

The logo for BESIII, consisting of the letters 'B', 'E', 'S', and 'III' in a stylized font. 'B' is blue, 'E' is red, 'S' is green, and 'III' is black.

Search for Charged Lepton Flavor Violation in J/ψ decays at BESIII


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Sun Yat-sen University

On behalf of **BESIII** Collaboration

New Frontiers in Lepton Flavor (INFN), PISA, Italy

2023.5.15

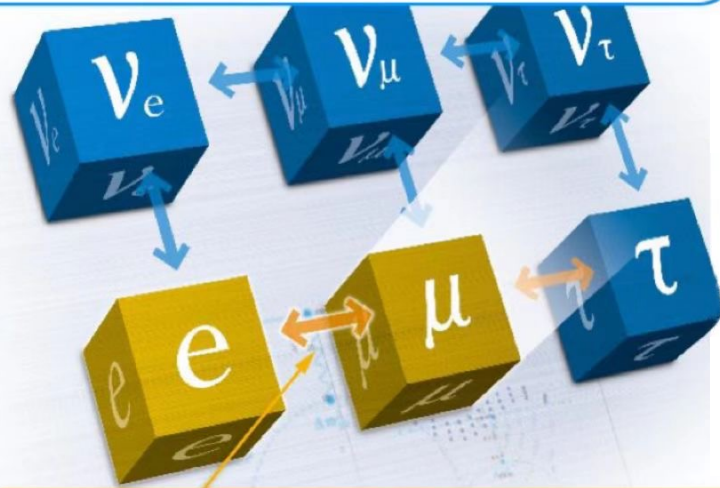




- ◆ Motivation
- ◆ BESIII introduction
- ◆ Search for charged lepton flavor violating decay $J/\psi \rightarrow e\tau$
- ◆ Search for charged lepton flavor violating decay $J/\psi \rightarrow e\mu$
- ◆ Summary

Motivation

Neutrino Flavor Violation is observed !



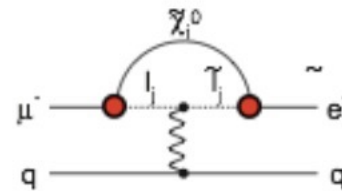
- ◆ Since LFV decay is forbidden in the SM, the observation of any LFV decay would be a signal of new physics beyond SM.
- ◆ In SM, Lepton Flavor is conserved for zero degenerate ν masses and now we have clear indication that ν s have non-zero mass.

charged Lepton Flavor Violation !? (cLFV)

◆ Models may enhance LFV effects up to a detectable level, such as leptoquark, Compositeness, Supersymmetry, Heavy Z' and Anomalous boson Coupling model.

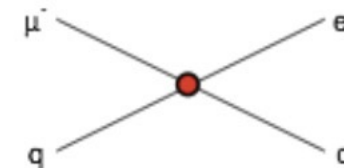
Supersymmetry

$$\text{rate} \sim 10^{-15}$$



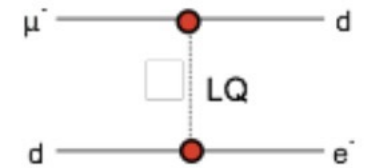
Compositeness

$$\Lambda_c \sim 3000 \text{ TeV}$$



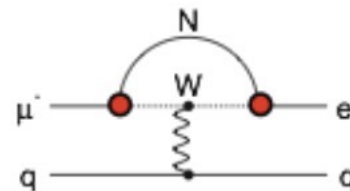
Leptoquark

$$M_{LQ} = 3000 (\lambda_{\mu d} \lambda_{e d})^{1/2} \text{ TeV}/c^2$$



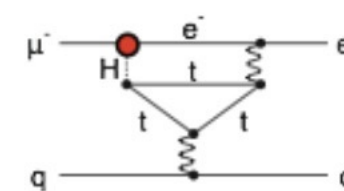
Heavy Neutrinos

$$|U_{\mu N} U_{e N}|^2 \sim 8 \times 10^{-13}$$



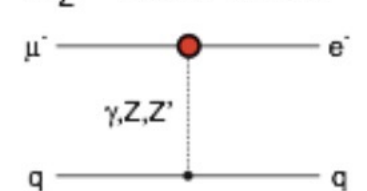
Second Higgs Doublet

$$g(H_{\mu e}) \sim 10^{-4} g(H_{\mu\mu})$$



**Heavy Z'
Anomal. Z Coupling**

$$M_{Z'} = 3000 \text{ TeV}/c^2$$

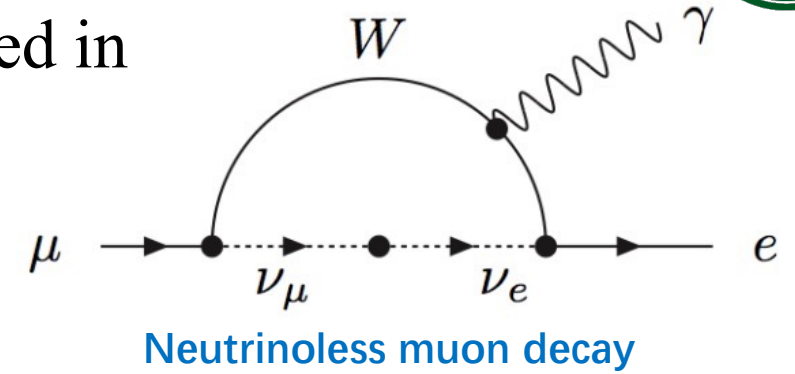


Motivation



- ◆ In the charged lepton sector, LFV is heavily suppressed in the Standard Model.

$$BR(\mu \rightarrow e\gamma) = \frac{3\alpha}{32\pi} \left| \sum_{i=2,3} U_{\mu i}^* U_{ei} \frac{\Delta m_{1i}^2}{M_W^2} \right|^2 < 10^{-54}$$



- ◆ Both experimental searches and upper-limit predictions, including μ, τ LFV decays, π, K LFV decays and $\phi, J/\psi$ two-body LFV decays, etc.

Leptoquarks can couple to a lepton-quark pair and induce the LFV two-body decays of J/ψ .

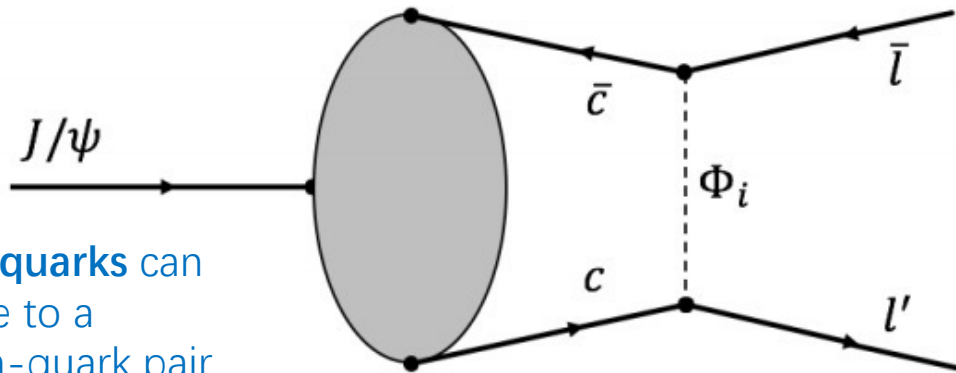


Diagram via leptoquarks

Phys. Rev. D 67, 114001 (2003)
Phys. Lett. B 496, 89 (2000)

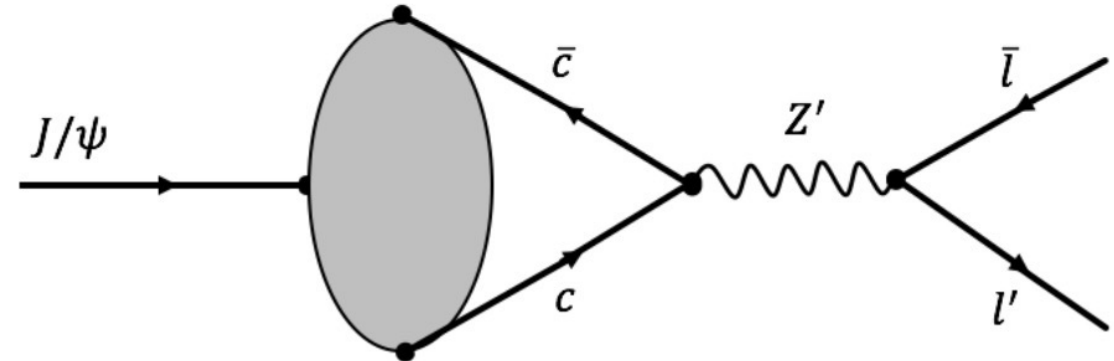


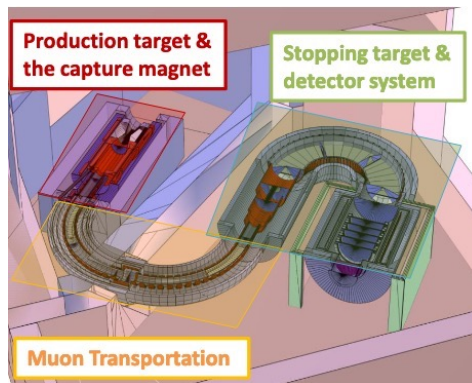
Diagram via a Z' in TC2 models



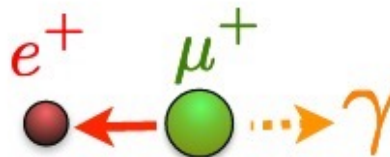
CLFV

- ◆ $B(\mu^+ \rightarrow e^+ \gamma) < 4.2 \times 10^{-13}$ @ 90% C.L. **MEG**
- ◆ $B(\tau^+ \rightarrow e^+ \gamma) < 3.3 \times 10^{-8}$ @ 90% C.L. **BABAR**
- ◆ $B(\mu \rightarrow 3e) < 1.0 \times 10^{-12}$ @ 90% C.L. **SINDRUM**
- ◆ $B(Z \rightarrow e^\pm \mu^\mp) < 7.5 \times 10^{-7}$ @ 90% C.L. **ATLAS**
- ◆ $B(\phi \rightarrow e^\pm \mu^\mp) < 2 \times 10^{-6}$ @ 90% C.L. **SND**
- ◆ $B(J/\psi \rightarrow \mu^\pm \tau^\mp) < 2 \times 10^{-6}$ @ 90% C.L. **BES**

