

# ***Luciano Girardello Memorial***

Milano Bicocca --16 January 2023



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- \* **Luciano has been my master thesis and PhD advisor (in Bicocca from 2004)**
- \* **Mentor for physics and science**
- \* **Luciano has been inspirational for a generation of "young" physicists**
- \* **We all remember his fascinating (and very soft) QFT lectures**
- \* **Many quotes of him that we still remember:**  
*"No emotional comments", "Non danno premi Nobel a caso", ....*

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- \* **Grateful to Luciano for his guiding and mentoring, Luciano guided me to supersymmetry and supergravity**
- \* **Passion for dynamical SUSY breaking**
- \* **Luciano: "Look at this paper (ISS '06), it is very interesting"**
- \* **Last years of scientific publications of Luciano with Antonio Amariti, Davide Forcella, Massimo Siani, Gabriele Tartaglino-Mazzucchelli ...**



# The role of impurities in cosmological first order phase transitions

**Alberto Mariotti**



Based on arXiv:2203.16450 (Phys. Rev. Lett. 129 (2022) 26, 261303)

with Simone Blasi

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# Why cosmological first order PT?

★ *Probe of Early Universe cosmology*

★ *In the Standard Model, QCD and EW PT are not first order*

**First Order Phase Transition would be signal of BSM physics**

\* *First order EW PT can lead to electroweak baryogenesis* →

*New physics in Higgs sector*

\* *New first order PT in dark matter sectors*

\* *FOPT are powerful sources of stochastic GW signal*

*FOPT proceeds through bubble formation*

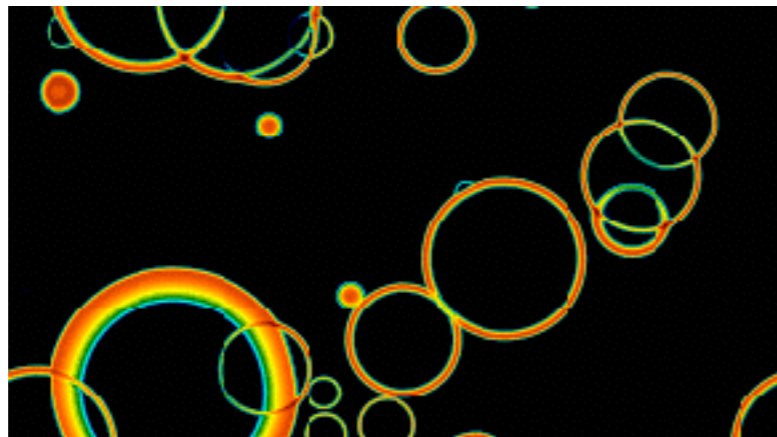


fig. from arXiv:1705.01783 D. Weir

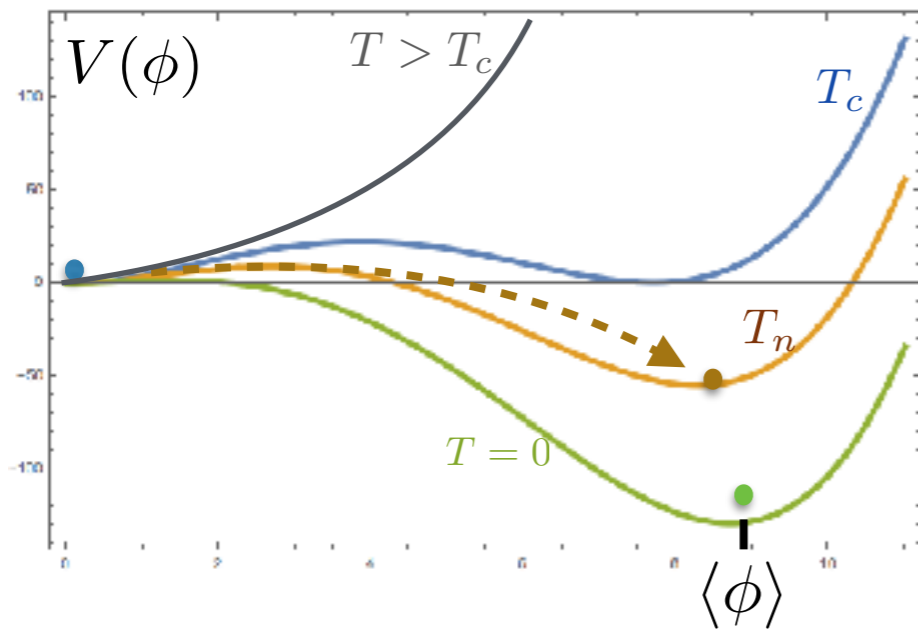
Target for current and future GW experiments

- ✦ *Ligo Virgo Kagra*
- ✦ *NANOGrav*
- ✦ *LISA*
- ✦ *Einstein Telescope*
- ✦ *Cosmic explorer*

# First order phase transition

★ **First Order Phase transition (FOPT) proceeds with bubble nucleation**

★ **Nucleation condition in homogeneous Universe**

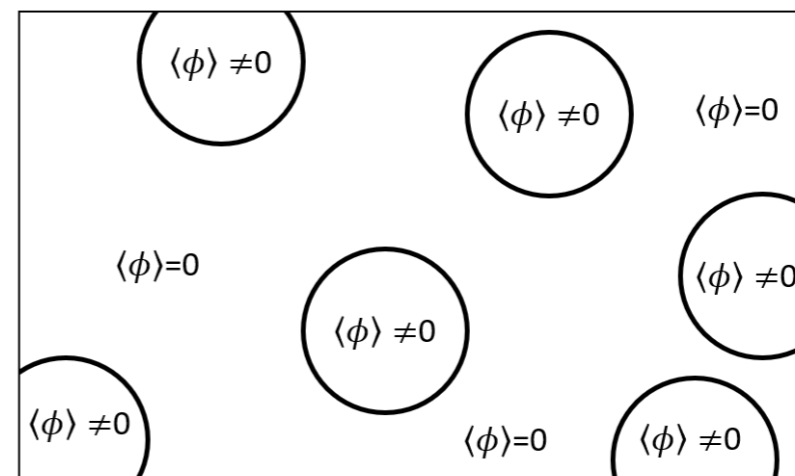
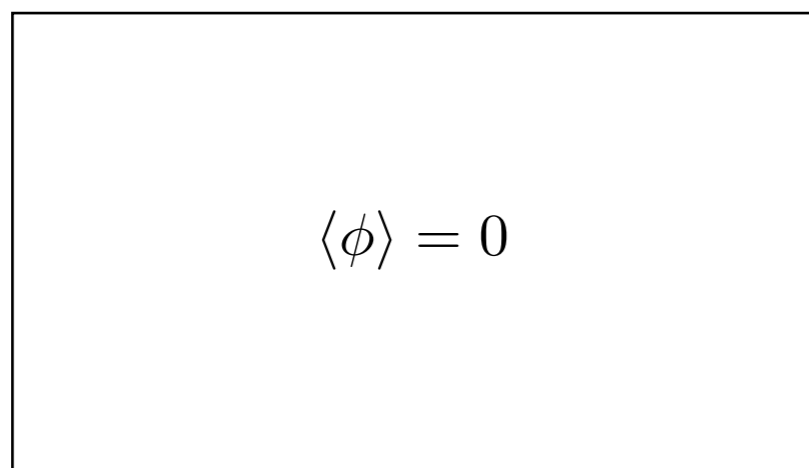


