

# $\bar{D}$ meson and nucleon interaction: from exotic hadrons to charm nuclei

Y. Yamaguchi, S. Y., A. Hosaka, Phys. Rev. D106, 094001 (2022)



Shigehiro YASUI

∈ Sasaki Lab. ⊂ SKCM<sup>2</sup> ⊂ Hiroshima University



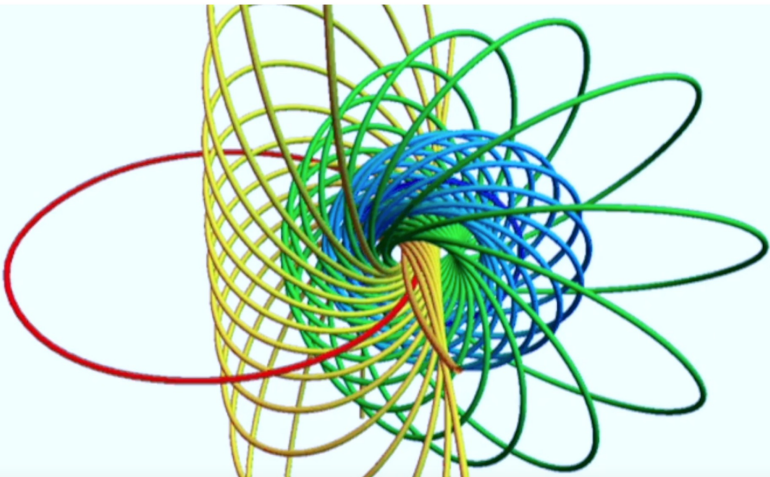
# International Institute for Sustainability with Knotted Chiral Meta Matter/SKCM<sup>2</sup>

World Premier International Research Center Initiative/WPI at Hiroshima University



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Building a sustainable world,

## knot by knot

The International Institute for Sustainability with Knotted Chiral Meta Matter



液晶・コロイド・ゲル

量子物質

数学・理論

(バイオ)ポリマー

SKCM<sup>2</sup>

Members: Smalyukh (HU/CU), 灰野 (HU), Senyuk (CU/HU), Dijkstra (UU), Hsu (AS), Vignolini (UCam), 佐藤 (RIKEN), 藤田 (HU), 堀 (HU), 小島居 (HU), Donnelly (MPI), Leonov (HU), 志垣 (HU), 黒田 (HU), 井上 (HU), 小島居 (HU), Kalman (TIT), 佐々木 (UWr/HU), Dunkel (MIT), Matsumoto (GT).

Legend:

- HU: 広島大学
- CU: コロラド大学 (アメリカ)
- UU: ユトレヒト大学 (オランダ)
- AS: 中央研究院 (台湾)
- UCam: ケンブリッジ大学 (イギリス)
- GT: ジョージア工科大学 (アメリカ)
- MIT: マサチューセッツ工科大学 (アメリカ)
- TIT: 東京工業大学
- MPI: マックスプランク研究所 (ドイツ)
- UWr: グロツワフ大学 (ポーランド)

- ✓ Cross-pollinates mathematical knot theory and chirality knowledge across disciplines and scales
- ✓ Creation of designable artificial knot-like particles that exhibit highly unusual and technologically useful properties

## Hadron & nuclear physics group

PI: Kenta SHIGAKI (HU, ALICE member)

**PI: Chihiro SASAKI (HU, Uni. of Wroclaw)**

coPI: Chiho NONAKA (HU)

coPI: Muneto NITTA (HU, Keio Uni.)

# Contents

1. Introduction: Why  $\bar{D}$  meson and nucleon?
2.  $\bar{D}$  meson and nucleon potential
3.  $B$  meson and nucleon potential
4. Discussions
5. Summary

# Contents

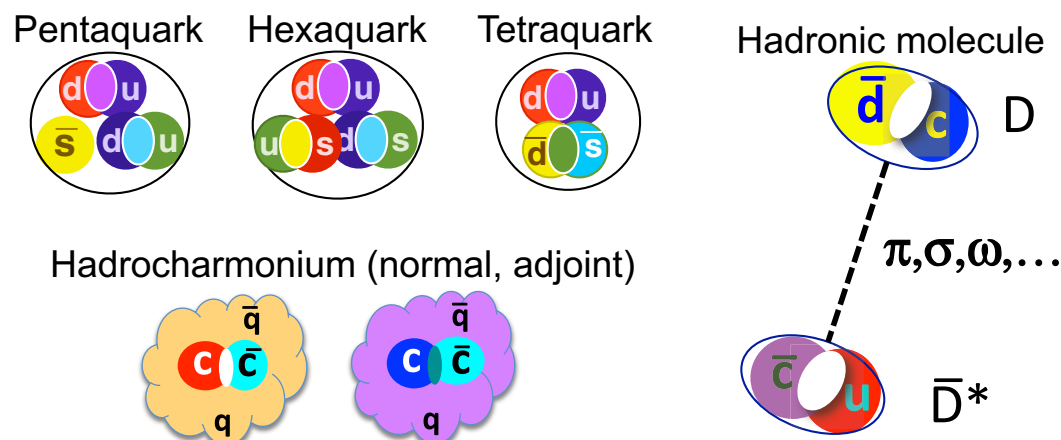
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# 1. Introduction

- Motivation to study exotic hadrons (multiquarks)
  - ✓ Color confinement (cf. Yang-Mills mass gap)
  - ✓ Flavor multiplets (unconventional assignment)
  - ✓ Multi-baryons (strange/charm/bottom nuclei)

## Exotic hadrons: Diversity of hadrons



Cf. S. L. Olsen, T. Skwamicki, D. Ziemninska, Rev. Mod. Phys. 90, 015003 (2018)

- We focus on heavy quarks!
    - ✓ Charm ( $c$ ) quark & bottom ( $b$ ) quark
    - ✓ Mass hierarchy ( $m_c, m_b \gg \Lambda_{\text{QCD}}$ )
    - ✓ Heavy quark spin symmetry
    - ✓ Many exotics have been found in experiments!
- $X, Y, Z, P_c, T_{cc}, \dots$

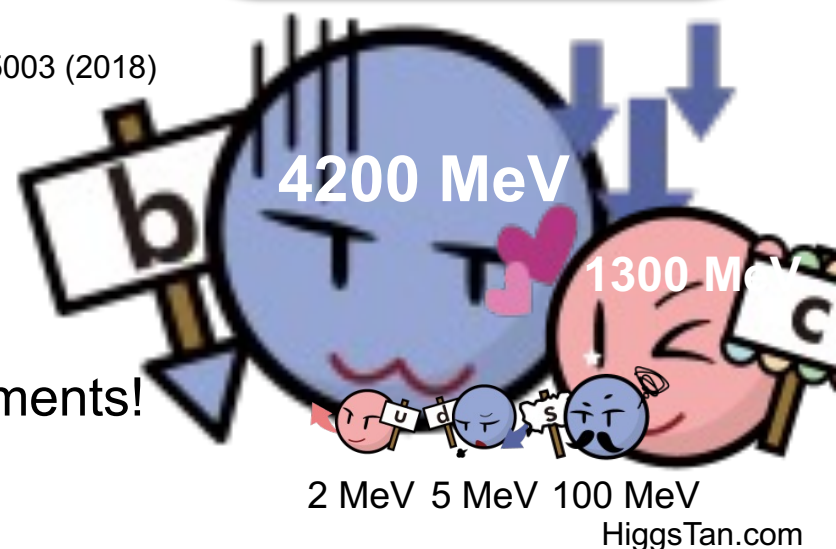


M. Gell-Mann  
"Quarks"

Phys. Lett.  
(1964)

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon  $b$  if we assign to the triplet  $t$  the following properties: spin  $\frac{1}{2}$ ,  $z = -\frac{1}{3}$ , and baryon number  $\frac{1}{3}$ .

$(qqqq\bar{q})$  and  $s^{-\frac{1}{3}}$  of the an now be mbinations  
 $(qqq), (qqq\bar{q}),$   
 of  $(q\bar{q}), (qq\bar{q}\bar{q}),$   
 baryon configura  
 tations 1, 8, and  
 the lowest meson  
 just 1 and 8.