Current best limit



COMET



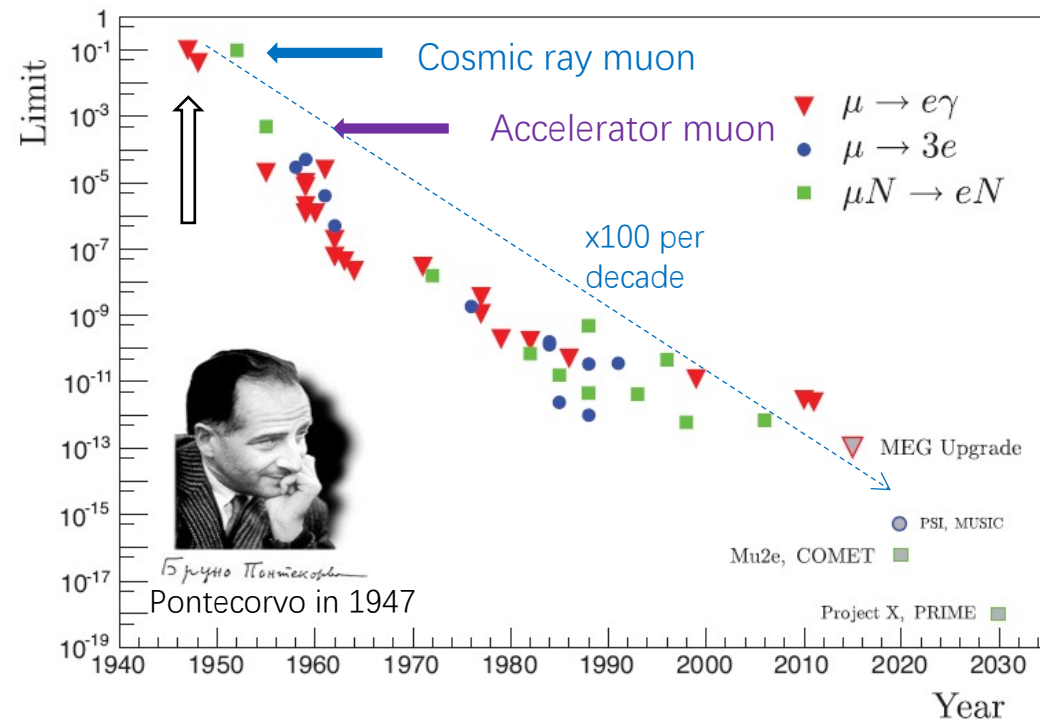
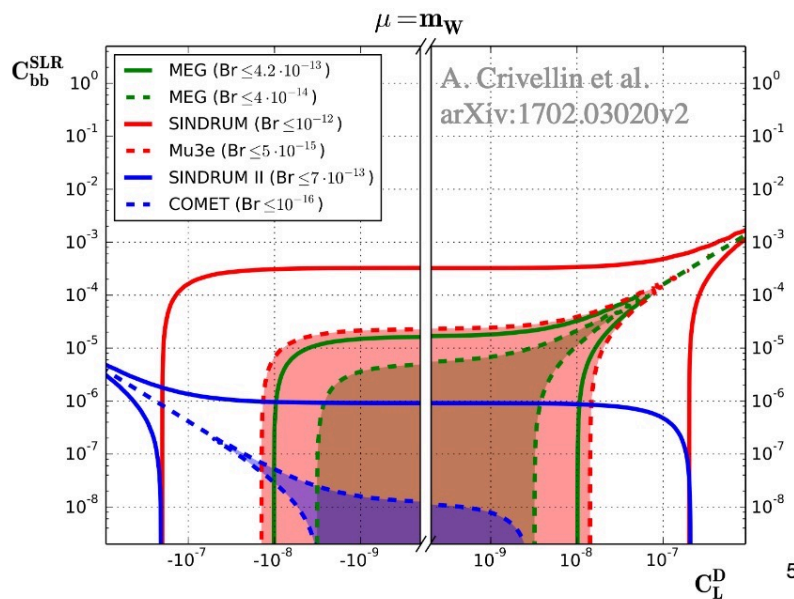
MEGII process

- ◆ **Mu2e** will search for CLFV with $\mu N \rightarrow e N$

Improve the current limit by a factor of 10^4
Search for New Physics with mass scale up to 10^4 TeV

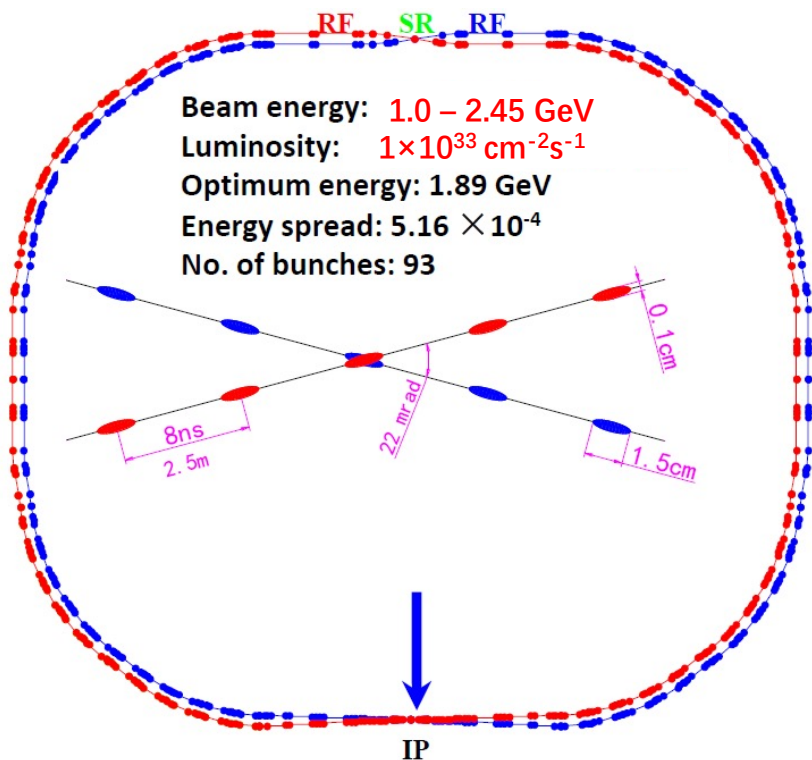
- ◆ **COMET** will search for CLFV with $\mu N \rightarrow e N$
Next goal $< 6 \times 10^{-17}$ (90% C.L.)

- ◆ **MEGII** and **Mu3e** has similar beam requirements.
Intensity $O(10^8)$ muon/s, low momentum $p = 28$ MeV/c
MEGII is expect to start next year the full engineering run aiming at a sensitivity down to 6×10^{-14} (90% C.L.)



Eur. Phys. J. C 76, 434 (2016)
Phys. Rev. Lett. 104, 021802 (2010)
Nucl. Phys. B 299, 1 (1988).
Phys. Rev. D 90, 072010 (2014)
Phys. Rev. D 81, 057102 (2010)
Phys. Lett. B 598, 172 (2004)

