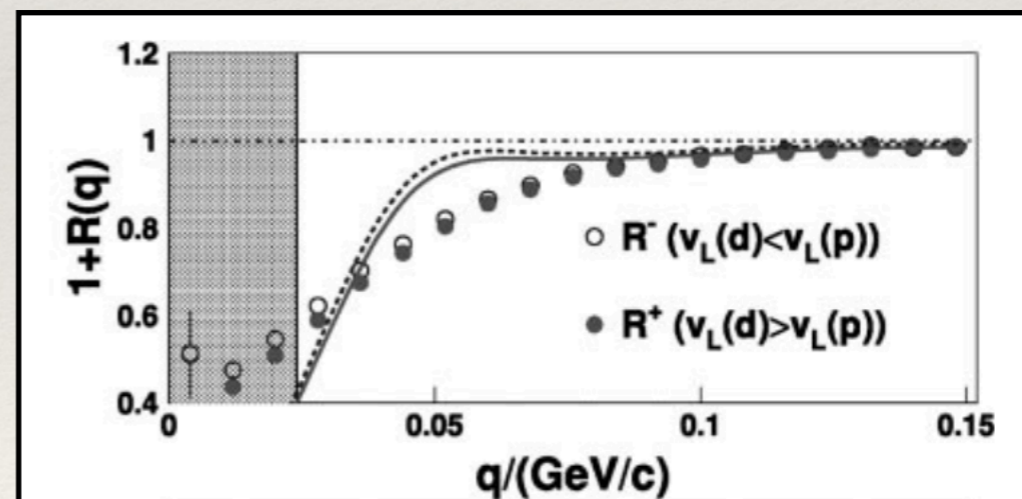


# Proton - cluster



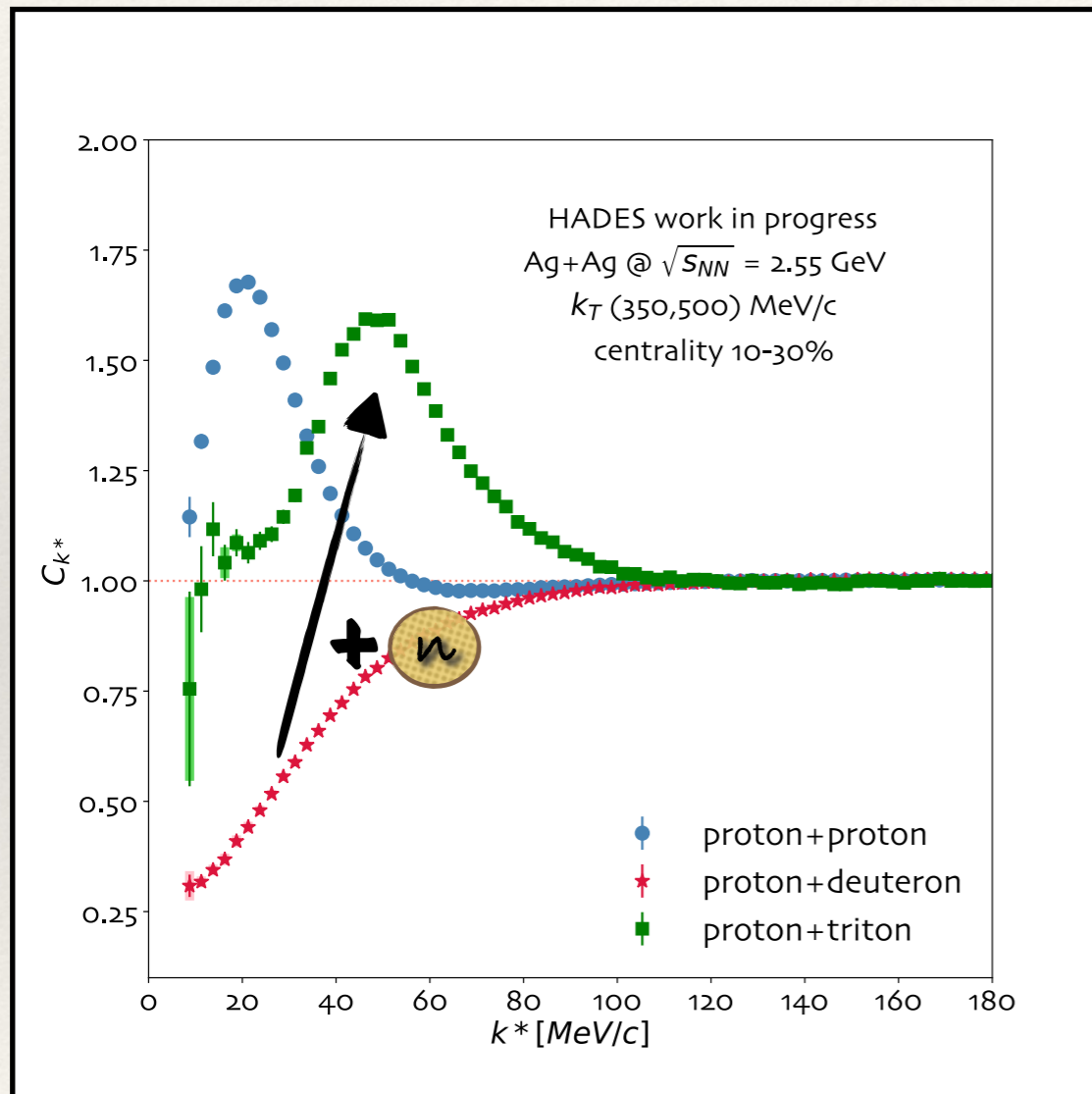
- After “adding” neutron to correlated system: repulsive interactions between p-d
- Better measurement precision than other published results

