

# *Molecular $\Omega_{cc}$ , $\Omega_{bc}$ and $\Omega_{bb}$ states.*

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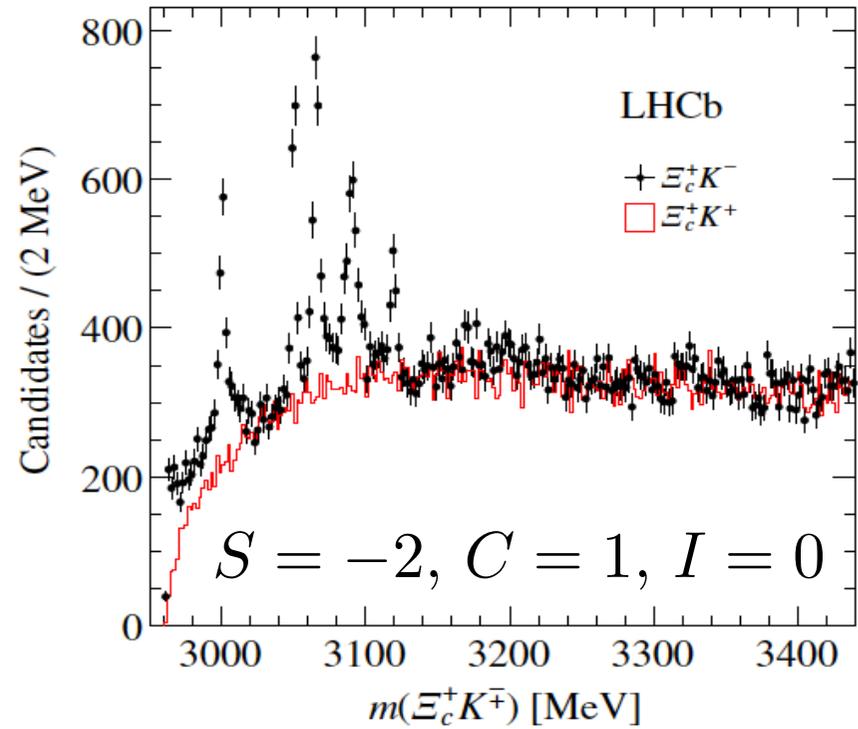
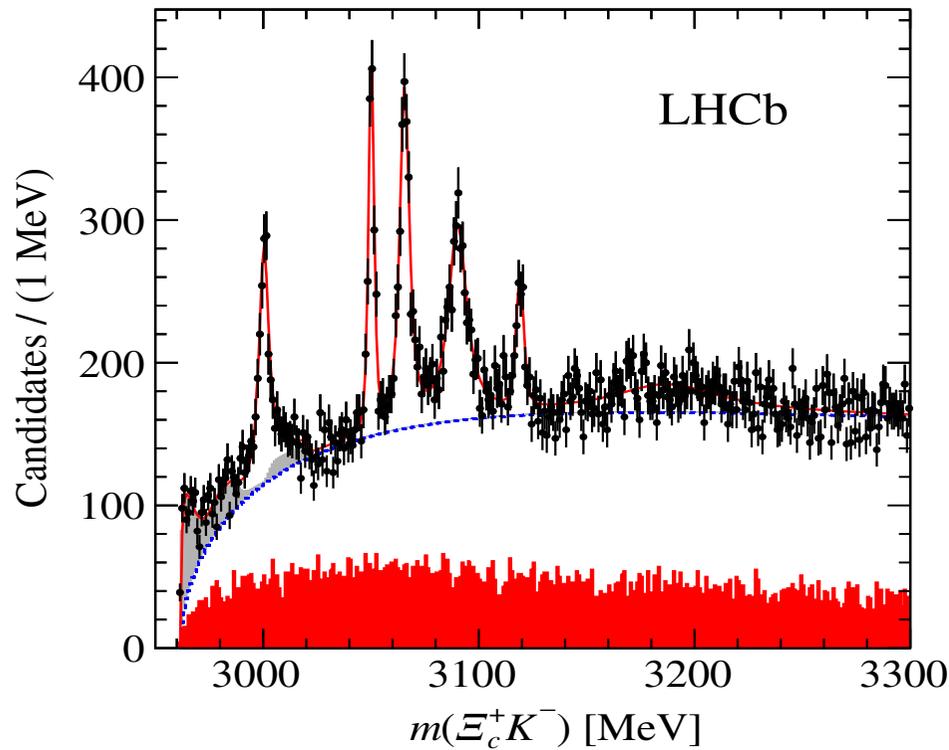
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Introduction: Historical Background ( $\Omega_c$  states)

The new  $\Omega'_c$ s observed at LHCb:

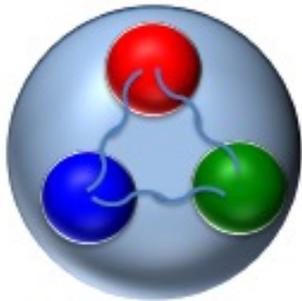
R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 118, 182001 (2017).



