

Results on four-charm-quark states by ATLAS and CMS

<https://arxiv.org/abs/2304.08962>

<https://cms-results.web.cern.ch/cms-results/public-results/preliminary-results/BPH-21-003/index.html>

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on behalf of the ATLAS & CMS Collaborations

HADRON2023



- New domain of exotics: all-heavy tetra-quarks
- CMS fully-charmed exotic states
 - First observation of $X(6600)$ and evidence of $X(7300)$ in $J/\psi J/\psi$
 - Confirmation of $X(6900)$ in $J/\psi J/\psi$
- ATLAS fully-charmed exotic states
 - Confirmation of $X(6900)$ in $J/\psi J/\psi$
 - Evidence of structures in $J/\psi \psi(2S)$
- Comparison among ATLAS, CMS and LHCb
- Possible future: triple J/ψ
- Summary

- First mention of 4c states at 6.2 GeV (1975)
 - Just one year after the discovery of J/ψ

We expect at least three exotic mesons with hidden charm, $c\bar{c}(p\bar{p}-n\bar{n})$ [between 3.7~4.1 GeV], $c\bar{c}\lambda\bar{\lambda}$ [~ 4.1 GeV] and $c\bar{c}c\bar{c}$ [~ 6.2 GeV] to which we refer as ψ_c , ψ_c' and ψ_c'' respectively. [Weisskopf, 1975]

Progress of Theoretical Physics, Vol. 54, No. 2, August 1975

A Possible Model for New Resonances

—Exotics and Hidden Charm—

Yoichi IWASAKI

Research Institute for Fundamental Physics
Kyoto University, Kyoto

(Received January 20, 1975)

- First calculation of 4c states (1981): Z. Phys. C 7 (1981) 317

L	S	J^{PC}	Mass (GeV)
1	0	1^{--}	6.55
	1	$0^{-+}, 1^{-+}, 2^{-+}$	
	2	$1^{--}, 2^{--}, 3^{--}$	
2	0	2^{++}	6.78
	1	$1^{+-}, 2^{+-}, 3^{+-}$	
	2	$0^{++}, 1^{++}, 2^{++}, 3^{++}, 4^{++}$	
3	0	3^{--}	6.98
	1	$2^{-+}, 3^{-+}, 4^{-+}$	
	2	$1^{--}, 2^{--}, 3^{--}, 4^{--}, 5^{--}$	

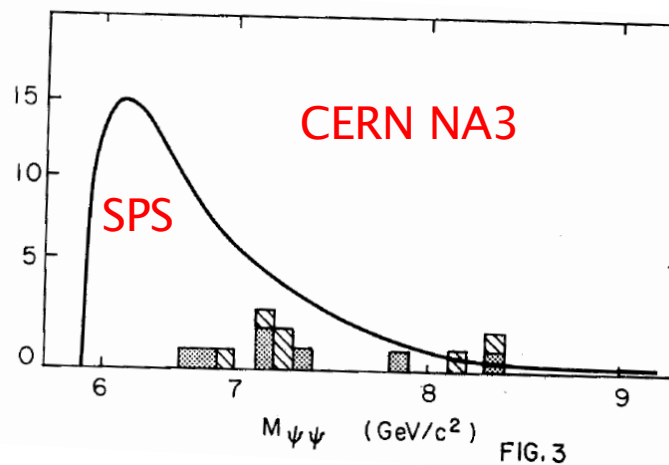
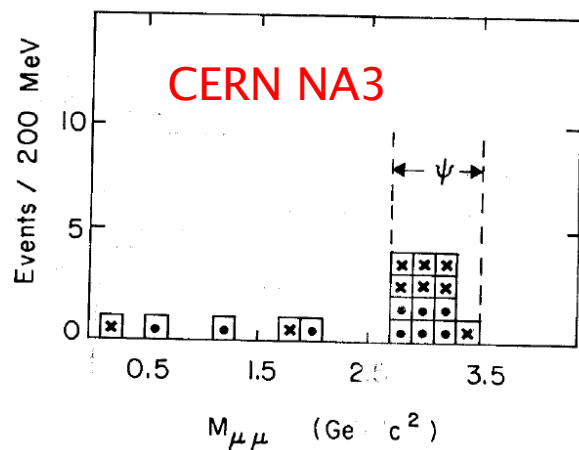
$$\left| (cc)_3^* - (\bar{c}\bar{c})_3 \right|$$

$$(cc)_6 - (\bar{c}\bar{c})_6^*$$

L	S	J^{PC}	Mass (GeV)
1	0	1^{--}	6.82
2	0	2^{++}	7.15
3	0	3^{--}	7.41

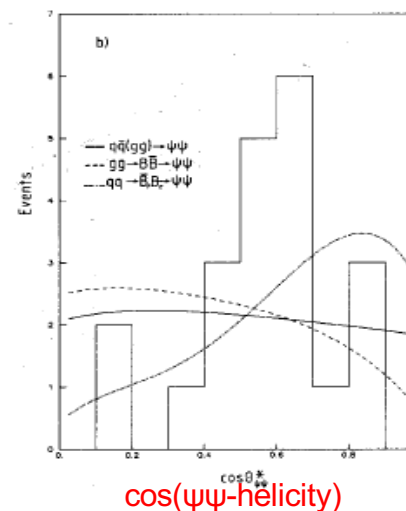
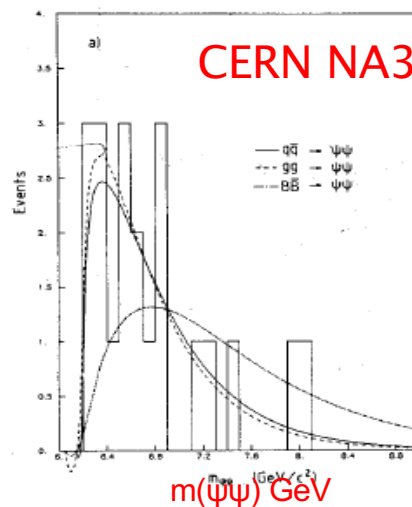
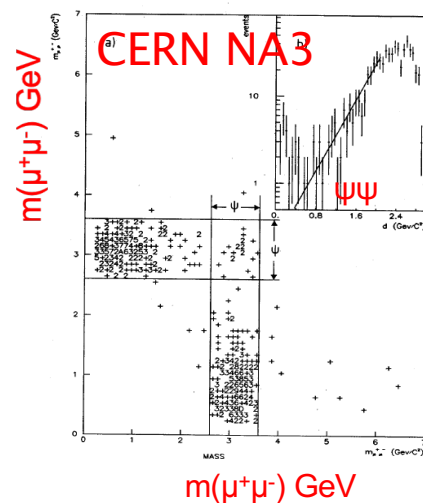
- A different exotic system compared to exotics with light quarks

J/ψ J/ψ events—first evidence (1982)



PLB114 (1982) 457

Was interpreted
as 2^{++} 4-quark state



PLB158 (1985) 85

2^{++} four-quark states, PRD29 (1984) 426

TABLE I. Parameters used in Eq. (8) to calculate the cross sections for vector-meson pair production. (+) and (−) denote two degenerate 2^{++} $Q^2\bar{Q}^2$ states. Except in the case of JJ , we take $4\pi/f_L^2=0.03$, due to the fact that the 2^{++} $Q^2\bar{Q}^2$ are expected to lie not far above the threshold. α_s is determined from Eq. (11).

$V_1 V_2$	$a \not{V}_1 V_2 / a$	$b_{\alpha\beta}^i / \alpha_s \frac{a}{\sqrt{8}} \delta_{\alpha\beta}$	M_J (GeV)	α_s	m_1
JJ	$1/\sqrt{3}$	$\left[\frac{2}{3}\right]^{1/2} \frac{4\pi}{f_L^2}$	7.0	0.18	3.10
$J\omega^{(+)}$	$1/\sqrt{6}$	$\frac{-1}{\sqrt{3}} \frac{4\pi}{f_L f_\omega}$	4.05	0.2	
$J\omega^{(-)}$	$1/\sqrt{12}$	$\left[\frac{2}{3}\right]^{1/2} \frac{4\pi}{f_L f_\omega}$	4.05	0.2	
$\Upsilon J^{(+)}$	$1/\sqrt{6}$	$\frac{-1}{\sqrt{3}} \frac{4\pi}{f_\Upsilon f_L}$	13.5	0.167	
$\Upsilon J^{(-)}$	$1/\sqrt{12}$	$\left[\frac{2}{3}\right]^{1/2} \frac{4\pi}{f_\Upsilon f_L}$	13.5	0.167	
$B_c^* \bar{B}_c^{*(+)}$	$-1/\sqrt{6}$	$\frac{-1}{\sqrt{3}} \frac{4\pi}{f_\Upsilon f_L}$	13.5	0.167	6.60
$B_c^* \bar{B}_c^{*(-)}$	$1/\sqrt{12}$	$\left[\frac{2}{3}\right]^{1/2} \frac{4\pi}{f_\Upsilon f_L}$	13.5	0.167	

There were other attempts

(cccc) *Phys. Rev. D 86, 034004 (2012)*

$0^{++'}$	$M = 5.966 \text{ GeV},$	$M - M_{\text{th}} = -228. \text{ MeV},$
$1^{+-'}$	$M = 6.051 \text{ GeV},$	$M - M_{\text{th}} = -142. \text{ MeV},$
2^{++}	$M = 6.223 \text{ GeV},$	$M - M_{\text{th}} = 29.5 \text{ MeV}.$

Below double J/ψ threshold
Search via $J/\psi \mu^+ \mu^-$, J/ψ^*

Above double J/ψ threshold
Search via $J/\psi J/\psi$

(bbcc)

0^{++a}	$M = 12.359 \text{ GeV},$	$M - M_{\text{th}} = -191. \text{ MeV}$
0^{++b}	$M = 12.471 \text{ GeV},$	$M - M_{\text{th}} = -78.7 \text{ MeV},$
1^{+-a}	$M = 12.424 \text{ GeV},$	$M - M_{\text{th}} = -126. \text{ MeV}$
1^{+-b}	$M = 12.488 \text{ GeV},$	$M - M_{\text{th}} = -62.5 \text{ MeV},$
1^{++}	$M = 12.485 \text{ GeV},$	$M - M_{\text{th}} = -64.9 \text{ MeV},$
2^{++}	$M = 12.566 \text{ GeV},$	$M - M_{\text{th}} = 16.1 \text{ MeV}.$

Below double B_c threshold
 $J/\psi Y(1S)$ threshold
? ...

(bbbb)

$0^{++'}$	$M = 18.754 \text{ GeV},$	$M - M_{\text{th}} = -544. \text{ MeV},$
$1^{+-'}$	$M = 18.808 \text{ GeV},$	$M - M_{\text{th}} = -490. \text{ MeV},$
2^{++}	$M = 18.916 \text{ GeV},$	$M - M_{\text{th}} = -382. \text{ MeV}.$

Above double B_c threshold
 $J/\psi Y(1S)$ threshold
Search via the above two channels

Below double $Y(1S)$ threshold
Search via $Y(1S) \mu^+ \mu^-$

- Many recent theoretical studies on $(c\bar{c}c\bar{c})$, $(b\bar{b}b\bar{b})$, $(b\bar{b}c\bar{c})$:
 - controversial on existence of bound states below $\eta_b \eta_b$ (or $\eta_c \eta_c$) threshold;
 - consistent on existence of resonant states above $\eta_b \eta_b$ (or $\eta_c \eta_c$) threshold.

- Signal: $X \rightarrow J/\psi J/\psi \rightarrow \mu^+ \mu^- \mu^+ \mu^-$

- Signal MC samples:

- $J^P = 0^+$ resonance

Generator: Pythia8, JHUGen

- Main background:

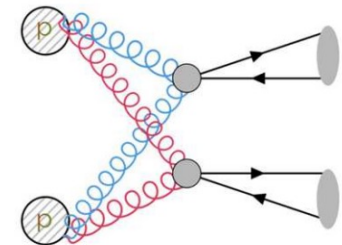
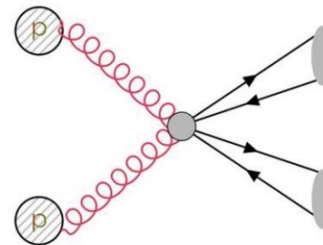
- Nonresonant single-parton scattering (NRSPS)

Generator: Pythia8, HelacOnia (next-to-next-to-leading order),
Cascade (next-to-leading order)

- Nonresonant double-parton scattering (NRDPS)

Generator: Pythia8

- Combinatorial background



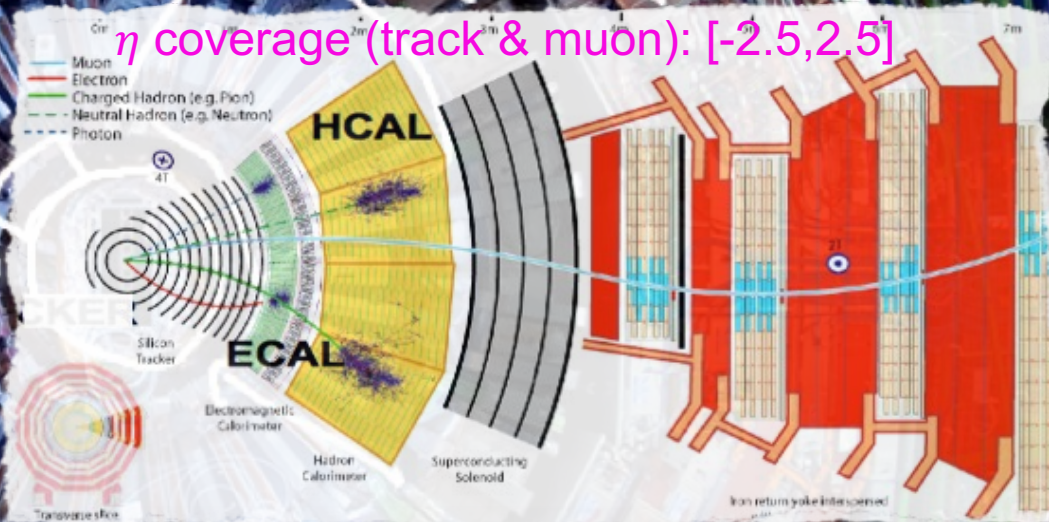
the Compact Muon Solenoid detector

3.8T Superconducting Solenoid

Hermetic ($|\eta| < 5.2$)
Hadron Calorimeter (HCAL)
[scintillators & brass]

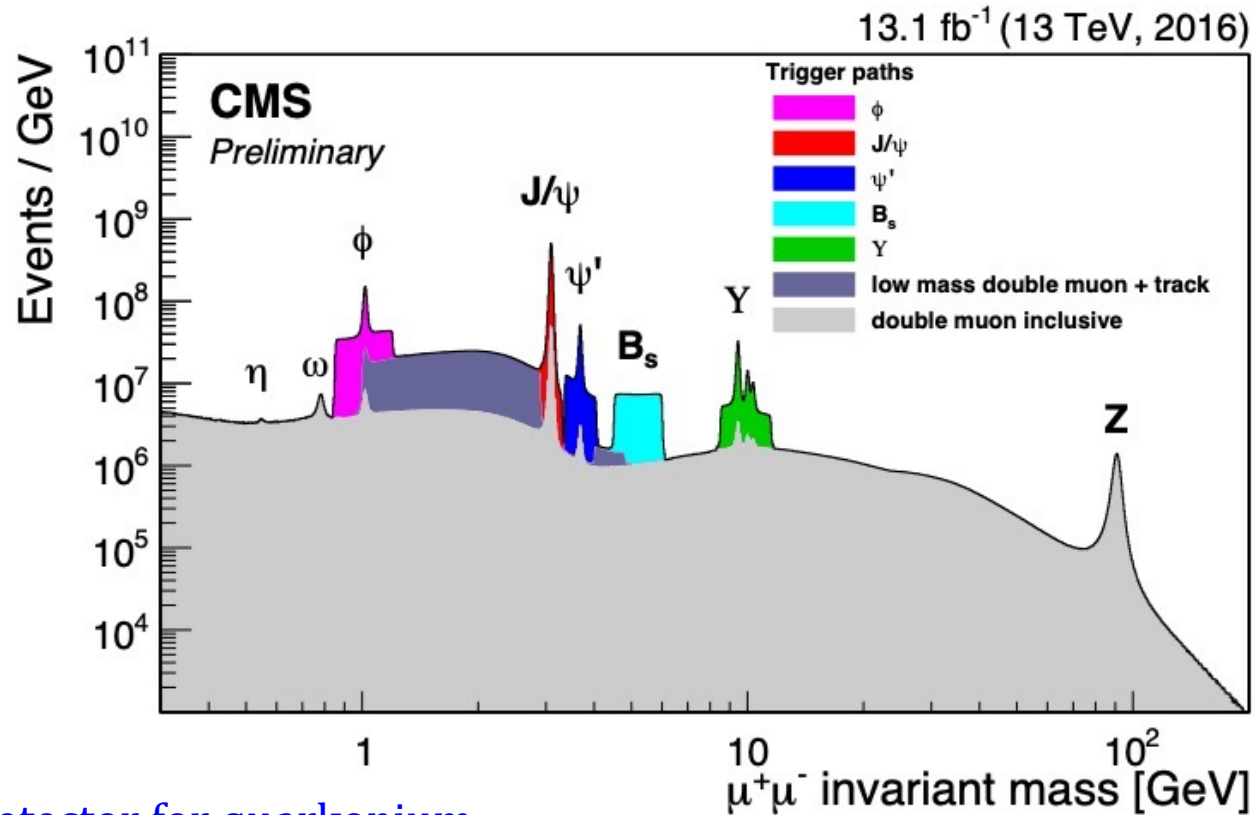
Lead tungstate
E/M Calorimeter (ECAL)