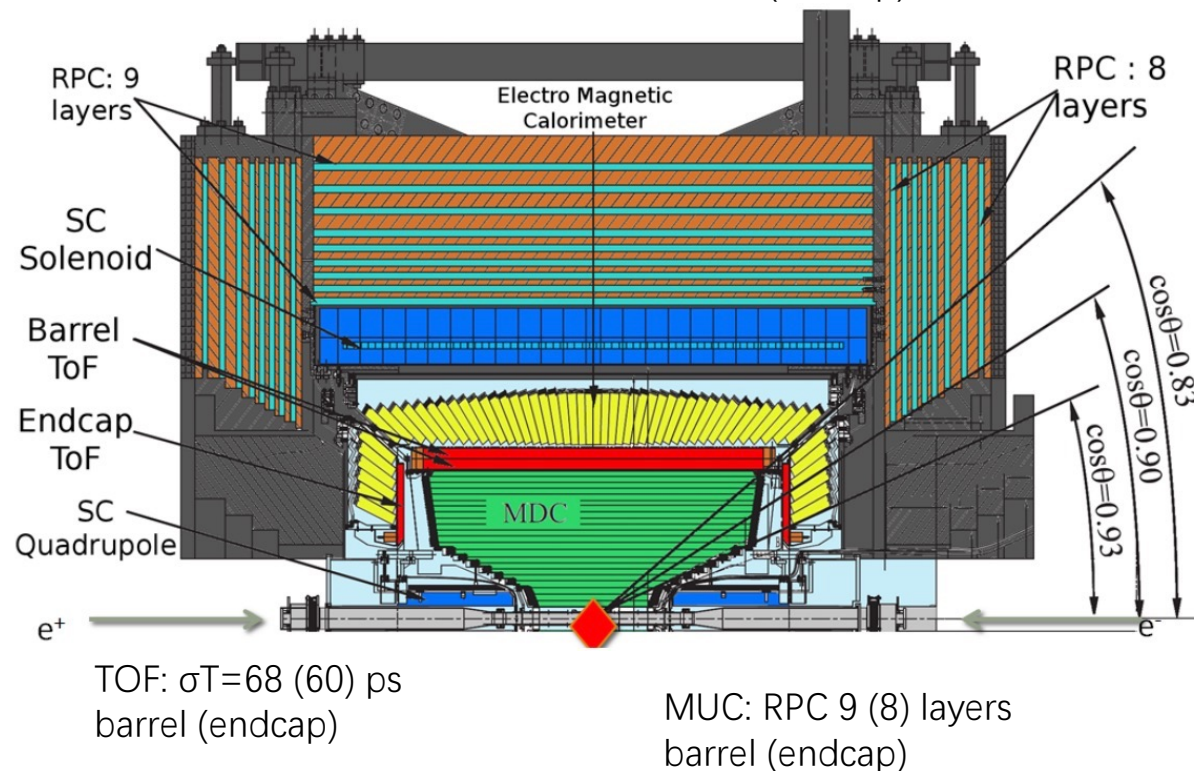
Beijing Electron Positron Collider II



BESIII Detector

MDC: $\sigma_p = 0.5\%$ @ 1 GeV/c
 dE/dx : 6%

EMC: CsI (TI) 2.5% (5.0%)
 barrel (endcap) @ 1 GeV



BESIII Physics Data

Physics of BESIII

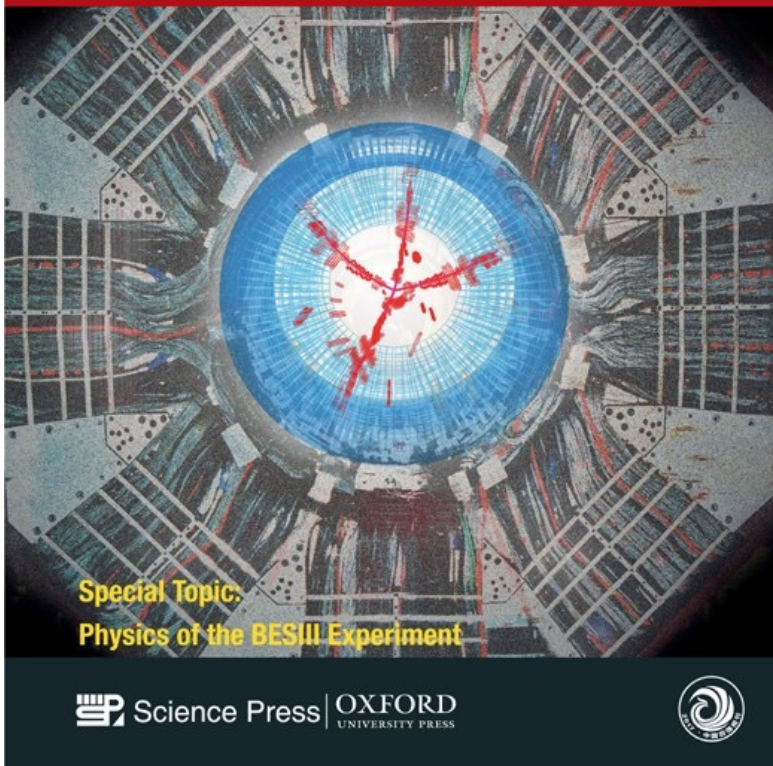
NSR 8 (11) 2021

NSR 国家科学评论
National
Science
Review

PRINT ISSN 2095-5138
ONLINE ISSN 2053-714X
academic.eup.com/nsr

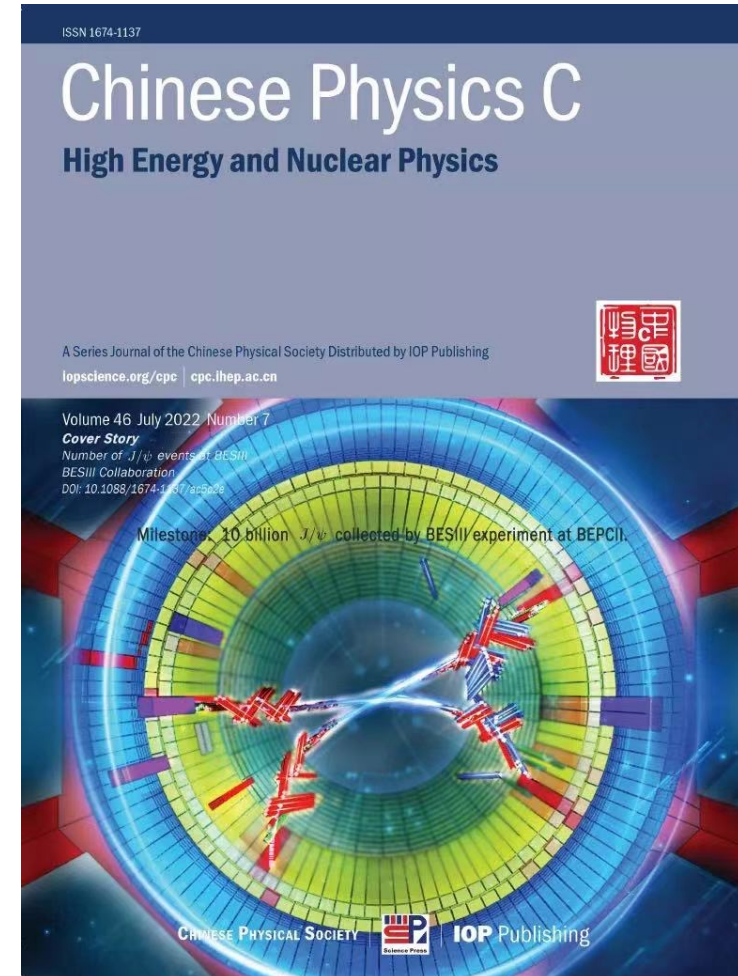


VOLUME 8 • ISSUE 11 • NOVEMBER 2021



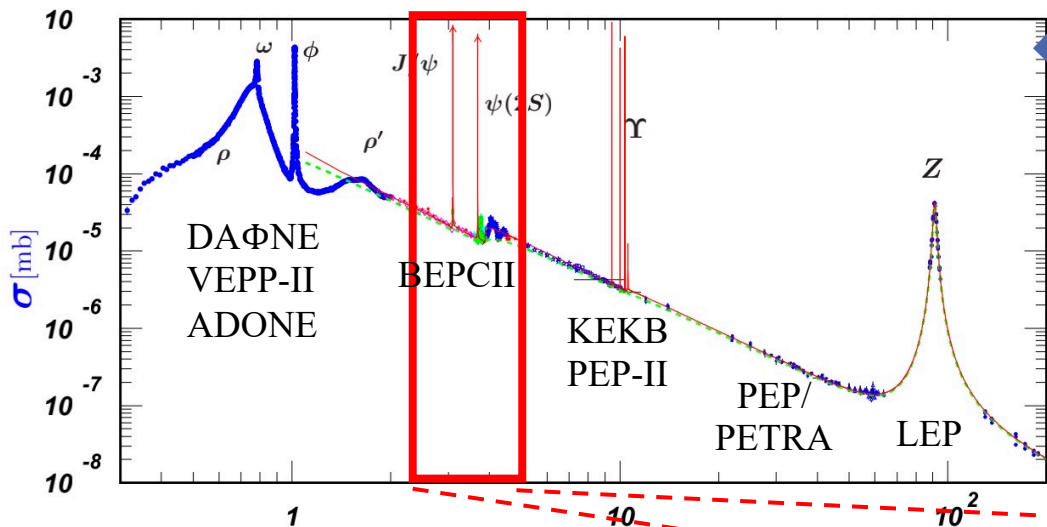
10 Billion J/ψ collected by BESIII

CPC 46 074001 (2022)



PhiPsi2022

BESIII data samples



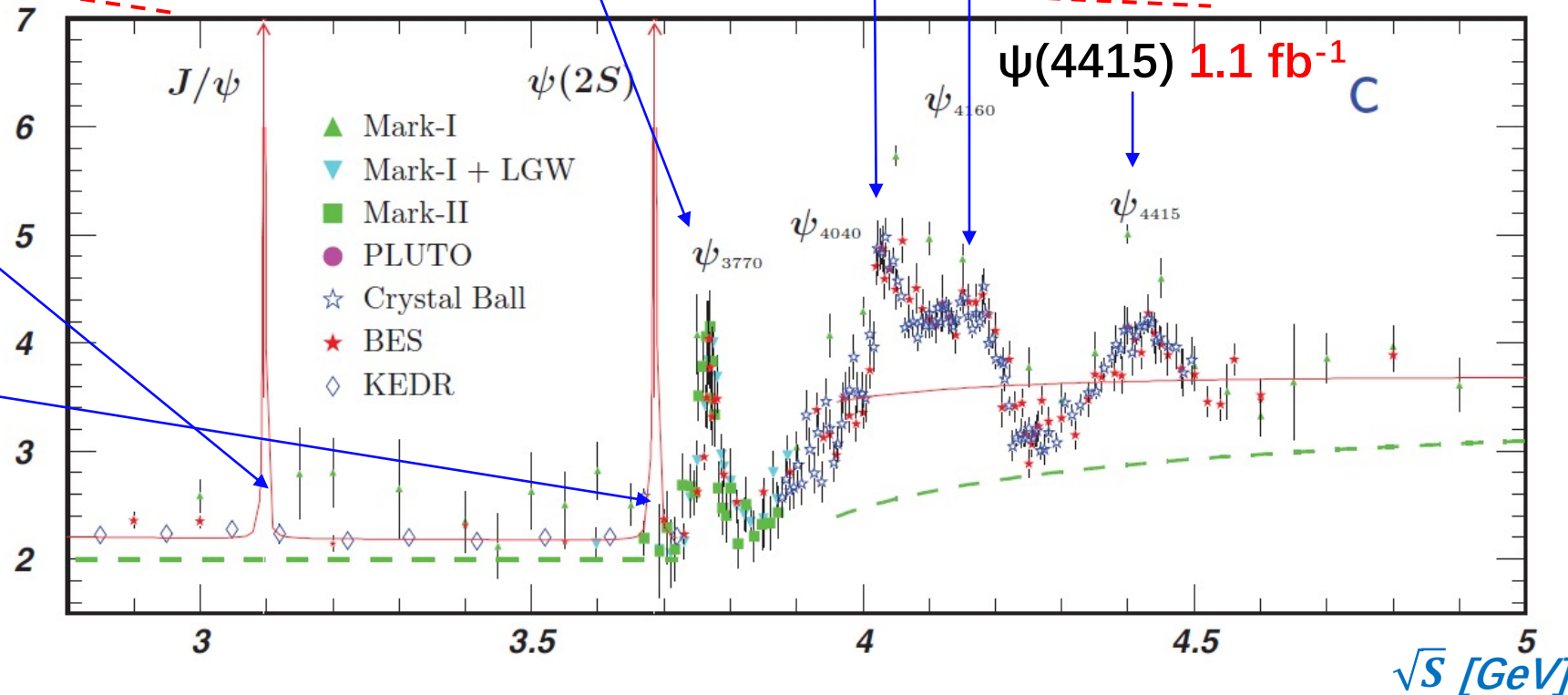
- ◆ BESIII has collected the largest data samples of J/ψ & $\psi(3686)$ on threshold in the world, $> 20 \text{ fb}^{-1}$ above 4.0 GeV in total

$\psi(3770)$ 2.9 fb^{-1} $\psi(4040)$ 0.5 fb^{-1}
 $\psi(4160)$ 3.2 fb^{-1}

J/ψ 1.0×10^{10}

$\psi(3686)$ 2.7×10^9

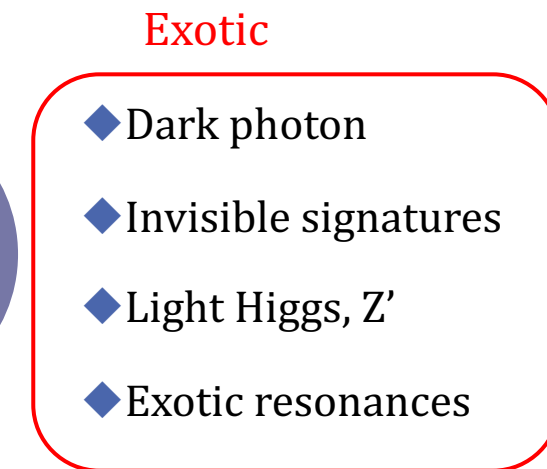
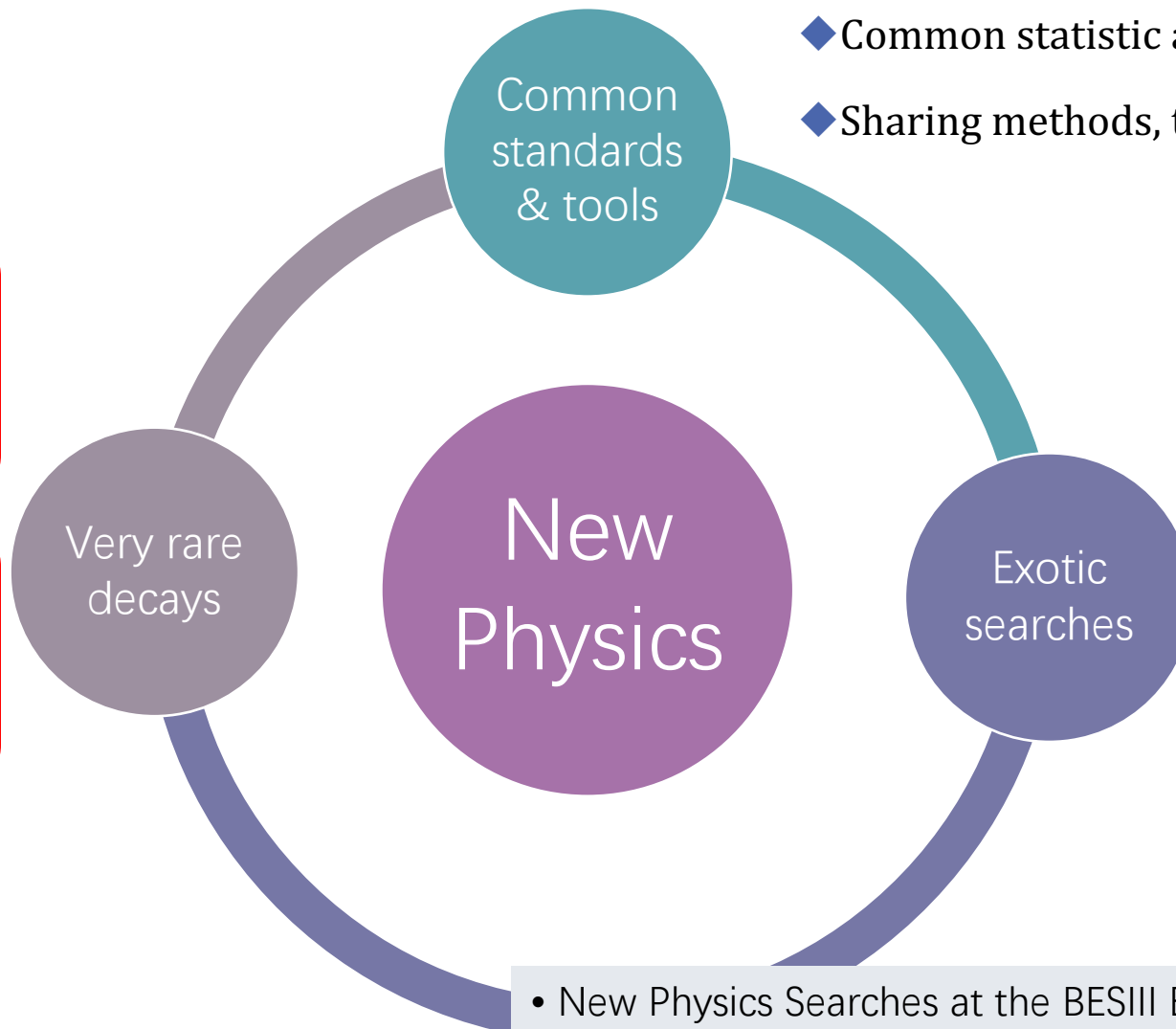
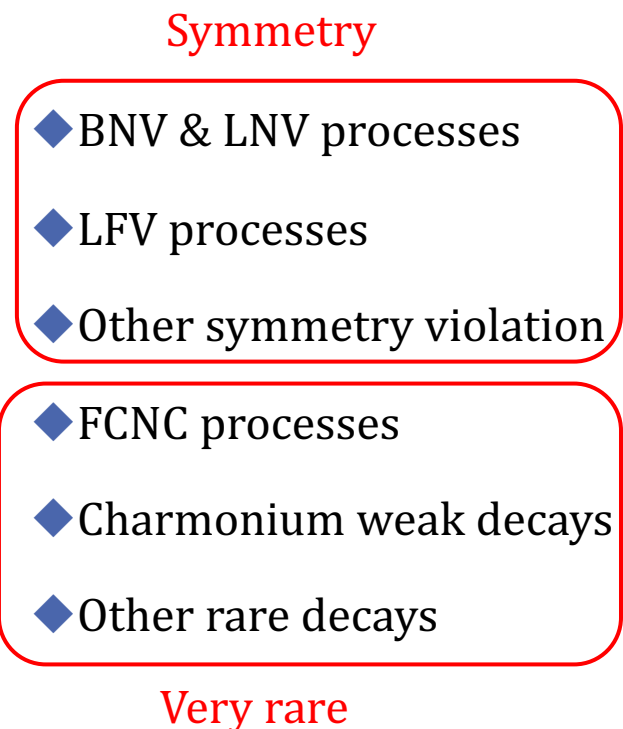
R



