

# **μTRISTAN**

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2304.14020, Kåre Fridell (KEK/Florida State U.), RK, Ryoto Takai (KEK/Sokendai)

Also, study in progress with Koji Nakamura (KEK), Sayuka Kita (Tsukuba U.), Toshiaki Kaji (Waseda U.), Taiki Yoshida (Waseda U.), Kohei Yorita (Waseda U.)

**muon4future, Venice, May 29-31, 2023**

# Clearly, we need next generation colliders.

1. We must investigate **the form of the Higgs potential** by the observation of self-interactions.
2. We must check the possibility that one can actually produce **dark matter** artificially.
3. We must look for **new physics** at least up to about 10TeV (~ a loop factor higher than the EW scale).

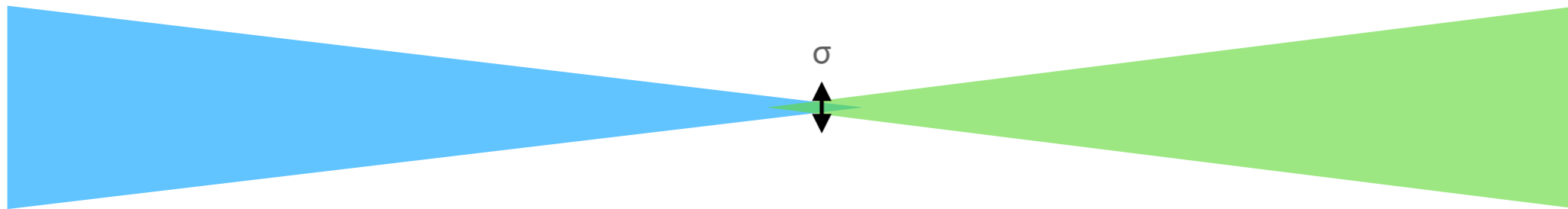
We cannot stop here.

Today, I talk about possibly a realistic scenario of  $\mu^+$  based colliders.

As you know, the most important (difficult) part of muon colliders is to obtain enough **luminosity** for particle physics.

# Luminosity

$$\mathcal{L} = \frac{N_{\text{beam1}} N_{\text{beam2}}}{4\pi\sigma_x\sigma_y} f_{\text{rep}}$$



We need a large number of muons and/or narrow beams.

As a reference,

$N_{\text{beam}}=10^{10}$  (1.6nC) / bunch

$\sigma=1\mu\text{m}$

$f_{\text{rep}}=1\text{MHz}$



$\sim 8 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1} \sim 25 \text{ fb}^{-1}/\text{year}$

We want  $\text{ab}^{-1}$  level luminosity for physics  
(HL-LHC, ILC)

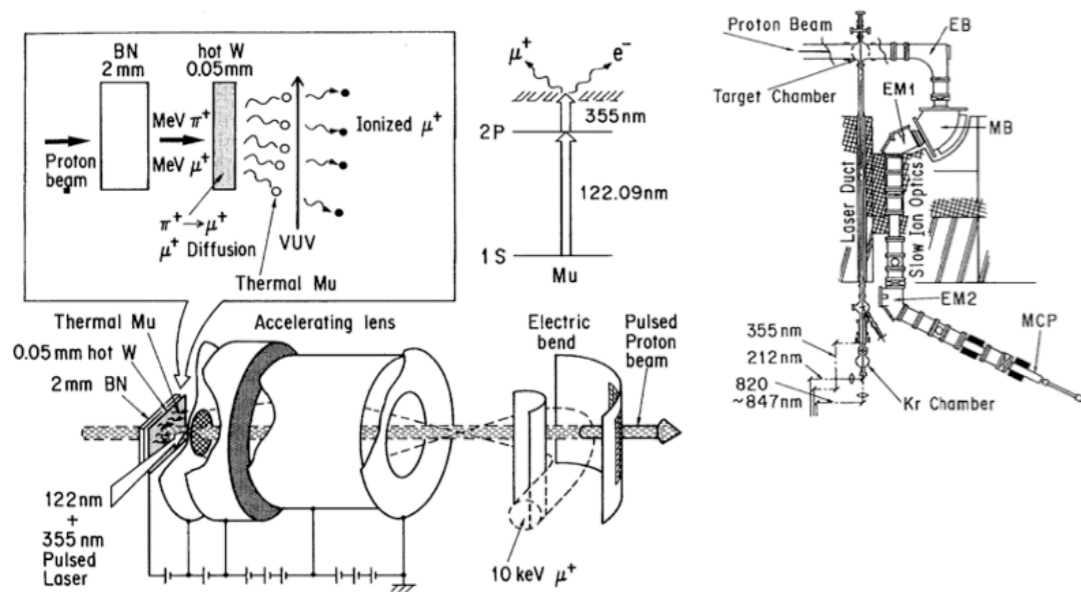
$\sigma$  is the most difficult part. The **cooling** is the key.

# Muon cooling

There is a rather mature(?) technology works for  $\mu^+$ .

Ultracold muon technology

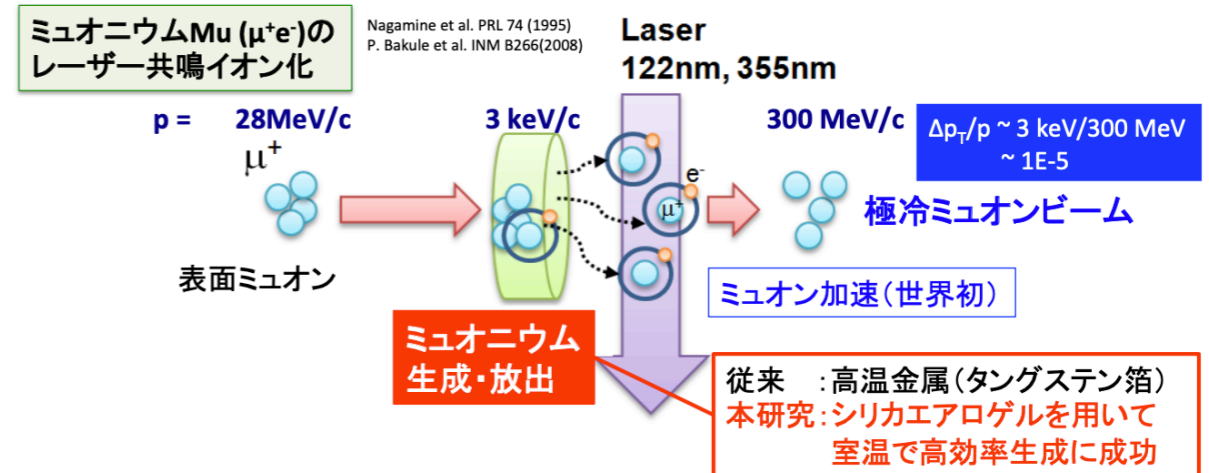
[K.Nagamine et al. 1995]



## ミュオンg-2/EDMと極冷ミュオンビーム

- J-PARCで行う新しいミュオンg-2/EDM精密測定** [www.g-2.kek.jp](http://www.g-2.kek.jp)
- BNLが報告した標準模型からのズレ( $3\sigma$ )の検証(0.1ppm)
  - 全く新しいコンセプトで主要系統誤差要因を払拭
    - ゼロ電場
    - コンパクトな蓄積磁石(0.7 m  $\ll$  14 m)
  - 通常に比べてエミッタンスが1/1000程度小さいミュオンビーム (極冷ミュオンビーム) が必須

This has been the key technology for the J-PARC muon g-2/EDM experiment.

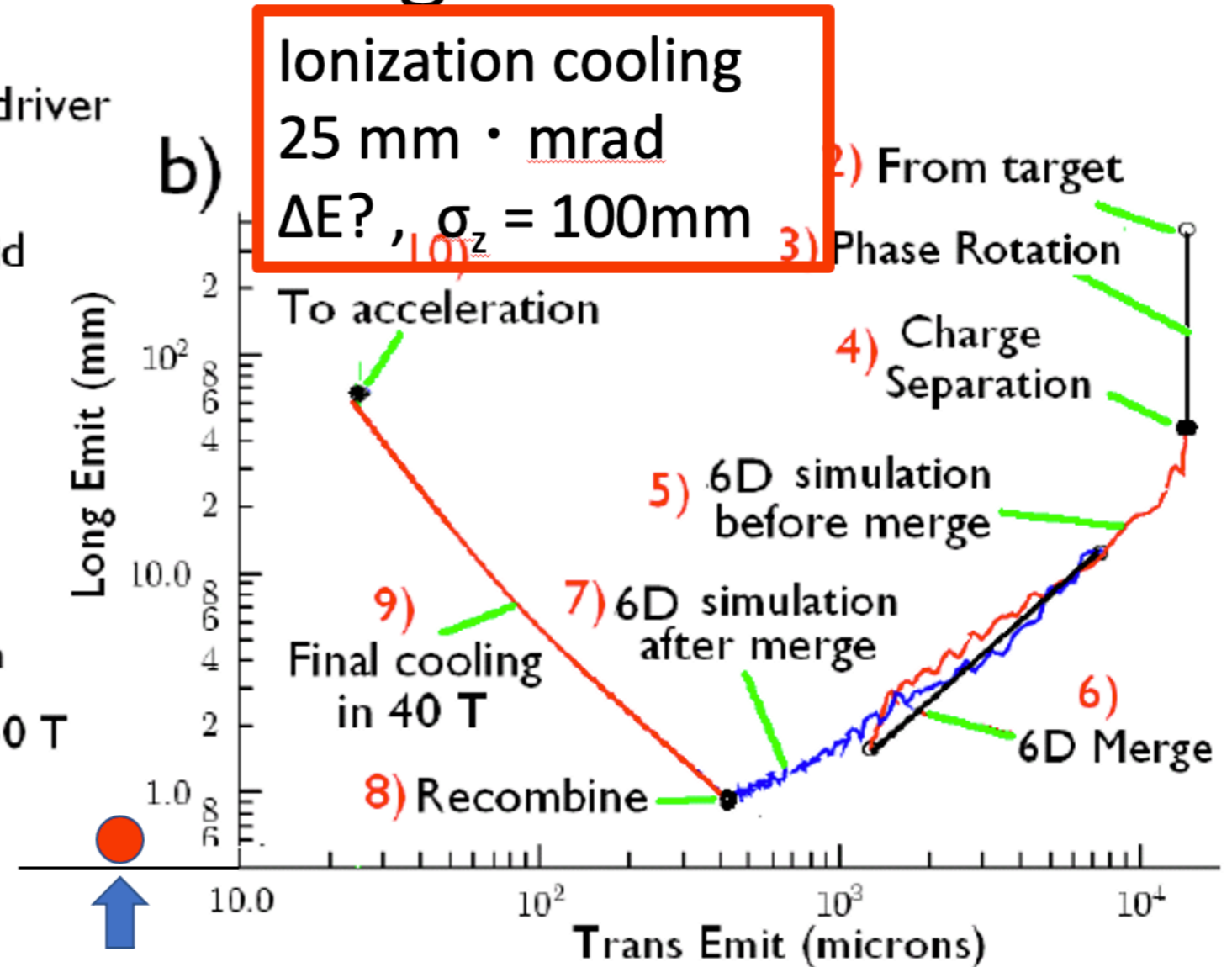
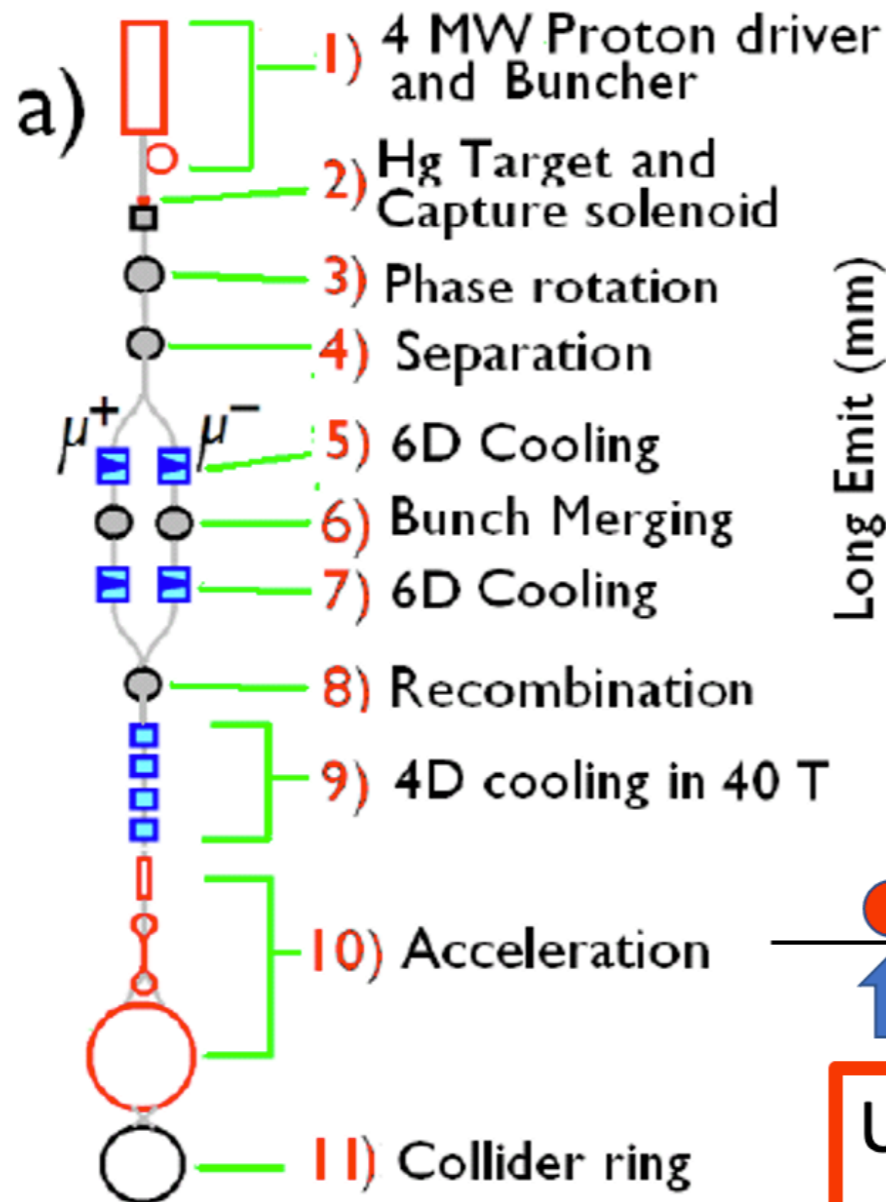


