

Molecular Ω_{cc} , Ω_{bc} and Ω_{bb} states.

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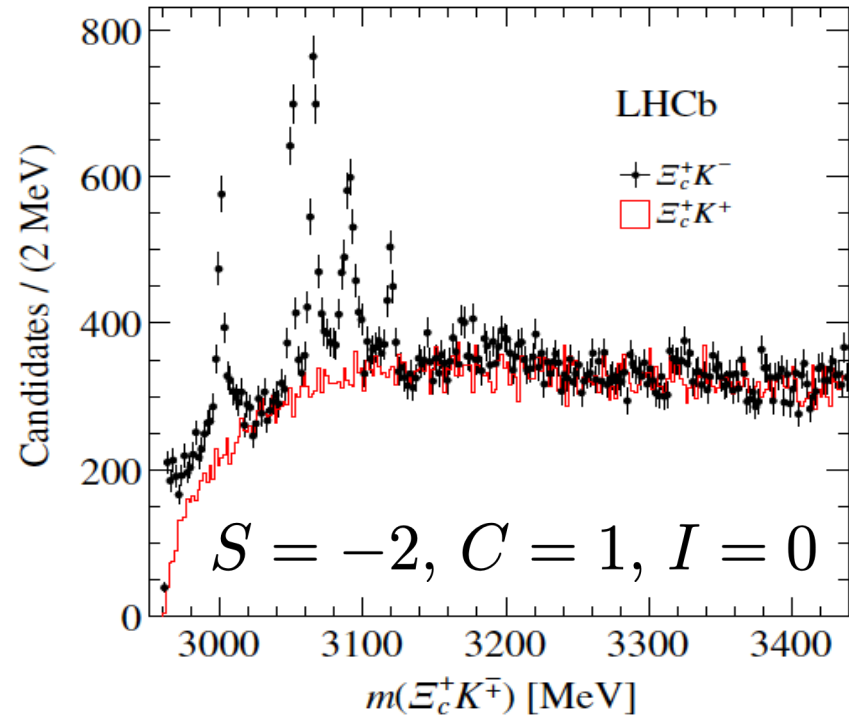
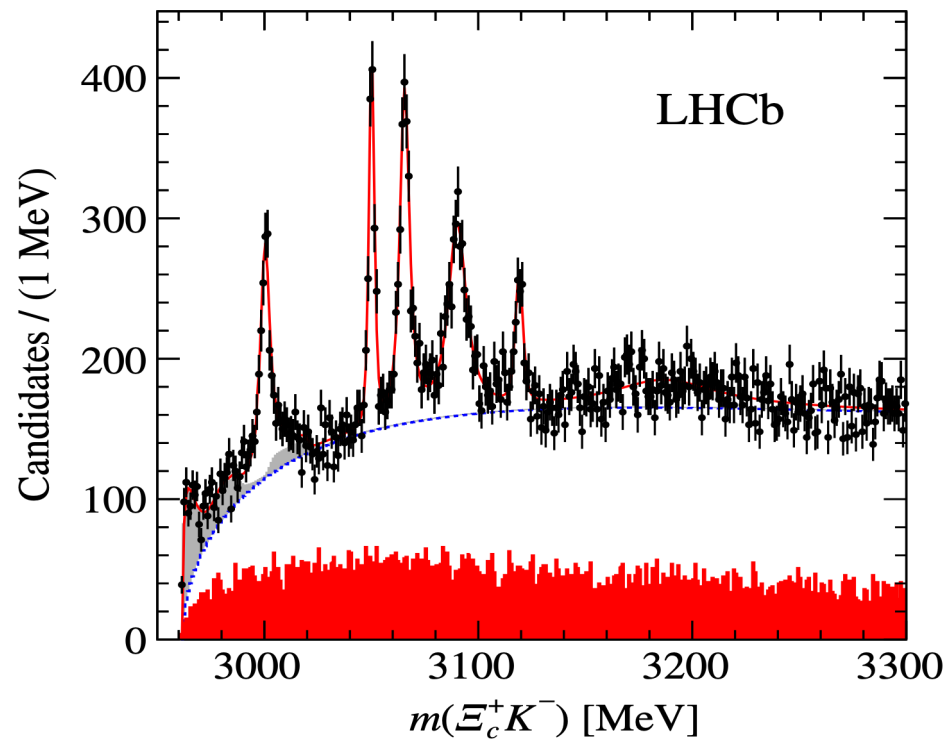
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Introduction: Historical Background (Ω_c states)

The new Ω_c' s observed at LHCb:

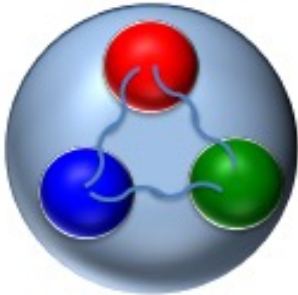
R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 118, 182001 (2017).