η coverage (track & muon): $[-2.5, 2.5]$



All Silicon Tracker
(Pixels and Microstrips)

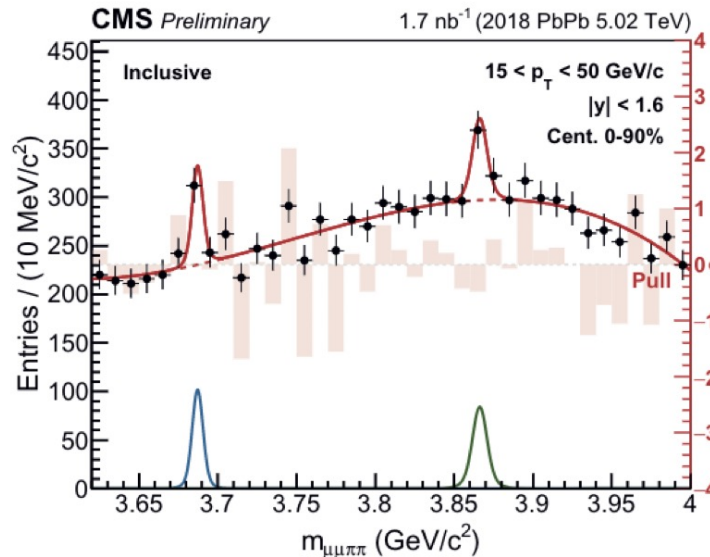
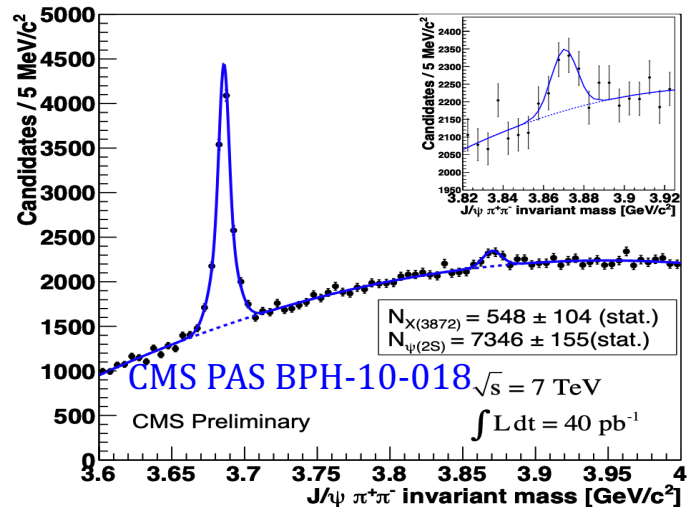
Redundant Muon System
(RPCs, Drift Tubes,
Cathode Strip Chambers)



Excellent detector for quarkonium

- Muon system
 - High-purity muon ID, $\Delta m/m \sim 0.6\%$ for J/ψ
- Silicon Tracking detector, $B=3.8T$
 - $\Delta p_T/p_T \sim 1\%$ & excellent vertex resolution
- Special triggers for different analyses at increasing Inst. Lumi.
 - μp_T , $(\mu\mu) p_T$, $(\mu\mu)$ mass, $(\mu\mu)$ vertex, and additional μ

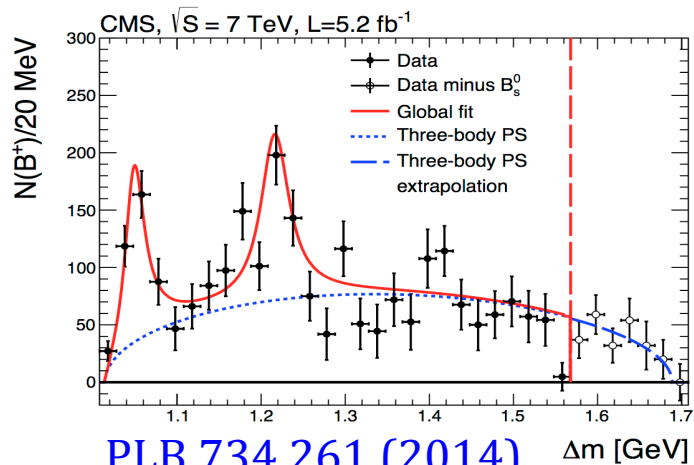
First LHC experiment re-discovered X(3872)



First X(3872) signal in PbPb

[Nucl. Phys. Vol 1005 \(2021\)121781](#)

First confirmation of Y(4140)



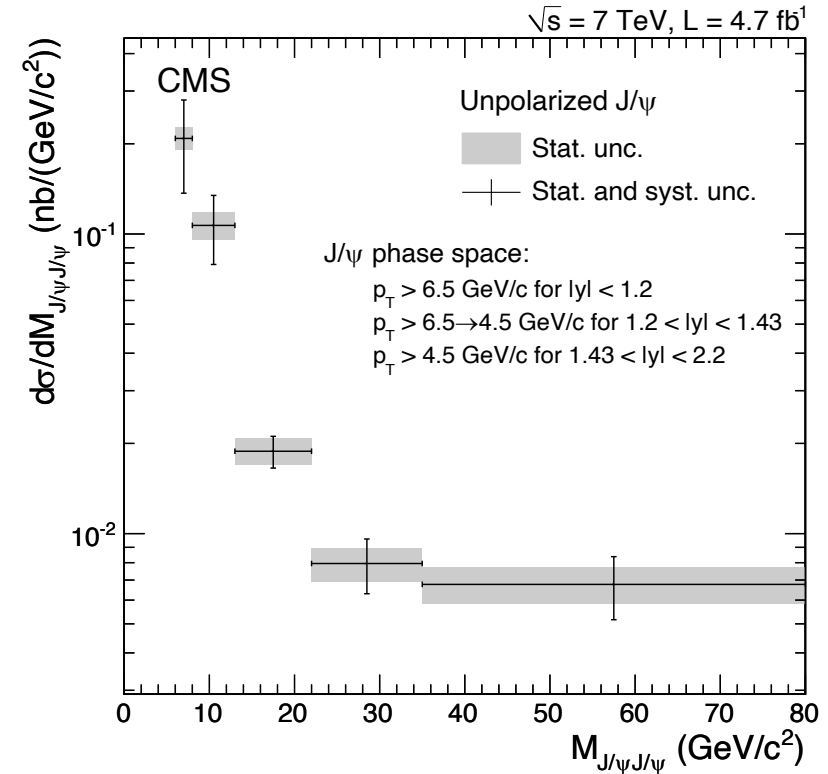
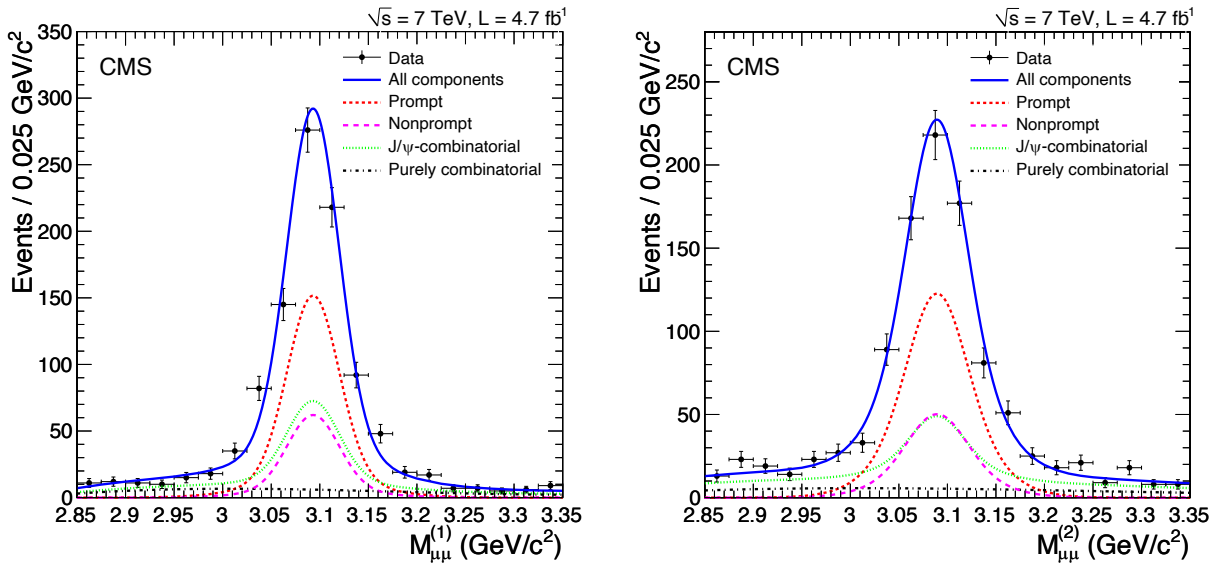
PLB 734 261 (2014)

CMS played the following leading roles:

- First LHC experiment to see X(3872)
- First experiment to see X(3872) in B_s^0 decay
- First experiment to see X(3872) in PbPb data
- First LHC experiment to see new exotic hadrons (Y(4140))

<https://www.nikhef.nl/~pkoppenb/particles.html>

J. High Energy Phys. 09 (2014) 094

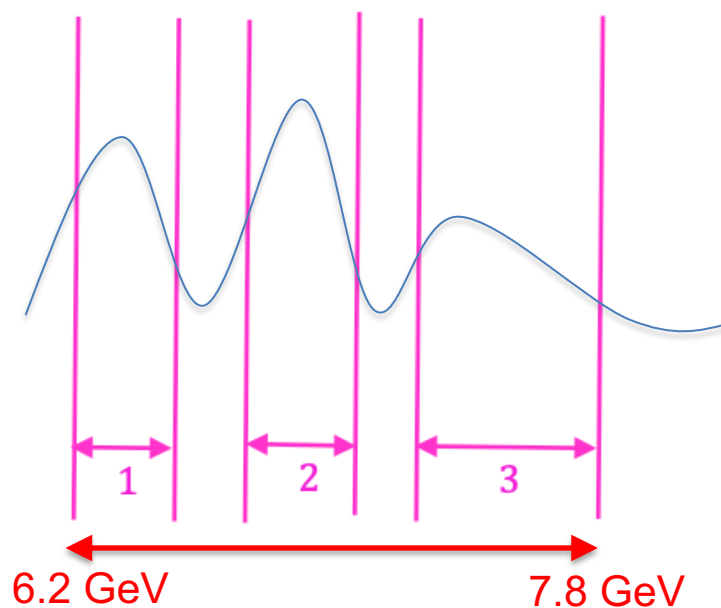


Total cross section, assuming unpolarized prompt $J/\psi J/\psi$ pair production
 1.49 ± 0.07 (stat.) ± 0.13 (syst.) nb

Different assumptions about the $J/\psi J/\psi$ polarization imply modifications to the cross section ranging from -31% to +27%.

We saw hints at Run I data (7 TeV & 8 TeV)
Proposed **three** signal regions for Run II data

Signal: $X \rightarrow J/\psi J/\psi \rightarrow \mu^+ \mu^- \mu^+ \mu^-$



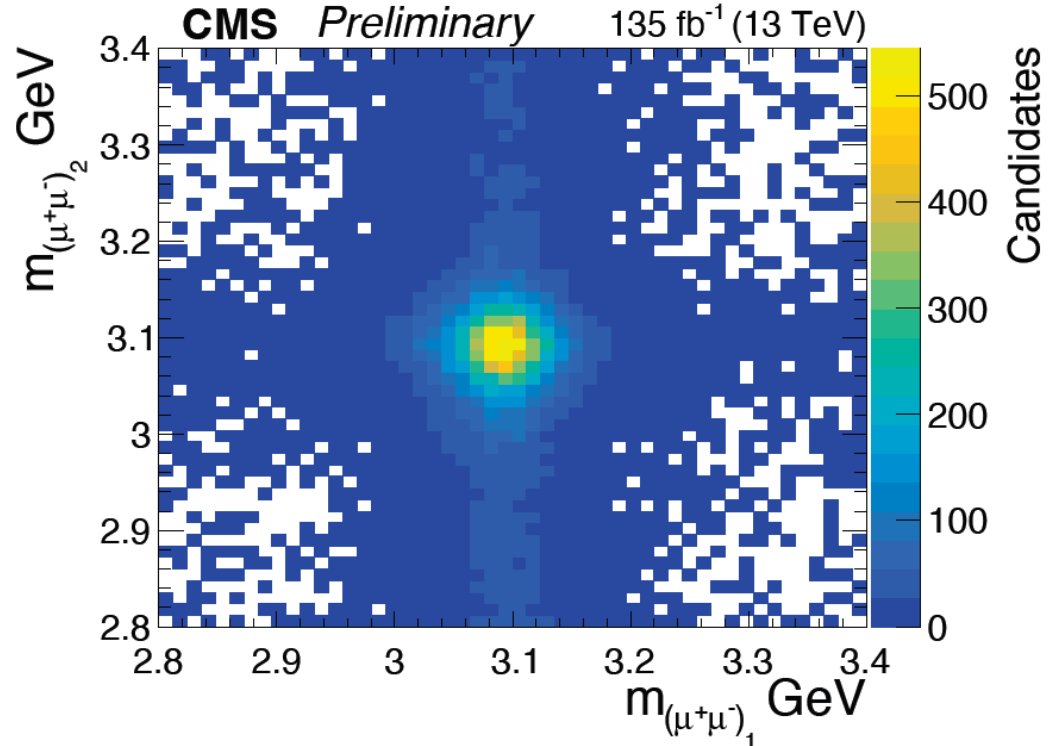
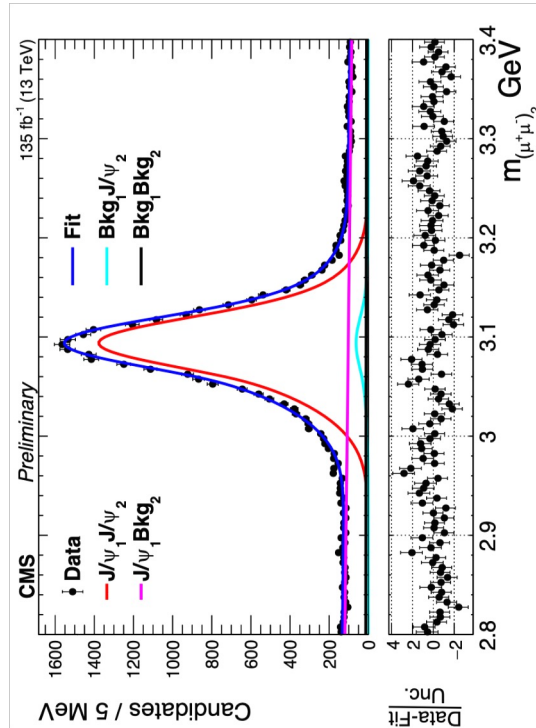
Blinded mass windows for Run II:

1. [6.3,6.6] GeV
2. [6.8,7.1] GeV
3. [7.2,7.8] GeV
(for potential wide structure)

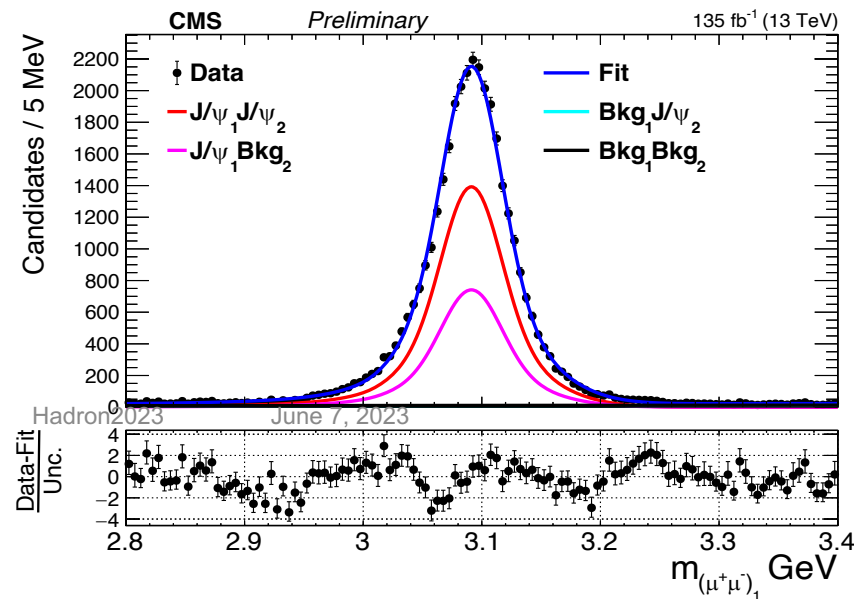
These mass windows will be windows
for LEE for potential structures

Run I data will be ignored for
significance calculation

CMS eventually decide to blind the whole region: [6.2, 7.8] GeV after LHCb released their result (13 TeV, 2020)