\sqrt{s} [GeV]



- ◆ Uniform blinding strategy and datasets
- ◆ Common statistic and standards
- ◆ Sharing methods, tools and codes



- New Physics Searches at the BESIII Experiment, S.J. Chen and S. Olsen, National Science Review 8, nwab189 (2021), arXiv: 2102.13290
- New Physics Program of BES, D.Y. Wang, in "30 Years of BES Physics"



- ◆ The cLFV decays of vector mesons $V \rightarrow l_i l_j$ are also predicted in various of extension models of SM:

$$\mathcal{B}(J/\psi \rightarrow e\mu) \text{ to } 10^{-16} \sim 10^{-9} @ 90\% \text{ C.L.}$$

$$\mathcal{B}(J/\psi \rightarrow e(\mu)\tau) \text{ to } 10^{-10} \sim 10^{-8} @ 90\% \text{ C.L.}$$

Phys. Rev. D 63, 016003,
 Phys. Rev. D 63, 016006
 Phys. Rev. D 83, 115015
 Phys. Lett. A 27, 1250172
 Phys. Rev. D 94, 074023,
 Phys. Rev. D 97, 056027

- ◆ Experimental results before:

Decay mode	BESII UL (90%)	BESIII UL (90%)
Number of J/ψ	58×10^6	225.3×10^6
$\mathcal{B}(J/\psi \rightarrow e\mu)$	$< 1.1 \times 10^{-6}$	$< 1.6 \times 10^{-7}$
$\mathcal{B}(J/\psi \rightarrow e\tau)$	$< 8.3 \times 10^{-6}$	-
$\mathcal{B}(J/\psi \rightarrow \mu\tau)$	$< 2.0 \times 10^{-6}$	-

Phys. Lett. B 561, 112007
 Phys. Lett. B 598, 172
 Phys. Rev. D 87, 112007



Search for charged lepton flavor
violating decay $J/\psi \rightarrow e\tau$

Data samples



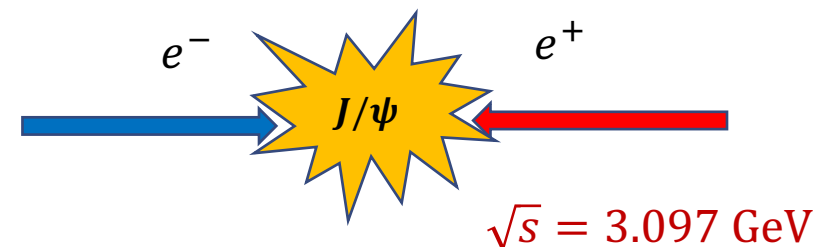
- ◆ Based on **10 billion** data set: 1310.6M collected @2009+2012 (sample I), 8774.01M collected @2017-2019 (sample II).

Decay chain	Generator	Generated
$J/\psi \rightarrow \omega f_2(1270), \omega \rightarrow \pi^0 \gamma, f_2(1270) \rightarrow \pi^+ \pi^-$	PHSP, VSP_PWAVE, TSS	5.8M
$J/\psi \rightarrow \eta n \bar{n}, \eta \rightarrow \gamma \gamma$	PHSP	5.8M
$J/\psi \rightarrow \pi^+ \pi^- \pi^0$	OMEGA-DALITZ	29M
$J/\psi \rightarrow \rho \pi$	HELAMP	29M
$J/\psi \rightarrow \pi^0 e^+ e^-$	PHSP	29M
$J/\psi \rightarrow \bar{p} n \pi^+$	PHSP	5.8M
$J/\psi \rightarrow K^* \bar{K}^0 (K^* \rightarrow K^+ \pi^-) + c.c.$	HELAMP, VSS	11.6M

Generator and number of events list for exclusive MC samples of 2009 and 2012

Decay chain	Generator	Generated
$J/\psi \rightarrow \omega f_2(1270), \omega \rightarrow \pi^0 \gamma, f_2(1270) \rightarrow \pi^+ \pi^-$	PHSP, VSP_PWAVE, TSS	19M
$J/\psi \rightarrow \rho \pi$ (include direct $\pi^+ \pi^- \pi^0$)	HELAMP, OMEGA-DALITZ	190M
$J/\psi \rightarrow \bar{p} n \pi^+$	PHSP	38M

Generator and number of events list for exclusive MC samples of 2018 and 2019



- ◆ Inclusive samples:
225 million @ 2009
1000 million @ 2012
4600 million @ 2018
4100 million @ 2019
- ◆ 1 million τ inclusive events with $J/\psi \rightarrow e\tau$ and τ inclusive decays to any decay channels

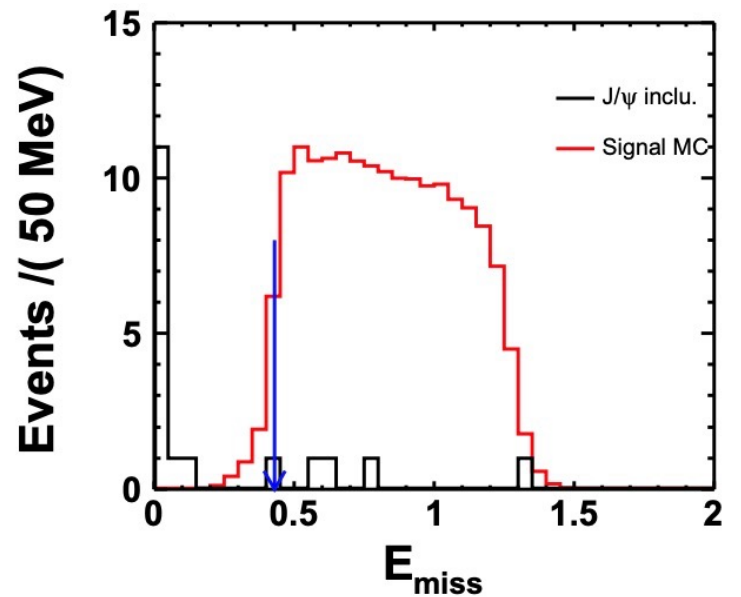
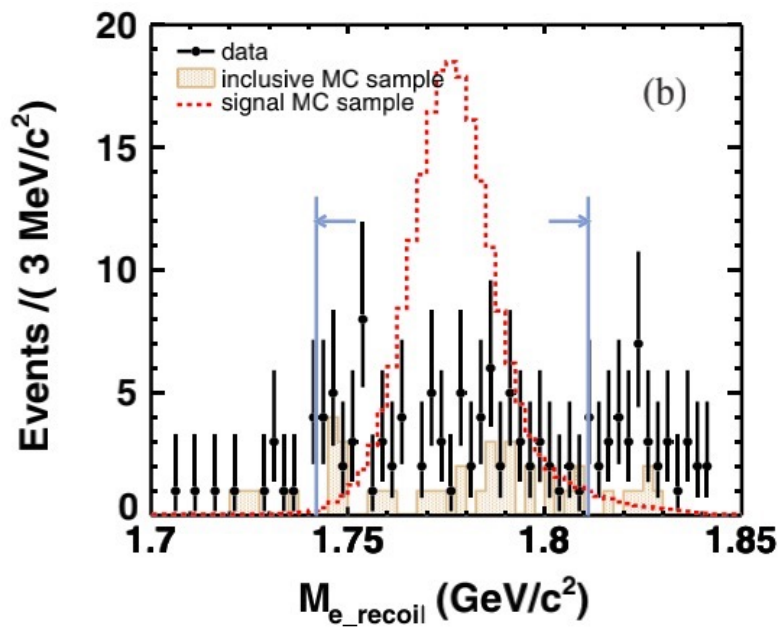
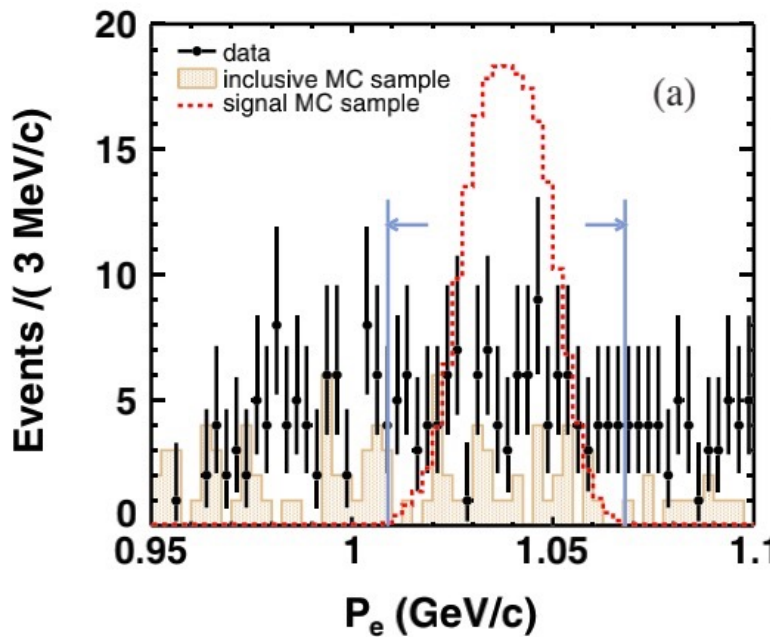
Event Selection