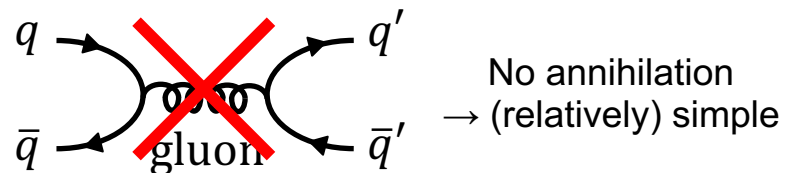
# 1. Introduction

-  $\bar{D}$  meson and nucleon (pentaquark)

✓  $\bar{c}qqqq$  ( $q = u, d$ ): no annihilation channel

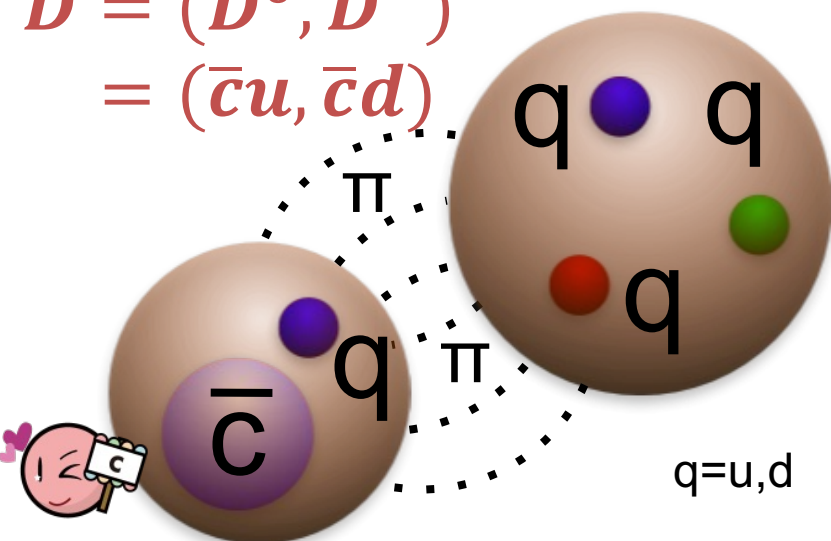
✓ (Anti-)charm nuclei? Cf. Review paper: Hosaka, Hyodo, Sudoh, Yamaguchi, Yasui, PPNP 96, 88 (2017)

✓ Extension to  $B$  meson and nucleon



$$\bar{D} = (\bar{D}^0, D^-)$$

$$= (\bar{c}u, \bar{c}d)$$



**$\bar{D}$  meson**  
(anti D meson)

**Nucleon**

*pentaquark (5 quark)*

chiral + HQS symmetries:

Cohen, Hohler, Lebed, PRD72, 074010 (2005)

Yasui, Sudoh, PRD80, 034008 (2009)

Yamaguchi, Ohkoda, Yasui, Hosaka, PRD84, 014032 (2011), ibid. 85, 054003 (2012)

etc.

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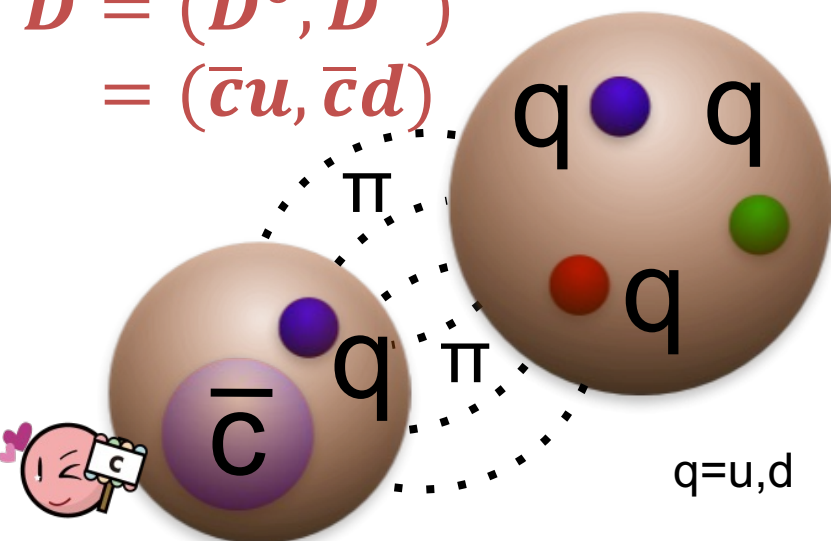
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→ (relatively) simple

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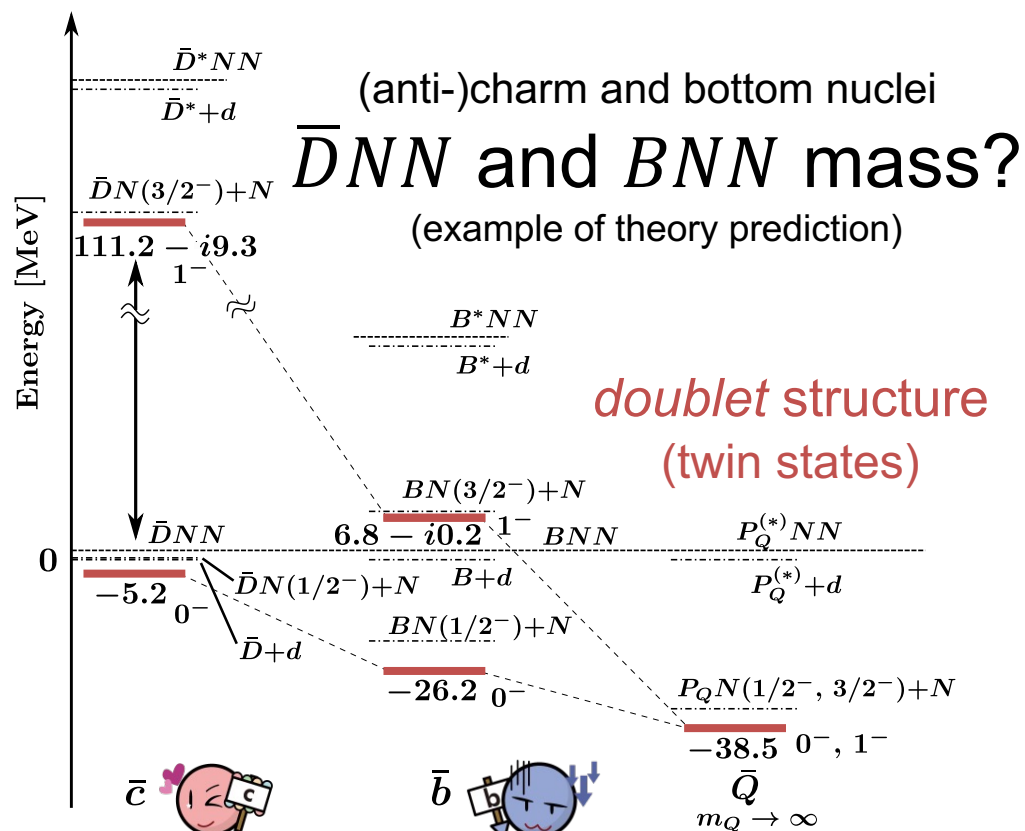
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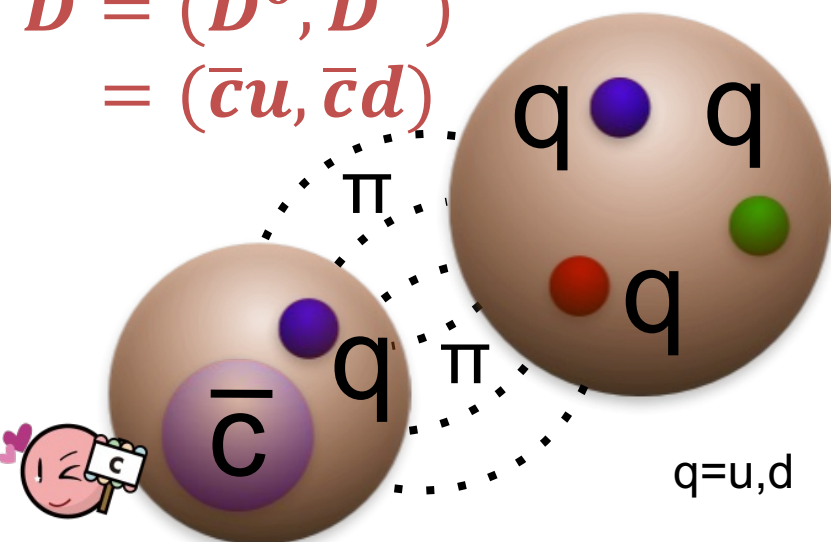
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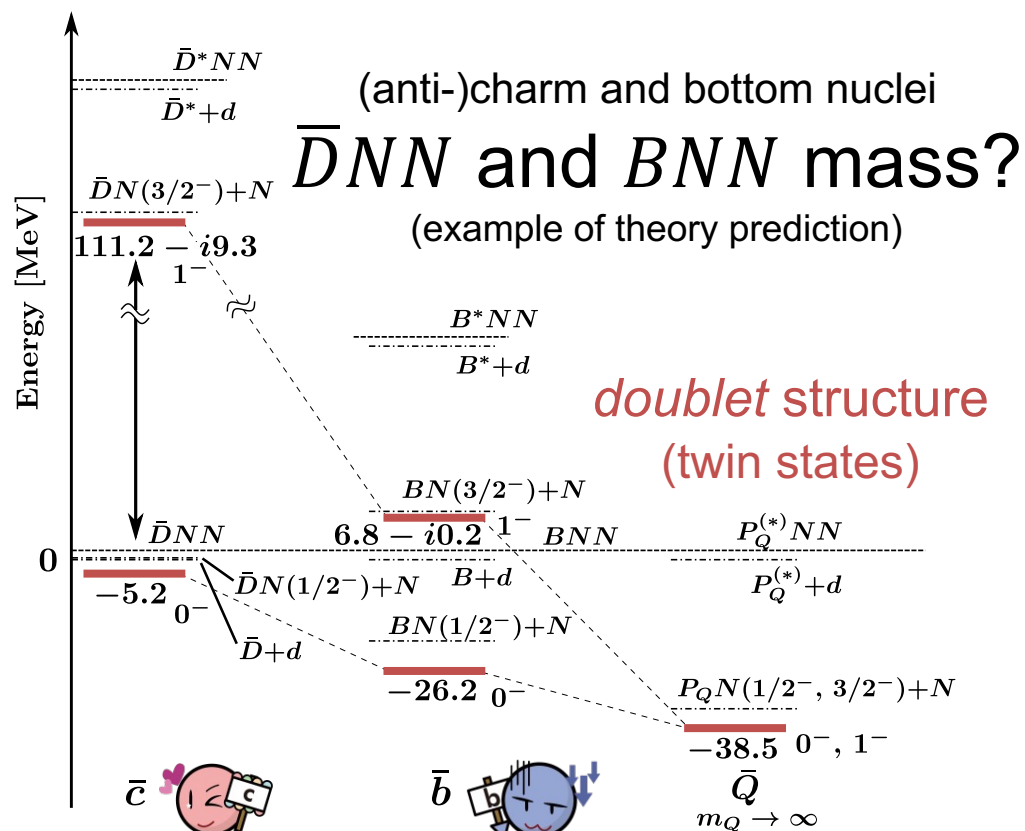
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Yamaguchi, Ohkoda, Yasui, Hosaka, PRD84, 014032 (2011), ibid. 85, 054003 (2012)