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Introduction: Historical Background (Ω_c states)

Constituent Quark Models (CQMs) interpretation:



- Bound states consisting of 1 heavy quark (c) and a P-wave (ss) diquark. (System that gives 5 possible combinations)

$$S_c = \frac{1}{2}, S_{ss} = 1 + L_{ss} = 1 \rightarrow J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$$

M. Karliner and J. L. Rosner, Phys. Rev. D 95, no.11, 114012 (2017).

W. Wang and R. L. Zhu, Phys. Rev. D 96, no.1, 014024 (2017).

Z. G. Wang, Eur. Phys. J. C 77, no.5, 325 (2017).

B. Chen and X. Liu, Phys. Rev. D 96, no.9, 094015 (2017).

- Alternative interpretation: some states (the 3 lightest ones) remain with (ss) diquark with 1P orbital excitation and the others with 2S radial excitations.

$$J^P = \frac{3}{2}^-, \frac{5}{2}^-, \frac{1}{2}^+, \frac{3}{2}^+$$

S. S. Agaev, K. Azizi and H. Sundu, EPL 118, no.6, 61001 (2017).

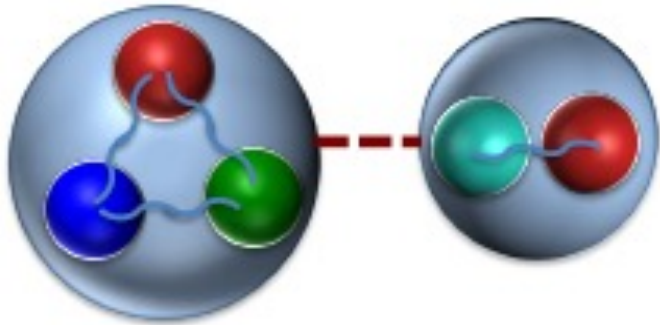
S. S. Agaev, K. Azizi and H. Sundu, Eur. Phys. J. C 77, no.6, 395 (2017).

H. Y. Cheng and C. W. Chiang, Phys. Rev. D 95, no.9, 094018 (2017).

K. L. Wang, L. Y. Xiao, X. H. Zhong and Q. Zhao, Phys. Rev. D 95, no.11, 116010 (2017).

Introduction: Historical Background (Ω_c states)

What about a molecular interpretation of these states?



R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 118, 182001 (2017).

| Resonance | Mass (MeV) | Γ (MeV) |
|--------------------|--|-----------------------|
| $\Omega_c(3000)^0$ | $3000.4 \pm 0.2 \pm 0.1^{+0.3}_{-0.5}$ | $4.5 \pm 0.6 \pm 0.3$ |
| $\Omega_c(3050)^0$ | $3050.2 \pm 0.1 \pm 0.1^{+0.3}_{-0.5}$ | $0.8 \pm 0.2 \pm 0.1$ |
| | | <1.2 MeV, 95% C.L. |
| $\Omega_c(3066)^0$ | $3065.6 \pm 0.1 \pm 0.3^{+0.3}_{-0.5}$ | $3.5 \pm 0.4 \pm 0.2$ |
| $\Omega_c(3090)^0$ | $3090.2 \pm 0.3 \pm 0.5^{+0.3}_{-0.5}$ | $8.7 \pm 1.0 \pm 0.8$ |
| $\Omega_c(3119)^0$ | $3119.1 \pm 0.3 \pm 0.9^{+0.3}_{-0.5}$ | $1.1 \pm 0.8 \pm 0.4$ |
| | | <2.6 MeV, 95% C.L. |

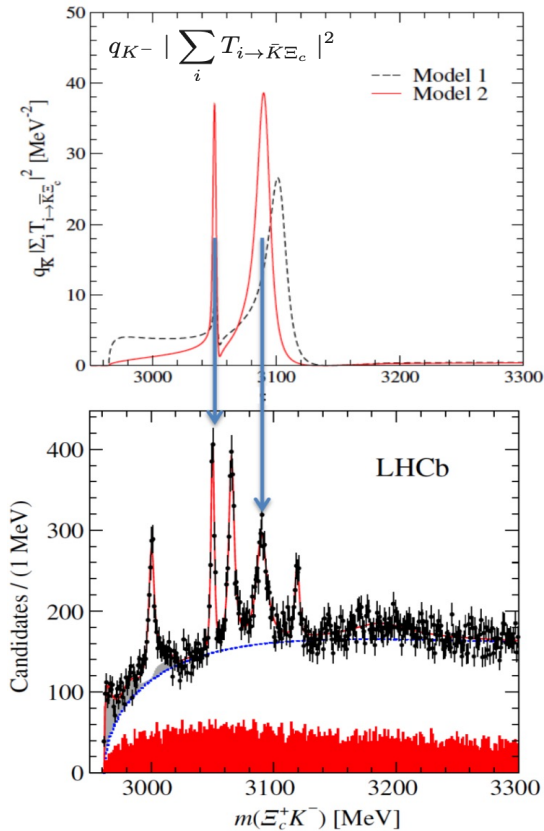
- The $\bar{K}\Xi_c$ (2964 MeV) and $\bar{K}\Xi'_c$ (3070 MeV) thresholds are within the energy range where the physical Ω_c states pop up!!!
- Prior to the experimental measurement, some theoretical works predicted some states in this sector :
 1. SU(8) spin-flavor sym. Model \rightarrow 5 states much more bound than the LHCb ones. O. Romanets et al., Physical. Rev. D85,114032 (2012)
 2. SU(4) finite range Model
 J. Hofmann and M.F.M. Lutz, Nucl. Phys. A 763, 90-139 (2005) \rightarrow 3 states below 2953 MeV
 C. E. Jimenez-Tejero, A. Ramos and I. Vidaña, Phys. Rev. C 80, 055206 (2009) \rightarrow 3 states, one at 3117 MeV ($\Gamma = 16$ MeV)!!!

