

Molecular states of D^*D^* \bar{K}^* and $B^*B^*K^*$ nature

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N. Ikeno, M. Bayar and E. Oset, Phys. Rev. D 107, 034006 (2023)

M. Bayar, N. Ikeno and L. Roca, Phys. Rev. D 107, 054042 (2023)



20th International Conference on Hadron Spectroscopy and Structure (HADRON 2023), June 5- 9th 2023



Exotic hadrons

Many exotics have been observed since the discovery of X(3872)

- $Z_c(3900)$: close to $D\bar{D}^*$, $c\bar{q}q\bar{c}$ ($q = u, d$)
- $Z_{cs}(3985)$: close to $\bar{D}_s^* D / \bar{D}_s D^*$, $c\bar{q}s\bar{c}$
- $X_0(2900)$, $X_1(2900)$: close $D^*\bar{K}^*$, $c\bar{q}s\bar{q}$
- $T_{cc}(3875)$: close to DD^* , $c\bar{q}c\bar{q}$

} clearly exotic mesonic structure

....

=> Cannot be explained as the ordinary mesons $q\bar{q}$

Many possible types of hadronic structures were proposed:
Tetraquarks, Meson-meson molecules,

These findings open the door to the formation of few body systems with several open heavy quarks like ccs, ccc, bbs, etc.

Our study: $D^*D^*\bar{K}^*$ and $B^*B^*\bar{K}^*$ states based on the molecular picture

Molecular states of $D^* D^* \bar{K}^*$ and $\bar{B}^* \bar{B}^* \bar{K}^*$ nature

$D^* D^* \bar{K}^*$ system [$c\bar{q}c\bar{q}s\bar{q}$] : Very Exotic system with **ccs** open quarks

- $D^* \bar{K}^*$ interaction: R. Molina, E. Oset, PLB811 (2020)
The $J^P = 0^+$ bound state is identified with the $X_0(2900)$
- $D^* D^*$ interaction: L. R. Dai, R. Molina, E. Oset, PRD 105 (2022)
Bound state in $I = 0$ and $J^P = 1^+$
(using the same q_{\max} of $D^* D$ interaction fixed by the $T_{cc}(3875)$ data
A. Feijoo, W. H. Liang, E. Oset, PRD104 (2021).)

$\bar{B}^* \bar{B}^* \bar{K}^*$ system [$b\bar{q}b\bar{q}s\bar{q}$] : Very Exotic system with **bbs** open quarks

- $\bar{B}^* \bar{K}^*$ interaction: E. Oset and L. Roca, EPJ.C 82 (2022)
- $\bar{B}^* \bar{B}^*$ interaction: L. R. Dai, E. Oset, A. Feijoo, R. Molina, L. Roca,
A. M. Torres and K. P. Khemchandani, PRD 105 (2022)

=> A search for possible bound states of the three-body system

Recent studies of three body systems of molecular nature

- $D\bar{D}K$ T. W. Wu et al., PRD100(2019); A. Martinez Torres, et al., PRD99(2019); Y. Huang et al., PRD101(2020).
- $D\bar{D}^*K$ X. L. Ren et al., PLB785, 112 (2018).
- DD^*K L. Ma et al., Chin. Phys. C43, 014102 (2019).
- $D\bar{D}K$ T. W. Wu, M. Z. Liu, L.S. Geng, et al., PRD103, L031501 (2021); X. Wei, Q. H. Shen, J. J. Xie, EPJC82 (2022)
- $D^*D^*D^*$ S. Q. Luo, W. Tian-Wei, M. Z. Liu, L. S. Geng, X. Liu, PRD105 (2022); M. Bayar, A. Martinez Torres, K. P. Khemchandani, R. Molina, E. Oset, EPJC83 (2023)
- $\bar{K}B^*B^*$ M. P. Valderrama, PRD98, 014022 (2018).
- $\bar{K}^{(*)}B^{(*)}\bar{B}^{(*)}$ X. L. Ren and Z. F. Sun, PRD 99, 094041 (2019).
- T_{bbb} as BBB H. Garcilazo, A. Valcarce, PLB784, 169(2018)

Method to solve the three-body system:

- Variational method
 - Fixed center approximation (FCA) to the Faddeev equations
- => Both methods gave similar results in the case of $D\bar{D}K$
- Also in the case of $D^*D^*D^*$

Fixed Center Approximation (FCA) to the Faddeev equation

There is a cluster of two bound particles D^*D^* and the third one (\bar{K}^*) collides with the components of this cluster without modifying the D^*D^* wave function.

