

# Studies on accuracy of the contributions from pair production in Babayaga generator - a status report

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# Aim of the work

- calculation of the virtual (determined by the [package bha\\_nnlo\\_hf](#)) and real corrections (Monte Carlo generators [EKHARA](#), [BHAGEN-1PH+...](#) and [HELAC-PHEGAS](#)) at NNLO for Bhabha scattering
- discussion of the numerical results for energies and with realistic cuts used at the  $\Phi$  factory Dafne, at the  $B$  factories PEP-II and at KEK and at the charm/ $\tau$  factory BEPC II, Beijing
- comparison complete calculations with approximate ones realized in the MC generator [BabaYaga](#)

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# The massive NNLO corrections

The complete NNLO  $N_f = 1, 2$  corrections to Bhabha scattering consist of three parts:

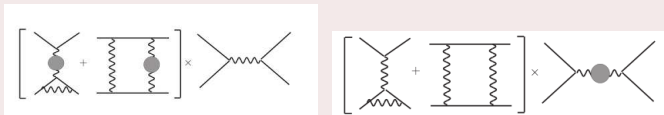
$$\begin{aligned} \frac{d\sigma_{N_f}^{\text{NNLO}}}{d\Omega} &= \frac{d\sigma_{\text{virt}}^{\text{NNLO } 1}}{d\Omega} + \frac{d\sigma_{\gamma}^{\text{NLO } 2}}{d\Omega} + \frac{d\sigma_{\text{real}}^{\text{LO } 3}}{d\Omega} \\ &= \frac{d\sigma_{e^+e^-}}{d\Omega} + \frac{d\sigma_{\mu^+\mu^-}}{d\Omega} + \frac{d\sigma_{\tau^+\tau^-}}{d\Omega} + \frac{d\sigma_{\text{had}}}{d\Omega}. \end{aligned} \quad (1)$$

1 - bha\_nnlo\_hf

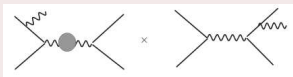
2 - BHAGEN-1PH+...,bha\_nnlo\_hf

3 - HELAC-PHEGAS,EKHARA

- the  $\sigma_{virt}^{NNLO}$  consists of virtual two-loop corrections  $\sigma_{2L}^{NNLO}$  and loop-by-loop corrections  $\sigma_{1L1L}^{NNLO}$



- contributions with real photon emission  $\sigma_{\gamma}^{NLO} = \sigma_{\gamma,soft}^{NLO}(\omega) + \sigma_{\gamma,hard}^{NLO}(\omega)$



- contributions with real pair or hadron emission

$$\sigma_{real}^{LO} = \sigma_{e^+e^-(e^+e^-)}^{LO} + \sigma_{e^+e^-(f+f^-)}^{LO} + \sigma_{e^+e^-(hadrons)}^{LO}$$

First results:

„Quest for precision in hadronic cross sections at low energy: Monte Carlo tools vs. experimental data”, EPJC(2010)66

# Cuts dependence study for different experiments

## 1. $\Phi$ factories KLOE/DAΦNE (Frascati)

- (a)  $\sqrt{s} = 1.02$  GeV
- (b)  $E_{min} = 0.4$  GeV
- (c) For  $\theta_{\pm}$  two selections have to be checked
  - i. tighter selection  $55^{\circ} < \theta_{\pm} < 125^{\circ}$
  - ii. wider selection  $20^{\circ} < \theta_{\pm} < 160^{\circ}$
- (d)  $\zeta_{max} = 4, 5, 6, 7, 8, \dots, 14^{\circ}$ , with reference value  $\zeta_{max} = 9^{\circ}$

