

Muon cooling at PSI

Giuseppe Lospalluto (ETH Zürich)

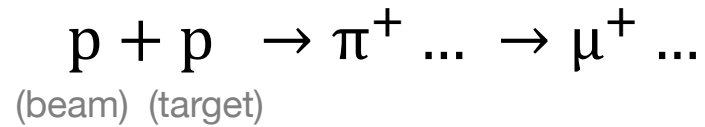
On the behalf of the muCool collaboration

Muon4Future, Venice

29 May 2023

Muon beamline at PSI

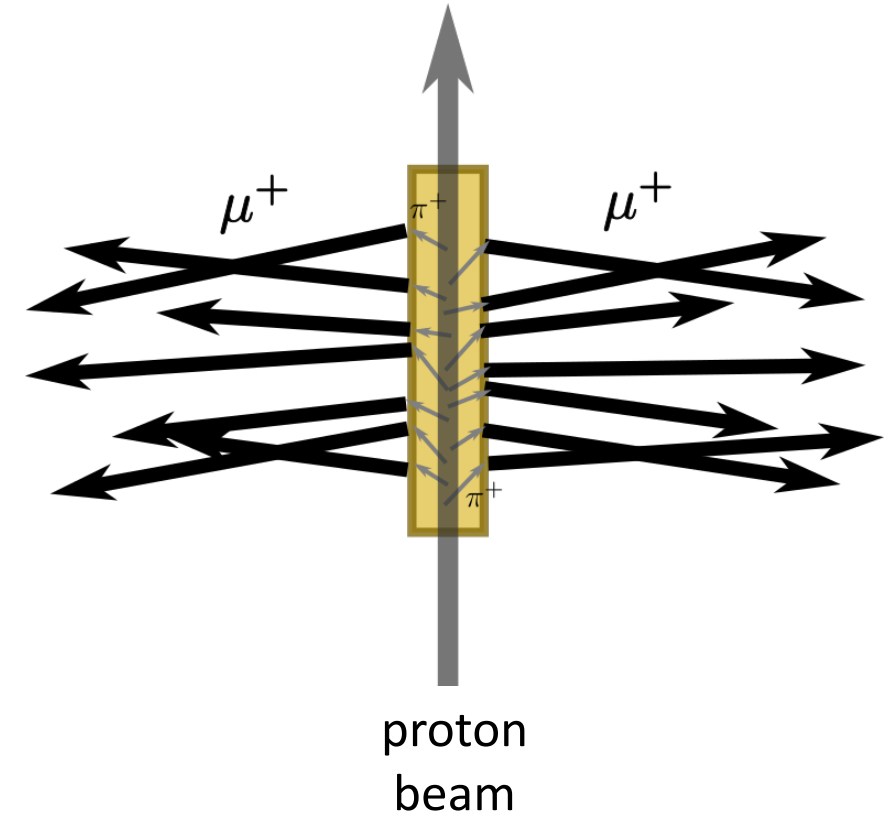
- High intensity cw positive muon beam (4.1 MeV) at the Paul Scherrer Institut (PSI)



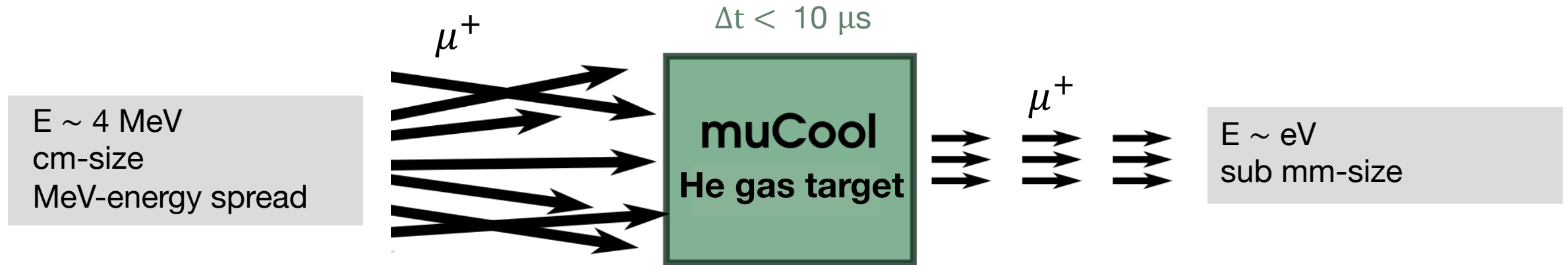
- What for?
e.g. Rare muon decay searches ($\mu^+ \rightarrow e^+ \gamma$, $\mu^+ \rightarrow e^+ e^- e^+$)

High “rate”, poor “quality”

- For several precision experiments “quality” is important
- How can we cool a muon beam? ($\tau_\mu = 2.2 \mu\text{s}$)



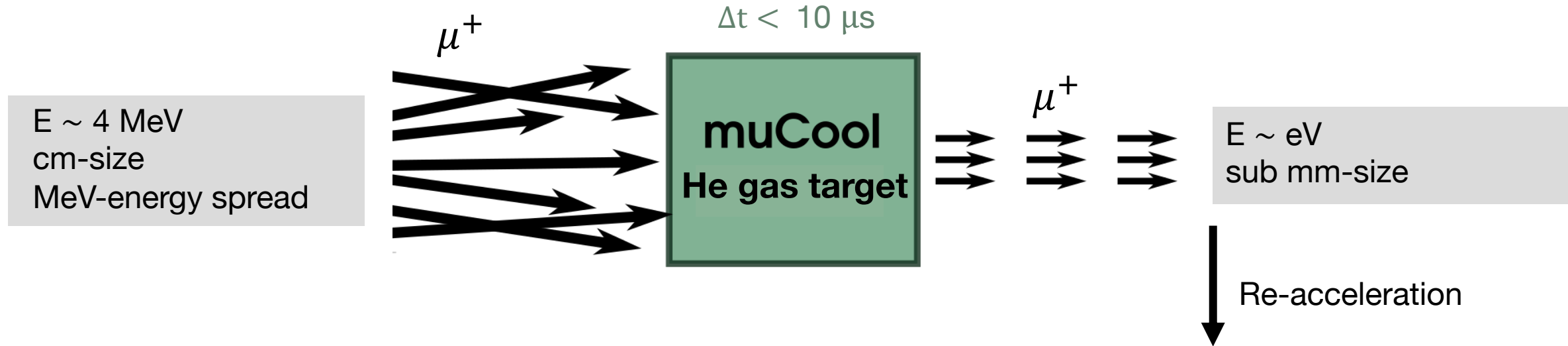
muCool : “fast” phase space compression



- Efficiency of $10^{-4} - 10^{-5}$
- Phase space improved by $> 10^8$

D. Taqqu. *Phys. Rev. Lett.* 97.194801 (2006)

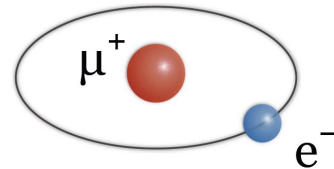
muCool : “fast” phase space compression



- Efficiency of $10^{-4} - 10^{-5}$
- Phase space improved by $> 10^8$

keV energies

- Muonium spectroscopy, muonium gravity experiments
- Material Science (μSR)



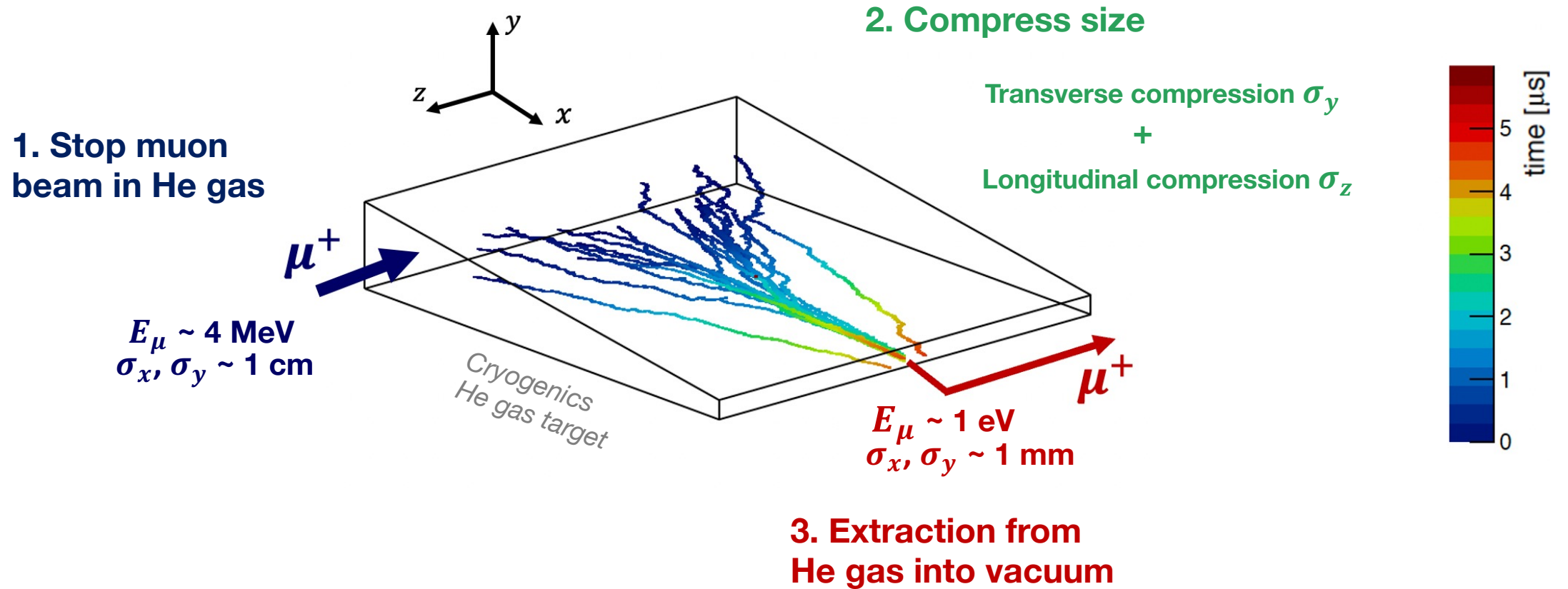
MeV energies

- Muon g-2/EDM with storage ring

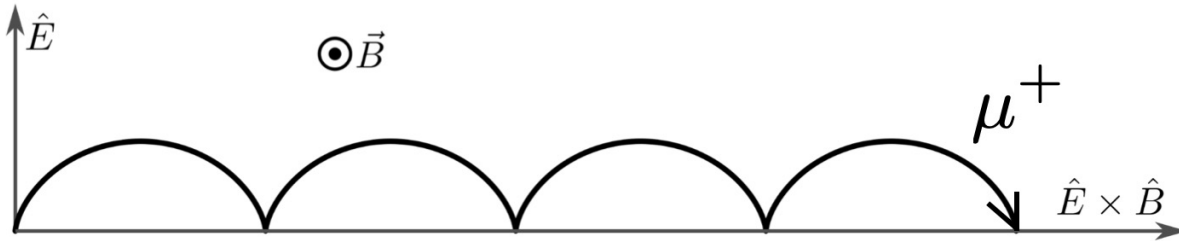
D. Taqqu. *Phys. Rev. Lett.* 97.194801 (2006)

muCool scheme

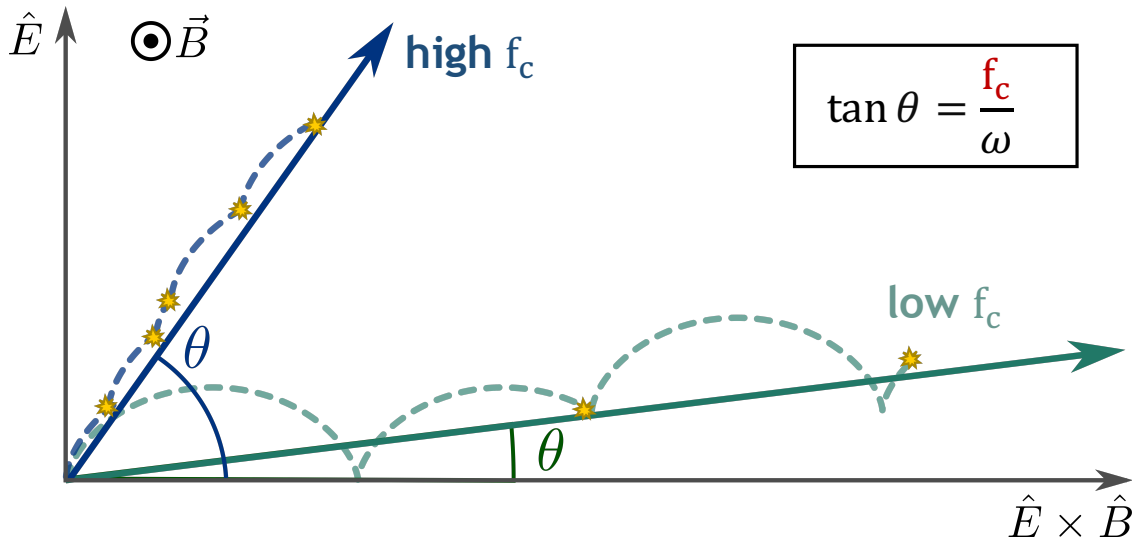
- Complex E-fields and B-field + density gradient compress the muon beam



Muon drift in crossed E and B-fields



In vacuum

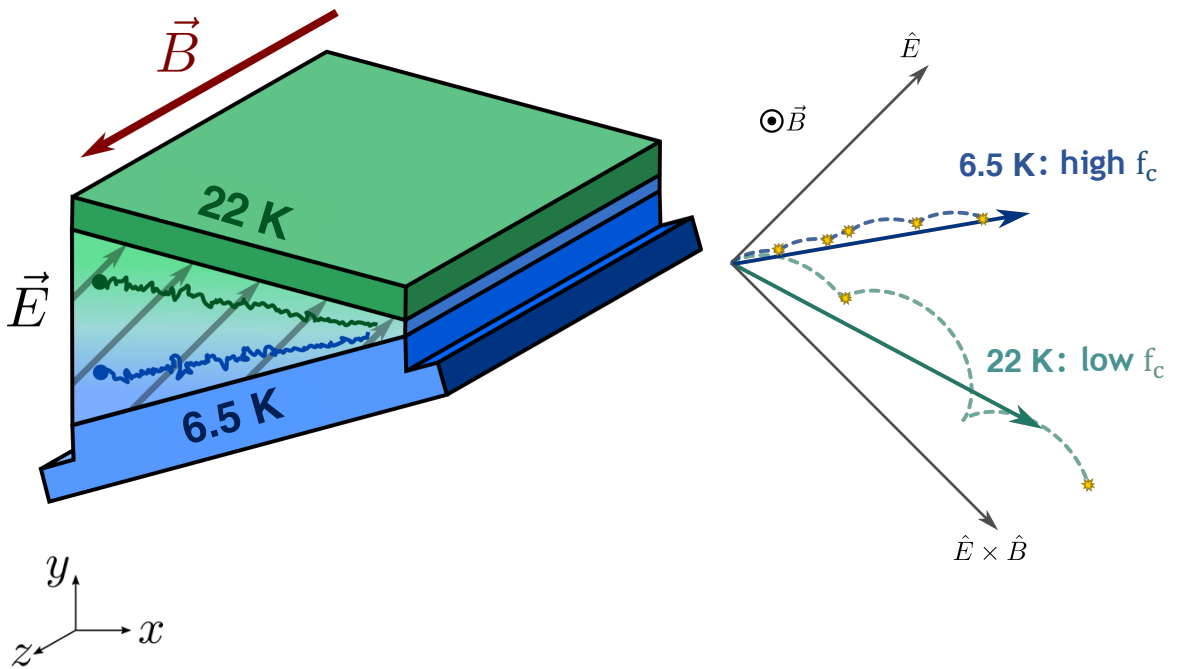


In gas

★ Collision with gas atoms at frequency f_c

muCool principle

Transverse Compression



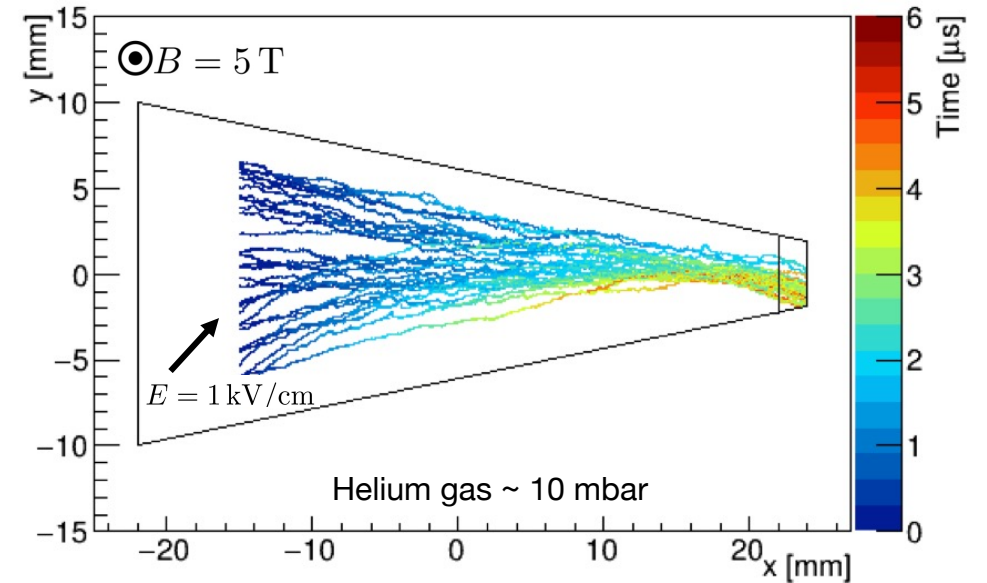
Drift velocity

$$\vec{v}_D = \frac{\mu E}{1 + \frac{w^2}{f_c^2}} \left(\hat{E} + \frac{w}{f_c} \left(\hat{E} \times \hat{B} \right) + \frac{w^2}{f_c^2} \left(\hat{E} \cdot \hat{B} \right) \hat{B} \right)$$

$= 0$

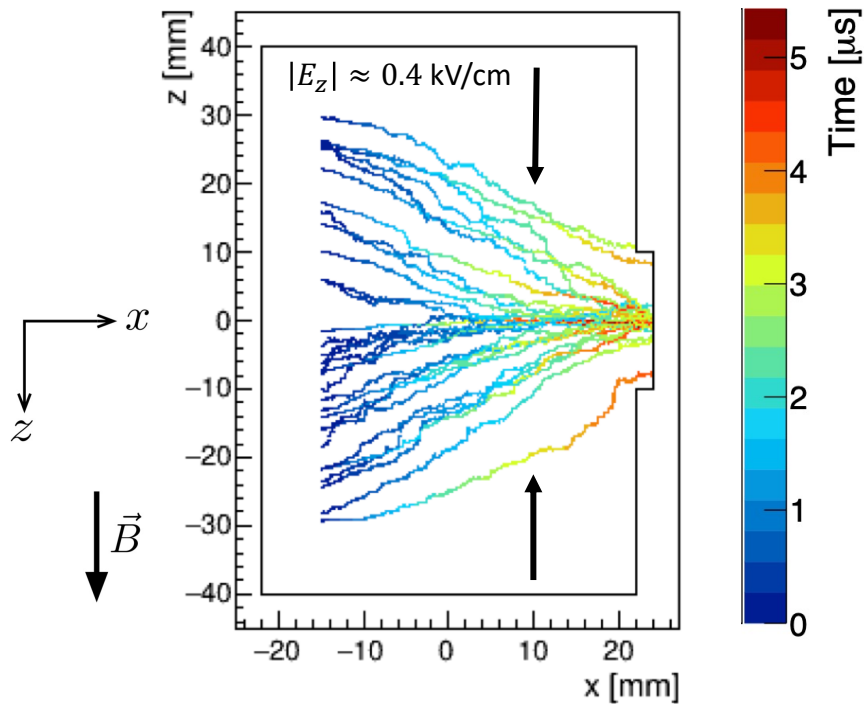
μ : muon mobility
 w : cyclotron frequency
 f_c : frequency of muon-He gas collisions

Simulated muon trajectories

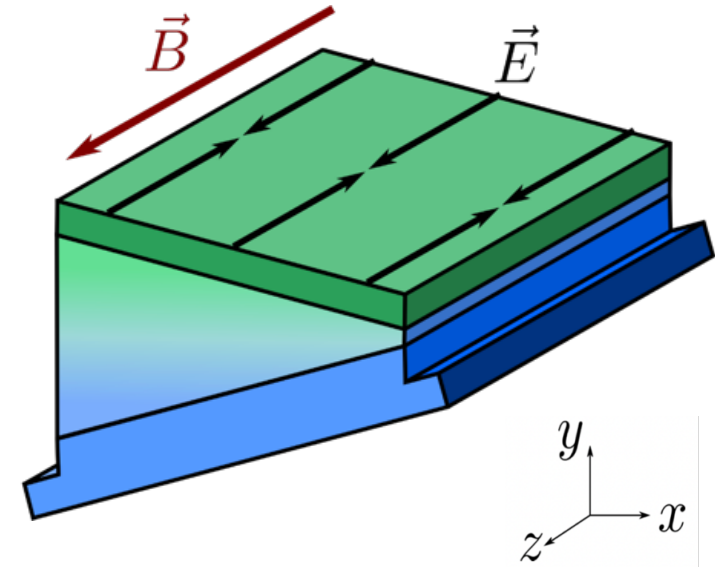


muCool principle

Simulated muon trajectories



Longitudinal Compression



Drift velocity

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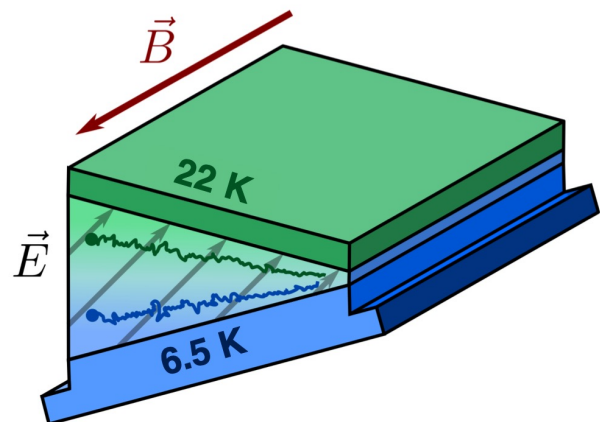
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Belosevic, I. et al. *Eur. Phys. J. C* 79:430 (2019)