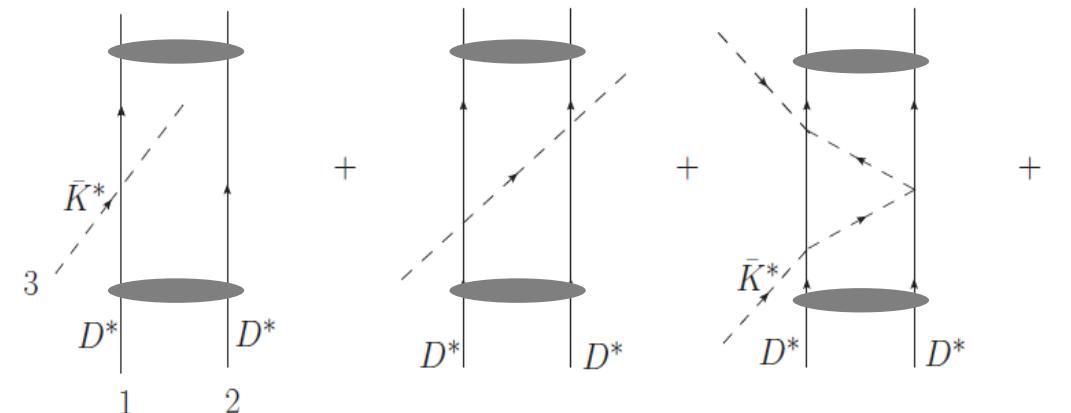
Total three-body scattering amplitude T

$$T \equiv T_1 + T_2$$

$$T_1 = t_1 + t_1 G_0 T_2,$$

$$T_2 = t_2 + t_2 G_0 T_1,$$

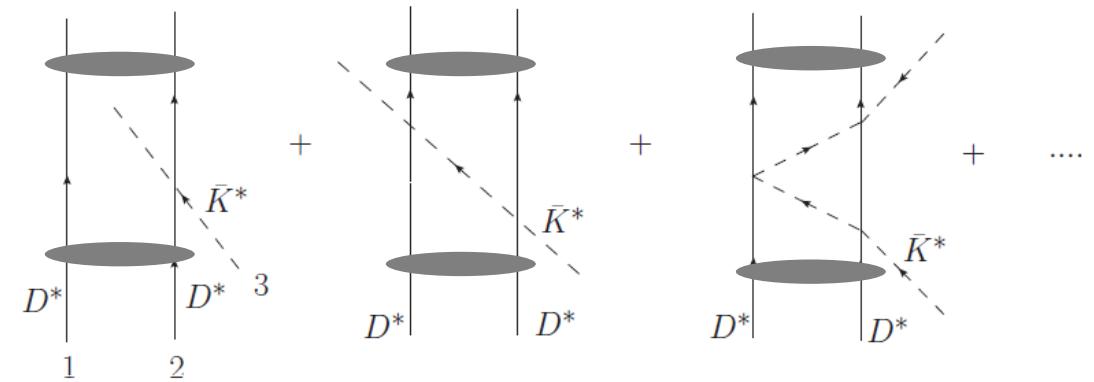
L. Roca and E. Oset, PRD82, 054013 (2010)



t_i is the scattering amplitude for $D^*(i)\bar{K}^*$ bar

G_0 is the \bar{K}^* propagator folded with the cluster wave function

$$G_0 = \frac{1}{2m_C} \int \frac{d^3 q}{(2\pi)^3} F(\vec{q}) \frac{1}{q^{02} - \vec{q}^2 - m_{\bar{K}^*}^2 + i\epsilon}$$



The form factor $F(q)$ encodes the information about the D^*D^* bound state:

$$F(\vec{q}) = \int d^3 \vec{r} e^{-i\vec{q} \cdot \vec{r}} \Psi_c^2(\vec{r}) = \frac{1}{N} \int_{|\vec{p}-\vec{q}| < q_{\max}} d^3 p \frac{1}{m_C - \sqrt{m_{D^*}^2 + \vec{p}^2} - \sqrt{m_{D^*}^2 + \vec{p}^2}} \frac{1}{m_C - \sqrt{m_{D^*}^2 + (\vec{p} - \vec{q})^2} - \sqrt{m_{D^*}^2 + (\vec{p} - \vec{q})^2}}$$

Normalization of the amplitudes

L. Roca and E. Oset, PRD82, 054013 (2010)

- S matrix in the diagram of double scattering:

$$S^{(2)} = -i(2\pi)^4 \delta^4(p_{\text{fin}} - p_{\text{in}}) \frac{1}{\mathcal{V}^2} \frac{1}{\sqrt{2\omega_{\bar{K}^*}}} \frac{1}{\sqrt{2\omega_{\bar{K}^*}}} \frac{1}{\sqrt{2\omega_{D^*}}} \frac{1}{\sqrt{2\omega_{D^*}}} \frac{1}{\sqrt{2\omega_{D^*}}} t_1 t_2$$

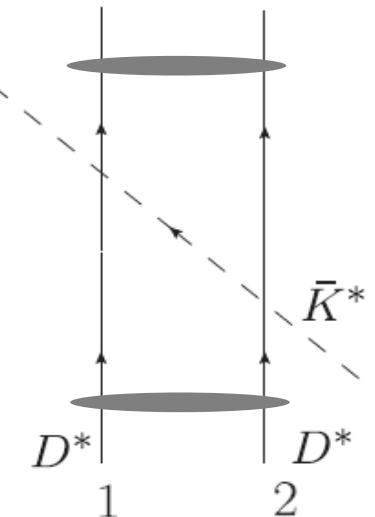
$$\int \frac{d^3 q}{(2\pi)^3} F(\vec{q}) \frac{1}{q^0 - \vec{q}^2 - m_{\bar{K}^*}^2 + i\epsilon},$$

where $F(q)$ is the form factor of the cluster

- Macroscopic perspective of $(D^*(1)D^*(2))_c \bar{K}^*$

$$S^{(2)} = -i(2\pi)^4 \delta^4(p_{\text{fin}} - p_{\text{in}}) \frac{1}{\mathcal{V}^2} \frac{1}{\sqrt{2\omega_{\bar{K}^*}}} \frac{1}{\sqrt{2\omega_{\bar{K}^*}}} \frac{1}{\sqrt{2\omega_C}} \frac{1}{\sqrt{2\omega_C}} T^{(2)}$$

$$\Rightarrow T^{(2)} = \frac{2\omega_C}{2\omega_{D^*}} \frac{2\omega_C}{2\omega_C} \frac{1}{2\omega_C} t_1 t_2 \int \frac{d^3 q}{(2\pi)^3} F(\vec{q}) \frac{1}{q^0 - \vec{q}^2 - m_{\bar{K}^*}^2 + i\epsilon}$$



It is convenient to write the partition functions suited to the macroscopic formalism as

$$\tilde{T}_1 = \tilde{t}_1 + \tilde{t}_1 \tilde{G}_0 \tilde{T}_2 \quad \text{by defining} \quad \tilde{t}_1 = \frac{2m_C}{2m_{D^*}} t_1 \quad \tilde{t}_2 = \frac{2m_C}{2m_{D^*}} t_2$$

$$\tilde{T}_2 = \tilde{t}_2 + \tilde{t}_2 \tilde{G}_0 \tilde{T}_1$$

$$\text{In this case, } t_1 = t_2, \text{ then } T_1 = T_2 \quad \tilde{T}_1 = \tilde{t}_1 + \tilde{t}_1 \tilde{G}_0 \tilde{T}_1; \quad \tilde{T}_1 = \frac{1}{\tilde{t}_1^{-1} - \tilde{G}_0}; \quad \tilde{T} = \tilde{T}_1 + \tilde{T}_2 = 2\tilde{T}_1$$

