

$b \rightarrow s$: Theory Status

Diego Guadagnoli
CNRS, LAPTh Annecy

This talk assignment before Dec. 20, 2022



This talk assignment after Dec. 20, 2022



Before any anomaly

Why new physics in B decays

- FCNCs enjoy a unique concurrence of suppression mechanisms in the SM

Loop & CKM & sometimes GIM & sometimes chiral

Why new physics in B decays

- FCNCs enjoy a unique concurrence of suppression mechanisms in the SM

Loop & CKM & sometimes GIM & sometimes chiral

- Due to high EXP & TH accuracies attainable in numerous cases and to the large number of observables one can construct

*FCNCs rank among the very best probes of beyond-SM effects
e.g. because of the high scales accessible*

Why new physics in B decays

- FCNCs enjoy a unique concurrence of suppression mechanisms in the SM

Loop & CKM & sometimes GIM & sometimes chiral

- Due to high EXP & TH accuracies attainable in numerous cases and to the large number of observables one can construct

*FCNCs rank among the very best probes of beyond-SM effects
e.g. because of the high scales accessible*

- $b \rightarrow s$ transitions are the FCNCs closest to 3rd gen. physics

Take meson mixings as an example

$$\Delta\mathcal{L}^{\Delta F=2} = \sum_{i \neq j} \frac{c_{ij}}{\Lambda^2} (\bar{Q}_{Li} \gamma^\mu Q_{Lj})^2 + \dots$$

Take meson mixings as an example

$$\Delta\mathcal{L}^{\Delta F=2} = \sum_{i \neq j} \frac{c_{ij}}{\Lambda^2} (\bar{Q}_{Li} \gamma^\mu Q_{Lj})^2 + \dots$$

[Isidori-Nir-Perez, 1002.0900]

Operator	Bounds on Λ in TeV ($c_{ij} = 1$)		Bounds on c_{ij} ($\Lambda = 1$ TeV)		Observables
	Re	Im	Re	Im	
$(\bar{s}_L \gamma^\mu d_L)^2$	9.8×10^2	1.6×10^4	9.0×10^{-7}	3.4×10^{-9}	$\Delta m_K; \epsilon_K$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	1.8×10^4	3.2×10^5	6.9×10^{-9}	2.6×10^{-11}	$\Delta m_K; \epsilon_K$
$(\bar{c}_L \gamma^\mu u_L)^2$	1.2×10^3	2.9×10^3	5.6×10^{-7}	1.0×10^{-7}	$\Delta m_D; q/p , \phi_D$
$(\bar{c}_R u_L)(\bar{c}_L u_R)$	6.2×10^3	1.5×10^4	5.7×10^{-8}	1.1×10^{-8}	$\Delta m_D; q/p , \phi_D$
$(\bar{b}_L \gamma^\mu d_L)^2$	5.1×10^2	9.3×10^2	3.3×10^{-6}	1.0×10^{-6}	$\Delta m_{B_d}; S_{\psi K_S}$
$(\bar{b}_R d_L)(\bar{b}_L d_R)$	1.9×10^3	3.6×10^3	5.6×10^{-7}	1.7×10^{-7}	$\Delta m_{B_d}; S_{\psi K_S}$
$(\bar{b}_L \gamma^\mu s_L)^2$		1.1×10^2		7.6×10^{-5}	Δm_{B_s}
$(\bar{b}_R s_L)(\bar{b}_L s_R)$		3.7×10^2		1.3×10^{-5}	Δm_{B_s}

Take meson mixings as an example

$$\Delta\mathcal{L}^{\Delta F=2} = \sum_{i \neq j} \frac{c_{ij}}{\Lambda^2} (\bar{Q}_{Li} \gamma^\mu Q_{Lj})^2 + \dots$$

[Isidori-Nir-Perez, 1002.0900]

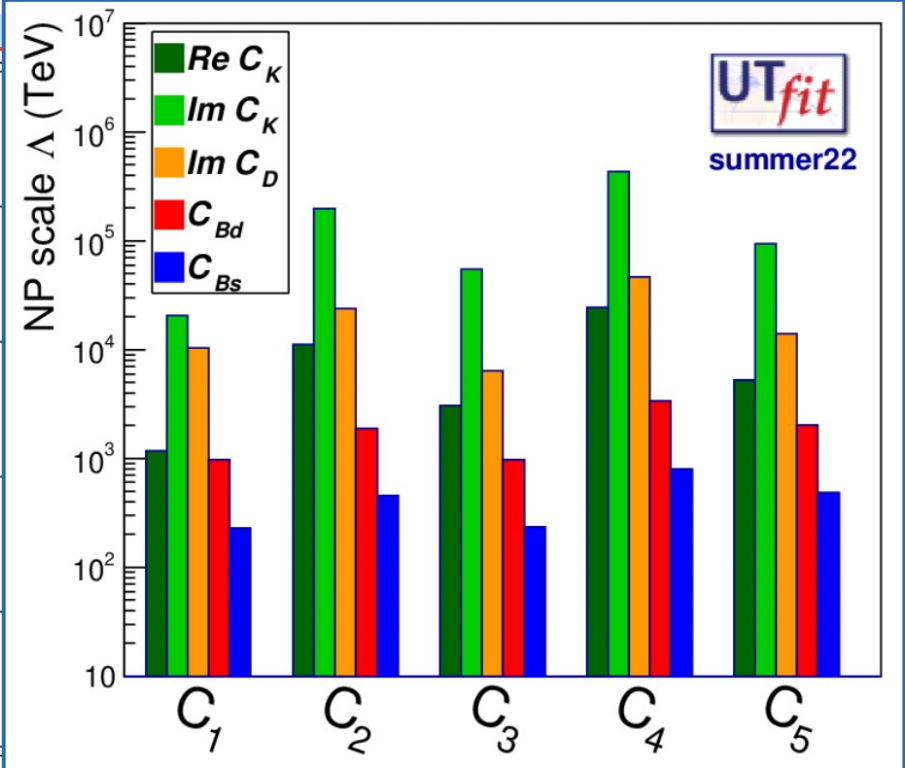
Operator	Bounds on Λ in TeV ($c_{ij} = 1$)		Bounds on c_{ij} ($\Lambda = 1$ TeV)		Observables
	Re	Im	Re	Im	
$(\bar{s}_L \gamma^\mu d_L)^2$	9.8×10^2	1.6×10^4	9.0×10^{-7}	3.4×10^{-9}	$\Delta m_K; \epsilon_K$
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	1.8×10^4	3.2×10^5	6.9×10^{-9}	2.6×10^{-11}	$\Delta m_K; \epsilon_K$
$(\bar{c}_L \gamma^\mu u_L)^2$	1.2×10^3	2.9×10^3	5.6×10^{-7}	1.0×10^{-7}	$\Delta m_D; q/p , \phi_D$
$(\bar{c}_R u_L)(\bar{c}_L u_R)$	6.2×10^3	1.5×10^4	5.7×10^{-8}	1.1×10^{-8}	$\Delta m_D; q/p , \phi_D$
$(\bar{b}_L \gamma^\mu d_L)^2$	5.1×10^2	9.3×10^2	3.3×10^{-6}	1.0×10^{-6}	$\Delta m_{B_d}; S_{\psi K_S}$
$(\bar{b}_R d_L)(\bar{b}_L d_R)$	1.9×10^3	3.6×10^3	5.6×10^{-7}	1.7×10^{-7}	$\Delta m_{B_d}; S_{\psi K_S}$
$(\bar{b}_L \gamma^\mu s_L)^2$		1.1×10^2		7.6×10^{-5}	Δm_{B_s}
$(\bar{b}_R s_L)(\bar{b}_L s_R)$		3.7×10^2		1.3×10^{-5}	Δm_{B_s}

- Typical scales probed are ≥ 1000 TeV
- TeV-scale effects typically requiring global-symmetry assumptions such as MFV

Take meson mixings as an example

$$\Delta\mathcal{L}^{\Delta F=2} = \sum_{i \neq j} \frac{c_{ij}}{\Lambda^2} (\bar{Q}_{Li} \gamma^\mu Q_{Lj})^2 + \dots$$

Operator	Bounds on Λ in TeV ($c_{ij} = 1$)	
	Re	Im
$(\bar{s}_L \gamma^\mu d_L)^2$	9.8×10^2	1.6×10^4
$(\bar{s}_R d_L)(\bar{s}_L d_R)$	1.8×10^4	3.2×10^5
$(\bar{c}_L \gamma^\mu u_L)^2$	1.2×10^3	2.9×10^3
$(\bar{c}_R u_L)(\bar{c}_L u_R)$	6.2×10^3	1.5×10^4
$(\bar{b}_L \gamma^\mu d_L)^2$	5.1×10^2	9.3×10^2
$(\bar{b}_R d_L)(\bar{b}_L d_R)$	1.9×10^3	3.6×10^3
$(\bar{b}_L \gamma^\mu s_L)^2$		1.1×10^2
$(\bar{b}_R s_L)(\bar{b}_L s_R)$		3.7×10^2



- Typical scales probed are ≥ 1000 TeV
- TeV-scale effects typically requiring global-symmetry assumptions such as MFV

Why new physics in B decays

It is sometimes stated that:

- The flavour problem is not a problem, it's a puzzle.

Even solving it, we'll learn nothing about the hierarchy problem, DM, ...

