

WPCF - Resonance Workshop 2023



Catania (Italy), November 6-10, 2023

Correlation Function studies at intermediate energies at CSHINE

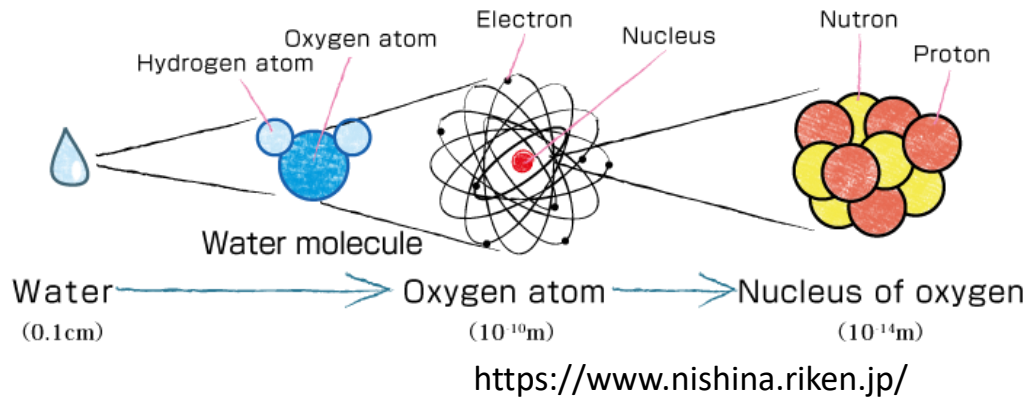
speaker : Yijie Wang
coauthor : Zhigang Xiao

■ Content

- **Research Background**
- **CSHINE Detector System**
- **HBT Method**
- **Isospin Chronology Result**
- **Summary**

■ Nucleus, Isospin, Symmetry Energy

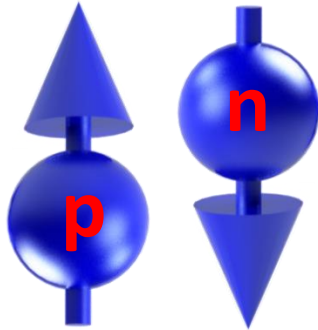
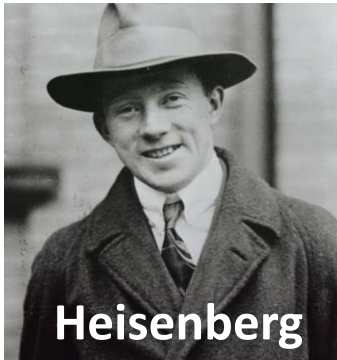
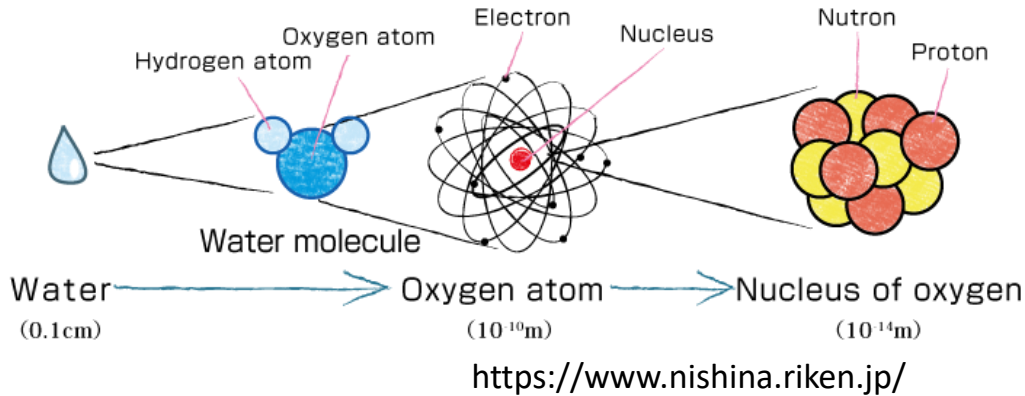
Molecule – Atom – Nucleus



<https://www.nishina.riken.jp/>

■ Nucleus, Isospin, Symmetry Energy

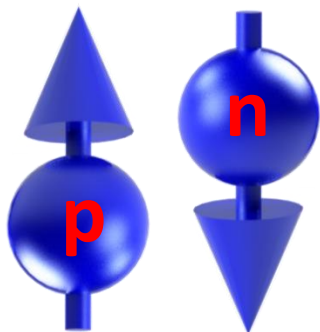
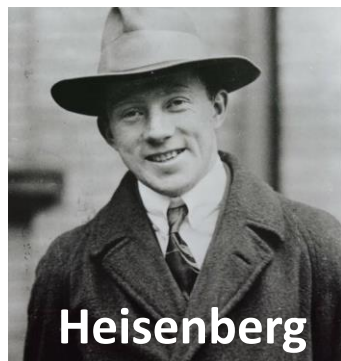
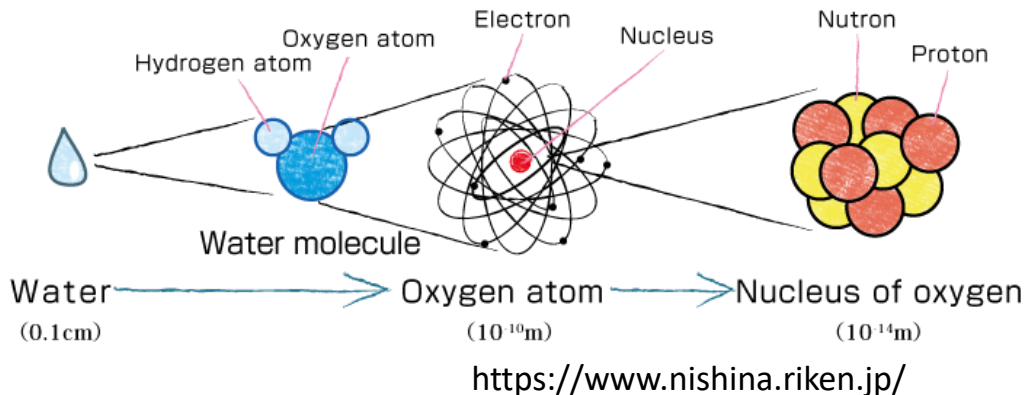
Molecule – Atom – Nucleus



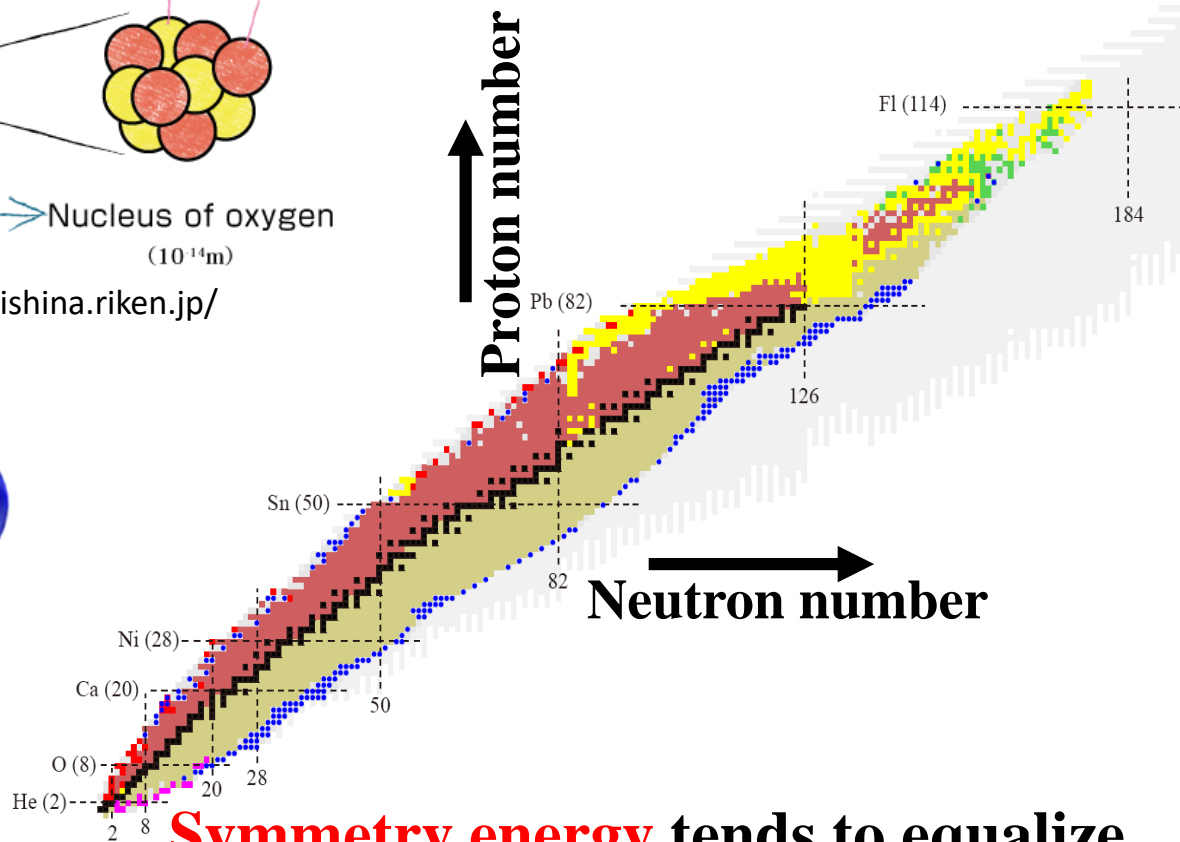
Isospin distinguishes
proton and neutron

■ Nucleus, Isospin, Symmetry Energy

Molecule – Atom – Nucleus



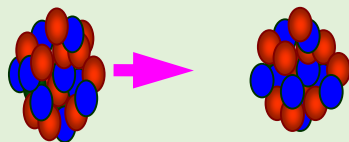
Isospin distinguishes proton and neutron



Symmetry energy tends to equalize the number of neutrons and protons

■ Heavy Ion Reaction, Isospin dynamic in zeptosecond scale

Heavy Ion Reaction ~ 10^{-22} s



30MeV/u ^{40}Ar

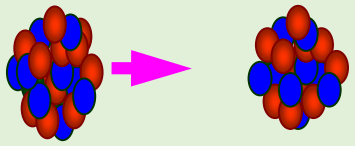
^{197}Au

Velocity: $\sim 0.25c$

Scale: $\sim 10^{-14}\text{m}$

Heavy Ion Reaction, Isospin dynamic in zeptosecond scale

Heavy Ion Reaction $\sim 10^{-22}$ s



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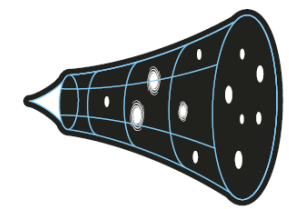
ATTOSECOND

$\sim 10^{-18}\text{s}$



HEARTBEAT

$\sim 1\text{s}$

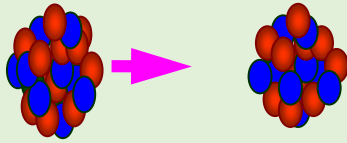


AGE OF THE UNIVERSE

$\sim 10^{18}\text{s}$

Heavy Ion Reaction, Isospin dynamic in zeptosecond scale

Heavy Ion Reaction $\sim 10^{-22}$ s

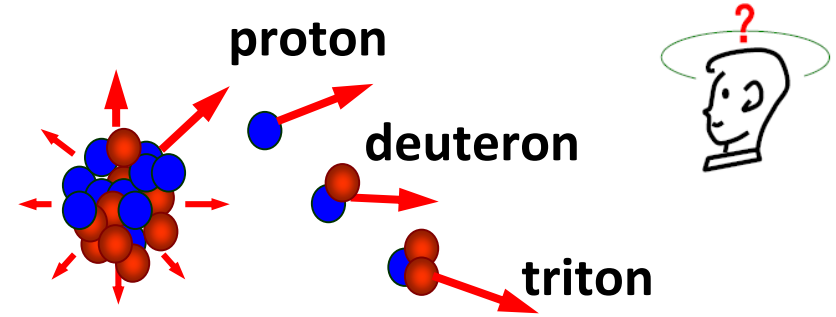


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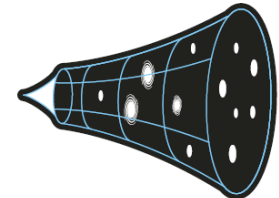
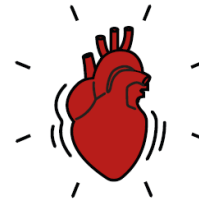
Question: Isospin dependent particle emission timescale and emission order?

Heavy Ion Reaction
 $\sim 10^{-22}\text{s}$

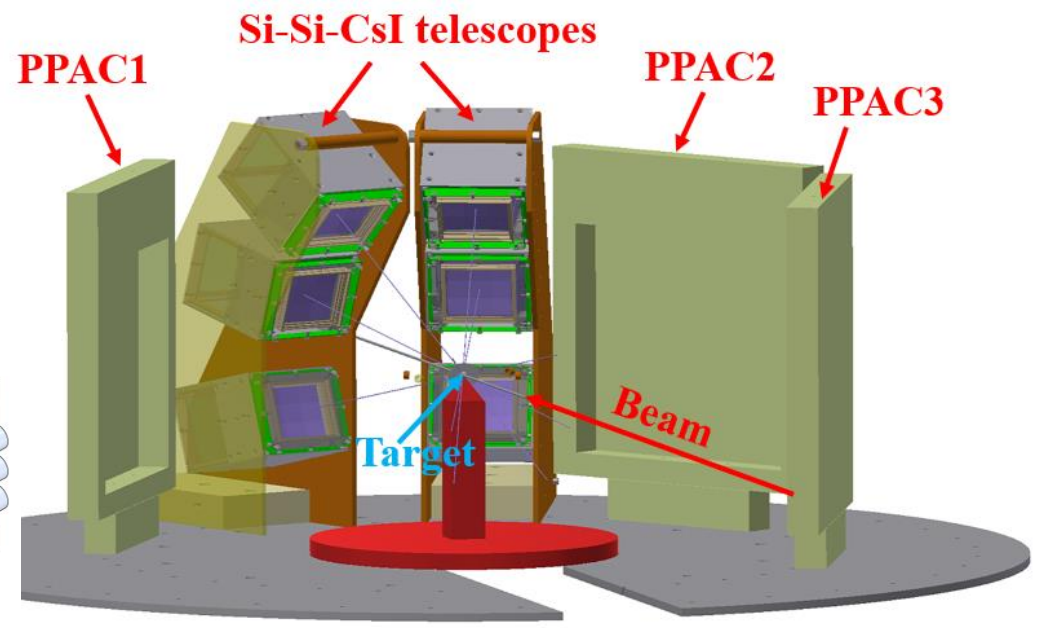
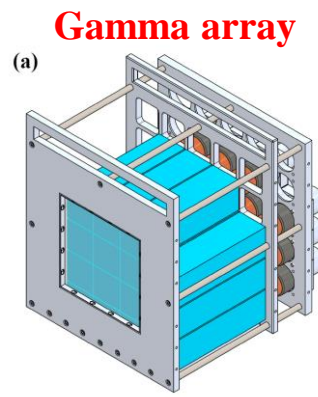
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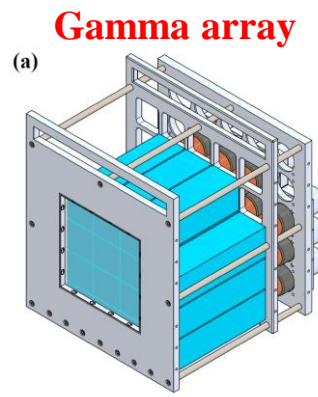
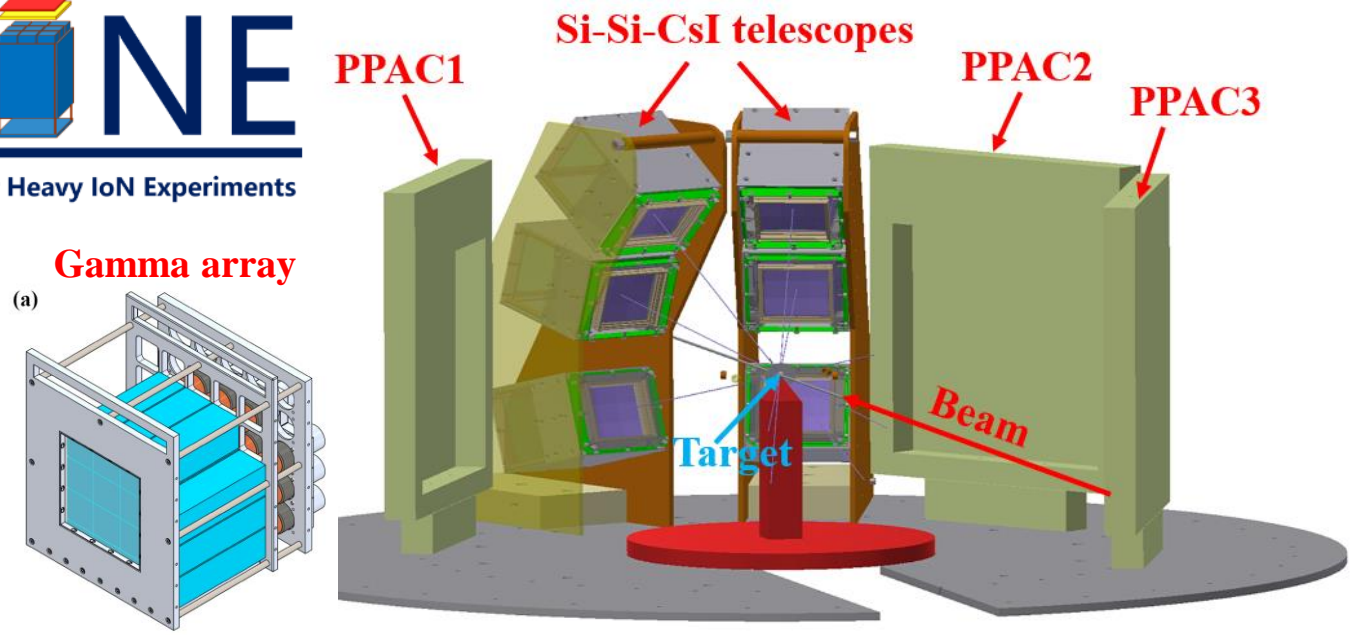
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■ Compact Spectrometer for Heavy Ion Experiment (CSHINE)

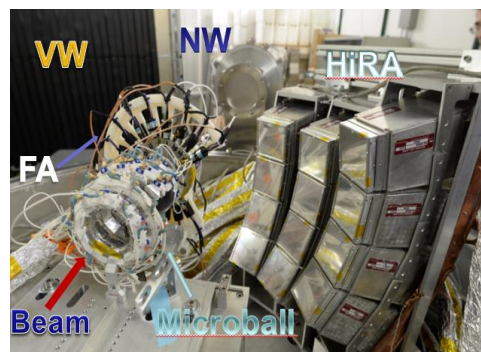


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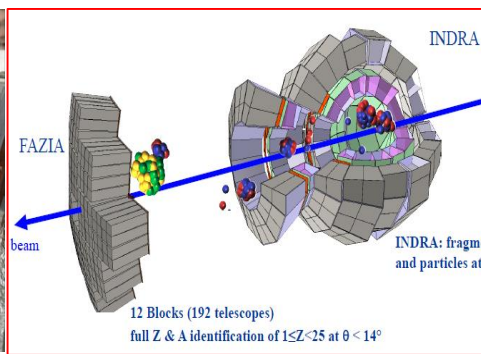


Compared with the large detector system in the world, CSHINE is relatively compact.

