

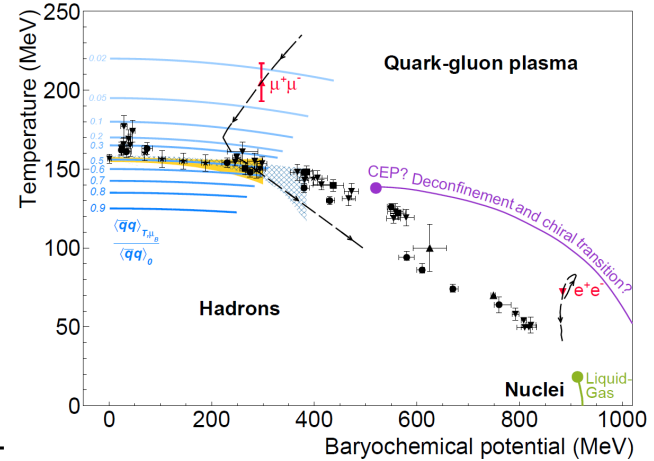
Coulomb effects on pion spectra and HBT correlations at few GeV/A beam energies

Malgorzata Gumberidze for the HADES Collaboration

Nuclear collisions at SIS18/HADES energies

HADES program:

- EOS of hot and dense matter
- Medium modifications of hadrons
- Various aspects of baryon-resonance physics in cold matter and vacuum



Nature Phys. **15** (2019) 10, 1040-1045 (update 2023 T. Galatyuk)

Measurements at SIS18 : Fixed target experiment

Interaction rate capability : up to 50kHz trigger rate

Large acceptance : full azimuthal coverage, 18°-85° polar one

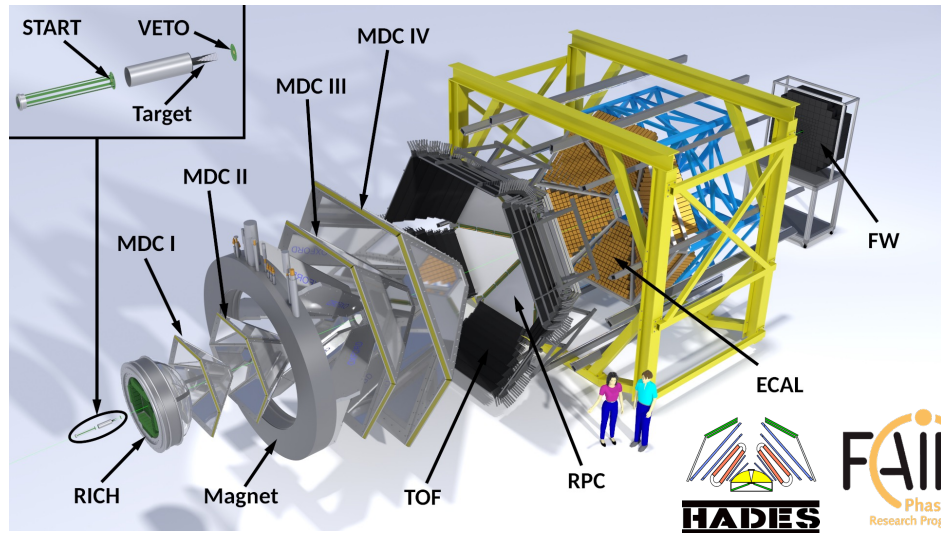
Similar conditions as expected in merging neutron stars (Nature Physics **15**, 1040-1045 (2019), J. Phys.: Conf. Ser. **878** 012031, Phys. Rev. Lett. **122**, 061101)

Tracking with low-mass Mini Drift Chambers (MDC)

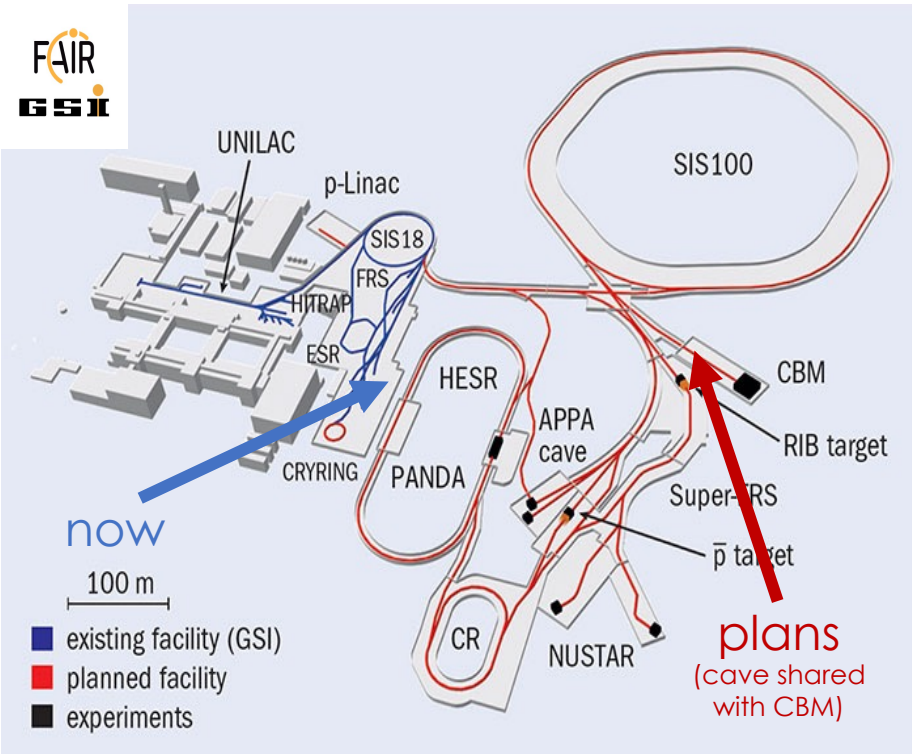
Hadron Identification

Time-of-flight (TOF, RPC) and/or dE/dx (MDC, TOF)

Centrality selection based on N_{hits} and Glauber Monte Carlo



HADES space-time coordinates



- **Nov 2002** C+C at $\sqrt{s_{NN}} = 2.7$ GeV
- **Jan 2004** p+p at $\sqrt{s} = 2.77$ GeV
- **Aug 2004** C+C at $\sqrt{s_{NN}} = 2.32$ GeV
- **Sep 2005** Ar+KCl at $\sqrt{s_{NN}} = 2.61$ GeV
- **Apr 2006** p+p at $\sqrt{s} = 2.42$ GeV
- **Apr 2007** p+p at $\sqrt{s} = 3.18$ GeV,
d+p at $\sqrt{s_{NN}} = 2.42$ GeV
- **Sep 2008** p+Nb at $\sqrt{s_{NN}} = 2.7$ GeV
- **Apr 2012** Au+Au at $\sqrt{s_{NN}} = 2.42$ GeV
- **Jul-Aug-Sep 2014** π^- + W/C/polyethylene
- **Mar 2019** Ag+Ag at $\sqrt{s_{NN}} = 2.55$ and 2.42 GeV
- **Feb 2022** p+p at $\sqrt{s} = 3.46$ GeV

