



Techniques for hadron spectroscopy studies at LHCb

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2023/06/07

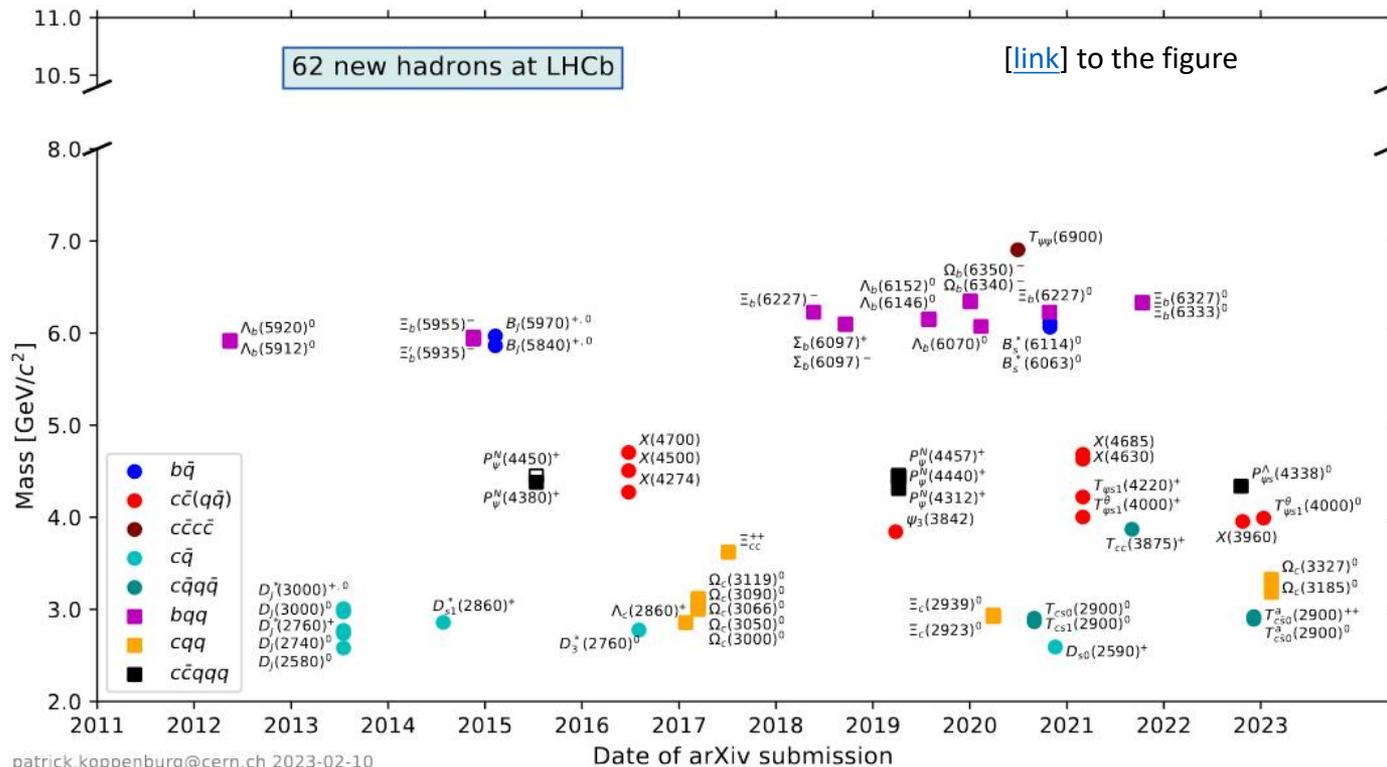
On behalf of the LHCb collaboration

Hadrons 2023

05-09 June 2023, Genova, Italy

b, c spectroscopy at LHCb

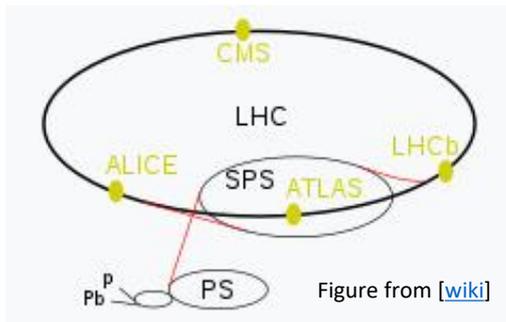
- LHCb: one of the major players of hadron spectroscopy study
 - Search for **new hadrons**
 - Measure **hadron properties** (lineshape, lifetime, decay modes...)



b, c spectroscopy at LHCb

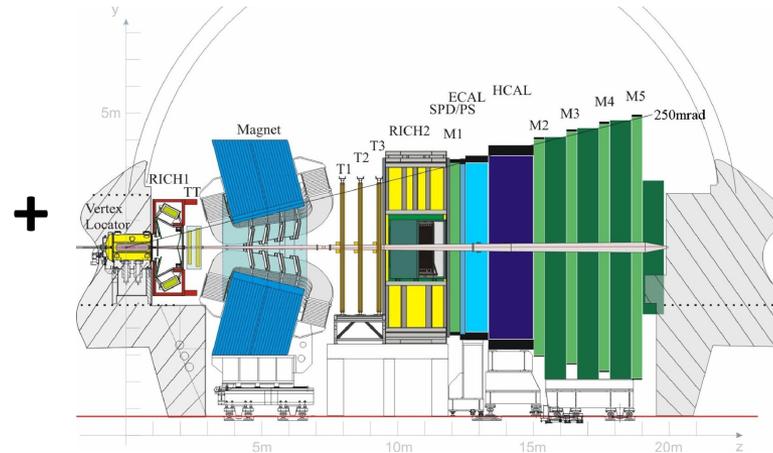
- Benefit from...

Large b, c hadron production cross-section @ LHC



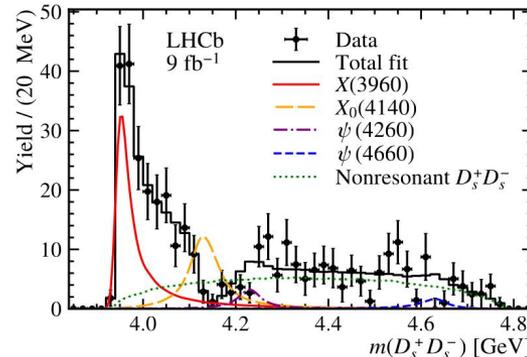
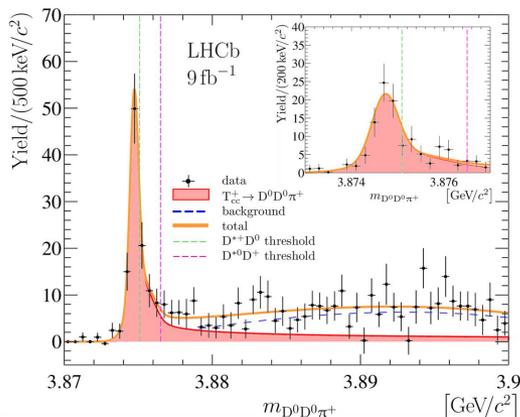
JINST 3 (2008) S08005, IJMPA 30 (2015) 1530022

LHCb detector optimized for the collection, reconstruction and identification of b, c signals



= High-stat. and good-quality heavy flavor dataset

Improved knowledge about hadron spectroscopy



arXiv:2210.15153, Tetraquark candidate in $D_s^+ D_s^-$ final state

Hadrons 2023

Data analysis

Menu of today:
 Development of data-analysis techniques benefiting recent LHCb results
 (Focus on amplitude analysis)

Selected topics

• Development of helicity amplitude formalism

[PRL 115 \(2015\) 072001](#)

$P_c(4380)$, $P_c(4450)$ observation



[Annals Phys. 7 \(1959\) 404](#)

Conventional helicity formalism

[arXiv:2208.03262](#)

Study of $\Lambda_c^+ \rightarrow pK\pi^-$ decay amplitude



[Advances in High Energy Physics \(2020\) 6674595](#)

[Chinese Phys. C 45 \(2021\) 063103](#)

[Phys.Rev.D 95 \(2017\) 7, 076010](#)

New principles for final-state alignment in helicity-based amplitude

[Science Bulletin 66 \(2021\) 1278](#)

Pentaquark evidence in $\Xi_b^- \rightarrow J/\psi \Lambda K^-$

[arXiv:2210.10346](#)

Observation of $P_{\psi_s}^\Lambda(4338)$



[Phys. Rev. D 101 \(2020\) 034033](#)