- \* Phase transition described by effective potential
- \* Thermal fluctuation induces nucleation of bubbles
- \* Nucleation rate/volume set by  $O(3)$  bounce action

$$\gamma_V(T) \sim T^4 e^{-S_3(T)/T}$$

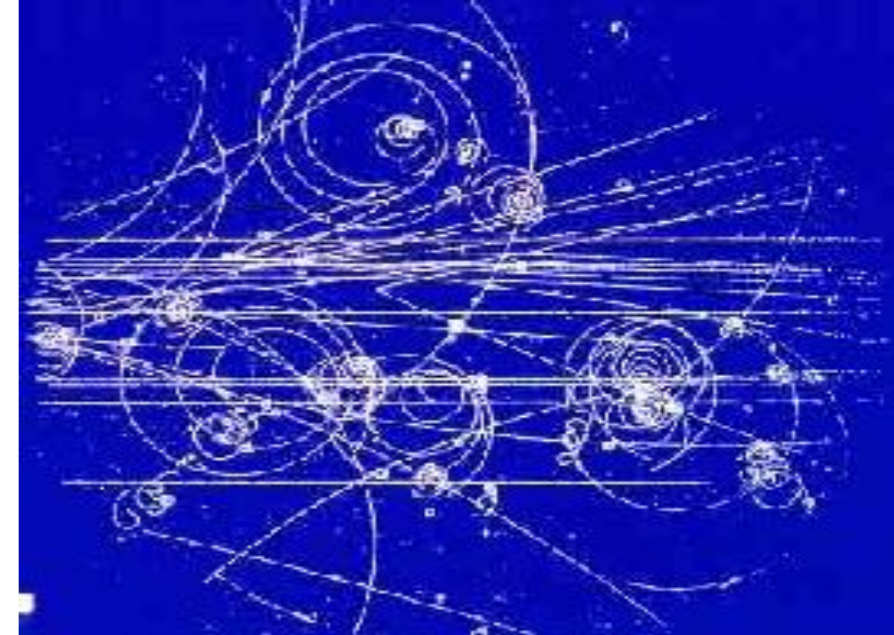
\* **Nucleation condition sets nucleation temperature**  $\gamma_V(T_n) \sim H(T_n)^4$

Homogeneous Universe in false vacuum



# ... however ... impurities

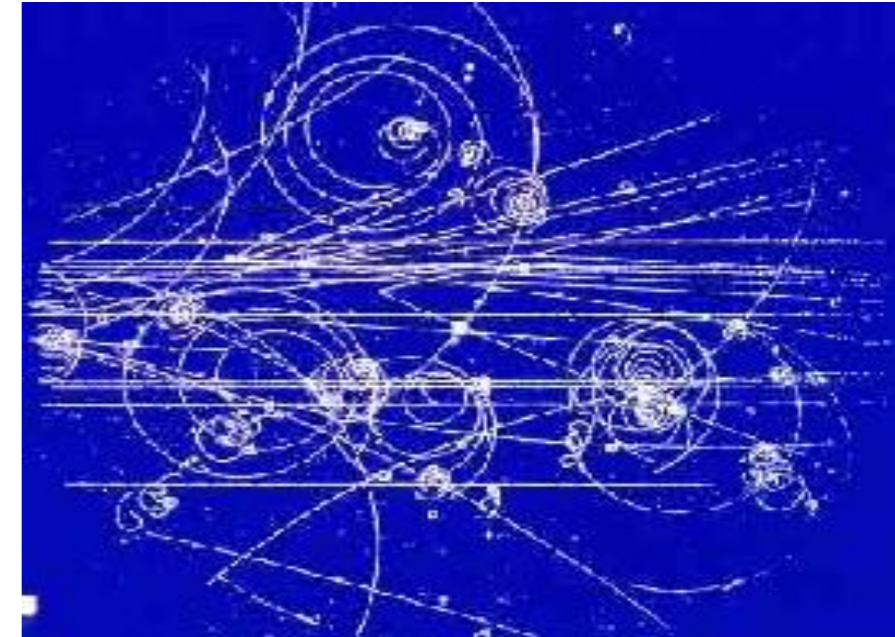
★ *Impurities drastically modify the nucleation process*



# ... however ... impurities

## ★ Impurities drastically modify the nucleation process ... also in cosmological phase transitions ...

- \* "Monopole and Vortex dissociation and decay of the false vacuum" *Steinhardt 1981*
- \* "Impurities in the Early Universe" *Hosotani 1982*
- \* "Cosmic separation of phases" *Witten 1984*
- \* "Phase transitions induced by cosmic strings" *Yajnik 1986*



## ★ The nature of impurities for cosmological PT

### \* High energy collisions

E.g. Affleck, De Luccia '79, --- Selivanov, Voloshin '85, --- Kuznetsov, Tinyakov '97 --- Strumia '23

### \* Compact objects like BH, gravitational effects

E.g. Hiscock '87, -- Gregory, Moss, Withers '14, -- Grinstein, Murphy '15, -- El-Menoufi, Huber, Manuel '20, Balkin et al '21, Strumia '22

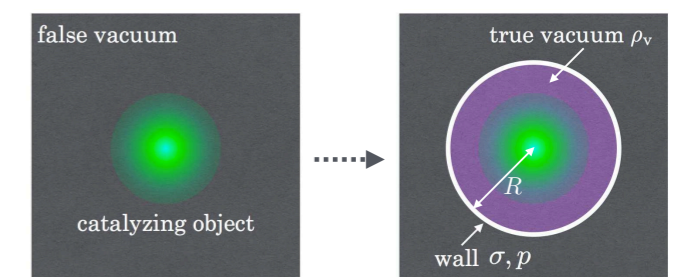


Fig. from Oshita et al.1808.01382

### \* Topological defects (strings, monopoles ...)

E.g. Steinhardt '81, Hosotani '82, Witten '84, Yajnik '86, Preskill Vilenkin '92, --- Kumar et al '10, -- Agrawal, Nee '22

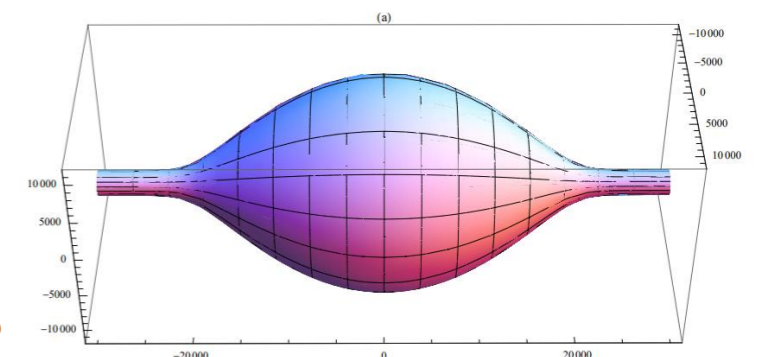


Fig. from Lee et al.1310.3005



# Why Topological defects as impurities

★ *What is the origin of the topological defects?*

★ *Remnants of PT depending on vacuum manifold topology* [Zel'dovich et al. '74, Kibble '76]

