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# Recent and ongoing studies from the A2 Collaboration at MAMI

Hadron Conference 2023

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scattering:

## Study of the nucleon structure and properties



#### Baryon spectroscopy





Sum rules

Fundamental relations between photon absorption and scattering:

- $GDH^* = \frac{1}{2\pi^2} \int_0^\infty d\nu \frac{(\sigma_P(\nu) \sigma_A(\nu))}{\nu} = \frac{\alpha}{M^2}$
- Baldin

$$\alpha_{E1} + \beta_{M1} = \frac{1}{2\pi^2} \int_0^\infty d\nu$$

• GGT\*  

$$\gamma_0 = \frac{1}{4\pi^2} \int_0^\infty d\nu \frac{(\sigma_P(\nu) - \sigma_A(\nu))}{\nu^3}$$



#### Compton scattering





\* Gerasimov-Drell-Hearn

\* Gell-Mann, Goldberger, and Thirring





A2

- 4-stage microtron
- Continuous polarized or unpolarized electron beam
- $I_{e^-}^{\max} = 20 \ \mu A \text{ or } 100 \ \mu A \text{ (pol/unpol)}$
- + Linac & 3 RTMs (MAMI B) ightarrow 883 MeV
- $\cdot$  HDSM (MAMI C)  $\rightarrow$  1604 MeV



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A2 setup





#### Photon tagging system





#### Tagger

A2 setup





## Target



#### Unpolarized target:



- Liquid hydrogen target (LH<sub>2</sub>)
- 10 cm long cell
- T = 20 K

### Target



#### Unpolarized target:



- Liquid hydrogen target (LH<sub>2</sub>)
- 10 cm long cell
- T = 20 K

#### Polarized target:



- Butanol (C<sub>4</sub>H<sub>9</sub>OH)
- 2 cm long cell
- T = 25 mK
- Polarization > 90%
- Relaxation time > 1000 h

#### **Detection** apparatus





#### **Multiwire Proportional Chambers**

Precise charged tracking/positioning  $\sigma_\theta \sim 2^\circ$ 

$$\sigma_{\phi}\sim 3^{\circ}$$



CB Energy







- probe to understand pQCD
- access to the different degree of freedoms of the nucleon



- probe to understand pQCD
- · access to the different degree of freedoms of the nucleon

A good tool to access baryon resonance is  $\gamma N \rightarrow \pi(\eta)N$ :

- Electromagnetic (EM) vertex is fully understood
- 4 matrix elements are needed to fully describe it
- To fully disentangle and access all possible states, different observables has to be measured

Beam		Target		Recoil		Both		
		Х	у	Ζ			)	<
					X'	Ζ'	X'	Ζ'
Unpolarized	σ		Т				$T_{X'}$	$T_{z'}$
Linear	Σ	Н	Р	G	$O_{X'}$	$O_{Z'}$	$L_{Z'}$	$L_{X'}$
Circular		F		Ε	$C_{X'}$	$C_{z'}$		



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Beam		Т	arge	et	Red	coil	Bc	oth
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Unpolarized	$\sigma$		Т				$T_{X'}$	$T_{Z'}$
Linear	Σ	Н	Р	G	$O_{X'}$	$O_{Z'}$	$L_{z'}$	$L_{X'}$
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Measured or planned at A2



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- EM iterations do not conserve isospin. One needs to measure both proton and neutron targets to access the full isospin decomposition
- Light nuclei (deuterium) are used as effective neutron target. Nuclear effects corrections needed to unambiguously extract the free-neutron information

## Helicity dependent $ec{\gamma}ec{p} ightarrow p\pi^0$ cross section in the $\Delta($ 1232) region







Significant improvement both in statistics and quality compared to existing data!

The determination of the quadrupole strength E2 in the  $\gamma N \rightarrow \Delta$  transition gives fundamental information on the proton structure

$$_{EM} = \frac{E_2}{M_1} = \frac{E_{1+}^{3/2}}{M_{1+}^{3/2}} = \frac{IM \left[ E_{1+}^{3/2} \right]}{IM \left[ M_{1+}^{3/2} \right]}$$

R

## Legendre fit to $\vec{\gamma}\vec{p} \rightarrow p\pi^0$ data in the $\Delta$ (1232) region





## Simultaneous measurement of double polarization E and G for $\gamma p ightarrow p \pi^0$



Elliptically polarized photons (long. pol. e<sup>-</sup> + diamond) and longitudinally polarized target:

$$\frac{d\sigma}{d\Omega}(\theta,\phi) = \frac{d\sigma}{d\Omega_0}(\theta) \left[1 - \frac{\mathsf{P}_{\mathsf{lin}}\cos(2(\alpha - \phi)) - \mathsf{P}_{\mathsf{z}}(-\mathsf{P}_{\mathsf{lin}}\mathsf{G}\sin(2(\alpha - \phi)) + \mathsf{P}_{\mathsf{circ}}\mathsf{E})\right]$$

- Excellent agreement between A2 (diamond) and CBELSA/TAPS (amorphous)
- Time and cost efficient measurement possible!