Dalitz-plot decomposition formula

• Speed up amplitude fits using GPUs

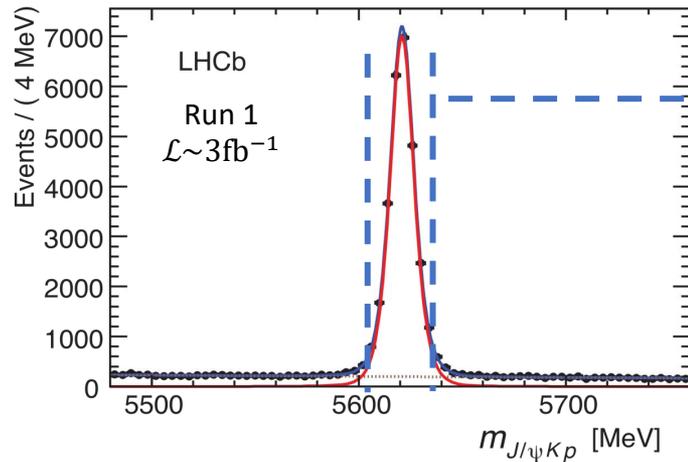
[arXiv:2301.04899](#)

Evidence of tetraquark candidate $T_{\psi_{s1}}^\theta(4000)^0$ ← A CUDA + RooFit based fit framework

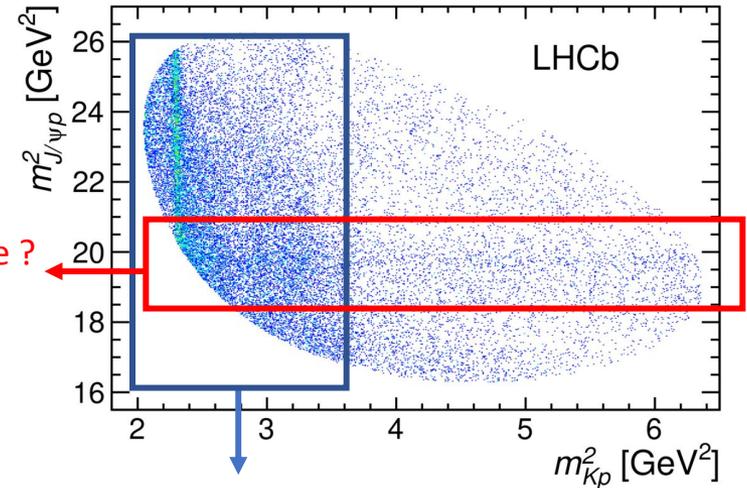
Focus on techniques. For relevant physics results, see the talks by Elisabetta [\[link\]](#) and Bo [\[link\]](#)

Development of helicity-based amplitude formalisms

Helicity formalism & P_c observation



$J/\psi p$ resonance ?
[$c\bar{c}uud$]



Conventional resonances $\Lambda^* \rightarrow pK$

- $\sim 20k \Lambda_b^0 \rightarrow J/\psi p K^-$ signals collected in Run1
- Clear $J/\psi p$ structure seen in Dalitz plot
- Multi-dimension amplitude analysis to extract properties of $J/\psi p$ intermediate states

Helicity formalism & P_C observation

- Two decay chains: Λ^* or P_C as intermediate state

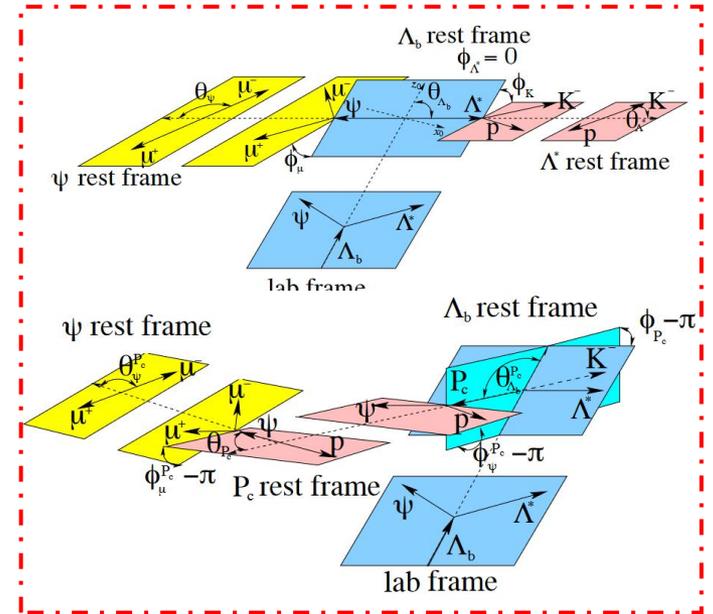
Λ^* chain:

$$\mathcal{M}_{\lambda_{\Lambda_b^0}, \lambda_p, \Delta\lambda_\mu}^{\Lambda^*} = \sum_n R_{\Lambda_n^*}(m_{Kp}) \mathcal{H}_{\lambda_p}^{\Lambda_n^* \rightarrow Kp} \sum_{\lambda_\psi} e^{i\lambda_\psi \phi_\mu} d_{\lambda_\psi, \Delta\lambda_\mu}^1(\theta_\psi) \times \sum_{\lambda_{\Lambda^*}} \mathcal{H}_{\lambda_{\Lambda^*}, \lambda_\psi}^{\Lambda_b^0 \rightarrow \Lambda^* \psi} e^{i\lambda_{\Lambda^*} \phi_K} d_{\lambda_{\Lambda_b^0}, \lambda_{\Lambda^*} - \lambda_\psi}^{\frac{1}{2}}(\theta_{\Lambda_b^0}) d_{\lambda_{\Lambda^*}, \lambda_p}^{J_{\Lambda_n^*}}(\theta_{\Lambda^*}).$$

P_C chain:

RBW-based lineshape

$$\mathcal{M}_{\lambda_{\Lambda_b^0}, \lambda_{P_C}, \Delta\lambda_\mu}^{P_C} = e^{i\lambda_{\Lambda_b^0} \phi_{P_C}} \sum_j R_{P_{Cj}}(M_{\psi p}) \sum_{\lambda_\psi} e^{i\lambda_\psi \phi_\mu} d_{\lambda_\psi, \Delta\lambda_\mu}^1(\theta_\psi) \times \sum_{\lambda_{P_C}} \mathcal{H}_{\lambda_{P_C}}^{\Lambda_b^0 \rightarrow P_{Cj} K} e^{i\lambda_{P_C} \phi_\psi} d_{\lambda_{\Lambda_b^0}, \lambda_{P_C}}^{\frac{1}{2}}(\theta_{\Lambda_b^0}) \mathcal{H}_{\lambda_\psi}^{P_{Cj} \rightarrow \psi p} d_{\lambda_{P_C}, \lambda_\psi - \lambda_{P_C}}^{J_{P_{Cj}}}(\theta_{P_C}),$$

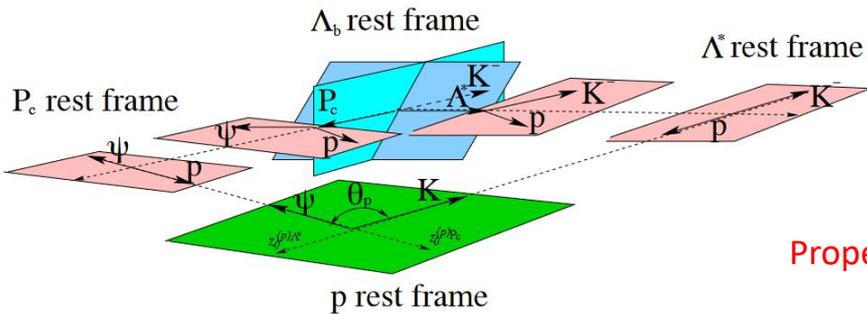
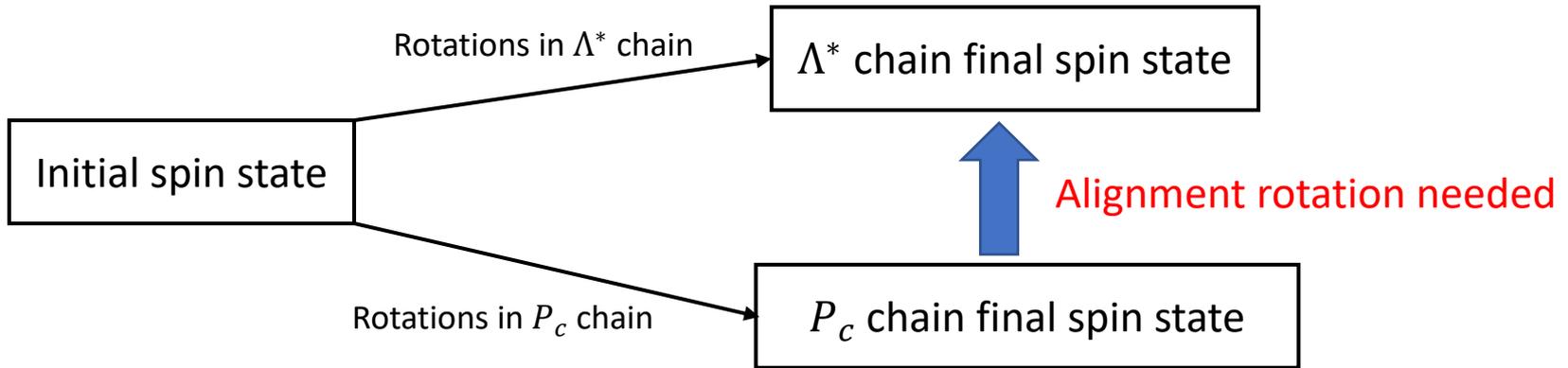