Defect	Dimension	Homotopy
Domain walls	2	$\pi_0(M)$
Strings	1	$\pi_1(M)$
Monopoles	Point-like	$\pi_2(M)$

*Their dynamics can source gravitational waves*

★ *They can be present if EW symmetry breaking is final step of a multi-step breaking of larger symmetry group*

*Typical in unified theories*

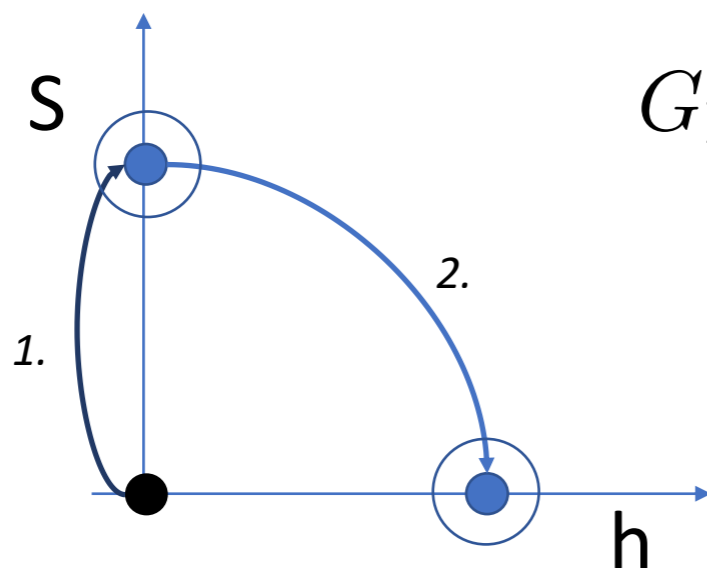
***Can the EW phase transition occur through impurities?  
Minimal realization of seeded EW via topological defects?***

*Blasi, AM 2203.16450*

# Simplest model for EW FOPT

★ Higgs ( $h$ ) plus Singlet  $S$  with a  $\mathbb{Z}_2 : S \rightarrow -S$

★ The electroweak phase transition occurs in **two steps**



$$G_{EW} \times \mathbb{Z}_2 \xrightarrow{1.} G_{EW} \xrightarrow{2.} U(1)_{em} \times \mathbb{Z}_2$$

★ Many pheno studies on Higgs Singlet EWPT

- \* Simplest new physics scenario with strong EW FOPT  
[Espinosa, Konstandin, Riva 1107.5441]
- \* Minimal mechanism for EW baryogenesis  
[Espinosa, Gripaos, Konstandin, Riva 1110.2876]
- \* Benchmark for gravitational wave signals  
[Caprini et al 1512.06239]
- \* Singlet is challenging to detect at colliders  
[Curtin, Meade, Yu 1409.0005]

◆ Order 1000 papers on this model in last 10 years

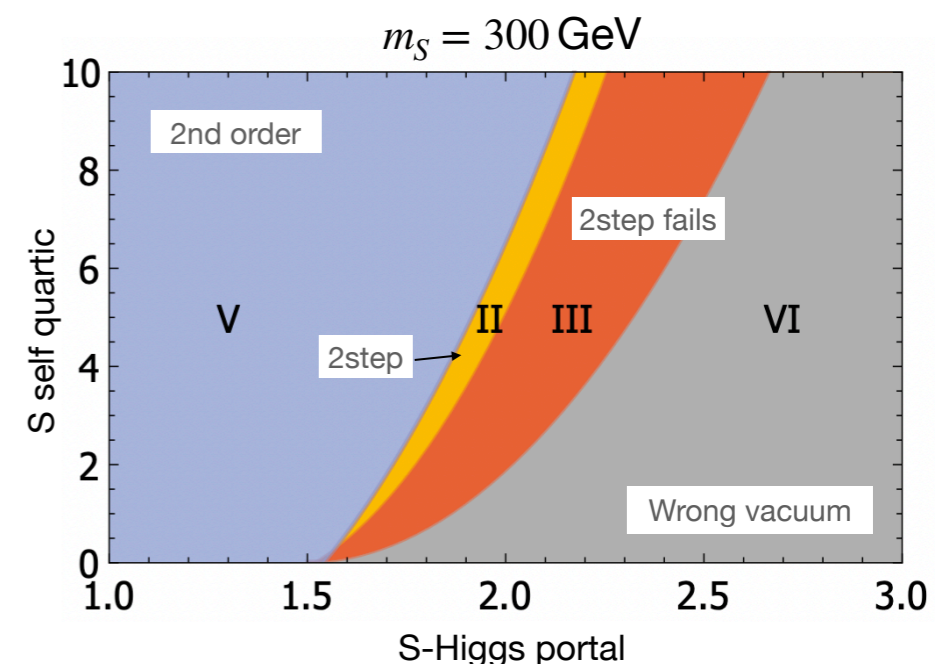
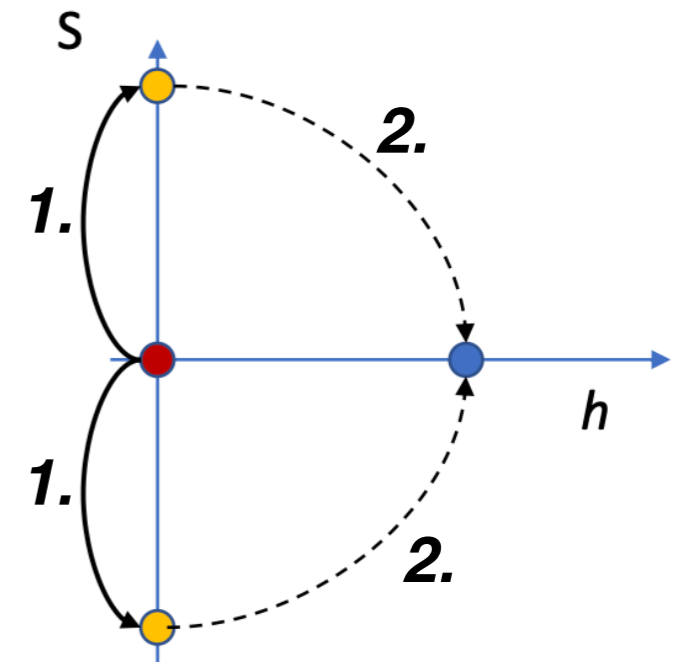
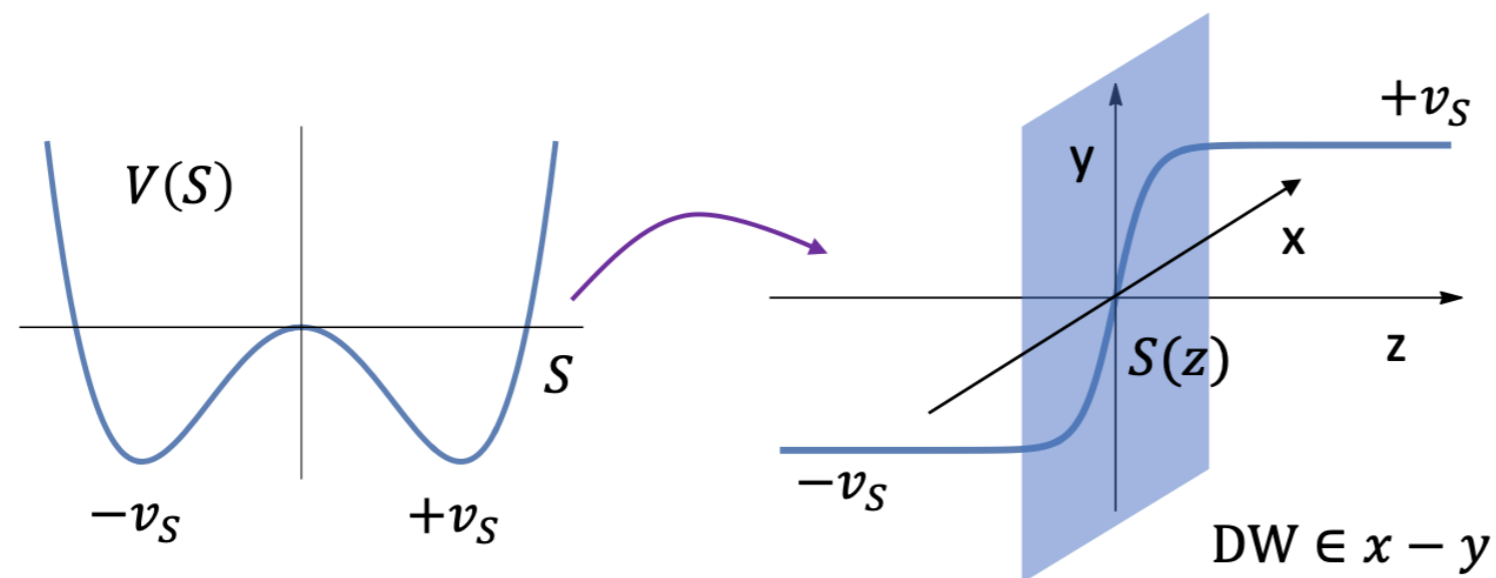