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Introduction: Historical Background ( $\Omega_c$  states)

**Constituent Quark Models (CQMs) interpretation:**



- Bound states consisting of 1 heavy quark (c) and a P-wave (ss) diquark. (System that gives 5 possible combinations)

$$S_c = \frac{1}{2}, S_{ss} = 1 + L_{ss} = 1 \rightarrow J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$$

M. Karliner and J. L. Rosner, Phys. Rev. D 95, no.11, 114012 (2017).

W. Wang and R. L. Zhu, Phys. Rev. D 96, no.1, 014024 (2017).

Z. G. Wang, Eur. Phys. J. C 77, no.5, 325 (2017).

B. Chen and X. Liu, Phys. Rev. D 96, no.9, 094015 (2017).

- Alternative interpretation: some states (the 3 lightest ones) remain with (ss) diquark with 1P orbital excitation and the others with 2S radial excitations.

$$J^P = \frac{3}{2}^-, \frac{5}{2}^-, \frac{1}{2}^+, \frac{3}{2}^+$$

S. S. Agaev, K. Azizi and H. Sundu, EPL 118, no.6, 61001 (2017).

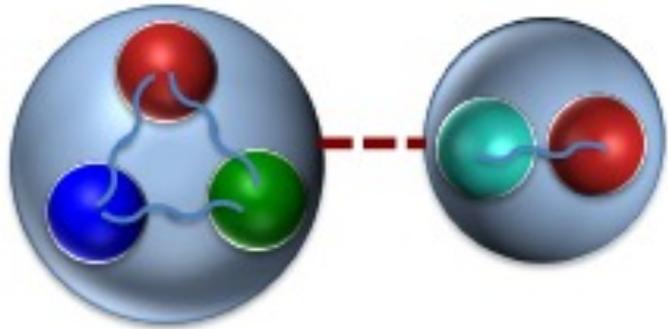
S. S. Agaev, K. Azizi and H. Sundu, Eur. Phys. J. C 77, no.6, 395 (2017).

H. Y. Cheng and C. W. Chiang, Phys. Rev. D 95, no.9, 094018 (2017).

K. L. Wang, L. Y. Xiao, X. H. Zhong and Q. Zhao, Phys. Rev. D 95, no.11, 116010 (2017).

Introduction: Historical Background ( $\Omega_c$  states)

## What about a molecular interpretation of these states?



R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 118, 182001 (2017).

Resonance	Mass (MeV)	$\Gamma$ (MeV)
$\Omega_c(3000)^0$	$3000.4 \pm 0.2 \pm 0.1^{+0.3}_{-0.5}$	$4.5 \pm 0.6 \pm 0.3$
$\Omega_c(3050)^0$	$3050.2 \pm 0.1 \pm 0.1^{+0.3}_{-0.5}$	$0.8 \pm 0.2 \pm 0.1$
		<1.2 MeV, 95% C.L.
$\Omega_c(3066)^0$	$3065.6 \pm 0.1 \pm 0.3^{+0.3}_{-0.5}$	$3.5 \pm 0.4 \pm 0.2$
$\Omega_c(3090)^0$	$3090.2 \pm 0.3 \pm 0.5^{+0.3}_{-0.5}$	$8.7 \pm 1.0 \pm 0.8$
$\Omega_c(3119)^0$	$3119.1 \pm 0.3 \pm 0.9^{+0.3}_{-0.5}$	$1.1 \pm 0.8 \pm 0.4$
		<2.6 MeV, 95% C.L.

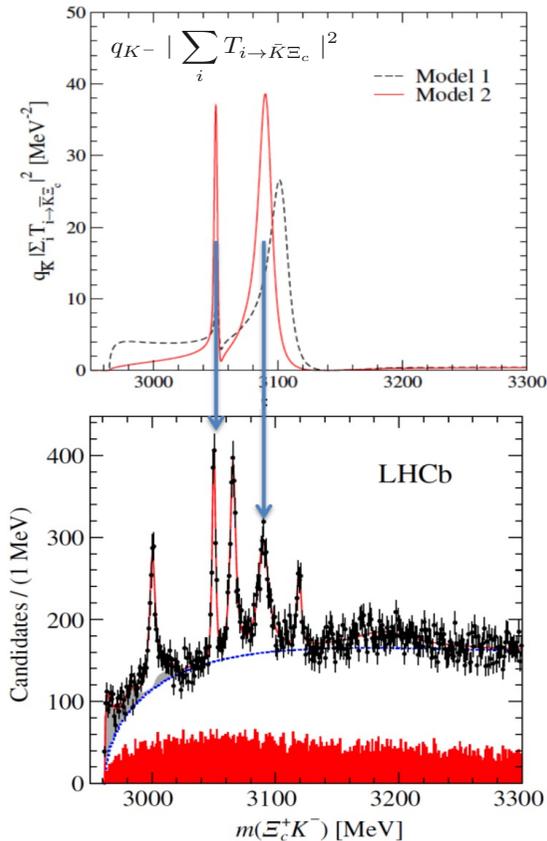
- The  $\bar{K}\Xi_c$  (2964 MeV) and  $\bar{K}\Xi'_c$  (3070 MeV) thresholds are within the energy range where the physical  $\Omega_c$  states pop up!!!
- Prior to the experimental measurement, some theoretical works predicted some states in this sector :
  - SU(8) spin-flavor sym. Model  $\rightarrow$  5 states much more bound than the LHCb ones. O. Romanets et al., Physical. Rev. D85,114032 (2012)
  - SU(4) finite range Model  
 J. Hofmann and M.F.M. Lutz, Nucl. Phys. A 763, 90-139 (2005)  $\rightarrow$  3 states below 2953 MeV  
 C. E. Jimenez-Tejero, A. Ramos and I. Vidaña, Phys. Rev. C 80, 055206 (2009)  $\rightarrow$  3 states, one at 3117 MeV ( $\Gamma = 16$  MeV)!!!