## 2. B-factories BABAR/PEP-II (SLAC) & BELLE/KEKB (KEK)

- (a)  $\sqrt{s} = 10.56$  GeV
- (b)  $|\vec{p}_+|/E_{beam} > 0.75$  and  $|\vec{p}_-|/E_{beam} > 0.50$   
or  $|\vec{p}_-|/E_{beam} > 0.75$  and  $|\vec{p}_+|/E_{beam} > 0.50$
- (c) For  $|\cos(\theta_{\pm})|$  the following selections have to be checked
  - i.  $|\cos(\theta_{\pm})| < 0.65$  and  $|\cos(\theta_+)| < 0.60$  or  $|\cos(\theta_-)| < 0.60$
  - ii.  $|\cos(\theta_{\pm})| < 0.70$  and  $|\cos(\theta_+)| < 0.65$  or  $|\cos(\theta_-)| < 0.65$
  - iii.  $|\cos(\theta_{\pm})| < 0.60$  and  $|\cos(\theta_+)| < 0.55$  or  $|\cos(\theta_-)| < 0.55$
- (d)  $\zeta_{max}^{3d} = 20, 22, 24, \dots, 40^{\circ}$ , with reference value  $\zeta_{max}^{3d} = 30^{\circ}$

## Cuts dependence study for different experiments

### 3. BES-III experiment at BEPCII (Beijing)

(a)  $\sqrt{s} = 3.686$  GeV, 3.65 GeV and 3.097 GeV

(b)  $|\cos\theta| < 0.8$ , where  $\theta$  is the polar angle of the electron or positron in the lab system, this corresponds to the barrel region of BES-III detector. Since in BEPC,  $e^+$  and  $e^-$  beams are colliding with equal energy but at a 22mrad crossing angle, the lab system is slightly different from the CoM system.

(c)  $E_{e^+} > 1.0$  GeV and  $E_{e^-} > 1.0$  GeV, where  $E$  is the energy deposited in the electromagnetic calorimeter (EMC).

(d)  $E/p$  for one track greater than 0.5 and the other track greater than 0.8, here  $E$  is the energy deposited in the electromagnetic calorimeter (EMC), and  $p$  is the track momentum measured in the Main Drift Chamber.

To see how the NNLO corrections depend on the event selection we obtained results also for  $|\cos\theta| < 0.7, 0.75, 0.85$  and  $0.9$

#### 4. B-factory Belle (KEK)- the reference event selection

Belle runs at an asymmetric  $e^+e^-$  collider, but all criteria are expressed in the CoM fram (a)  $\sqrt{s}=10.58$  GeV

(b) For  $\theta_{\pm}$  two selections have to be checked

i.  $50.5^\circ < \theta_{\pm} < (180 - 50.5)^\circ$

ii.  $45.5^\circ < \theta_{\pm} < (180 - 45.5)^\circ$

iii.  $55.5^\circ < \theta_{\pm} < (180 - 55.5)^\circ$

(c) Two charged tracks have momentum  $> 2.645$  GeV

(d) The track with maximum deposited energy in EMC greater than 2 GeV,

(e) The sum of the deposited energies of all tracks in EMC is greater than 4 GeV

(both charged and neutral particle can deposite energy in EMC and it is not checked if the particle is charged or neutral)

(f) Acollinearity angle (2D)  $\zeta_{max}=5,6,7,8,\dots,15^\circ$ , with reference value  $\zeta_{max}=10^\circ$

(g) Transverse momentum of any observed charged particle greater than 0.1 GeV

Where:

$$\zeta = |\theta_+ + \theta_- - 180| \quad (2)$$

$$\zeta^{3d} = |\arccos s(\vec{p}_+ \vec{p}_- / |\vec{p}_+| |\vec{p}_-|) 180 / \pi - 180| \quad (3)$$