Fig. adapted from Kurup, Perelstein [1704.03381] PRD

# ... but ...

## ★ *Domain walls are formed in first step!*

- \* Disconnected vacuum manifold after first step
- \* Walls are formed at boundaries between different domains

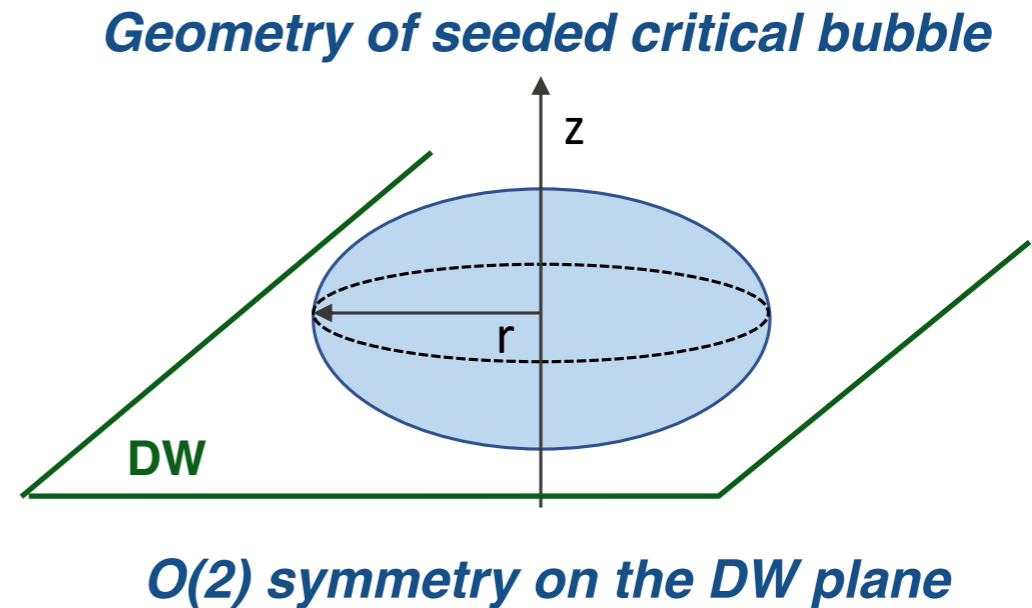
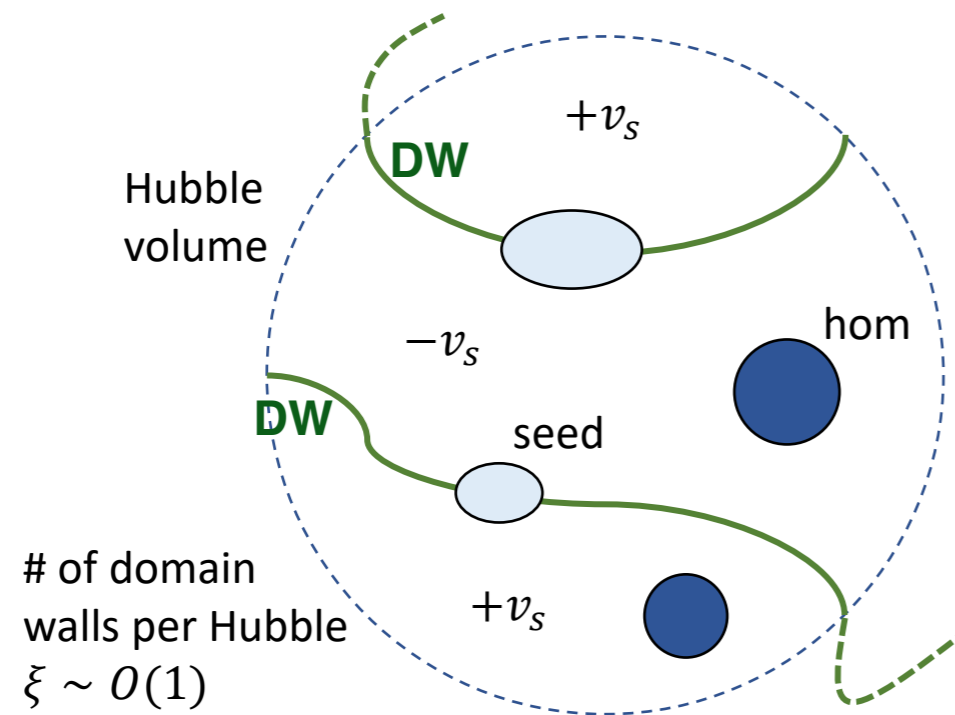


★ They can act as **seed** for the second step of the PT, when EW symmetry is broken