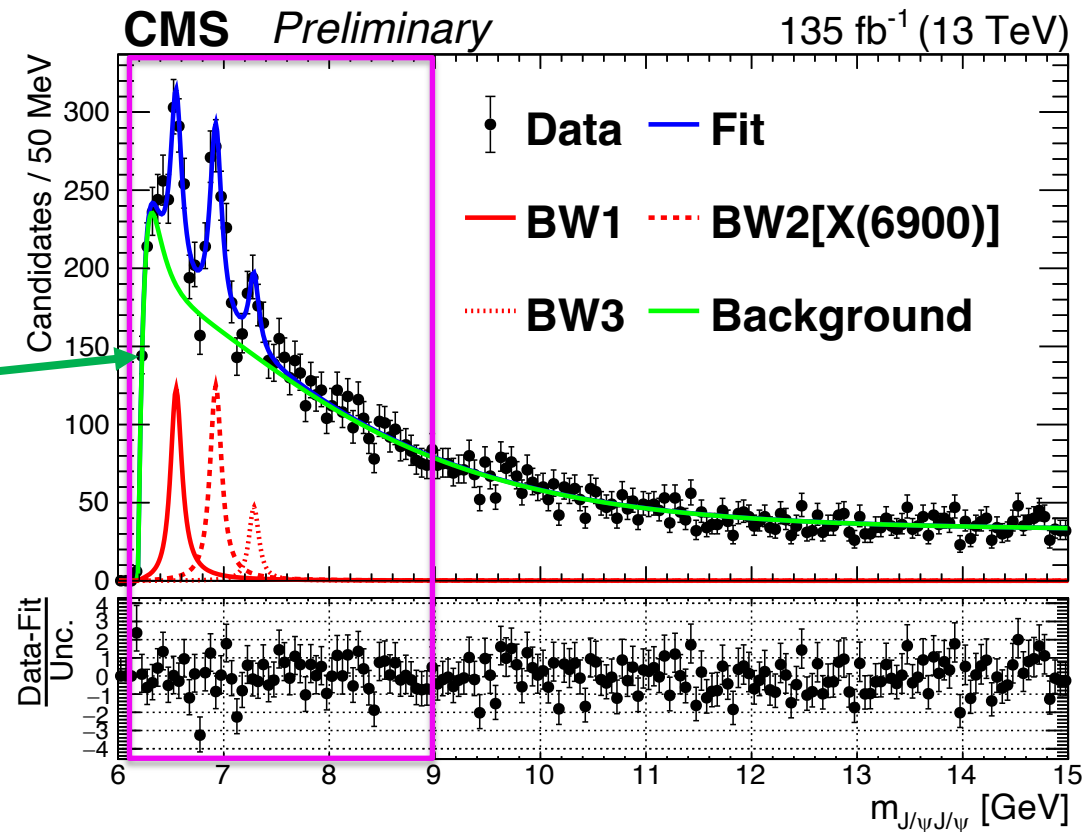
- CMS data: 135 fb^{-1} , taken in 2016, 2017 and 2018 LHC runs
- J/ψ mass and vertex related cuts removed
- Clean J/ψ signals are seen



CMS background (SPS + DPS + BW0)

$\chi^2 \text{ prob} = 79\%$

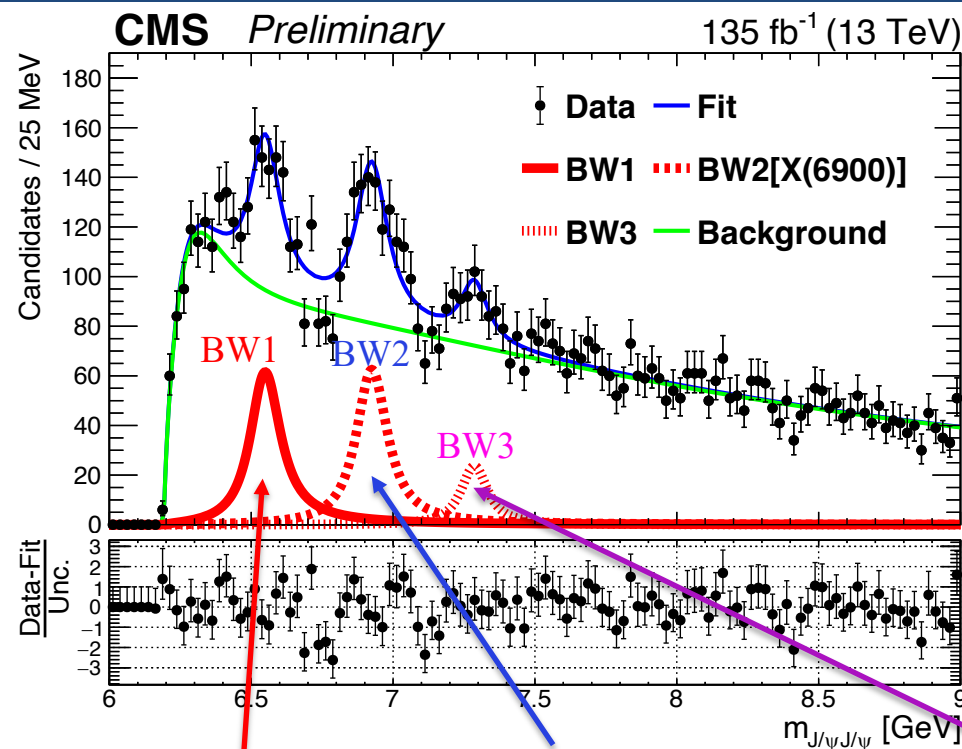
[6.2,15] GeV



- Most significant structure is a BW at threshold, **BW0**--what is its meaning?
- **Treat BW0 as part of background** due to:
 - **BW0 parameters very sensitive to SPS and DPS model assumptions**
 - A region populated by feed-down from possible higher mass states
 - Possible coupled-channel interactions, pomeron exchange processes...
- **SPS+DPS+BW0 as our background**

χ^2 Prob. = 1%

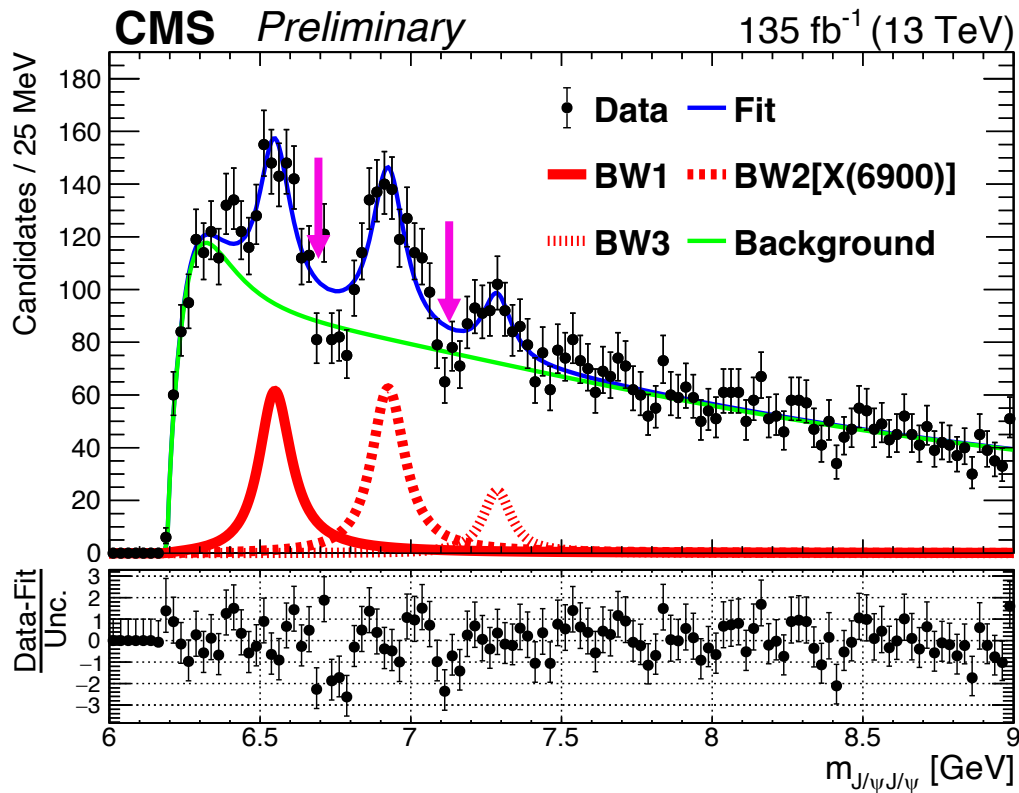
[6.2, 7.8] GeV



Statistical significance based on:

$$2 \ln(L_0/L_{\max})$$

	BW1 (MeV)	BW2 (MeV)	BW3 (MeV)
m	6552 ± 10	6927 ± 9	7287 ± 19
Γ	124 ± 29	122 ± 22	95 ± 46
N	474 ± 113	492 ± 75	156 ± 56
σ(stat.)	6.5	9.4	4.1
σ(stat. + syst.)	5.7	9.4	4.1
	Observation	Confirmation of X(6900) from LHCb	Evidence



- Possibility #1:
 - Interference among structures?

- Possibility #2:
 - Multiple fine structures to reproduce the dips?
 - Mentioned in PAS

- More secrets to dig out
- We explored possibility #1 in detail

- Explored fit with interference among various combinations of BWs
- Pdf for three BW interference

$$Pdf(m) = N_{X_0} \cdot |BW_0|^2 \otimes R(M_0)$$

$$+ N_{X \text{ and interf}} \cdot |r_1 \cdot \exp(i\phi_1) \cdot BW_1 + BW_2 + r_3 \cdot \exp(i\phi_3) \cdot BW_3|^2$$

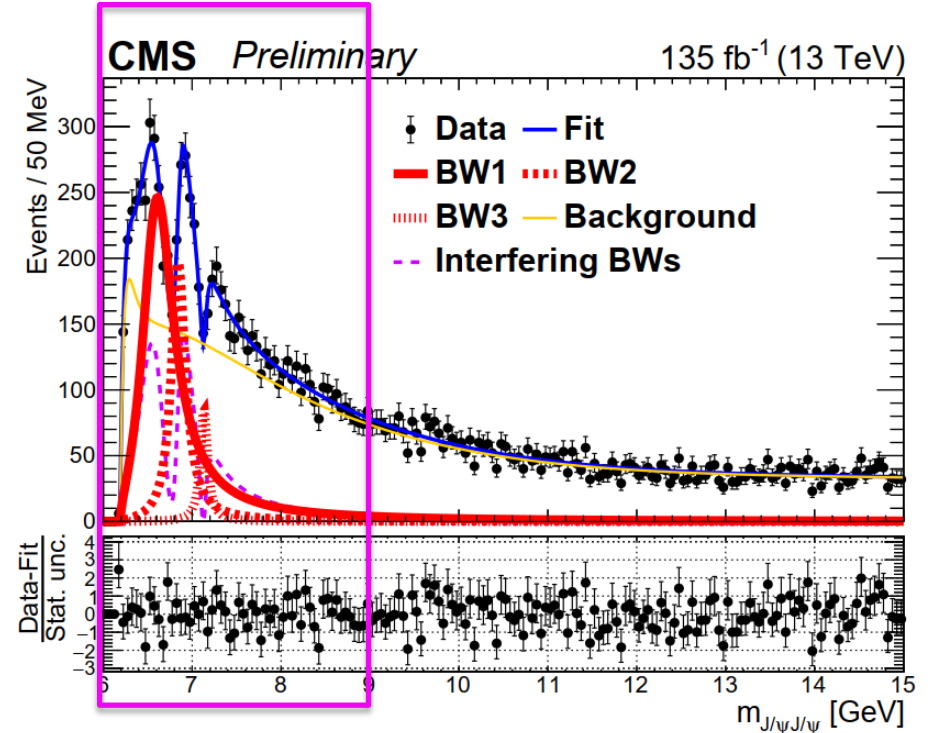
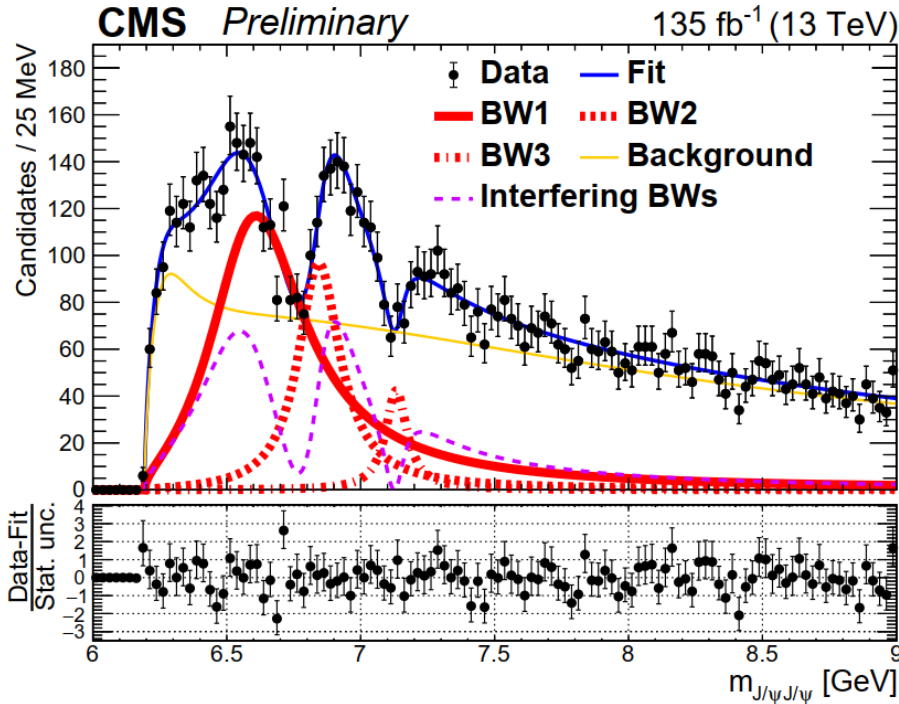
$$+ N_{NRSPS} \cdot f_{SPS}(m) + N_{NRDPS} \cdot f_{DPS}(m)$$

Interf. term

- Studied many ways interference due to possible J^{PC} and quantum coherence
 - 2-object-interference among BW0, BW1, BW2, BW3
 - 3-object-interference among BW0, BW1, BW2, BW3
 - 4-object-interference among BW0, BW1, BW2, BW3

Final CMS choice: interference among BW1, BW2, BW3

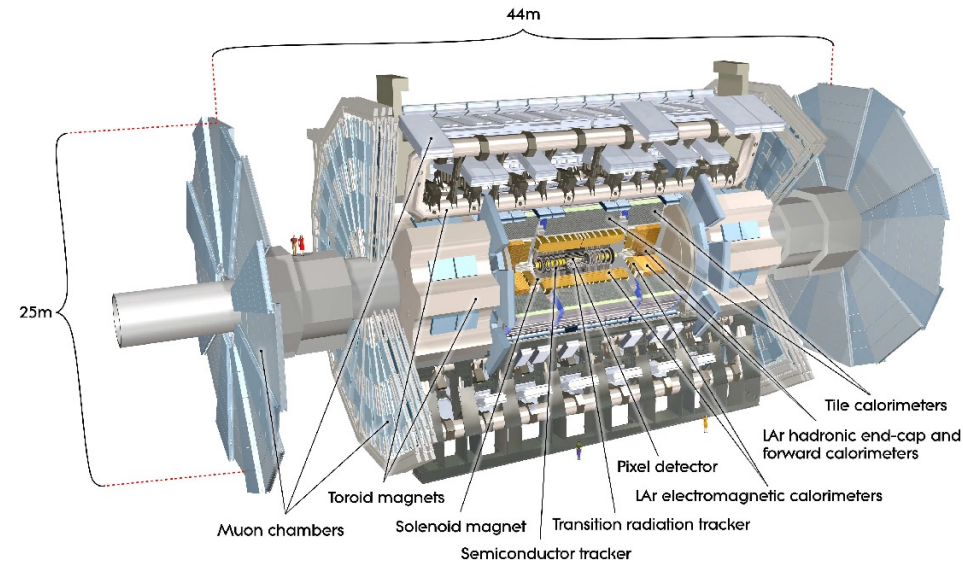
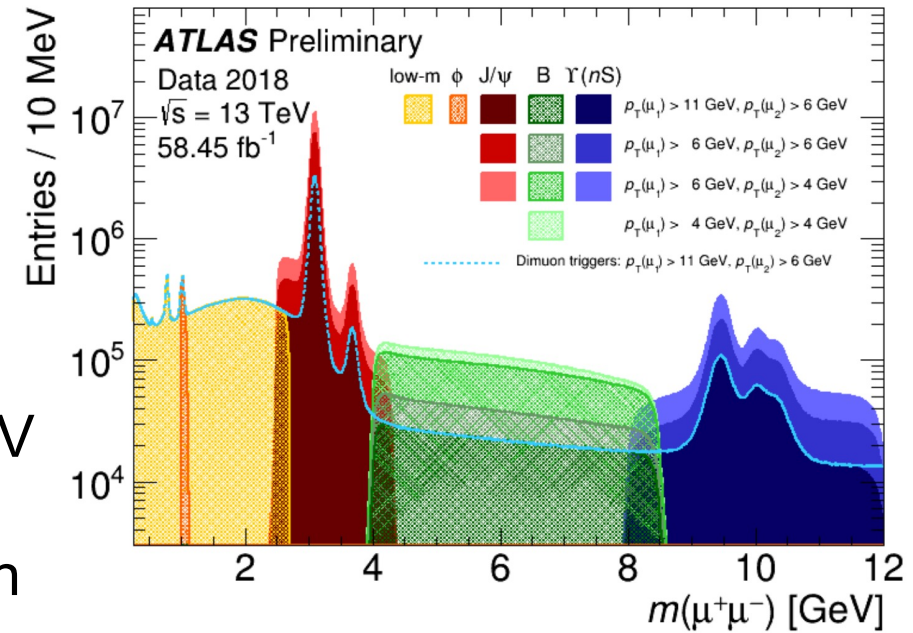
[CMS PAS BPH-21-003](#)