Consideration of the isospin and spin of the $D^*\bar{K}^*$ amplitudes t_1

Cluster: D^*D^* bound state in $I = 0$ and $J^P = 1^+$ L. R. Dai, R. Molina, E. Oset, PRD 105 (2022)

$$|D^*D^*, I = 0\rangle = -\frac{1}{\sqrt{2}}(D^{*+}D^{*0} - D^{*0}D^{*+})$$

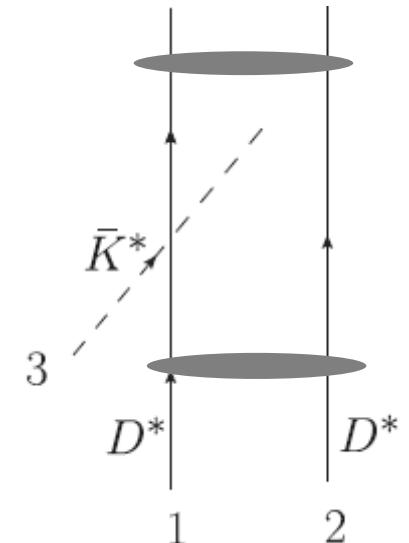
- Isospin considerations:

To make a connection with the $D^*\bar{K}^*$ isospin amplitudes, we combine the third component of $D^*(1)$ with the one of \bar{K}^*

$$|I(D^*(1)\bar{K}^*), I_3(D^*(1)\bar{K}^*)\rangle |I_3(D^*(2))\rangle \text{ with } I_3 = 1/2 \text{ of } K^*$$

$$\frac{1}{\sqrt{2}}\frac{1}{\sqrt{2}}\left(\left\langle D^*D^*, \frac{1}{2}, -\frac{1}{2} \right| - \left\langle D^*D^*, -\frac{1}{2}, \frac{1}{2} \right|\right) \left\langle \bar{K}^*, \frac{1}{2} \right| |t_1| \left(\left| D^*D^*, \frac{1}{2}, -\frac{1}{2} \right\rangle - \left| D^*D^*, -\frac{1}{2}, \frac{1}{2} \right\rangle \right) \left| \bar{K}^*, \frac{1}{2} \right\rangle$$

$$t_1 = \frac{3}{4}t_{D^*\bar{K}^*}^{I=1} + \frac{1}{4}t_{D^*\bar{K}^*}^{I=0}$$



- Spin consideration: three total spins $J=0, 1, 2$ for $D^*D^*\bar{K}^*$

$$\text{For } J=0 \quad t_1 = t_{D^*\bar{K}^*}^{j=1}$$

$$\text{For } J=1 \quad t_1 = \frac{1}{4} \left(\frac{4}{3}t_{D^*\bar{K}^*}^{j=0} + t_{D^*\bar{K}^*}^{j=1} + \frac{5}{3}t_{D^*\bar{K}^*}^{j=2} \right).$$

$$\text{For } J=2 \quad t_1 = \frac{1}{4}t_{D^*\bar{K}^*}^{j=1} + \frac{3}{4}t_{D^*\bar{K}^*}^{j=2}$$

Consideration of the isospin and spin of the $D^*\bar{K}^*$ amplitudes

Combining the isospin and the spin decomposition of the amplitudes, we find the final contributions

$$\text{For } J=0 \quad t_1 = \frac{3}{4}t^{I=1, j=1} + \frac{1}{4}t^{I=0, j=1}$$

$$\text{For } J=1 \quad t_1 = \frac{1}{16} \left\{ 5t^{I=1, j=2} + 3t^{I=1, j=1} + 4t^{I=1, j=0} + \frac{5}{3}t^{I=0, j=2} + t^{I=0, j=1} + \frac{4}{3}t^{I=0, j=0} \right\}$$

$$\text{For } J=2 \quad t_1 = \frac{1}{16} \left\{ 9t^{I=1, j=2} + 3t^{I=1, j=1} + 3t^{I=0, j=2} + t^{I=0, j=1} \right\}$$

- The $D^*\bar{K}^*$ amplitude t for the different I, j states

Bethe-Salpeter eq.

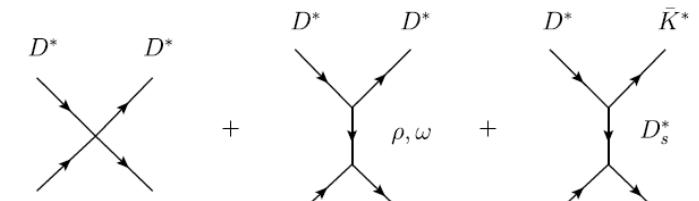
$$t_1 = \frac{1}{V^{-1} - G_{D^*\bar{K}^*}}$$

R. Molina, T. Branz, and E. Oset, PRD82(2010) 014010

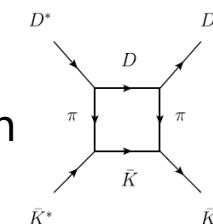
R. Molina, E. Oset, PLB811 (2020)

The interaction V of $D^*\bar{K}^*$ in $I=0$ is attractive

$I(J^P)$	$M[\text{MeV}]$	$\Gamma[\text{MeV}]$	Coupled channels	state
$0(2^+)$	2775	38	$D^*\bar{K}^*$?
$0(1^+)$	2861	20	$D^*\bar{K}^*$?
$0(0^+)$	2866	57	$D^*\bar{K}^*$	$X_0(2866)$