Presentation based on pion production from AuAu@1.23AGeV collisions

Eur.Phys.J.A 56 (2020) 259

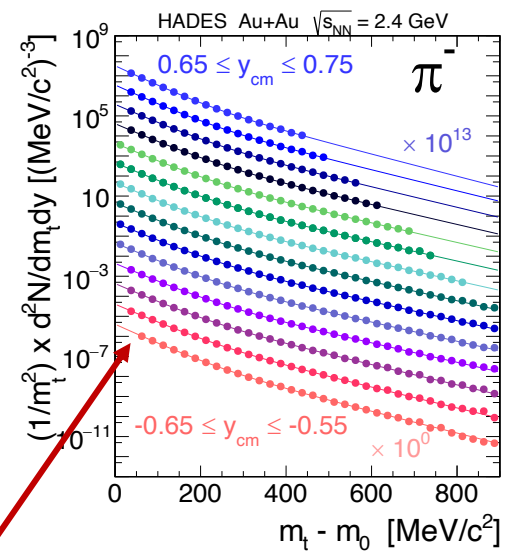
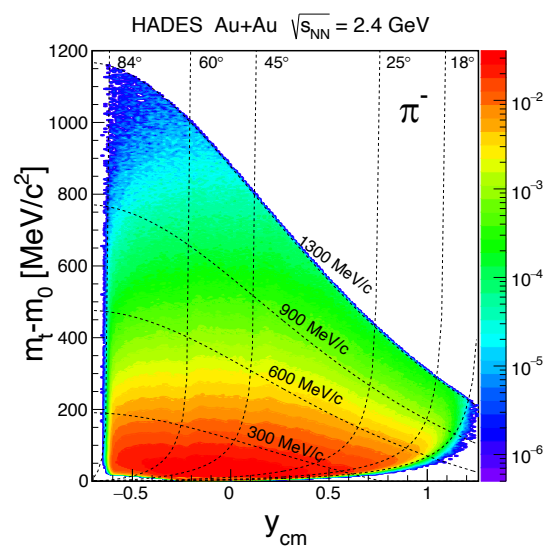
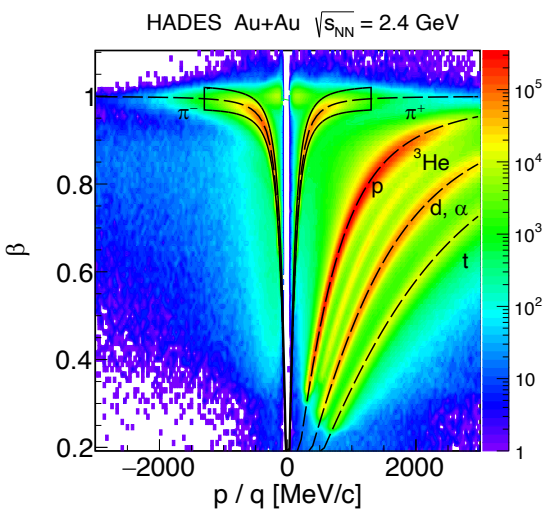
Eur.Phys.J.A 58 (2022) 166

Charged pion production in Au+Au collisions at 1.23A GeV

- Pions are most abundantly produced particles
- Sensitive to bulk properties of hot and dense matter
- Huge data sample → detailed multi-differential analysis possible
- Particle ID based on velocity vs. momentum

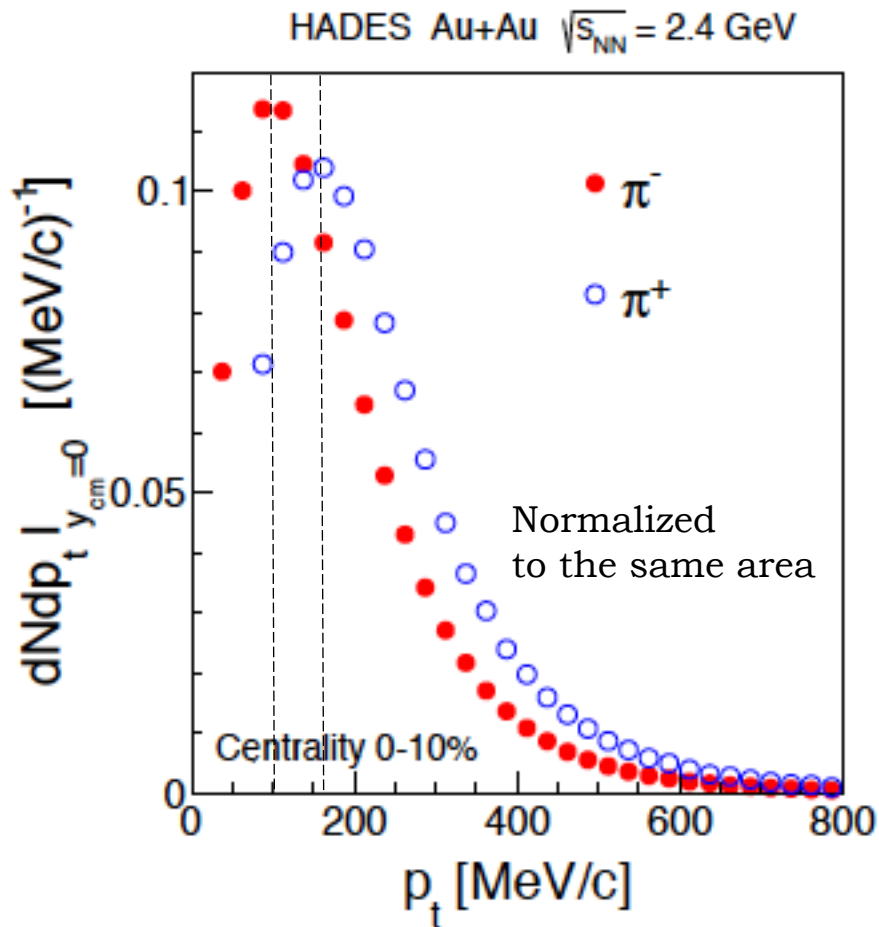
Particle identification

Phase-space



Curves corresponds to two-slope Boltzmann fits commonly used for extrapolation outside of the detector acceptance at low and high transverse mass

Coulomb effects on the pion spectra



→ Split between peak positions:
100 MeV/c for π^- vs. 160 MeV/c for π^+

→ Can be attributed to the Coulomb interaction of the pions with the positive charge of the fireball.

- π^- are decelerated
- π^+ are accelerated

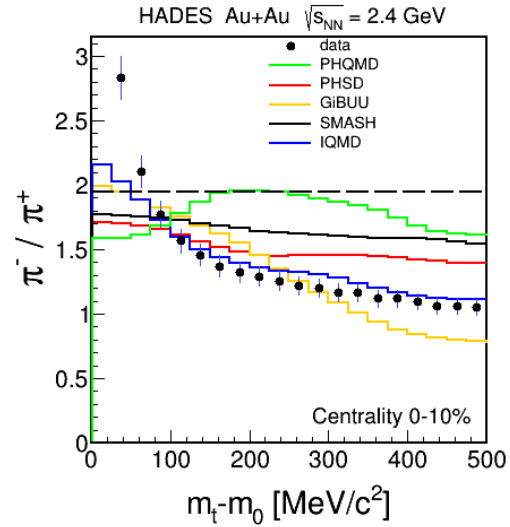
$$E_f(p_f) = E_i(p_i) \pm V_C$$

How to account for the Coulomb effect ?