Y. Bao et al. *Phys. Rev. Lett.* 112:224801 (2014)

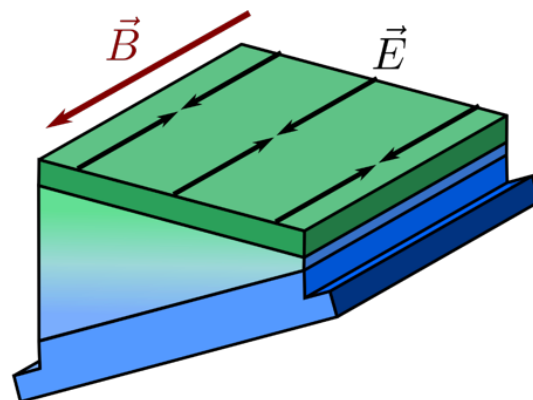
muCool principle

Transverse Compression



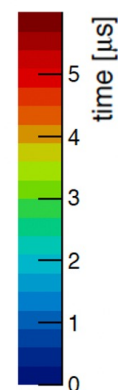
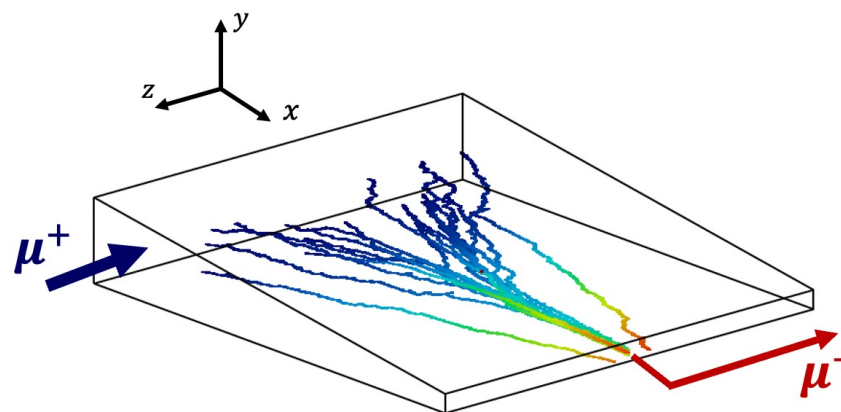
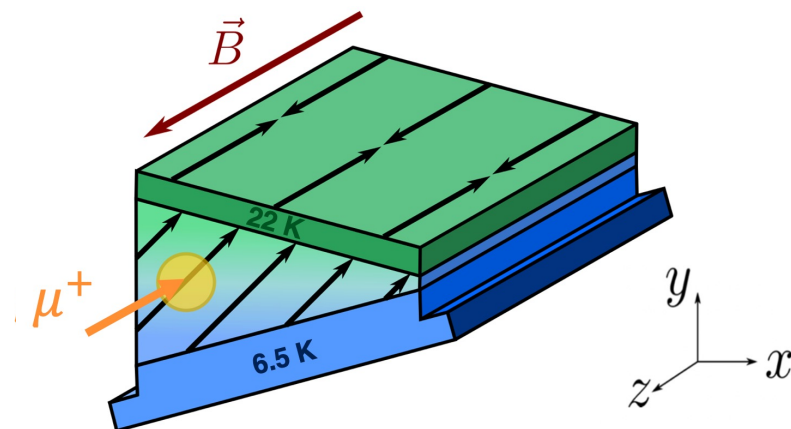
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Longitudinal Compression



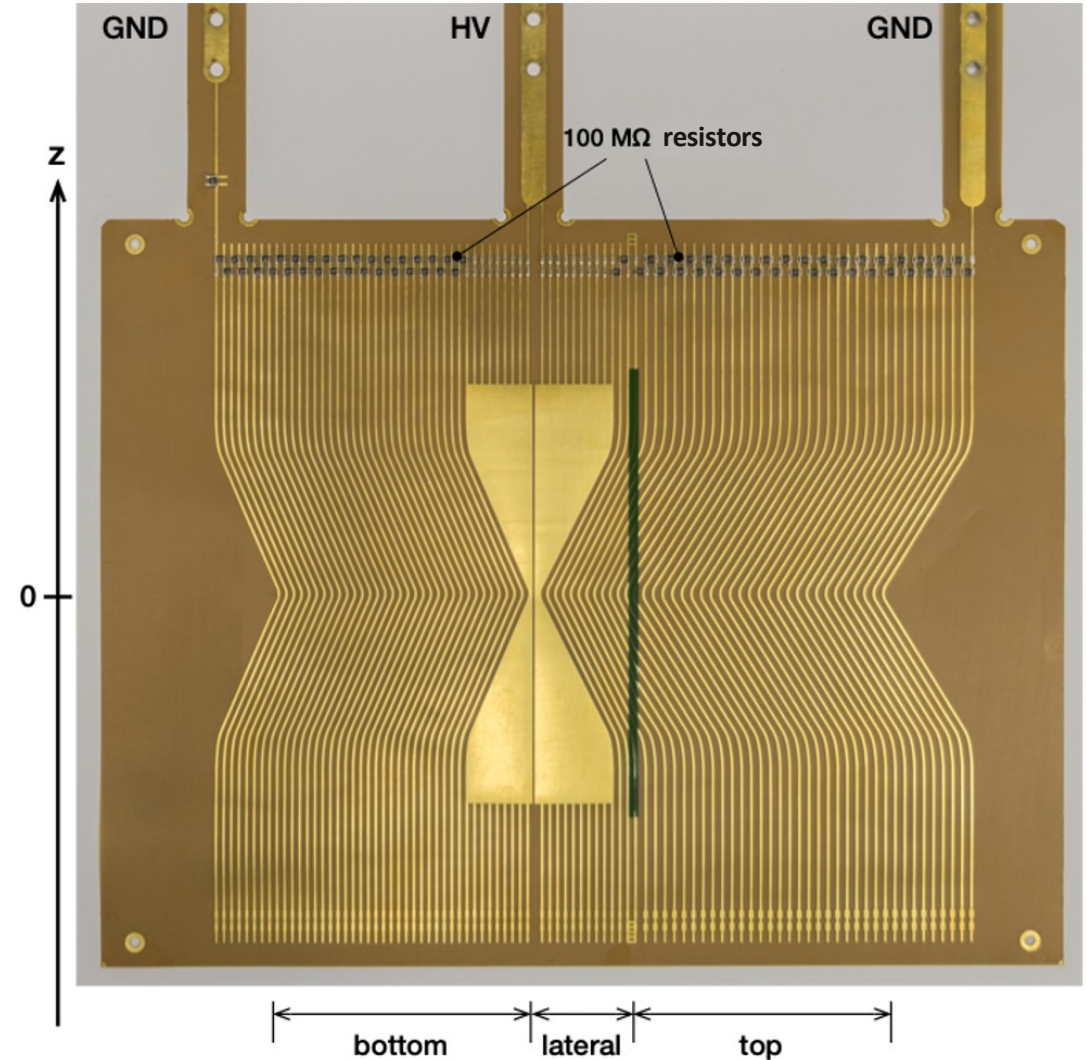
=

Mixed Compression



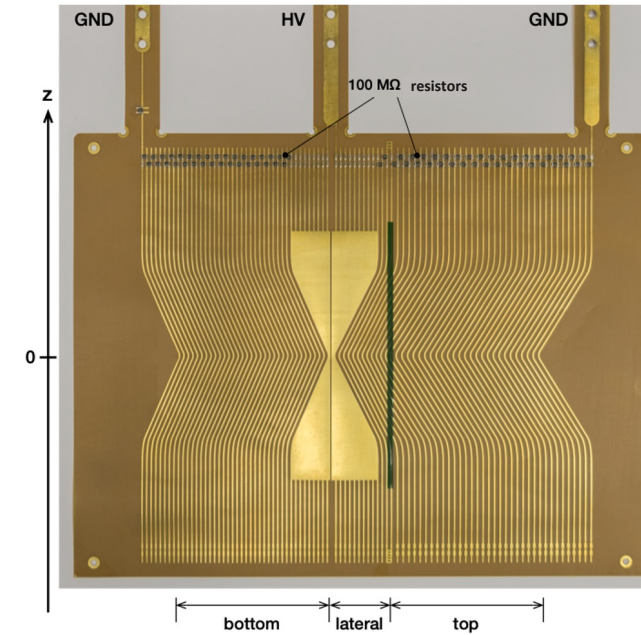
Target realisation

- Lined Kapton-foil: Electric field for mixed compression



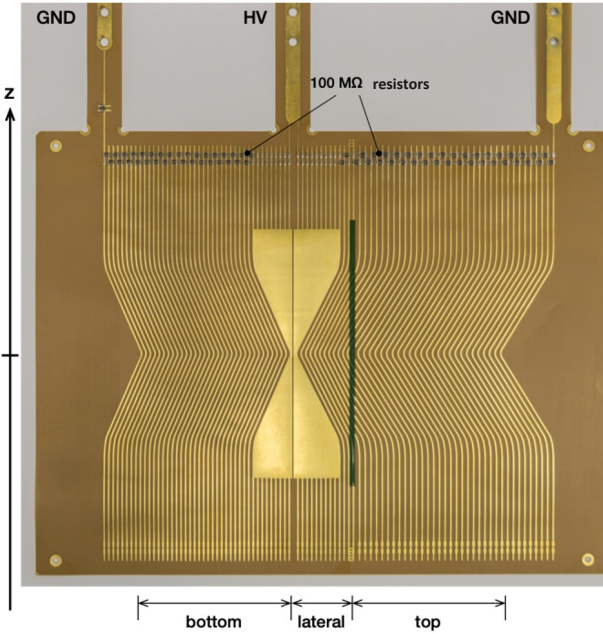
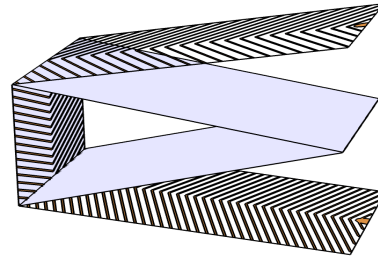
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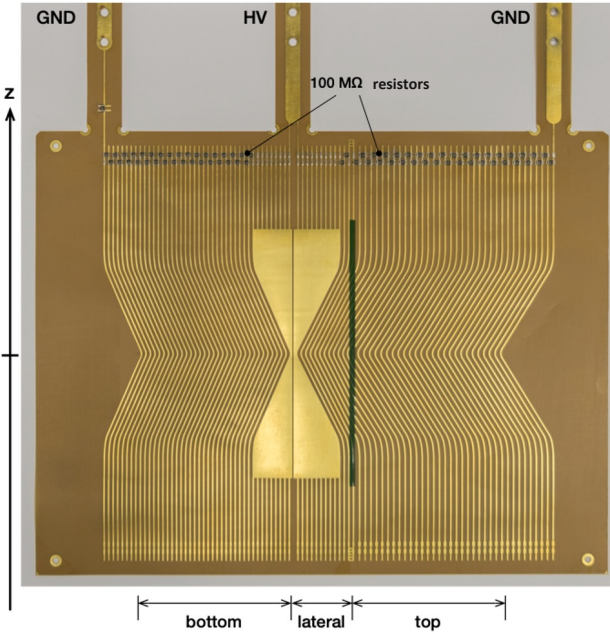
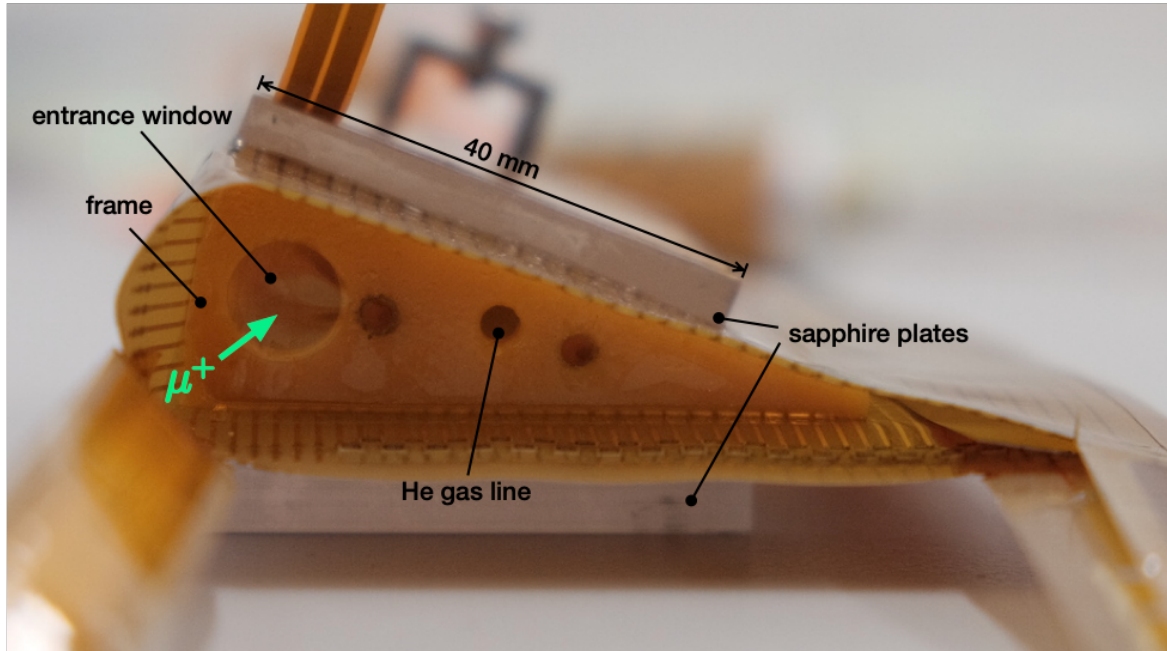
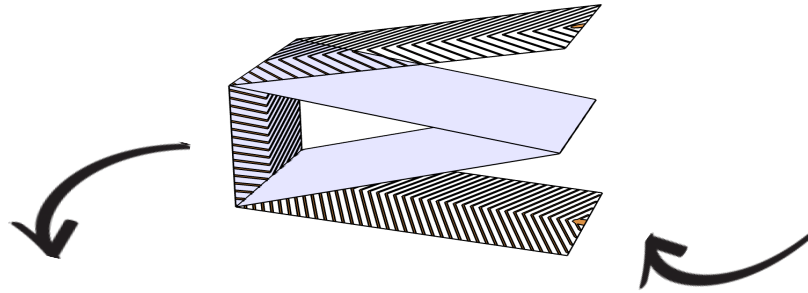
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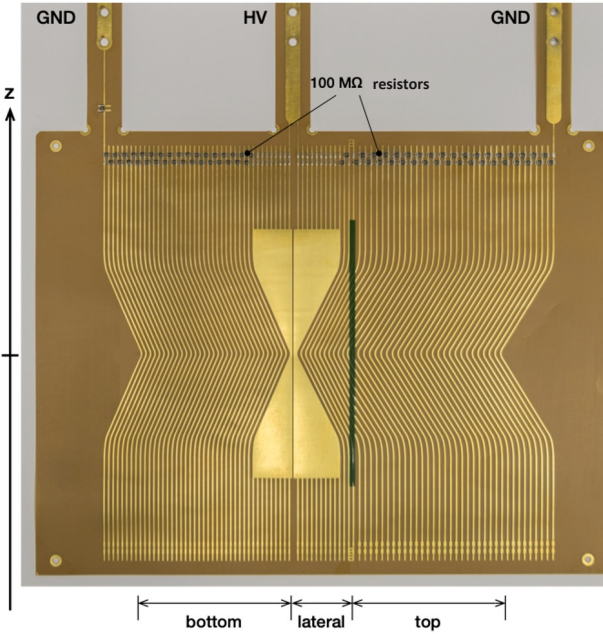
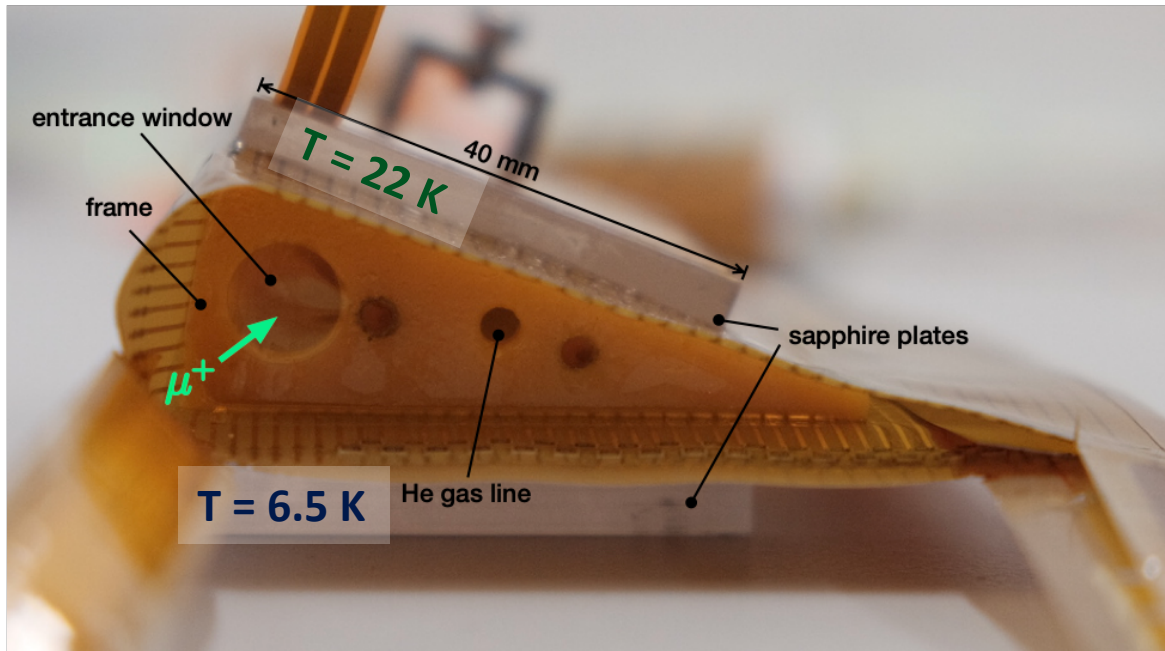
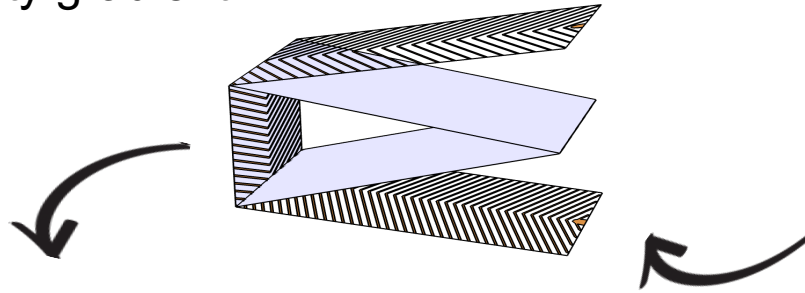
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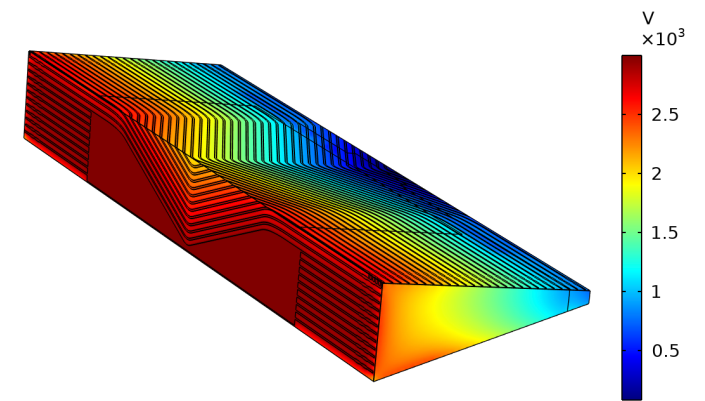
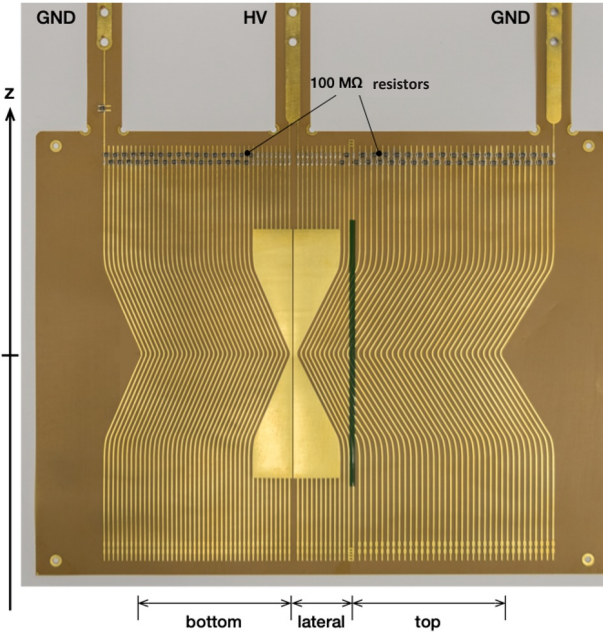
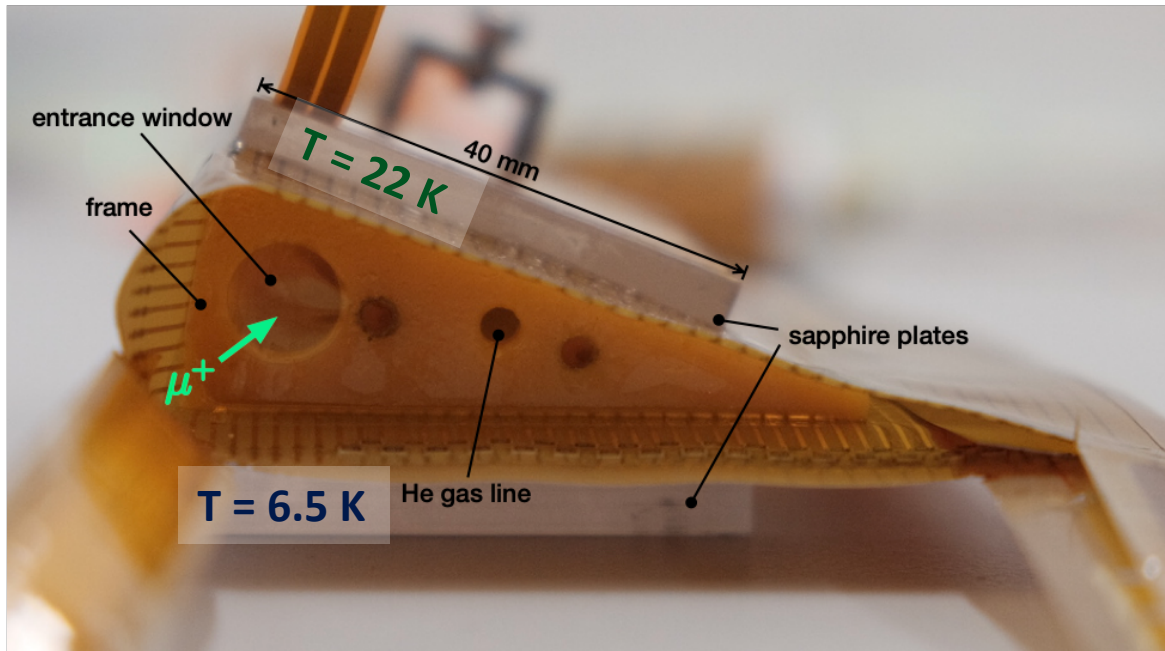
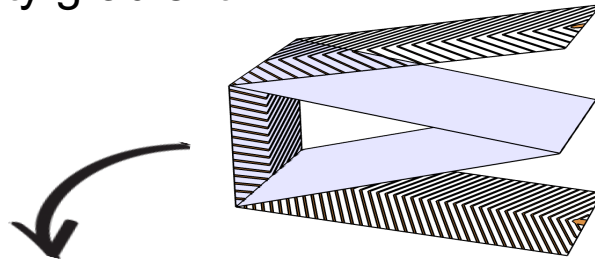
Target realisation

- Lined Kapton-foil: Electric field for mixed compression
- Sapphire plates: Vertical density gradient



Target realisation

- Lined Kapton-foil: Electric field for mixed compression
- Sapphire plates: Vertical density gradient