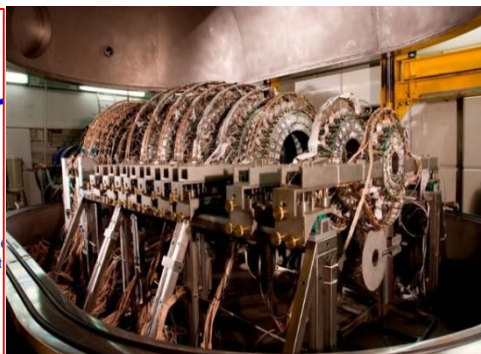
HiRA@FRIB



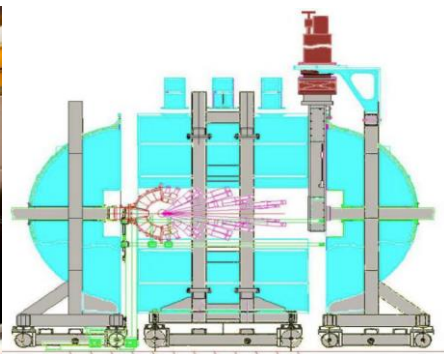
INDRA@GANIL



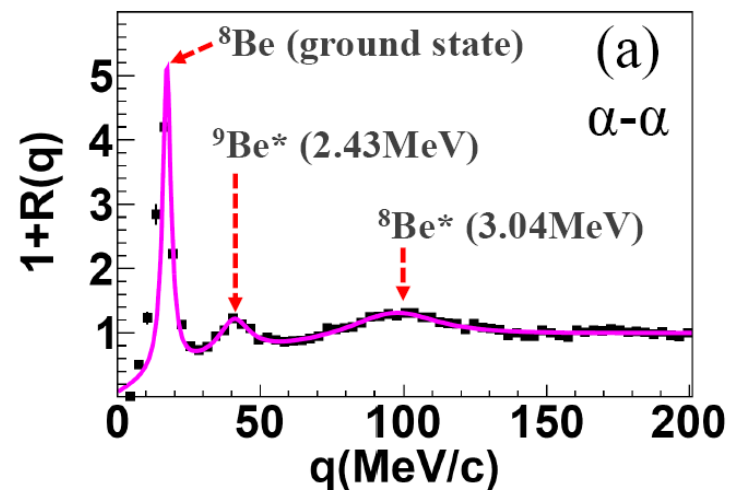
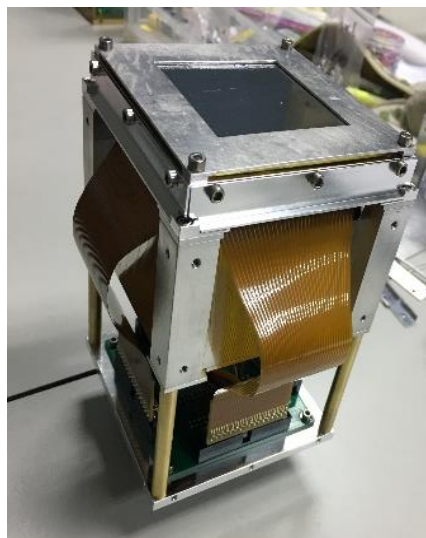
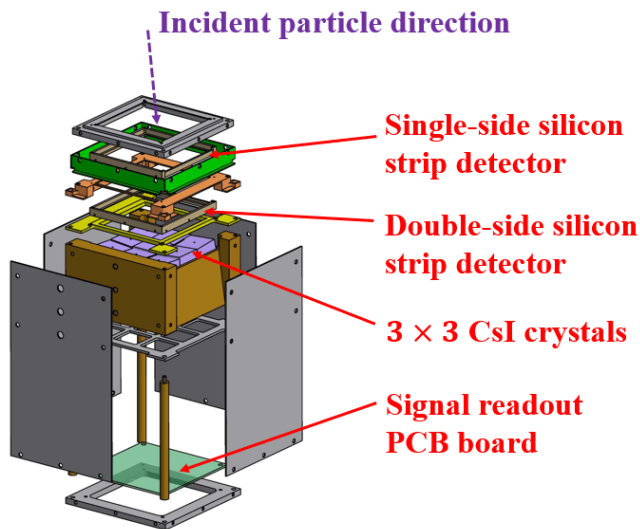
CHIMERA @ INFN



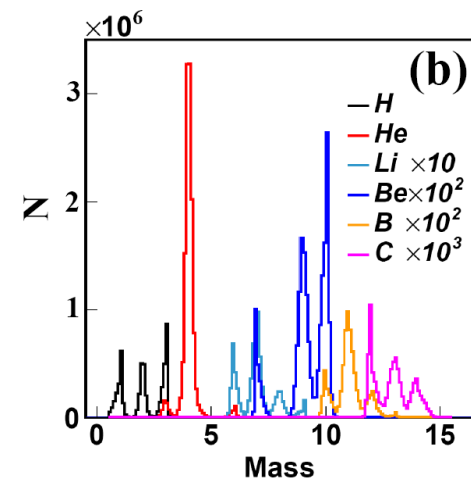
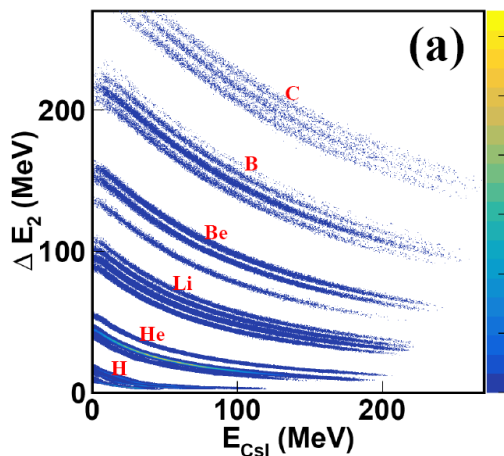
NIMROD@TAMU



■ Silicon Strip Detector Telescope (SSDT)



Silicon strip width: 2mm
 SSDT energy resolution: 2%
 For **light charge particles**



Nucl. Sci. Tech. 32, 4 (2021)

Nucl. Inst. Meth. A, 1011, 165592 (2021)

Parallel Plate Avalanche Chamber (PPAC)

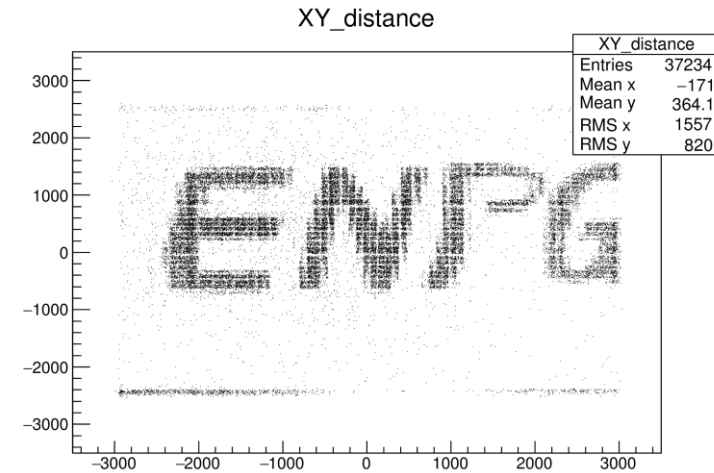
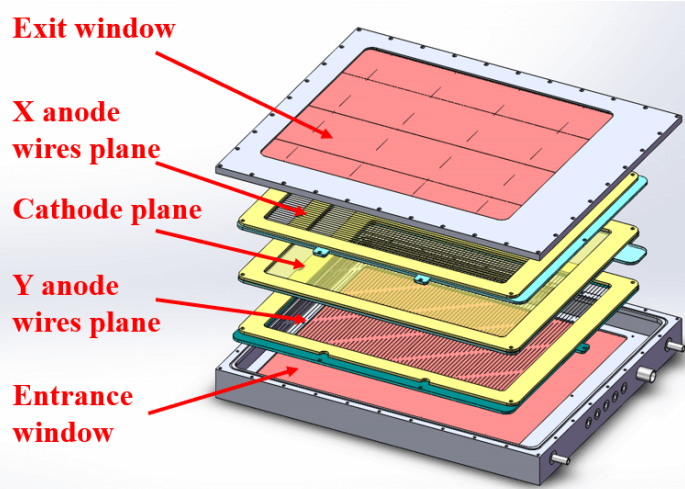
Exit window

X anode wires plane

Cathode plane

Y anode wires plane

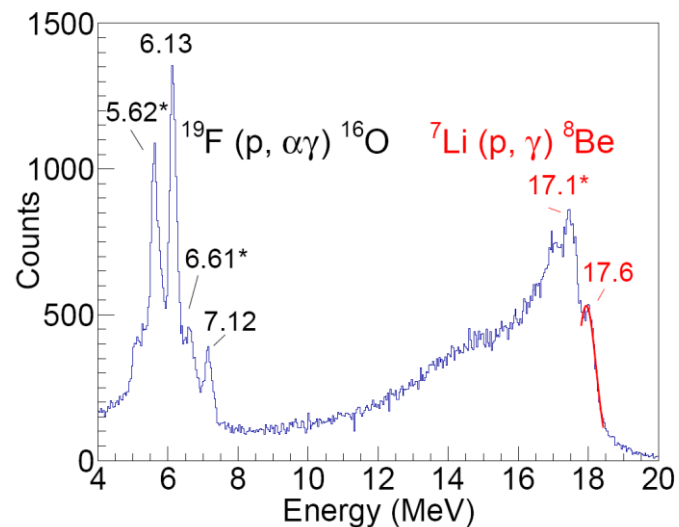
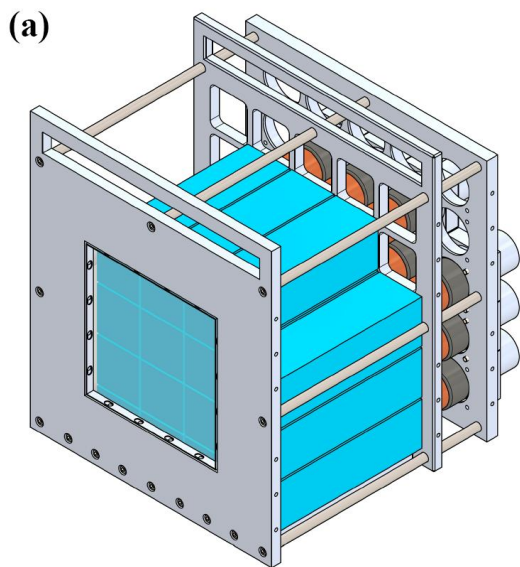
Entrance window



Time resolution: 260ps
Position resolution: 1.4mm
Sensitive area: 240mm*280mm
For **fission fragments**

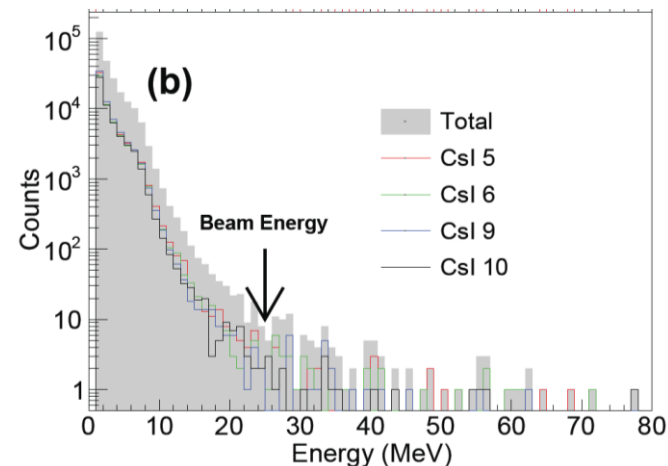
Nuclear Engineering and Technology 52,3 (2019)

High Energy Gamma Detector Array



Energy resolution: 3%
Energy range: 10-80MeV
For **high energy gamma**

Nucl. Inst. Meth. A, 1053, 168330 (2023)



■ CSHINE upgrade: Neutron detector Array

Heavy ion reAction Neutron MEasurement detector (HANMER)

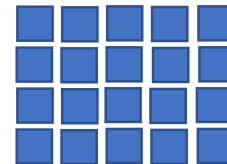


Plastic scintillator + PMT

15cm * 15cm * 15cm

4 * 5 units

For **neutron**



■ Physics studies at CSHINE:

① Light charge particles

- a, Isospin relaxation
- b, E_{sym} in nEoS
- c, HBT correlation
- d, Yield Ratio

...

② Fission fragments

- a, Fast fission
- b, Fission dynamics
- c, Folding angle
- d, Neck formation

...

③ High energy gamma

- a, np bremsstrahlung
- b, Short Range Corr.
- c, $np \rightarrow d + \text{gamma}$
- d, E_{γ} spectrum

...

④ Future plane

- a, n-n HBT correlation
- b, t and ^3He emission
- c, $\theta(n/p)$ distribution
- d, Resonance decay

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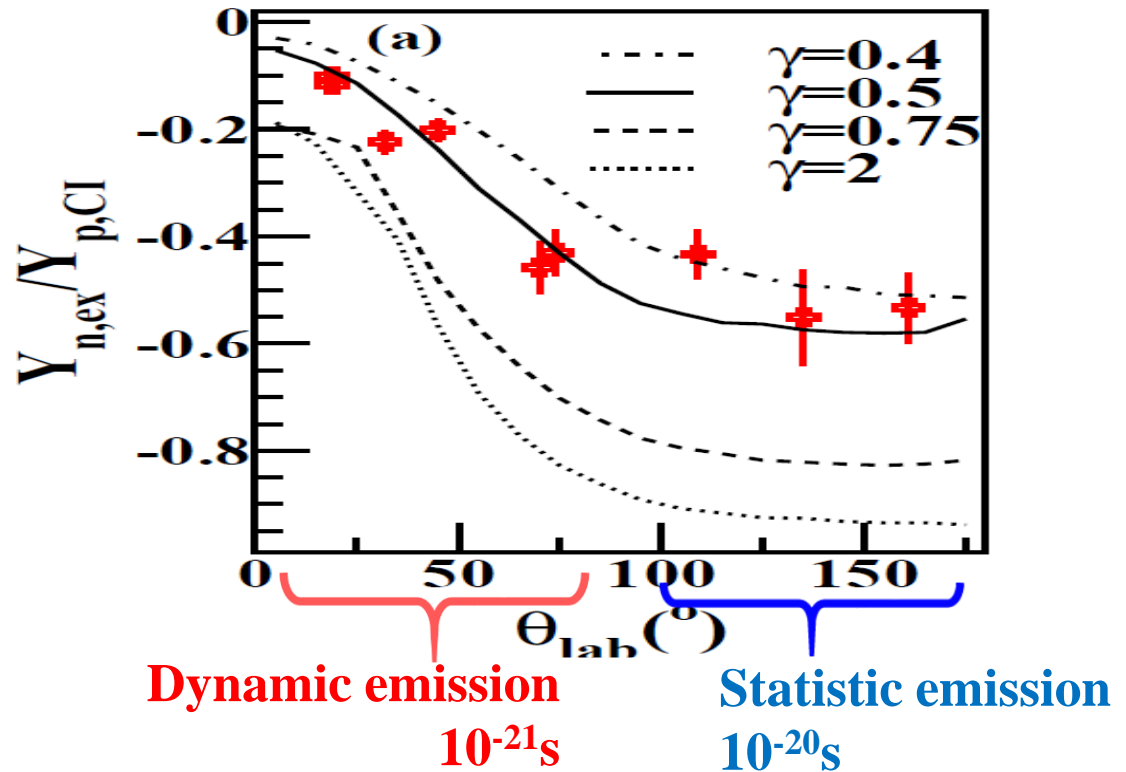
...

■ Previous knowledge of Isospin Relaxation

Neutron excess probe:

$$\frac{Y_{n,ex}}{Y_{p,Cl}} = \frac{\sum y_i(N_i - Z_i)}{\sum y_i Z_i},$$

Time → Angle



■ Previous knowledge of Isospin Relaxation

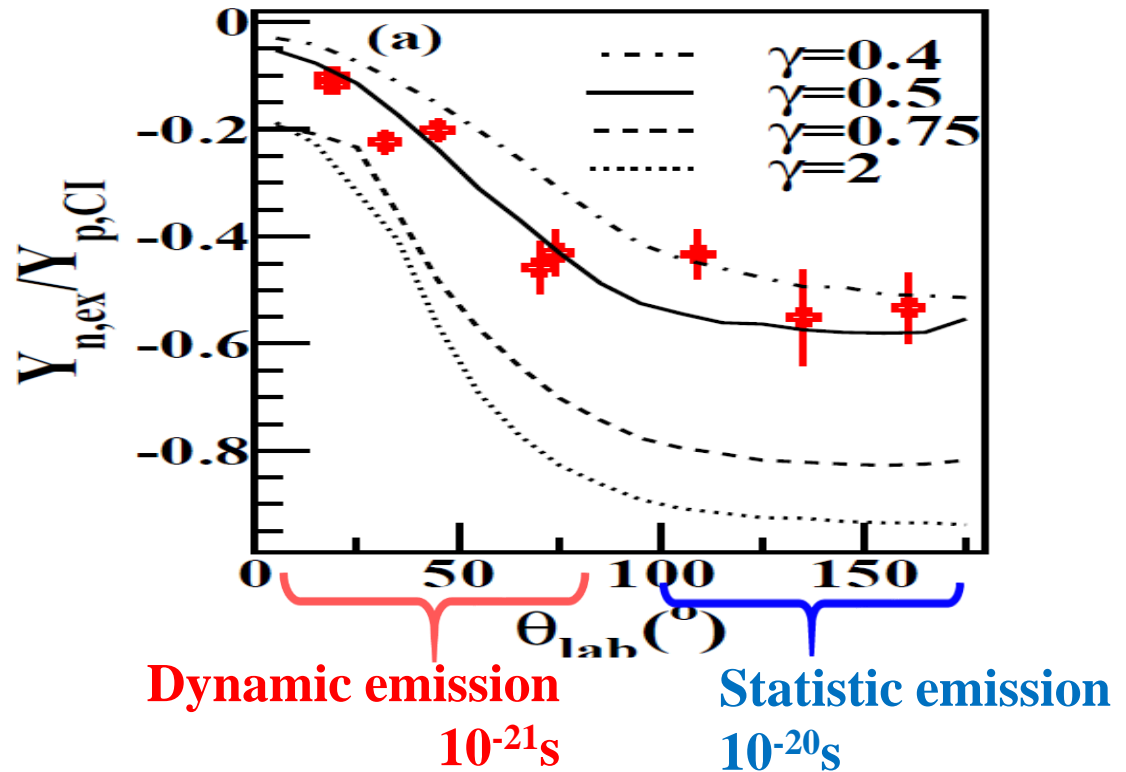
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Result: Neutron rich particle emitted earlier!

PRC 95, 041602(R) (2017)



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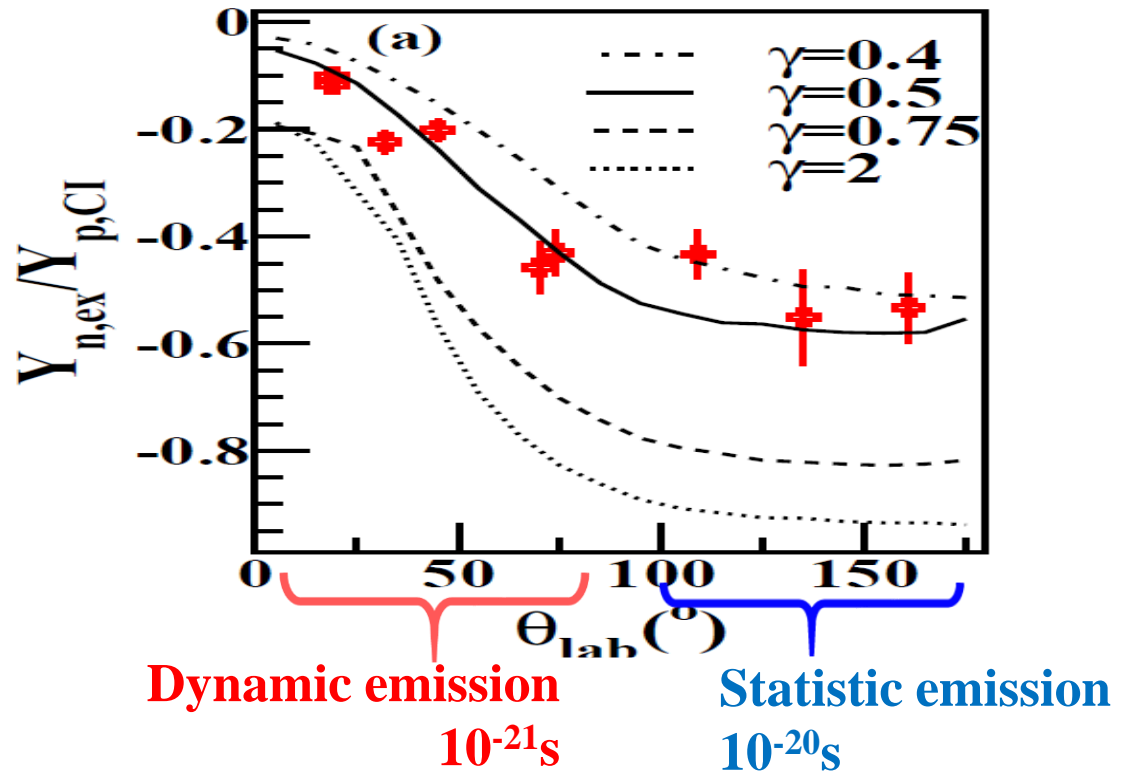
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One-body observable at final state only delivers **qualitative** picture of isospin dynamics.

■ HBT intensity interferometer

How to determine particle emission timescale and order **quantitatively**?