## KLOE:

BORN = 542.663(6) nb

$\sigma_{BY} = 455.71(5)$  nb - all  $\sigma_{BY}$  without vacuum polarisation

$\sqrt{s} = 1.02$  GeV

$E_{min} = 0.4$  GeV

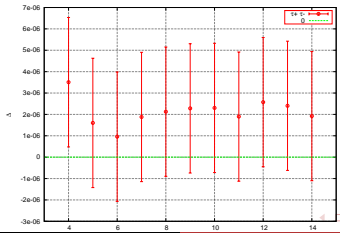
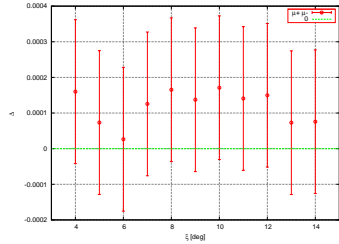
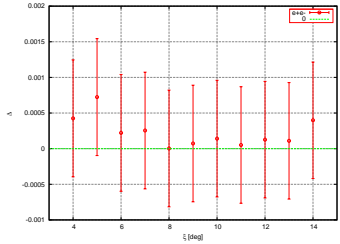
$55^\circ < \theta_{\pm} < 125^\circ$

$\zeta_{max} = 9^\circ$

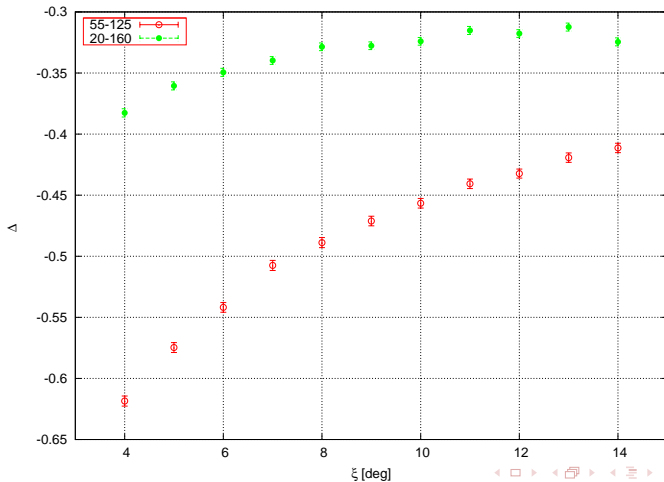
particles	$\sigma_h$ [nb]	$\sigma_{v+s}$ [nb]	$\sigma_{pairs}$ [nb]	sum [nb]
<b>NNLO</b>				
electron	9.5021(2)	-11.5666	0.2712(15)	-1.7933(3)
muon	1.49406(3)	-1.7356(2)	$0.246(7) \cdot 10^{-7}$	-0.2415(2)
tau	0.0201637(4)	-0.023412(2)	0	-0.003248(2)
<b>sum all: <math>\sigma^{NNLO}</math></b>				<b>-2.0381(4)</b>
<b>BabaYaga NNLO</b>				
electron	9.5020(8)	-11.0722(1)	-	-1.5702(8)
muon	1.4941(1)	-1.74421(6)	-	-0.2501(1)
tau	0.020164(2)	-0.0237027(6)	-	-0.003539(2)
<b>sum all: <math>\sigma_{BY}^{NNLO}</math></b>				<b>-1.8239(8)</b>
$\sigma^{NNLO} - \sigma_{BY}^{NNLO}$				-0.2143(9)
<b>relative difference: <math> \sigma^{NNLO} - \sigma_{BY}^{NNLO}  / \sigma_{BY}</math></b>				<b>0.471(4)%<math>\infty</math></b>

**Attention:**  $\sigma_{BY}^{20 < \theta_{\pm} < 160, \zeta_{max} = 9} = 6114.9(6)$  nb

$$\Delta = \frac{|\sigma_h - \sigma_{hBY}|}{\sigma_h} - \text{comparison between hard parts}$$



$$\Delta = \frac{\sigma^{NNLO} - \sigma_{BY}^{NNLO}}{\sigma_{BY}} 10^3 \text{ - relative difference \%}$$