Decay width

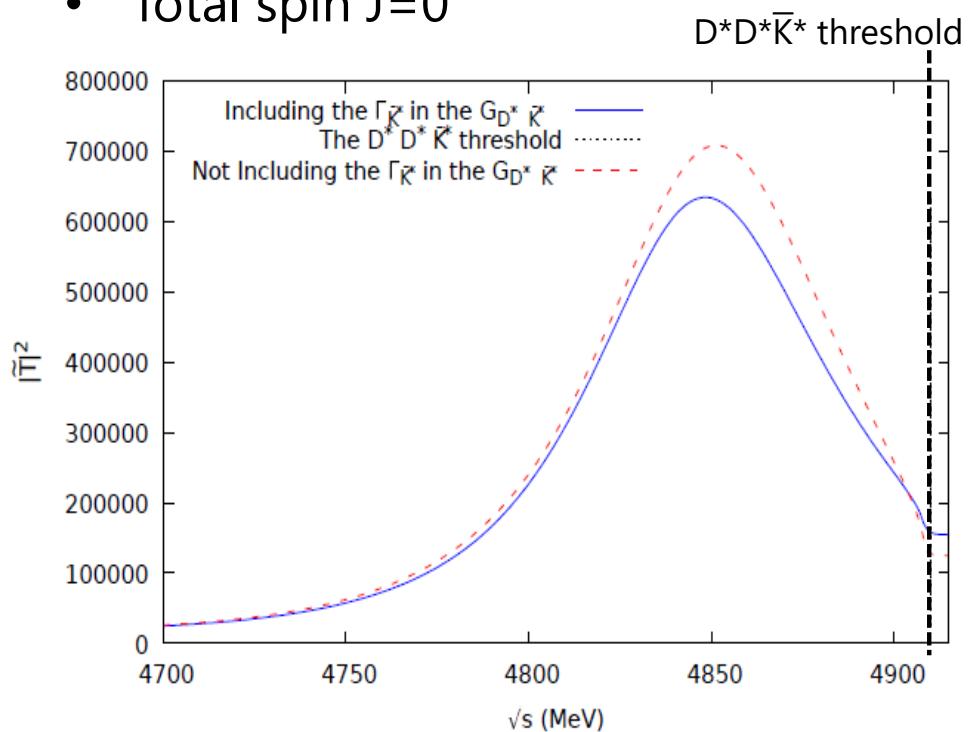


In $I = 1$, V is repulsive \Rightarrow No bound state

Bound states of $D^* D^* \bar{K}^*$

N. Ikeno, M. Bayar, E. Oset,
PRD107, 034006 (2023)

- Total spin $J=0$

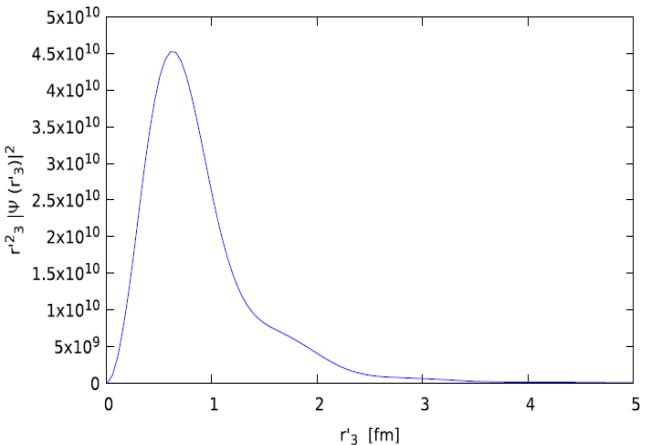


- A clear peak around 4845 MeV, about 61 MeV below the $D^* D^* \bar{K}^*$ threshold

$D^* D^*$ is bound by about 4-6 MeV
 $D^* \bar{K}^*$ is bound by about 30 MeV
 \Rightarrow The interaction of \bar{K}^* with two D^* would give rise to a binding about twice as big as the one of $D^* \bar{K}^*$

- The width is around 80 MeV
 Consideration \bar{K}^* decay width by means of a convolution of the loop function

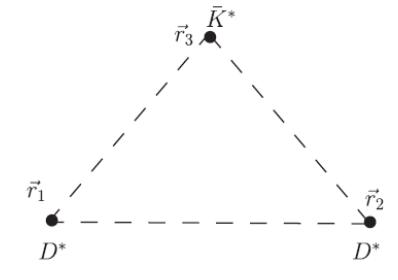
- Wave function for the \bar{K}^* in the $D^* D^* \bar{K}^*$ system at rest.



D. Gamermann, J. Nieves, E. Oset,
E. Ruiz Arriola, PRD 81(2010)014029

$$|\Psi(r'_3)|^2 = \int d^3 r_1 d^3 r_2 (|\phi(\vec{r}_{31})|^2 + |\phi(\vec{r}_{32})|^2) |\phi'(\vec{r}_{12})|^2 \\ \times \delta^3(m_{D^*} \vec{r}_1 + m_{D^*} \vec{r}_2 + m_{\bar{K}^*} \vec{r}_3),$$

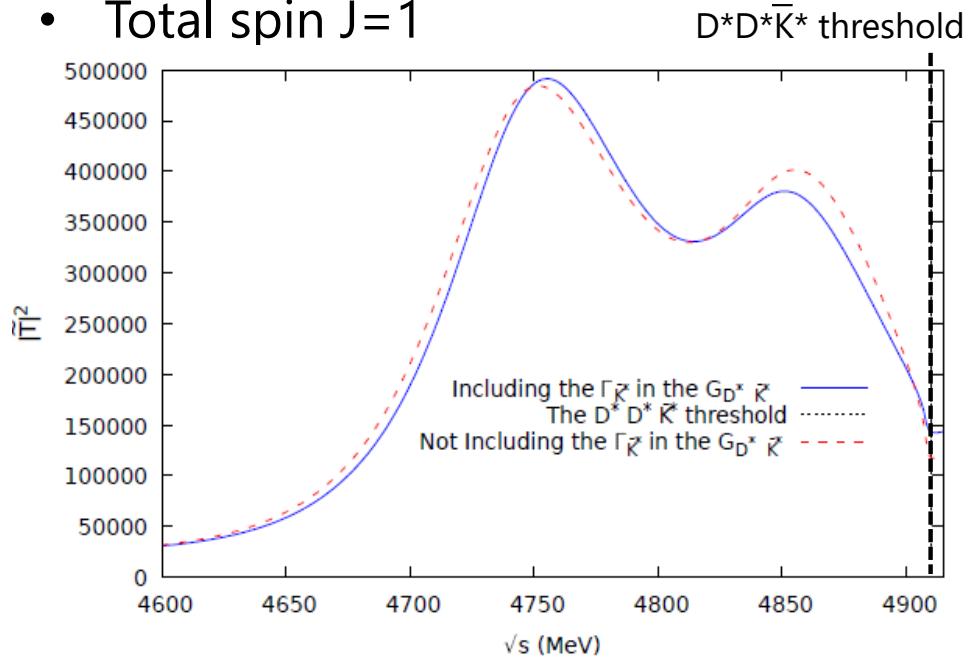
- A peak around 0.7 fm
- The mean square radius ~ 1 fm
 Bigger than that of the proton (0.84 fm),
 Smaller than that of the deuteron (2.1 fm)