etc.



*Can (anti-)charm nuclei exist in our nature?*



# 1. Introduction

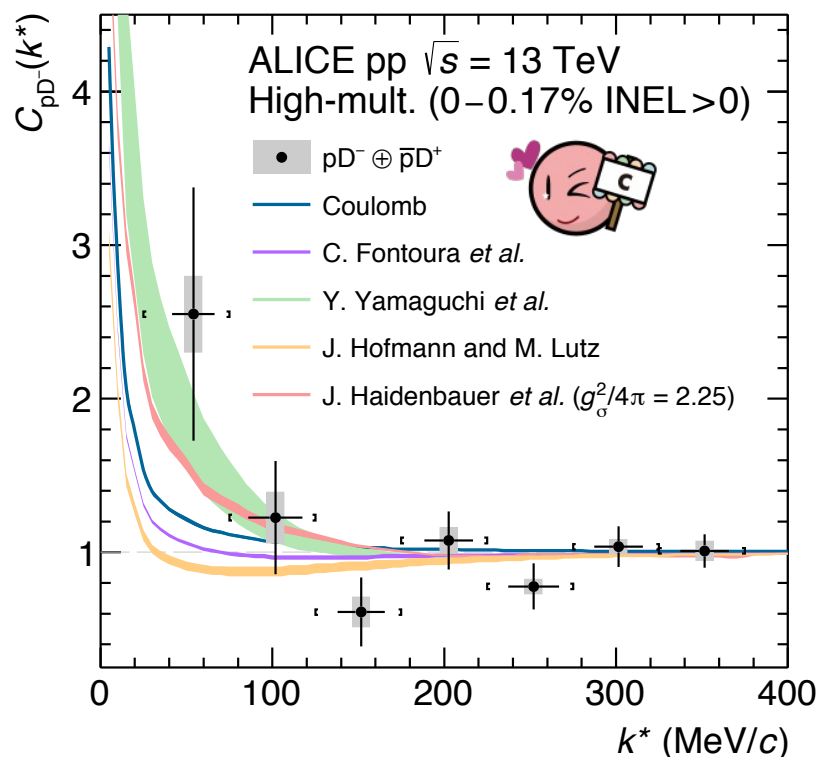
- 2022: First experiment for  $\bar{D}N$  interaction!

✓ ALICE at LHC Phys. Rev. D106, 052010 (2022) ← analysis by Kamiya, Hyodo, **Ohnishi**

✓  $D^-p$  ( $\bar{D}N$ ) correlation function from proton-proton collisions

✓ Attraction suggested? (Cf.  $KN$  is repulsive.)

Cf. Hyperon interaction:  
Ohnishi et al., Nucl.  
Phys. A954, 294 (2016)



	Model	$f_0$ (I = 0)	$f_0$ (I = 1)	$n_{\sigma}$
	Coulomb			(1.1–1.5)
attraction	Haidenbauer et al. [21]			
	– $g^2_{\sigma}/4\pi = 1$	0.14	–0.28	(1.2–1.5)
	– $g^2_{\sigma}/4\pi = 2.25$	0.67	0.04	(0.8–1.3)
repulsion	Hofmann and Lutz [22]	–0.16	–0.26	(1.3–1.6)
attraction (bound)	Yamaguchi et al. [24]	–4.38	–0.07	(0.6–1.1)
attraction	Fontoura et al. [23]	0.16	–0.25	(1.1–1.5)

[21] Haidenbauer, Krein, Meißner, Sibirtsev, EPJ. A33, 107 (2007)

[22] Hofmann, Lutz, NPA763, 90 (2005)

[24] Yamaguchi, Ohkoda, Yasui, Hosaka, PRD84, 014032 (2011)

[23] Fontoura, Krein, Vizcarra, PRC87, 025206 (2013)

We should explore  $\bar{D}$  meson and nucleon interaction  
**more seriously!**

# 1. Introduction

My few contributions since 2009...

PHYSICAL REVIEW D **80**, 034008 (2009)

## Exotic nuclei with open heavy flavor mesons

Shigehiro Yasui<sup>1,\*</sup> and Kazutaka Sudoh<sup>2,†</sup>

PHYSICAL REVIEW D **84**, 014032 (2011)

## Exotic baryons from a heavy meson and a nucleon: Negative parity states

Yasuhiro Yamaguchi,<sup>1</sup> Shunsuke Ohkoda,<sup>1</sup> Shigehiro Yasui,<sup>2</sup> and Atsushi Hosaka<sup>1</sup>

PHYSICAL REVIEW D **85**, 054003 (2012)

## Exotic baryons from a heavy meson and a nucleon: Positive parity states

Yasuhiro Yamaguchi,<sup>1</sup> Shunsuke Ohkoda,<sup>1</sup> Shigehiro Yasui,<sup>2</sup> and Atsushi Hosaka<sup>1</sup>

Physics Letters B 727 (2013) 185–189

Contents lists available at ScienceDirect

Physics Letters B

[www.elsevier.com/locate/physletb](http://www.elsevier.com/locate/physletb)



PHYSICAL REVIEW D **91**, 034034 (2015)

## Heavy quark symmetry in multihadron systems

Yasuhiro Yamaguchi,<sup>1</sup> Shunsuke Ohkoda,<sup>1</sup> Atsushi Hosaka,<sup>1,2</sup> Tetsuo Hyodo,<sup>3</sup> and Shigehiro Yasui<sup>4,5,\*</sup>

## Spin degeneracy in multi-hadron systems with a heavy quark

Shigehiro Yasui<sup>a,\*</sup>, Kazutaka Sudoh<sup>b</sup>, Yasuhiro Yamaguchi<sup>c</sup>, Shunsuke Ohkoda<sup>c</sup>,  
Atsushi Hosaka<sup>c</sup>, Tetsuo Hyodo<sup>d,1</sup>



Nuclear Physics A 927 (2014) 110–118

[www.elsevier.com/locate/nucphysa](http://www.elsevier.com/locate/nucphysa)



PTEP

Prog. Theor. Exp. Phys. **2017**, 093D02 (14 pages)

DOI: 10.1093/ptep/ptx112

## Mesic nuclei with a heavy antiquark

Yasuhiro Yamaguchi<sup>1,2,\*</sup> and Shigehiro Yasui<sup>3</sup>

## Exotic dibaryons with a heavy antiquark

Yasuhiro Yamaguchi<sup>a,\*</sup>, Shigehiro Yasui<sup>b</sup>, Atsushi Hosaka<sup>a,c</sup>

PHYSICAL REVIEW C **87**, 015202 (2013)