◆ $J/\psi \rightarrow e\tau, \tau \rightarrow \pi\pi^0\nu$

- ◆ Select one electron and one charged pion
- ◆ At least two photon showers and one π^0
- ◆ The final-state electron from the process $J/\psi \rightarrow e\tau$ is monochromatic, therefore the momentum of the electron P_e and the recoiling mass against the electron M_{e_recoil}
- ◆ One undetected neutrino with missing energy $E_{miss} > 0.43\text{GeV}$

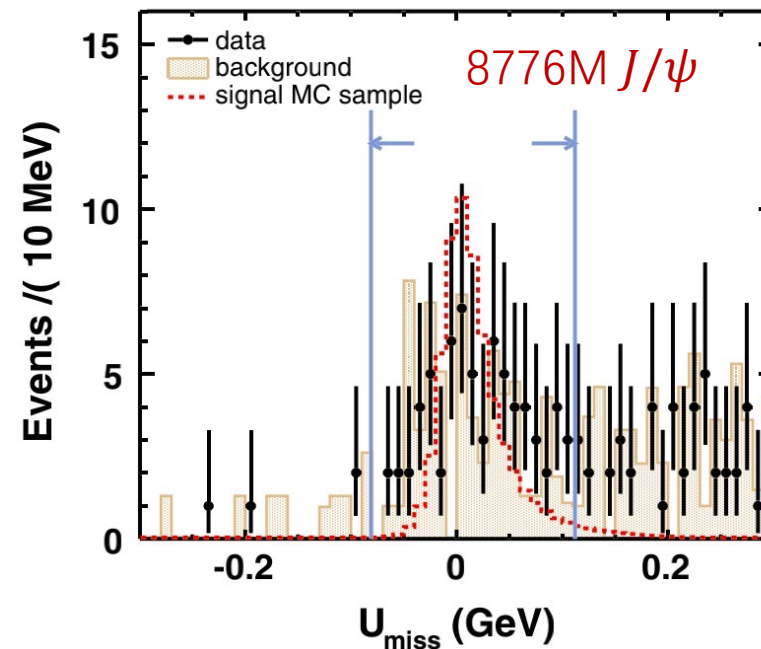
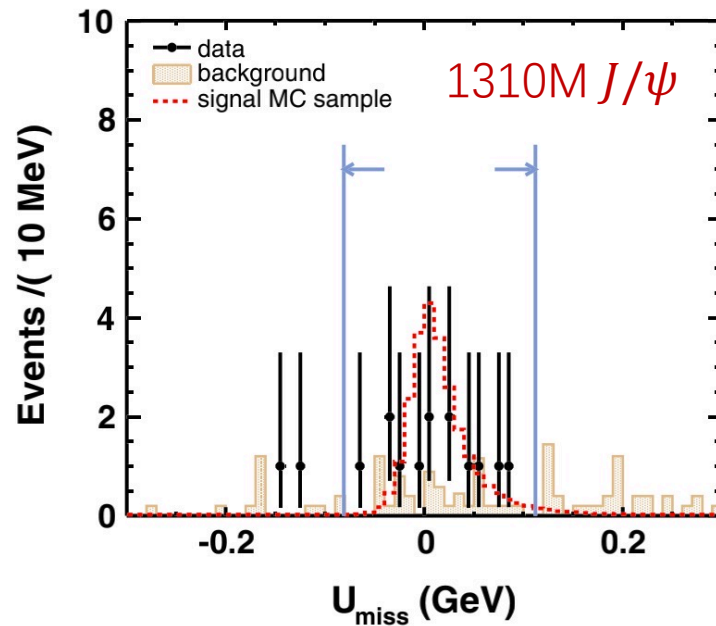
$$E_{miss} = E_{CMS} - E_e - E_\pi - E_{\pi^0}$$

$$\vec{p}_{miss} = \vec{p}_{J/\psi} - \vec{p}_e - \vec{p}_\pi - \vec{p}_{\pi^0}$$



Background study

- ◆ The dominant background contaminations stem from the continuum process (e.g. radiative Bhabha) and from hadronic J/ψ decays such as $J/\psi \rightarrow \pi^+ \pi^- \pi^0$
- ◆ $U_{miss} = E_{miss} - c|\vec{P}_{miss}|$, The areas between the arrows represent the signal region.
- ◆ In total, 6.9 ± 1.9 (63.6 ± 13.2) background events are expected for the data sample I (II).



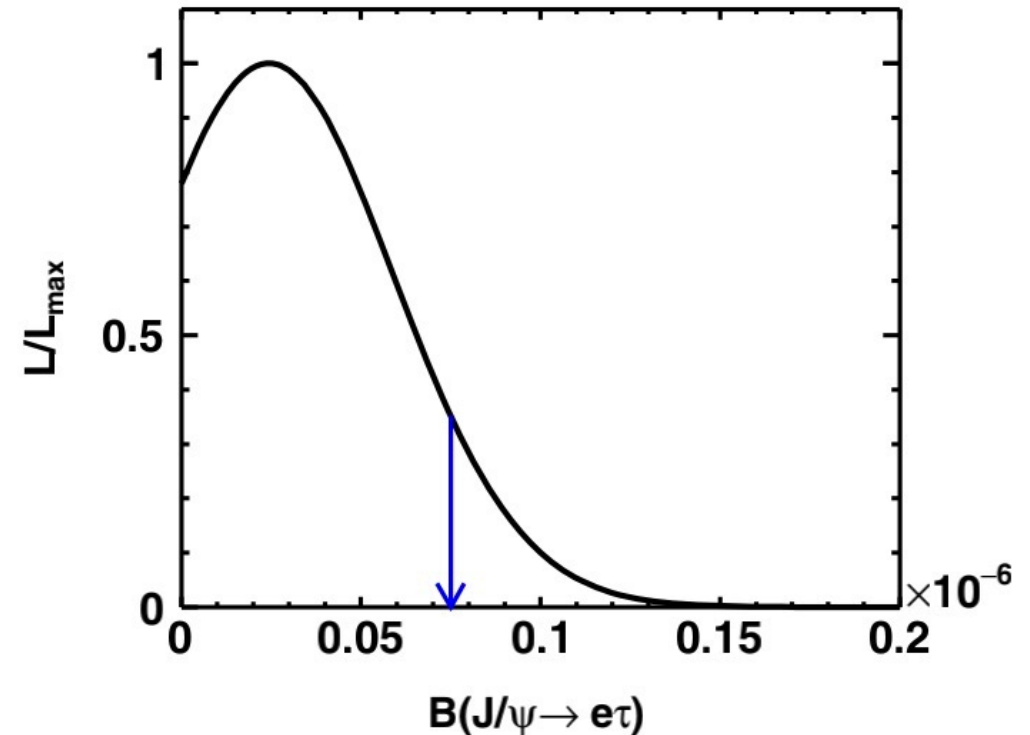
◆ Determination of upper limit at 90% confidence level (C.L.) with Bayesian method.

Combined result:

$$B(J/\psi \rightarrow e\tau) < 7.5 \times 10^{-8} \text{ @ 90\% C.L.}$$

◆ The 1st submitted paper based on full 10 billion J/ψ data of BESIII

◆ This result improves the previous published limits by **two orders of magnitude** and is comparable with the theoretical predictions.



Phys. Rev. D 103, 112007 (2021)



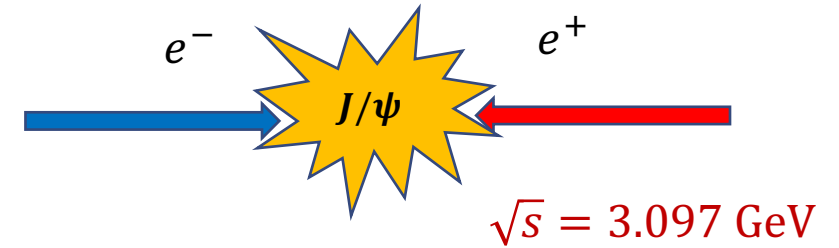
Search for charged lepton flavor
violating decay $J/\psi \rightarrow e\mu$

Data samples



Data size 09+17-19 (10^6)

➤ Data: Full J/ψ	8998	
$\psi(3770)$	2.93 fb^{-1}	
$\chi_{c1}(1P)$	458.21 pb^{-1}	
3.080GeV data	168.58 pb^{-1}	
➤ Signal MC: $J/\psi \rightarrow e\mu$	0.1+0.1+0.1	PHOTOS VLL
➤ Exclusive MC		
$J/\psi \rightarrow ee$	133.8+5239	PHOTOS VLL
$J/\psi \rightarrow \mu\mu$	133.6+5230	PHOTOS VLL
$J/\psi \rightarrow \pi\pi$	0.33+12.90	VSS
$J/\psi \rightarrow KK$	0.64+25.10	VSS
$J/\psi \rightarrow pp$	4.75+1860	J2BB1
➤ Continuum MC:		
$ee \rightarrow ee(\gamma)$	81+526.1	Babayaga
$ee \rightarrow \mu\mu(\gamma)$	0.3+1.9	Babayaga
➤ Inclusive MC: Full J/ψ	230+8774	Evtgen & LundCharm



Preliminary Selection

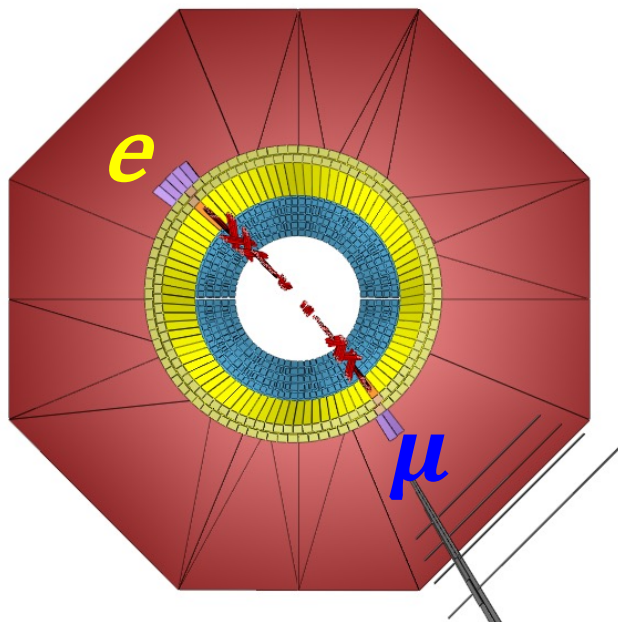


➤ Good charged track:

- $|V_r| < 1.0 \text{ cm}$;
- $|V_z| < 10.0 \text{ cm}$;
- $|\cos\theta| < 0.93$;
- $N_{charge}^{good} = 2, \Sigma Q = 0$;
- Two charged tracks $\Delta T \leq 1.0 \text{ ns}$

➤ Good photon:

- Barrel ($|\cos\theta| < 0.80$) $E_{\gamma 1} > 25 \text{ MeV}$;
- Endcap ($0.86 < |\cos\theta| < 0.92$) $E_{\gamma 2} > 50 \text{ MeV}$;
- Gap ($0.80 < |\cos\theta| < 0.86$) $E_{\gamma 3} > 50 \text{ MeV}$;
- TDC time window $[0, 700] \text{ ns}$;
- Angle with nearest charged track $> 20^\circ$;
- Reject the events with $N_\gamma > 0$



➤ Particle ID:

- π : $\text{prob}(\pi) \geq 0 \ \&\& \ \text{prob}(\pi) \geq \text{prob}(K)$;
- K : $\text{prob}(K) \geq 0 \ \&\& \ \text{prob}(K) \geq \text{prob}(\pi)$;
- p : $\text{prob}(p) \geq 0 \ \&\& \ \text{prob}(p) \geq \text{prob}(K) \ \&\& \ \text{prob}(p) \geq \text{prob}(\pi)$

Event Selection



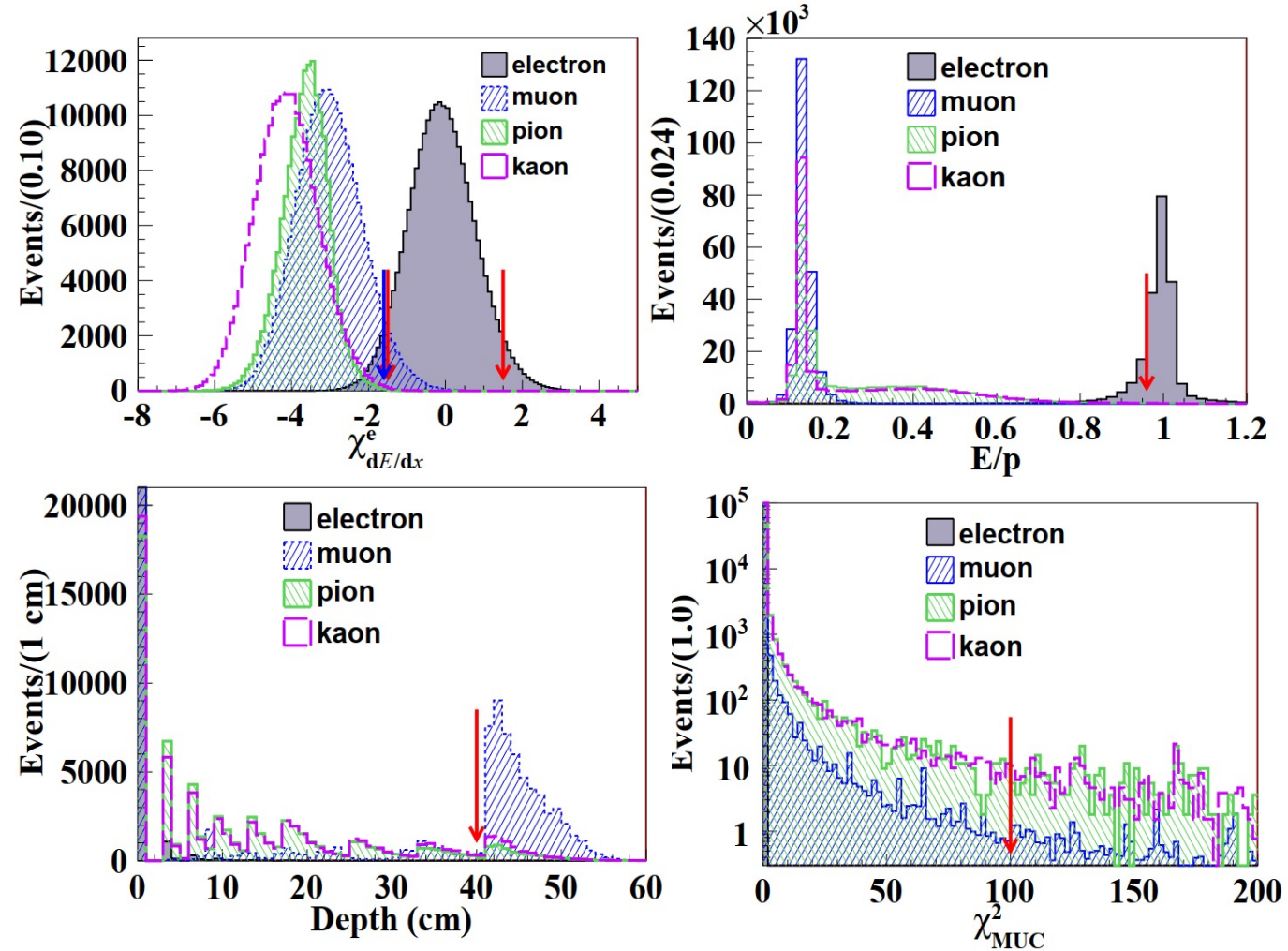
- ◆ Each J/ψ candidate is reconstructed with two back-to-back good charged tracks, which will be further identified as electron and muon.

Electron identification :

- Not associated in the MUC
- $-1.5 < \chi_{dE/dx}^e < 1.5$ ($\chi_{dE/dx}^e$ is defined as the difference between measured and expected dE/dx under the electron hypothesis normalized by the dE/dx resolution)
- $E/p > 0.96$ (E is the deposite energy in the EMC and p is the modulus of the momentum from the MDC)

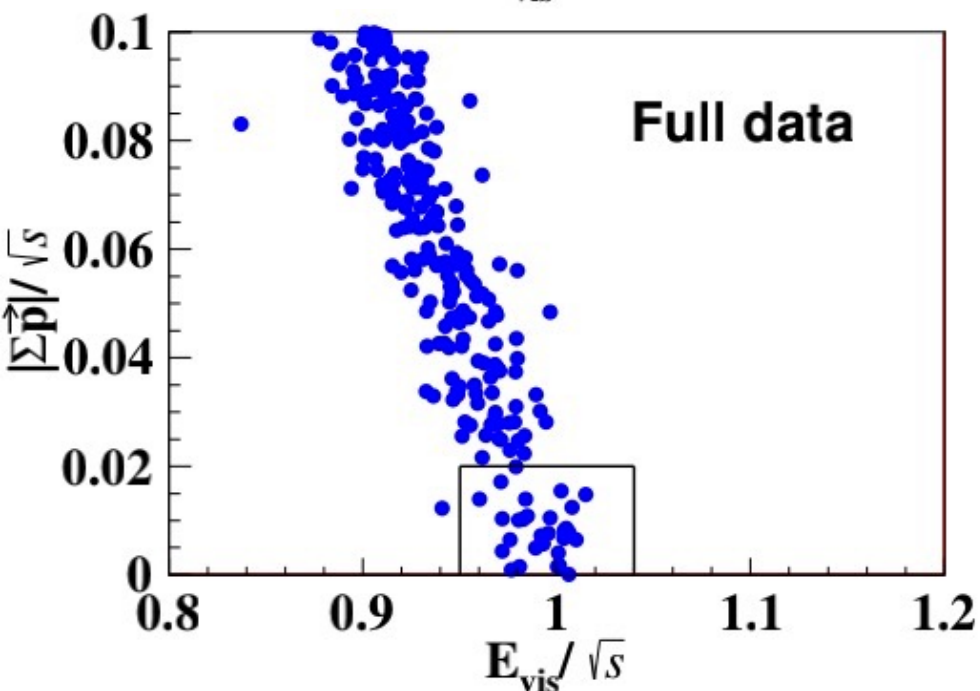
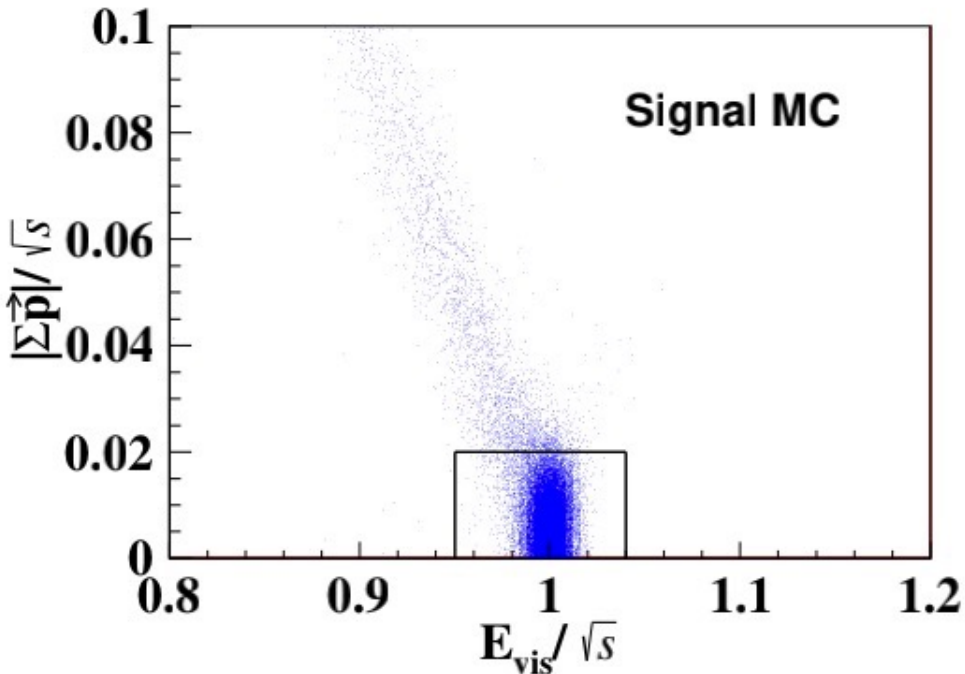
Muon identification :

- $0.1 < E < 0.3$ GeV, $\chi_{dE/dx}^e < -1.6$
- The penetration depth of the track in the MUC > 40 cm
- Each candidate track must penetrate more than three layers in the MUC, and $\chi_{MUC}^2 < 100$





Selection and Background study



- ◆ The signal region is defined with $|\Sigma\vec{p}|/\sqrt{s} \leq 0.02$ and $0.95 \leq E_{vis}/\sqrt{s} \leq 1.04$
 - ◆ $|\Sigma\vec{p}|$: the magnitude of the vector sum of the momenta
 - ◆ E_{vis} : the total reconstructed energy of e and μ in the event
- ◆ J/ψ MC events $\rightarrow J/\psi$ decay background (N_{bkg1})
- ◆ $\psi(3770)$, $\chi_{c1}(1P)$ and $3.080GeV$ data \rightarrow Continuum background (N_{bkg2})
- ◆ The normalized background is estimated to be $N_{bkg1}^{norm} = 24.8 \pm 1.5$ and $N_{bkg2}^{norm} = 12.0 \pm 3.7$.
- ◆ By analyzing the full data, **29 candidate events** are observed, consistent with background estimation.



Sources	Δ_{sys} [%]
Tracking and PID	13
TOF timing	0.52
Photon veto	0.83
$ \Delta\theta $ and $ \Delta\phi $	2.6
Total	14

- ◆ Control samples $J/\psi(e^+e^-) \rightarrow e^+e^-$ and $J/\psi \rightarrow \mu^+\mu^-$ are used to estimate the systematic uncertainties of tracking and PID of electron and muon, TOF timing, γ veto, and $|\Delta\theta|$ and $|\Delta\phi|$ requirement.
- ◆ They are added in quadrature to the total efficiency-related systematic uncertainty of 14%.