Wigner-D function to associate initial & final spin states of each two-body decay node

Use angles between particle momenta/momentum planes to obtain angular variables

Helicity formalism & P_C observation

- **Combine two chains to get final matrix element**
 - Need a consistent definition of initial & final spin state

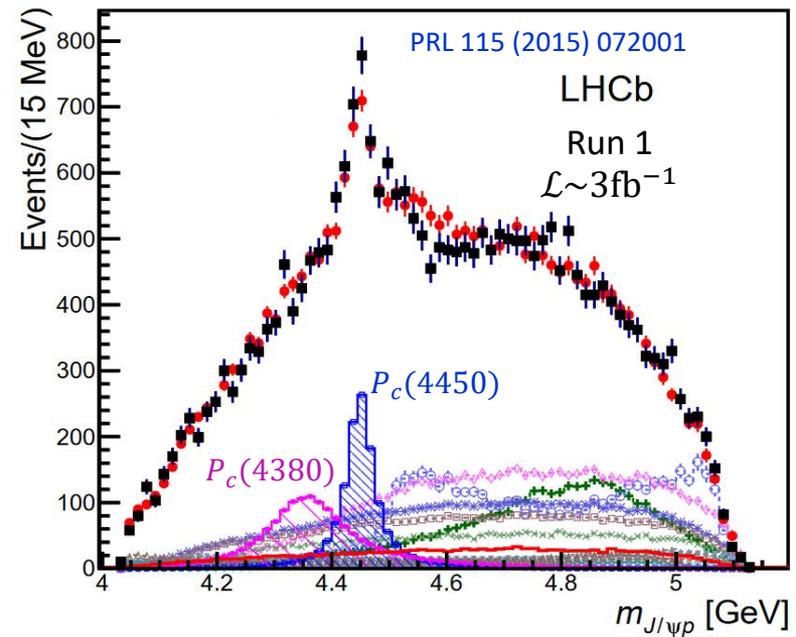
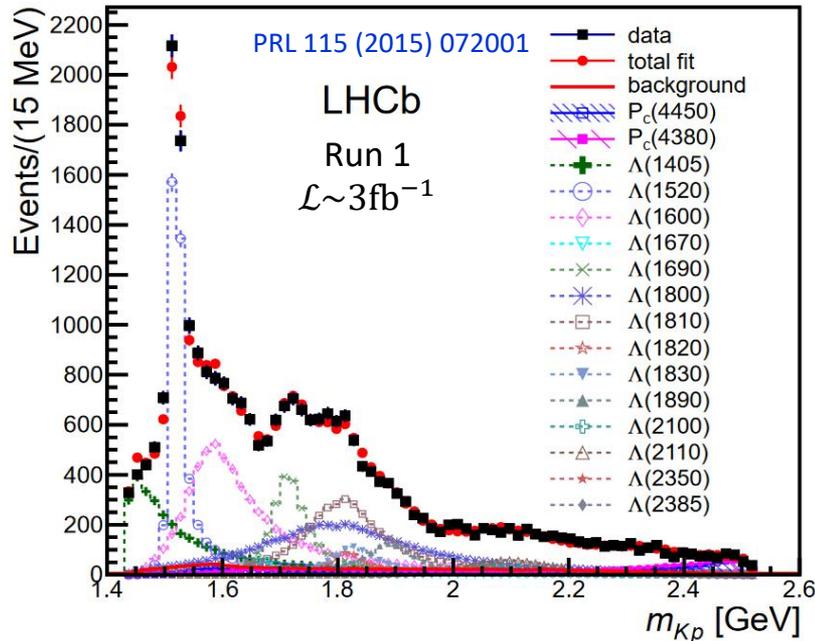


$$|\mathcal{M}|^2 = \sum_{\lambda_{\Lambda_b^0} = \pm\frac{1}{2}} \sum_{\lambda_p = \pm\frac{1}{2}} \sum_{\Delta\lambda_\mu = \pm 1} \left| \mathcal{M}_{\lambda_{\Lambda_b^0}, \lambda_p, \Delta\lambda_\mu}^{\Lambda^*} + e^{i\Delta\lambda_\mu \alpha_\mu} \sum_{\lambda_p} d_{\lambda_p, \lambda_p}^{\frac{1}{2} P_C}(\theta_p) \mathcal{M}_{\lambda_{\Lambda_b^0}, \lambda_p, \Delta\lambda_\mu}^{P_C} \right|^2$$

Properly align the definition of final-state spin states in different chains

Helicity formalism & P_c observation

- Two $J/\psi p$ resonances with significance $> 5\sigma$
 - minimal quark content $[c\bar{c}uud]$, good candidate for pentaquarks



- Follow-up analyses:

- Confirmed in Model-independent analysis [PRL 117\(2016\)082002](#)
- Similar structure seen in Cabibbo suppressed $\Lambda_b^0 \rightarrow J/\psi p \pi^-$ [PRL 117\(2016\)082003](#)
- $P_c(4312)$, $P_c(4440)$, $P_c(4457)$ observed in Run1+2 data [PRL 122\(2019\)222001](#)

The missing quantum effect ?

- The conventional helicity formalism

(SU2)

Decay angles rotating spin states

Fully determine

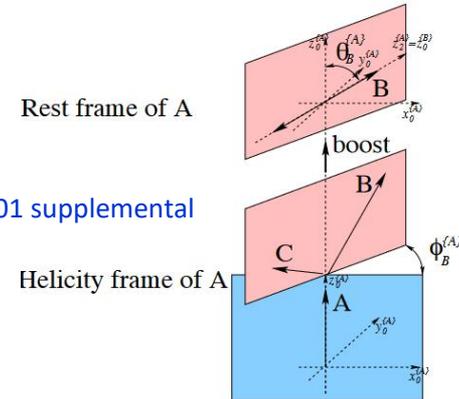
(SO3)

Rotations in momentum space

$$\mathcal{M} = \mathcal{H}_{\lambda_B, \lambda_C}^{A \rightarrow BC} D_{m_A, \lambda_B - \lambda_C}^{J_A}(\phi_B, \theta_A, 0)^*$$

$$\begin{aligned} \phi_B &= \text{atan2}(p_{B,y}^{\{A\}}, p_{B,x}^{\{A\}}) \\ &= \text{atan2}(\hat{y}_0^{\{A\}} \cdot \vec{p}_B^{\{A\}}, \hat{x}_0^{\{A\}} \cdot \vec{p}_B^{\{A\}}) \\ &= \text{atan2}((\hat{z}_0^{\{A\}} \times \hat{x}_0^{\{A\}}) \cdot \vec{p}_B^{\{A\}}, \hat{x}_0^{\{A\}} \cdot \vec{p}_B^{\{A\}}), \\ \cos \theta_A &= \hat{z}_0^{\{A\}} \cdot \hat{p}_B^{\{A\}}. \end{aligned}$$

PRL 115 (2015) 072001 supplemental



Quantum effects missing for **baryons** ?