Full dynamic evolution (e.g. transport model) would be the best

- Only IQMD and GiBUU include “Coulomb effect”
- Only as a mean field

Simple parametrization: *PRC57, 2536 (1998), arXiv:1408.1369*
Phys. Lett.B420,20 (1998) , Nucl.Phys.A 610,286c (1996)



- Shift of energy : $E_f(p_f) = E_i(p_i) \pm V_{\text{eff}}$,
- One needs Jacobian of variable transformation
- Expanding source (spherically symmetric) : *Barz et al. PRC57 (1998)*

$$V_{\text{eff}} = \begin{cases} V_C (1 - e^{-x^2}) & \text{for a 2D expansion,} \\ V_C (\text{erf}(x) - (2/\sqrt{\pi})xe^{-x^2}) & \text{for a 3D expansion,} \end{cases} \quad x = \sqrt{(E_\pi/m_\pi - 1)m_p/T_p}$$

For low-energy

→ Original fit function: $\frac{1}{m_t^2} \frac{d^2 N}{dm_t dy} = A \left(f e^{-m_t/T_1} + (1 - f) e^{-m_t/T_2} \right)$

$Jac = \frac{E_i p_i}{E_f p_f}$

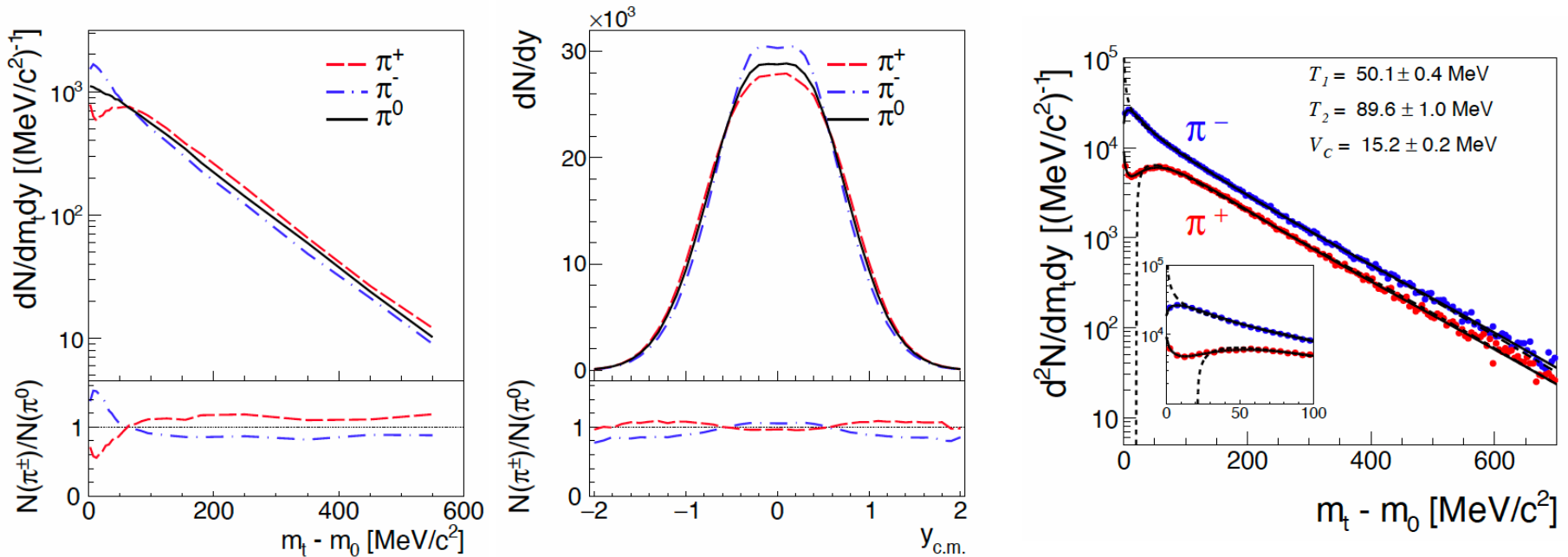
(double-Boltzmann)

→ Transformed one : $\frac{1}{m_t^2} \frac{d^2 N}{dm_t dy} = A \left(f e^{-E_i/T_1} + (1 - f) e^{-E_i/T_2} \right) \cdot Jac \cdot Jac E f f$

Toy simulations with thermal source

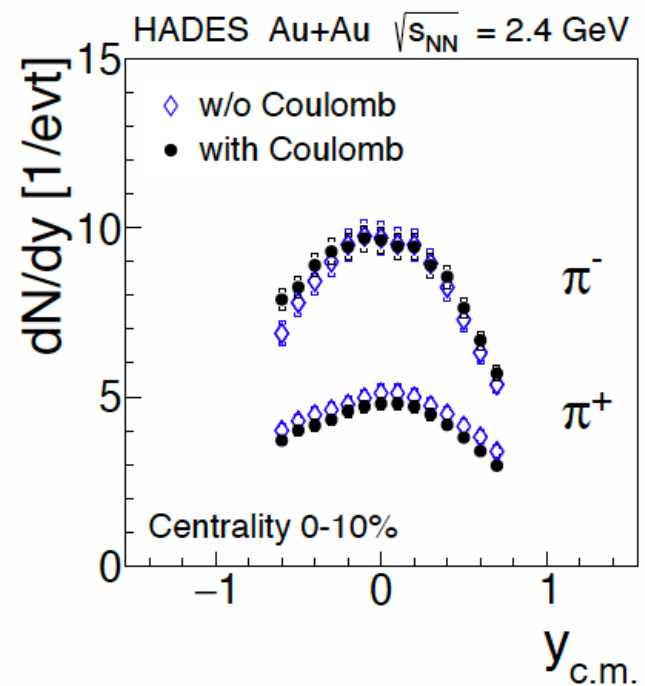
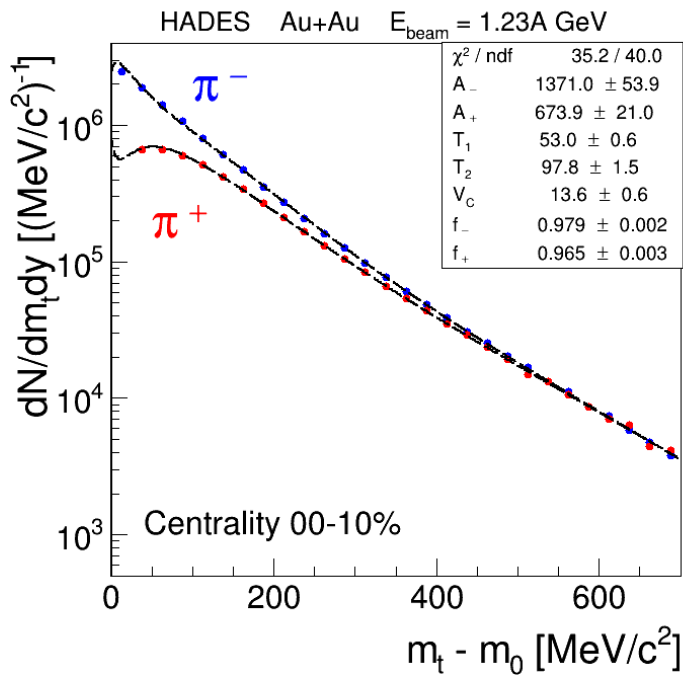
Coulomb-modified thermal source implemented in Pluto event generator with parameters:

→ $T_1 = 5\text{eV}$, $T_2 = 90\text{MeV}$, $\text{frac} = 0.95$ and $V_c = 15\text{ MeV}$