Why new physics in B decays

It is sometimes stated that:

- The flavour problem is not a problem, it's a puzzle.
Even solving it, we'll learn nothing about the hierarchy problem, DM, ...
- But if flavour is a puzzle, then all global / discrete symmetries broken by the SM flavour dynamics are just accidental.
i.e. they could be broken very differently by any extension of the SM
– at whatever scale this may play out

Why new physics in B decays

It is sometimes stated that:

- The flavour problem is not a problem, it's a puzzle.
Even solving it, we'll learn nothing about the hierarchy problem, DM, ...
- But if flavour is a puzzle, then all global / discrete symmetries broken by the SM flavour dynamics are just accidental.
i.e. they could be broken very differently by any extension of the SM
– at whatever scale this may play out
- And if flavour is after all not just a puzzle, then flavour observables are all the more important (see e.g. the recent [\[Davighi, Isidori, 2303.01520\]](#))

Why new physics in B decays

It is sometimes stated that:

- The flavour problem is not a problem, it's a puzzle.
Even solving it, we'll learn nothing about the hierarchy problem, DM, ...
- But if flavour is a puzzle, then all global / discrete symmetries broken by the SM flavour dynamics are just accidental.
i.e. they could be broken very differently by any extension of the SM
– at whatever scale this may play out
- And if flavour is after all not just a puzzle, then flavour observables are all the more important (see e.g. the recent [\[Davighi, Isidori, 2303.01520\]](#))
- In either case, if focus is on the highest scales attainable, flavour observables remain among the deepest probes

Anomalies (?)

NP before Dec. 20

We had a long-sought “seed” for NP.

NP before Dec. 20

We had a long-sought “seed” for NP.

- TH-clean observables
 - whose prediction was solid enough to be widely accepted: $\text{unity} \pm 1\%$
 - whose measurement was discrepant in several updates

NP before Dec. 20

We had a long-sought “seed” for NP.

- TH-clean observables
 - whose prediction was solid enough to be widely accepted: $\text{unity} \pm 1\%$
 - whose measurement was discrepant in several updates
- The NP hinted at by this “seed” was somewhat unexpected, a gross violation of:
 - an exact symmetry of the SM gauge sector
 - a near-symmetry (at least observationally) of the SM Yukawa sector

NP before Dec. 20

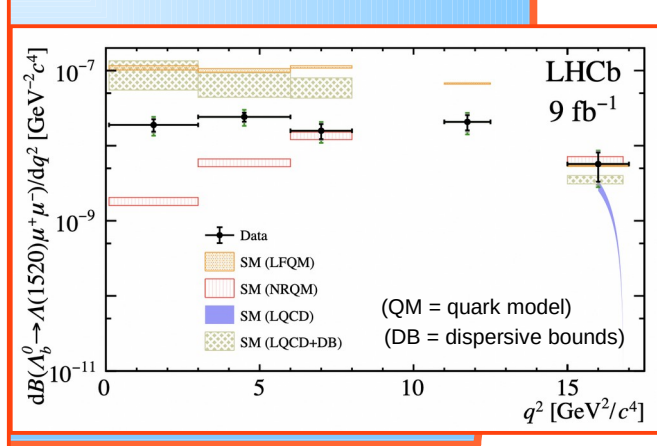
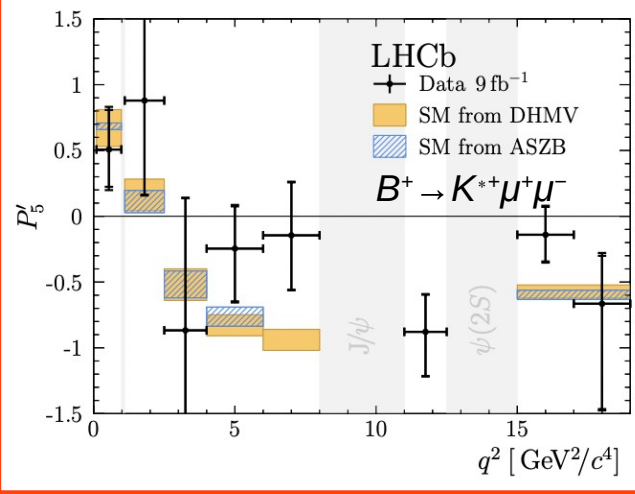
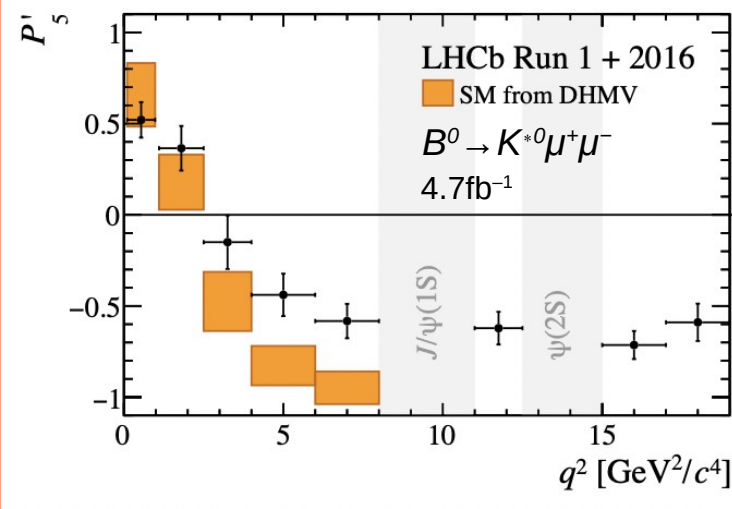
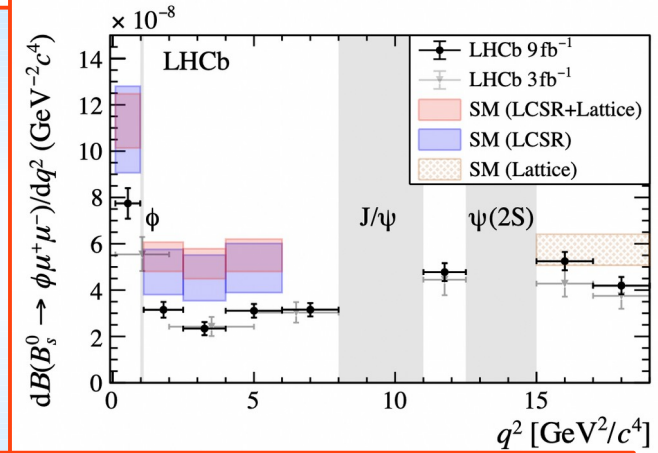
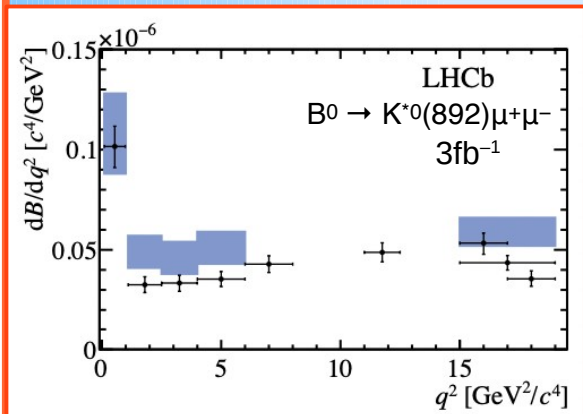
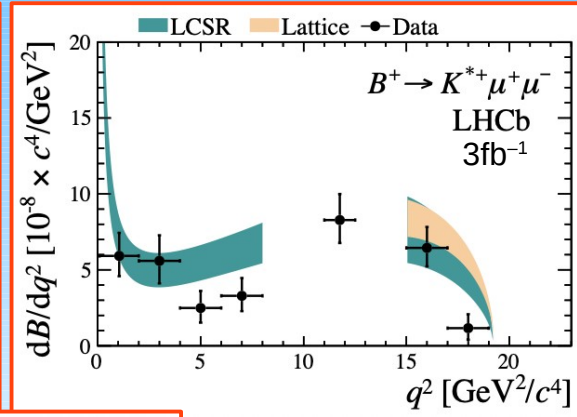
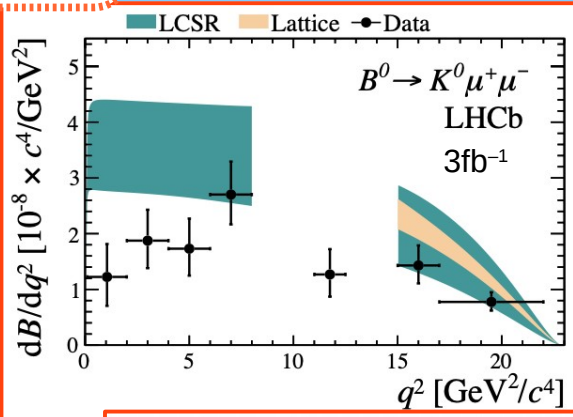
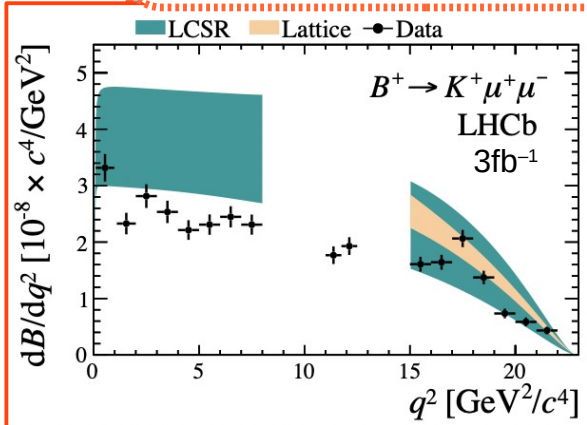
We had a long-sought “seed” for NP.