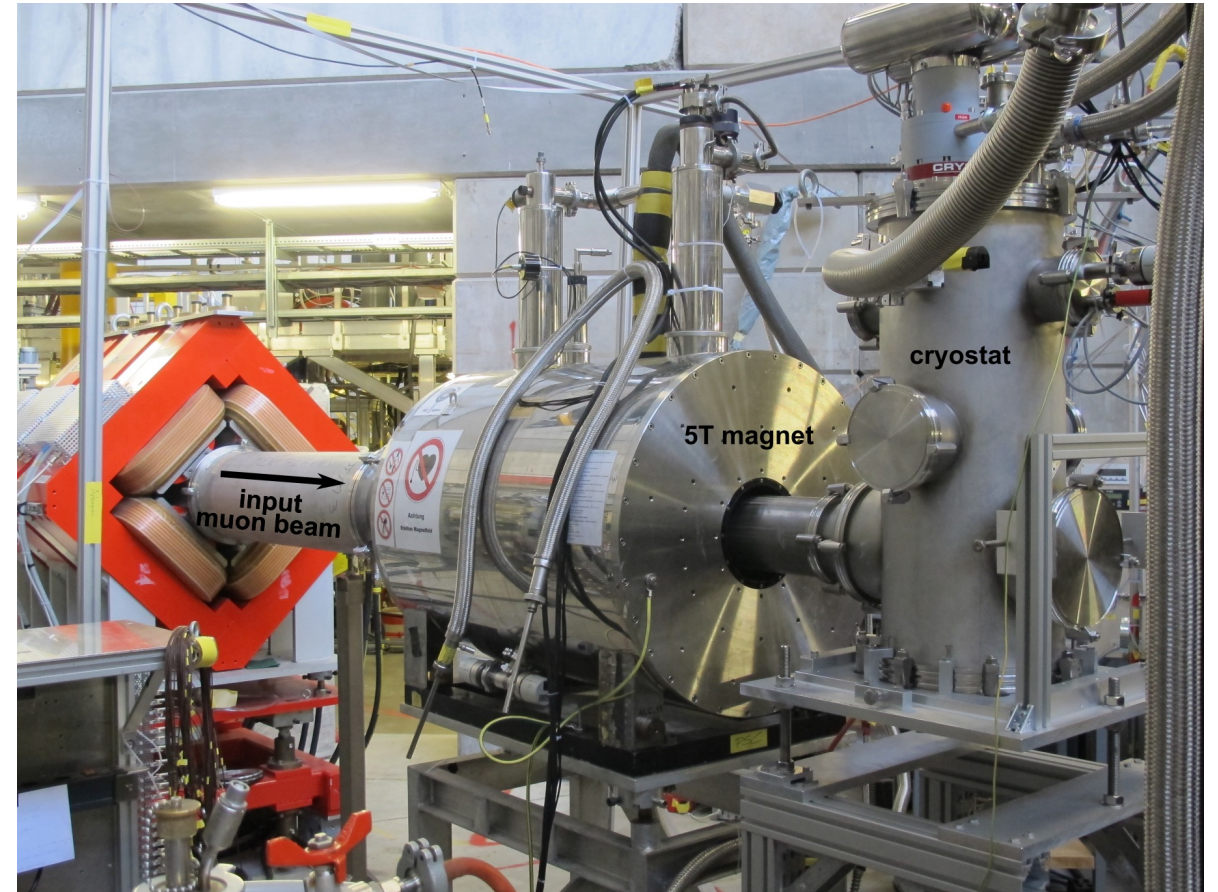
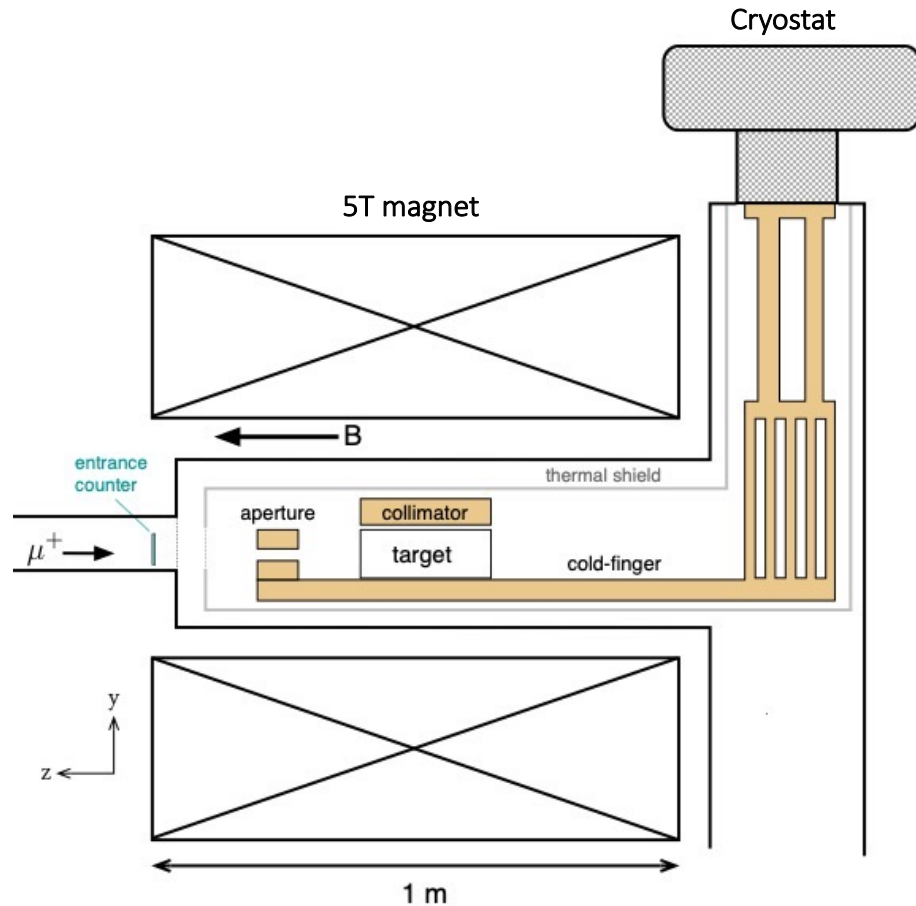


Electric potential simulation

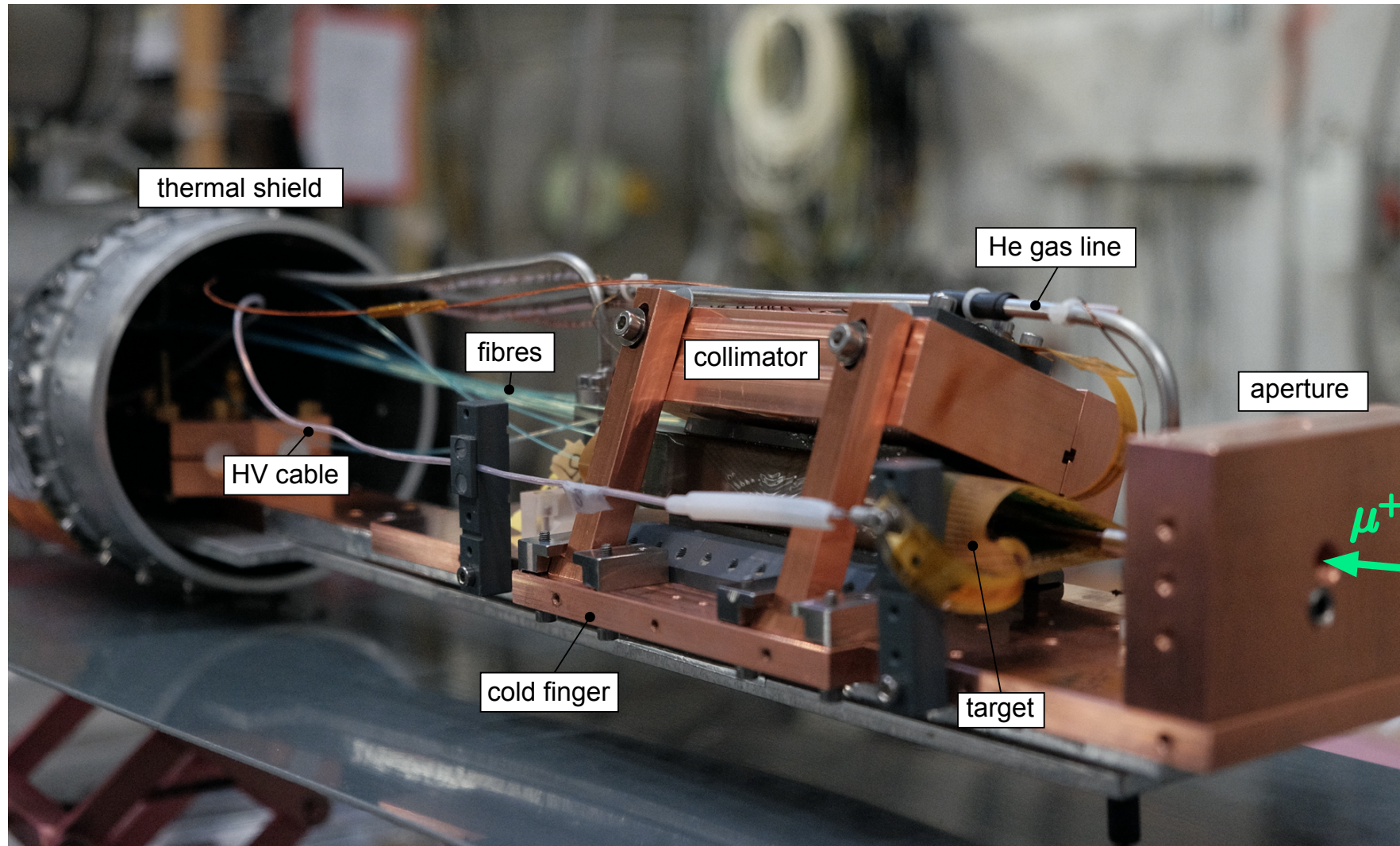
Experiment

Test of mixed compression (2019)

- PSI π E1 beamline
- Momentum tuned ~ 15 MeV/c

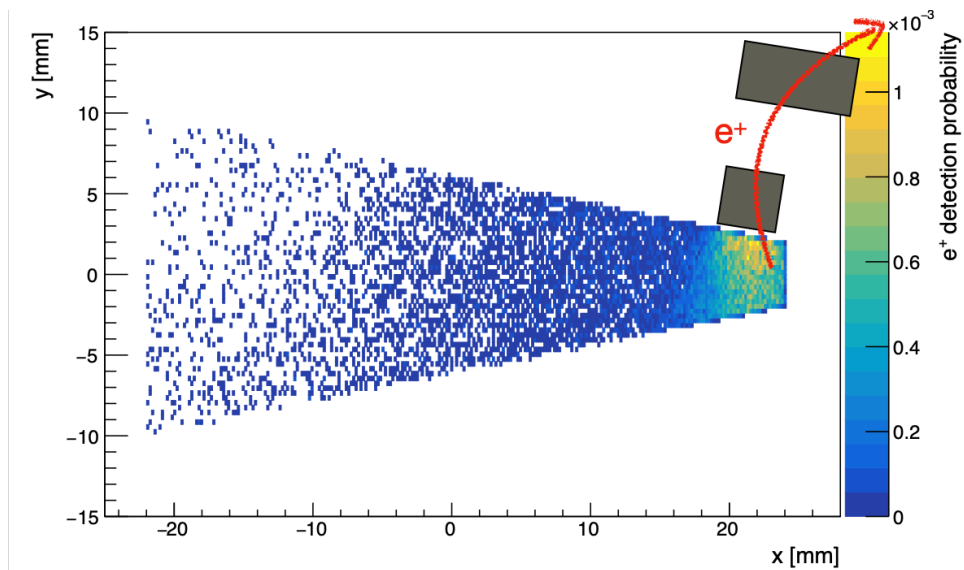
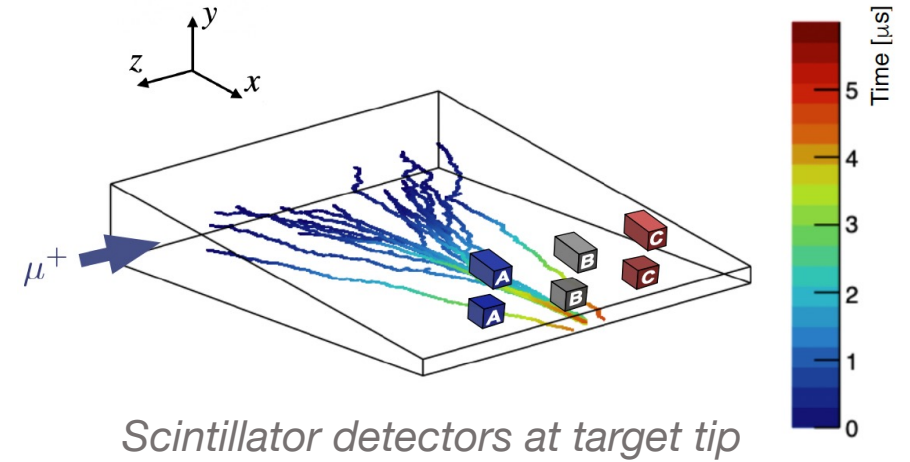


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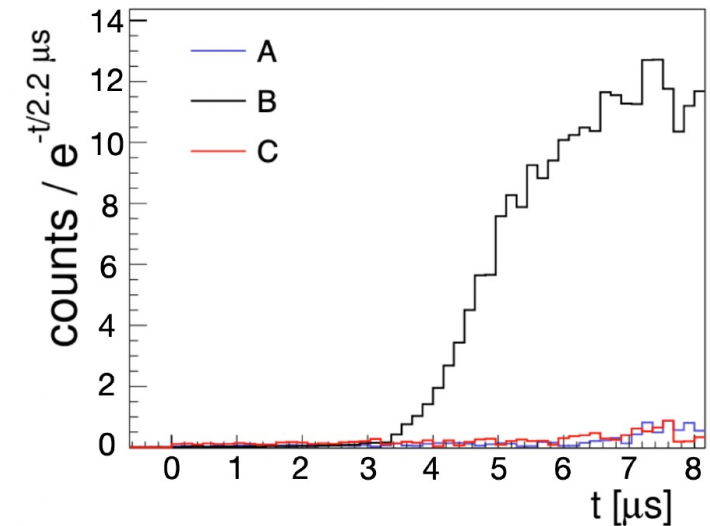


Test of mixed compression

- “Indirectly” measure muon position by detecting decay positrons
- $t = 0$ given by entrance counter
- Large increase of counts: all muons reached target tip



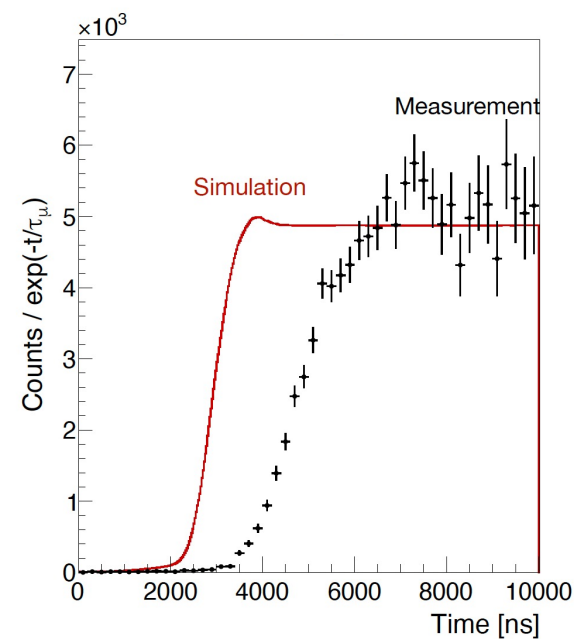
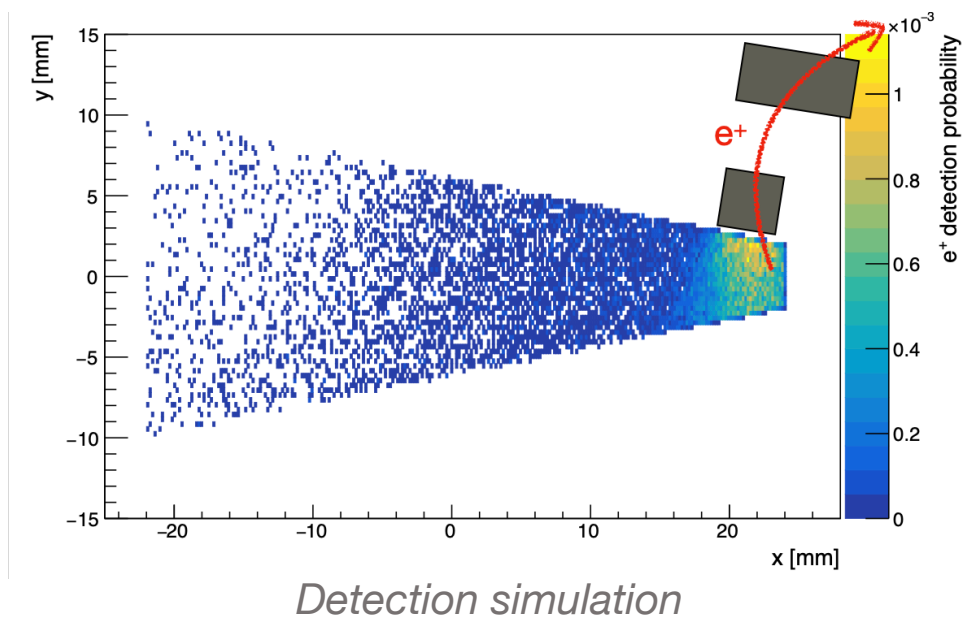
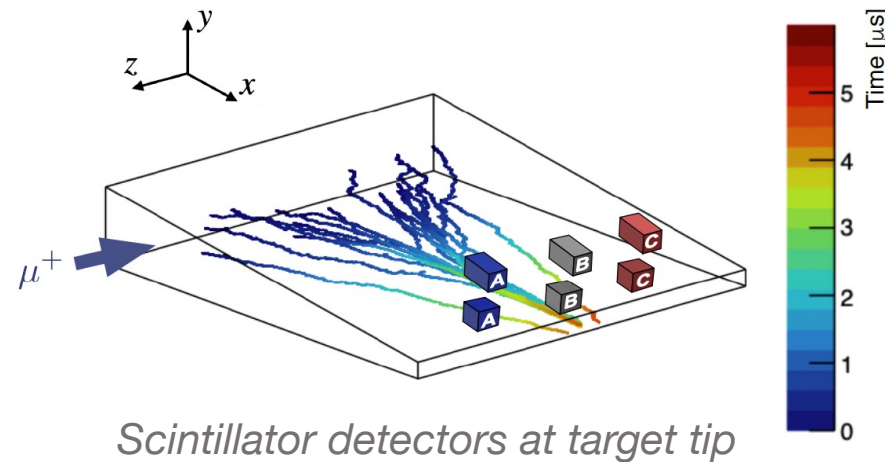
Detection simulation



Measured time spectra (2019 beamtime)

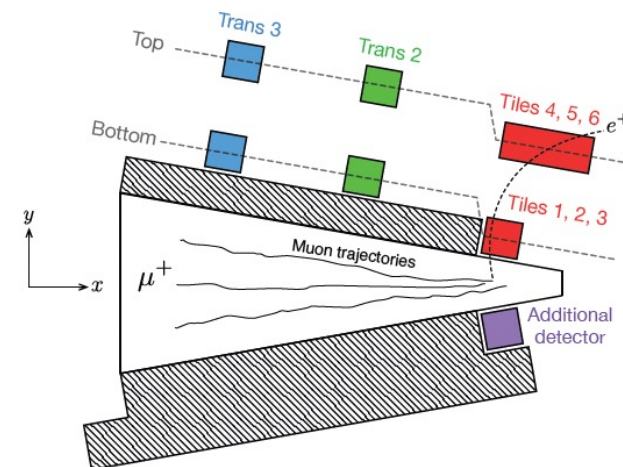
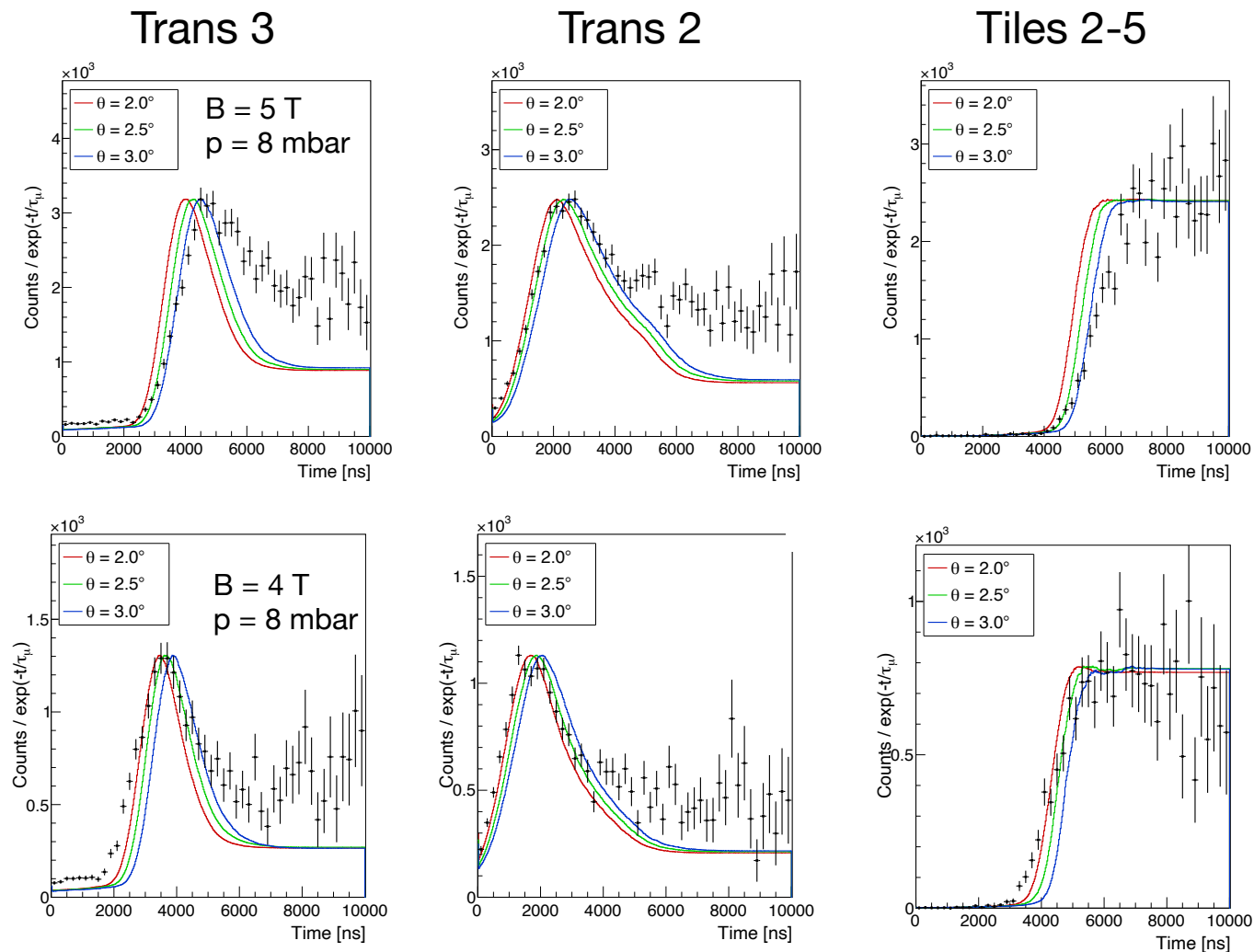
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observed
tension?