## Introduction: Historical Background ( $\Omega_c$ states)

### Molecular-Picture Models revisited

G. Montaña, A. F. and A. Ramos, Eur. Phys. J. A 54, no.4, 64 (2018)

$\Omega_c$  states dynamically generated by the s-wave interaction between a pseudoscalar meson and a ground state baryon:



$0^- \oplus \frac{1}{2}^+$ interaction in the $(I, S, C) = (0, -2, 1)$ sector					
Model 1					
$M$ [MeV]	3051.6		3103.3		
$\Gamma$ [MeV]	0.45		17		
	$ g_i $	$-g_i^2 dG/dE$	$ g_i $	$-g_i^2 dG/dE$	
$\bar{K} \Xi_c(2964)$	0.11	$0.00 + i 0.00$	0.58	$0.01 + i 0.03$	
$\bar{K} \Xi'_c(3070)$	1.67	$0.54 + i 0.01$	0.30	$0.01 - i 0.01$	
$D \Xi(3189)$	1.10	$0.05 - i 0.01$	4.08	$0.90 - i 0.05$	
$\eta \Omega_c(3246)$	2.08	$0.23 + i 0.00$	0.44	$0.01 + i 0.01$	
$\eta' \Omega_c(3656)$	0.04	$0.00 + i 0.00$	0.28	$0.00 + i 0.00$	

The state at 3051 MeV mainly composed by  $K \Xi'_c$  and  $\eta \Omega_c$

The state at 3103 MeV is basically a  $D \Xi$  bound state

→ 10 MeV too heavy and too wide...

### Experimental states

$$\Omega_c(3050)^0 : M = 3050.2 \pm 0.1 \pm 0.1_{-0.5}^{+0.3} \text{ MeV},$$

$$\Gamma = 0.8 \pm 0.2 \pm 0.1 \text{ MeV},$$

$$\Omega_c(3090)^0 : M = 3090.2 \pm 0.3 \pm 0.5_{-0.5}^{+0.3} \text{ MeV},$$

$$\Gamma = 8.7 \pm 1.0 \pm 0.8 \text{ MeV}$$

Assuming this scheme, spin-parity can only be 1/2-!

*Introduction: Historical Background ( $\Omega_c$  states)*

## Molecular-Picture Models revisited

V. R. Debastiani, J. M. Dias, W. H. Liang and E. Oset, Phys. Rev. D 97, no.9, 094035 (2018)

- Extension of the local hidden gauge approach with heavy-baryon states as a spectator c quark + sym. wave functions of the remaining light quarks
- Inclusion of pseudoscalar-decuplet baryon channels

→ Same 2 states with  $J^P = \frac{1}{2}^-$  and a new  $J^P = \frac{3}{2}^-$   $\Omega_c$  resonance which could be identified with the LHCb  $\Omega_c(3119)$

J. Nieves, R. Pavao and L. Tolos, Eur. Phys. J. C 78, no.2, 114 (2018)

- $SU(6)_{\text{lf}}$  xHQSS-extended WT meson-baryon interaction
- The symmetries automatically account for the additional presence of additional vector mesons and  $3/2^+$  baryons

→ 2 states with  $J^P = \frac{1}{2}^-$  and 1  $J^P = \frac{3}{2}^-$  state consistent with the experimental  $\Omega_c(3000)$ ,  $\Omega_c(3050)$  and  $\Omega_c(3119)$

## Introduction: Historical Background ( $\Omega_b$ states)

R. Aaij et al. [LHCb], Phys. Rev. Lett. 124, no.8, 082002 (2020)

	$\delta M_{\text{peak}}$ [MeV]	Mass [MeV]	Width [MeV]
$\Omega_b(6316)^-$	$523.74 \pm 0.31 \pm 0.07$	$6315.64 \pm 0.31 \pm 0.07 \pm 0.50$	$< 2.8$ (4.2)
$\Omega_b(6330)^-$	$538.40 \pm 0.28 \pm 0.07$	$6330.30 \pm 0.28 \pm 0.07 \pm 0.50$	$< 3.1$ (4.7)
$\Omega_b(6340)^-$	$547.81 \pm 0.26 \pm 0.05$	$6339.71 \pm 0.26 \pm 0.05 \pm 0.50$	$< 1.5$ (1.8)
$\Omega_b(6350)^-$	$557.98 \pm 0.35 \pm 0.05$	$6349.88 \pm 0.35 \pm 0.05 \pm 0.50$	$< 2.8$ (3.2)
			$1.4^{+1.0}_{-0.8} \pm 0.1$