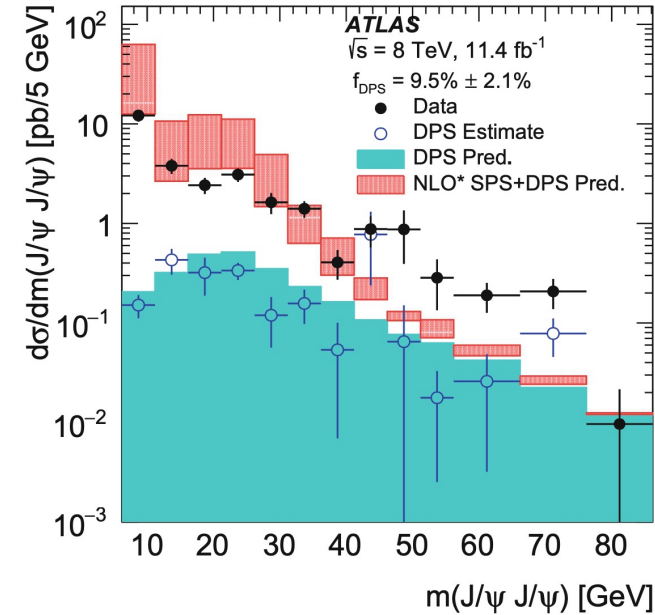
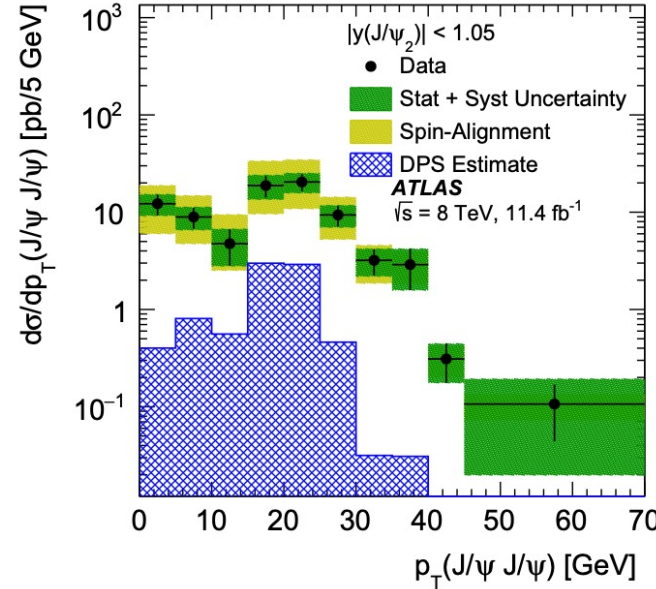
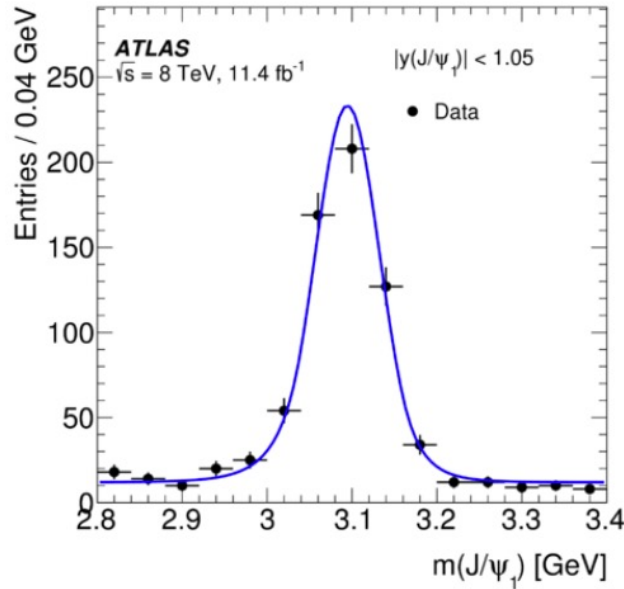
- Fit with interf. among BW1, BW2, and BW3 describes data well
- Measured mass and width in the interference fit

		BW1	BW2	BW3
Interference	m [MeV]	6638^{+43+16}_{-38-31}	6847^{+44+48}_{-28-20}	7134^{+48+41}_{-25-15}
	Γ [MeV]	$444^{+226+109}_{-199-235}$	191^{+66+25}_{-49-17}	97^{+40+29}_{-29-26}

- ATLAS has collected a large set of data
 - Run 1 (2010-2013): $4.9 fb^{-1}$ at 7 TeV and $20.3 fb^{-1}$ at 8 TeV
 - Run 2 (2015-2018): $139 fb^{-1}$ at 13 TeV
- Analysis focus mostly on final states with muons.
- Dedicated B-physics triggers.
- Excellent track and muon identification with the goodness of the inner detector and muon spectrometer.



EPJC 77 (2017) 76



82.2 ± 8.3 (stat) ± 6.3 (syst) ± 0.9 (BF) ± 1.6 (lumi) pb in the central region and
 78.3 ± 9.2 (stat) ± 6.6 (syst) ± 0.9 (BF) ± 1.5 (lumi) pb in the forward region
 (assumes unpolarised J/ψ mesons and does not include the J/ψ spin-alignment systematic uncertainty)

$$f_{\text{DPS}} = (9.2 \pm 2.1 \text{ (stat)} \pm 0.5 \text{ (syst)})\%$$

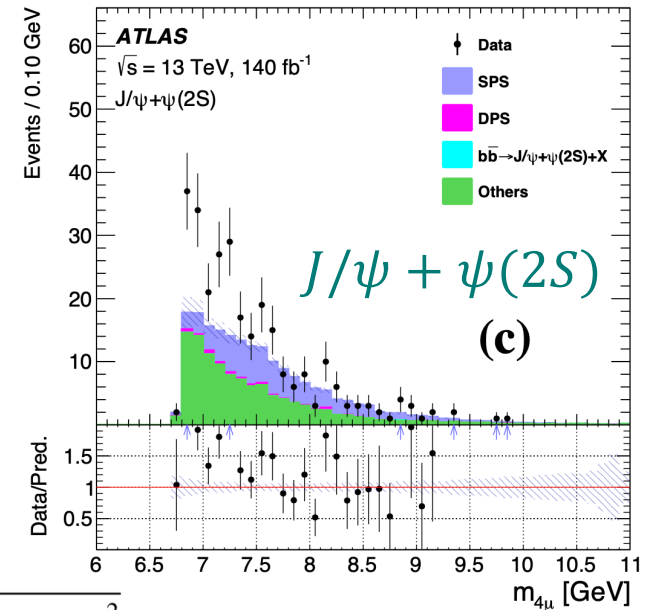
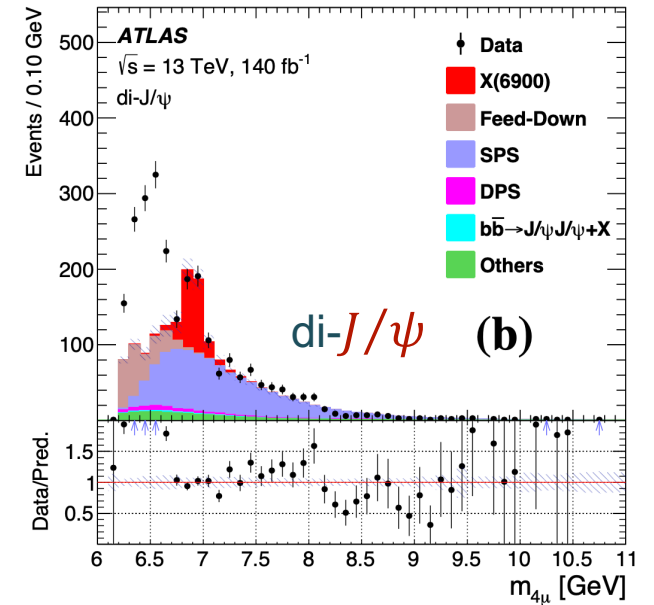
$$\sigma_{\text{eff}} = 6.3 \pm 1.6 \text{ (stat)} \pm 1.0 \text{ (syst)} \pm 0.1 \text{ (BF)} \pm 0.1 \text{ (lumi) mb}$$

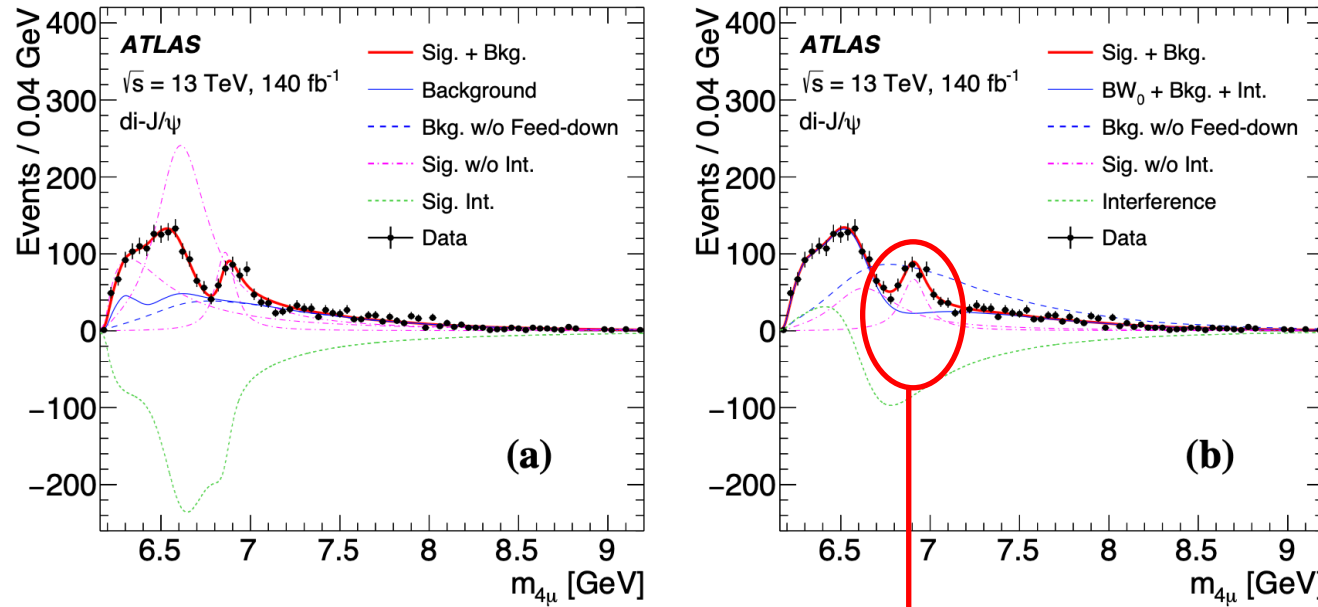
Hunt for di- J/ψ resonances by ATLAS at 13 TeV

- Signal: $T_{cc\bar{c}\bar{c}} \rightarrow J/\psi + J/\psi$ or $J/\psi + \psi(2S) \rightarrow 4\mu$
- Backgrounds:
 - Prompt: SPS and DPS
 - Non-prompt: $b\bar{b} \rightarrow J/\psi + J/\psi/\psi(2S) + X \rightarrow 4\mu$
 - Others: Single J/ψ background and non-peaking background containing no real J/ψ candidate
- **Excess in both channels**
- The unbinned maximum likelihood fits are performed in the 4μ mass spectrum.
 - The signal pdf: several interfering BW multiplied with a phase space factor and convolved with a mass resolution function

$$\text{di-}J/\psi : f_s(x) = \left| \sum_{i=0}^2 \frac{z_i}{x^2 - m_i^2 + im_i\Gamma_i} \right|^2 \sqrt{1 - \frac{4m_{J/\psi}^2}{x^2}} \otimes R(\alpha)$$

$$J/\psi + \psi(2S) : f_s(x) = \left(\left| \sum_{i=0}^2 \frac{z_i}{x^2 - m_i^2 + im_i\Gamma_i} \right|^2 + \left| \frac{z_3}{x^2 - m_3^2 + im_3\Gamma_3} \right|^2 \right) \sqrt{1 - \left(\frac{m_{J/\psi} + m_{\psi(2S)}}{x} \right)^2} \otimes R(\alpha)$$



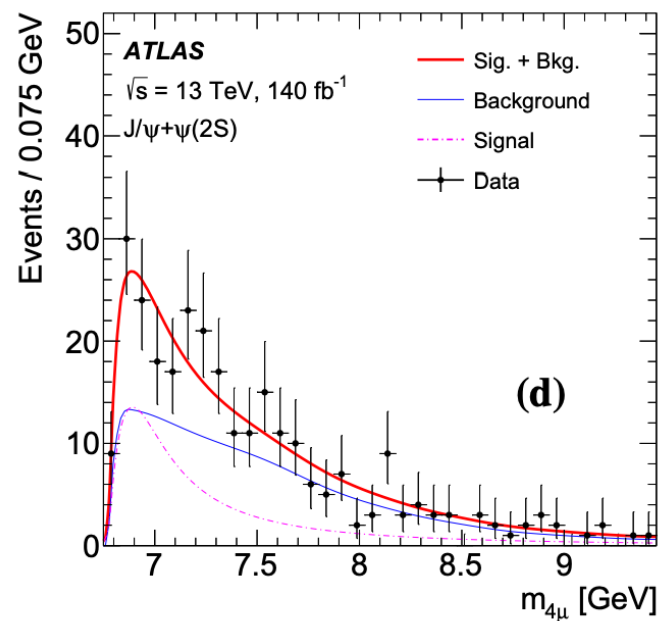
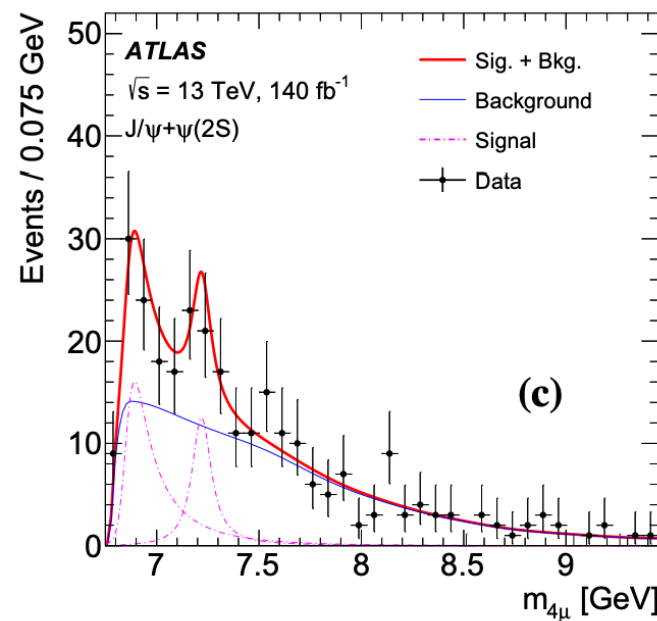


Extracted masses and widths (GeV)

di- J/ψ	model A	model B
m_0	$6.41 \pm 0.08^{+0.08}_{-0.03}$	$6.65 \pm 0.02^{+0.03}_{-0.02}$
Γ_0	$0.59 \pm 0.35^{+0.12}_{-0.20}$	$0.44 \pm 0.05^{+0.06}_{-0.05}$
m_1	$6.63 \pm 0.05^{+0.08}_{-0.01}$	—
Γ_1	$0.35 \pm 0.11^{+0.11}_{-0.04}$	—
m_2	$6.86 \pm 0.03^{+0.01}_{-0.02}$	$6.91 \pm 0.01 \pm 0.01$
Γ_2	$0.11 \pm 0.05^{+0.02}_{-0.01}$	$0.15 \pm 0.03 \pm 0.01$
$\Delta s/s$	$\pm 5.1\%^{+8.1\%}_{-8.9\%}$	—

- **Model A**: analogous to LHCb model I, but **2 auxiliary BWs** interfere with **X(6900)**
- **Model B**: analogous to LHCb model II, **one auxiliary BW** interferes with NRSPS
- Both models describe the data well
 - the broad structure at the lower mass could result from other physical effects, such as the feed-down
- The 3rd peak mass is consistent with the LHCb observed X(6900), with significance $> 5\sigma$