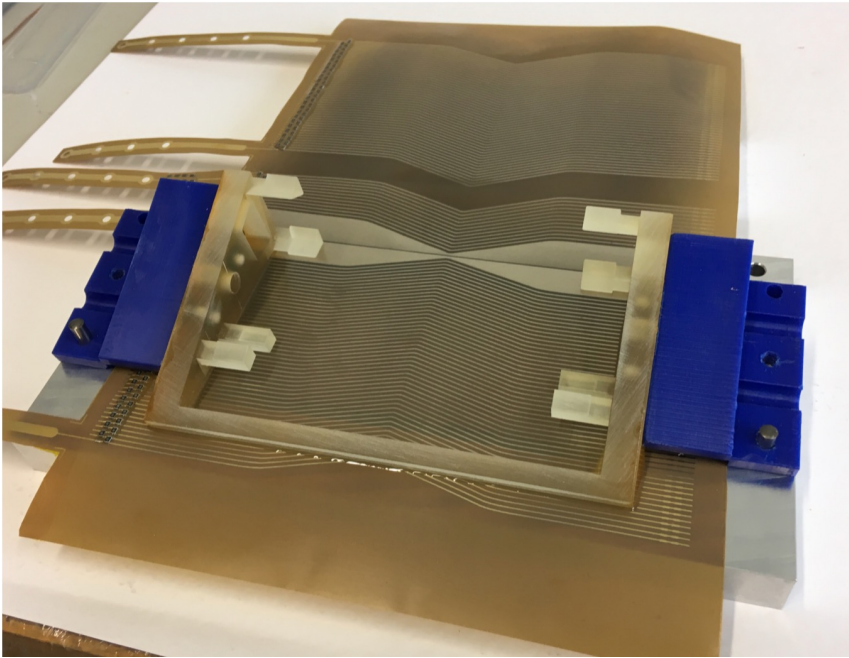
Tuning target parameters



Good agreement between simulations and measurements

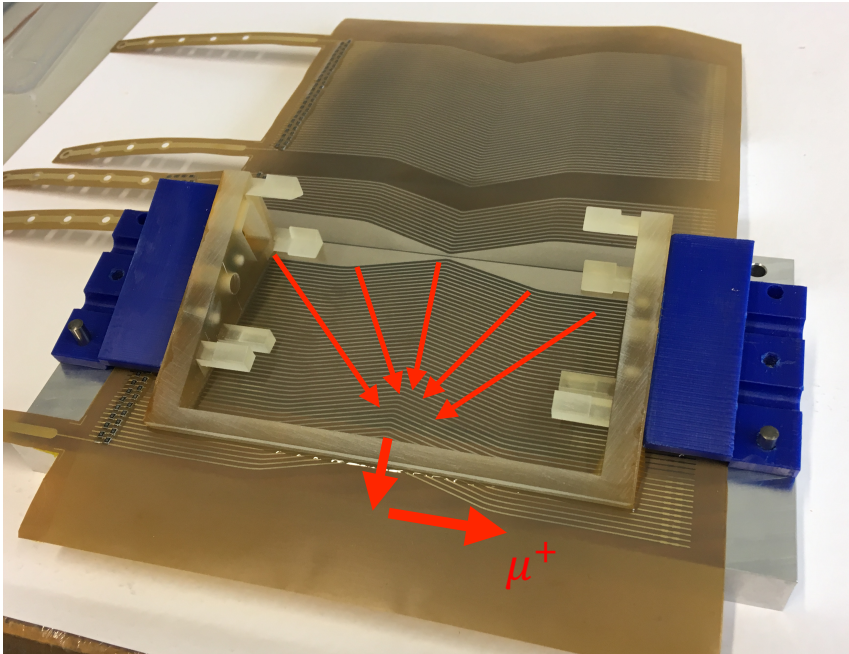
- For “realistic” tuning of the target conditions
- For several detectors
- For several conditions (E, B, p)

Next steps?



Open up muCool target

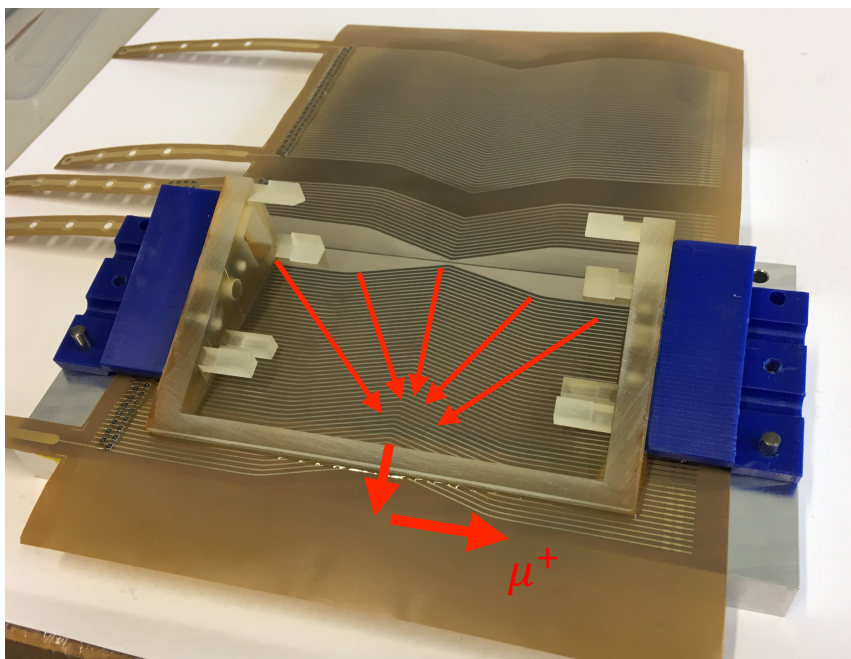
Next steps?



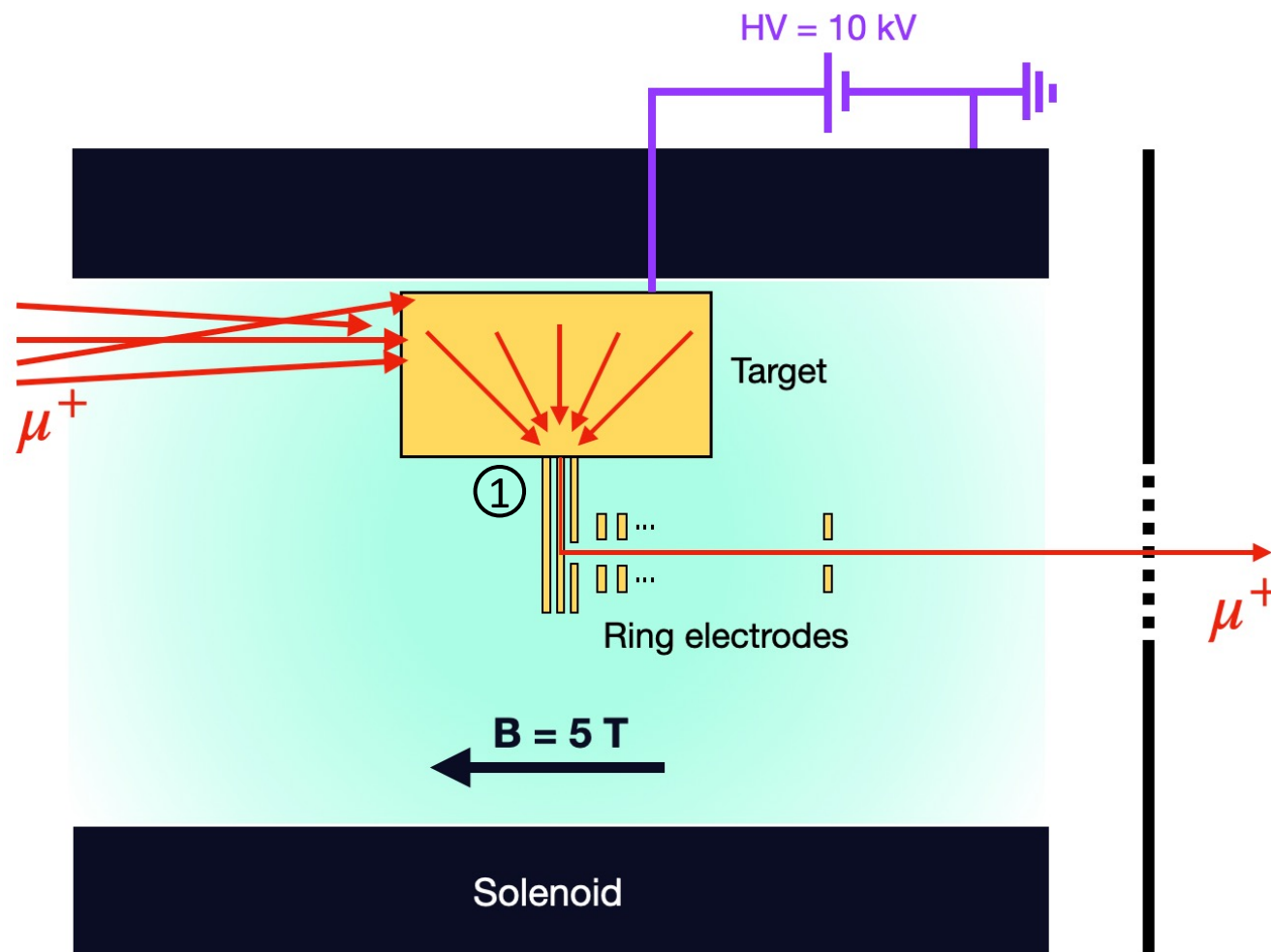
Make a hole and extract muons

Next steps?

- ① Muon extraction from gas target into vacuum via tiny orifice (eV energy muons)

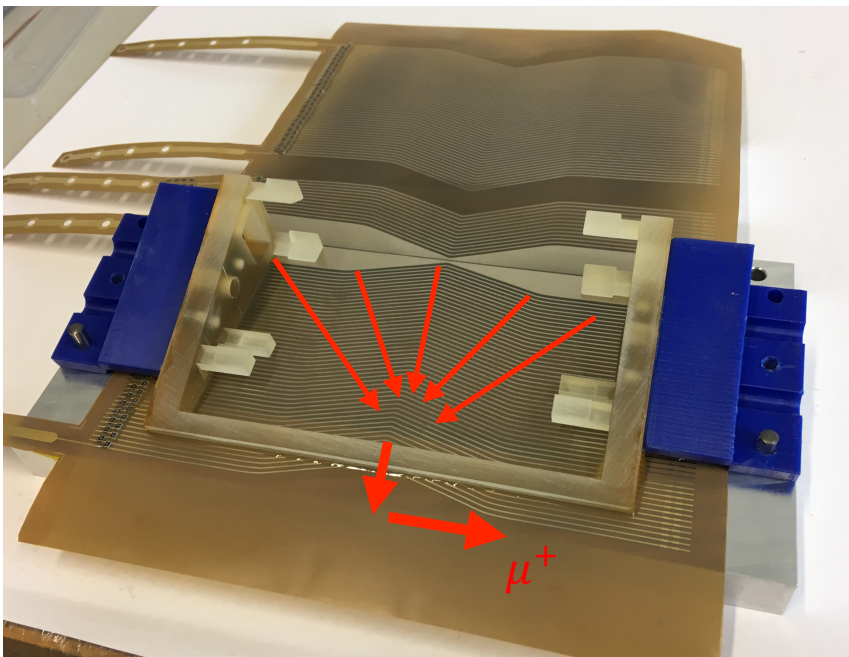


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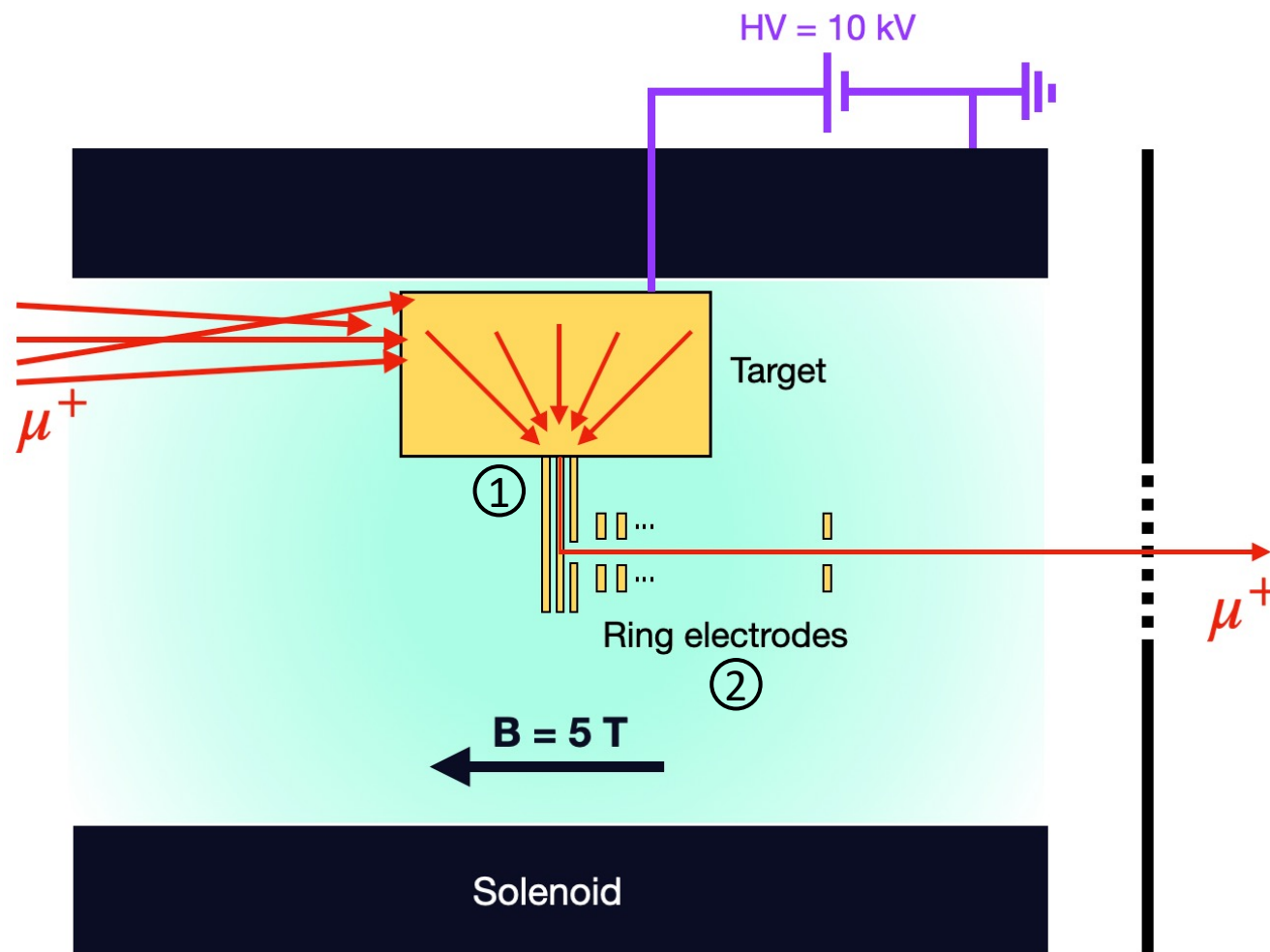


Next steps?

- ① Muon extraction from gas target into vacuum via tiny orifice (eV energy muons)
- ② Re-acceleration to 10 keV

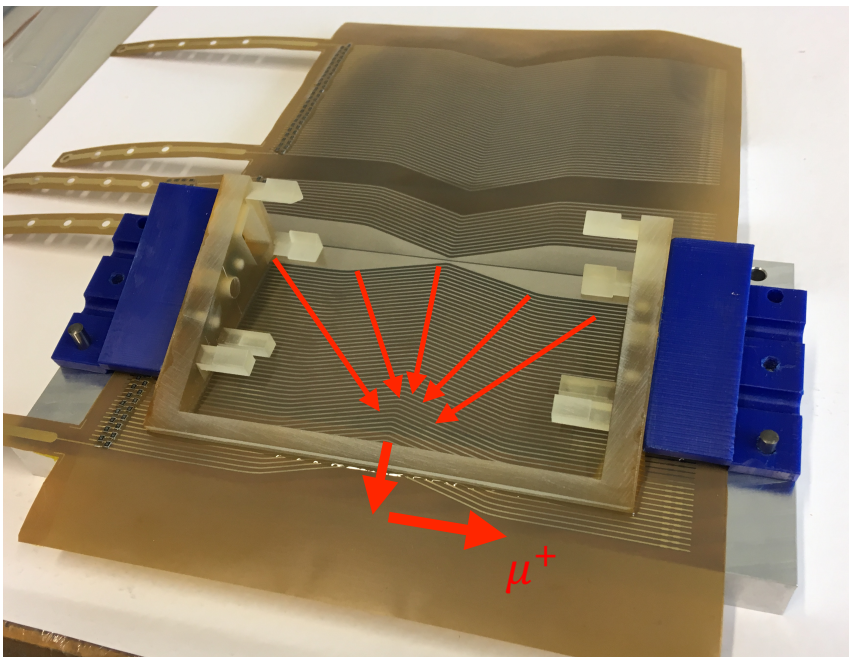


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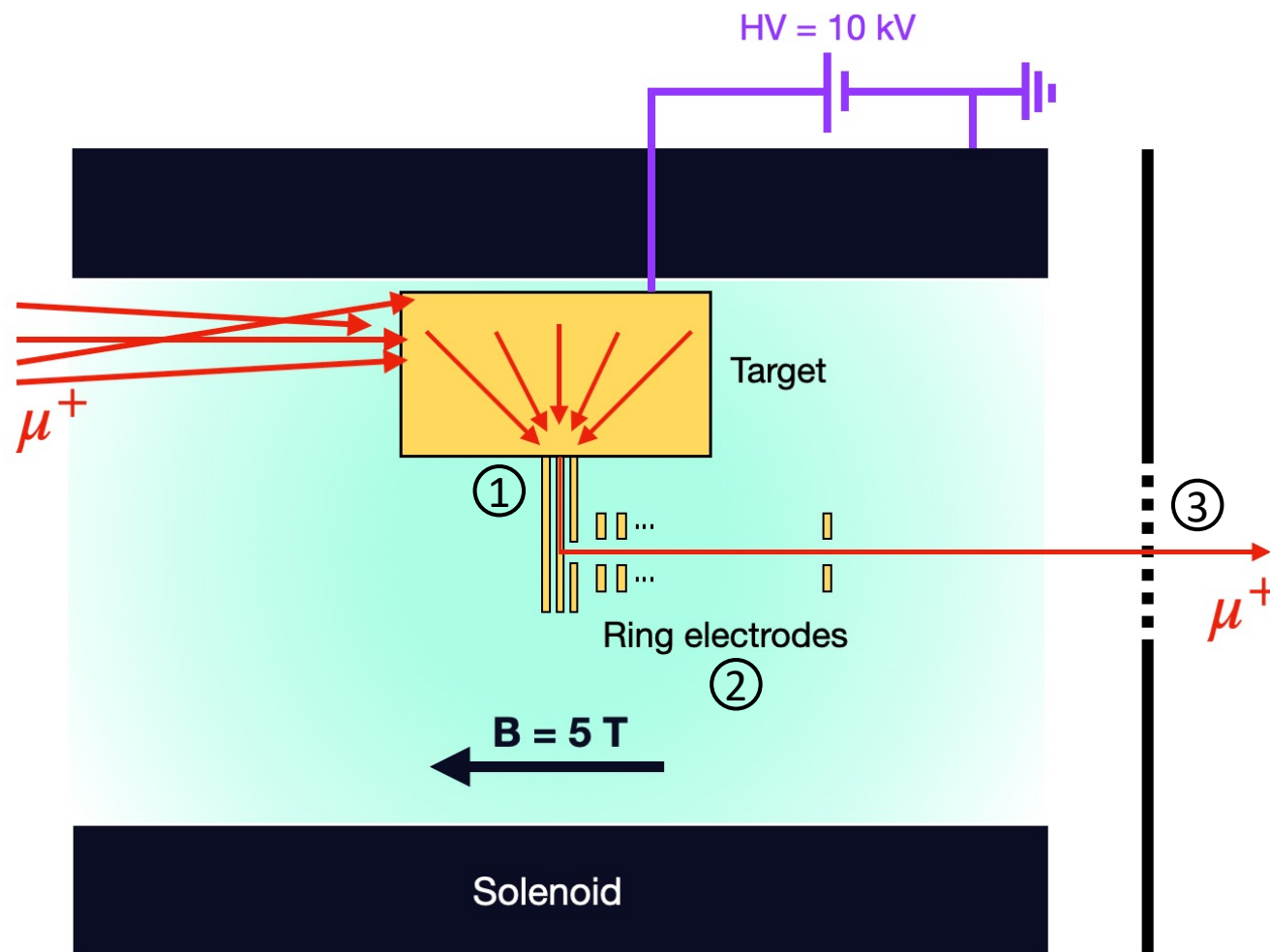


Next steps?