Introduction: Historical Background (Ω_c states)

Molecular-Picture Models revisited

G. Montaña, A. F. and A. Ramos, Eur. Phys. J. A 54, no.4, 64 (2018)

Ω_c states dynamically generated by the s-wave interaction between a pseudoscalar meson and a ground state baryon:



$0^- \oplus \frac{1}{2}^+$ interaction in the $(I, S, C) = (0, -2, 1)$ sector

| | Model 1 | | | |
|------------------------|---------|----------------|---------|----------------|
| M [MeV] | 3051.6 | | 3103.3 | |
| Γ [MeV] | 0.45 | | 17 | |
| | $ g_i $ | $-g_i^2 dG/dE$ | $ g_i $ | $-g_i^2 dG/dE$ |
| $\bar{K} \Xi_c(2964)$ | 0.11 | 0.00 + i 0.00 | 0.58 | 0.01 + i 0.03 |
| $\bar{K} \Xi_c'(3070)$ | 1.67 | 0.54 + i 0.01 | 0.30 | 0.01 - i 0.01 |
| $D \Xi(3189)$ | 1.10 | 0.05 - i 0.01 | 4.08 | 0.90 - i 0.05 |
| $\eta \Omega_c(3246)$ | 2.08 | 0.23 + i 0.00 | 0.44 | 0.01 + i 0.01 |
| $\eta' \Omega_c(3656)$ | 0.04 | 0.00 + i 0.00 | 0.28 | 0.00 + i 0.00 |

The state at 3051 MeV mainly composed by $K \Xi_c'$ and $\eta \Omega_c$

The state at 3103 MeV is basically a $D \Xi$ bound state

→ 10 MeV too heavy and too wide...

Experimental states

$$\Omega_c(3050)^0 : M = 3050.2 \pm 0.1 \pm 0.1_{-0.5}^{+0.3} \text{ MeV},$$

$$\Gamma = 0.8 \pm 0.2 \pm 0.1 \text{ MeV},$$

$$\Omega_c(3090)^0 : M = 3090.2 \pm 0.3 \pm 0.5_{-0.5}^{+0.3} \text{ MeV},$$

$$\Gamma = 8.7 \pm 1.0 \pm 0.8 \text{ MeV}$$

Assuming this scheme, spin-parity can only be 1/2-!

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Introduction: Historical Background (Ω_c states)

Molecular-Picture Models revisited

V. R. Debastiani, J. M. Dias, W. H. Liang and E. Oset, Phys. Rev. D 97, no.9, 094035 (2018)

- Extension of the local hidden gauge approach with heavy-baryon states as a spectator c quark + sym. wave functions of the remaining light quarks
- Inclusion of pseudoscalar-decuplet baryon channels

→ Same 2 states with $J^P = \frac{1}{2}^-$ and a new $J^P = \frac{3}{2}^-$ Ω_c resonance which could be identified with the LHCb $\Omega_c(3119)$

J. Nieves, R. Pavao and L. Tolos, Eur. Phys. J. C 78, no.2, 114 (2018)

- $SU(6)_{\text{lf}} \times \text{HQSS}$ -extended WT meson-baryon interaction
- The symmetries automatically account for the additional presence of additional vector mesons and $3/2^+$ baryons

→ 2 states with $J^P = \frac{1}{2}^-$ and 1 $J^P = \frac{3}{2}^-$ state consistent with the experimental $\Omega_c(3000)$, $\Omega_c(3050)$ and $\Omega_c(3119)$

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Introduction: Historical Background (Ω_b states)

R. Aaij et al. [LHCb], Phys. Rev. Lett. 124, no.8, 082002 (2020)

| | δM_{peak} [MeV] | Mass [MeV] | Width [MeV] |
|--------------------|--------------------------------|--------------------------------------|-----------------------------|
| $\Omega_b(6316)^-$ | $523.74 \pm 0.31 \pm 0.07$ | $6315.64 \pm 0.31 \pm 0.07 \pm 0.50$ | < 2.8 (4.2) |
| $\Omega_b(6330)^-$ | $538.40 \pm 0.28 \pm 0.07$ | $6330.30 \pm 0.28 \pm 0.07 \pm 0.50$ | < 3.1 (4.7) |
| $\Omega_b(6340)^-$ | $547.81 \pm 0.26 \pm 0.05$ | $6339.71 \pm 0.26 \pm 0.05 \pm 0.50$ | < 1.5 (1.8) |
| $\Omega_b(6350)^-$ | $557.98 \pm 0.35 \pm 0.05$ | $6349.88 \pm 0.35 \pm 0.05 \pm 0.50$ | < 2.8 (3.2) |
| | | | $1.4^{+1.0}_{-0.8} \pm 0.1$ |

Predictions by Molecular-Picture Models:

- W. H. Liang, J. M. Dias, V. R. Debastiani and E. Oset, Nucl. Phys. B 930, 524 (2018)
7 Ω_b^- states were generated dynamically with 1/2- and 3/2- (lowest mass 50MeV above $\Omega_b^-(6350)$)
- W. H. Liang and E. Oset, Phys. Rev. D 101, no.5, 054033 (2020)
Arguments against the molecular nature of these states, instead structures at higher energies should be analysed
- J. Nieves, R. Pavao and L. Tolos, Eur. Phys. J. C 80, 22 (2020)
Prediction of a 1/2- state $\Omega_b^-(6360)$ as member of a sextet jointly with $\Xi_b(6227)$ and $\Sigma_b(6227)$
- G. Montaña, A. F. and A. Ramos, Eur. Phys. J. A 54, no.4, 64 (2018)
2 Ω_b^- states were generated dynamically with 1/2- (lowest mass 70MeV above $\Omega_b^-(6350)$)

Ω_{QQ} states

→ The plans of LHCb to measure Ω_{cc} , Ω_{bc} and Ω_{bb} states has motivated the present study.

