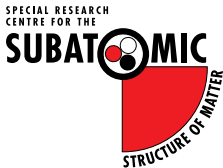


Understanding the nature of baryon resonances

Derek Leinweber

In collaboration with: Curtis Abell, Liam Hockley, Waseem Kamleh,
Yan Li, Zhan-Wei Liu, Finn Stokes, Tony Thomas, Jia-Jun Wu



The spectrum of a simple quark model: N and Λ baryons

$N(1/2+)$ ————— $2h\omega$
~2.0 GeV

$\Lambda(1/2-)$ —————
 $N(1/2-)$ ————— $1h\omega$
~1.5 GeV

$\Lambda(1/2+)$ —————
 $N(1/2+)$ ————— $0h\omega$
~1 GeV Quark Model

The challenge of experiment

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~2.0 GeV



$\Lambda(1/2-)$ —————
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$\Lambda^*(1670)$ —————
 $N^*(1535)$ —————
 $N^*(1440)$ —————
 $\Lambda^*(1405)$ —————

$\Lambda(1/2+)$ —————
 $N(1/2+)$ ————— $0h\omega$
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$\Lambda(1115)$ —————
 $N(940)$ —————
Experiment

Prologue

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- What's new are formalisms able to bring these descriptions to the finite-volume of lattice QCD.
- Lattice QCD calculations of the excitation spectrum provide new constraints.
- It's time to reconsider our early notions about the quark-model and its excitation spectrum.

Outline

- Hamiltonian Effective Field Theory (HEFT)
 - Coupled-channel analysis technique aimed at resonance physics.
 - Incorporates the Lüscher formalism.
 - Connects scattering observables to the finite-volume spectrum of lattice QCD.

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- Roper $N(1440)$ Resonance:
 - Lattice QCD results constrain the HEFT description of experimental data.
 - Poses a new resolution of the missing baryon resonances problem.

Hamiltonian Effective Field Theory (HEFT)

J. M. M. Hall, *et al.* [CSSM], Phys. Rev. D **87** (2013) 094510 [arXiv:1303.4157 [hep-lat]]

C. D. Abell, DBL, A. W. Thomas, J. J. Wu, Phys. Rev. D **106** (2022) 034506 [arXiv:2110.14113 [hep-lat]]

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- Fitting resonance phase-shift data and inelasticities,
 - Predictions of the finite-volume spectrum are made.
- The eigenvectors of the Hamiltonian provide insight into the composition of the energy eigenstates.
 - Insight is similar to that provided by correlation-matrix eigenvectors in Lattice QCD.

Infinite Volume Model

- The rest-frame Hamiltonian has the form $H = H_0 + H_I$, with

$$H_0 = \sum_{B_0} |B_0\rangle m_{B_0} \langle B_0| + \sum_{\alpha} \int d^3k |\alpha(\mathbf{k})\rangle \omega_{\alpha}(\mathbf{k}) \langle \alpha(\mathbf{k})|,$$

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- $|\alpha(\mathbf{k})\rangle$ designates a two-particle non-interacting basis-state channel with energy

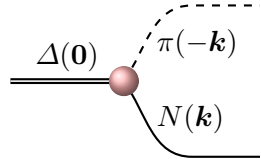
$$\omega_{\alpha}(\mathbf{k}) = \omega_{\alpha_M}(\mathbf{k}) + \omega_{\alpha_B}(\mathbf{k}) = \sqrt{\mathbf{k}^2 + m_{\alpha_M}^2} + \sqrt{\mathbf{k}^2 + m_{\alpha_B}^2},$$

for $M = \text{Meson}$, $B = \text{Baryon}$.

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- The interaction Hamiltonian includes two parts, $H_I = g + v$.
- $1 \rightarrow 2$ particle vertex

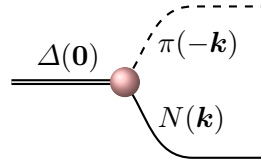
$$g = \sum_{\alpha, B_0} \int d^3k \left\{ |\alpha(\mathbf{k})\rangle G_{\alpha, B_0}^\dagger(k) \langle B_0| + h.c. \right\} ,$$



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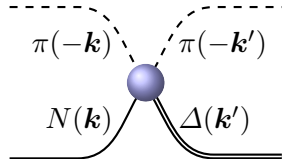
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- $2 \rightarrow 2$ particle vertex

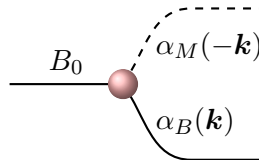
$$v = \sum_{\alpha, \beta} \int d^3k d^3k' |\alpha(\mathbf{k})\rangle V_{\alpha, \beta}^S(k, k') \langle \beta(\mathbf{k}')|.$$



S-wave vertex interactions

- S -wave vertex interactions between the one baryon and two-particle meson-baryon channels for e.g. $N^*(1535)$ or $\Lambda^*(1405)$ cases take the form

$$G_{\alpha,B_0}(k) = g_{B_0\alpha} \frac{\sqrt{3}}{2\pi f_\pi} \sqrt{\omega_{\alpha_M}(k)} u(k, \Lambda),$$



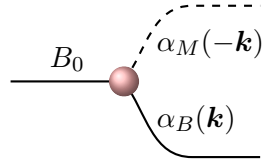
with regulator

$$u(k, \Lambda) = \left(1 + \frac{k^2}{\Lambda^2} \right)^{-2}.$$

P -wave and higher vertex interactions

- P -wave and higher vertex interactions for the $\Delta(1232)$ or $N^*(1440)$ take the form

$$G_{\alpha, B_0}(k) = g_{B_0\alpha} \frac{1}{4\pi^2} \left(\frac{k}{f_\pi} \right)^{l_\alpha} \frac{u(k, \Lambda)}{\sqrt{\omega_{\alpha_M}(k)}},$$



where l_α is the orbital angular momentum in channel α .

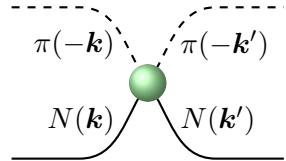
Two-to-two particle interactions

- For the direct two-to-two particle interaction, we introduce separable potentials.

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- For the S_{11} πN channel

$$V_{\pi N, \pi N}^S(k, k') = v_{\pi N, \pi N} \frac{3}{4\pi^2 f_\pi^2} \tilde{u}_{\pi N}(k, \Lambda) \tilde{u}_{\pi N}(k', \Lambda)$$



where the scattering potential gains a low energy enhancement via

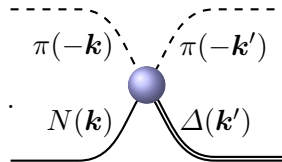
$$\tilde{u}_{\pi N}(k, \Lambda) = u(k, \Lambda) \frac{m_\pi^{\text{phys}} + \omega_\pi(k)}{\omega_\pi(k)}$$

and $u(k, \Lambda)$ takes the dipole form.

Two-to-two particle interactions

- For P -wave scattering in the $\Delta(1232)$ or $N^*(1440)$ channels

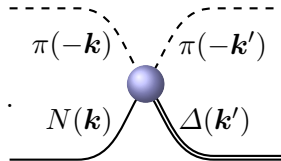
$$V_{\alpha,\beta}^S(k, k') = v_{\alpha,\beta} \frac{1}{4\pi^2 f_\pi^2} \frac{k}{\omega_{\alpha_M}(k)} \frac{k'}{\omega_{\beta_M}(k')} u(k, \Lambda) u(k', \Lambda).$$



Two-to-two particle interactions

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- For the $\Lambda^*(1405)$, the Weinberg-Tomozawa term is considered

$$V_{\alpha,\beta}^S(k, k') = g_{\alpha,\beta}^{\Lambda^*} \frac{[\omega_{\alpha_M}(k) + \omega_{\beta_M}(k')] u(k, \Lambda) u(k', \Lambda)}{16 \pi^2 f_\pi^2 \sqrt{\omega_{\alpha_M}(k) \omega_{\beta_M}(k')}} ,$$

Infinite-Volume scattering amplitude

- The T -matrices for two particle scattering are obtained by solving the coupled-channel integral equations

$$T_{\alpha,\beta}(k, k'; E) = \tilde{V}_{\alpha,\beta}(k, k'; E) + \sum_{\gamma} \int q^2 dq \frac{\tilde{V}_{\alpha,\gamma}(k, q; E) T_{\gamma,\beta}(q, k'; E)}{E - \omega_{\gamma}(q) + i\epsilon}.$$

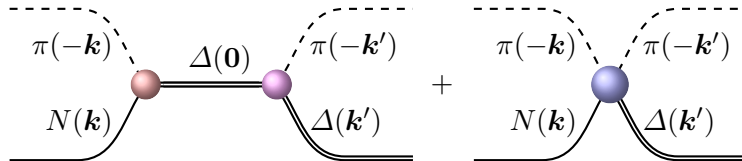
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- The coupled-channel potential is readily calculated from the interaction Hamiltonian

$$\tilde{V}_{\alpha,\beta}(k, k') = \sum_{B_0} \frac{G_{\alpha,B_0}^{\dagger}(k) G_{\beta,B_0}(k')}{E - m_{B_0}} + V_{\alpha,\beta}^S(k, k'),$$



Infinite-Volume scattering matrix

- The S-matrix is related to the T -matrix by

$$S_{\alpha,\beta}(E) = 1 - 2i \sqrt{\rho_{\alpha}(E) \rho_{\beta}(E)} T_{\alpha,\beta}(k_{\alpha \text{ cm}}, k_{\beta \text{ cm}}; E),$$

with

$$\rho_{\alpha}(E) = \pi \frac{\omega_{\alpha_M}(k_{\alpha \text{ cm}}) \omega_{\alpha_B}(k_{\alpha \text{ cm}})}{E} k_{\alpha \text{ cm}},$$

and $k_{\alpha \text{ cm}}$ satisfies the on-shell condition

$$\omega_{\alpha_M}(k_{\alpha \text{ cm}}) + \omega_{\alpha_B}(k_{\alpha \text{ cm}}) = E.$$

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- The cross section $\sigma_{\alpha,\beta}$ for the process $\alpha \rightarrow \beta$ is

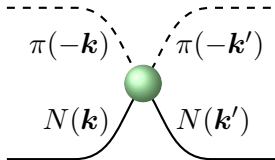
$$\sigma_{\alpha,\beta} = \frac{4\pi^3 k_{\alpha \text{ cm}} \omega_{\alpha_M}(k_{\alpha \text{ cm}}) \omega_{\alpha_B}(k_{\alpha \text{ cm}}) \omega_{\beta_M}(k_{\alpha \text{ cm}}) \omega_{\beta_B}(k_{\alpha \text{ cm}})}{E^2 k_{\beta \text{ cm}}} |T_{\alpha,\beta}(k_{\alpha \text{ cm}}, k_{\beta \text{ cm}}; E)|^2.$$

πN phase shift and inelasticity

- The S-matrix is related to the T -matrix by

$$\begin{aligned} S_{\pi N, \pi N}(E) &= 1 - 2i\pi \frac{\omega_\pi(k_{\text{cm}}) \omega_N(k_{\text{cm}})}{E} k_{\text{cm}} T_{\pi N, \pi N}(k_{\text{cm}}, k_{\text{cm}}; E), \\ &= \eta(E) e^{2i\delta(E)}. \end{aligned}$$

- In solving for the energy eigenstates...