## $\bar{D}$ and $B$ mesons in a nuclear medium

S. Yasui<sup>\*</sup>

KEK Theory Center, Institute of Particle and Nuclear Studies, High Energy Accelerator Research Organization, 1-1 Oho,  
Ibaraki 305-0801, Japan

K. Sudoh

PHYSICAL REVIEW C **89**, 015201 (2014)

## Probing gluon dynamics by charm and bottom mesons in nuclear theory with $1/M$ corrections

S. Yasui<sup>1,\*</sup> and K. Sudoh<sup>2</sup>

Progress in Particle and Nuclear Physics 96 (2017) 88–153

Contents lists available at ScienceDirect

## Progress in Particle and Nuclear Physics

journal homepage: [www.elsevier.com/locate/ppnp](http://www.elsevier.com/locate/ppnp)



Review

## Heavy hadrons in nuclear matter

Atsushi Hosaka<sup>a,b</sup>, Tetsuo Hyodo<sup>c</sup>, Kazutaka Sudoh<sup>d</sup>, Yasuhiro Yamaguchi<sup>c,e</sup>,  
Shigehiro Yasui<sup>f,\*</sup>



# 1. Introduction

## $\bar{D}N$ ( $BN$ ) potential; the *latest* version

PHYSICAL REVIEW D **106**, 094001 (2022)

### Open charm and bottom meson-nucleon potentials *à la* the nuclear force

Yasuhiro Yamaguchi<sup>\*</sup>

*Department of Physics, Nagoya University, Nagoya 464-8602, Japan  
and Advanced Science Research Center, Japan Atomic Energy Agency (JAEA),  
Tokai 319-1195, Japan*

Shigehiro Yasui<sup>†</sup>

*Research and Education Center for Natural Sciences, Keio University,  
Hiyoshi 4-1-1, Yokohama, Kanagawa 223-8521, Japan*

Atsushi Hosaka<sup>‡</sup>

*Research Center for Nuclear Physics (RCNP), Ibaraki, Osaka 567-0047, Japan;  
Advanced Science Research Center, Japan Atomic Energy Agency, Tokai, Ibaraki 319-1195, Japan  
and Theoretical Research Division, Nishina Center, RIKEN, Hirosawa, Wako, Saitama 351-0198, Japan*

I talk on this.





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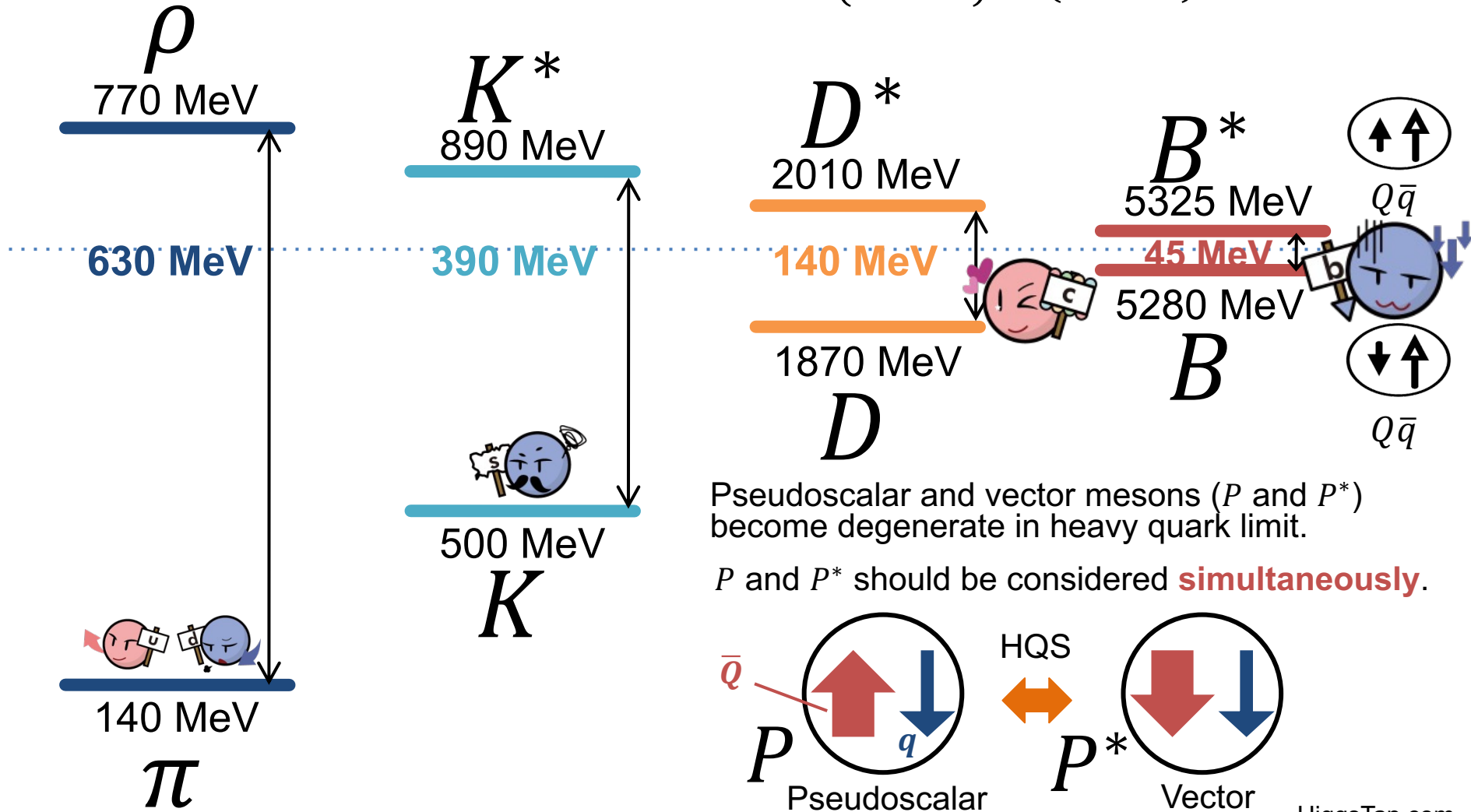
## 2. $\bar{D}$ meson and nucleon potential

- Structure of  $\bar{D}$  meson: Heavy quark spin symmetry (HQS)

✓ HQS:  $Q \rightarrow SQ$  with  $S \in \text{SU}(2)_{\text{heavy quark spin}}$

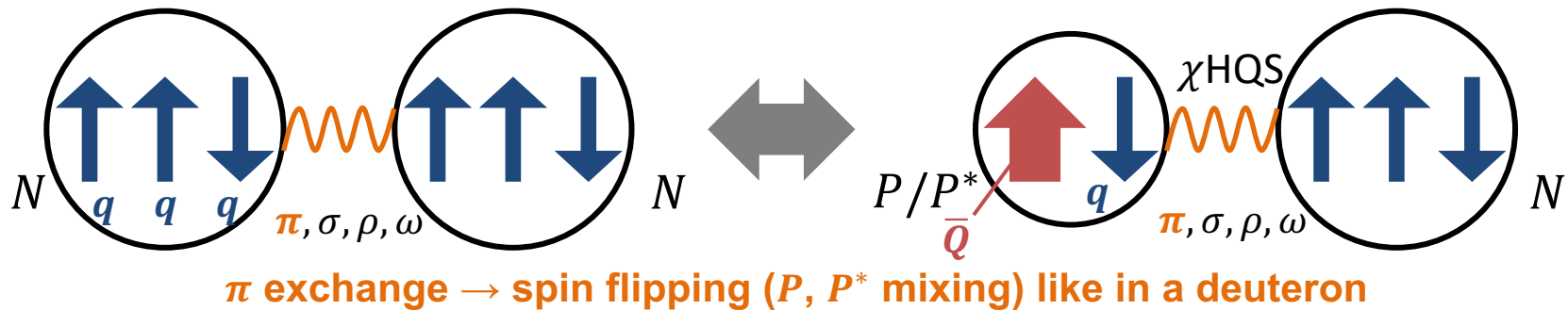
✓  $D$  and  $D^*$  mesons as HQS doublet  $\bar{D} = (\bar{D}^0, D^-) = (\bar{c}u, \bar{c}d) \quad \begin{matrix} u & c & t \end{matrix}$

✓  $B$  and  $B^*$  mesons also  $B = (B^+, B^0) = (\bar{b}u, \bar{b}d) \quad \begin{matrix} d & s & b \end{matrix}$