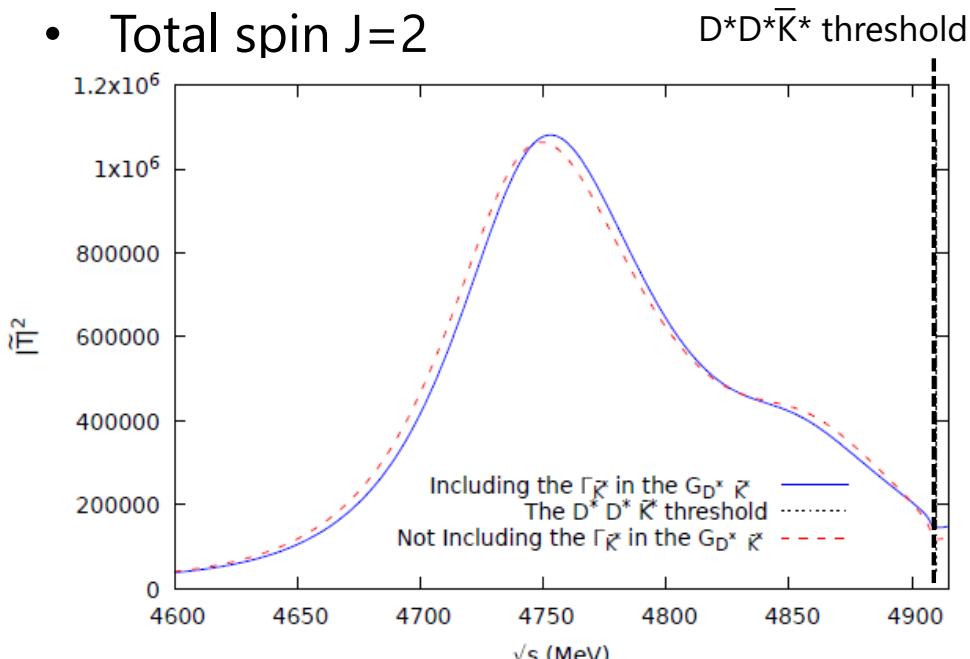
Bound states of $D^* D^* \bar{K}^*$

N. Ikeno, M. Bayar, E. Oset,
PRD107, 034006 (2023)

- Total spin $J=1$



- Total spin $J=2$



We see two peaks, indicating two states

=> Easy to trace the origin of the peaks

- Total spin $J=1$ case

First peak (higher energy) is due to $t^{I=0,j=0,1}$
Second peak is due to $t^{I=0,j=2}$

- Total spin $J=2$ case

First peak (higher energy) is due to $t^{I=0,j=1}$
Second peak is due to $t^{I=0,j=2}$

Spin consideration:

$$\text{For } J=1 \quad t_1 = \frac{1}{4} \left(\frac{4}{3} t_{D^* \bar{K}^*}^{j=0} + t_{D^* \bar{K}^*}^{j=1} + \frac{5}{3} t_{D^* \bar{K}^*}^{j=2} \right).$$

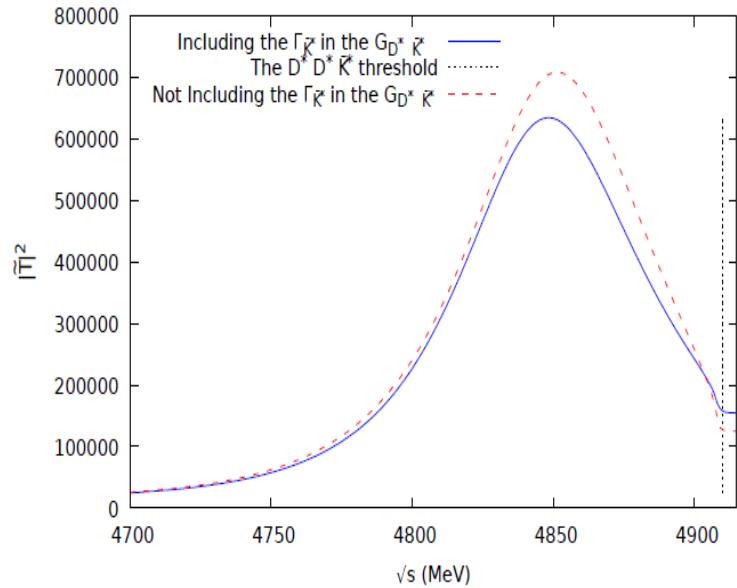
$$\text{For } J=2 \quad t_1 = \frac{1}{4} t_{D^* \bar{K}^*}^{j=1} + \frac{3}{4} t_{D^* \bar{K}^*}^{j=2}$$

$I(J^P)$	$M[\text{MeV}]$	$\Gamma[\text{MeV}]$	Coupled channels	state
$0(2^+)$	2775	38	$D^* \bar{K}^*$?
$0(1^+)$	2861	20	$D^* \bar{K}^*$?
$0(0^+)$	2866	57	$D^* \bar{K}^*$	$X_0(2866)$