### Predictions by Molecular-Picture Models:

- W. H. Liang, J. M. Dias, V. R. Debastiani and E. Oset, Nucl. Phys. B 930, 524 (2018)  
7  $\Omega_b^-$  states were generated dynamically with 1/2- and 3/2- (lowest mass 50MeV above  $\Omega_b^-(6350)$ )
- W. H. Liang and E. Oset, Phys. Rev. D 101, no.5, 054033 (2020)  
Arguments against the molecular nature of these states, instead structures at higher energies should be analysed
- J. Nieves, R. Pavao and L. Tolos, Eur. Phys. J. C 80, 22 (2020)  
Prediction of a 1/2- state  $\Omega_b^-(6360)$  as member of a sextet jointly with  $\Xi_b(6227)$  and  $\Sigma_b(6227)$
- G. Montaña, A. F. and A. Ramos, Eur. Phys. J. A 54, no.4, 64 (2018)  
2  $\Omega_b^-$  states were generated dynamically with 1/2- (lowest mass 70MeV above  $\Omega_b^-(6350)$ )

## $\Omega_{QQ}$ states

→ The plans of LHCb to measure  $\Omega_{cc}$ ,  $\Omega_{bc}$  and  $\Omega_{bb}$  states has motivated the present study.

Theoretical studies dedicated to this topic from different approaches:

- Quark Models

Mod. Phys. Lett. A 14, 135 (1999), Phys. Rev. D 66, 014008 (2002), Int. J. Mod. Phys. A 23, 2817 (2008)  
Phys. Lett. B 683, 21 (2010), Phys. Rev. D 98, 094021 (2018), Chin. Phys. C 44, 013102 (2020)

...

- Lattice QCD

Phys. Rev. D 64, 094509 (2001), Phys. Rev. D 90, 094507 (2014 )  
Phys. Rev. D 94, 074003 (2016), Phys. Rev. D 98, 114505 (2018)

...

- QCD sum rules

Eur. Phys. J. A 45, 267 (2010), Chin. Phys. C 42, 123102 (2018)  
Eur. Phys. J. C 78, 826 (2018)

...

- Other approaches

Phys. Rev. D 83, 056006 (2011), Phys. Rev. Lett. 115, 122001 (2015),  
Phys. Rev. D 102, 014013 (2020), [Erratum: Phys.Rev.D 104, 059901 (2021),  
Phys. Rev. D 104, 074027 (2021)

## $\Omega_{QQ}$ states: Sectors with their corresponding meson-baryon basis

W. F. Wang, A. F., J. Song and E. Oset, arXiv:2208.14858 [hep-ph]

TABLE I: Threshold masses (in MeV) of different channels for  $\Omega_{cc}$ .

$PB(\frac{1}{2}^+), J^P = \frac{1}{2}^-$	$\Xi_{cc}\bar{K}$ 4115	$\Omega_{cc}\eta$ 4263	$\Xi_c D$ 4338	$\Xi'_c D$ 4448
$PB(\frac{3}{2}^+), J^P = \frac{3}{2}^-$	$\Xi_{cc}^*\bar{K}$ 4168	$\Omega_{cc}^*\eta$ 4320	$\Xi_c^* D$ 4516	
$VB(\frac{1}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-$	$\Xi_{cc}\bar{K}^*$ 4512	$\Omega_{cc}\omega$ 4495	$\Xi_c D^*$ 4478	$\Xi'_c D^*$ 4588
$VB(\frac{3}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$	$\Xi_{cc}^*\bar{K}^*$ 4565	$\Omega_{cc}^*\omega$ 4552	$\Xi_c^* D^*$ 4656	

TABLE II: Threshold masses (in MeV) of different channels for  $\Omega_{bb}$ .

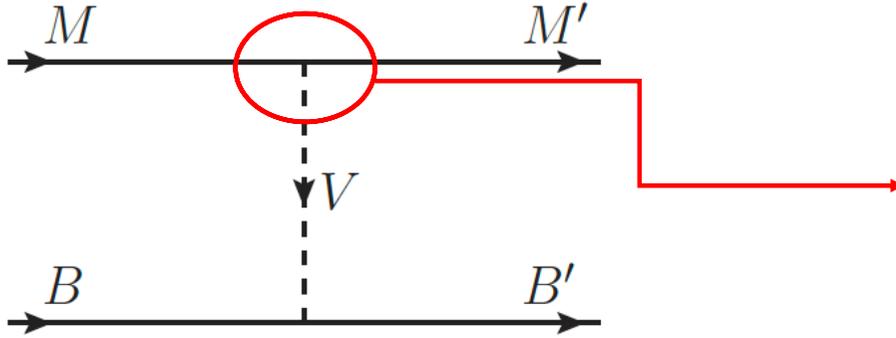
$PB(\frac{1}{2}^+), J^P = \frac{1}{2}^-$	$\Xi_{bb}\bar{K}$ 10833	$\Omega_{bb}\eta$ 10778	$\Xi_b\bar{B}$ 11076	$\Xi'_b\bar{B}$ 11214
$PB(\frac{3}{2}^+), J^P = \frac{3}{2}^-$	$\Xi_{bb}^*\bar{K}$ 10863	$\Omega_{bb}^*\eta$ 10806	$\Xi_b^*\bar{B}$ 11231	
$VB(\frac{1}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-$	$\Xi_{bb}\bar{K}^*$ 11230	$\Omega_{bb}\omega$ 11010	$\Xi_b\bar{B}^*$ 11122	$\Xi'_b\bar{B}^*$ 11260
$VB(\frac{3}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$	$\Xi_{bb}^*\bar{K}^*$ 11260	$\Omega_{bb}^*\omega$ 11038	$\Xi_b^*\bar{B}^*$ 11277	

TABLE III: Threshold masses (in MeV) of different channels for  $\Omega_{bc}$ .