- TH-clean observables
 - whose prediction was solid enough to be widely accepted: $\text{unity} \pm 1\%$
 - whose measurement was discrepant in several updates
- The NP hinted at by this “seed” was somewhat unexpected, a gross violation of:
 - an exact symmetry of the SM gauge sector
 - a near-symmetry (at least observationally) of the SM Yukawa sector
- But it was supported by a number of (less TH-clean) measurements
 - that in isolation displayed only mild disagreements
 - but in aggregate suggested a coherent picture

NP after Dec. 20

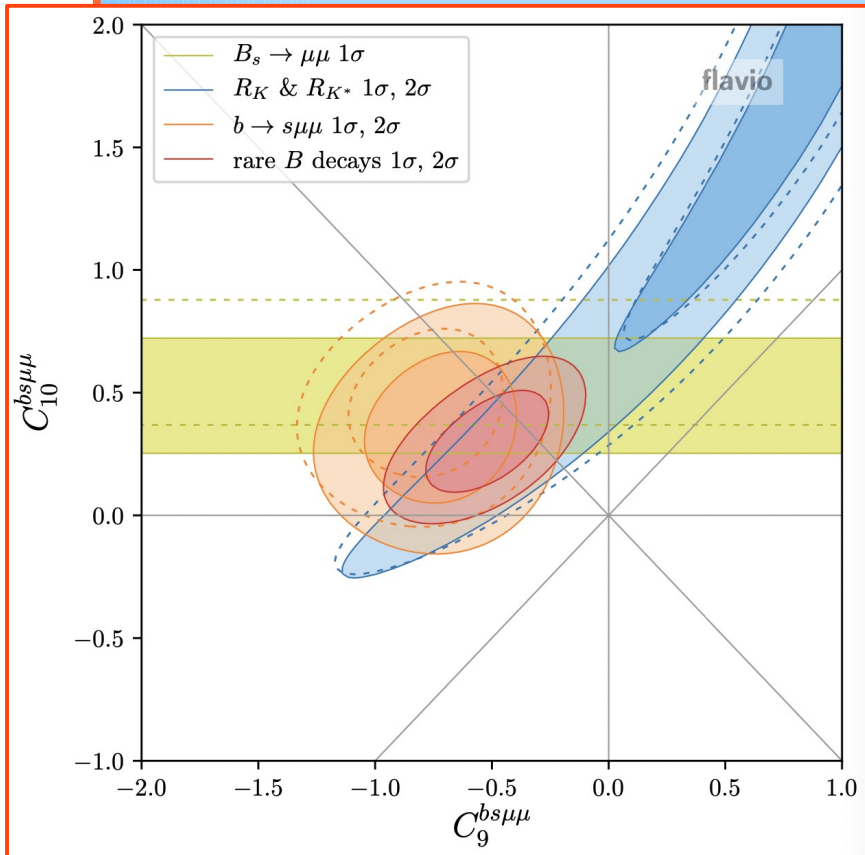
- The more (TH-)solid NP hints have disappeared – overnight.
- The remaining discrepancies (in $b \rightarrow s$ BRs and angular obs. & in $RD^{(*)}$) are debatable

$b \rightarrow s$ discrepant data



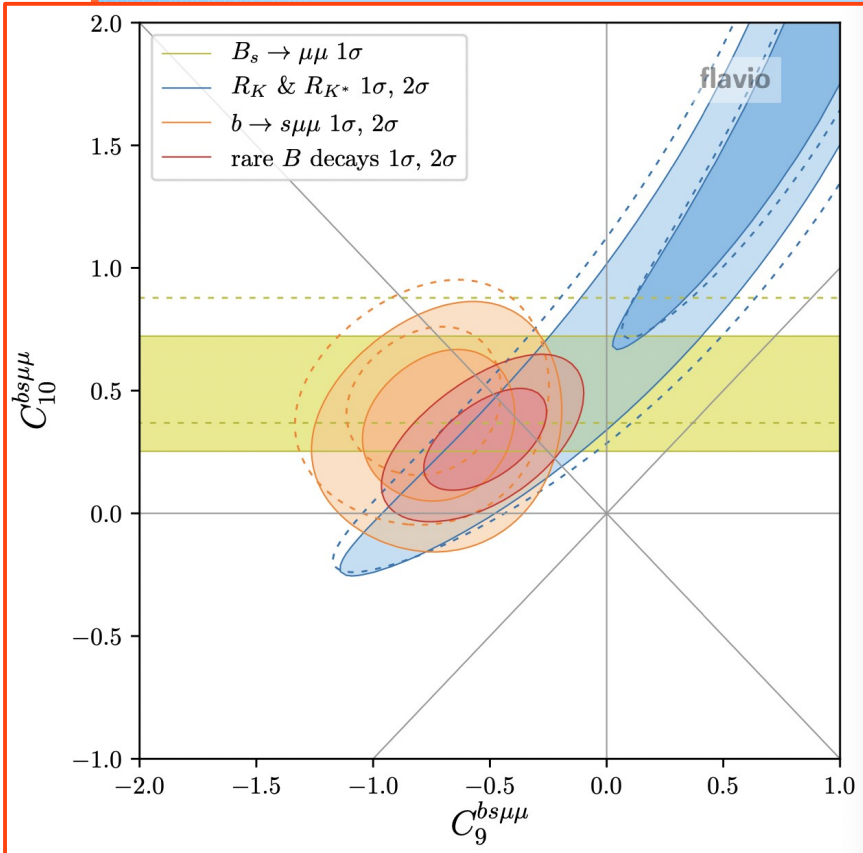
WET bounds

[Altmannshofer, Stangl, 2103.13370]

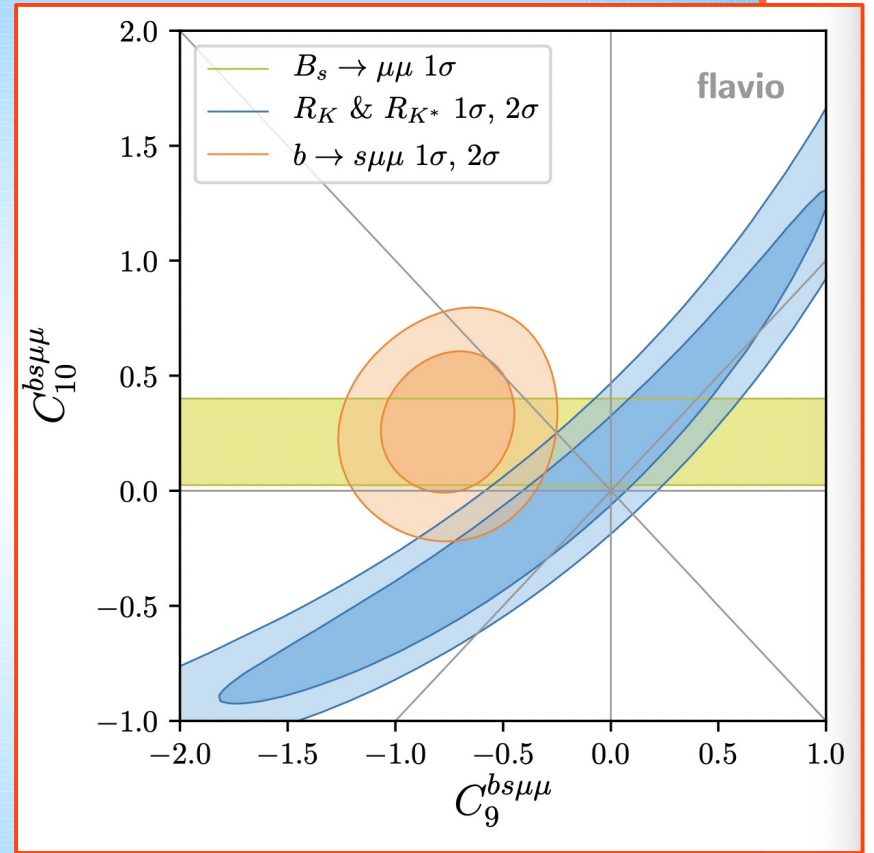


WET bounds

[Altmannshofer, Stangl, 2103.13370]



[Greljo et al., 2212.10497]



Tension between LFU ratios (blue) and $b \rightarrow s\mu^+\mu^-$ data (orange)

WET bounds

[Greljo *et al.*, 2212.10497]

Tension solvable with LFU NP, in either the C_9 or the $C_9 = -C_{10}$ direction

$$C_9^{bsee} = C_9^{\text{univ.}}$$

$$C_9^{bs\mu\mu} = C_9^{\text{univ.}} + \Delta C_9^{bs\mu\mu}$$

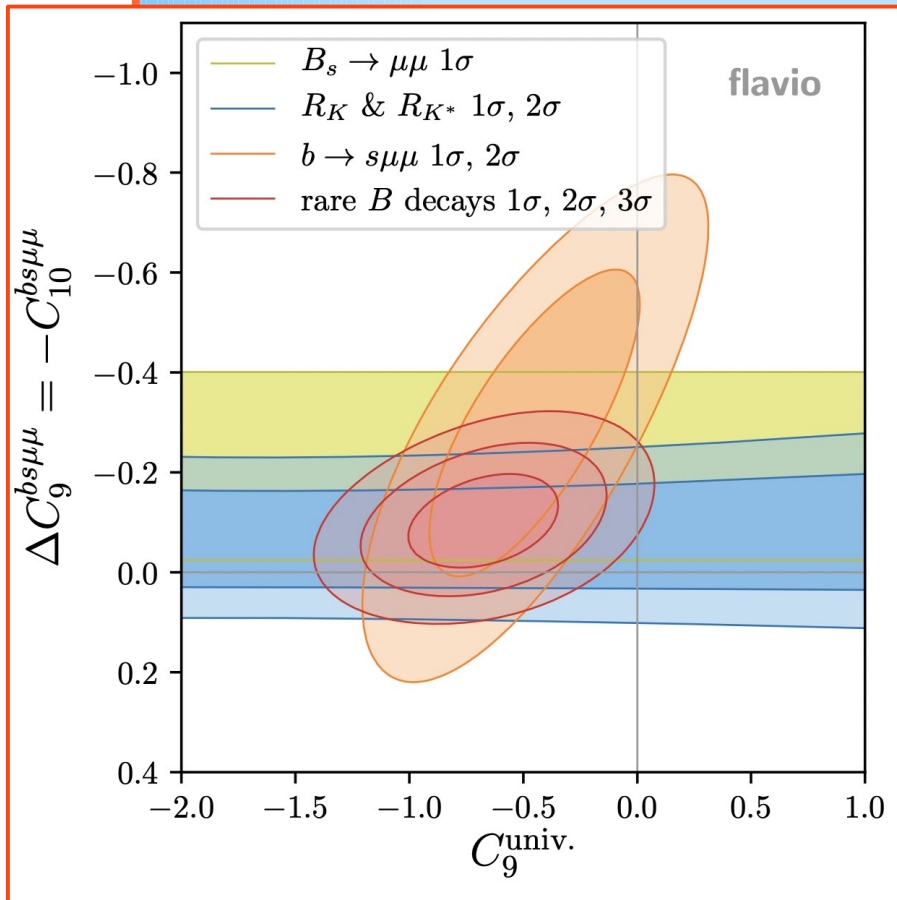
WET bounds

[Greljo et al., 2212.10497]