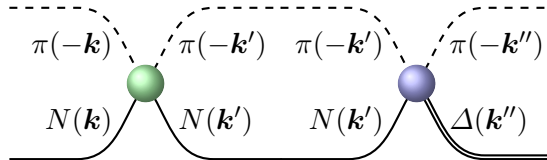


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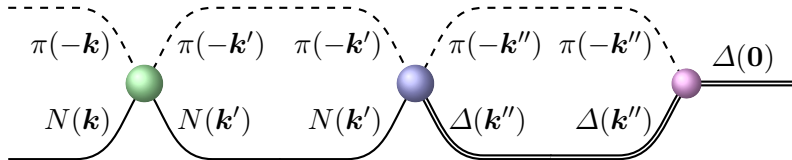


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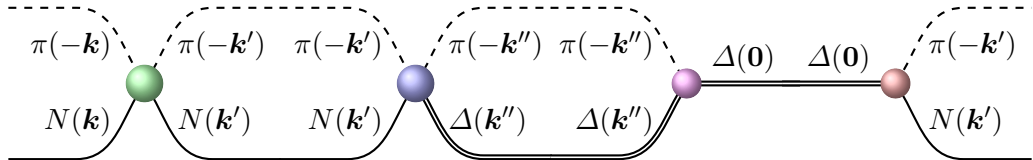


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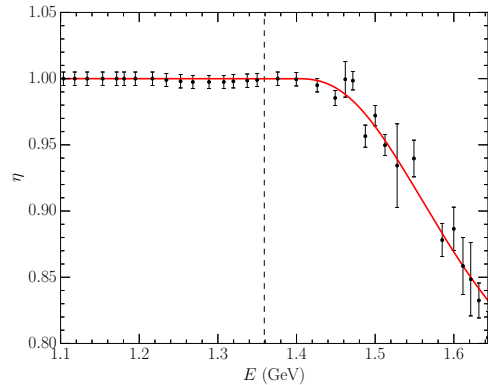
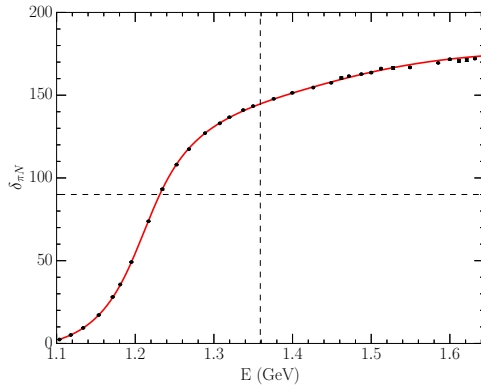
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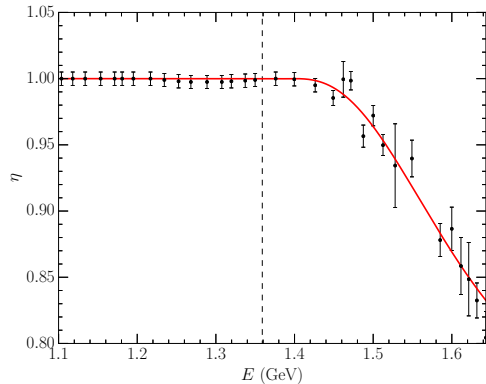
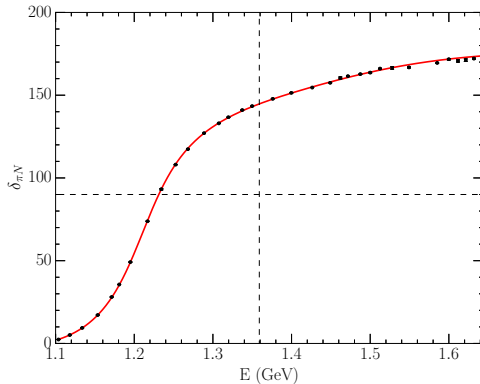
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P -wave πN scattering in the Δ channel - 2 channel πN and $\pi\Delta$



P -wave πN scattering in the Δ channel - 2 channel πN and $\pi\Delta$



- Here $\Lambda = 0.8$ GeV, but $0.6 \leq \Lambda \leq 1.2$ GeV is acceptable.

Finite Volume Analysis - Hamiltonian Matrix

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with $n_i = 0, 1, 2, \dots$ and integer $n = n_x^2 + n_y^2 + n_z^2$.

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- The degeneracy of each k_n is described by $C_3(n)$, which counts the number of ways the integers n_x , n_y , and n_z , can be squared and summed to n .
- The non-interacting Hamiltonian takes the form

$$H_0 = \text{diag}(m_{B_0}, \omega_{\pi N}(k_0), \omega_{\pi \Delta}(k_0), \omega_{\pi N}(k_1), \omega_{\pi \Delta}(k_1), \dots)$$

Interaction Hamiltonian Terms

- $1 \rightarrow 2$ particle interaction terms sit in the first row and column.

$$H_I = \begin{pmatrix} 0 & \overline{G}_{\pi N, B_0}(k_0) & \cdots & \overline{G}_{\pi \Delta, B_0}(k_0) & \overline{G}_{\pi N, B_0}(k_1) & \cdots & \overline{G}_{\pi \Delta, B_0}(k_1) \cdots \\ \overline{G}_{\pi N, B_0}^\dagger(k_0) & 0 & & & & & \\ \vdots & & 0 & & & & \\ \overline{G}_{\pi \Delta, B_0}^\dagger(k_0) & & & \ddots & & & \\ \overline{G}_{\pi N, B_0}^\dagger(k_1) & & & & & & \\ \vdots & & & & & & \\ \overline{G}_{\pi \Delta, B_0}^\dagger(k_1) & & & & & & \\ \vdots & & & & & & \end{pmatrix}.$$

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- \cdots allow for additional channels.
- $2 \rightarrow 2$ particle interaction terms, $\overline{V}_{\alpha, \beta}^S(k_n, k_{n'})$, fill out the rest of the matrix.

Relation to infinite-volume contributions

- The finite volume Hamiltonian interaction terms are related to the infinite-volume contributions via

$$\int k^2 dk = \frac{1}{4\pi} \int d^3k \rightarrow \frac{1}{4\pi} \sum_{n \in \mathbb{Z}^3} \left(\frac{2\pi}{L} \right)^3 = \frac{1}{4\pi} \sum_{n \in \mathbb{Z}} C_3(n) \left(\frac{2\pi}{L} \right)^3 .$$

such that

$$\begin{aligned} \bar{G}_{\alpha, B_0}(k_n) &= \sqrt{\frac{C_3(n)}{4\pi}} \left(\frac{2\pi}{L} \right)^{\frac{3}{2}} G_{\alpha, B_0}(k_n) , \\ \bar{V}_{\alpha\beta}^S(k_n, k_m) &= \sqrt{\frac{C_3(n)}{4\pi}} \sqrt{\frac{C_3(m)}{4\pi}} \left(\frac{2\pi}{L} \right)^3 V_{\alpha\beta}^S(k_n, k_m) . \end{aligned}$$

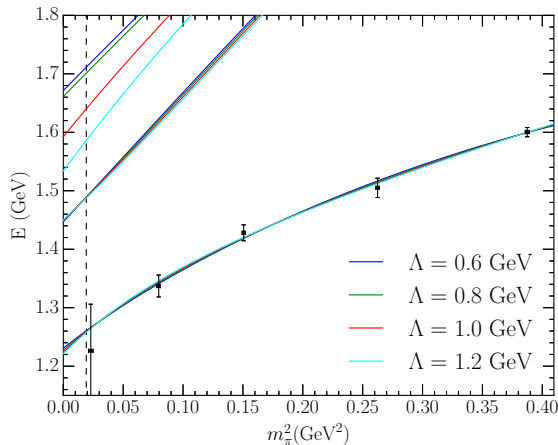
Finite Volume Eigenmode Solution

- Standard Lapack routines provide eigenmode solutions of

$$\langle i | H | j \rangle \langle j | E_\alpha \rangle = E_\alpha \langle i | E_\alpha \rangle,$$

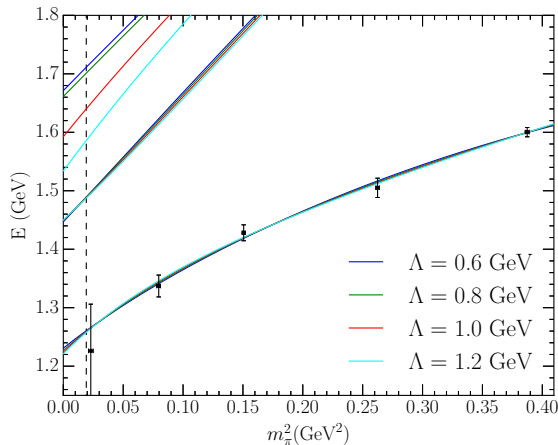
- where $|i\rangle$ and $|j\rangle$ are the non-interacting basis states,
- E_α is the energy eigenvalue, and
- $\langle i | E_\alpha \rangle$ is the eigenvector of the
- Hamiltonian matrix $\langle i | H | j \rangle$.

Mass dependence of energy eigenstates - Fit to PACS-CS Δ masses



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- Physical results extended via $m_0 \rightarrow m_0(m_\pi^2)$.
- Lattice QCD results can constrain the Hamiltonian description of experimental data.

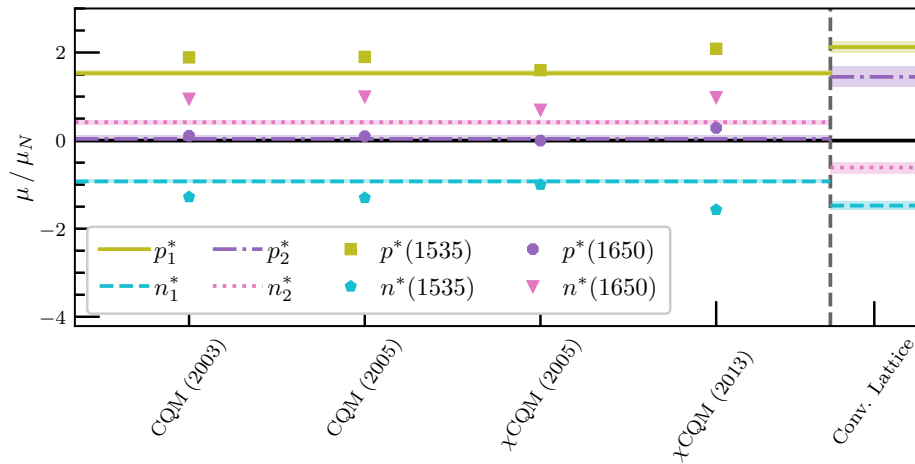
New examination of low-lying odd-parity nucleon resonances

- Motivated by lattice QCD calculations of the electromagnetic form factors of the two low-lying odd-parity states.

F. M. Stokes, W. Kamleh, DBL, Phys. Rev. D **102** (2020) 014507 [arXiv:1907.00177 [hep-lat]].

- Confirms quark model predictions for N^* magnetic moments.