Fit parameters agree with the input

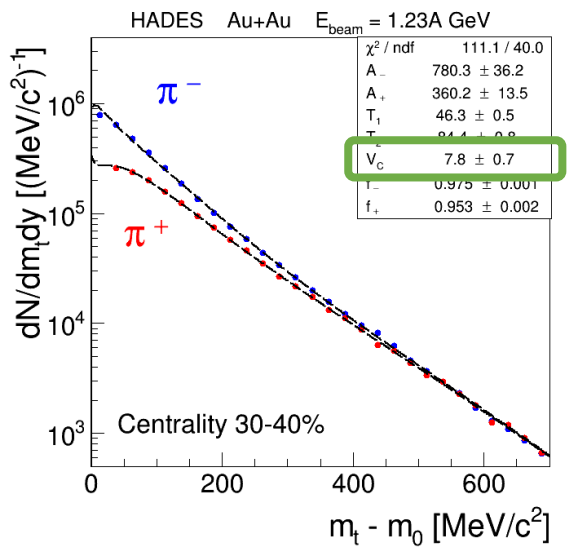
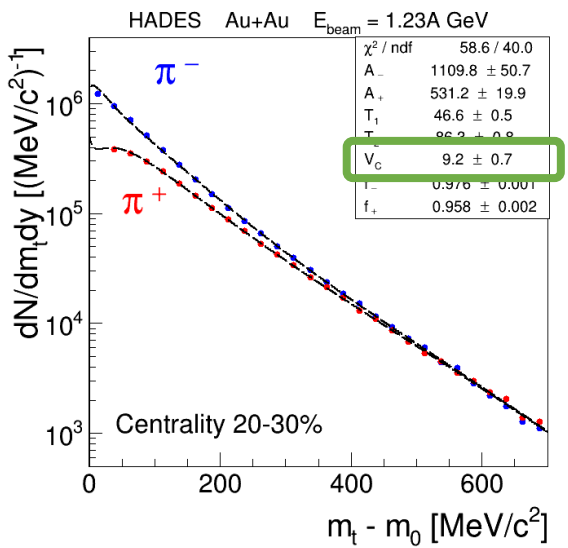
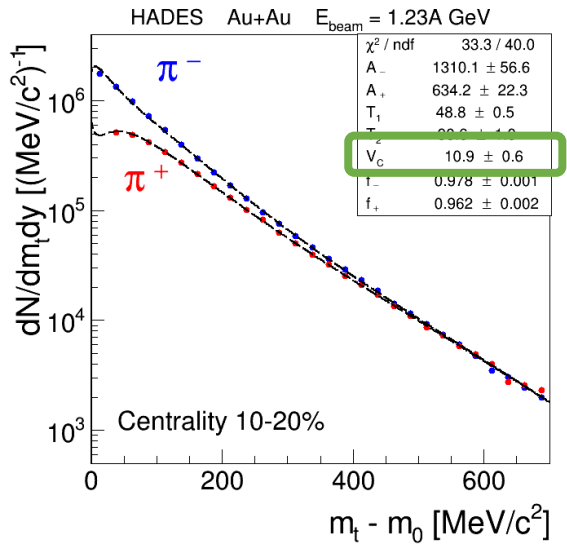
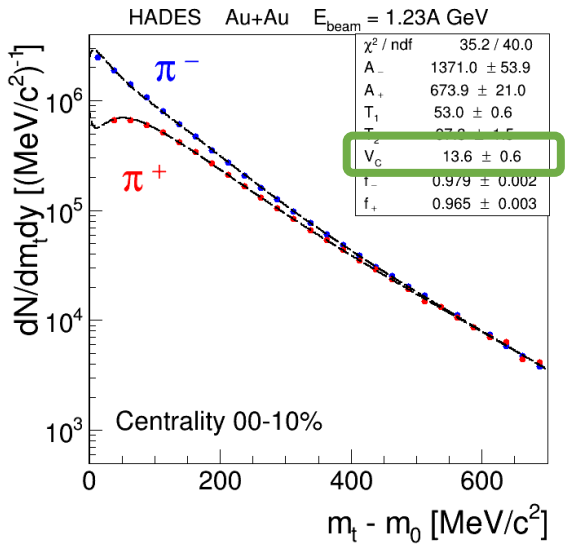
Extracting Coulomb potential. Rapidity dependence



- Combined fit to both charges
 - most central events
 - mid-rapidity
- All parameters in the fit are free

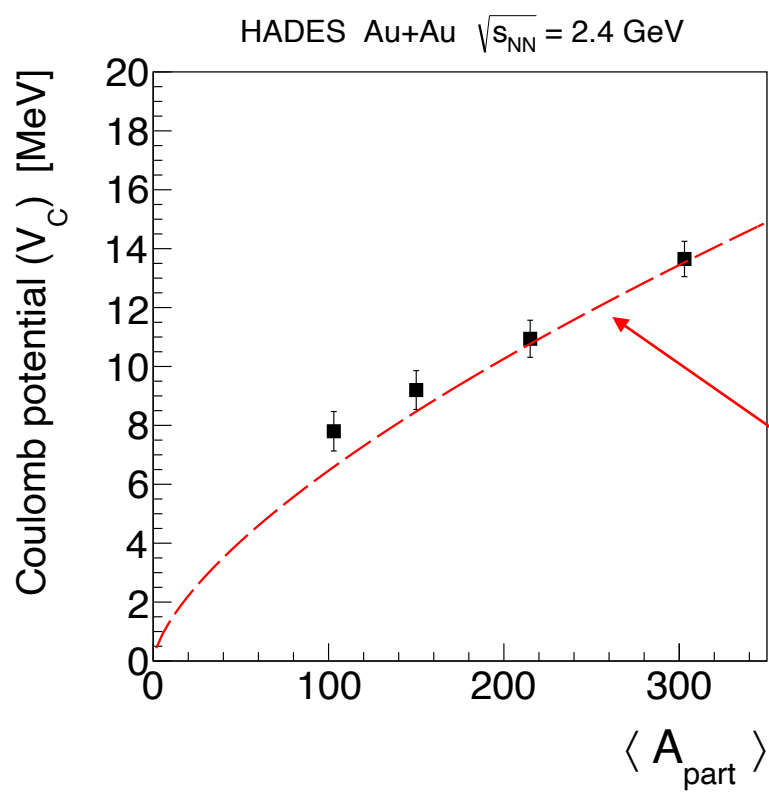
Including Coulomb effects gives more reliable fit, to use for extrapolation

Centrality dependence



- Combined fit
- to both charges
 - 4 centralities
 - mid-rapidity spectra
- All fit parameters free

Centrality dependence



Pions decoupling from fireball at freeze-out

$$\langle V_c \rangle = \frac{6}{5} \frac{Ze^2}{R} \quad \text{Hard-sphere model}$$

for constant freeze-out density

$$R \propto A^{1/3}$$

$$Z \propto A$$

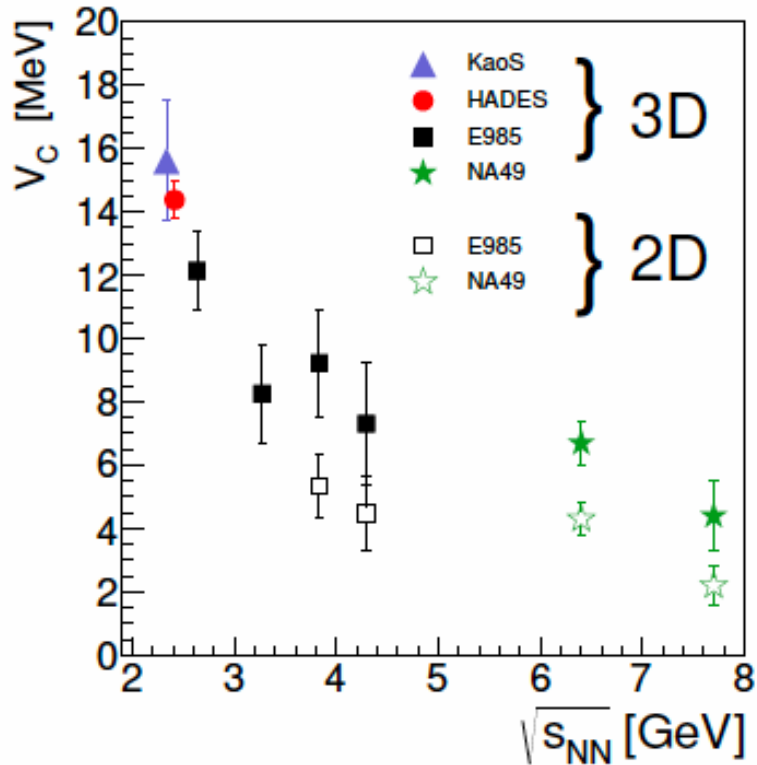


Normalized to 0-10%

$$V_C \propto A^{2/3}$$

- Coulomb potential scales with A_{part} roughly like $A^{2/3}$
- Deviations can be caused by spectator charges which are not taken into account in the parametrization