- ① Muon extraction from gas target into vacuum via tiny orifice (eV energy muons)
- ② Re-acceleration to 10 keV
- ③ Extraction from 5T solenoid

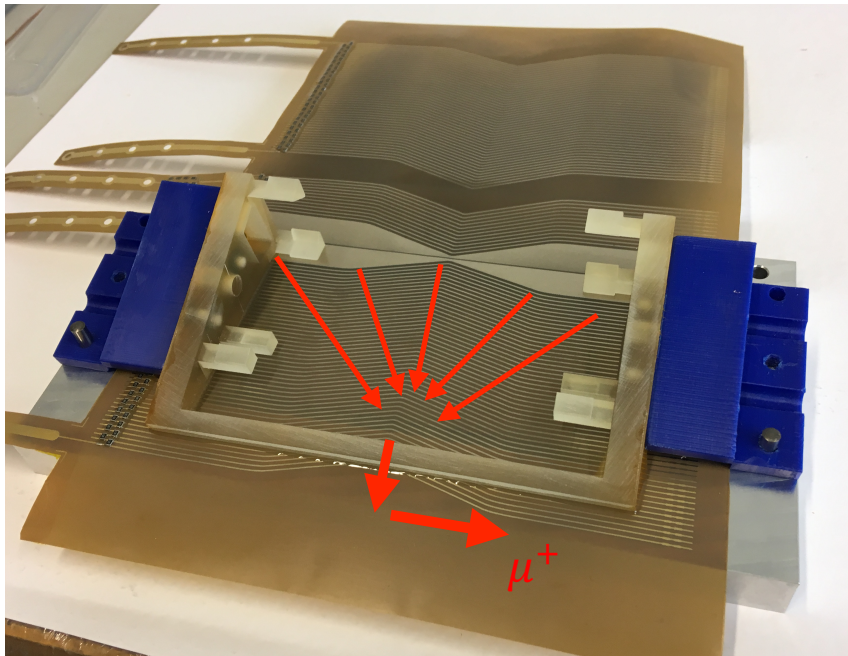


Make a hole and extract muons

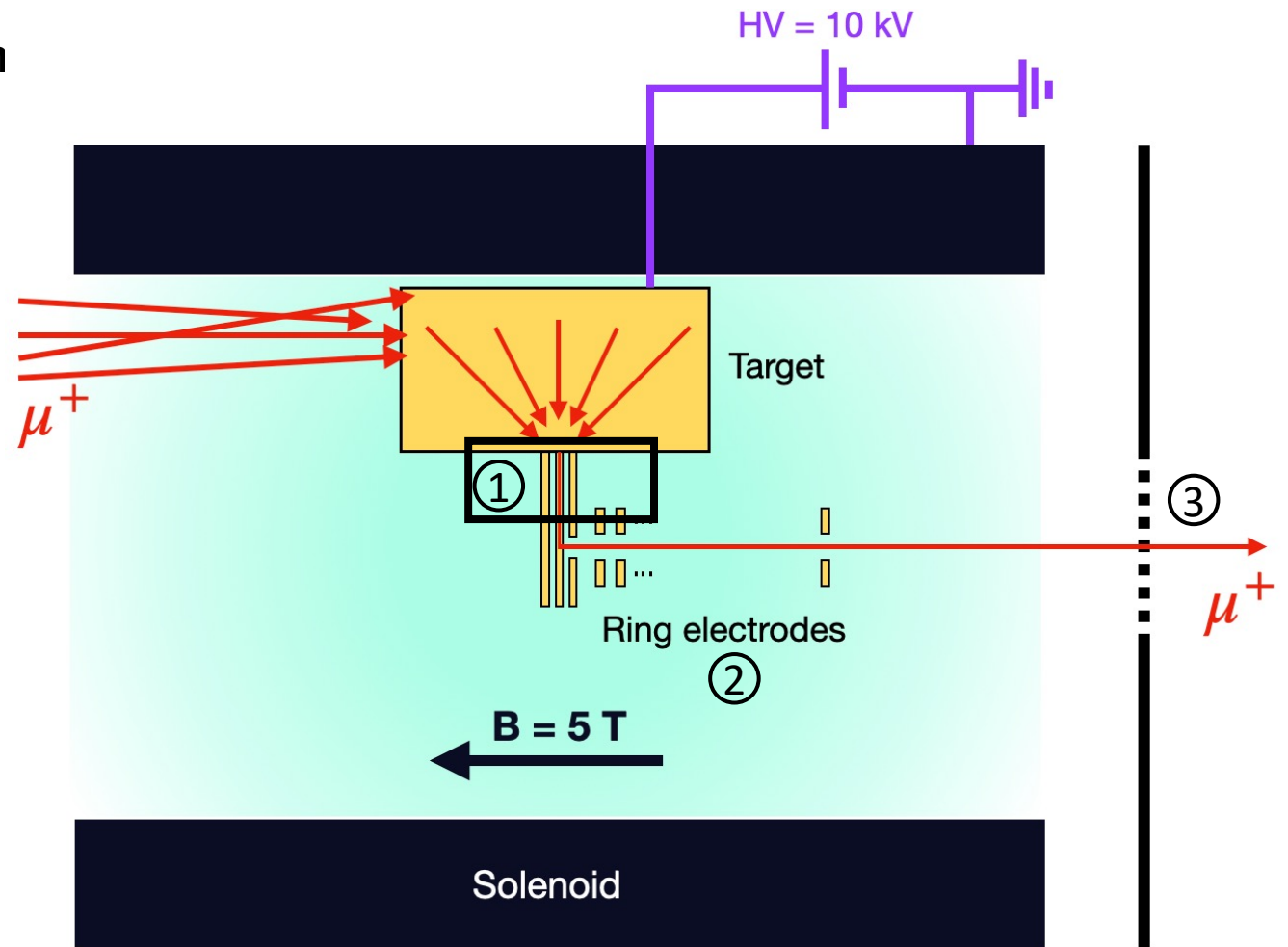


Next steps?

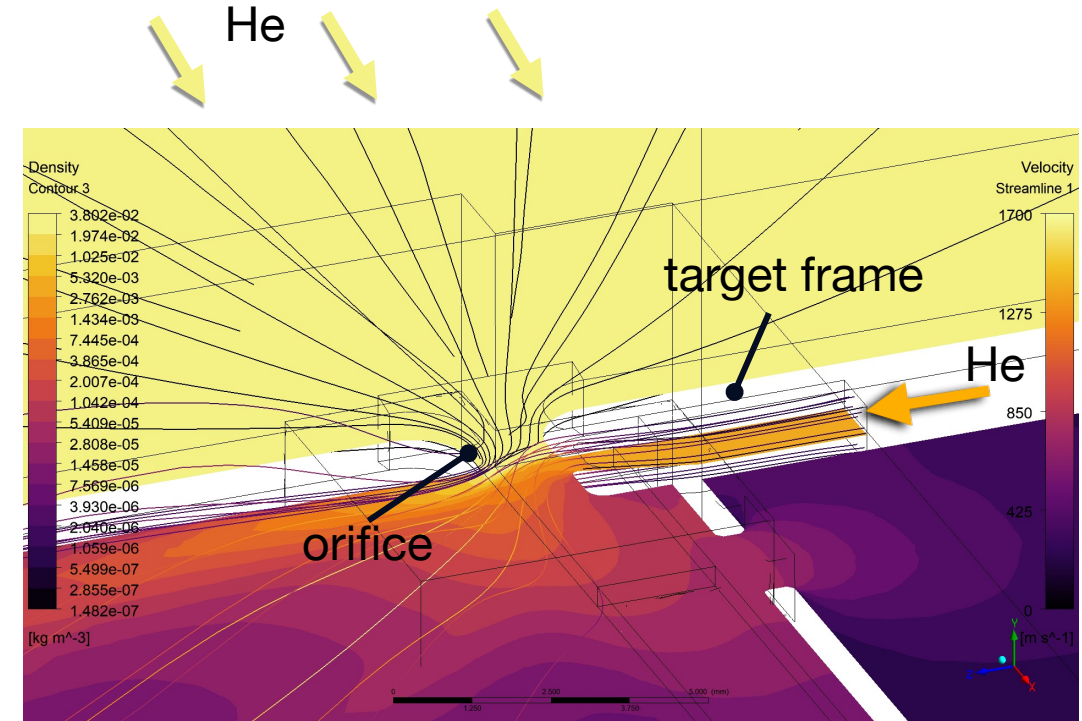
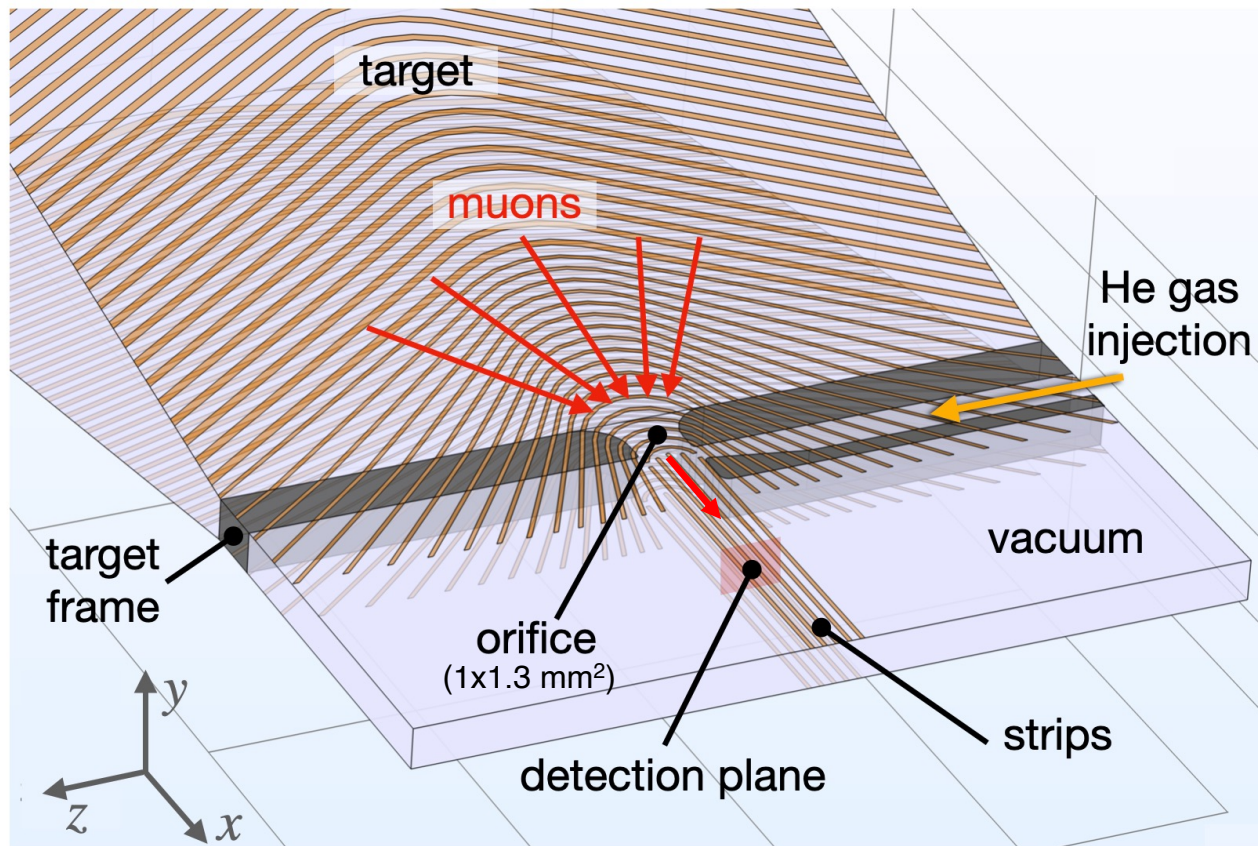
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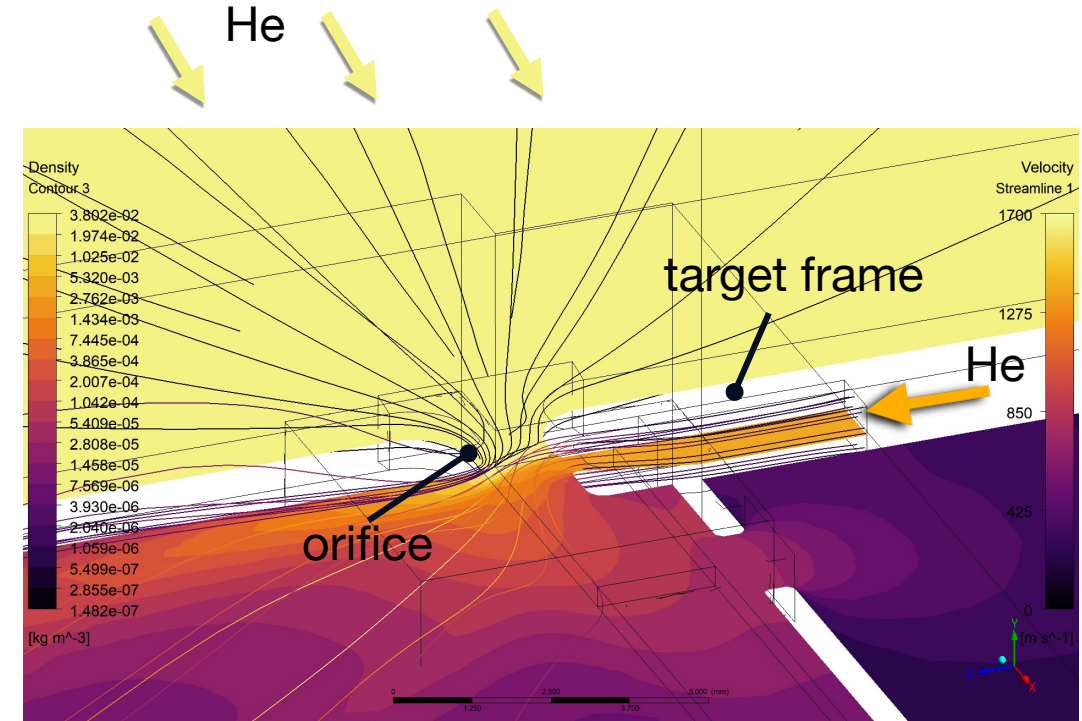
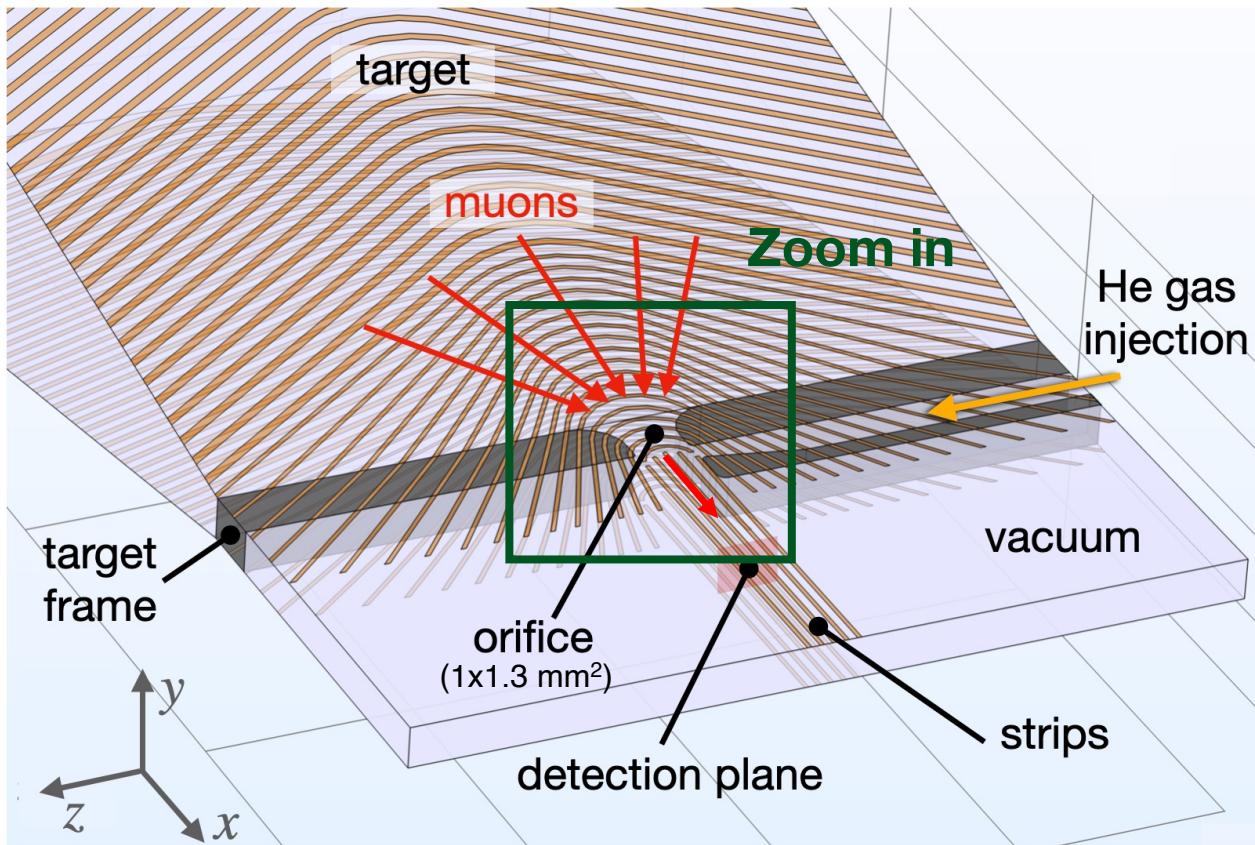
Muon extraction from gas target into vacuum



He gas injected from

- the back-wall of the target*
- the side: \perp to \vec{v}_D of muons*

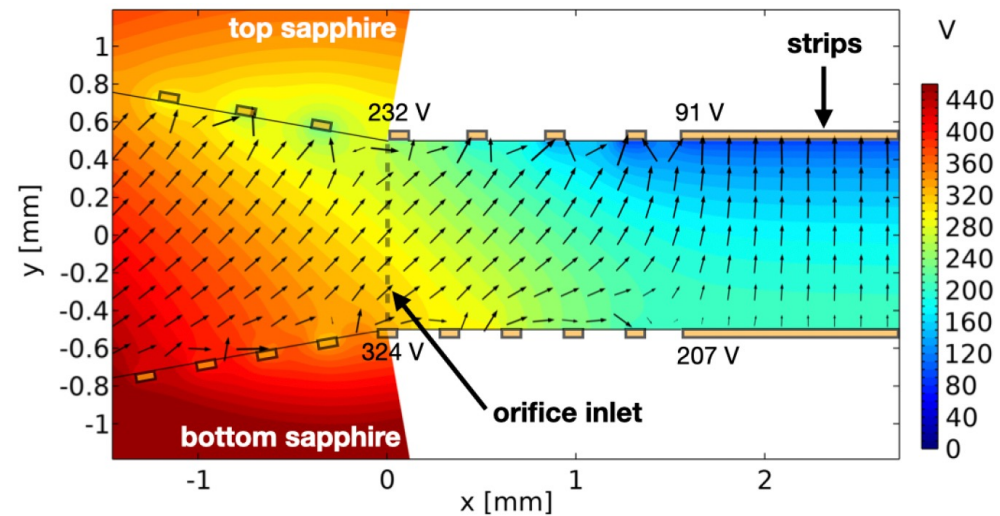
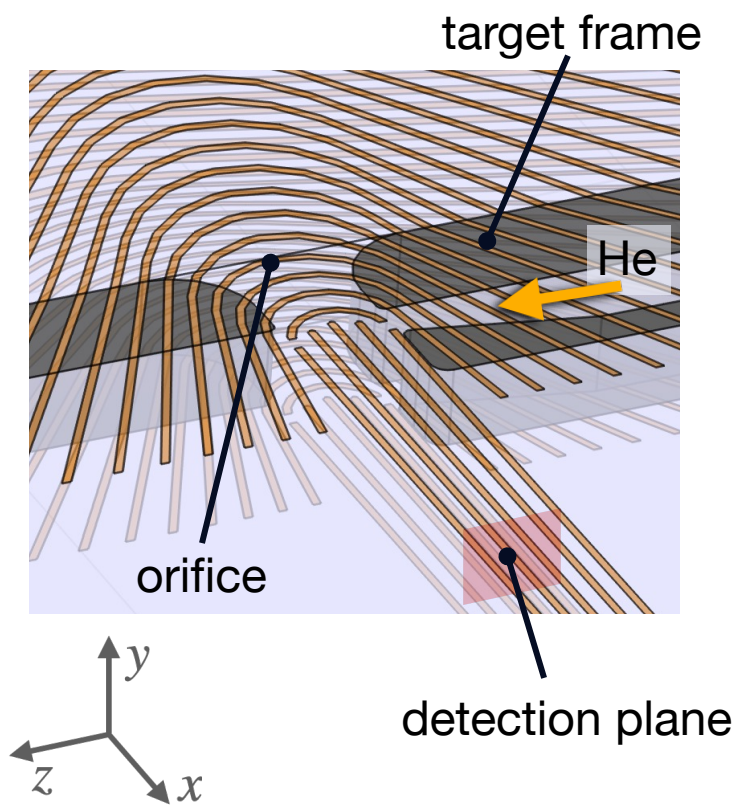
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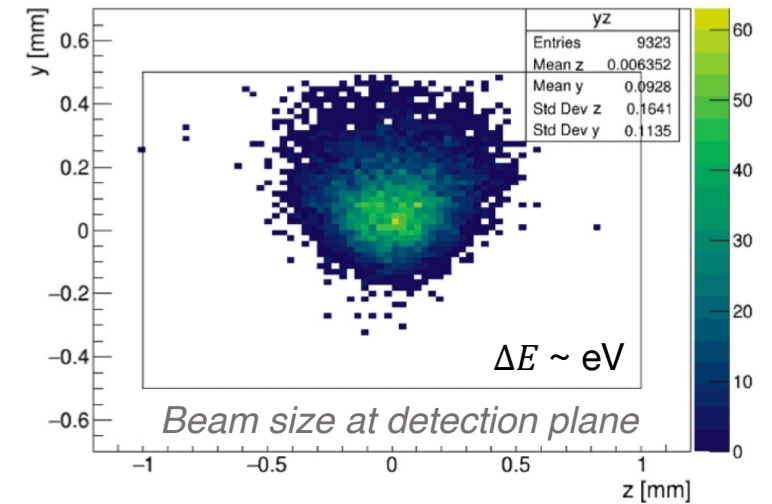
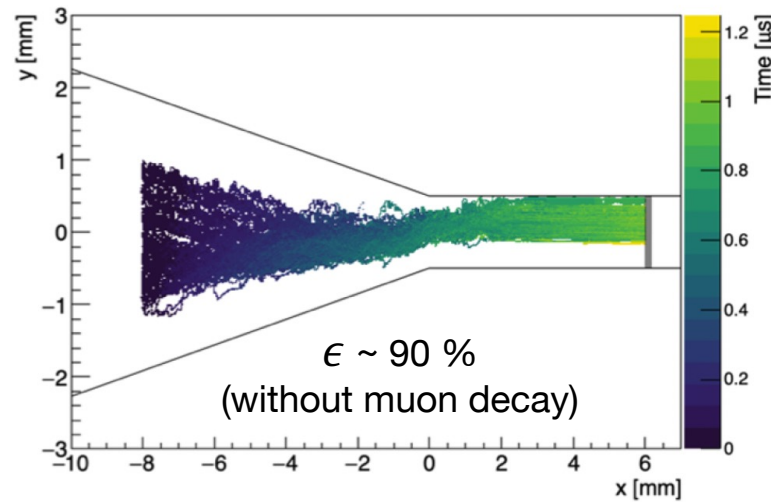
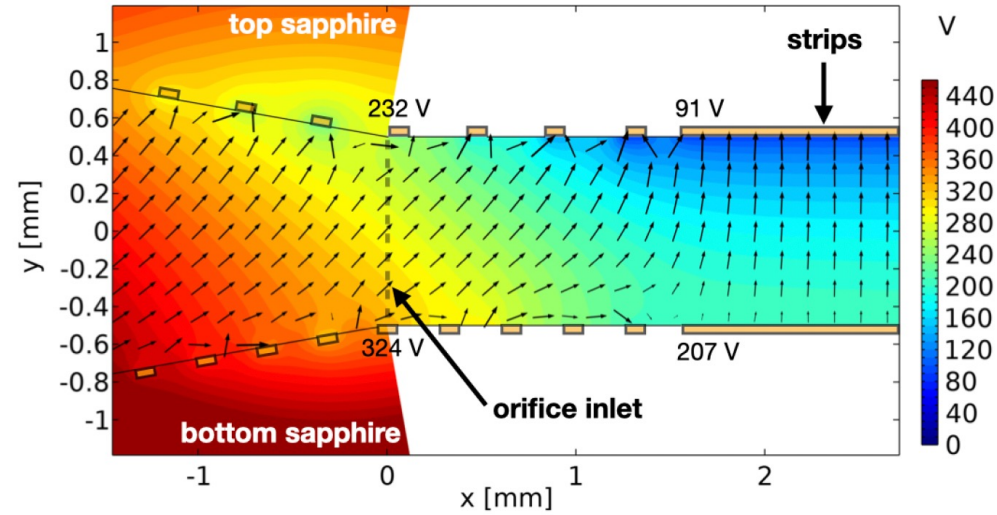
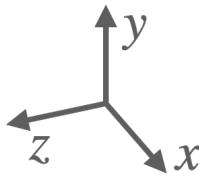
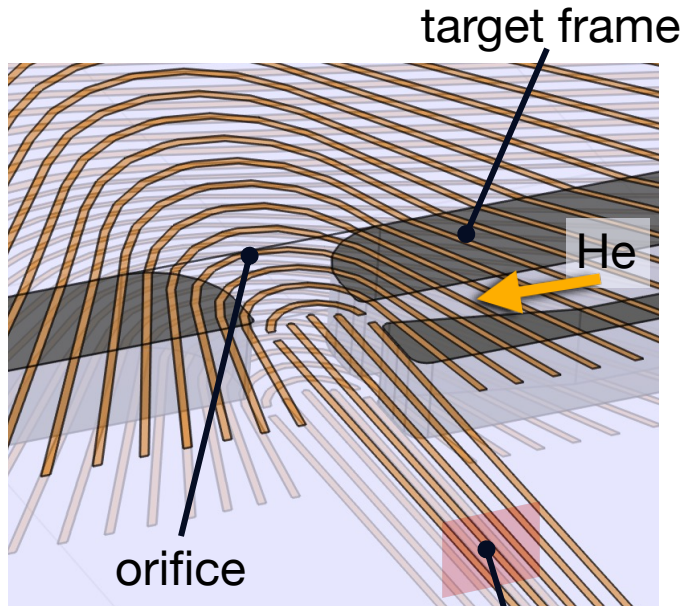
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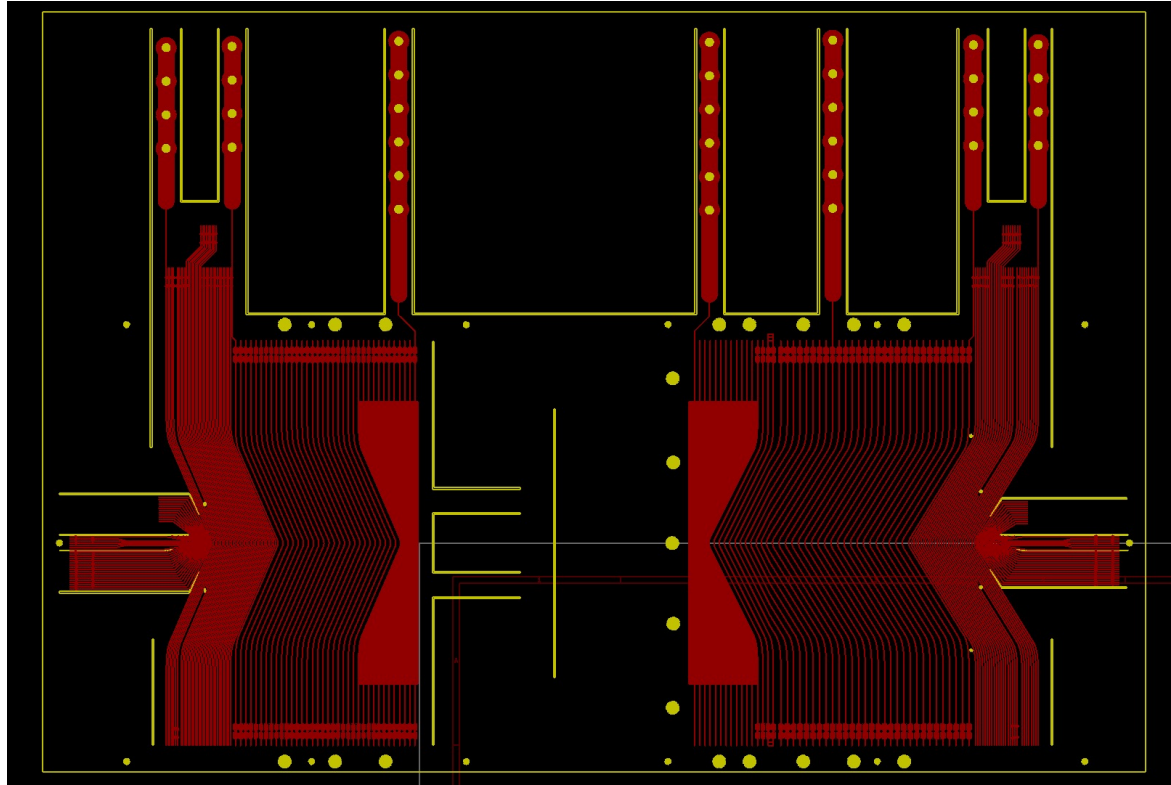
Electric field design