Tension solvable with LFU NP, in either the C_9 or the $C_9 = -C_{10}$ direction

$$C_9^{bsee} = C_9^{\text{univ.}}$$

$$C_9^{bs\mu\mu} = C_9^{\text{univ.}} + \Delta C_9^{bs\mu\mu}$$



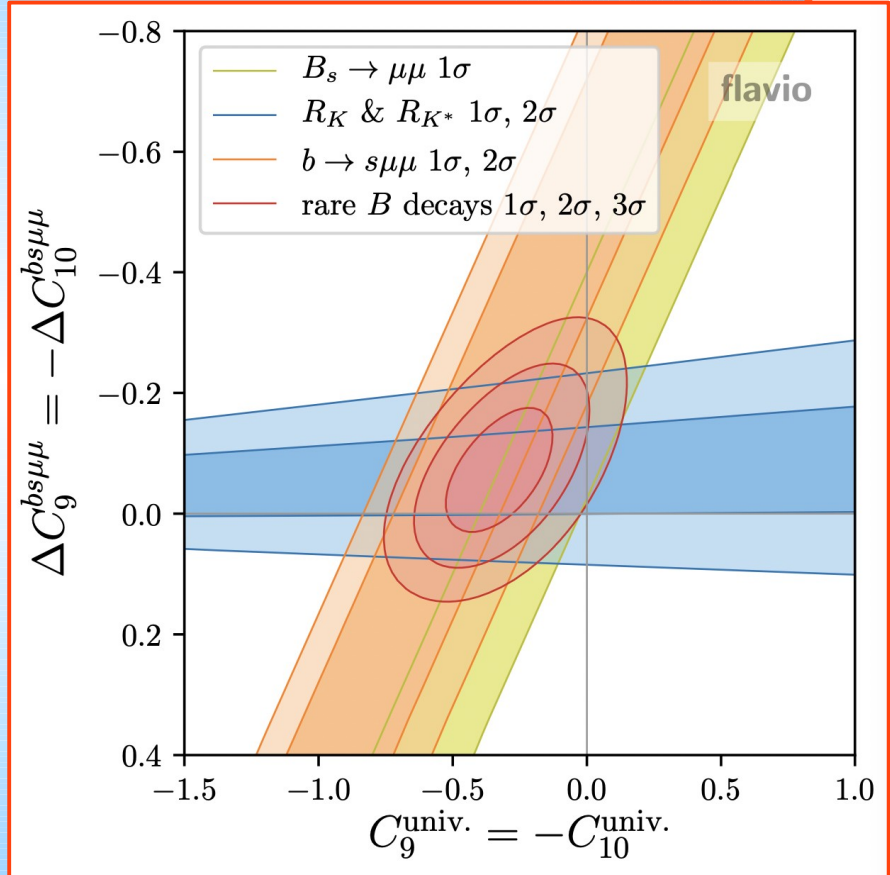
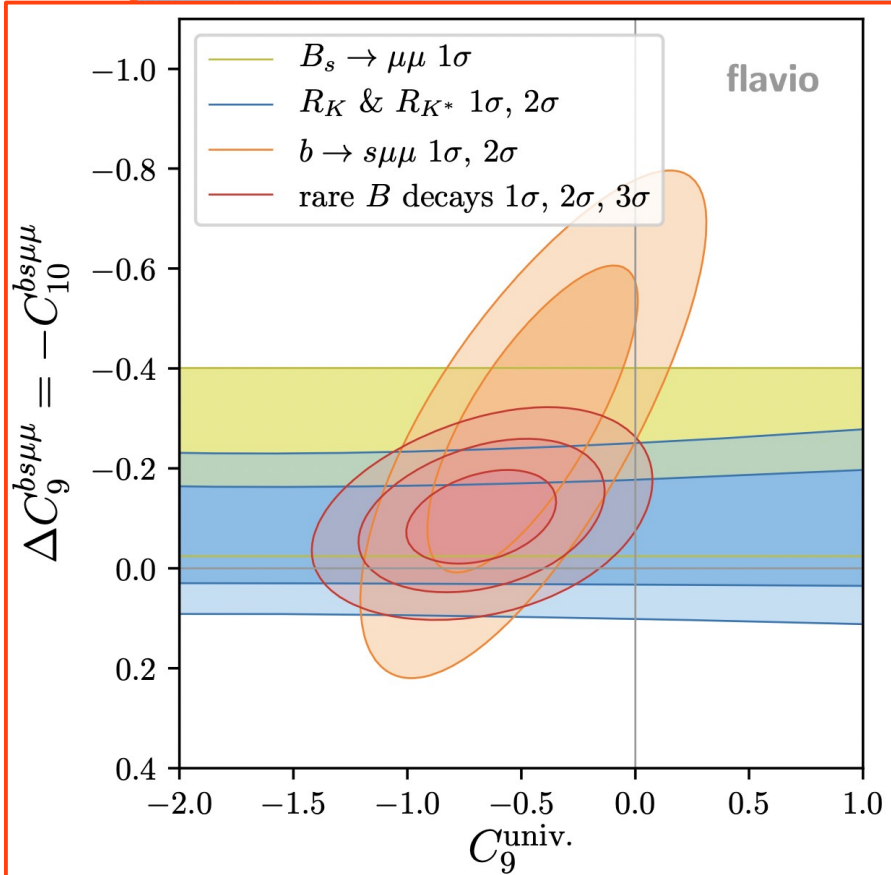
WET bounds

[Greljo et al., 2212.10497]

Tension solvable with LFU NP, in either the C_9 or the $C_9 = -C_{10}$ direction

$$C_9^{bsee} = C_9^{\text{univ.}}$$

$$C_9^{bs\mu\mu} = C_9^{\text{univ.}} + \Delta C_9^{bs\mu\mu}$$



- Purely muonic shift consistent with 0
- Univ. contrib. $O(13\%)$ for C_9 -only, or half as much for C_L

Connection with $b \rightarrow c$?

- $C_9^{\text{univ.}}$ of the correct size can be generated through RGE effects
[Bobeth-Haisch, 2011] [Crivellin *et al.*, 2018] [Aebischer *et al.*, 2019]

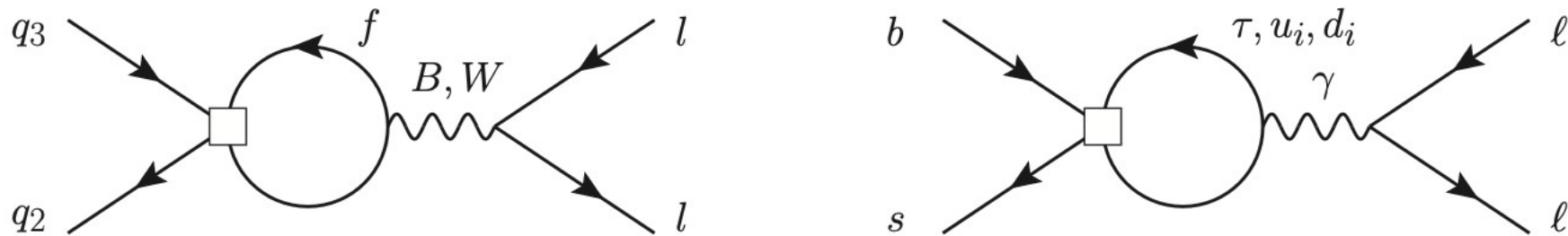


Figure 3: Diagrams inducing a contribution to C_9 through RG running above (left panel) and below (right panel) the EW scale. A sizeable contribution to C_9 is obtained when $f = u_{1,2}, d_{1,2,3}$ or l_3 , see text for details.