Beam energy dependence of V_c

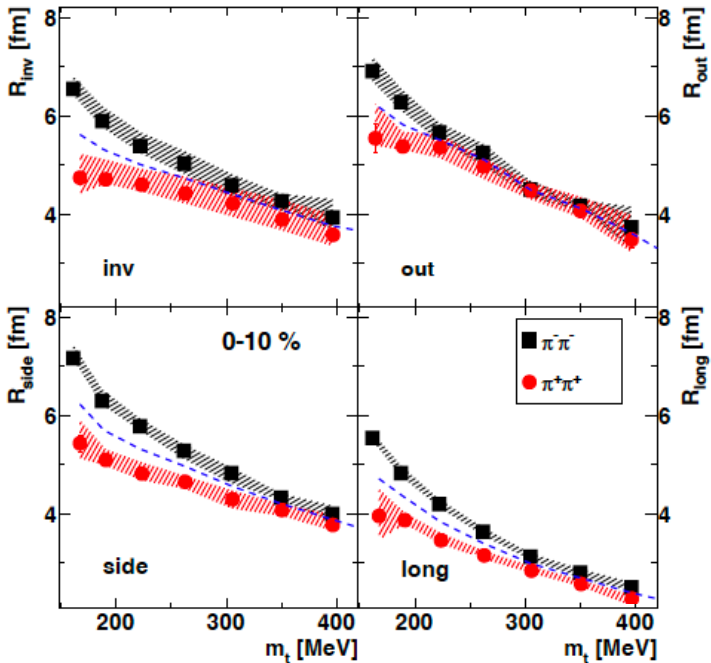


Potential is decreasing with increasing beam energy

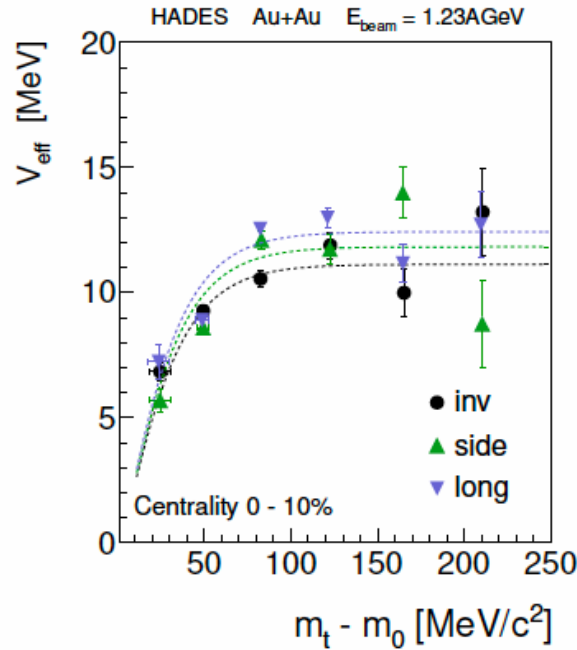
- stronger expansion \rightarrow larger radii \rightarrow lower $V_c = Z/R$
- 3D \rightarrow 2D
- Less stopping? Is this true at AGS energies already or does that set in at SPS only

Coulomb potential from HBT radii

- Coulomb potential acts on the relative momentum of charged-pion pairs, affecting the extracted HBT radii.
- V_{eff} (mt) can be extracted using :
$$V_{\text{eff}}(m_t) = \frac{m_t^2 - m_\pi^2}{4m_t} \frac{R_{\pi^-\pi^-}^2 - R_{\pi^+\pi^+}^2}{R_{\pi^0\pi^0}^2}.$$
- V_C can be extracted from V_{eff} (mt) considering an 3D expanding source (along to the single particle consideration)

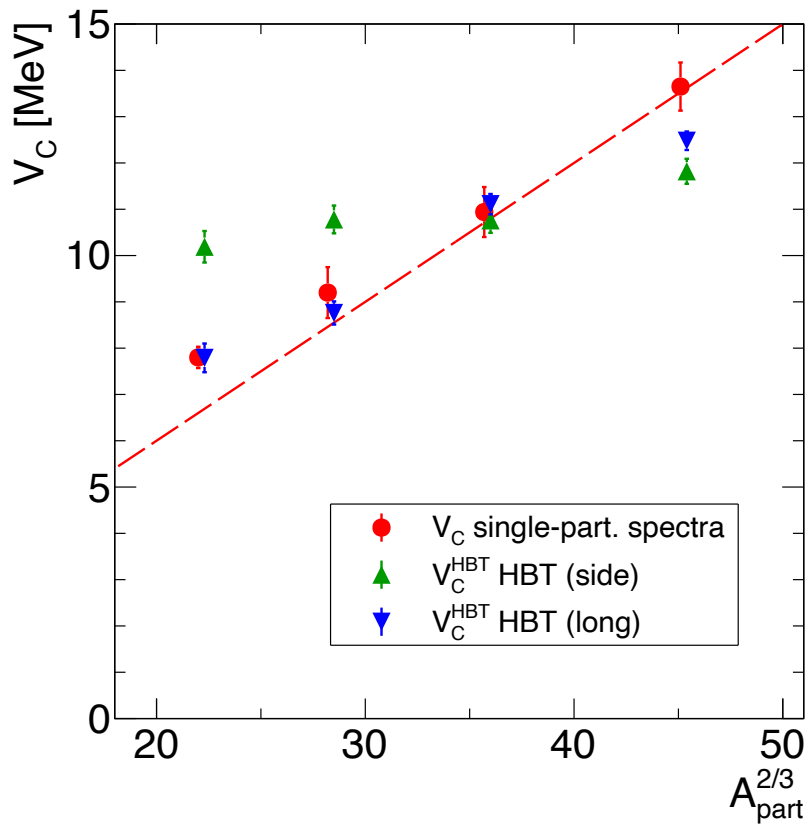


- HBT analysis provides various radii: $R^{\text{inv}}, R^{\text{side}}, R^{\text{out}}, R^{\text{long}}$
- R^{out} not considered here