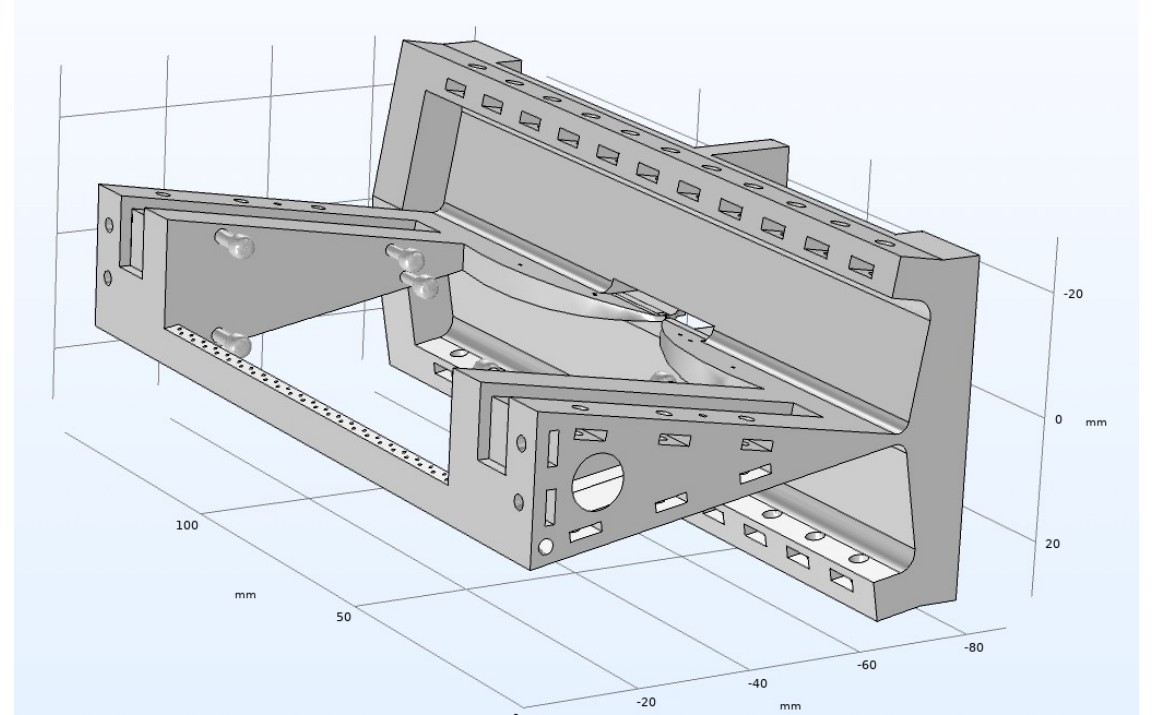
Electric field design and Geant4 simulations



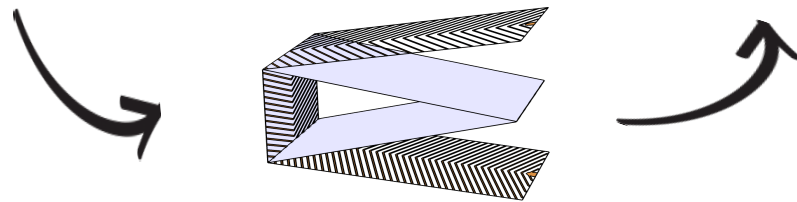
Target production



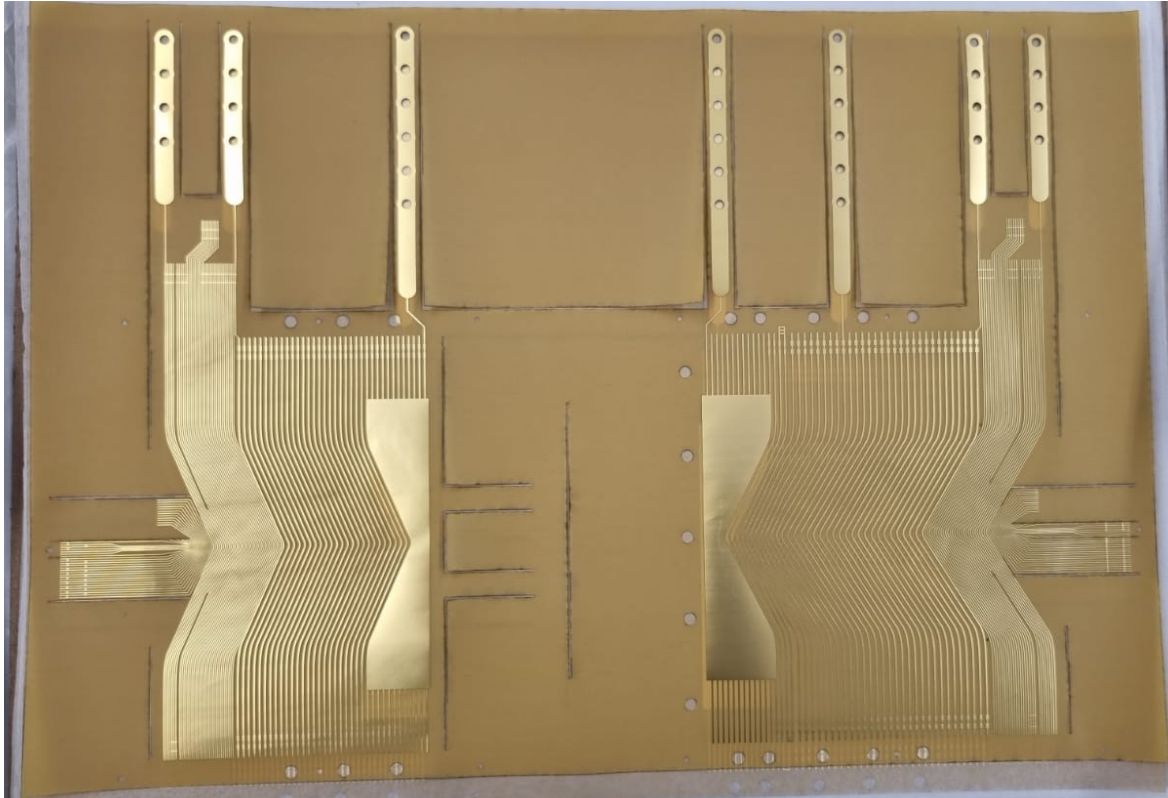
Electrode lines on Kaptan foil



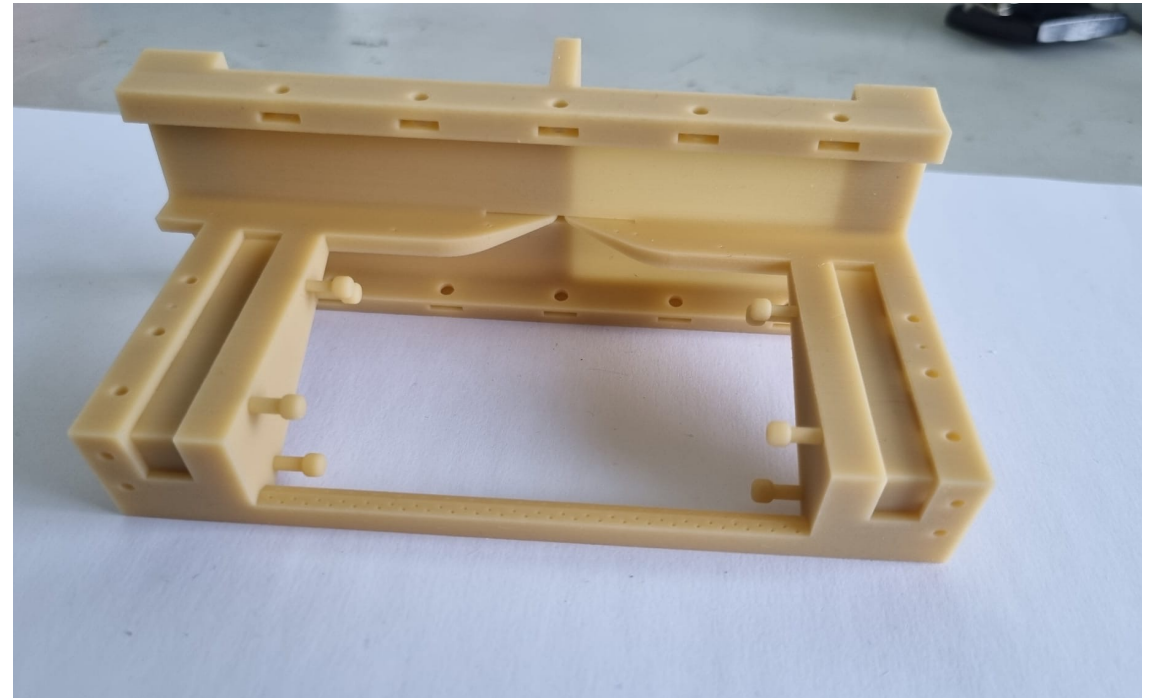
Target frame



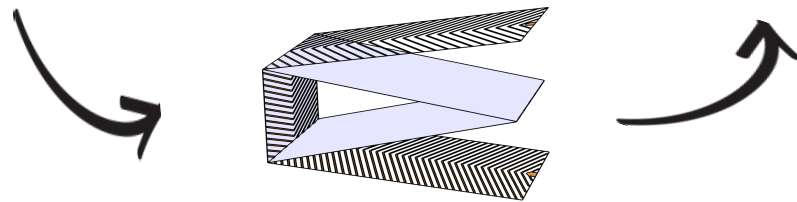
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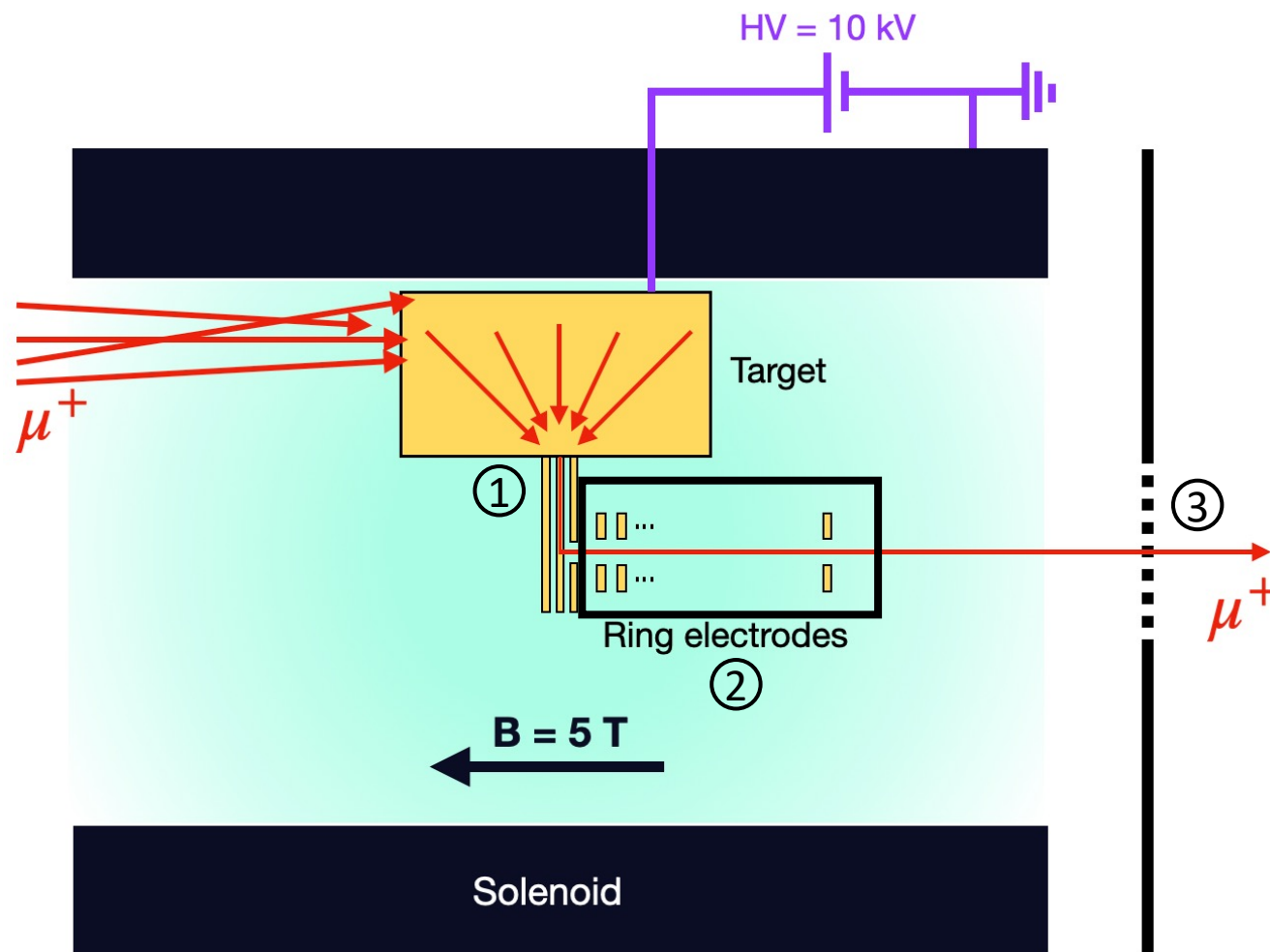
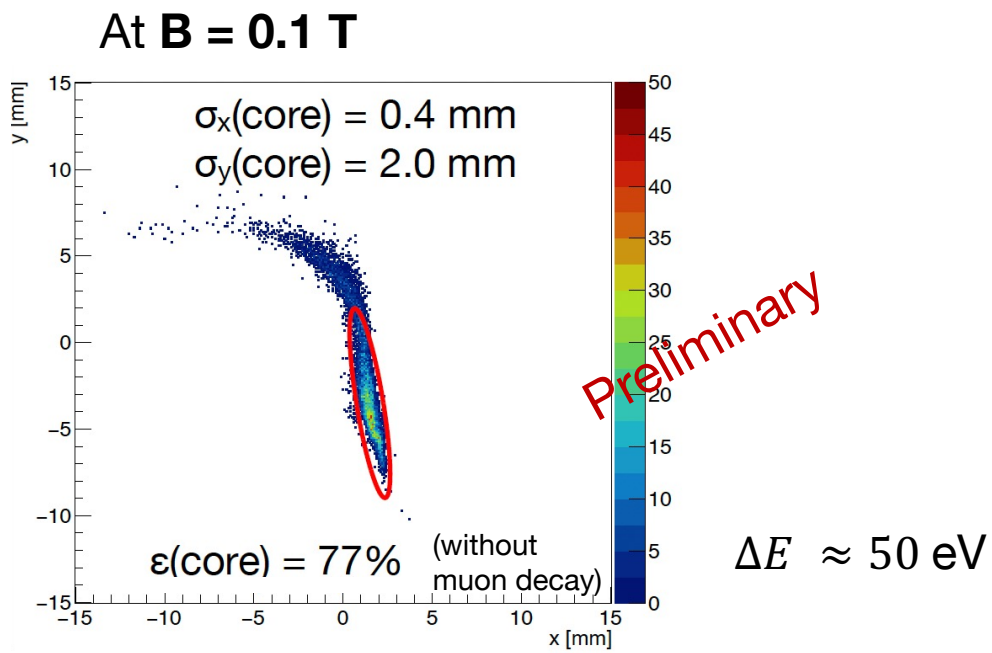


Target frame



Next steps?

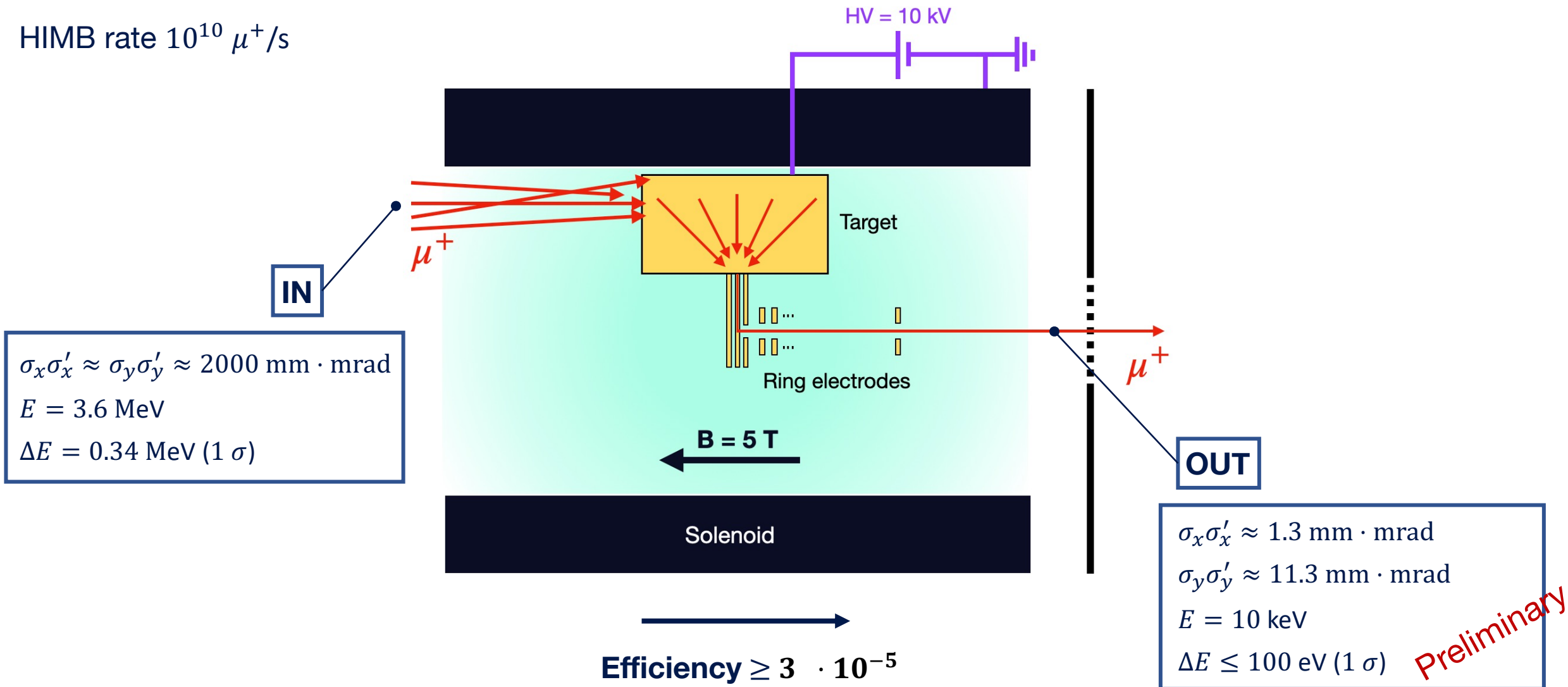
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M. Sakurai. *PhD thesis (ETH Zurich)* (2023)