■ HBT intensity interferometer

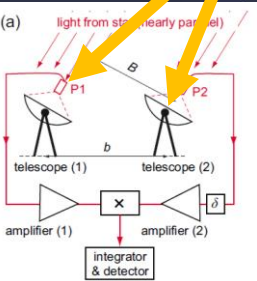
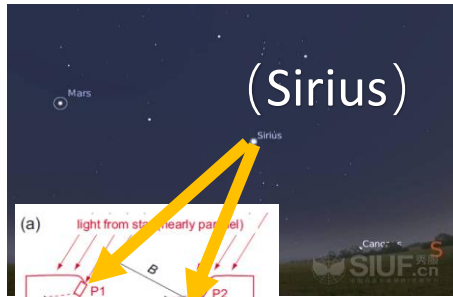
How to determine particle emission timescale and order **quantitatively**?

HBT is an approach to extract space and time information of the emission source!

HBT intensity interferometer

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➤ 1956, Hanbury Brown and Twiss ;
Angular diameter of Sirius
(Astronomy)

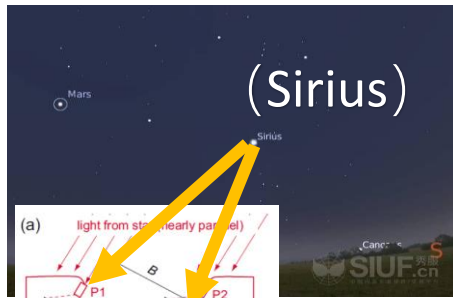
Nature 178, 4541 (1956)



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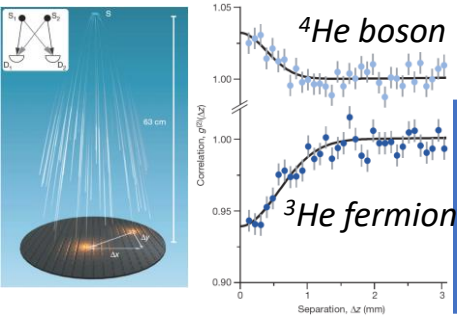
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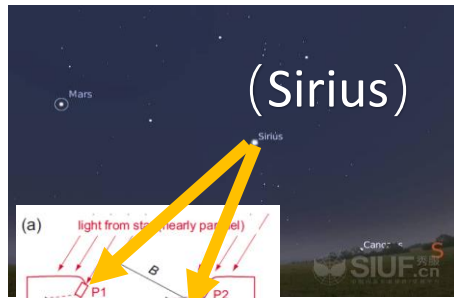
➤ 2007, T. Jeltjes et al. ;
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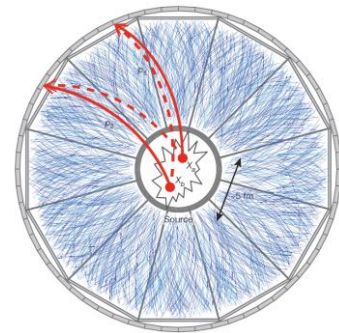
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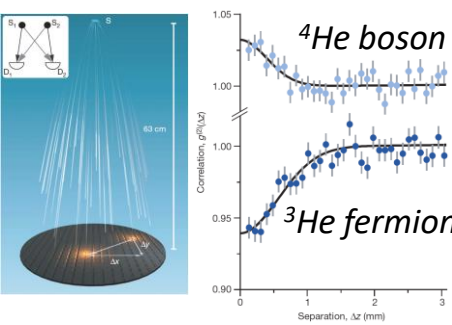
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➤ 2015, STAR;
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Nature 527, 345(2015)



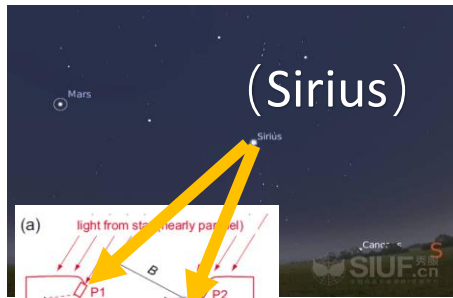
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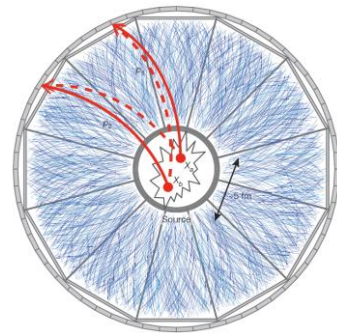
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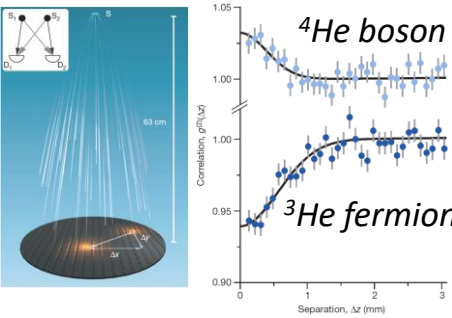
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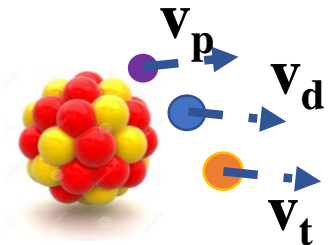
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➤ 2007, T. Jeltsov et al. ;
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➤ 2022, ENPG group ;
isospin chronology
(Nuclear physics)



Physics Letters B, 825, 136856 (2022)

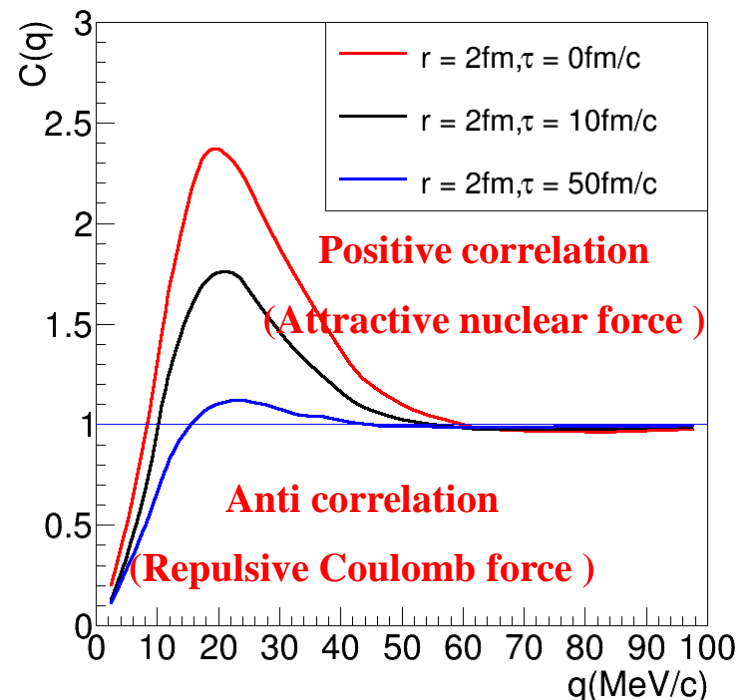
HBT principle (Nuclear emission source)

1977, S. Koonin use HBT to proton-proton correlation

$$\frac{1}{\sigma} \frac{d\sigma}{dp_1 dp_2} = \int_{-\infty}^{\infty} dt_1 dt_2 \int d\mathbf{r}_1 d\mathbf{r}_2 \underbrace{D(\mathbf{r}_1 t_1, p_1) D(\mathbf{r}_2 t_2, p_2)}_{\text{The temporal and spatial distribution of proton emission from the emission source}}$$

$$\times \left\{ \underbrace{\frac{1}{4} \left| {}^1\Psi_{p_1 p_2}(\mathbf{r}_1, \mathbf{r}_2) \right|^2 + \frac{3}{4} \left| {}^3\Psi_{p_1 p_2}(\mathbf{r}_1, \mathbf{r}_2) \right|^2}_{\text{Wave function and relative motion}} \right\}$$

1977_S. Koonin_PLB

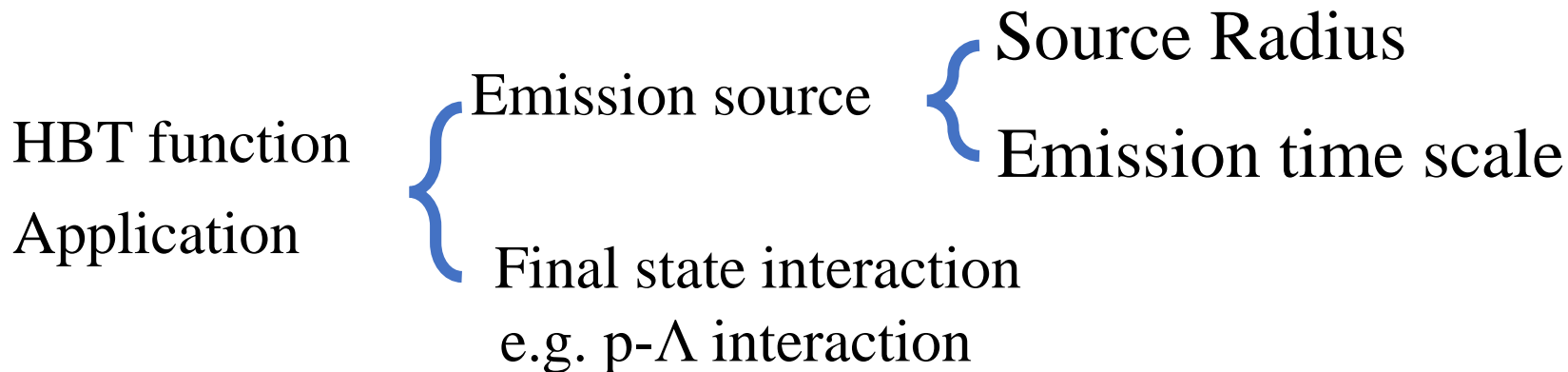
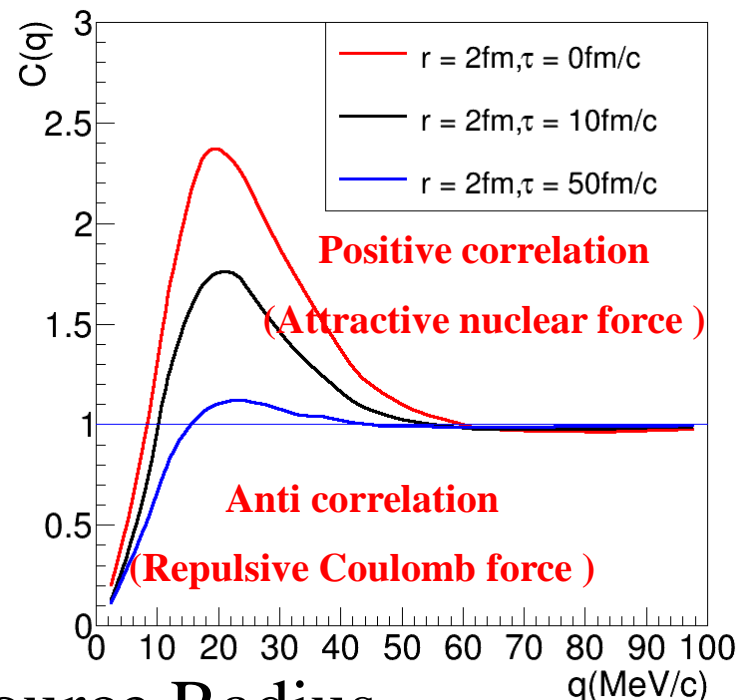


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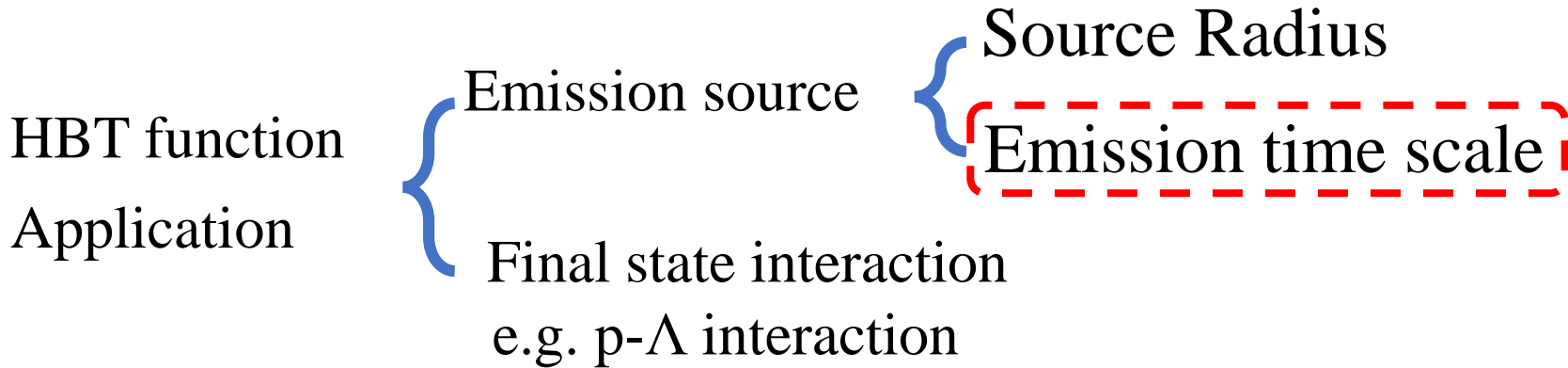
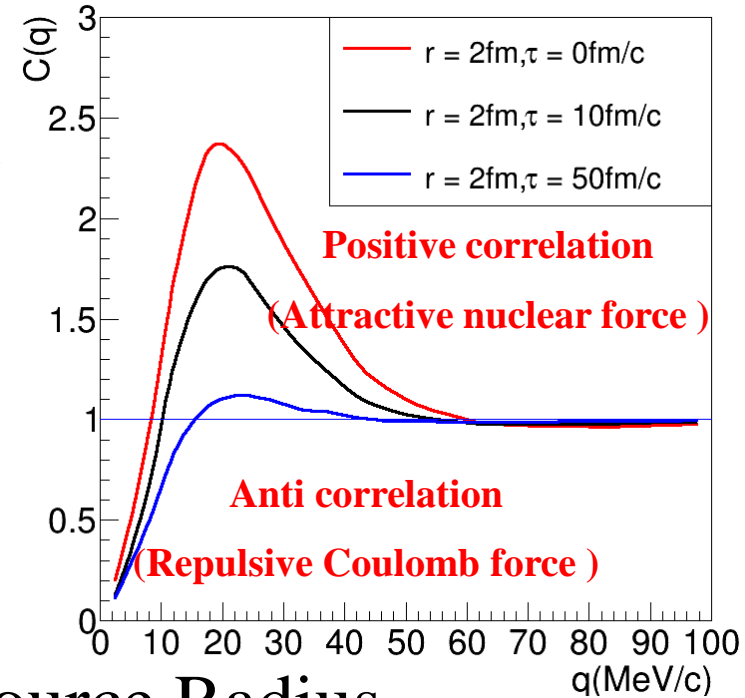


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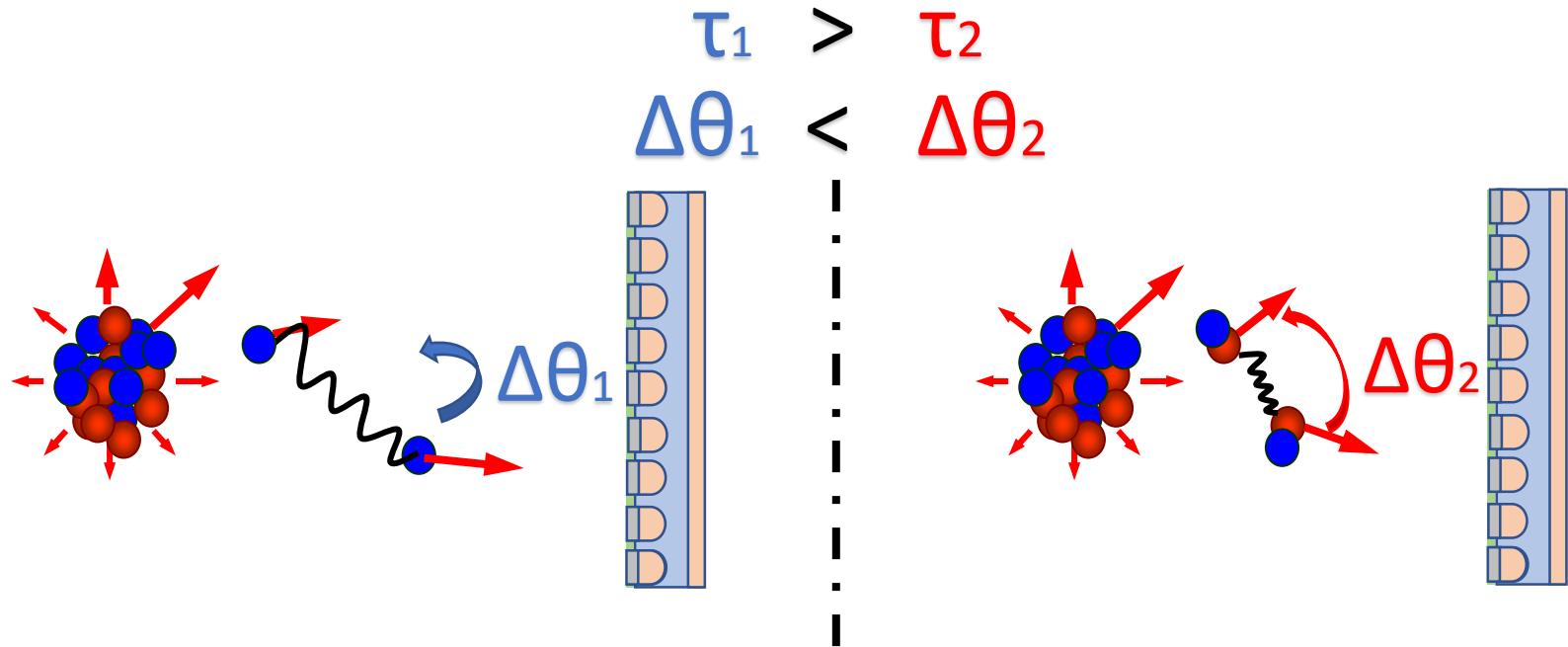
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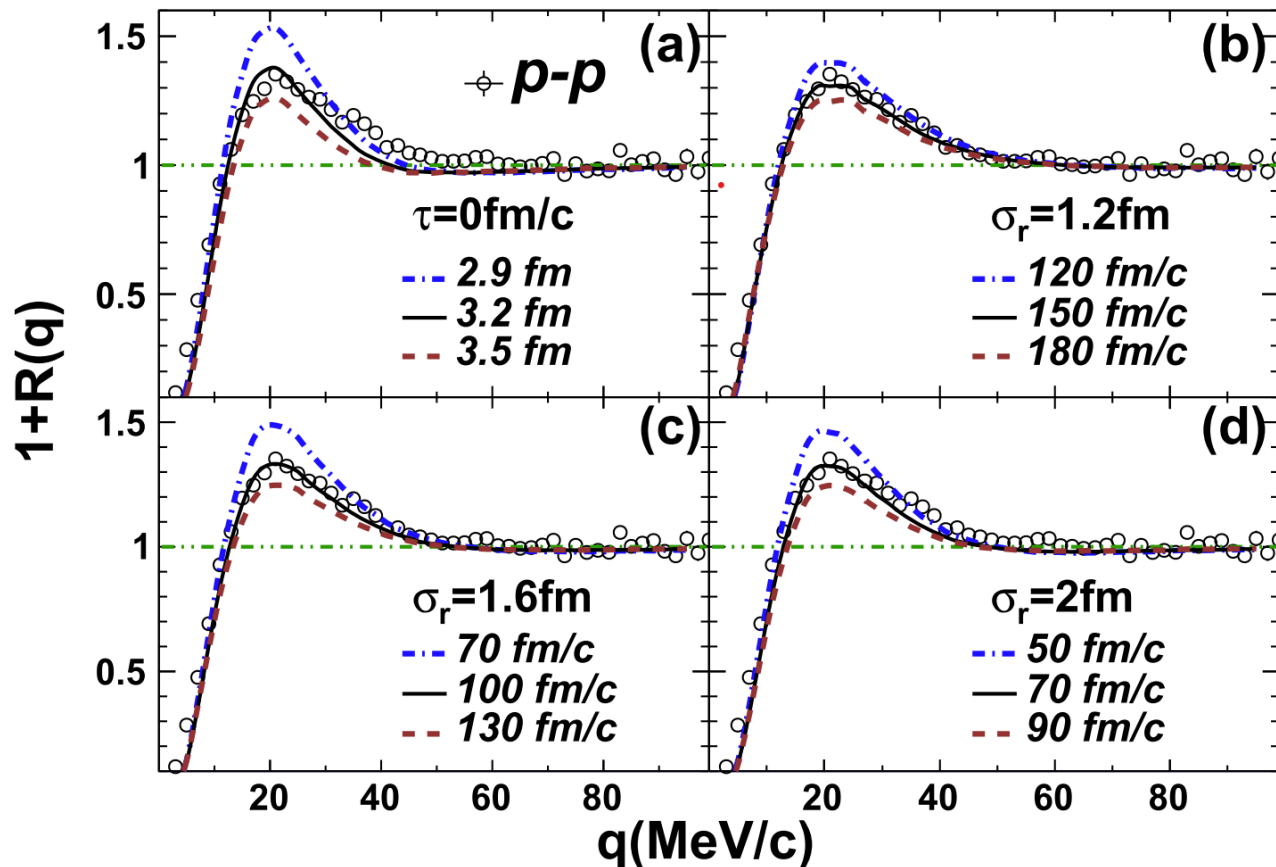