Looks like a low-emittance  $\mu^+$  beam is already there!

Mibe-san's slide

Also, polarized beam is possible. (non-trivial though)

# Emittance : Ionization cooling vs Ultra Cold



Ultra Cold  $\mu^+$   
 $< 5 \text{ mm} \cdot \text{mrad}$   
 $\Delta E = 1 \text{ eV}$ ,  $\sigma_z = 1 \text{ mm}$

# $\mu$ TRISTAN

$\mu^+e^-/\mu^+\mu^+$  collider with 1 TeV  $\mu^+$  beam.

**PTEP**

Prog. Theor. Exp. Phys. **2022** 053B02(16 pages)  
DOI: 10.1093/ptep/ptac059

30 GeV  $e^-$  / 1 TeV  $\mu^+$  : Higgs factory,  $\sqrt{s}=346\text{ GeV}$   
1 TeV  $\mu^+$  / 1 TeV  $\mu^+$  : new physics search,  $\sqrt{s}=2\text{ TeV}$

## $\mu$ TRISTAN

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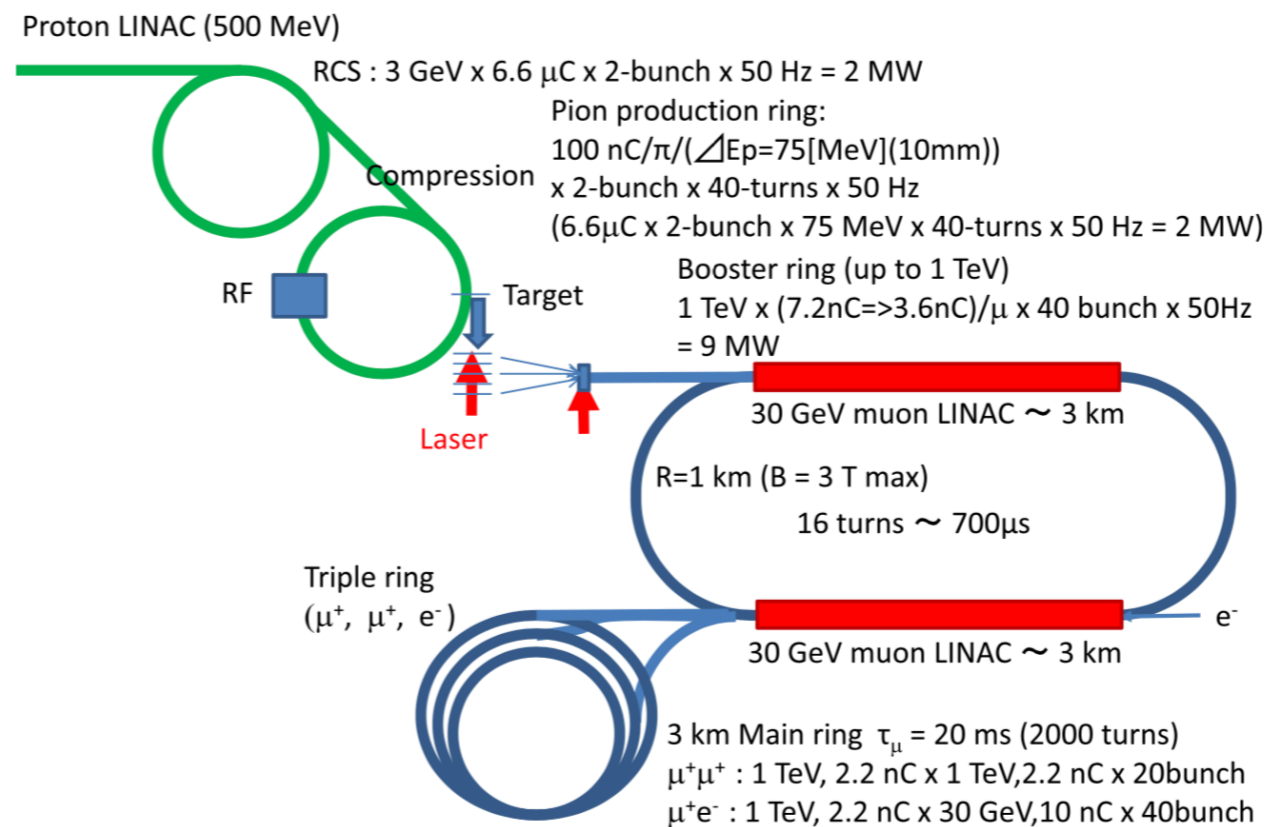
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Received January 21, 2022; Revised March 18, 2022; Accepted March 28, 2022; Published March 28, 2022

The ultra-cold muon technology developed for the muon  $g-2$  experiment provides a low-emittance  $\mu^+$  beam which can be accelerated and used for experiments. We consider the possibility of new collider experiments by  $\mu^+$  beam up to 1 TeV. Allowing the  $\mu^+$  beam to collide with a high-intensity TRISTAN energy,  $E_{e^-} = 30\text{ GeV}$ , in a storage ring with the same size as TRISTAN (circumference of 3 km), one can realize a collider experiment with the center-of-mass energy  $\sqrt{s} = 346\text{ GeV}$ , which allows the production of Higgs bosons through vector boson fusion processes. We estimate the deliverable luminosity with existing accelerator technology.  $\mu^+\mu^+$  colliders up to  $\sqrt{s} = 2\text{ TeV}$  are also possible using the same technology.  $\mu^+\mu^+$  colliders up to  $\sqrt{s} = 2\text{ TeV}$  are also possible using the same technology.  $\mu^+\mu^+$  colliders up to  $\sqrt{s} = 2\text{ TeV}$  are also possible using the same technology.



**Fig. 1.** Conceptual design of the  $\mu^+e^-/\mu^+\mu^+$  collider.

# How many cold muons?

1/(20ms) where 20ms is the lifetime of the 1TeV muon

J-PARC like proton driver:  $6.6 \mu\text{C} * 50 \text{ Hz} * 2 \text{ bunches} = 4.1 \times 10^{15} \text{ protons/s}$  realistic

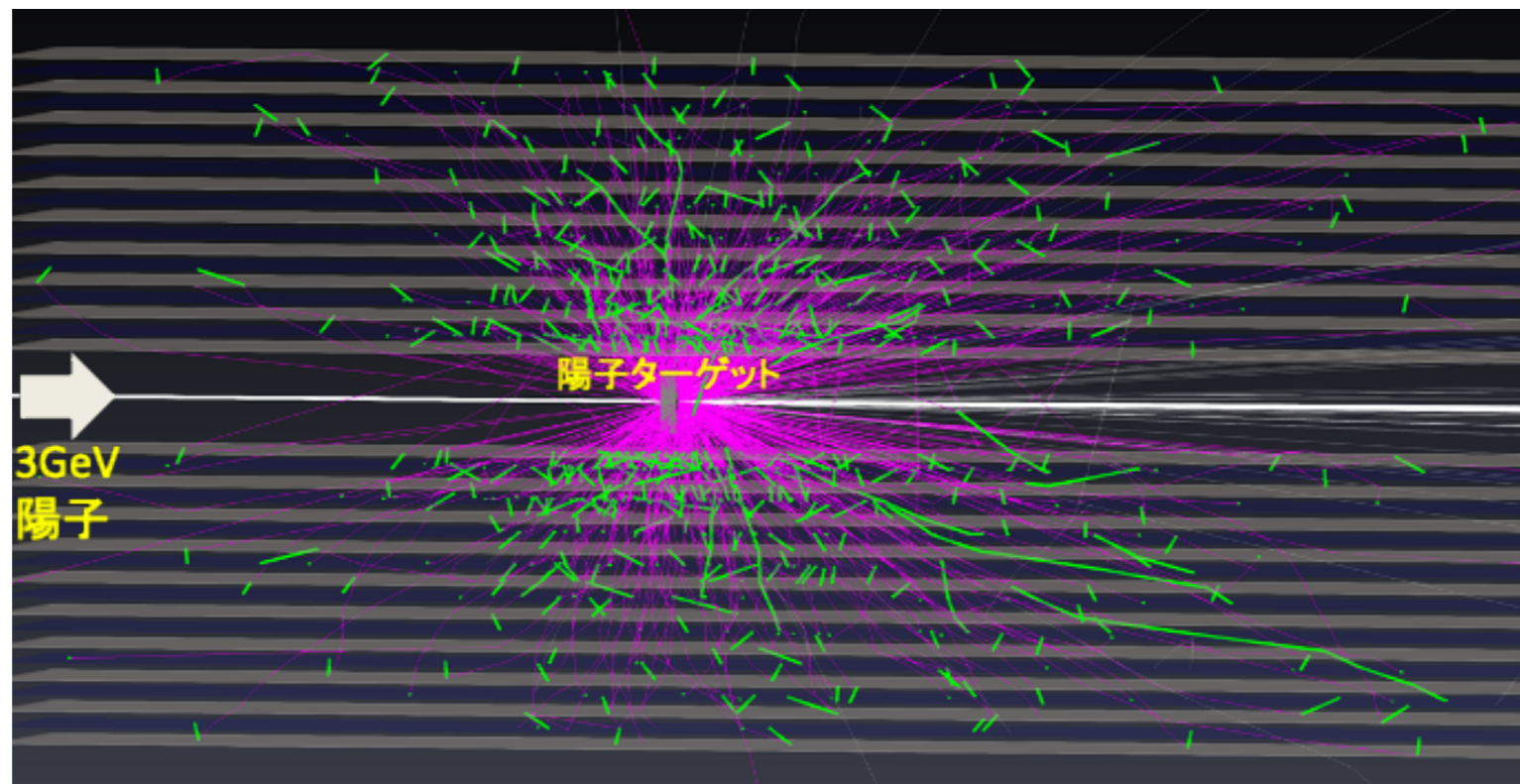
pion production target: 40 hits/bunch    0.016  $\pi^+$ /proton     $2.6 \times 10^{15} \pi^+$ /s    maybe realistic

pion stopping target: 0.5 stopping efficiency \* 0.07 muons/ $\pi^+$      $9 \times 10^{13} \mu^+$ /s    maybe challenging

$10^5$  larger than J-PARC MLF.