### BaBar:

BORN = 5.481(1) nb

$\sigma_{BY} = 5.195(2)$  nb

(a)  $\sqrt{s} = 10.56$  GeV

(b)  $|\vec{p}_+|/E_{beam} > 0.75$  and  $|\vec{p}_-|/E_{beam} > 0.50$

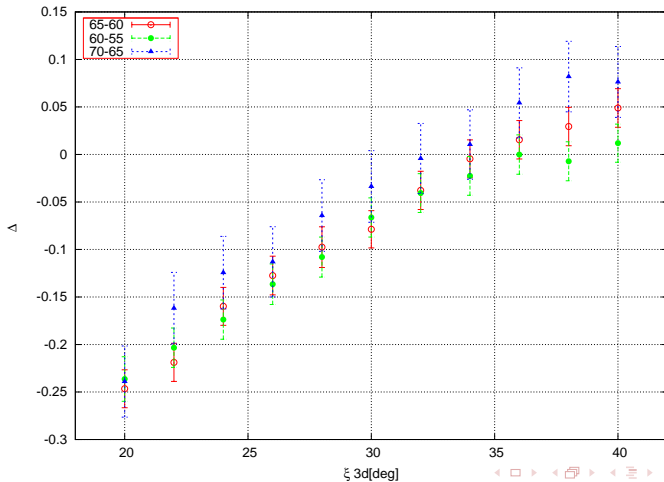
or  $|\vec{p}_-|/E_{beam} > 0.75$  and  $|\vec{p}_+|/E_{beam} > 0.50$

(c)  $|\cos(\theta_{\pm})| < 0.65$  and  $|\cos(\theta_+)| < 0.60$  or  $|\cos(\theta_-)| < 0.60$

(d)  $\zeta_{max}^{3d} = 30^\circ$

articles	$\sigma_h$ [nb]	$\sigma_{\nu+s}$ [nb]	$\sigma_{pairs}$ [nb]	sum [nb]
<b>NNLO</b>				
electron	0.202439(6)	-0.223667	0.01355(8)	-0.00768(8)
muon	0.0757889(2)	-0.079231(2)	0.000451(2)	-0.002991(3)
tau	0.0138398(4)	-0.0144654(2)	0.120(3)*10 <sup>-8</sup>	-0.0006257(5)
<b>sum all: <math>\sigma^{NNLO}</math></b>				<b>-0.01130(8)</b>
<b>BabaYaga NNLO</b>				
electron	0.20244(2)	-0.20971(5)	-	-0.00727(5)
muon	0.07580(1)	-0.07872(2)	-	-0.00292(2)
tau	0.013847(4)	-0.014541(4)	-	-0.000694(6)
<b>sum all: <math>\sigma_{BY}^{NNLO}</math></b>				<b>-0.01088(5)</b>
$\sigma^{NNLO} - \sigma_{BY}^{NNLO}$				-0.00042(9)
<b>relative difference: <math> \sigma^{NNLO} - \sigma_{BY}^{NNLO} /\sigma_{BY}</math></b>				<b>0.08(2)%</b>

$$\Delta = \frac{\sigma^{NNLO} - \sigma_{BY}^{NNLO}}{\sigma_{BY}} 10^3 \text{ - relative difference \%}$$



## BES

Born = 173.98(2) nb

$\sigma_{BY} = 158.23(2)$

(a)  $\sqrt{s} = 3.097$  GeV

(b)  $|\cos\theta| < 0.8$

articles	$\sigma_h$ [nb]	$\sigma_{v+s}$ [nb]	$\sigma_{pairs}$ [nb]	sum [nb]
<b>NNLO</b>				
electron	4.16202(12)	-4.71708	0.19977(116)	-0.3553(12)
muon	1.01652(3)	-1.09665(1)	0.001337(5)	-0.078793(3)
tau	0.049672(2)	-0.0540(1)	0	-0.0044(1)
<b>sum all: <math>\sigma^{NNLO}</math></b>				<b>-0.439(1)</b>
<b>BabaYaga NNLO</b>				
electron	4.1620(10)	-4.48183(21)	-	-0.3198(10)
muon	1.0165(3)	-1.0961(1)	-	-0.0796(3)
tau	0.04966(2)	-0.05421(1)	-	-0.00455(2)
<b>sum all: <math>\sigma_{BY}^{NNLO}</math></b>				<b>-0.404(1)</b>
$\sigma^{NNLO} - \sigma_{BY}^{NNLO}$				-0.035(1)
<b>relative difference: <math> \sigma^{NNLO} - \sigma_{BY}^{NNLO} /\sigma_{BY}</math></b>				<b>0.23(8)%</b>