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## Unpolarized $\gamma p \rightarrow n \pi^0 \pi^+$ cross section



# First decomposition of all intermediate reaction states (full event-by-event kinematic reconstruction)

Precise diff. cross section also measured,

paper in preparation

## Helicity dependent $\vec{\gamma}\vec{p} \rightarrow n\pi^0\pi^+$ cross section





## Helicity dependent $\vec{\gamma}\vec{D} \rightarrow \gamma B(B = np \text{ or } d)$ cross section





PWA models for free p + free n

> Predicted decrease in cross-section (due to FSI) in the  $\Delta$ (1232) region is not sufficient to describe data

Precise diff. cross section also measured: F. Cividini et al. [A2], EPJA 58 113 (2022)







Nuclear model (A. Fix)

- W < 1300 MeV: phase space for QF production and nucleon p > 350 MeV is very small (large nuclear effects)
- W > 1300 MeV: use data to extract free neutron properties without (significant) model dependent corrections

Precise E on proton also measured: F. Cividini et al. [A2], EPJA 58 113 (2022)







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Accessing hadron internal structure — measuring unpolarized and polarized Compton scattering observables:

- Clear probe to understand non-pQCD
- Gives access to structure-dependent properties:
  - + scalar polarizabilities:  $\alpha_{\rm E1}$  and  $\beta_{\rm M1}$
  - spin polarizabilities:  $\gamma_{\text{E1E1}}, \gamma_{\text{M1M1}}, \gamma_{\text{M1E2}},$  and  $\gamma_{\text{E1M2}}$



 $\gamma(k) + P(q) \rightarrow \gamma(k') + P(q')$ 



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$$\gamma(k) + P(q) \rightarrow \gamma(k') + P(q')$$

#### Describe response of a nucleon to:

- External electric field  $\vec{p} = \alpha_{E1} \times \vec{E}$
- External magnetic field  $\vec{m} = \overrightarrow{\beta_{\rm M1}} \times \vec{H}$



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  - spin polarizabilities:  $\gamma_{\text{E1E1}}, \gamma_{\text{M1M1}}, \gamma_{\text{M1E2}}, \text{and } \gamma_{\text{E1M2}}$
- Contribute to 2 $\gamma$  exchange in  $\mu$ H Lamb shift



$$\gamma(k) + P(q) \rightarrow \gamma(k') + P(q')$$



## Compton scattering - Hamiltonian

 $\cdot$  Zeroth order: mass (m) and electric charge (e)

$$H_{\mathrm{eff}}^{(0)} = rac{ec{\pi}^2}{2m} + e\phi$$
 (where  $ec{\pi} = ec{p} - eec{\mathsf{A}}$ )

• First order: anomalous magnetic moment (k)

$$H_{\text{eff}}^{(1)} = -\frac{e(1+k)}{2m}\vec{\sigma}\cdot\vec{H} - \frac{e(1+2k)}{8m^2}\vec{\sigma}\cdot\left[\vec{E}\times\vec{\pi}-\vec{\pi}\times\vec{E}\right]$$

- Second order: scalar polarizabilities  $\alpha_{\rm E1}$  and  $\beta_{\rm M1}$ 

$$H_{\rm eff}^{(2)} = -4\pi \left[\frac{1}{2} \boldsymbol{\alpha}_{\rm E1} \vec{E}^2 + \frac{1}{2} \boldsymbol{\beta}_{\rm M1} \vec{H}^2\right]$$

- Third order: spin polarizabilities  $\gamma_{\rm E1E1},\,\gamma_{\rm M1M1},\,\gamma_{\rm M1E2}$  and  $\gamma_{\rm E1M2}$ 

$$\begin{aligned} H_{\text{eff}}^{(3)} &= -4\pi \left[ \frac{1}{2} \gamma_{\text{E1E1}} \vec{\sigma} \cdot (\vec{E} \times \dot{\vec{E}}) + \frac{1}{2} \gamma_{\text{M1M1}} \vec{\sigma} \cdot (\vec{H} \times \dot{\vec{H}}) \right. \\ &\left. - \gamma_{\text{M1E2}} E_{ij} \sigma_i H_j + \gamma_{\text{E1M2}} H_{ij} \sigma_i E_j \right] \end{aligned}$$

# A2

#### Theory needed:

- Dispersion Relation (DR)
- Chiral Perturbation Theory ( $\chi$ PT)

They can be used to fit Compton scattering data

#### Results on the beam asymmetry $\Sigma_3$

Beam asymmetry:

PARALLEL

PERPENDICULAR

X

X

 $\Sigma_3 = rac{\mathsf{d}\sigma_{\parallel} - \mathsf{d}\sigma_{\perp}}{\mathsf{d}\sigma_{\parallel} + \mathsf{d}\sigma_{\perp}}$ 