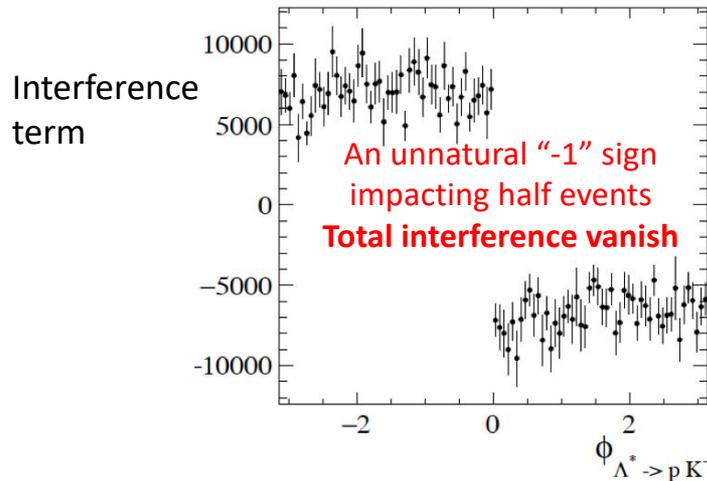
$$\begin{aligned} d_{\lambda_1, \lambda_2}^J(\theta_A) &= -\mathbf{1} \times d_{\lambda_1, \lambda_2}^J(\theta_A + 2\pi) \\ e^{i\lambda\phi_B} &= -\mathbf{1} \times e^{i\lambda(\phi_B + 2\pi)} \end{aligned}$$

Cannot set a preference between θ_A & $\theta_A + 2\pi$, ϕ_B & $\phi_B + 2\pi$

- Arbitrary “-1” terms in any single-chain amplitudes:
 - Generate tricky behavior in interference of different chains

Impact on interference

- The Λ^* , P_c interference using the formula for P_c observation



Impact of missing of the quantum effects consistent with the statement in [PRL 115 \(2015\) 072001](#)

polarization of zero. Interferences between various Λ_n^* and P_{cj}^+ resonances vanish in the integrated rates unless the resonances belong to the same decay chain and have the same quantum numbers.

- Impact on the first P_c analysis:
 - No impact on Λ^* -only fit quality
 - Reduce the flexibility of $\Lambda^* + P_c$ model
 - P_c properties (to be) updated in Run1+2 analysis

[PRL 122\(2019\)222001](#): Two-peak nature of $P_c(4450)$ observed;

Properties of $P_c(4380)$ to be updated in future amplitude analysis

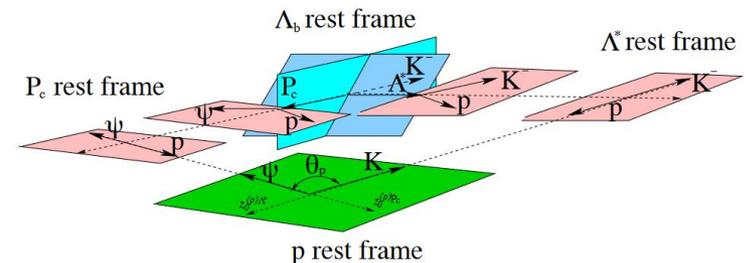
Recover the missing quantum effect

- Main idea:
 - Origin of the issue is improper alignment of final-state definitions for each decay chain due to arbitrary “-1” term
 - Seek for new principles for final-state alignment

Conventional method

Rely on graphic picture

Use angles between particle momenta or momentum planes to define alignment operator



Recover the missing quantum effect

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New method

Directly write down all rotation/boost operators associating initial/final spin-state frames, using a representation where $\theta \rightarrow \theta + 2\pi$ is visible

Advances in High Energy Physics (2020) 6674595

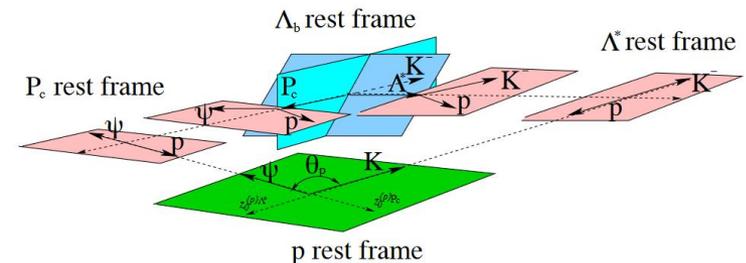
$$\begin{aligned} & \widehat{R}(\alpha_1^{W,R}, \beta_1^{W,R}, \gamma_1^{W,R}) \widehat{R}(\phi_R, \theta_R, 0) \widehat{R}(\phi_1^R, \theta_1^R, 0) |\mathbf{p}_1^R, s_1, \lambda_1^R\rangle \\ &= \sum_{\mu_1^R} D_{\mu_1^R, \lambda_1^R}^{s_1}(\phi_1^R, \theta_1^R, 0) \times \sum_{\nu_1^R} D_{\nu_1^R, \mu_1^R}^{s_1}(\phi_R, \theta_R, 0) \sum_{m_1} D_{m_1, \nu_1^R}^{s_1} \\ & \times (\alpha_1^{W,R}, \beta_1^{W,R}, \gamma_1^{W,R}) |\mathbf{p}_1^A, s_1, m_1\rangle. \end{aligned}$$

Advances in High Energy Physics (2020) 6674595; Chinese Phys. C 45 (2021) 063103

$$R_z(\alpha) = \begin{pmatrix} e^{-i\alpha/2} & 0 \\ 0 & e^{i\alpha/2} \end{pmatrix} R_y(\alpha) = \begin{pmatrix} \cos(\alpha/2) & -\sin(\alpha/2) \\ \sin(\alpha/2) & \cos(\alpha/2) \end{pmatrix}$$

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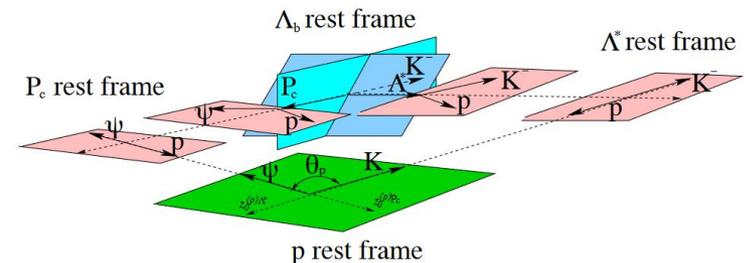
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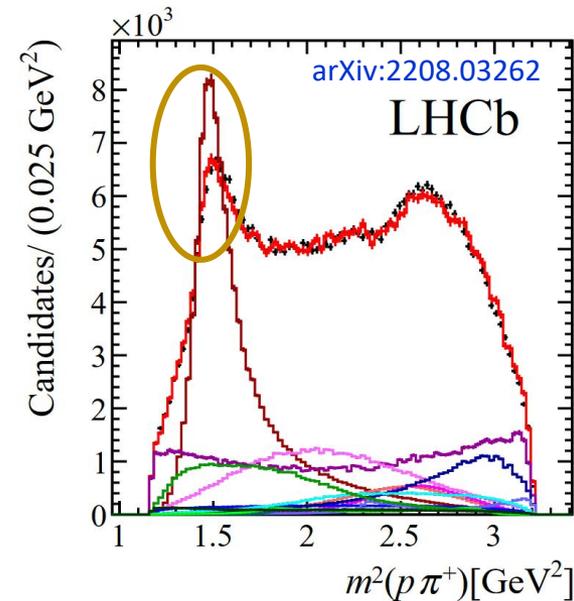
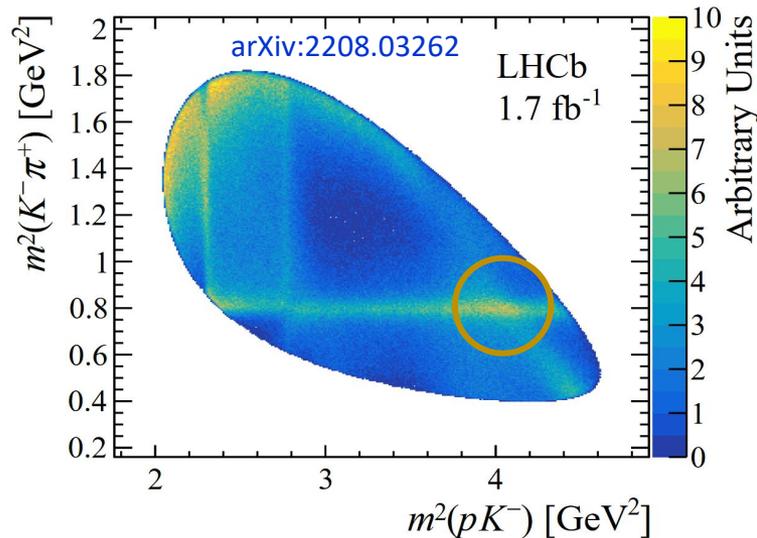
New method implemented in

$\Lambda_c^+ \rightarrow pK\pi^-$ amplitude analysis
[arXiv:2208.03262](https://arxiv.org/abs/2208.03262)