$PB(\frac{1}{2}^+), J^P = \frac{1}{2}^-$	$\Xi_{bc}\bar{K}$ 7415	$\Omega_{bc}\eta$ 7559	$\Xi_b D$ 7667	$\Xi_c\bar{B}$ 7747
$PB(\frac{1}{2}^+), J^P = \frac{1}{2}^-$	$\Xi'_{bc}\bar{K}$ 7441	$\Omega'_{bc}\eta$ 7595	$\Xi'_b D$ 7805	$\Xi'_c\bar{B}$ 7857
$PB(\frac{3}{2}^+), J^P = \frac{3}{2}^-$	$\Xi_{bc}^*\bar{K}$ 7466	$\Omega_{bc}^*\eta$ 7614	$\Xi_b^* D$ 7822	$\Xi_c^*\bar{B}$ 7925
$VB(\frac{1}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-$	$\Xi_{bc}\bar{K}^*$ 7812	$\Omega_{bc}\omega$ 7791	$\Xi_b D^*$ 7807	$\Xi_c\bar{B}^*$ 7793
$VB(\frac{1}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-$	$\Xi'_{bc}\bar{K}^*$ 7838	$\Omega'_{bc}\omega$ 7827	$\Xi'_b D^*$ 7945	$\Xi'_c\bar{B}^*$ 7903
$VB(\frac{3}{2}^+), J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$	$\Xi_{bc}^*\bar{K}^*$ 7863	$\Omega_{bc}^*\omega$ 7846	$\Xi_b^* D^*$ 7962	$\Xi_c^*\bar{B}^*$ 7971

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$$\mathcal{L}_{VPP} = -ig \langle [P, \partial_\mu P] V^\mu \rangle$$

$$\mathcal{L}_{VVV} = ig \langle (V^\mu \partial_\nu V_\mu - \partial_\nu V^\mu V_\mu) V^\nu \rangle$$

Charm sector

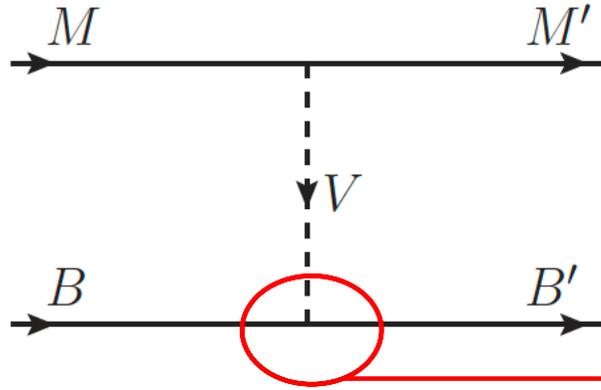
$$P = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{3}}\eta + \frac{1}{\sqrt{6}}\eta' & \pi^+ & K^+ & \bar{D}^0 \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{3}}\eta + \frac{1}{\sqrt{6}}\eta' & K^0 & D^- \\ K^- & \bar{K}^0 & -\frac{1}{\sqrt{3}}\eta + \sqrt{\frac{2}{3}}\eta' & D_s^- \\ D^0 & D^+ & D_s^+ & \eta_c \end{pmatrix}$$

$$V = \begin{pmatrix} \frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & \rho^+ & K^{*+} & \bar{D}^{*0} \\ \rho^- & -\frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & K^{*0} & \bar{D}^{*-} \\ K^{*-} & \bar{K}^{*0} & \phi & D_s^{*-} \\ D^{*0} & D^{*+} & D_s^{*+} & J/\psi \end{pmatrix}$$

Bottom sector

$$P = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{3}}\eta + \frac{1}{\sqrt{6}}\eta' & \pi^+ & K^+ & B^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{3}}\eta + \frac{1}{\sqrt{6}}\eta' & K^0 & B^0 \\ K^- & \bar{K}^0 & -\frac{1}{\sqrt{3}}\eta + \sqrt{\frac{2}{3}}\eta' & B_s^0 \\ B^- & \bar{B}^0 & \bar{B}_s^0 & \eta_b \end{pmatrix}$$

$$V = \begin{pmatrix} \frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & \rho^+ & K^{*+} & B^{*+} \\ \rho^- & -\frac{1}{\sqrt{2}}\rho^0 + \frac{1}{\sqrt{2}}\omega & K^{*0} & B^{*0} \\ K^{*-} & \bar{K}^{*0} & \phi & B_s^{*0} \\ B^{*-} & \bar{B}^{*0} & \bar{B}_s^{*0} & \Upsilon \end{pmatrix}$$



$$\langle \phi_{flavor}^{B'} \chi_{spin}^{B'} | gq\bar{q} | \phi_{flavor}^B \chi_{spin}^B \rangle$$

$$\tilde{\mathcal{L}}_{VBB} \equiv gq\bar{q}(V) = g \begin{Bmatrix} \frac{1}{\sqrt{2}}(u\bar{u} - d\bar{d}), & \rho^0 \\ \frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d}), & \omega \\ s\bar{s}, & \phi \end{Bmatrix}$$

Symmetric spin-flavor wave function  $\phi_{flavor} \cdot \chi_{spin}$

TABLE IV: Wave functions of baryon states.