X(6900) $> 5\sigma$

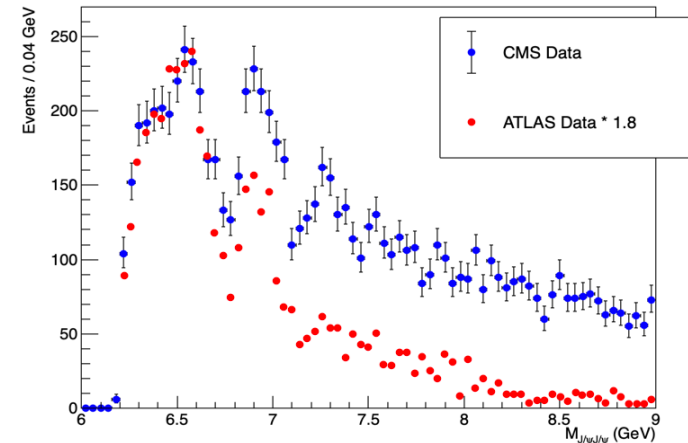
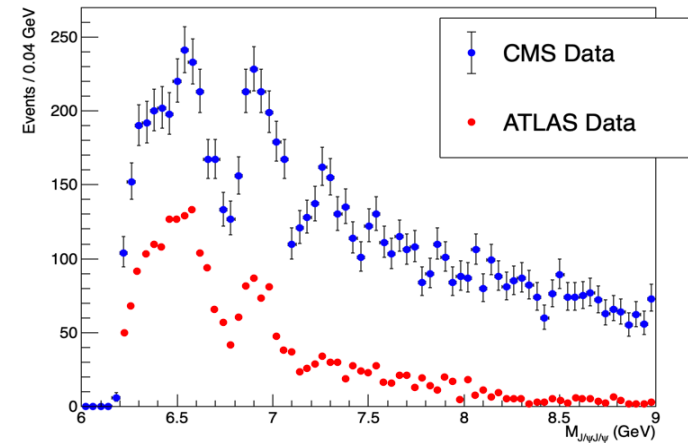
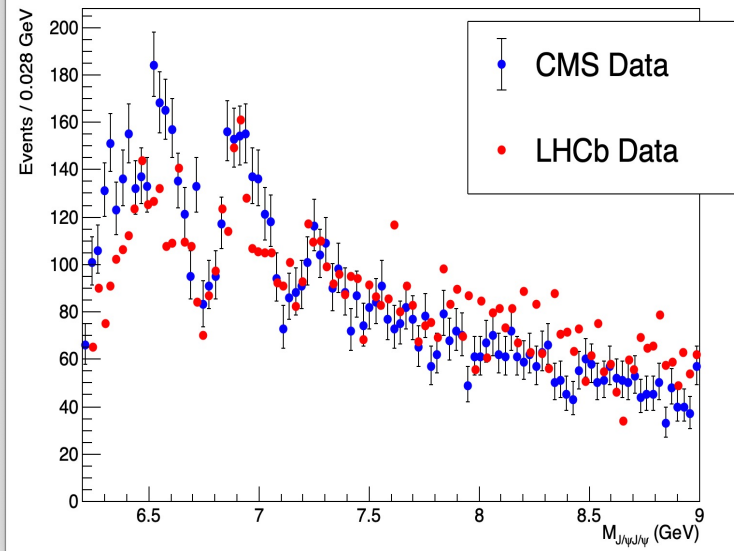


- **Model α :** $X(6900) + 2^{\text{nd}}$ resonance
 - Two bumps together: 4.7σ
 - 2^{nd} bump alone: 3σ
- **Model β :** a single resonance $X(6900)$ in this channel
 - 4.3σ

Extracted masses and widths (GeV)

$J/\psi + \psi(2S)$	model α	model β
m_3 or m	$7.22 \pm 0.03^{+0.01}_{-0.03}$	$6.96 \pm 0.05 \pm 0.03$
Γ_3 or Γ	$0.09 \pm 0.06^{+0.06}_{-0.03}$	$0.51 \pm 0.17^{+0.11}_{-0.10}$
$\Delta s/s$	$\pm 21\% \pm 14\%$	$\pm 20\% \pm 12\%$

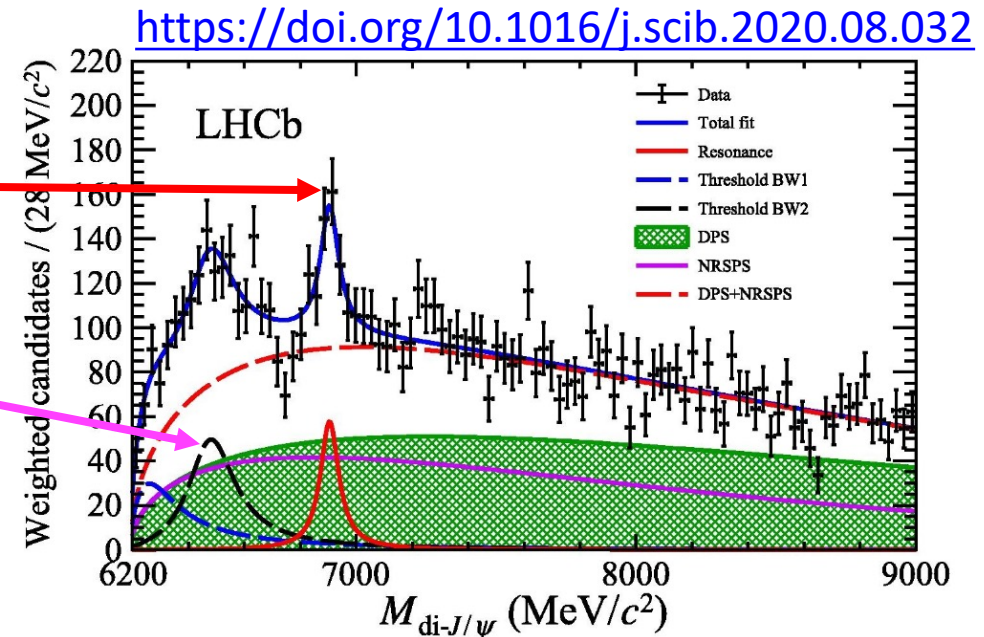
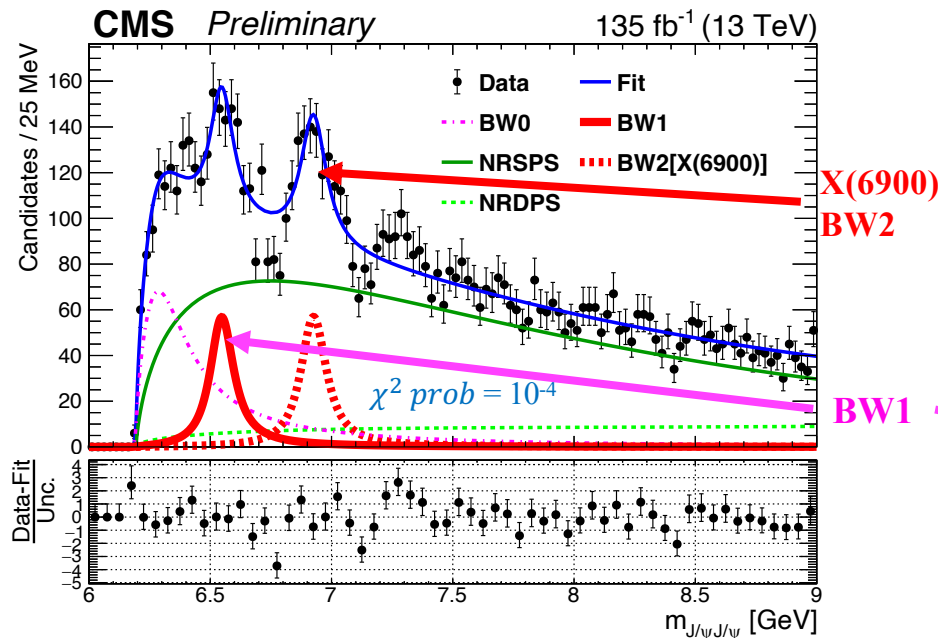
Disclaimer: comparison plots in this page are not made by ATLAS/CMS/LHCb
(taken from <https://indico.cern.ch/event/1158681/contributions/5162594/>)



- Comparing with LHCb, CMS has:
 - $135/(3+6) \approx 15X$ int. lum.
 - $(5/3)^4 \approx 8X$ muon acceptance
 - Higher muon p_T (>3.5 or 2.0 GeV vs >0.6 GeV)
 - Similar number of final events, but much less DPS
 - $2X$ yield @CMS for X(6900)

- Comparing with CMS, ATLAS has:
 - $1/3 - 1/2$ of CMS data (trigger?)
 - dR cut—remove high mass events

Fit CMS data with LHCb model I: 2 auxiliary BWs + X(6900) + bkg



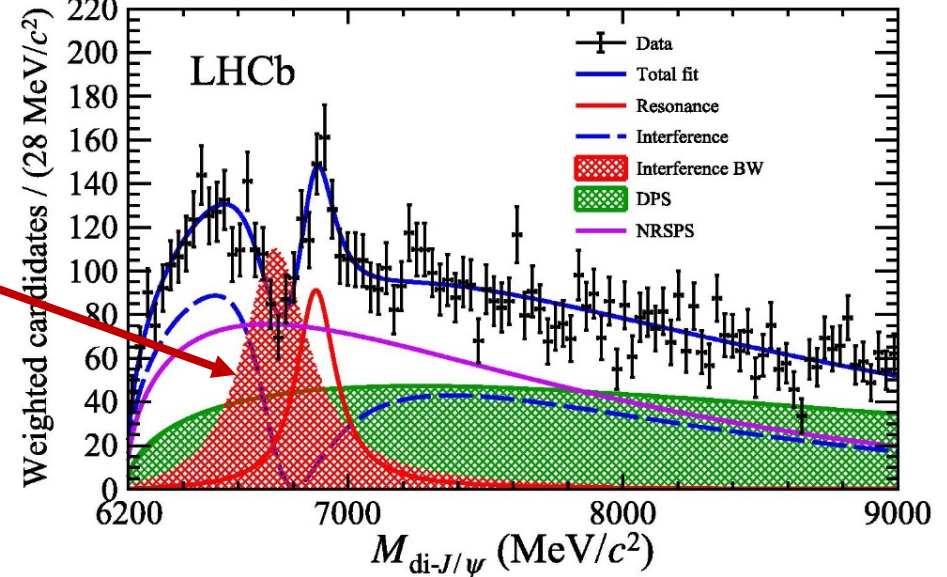
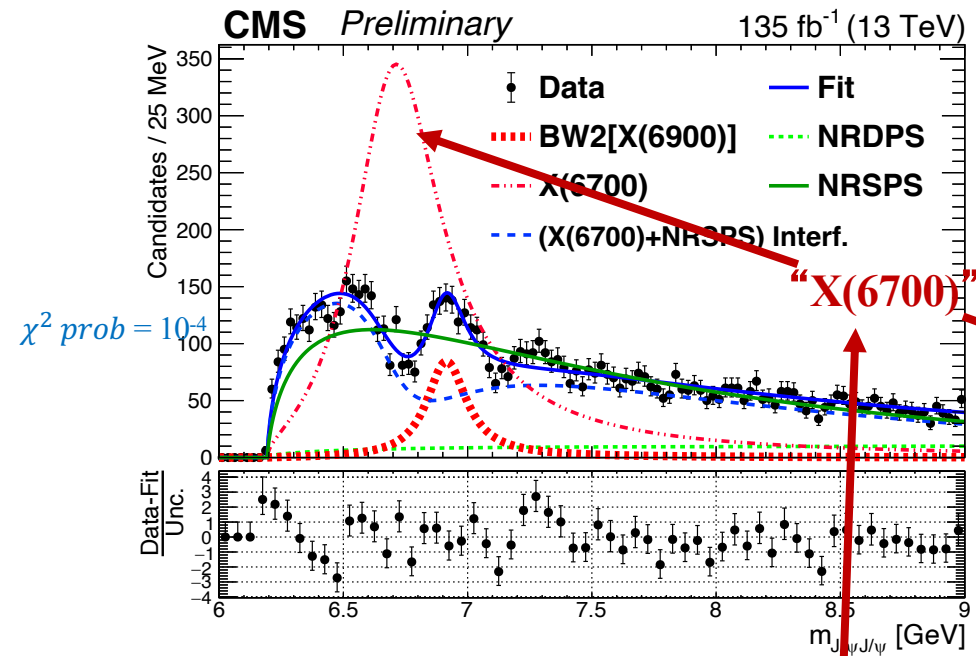
Exp.	Fit	$m(\text{BW1})$	$\Gamma(\text{BW1})$	$m(6900)$	$\Gamma(6900)$
LHCb [15]	Model I	unrep.	unrep.	$6905 \pm 11 \pm 7$	$80 \pm 19 \pm 33$
CMS	Model I	6550 ± 10	112 ± 27	6927 ± 10	117 ± 24

BW2 are in good agreement with LHCb X(6900)

- LHCb did not give parameters for BW1
 - CMS has a **shoulder** before BW1
 - helps make BW1 distinct
- Does not describe 2 dips well*

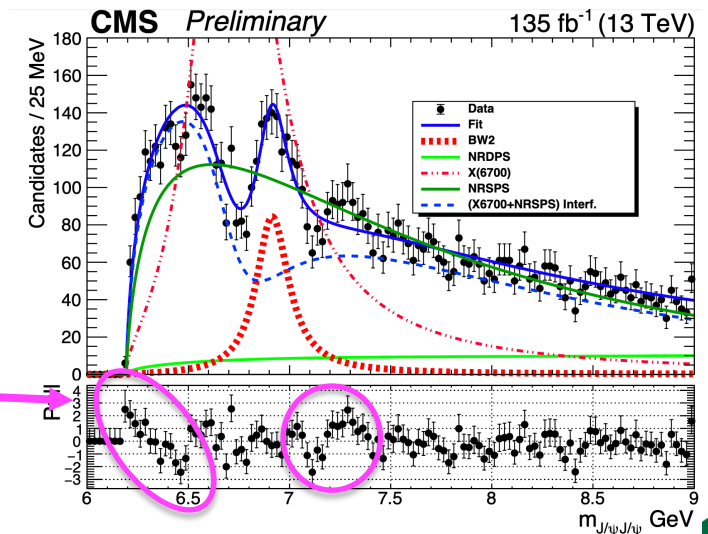
Fit CMS data with LHCb model II : “X(6700)” interferes with NRSPS + X(6900) + Bkg

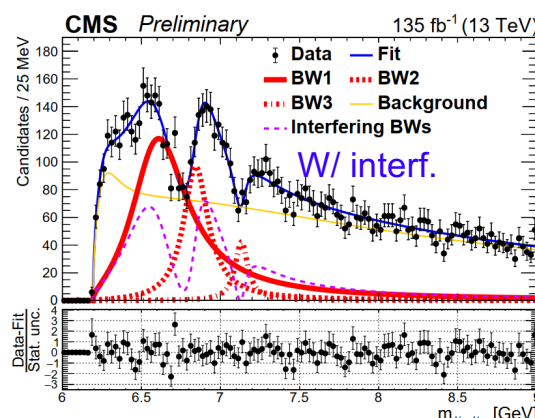
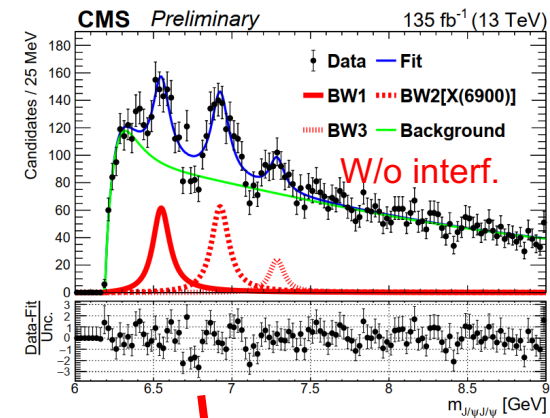
<https://doi.org/10.1016/j.scib.2020.08.032>



Exp.	Fit	$m(\text{BW1})$	$\Gamma(\text{BW1})$	$m(6900)$	$\Gamma(6900)$
LHCb [15]	Model II	6741 ± 6	288 ± 16	$6886 \pm 11 \pm 11$	$168 \pm 33 \pm 69$
CMS	Model II	6736 ± 38	439 ± 65	6918 ± 10	187 ± 40

- CMS obtained larger amplitude and wider width for X(6700)
- Does not describe X(6600) and below
- Does not describe X(7200) region