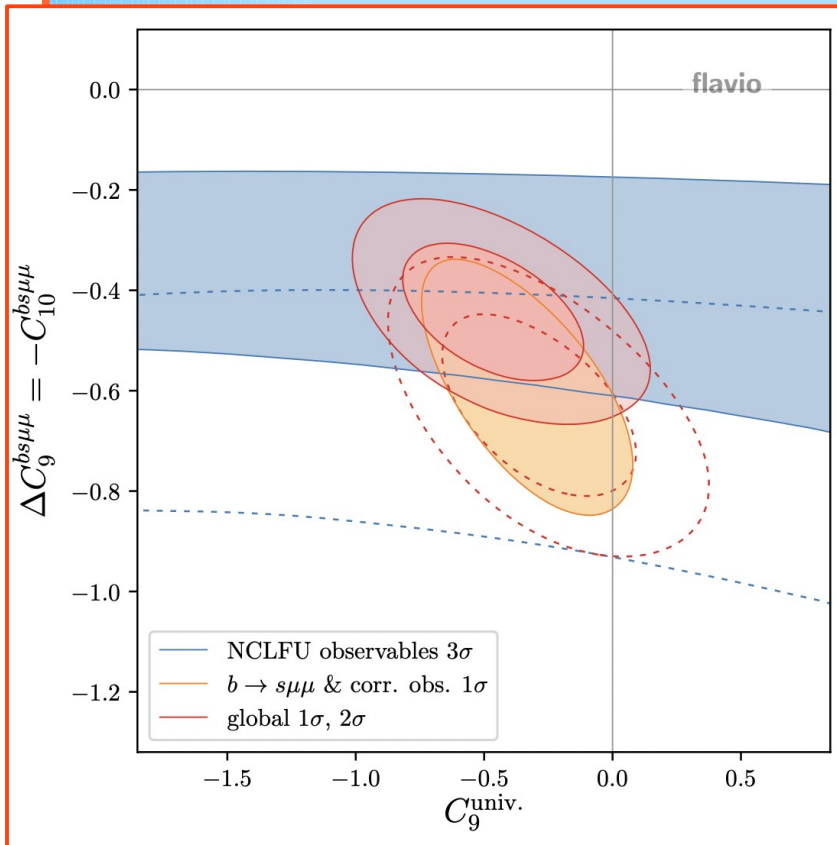
Connection with $b \rightarrow c$ after Dec. 20?

Exercise not yet done quantitatively AFAIK. But it will probably work:

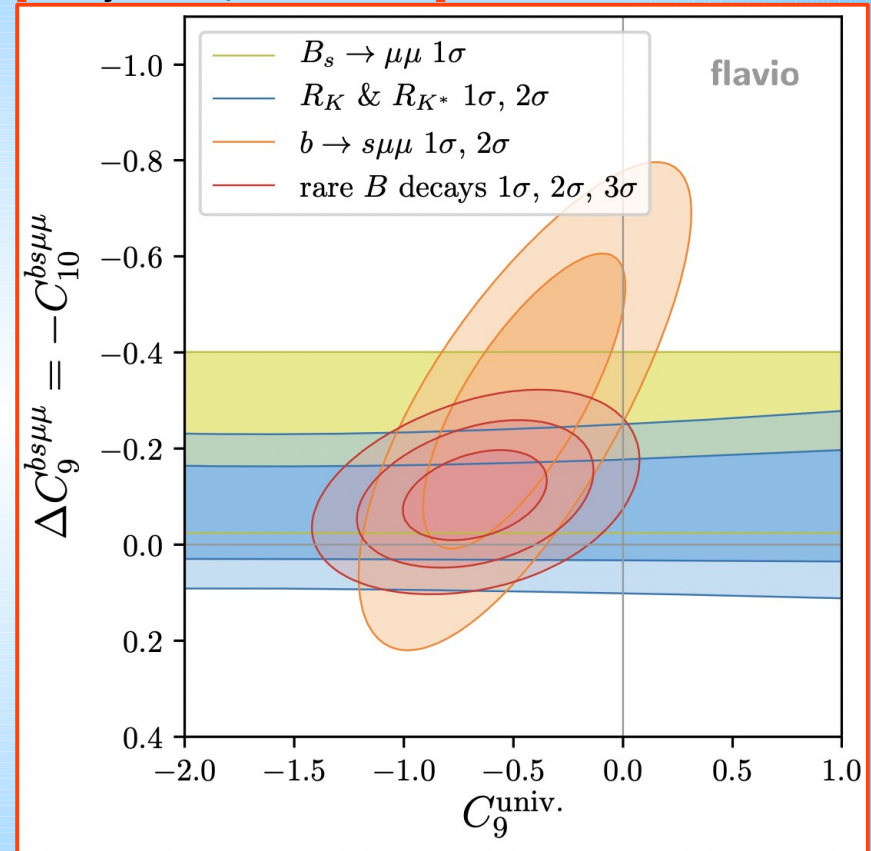
Connection with $b \rightarrow c$ after Dec. 20?

Exercise not yet done quantitatively AFAIK. But it will probably work:

[Aebischer et al., 1903.10434]



[Greljo et al., 2212.10497]

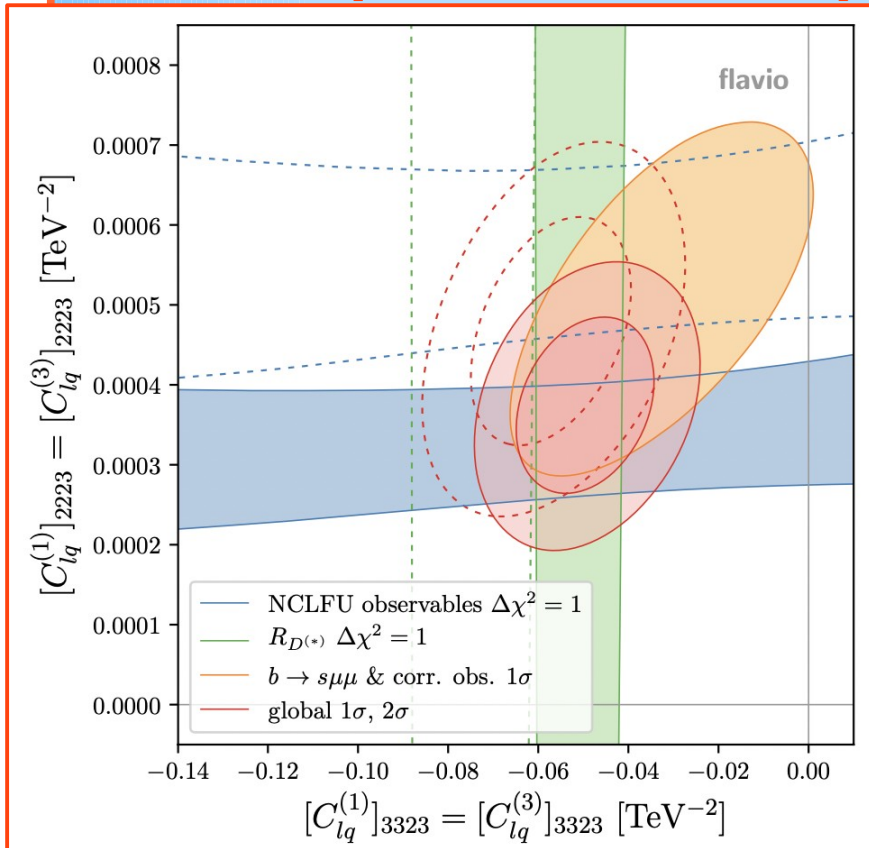


- $C_9^{univ.}$ has slightly increased in central value from pre- to post-Dec. 20

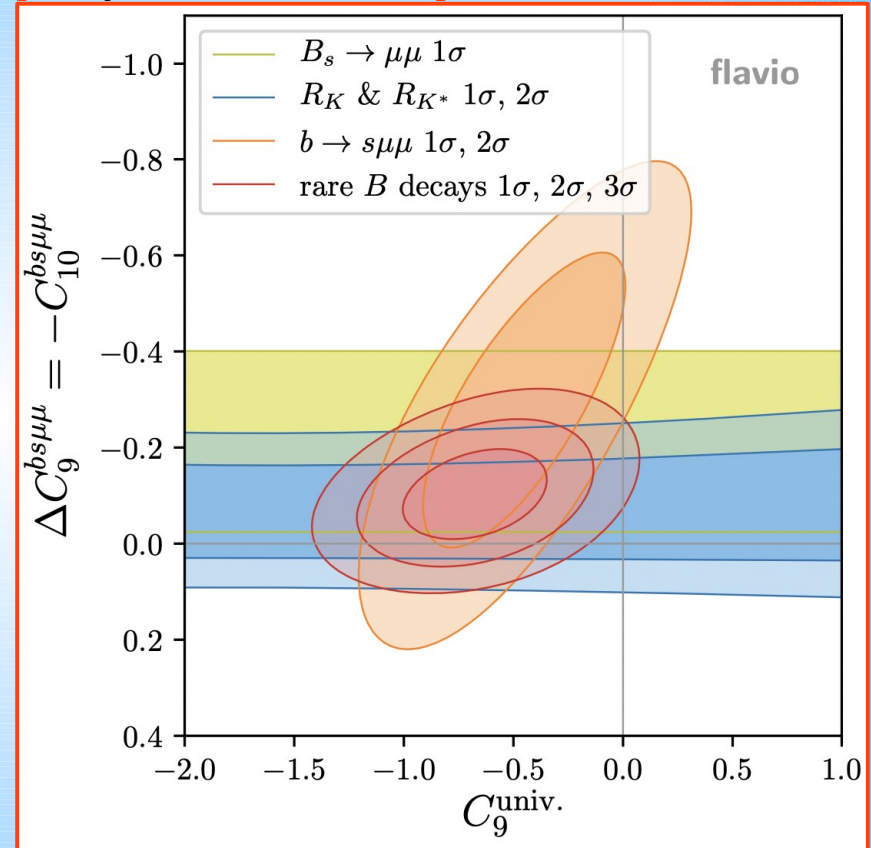
Connection with $b \rightarrow c$ after Dec. 20?

Exercise not yet done quantitatively AFAIK. But it will probably work:

[Aebischer et al., 1903.10434]



[Greljo et al., 2212.10497]



- But $RD^{(*)}$ prefers the part of the yellow ellipse closer to zero (in the y-axis direction)

Connection with $b \rightarrow c$?