Efficiency estimates

HIMB rate $10^{10} \mu^+ / s$

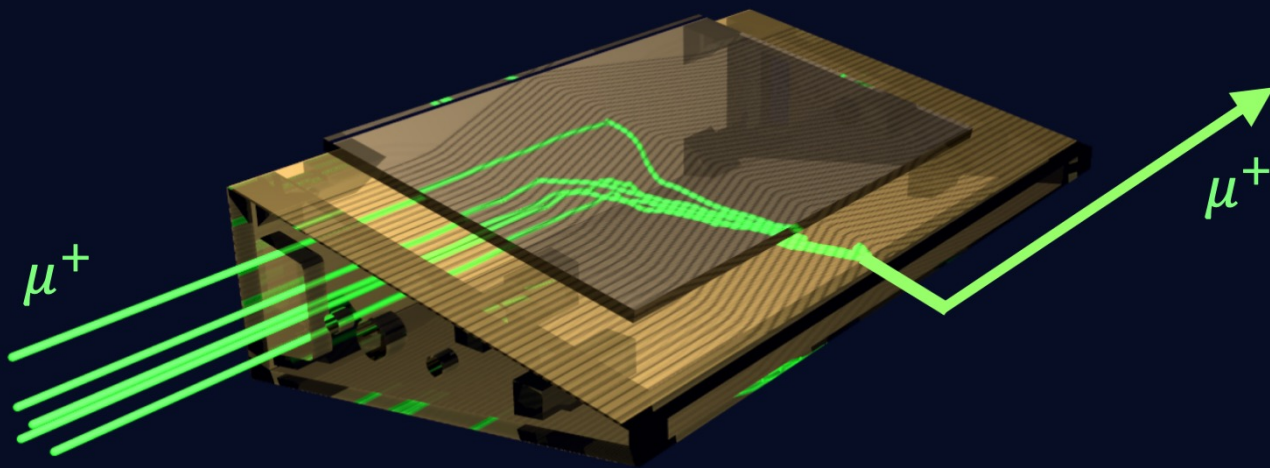


Summary

- muCool proposes a “fast” phase space compression scheme for μ^+ beam for future low energy experiments
- This is achieved with complex E-fields and B-field in combination with a He gas density gradient
- **Mixed compression stage successfully tested!**
- Performed simulations of muon extraction into vacuum and re-acceleration: target development ongoing

Summary

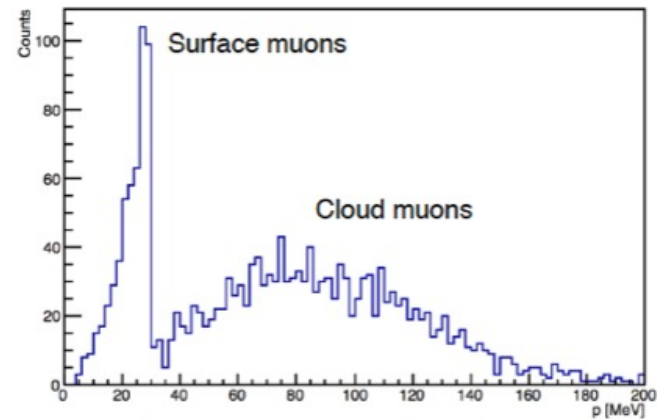
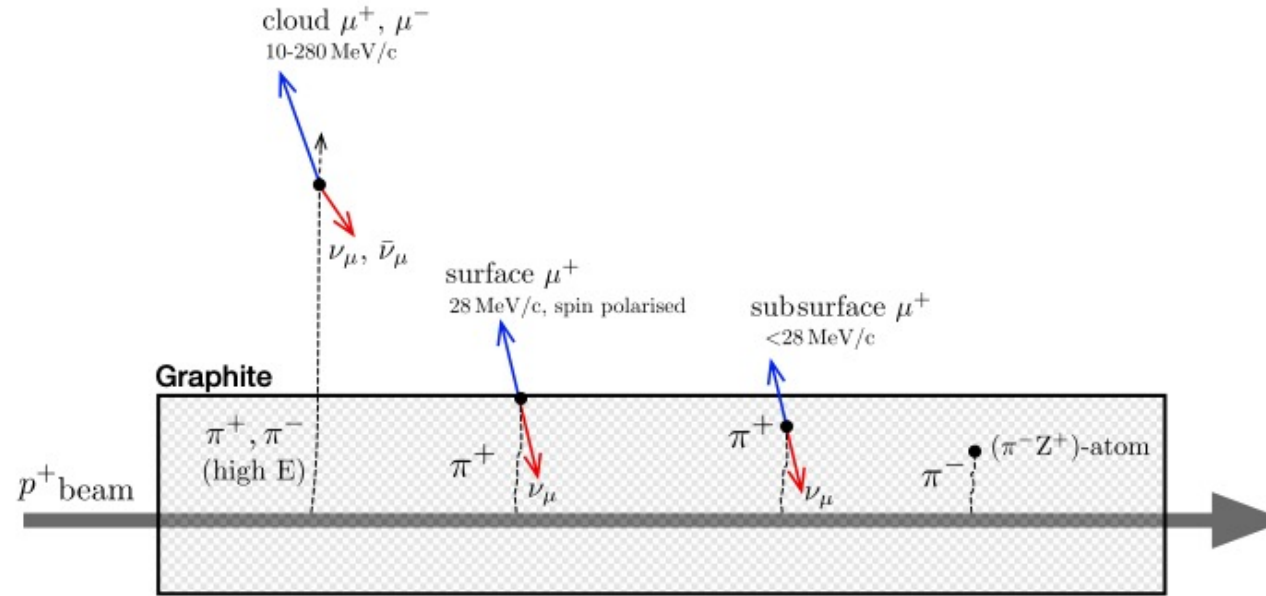
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- **Mixed compression stage successfully tested!**
- Performed simulations of muon extraction into vacuum and re-acceleration: target development ongoing



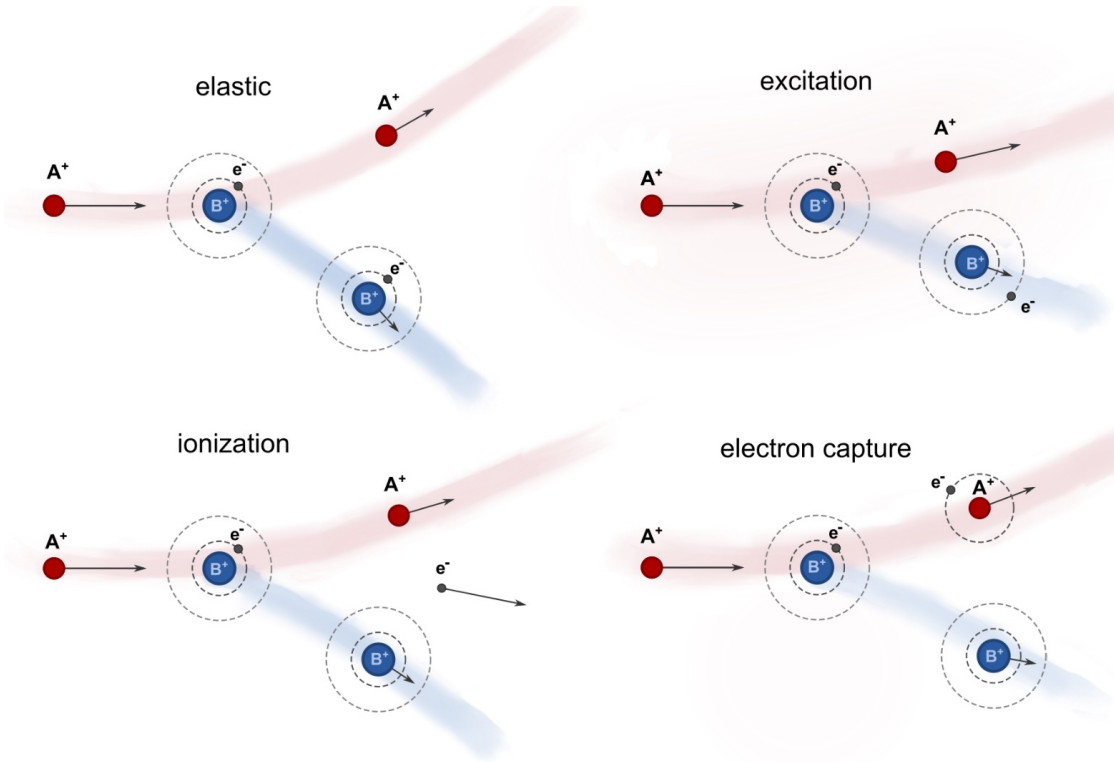
Thank you!

EXTRA SLIDES

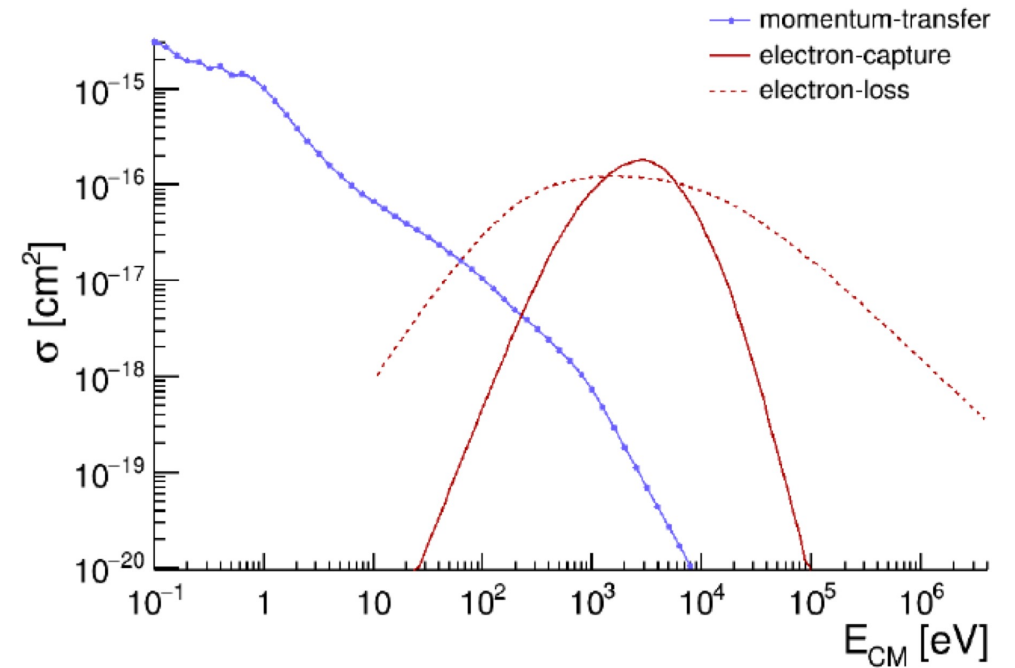
Muon production



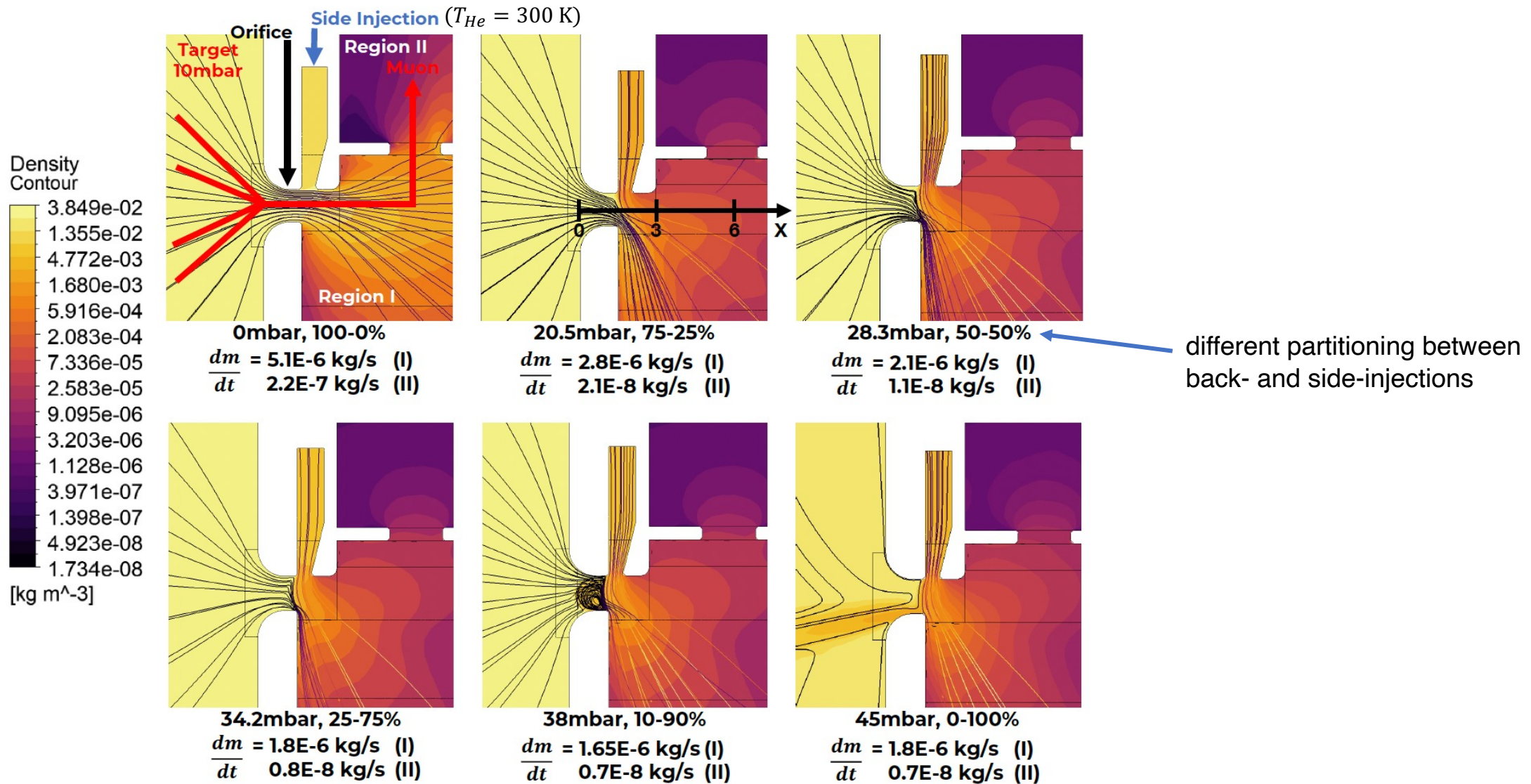
Muon-helium collisions



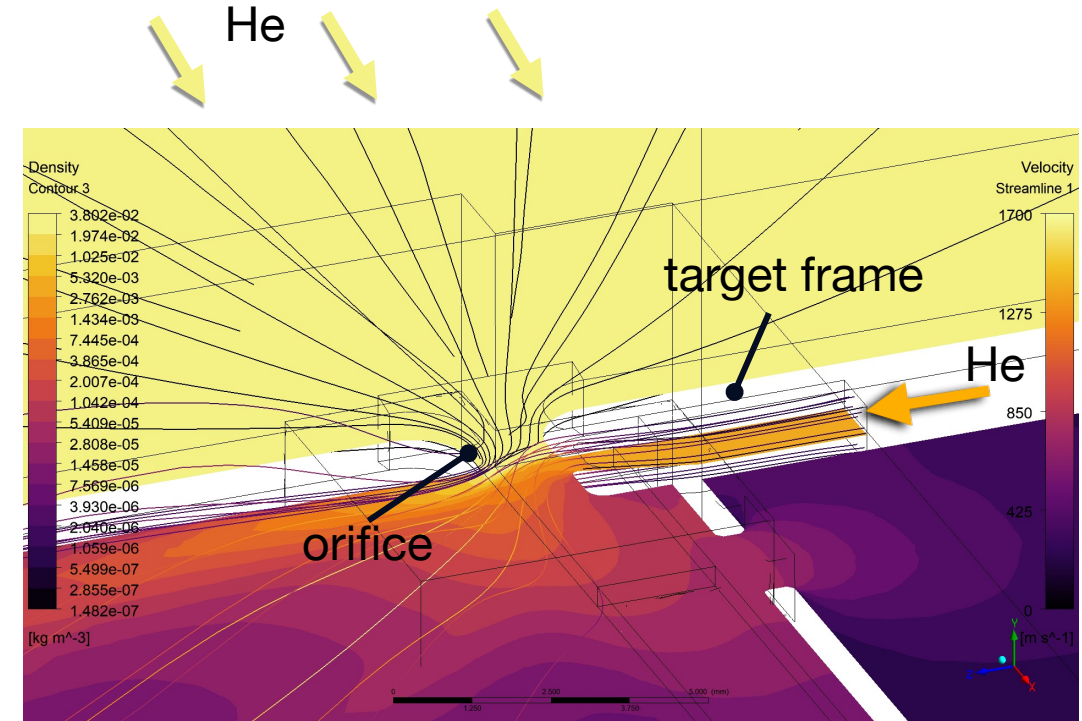
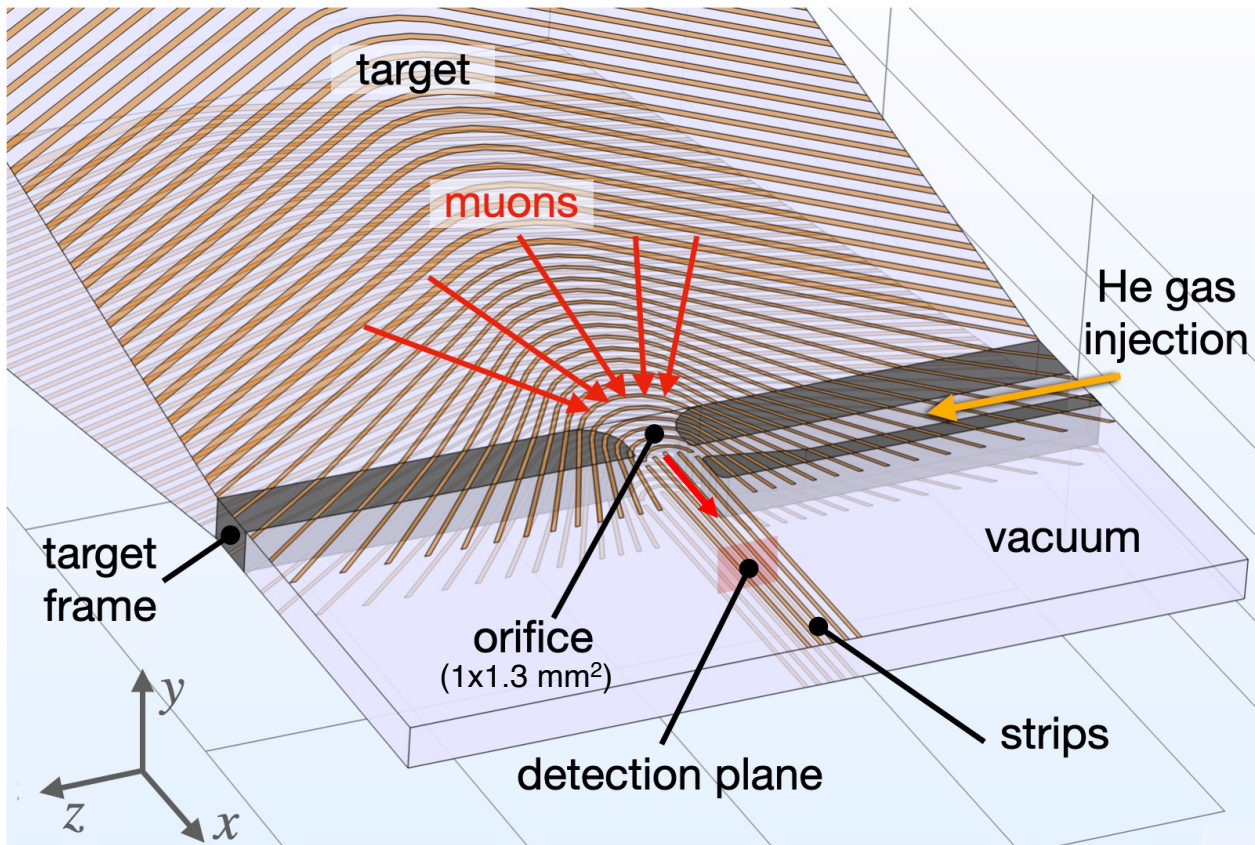
- collision type depends on muon energy
- consequences of the collisions: *energy loss, direction change*



He gas injection schemes

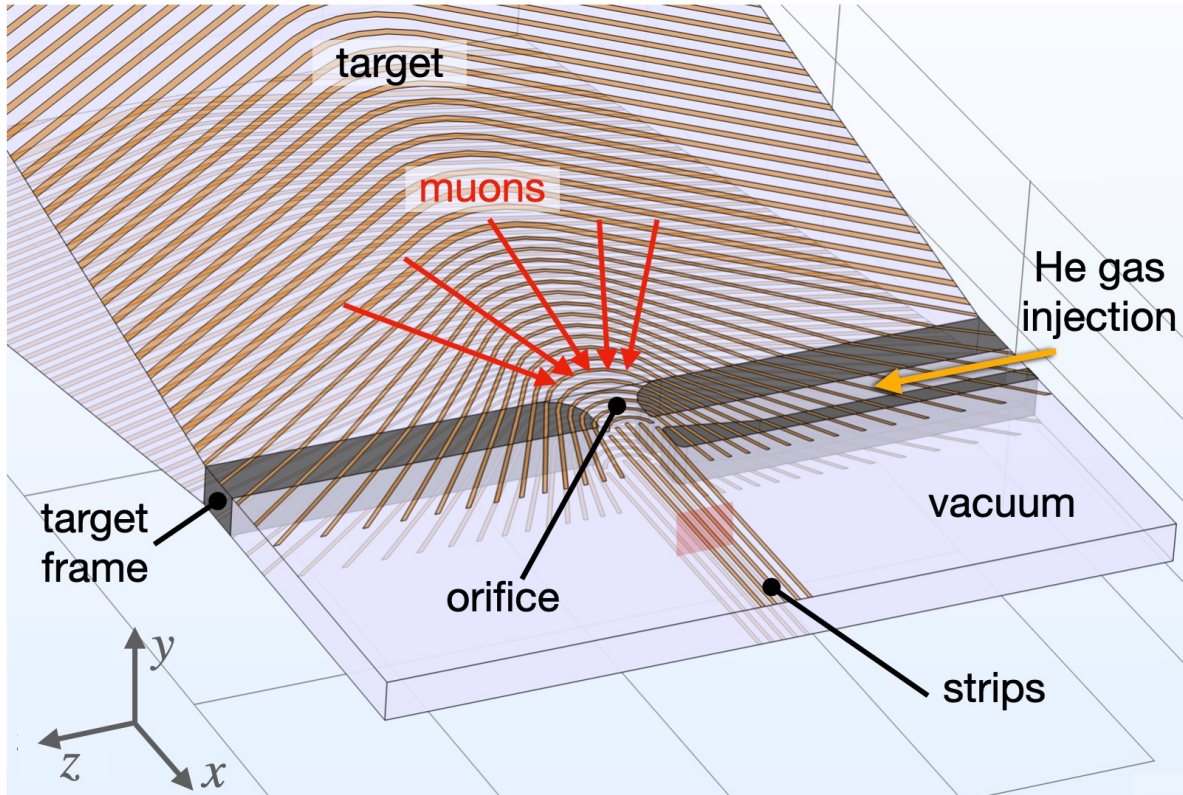


Muon extraction from gas target into vacuum

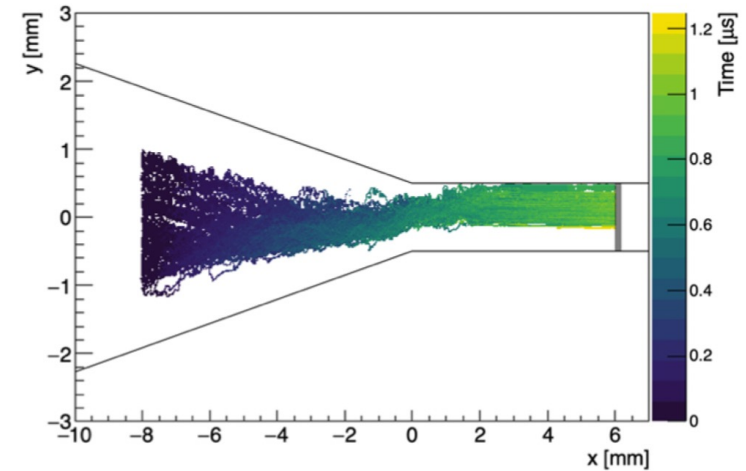
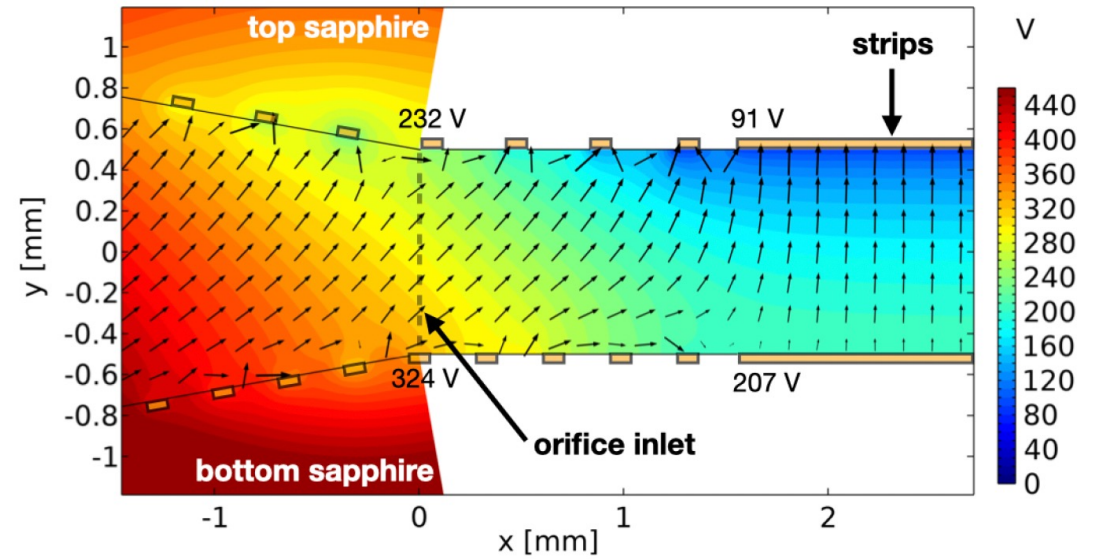