Super muon factory!

simulation: (in progress)



pink: pion  
green: muon



# Luminosity?

J-PARC like proton driver:  $6.6 \mu\text{C} * 50 \text{ Hz} * 2 \text{ bunches} = 4.1 \times 10^{15} \text{ protons/s}$   
 pion production target: 40 hits/bunch 0.016  $\pi^+$ /proton  $2.6 \times 10^{15} \pi^+$ /s  
 pion stopping target: 0.5 stopping efficiency \* 0.07 muons/ $\pi^+$   $9 \times 10^{13} \mu^+$ /s

$6.6 \mu\text{C} \times 2 \times 0.016 \times 0.5 \times 0.07 \sim 7 \text{ nC} / \text{bunch} \sim 4 \times 10^{10} \text{ muons/bunch}$

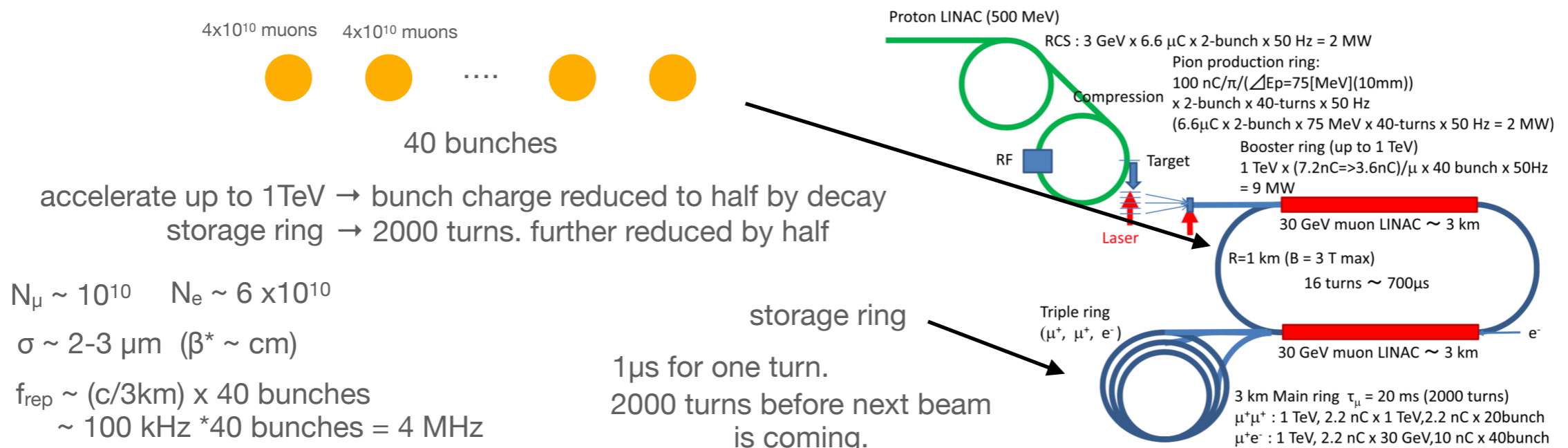
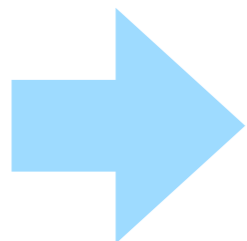


Fig. 1. Conceptual design of the  $\mu^+e^-/\mu^+\mu^+$  collider.



$$\mathcal{L}_{\mu^+e^-} = 4.6 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}.$$

$$\mathcal{L}_{\mu^+\mu^+} = 5.7 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}.$$

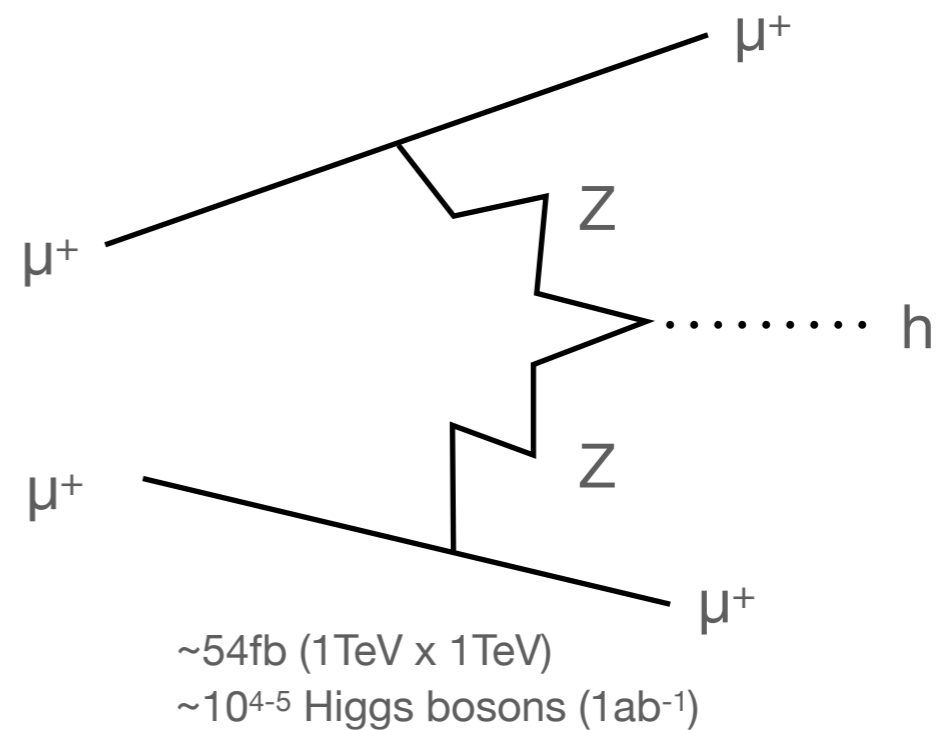
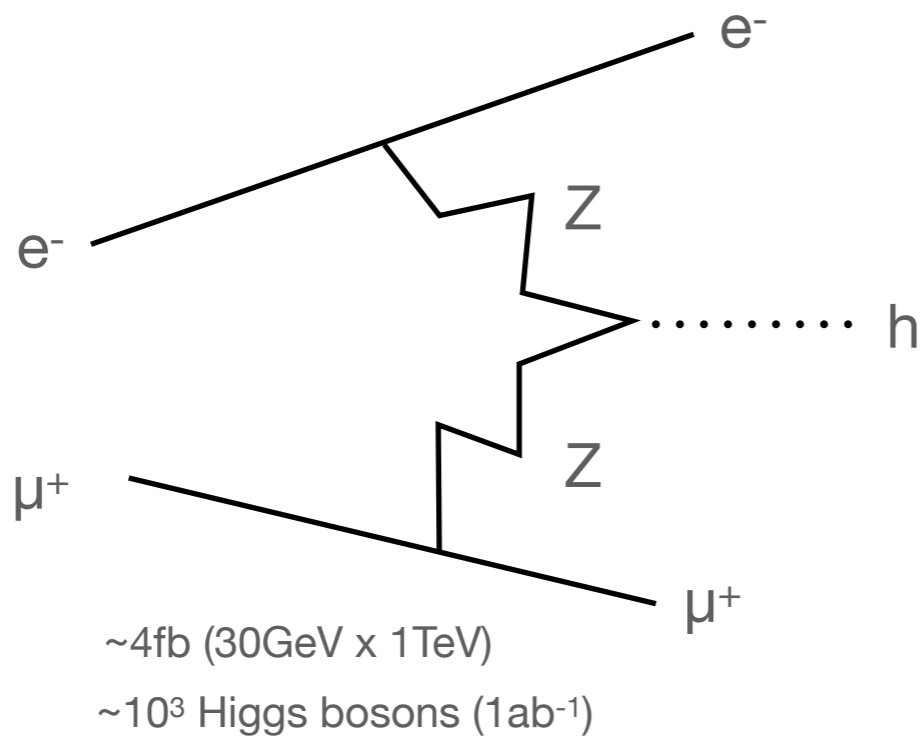
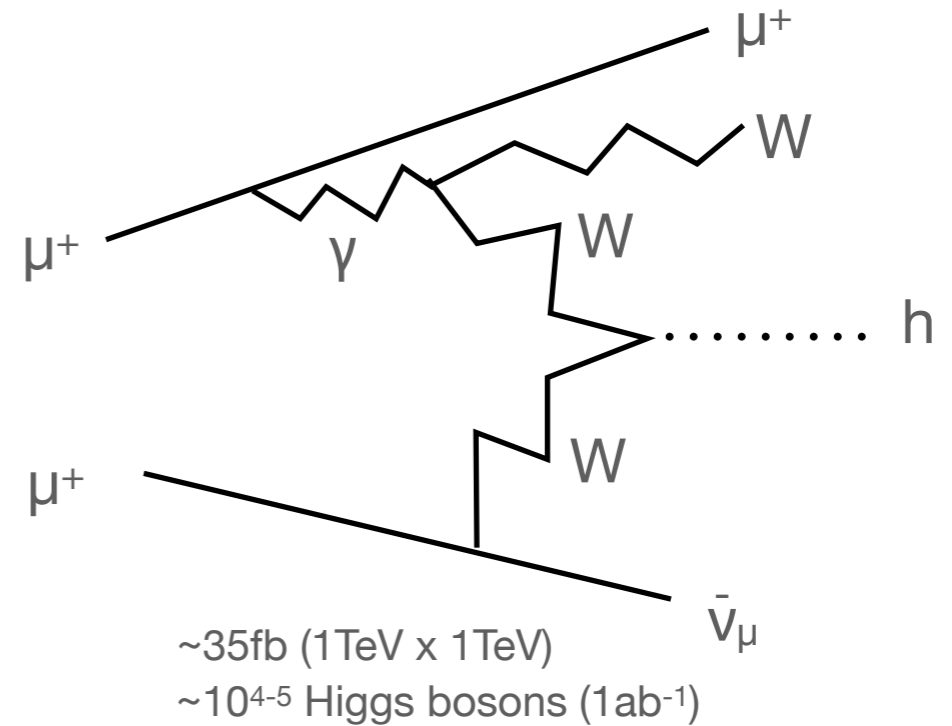
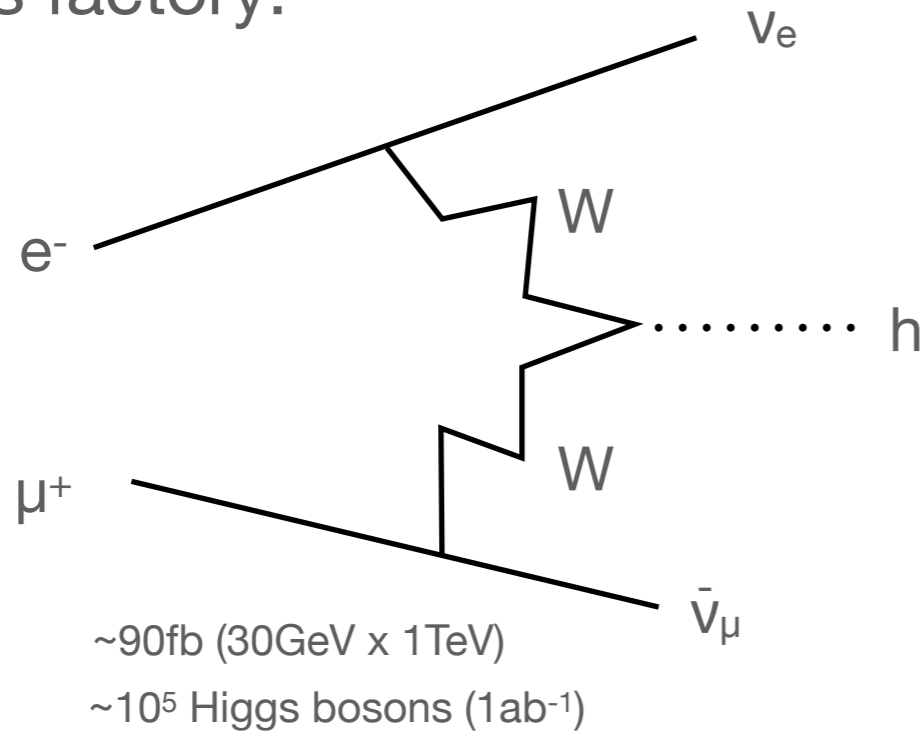
( $\beta^*$  may be much smaller?)

$\text{ab}^{-1}$  level for 10yrs running.