## BES

BORN = 129.0958(4) nb

$\sigma_{BY} = 116.41(2)$  nb

(a)  $\sqrt{s} = 3.65$  GeV

(b)  $|\cos\theta| < 0.8$

articles	$\sigma_h$ [nb]	$\sigma_{v+s}$ [nb]	$\sigma_{pairs}$ [nb]	sum [nb]
<b>NNLO</b>				
electron	3.19544(9)	-3.55544	0.188856(997)	-0.171(1)
muon	0.83245(2)	-0.88149(1)	0.002003(6)	-0.04704(1)
tau	0.058674(2)	-0.0633(1)	0	-0.0046(1)
<b>sum all: <math>\sigma^{NNLO}</math></b>				<b>-0.223(1)</b>
<b>BabaYaga NNLO</b>				
electron	3.1960(3)	-3.3730(2)	-	-0.1770(4)
muon	0.83252(7)	-0.88041(9)	-	-0.0479(1)
tau	0.058679(7)	-0.06323(2)	-	-0.00455(2)
<b>sum all: <math>\sigma_{BY}^{NNLO}</math></b>				<b>-0.2295(4)</b>
$\sigma^{NNLO} - \sigma_{BY}^{NNLO}$				0.006(1)
<b>relative difference: <math> \sigma^{NNLO} - \sigma_{BY}^{NNLO} /\sigma_{BY}</math></b>				<b>0.057(9)%</b>

## BES

BORN = 123.32(1) nb

$\sigma_{BY} = 114.27(2)$  nb

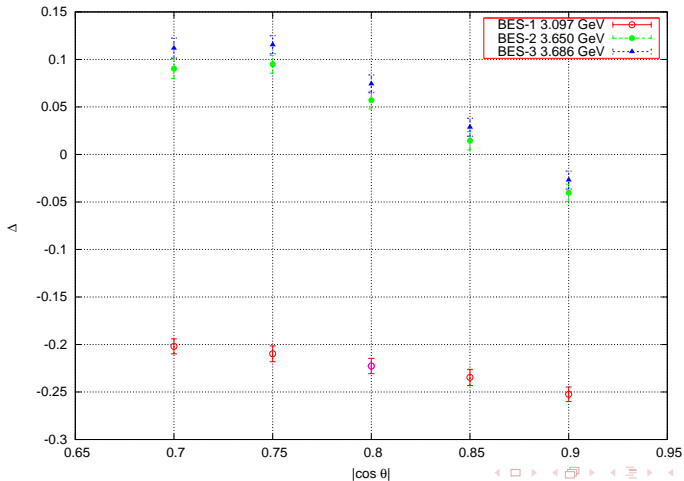
(a)  $\sqrt{s} = 3.686$  GeV

(b)  $|\cos\theta| < 0.8$

articles	$\sigma_h$ [nb]	$\sigma_{v+s}$ [nb]	$\sigma_{pairs}$ [nb]	sum [nb]
<b>NNLO</b>				
electron	3.14439(9)	-3.49579	0.187401(985)	-0.1640(9)
muon	0.82215(2)	-0.86988(1)	0.00203527(637)	-0.04570(7)
tau	0.057923(2)	-0.0622(1)	-	-0.0043(1)
<b>sum all: <math>\sigma^{NNLO}</math></b>				<b>-0.2140(9)</b>
<b>BabaYaga NNLO</b>				
electron	3.1447(3)	-3.3163(2)	-	-0.1716(4)
muon	0.82221(7)	-0.8688(1)	-	-0.04659(12)
tau	0.057928(7)	-0.06219(2)	-	-0.00426(2)
<b>sum all: <math>\sigma_{BY}^{NNLO}</math></b>				<b>-0.2225(4)</b>
$\sigma^{NNLO} - \sigma_{BY}^{NNLO}$				0.0085(1)
<b>relative difference: <math> \sigma^{NNLO} - \sigma_{BY}^{NNLO} /\sigma_{BY}</math></b>				<b>0.074(9)%</b>



$$\Delta = \frac{\sigma^{NNLO} - \sigma_{BY}^{NNLO}}{\sigma_{BY}} 10^3 \text{ - relative difference \%}$$