■ Simple understand between HBT and emission timescale



**When the emission timescale is shorter,
the separate angle of two particles will be larger.**

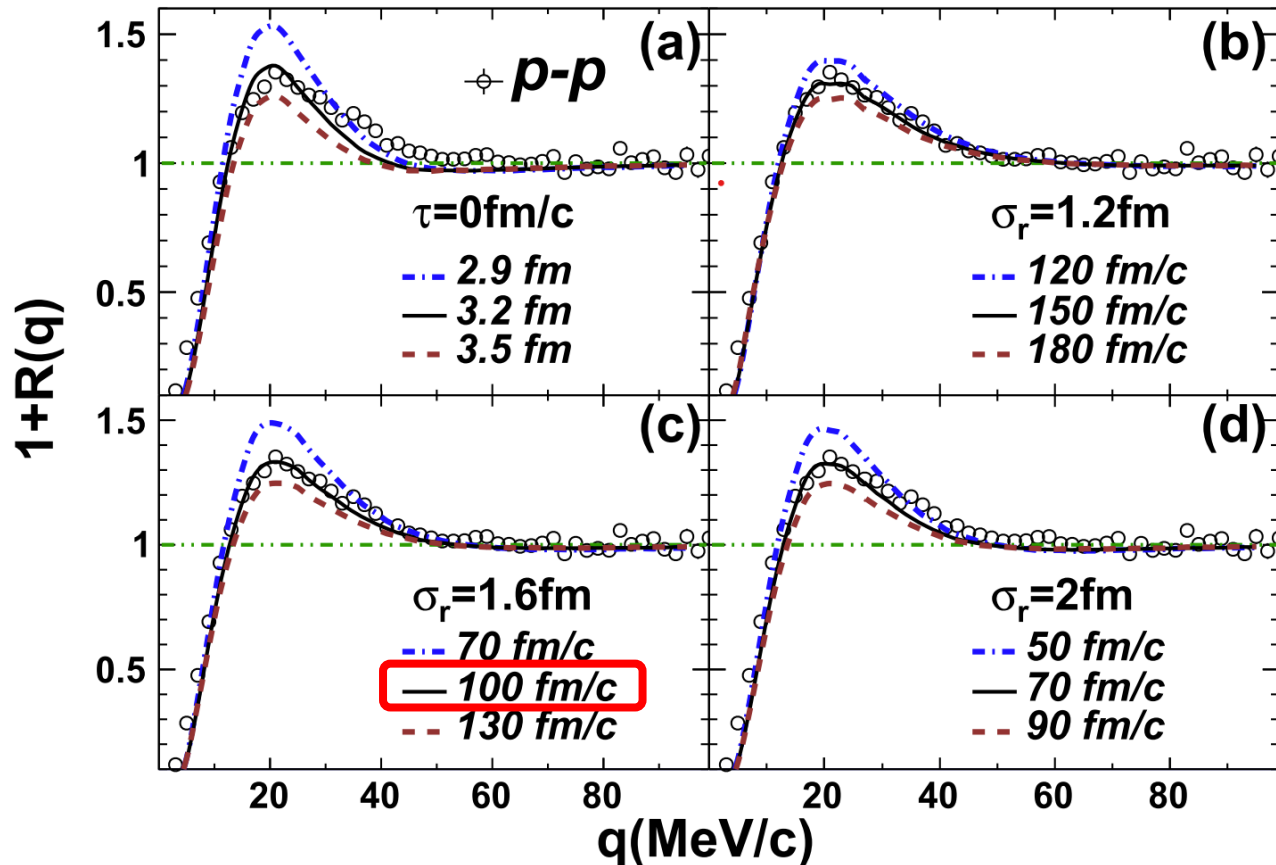
Proton correlation function compared with CRAB calculation:



Physics Letters B, 825, 136856 (2022)

CRAB: S. Pratt, CRAB version 3, <https://web.pa.msu.edu/people/pratts/freecodes/crab/home.html>

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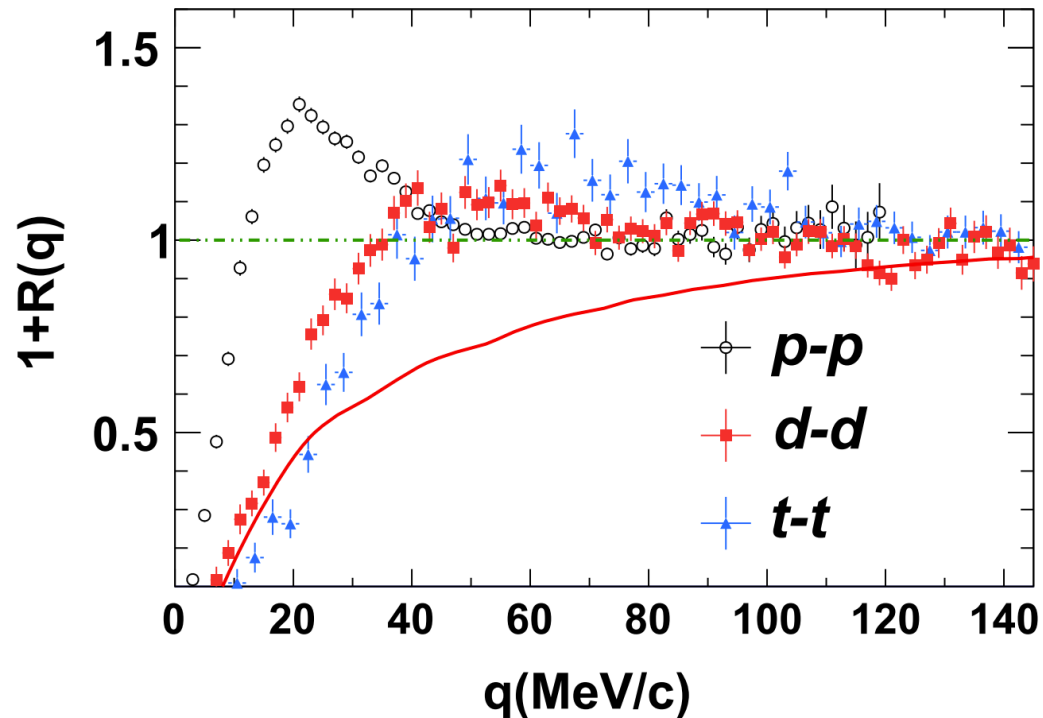


Best fit, Proton emission timescale: $\tau_p \approx 100 \text{ fm/c}$

Physics Letters B, 825, 136856 (2022)

CRAB: S. Pratt, CRAB version 3, <https://web.pa.msu.edu/people/pratts/freecodes/crab/home.html>

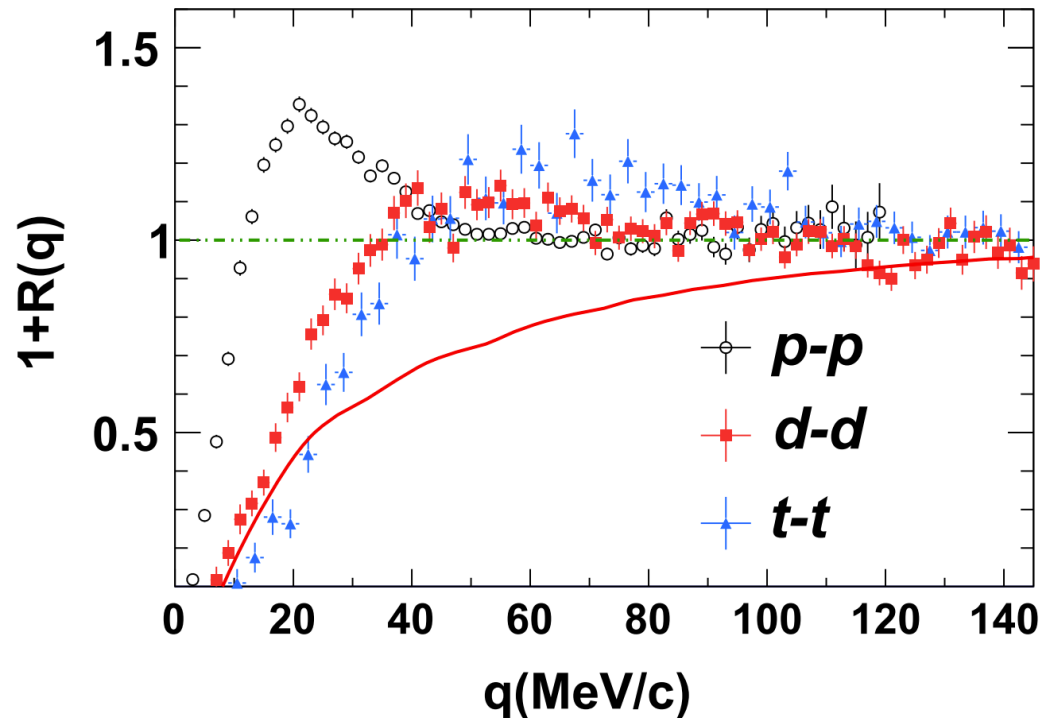
Deuteron-deuteron and triton-triton correlation function:



Physics Letters B, 825, 136856 (2022)

CRAB: S. Pratt, CRAB version 3, <https://web.pa.msu.edu/people/pratts/freecodes/crab/home.html>

Deuteron-deuteron and triton-triton correlation function:

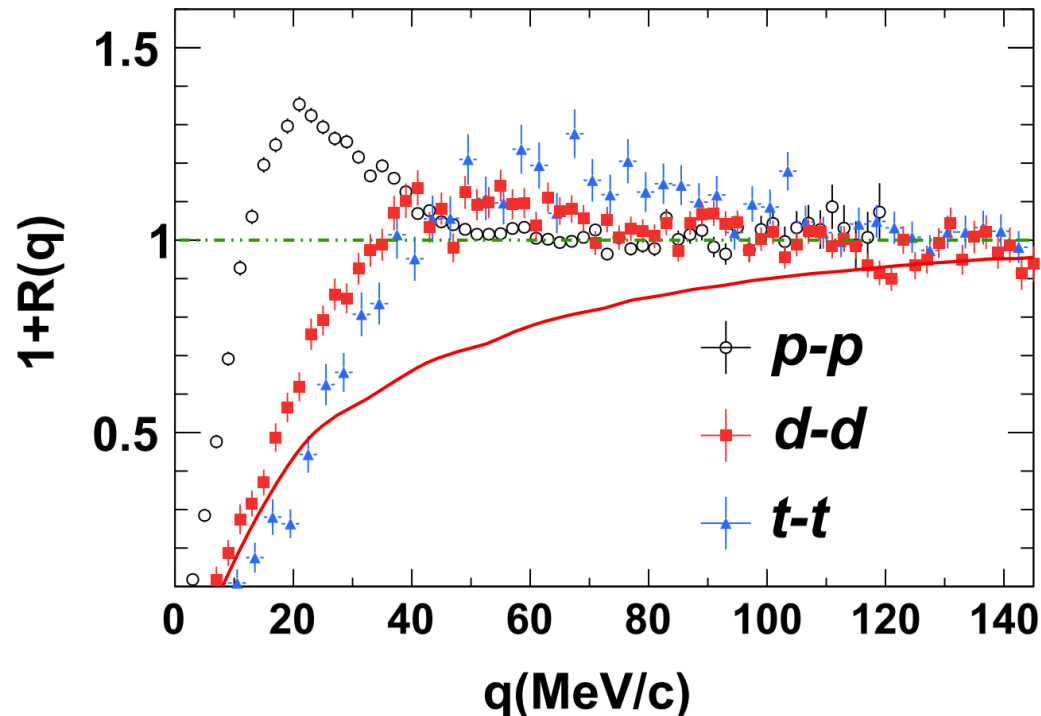


Original plan: Get the p, d, t timescale with CRAB,
and determine the emission order directly.

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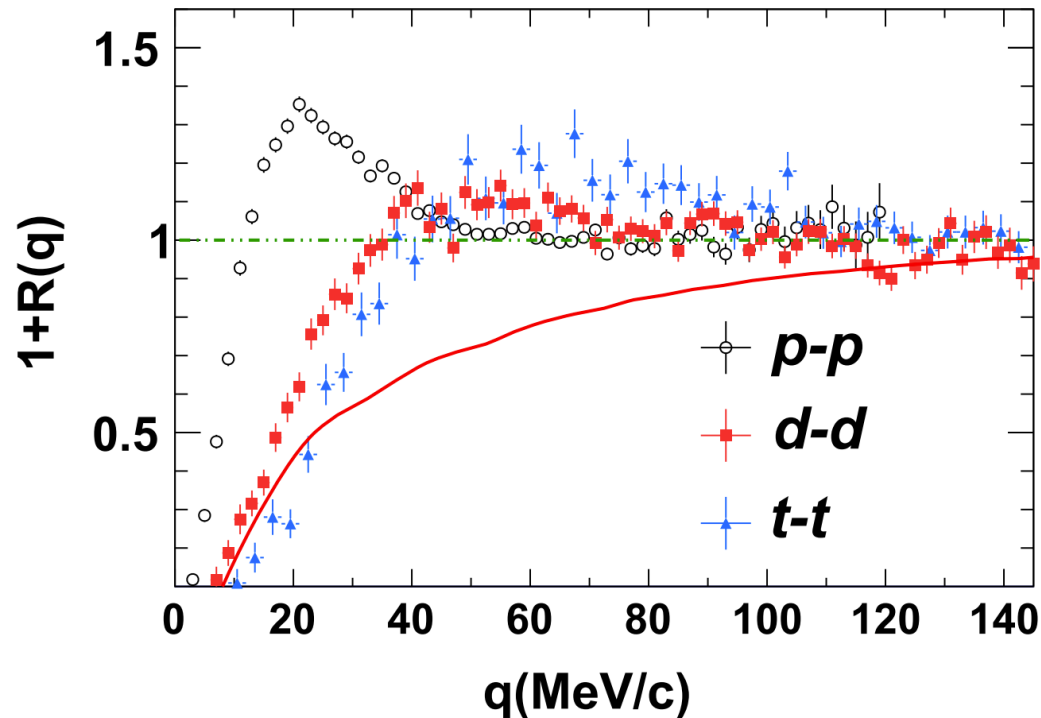
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Situation: With Woods-Saxon potential, CRAB can't reproduce the d - d CF.

Physics Letters B, 825, 136856 (2022)

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Deuteron-deuteron and triton-triton correlation function:



Original plan: Get the p, d, t timescale with CRAB,
and determine the emission order directly.

Situation: With Woods-Saxon potential, CRAB can't reproduce the d - d CF.

Question: How to determine the emission order of p, d, t ?

Physics Letters B, 825, 136856 (2022)

CRAB: S. Pratt, CRAB version 3, <https://web.pa.msu.edu/people/pratts/freecodes/crab/home.html>

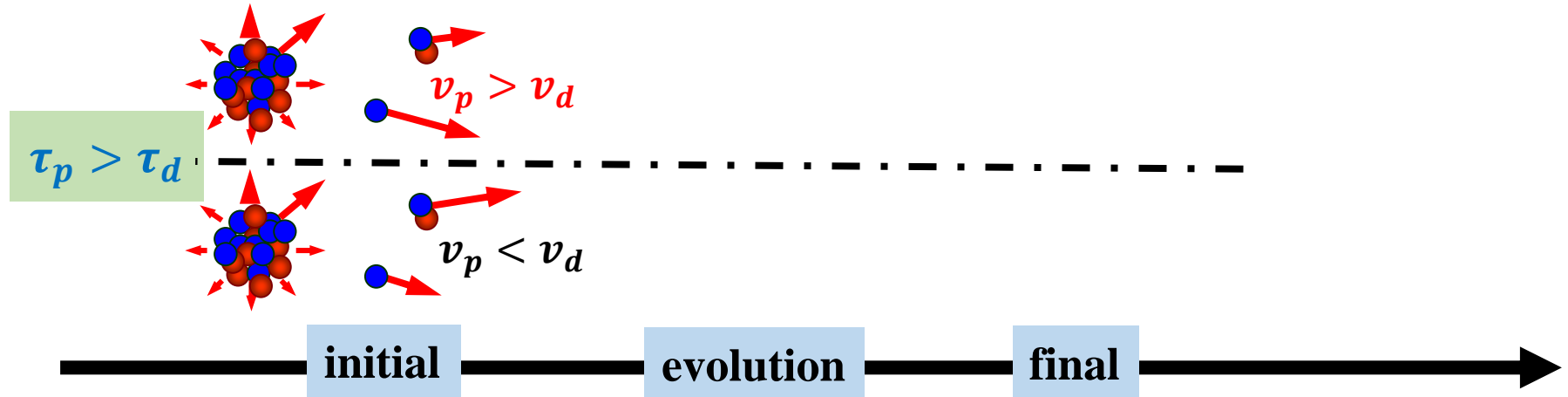
■ Particle emission order

Velocity-gated correlation function method [*PhysRevLett.91.092701*
PhysRevC.35.1695]

■ Particle emission order

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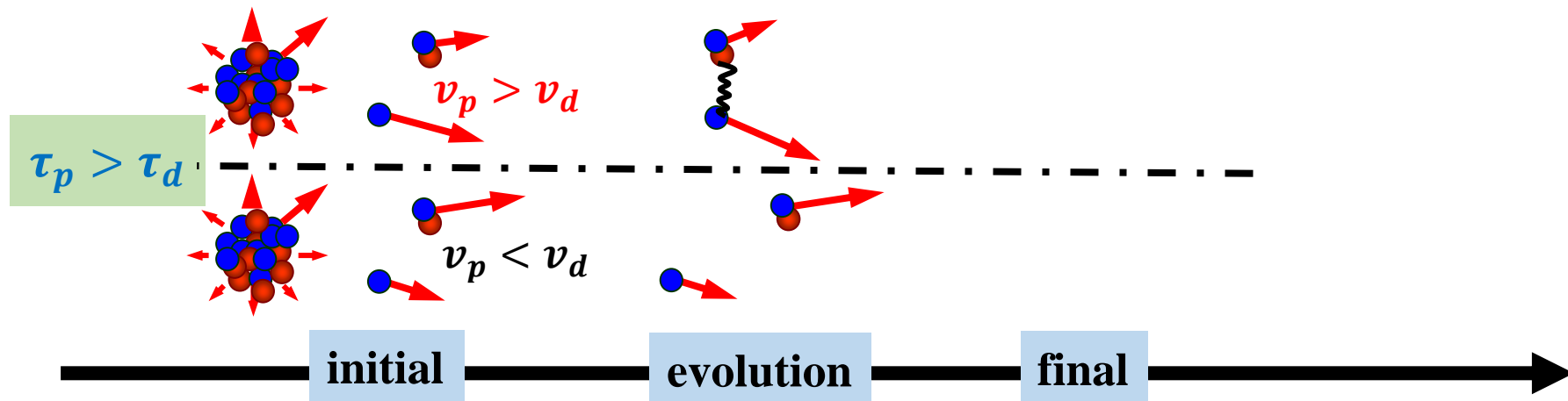
Taking proton and deuteron as example:



■ Particle emission order

Velocity-gated correlation function method [*PhysRevLett.91.092701*]
[*PhysRevC.35.1695*]