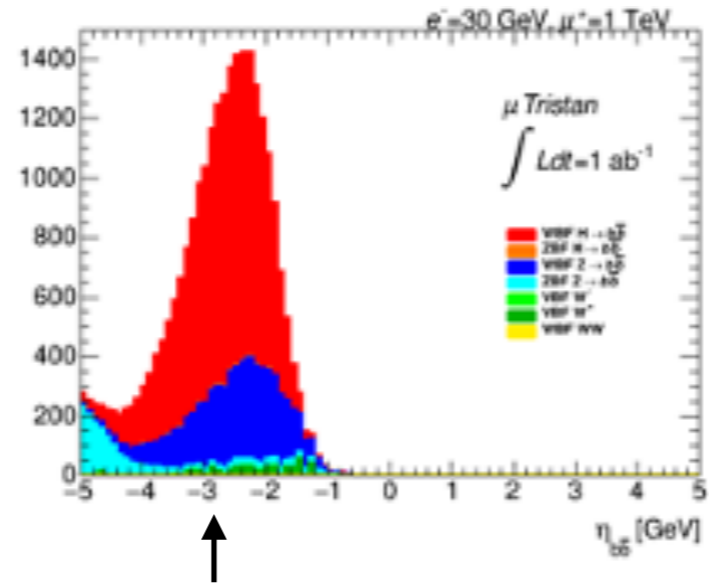
not bad.

# What can we do at $\mu$ TRISTAN?

Higgs factory:

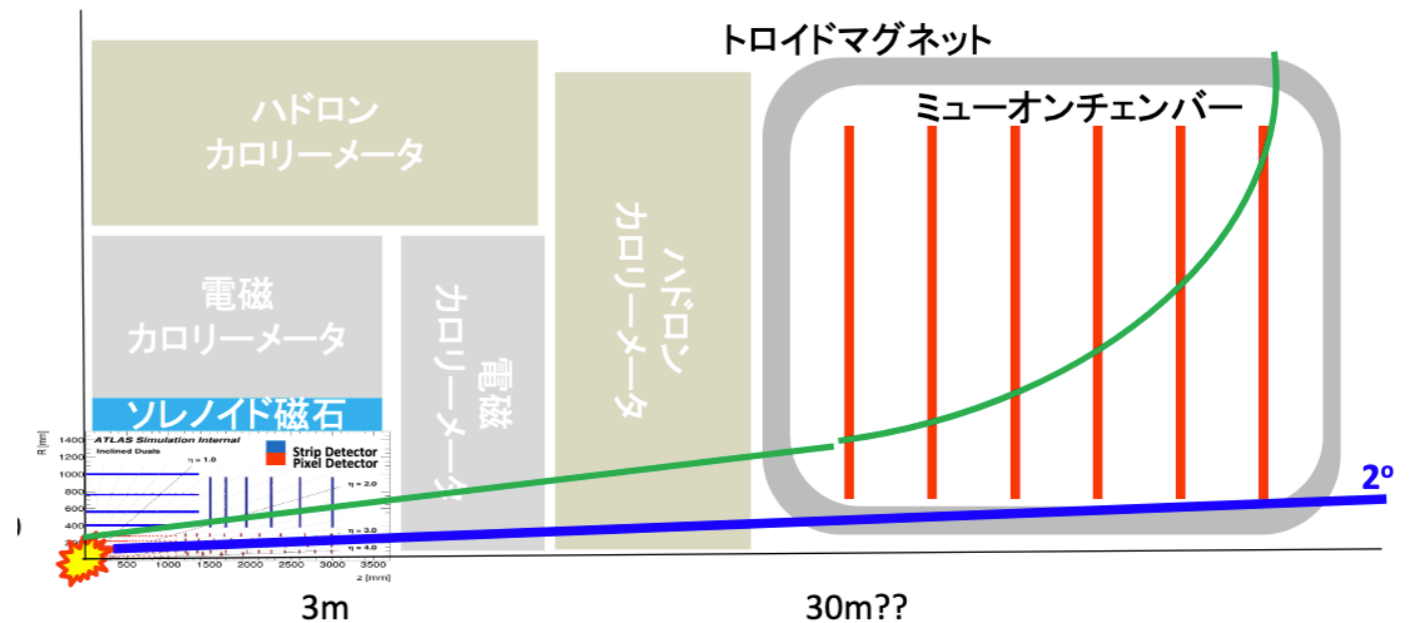
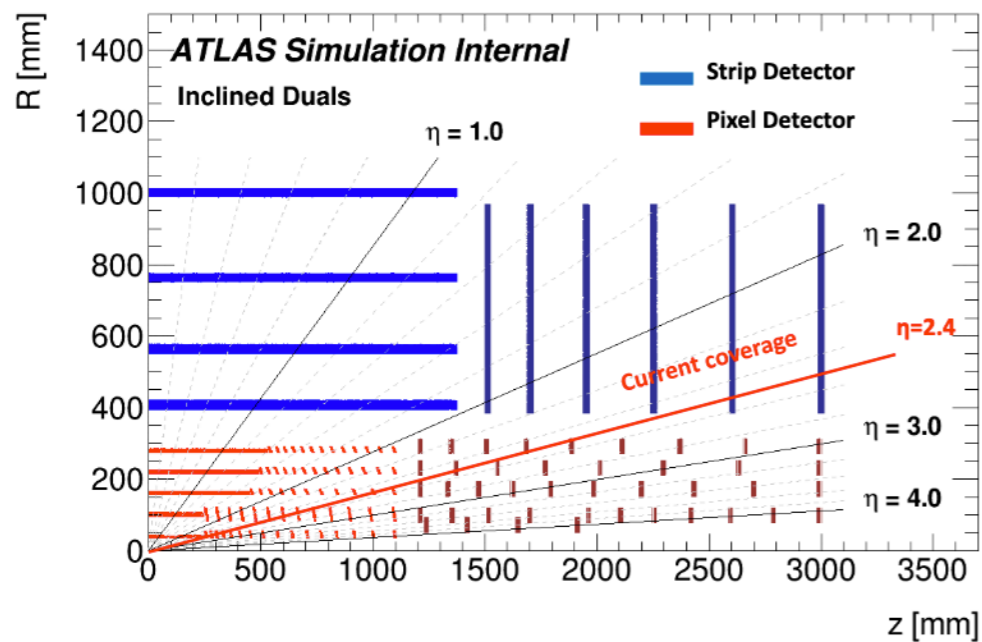


# $\mu^+e^-$ : Very asymmetric



All the particles go to the direction of the muon.

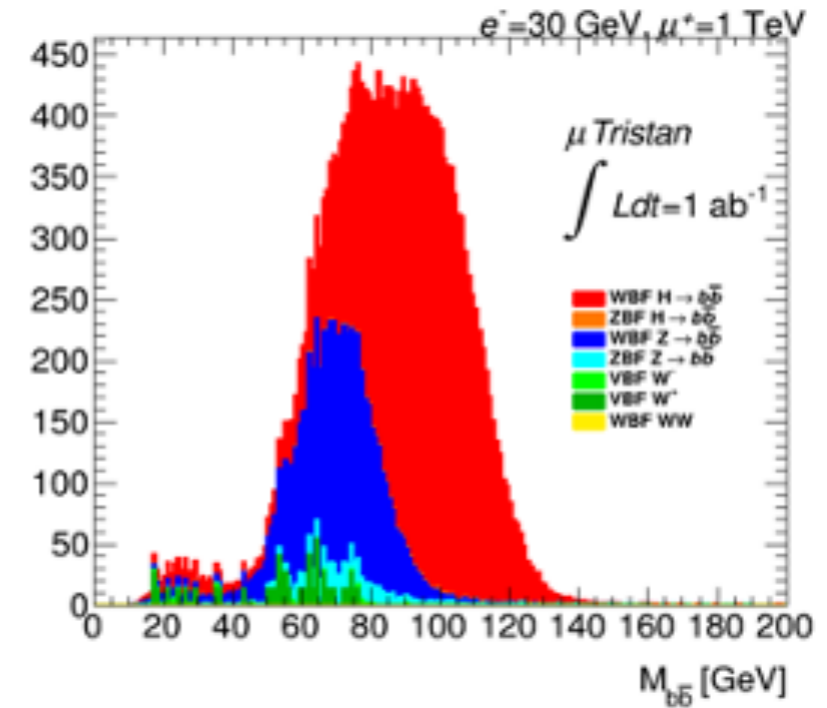
We need a coverage of  $\eta \sim -4$  ( $2^\circ$ ), which is the same level as the design of the ATLAS at HL-LHC.



# Higgs coupling

Study in progress in collaboration with Koji Nakamura and Sayuka Kita.

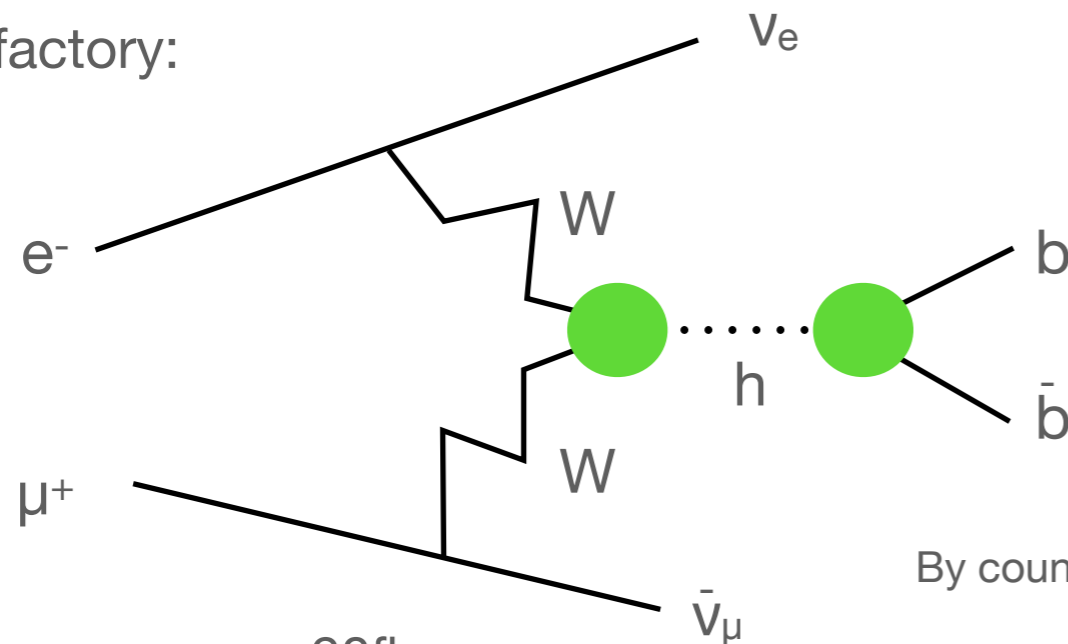
simulation with the ATLAS detector for HL-LHC



acceptance  $\sim 23\%$

(This should improve a lot with a detector designed for this collider.)

Higgs factory:



$\sim 90\text{fb}$

$\sim 10^5$  Higgs bosons

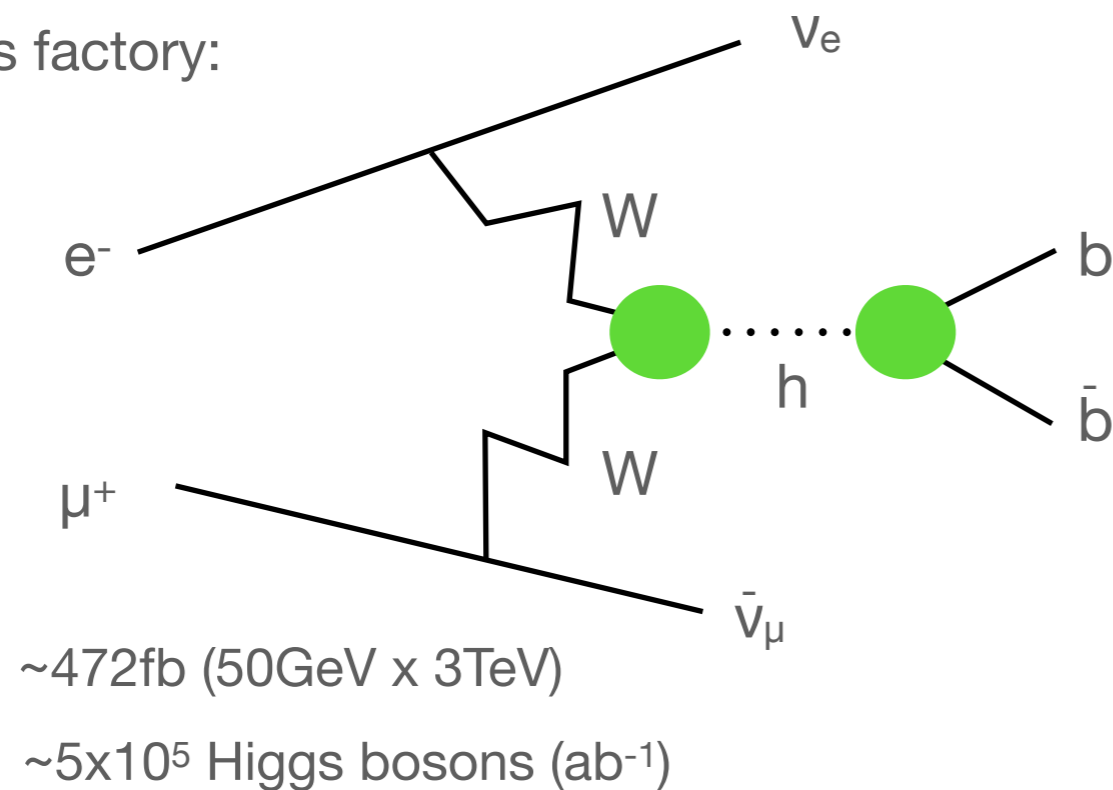
By counting the number of events and compare with the SM prediction

$$\begin{aligned} \Delta(\kappa_W + \kappa_b - \kappa_H)_{\text{stat}} &= \frac{1}{2} \frac{1}{\sqrt{N(\text{WBF}) \times \text{Br}(h \rightarrow b\bar{b}) \times \text{efficiency}}} \\ &= 3.1 \times 10^{-3} \times \left( \frac{\text{integrated luminosity}}{1.0 \text{ ab}^{-1}} \right)^{-1/2} \left( \frac{\text{efficiency}}{0.5} \right)^{-1/2} \end{aligned}$$

sub percent level measurements.