## BELLE:

BORN = 6.73555(4) nb

$\sigma_{BY} = 5.501(5)$  nb

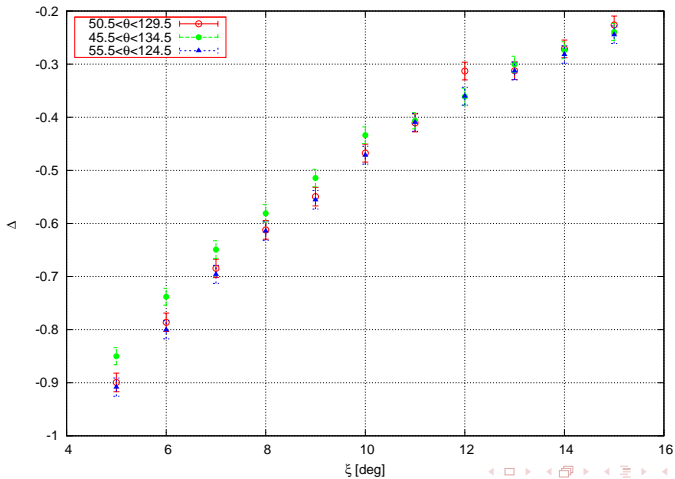
(a)  $\sqrt{s} = 10.58$  GeV

(b)  $50.5^\circ < \theta_{\pm} < (180 - 50.5)^\circ$

(c)  $\zeta_{max} = 10^\circ$

articles	$\sigma_h$ [nb]	$\sigma_{v+s}$ [nb]	$\sigma_{pairs}$ [nb]	sum [nb]
<b>NNLO</b>				
electron	0.21572(7)	-0.25596	0.01310(5)	-0.02714(9)
muon	0.080377(8)	-0.09009(1)	0.000759(1)	-0.00895(2)
tau	0.014428(4)	-0.01602(1)	0.0000321(1)	-0.00156(1)
<b>sum all: <math>\sigma^{NNLO}</math></b>				<b>-0.03765(9)</b>
<b>BabaYaga NNLO</b>				
electron	0.21563(2)	-0.23994(2)	-	-0.02431(3)
muon	0.080376(6)	-0.08948(2)	-	-0.009104(2)
tau	0.014423(1)	-0.016091(7)	-	-0.001668(7)
<b>sum all: <math>\sigma_{BY}^{NNLO}</math></b>				<b>-0.03508(3)</b>
$\sigma^{NNLO} - \sigma_{BY}^{NNLO}$				-0.00257
<b>relative difference: <math> \sigma^{NNLO} - \sigma_{BY}^{NNLO}  / \sigma_{BY}</math></b>				<b>0.47(2)%</b>

$$\Delta = \frac{\sigma^{NNLO} - \sigma_{BY}^{NNLO}}{\sigma_{BY}} 10^3 \text{ - relative difference \%}$$



"Monte Carlo luminosity tools: status and perspectives", Guido Montagna, 8th Meeting of the RMCLow Working Group Liverpool, 18-19 September, 2010

## Status of the MC theoretical accuracy

Main conclusion of the Luminosity Section of the WG Report

Putting the various sources of uncertainties (for large-angle Bhabha) all together...