$\Xi_b^- \rightarrow J/\psi \Lambda K^-$ amplitude analysis for pentaquark search
[Science Bulletin 66 \(2021\) 1278](https://www.sciencedirect.com/journal/science-bulletin)

$\Lambda_c^+ \rightarrow p K^- \pi^+$ amplitude analysis

- 2016 data, $\mathcal{L} = 0.5 \text{ fb}^{-1}$; $\sim 400\text{k}$ signals;
- Helicity-based Am.An.; Measure polarization, resonance fractions and decay parameters
- Large interference seen between different chains

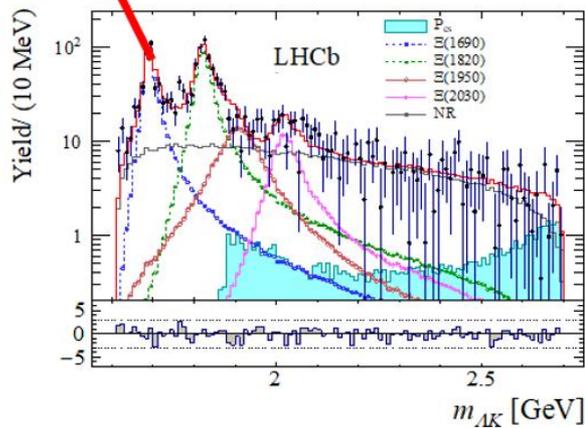


Large **interference** between $\Delta(1232)^{++}$ and $K^*(892)$

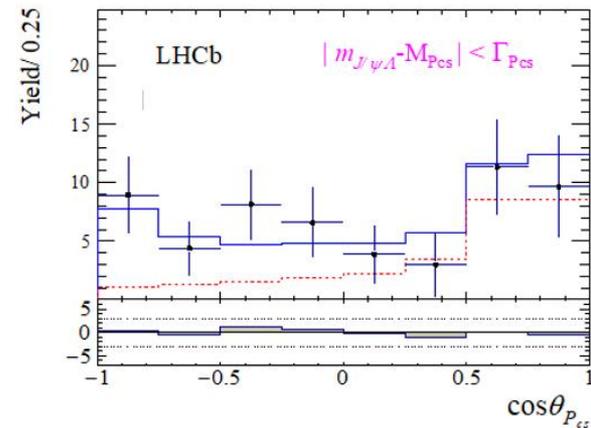
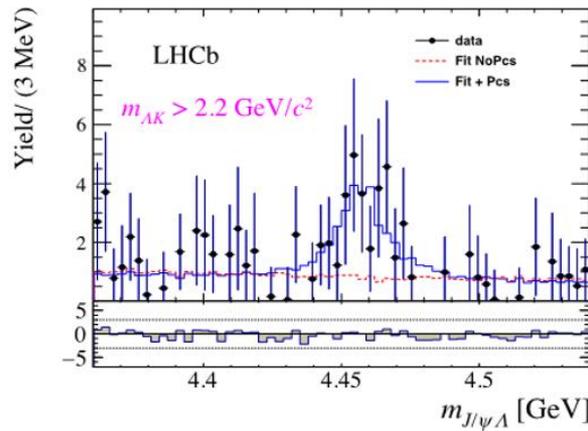
$\Xi_b^- \rightarrow J/\psi \Lambda K^-$ amplitude analysis

- Consider Λ as final-state particle, similar spin structure as $\Lambda_b^0 \rightarrow J/\psi p K^-$ decay
- Use same amplitude formalism, with alignment-issue fixed
 - **3. 1σ significance** when syst. uncertainty considered

Two Ξ_b^{*-} states



Zooms in to P_{CS} signal region for better visibility



P_{CS} mass 19MeV below the $\Xi_c^0 \bar{D}^{*0}$ threshold. Statistic not enough for J^P determination.

Dalitz-plot decomposition (DPD) formula

• $\mathcal{M} \sim \langle \text{init.} | \text{fin.} \rangle \sim \langle \text{init.} | \sum_i R_i \rangle \dots \langle \sum_i R_i | \text{fin.} \rangle$

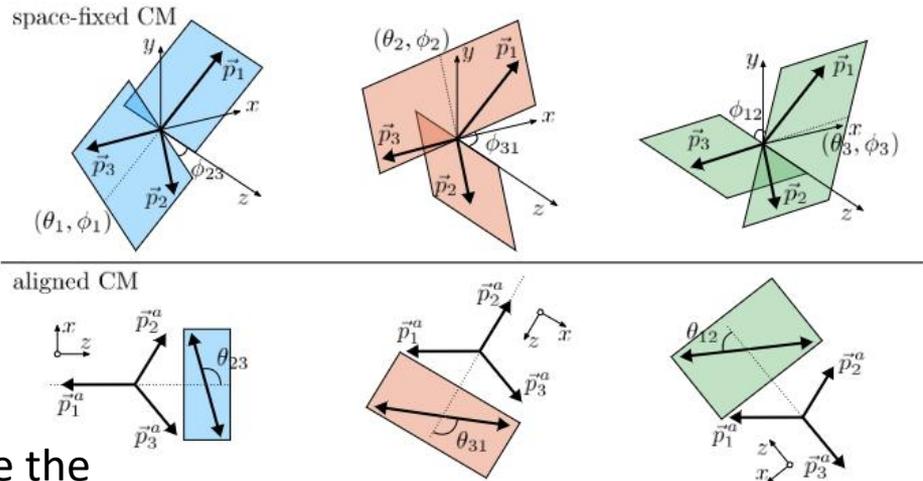
Wigner-D functions

Choice of intermediate spin state/frame not unique. Alternative choice: DPD formula

- DPD formula for 3-body decay
 - $0 \rightarrow 123$

An arbitrary initial spin frame

Same Euler rotation for all decay chains
(One Wigner-D function)



All momenta (spin-axis of helicity states) aligned to x-z plane; $\hat{p}_1 = -\hat{z}$

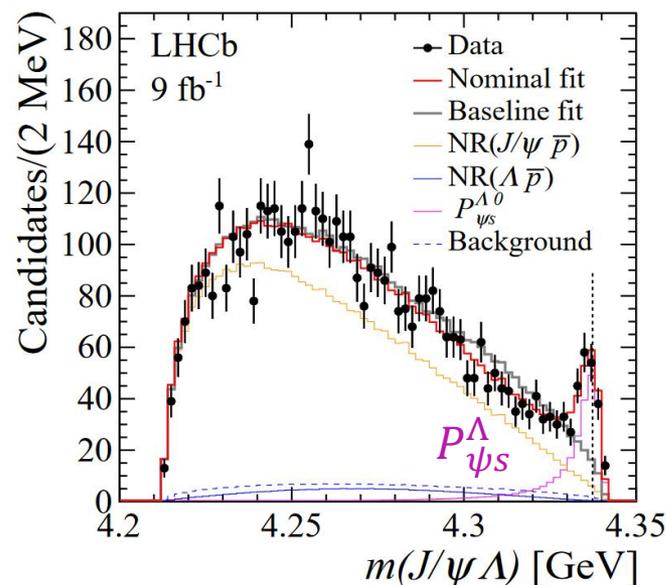
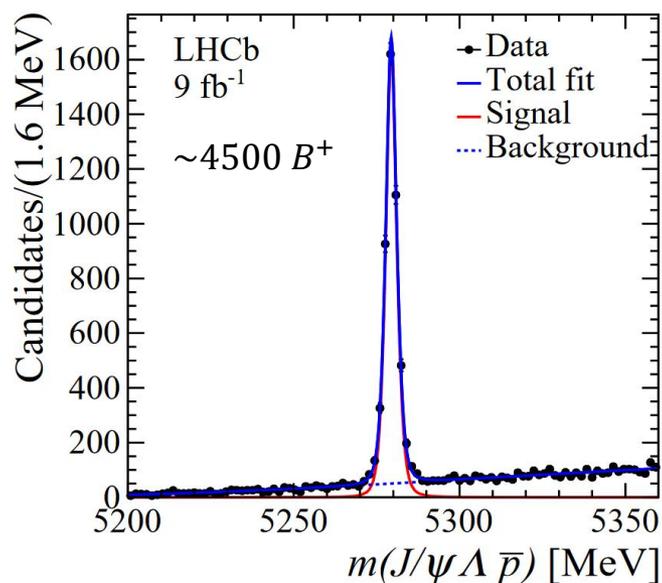
Use conventional helicity formula to write the rest part of amplitude