*FOPi Collaboration: Eur. Phys. J. A 6, 185–195 (1999)*



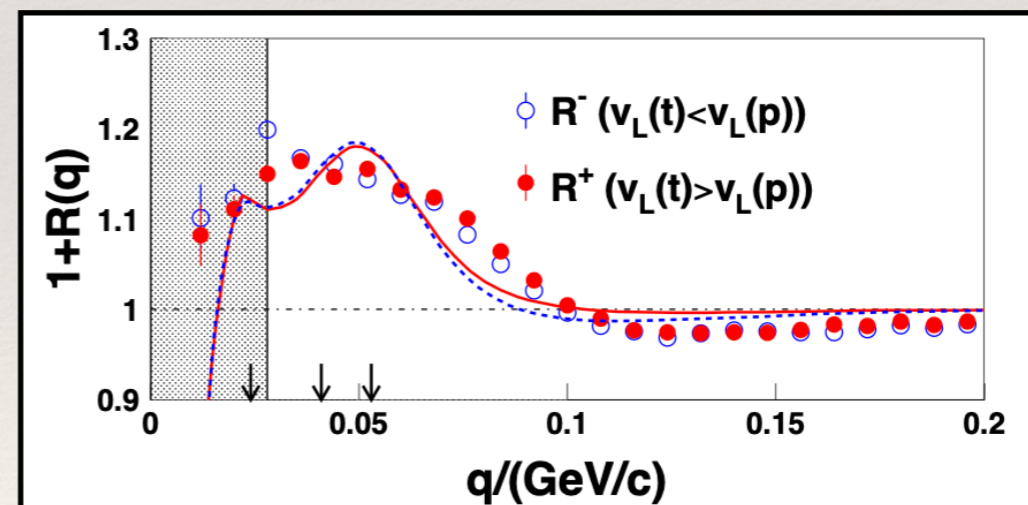


# Proton - cluster



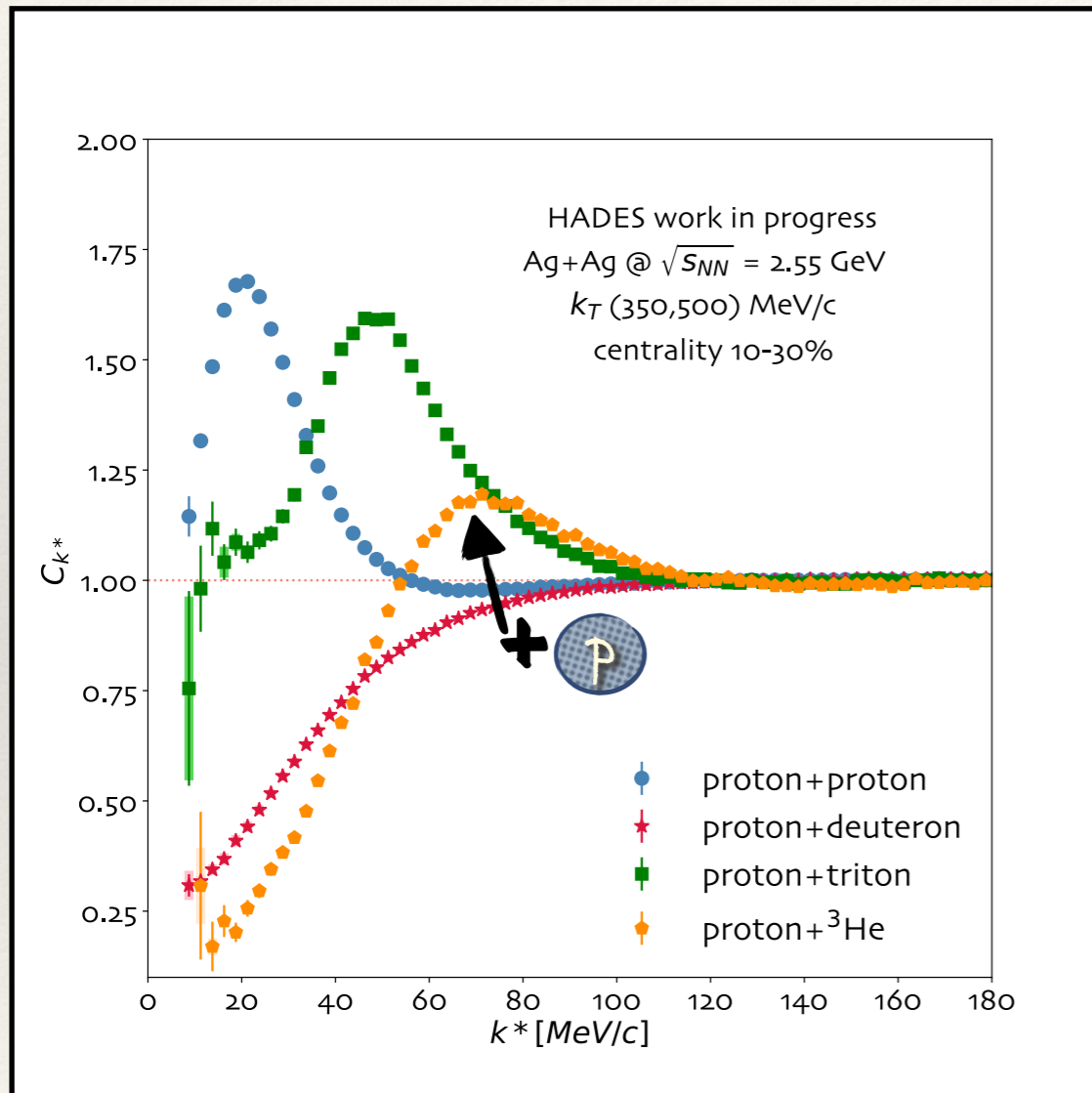
- After “adding” neutron to correlated system:  
Strong positive correlation
- Visible sharp peak caused by the possible  
light nuclei decay

*FOPI Collaboration: Eur. Phys. J. A 6, 185–195 (1999)*



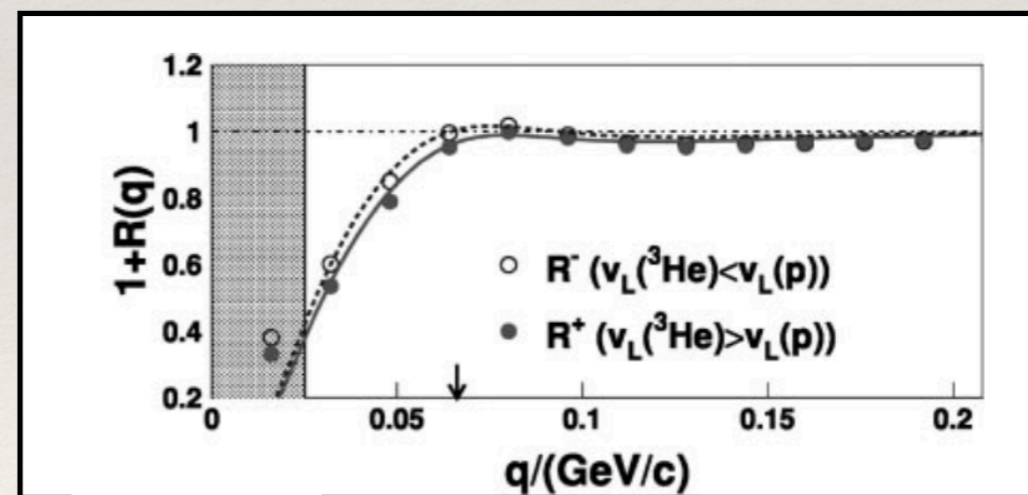


# Proton - cluster



- After “adding” proton to correlated system:  
Strong positive correlation
- The positive enhancement barely visible in  
FOPI’s data