State	$I, J$	flavor	spin
$\Xi_{cc}^{++}$	$1/2, 1/2$	$ccu$	$\chi_{MS}(12)$
$\Xi_{cc}^+$	$1/2, 1/2$	$ccd$	$\chi_{MS}(12)$
$\Omega_{cc}^+$	$0, 1/2$	$ccs$	$\chi_{MS}(12)$
$\Xi_c^+$	$1/2, 1/2$	$\frac{1}{\sqrt{2}}c(us - su)$	$\chi_{MA}(23)$
$\Xi_c^0$	$1/2, 1/2$	$\frac{1}{\sqrt{2}}c(ds - sd)$	$\chi_{MA}(23)$
$\Xi_c^{\prime+}$	$1/2, 1/2$	$\frac{1}{\sqrt{2}}c(us + su)$	$\chi_{MS}(23)$
$\Xi_c^{\prime0}$	$1/2, 1/2$	$\frac{1}{\sqrt{2}}c(ds + sd)$	$\chi_{MS}(23)$
$\Omega_c^0$	$0, 1/2$	$css$	$\chi_{MS}(23)$

$$\chi_{MS}(12) = \frac{1}{\sqrt{6}}(\uparrow\uparrow\uparrow + \downarrow\uparrow\uparrow - 2\uparrow\uparrow\downarrow)$$

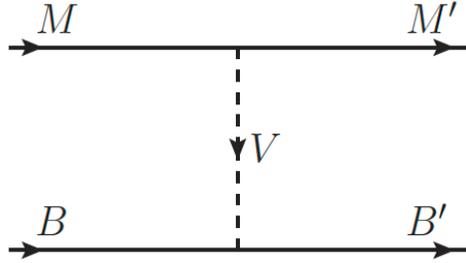
$$\chi_{MS}(23) = \frac{1}{\sqrt{6}}(\uparrow\downarrow\uparrow + \uparrow\uparrow\downarrow - 2\downarrow\uparrow\uparrow)$$

$$\chi_{MA}(23) = \frac{1}{\sqrt{2}}(\uparrow\uparrow\downarrow - \uparrow\downarrow\uparrow)$$

$$\langle \chi_{MS}(12) | \chi_{MS}(23) \rangle = -\frac{1}{2}$$

$$\langle \chi_{MS}(12) | \chi_{MA}(23) \rangle = -\frac{\sqrt{3}}{2}$$

W. Roberts and M. Pervin, Int. J. Mod. Phys. A 23, 2817 (2008)



$$V_{ij} = -C_{ij} \frac{1}{4f_{\pi}^2} (p_1^0 + p_3^0)$$

$$\frac{1}{(q^0)^2 - |\vec{q}|^2 - m_{D^*}^2} \approx \frac{1}{(m_D - m_{\eta})^2 - m_{D^*}^2}$$

TABLE V: Coefficients  $C_{ij}$  for the PB sector with  $J^P = \frac{1}{2}^-$ .

	$\Xi_{cc}\bar{K}$	$\Omega_{cc}\eta$	$\Xi_c D$	$\Xi'_c D$
$\Xi_{cc}\bar{K}$	2	$\frac{2\sqrt{2}}{\sqrt{3}}$	$\frac{-\sqrt{3}}{2\sqrt{2}}\lambda$	$\frac{1}{2\sqrt{2}}\lambda$
$\Omega_{cc}\eta$		0	$-\frac{1}{2}\lambda$	$\frac{-1}{2\sqrt{3}}\lambda$
$\Xi_c D$			2	0
$\Xi'_c D$				2

$$\lambda \equiv \frac{-m_V^2}{(m_D - m_{\eta})^2 - m_{D^*}^2} \approx 0.25$$

TABLE IX: Coefficients  $C_{ij}$  for the PB sector with  $J^P = \frac{1}{2}^-$ .

	$\Omega_{bb}\eta$	$\Xi_{bb}\bar{K}$	$\Xi_b\bar{B}$	$\Xi'_b\bar{B}$
$\Omega_{bb}\eta$	0	$\frac{2\sqrt{2}}{\sqrt{3}}$	0	0
$\Xi_{bb}\bar{K}$		2	0	0
$\Xi_b\bar{B}$			2	0
$\Xi'_b\bar{B}$				2

$$\lambda = 0$$

Unitarized T-matrix from coupled-channel Bethe-Salpeter equation solved through On-shell factorization:

$$T_{ij} = (1 - V_{il}G_l)^{-1}V_{lj}$$

Meson-baryon loop function

$$G_l^{\text{cut}} = \int_0^\Lambda \frac{d^3q}{(2\pi)^3} \frac{1}{2\omega_l(\vec{q})} \frac{M_l}{E_l(\vec{q})} \frac{1}{\sqrt{s} - \omega_l(\vec{q}) - E_l(\vec{q}) + i\epsilon}$$

Cut-off regularization method  $\Lambda = 650\text{MeV}$

TABLE XVIII: The poles for  $\Omega_{cc}$  along with their coupling constants (in units of MeV) to various channels in the  $J^P = \frac{1}{2}^-$  sector from  $PB(\frac{1}{2}^+)$ .