Source of error (%)	$\Phi$ -factories	$\sqrt{s} = 3.5$ GeV	B-factories
$ \delta_{VP}^{err} $ [Jegerlehner]	0.00	0.01	0.03
$ \delta_{VP}^{err} $ [HMNT]	0.02	0.01	0.02
$ \delta_{SV,\alpha^2}^{err} $	0.02	0.02	0.02
$ \delta_{HH,\alpha^2}^{err} $	0.00	0.00	0.00
$ \delta_{SV,H,\alpha^2}^{err} $ [in progress]	0.05	0.05	0.05
$ \delta_{pairs}^{err} $ [in progress]	$\sim 0.05$	$\sim 0.1^1$	$\sim 0.02^2$
$ \delta_{total}^{err} $ linearly	$0.12 \div 0.14$	0.18	$0.11 \div 0.12$
$ \delta_{total}^{err} $ in quadrature	$0.07 \div 0.08$	0.11	$0.06 \div 0.07$

- For the experiments on top of and closely around the  $J/\psi$  resonance, the accuracy slightly deteriorates, because of the differences between the predictions of independent  $\Delta\alpha_{had}^{(5)}(q^2)$  routines [see next slide]
- ★ The present error estimate appears to be **rather robust and sufficient for high-precision luminosity measurements**. It is comparable with that achieved about ten years ago for small-angle Bhabha luminosity monitoring at LEP/SLC

<sup>1</sup>Very preliminary, work in progress using realistic BES-III and CLEO-c luminosity cuts

<sup>2</sup>Preliminary and assuming BaBar cuts. Work in progress for BELLE event selection

**KLOE:**

$$|\delta_{pairs}^{err}| \sim 0.5 \text{ ‰}$$

$$\left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{reference} = 0.471(4) \text{ ‰}, \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{max} = 0.619(4) \text{ ‰}$$

**B - factories:**

$$|\delta_{pairs}^{err}| \sim 0.2 \text{ ‰}$$

$$\text{BaBar: } \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{reference} = 0.08(2) \text{ ‰}, \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{max} = 0.1(2) \text{ ‰}$$

$$\text{Belle: } \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{reference} = 0.47(2) \text{ ‰}, \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{max} = 0.91(2) \text{ ‰}$$

**BES vs.  $\sqrt{s} = 3.5\text{GeV}$ :**

$$|\delta_{pairs, \sqrt{s}=3.5}^{err}| \sim 1 \text{ ‰}$$

**BES:**

$$\sqrt{s} = 3.097\text{GeV: } \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{reference} = 0.23(8)\text{ ‰}, \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{max} = 0.25(7) \text{ ‰}$$

$$\sqrt{s} = 3.650\text{GeV: } \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{reference} = 0.057(9)\text{ ‰}, \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{max} = 0.095(9) \text{ ‰}$$

$$\sqrt{s} = 3.686\text{GeV: } \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{reference} = 0.074(9)\text{ ‰}, \left| \frac{\sigma^{NNLO} - \sigma^{NNLO}}{\sigma_{BY}} \right|_{max} = 0.11(1) \text{ ‰}$$

# Hadrons - in progress

particles	$\sigma_h$	$\sigma_{v+s}$	$\sigma_{pairs}$	sum
<b>KLOE, <math>55^\circ &lt; \theta_{\pm} &lt; 125^\circ</math>, <math>\zeta_{max}=9^\circ</math></b>				
<b>NNLO</b>				
pions	1.17402(8)	-1.35988(2)	0	-0.18586(8)
hadrons	1.5248(5)	in progress	-	in progress
<b>BabaYaga NNLO</b>				
hadrons	1.5247(5)	-1.126(2)	-	0.399(2)

particles	$\sigma_h$	$\sigma_{v+s}$	$\sigma_{pairs}$	sum
<b>BaBar, <math> \cos(\theta_{\pm})  &lt; 0.65</math> and <math> \cos(\theta_+)  &lt; 0.60</math> or <math> \cos(\theta_-)  &lt; 0.60</math>, <math>\zeta_{max}^{3d} = 30^\circ</math></b>				
<b>NNLO</b>				
pions	0.051037(2)	-0.053328(3)	0.000030(3)	-0.002261(5)
hadrons	0.17995(2)	in progress	-	in progress
<b>BabaYaga NNLO</b>				
hadrons	0.17984(2)	-0.18760(4)	-	-0.00776(4)