N^* Magnetic Moments and the constituent quark model $m_\pi = 702$ MeV



F. M. Stokes, W. Kamleh, DBL, Phys. Rev. D **102** (2020) 014507 [arXiv:1907.00177 [hep-lat]].

Model Calculation References

- CQM (2003)

W.-T. Chiang, S. N. Yang, M. Vanderhaeghen, and D. Drechsel, Magnetic dipole moment of the S 11 (1535) from the $\gamma p \rightarrow \gamma \eta p$ reaction, Nucl. Phys. **A723**, 205 (2003), nucl-th/0211061

- χ CQM (2005)

J. Liu, J. He, and Y. Dong, Magnetic moments of negative-parity low-lying nucleon resonances in quark models, Phys. Rev. **D71**, 094004 (2005).

- χ CQM (2013)

N. Sharma, A. Martinez Torres, K. Khemchandani, and H. Dahiya, Magnetic moments of the low-lying $1/2^-$ octet baryon resonances, Eur. Phys. J. **A49**, 11 (2013), arXiv:1207.3311

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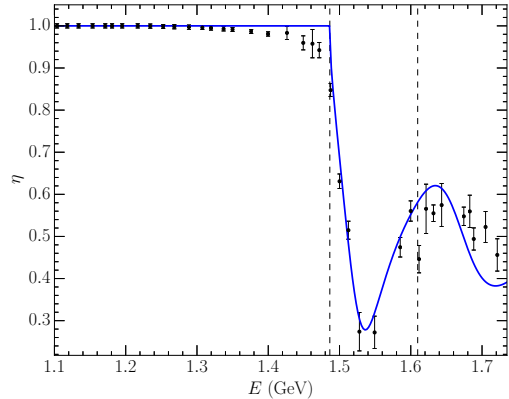
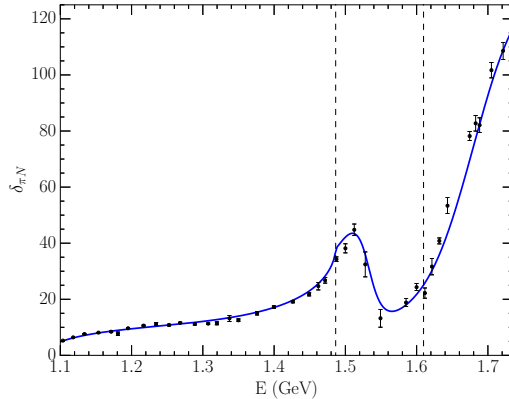
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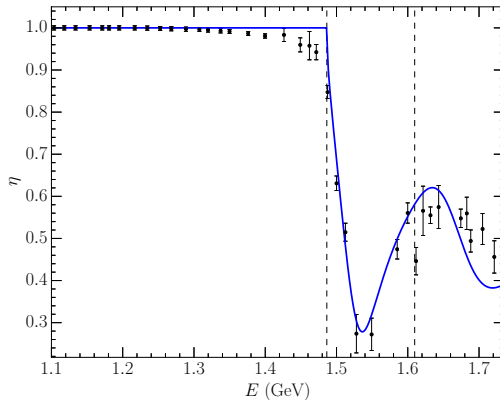
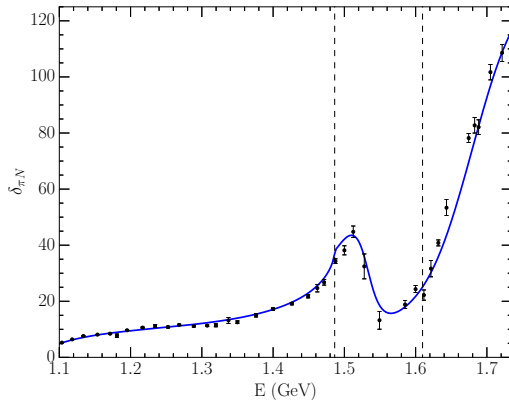
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 - Pole positions agree with PDG.

Phase shift and inelasticity for the low-lying odd-parity spin-1/2 nucleon resonances



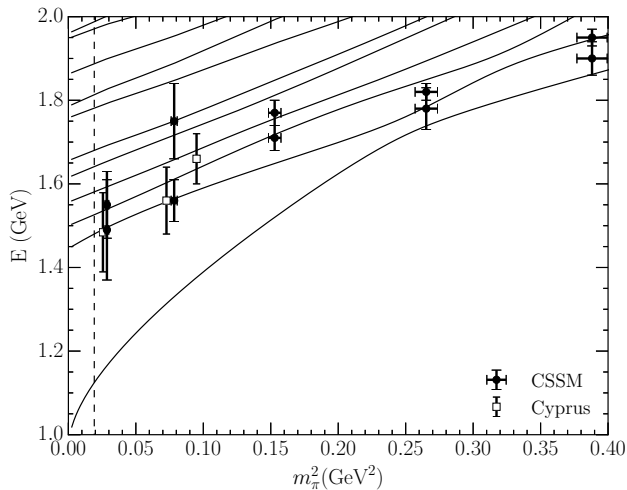
- WI08 single-energy data from SAID.
- Vertical lines indicate the opening of the ηN and $K\Lambda$ thresholds.

Phase shift and inelasticity for the low-lying odd-parity spin-1/2 nucleon resonances

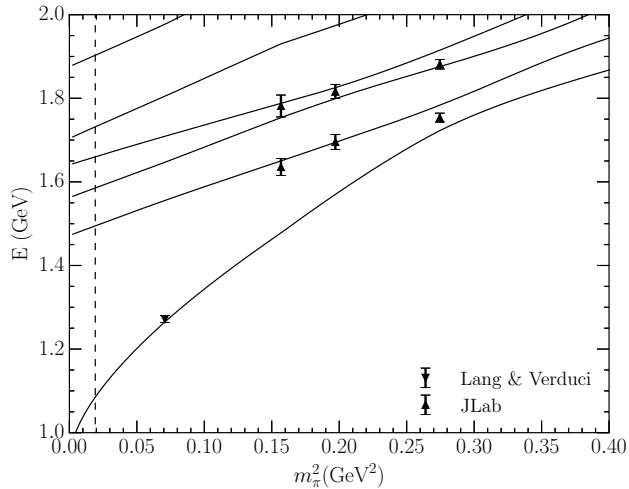


- WI08 single-energy data from SAID.
- Note the three-body $\pi\pi N$ threshold at 1.22 GeV.

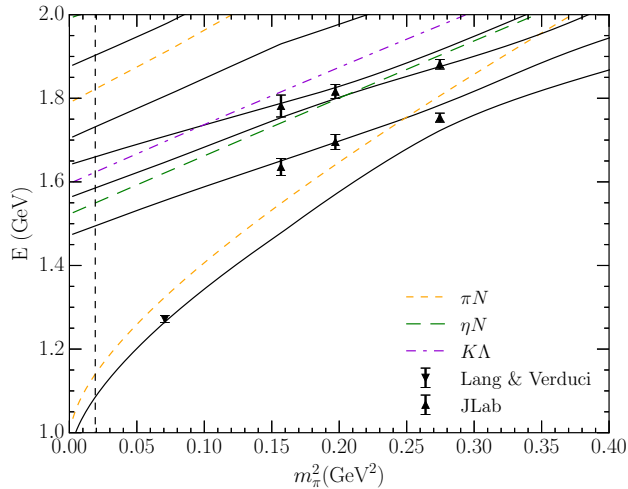
Finite-volume $L = 3$ fm energy levels for low-lying odd-parity spin-1/2 nucleons



Finite-volume $L = 2$ fm energy levels for low-lying odd-parity spin-1/2 nucleons



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Finite Volume Eigenmode Solution

- Standard Lapack routines provide eigenmode solutions of

$$\langle i | H | j \rangle \langle j | E_\alpha \rangle = E_\alpha \langle i | E_\alpha \rangle.$$

- Eigenvector $\langle i | E_\alpha \rangle$ describes the composition of the eigenstate $| E_\alpha \rangle$ in terms of the basis states $| i \rangle$ with

$$| i \rangle = | B_0 \rangle, \quad | \pi N, k_0 \rangle, \quad | \pi N, k_1 \rangle, \quad \cdots | \eta N, k_0 \rangle, \quad | \eta N, k_1 \rangle, \quad \cdots.$$

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- The overlap of the bare basis state $| B_0 \rangle$ with eigenstate $| E_\alpha \rangle$,

$$\langle B_0 | E_\alpha \rangle,$$

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relative to the ground state.

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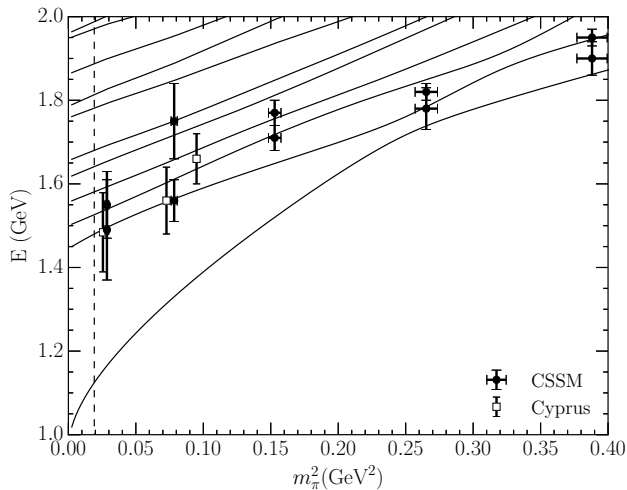
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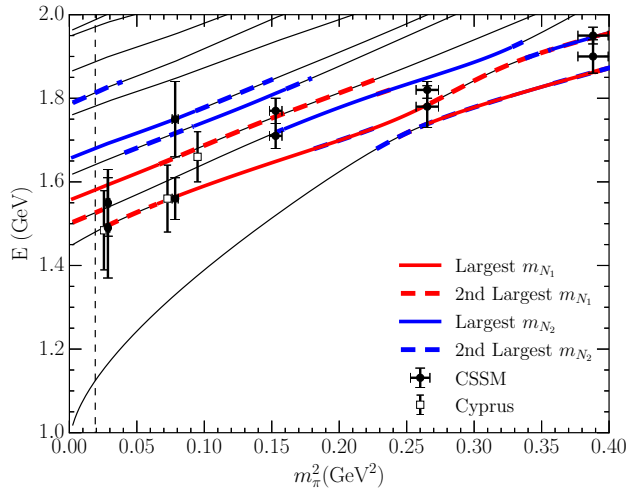
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- Element $\langle B_0 | E_\alpha \rangle$ of the eigenvector governs the likelihood of observing $|E_\alpha\rangle$.