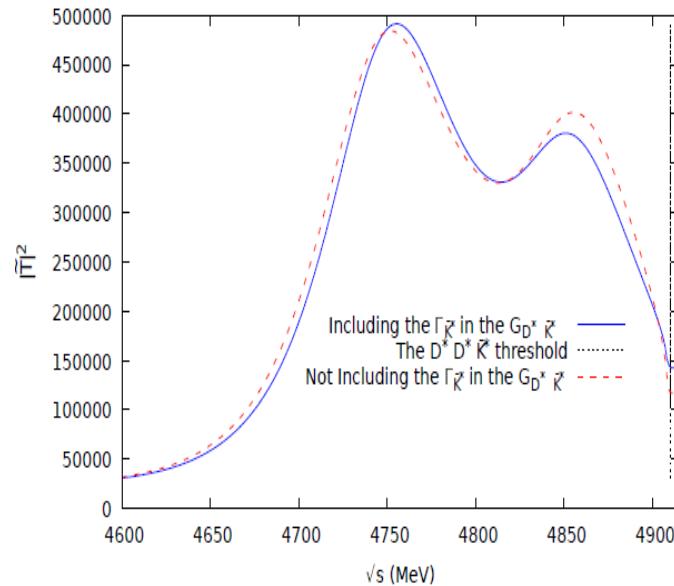
Bound states of $D^* D^* \bar{K}^*$

N. Ikeno, M. Bayar, E. Oset,
PRD107, 034006 (2023)

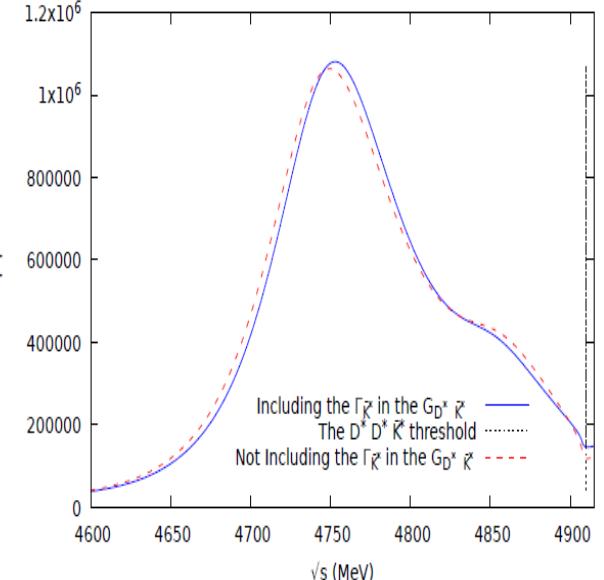
- Total spin $J=0$



- Total spin $J=1$



- Total spin $J=2$



J	M [MeV]	B [MeV]	Γ [MeV]	Main decay mode
0 (State I)	4845	61	80	$D^* D^* \bar{K}$
1 (State I)	4850	56	94	$D^* D \bar{K}$, $D^* D^* \bar{K}$
1 (State II)	4754	152	100	$D^* D \bar{K}$, $D^* D^* \bar{K}$
2 (State I)	4840	66	85	$D^* D^* \bar{K}$
2 (State II)	4755	151	100	$D^* D \bar{K}$, $D^* D^* \bar{K}$

Bound states obtained:
One state for $J = 0$
two states for $J = 1, 2$

$BE = 56$ MeV to 152 MeV
 $\Gamma = 80$ MeV to 100 MeV

Bound states of $\bar{B}^* \bar{B}^* \bar{K}^*$

M. Bayar, N. Ikeno and L. Roca,
PRD107, 054042 (2023)

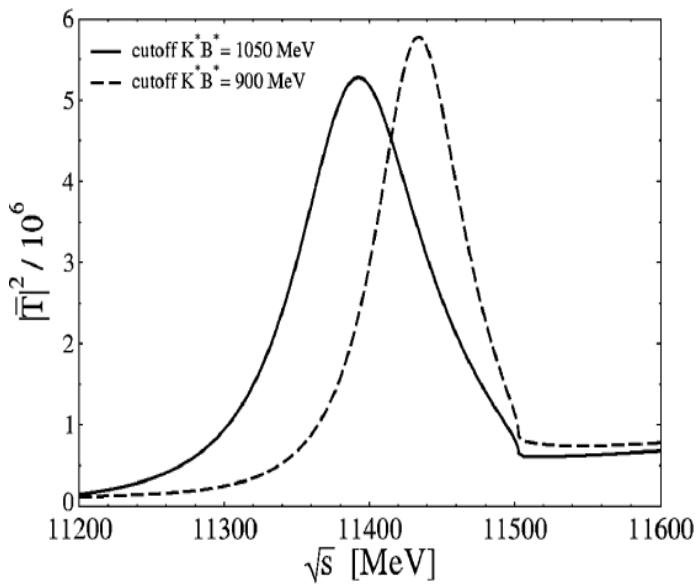
- Similar calculations of $D^* D^* \bar{K}^*$ except the interaction of $\bar{B}^* \bar{B}^* \bar{K}^*$

$\bar{B}^* \bar{K}^*$ interaction is strongly attractive E. Oset and L. Roca, EPJ.C 82 (2022)

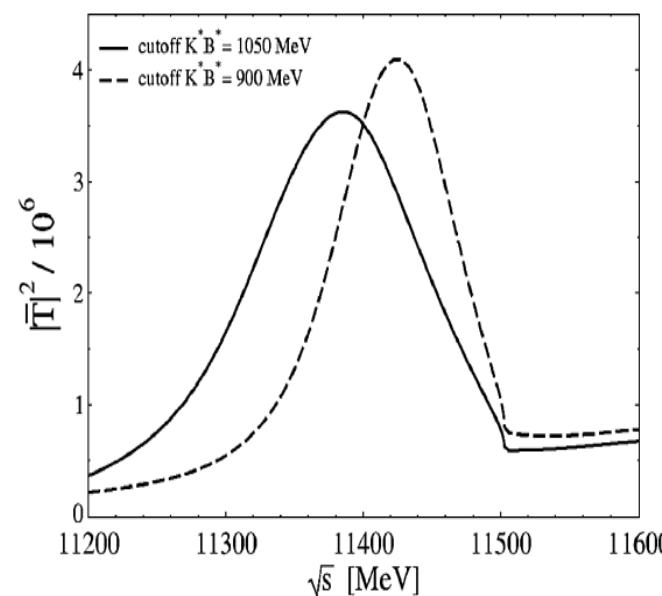
$\bar{B}^* \bar{B}^*$ in $I(J^P) = 0(1^+)$ is bound with BE about 40 MeV