Phys. Rev. D 101 (2020) 034033

Angular variables can be derived using Dalitz-plot variables

Observation of $P_{\psi_S}^\Lambda(4338)$

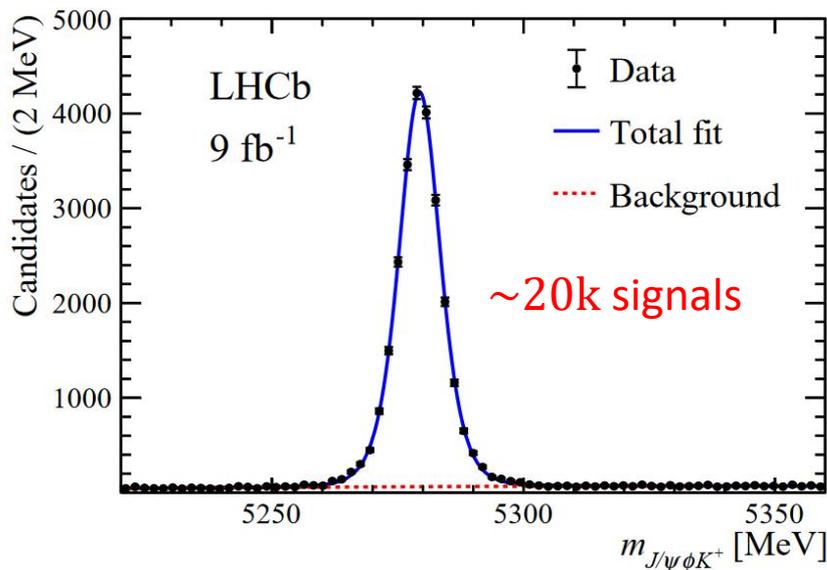
- Search for $J/\psi p$ and $J/\psi \Lambda$ states in $B^+ \rightarrow J/\psi p \bar{\Lambda}$
 - B^+ is spin-zero. 1st Euler rotation is a constant term
 - 2D Dalitz amplitude for 3-body B^+ decay (DPD) [arXiv:2210.10346; supplemental A](#)
 - 2D amplitude of $J/\psi \rightarrow \mu^+ \mu^-$ + 2D amplitude of $\Lambda \rightarrow p \pi$
- 6D amplitude analysis on $\sim 4500 B^+ \rightarrow J/\psi p \bar{\Lambda}$ decays
 - $P_{\psi_S}^\Lambda$ significance $> 10\sigma$



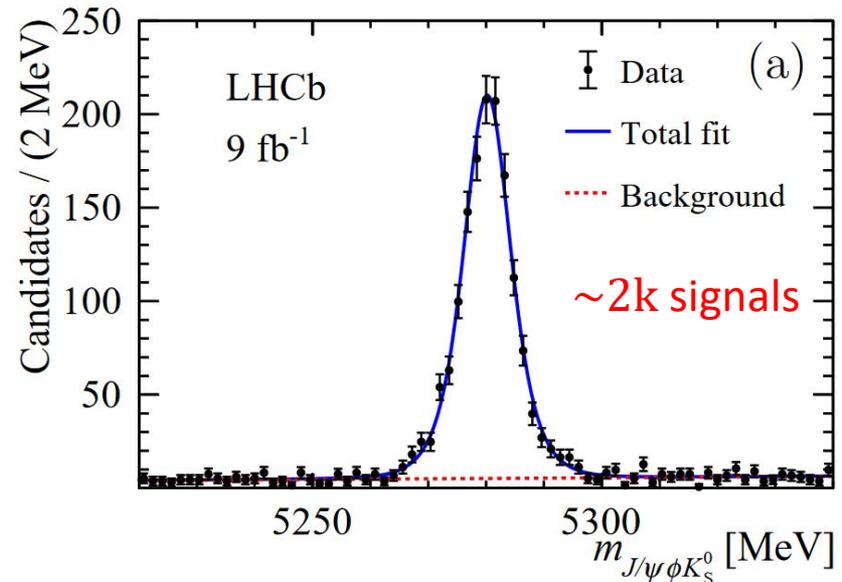
Speed up amplitude fits using GPUs

Study of $B^0 \rightarrow J/\psi K_S^0 \phi$ decay

- $T_{\psi s1}^\theta(4000)^+$ observed in $B^+ \rightarrow J/\psi K^+ \phi$ channel
- Search for its isospin partner in $B^0 \rightarrow J/\psi K_S^0 \phi$ decay
 - Joint amplitude fit using $B^+ \rightarrow J/\psi K^+ \phi$ and $B^0 \rightarrow J/\psi K_S^0 \phi$ events collected in LHCb Run1+Run2



[PRL 117 \(2021\) 082001](#)



[arXiv:2301.04899](#)

Construction of likelihood function

- To obtain a log-likelihood value:

$$\ln \mathcal{L} = \sum_i \left(\ln(1 - \beta) P_{i, \text{sig}}(\vec{\omega}) + \beta \underbrace{P_{i, \text{bkg}}}_{\text{Parameterized using sideband data}} \right)$$

Loop over all data events in signal region (~20k)

$$\text{Signal PDF: } P_{i, \text{sig}} = \frac{|\mathcal{M}_i(\vec{\omega})|^2 \times \Phi_i \times \epsilon_i}{I_{\text{norm}}(\vec{\omega})}$$

Loop over uniform phase-space MC events passing all event selections (400k)

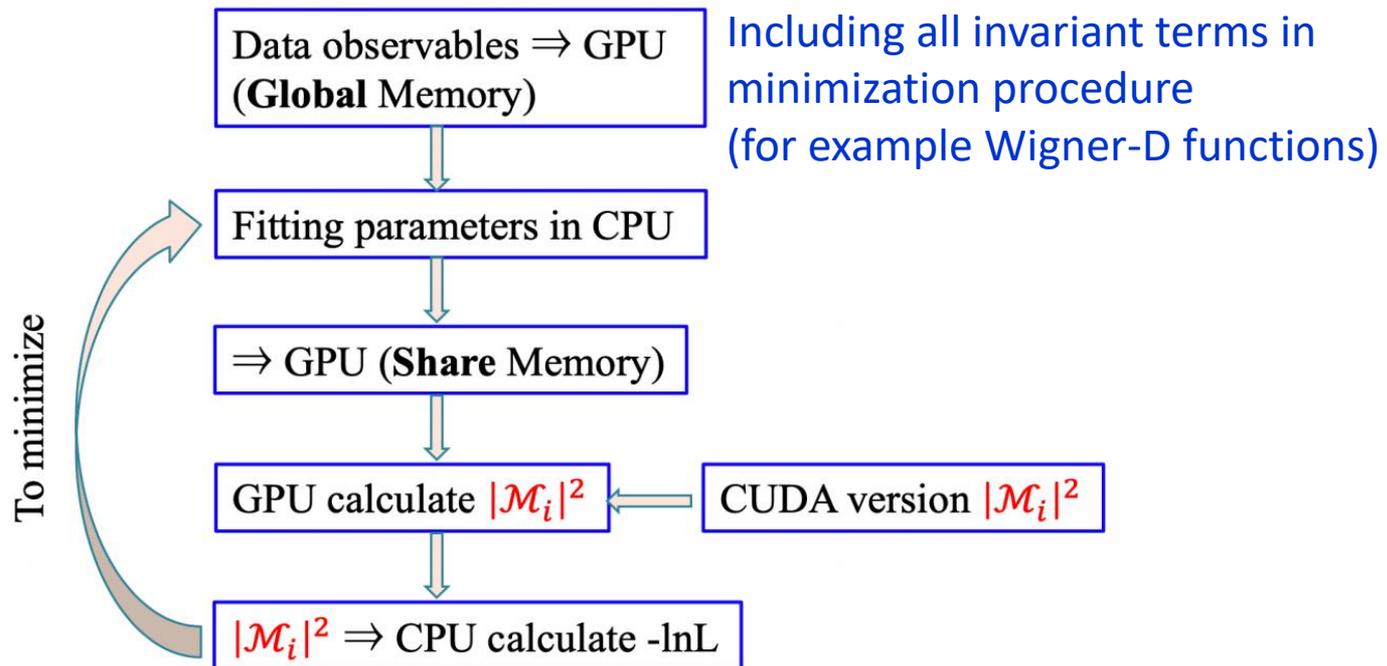
Norm. factor obtained numerically using MC: $I_{\text{norm}} = \sum_j |\mathcal{M}_j(\vec{\omega})|^2$

- Need to calculate matrix element for **~0.4M times**
- Amplitude computations for each data/MC events are independent on each other. Use GPUs to handle the them in parallel