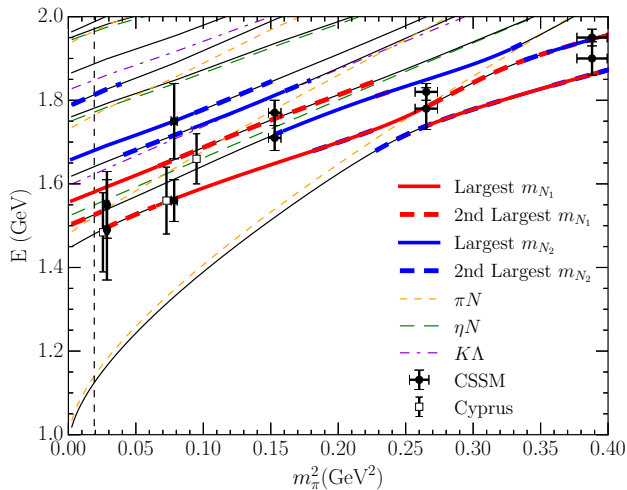
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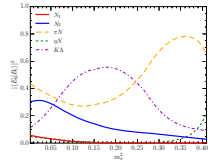
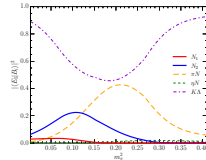
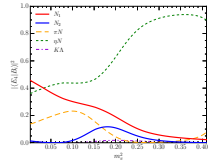
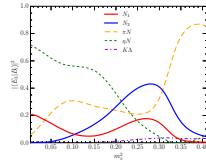
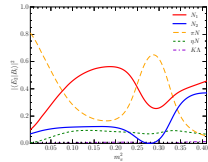
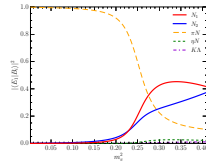
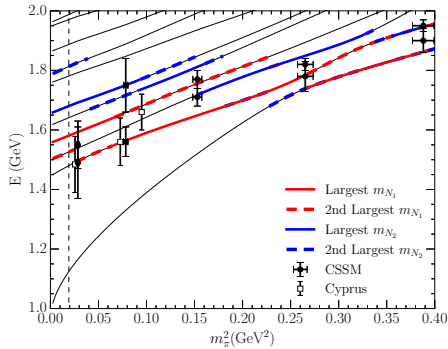
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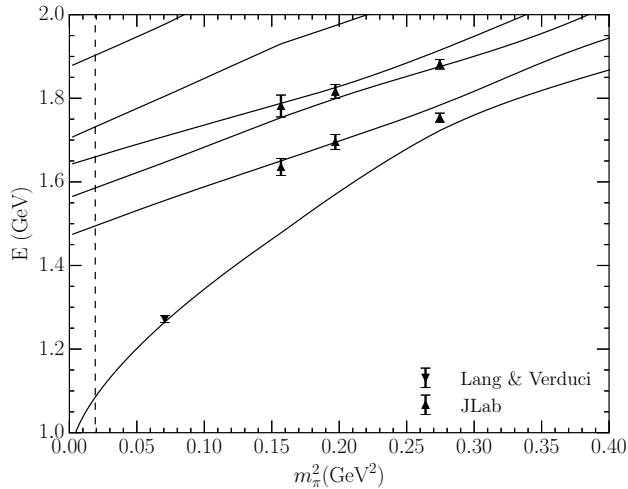
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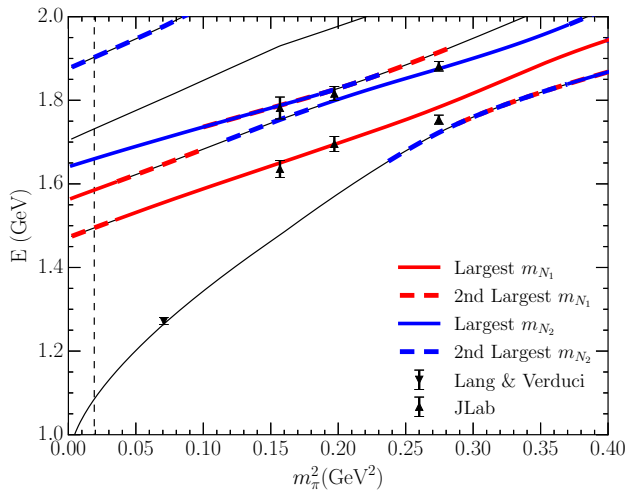
Energy eigenstate composition - 3 fm lattice



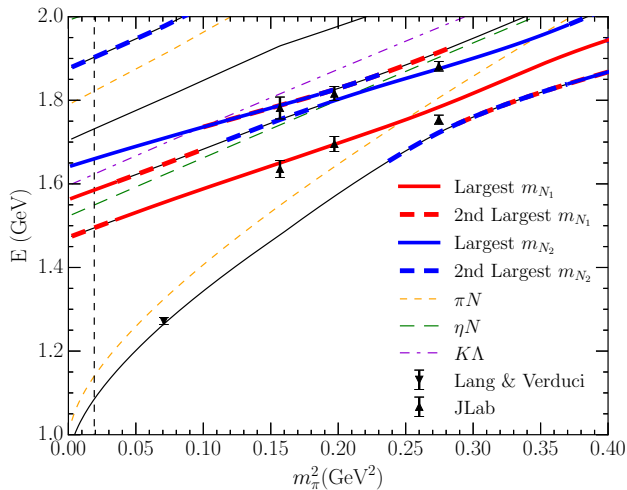
Finite-volume $L = 2$ fm energy levels for low-lying odd-parity spin-1/2 nucleons



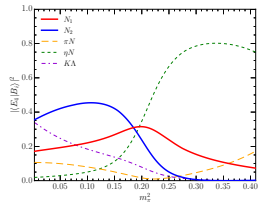
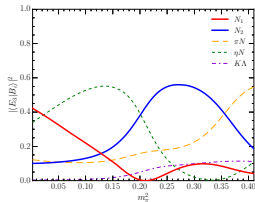
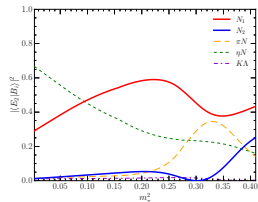
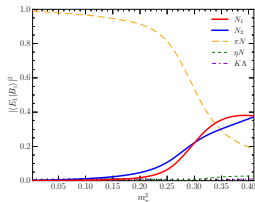
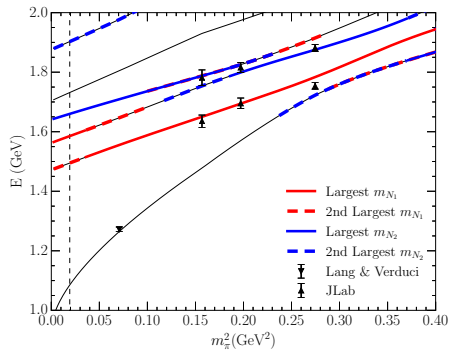
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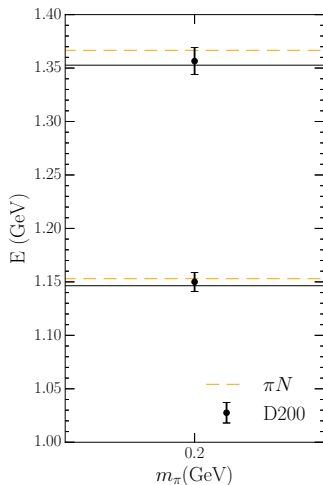
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Energy eigenstate composition - 2 fm lattice



CLS Consortium finite-volume lattice energies relevant to $N1/2^-$ channel



- Solid lines are HEFT energy eigenvalues.
- Bullets are lattice QCD results from

J. Bulava, *et al.*, Nucl. Phys. B **987** (2023), 116105 [arXiv:2208.03867 [hep-lat]].

Analysis of low-lying odd-parity Λ resonances

Z. W. Liu, *et al.* [CSSM], Phys. Rev. D **95** (2017) 014506 [arXiv:1607.05856 [nucl-th]]

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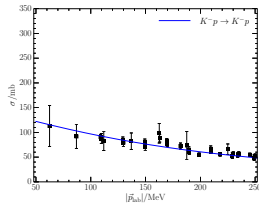
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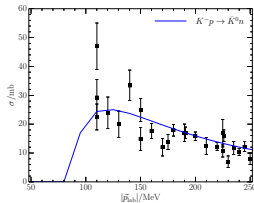
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- These 13 parameters are constrained by experimental data.

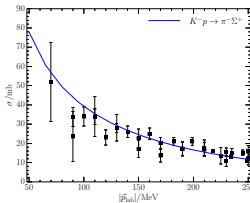
Couplings and m_{B_0} Constrained by Experiment



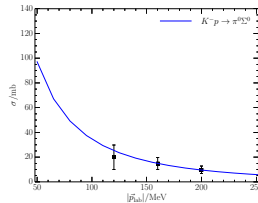
(a) $K^- p \rightarrow K^- p$



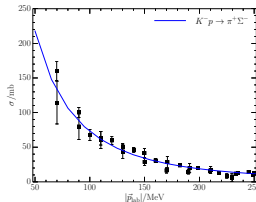
(b) $K^- p \rightarrow \bar{K}^0 n$



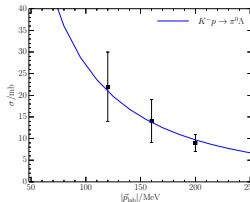
(c) $K^- p \rightarrow \pi^- \Sigma^+$



(d) $K^- p \rightarrow \pi^0 \Sigma^0$

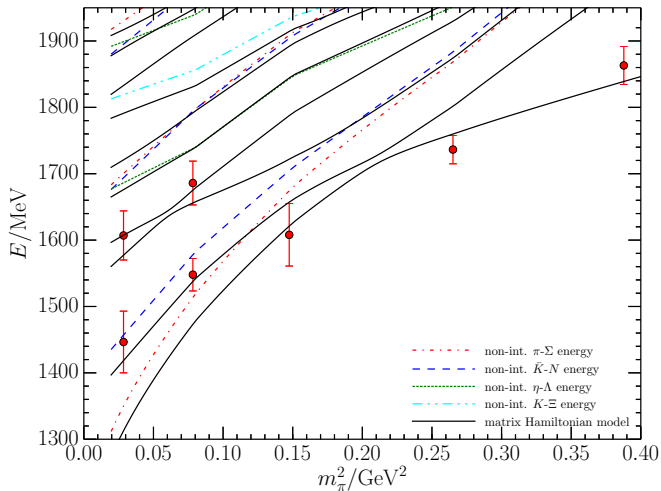


(e) $K^- p \rightarrow \pi^+ \Sigma^-$

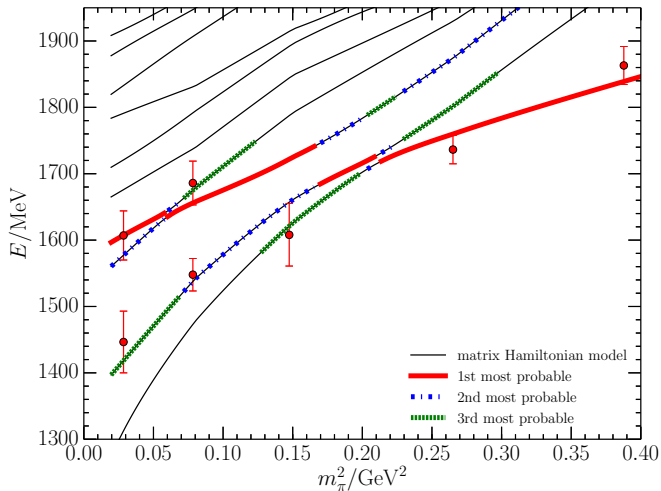


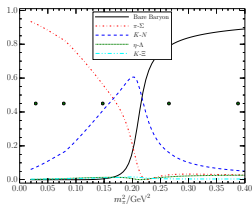
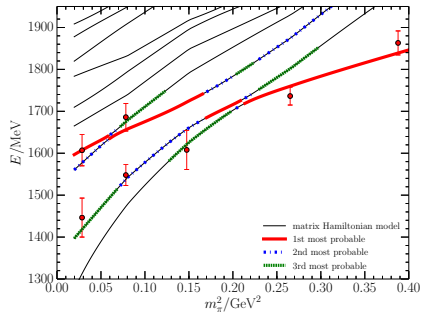
(f) $K^- p \rightarrow \pi^0 \Lambda$