Theoretical studies dedicated to this topic from different approaches:

- Quark Models

Mod. Phys. Lett. A 14, 135 (1999), Phys. Rev. D 66, 014008 (2002), Int. J. Mod. Phys. A 23, 2817 (2008)
Phys. Lett. B 683, 21 (2010), Phys. Rev. D 98, 094021 (2018), Chin. Phys. C 44, 013102 (2020)

...

- Lattice QCD

Phys. Rev. D 64, 094509 (2001), Phys. Rev. D 90, 094507 (2014)
Phys. Rev. D 94, 074003 (2016), Phys. Rev. D 98, 114505 (2018)

...

- QCD sum rules

Eur. Phys. J. A 45, 267 (2010), Chin. Phys. C 42, 123102 (2018)
Eur. Phys. J. C 78, 826 (2018)

...

- Other approaches

Phys. Rev. D 83, 056006 (2011), Phys. Rev. Lett. 115, 122001 (2015),
Phys. Rev. D 102, 014013 (2020), [Erratum: Phys.Rev.D 104, 059901 (2021),
Phys. Rev. D 104, 074027 (2021)

Ω_{QQ} states: Sectors with their corresponding meson-baryon basis

W. F. Wang, A. F., J. Song and E. Oset, arXiv:2208.14858 [hep-ph]

TABLE I: Threshold masses (in MeV) of different channels for Ω_{cc} .

| | | | | |
|--|-----------------------|-----------------------|---------------|--------------|
| $PB(\frac{1}{2}^+), J^P = \frac{1}{2}^-$ | $\Xi_{cc}\bar{K}$ | $\Omega_{cc}\eta$ | $\Xi_c D$ | $\Xi'_c D$ |
| | 4115 | 4263 | 4338 | 4448 |
| $PB(\frac{3}{2}^+), J^P = \frac{3}{2}^-$ | $\Xi_{cc}^*\bar{K}$ | $\Omega_{cc}^*\eta$ | $\Xi_c^* D$ | |
| | 4168 | 4320 | 4516 | |
| $VB(\frac{1}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-$ | $\Xi_{cc}\bar{K}^*$ | $\Omega_{cc}\omega$ | $\Xi_c D^*$ | $\Xi'_c D^*$ |
| | 4512 | 4495 | 4478 | 4588 |
| $VB(\frac{3}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$ | $\Xi_{cc}^*\bar{K}^*$ | $\Omega_{cc}^*\omega$ | $\Xi_c^* D^*$ | |
| | 4565 | 4552 | 4656 | |

TABLE II: Threshold masses (in MeV) of different channels for Ω_{bb} .

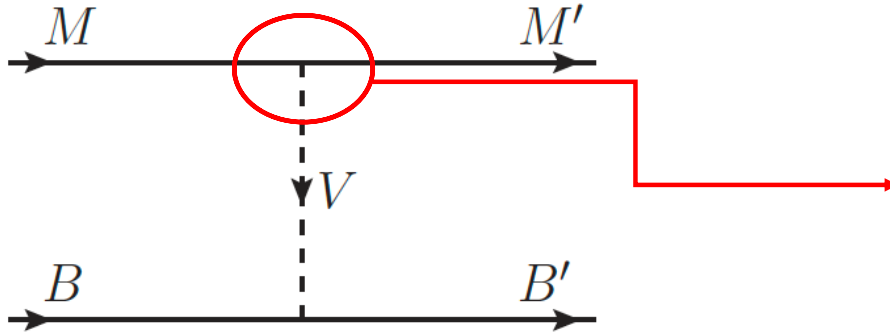
| | | | | |
|--|-----------------------|-----------------------|--------------------|-------------------|
| $PB(\frac{1}{2}^+), J^P = \frac{1}{2}^-$ | $\Xi_{bb}\bar{K}$ | $\Omega_{bb}\eta$ | $\Xi_b\bar{B}$ | $\Xi'_b\bar{B}$ |
| | 10833 | 10778 | 11076 | 11214 |
| $PB(\frac{3}{2}^+), J^P = \frac{3}{2}^-$ | $\Xi_{bb}^*\bar{K}$ | $\Omega_{bb}^*\eta$ | $\Xi_b^*\bar{B}$ | |
| | 10863 | 10806 | 11231 | |
| $VB(\frac{1}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-$ | $\Xi_{bb}\bar{K}^*$ | $\Omega_{bb}\omega$ | $\Xi_b\bar{B}^*$ | $\Xi'_b\bar{B}^*$ |
| | 11230 | 11010 | 11122 | 11260 |
| $VB(\frac{3}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$ | $\Xi_{bb}^*\bar{K}^*$ | $\Omega_{bb}^*\omega$ | $\Xi_b^*\bar{B}^*$ | |
| | 11260 | 11038 | 11277 | |

TABLE III: Threshold masses (in MeV) of different channels for Ω_{bc} .