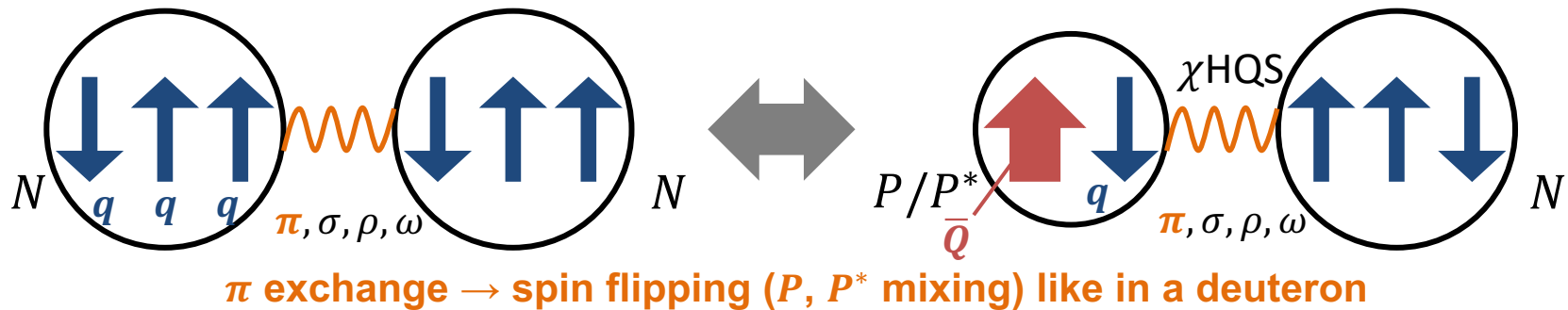
## 2. $\bar{D}$ meson and nucleon potential

- $\bar{D}$  meson and nucleon potential ( $P = \bar{D}$ ,  $P^* = \bar{D}^*$ )
  - ✓  $PN - P^*N$  mixing ( $P$  and  $P^*$  are interchangeable.)
  - ✓ **Chiral ( $\chi$ ) symmetry + Heavy-quark spin (HQS) symmetry**
  - ✓ OPEP (one-pion exchange potential)  $\leftarrow \chi + \text{HQS}$
  - ✓ Scalar ( $\sigma$ ), vector ( $\rho, \omega$ ) exchanges
  - ✓ Analogy to nucleon-nucleon ( $NN$ ) pot. (Note:  $1/\sqrt{2}$  factor for  $P^{(*)}P^{(*)}m$ )



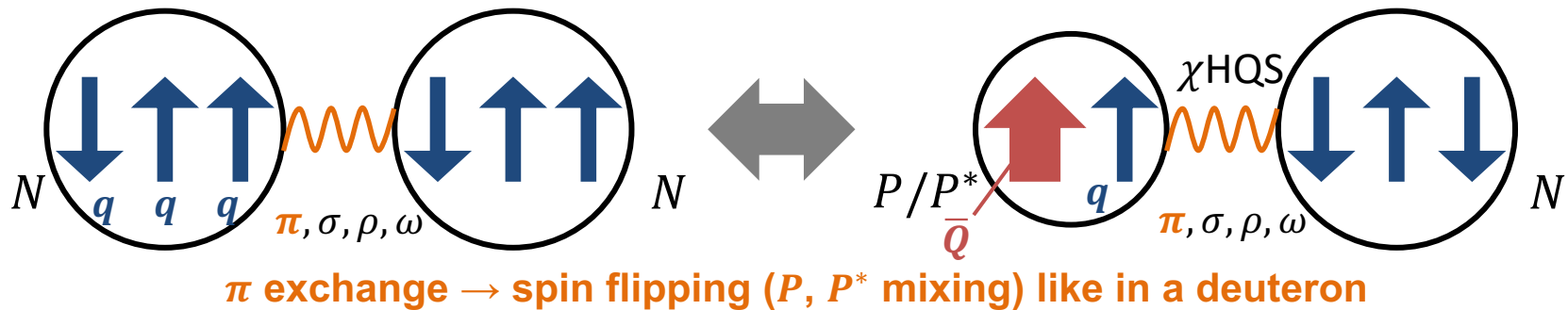
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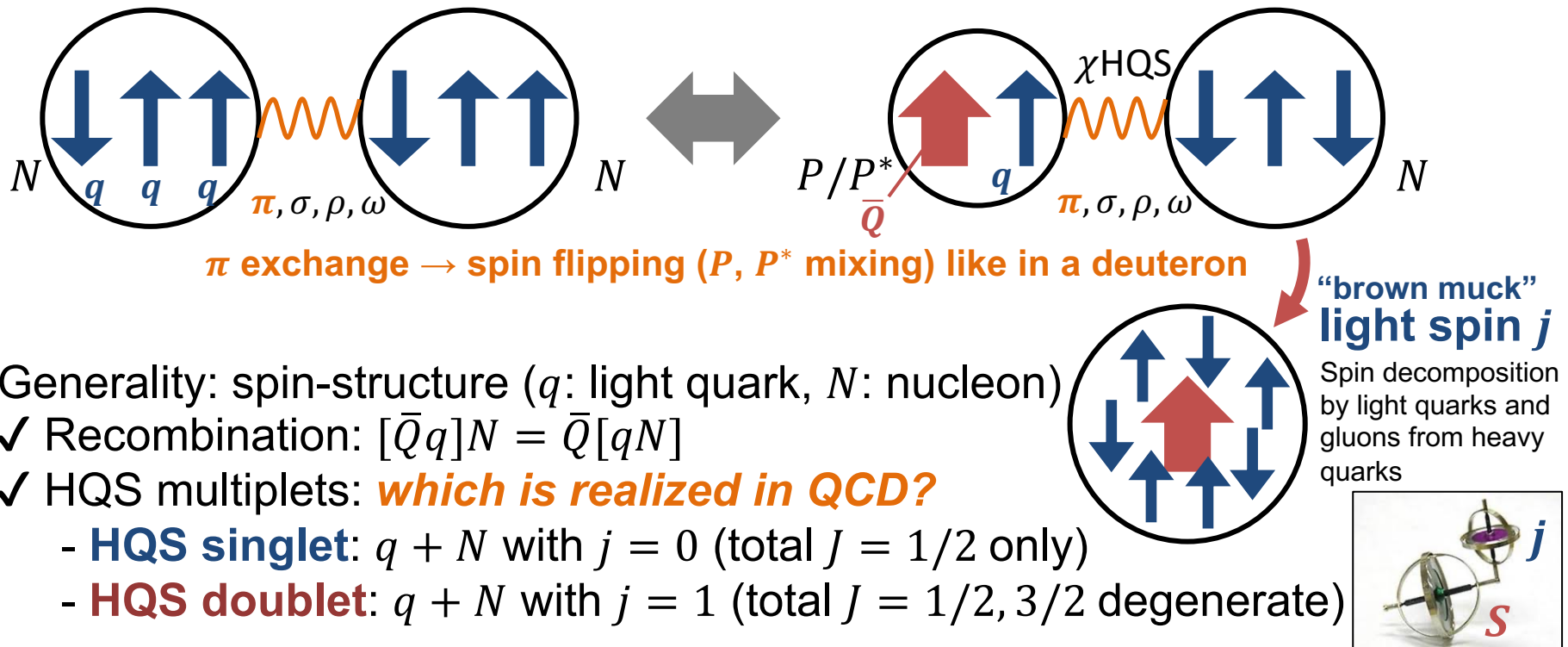
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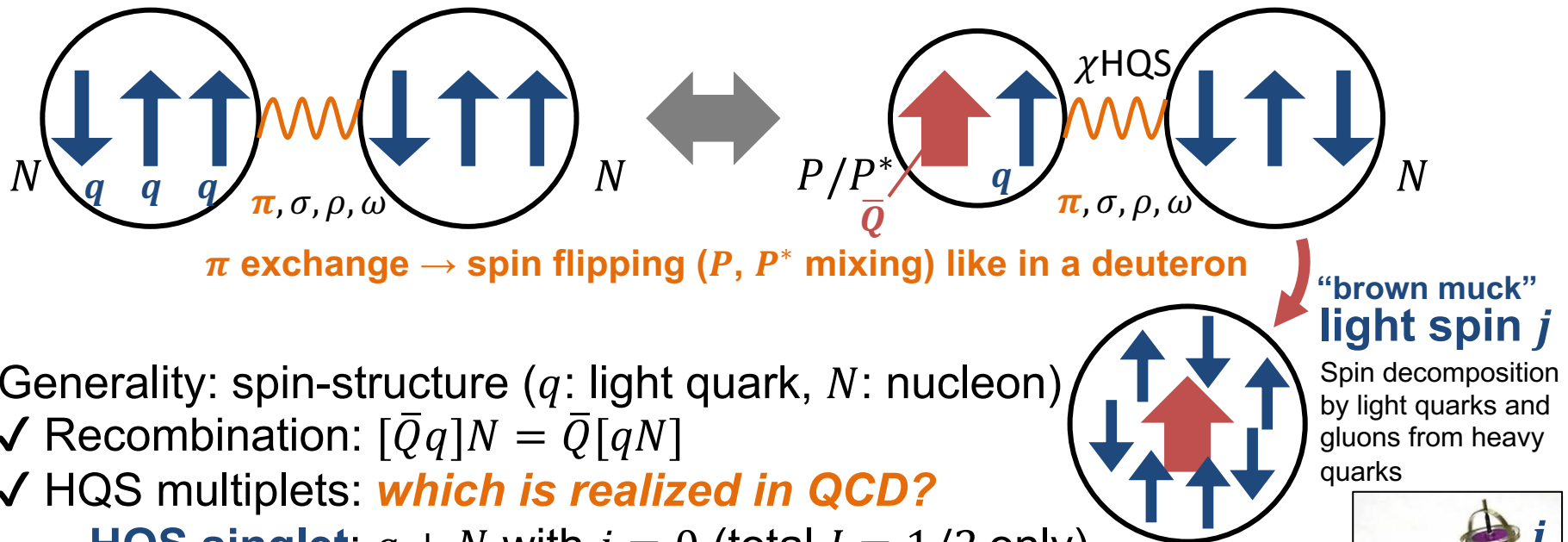
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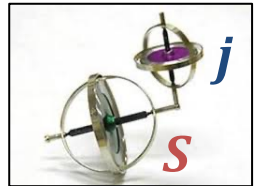