Finite Volume Λ Spectrum for $L = 3$ fm

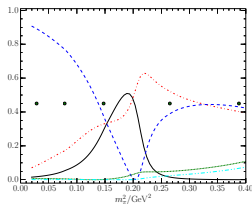


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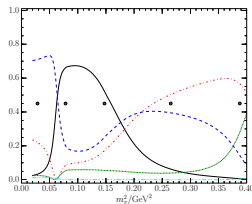




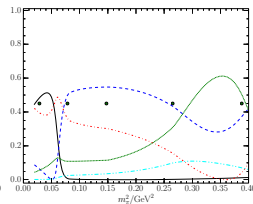
(a) State 1



(b) State 2

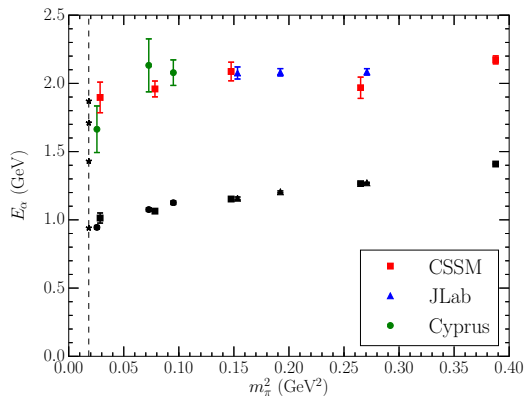


(c) State 3



(d) State 4

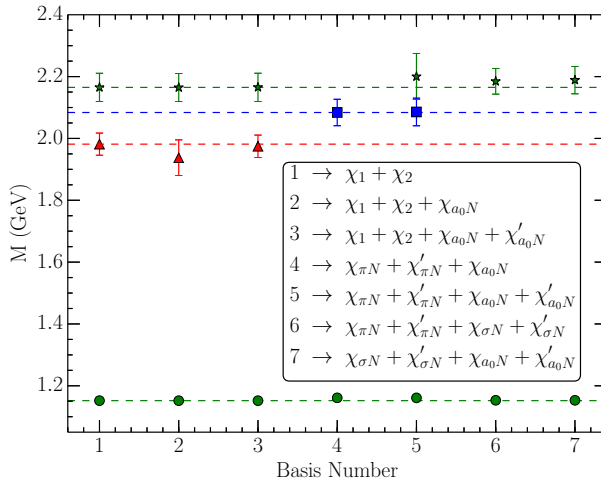
Where is the Roper resonance?



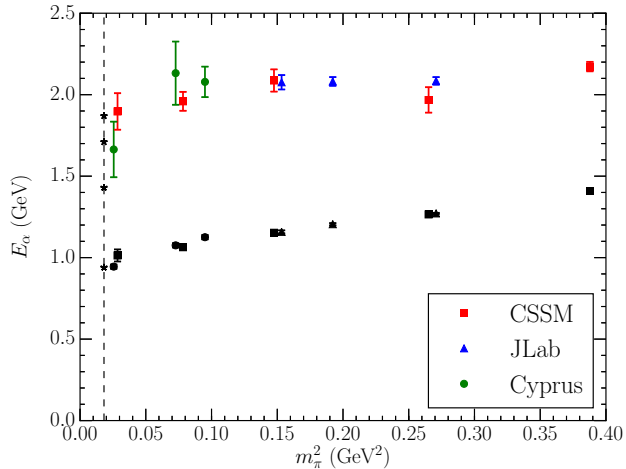
- Cyprus: C. Alexandrou, *et al.* (AMIAS), Phys. Rev. D **91**, 014506 (2015) arXiv:1411.6765 [hep-lat]
- CSSM: Z. W. Liu, *et al.* [CSSM], Phys. Rev. D **95**, 034034 (2017) arXiv:1607.04536 [nucl-th]
- JLab: R. G. Edwards, *et al.* [HSC] Phys. Rev. D **84**, 074508 (2011) [arXiv:1104.5152 [hep-ph]].

Search for low-lying lattice QCD eigenstates in the Roper regime

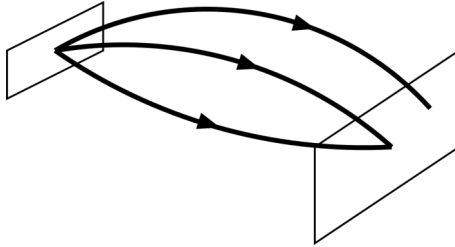
A. L. Kiratidis, *et al.*, [CSSM] Phys. Rev. D **95**, no. 7, 074507 (2017) [arXiv:1608.03051 [hep-lat]].



Have we seen the $2s$ excitation of the quark model?

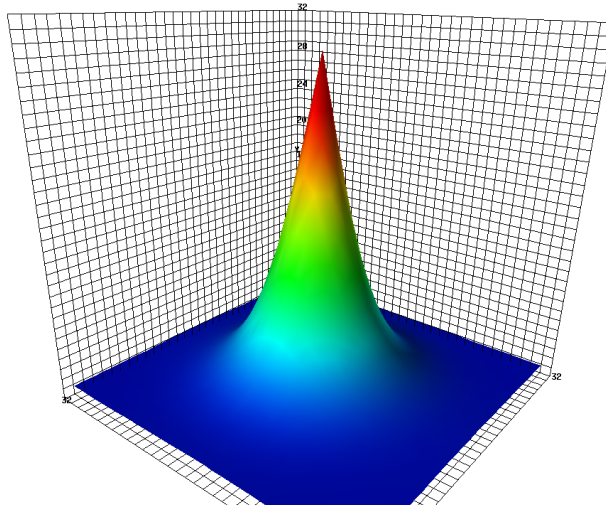


Landau-Gauge Wave functions from the Lattice

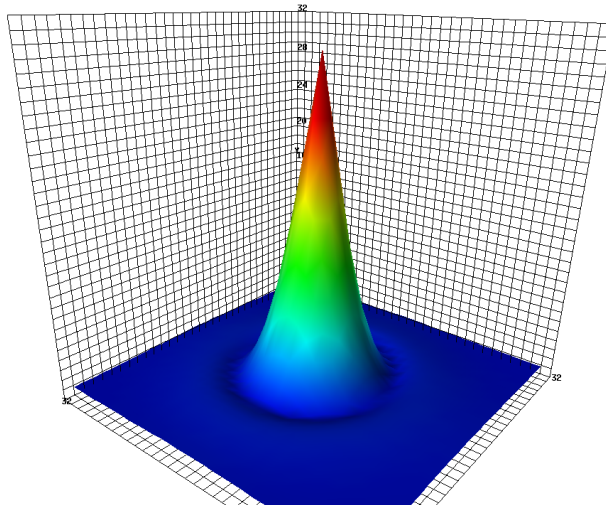


- Measure the *overlap* of the annihilation operator with the state as a function of the quark positions.

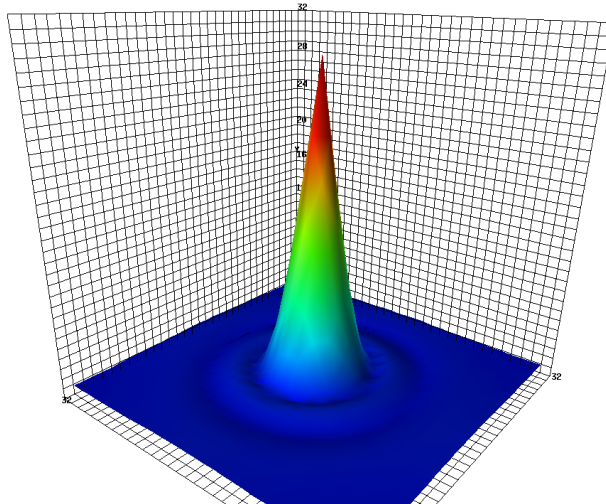
d -quark probability density in ground state proton [CSSM]



d -quark probability density in 1st excited state of proton [CSSM]

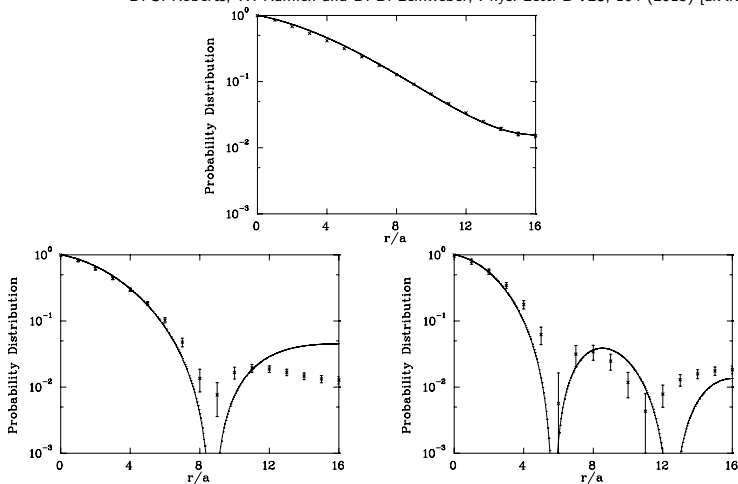


d -quark probability density in $N = 3$ excited state of proton [CSSM]

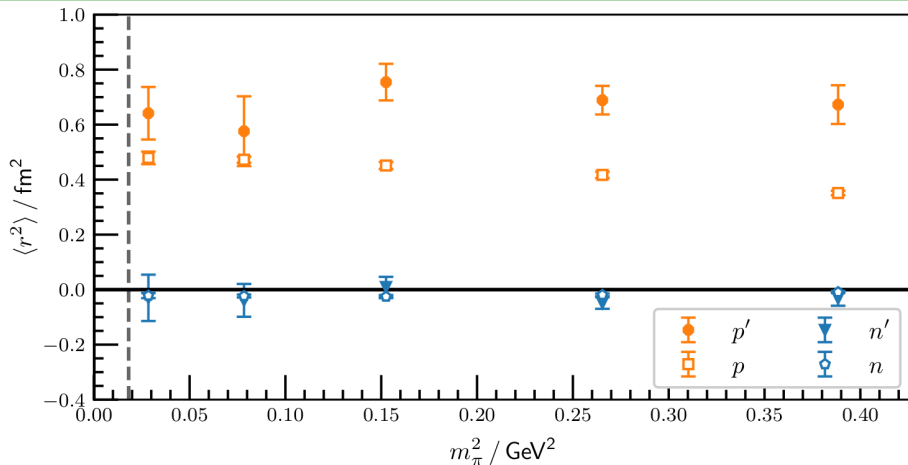


Comparison with the Simple Quark Model [CSSM]