HBT published in:
 Phys.Lett.B 795 (2019) 446-451
 Eur.Phys.J.A 56 (2020) 5, 140

Extracted V_C , single spectra vs HBT

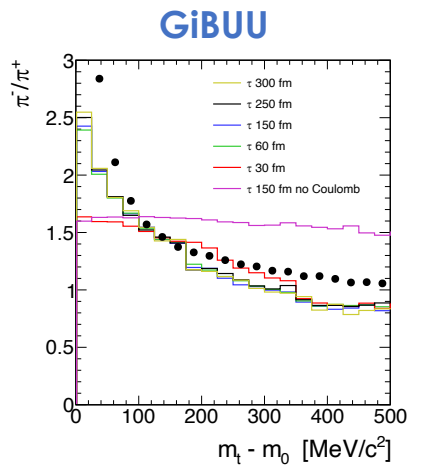
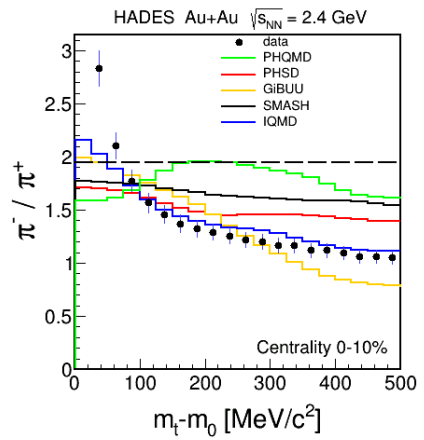
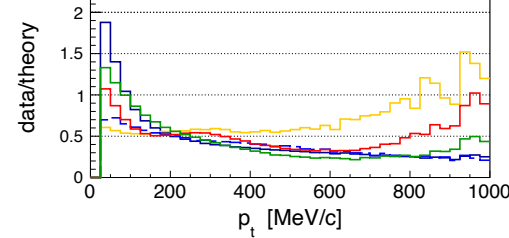
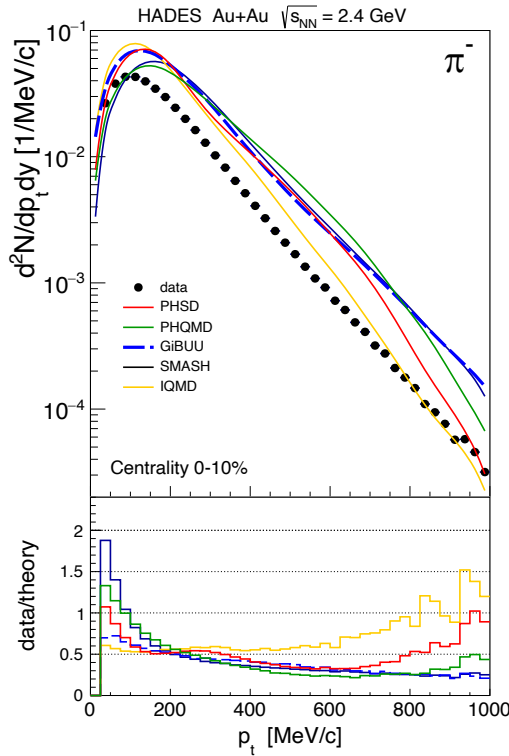
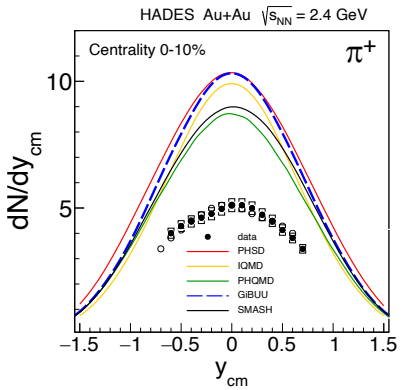
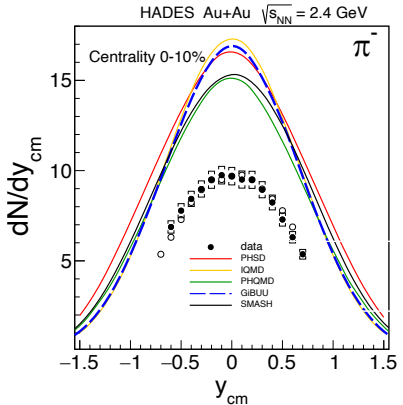


Reasonable agreement between HBT and single particles spectra results.

We do have a fair/reasonable agreement but close inspection shows systematic differences:

- Do we compare the same volumes ?
- HBT measures a homogeneity radius !

Comparison to transport models (status from 2020)

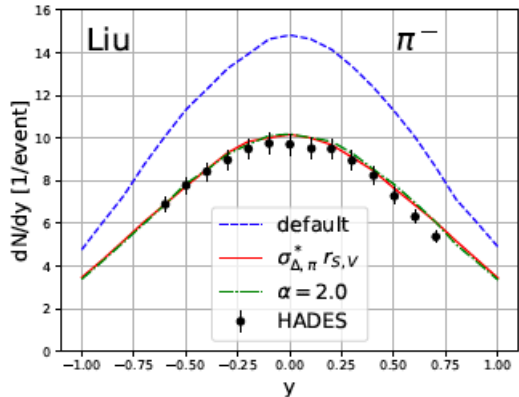
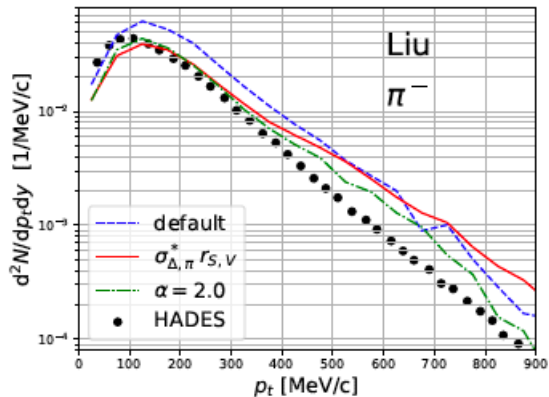
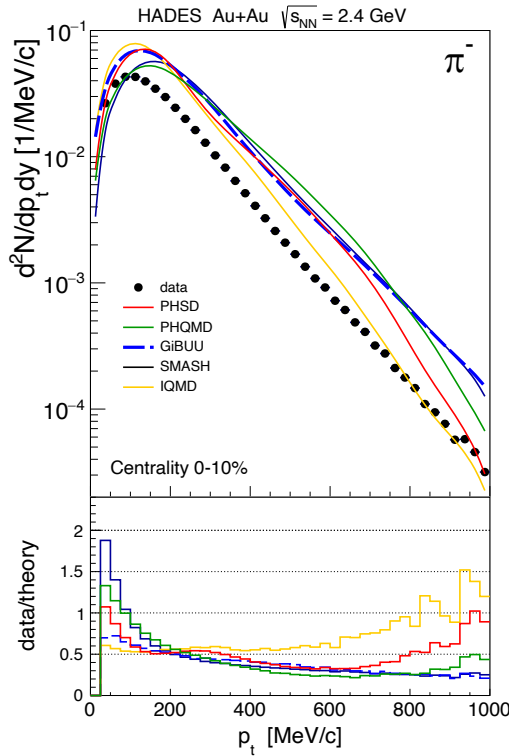
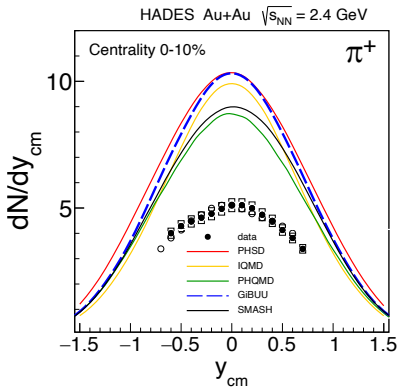
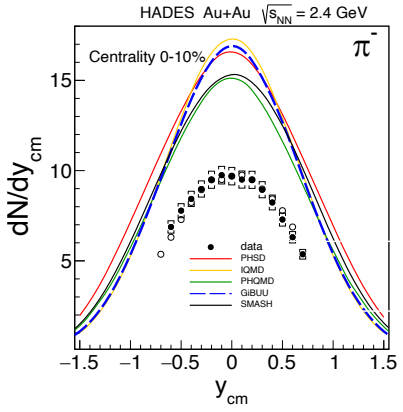


Measured pion yields are compared with various transport model calculation. All models overshoot our data by nearly a factor 2!