# Higher energy? $\mu$ Tevatron?

Higgs factory:



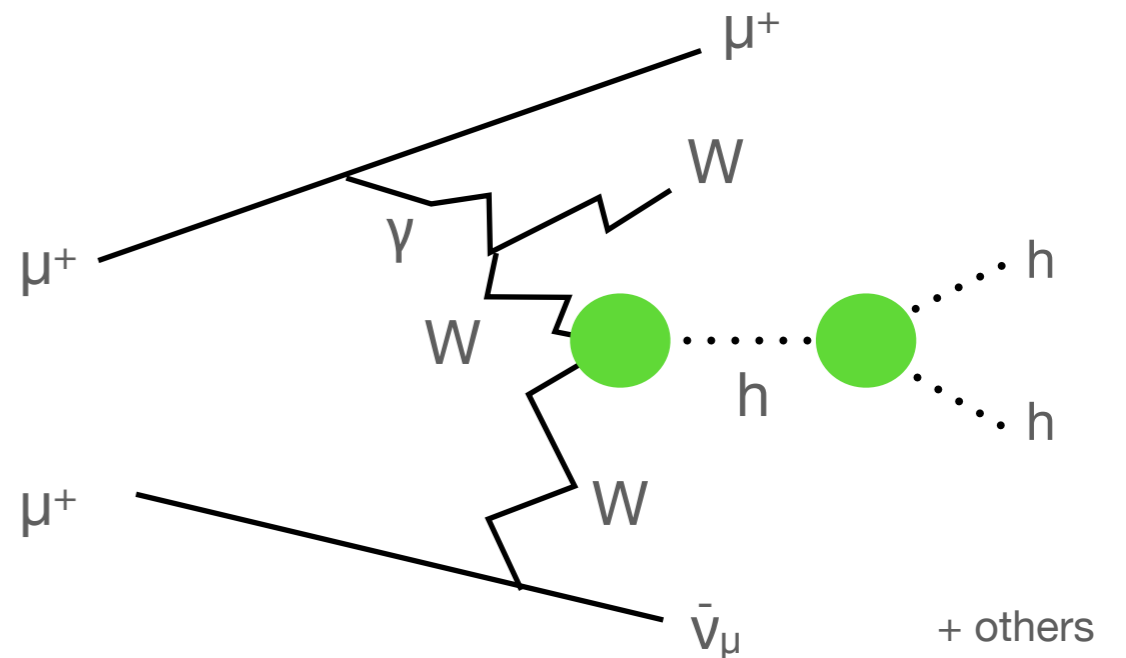
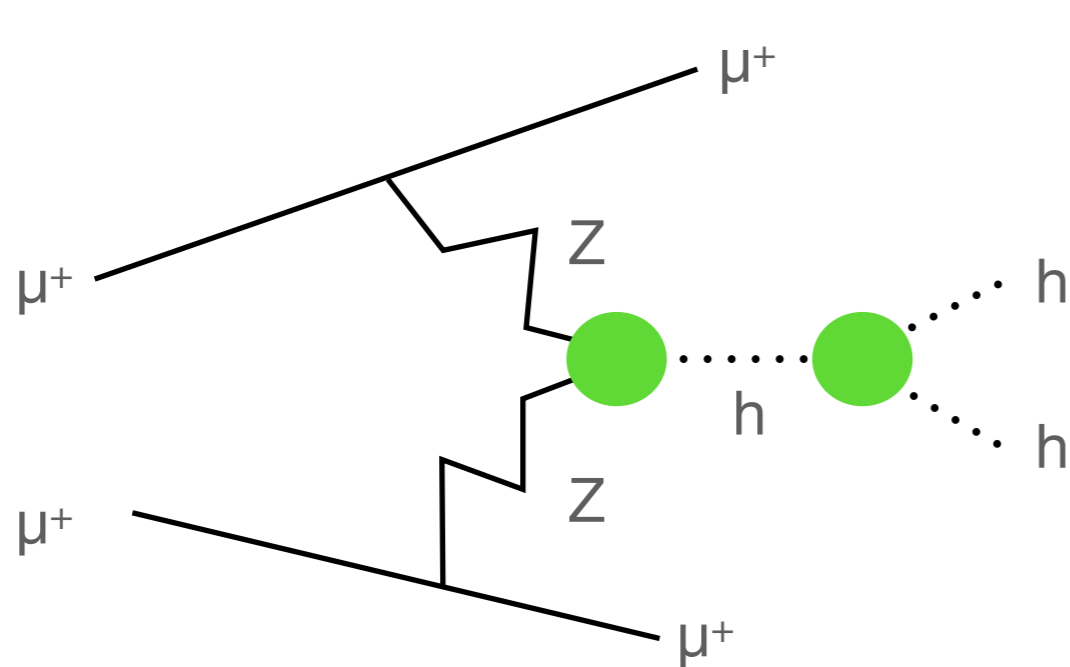
50GeV electron + 3TeV muon at a **6km** ring

$$\sqrt{s} = 775 \text{ GeV}$$

hh production: 89 events/ $\text{ab}^{-1}$  (maybe we need more for coupling measurements)



# Higgs production@ $\mu^+\mu^+$

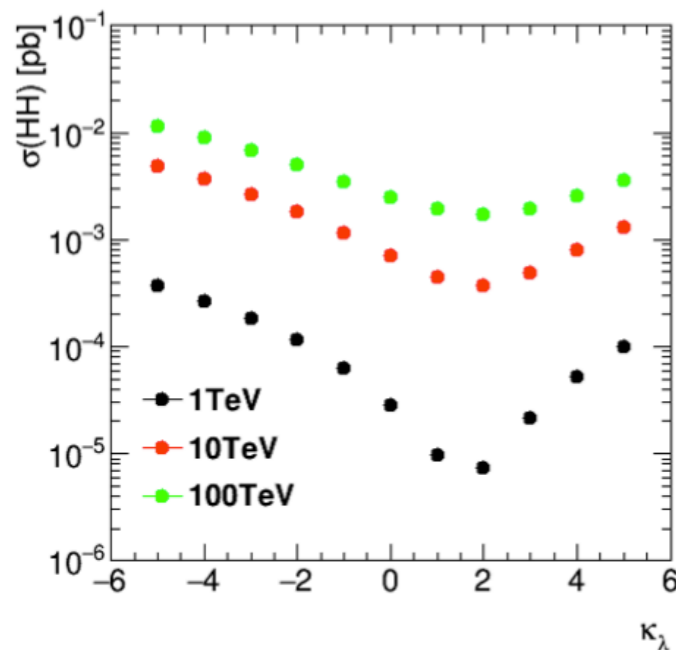


about 1/3 of  $\mu^+\mu^-$

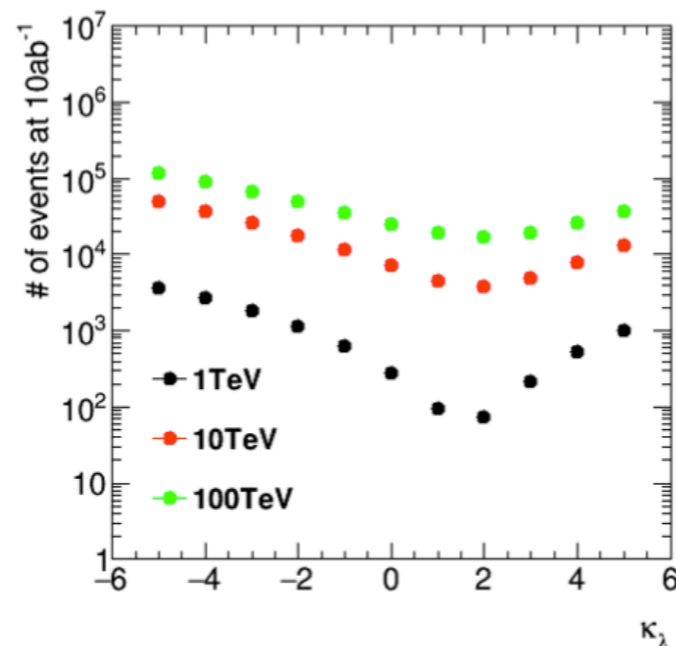
$\sqrt{s}$ [TeV]	ZBF [fb]	Photon emission [fb]
2	0.075	0.010
10	0.62	0.30
20	1.1	0.75

ZBF:

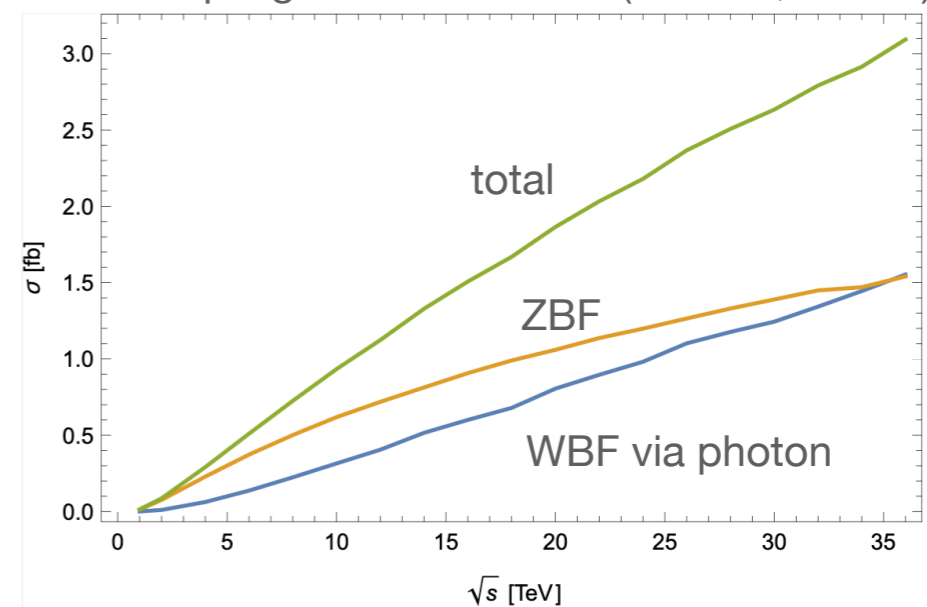
## Cross section



## # of Events in 10ab<sup>-1</sup>

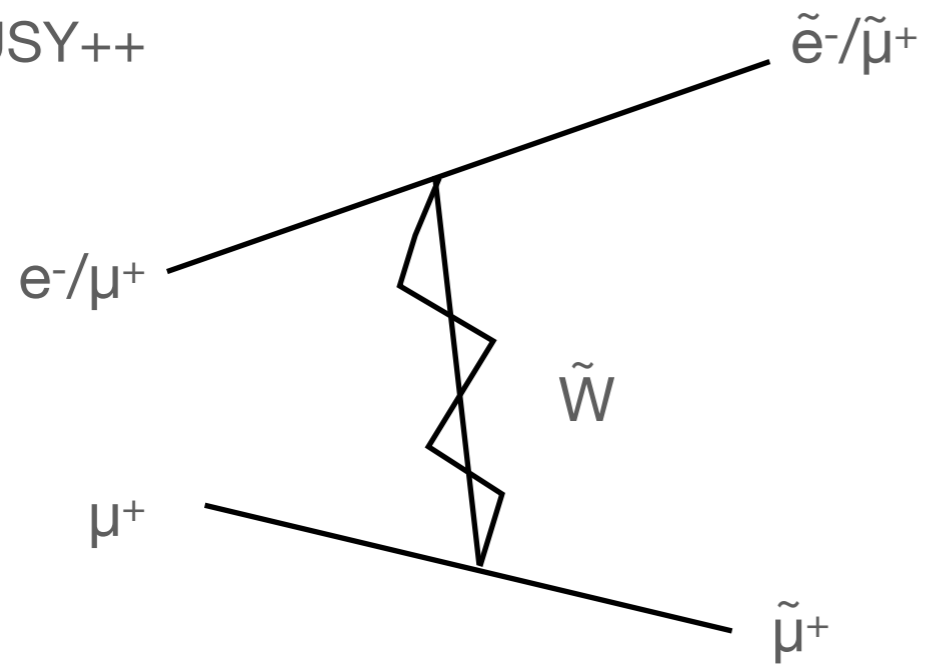


hhh coupling at 5-10% level? (@10TeV, 10ab<sup>-1</sup>)