D. S. Roberts, W. Kamleh and D. B. Leinweber, Phys. Lett. B **725**, 164 (2013) [arXiv:1304.0325 [hep-lat]].

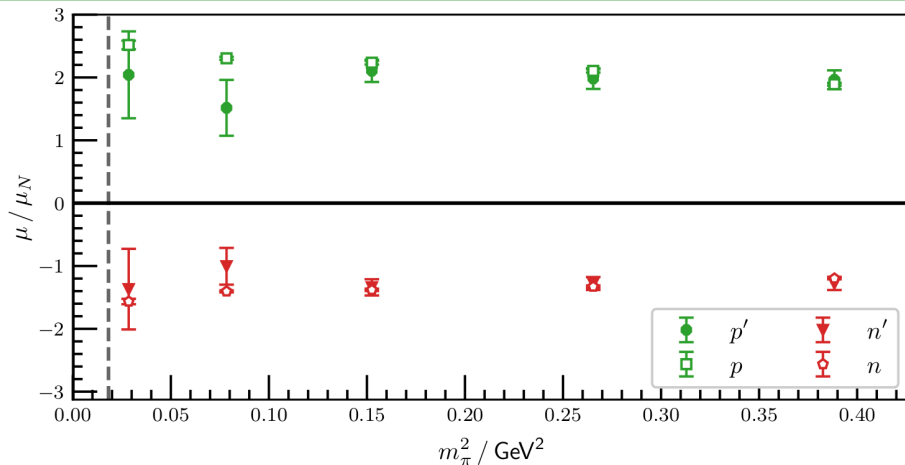


First positive-parity excitation: Charge Radii



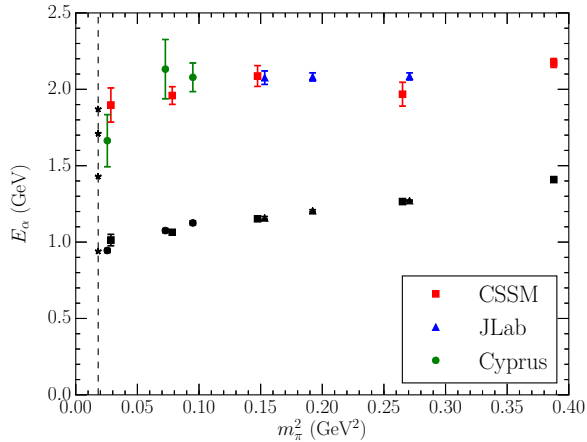
F. M. Stokes, W. Kamleh, DBL, Phys. Rev. D **102** (2020) 014507 [arXiv:1907.00177 [hep-lat]].

First positive-parity excitation: Magnetic moments

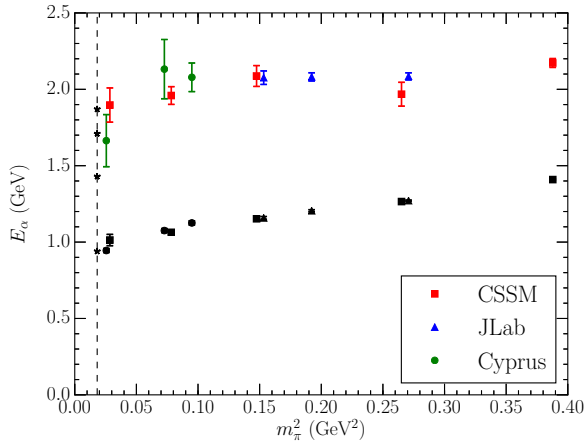


F. M. Stokes, W. Kamleh, DBL, Phys. Rev. D **102** (2020) 014507 [arXiv:1907.00177 [hep-lat]].

The $2s$ excitation of the nucleon sits at 1.9 GeV

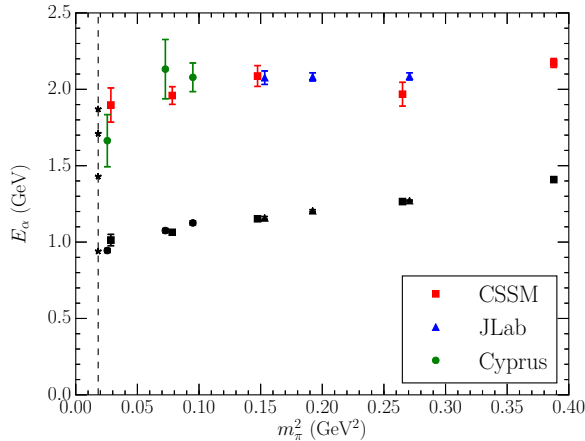


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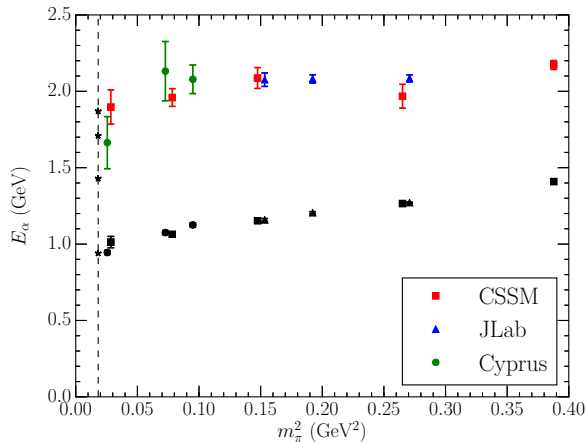
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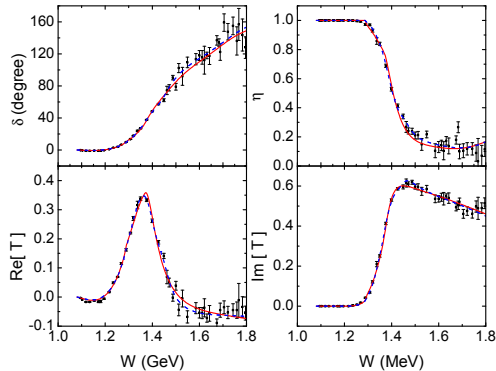
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- What about the Roper resonance?

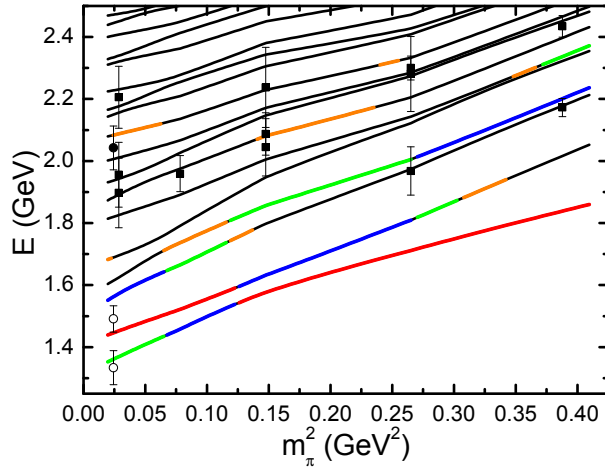
Positive-parity Nucleon Spectrum: Bare Basis State with $m_0 = 1.7$ GeV

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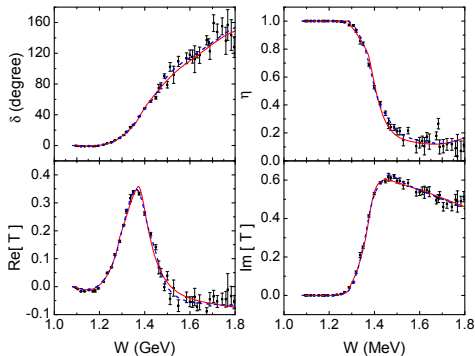
1.7 GeV Bare Basis State: Hamiltonian Model N' Spectrum



Positive-parity Nucleon Spectrum: Bare Basis State with $m_0 = 2.0$ GeV

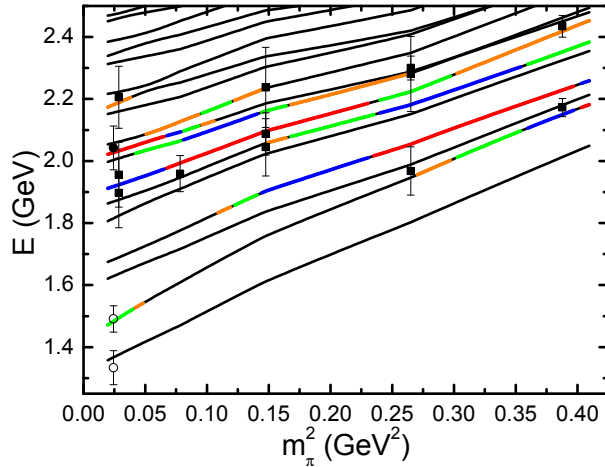
J. j. Wu, *et al.* [CSSM], arXiv:1703.10715 [nucl-th]

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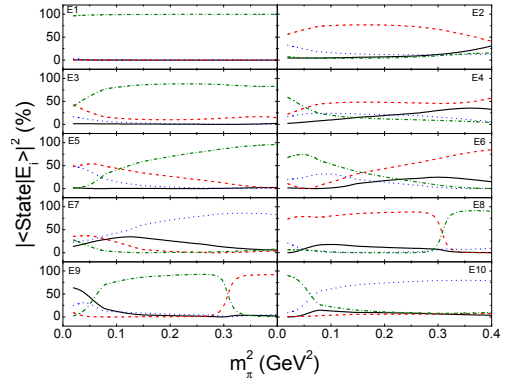
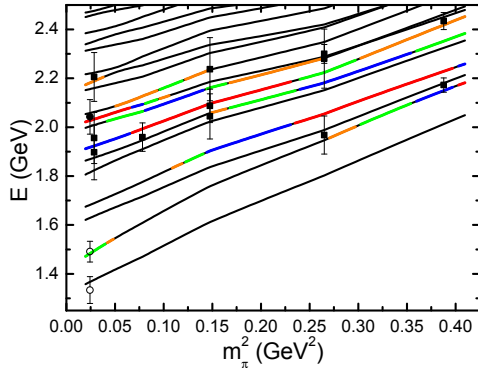


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2.0 GeV Bare Basis State: Hamiltonian Model N' Spectrum



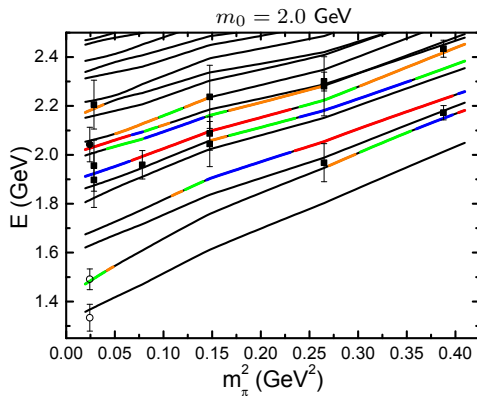
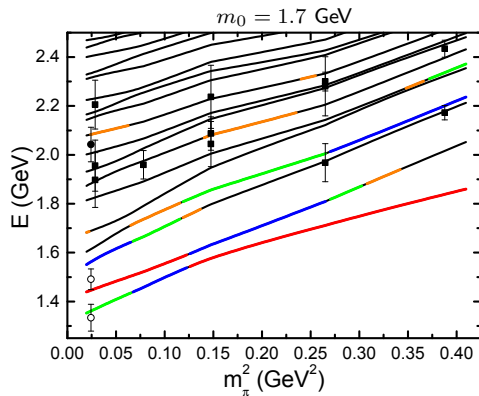
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C. B. Lang, L. Leskovec, M. Padmanath and S. Prelovsek, Phys. Rev. D **95**, no. 1, 014510 (2017) [arXiv:1610.01422 [hep-lat]].

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(left) Meson dressings of a quark-model like core.