*FOPI Collaboration: Eur. Phys. J. A 6, 185–195 (1999)*

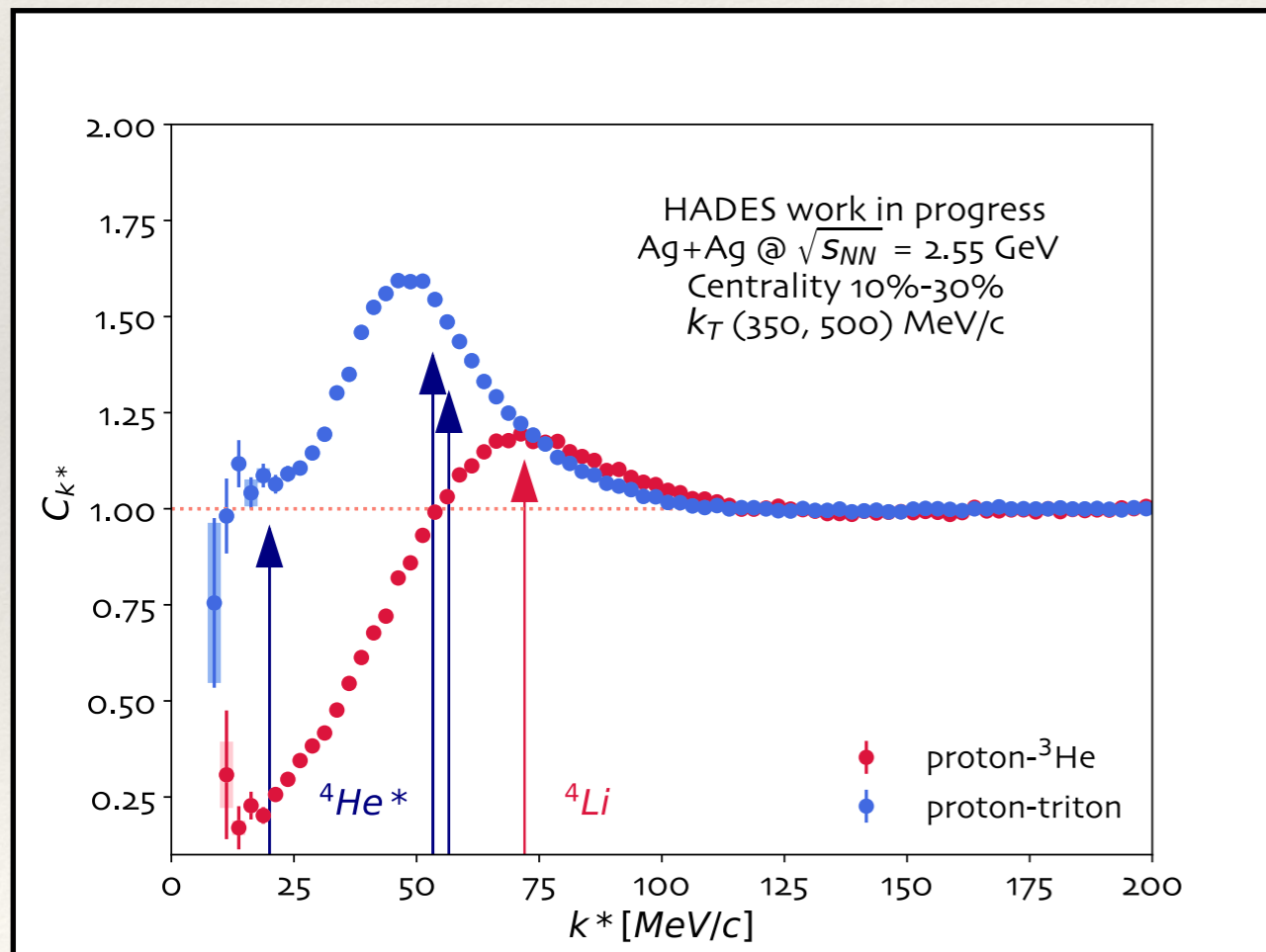




# Proton - cluster

## Proton-Triton vs Proton-<sup>3</sup>He

- Similar masses
- Same baryon number
- Different electric charges!

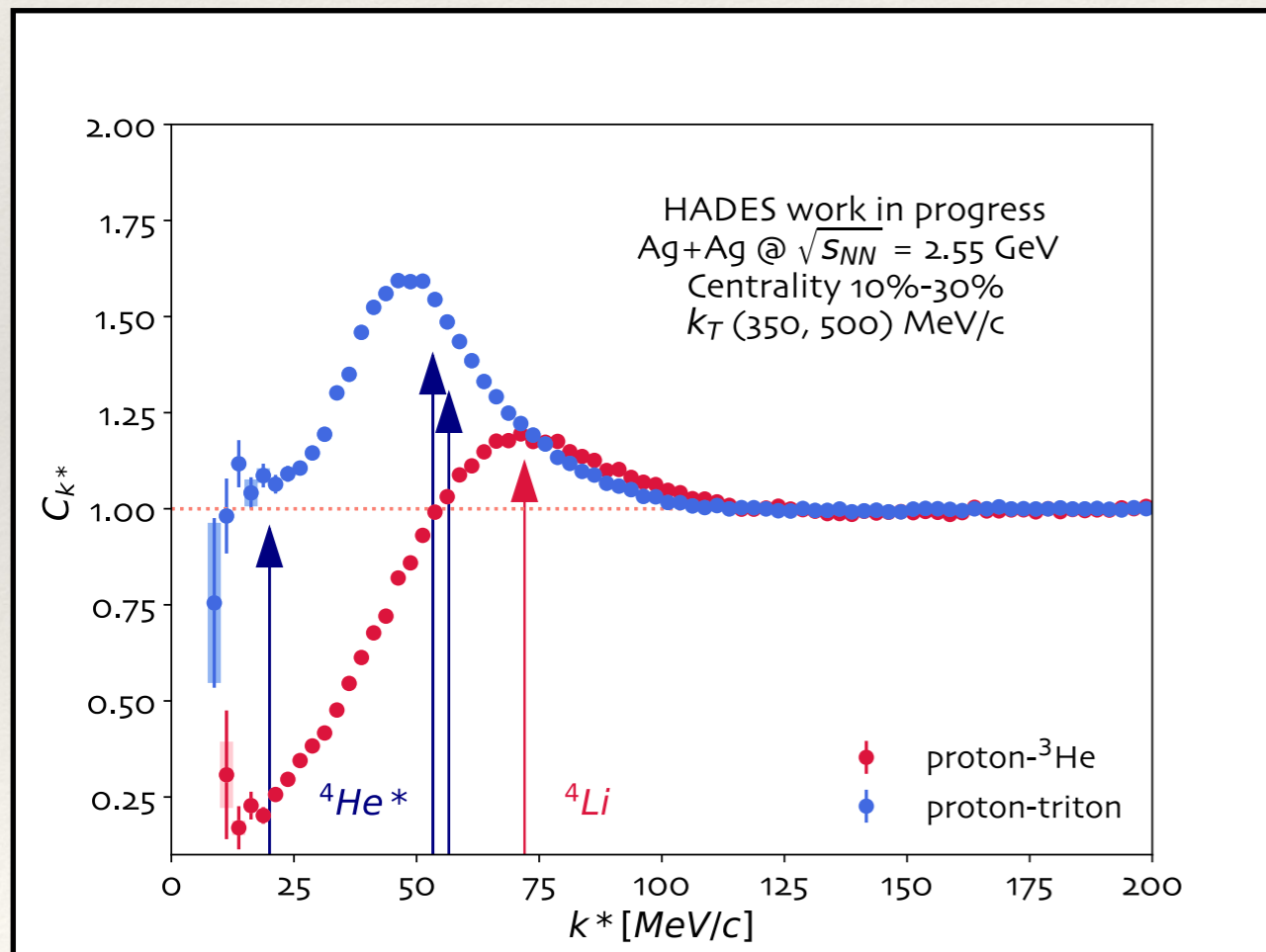




# Proton - cluster

## Proton-Triton vs Proton-<sup>3</sup>He

- Similar masses
- Same baryon number
- Different electric charges!