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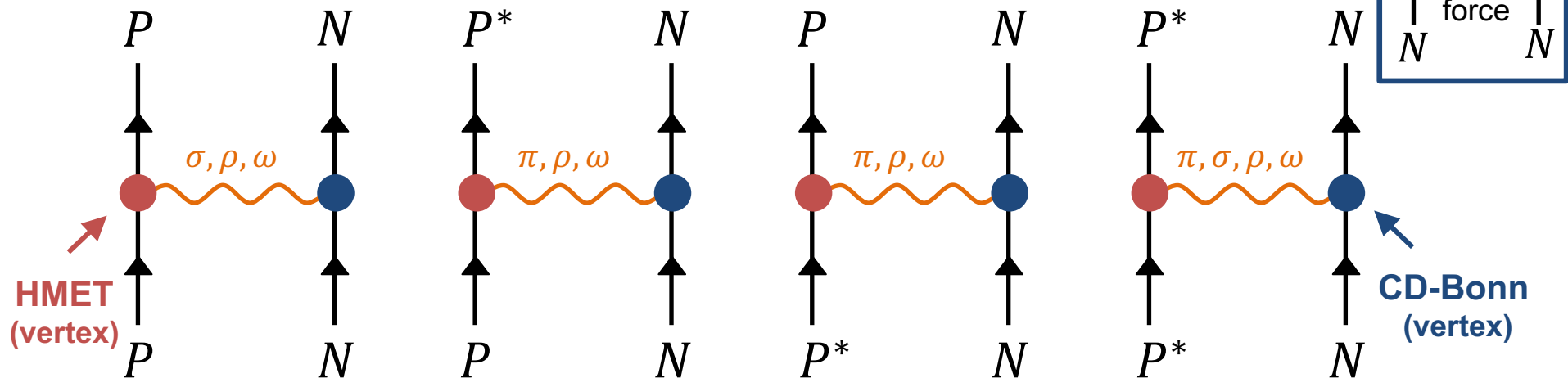
- Generality: spin-structure ( $q$ : light quark,  $N$ : nucleon)
  - ✓ Recombination:  $[\bar{Q}q]N = \bar{Q}[qN]$
  - ✓ HQS multiplets: **which is realized in QCD?**
    - **HQS singlet**:  $q + N$  with  $j = 0$  (total  $J = 1/2$  only)
    - **HQS doublet**:  $q + N$  with  $j = 1$  (total  $J = 1/2, 3/2$  degenerate)
- We need to solve QCD in order to get the potential, but it's difficult.
  - ✓ We still rely on model calculations.





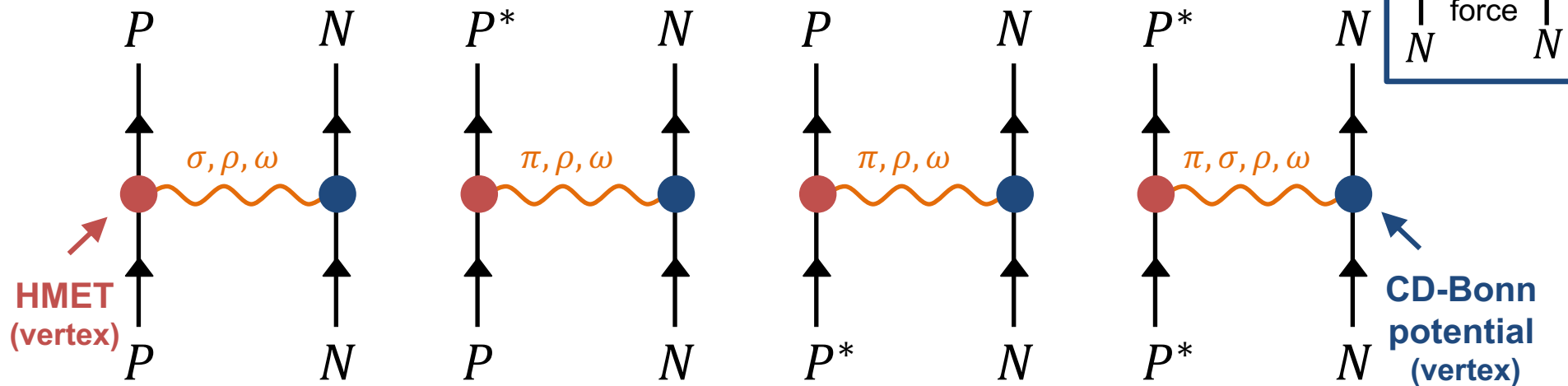
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- ✓  $PN - P^*N$  channel mixing (multi-channel)



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- **Heavy Meson Effective Theory (HMET)** Luke, Manohar, Wise, Casalbuoni, ...

✓ Hadronic effective theory based on  $\chi$ +HQS symmetries for  $P$  and  $P^*$

✓ Effective field:  $H_\alpha = (P_\alpha^{*\mu} \gamma_\mu + P_\alpha \gamma_5) \frac{1 - \not{v}}{2}$   $H_\alpha \xrightarrow[\text{HQS}]{\chi \text{ sym.}} S H_\beta U_{\beta\alpha}^\dagger$

✓  $P^{(*)}P^{(*)}m$  vertices are uniquely determined ( $m = \pi, \sigma, \rho, \omega$ )

$$\mathcal{L}_{\pi HH} = ig_\pi \text{tr}(H_\alpha \bar{H}_\beta \gamma_\mu \gamma_5 A_{\beta\alpha}^\mu)$$

$$\mathcal{L}_{\sigma_I HH} = g_{\sigma_I} \text{tr}(H \sigma_I \bar{H})$$

$$\begin{aligned} \mathcal{L}_{v HH} = & -i\beta \text{tr}(H_b v^\mu (\rho_\mu)_{ba} \bar{H}_a) \\ & + i\lambda \text{tr}(H_b \sigma^{\mu\nu} (F_{\mu\nu}(\rho))_{ba} \bar{H}_a) \end{aligned}$$

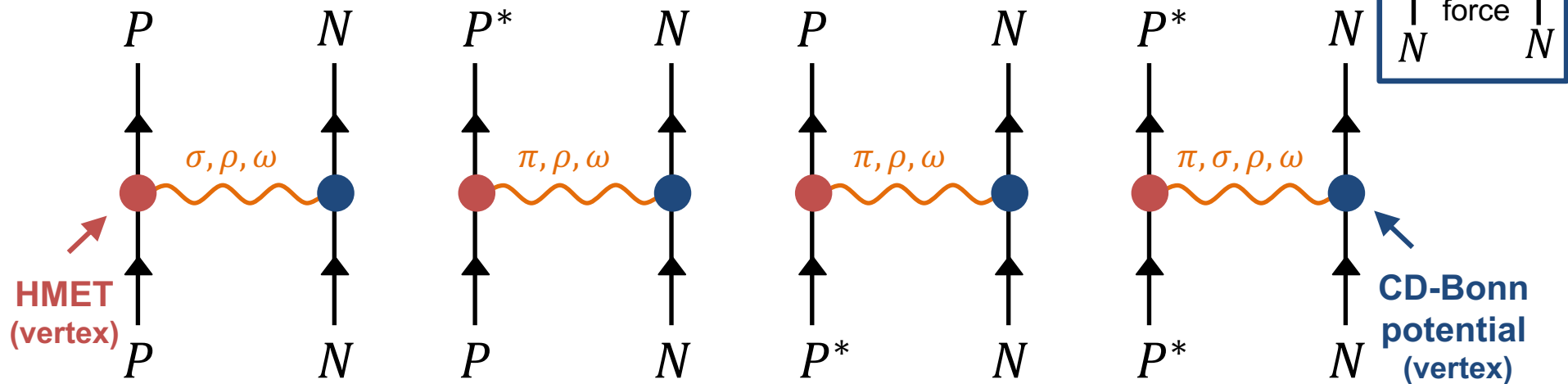
Previous works:

$\pi$  only: Yasui, Sudoh, PRD80, 034008 (2009)

$\pi, \rho, \omega$ : Yamaguchi, Ohkoda, Yasui, Hosaka, PRD84 014032 (2011),  
ibid. 054003 (2012)

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$$\mathcal{L}_{\pi HH} = ig_\pi \text{tr}(H_\alpha \bar{H}_\beta \gamma_\mu \gamma_5 A_{\beta\alpha}^\mu)$$

$$\mathcal{L}_{\sigma_I HH} = g_{\sigma_I} \text{tr}(H \sigma_I \bar{H}) \leftarrow \sigma \text{ is new!}$$

$$\begin{aligned} \mathcal{L}_{v HH} = & -i\beta \text{tr}(H_b v^\mu (\rho_\mu)_{ba} \bar{H}_a) \\ & + i\lambda \text{tr}(H_b \sigma^{\mu\nu} (F_{\mu\nu}(\rho))_{ba} \bar{H}_a) \end{aligned}$$

**$\sigma$  is important for  $NN$  ( $I = 0, 1$  channels):**  
 **$\sigma_0$  (weak coupling) for  $NN$  with  $I = 0$**   
 **$\sigma_1$  (strong coupling) for  $NN$  with  $I = 1$**

Previous works:

$\pi$  only: Yasui, Sudoh, PRD80, 034008 (2009)

$\pi, \rho, \omega$ : Yamaguchi, Ohkoda, Yasui, Hosaka, PRD84 014032 (2011),  
 ibid. 054003 (2012)

## 2. $\bar{D}$ meson and nucleon potential

-  $P^{(*)}N$  state ( $J^P = 1/2^-, I = 0$  or  $1$ ) Note: applicable to  $J^P = 3/2^-$  (HQS partner)

✓ Particle basis:  $PN(^2S_{1/2}), P^*N(^2S_{1/2}), P^*N(^4D_{1/2}) \leftarrow 3 \text{ channels}$

✓ HQS basis:  $\bar{Q}_{S=1/2}[qN]_{j=0,1}$  Cf. Yasui, Sudoh, Yamaguchi, Ohkoda, Hosaka, Hyodo, PLB727, 185 (2013); PRD91, 034034 (2015)

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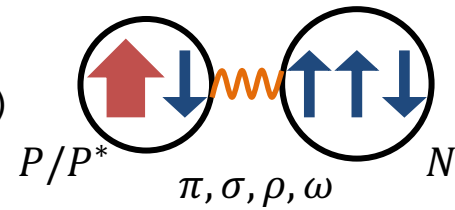
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-  $P^{(*)}N(1/2^-)$  Hamiltonian  $H_{JP} = K_{JP} + V_{JP}^\pi + V_{JP}^{\sigma_I} + V_{JP}^\rho + V_{JP}^\omega$

✓ Kinetic term  $K_{1/2^-} = \text{diag}(K_0, K_0^*, K_2^*)$  (S-wave, S-wave, D-wave)

✓  $\pi, \sigma, \nu(= \rho, \omega)$  pot. term ( $1/\sqrt{2}$  factor included)



$$V_{1/2^-}^\pi = \begin{pmatrix} 0 & \sqrt{3}C_\pi & -\sqrt{6}T_\pi \\ \sqrt{3}C_\pi & -2C_\pi & -\sqrt{2}T_\pi \\ -\sqrt{6}T_\pi & -\sqrt{2}T_\pi & C_\pi - 2T_\pi \end{pmatrix} \quad V_{1/2^-}^{\sigma_I} = \begin{pmatrix} C_{\sigma_I} & 0 & 0 \\ 0 & C_{\sigma_I} & 0 \\ 0 & 0 & C_{\sigma_I} \end{pmatrix}$$

$$V_{1/2^-}^\nu = \begin{pmatrix} C'_v & 2\sqrt{3}C_v & \sqrt{6}T_v \\ 2\sqrt{3}C_v & C'_v - 4C_v & \sqrt{2}T_v \\ \sqrt{6}T_v & \sqrt{2}T_v & C'_v + 2C_v + 2T_v \end{pmatrix} \quad \text{including HQS singlet/doublet}$$

✓ **Tensor force** ( $T_\pi, T_v$ ) induces strong mixing among 3 channels

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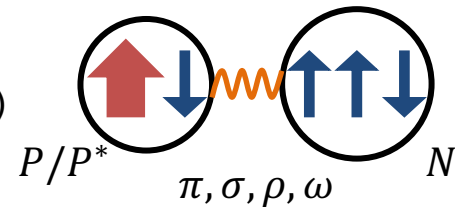
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✓ **Tensor force** ( $T_\pi, T_v$ ) induces strong mixing among 3 channels

✓ Model parameters

-  $\pi$  pot. coupling ( $D^* \rightarrow D\pi$ )

-  $\nu = \rho, \omega$  pot. couplings (universal couplings)

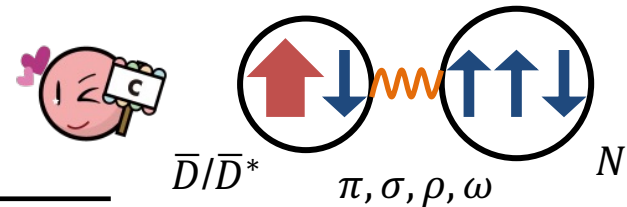
-  $\sigma$  pot. coupling  $\sim 1/3$  of  $NN$  (# of light quarks in  $P^{(*)}$  meson)

- Momentum cutoffs (size ratios of  $\bar{D}$  ( $B$ ) and  $N$  from quark model)

## 2. $\bar{D}$ meson and nucleon potential

- Results ( $\bar{D}$  and  $N$ )

✓ bound states ( $I = 0, 1$ )



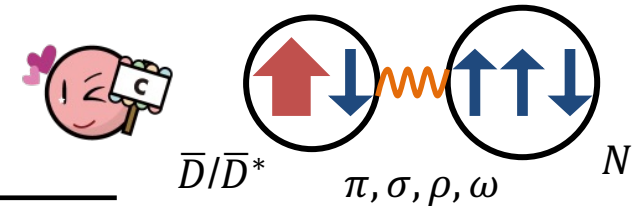
$\bar{D}N$	B.E. [MeV]	Mixing ratio [%]	
$I(J^P) = 0(1/2^-)$	1.38	$\bar{D}N(^2S_{1/2})$	96.1
		$\bar{D}^*N(^2S_{1/2})$	1.94
		<b>“shallow”</b> $\bar{D}^*N(^4D_{1/2})$	1.93
$I(J^P) = 1(1/2^-)$	5.99	$\bar{D}N(^2S_{1/2})$ :	88.9
		$\bar{D}^*N(^2S_{1/2})$ :	10.9
		<b>“deep”</b> $\bar{D}^*N(^4D_{1/2})$ :	0.11

Cf. Deuteron binding energy 2.2 MeV

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$\bar{D}N$	B.E. [MeV]	Mixing ratio [%]	
$I(J^P) = 0(1/2^-)$ “ $j = 1$ ”	1.38 “shallow”	$\bar{D}N(^2S_{1/2})$ 96.1	Cf. Deuteron binding energy 2.2 MeV
		$\bar{D}^*N(^2S_{1/2})$ 1.94	
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$I(J^P) = 1(1/2^-)$ “ $j = 0$ ”	5.99 “deep”	$\bar{D}N(^2S_{1/2})$ : 88.9	
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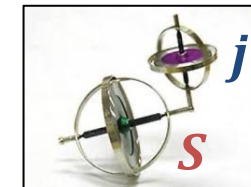
-  $I = 0$ : shallow bound state (consistent with previous works)

-  $I = 1$ : deeply bound state (new!)