(right) Resonance generated by strong rescattering in meson-baryon channels.

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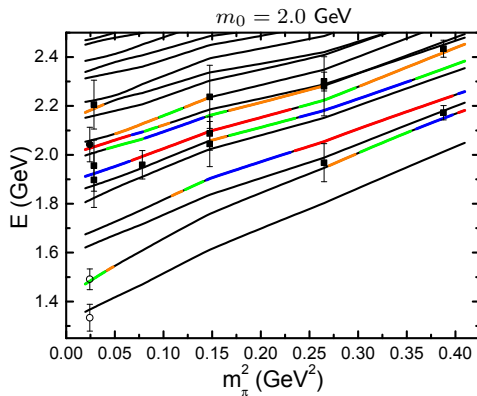
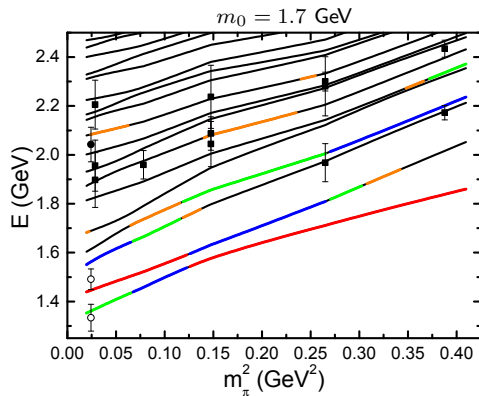
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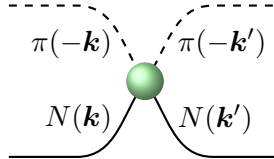
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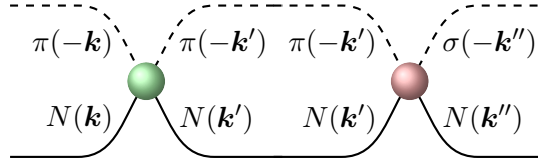
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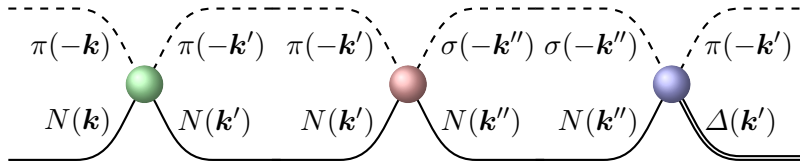
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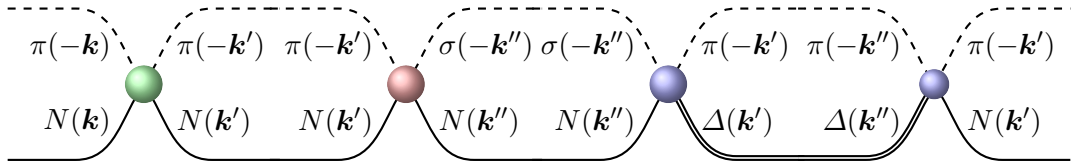
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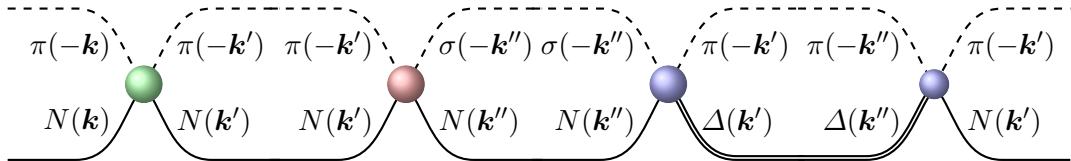
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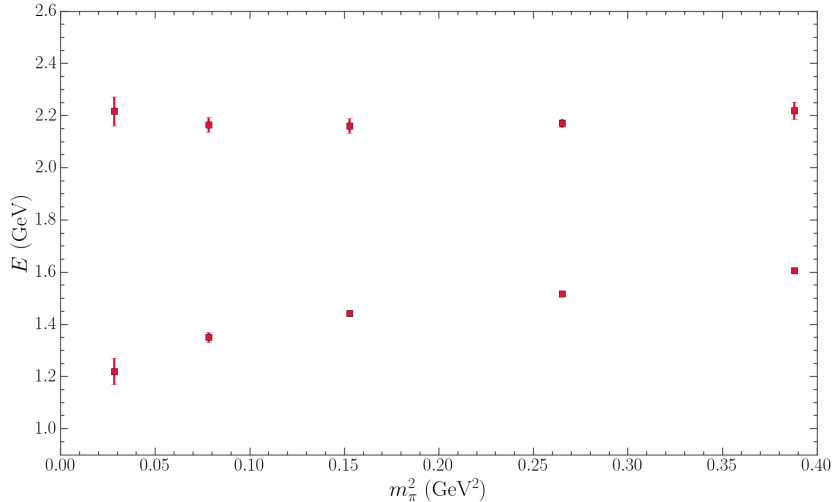
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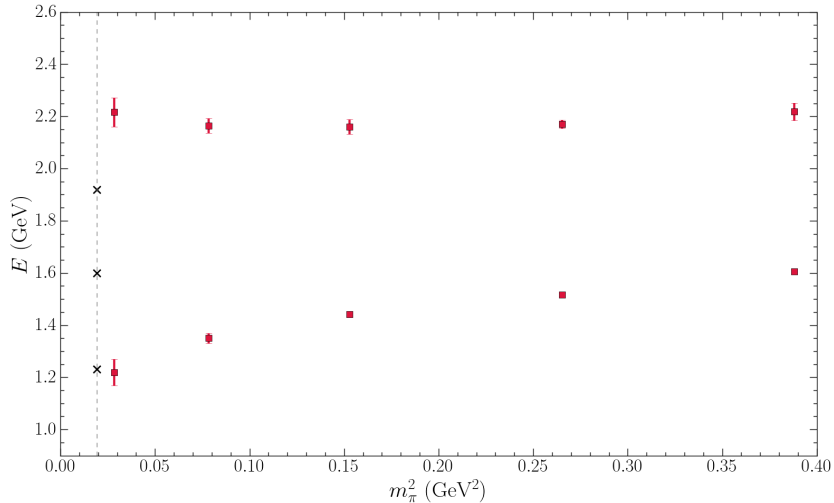


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Nucleon and Delta Resonance Predistions from the Quark Model

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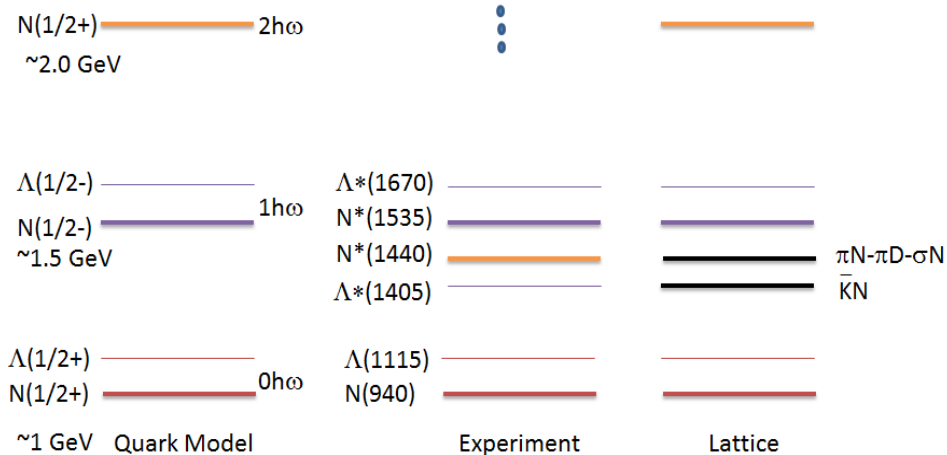
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 - State composition matches when the $2s$ excitation of the quark model sits at ~ 2 GeV.

The spectrum of quark-model-like states is relatively simple



HEFT Extensions

- Formalism for partial-wave mixing in HEFT has been developed in Y. Li, J. J. Wu, C. D. Abell, D. B. L. and A. W. Thomas. Phys. Rev. D **101**, no.11, 114501 (2020) [arXiv:1910.04973 [hep-lat]]
- And extended to moving and elongated finite-volumes in Y. Li, J. J. Wu, D. B. L. and A. W. Thomas Phys. Rev. D **103** no.9, 094518 (2021) [arXiv:2103.12260 [hep-lat]].

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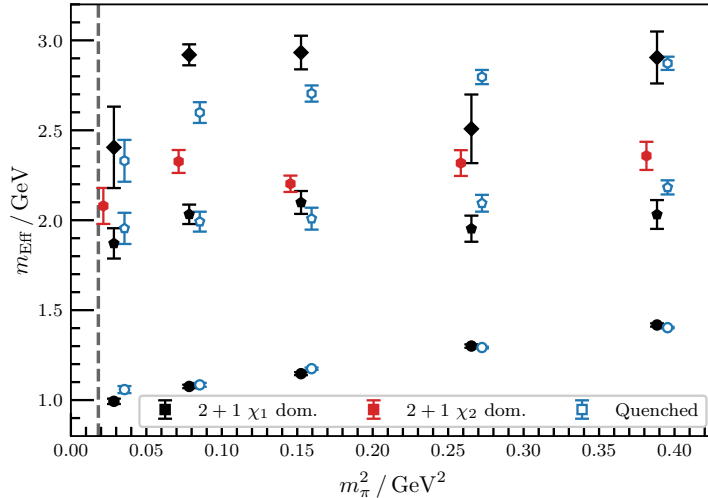
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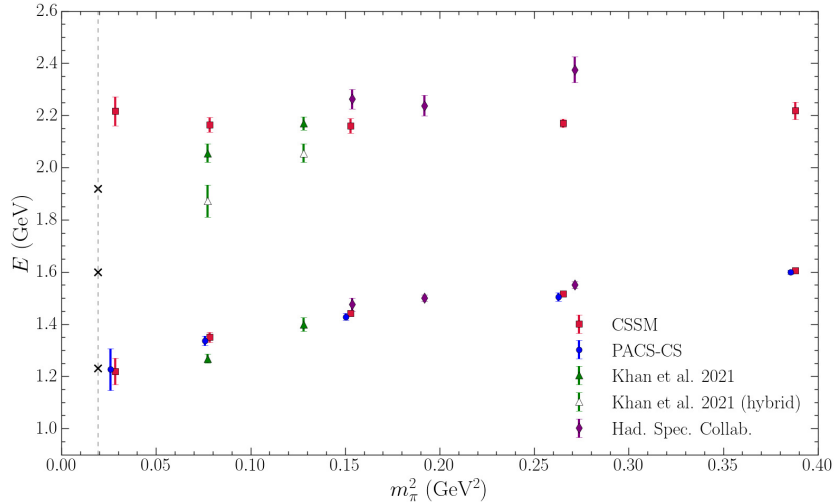
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 - Sickness: Negative-metric issues corrupt states with large meson-baryon components.
- Is there a state ~ 1.9 GeV that is insensitive to quenching?