Poles		$\Xi_{cc}\bar{K}$	$\Omega_{cc}\eta$	$\Xi_{cc}D$	$\Xi'_{cc}D$
4069.86	$g_i$	<b>2.63</b>	1.55	-1.10	0.26
	$g_i G_i^{II}$	<b>-40.42</b>	-13.26	3.59	-0.65
4205.22 + $i0.94$	$g_i$	0.10 + $i0.20$	0.04 + $i0.09$	<b>6.25 - <math>i0.04</math></b>	0.09 + $i0.01$
	$g_i G_i^{II}$	-5.86 - $i1.84$	-0.57 - $i1.32$	<b>-31.79 + <math>i0.06</math></b>	-0.30 - $i0.05$
4310.76 + $i0.28$	$g_i$	0.02 + $i0.01$	-0.13 - $i0.04$	-0.02 + $i0.00$	<b>6.35 + <math>i0.00</math></b>
	$g_i G_i^{II}$	-0.45 + $i0.64$	3.47 - $i0.96$	0.23 - $i0.01$	<b>-31.95 - <math>i0.05</math></b>

TABLE XIX: The poles for  $\Omega_{cc}$  along with their coupling constants (in units of MeV) to various channels in the  $J^P = \frac{1}{2}^-, \frac{3}{2}^-$  sector from  $VB(\frac{1}{2}^+)$ .

Poles		$\Xi_{cc}D^*$	$\Omega_{cc}\omega$	$\Xi_{cc}\bar{K}^*$	$\Xi'_{cc}D^*$
4332.86	$g_i$	<b>6.51</b>	-0.70	-1.35	-0.07
	$g_i G_i^{II}$	<b>-29.78</b>	5.66	9.74	0.23
4405.47	$g_i$	1.27	1.41	<b>3.81</b>	0.83
	$g_i G_i^{II}$	-8.44	-15.17	<b>-35.89</b>	-3.33
4446.29	$g_i$	-0.08	-0.32	-0.24	<b>6.58</b>
	$g_i G_i^{II}$	0.73	4.34	2.81	<b>-30.80</b>

TABLE XXI: The poles for  $\Omega_{cc}$  along with their coupling constants (in units of MeV) to various channels in the  $J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$  sector from  $VB(\frac{3}{2}^+)$ .

Poles		$\Omega_{cc}\omega$	$\Xi_{cc}\bar{K}^*$	$\Xi'_{cc}D^*$
4446.59	$g_i$	1.59	<b>3.93</b>	2.64
	$g_i G_i^{II}$	-16.03	<b>-35.31</b>	-9.69
4520.38	$g_i$	-0.18	-0.94	<b>6.10</b>
	$g_i G_i^{II}$	2.78	12.44	<b>-29.41</b>

TABLE XXII: The poles for  $\Omega_{bb}$  along with their coupling constants (in units of MeV) to various channels in the  $J^P = \frac{1}{2}^-$  sector from  $PB(\frac{1}{2}^+)$ .

Poles		$\Omega_{bb}\eta$	$\Xi_{bb}\bar{K}$	$\Xi_{bb}\bar{B}$	$\Xi'_{bb}\bar{B}$
10741.65	$g_i$	1.50	<b>2.72</b>	0	0
	$g_i G_i^{II}$	-25.56	<b>-34.78</b>	0	0
10864.15	$g_i$	0	0	<b>11.87</b>	0
	$g_i G_i^{II}$	0	0	<b>-20.43</b>	0
11001.63	$g_i$	0	0	0	<b>11.87</b>
	$g_i G_i^{II}$	0	0	0	<b>-20.43</b>

TABLE XXIII: The poles for  $\Omega_{bb}$  along with their coupling constants (in units of MeV) to various channels in the  $J^P = \frac{1}{2}^-, \frac{3}{2}^-$  sector from  $VB(\frac{1}{2}^+)$ .

Poles	$\Omega_{bb}\omega$	$\Xi_b \bar{B}^*$	$\Xi_{bb} \bar{K}^*$	$\Xi_b' \bar{B}^*$
10909.88	$g_i$	0	<b>11.92</b>	0
	$g_i G_i^{II}$	0	<b>-20.35</b>	0
11047.36	$g_i$	0	0	<b>11.92</b>
	$g_i G_i^{II}$	0	0	<b>-20.34</b>

TABLE XXVIII: The poles for  $\Omega_{bc}$  along with their coupling constants (in units of MeV) to various channels in the  $J^P = \frac{3}{2}^-$  sector from  $PB(\frac{3}{2}^+)$ .