#### Results on the unpolarized cross-section





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- Only new data used as input
- Systematic errors included as normalization factor (S) for each individual data set
- Baldin sum rule constraint added as an additional point with its error

$$\alpha_{E1} + \beta_{M1} = \int_{\omega_0}^{\infty} d\omega \frac{\sigma_{tot}(\omega)}{\omega^2} = 13.8 \pm 0.4$$

V. Olmos de León et al., Eur Phys J A **10**, 207 (2001)



- Only new data used as input
- Systematic errors included as normalization factor (S) for each individual data set
- Baldin sum rule constraint added as an additional point with its error
- Spin polarizabilities fixed to the most recent experimental evaluation
- Scalar polarizabilities always in units of 10<sup>-4</sup> fm<sup>3</sup>

$$\chi^{2}(\mathcal{P}) = \sum_{j}^{N_{sets}} \left( \sum_{i}^{N_{pt}^{j}} \left( \frac{S_{j}O_{ij}^{exp} - O_{ij}^{thr}(\mathcal{P})}{S_{j}\Delta O_{ij}^{exp}} \right)^{2} + \left( \frac{S_{j} - 1}{\Delta S_{j}} \right)^{2} \right)$$



E. Mornacchi (A2), Phys. Rev. Lett. 128, 132503 (2022)

	HDPV	BChPT	HBChPT
$\alpha_{E1}$	$11.23 \pm 0.49$	$10.65\pm0.50$	$11.10\pm0.52$
$\beta_{M1}$	$2.79\pm0.32$	$3.28\pm0.33$	$3.36\pm0.38$
Sσ	$1.011\pm0.015$	$1.013\pm0.015$	$1.043 \pm 0.016$
SΣ	$0.994\pm0.015$	$0.996\pm0.015$	$1.001\pm0.015$
$\chi^2/DOF$	82.10/93 = 0.89	82.96/93 = 0.89	83.16/93 = 0.89

$$\begin{split} \alpha_{E1} &= 10.99 \pm 0.16_{\text{stat.}} \pm 0.47_{\text{sys.}} \pm 0.17_{\gamma_{\text{S}}} \pm 0.34_{\text{mod.}} \\ \beta_{\text{M1}} &= 3.14 \pm 0.21_{\text{stat.}} \pm 0.24_{\text{sys.}} \pm 0.20_{\gamma_{\text{S}}} \pm 0.35_{\text{mod.}} \end{split}$$





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SΣ	$0.994\pm0.015$	$0.996\pm0.015$	$1.001\pm0.015$
$\chi^2/{ m DOF}$	82.10/93 = 0.89	82.96/93 = 0.89	83.16/93 = 0.89

- Highest precision Compton scattering data set below  $\pi$ -photoproduction threshold!
- Precise extraction of the scalar polarizabilities from one single data set





- Using all available datasets as input: 25 datasets, 388 data points
- All six polarizabilities are treated as free parameters
- Parametric bootstrap technique needed to include all possible sources of systematic uncertainties:

$$e_{i,j}^{(0)} \rightarrow e_{i,j}^{(b)} = (1 + \delta_{j,b})(e_{i,j}^{(0)} + r_{i,j,b}\sigma_{i,j}^{(0)})$$

- inclusion of common systematic uncertainties without any *a priori* distribution assumption
- $\cdot$  probability distribution of the fit parameters obtained by the procedure
- uncertainties on nuisance model parameters are taken into account in the sampling procedure
- + fit p-value is provided if goodness-of-fit distribution is not given by the  $\chi^2$

#### Extracting all the six leading-order polarizabilities





E. Mornacchi et al., Phys. Rev. Lett. 129, 102501 (2022)

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## Extracting all the six leading-order polarizabilities





- First simultaneous & self-consistent extraction of the six static proton polarizabilities
- Errors competitive with the existing extractions obtained with constraints

E. Mornacchi et al., Phys. Rev. Lett. 129, 102501 (2022)

## Conclusions



A2 Collaboration has an intensive program to study the nucleon internal structure! Photon absorption

	$p\pi^{0} \gamma p \rightarrow p\pi^{-}\pi$
25	$y \rightarrow p\eta' \rightarrow \gamma p \rightarrow p$

- High precision data measured for different final states and observables
- Simultaneous measurement of *E* and *G* thanks to elliptical polarization
- Relevant improvement to different PWAs

## Conclusions



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(in the second s	p = 0.00 p = p = 0.00 p = p = 0.00 p = p = 0.00 p =
	$\gamma p \rightarrow p \eta^{*} \rightarrow \gamma p \rightarrow \eta^{*}$

#### Photon scattering



- High precision data measured for different final states and observables
- Simultaneous measurement of *E* and *G* thanks to elliptical polarization
- Relevant improvement to different PWAs
- Highest statistics Compton scattering data set below  $\pi$ -threshold published
- First concurrent extraction of the six LO proton polarizabilities
- New physics program on neutron planned in A2 with improved detector system

#### Many more results expected in the next few years. Stay tuned!

## Conclusions



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