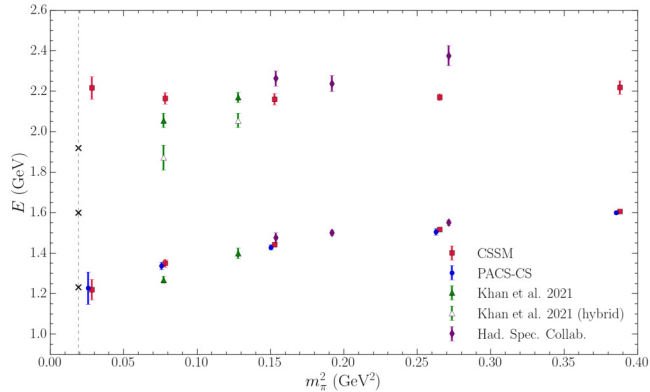
Comparison of 2+1 flavour and quenched lattice simulation results



Δ -baryon spectrum from lattice QCD



Δ -baryon spectrum from lattice QCD



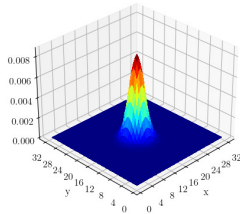
PACS-CS: S. Aoki *et al.* [PACS-CS], Phys. Rev. D **79** (2009) 034503 [arXiv:0807.1661 [hep-lat]].

Kahn et al.: T. Khan, D. Richards and F. Winter, Phys. Rev. D **104** (2021) 034503 [arXiv:2010.03052 [hep-lat]].

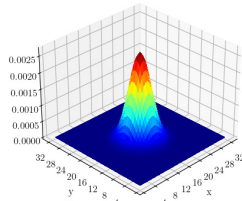
Had. Spec. Collab.: J. Bulava, *et al.*, Phys. Rev. D **82** (2010) 014507 [arXiv:1004.5072 [hep-lat]].

Accessing the Radial Excitations of the Nucleon - CSSM Techniques

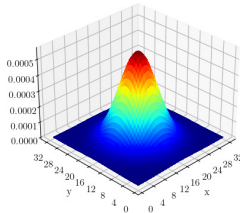
Smearing level 16



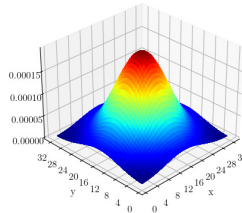
Smearing level 35



Smearing level 100



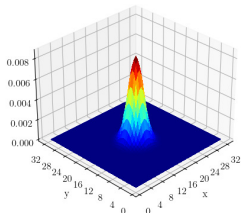
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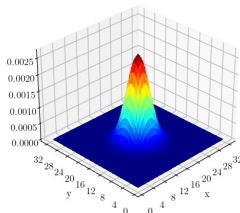
- Circa 2010.
- Local 3-quark interpolating fields.
- Quark-level source smearing techniques.

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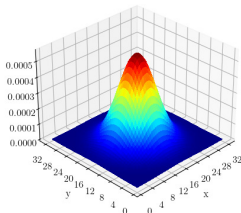
Smearing level 16



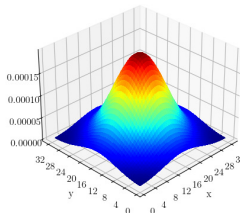
Smearing level 35



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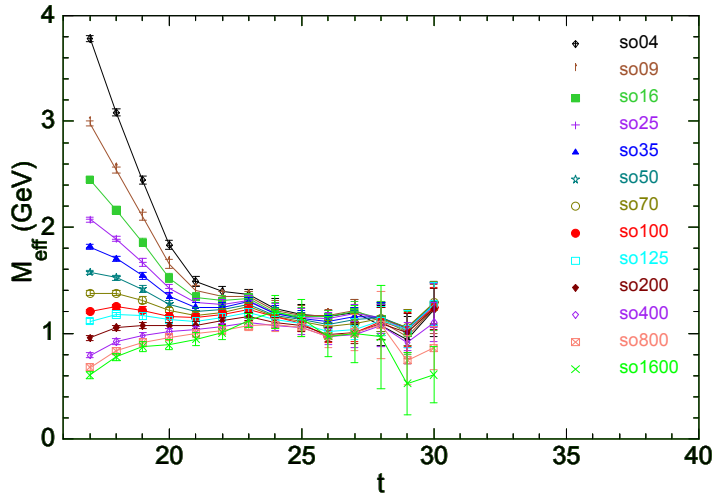


Smearing level 200



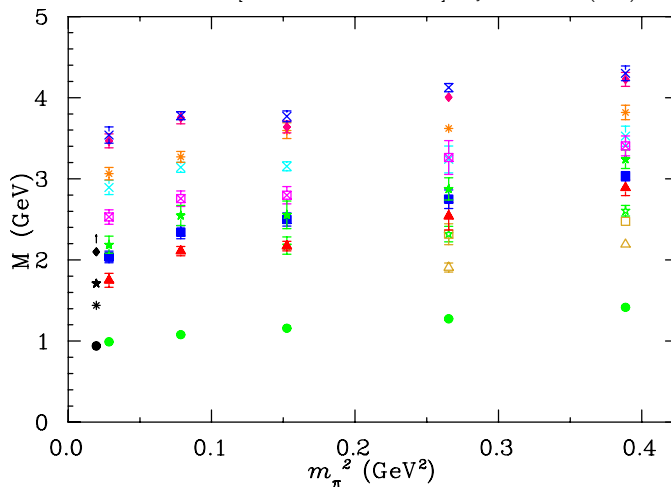
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- Local 3-quark interpolating fields.
- Quark-level source smearing techniques.
- Correlation matrix techniques
 - Identify linear combinations of sources to isolate states.
 - Opposite sign superpositions create wave function nodes.

Smeared Source Correlation Functions



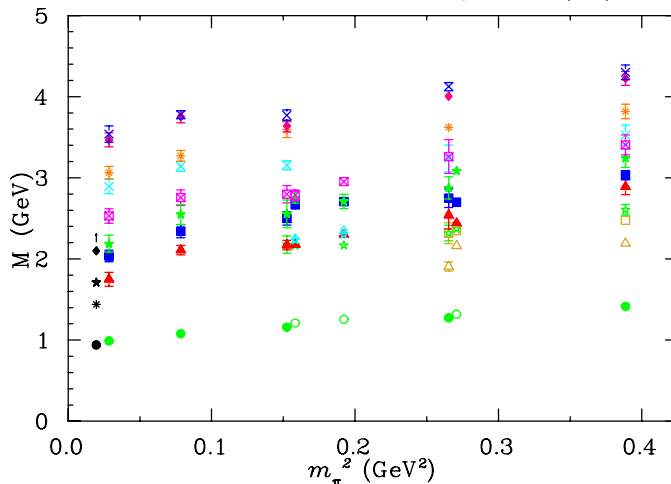
Positive Parity Nucleon Spectrum CSSM

M. S. Mahbub *et al.* [CSSM Lattice Collaboration], Phys. Lett. B **707** (2012) 389 arXiv:1011.5724 [hep-lat].



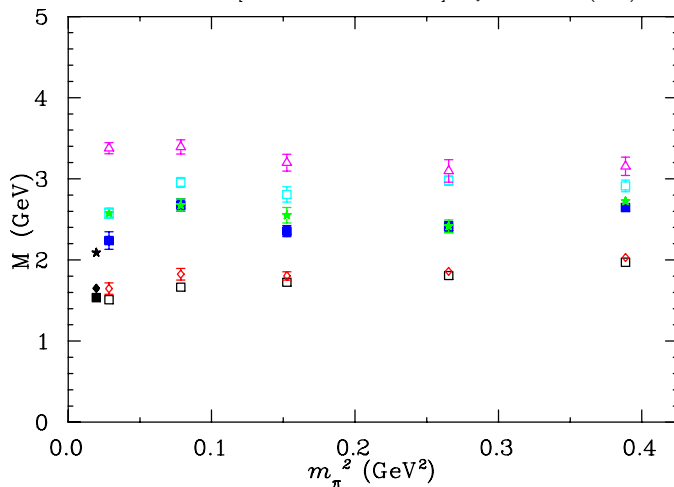
Positive Parity Nucleon Spectrum CSSM & JLab HSC

R. G. Edwards, J. J. Dudek, D. G. Richards and S. J. Wallace, Phys. Rev. D **84** (2011) 074508 arXiv:1104.5152 [hep-ph].



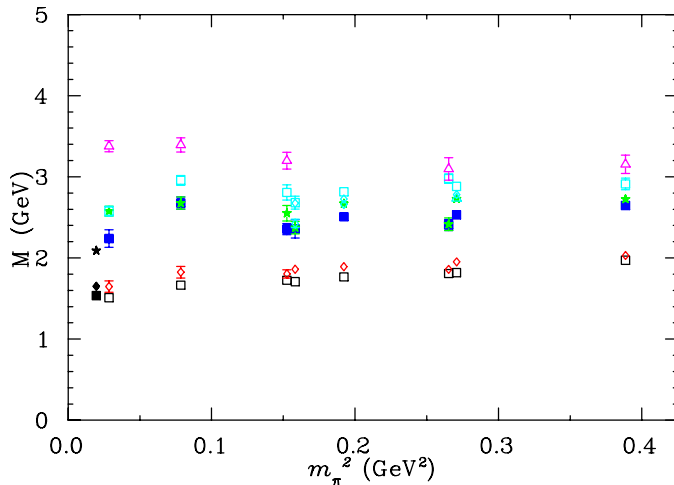
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D. Leinweber, *et al.* JPS Conf. Proc. **10** (2016), 010011 [arXiv:1511.09146 [hep-lat]].

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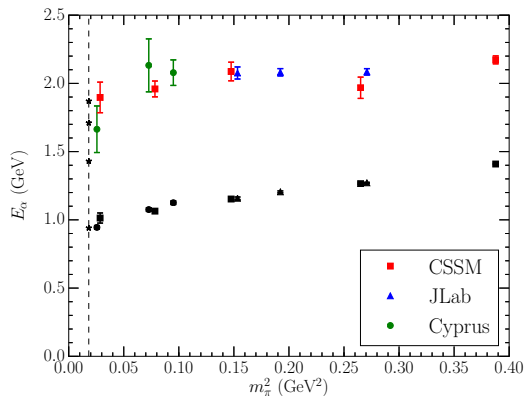
- Cyprus Twisted Mass and Clover Fermion results

C. Alexandrou, *et al.*, Phys. Rev. D **89** (2014) no.3, 034502 [arXiv:1302.4410 [hep-lat]].

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C. Alexandrou, *et al.*, Phys. Rev. D **89** (2014) no.3, 034502 [arXiv:1302.4410 [hep-lat]].
- Correlation functions subsequently analysed in the Athens Model Independent Analysis Scheme (AMIAS).
C. Alexandrou, *et al.*, Phys. Rev. D **91** (2015) no.1, 014506 [arXiv:1411.6765 [hep-lat]].

Positive Parity Nucleon Spectrum Circa 2017



Strange Magnetic Form Factor of the $\Lambda(1405)$

J. M. M. Hall, *et al.* [CSSM], Phys. Rev. Lett. **114**, 132002 (2015) arXiv:1411.3402 [hep-lat]

- Provides direct insight into the possible dominance of a molecular $\bar{K}N$ bound state.

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- In forming such a molecular state, the $\Lambda(u, d, s)$ valence quark configuration is complemented by
 - A u, \bar{u} pair making a $K^-(s, \bar{u})$ - proton (u, u, d) bound state, or
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- Thus, the strange quark does not contribute to the magnetic form factor of the $\Lambda(1405)$ when it is dominated by a $\bar{K}N$ molecule.

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