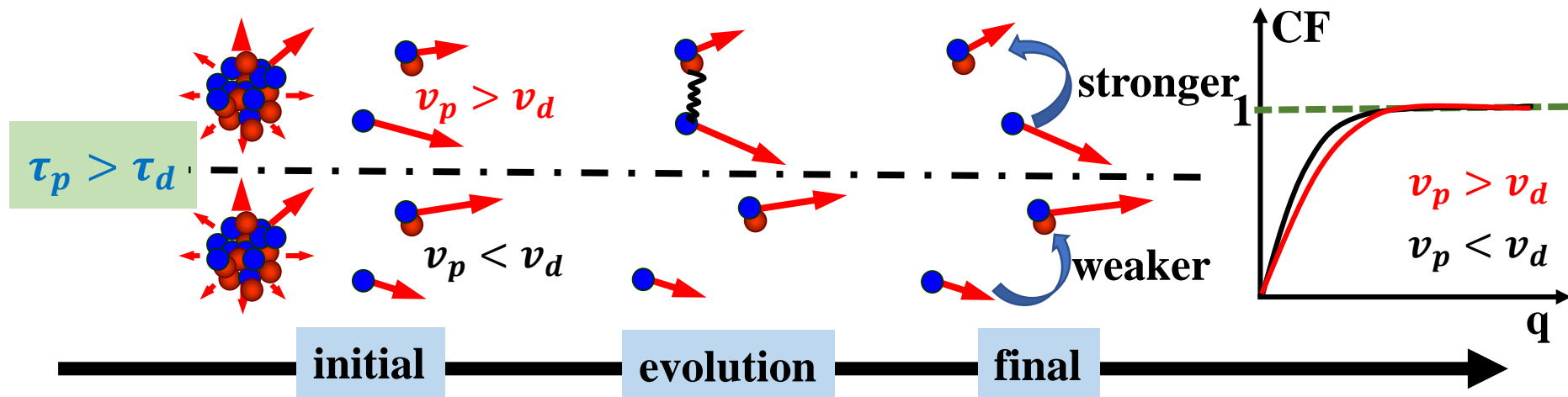
Taking proton and deuteron as example:



Particle emission order

Velocity-gated correlation function method [*PhysRevLett.91.092701*]
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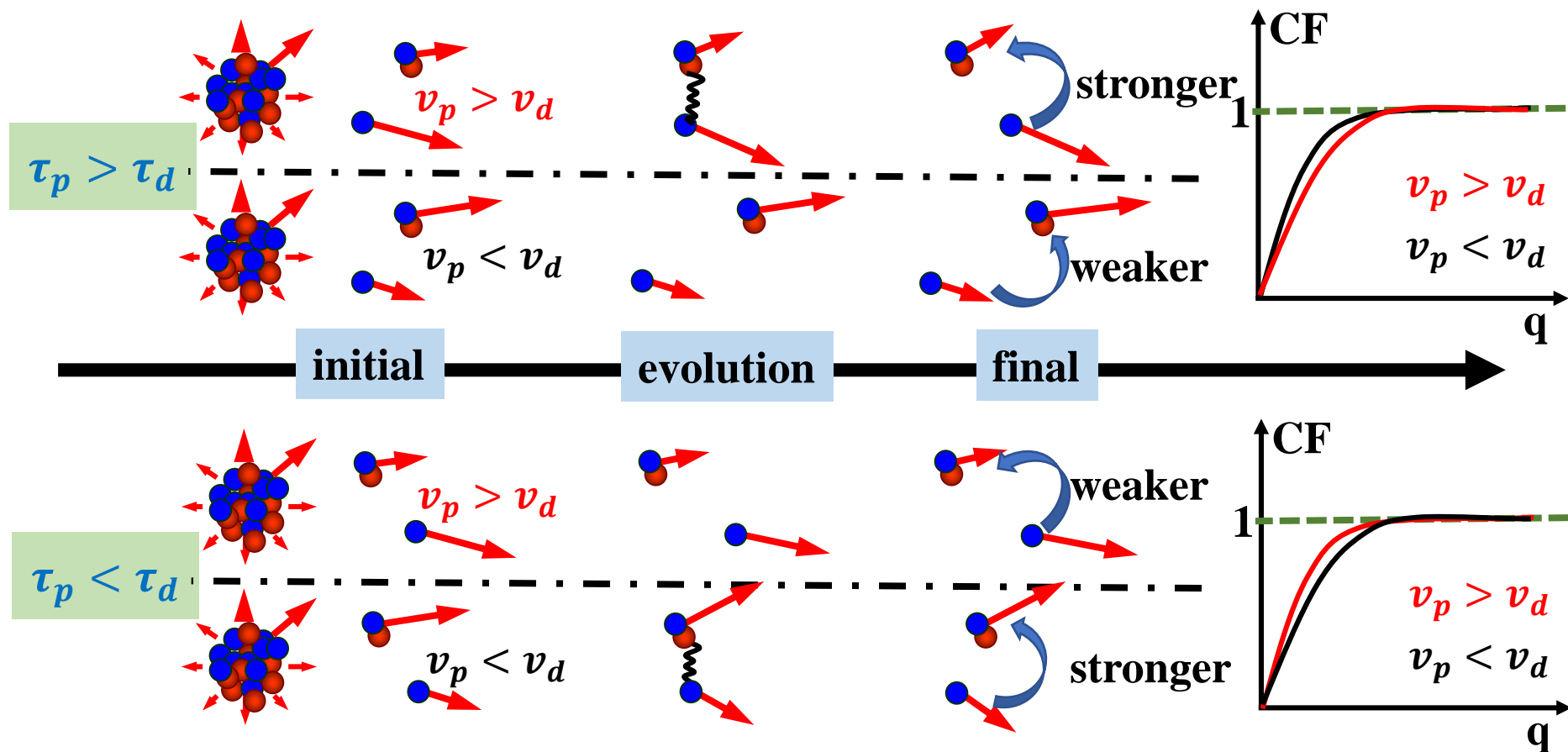
Taking proton and deuteron as example:



Particle emission order

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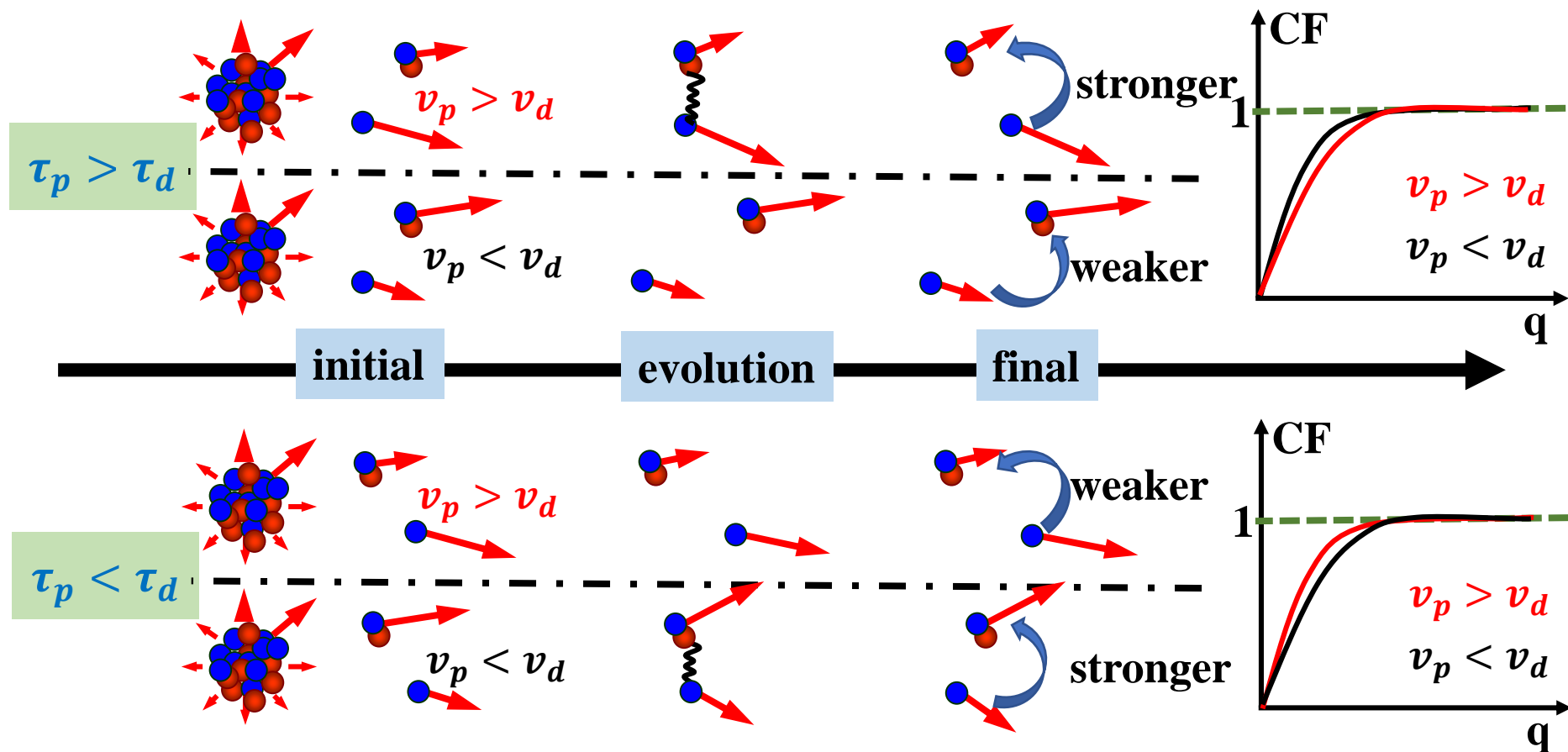
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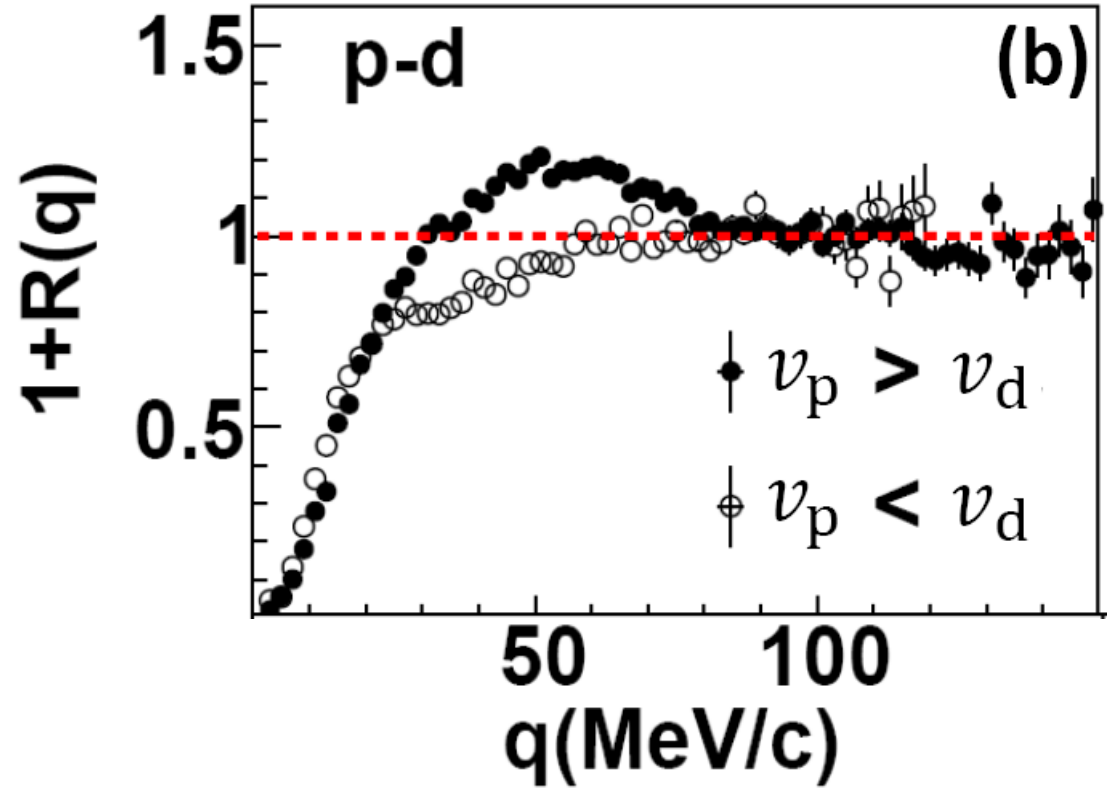
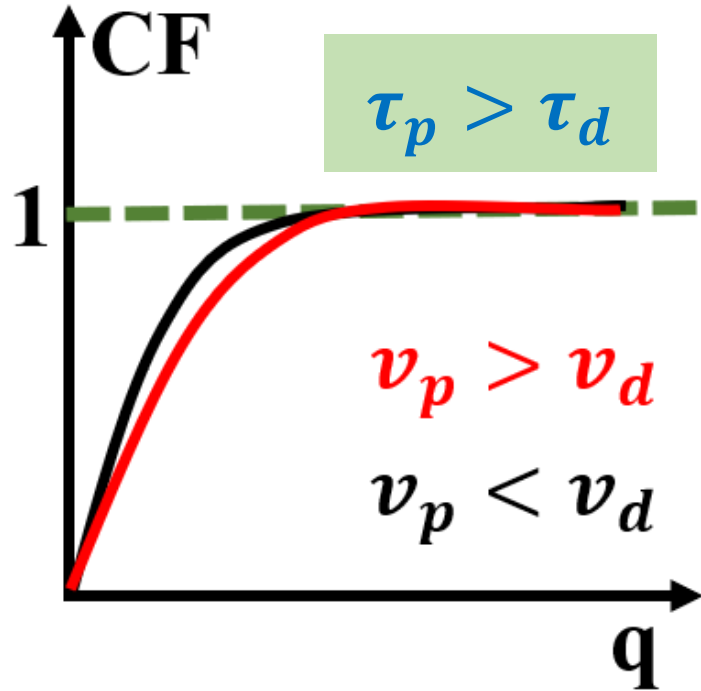
Particle emission order

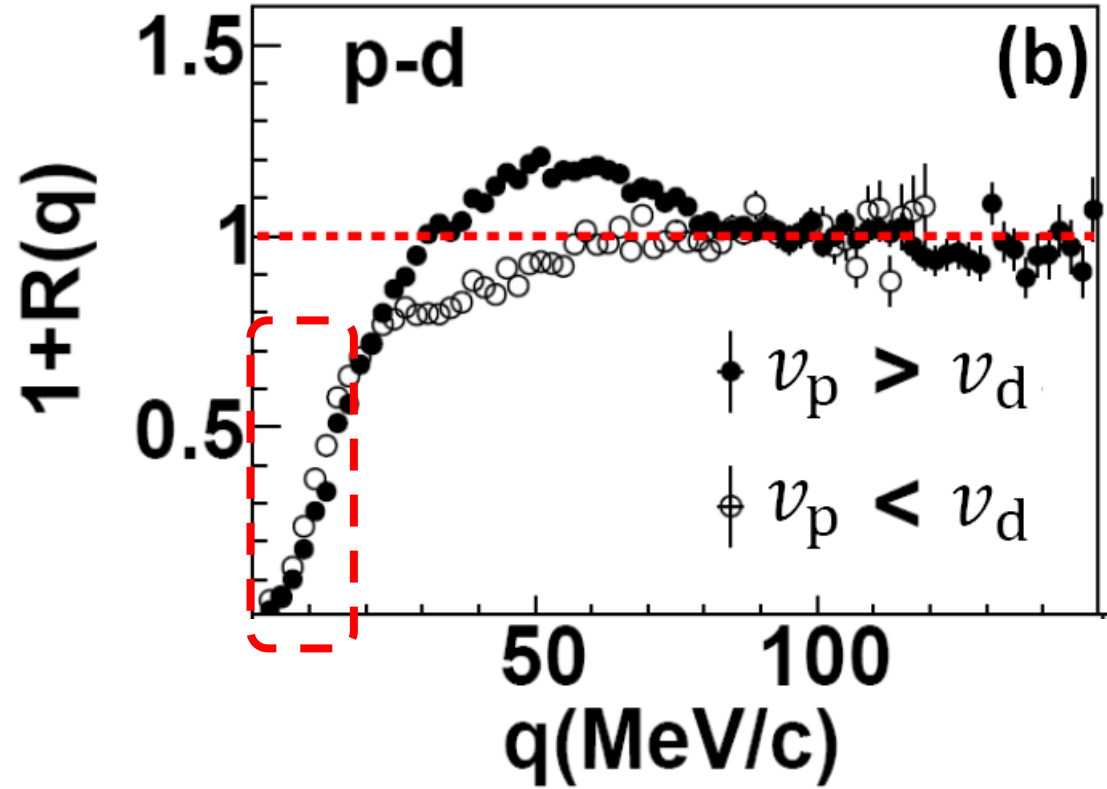
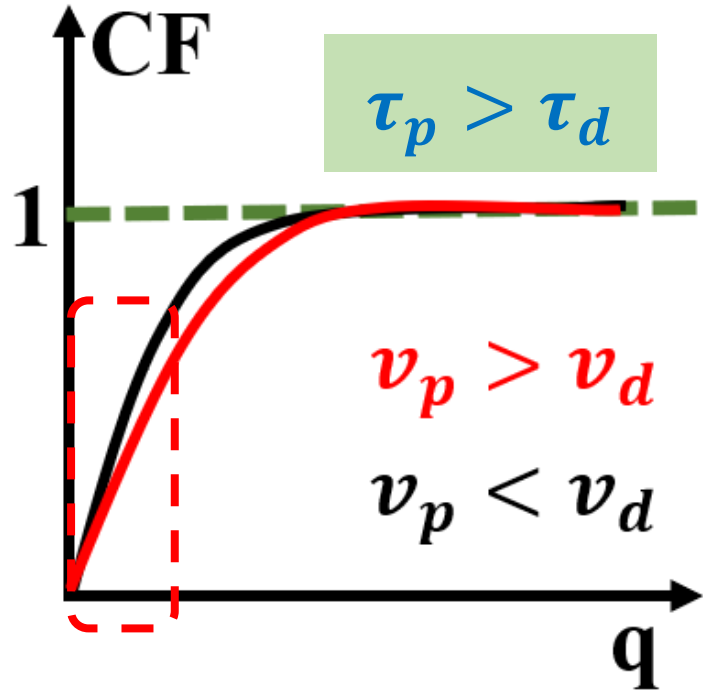
Velocity-gated correlation function method [*PhysRevLett.91.092701*] [*PhysRevC.35.1695*]

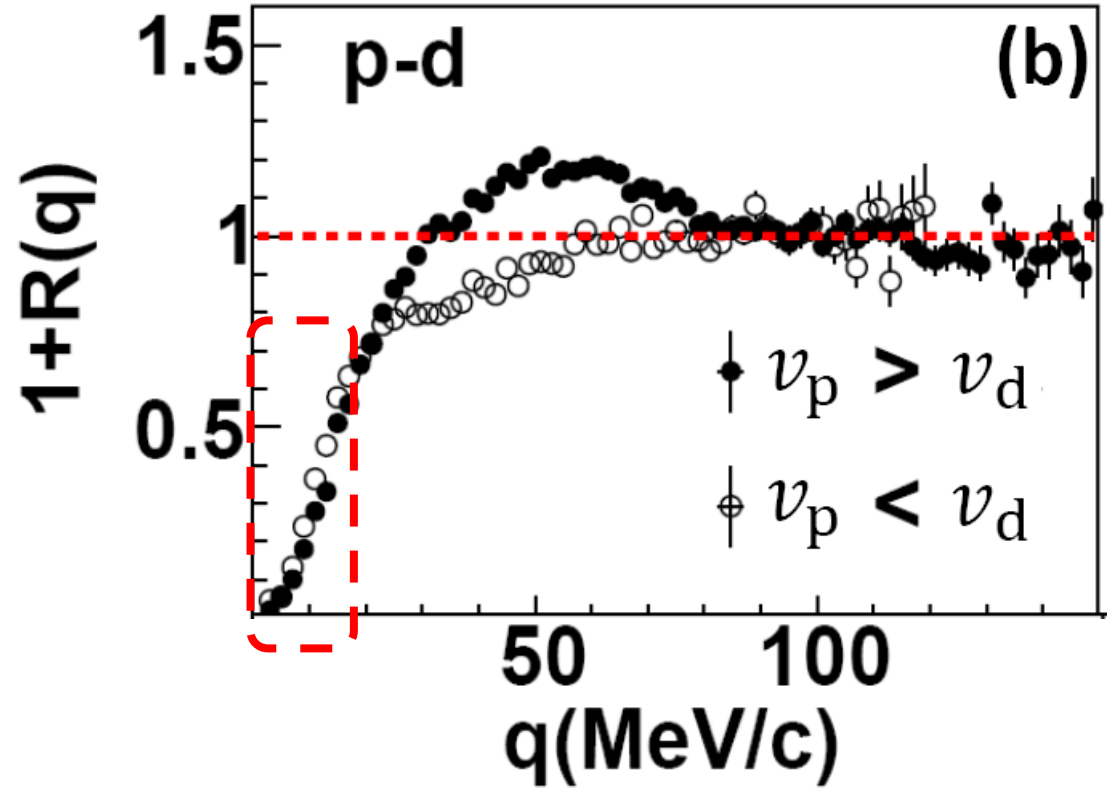
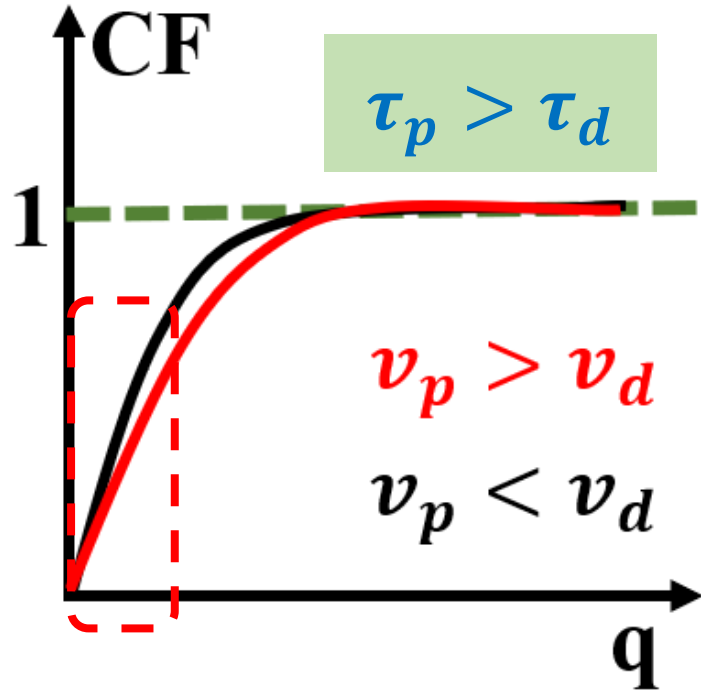
Taking proton and deuteron as example:



Particle with higher velocity showing strong anti-correlation means this particle is emitted later!