| | | | | |
|--|-----------------------|-----------------------|---------------|--------------------|
| $PB(\frac{1}{2}^+), J^P = \frac{1}{2}^-$ | $\Xi_{bc}\bar{K}$ | $\Omega_{bc}\eta$ | $\Xi_b D$ | $\Xi_c\bar{B}$ |
| | 7415 | 7559 | 7667 | 7747 |
| $PB(\frac{1}{2}^+), J^P = \frac{1}{2}^-$ | $\Xi'_{bc}\bar{K}$ | $\Omega'_{bc}\eta$ | $\Xi'_b D$ | $\Xi'_c\bar{B}$ |
| | 7441 | 7595 | 7805 | 7857 |
| $PB(\frac{3}{2}^+), J^P = \frac{3}{2}^-$ | $\Xi_{bc}^*\bar{K}$ | $\Omega_{bc}^*\eta$ | $\Xi_b^* D$ | $\Xi_c^*\bar{B}$ |
| | 7466 | 7614 | 7822 | 7925 |
| $VB(\frac{1}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-$ | $\Xi_{bc}\bar{K}^*$ | $\Omega_{bc}\omega$ | $\Xi_b D^*$ | $\Xi_c\bar{B}^*$ |
| | 7812 | 7791 | 7807 | 7793 |
| $VB(\frac{1}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-$ | $\Xi'_{bc}\bar{K}^*$ | $\Omega'_{bc}\omega$ | $\Xi'_b D^*$ | $\Xi'_c\bar{B}^*$ |
| | 7838 | 7827 | 7945 | 7903 |
| $VB(\frac{3}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$ | $\Xi_{bc}^*\bar{K}^*$ | $\Omega_{bc}^*\omega$ | $\Xi_b^* D^*$ | $\Xi_c^*\bar{B}^*$ |
| | 7863 | 7846 | 7962 | 7971 |

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$$\mathcal{L}_{VPP} = -ig \langle [P, \partial_\mu P] V^\mu \rangle$$

$$\mathcal{L}_{VVV} = ig \langle (V^\mu \partial_\nu V_\mu - \partial_\nu V^\mu V_\mu) V^\nu \rangle$$

Charm sector

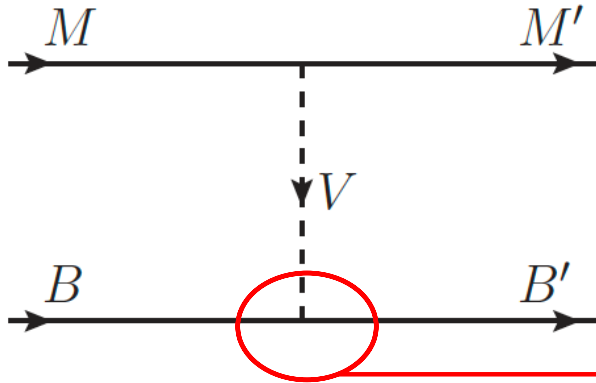
$$P = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{3}}\eta + \frac{1}{\sqrt{6}}\eta' & \pi^+ & K^+ & \bar{D}^0 \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{3}}\eta + \frac{1}{\sqrt{6}}\eta' & K^0 & D^- \\ K^- & \bar{K}^0 & -\frac{1}{\sqrt{3}}\eta + \sqrt{\frac{2}{3}}\eta' & D_s^- \\ D^0 & D^+ & D_s^+ & \eta_c \end{pmatrix}$$

$$V = \begin{pmatrix} \frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & \rho^+ & K^{*+} & \bar{D}^{*0} \\ \rho^- & -\frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & K^{*0} & \bar{D}^{*-} \\ K^{*-} & \bar{K}^{*0} & \phi & D_s^{*-} \\ D^{*0} & D^{*+} & D_s^{*+} & J/\psi \end{pmatrix}$$

Bottom sector

$$P = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{3}}\eta + \frac{1}{\sqrt{6}}\eta' & \pi^+ & K^+ & B^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{3}}\eta + \frac{1}{\sqrt{6}}\eta' & K^0 & B^0 \\ K^- & \bar{K}^0 & -\frac{1}{\sqrt{3}}\eta + \sqrt{\frac{2}{3}}\eta' & B_s^0 \\ B^- & \bar{B}^0 & \bar{B}_s^0 & \eta_b \end{pmatrix}$$

$$V = \begin{pmatrix} \frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & \rho^+ & K^{*+} & B^{*+} \\ \rho^- & -\frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & K^{*0} & B^{*0} \\ K^{*-} & \bar{K}^{*0} & \phi & B_s^{*0} \\ B^{*-} & \bar{B}^{*0} & \bar{B}_s^{*0} & \Upsilon \end{pmatrix}$$



$$\langle \phi_{flavor}^{B'} \chi_{spin}^{B'} | gq\bar{q} | \phi_{flavor}^B \chi_{spin}^B \rangle$$

$$\tilde{\mathcal{L}}_{VBB} \equiv gq\bar{q}(V) = g \begin{Bmatrix} \frac{1}{\sqrt{2}}(u\bar{u} - d\bar{d}), & \rho^0 \\ \frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d}), & \omega \\ s\bar{s}, & \phi \end{Bmatrix}$$

Symmetric spin-flavor wave function $\phi_{flavor} \cdot \chi_{spin}$

TABLE IV: Wave functions of baryon states.