## Positive correlations caused by decays of unstable light nuclei



- ( $J^\pi = 2^-, \Gamma = 6.0 \text{ MeV}, \Gamma_p/\Gamma = 1, k_1^* \approx 72 \text{ MeV}/c$ )

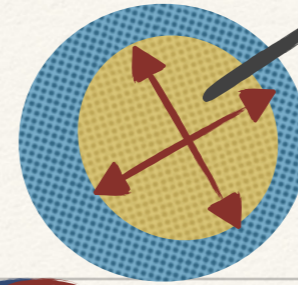


- ( $E = 20.21 \text{ MeV}, J^\pi = 0^+, \Gamma = 0.5 \text{ MeV}, \Gamma_p/\Gamma = 1, k_1^* = 20 \text{ MeV}/c$ )
- ( $E = 21.01 \text{ MeV}, J^\pi = 0^+, \Gamma = 0.84 \text{ MeV}, \Gamma_p/\Gamma = 0.76, k_2^* = 53.3 \text{ MeV}/c$ )
- ( $E = 21.84 \text{ MeV}, J^\pi = 2, \Gamma = 2.01 \text{ MeV}, \Gamma_p/\Gamma = 0.63, k_3^* = 56.6 \text{ MeV}/c$ )



# Proton - Proton

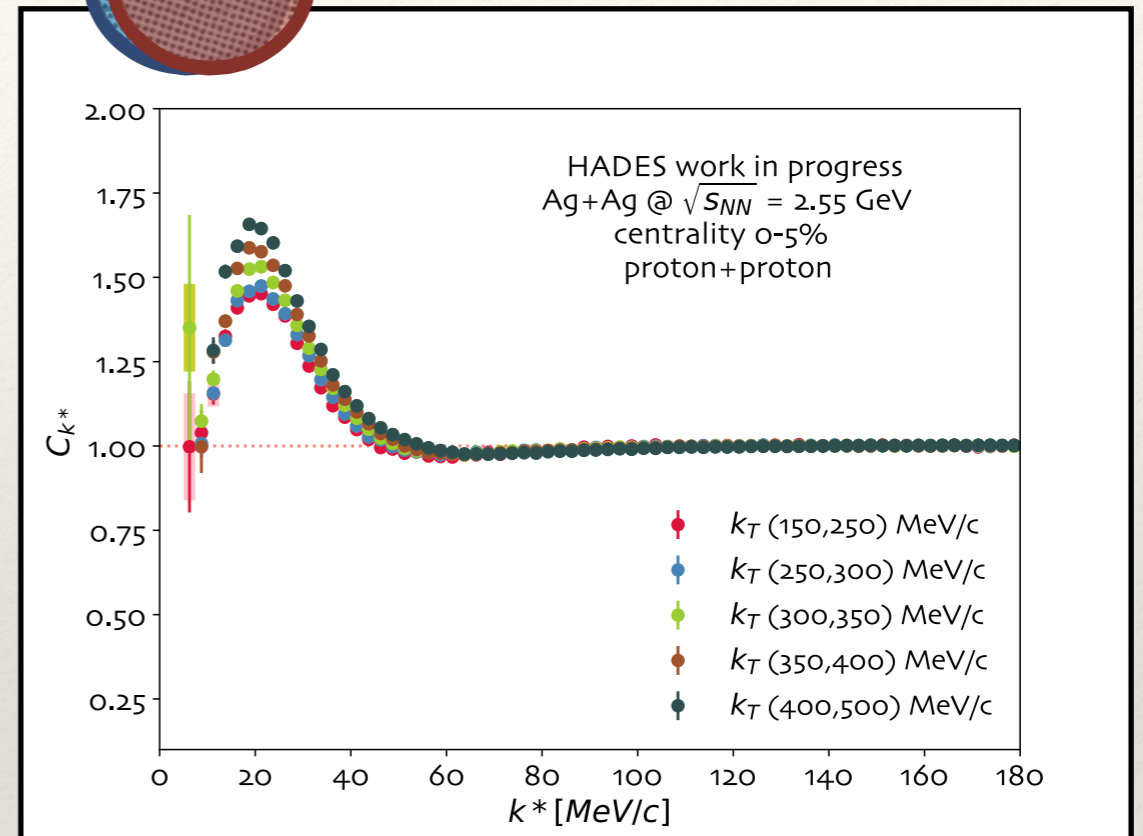
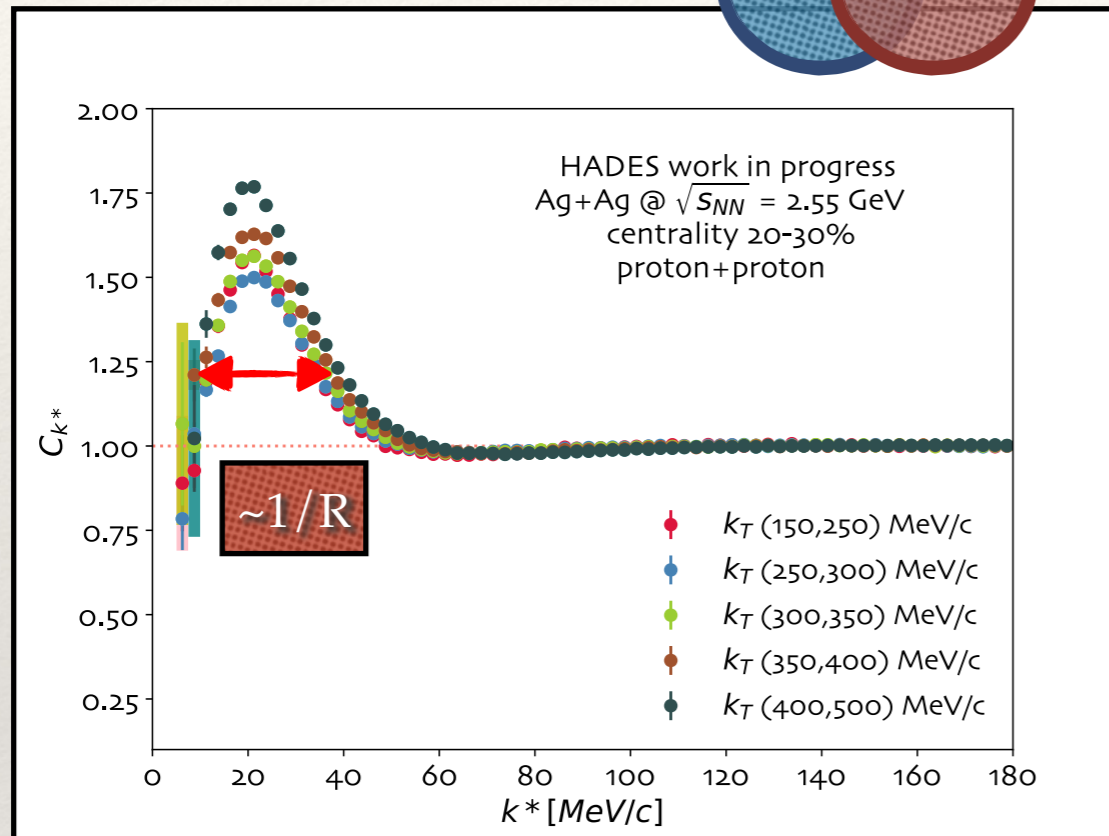
Lower  $k_T$