Beware: properly using LQCD + unitarity, $R(D^{(*)})$ significance $\sim 1.4\sigma$
[Martinelli, Simula, Vittorio, 2021]

Models

[Greljo et al., 2212.10497]

Post-Dec. 20 exercise:

generate $O(10\%)$, lepton universal effects in $b \rightarrow s \ell^+ \ell^-$

Models

[Greljo et al., 2212.10497]

Post-Dec. 20 exercise:

generate $O(10\%)$, lepton universal effects in $b \rightarrow s \ell^+ \ell^-$

Gauged U(1)'s

- B – L direction + quark-flavour violation through VL heavy quarks

Models


[Greljo et al., 2212.10497]

Post-Dec. 20 exercise:

generate O(10%), lepton universal effects in $b \rightarrow s \ell^+ \ell^-$

Gauged U(1)'s

- B – L direction + quark-flavour violation through VL heavy quarks

 challenged by $\Delta F = 2$ & $pp, ee \rightarrow \ell\ell$

Models

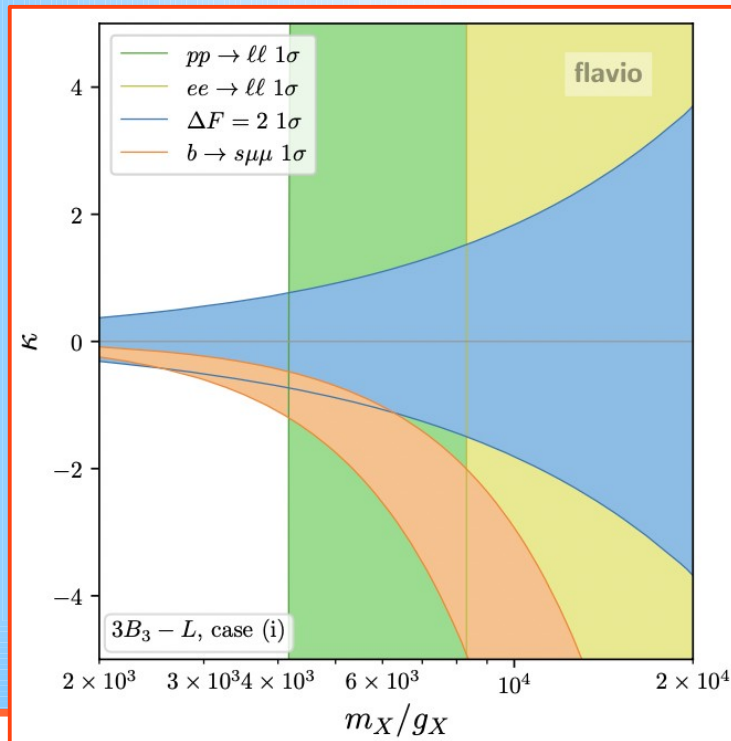
[Greljo et al., 2212.10497]

Post-Dec. 20 exercise:

generate O(10%), lepton universal effects in $b \rightarrow s \ell^+ \ell^-$

Gauged U(1)'s

- B – L direction + quark-flavour violation through VL heavy quarks
➡ challenged by $\Delta F = 2$ & $pp, ee \rightarrow \ell\ell$
- 3rd-(quark)-gen-philic variant: $3 B_3 - L$



➡ $pp \rightarrow \ell\ell$ gets less stringent,
but tension w/ $ee \rightarrow \ell\ell$ persists

Models

[Greljo et al., 2212.10497]

Post-Dec. 20 exercise:

generate $O(10\%)$, lepton universal effects in $b \rightarrow s \ell^+ \ell^-$

Scalar LQs

- Three “leptonic flavours” of $S \sim (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$

Models

[Greljo et al., 2212.10497]

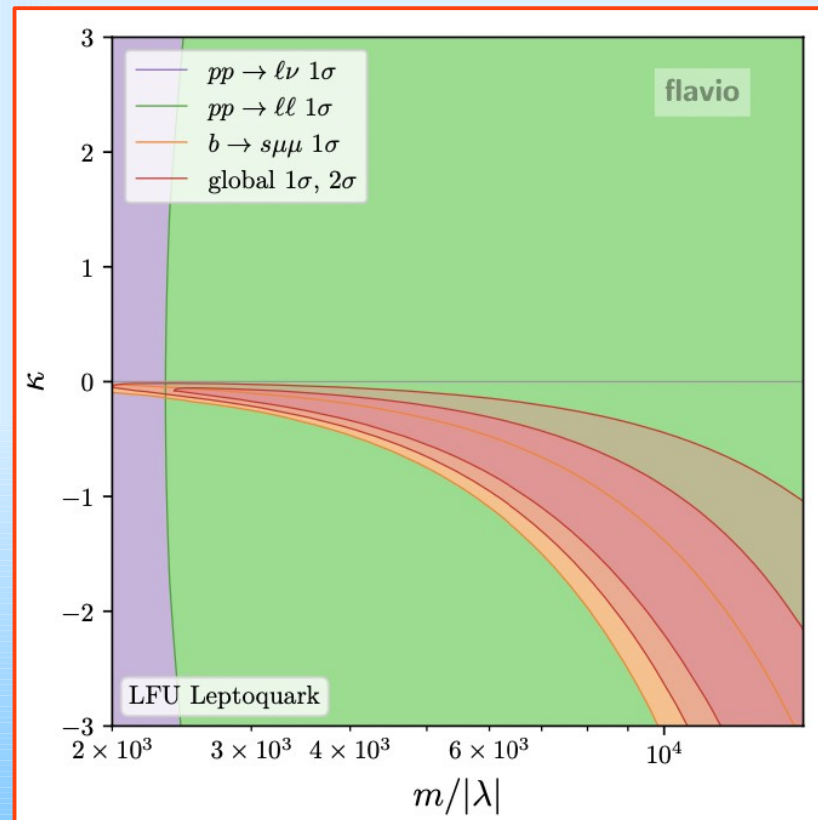
Post-Dec. 20 exercise:

generate O(10%), lepton universal effects in $b \rightarrow s \ell^+ \ell^-$

Scalar LQs

- Three “leptonic flavours” of $S \sim (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$

Semilep at tree level, but $\Delta F = 2$ & $ee \rightarrow \ell\ell$ only at loop level



The important work ahead

(= long-distance)

NP after Dec. 20

Main points

- ① The TH-cleaner bits (LUV observables; $B_s \rightarrow \mu^+\mu^-$) are gone

Main points

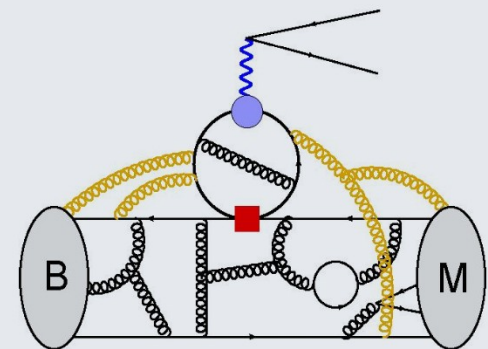
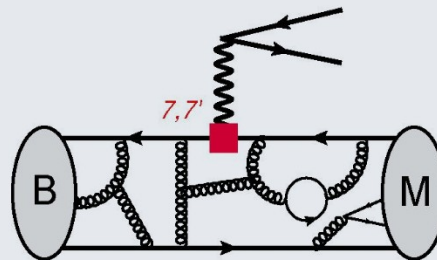
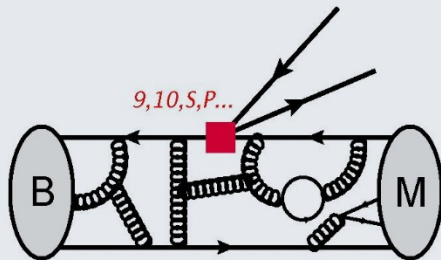
- ① The TH-cleaner bits (LUV observables; $B_s \rightarrow \mu^+\mu^-$) are gone
- ② Remaining hints suggest:
 - C_9^{NP} (or C_L^{NP}) at low q^2 , but not at high q^2 ?
 - C_9^{NP} (or C_L^{NP}) in di-muons, and also in di-electrons?

While waiting for updates of discrepant measurements, progress relies on a solid understanding of “non-local FFs” in $b \rightarrow s \ell^+\ell^-$ (because of ①)

Per aspera (= long-distance contributions) ad astra

Form factors in $b \rightarrow s\ell\ell$

$$\mathcal{H}(b \rightarrow s\ell\ell) = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_{i=1}^{10} C_i(\mu) \mathcal{O}_i(\mu)$$



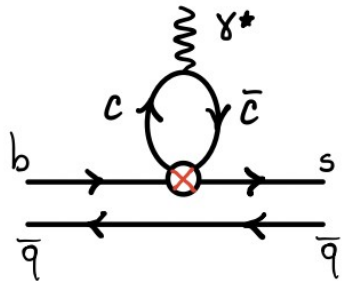
$$A_\lambda^{L,R}(B \rightarrow M_\lambda \ell\ell) = \mathcal{N}_\lambda \left\{ (C_9 \mp C_{10}) \mathcal{F}_\lambda(q^2) + \frac{2m_b M_B}{q^2} \left[C_7 \mathcal{F}_\lambda^T(q^2) - 16\pi^2 \frac{M_B}{m_b} \mathcal{H}_\lambda(q^2) \right] \right\}$$

$$\mathcal{H}_\mu(k, q) = i \int d^4x e^{iq \cdot x} \langle \bar{M}(k) | T \{ \mathcal{J}_\mu^{\text{em}}(x), C_i \mathcal{O}_i \} | \bar{B}(q+k) \rangle$$

Non-local form-factors

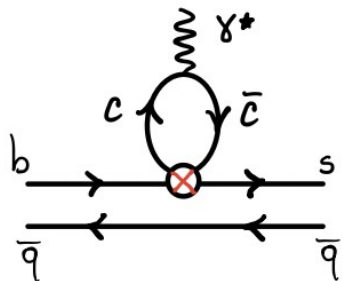
→ Main contributions: the “charm-loops” $\mathcal{O}_{2(1)}^c = (\bar{s}_L \gamma_\mu (T^a) c_L) (\bar{c}_L \gamma^\mu (T^a) b_L)$