| State | I, J | flavor | spin |
|-------------------|----------|--------------------------------|-----------------|
| Ξ_{cc}^{++} | 1/2, 1/2 | ccu | $\chi_{MS}(12)$ |
| Ξ_{cc}^+ | 1/2, 1/2 | ccd | $\chi_{MS}(12)$ |
| Ω_{cc}^+ | 0, 1/2 | ccs | $\chi_{MS}(12)$ |
| Ξ_c^+ | 1/2, 1/2 | $\frac{1}{\sqrt{2}}c(us - su)$ | $\chi_{MA}(23)$ |
| Ξ_c^0 | 1/2, 1/2 | $\frac{1}{\sqrt{2}}c(ds - sd)$ | $\chi_{MA}(23)$ |
| $\Xi_c^{\prime+}$ | 1/2, 1/2 | $\frac{1}{\sqrt{2}}c(us + su)$ | $\chi_{MS}(23)$ |
| $\Xi_c^{\prime0}$ | 1/2, 1/2 | $\frac{1}{\sqrt{2}}c(ds + sd)$ | $\chi_{MS}(23)$ |
| Ω_c^0 | 0, 1/2 | css | $\chi_{MS}(23)$ |

$$\chi_{MS}(12) = \frac{1}{\sqrt{6}}(\uparrow\downarrow\uparrow + \downarrow\uparrow\uparrow - 2\uparrow\uparrow\downarrow)$$

$$\chi_{MS}(23) = \frac{1}{\sqrt{6}}(\uparrow\downarrow\uparrow + \uparrow\uparrow\downarrow - 2\downarrow\uparrow\uparrow)$$

$$\chi_{MA}(23) = \frac{1}{\sqrt{2}}(\uparrow\uparrow\downarrow - \uparrow\downarrow\uparrow)$$

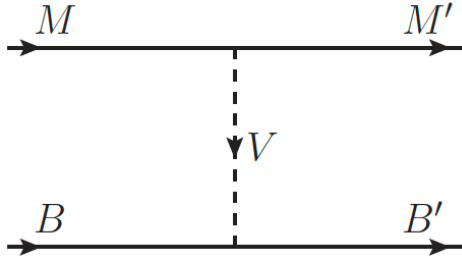
$$\langle \chi_{MS}(12) | \chi_{MS}(23) \rangle = -\frac{1}{2}$$

$$\langle \chi_{MS}(12) | \chi_{MA}(23) \rangle = -\frac{\sqrt{3}}{2}$$

W. Roberts and M. Pervin, Int. J. Mod. Phys. A 23, 2817 (2008)

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Ω_{QQ} states: Formalism



W. F. Wang, A. F., J. Song and E. Oset, arXiv:2208.14858 [hep-ph]

$$V_{ij} = -C_{ij} \frac{1}{4f_\pi^2} (p_1^0 + p_3^0)$$

$$\frac{1}{(q^0)^2 - |\vec{q}|^2 - m_{D^*}^2} \approx \frac{1}{(m_D - m_\eta)^2 - m_{D^*}^2}$$

TABLE V: Coefficients C_{ij} for the PB sector with $J^P = \frac{1}{2}^-$.

| | $\Xi_{cc}\bar{K}$ | $\Omega_{cc}\eta$ | $\Xi_c D$ | $\Xi'_c D$ |
|-------------------|-------------------|------------------------------|--------------------------------------|-------------------------------|
| $\Xi_{cc}\bar{K}$ | 2 | $\frac{2\sqrt{2}}{\sqrt{3}}$ | $\frac{-\sqrt{3}}{2\sqrt{2}}\lambda$ | $\frac{1}{2\sqrt{2}}\lambda$ |
| $\Omega_{cc}\eta$ | | 0 | $-\frac{1}{2}\lambda$ | $\frac{-1}{2\sqrt{3}}\lambda$ |
| $\Xi_c D$ | | | 2 | 0 |
| $\Xi'_c D$ | | | | 2 |

$$\lambda \equiv \frac{-m_V^2}{(m_D - m_\eta)^2 - m_{D^*}^2} \approx 0.25$$

TABLE IX: Coefficients C_{ij} for the PB sector with $J^P = \frac{1}{2}^-$.

| | $\Omega_{bb}\eta$ | $\Xi_{bb}\bar{K}$ | $\Xi_b \bar{B}$ | $\Xi'_b \bar{B}$ |
|-------------------|-------------------|------------------------------|-----------------|------------------|
| $\Omega_{bb}\eta$ | 0 | $\frac{2\sqrt{2}}{\sqrt{3}}$ | 0 | 0 |
| $\Xi_{bb}\bar{K}$ | | 2 | 0 | 0 |
| $\Xi_b \bar{B}$ | | | 2 | 0 |
| $\Xi'_b \bar{B}$ | | | | 2 |

$$\lambda = 0$$

Unitarized T-matrix from coupled-channel Bethe-Salpeter equation solved through On-shell factorization:

$$T_{ij} = (1 - V_{il}G_l)^{-1}V_{lj}$$

Meson-baryon loop function

$$G_l^{\text{cut}} = \int_0^\Lambda \frac{d^3q}{(2\pi)^3} \frac{1}{2\omega_l(\vec{q})} \frac{M_l}{E_l(\vec{q})} \frac{1}{\sqrt{s} - \omega_l(\vec{q}) - E_l(\vec{q}) + i\epsilon}$$

Cut-off regularization method $\Lambda = 650\text{MeV}$

TABLE XVIII: The poles for Ω_{cc} along with their coupling constants (in units of MeV) to various channels in the $J^P = \frac{1}{2}^-$ sector from $PB(\frac{1}{2}^+)$.