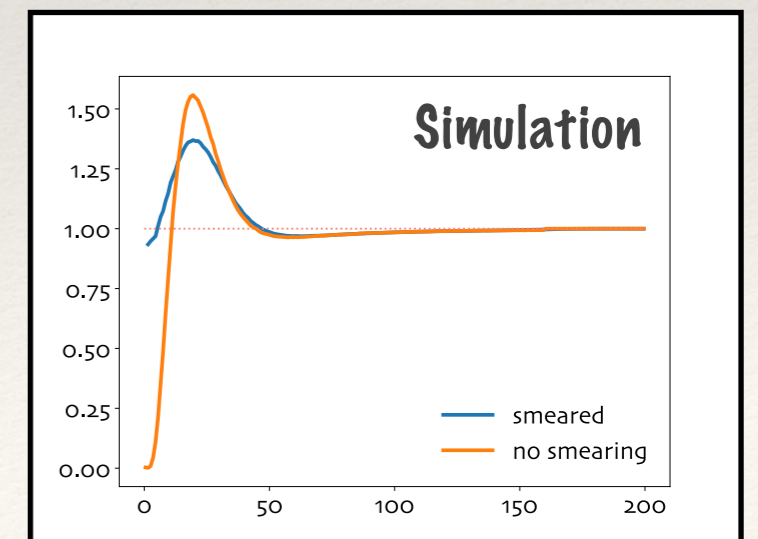
High  $k_T$



$k_T$  - average transverse momentum of pair



- High statistics allows the extended  $k_T$  dependence studies
- Strength of correlations increasing with  $k_T$  - smaller R of source
- Low  $k^*$  strongly affected by the momentum resolution and track merging suppression



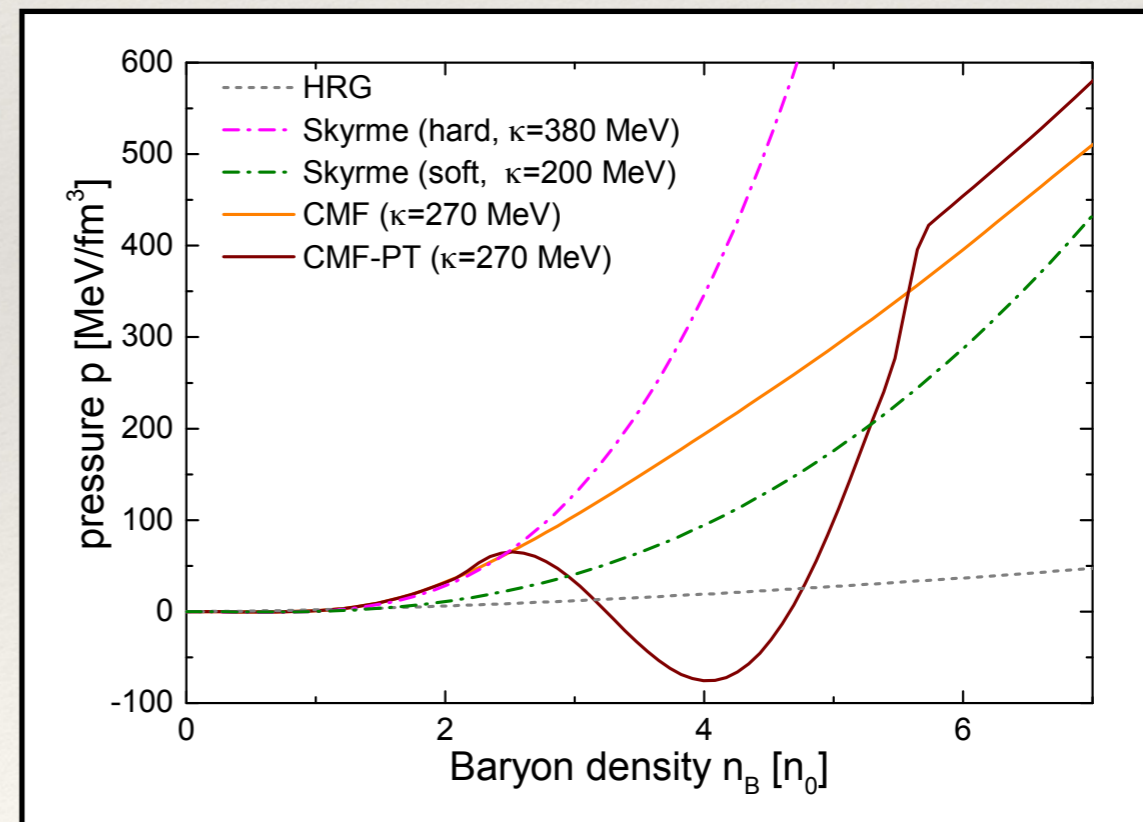


# Proton - Proton vs EoS

UrQMD

- Soft (Skyrme)
  - Hard (Skyrme)
  - Chiral Mean Field
  - Chiral Mean Field + Phase Transition
- 
- Cascade mode (HRG)

*J. Steinheimer, et al: Eur.Phys.J.C 82 (2022) 911*  
*S.A. Bass, et al: Prog. Part. Nucl. Phys. 41 (1998) 225-370*  
*M. Bleicher J. Phys. G: Nucl. Part. Phys. 25 (1999) 1859-1896*





# Proton - Proton vs EoS

UrQMD

- Soft (Skyrme)
  - Hard (Skyrme)
  - Chiral Mean Field
  - Chiral Mean Field + Phase Transition
- 
- Cascade mode (HRG)