1^1P_1	1^{--}	363.9	320.3	-366.7	337.5	-14.4	0	0	-2.6	6553	-	-
1^3P_0	0^{++}	356.7	320.2	-366.7	337.5	-7.2	-30.9	-43.1	-2.6	6460	6398.1	$\eta_c(1S)\chi_{c0}(1P)$
1^3P_1	1^{++}	356.6	320.3	-366.7	337.5	-7.2	-28.4	21.5	-2.7	6554	6494.1	$\eta_c(1S)\chi_{c1}(1P)$
1^3P_2	2^{++}	356.6	320.2	-366.7	337.5	-7.2	28.4	-2.1	-2.4	6587	6539.6	$\eta_c(1S)\chi_{c2}(1P)$
1^5P_1	1^{--}	342.4	320.4	-366.7	337.5	7.2	-85.3	-30.2	-2.7	6489	6508.8	$\eta_c(1S)h_{c1}(1P)$
1^5P_2	2^{--}	342.2	320.2	-366.7	337.5	7.2	-28.4	30.2	-2.5	6577	6607.6	$J/\psi(1S)\chi_{c1}(1P)$
1^5P_3	3^{--}	342.3	320.3	-366.7	337.5	7.2	56.9	-8.6	-2.5	6623	6653.1	$J/\psi(1S)\chi_{c2}(1P)$
2^1P_1	1^{--}	414.7	688.7	-263.4	548.6	-11.2	0	0	-1.6	6925	-	-
2^3P_0	0^{++}	410.0	689.6	-263.4	548.6	-5.6	-46.2	-34.5	-1.7	6851	-	-
2^3P_1	1^{++}	410.0	689.6	-263.4	548.6	-5.6	-23.1	17.2	-1.6	6926	-	-
2^3P_2	2^{++}	410.0	689.6	-263.4	548.7	-5.6	23.1	-3.4	-1.7	6951	-	-
2^5P_1	1^{--}	398.7	689.5	-263.4	548.6	-5.6	-69.3	-24.2	-1.7	6847	-	-
2^5P_2	2^{--}	398.7	689.5	-263.4	548.6	5.6	-23.1	24.2	-1.5	6944	-	-
2^5P_3	3^{--}	398.8	689.7	-263.4	548.6	5.6	46.2	-6.9	-1.6	6982	-	-
3^1P_1	1^{--}	479.8	982.2	-215.5	727.8	-9.3	0	0	-1.1	7221	-	-
3^3P_0	0^{++}	475.2	982.7	-215.5	727.7	-4.6	-41.9	-31.0	-1.2	7153	-	-
3^3P_1	1^{++}	475.1	982.6	-215.5	727.7	-4.6	-20.9	15.5	-1.2	7220	-	-
3^3P_2	2^{++}	475.1	982.6	-215.5	727.8	-4.6	20.9	-3.1	-1.0	7243	-	-
3^5P_1	1^{--}	465.9	982.8	-215.5	727.7	4.6	-62.8	-21.7	-1.2	7150	-	-
3^5P_2	2^{--}	465.7	982.6	-215.5	727.8	-4.6	-20.9	21.7	-1.1	7236	-	-
3^5P_3	3^{--}	465.8	982.6	-215.5	727.8	4.6	41.9	-6.2	-1.1	7271	-	-

[arXiv:2108.04017 \[hep-ph\]](https://arxiv.org/abs/2108.04017)

P-wave

$$M[\text{BW1}] = 6552 \pm 10 \pm 12 \text{ MeV}$$

$$M[\text{BW2}] = 6927 \pm 9 \pm 5 \text{ MeV}$$

$$M[\text{BW3}] = 7287 \pm 19 \pm 5 \text{ MeV}$$

Table 1. Predictions of the masses (MeV) of S-wave fully heavy $T_{4Q}(nS)$ tetraquarks. Only 0^{++} and 2^{++} are considered for $T_{bc\bar{b}\bar{c}}$. The uncertainty is from the coupling constant $\alpha_s = 0.35 \pm 0.05$.

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$T_{4Q}(nS)$ states	J^P	Mass(n=1)	Mass(n=2)	Mass(n=2)	Mass(n=3)
$T_{cc\bar{c}\bar{c}}$	0^{++}	6055^{+69}_{-74}	6555^{+36}_{-37}	6883^{+27}_{-27}	7154^{+22}_{-22}
$T_{cc\bar{c}\bar{c}}$	2^{++}	6090^{+62}_{-66}	6600^{+34}_{-35}	6880^{+27}_{-26}	7160^{+22}_{-22}
$T'_{cc\bar{c}\bar{c}}$	0^{++}	5984^{+64}_{-67}	6468^{+35}_{-35}	6775^{+26}_{-26}	7066^{+21}_{-21}
$T_{bc\bar{b}\bar{c}}$	0^{++}	12387^{+109}_{-120}	12911^{+48}_{-49}	13200^{+35}_{-36}	13429^{+29}_{-30}
$T_{bc\bar{b}\bar{c}}$	2^{++}	12401^{+117}_{-106}	12914^{+49}_{-49}	13202^{+35}_{-35}	13430^{+29}_{-29}
$T'_{bc\bar{b}\bar{c}}$	0^{++}	12300^{+106}_{-117}	12816^{+48}_{-50}	13044^{+35}_{-35}	13333^{+29}_{-29}
$T_{bb\bar{b}\bar{b}}$	0^{++}	18475^{+151}_{-169}	19073^{+59}_{-63}	19533^{+42}_{-42}	19566^{+33}_{-35}
$T_{bb\bar{b}\bar{b}}$	2^{++}	18483^{+149}_{-168}	19075^{+59}_{-62}	19555^{+41}_{-43}	19567^{+33}_{-35}
$T'_{bb\bar{b}\bar{b}}$	0^{++}	18383^{+149}_{-167}	18976^{+59}_{-62}	19556^{+43}_{-42}	19468^{+34}_{-34}

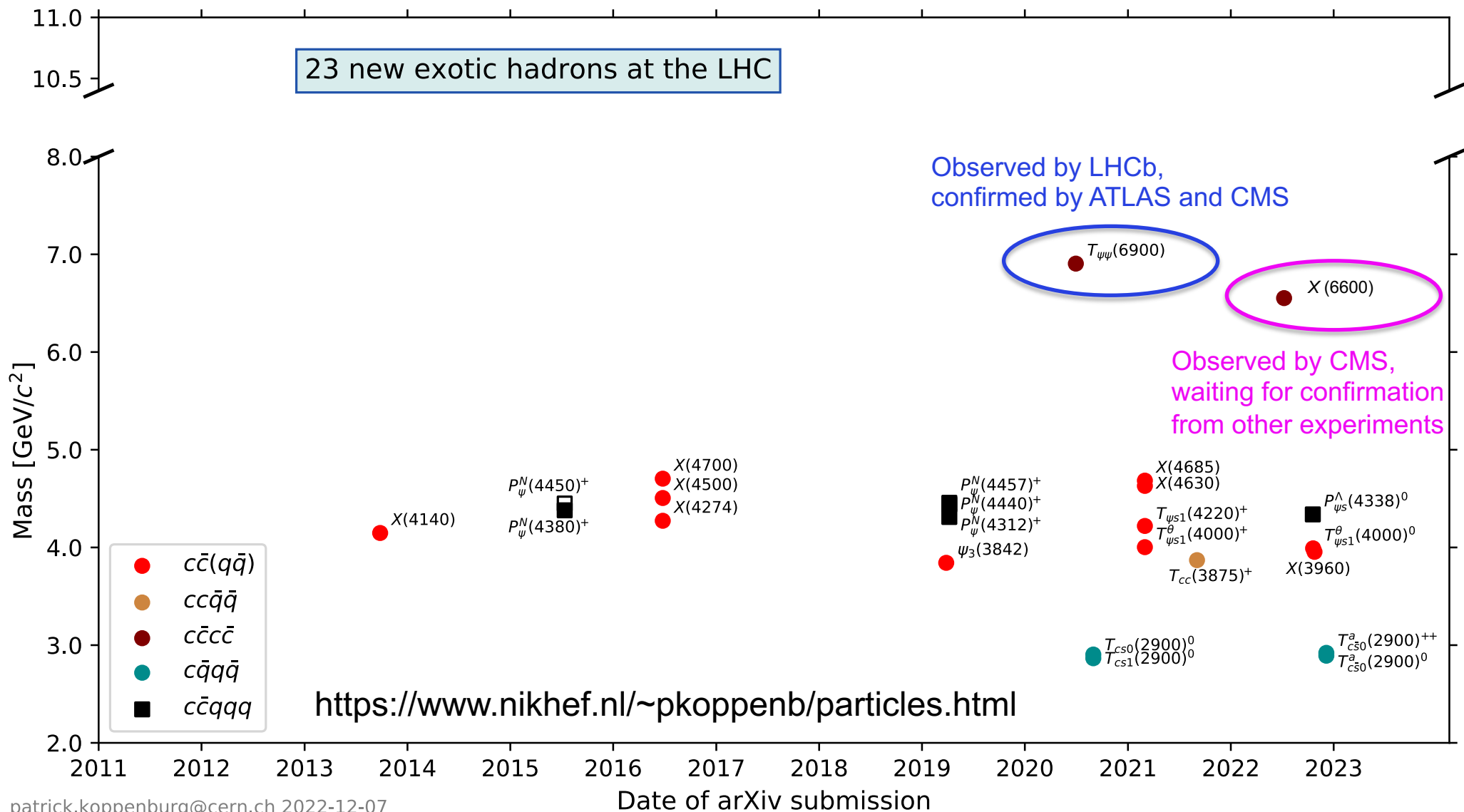
S-wave

$$M[\text{BW1}] = 6638 \pm 10 \pm 12 \text{ MeV}$$

$$M[\text{BW2}] = 6847 \pm 9 \pm 5 \text{ MeV}$$

$$M[\text{BW3}] = 7134 \pm 19 \pm 5 \text{ MeV}$$

- Radial excited p-wave states (like J/ψ series)?
- Or Radial excited S-wave states?
- Theoretical situation difficulty & confusing
 - Important next step: measure J^{PC} to clarify
- Natural question: what about YY final state?

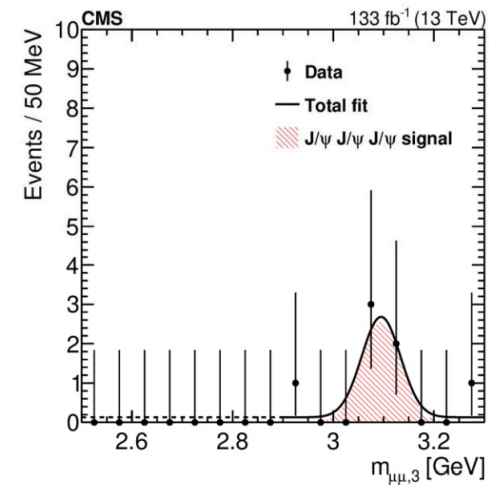
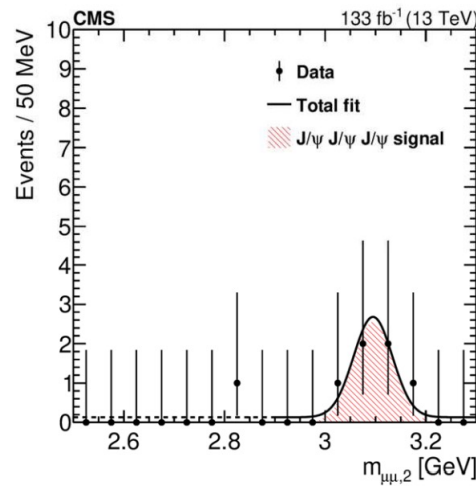
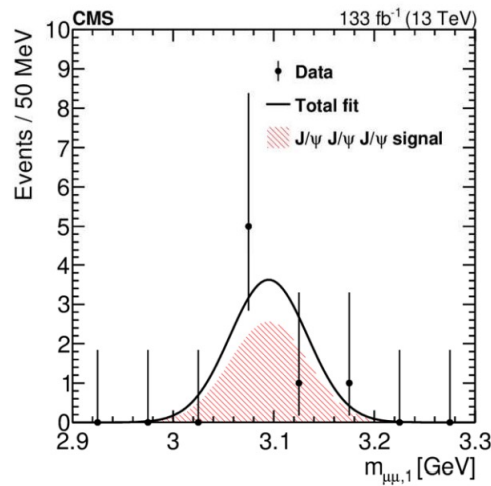
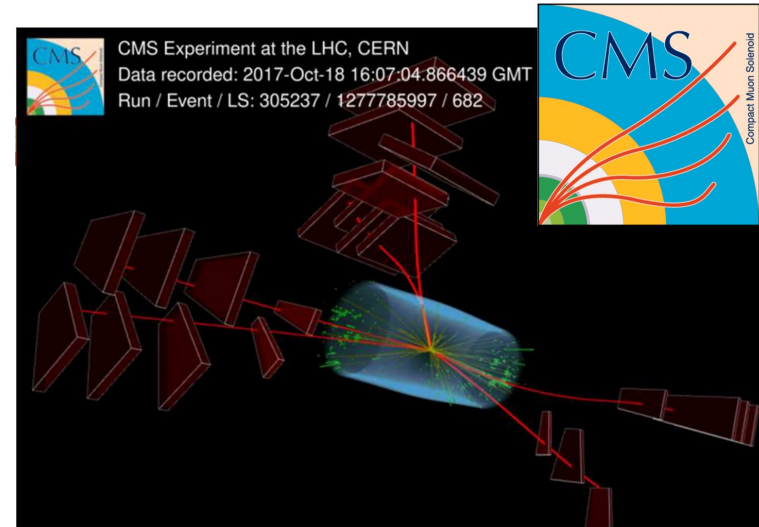


Signal yield: $5_{-1.9}^{+2.6}$ events

Significance $> 5\sigma$

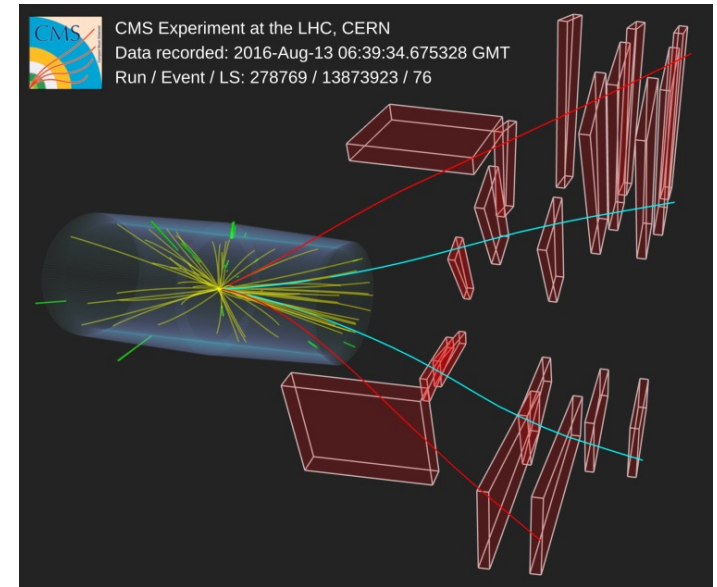
$$\sigma(pp \rightarrow J/\psi J/\psi J/\psi X) = 272 +141-104 \text{ (stat)} \pm 17 \text{ (syst) fb}$$

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“6c” search in future?

- All-heavy quark exotic structures offer a system easier to understand
 - A new window to understand strong interaction
- CMS found 3 significant structures in $\text{di-J}/\psi$ mass spectrum
 - X(6900) consistent with LHCb
 - **First observation of X(6600)** and evidence of X(7300) in $\text{di-J}/\psi$
 - Dips in data show possible interference effects
 - **A family of structures which are candidates for all-charm tetra-quarks!**
- ATLAS found significant excess in di-charmonium mass spectrum
 - X(6900) and low mass consistent with LHCb in $\text{di-J}/\psi$ channel
 - Evidence of structures in the $\text{J}/\psi + \psi(2S)$ channel
- Triple J/ψ production has also been observed for the first time
- First observation of $\text{J}/\psi + \text{Y}(1S)$ in pp collisions by LHCb last month (arXiv:2305.15580)



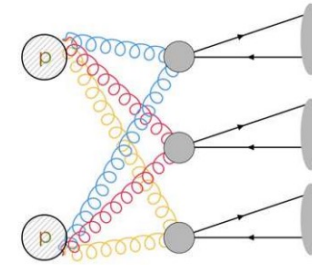
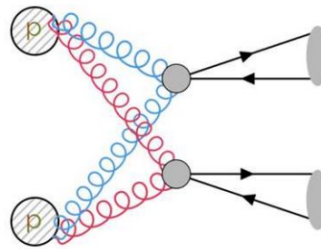
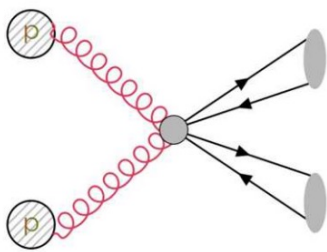
X(6600) event display



Backup



- Study interplay of soft QCD with (semi)hard QCD and EW physics
- Sensitivity to perturbative heavy flavor generation and nonperturbative initial and final state effects
- Initial state: e.g. sensitivity to the concepts of single (SPS), double (DPS) and triple (TPS) parton scattering



parameterized by σ_{eff}

$$\sigma_{\text{DPS}}^{AB} = \frac{1}{1 + \delta_{AB}} \frac{\sigma^A \sigma^B}{\sigma_{\text{eff}}}$$

- Final state: e.g. sensitivity to heavy flavour hadron formation (colour singlet vs. colour octet), sensitivity to resonant multi-heavy-flavor states

Muon selection

- $p_T(\mu^\pm) > 2.0 \text{ GeV}/c$
- $|\eta(\mu^\pm)| < 2.4$
- All muons are soft
- For 2017-18 years: $p_T(\mu^\pm) > 3.5 \text{ GeV}/c$ for at least one $\mu^+\mu^-$ pair, which has $vtxprob(\mu^+\mu^-) > 0.5\%$ and $2.95 < m_{\mu^+\mu^-} < 3.25 \text{ GeV}$