| Poles | | $\Xi_{cc}\bar{K}$ | $\Omega_{cc}\eta$ | $\Xi_c D$ | $\Xi'_c D$ |
|-----------------|----------------|-------------------|-------------------|-----------------------|-----------------------|
| 4069.86 | g_i | 2.63 | 1.55 | -1.10 | 0.26 |
| | $g_i G_i^{II}$ | -40.42 | -13.26 | 3.59 | -0.65 |
| 4205.22 + i0.94 | g_i | 0.10 + i0.20 | 0.04 + i0.09 | 6.25 - i0.04 | 0.09 + i0.01 |
| | $g_i G_i^{II}$ | -5.86 - i1.84 | -0.57 - i1.32 | -31.79 + i0.06 | -0.30 - i0.05 |
| 4310.76 + i0.28 | g_i | 0.02 + i0.01 | -0.13 - i0.04 | -0.02 + i0.00 | 6.35 + i0.00 |
| | $g_i G_i^{II}$ | -0.45 + i0.64 | 3.47 - i0.96 | 0.23 - i0.01 | -31.95 - i0.05 |

TABLE XXI: The poles for Ω_{cc} along with their coupling constants (in units of MeV) to various channels in the $J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$ sector from $VB(\frac{3}{2}^+)$.

| Poles | | $\Omega_{cc}\omega$ | $\Xi_{cc}\bar{K}^*$ | $\Xi_c D^*$ |
|---------|----------------|---------------------|---------------------|---------------|
| 4446.59 | g_i | 1.59 | 3.93 | 2.64 |
| | $g_i G_i^{II}$ | -16.03 | -35.31 | -9.69 |
| 4520.38 | g_i | -0.18 | -0.94 | 6.10 |
| | $g_i G_i^{II}$ | 2.78 | 12.44 | -29.41 |

TABLE XIX: The poles for Ω_{cc} along with their coupling constants (in units of MeV) to various channels in the $J^P = \frac{1}{2}^-, \frac{3}{2}^-$ sector from $VB(\frac{1}{2}^+)$.

| Poles | | $\Xi_c D^*$ | $\Omega_{cc}\omega$ | $\Xi_{cc}\bar{K}^*$ | $\Xi'_c D^*$ |
|---------|----------------|---------------|---------------------|---------------------|---------------|
| 4332.86 | g_i | 6.51 | -0.70 | -1.35 | -0.07 |
| | $g_i G_i^{II}$ | -29.78 | 5.66 | 9.74 | 0.23 |
| 4405.47 | g_i | 1.27 | 1.41 | 3.81 | 0.83 |
| | $g_i G_i^{II}$ | -8.44 | -15.17 | -35.89 | -3.33 |
| 4446.29 | g_i | -0.08 | -0.32 | -0.24 | 6.58 |
| | $g_i G_i^{II}$ | 0.73 | 4.34 | 2.81 | -30.80 |

TABLE XXII: The poles for Ω_{bb} along with their coupling constants (in units of MeV) to various channels in the $J^P = \frac{1}{2}^-$ sector from $PB(\frac{1}{2}^+)$.

| Poles | | $\Omega_{bb}\eta$ | $\Xi_{bb}\bar{K}$ | $\Xi_b \bar{B}$ | $\Xi'_b \bar{B}$ |
|----------|----------------|-------------------|-------------------|-----------------|------------------|
| 10741.65 | g_i | 1.50 | 2.72 | 0 | 0 |
| | $g_i G_i^{II}$ | -25.56 | -34.78 | 0 | 0 |
| 10864.15 | g_i | 0 | 0 | 11.87 | 0 |
| | $g_i G_i^{II}$ | 0 | 0 | -20.43 | 0 |
| 11001.63 | g_i | 0 | 0 | 0 | 11.87 |
| | $g_i G_i^{II}$ | 0 | 0 | 0 | -20.43 |

Ω_{QQ} states: Results

W. F. Wang, A. F., J. Song and E. Oset, arXiv:2208.14858 [hep-ph]

TABLE XXIII: The poles for Ω_{bb} along with their coupling constants (in units of MeV) to various channels in the $J^P = \frac{1}{2}^-, \frac{3}{2}^-$ sector from $VB(\frac{1}{2}^+)$.

| Poles | $\Omega_{bb}\omega$ | $\Xi_b B^*$ | $\Xi_{bb} K^*$ | $\Xi_b' B^*$ |
|----------|---------------------|-------------|----------------|---------------|
| 10909.88 | g_i | 0 | 11.92 | 0 |
| | $g_i G_i^{II}$ | 0 | -20.35 | 0 |
| 11047.36 | g_i | 0 | 0 | 11.92 |
| | $g_i G_i^{II}$ | 0 | 0 | -20.34 |

TABLE XXVIII: The poles for Ω_{bc} along with their coupling constants (in units of MeV) to various channels in the $J^P = \frac{3}{2}^-$ sector from $PB(\frac{3}{2}^+)$.

| Poles | $\Xi_{bc}^* K$ | $\Omega_{bc}^* \eta$ | $\Xi_b^* D$ | $\Xi_c^* B$ |
|-------------------|----------------|----------------------------------|----------------------------------|------------------------------------|
| 7415.55 | g_i | 2.63 | 1.56 | 1.21 |
| | $g_i G_i^{II}$ | -40.83 | -13.37 | -3.05 |
| 7667.65 + $i1.40$ | g_i | -0.02 - $i0.20$ | 0.02 - $i0.06$ | 6.25 - $i0.05$ |
| | $g_i G_i^{II}$ | 6.82 + $i0.98$ | 0.53 + $i1.88$ | -32.26 + $i0.09$ |
| 7740.93 | g_i | 0 | 0 | 11.52 |
| | $g_i G_i^{II}$ | 0 | 0 | -20.08 |