CUDA + RooFit based framework

- **Idea: Let GPU to calculate $|\mathcal{M}_i|^2$ for events of both data and MC**
 - CUDA (GPU based C++) for computation of $|\mathcal{M}_i|^2$
 - CUDA memory transfers between CPU and GPU

Version 1



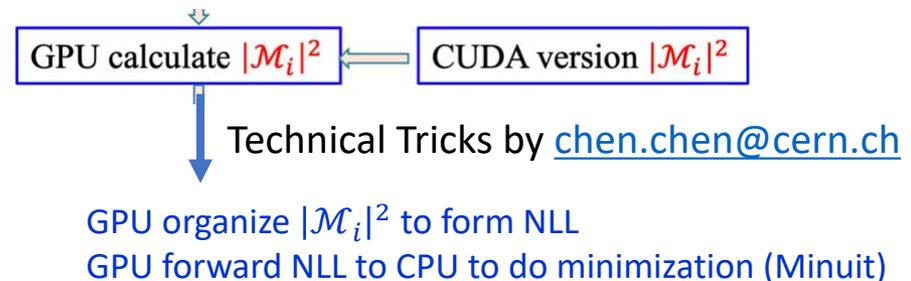
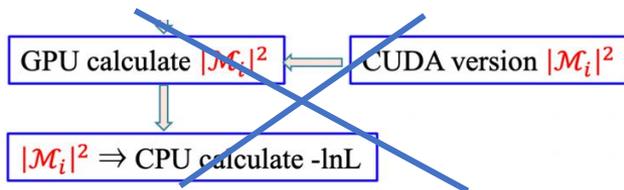
GPU type: RTA 3090

Optimization of the framework

- Optimization of the GPU sector zhihong.shen@cern.ch
 - Tools: [Nsight Systems](#) (nsys) and [Nsight Compute](#) (ncu) by Nvidia

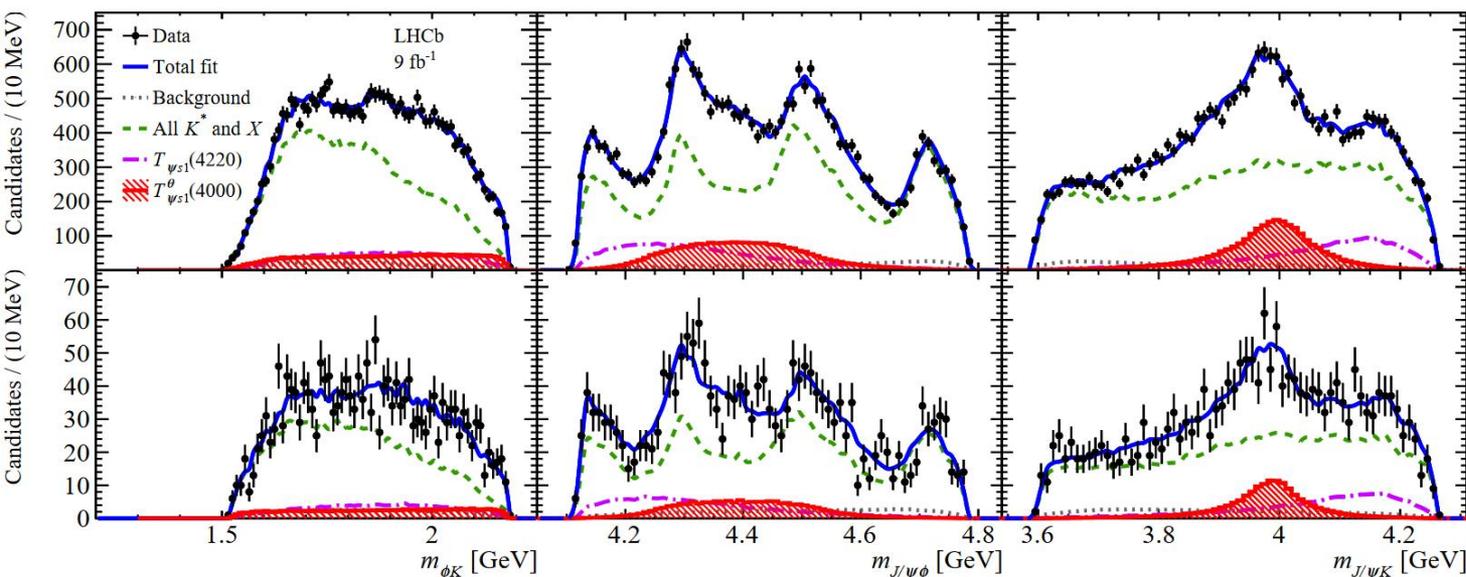
Methods	Impact on GPU time calculating one log-likelihood value
Malloc once and reuse the memory	8.8ms -> 7.7ms
Double -> Float	7.7ms -> 3.7ms
Use less registers	3.7ms -> 3.4ms
Reduce branch structure	3.4ms -> 2.6ms

- Re-organize the task of GPU and CPU
 - CPU part start to dominate the time consumption



Performance & achievement

- ~ 10 mins to run an amplitude fit
 - Even fast enough for toy studies with hundreds of fits needed
- Physics result



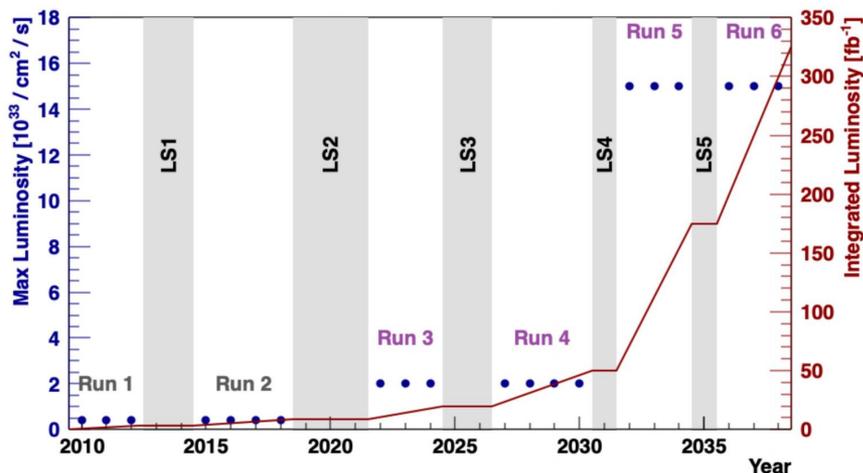
- Evidence of $T_{\psi s 1}^\theta(4000)^0$ seen in $J/\psi K_S^0$ system ($\sim 4\sigma$)
- Mass, width consistent with $T_{\psi s 1}^\theta(4000)^+$ isospin partner

Summary

Summary

- LHCb has made a great contribution to hadron spectroscopy studies, and is smoothly boosting the field to a new level

More & more high-quality data is coming.
Improved stat. precision



Stay tuned 😊

Thank you for your attention !

To persist the **ability of handling the ever larger** data flow:

*Improved trigger system, [Real-Time Analysis](#)
Advanced software tools for [Data Processing and Analysis](#)*

Example in this talk:

Use GPUs to speed up amplitude analysis

Develop & use **new phenomenological models** in data analysis, minimize relevant systematic uncertainties, to match the ever better stat. precision

Example in this talk:

Development of the general formalism for helicity amplitudes

Back up

Dalitz-plot decomposition (DPD) formula

- Split the amplitude into different sectors featuring different aspects of the decays
 - Example: $\Lambda_b^0 \rightarrow J/\psi p K^-$ amplitude

$$(M_{\lambda,\xi}^\Lambda)_{\text{LHCb}} = \sum_{\nu,\mu} D_{\Lambda,\nu}^{J*}(\phi_1, \theta_1, \phi_{23}) \quad \text{Shared by } P_c, \Lambda^* \text{ chains} \quad \text{Dalitz-variable-dependent amplitude } \mathcal{M}_{P_c} + \mathcal{M}_{\Lambda^*}, \text{ dominate the interference behavior}$$