*Minimal realization of seeded EW phase transition*

# Seeded vs homogeneous nucleation

★ *Nucleation probability enhanced at the DW location*



\* *Nucleation rate/surface set by  $O(2)$  bounce action*

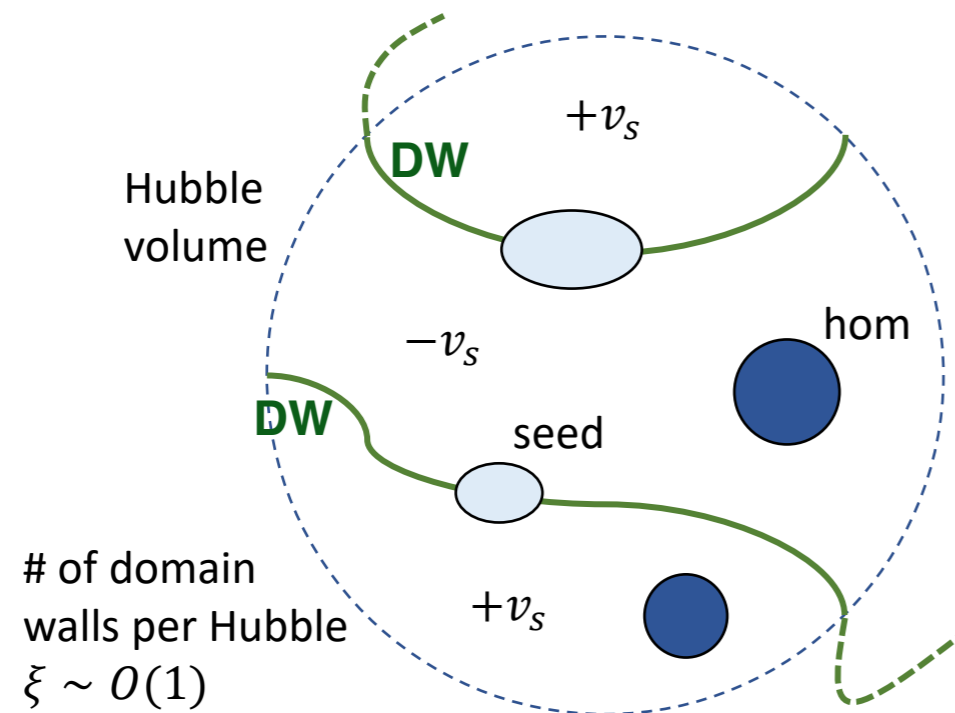
$$\gamma_S \sim T^3 e^{-S_2/T}$$

\* *Seeded nucleation condition*

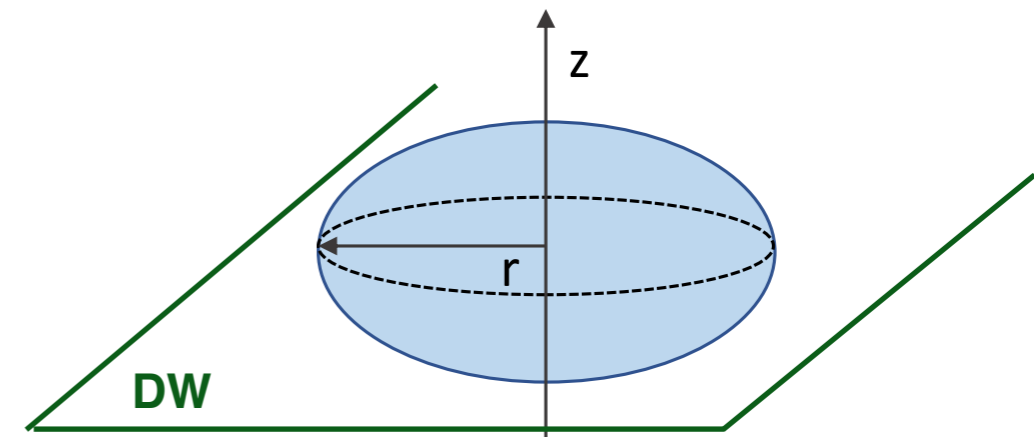
$$\xi \gamma_S \sim H^3$$

# Seeded vs homogeneous nucleation

## ★ Nucleation probability enhanced at the DW location



## Geometry of seeded critical bubble



## $O(2)$ symmetry on the DW plane

### \* Nucleation rate/surface set by $O(2)$ bounce action

$$\gamma_S \sim T^3 e^{-S_2/T}$$

### \* Seeded nucleation condition

$$\xi \gamma_S \sim H^3$$

◆ Bounce action for the  $O(2)$  symmetric seeded bubble

◆ How to compute it?

# Thin wall approximation

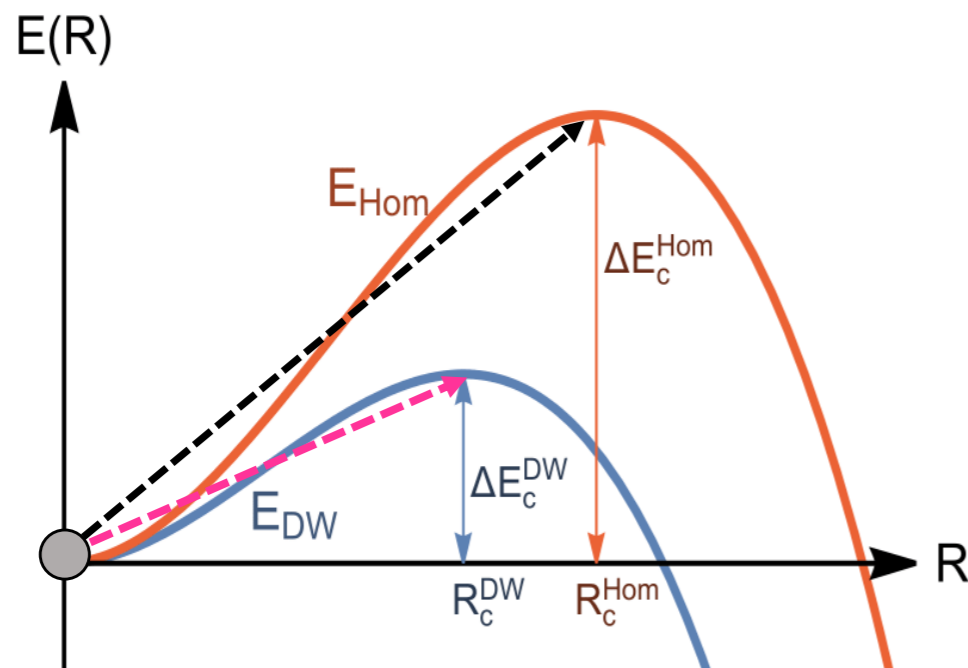
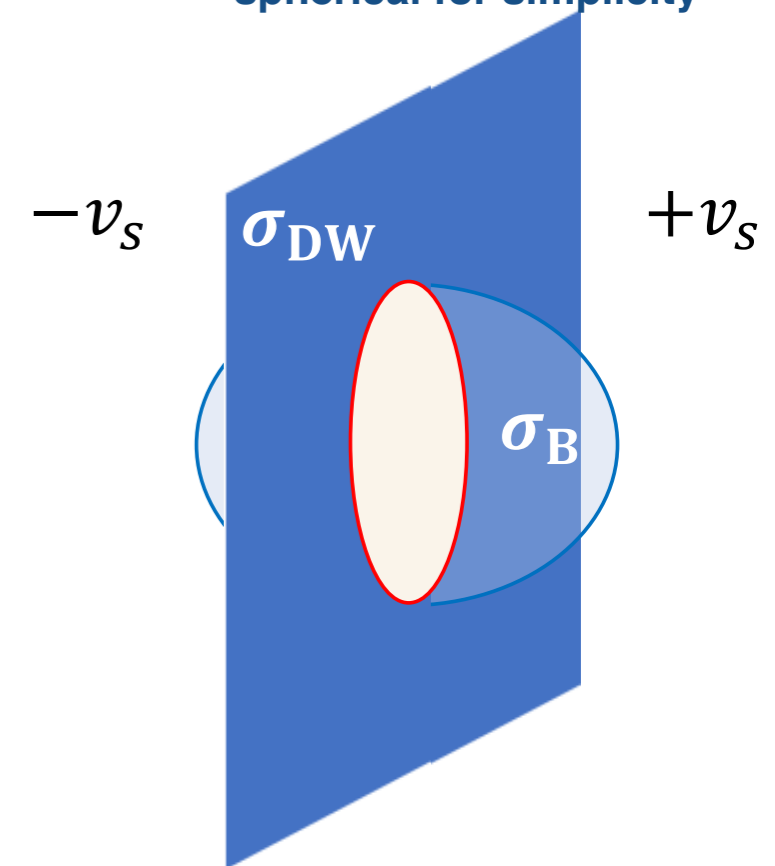
## ★Thin wall approximation to estimate energy of critical bubble