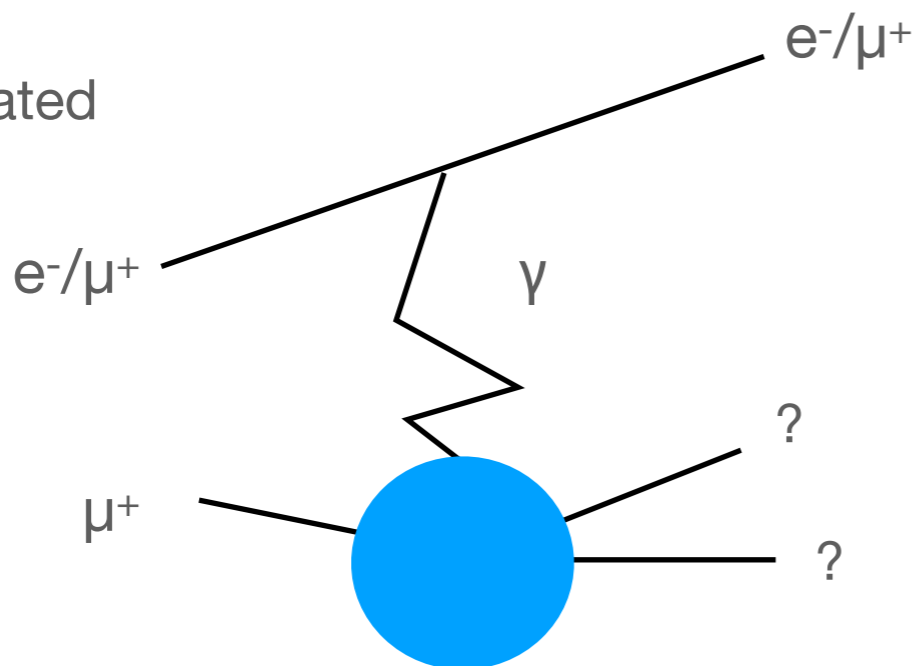
# New physics?

SUSY<sub>++</sub>

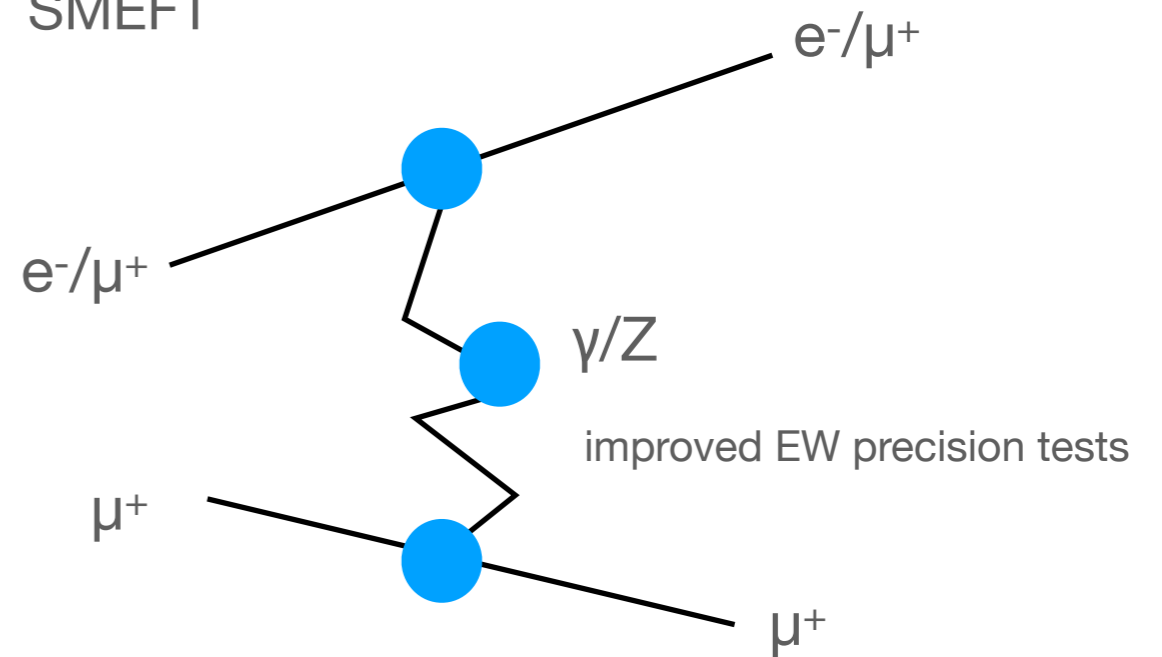


TeV mass new particles

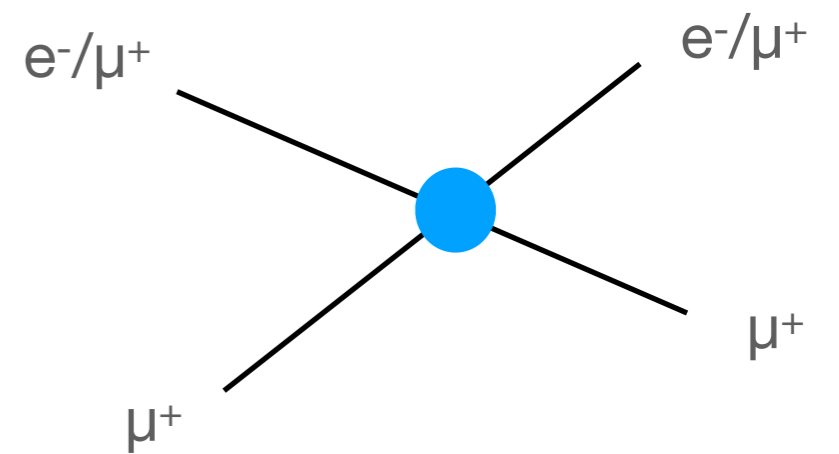
$g-2$  motivated



SMEFT



improved EW precision tests

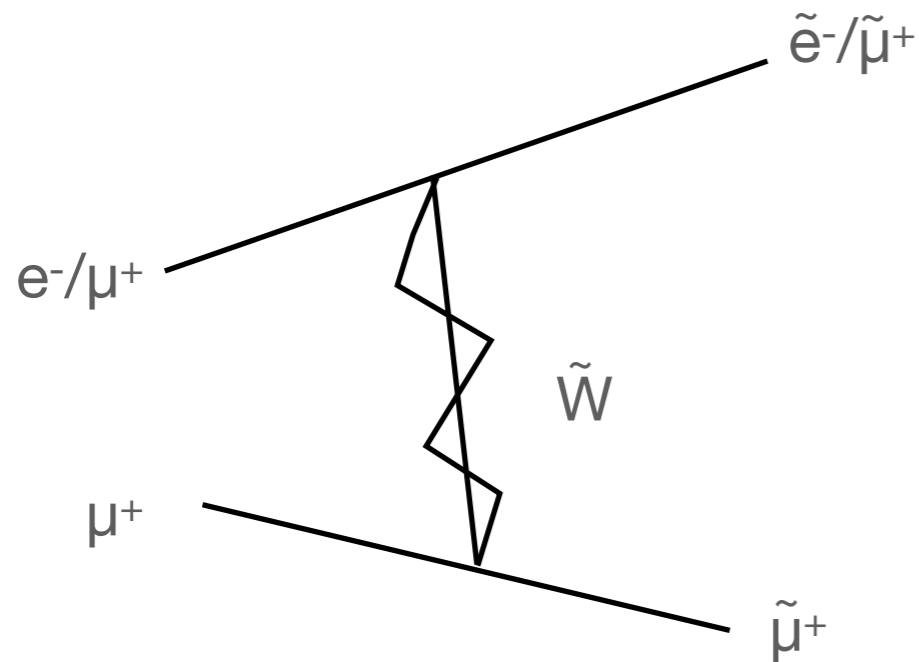
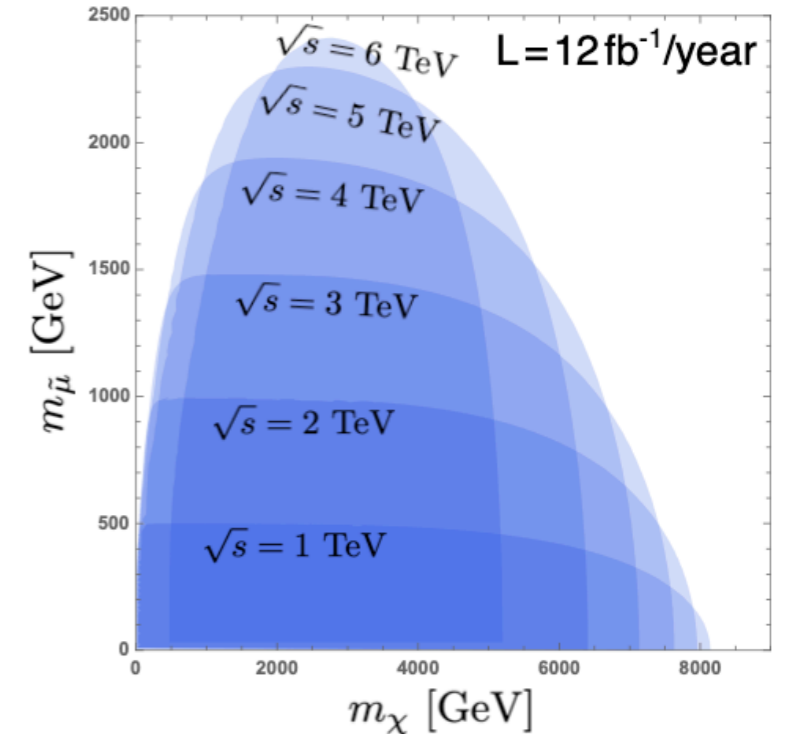
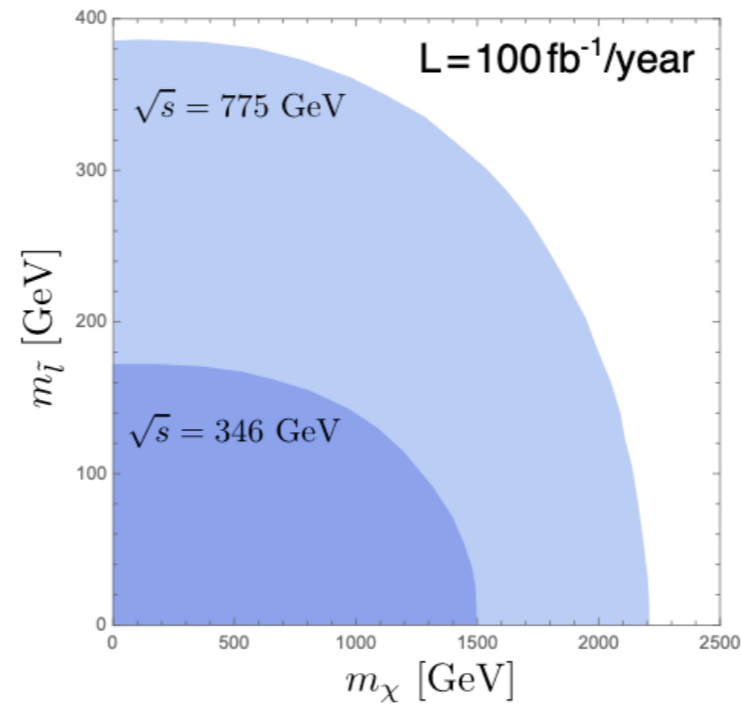


probe 100TeV scale physics!?