→ This triggered new efforts on the theory side to improve the agreement

Comparison to transport models (status from 2020)

Pesent GiBUU 2023



C.Kummer et al.
arXiv:2309.09042v1

Measured pion yields are compared with various transport model calculation.
All models overshoot our data by nearly a factor 2!

- Improvement in EOS
- In-medium modification of
 - Cross sections
 - Delta resonance

Summary

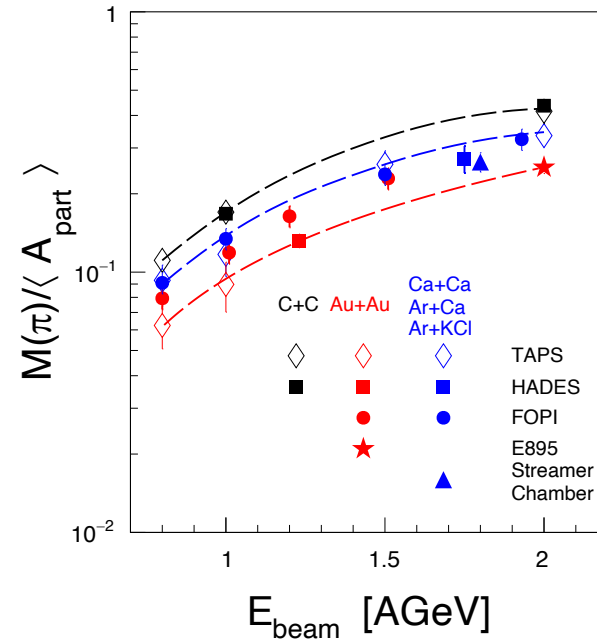
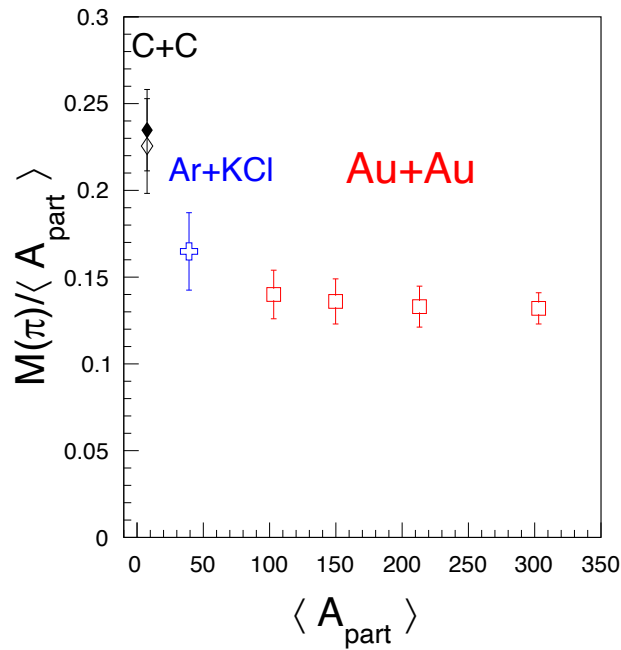
- HADES measured charged pion production with unprecedented statistics in Au+Au collisions.
- A detailed multi-differential analysis has been done, including Coulomb modifications of the pion spectra.
- The evolution of the Coulomb potential with collision centrality and beam energy has been presented.
- Effects of the Coulomb potential on 2-pion interferometry have been presented as well, consistent with the potentials obtained from the single-pion spectra.

Outlook

- Agreement with transport calculations is expected to improve in the near future.
- HADES will continue these studies with new data to be gathered in a beam-energy scan (0.2 - 0.8 AGeV) scheduled for March 2024.

Back-up slides

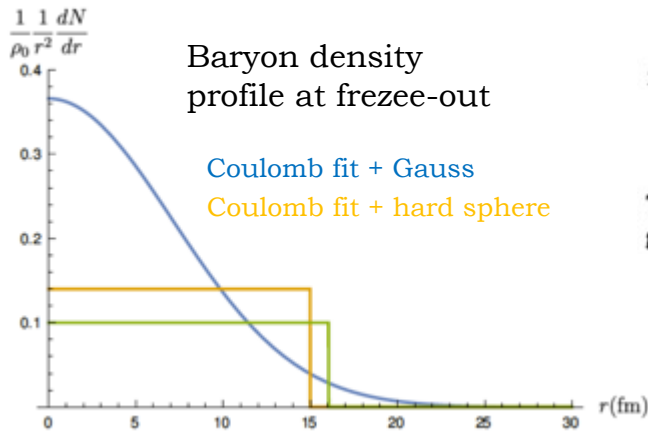
Pion systematic : A_{part} and E_{beam} dependence



Strong system size and energy dependence

Hadron resonance gas

Vc \longrightarrow charge radius \longrightarrow Baryon density distribution
 assuming charge radius = matter radius



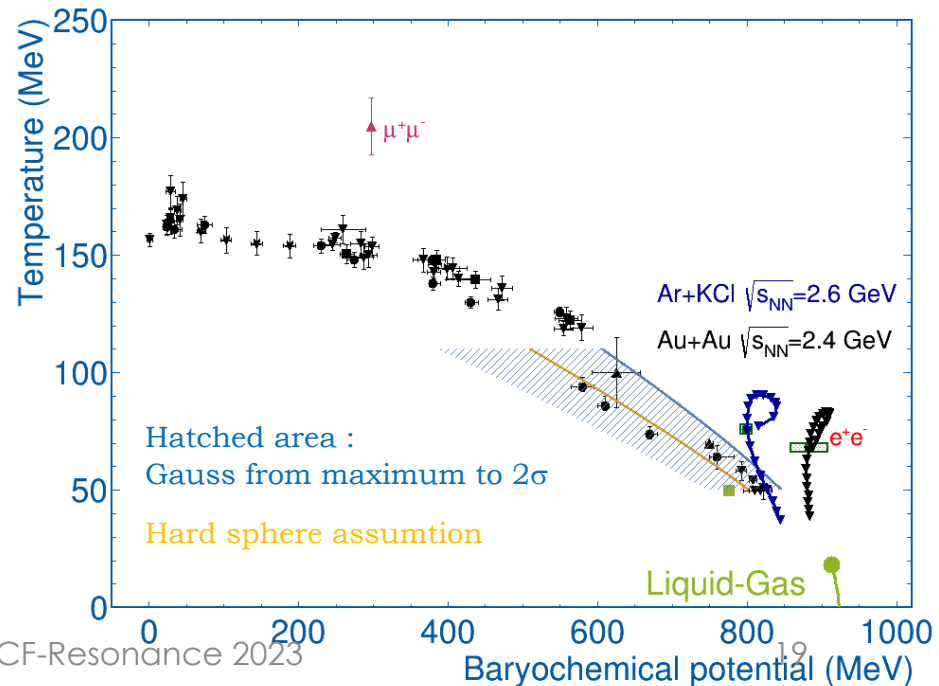
† We may write out for reference the formula for the chemical potential of a monatomic ideal gas with statistical weight (degree of degeneracy) of the ground state g :

$$\mu = T \log \left[\frac{P}{gT^{5/2}} \left(\frac{2\pi\hbar^2}{m} \right)^{3/2} \right] = T \log \left[\frac{N}{gV} \left(\frac{2\pi\hbar^2}{mT} \right)^{3/2} \right]. \quad (46.1a)$$