*As in Homogeneous PT*

$$E(R) \simeq 4\pi R^2 \sigma_B - \frac{4}{3} \pi R^3 \Delta V - \pi R^2 \sigma_{DW}$$

Surface tension of the bubble      Potential energy difference      Gain of eating DW inside bubble  
Tension of the DW

Assume bubble on DW  $O(3)$  spherical for simplicity



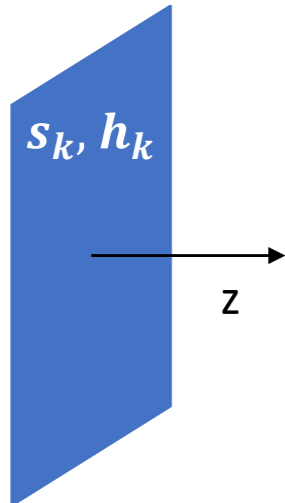
★Domain walls catalyze phase transition

$$\text{Rate} \sim e^{-\Delta E/T}$$

# Kaluza Klein reduction method

## ★ Study 3-dimensional theory on the domain wall

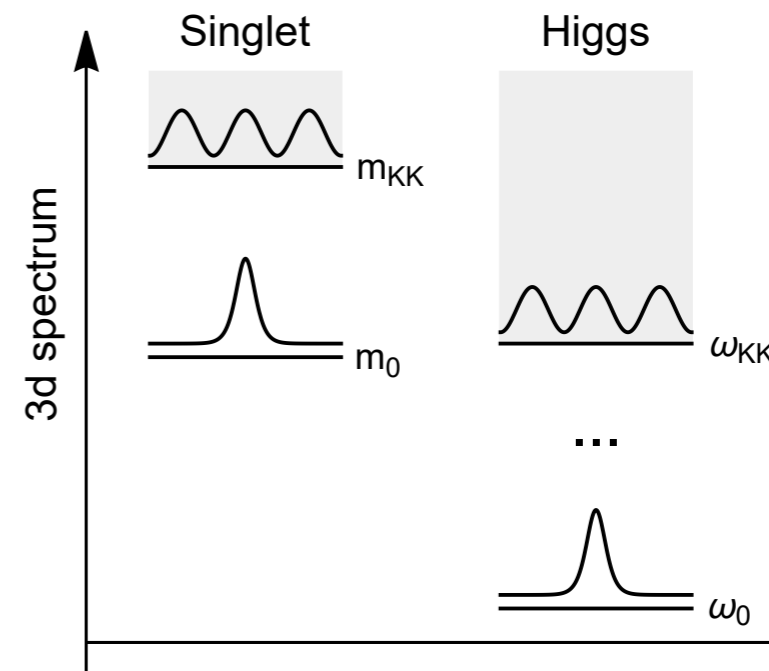
- \* KK spectrum contains massive localized states gapped to a continuum
- \* Bound states correspond to localized profiles in the z-direction
- \* Scattering states correspond to continuum



$$S = S_{\text{DW}}(z) + \sum_k s_k(x_\mu) \sigma_k(z)$$

$$h = \sum_k h_k(x_\mu) \phi_k(z)$$

$$x_\mu = t, x, y$$



### ◆ Metastability of DW controlled by the 3d h mass

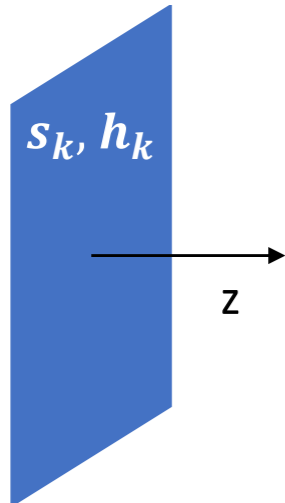
$\omega_0^2(T) < 0$  Classical instability of DW