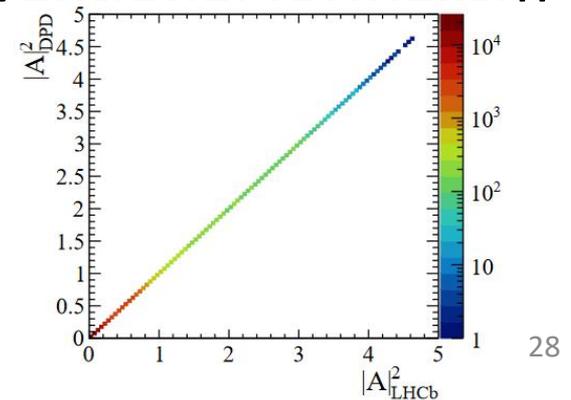
$$\begin{aligned} & \times \left(\sum_s \sum_\tau \sqrt{2} n_s d_{\nu,\tau-\mu}^{1/2}(0) H_{\tau,\mu}^{0 \rightarrow (23),1} X_s(\sigma_1) d_{\tau,\lambda}^s(\theta_{23}) H_{\lambda,0}^{(23) \rightarrow 2,3} \quad \Lambda^* \text{ chain} \right. \\ & \left. + \sum_s \sum_{\tau,\mu',\lambda'} \sqrt{2} n_s d_{\nu,\tau}^{1/2}(\hat{\theta}_{3(1)}) H_{\tau,0}^{0 \rightarrow (12),3} X_s(\sigma_3) d_{\tau,\mu'-\lambda'}^s(\theta_{12}) H_{\mu',\lambda'}^{(12) \rightarrow 1,2} d_{\lambda'\lambda}^{1/2}(\zeta_{3(1)}^2) d_{\mu'\mu}^1(\zeta_{3(1)}^1) \right) P_c \text{ chain} \end{aligned}$$

$$\times \sqrt{3} e^{i\mu(\phi_{23} + \phi'_+)} d_{\mu\xi}^1(\theta_+) H_{\lambda_+,\lambda_-}^{1 \rightarrow \mu^+,\mu^-}, J/\psi \rightarrow \mu^+ \mu^- \text{ decay amplitude shared by two chains}$$

- A good agreement found with the conventional formalism

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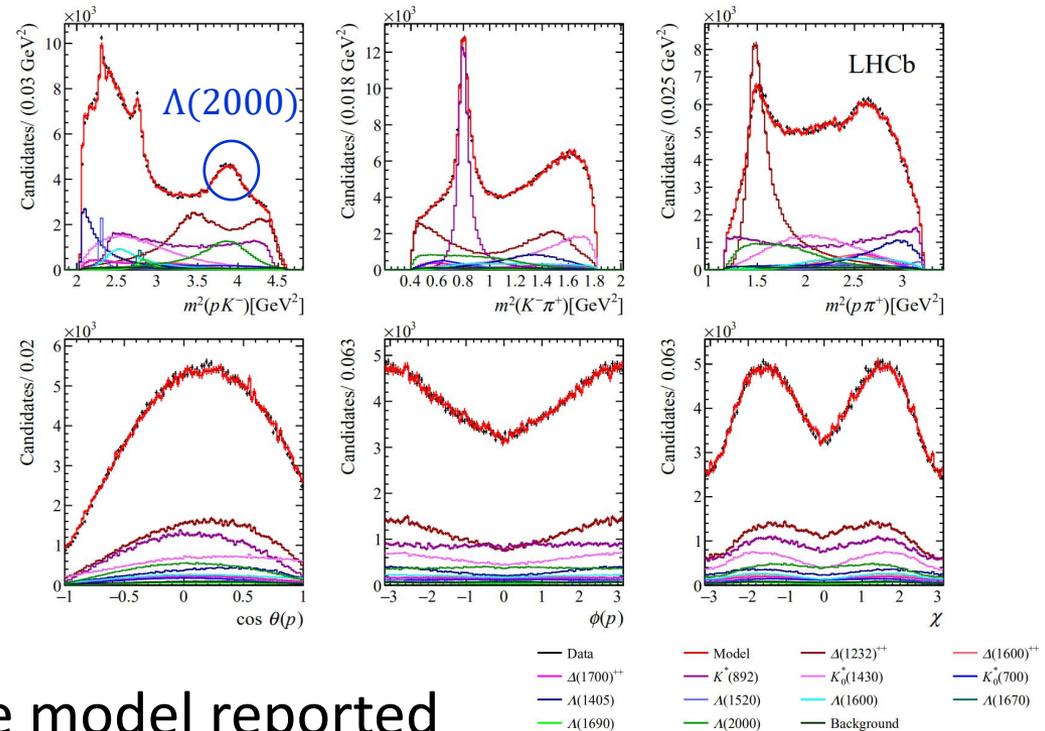
DPD V.S. conventional helicity formula



$\Lambda_c^+ \rightarrow p K^- \pi^+$ amplitude analysis

- 2016 data, $\mathcal{L} = 0.5\text{fb}^{-1}$; $\sim 400\text{k}$ signals; helicity-based Am.An.

Resonance	J^P	Mass (MeV)	Width (MeV)
$\Lambda(1405)$	$1/2^-$	1405.1	50.5
$\Lambda(1520)$	$3/2^-$	1515 – 1523	10 – 20
$\Lambda(1600)$	$1/2^+$	1630	250
$\Lambda(1670)$	$1/2^-$	1670	30
$\Lambda(1690)$	$3/2^-$	1690	70
$\Lambda(2000)$	$1/2^-$	1900 – 2100	20 – 400
<hr/>			
$\Delta(1232)^{++}$	$3/2^+$	1232	117
$\Delta(1600)^{++}$	$3/2^+$	1640	300
$\Delta(1700)^{++}$	$3/2^-$	1690	380
<hr/>			
$K_0^*(700)$	0^+	824	478
$K^*(892)$	1^-	895.5	47.3
$K_0^*(1430)$	0^+	1375	190



- All parameters of amplitude model reported
- Mass and width of $\Lambda(2000)$ determined

$$m = 1988 \pm 2 \pm 21 \text{ MeV}$$

$$\Gamma = 179 \pm 4 \pm 16 \text{ MeV}$$

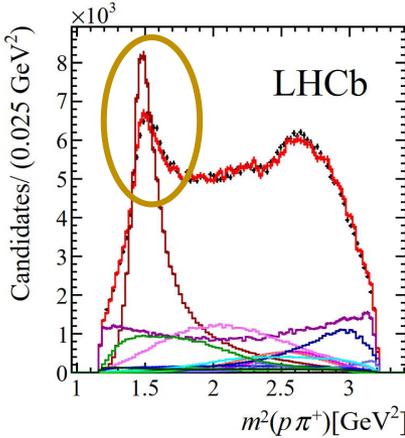
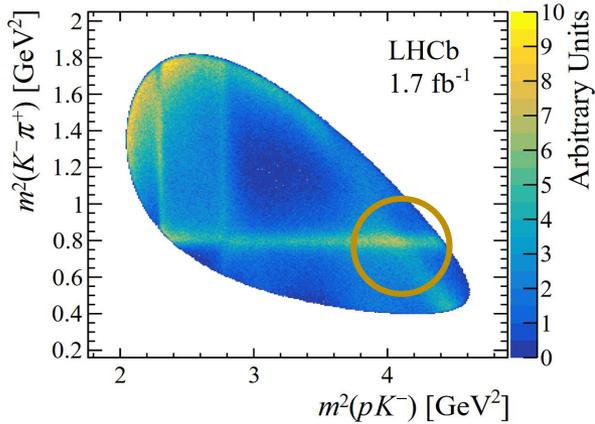
Λ_c^+ polarization measurement

$$p(\Omega, \mathbf{P}) = \frac{1}{\mathcal{N}} \sum_{m_p=\pm 1/2} \left\{ (1 + P_z) |\mathcal{A}_{1/2, m_p}(\Omega)|^2 + (1 - P_z) |\mathcal{A}_{-1/2, m_p}(\Omega)|^2 + 2\text{Re} \left[(P_x - iP_y) \mathcal{A}_{1/2, m_p}^*(\Omega) \mathcal{A}_{-1/2, m_p}(\Omega) \right] \right\}$$

Final-state kinematics

Initial spin structure of Λ_c^+

- Large interference seen between different chains



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Large interference between $\Delta(1232)^{++}$ and $K^*(892)$

Λ_c^+ polarization from semileptonic b -decays measured, with 2 different definitions of initial spin axis

Model dependency contributes to the **largest syst. uncertainty** (second term)

Component	Value (%)
$P_x (lab)$	$60.32 \pm 0.68 \pm 0.98 \pm 0.21$
$P_y (lab)$	$-0.41 \pm 0.61 \pm 0.16 \pm 0.07$
$P_z (lab)$	$-24.7 \pm 0.6 \pm 0.3 \pm 1.1$
$P_x (\tilde{B})$	$21.65 \pm 0.68 \pm 0.36 \pm 0.15$
$P_y (\tilde{B})$	$1.08 \pm 0.61 \pm 0.09 \pm 0.08$
$P_z (\tilde{B})$	$-66.5 \pm 0.6 \pm 1.1 \pm 0.1$