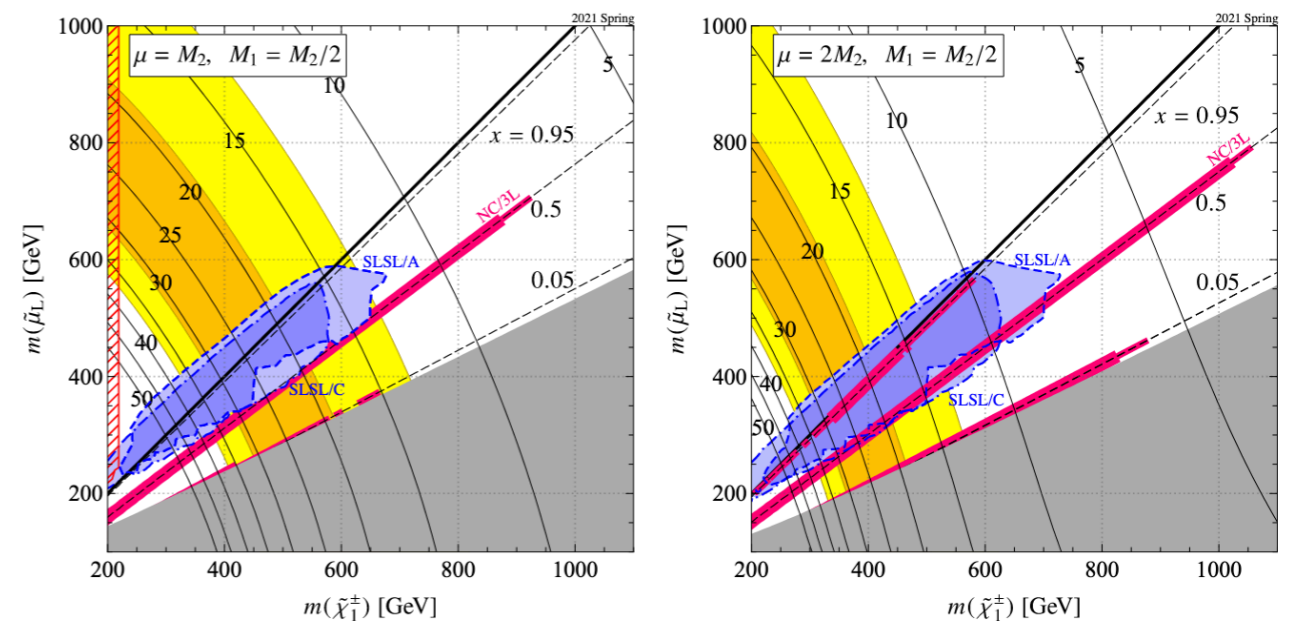
# Supersymmetry

Regions for  $N_{\text{event/year}} > 100$ .



Scalar muons up to TeV even for very heavy gauginos.  
Almost completely cover the muon  $g-2$  motivated region.

[Endo, Hamaguchi, Iwamoto, Kitahara '21]

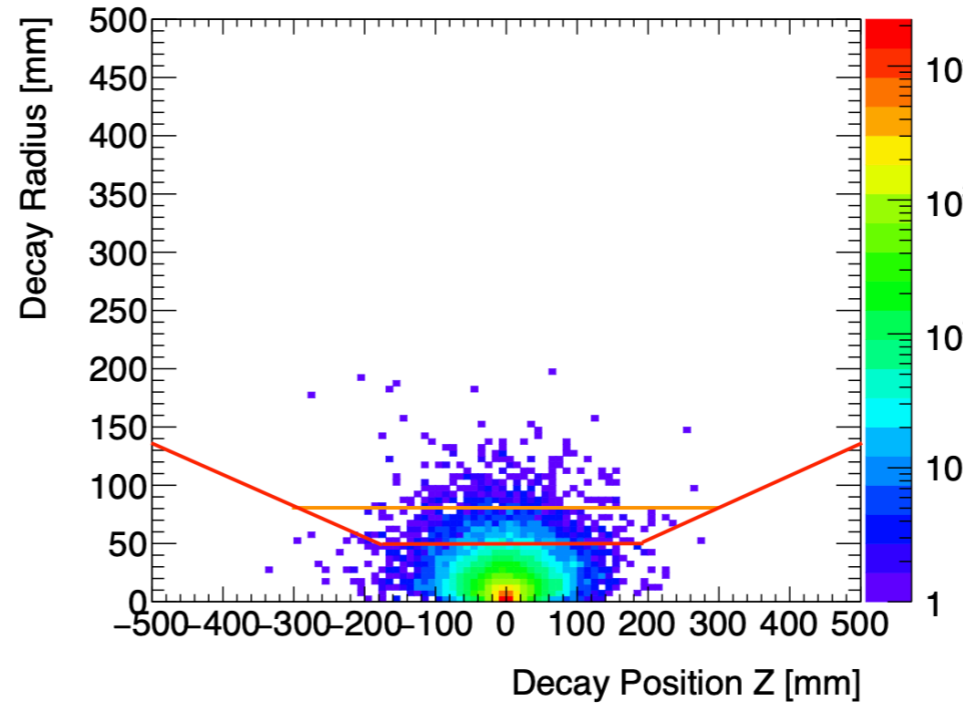
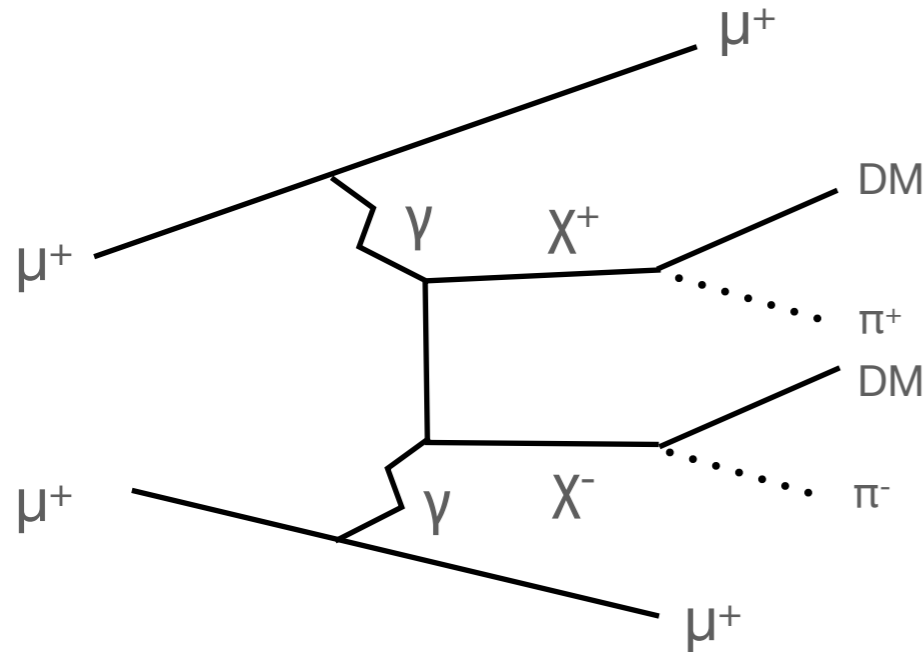


(A)  $\mu = M_2, M_1 = M_2/2$ .

(B)  $\mu = 2M_2, M_1 = M_2/2$ .

# DM search

$\sqrt{s} = 10 \text{ TeV}$ , 質量 1 TeV Higgsino の崩壊マップ



崩壊半径

• Case A  $> 80 \text{ mm}$

• Case B  $> 50 \text{ mm}$

$|\eta| < 2.0$

を再構成できると仮定

# of expected events @  $1 \text{ ab}^{-1}$

	R > 50 mm	R > 80 mm
$\sigma = 124.7 \text{ ab}$ $\mu^+\mu^+ \rightarrow \chi^+\chi^-\mu^+\mu^+$ (2 muons + at least 1 chargino)	2.4	0.5

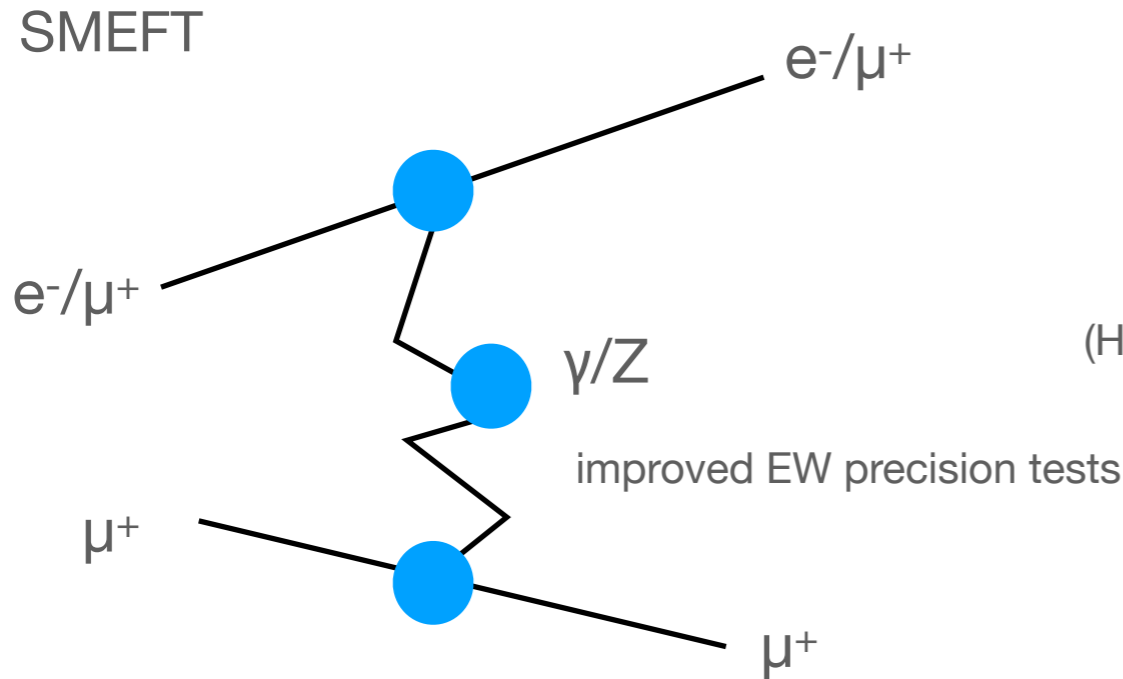
assumed a muon system which can detect forward muons ( $|\eta| < 6$ )

Looks like 1TeV Higgsino is within the reach.

(@10TeV machine)

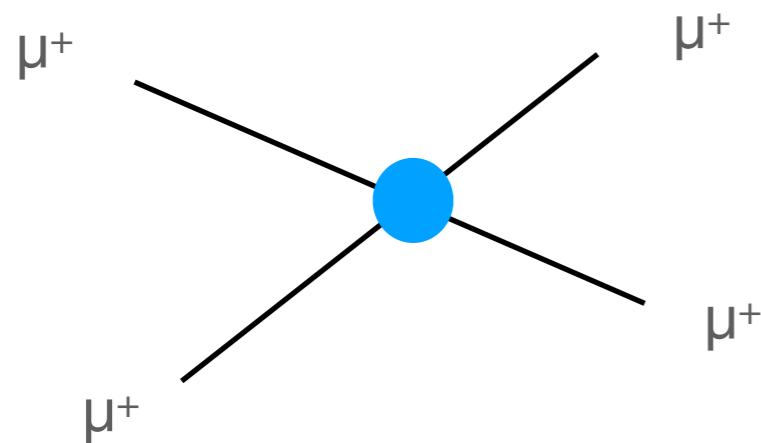
# Indirect searches

Basically the SM process has peak at the forward region, while interference with new physics (dim-6 operators) give events in the central region.