He gas density simulations with 65% back-injection and 35% side-injection

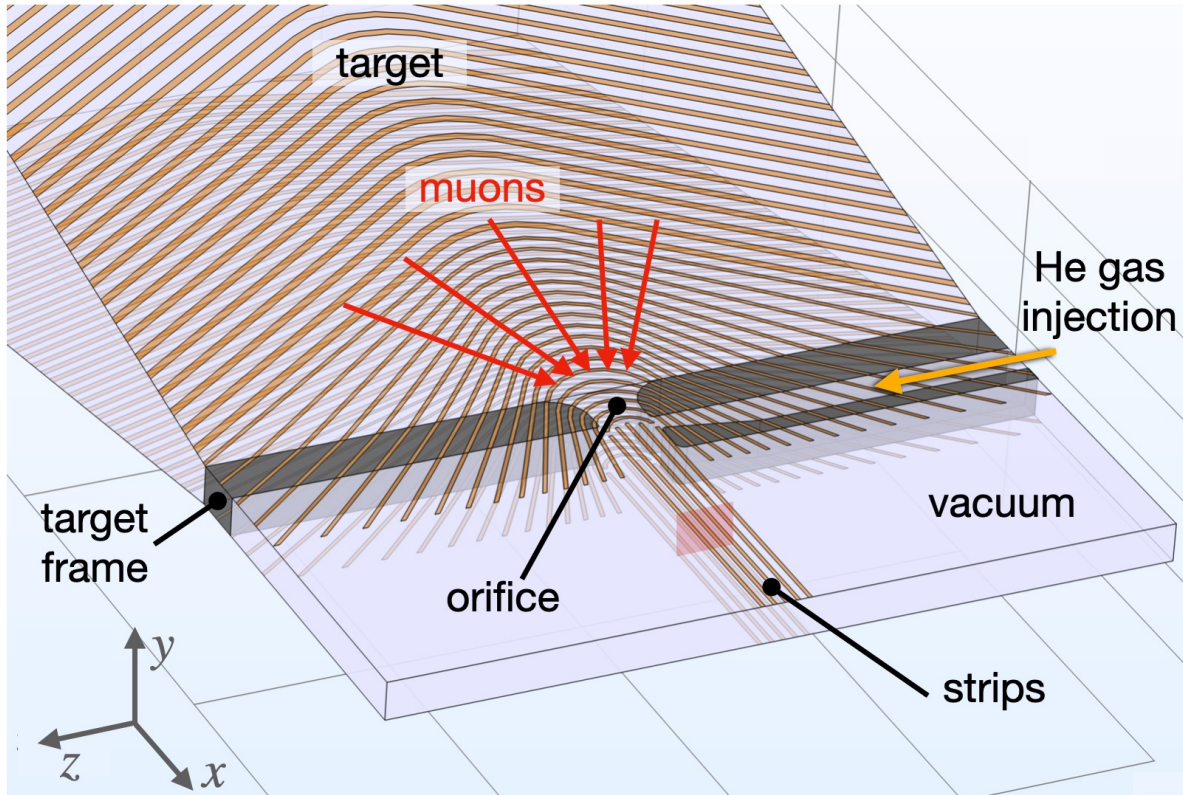
Extraction: xy plane



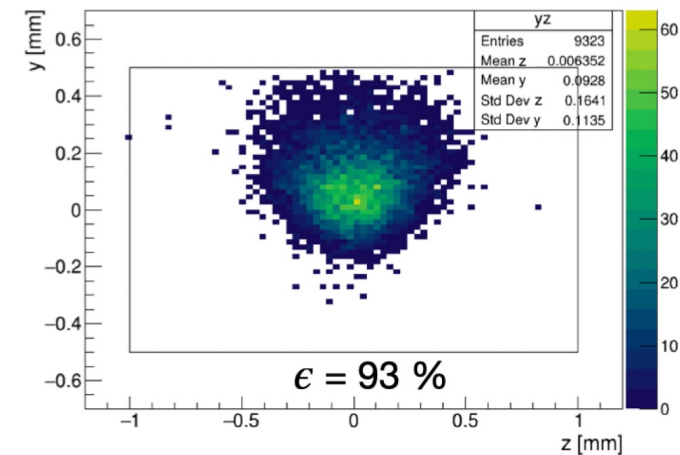
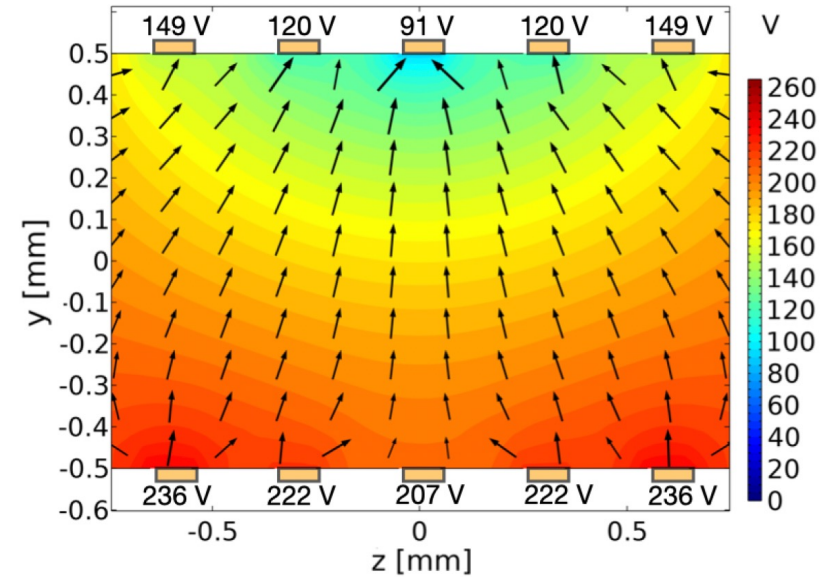
Position the parallel strips at x point where density drops sufficiently, i.e. drift angle in $\vec{E} \times \vec{B}$ tends to 0



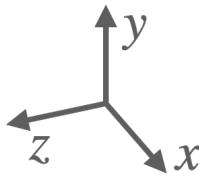
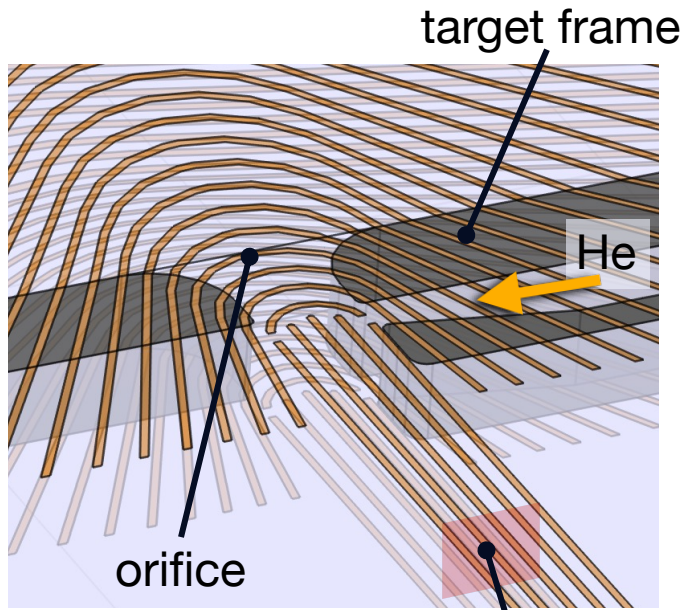
Extraction: zy plane



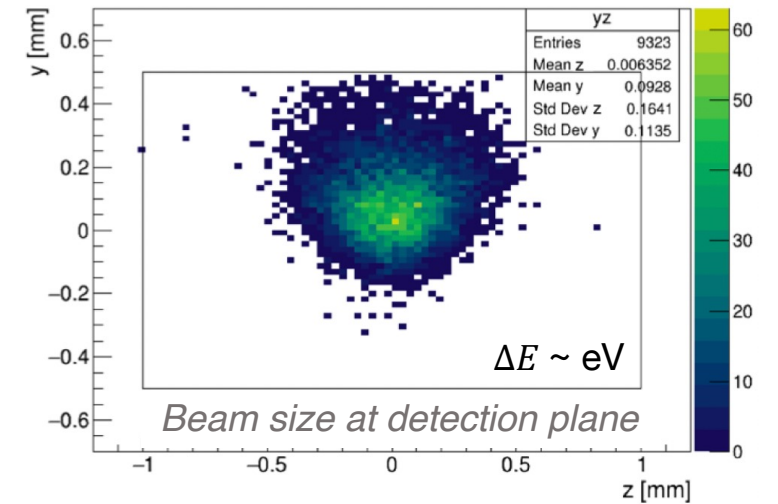
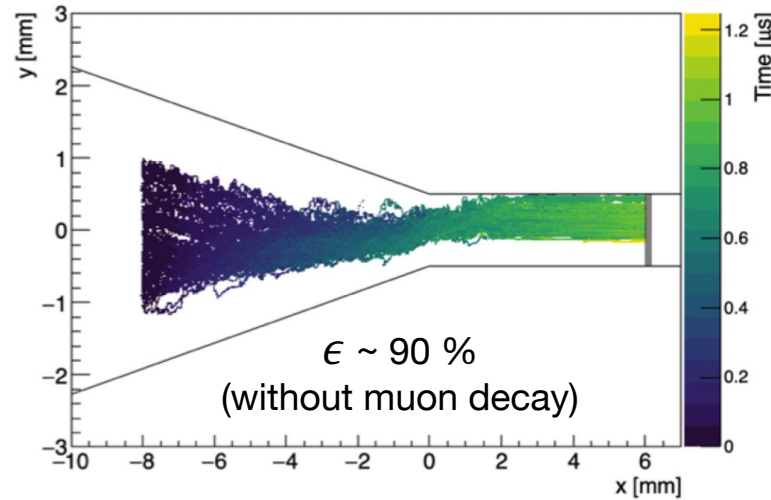
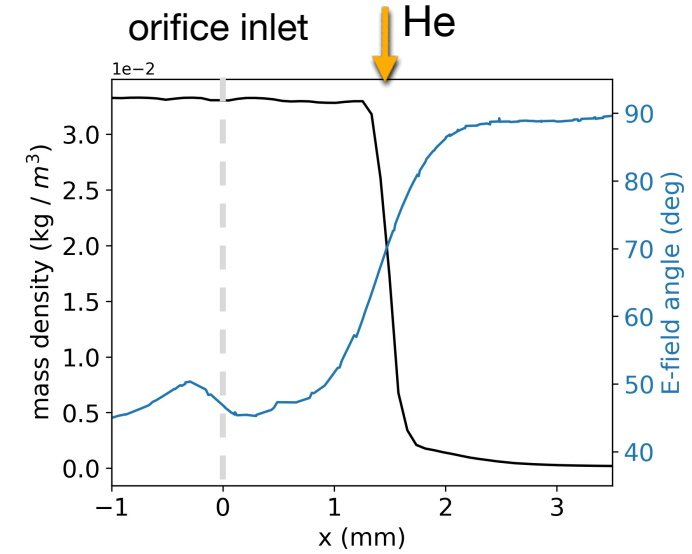
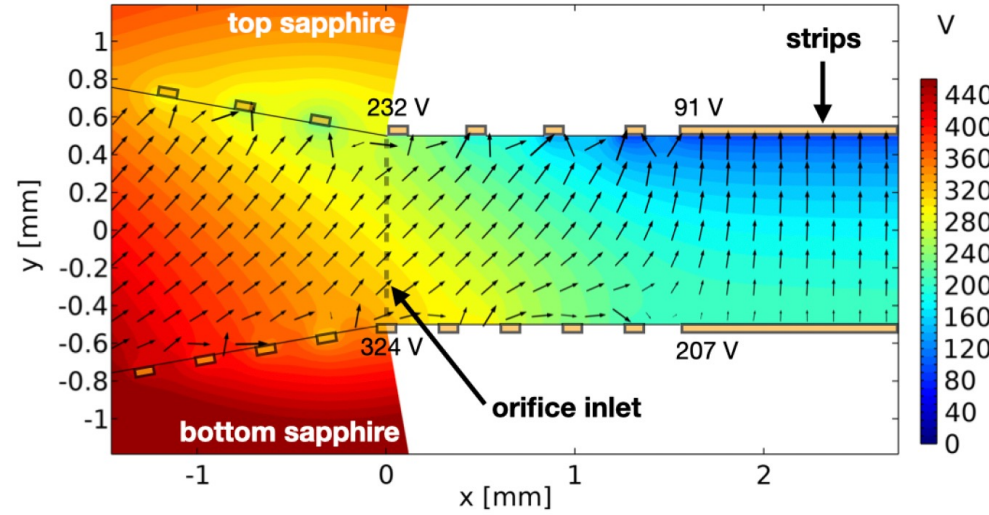
Position the parallel strips at x point where density drops sufficiently, i.e. drift angle in $\vec{E} \times \vec{B}$ tends to 0



Electric field design and Geant4 simulations



detection plane



Preliminary conclusions

Baseline Efficiency	Possible Improvements	Description
$5.5 \cdot 10^{-1}$		Coupling to 5T solenoid
$4.6 \cdot 10^{-1}$	$\times 2$	Into target entrance
$6 \cdot 10^{-3}$	$\times 1.6$	Stopping in He gas
$8 \cdot 10^{-2}$	$\times 1.5$	Compression towards orifice ($5 \mu s$)
$9 \cdot 10^{-1}$		Extraction from orifice
$5 \cdot 10^{-1}$		Drift to re-acceleration region ($0.5 \mu s$)
$8 \cdot 10^{-1}$		Re-acceleration up to iron grid
$7 \cdot 10^{-1}$		Transmission to B-field free region
$3 \cdot 10^{-5}$	$\times 4.8$	Total baseline compression efficiency (and possible improvement)

HIMB rate: $10^{10} \mu/s$

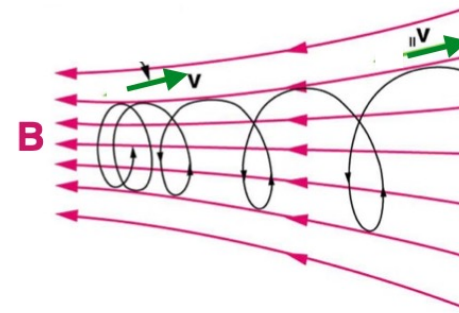
- ☑ Material science: distribute the muCool beam to several μ SR setups at 40 kHz each
- ☑ Efficient Mu production: Mu-spectroscopy and Mu-gravity
- ☑ Re-accelerate to higher energies: e.g. 60 MeV for storage-ring-like experiments as μ EDM or g-2

Extraction from B-field

- ▶ Charge particles follow magnetic field lines

$$r_i \sim r_0 \sqrt{\frac{B_0}{B_i}}$$

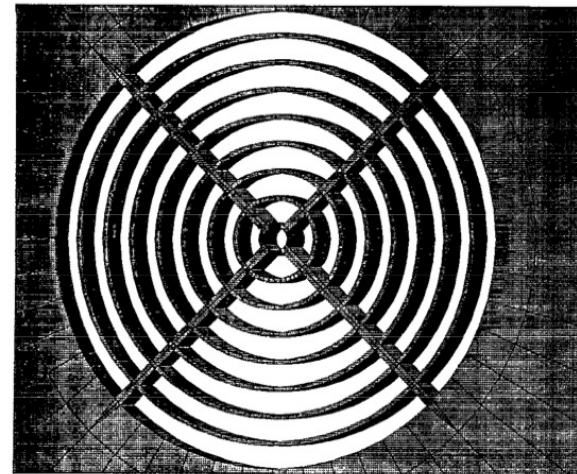
$$\Delta E_{\perp i} \sim \Delta E_{\perp 0} \frac{B_i}{B_0}$$



- ▶ The magnetic field can be terminated so that the beam transits from a region to another region with different field strengths. But in this process the charge particle receive an additional traverse momentum

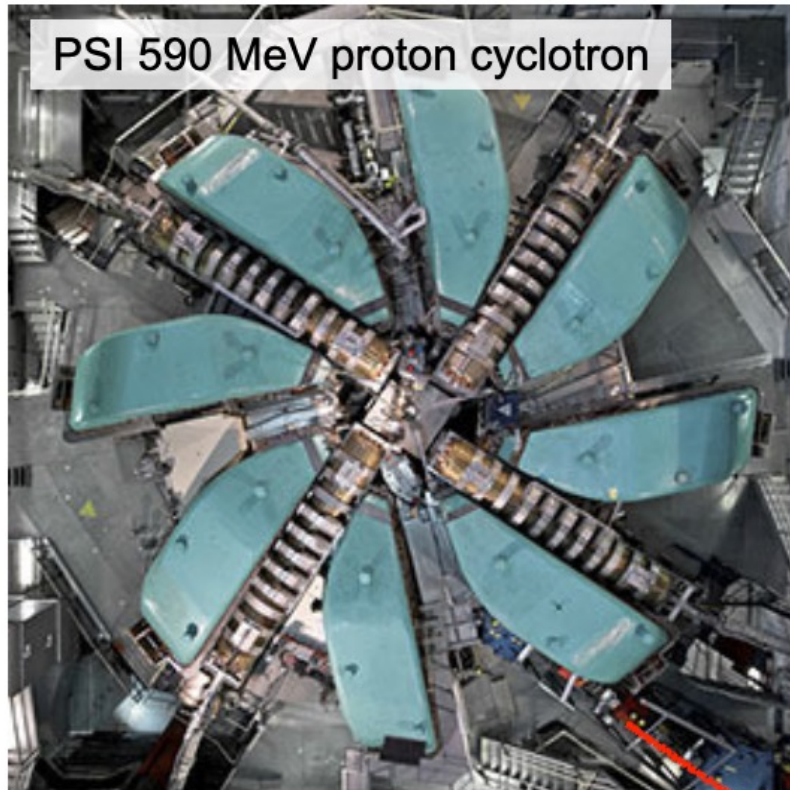
$$\Delta p_{\perp} = e \int_0^t v_z B_{\perp} dt \sim \frac{ewB_i}{2} ,$$

$$\Delta E_{\perp} = \frac{e^2}{8m} w^2 B_i^2 ,$$



Gerola et al., *Rev. Sci. Instrum.* 66 (7) 1995

Protons and muons at PSI



PSI 590 MeV proton cyclotron

to graphite targets

Muon beam

- Trade-off between “rate” and “quality”
- e.g. π E5 beamline at PSI

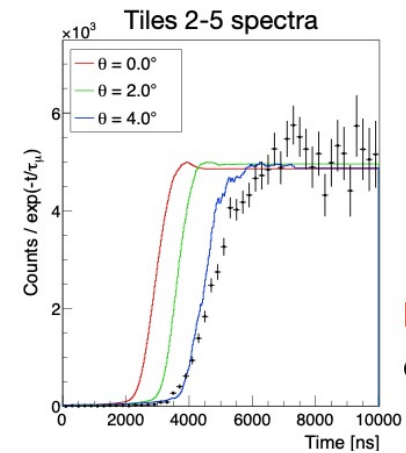
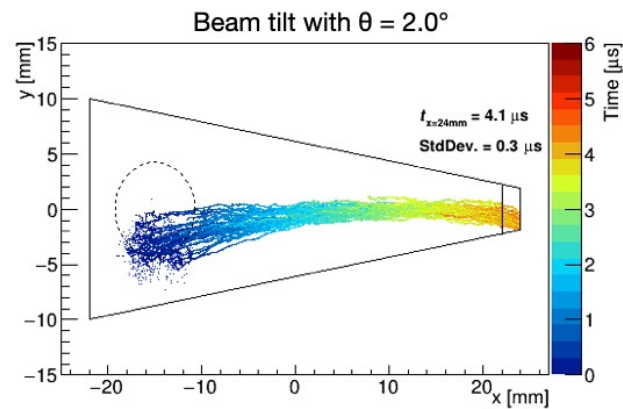
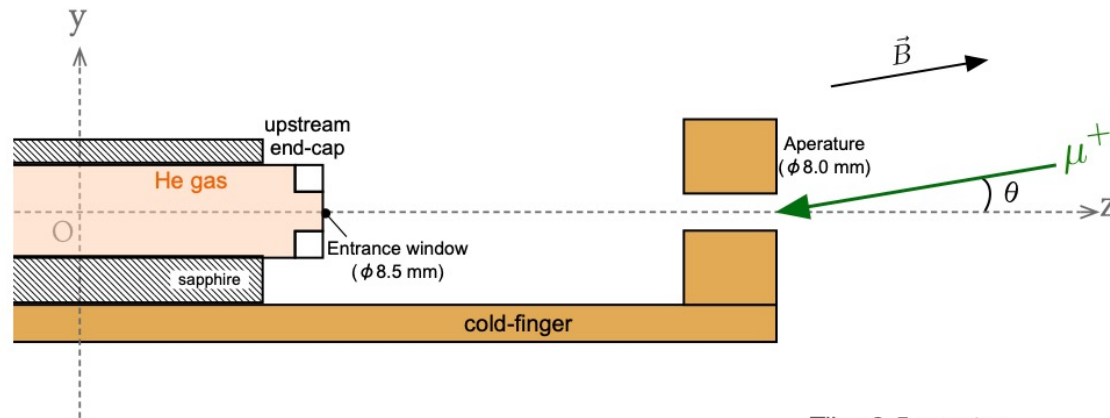
100 MHz at 28 MeV/c

$\sigma_x \sim 1$ cm

$\sigma_E \sim 0.5$ MeV

Sensitivity to misalignment of incoming beam

- Misalignment between target axis and magnetic field
 - Maximum possible angle: $\theta_{\text{MAX}} \sim 4.5^\circ$



**Large effect
on drift time**

Scintillators position and data