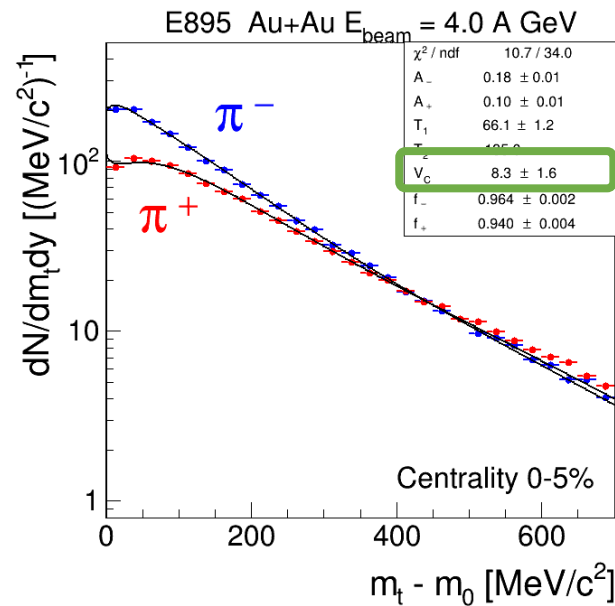
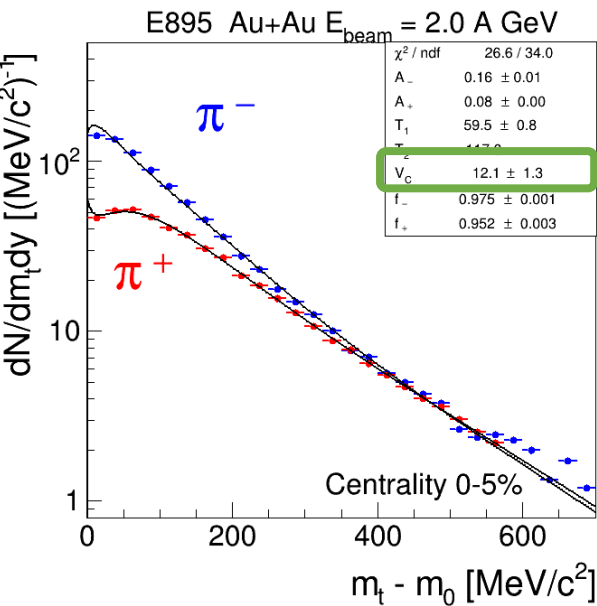
This applies also to a Boltzmann gas of elementary particles; for instance, in an electron gas $g = 2$.

L. D. Landau and E. M. Lifshitz,
Statistical Physics 2nd ed. Course of Theoretical Physics,
 Vol. 5 (Pergamon Press Ltd., 1969).

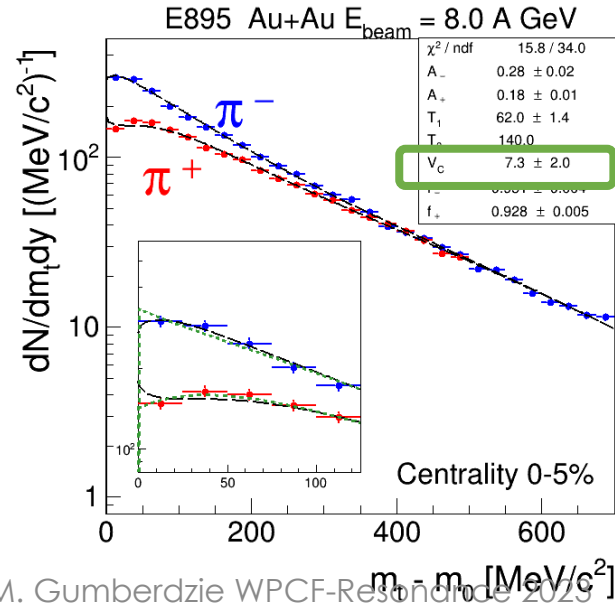
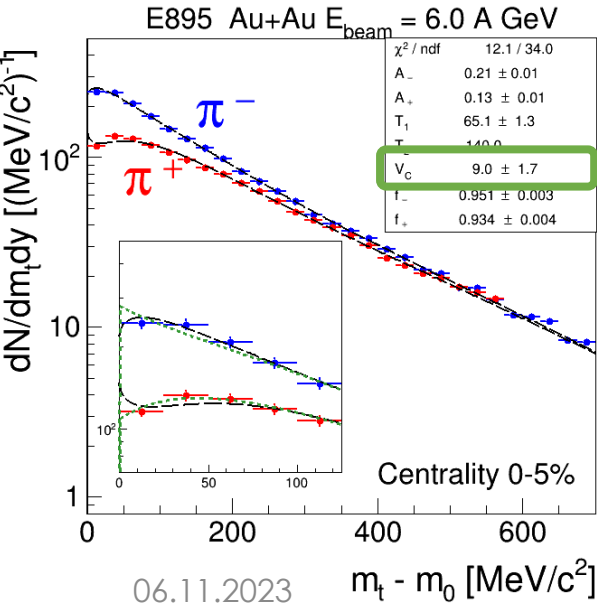
- Independent way of estimating freeze-out point/region in phase diagram
- Result consistent with the fits to particle yields



Beam energy dependence: E895 experiment at AGS

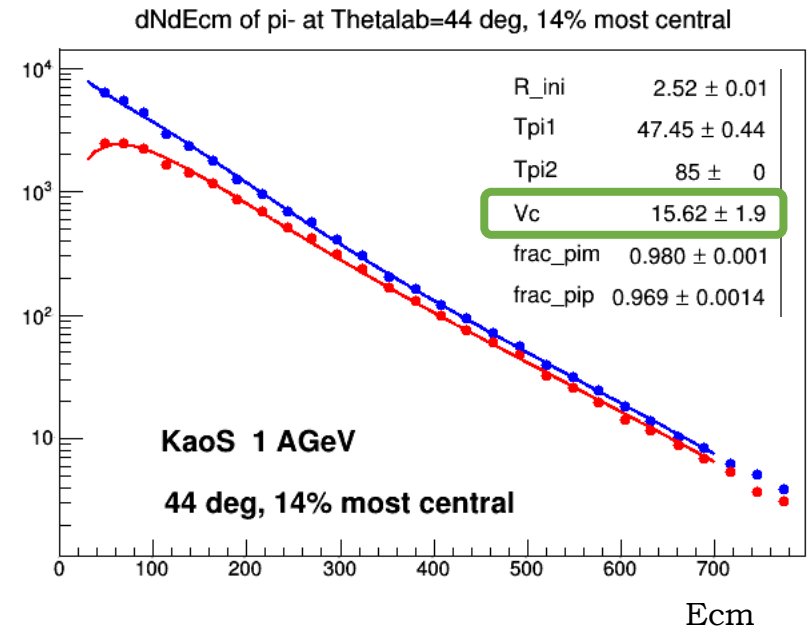


- in our fits T2 is fixed to published values
- other parameters set to be free,



data taken from :
http://nuclear.ucdavis.edu/~e895/published_spectra.html

Beam energy dependence : Kaos and Fopi



Phys. Lett. B420, 20 (1998)