Upper limit



$$L = P(N_{obs} | N_{J/\psi} \cdot \mathcal{B} \cdot \hat{\epsilon}_{sig} + \hat{N}_{bkg1} + \hat{N}_{bkg2}) \cdot G(\hat{\epsilon}_{sig} | \epsilon_{sig}^{MC}, \epsilon_{sig}^{MC} \cdot \sigma_{sig}^{MC}) \\ \cdot P(N_{inc}^{J/\psi-MC} | \hat{N}_{bkg1} \cdot f_1) \cdot \prod_k P(N_{cont}^k | \hat{N}_{bkg2} \cdot f_2) \cdot G(N_{J/\psi} | N_{J/\psi}^{data}, \delta N_{J/\psi}^{data})$$

N_{cont}^k : Continuum background at different energy points

ϵ_{sig}^{MC} : Detection efficiency

$N_{inc}^{J/\psi}$: J/ψ decay background

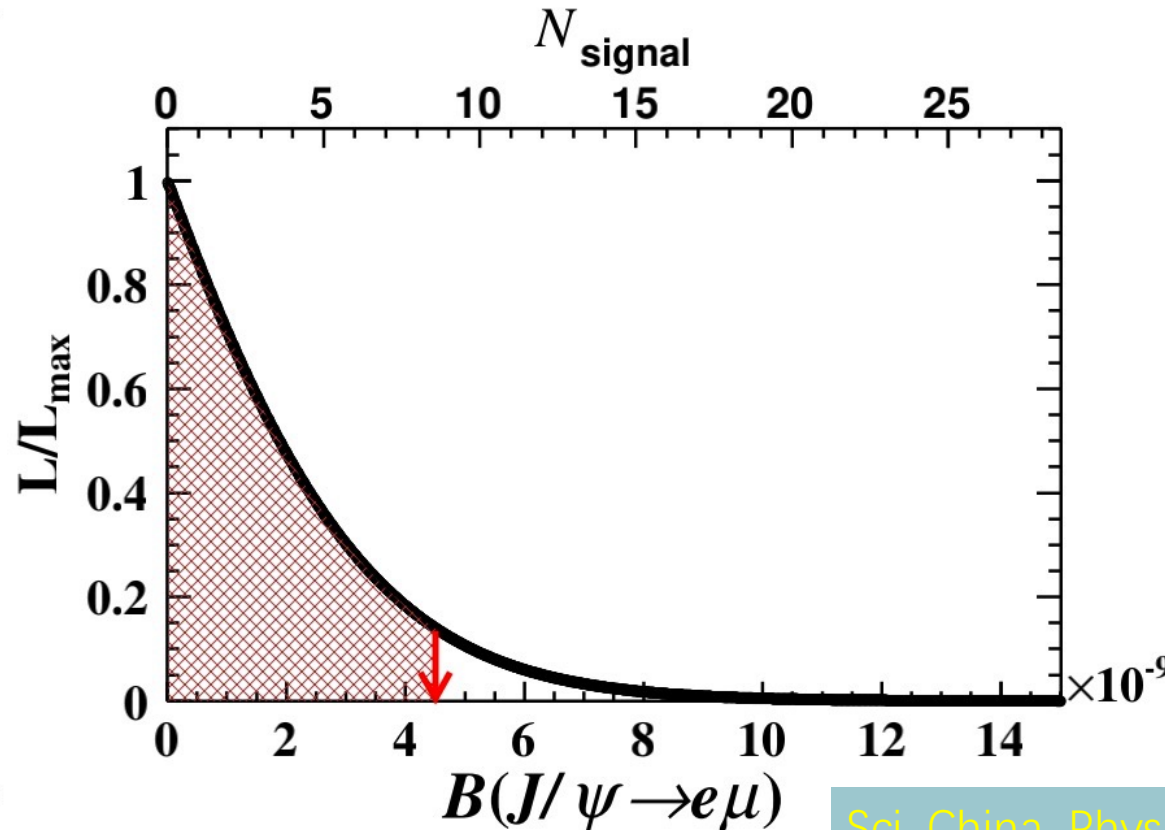
N_{obs} : Observed events

σ_{sig}^{MC} : Relative systematics

◆ $\mathcal{B}(J/\psi \rightarrow e\mu)$

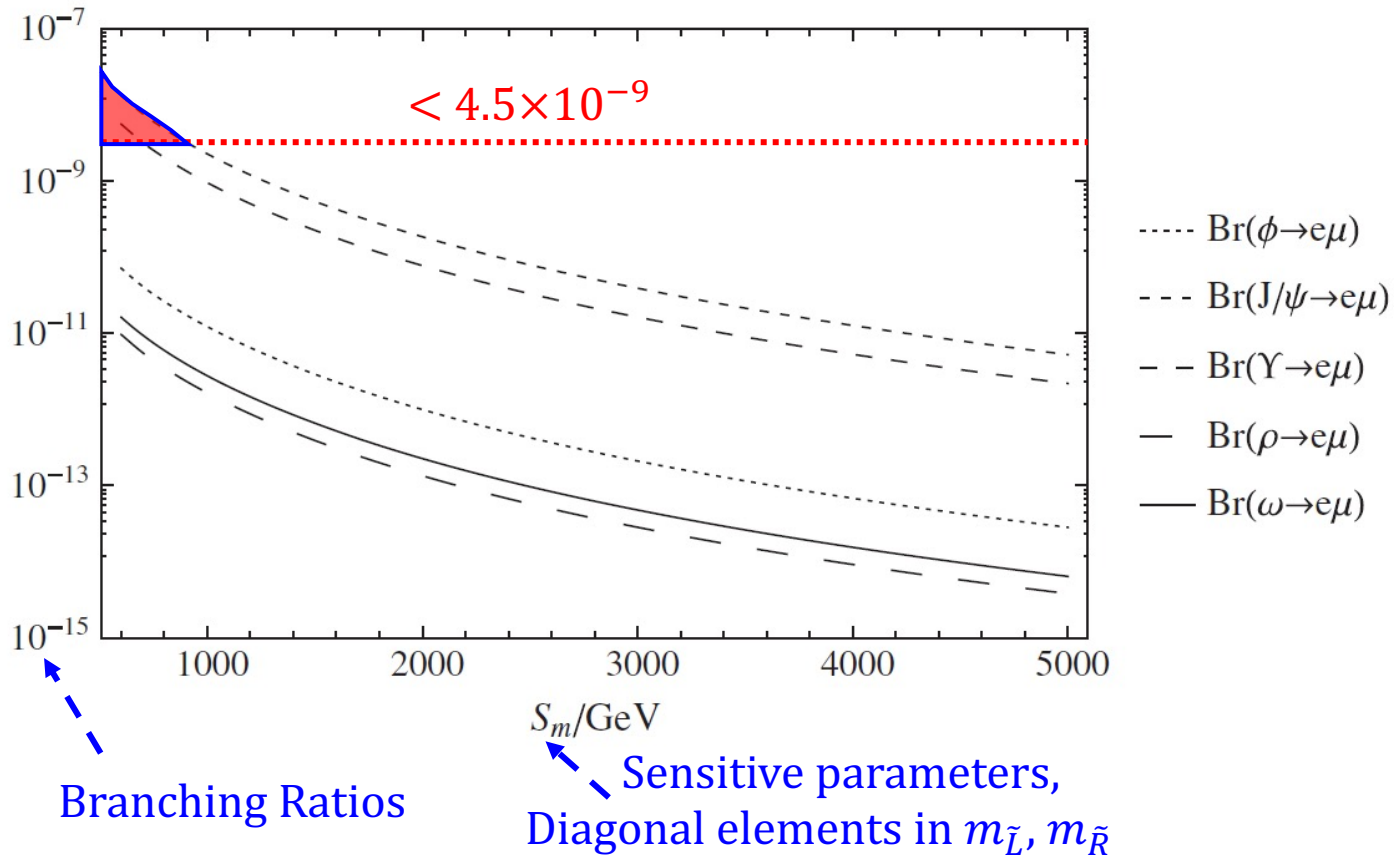
$< 4.5 \times 10^{-9}$ @ 90% C.L.

Parameter	Value
N_{obs}	29
$N_{J/\psi}^{data}$	8.998×10^9
$\delta N_{J/\psi}^{data}$	0.040×10^9
ϵ_{sig}^{MC}	21%
σ_{sig}^{EFF}	14%
$N_{J/\psi-MC}^{bkg1}$	275
$N_{cont}^{3.773}$	10
$N_{cont}^{3.510}$	1
$N_{cont}^{3.080}$	0
f_1	0.09090
$f_2^{3.773}$	1.3416
$f_2^{3.510}$	7.4390
$f_2^{3.080}$	15.553



Sci. China-Phys. Mech. Astron. 66, 221011 (2023)

$$\mathcal{B}(J/\psi \rightarrow e\mu) < 4.5 \times 10^{-9} \text{ @ 90\% C.L.}$$



Phys. Rev. D 97, 056027 (2018)

- ◆ Excluding the parameter space of some models, such as **BLMSSM** model, a supersymmetric model where baryon (B) and lepton (L) numbers are local gauge symmetries.
- ◆ Improves the previous published limits by **a factor of more than 30** and comparable with the theoretical predictions
- ◆ The **most precise result** of CLFV search in heavy quarkonium systems

- ◆ BESIII has great potentials with unique (and increasing) datasets and analysis techniques, performed wide range study of new physics, with many first searches or best limits.
- ◆ Some new physics models can inspire the CLFV decay rate up to a detectable level.
- ◆ The latest searching results for CLFV decays on J/ψ are reported.
- ◆ The UL is set to be $\mathcal{B}(J/\psi \rightarrow e\tau) < 7.5 \times 10^{-8}$ @ 90% CL.
- ◆ The UL is set to be $\mathcal{B}(J/\psi \rightarrow e\mu) < 4.5 \times 10^{-9}$ @ 90% CL, which is the **most stringent CLFV result in heavy quarkonium sector** up to now.