Per aspera (= long-distance contributions) ad astra

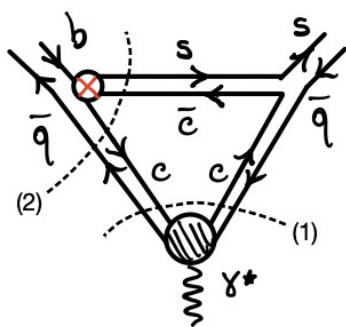


Per aspera (= long-distance contributions) ad astra

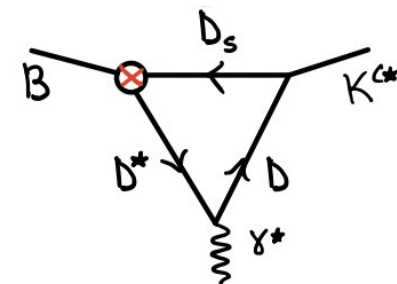
[Ciuchini et al., 2212.10516]



(a)



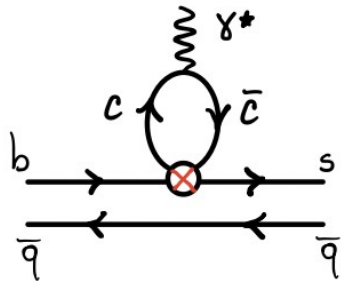
(b)



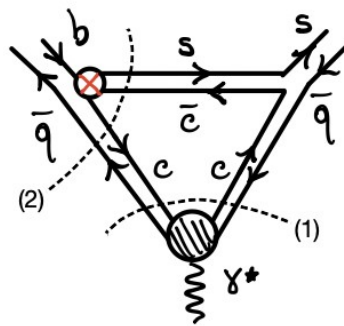
(c)

Per aspera (= long-distance contributions) ad astra

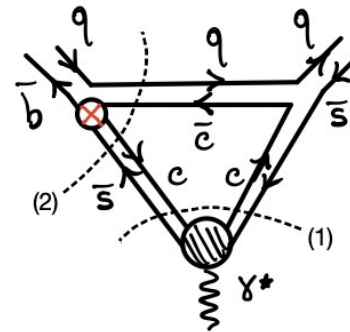
[Ciuchini et al., 2212.10516]



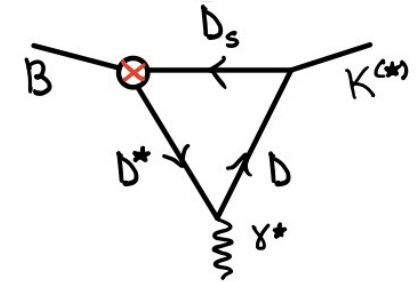
(a)



(b)



(c)



What about contribs. (b)?

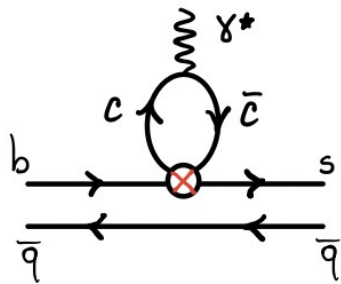
In principle, well-known to be there, e.g.

► On-shell cuts in the variable $(q+k)^2$ (the “forward” or “decay” channel) include branch cuts from intermediate states such as $B \rightarrow \bar{D}D_s \rightarrow K^*\ell^+\ell^-$. The physical point $(q+k)^2 = M_B^2$ lies on these cuts, which implies that the functions $\mathcal{H}_\lambda(q^2)$ are complex-valued for all values of q^2 . But this imaginary part is not associated with any singularity in the variable q^2 . Thus, one can write $\mathcal{H}_\lambda(q^2) = \mathcal{H}_\lambda^{(\text{re})}(q^2) + i\mathcal{H}_\lambda^{(\text{im})}(q^2)$, with $\mathcal{H}_\lambda^{(\text{re,im})}(q^2)$ satisfying the analytic properties of the previous point as functions of q^2 , and obeying the same dispersion relation.

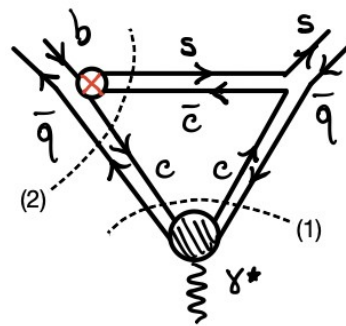
[Bobeth et al., 2017]

Per aspera (= long-distance contributions) ad astra

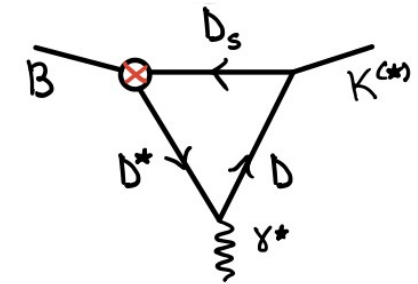
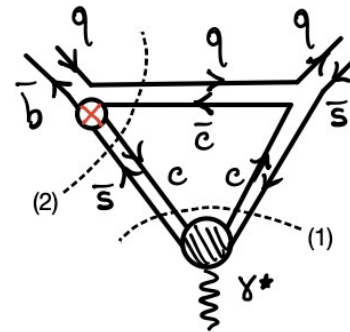
[Ciuchini et al., 2212.10516]



(a)



(b)



(c)

What about contribs. (b)?

In principle, well-known to be there, e.g.

► On-shell cuts in the variable $(q+k)^2$ (the “forward” or “decay” channel) include branch cuts from intermediate states such as $B \rightarrow \bar{D}D_s \rightarrow K^*\ell^+\ell^-$. The physical point $(q+k)^2 = M_B^2$ lies on these cuts, which implies that the functions $\mathcal{H}_\lambda(q^2)$ are complex-valued for all values of q^2 . But this imaginary part is not associated with any singularity in the variable q^2 . Thus, one can write $\mathcal{H}_\lambda(q^2) = \mathcal{H}_\lambda^{(\text{re})}(q^2) + i\mathcal{H}_\lambda^{(\text{im})}(q^2)$, with $\mathcal{H}_\lambda^{(\text{re,im})}(q^2)$ satisfying the analytic properties of the previous point as functions of q^2 , and obeying the same dispersion relation.

[Bobeth et al., 2017]

In practice, however...

to this kind of contributions, but the analytic structure of triangle diagrams is quite involved, depending on the values of external momenta and internal masses. A dispersion relation in q^2 of the kind used in refs. [43, 45–48], based on the cut denoted by (1) in Fig. 1 (b), could be written if the B invariant mass were below the threshold for the production of charmed intermediate states. However, when the B invariant mass raises above the threshold for cut (2), an additional singularity moves into the q^2 integration domain, requiring a nontrivial deformation of the path (see for example the detailed discussion in ref. [94]). Another possibility would be to get an

[Ciuchini et al., 2212.10516]

Looking elsewhere in q^2 : Effects?

*Long-distance issues at low vs. high q^2 are different
whereas above-EWSB new effects are the same*

Inclusive $b \rightarrow s \ell^+ \ell^-$

[Isidori *et al.*, 2305.03076]

- Look for proxies of the inclusive $b \rightarrow s \ell^+ \ell^-$ rate at high q^2

Inclusive $b \rightarrow s \ell^+ \ell^-$

[Isidori et al., 2305.03076]

- Look for proxies of the inclusive $b \rightarrow s \ell^+ \ell^-$ rate at high q^2
 - For $q^2 = 15 \text{ GeV}^2$, rate dominated by 3 modes ($B \rightarrow K^*$ & $B \rightarrow K\pi$)

Inclusive $b \rightarrow s \ell^+ \ell^-$

[Isidori et al., 2305.03076]

- Look for proxies of the inclusive $b \rightarrow s \ell^+ \ell^-$ rate at high q^2
 - For $q^2 = 15 \text{ GeV}^2$, rate dominated by 3 modes ($B \rightarrow K^*$ & $B \rightarrow K\pi$)
 - And this prediction agrees with the inclusive prediction from the ratio

$$R_{\text{incl}}^{(\ell)}(q_0^2) = \int_{q_0^2}^{m_B^2} dq^2 \frac{d\Gamma(B \rightarrow X_s \bar{\ell} \ell)}{dq^2} \bigg/ \int_{q_0^2}^{m_B^2} dq^2 \frac{d\Gamma(B \rightarrow X_u \bar{\ell} \nu)}{dq^2}$$

[Ligeti-Tackmann, '07]