CorA1

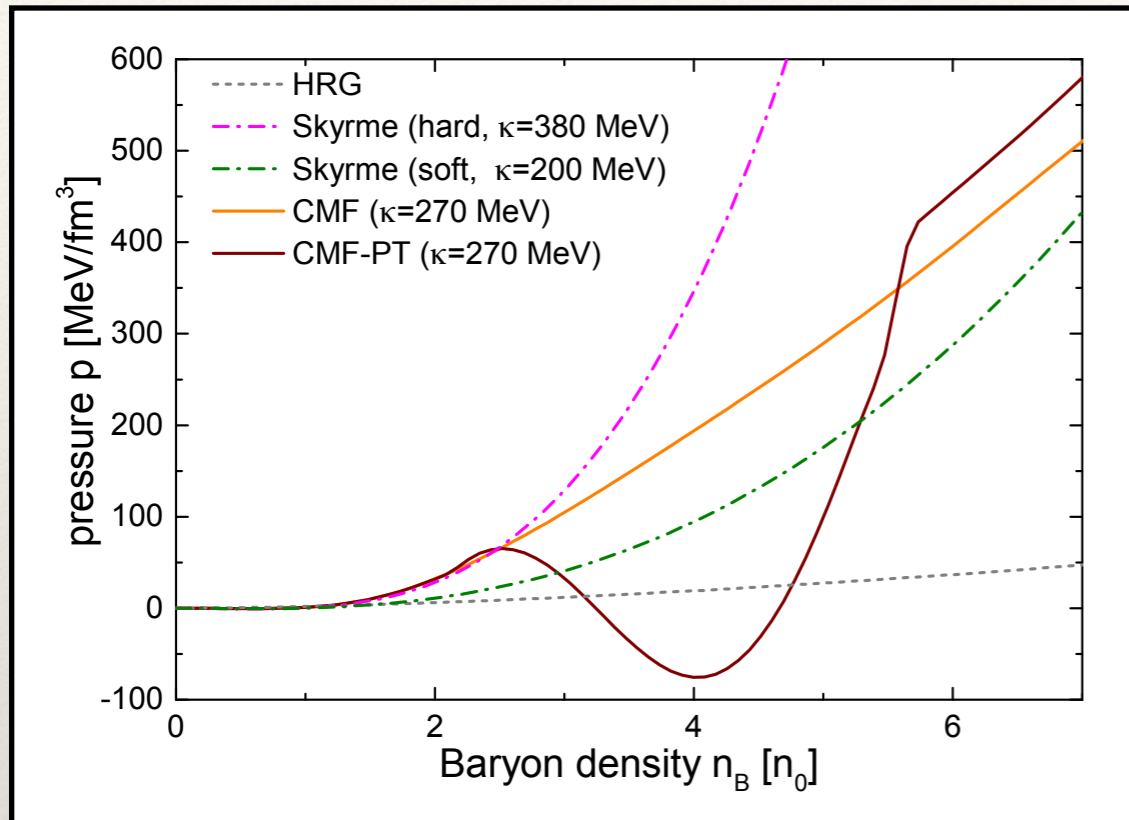
<https://github.com/scottedwardpratt/coral/>

$$C(k^{\star}) = \int S(r^{\star}) |\Psi(k^{\star}, r^{\star})|^2 d^3 r^{\star}$$

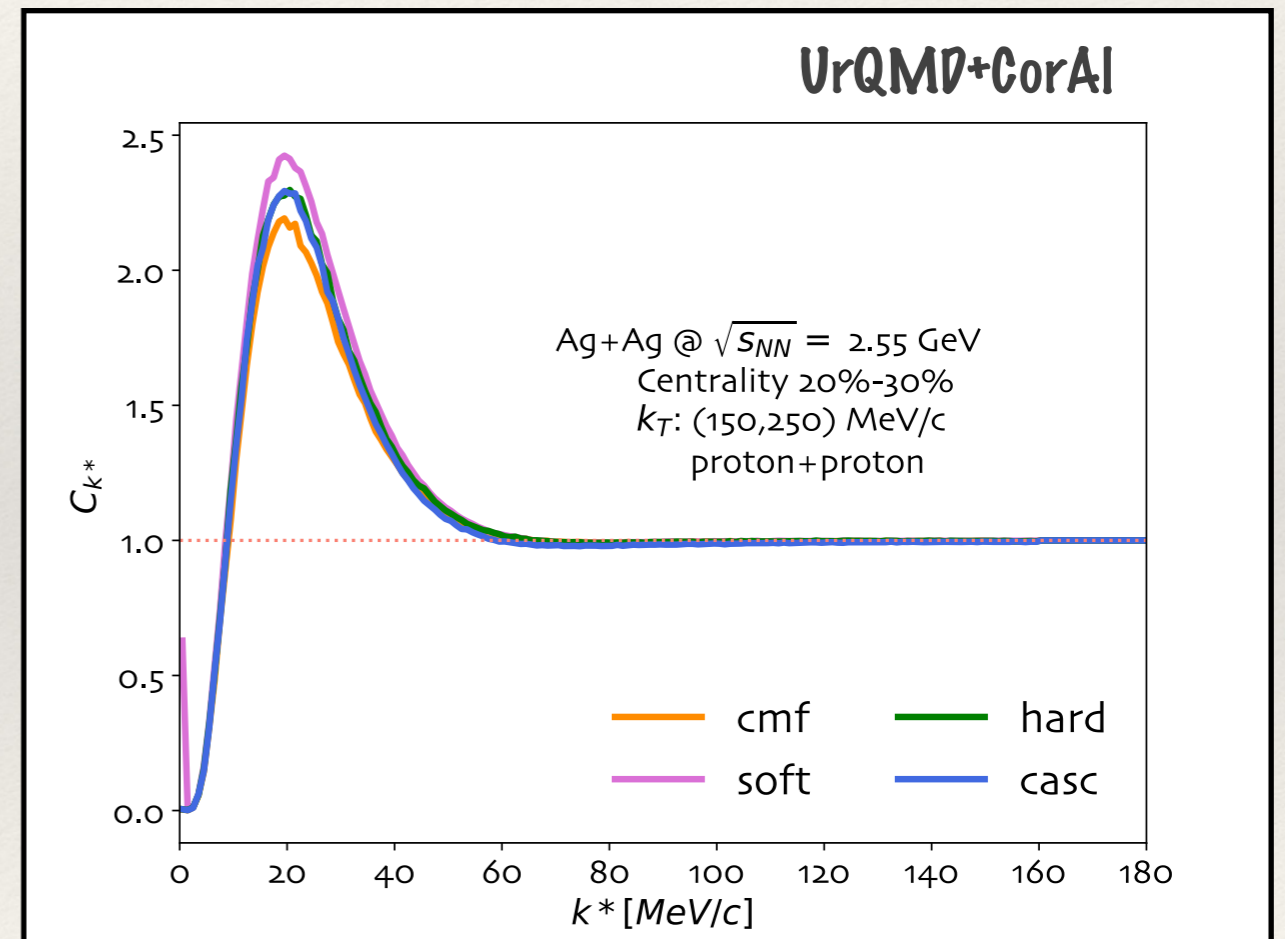
Reid potential for p+p from:  
V.G.J. Stoks et al., Phys. Rev. C 49, 2950 (1994)