		RR	RL	LR	LL
S T (H current)(L current)	$C_{HWB}$	6.9 TeV	24 TeV	26 TeV	6.9 TeV
	$C_{HD}$	6.8 TeV	9.0 TeV	14 TeV	6.8 TeV
	$C_{H\ell}^{(1)}$	15 TeV	0	20 TeV	15 TeV
	$C_{H\ell}^{(3)}$	20 TeV	18 TeV	35 TeV	20 TeV
	$C_{He}$	16 TeV	19 TeV	0	16 TeV
4-fermi	$C_{\ell\ell}$	9.6 TeV	13 TeV	43 TeV	9.6 TeV
	$C_{\ell\ell}''$	0	0	47 TeV	0
	$C_{e\mu}$	0	66 TeV	0	0
	$C_{\ell e}$	0	0	0	44 TeV
	$C_{\ell e}^{ee\mu\mu}$	0	0	0	0
	$C_{\ell e}^{\mu\mu ee}$	44 TeV	0	0	0
	$C_{\ell e}^{\mu\mu ee}$	44 TeV	0	0	0

Table 2: Constraints on SMEFT operators at two-sigma level.  $E_e = 30$  GeV and  $E_\mu = 1$  TeV, which amounts to  $\sqrt{s} = 346$  GeV. The bin size for  $\Theta_e$  is taken as  $1^\circ$ . We require both muon and electron to go into the range of  $15.4^\circ \lesssim \Theta \lesssim 178^\circ$ , corresponding to  $\eta_{max} = 2$  for the muon beam side and  $\eta_{max} = 4$  for the electron beam side. As a result, the angle range of the electron is  $62.8^\circ \lesssim \Theta_e \lesssim 178^\circ$ .

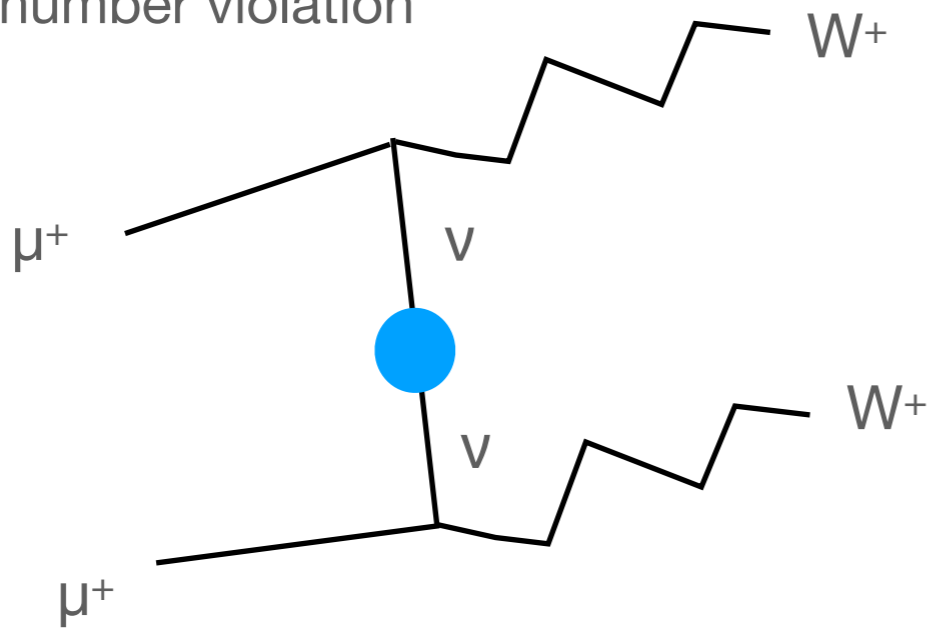


		RR	LL	RL
S T (H current)(L current)	$C_{HWB}$	10 TeV	9.4 TeV	2.3 TeV
	$C_{HD}$	5.5 TeV	3.5 TeV	2.3 TeV
	$C_{H\ell}^{(1)}$	8.0 TeV	0	4.9 TeV
	$C_{H\ell}^{(3)}$	14 TeV	7.0 TeV	6.7 TeV
	$C_{He}$	0	7.5 TeV	5.3 TeV
4-fermi	$C_{\ell\ell}$	7.7 TeV	5.0 TeV	3.3 TeV
	$C_{\ell\ell}^{\mu\mu\mu\mu}$	100 TeV	0	0
	$C_{ee}^{\mu\mu\mu\mu}$	0	100 TeV	0
	$C_{\ell e}^{\mu\mu\mu\mu}$	0	0	46 TeV

Table 1: Constraints on SMEFT operators at 2-sigma level.  $\sqrt{s} = 2$  TeV. The bin size for  $\theta$  is taken as  $1^\circ$  and each bin covers the range  $\theta_i - 0.5^\circ < \theta < \theta_i + 0.5^\circ$ . The considered range of  $\theta_i$  is  $16^\circ \leq \theta_i \leq 164^\circ$ .

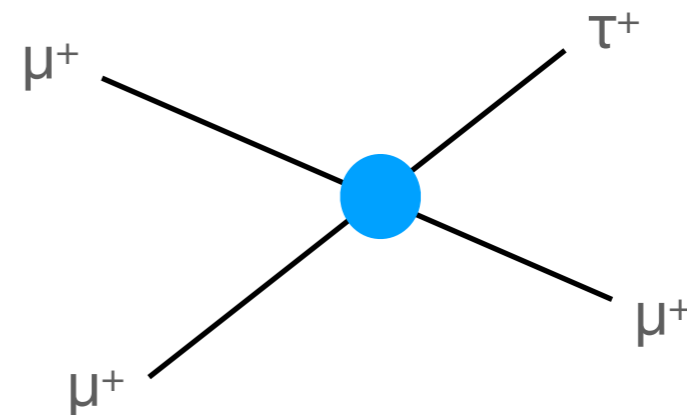
# Lepton number/flavor violation?

lepton number violation

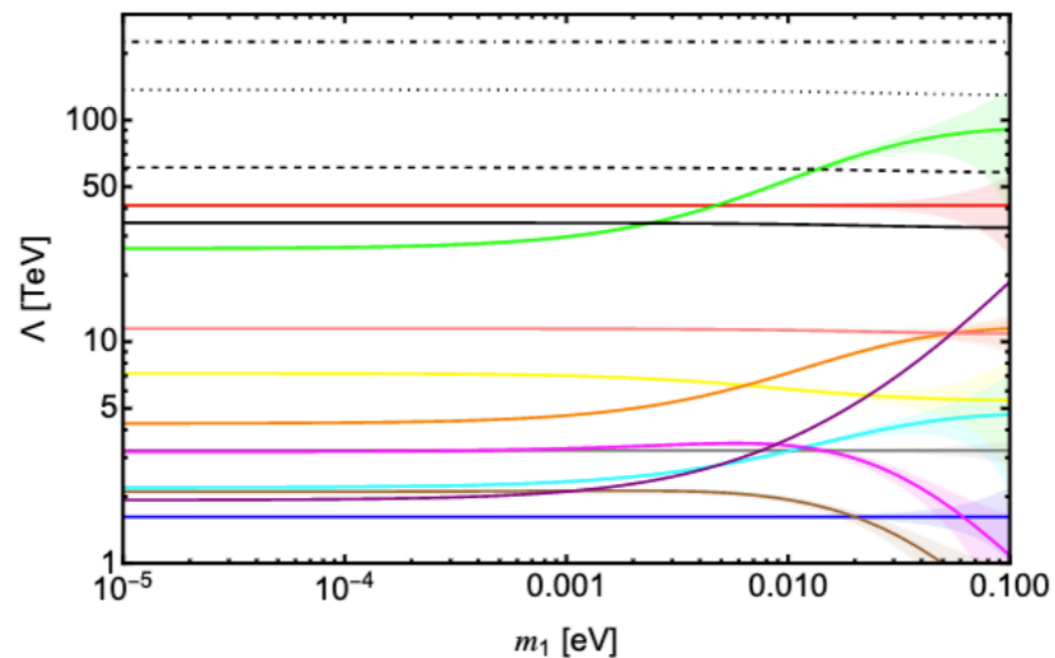


lepton flavor violation

[Fridell, RK and Takai '23]



Can be better than rare decays!



comparison with  $\mu \rightarrow 3e$  decay  
type-II seesaw model

- $\mu \rightarrow e\gamma$
- $\mu \rightarrow 3e$
- $\tau \rightarrow e\gamma$
- $\tau \rightarrow \mu\gamma$
- $\tau \rightarrow 3e$
- $\tau^- \rightarrow \mu^+ \mu^- e^-$
- $\tau^- \rightarrow e^+ \mu^- \mu^-$
- $\tau^- \rightarrow e^+ e^- \mu^-$
- $\tau^- \rightarrow \mu^+ e^- e^-$
- $\tau \rightarrow 3\mu$
- $M \rightarrow \bar{M}$
- 100 events (2 TeV, 1  $\text{ab}^{-1}$ )
- - - 10 events (2 TeV, 1  $\text{ab}^{-1}$ )
- ⋯⋯⋯ 100 events (10 TeV, 10  $\text{ab}^{-1}$ )
- ⋯⋯⋯ elastic (2 TeV, 1  $\text{ab}^{-1}$ )

# Summary

We are not satisfied with the current understanding of particle physics. Too much unknowns. Full of mysteries.

$\mu^+$  may have a chance. Interesting to consider a km size experiment as a relatively near future project.

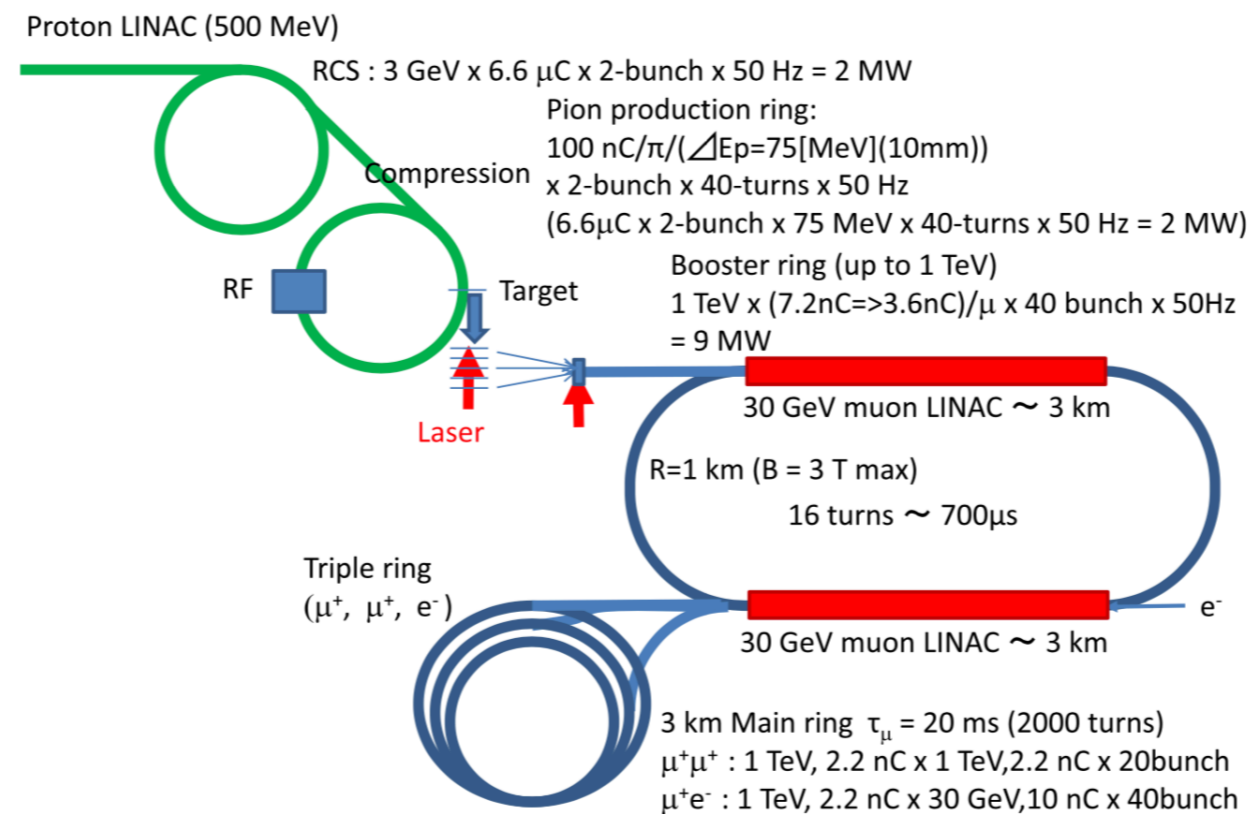


Fig. 1. Conceptual design of the  $\mu^+e^-/\mu^+\mu^+$  collider.