Inclusive $b \rightarrow s \ell^+ \ell^-$

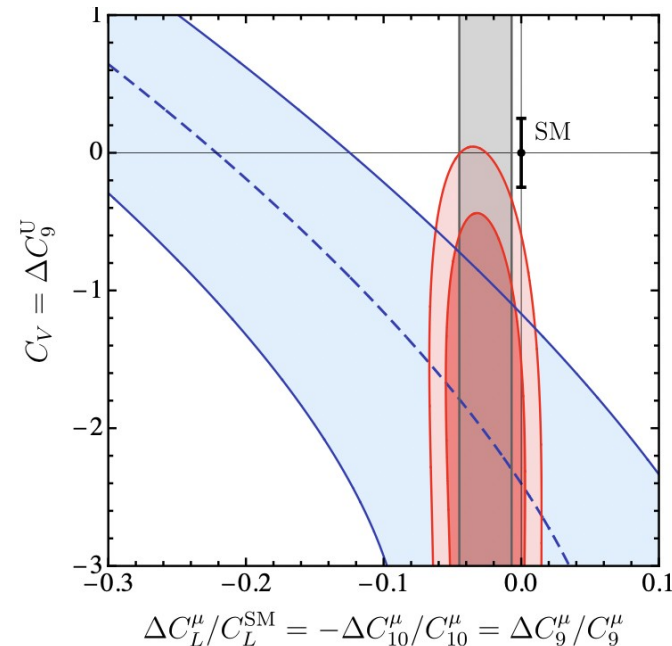
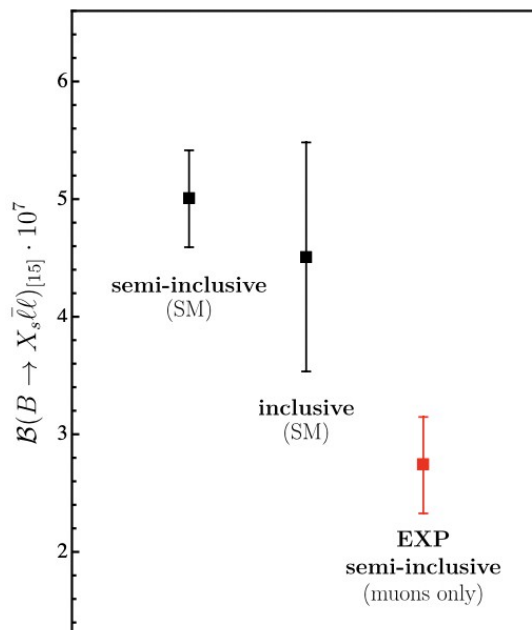
[Isidori et al., 2305.03076]

- Look for proxies of the inclusive $b \rightarrow s \ell^+ \ell^-$ rate at high q^2
 - For $q^2 = 15 \text{ GeV}^2$, rate dominated by 3 modes ($B \rightarrow K^*$ & $B \rightarrow K\pi$)
 - And this prediction agrees with the inclusive prediction from the ratio

$$R_{\text{incl}}^{(\ell)}(q_0^2) = \int_{q_0^2}^{m_B^2} dq^2 \frac{d\Gamma(B \rightarrow X_s \bar{\ell}\ell)}{dq^2} \bigg/ \int_{q_0^2}^{m_B^2} dq^2 \frac{d\Gamma(B \rightarrow X_u \bar{\ell}\nu)}{dq^2}$$

[Ligeti-Tackmann, '07]

- Comparison with $B \rightarrow K^*$ measurements from LHCb yields



$B_s \rightarrow \mu\mu\gamma$ at high q^2

[Dettori, DG, Reboud, '17]

Basic Idea Extract $B_s \rightarrow \mu\mu\gamma$ from $B_s \rightarrow \mu\mu$ event sample,
by enlarging $m_{\mu\mu}$ below B_s peak

$B_s \rightarrow \mu\mu\gamma$ at high q^2

[Dettori, DG, Reboud, '17]

Basic Idea *Extract $B_s \rightarrow \mu\mu\gamma$ from $B_s \rightarrow \mu\mu$ event sample,
by enlarging $m_{\mu\mu}$ below B_s peak*

- *Essential precondition: controlling all other backgrounds*


Strategy now being applied at LHCb, resulting in a first limit

[LHCb, 2108.09283-4]


Basic Idea *Extract $B_s \rightarrow \mu\mu\gamma$ from $B_s \rightarrow \mu\mu$ event sample, by enlarging $m_{\mu\mu}$ below B_s peak*

- *Essential precondition: controlling all other backgrounds*
Strategy now being applied at LHCb, resulting in a first limit
[LHCb, 2108.09283-4]
- *High q^2 offers several TH advantages*
 - *Probes in complementary kin. region (high q^2) the tensions reported in semi-lep BRs*


Basic Idea *Extract $B_s \rightarrow \mu\mu\gamma$ from $B_s \rightarrow \mu\mu$ event sample, by enlarging $m_{\mu\mu}$ below B_s peak*

- *Essential precondition: controlling all other backgrounds*
Strategy now being applied at LHCb, resulting in a first limit
[LHCb, 2108.09283-4]
 - *High q^2 offers several TH advantages*
 - *Probes in complementary kin. region (high q^2) the tensions reported in semi-lep BRs*
-  *Although high q^2 not immune from long-distance challenges, they are different than low q^2*

Basic Idea *Extract $B_s \rightarrow \mu\mu\gamma$ from $B_s \rightarrow \mu\mu$ event sample, by enlarging $m_{\mu\mu}$ below B_s peak*

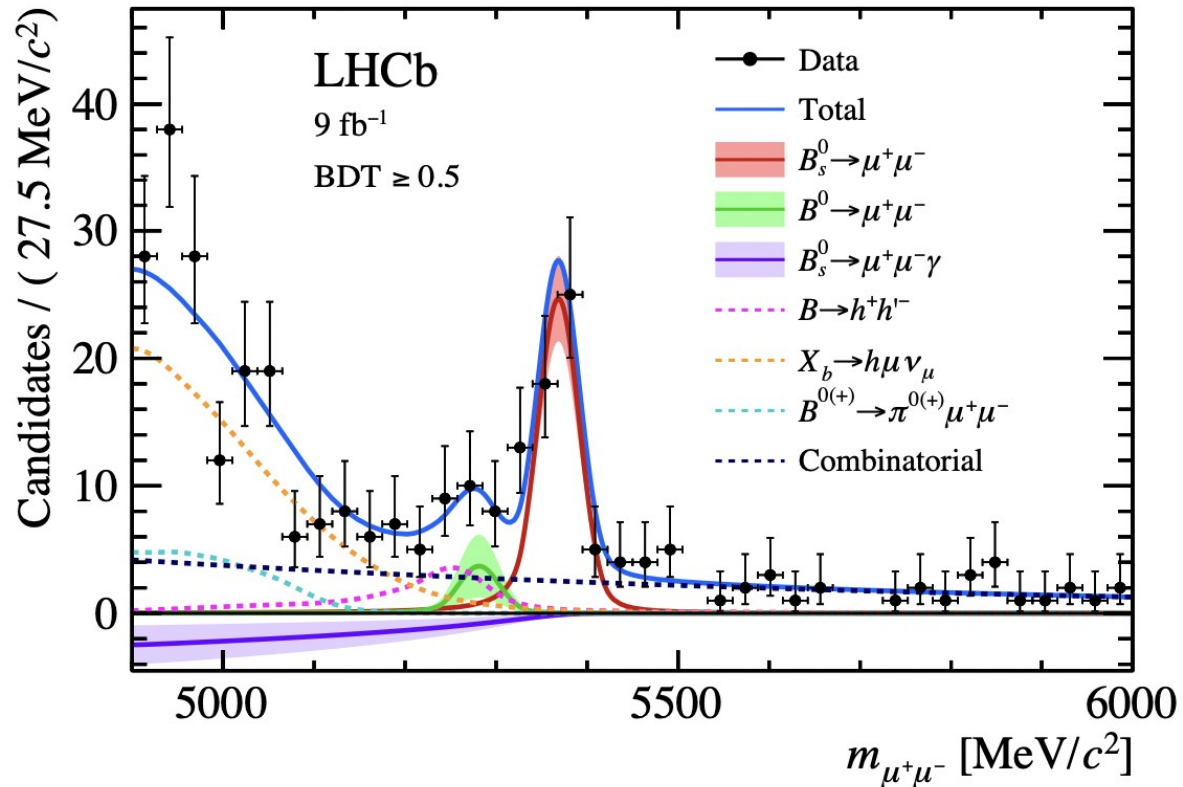
- *Essential precondition: controlling all other backgrounds*
Strategy now being applied at LHCb, resulting in a first limit
[LHCb, 2108.09283-4]
- *High q^2 offers several TH advantages*
 - *Probes in complementary kin. region (high q^2) the tensions reported in semi-lep BRs*
 -  *Although high q^2 not immune from long-distance challenges, they are different than low q^2*
 - *Test is strong, given the very different underlying exp method*

Basic Idea *Extract $B_s \rightarrow \mu\mu\gamma$ from $B_s \rightarrow \mu\mu$ event sample, by enlarging $m_{\mu\mu}$ below B_s peak*

- *Essential precondition: controlling all other backgrounds*
Strategy now being applied at LHCb, resulting in a first limit
[LHCb, 2108.09283-4]
- *High q^2 offers several TH advantages*
 - *Probes in complementary kin. region (high q^2) the tensions reported in semi-lep BRs*
 -  *Although high q^2 not immune from long-distance challenges, they are different than low q^2*
 - *Test is strong, given the very different underlying exp method*
 - *Preferred region for lattice QCD*

$B_s \rightarrow \mu\mu\gamma$ at high q^2

[thanks F. Dettori]



$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = \left(3.09^{+0.46+0.15}_{-0.43-0.11} \right) \times 10^{-9}$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) = \left(1.2^{+0.8}_{-0.7} \pm 0.1 \right) \times 10^{-10} < 2.6 \times 10^{-10}$$

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^- \gamma)_{m_{\mu\mu} > 4.9 \text{ GeV}} = (-2.5 \pm 1.4 \pm 0.8) \times 10^{-9} < 2.0 \times 10^{-9}$$

No significant signal for $B^0 \rightarrow \mu^+ \mu^-$ and $B_s^0 \rightarrow \mu^+ \mu^- \gamma$, upper limits at 95%

First world limit on $B_s^0 \rightarrow \mu^+ \mu^- \gamma$ decay

Conclusions

- *Possible hints of NP in $b \rightarrow s\mu\mu$ transitions persist but only on observables for which certain possibly sizeable, long-distance contributions, are not known quantitatively*
- *To make progress, we have to address the size of such contributions*
- *Or we may look in other kinematic regions not affected by such theory uncertainty*