$\omega_0^2(T) > 0$  Classically stable DW  
Seeded Tunnelling at  $T < T_c$

# Kaluza Klein reduction method

## ★ Study 3-dimensional theory on the domain wall

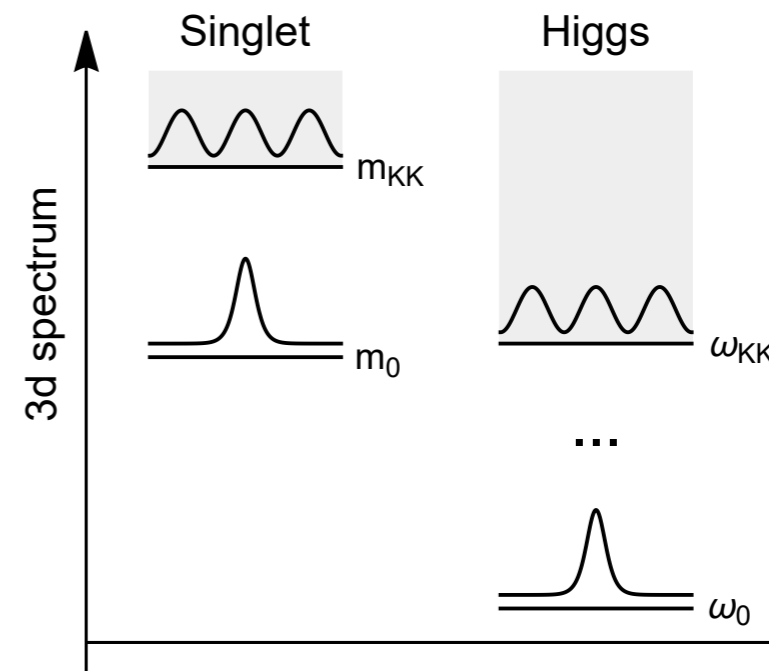
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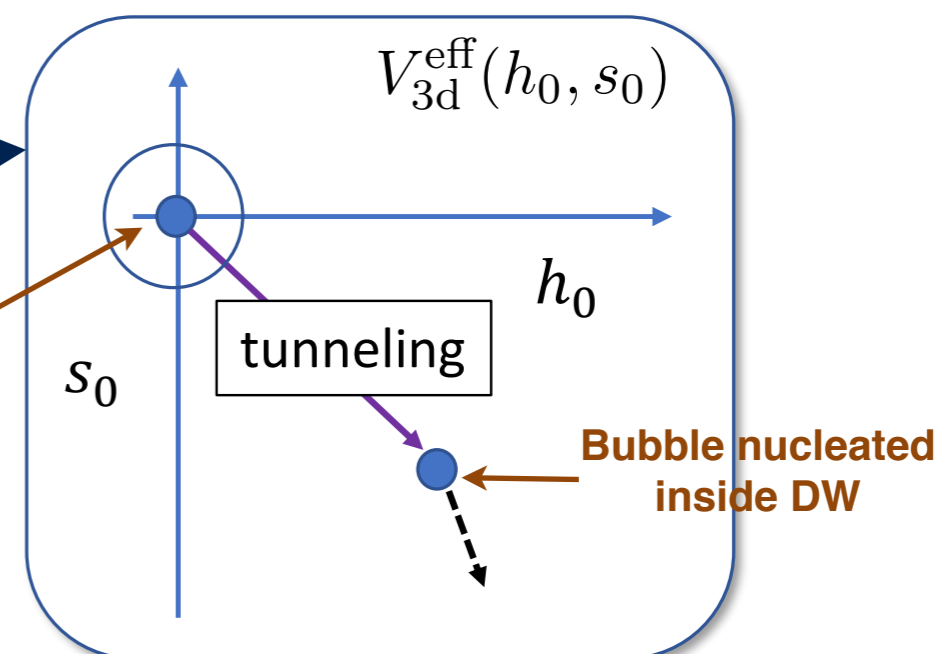
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$\omega_0^2(T) < 0$  Classical instability of DW

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Seeded Tunnelling at  $T < T_c$

Unperturbed  
domain wall  
No bubble

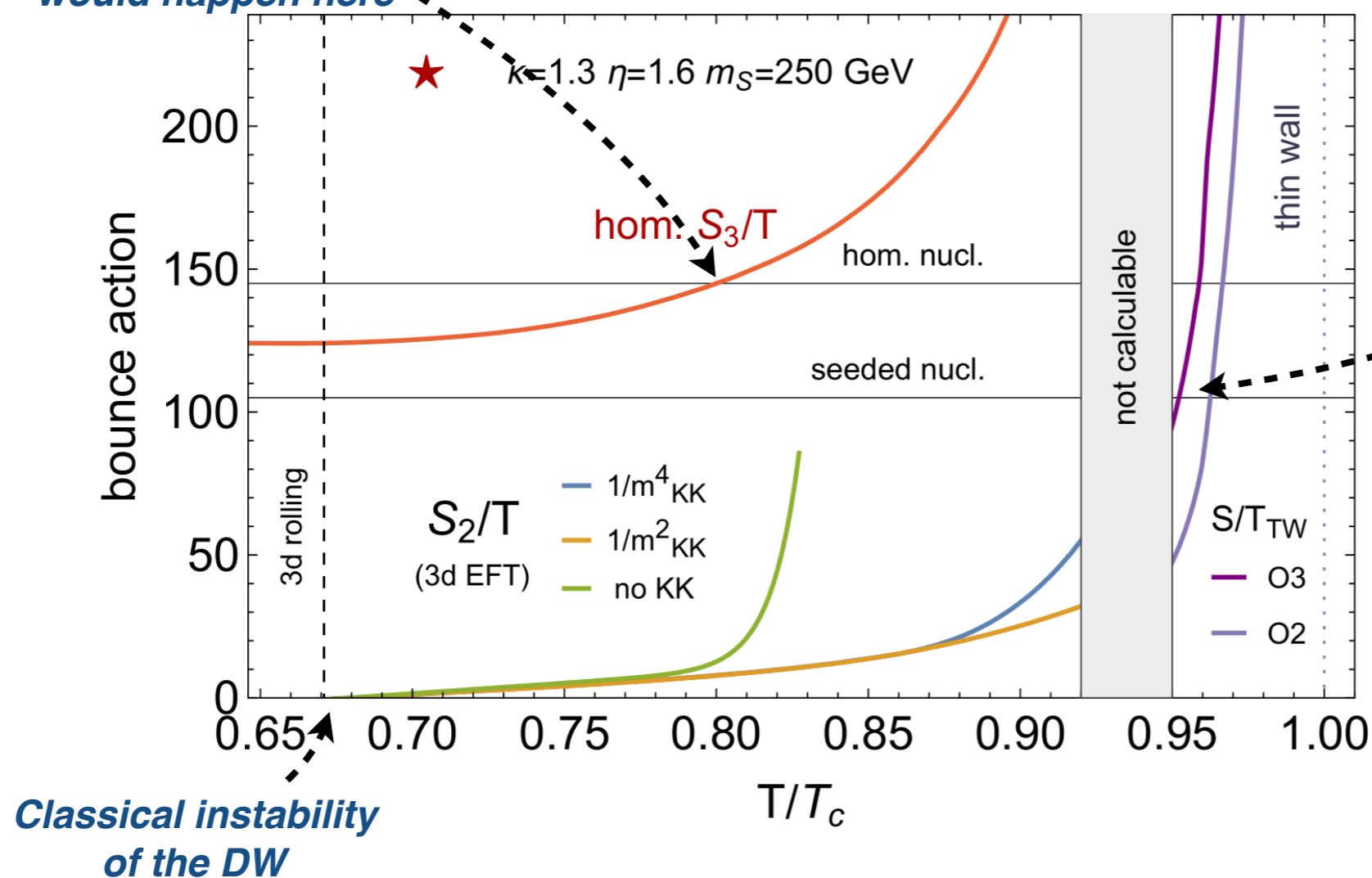
### ◆ The $O(2)$ seeded bubble profile can be obtained