# Proton - Proton vs EoS



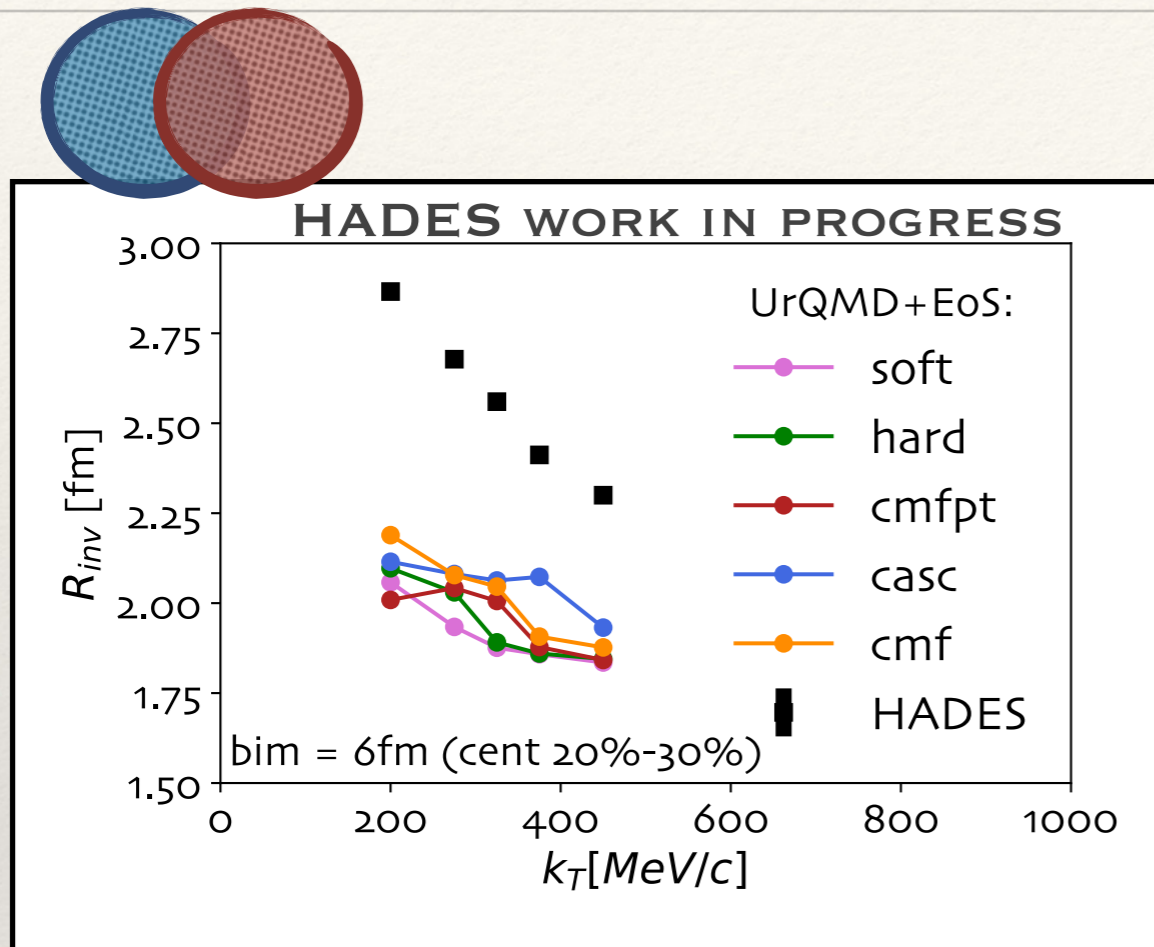
HRG = cascade



- Smallest source - Soft EoS
- Biggest one - Chiral mean field
- No difference between hard Skyrme and cascade mode (HRG)



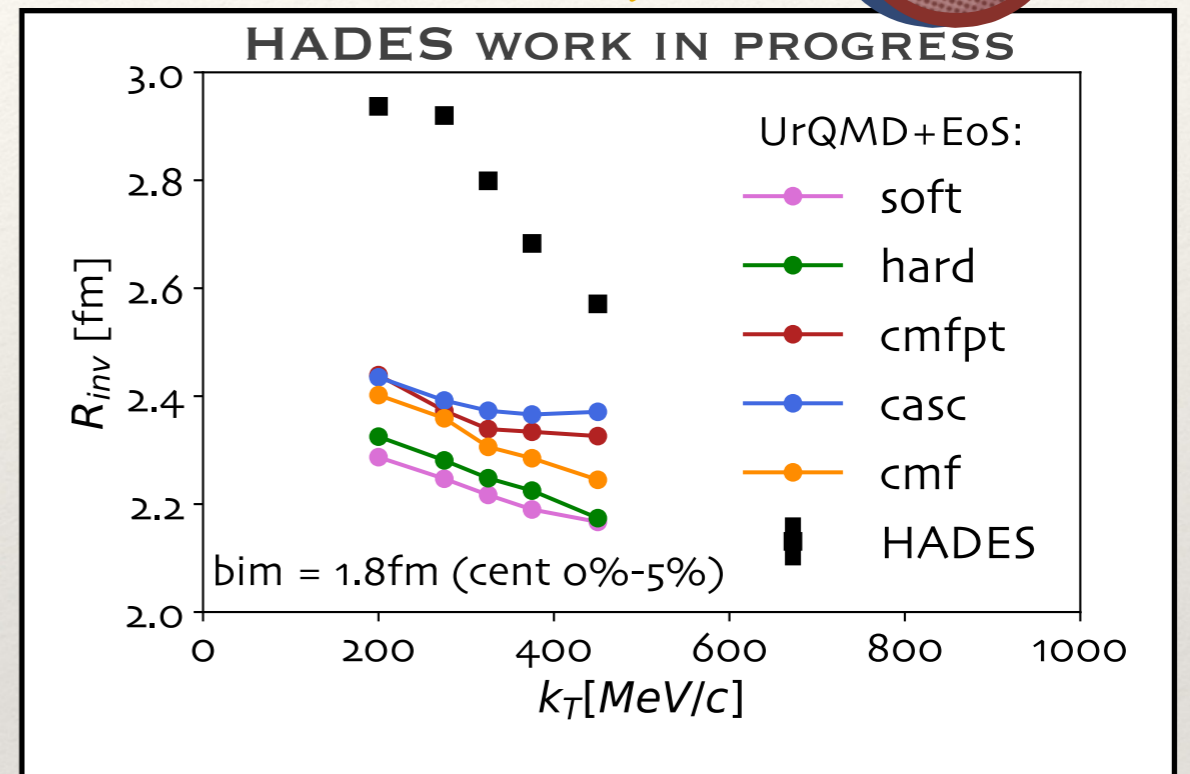
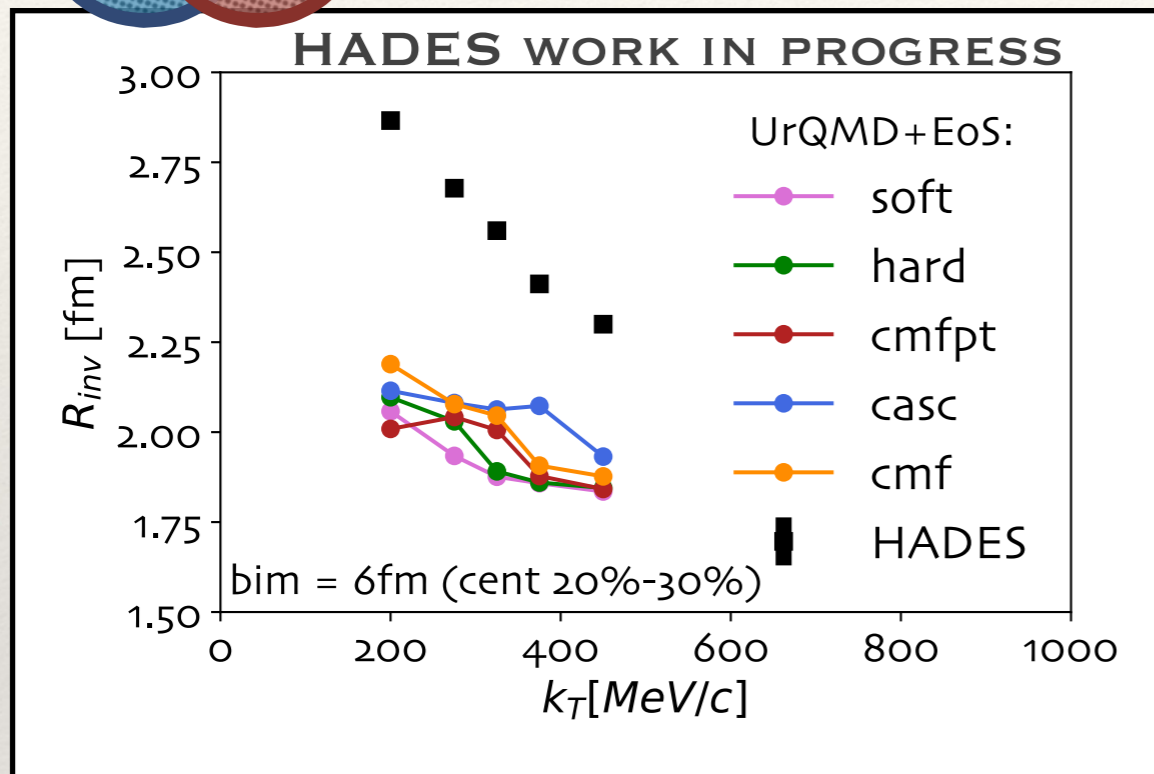
# Proton - Proton vs EoS