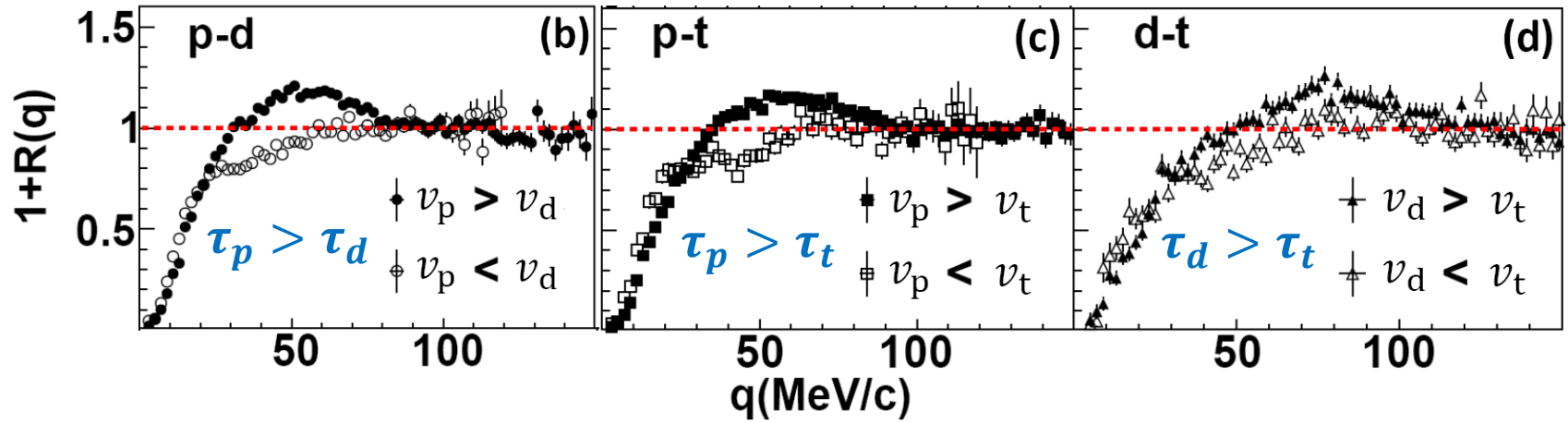


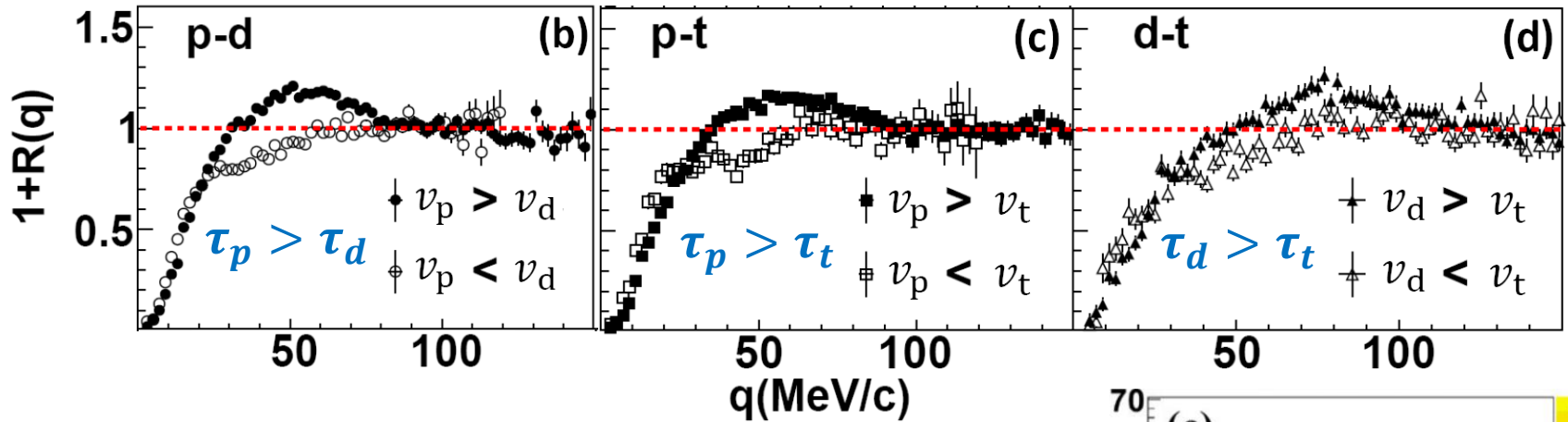


Deuteron is emitted earlier than proton! $\tau_p > \tau_d$

Particle emission order

$^{40}\text{Ar}@30\text{MeV/u} + ^{197}\text{Au}$

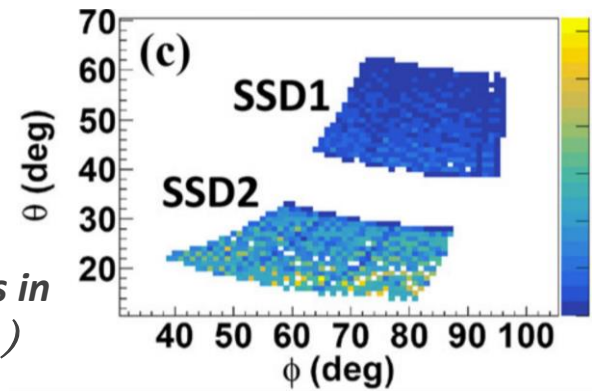


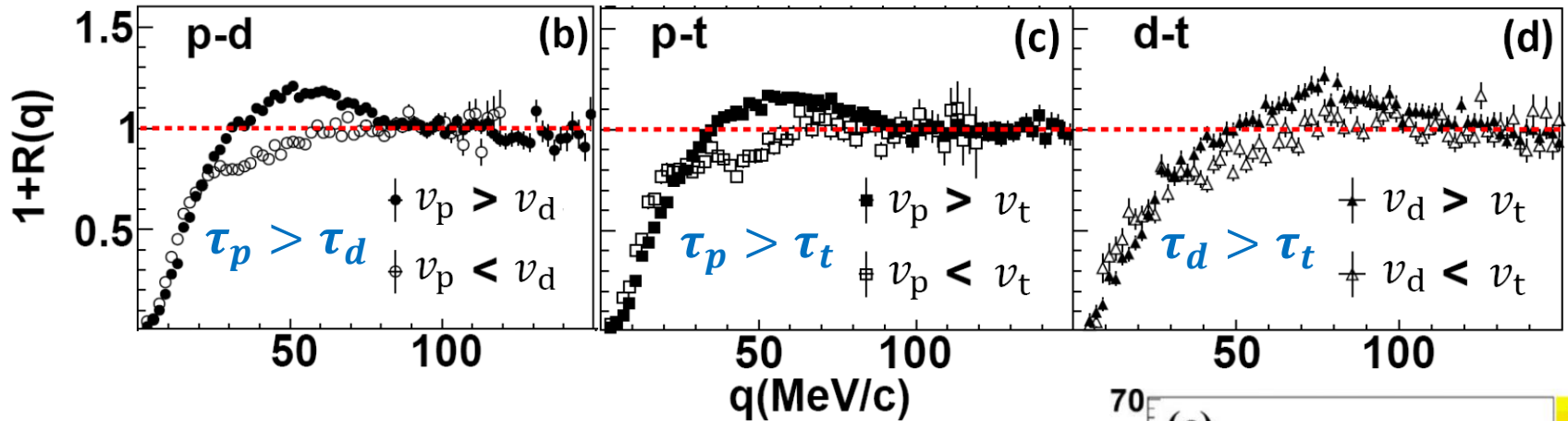


$$\tau_p > \tau_d > \tau_t$$

Neutron rich particles emitted earlier !

The Emission Order of Hydrogen Isotopes via Correlation Functions in 30 MeV/u Ar+Au Reactions (Physics Letters B, 825, 136856 (2022))

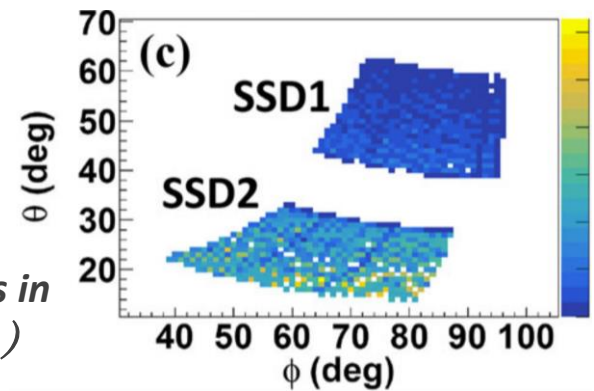




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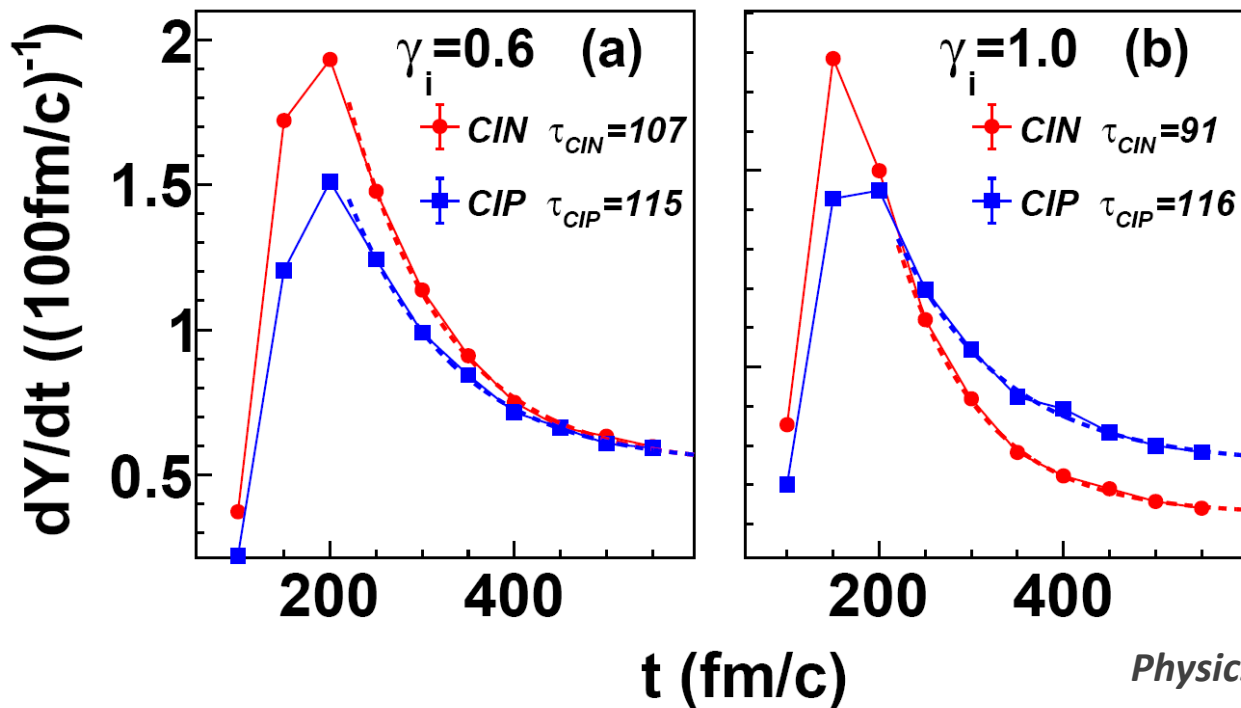


Consistent with the results of R. Ghetti et al[*PhysRevLett.91,092701.*].

Dynamic emission order in $61\text{MeV/u } ^{36}\text{Ar} + ^{27}\text{Al}$:

$$\tau_p > \tau_d > \tau_n$$

ImQMD calculation results of particle emission timescale

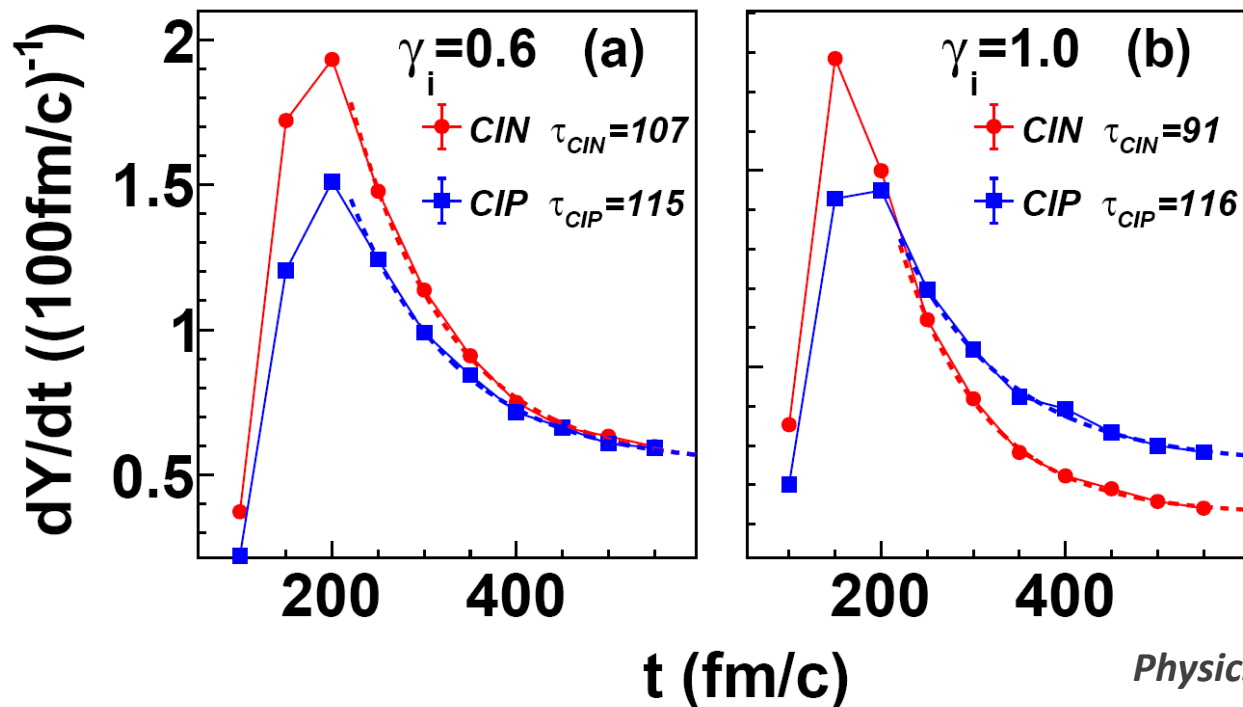


CIN: Coalescence
Invariant Neutron

CIP: Coalescence
Invariant Proton

Physics Letters B, 825, 136856 (2022)

ImQMD calculation results of particle emission timescale



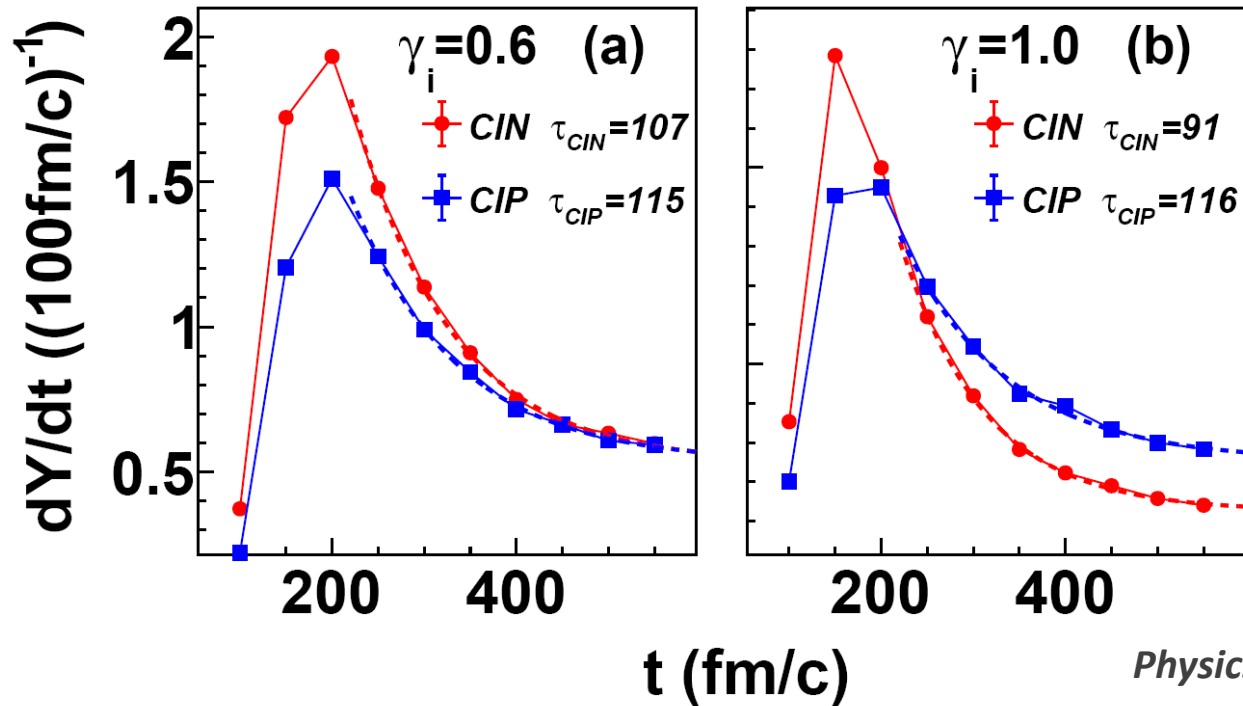
CIN: Coalescence
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Physics Letters B, 825, 136856 (2022)

$(\tau_{CIP} - \tau_{CIN})_{\gamma_i=1.0}$ is larger than $(\gamma_i=0.6)$, showing dependence on $E_{\text{sym}}(\rho)$

ImQMD calculation results of particle emission timescale



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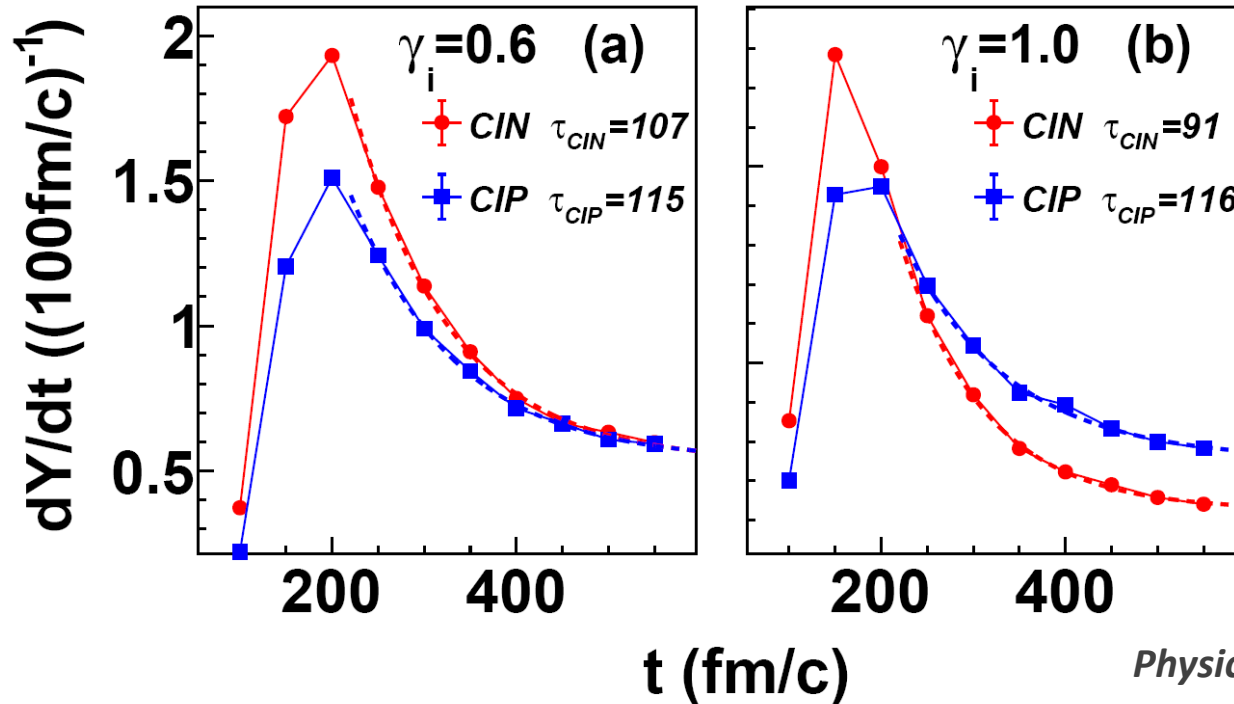
CIP: Coalescence
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Physics Letters B, 825, 136856 (2022)