# Bounce action

Homogeneous nucleation  
would happen here

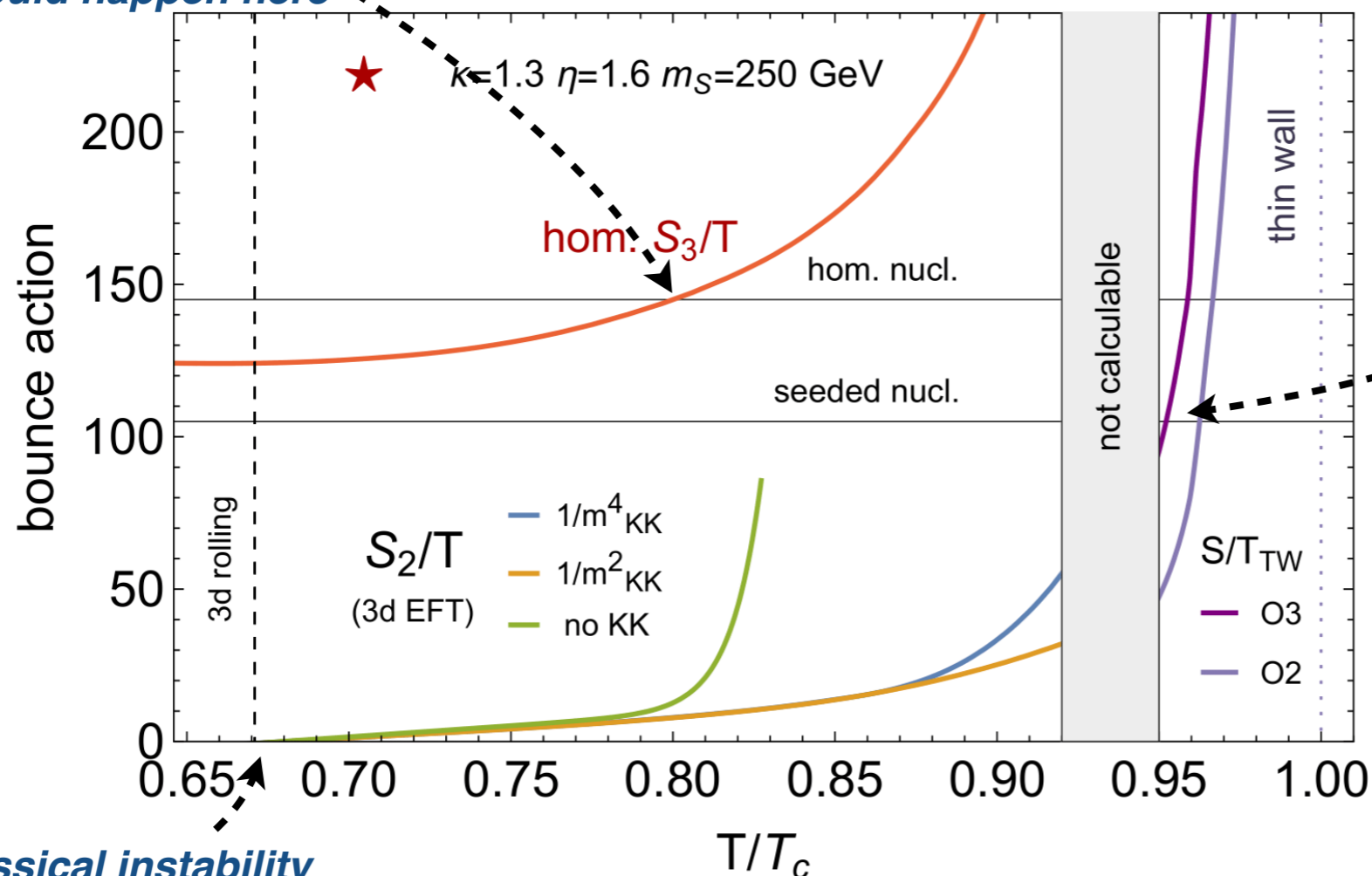


Seeded nucleation  
occurs here

★ *PT via nucleation on the DW always dominates*

# Bounce action

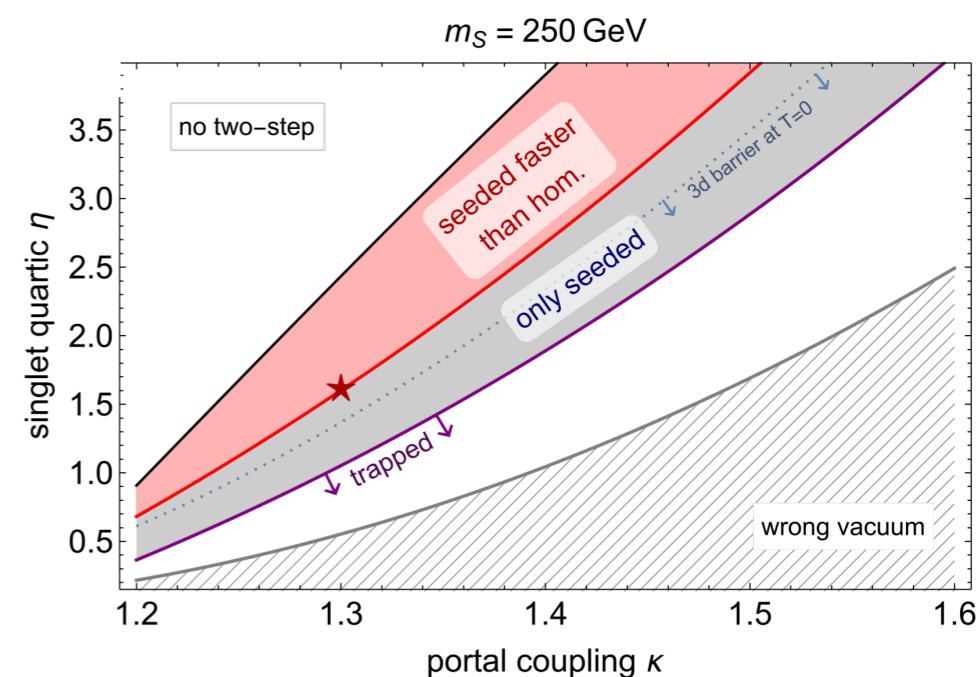
Homogeneous nucleation  
would happen here



Seeded nucleation  
occurs here

Classical instability  
of the DW

- ★ PT via nucleation on the DW always dominates
- ★ Completely new phenomenology of EW PT
- ★ Strong impact on parameter space



# Conclusions

★ *Impurities (topological defects) play a role in cosmological PT*

★ *Topological defects emerge in multi-step phase transitions*

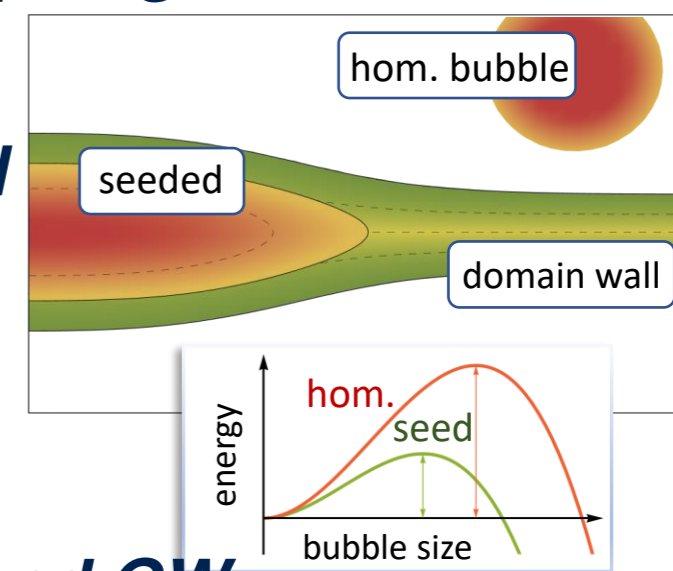
➔ *The EW phase transition **can be seeded** by topological defects*

★ *Minimal realization with DW in Higgs Singlet model*

★ *It can impact several well-known models*

\* E.g. Other Minimal extensions of Higgs sector, 2HDM, ...

★ *Phenomenological implications for baryogenesis and GW*



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***\* Thanks to Luciano for his legacy***