L. R. Dai, E. Oset, A. Feijoo, R. Molina, L. Roca, A. M. Torres and K. P. Khemchandani, PRD 105 (2022)

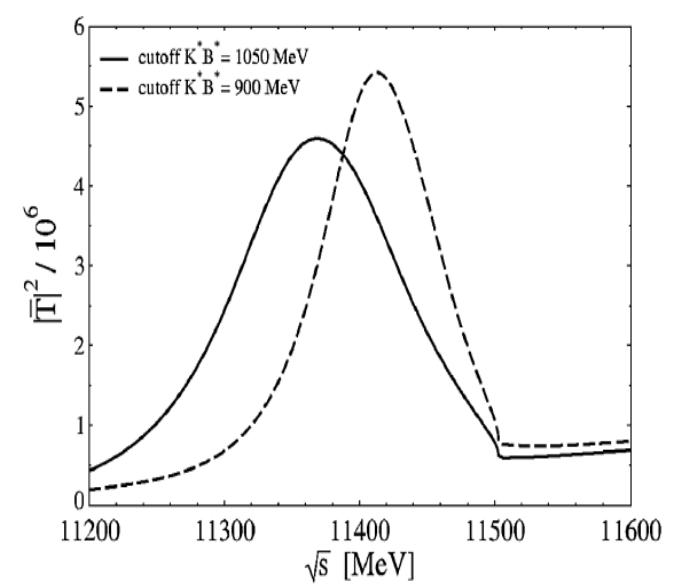
- Total spin $J=0$



- Total spin $J=1$



- Total spin $J=2$



different cutoff parameter of $K^* B^*$
 $q_{\max} = 900, 1050$ MeV

One bound state is obtained for each J

Bound states of $\bar{B}^* \bar{B}^* \bar{K}^*$

M. Bayar, N. Ikeno and L. Roca,
PRD107, 054042 (2023)

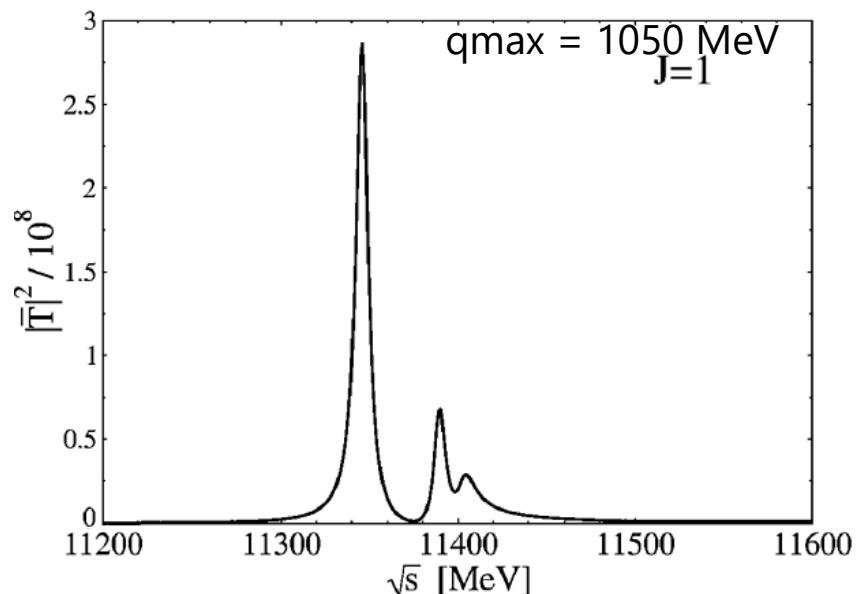
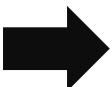
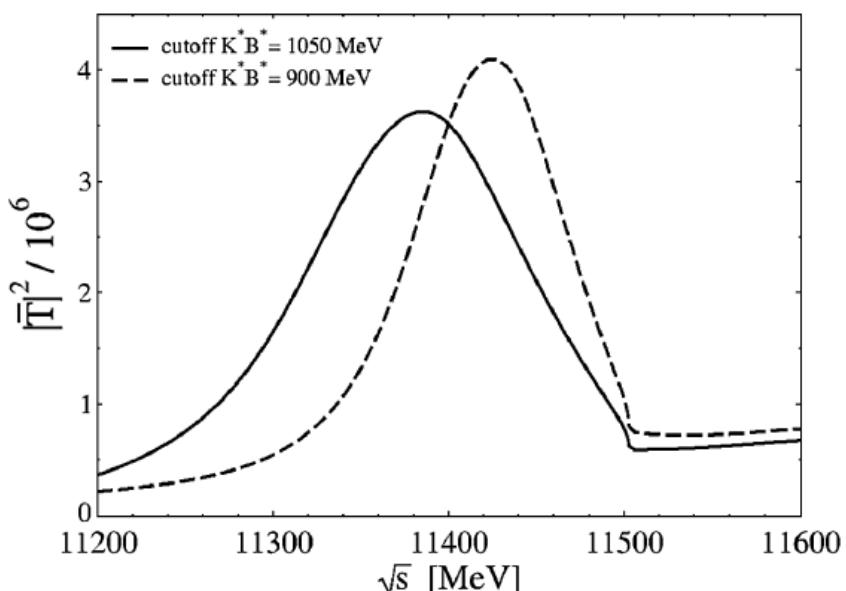
J	E_B [MeV]	Γ [MeV]
0	109–150	72–104
1	118–158	106–153
2	130–174	103–149

BE and Γ are larger than those of $D^* D^* K^*$

$D^* D^* K^*$ case:

BE = 56 - 152 MeV, Γ = 80-100 MeV

- We artificially reduced the dominant source of the imaginary part of the $K^* B^*$ amplitude to 5% of its true value.
We can see three clear narrow peaks in the three-body amplitudes



Summary

Molecular states of $D^*D^*\bar{K}^*$ and $\bar{B}^*\bar{B}^*\bar{K}^*$ nature

- Very exotic hadron contains ccs and bbs open quarks, respectively
- We searched the bound state of three-body system
 - Both D^*D^* and B^*B^* have a bound state in $I=0$.
 - Both D^*K^* and B^*K^* Interactions are attractive.
- We used FCA to the Faddeev equations
- We obtained bound states with total spin $J = 0, 1, 2$ in FCA
- We hope that these super-exotic mesons, with open strange and double-charm(bottom) flavor, can be experimentally found in a near future

Wave function

The unitary approach that we use to obtain the D*D*bound states can be easily visualized as coming from the use of a separable potential of the type

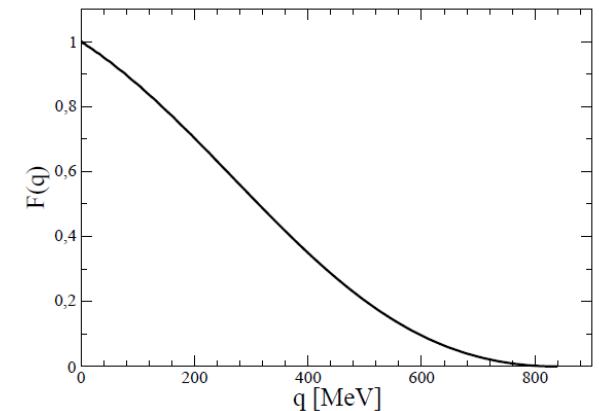
$$V(\vec{q}, \vec{q}') = V\theta(q_{\max} - |\vec{q}|)\theta(q_{\max} - |\vec{q}'|)$$

one can easily deduce **the wave function in momentum space** as

$$\Psi(\vec{p}) = g_R \frac{\theta(q_{\max} - |\vec{p}|)}{E - \omega_1(\vec{p}) - \omega_2(\vec{p})} \quad \text{where } g_R \text{ is the coupling of the state to the two components of the state}$$