J/ψ selection

- $2.95 < m_{J/\psi} < 3.25 \text{ GeV}$
- $p_T(J/\psi) > 3.5 \text{ GeV}/c$
- $vtxprob(J/\psi) > 0.5\%$
- Constrained $vtxprob(J/\psi) > 0.1\%$

J/ψJ/ψ selection

- $vtxprob(4\mu) > 0.5\%$
- $vtxprob(J/\psi J/\psi) > 0.1\%$
- Proper HLT is fired in event

Multiple candidates

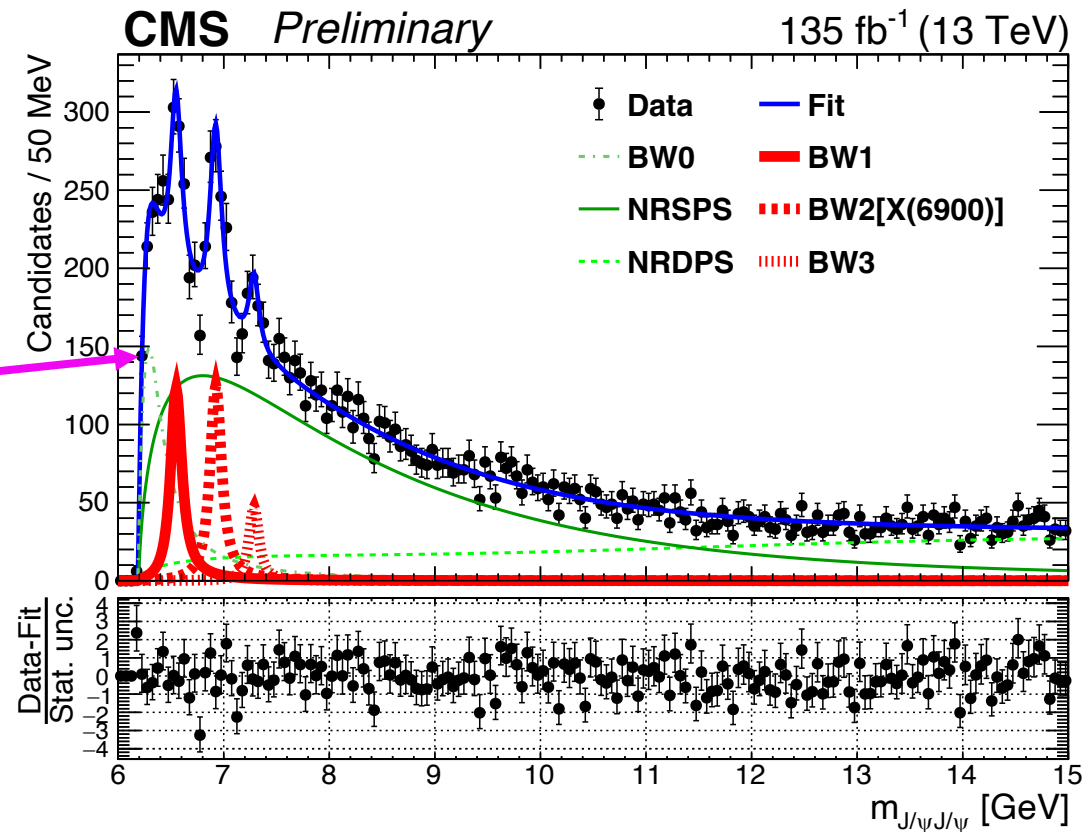
- Choose the best candidate with minimum $\left(\frac{M(J/\psi_1) - M(J/\psi_{PDG})}{\sigma(M(J/\psi_1))}\right)^2 + \left(\frac{M(J/\psi_2) - M(J/\psi_{PDG})}{\sigma(M(J/\psi_2))}\right)^2$ value if there are 4 muons in event, but more than one candidate ($\sim 0.2\%$)
- Keep all candidates if there are more than 4 muons in event ($\sim 0.2\%$)

Baseline mass variable – invariant mass of two constrained J/ψ candidates

CMS background (SPS + DPS + BW0)

$\chi^2 \text{ prob} = 79\%$

[6.2,15] GeV



- Most significant structure is a BW at threshold, **BW0**--what is its meaning?
- **Treat BW0 as part of background** due to:
 - **BW0 parameters very sensitive to SPS and DPS model assumptions**
 - A region populated by feed-down from possible higher mass states
 - Possible coupled-channel interactions, pomeron exchange processes...

- To include systematics, alternative resonance/background shapes applied in the fit.
- Calculate signal- and null-hypothesis NLL_{syst} including systematic using:

$$NLL_{(syst-sig)} = \text{Min}\{NLL_{(nom-sig)}, NLL_{(alt-i-sig)}+0.5+0.5\cdot\Delta dof\}$$
 - ❑ $NLL_{(nom-sig)}$: the NLL of nominal 'signal hypothesis' fit.
 - ❑ $NLL_{(alt-i-sig)}$: the NLL of i-th alternative fit of 'signal hypothesis'
 - ❑ Δdof : the additional free parameters comparing to the nominal 'signal hypothesis' fit.
- $NLL_{(syst-null)} = \text{Min}\{NLL_{(nom-null)}, NLL_{(alt-j-null)}+0.5+0.5\cdot\Delta dof\}$
- Significance including systematics as usual from $NLL_{(syst-null)} - NLL_{(syst-sig)}$

	Significance with syst.
BW1	5.7σ
BW2	<i>no sensible changes</i>
BW3	<i>no sensible changes</i>

- S-wave relativistic Breit-Wigner (used in default fit):

$$BW(m; m_0, \Gamma_0) = \frac{\sqrt{m\Gamma(m)}}{m_0^2 - m^2 - im\Gamma(m)}, \text{ where } \Gamma(m) = \Gamma_0 \frac{qm_0}{q_0 m},$$

q is the momentum of a daughter in the mother particle rest frame; q_0 means the value at peak position ($m = m_0$).

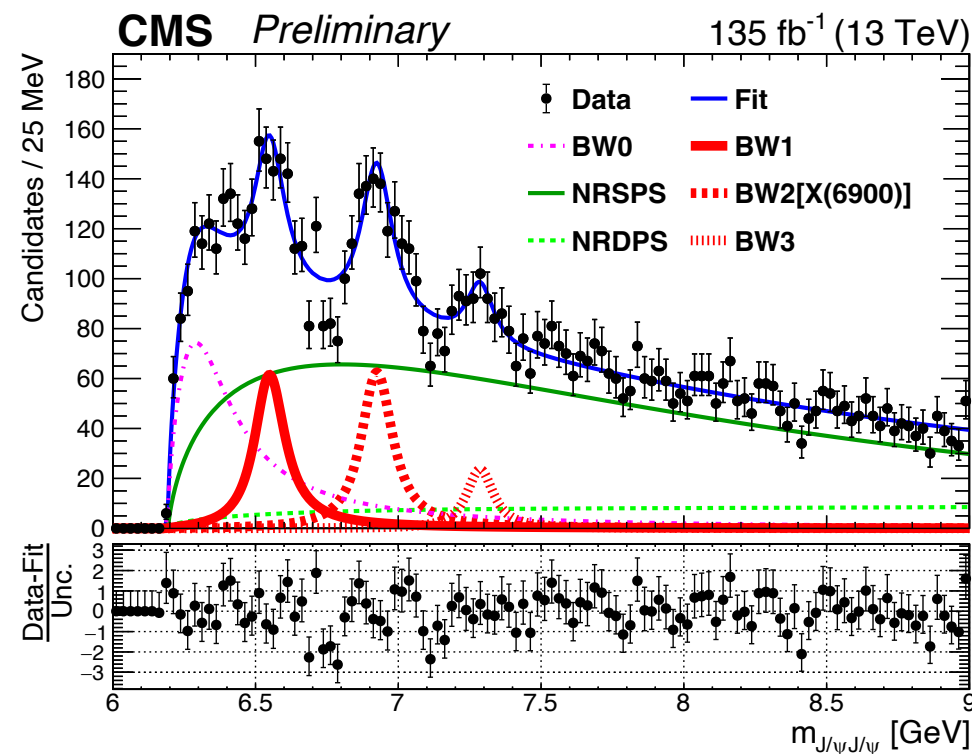
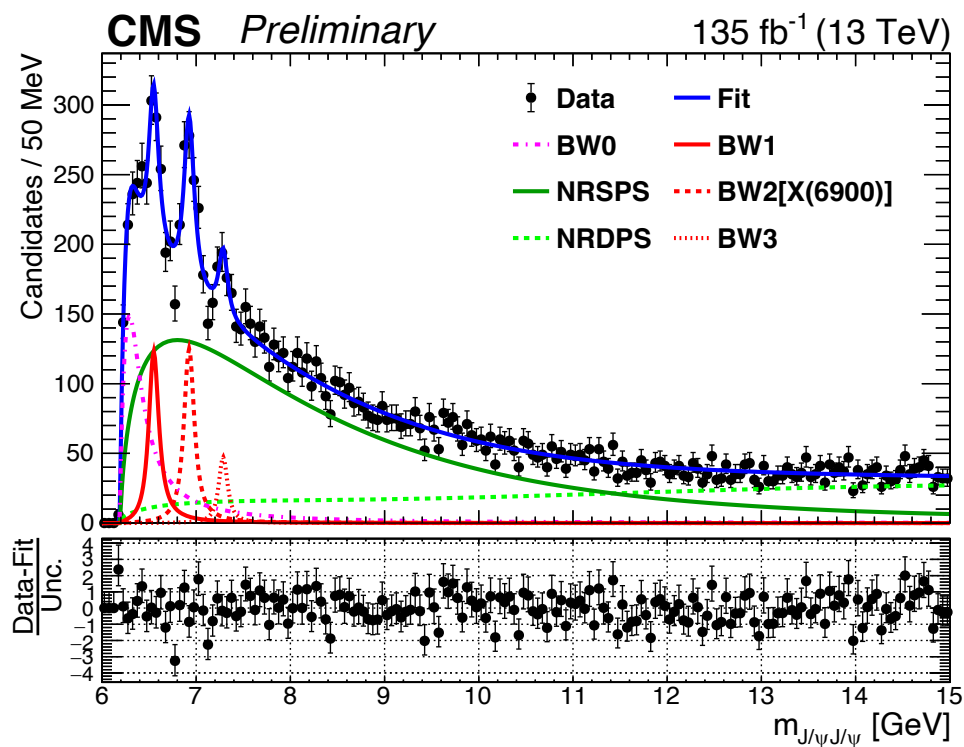
- NRSPS and NRDPS:

$$f_{NRSPS}(x, x_0, \alpha, p_1, p_2, p_3)$$

$$= (x - x_0)^\alpha \cdot \left(1 - \left(\frac{1}{(15 - x_0)^2} - \frac{p_1}{10} \right) \cdot (15 - x)^2 \right) \cdot \exp \left(- \frac{(x - x_0)^{p_3}}{2 \cdot p_2^{p_3}} \right),$$

$$f_{NRDPS}(x, a, p_0, p_1, p_2) = \sqrt{x_t} \cdot \exp(-a \cdot x_t) \cdot (p_0 + p_1 \cdot x_t + p_2 \cdot x_t^2),$$

where $x_0 = 2m_{J/\psi}$, $x_t = x - x_0$



Source	ΔM_{BW1}	ΔM_{BW2}	ΔM_{BW3}	$\Delta \Gamma_{BW1}$	$\Delta \Gamma_{BW2}$	$\Delta \Gamma_{BW3}$
signal shape	3	4	3	14	7	7
NRDPS	1	< 1	< 1	3	3	4
NRSPS	3	1	1	18	15	17
momentum scaling	1	3	4	-	-	-
mass resolution	< 1	< 1	< 1	< 1	< 1	1
combinatorial background	< 1	< 1	< 1	2	3	3
efficiency	< 1	< 1	< 1	1	< 1	1
feeddown shape	11	1	1	25	8	6
total	12	5	5	34	19	20

- Investigated effects of systematics on local significance by a profiling procedure
- A discrete set of individual alternative signal and background hypotheses tested in minimization
 - Significant change: BW1 significance changed from 6.5σ to $>5.7\sigma$
 - No relative significance changes for BW2 and BW3

$$M[BW1] = 6552 \pm 10 \pm 12 \text{ MeV} \quad \Gamma[BW1] = 124 \pm 29 \pm 34 \text{ MeV} \quad >5.7\sigma$$

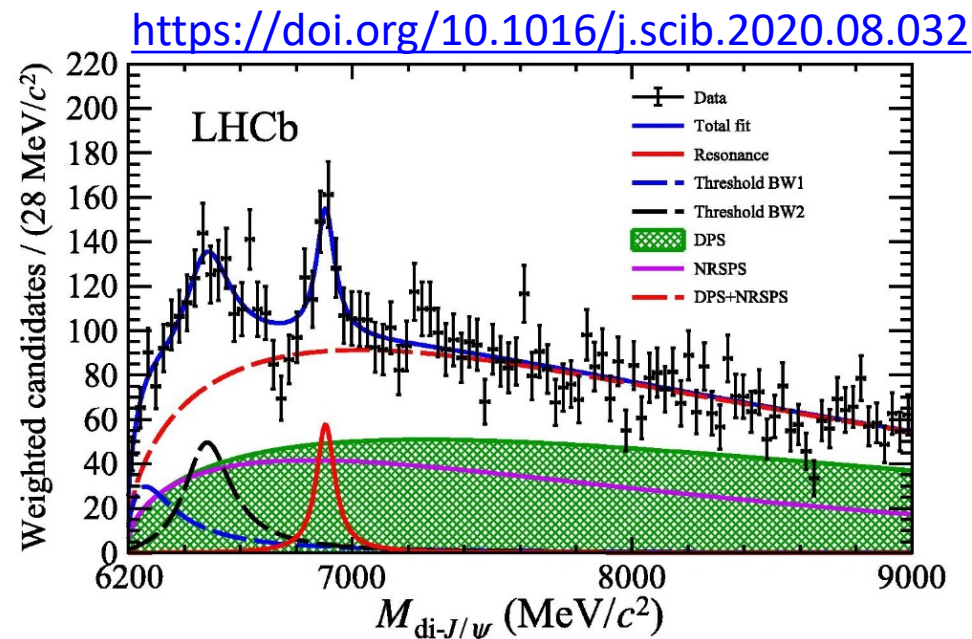
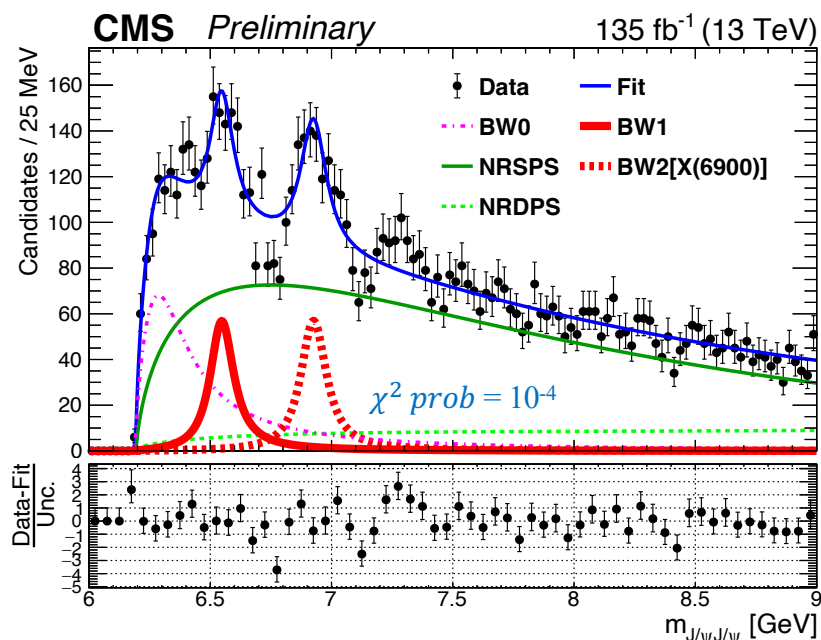
$$M[BW2] = 6927 \pm 9 \pm 5 \text{ MeV} \quad \Gamma[BW2] = 122 \pm 22 \pm 19 \text{ MeV} \quad >9.4\sigma$$

$$M[BW3] = 7287 \pm 19 \pm 5 \text{ MeV} \quad \Gamma[BW3] = 95 \pm 46 \pm 20 \text{ MeV} \quad >4.1\sigma$$

Fit	Dominant sources	ΔM_{BW1}	ΔM_{BW2}	ΔM_{BW3}	$\Delta \Gamma_{BW1}$	$\Delta \Gamma_{BW2}$	$\Delta \Gamma_{BW3}$
Interference	Signal shape	7	12	7	56	8	7
	NRDPS	1	3	2	18	6	2
	NRSPS	9	14	13	85	9	20
	Resolution	8	4	1	24	7	13
	Combinatorial bkg.	7	2	< 1	5	3	2
	Feeddown shape	-27	+44	+38	-208	+19	+12
Full uncertainty		+16 -31	+48 -20	+41 -15	+109 -235	+25 -17	+29 -26