TABLE XXVI: The poles for Ω_{bc} along with their coupling constants (in units of MeV) to various channels in the $J^P = \frac{1}{2}^-$ sector from $PB(\frac{1}{2}^+)$.

| Poles | $\Xi_{bc} K$ | $\Xi_{bc}' K$ | $\Omega_{bc} \eta$ | $\Omega_{bc}' \eta$ | $\Xi_b D$ | $\Xi_c B$ | $\Xi_b' D$ | $\Xi_c' B$ |
|-------------------|----------------|----------------------------------|----------------------------------|----------------------------------|------------------------------------|------------------------------------|---------------|------------------------------------|
| 7362.26 | g_i | 2.64 | 0 | 1.57 | 0 | 1.70 | 0 | 0 |
| | $g_i G_i^{II}$ | -40.41 | 0 | -13.52 | 0 | -5.35 | 0 | 0 |
| 7392.60 | g_i | 0 | 2.61 | 0 | 1.51 | 0 | 0 | -0.73 |
| | $g_i G_i^{II}$ | 0 | -41.08 | 0 | -12.83 | 0 | 0 | 1.81 |
| 7514.32 + $i2.21$ | g_i | -0.14 - $i0.27$ | 0 | -0.05 - $i0.13$ | 0 | 6.19 - $i0.08$ | 0 | 0 |
| | $g_i G_i^{II}$ | 9.18 + $i2.42$ | 0 | 0.83 + $i2.04$ | 0 | -32.11 + $i0.12$ | 0 | 0 |
| 7566.65 | g_i | 0 | 0 | 0 | 0 | 0 | 11.50 | 0 |
| | $g_i G_i^{II}$ | 0 | 0 | 0 | 0 | 0 | -20.01 | 0 |
| 7641.20 + $i2.26$ | g_i | 0 | -0.06 - $i0.03$ | 0 | 0.34 + $i0.11$ | 0 | 0 | 6.50 + $i0.02$ |
| | $g_i G_i^{II}$ | 0 | 1.60 - $i1.76$ | 0 | -10.29 + $i2.74$ | 0 | 0 | -32.20 - $i0.41$ |
| 7674.29 | g_i | 0 | 0 | 0 | 0 | 0 | 0 | 11.53 |
| | $g_i G_i^{II}$ | 0 | 0 | 0 | 0 | 0 | 0 | -20.05 |

TABLE XXIX: The poles for Ω_{bc} along with their coupling constants (in units of MeV) to various channels in the $J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$ sector from $VB(\frac{3}{2}^+)$.

| Poles | $\Omega_{bc}^* \omega$ | $\Xi_{bc}^* K^*$ | $\Xi_b^* D^*$ | $\Xi_c^* B^*$ |
|---------|------------------------|------------------|---------------|---------------|
| 7729.11 | g_i | 1.60 | 3.82 | 3.54 |
| | $g_i G_i^{II}$ | -15.96 | -33.56 | -12.92 |
| 7786.71 | g_i | 0 | 0 | 11.61 |
| | $g_i G_i^{II}$ | 0 | 0 | -19.99 |
| 7811.82 | g_i | -0.23 | -1.24 | 5.71 |
| | $g_i G_i^{II}$ | 3.72 | 16.77 | -28.48 |

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Ω_{QQ} states: Summary

We have studied Ω_{cc} , Ω_{bc} and Ω_{bb} molecular states arising from the meson-baryon interaction with different J^P within an extension of the hidden gauge approach.

- $(C = 2, S = -1, I = 0)$ sector

$$\text{PB}(\frac{1^+}{2}): 3 \text{ states, } J^P = \frac{1^-}{2}$$

$$\text{PB}(\frac{3^+}{2}): 2 \text{ states, } J^P = \frac{3^-}{2}$$

$$\text{VB}(\frac{1^+}{2}): 3 \text{ states, } J^P = \frac{1^-}{2}, \frac{3^-}{2}$$

$$\text{VB}(\frac{3^+}{2}): 2 \text{ states, } J^P = \frac{1^-}{2}, \frac{3^-}{2}, \frac{5^-}{2}$$

- $(B = -2, S = -1, I = 0)$ sector

$$\text{PB}(\frac{1^+}{2}): 3 \text{ states, } J^P = \frac{1^-}{2}$$

$$\text{PB}(\frac{3^+}{2}): 2 \text{ states, } J^P = \frac{3^-}{2}$$

$$\text{VB}(\frac{1^+}{2}): 2 \text{ states, } J^P = \frac{1^-}{2}, \frac{3^-}{2}$$

$$\text{VB}(\frac{3^+}{2}): 1 \text{ states, } J^P = \frac{1^-}{2}, \frac{3^-}{2}, \frac{5^-}{2}$$

- $(C = 1, B = -1, S = -1, I = 0)$ sector

$$\text{PB}(\frac{1^+}{2}): 6 \text{ states, } J^P = \frac{1^-}{2}$$

$$\text{PB}(\frac{3^+}{2}): 3 \text{ states, } J^P = \frac{3^-}{2}$$

$$\text{VB}(\frac{1^+}{2}): 6 \text{ states, } J^P = \frac{1^-}{2}, \frac{3^-}{2}$$

$$\text{VB}(\frac{3^+}{2}): 3 \text{ states, } J^P = \frac{1^-}{2}, \frac{3^-}{2}, \frac{5^-}{2}$$

Experimental outputs for these sectors are expected to be provided by LHCb in 2y approx.

Thank you for your attention!

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