The form factor F(q) encodes the information about the D*D* bound state:

$$\begin{aligned} F(\vec{q}) &= \int d^3\vec{r} e^{-i\vec{q}\cdot\vec{r}} \Psi_c^2(\vec{r}) \\ &= \frac{1}{N} \int_{|\vec{p}-\vec{q}| < q_{\max}} d^3p \frac{1}{m_C - \sqrt{m_{D^*}^2 + \vec{p}^2} - \sqrt{m_{D^*}^2 + \vec{p}^2}} \frac{1}{m_C - \sqrt{m_{D^*}^2 + (\vec{p}-\vec{q})^2} - \sqrt{m_{D^*}^2 + (\vec{p}-\vec{q})^2}} \end{aligned}$$



To obtain the wave function in coordinate space we write

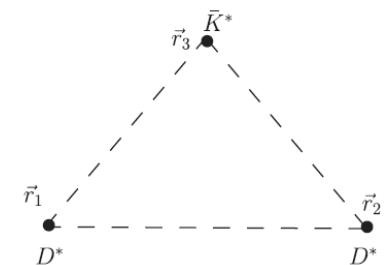
$$\phi(\vec{r}) \equiv \langle \vec{r} | \phi \rangle = \int \frac{d^3q}{(2\pi)^{3/2}} e^{i\vec{q}\cdot\vec{r}} \phi(\vec{q}) \quad e^{i\vec{q}\cdot\vec{r}} = 4\pi \sum_{\ell} i^{\ell} j_{\ell}(qr) \sum_m Y_{\ell m}^*(\hat{q}) Y_{\ell m}(\hat{r}).$$

$$\phi(\vec{r}) = \frac{2\pi}{(2\pi)^{3/2}} g_R \frac{2}{r} \int_0^{q_{\max}} q dq \frac{\sin(qr)}{E - \omega_1(q) - \omega_2(q)}$$

Wave function for the K^* in the $D^*D^*K^*$ system at rest.

- we have a K^* orbiting around the cluster of D^*D^* . The K^* will orbit around one D^* and sometimes around the other D^* . In this picture we can have the K^* distribution given by

$$|\Psi(\vec{r}_3')|^2 = \int d^3 r_1 d^3 r_2 (|\phi(\vec{r}_{31})|^2 + |\phi(\vec{r}_{32})|^2) |\phi'(\vec{r}_{12})|^2 \\ \times \delta^3(m_{D^*} \vec{r}_1 + m_{D^*} \vec{r}_2 + m_{\bar{K}^*} \vec{r}_3),$$



D^{*} K^{*} amplitudes

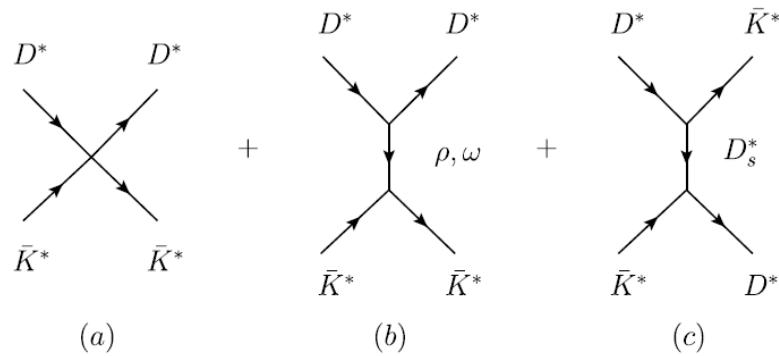


Fig. 1. Feynman diagrams for the terms of the hidden local gauge approach contributing to the $D^* \bar{K}^* \rightarrow D^* \bar{K}^*$ interaction at the tree level; (a) contact term; (b) exchange of light vectors; (c) exchange of a heavy vector.

Tree level amplitudes for D^*K^* in $I = 0$. The last column shows the value of V at threshold.

J	Amplitude	Contact	V-exchange	\sim Total
0	$D^* \bar{K}^* \rightarrow D^* \bar{K}^*$	$4g^2$	$-\frac{g^2(p_1+p_4).(p_2+p_3)}{m_{D_s^*}^2} + \frac{1}{2}g^2(\frac{1}{m_\omega^2} - \frac{3}{m_\rho^2})(p_1+p_3).(p_2+p_4)$	$-9.9g^2$
1	$D^* \bar{K}^* \rightarrow D^* \bar{K}^*$	0	$\frac{g^2(p_1+p_4).(p_2+p_3)}{m_{D_s^*}^2} + \frac{1}{2}g^2(\frac{1}{m_\omega^2} - \frac{3}{m_\rho^2})(p_1+p_3).(p_2+p_4)$	$-10.2g^2$
2	$D^* \bar{K}^* \rightarrow D^* \bar{K}^*$	$-2g^2$	$-\frac{g^2(p_1+p_4).(p_2+p_3)}{m_{D_s^*}^2} + \frac{1}{2}g^2(\frac{1}{m_\omega^2} - \frac{3}{m_\rho^2})(p_1+p_3).(p_2+p_4)$	$-15.9g^2$

TABLE XII. Amplitudes for $C = 1$, $S = -1$ and $I = 1$.

J	Amplitude	Contact	V exchange	~Total
0	$D^* \bar{K}^* \rightarrow D^* \bar{K}^*$	$-4g^2$	$\frac{g^2(p_1+p_4).(p_2+p_3)}{m_{D_s^*}^2} + \frac{g^2}{2}(\frac{1}{m_\omega^2} + \frac{1}{m_\rho^2})(p_1 + p_3).(p_2 + p_4)$	$9.7g^2$
1	$D^* \bar{K}^* \rightarrow D^* \bar{K}^*$	0	$-\frac{g^2(p_1+p_4).(p_2+p_3)}{m_{D_s^*}^2} + \frac{g^2}{2}(\frac{1}{m_\omega^2} + \frac{1}{m_\rho^2})(p_1 + p_3).(p_2 + p_4)$	$9.9g^2$
2	$D^* \bar{K}^* \rightarrow D^* \bar{K}^*$	$2g^2$	$\frac{g^2(p_1+p_4).(p_2+p_3)}{m_{D_s^*}^2} + \frac{g^2}{2}(\frac{1}{m_\omega^2} + \frac{1}{m_\rho^2})(p_1 + p_3).(p_2 + p_4)$	$15.7g^2$

Fig. 2. Box diagram accounting for the width of the $\bar{D}^*\bar{K}^*$ state decaying to $D\bar{K}$.