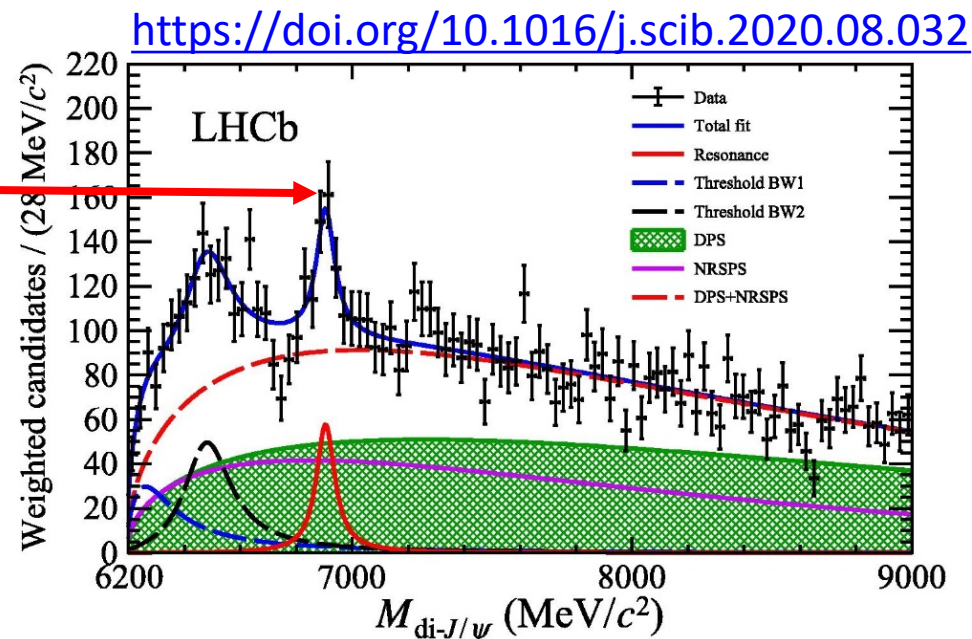
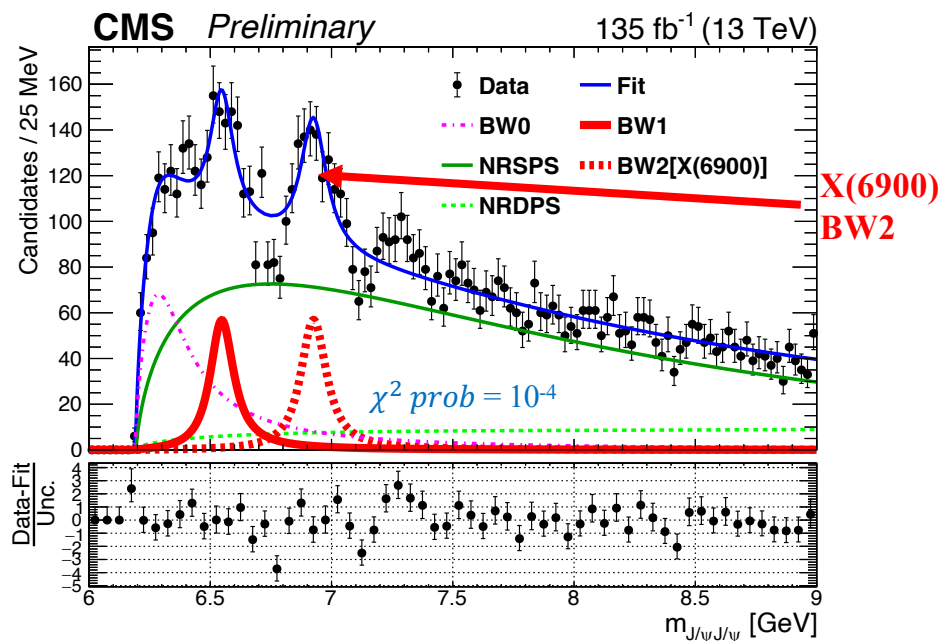
- Total systematic uncertainty is quadrature sum of each source
- Systematic uncertainties from feeddown contribution are asymmetric
- Systematic uncertainties from other sources are symmetric

Fit CMS data with LHCb model I : 2 auxiliary BWs + X(6900) + bkg



Exp.	Fit	$m(\text{BW1})$	$\Gamma(\text{BW1})$	$m(6900)$	$\Gamma(6900)$
LHCb [15]	Model I	unrep.	unrep.	$6905 \pm 11 \pm 7$	$80 \pm 19 \pm 33$
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Fit CMS data with LHCb model I : 2 auxiliary BWs + X(6900) + bkg

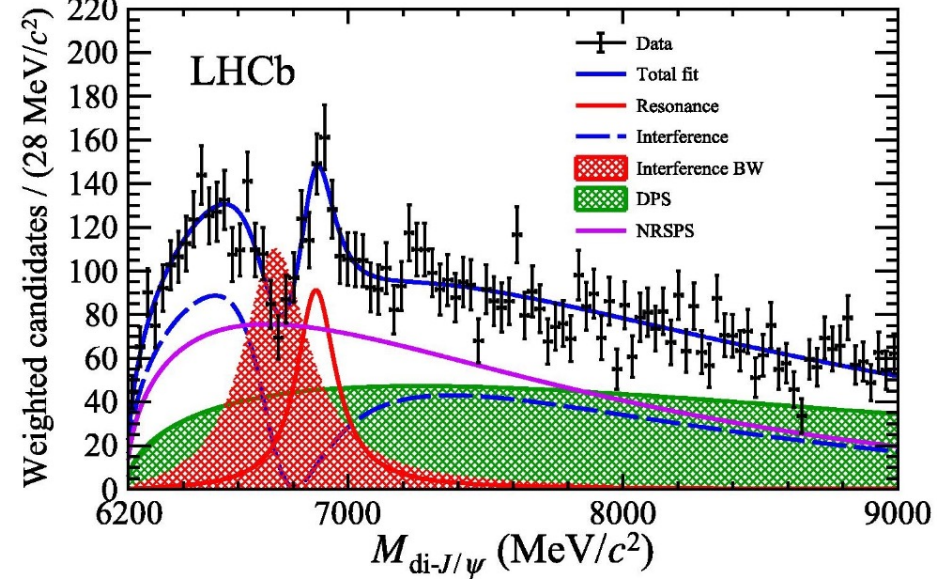
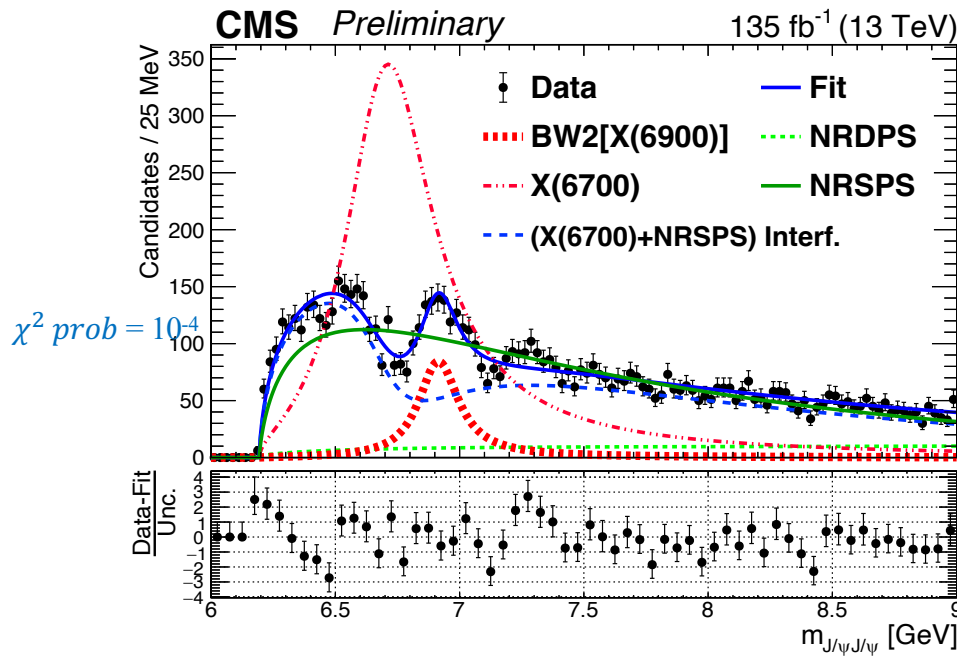


BW2 are in good agreement with LHCb X(6900)

Exp.	Fit	$m(\text{BW1})$	$\Gamma(\text{BW1})$	$m(6900)$	$\Gamma(6900)$
LHCb [15]	Model I	unrep.	unrep.	$6905 \pm 11 \pm 7$	$80 \pm 19 \pm 33$
CMS	Model I	6550 ± 10	112 ± 27	6927 ± 10	117 ± 24

Fit CMS data with LHCb model II : “X(6700)” interferes with NRSPS + X(6900) + Bkg

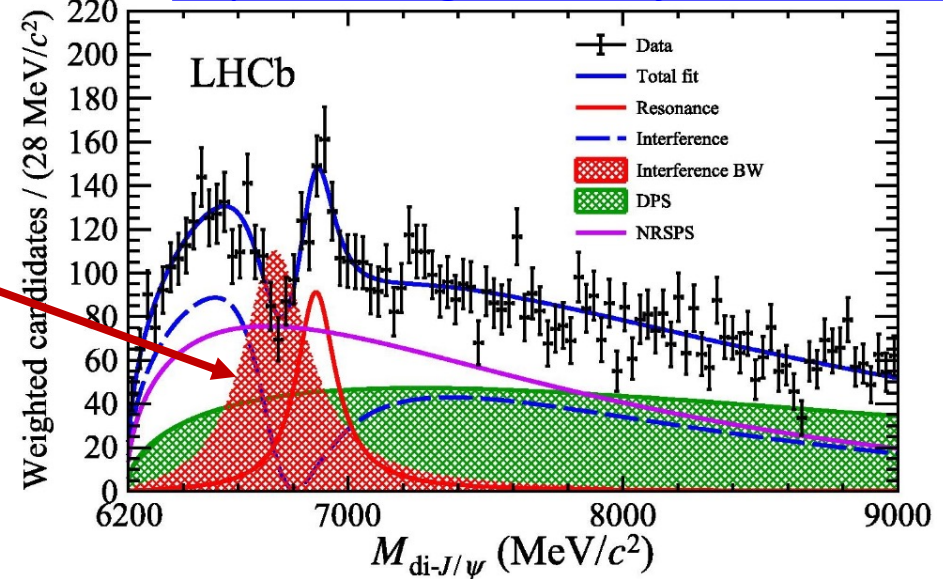
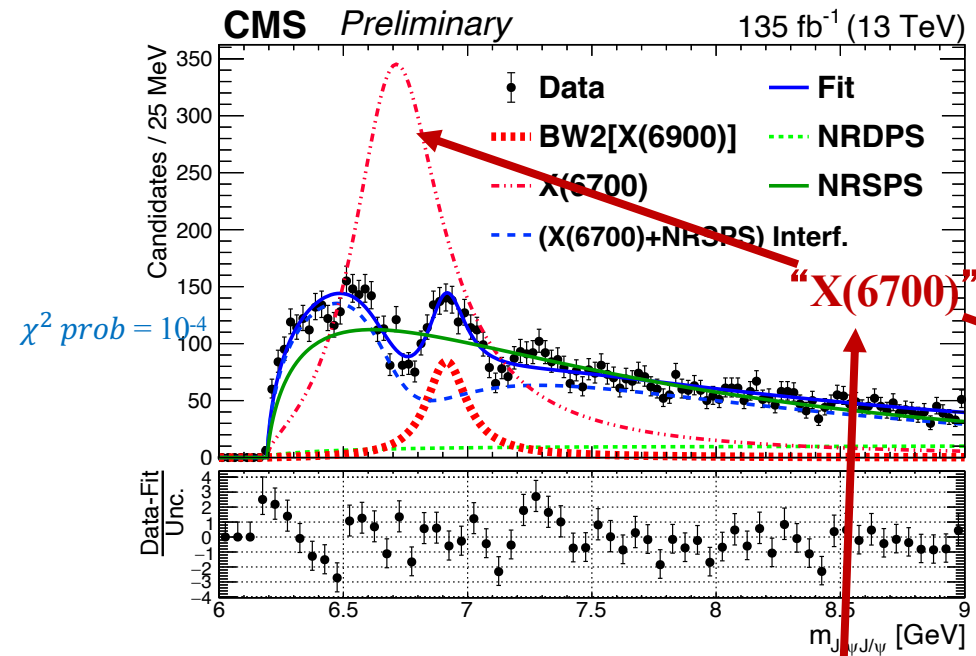
<https://doi.org/10.1016/j.scib.2020.08.032>



Exp.	Fit	$m(\text{BW1})$	$\Gamma(\text{BW1})$	$m(6900)$	$\Gamma(6900)$
LHCb [15]	Model II	6741 ± 6	288 ± 16	$6886 \pm 11 \pm 11$	$168 \pm 33 \pm 69$
CMS	Model II	6736 ± 38	439 ± 65	6918 ± 10	187 ± 40

Fit CMS data with LHCb model II : “X(6700)” interferes with NRSPS + X(6900) + Bkg

<https://doi.org/10.1016/j.scib.2020.08.032>



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- CMS obtained larger amplitude and wider width for X(6700)

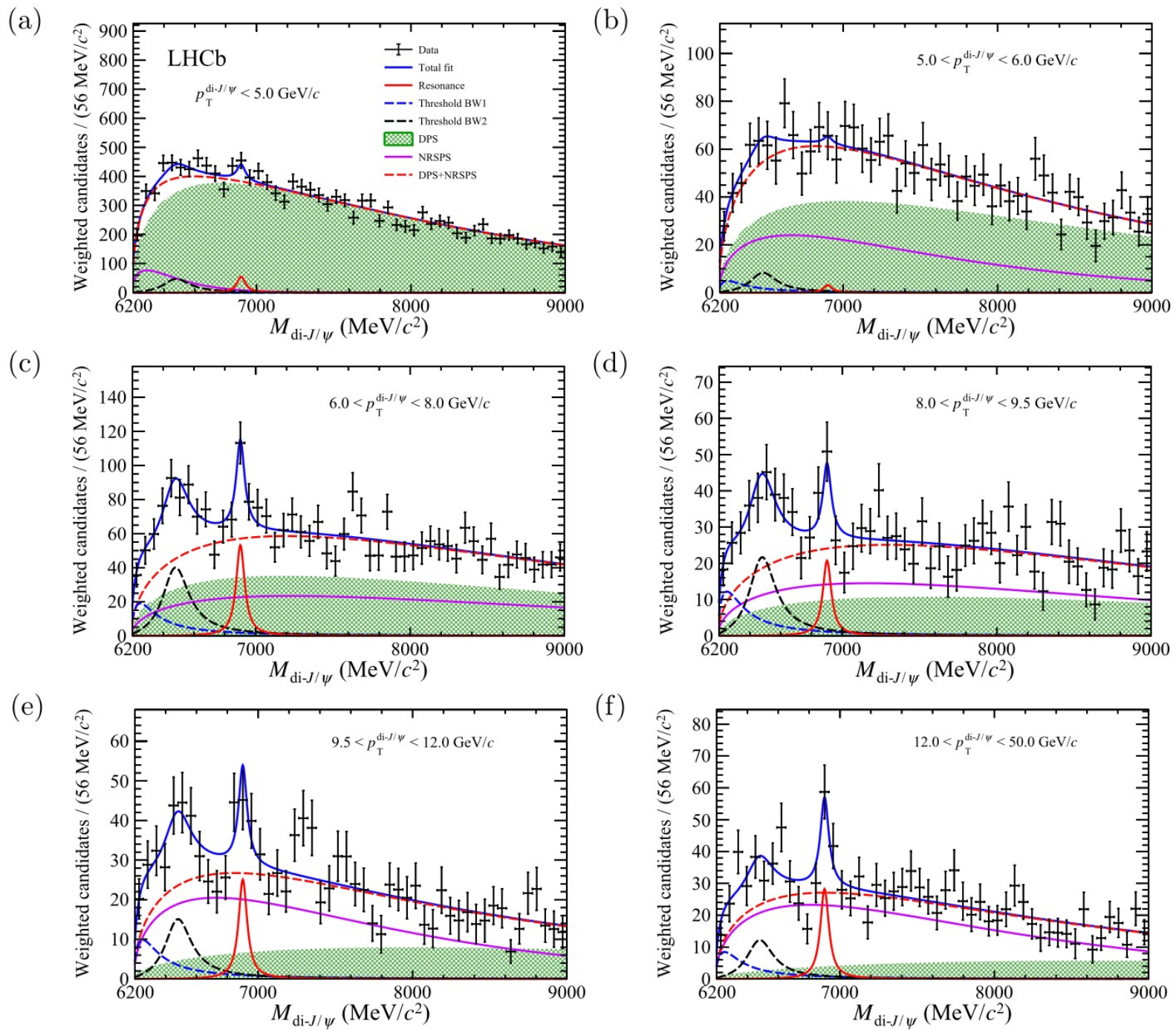


Fig. 4. Invariant mass spectra of weighted di- J/ψ candidates in bins of $p_T^{\text{di-}J/\psi}$ and overlaid projections of the $p_T^{\text{di-}J/\psi}$ -binned fit with model I.