Poles	$\Xi_{bc}^* \bar{K}$	$\Omega_{bc}^* \eta$	$\Xi_b^* D$	$\Xi_c^* \bar{B}$
7415.55	$g_i$	<b>2.63</b>	1.56	1.21
	$g_i G_i^{II}$	<b>-40.83</b>	-13.37	-3.05
7667.65 + i1.40	$g_i$	-0.02 - i0.20	0.02 - i0.06	<b>6.25 - i0.05</b>
	$g_i G_i^{II}$	6.82 + i0.98	0.53 + i1.88	<b>-32.26 + i0.09</b>
7740.93	$g_i$	0	0	<b>11.52</b>
	$g_i G_i^{II}$	0	0	<b>-20.08</b>

TABLE XXVI: The poles for  $\Omega_{bc}$  along with their coupling constants (in units of MeV) to various channels in the  $J^P = \frac{1}{2}^-$  sector from  $PB(\frac{1}{2}^+)$ .

Poles	$\Xi_{bc} \bar{K}$	$\Xi_{bc}' \bar{K}$	$\Omega_{bc} \eta$	$\Omega_{bc}' \eta$	$\Xi_b D$	$\Xi_c \bar{B}$	$\Xi_b' D$	$\Xi_c' \bar{B}$
7362.26	$g_i$	<b>2.64</b>	0	1.57	0	1.70	0	0
	$g_i G_i^{II}$	<b>-40.41</b>	0	-13.52	0	-5.35	0	0
7392.60	$g_i$	0	<b>2.61</b>	0	1.51	0	0	-0.73
	$g_i G_i^{II}$	0	<b>-41.08</b>	0	-12.83	0	0	1.81
7514.32 + i2.21	$g_i$	-0.14 - i0.27	0	-0.05 - i0.13	0	<b>6.19 - i0.08</b>	0	0
	$g_i G_i^{II}$	9.18 + i2.42	0	0.83 + i2.04	0	<b>-32.11 + i0.12</b>	0	0
7566.65	$g_i$	0	0	0	0	0	<b>11.50</b>	0
	$g_i G_i^{II}$	0	0	0	0	0	<b>-20.01</b>	0
7641.20 + i2.26	$g_i$	0	-0.06 - i0.03	0	0.34 + i0.11	0	0	<b>6.50 + i0.02</b>
	$g_i G_i^{II}$	0	1.60 - i1.76	0	-10.29 + i2.74	0	0	<b>-32.20 - i0.41</b>
7674.29	$g_i$	0	0	0	0	0	0	<b>11.53</b>
	$g_i G_i^{II}$	0	0	0	0	0	0	<b>-20.05</b>

TABLE XXIX: The poles for  $\Omega_{bc}$  along with their coupling constants (in units of MeV) to various channels in the  $J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$  sector from  $VB(\frac{3}{2}^+)$ .

Poles	$\Omega_{bc}^* \omega$	$\Xi_{bc}^* \bar{K}^*$	$\Xi_b^* D^*$	$\Xi_c^* \bar{B}^*$
7729.11	$g_i$	1.60	<b>3.82</b>	3.54
	$g_i G_i^{II}$	-15.96	<b>-33.56</b>	-12.92
7786.71	$g_i$	0	0	0
	$g_i G_i^{II}$	0	0	0
7811.82	$g_i$	-0.23	-1.24	<b>5.71</b>
	$g_i G_i^{II}$	3.72	16.77	<b>-28.48</b>

## $\Omega_{QQ}$ states: Summary

We have studied  $\Omega_{cc}$ ,  $\Omega_{bc}$  and  $\Omega_{bb}$  molecular states arising from the meson-baryon interaction with different  $J^P$  within an extension of the hidden gauge approach.

- $(C = 2, S = -1, I = 0)$  sector

$$\text{PB}(\frac{1}{2}^+): 3 \text{ states, } J^P = \frac{1}{2}^-$$

$$\text{PB}(\frac{3}{2}^+): 2 \text{ states, } J^P = \frac{3}{2}^-$$

$$\text{VB}(\frac{1}{2}^+): 3 \text{ states, } J^P = \frac{1}{2}^-, \frac{3}{2}^-$$

$$\text{VB}(\frac{3}{2}^+): 2 \text{ states, } J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$$

- $(B = -2, S = -1, I = 0)$  sector

$$\text{PB}(\frac{1}{2}^+): 3 \text{ states, } J^P = \frac{1}{2}^-$$

$$\text{PB}(\frac{3}{2}^+): 2 \text{ states, } J^P = \frac{3}{2}^-$$

$$\text{VB}(\frac{1}{2}^+): 2 \text{ states, } J^P = \frac{1}{2}^-, \frac{3}{2}^-$$

$$\text{VB}(\frac{3}{2}^+): 1 \text{ states, } J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$$

- $(C = 1, B = -1, S = -1, I = 0)$  sector

$$\text{PB}(\frac{1}{2}^+): 6 \text{ states, } J^P = \frac{1}{2}^-$$

$$\text{PB}(\frac{3}{2}^+): 3 \text{ states, } J^P = \frac{3}{2}^-$$

$$\text{VB}(\frac{1}{2}^+): 6 \text{ states, } J^P = \frac{1}{2}^-, \frac{3}{2}^-$$

$$\text{VB}(\frac{3}{2}^+): 3 \text{ states, } J^P = \frac{1}{2}^-, \frac{3}{2}^-, \frac{5}{2}^-$$

Experimental outputs for these sectors are expected to be provided by LHCb in 2y approx.

Thank you for your attention!

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