$(\tau_{CIP} - \tau_{CIN})_{\gamma_i=1.0}$ is larger than $(\gamma_i=0.6)$, showing dependence on $E_{\text{sym}}(\rho)$

A new way to study $E_{\text{sym}}(\rho)$ and isospin dynamics

ImQMD calculation results of particle emission timescale



CIN: Coalescence Invariant Neutron

CIP: Coalescence Invariant Proton

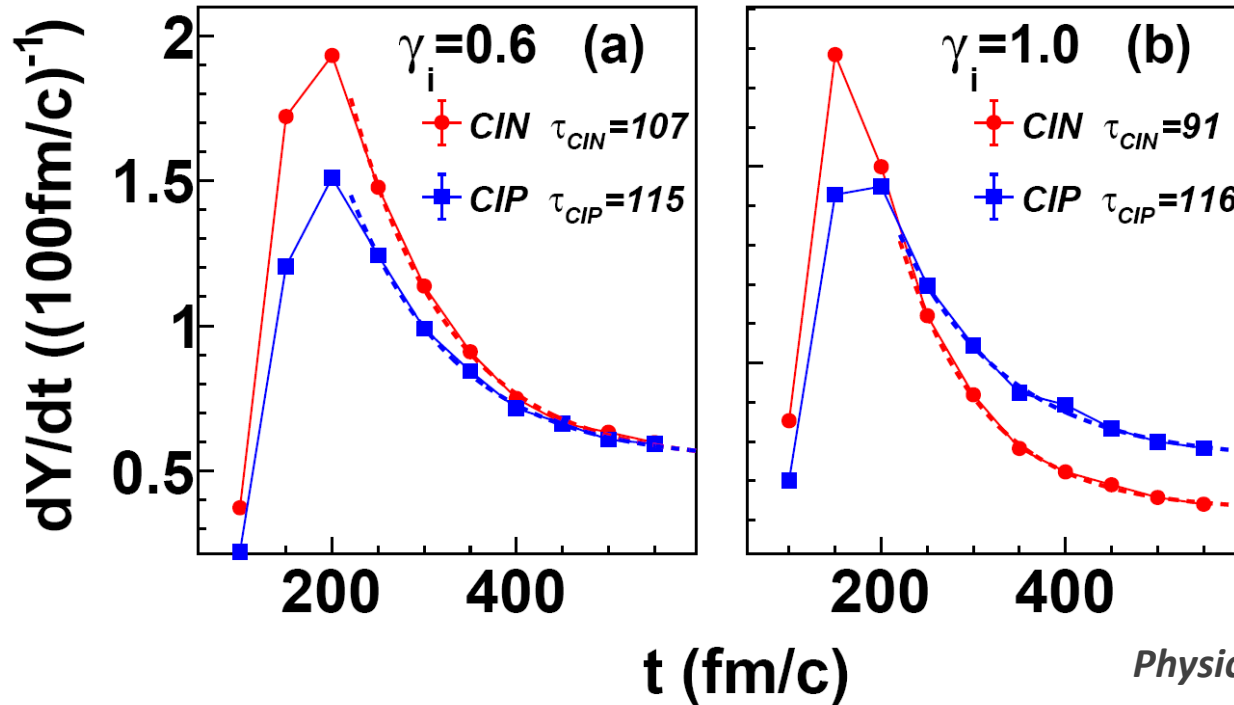
Physics Letters B, 825, 136856 (2022)

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A new way to study $E_{\text{sym}}(\rho)$ and isospin dynamics

Further Question: Coupling between isospin dynamics and **light particle formation?**

ImQMD calculation results of particle emission timescale



CIN: Coalescence Invariant Neutron

CIP: Coalescence Invariant Proton

Physics Letters B, 825, 136856 (2022)

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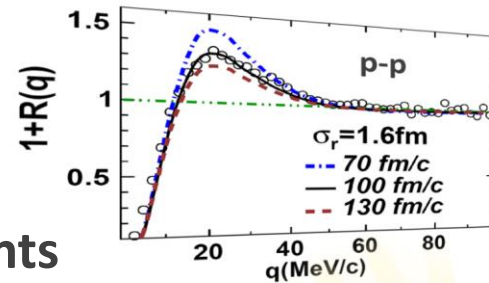
A new way to study $E_{\text{sym}}(\rho)$ and isospin dynamics

Further Question: Coupling between isospin dynamics and **light particle formation?**

Observing the ping-pong modality of the isospin degree of freedom in cluster emission from heavy-ion reactions (Physical Review C 107, L041601 (2023))

Summary

① CSHINE system,
HIRs in RIBLL1, IMP, Lanzhou, China
HBT correlation function measurements



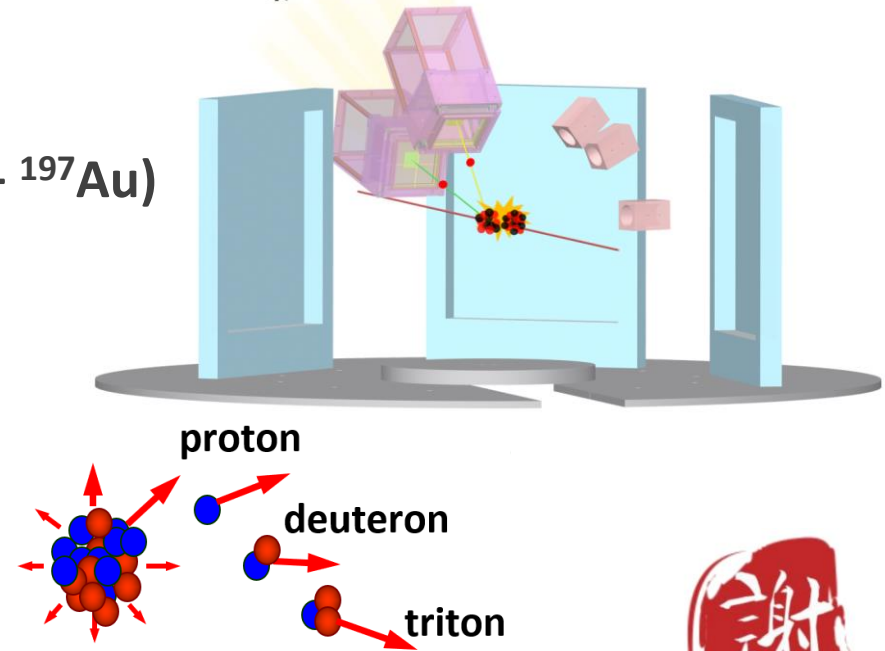
② Isospin chronology ($^{40}\text{Ar}@30\text{MeV/u} + ^{197}\text{Au}$)
Proton **emission timescale**:

$$\tau_p \approx 100\text{fm}/c$$

Emission order of hydrogen isotopes:

$$\tau_p > \tau_d > \tau_t$$

Neutron rich particle emitted earlier



③ Future plan: a, n-n HBT correlation; b, t and ^3He emission
c, $\theta(n/p)$ distribution; d, Resonance decay

...

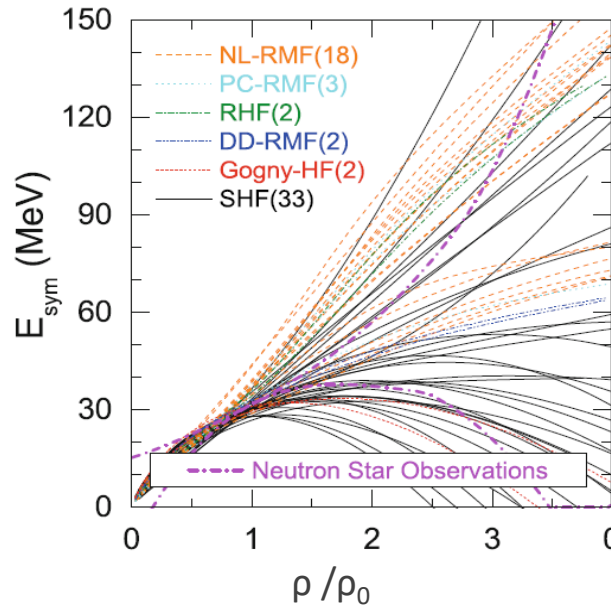


■ backup



■ Current situation of **E_{sym}**

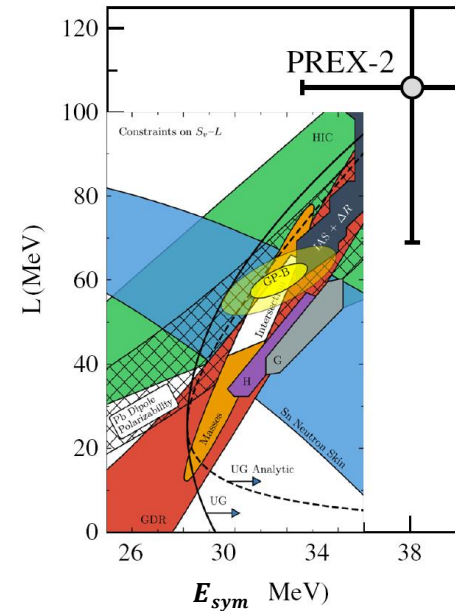
B.A.Li et. al. Eur. Phys. J. A (2019) 55: 117



$$E_{sym}(\rho_0) = 31.6 \pm 2.7 \text{ MeV}$$

$$L(\rho_0) = 58.9 \pm 16 \text{ MeV}$$

PRL 126, 172503 (2021) neutron skin



$$E_{sym}(\rho_0) = 38.1 \pm 4.7 \text{ MeV}$$

$$L(\rho_0) = 106 \pm 37 \text{ MeV}$$

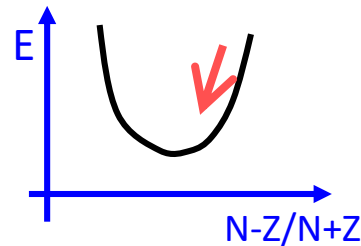
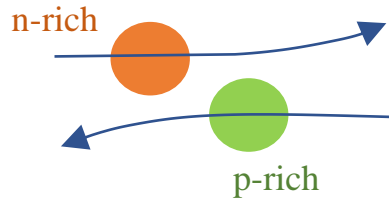
How Esym influence Heavy ion reaction(HIR) process?

Eur. Phys. J. A (2014) 50: 36

1. Isospin Diffusion:

$$j_{np} = j_n^I - j_p^I = -(D_n^I - D_p^I) \nabla I$$

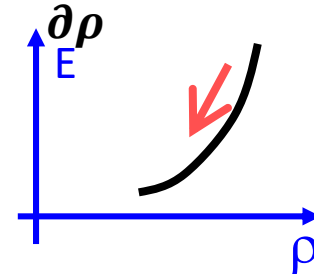
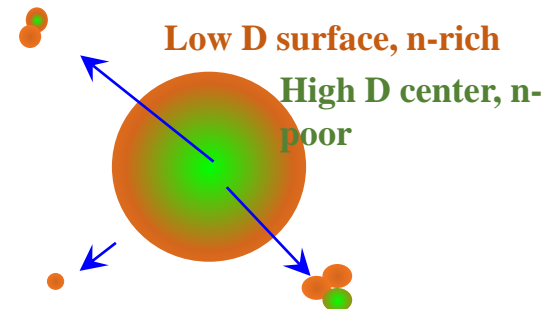
$$D_n^I - D_p^I \propto 4\rho E_{sym}(\rho)$$



2. Isospin Drift:

$$j_{np} = j_n^\rho - j_p^\rho = (D_n^\rho - D_p^\rho) \nabla \rho$$

$$D_n^\rho - D_p^\rho \propto 4I \frac{\partial E_{sym}(\rho)}{\partial \rho}$$



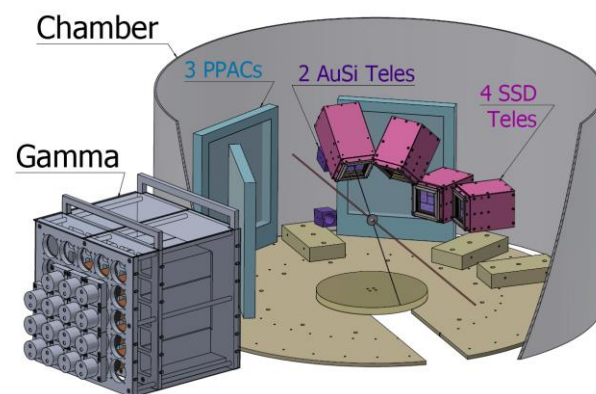
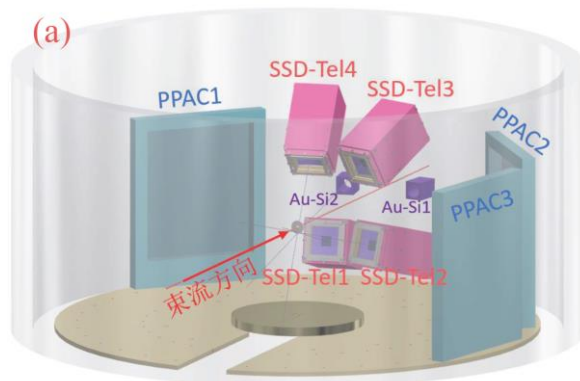
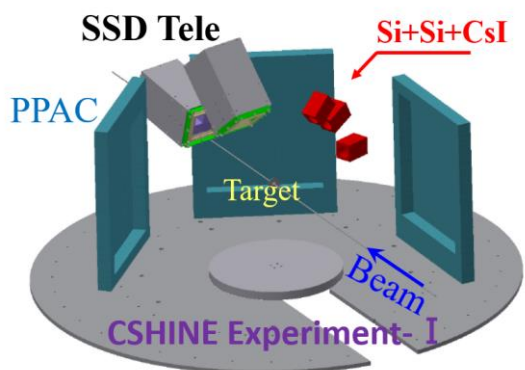
Experiments on CSHINE

At RIBLL1, HIRFL, IMP, Lanzhou

2018, $^{40}\text{Ar}@30\text{MeV/u} + ^{197}\text{Au}$
2*SSDT + 3*PPAC

2019, $^{86}\text{Kr}@25\text{MeV/u} + ^{208}\text{Pb}$
4*SSDT + 3*PPAC

2022, $^{86}\text{Kr}@25\text{MeV/u} + ^{124}\text{Sn}$
4*SSDT + 3*PPAC + Gamma array

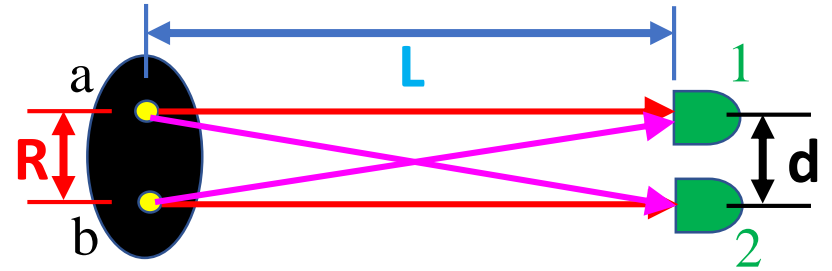


■ HBT principle (Light source)

- light emitted from source as spherical wave

$$A = \alpha e^{ik|\vec{r}-\vec{r}_a|+i\varphi_a}/|\vec{r}-\vec{r}_a|$$

$$I = A^2$$



- Two-point correlation function definition

$$C(\vec{d}, k_1, k_2) = \frac{\langle I_1 I_2 \rangle}{\langle I_1 \rangle \langle I_2 \rangle} = 1 + 2 \frac{\langle \alpha^2 \rangle \langle \beta^2 \rangle}{(\alpha^2 + \beta^2)^2} \cos \left((\vec{k}_2 - \vec{k}_1) \cdot \vec{R} \right)$$

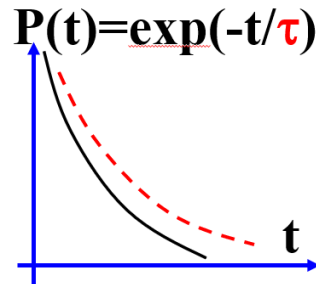
- Continuous source correlation function (Fourier transform of the density distribution of source)

$$C(\vec{d}, k_1, k_2) - 1 = \left| \int \rho(r) e^{i(\vec{k}_1 - \vec{k}_2) \cdot \vec{r}} d^3 r \right|^2$$

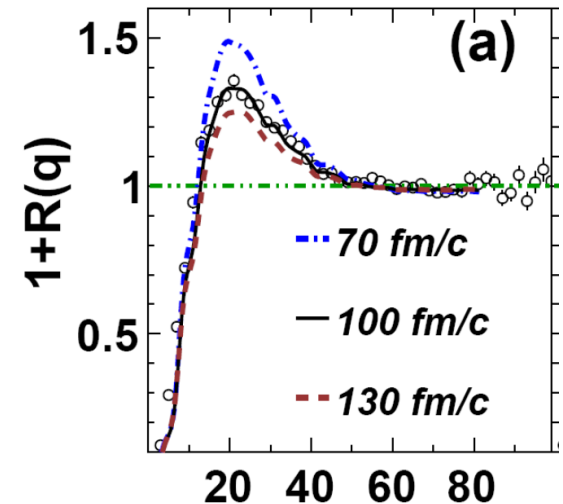
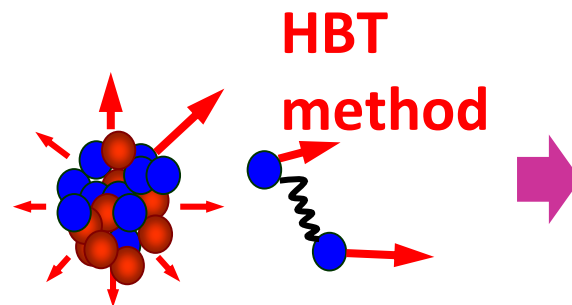
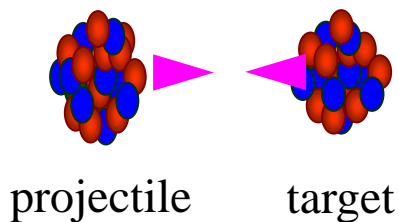
■ Physics result1: Isospin chronology

- ✿ What's the relationship between **emission timescale** and $E_{\text{sym}}(\rho)$?
More stiffer $E_{\text{sym}}(\rho)$, more neutron-rich particles easier emission!