## Issues to be discussed here

Comparison of results with vacuum polarization obtained using :VPHLMNT (T.Teubner et all.) and hadr5n09 (F. Jegerlehner) (all results from BabaYaga) - all results in nb

**KLOE:**  $55^\circ < \theta_{\pm} < 125^\circ$ ,  $\zeta_{max}=4^\circ$   
 $\sigma_{BY} = 436.85(5)$

vacpol	$\sigma_h$	$\sigma_{v+s}$	sum:
VPHLMNT(2009)	1.4346(5)	-1.126(2)	0.309(2)
hadr5n09	1.6264(6)	-1.405(2)	0.221(2)
<b>relative difference:</b> $ \frac{\sigma_{VPHLMNT}^{NNLO} - \sigma_{hadr5n09}^{NNLO}}{\sigma_{BY}} $			0.201(6)‰

**BES:**  $\sqrt{s} = 3.650$  GeV,  $|\cos \theta| < 0.8$   
 $\sigma_{BY} = 116.41(2)$  nb

vacpol	$\sigma_h$	$\sigma_{v+s}$	sum:
VPHLMNT2.0(2010)	1.6613(3)	-1.7860(2)	-0.1247(4)
hadr5n09	1.6471(7)	-1.7686(2)	-0.1215(7)
<b>relative difference:</b> $ \frac{\sigma_{VPHLMNT}^{NNLO} - \sigma_{hadr5n09}^{NNLO}}{\sigma_{BY}} $			0.0275‰

## Issues to be discussed here

**BES:**  $\sqrt{s} = 3.686 \text{ GeV}, |\cos \theta| < 0.8$

$\sigma_{BY} = 114.27(2) \text{ nb}$

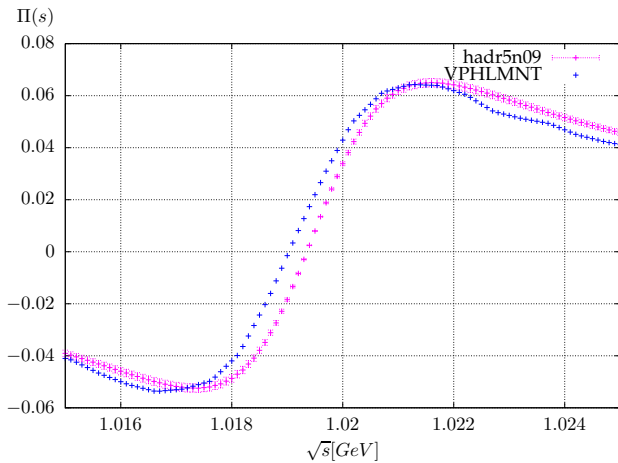
vacpol	$\sigma_h$	$\sigma_{v+s}$	sum:
VPHLMNT2.0(2010)	10.006(4)	-16.80(1)	-6.79(1)
hadr5n09	9.60(1)	-16.28(2)	-6.68(3)
<b>relative difference:</b> $\left  \frac{\sigma_{VPHLMNT}^{NNLO} - \sigma_{hadr5n09}^{NNLO}}{\sigma_{BY}} \right $			0.96‰

**BES:**  $\sqrt{s} = 3.097 \text{ GeV}, |\cos \theta| < 0.9$

$\sigma_{BY} = 378.48(5) \text{ nb}$

vacpol	$\sigma_h$	$\sigma_{v+s}$	sum:
VPHLMNT2.0(2010)	-116.50(6)	287.7(3)	171.2(3)
hadr5n09	-119.1(2)	291.9(3)	172.8(4)
<b>relative difference:</b> $\left  \frac{\sigma_{VPHLMNT}^{NNLO} - \sigma_{hadr5n09}^{NNLO}}{\sigma_{BY}} \right $			4.227‰





$\frac{\text{hadr5n09-VPMLMNT}}{\text{VPMLMNT}}$