# Proton - Proton vs EoS

Increase of net baryon density

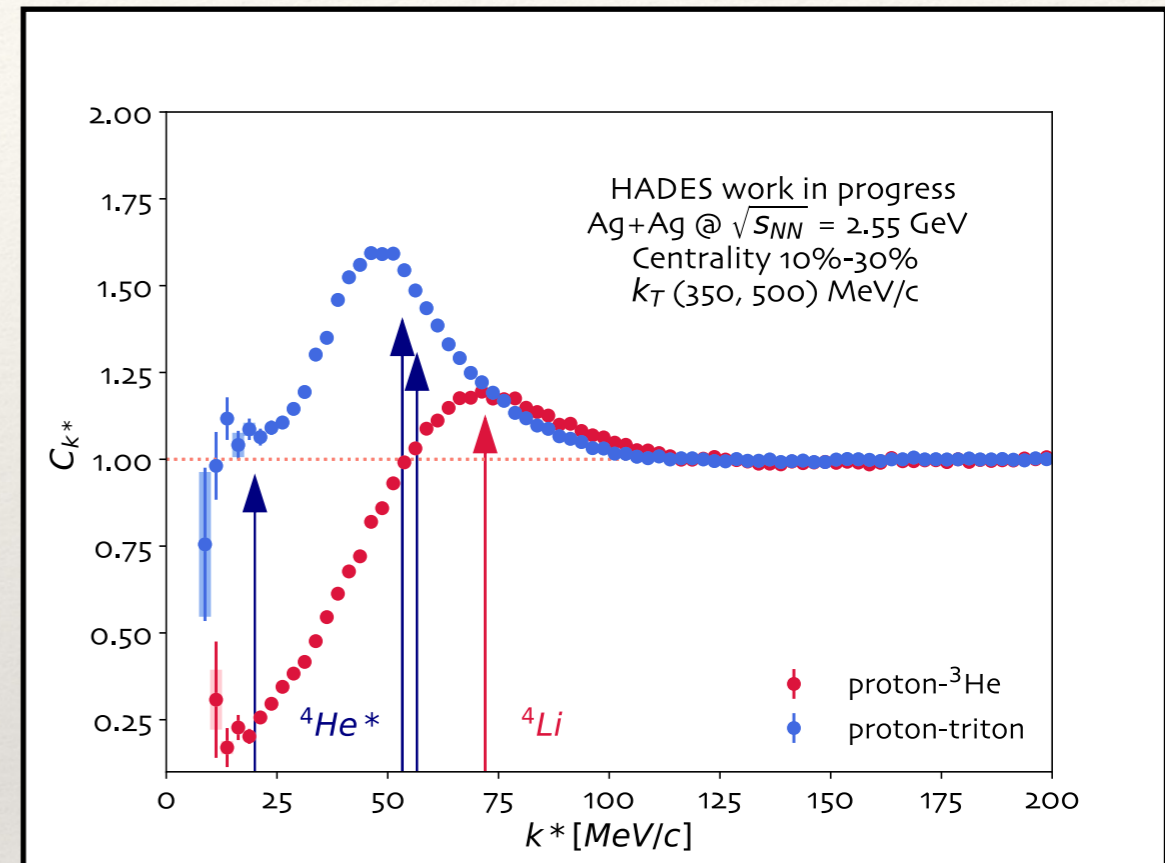


- UrQMD does not reproduce the HADES data. Possible reasons:
  - Simulations do not include productions of d, t, He-3...
  - Difficult to estimate the contribution of protons “feed-down” (e.g.  $^5\text{Li}$ )
  - Assumption of gaussian source in fitting procedure
- For central collisions (higher  $n_b$ ) differences between EoS increasing
- Skyrme EoS the furthest from experimental data



# Summary and outlook

- High precision measurements of proton - proton and proton - cluster correlation functions
- Identified presence and decays of exotic states of  ${}^4\text{He}^*$  and  ${}^4\text{Li}$
- Extended studies of  $k_T$  dependance of proton-proton correlations
- EoS sensitive to proton femtoscopy



Finalizing of:

- Studies of SI in proton - cluster interactions
- Systematic uncertainty analysis

THANK YOU  
for your attention!