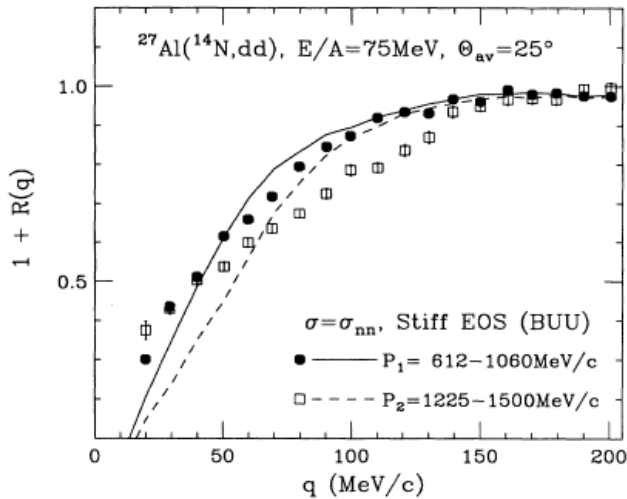
✿ Emission timescale τ



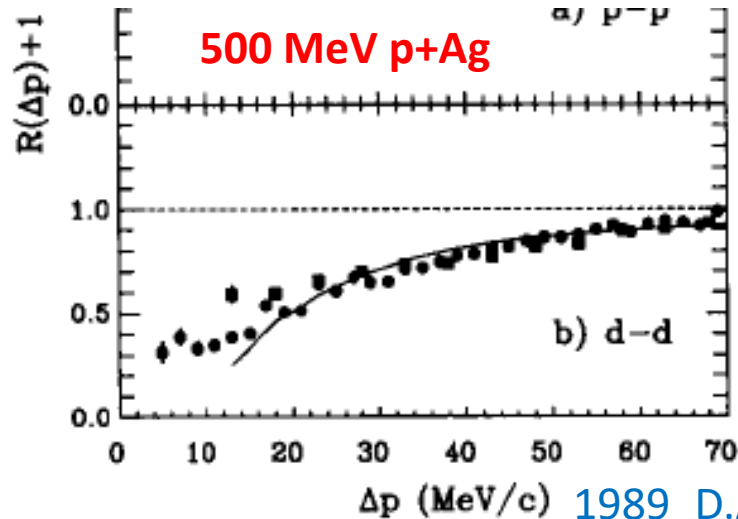
Heavy Ion Reaction



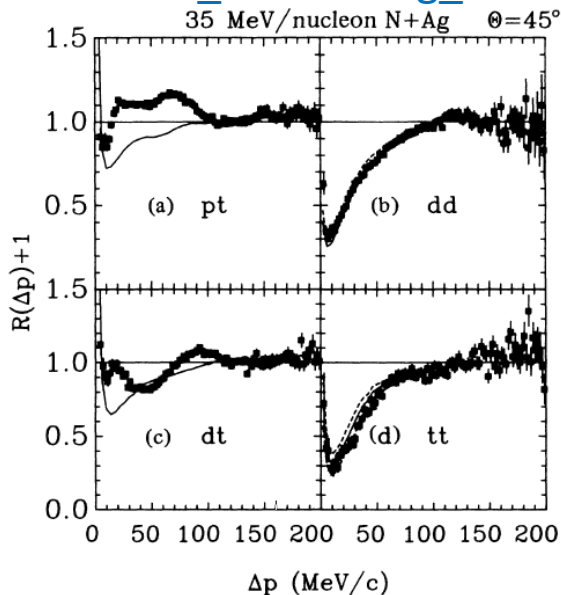
Deuteron-deuteron correlation function



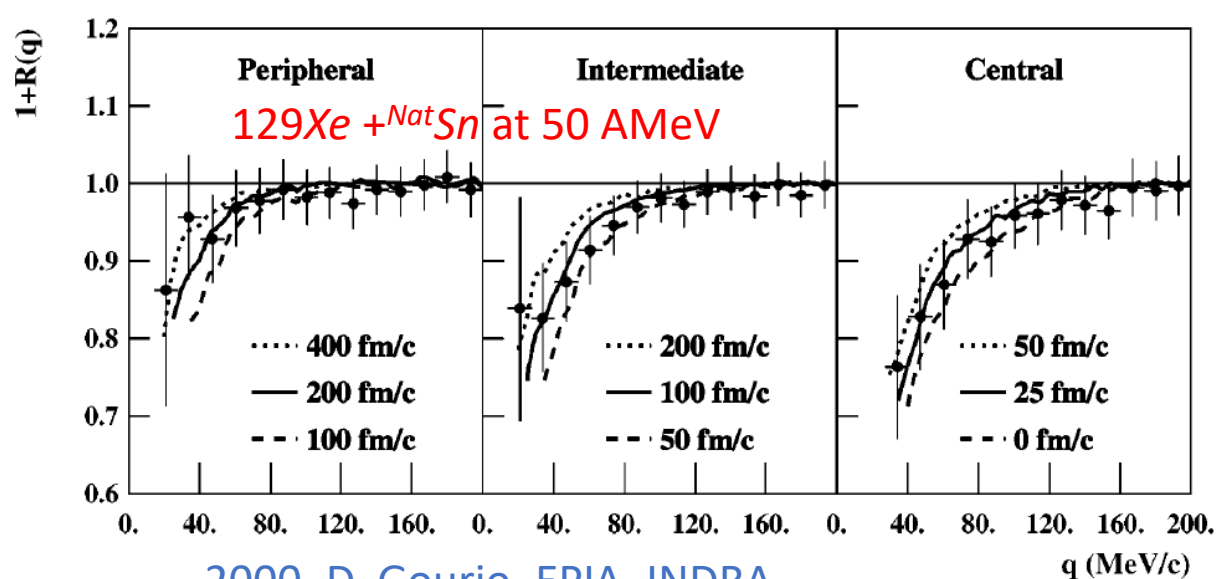
1993_W. G. Gong_PRC



1989_D.A. CEBRA_MSU_PLB



1988_D. Fox_MSU_PRC



2000_D. Gourio_EPJA_INDRA

Deuteron-deuteron correlation function

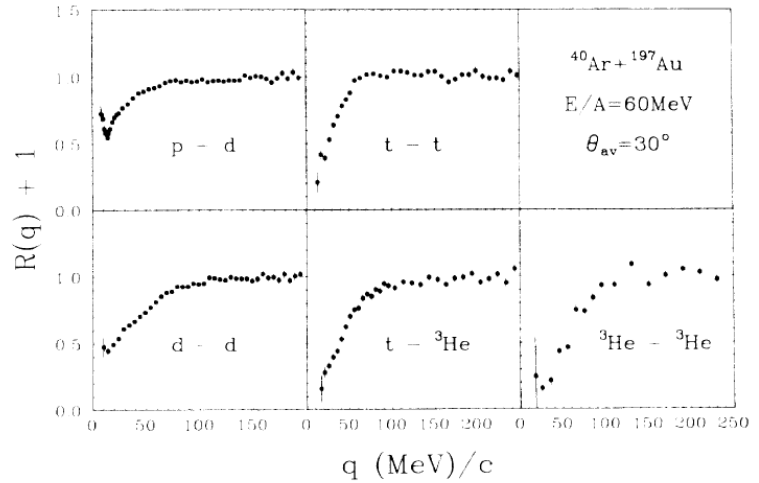
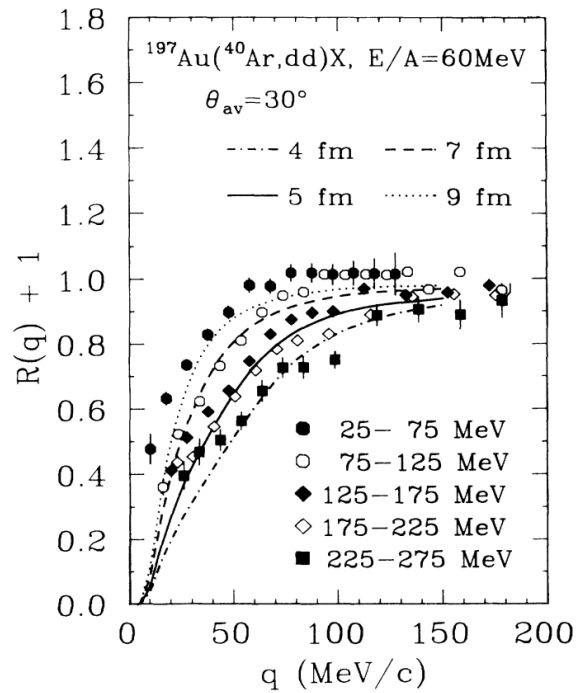
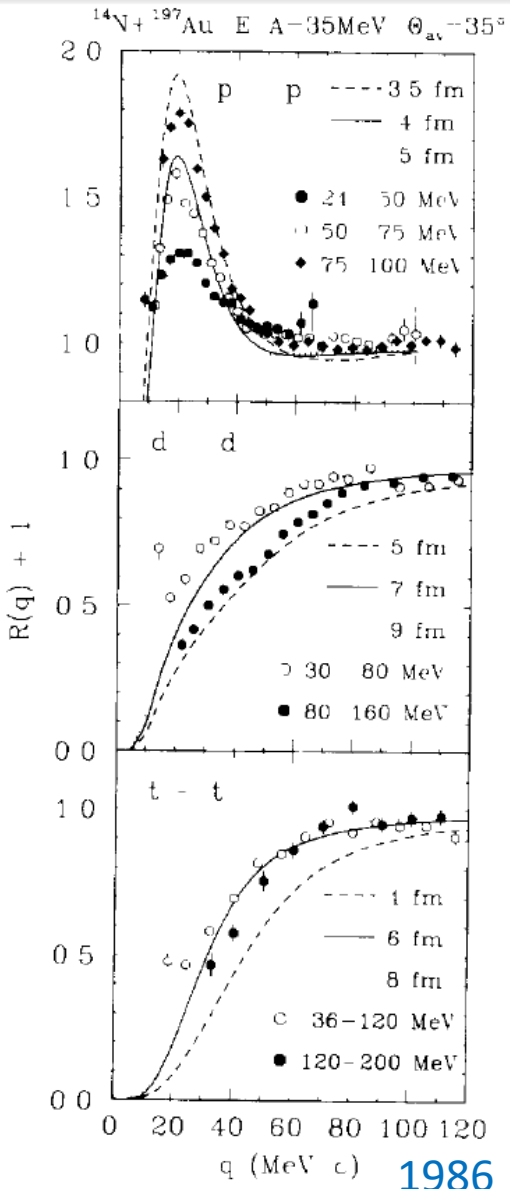
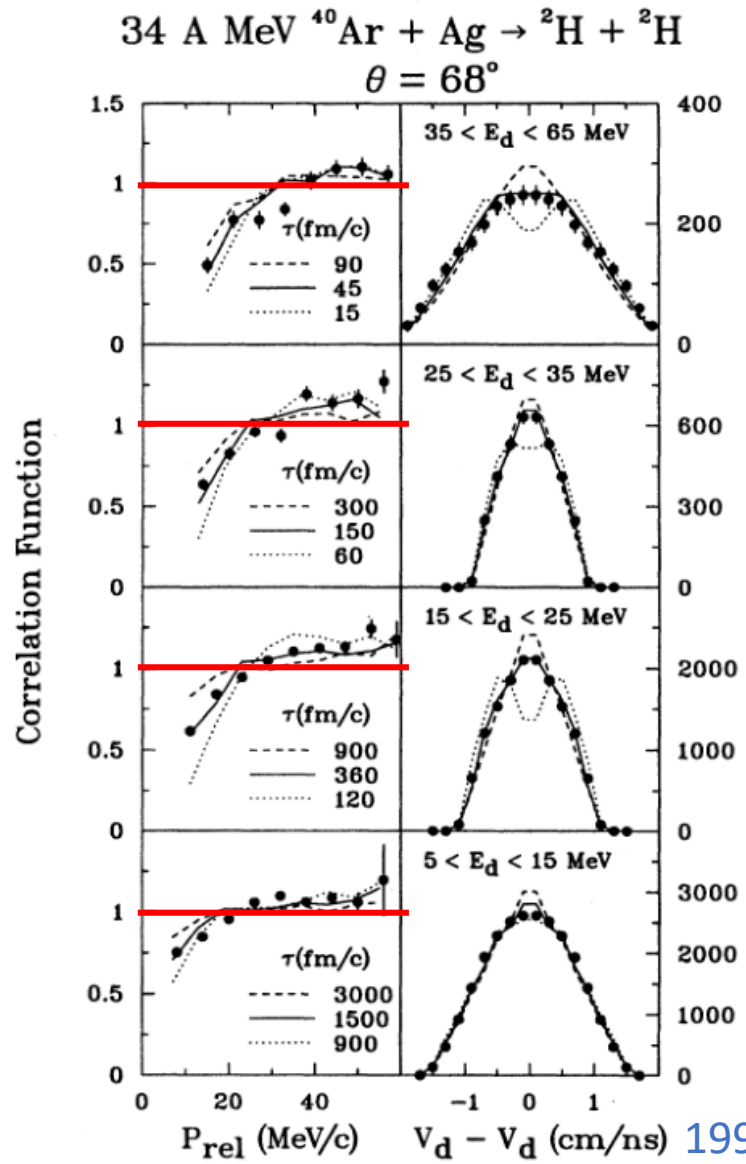


FIG. 13. p-d, d-d, t-t, t- ^3He , and ^3He - ^3He correlation functions.

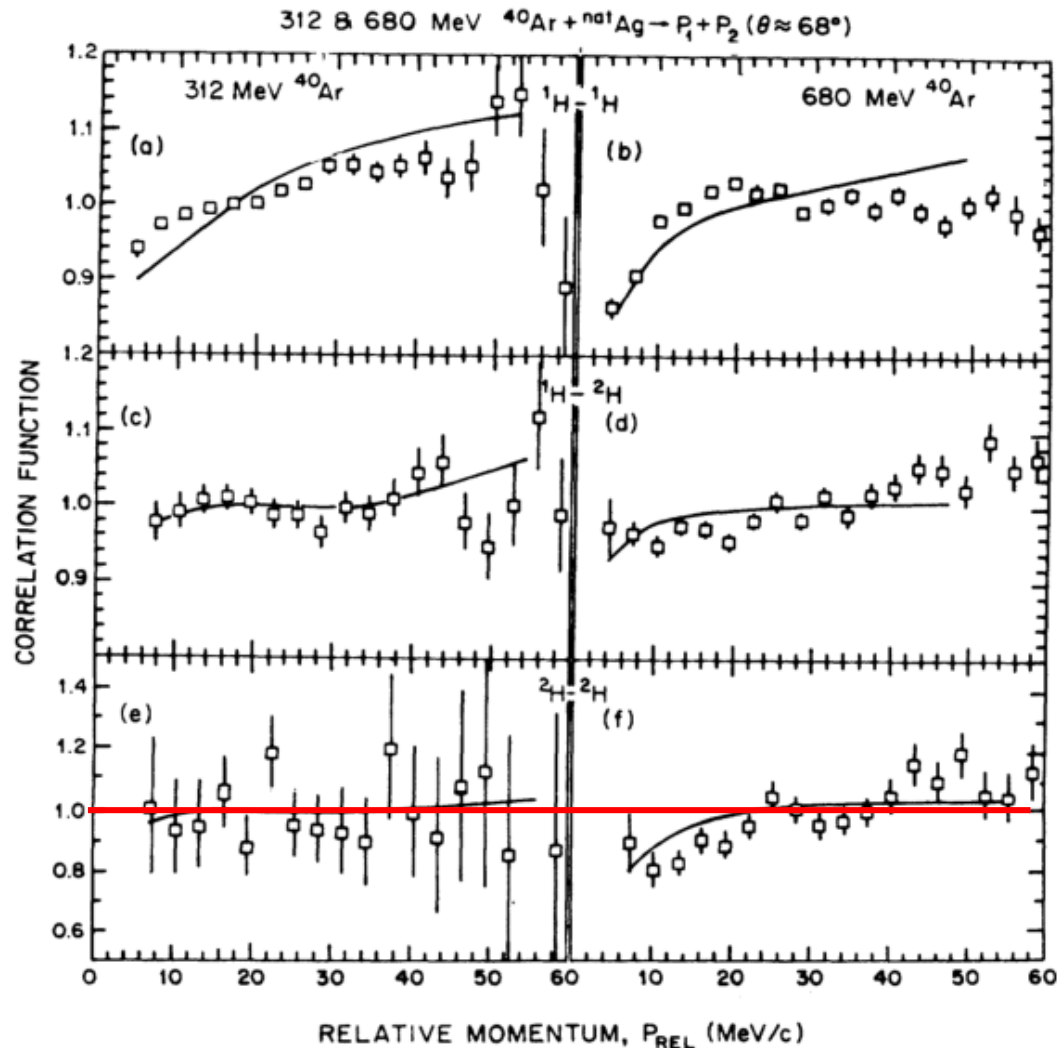
1987_J. Pochodzalla_PhysRevC.35.1695

1986_J. POCHODZALLA_MSU_PLB

Deuteron-deuteron correlation function



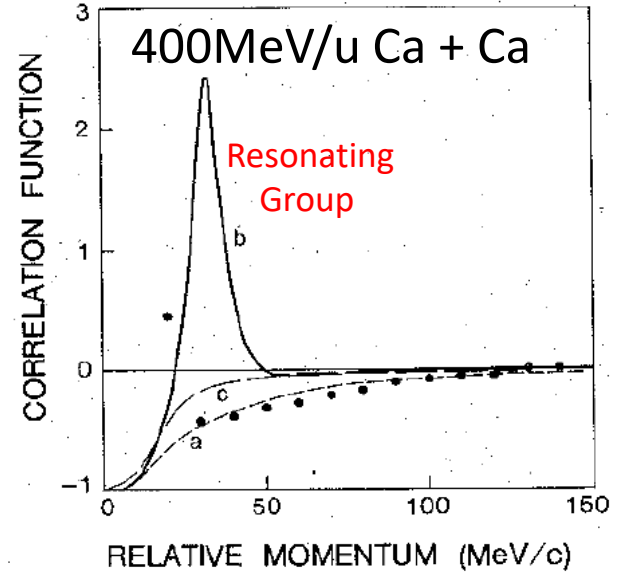
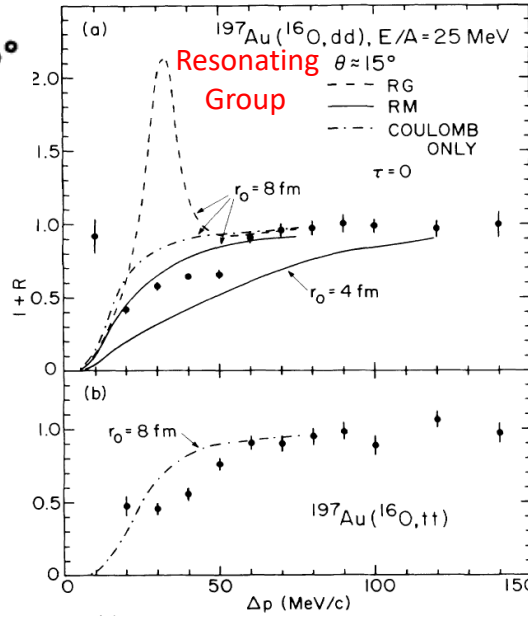
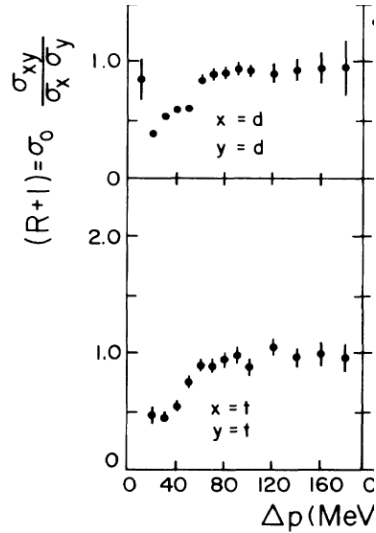
1995_C. J. Gelderloos_PhysRevC.52.R2834



1991_A. Elmaani_PhysRevC.43.R2474

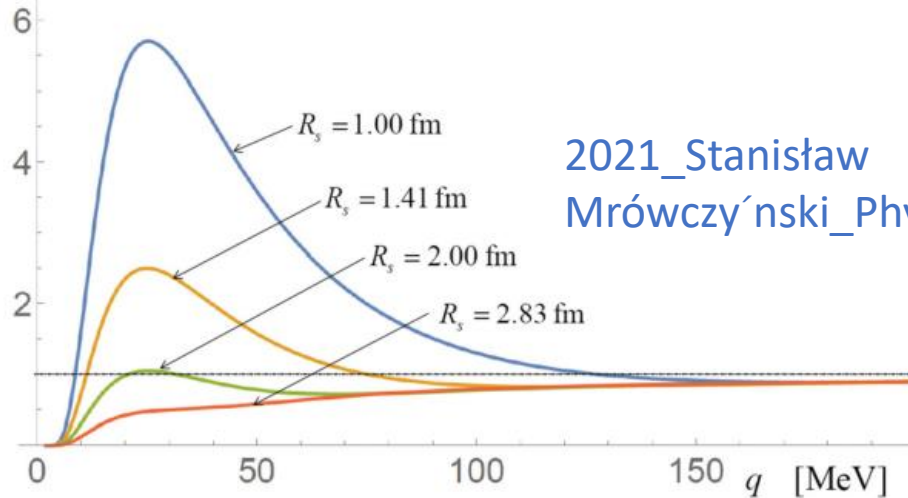
Deuteron-deuteron correlation function

$^{197}\text{Au}(^{16}\text{O},xy), E/A = 25 \text{ MeV}, \theta \approx 15^\circ$



$R(q)$

1985_C. B. Chitwood_MSU_PRL



2021_Stanisław

Mrówczyński_PhysRevC.104.024909

1986_David H. Boal_PRC