Thank you



PRD.67,114001

Lagrangian: $\mathcal{L}_{\text{eff}}^{\text{leptoquark}} = \bar{c}(\lambda_L^A P_L + \lambda_R^A P_R)\mu\Phi_A + \bar{c}(\lambda_L^A P_L + \lambda_R^A P_R)\tau\Phi_A$
 + H.c.,

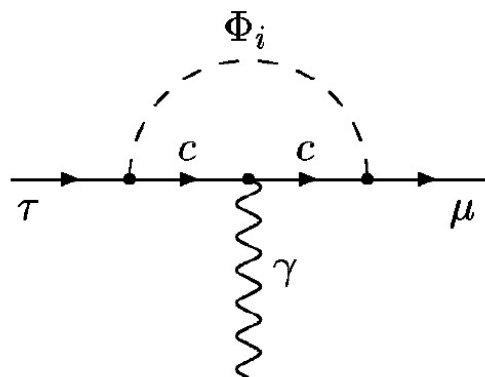
$$\Phi_1: [\lambda_{ij}^{(1)} \bar{Q}_{Lj} e_{Ri} + \tilde{\lambda}_{ij}^{(1)} \bar{u}_{Rj} L_{Li}] \Phi_1,$$

$$\Phi_3: [\lambda_{ij}^{(3)} \bar{Q}_{Lj}^c L_{Li} + \tilde{\lambda}_{ij}^{(3)} \bar{u}_{Rj}^c e_{Ri}] \Phi_3.$$

$$\Gamma(J/\psi \rightarrow \mu\tau) = \frac{|\mathbf{p}|}{32\pi^2 M_{J/\psi}} \int |\mathcal{M}|^2 d\Omega$$

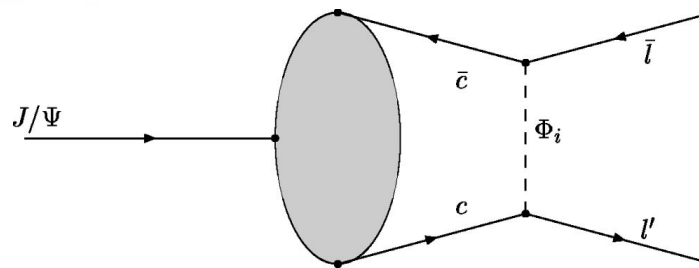
$$= \frac{g_{J/\psi}^2}{96\pi} \frac{m_\tau^2}{M_{J/\psi}} \left(1 + 2 \frac{M_{J/\psi}^2}{m_\tau^2} \right)$$

$$\times \left(1 - \frac{m_\tau^2}{M_{J/\psi}^2} \right)^2 \cdot \frac{|\lambda_L^{c\mu} \lambda_L^{c\tau}|^2 + |\lambda_R^{c\mu} \lambda_R^{c\tau}|^2}{M_\Phi^4},$$



$$\frac{|\lambda_L^{c\mu} \lambda_L^{c\tau}|^2 + |\lambda_R^{c\mu} \lambda_R^{c\tau}|^2}{M_\Phi^4} < 1.5 \times 10^{-10}.$$

$$\mathcal{B}(J/\psi \rightarrow e\mu) < 3.5 \times 10^{-15}$$



$$\text{Br}(J/\psi \rightarrow \mu\tau) = \frac{9}{2^9 \pi^2 \alpha^2} m_\tau^2 M_{J/\psi}^2 \left(1 + 2 \frac{M_{J/\psi}^2}{m_\tau^2} \right)$$

$$\times \left(1 - \frac{m_\tau^2}{M_{J/\psi}^2} \right)^2 \cdot \frac{|\lambda_L^{c\mu} \lambda_L^{c\tau}|^2 + |\lambda_R^{c\mu} \lambda_R^{c\tau}|^2}{M_\Phi^4}$$

$$\times \text{Br}(J/\psi \rightarrow e^+ e^-).$$

$$\Gamma(J/\psi \rightarrow e^+ e^-) = \frac{16\pi}{27} \alpha^2 \frac{g_{J/\psi}^2}{M_{J/\psi}^3},$$

$$\text{Br}(\tau \rightarrow \mu\gamma) = \frac{3}{2^9 \pi^2 G_F^2} \cdot \frac{|\lambda_L^{c\mu} \lambda_L^{c\tau}|^2 + |\lambda_R^{c\mu} \lambda_R^{c\tau}|^2}{M_\Phi^4}$$

$$\times \text{Br}(\tau \rightarrow \mu \nu_\tau \bar{\nu}_\mu),$$

$J/\psi \rightarrow e\mu$ angle

- $|\Delta\theta| = |180^\circ - (\theta_1 + \theta_2)|$
- $|\Delta\phi| = |180^\circ - |\phi_1 - \phi_2||$

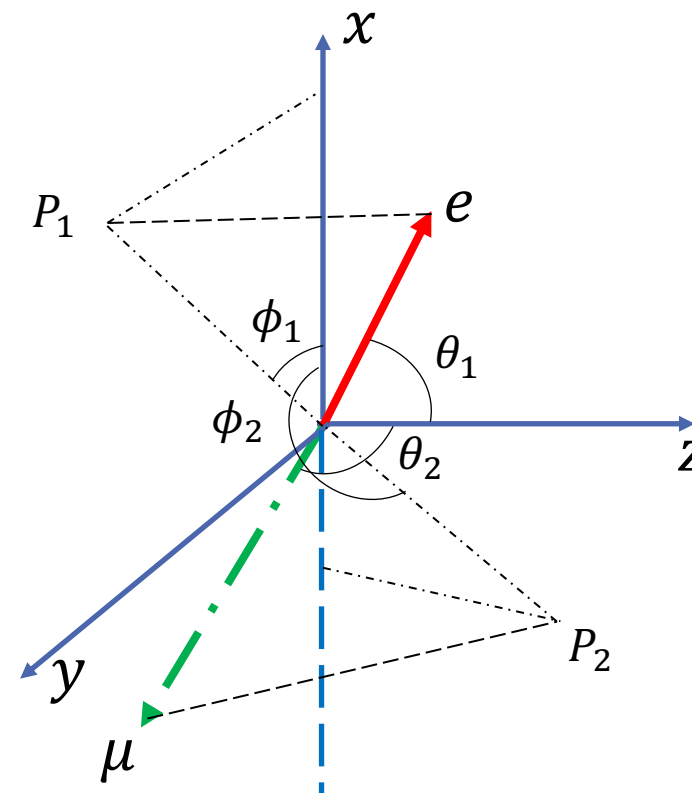
CLFV in SM

$$\Gamma(\mu \rightarrow e\gamma) \approx \frac{G_F^2 m_\mu^5}{192\pi^3} \left(\frac{\alpha}{2\pi}\right) \sin^2 2\theta \sin^2 \left(\frac{1.27\Delta m^2}{M_W^2}\right)$$

$\mu - \text{decay}$ $\gamma - \text{vertex}$ $\vartheta - \text{oscillation}$

$$\approx \frac{G_F^2 m_\mu^5}{192\pi^3} \left(\frac{3\alpha}{32\pi}\right) \left(\frac{\Delta m_{23}^2 s_{13} c_{13} s_{23}}{M_W^2}\right)^2$$

with $\Delta \sim 10^{-3} eV^2, M_W \sim O(10^{11}) eV \approx O(10^{-54})$





Cut flow	Efficiency 2009 (%)	Efficiency 2017-2019 (%)
Generated(100000, 200000)	100	100
$N_{charged}^{good} = 2, \sum Q = 0$	88.00	87.27
$\Delta TOF \leq 1.0$ ns	86.45	85.67
$E/P > 0.5$ for electron, $E/P < 0.5$ for muon	83.31	82.60
$E_{\gamma B} < 0.025$ GeV, $E_{\gamma G} < 0.050$ GeV, $E_{\gamma E} < 0.050$ GeV	76.00	74.47
$N_{hits}^e = 0$ for electron in MUC	73.33	71.15
$E/P > 0.96$ for electron	60.34	59.09
$ \chi_{dE/dx}^e < 1.5$ for electron	55.37	53.37
0.1 GeV $< E_{deposited} < 0.3$ GeV for muon	54.35	52.35
$0 < \chi_{MUC}^2 < 100$ for muon	32.35	40.33
$d_\mu > 40$ cm for muon	27.38	30.06
$\chi_{dE/dx}^e < -1.6$ for muon	26.04	28.42
$ \Delta\theta < 1.2^\circ, \Delta\phi < 1.5^\circ$	24.21	24.96
$ \vec{p} /\sqrt{s} \leq 0.02, 0.95 \leq E_{vis}/\sqrt{s} \leq 1.04$	20.67	21.20

- $\chi_{dE/dx}^e$: difference between the measured and expected χ_{dedx} for the electron hypothesis.
- d_μ : penetration depth in MUC **NumLayers**: penetration layers **MaxHitsInLayer**: Max hits in one layer
- **Signal efficiency**: $\epsilon_{sig}^{MC} = \sum \epsilon_{sig}^i \times \frac{n^i}{N} = (21.18 \pm 0.13)\%$



Sample	Mode	Size 09+17-19 (M)	Survived	Scale factor	Normalized
Exclusive MC	$J/\psi \rightarrow e^+e^-$	133.8+5239	0+58	1/10.0	5.80 ± 0.76
	$J/\psi \rightarrow \mu^+\mu^-$	133.6+5230	1+174	1/10.0	17.40 ± 1.32
	$J/\psi \rightarrow \pi^+\pi^-$	0.33+12.90	0+27	1/10.0	2.70 ± 0.52
	$J/\psi \rightarrow K^+K^-$	0.64+25.10	0+0	1/10.0	0
	$J/\psi \rightarrow p^+p^-$	4.75+1860	0+0	1/10.0	0
Inclusive MC	$J/\psi \rightarrow anything$	230+8774	0+6+9=15	8.2	1.83 ± 0.47
Continuum MC	$e^+e^- \rightarrow e^+e^-(\gamma)$	81+274.8+251.3	0	9.0	0
	$e^+e^- \rightarrow \mu^+\mu^-(\gamma)$	0.3+1.0+0.9	0+0+0	9.0	0
Data	$\psi(3770)$ data \rightarrow 09	2.93 fb ⁻¹	10	1.3416	13.42 ± 4.24
	$\chi_{c1}(1P)$ data \rightarrow 18,19	458.21 pb ⁻¹	1	7.4390	7.44 ± 7.44
	3.080GeV data	224.04 + 877.52	0	15.5533	-

$$\hat{\mu} = \frac{\sum_{i=1}^n \frac{\mu_i}{\sigma_i^2}}{\sum_{i=1}^n \frac{1}{\sigma_i^2}} = \frac{\sum_{i=1}^n \omega_i \mu_i}{\sum_{i=1}^n \omega_i}, V(\hat{\mu}) = \frac{1}{\sum_{i=1}^n \frac{1}{\sigma_i^2}} = \frac{1}{\sum_{i=1}^n \omega_i}$$



- ◆ The normalized background in the signal region N_{bkg1}^{norm} is calculated as,

$$N_{bkg1}^{norm} = N_{bkg1}^{J/\psi-MC} \cdot f_1, \quad f_1 = \frac{N_{J/\psi}^{data}}{N_{J/\psi}^{MC}}$$

- $N_{bkg1}^{J/\psi-MC}$: the number of J/ψ background decays in the J/ψ inclusive and exclusive MC samples
- $N_{J/\psi}^{data}$: the total number of J/ψ events in the data
- $N_{J/\psi}^{MC}$: the total number of equivalent J/ψ events in the J/ψ inclusive and exclusive MC samples

The normalized number in the signal region is estimated to be $N_{bkg1}^{norm} = 24.8 \pm 1.5$.

- ◆ By assuming a $1/s$ energy-dependence of the cross sections, the normalized number of continuum backgrounds at the J/ψ peak, $N_{bkg2}^{norm,k}$, can be obtained by

$$N_{bkg2}^{norm,k} = N_{cont}^k \times f_2^k, \quad f_2^k = \frac{\mathcal{L}_{J/\psi}}{\mathcal{L}_k} \times \frac{s_k}{s_{J/\psi}}$$

- N_{cont}^k : the number of background events survived in the signal region at the energy with index k
- $\mathcal{L}_k, \mathcal{L}_{J/\psi}$: the integrated luminosities at energies k and at the J/ψ peak

The normalized number is estimated to be $N_{bkg2}^{norm} = 12.0 \pm 3.7$.



$$G_{BL} = SU(3)_C \otimes SU(2)_L \otimes U(1)_Y \otimes U(1)_B \otimes U(1)_L$$

In the BLMSSM, the local B and L are spontaneously broken at the TeV scale.

The superpotential of the BLMSSM is written as:

$$\mathcal{W}_{\text{BLMSSM}} = \mathcal{W}_{\text{MSSM}} + \mathcal{W}_B + \mathcal{W}_L + \mathcal{W}_X$$

$$(m_{\tilde{L}}^2)_{ii} = (m_{\tilde{R}}^2)_{ii} = S_m^2$$