- Both  $\pi$  and  $\sigma$  are important

- Note:  $\sigma$  pot. in  $I = 1$  is very strong

- Internal spin: “ $j = 1$ ” for  $I = 0$  and “ $j = 0$ ” for  $I = 1$  (approximate)



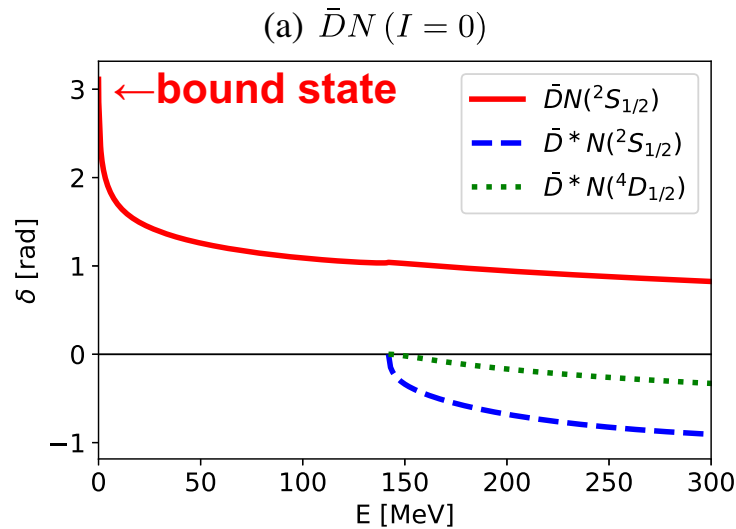
“brown muck”  
(light component)

heavy quark

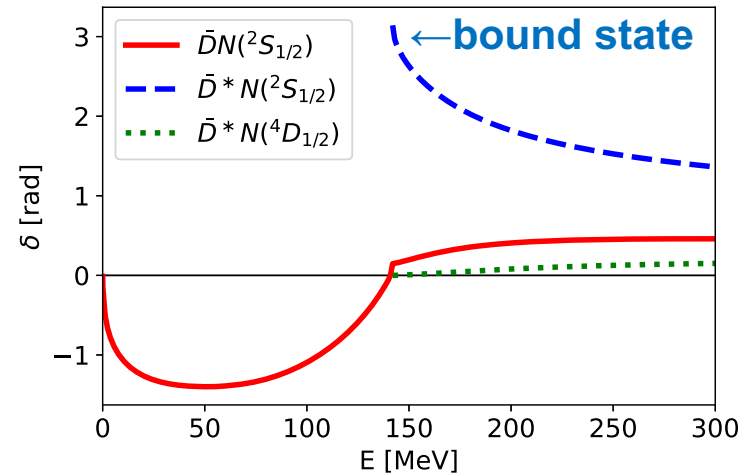


## 2. $\bar{D}$ meson and nucleon potential

### ✓ Phase shifts



(b)  $\bar{D}N$  ( $I = 1$ )  $\bar{D}/\bar{D}^*$   $\pi, \sigma, \rho, \omega$   $N$



### ✓ Scattering lengths

$\bar{D}N$	$a$ [fm]
$0(1/2^-)$	$\bar{D}N(^2S_{1/2})$ 5.21
	$\bar{D}^*N(^2S_{1/2})$ $0.868 - i3.72 \times 10^{-2}$
$1(1/2^-)$	$\bar{D}N(^2S_{1/2})$ 2.60
	$\bar{D}^*N(^2S_{1/2})$ $0.944 - i0.722$

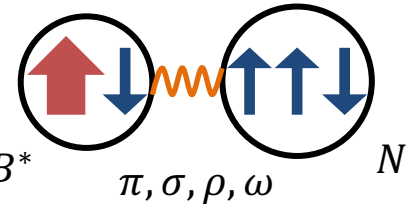


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### 3. $B$ meson and nucleon potential

- Applicable for  $B$  meson and nucleon (more ideal in view of HQS)
- Results ( $B$  and  $N$ )
  - ✓ Bound states ( $I=0, 1$ )

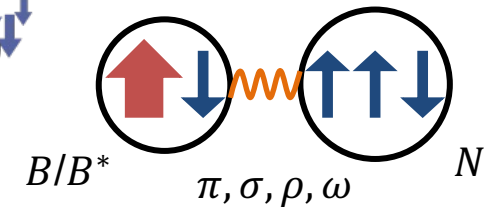


$BN$	B.E. [MeV]	Mixing ratio [%]	
$I(J^P) = 0(1/2^-)$	29.7 "deep"	$BN(^2S_{1/2})$	76.4
		$B^*N(^2S_{1/2})$	14.1
		$B^*N(^4D_{1/2})$	9.46
$I(J^P) = 1(1/2^-)$	66.0 "very deep"	$BN(^2S_{1/2})$	38.5
		$B^*N(^2S_{1/2})$	61.5
		$B^*N(^4D_{1/2})$	$1.82 \times 10^{-2}$

Cf. Deuteron binding energy 2.2 MeV

### 3. $B$ meson and nucleon potential

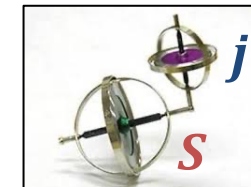
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- $I = 0$ : deeply bound state (consistent with previous works)
- $I = 1$ : more deeply bound state (new!)
- Both  $\pi$  and  $\sigma$  are important
- Note:  $\sigma$  pot. in  $I = 1$  is very strongly attractive
- Internal spin: “j = 1” for  $I = 0$  and “j = 0” for  $I = 1$  (approximate)

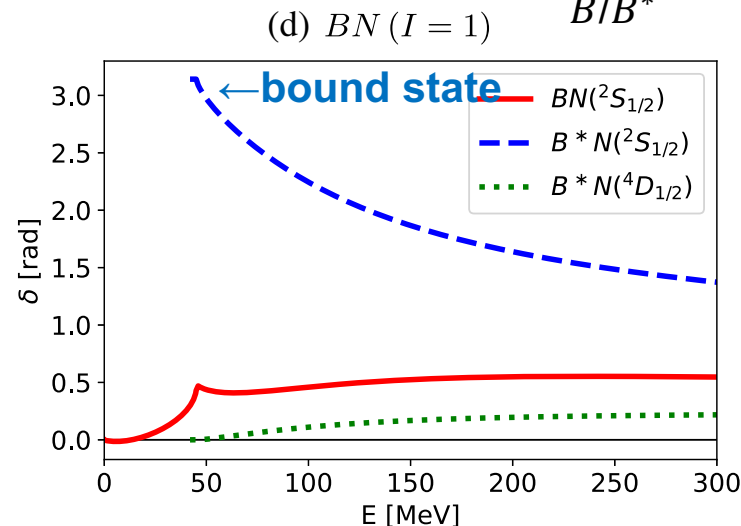
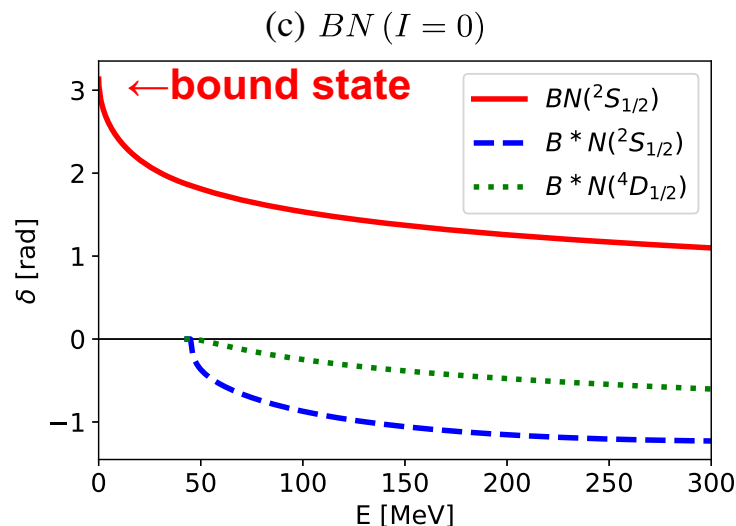
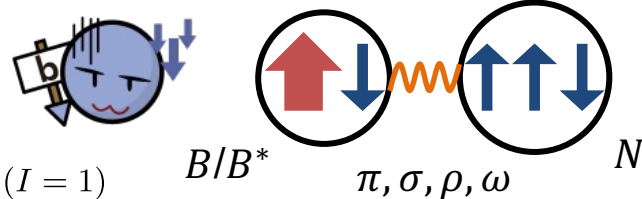


**“brown muck”**  
(light component)

**heavy quark**

### 3. $B$ meson and nucleon potential

#### ✓ Phase shifts



#### ✓ Scattering lengths

$BN$	$a$ [fm]
$0(1/2^-)$	$BN(^2S_{1/2})$ 1.25
	$B^*N(^2S_{1/2})$ $1.03 - i1.07 \times 10^{-2}$
$1(1/2^-)$	$BN(^2S_{1/2})$ $3.84 \times 10^{-2}$
	$B^*N(^2S_{1/2})$ $0.263 - i0.585$

#### ✓ Why not to research $BN$ correlation function from heavy-ion collisions?

- Very few theoretical works on  $BN$  interaction
- Should we explore  $B^0p$  ( $I = 0$  and  $1$ ) channel?





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# 4. Discussions

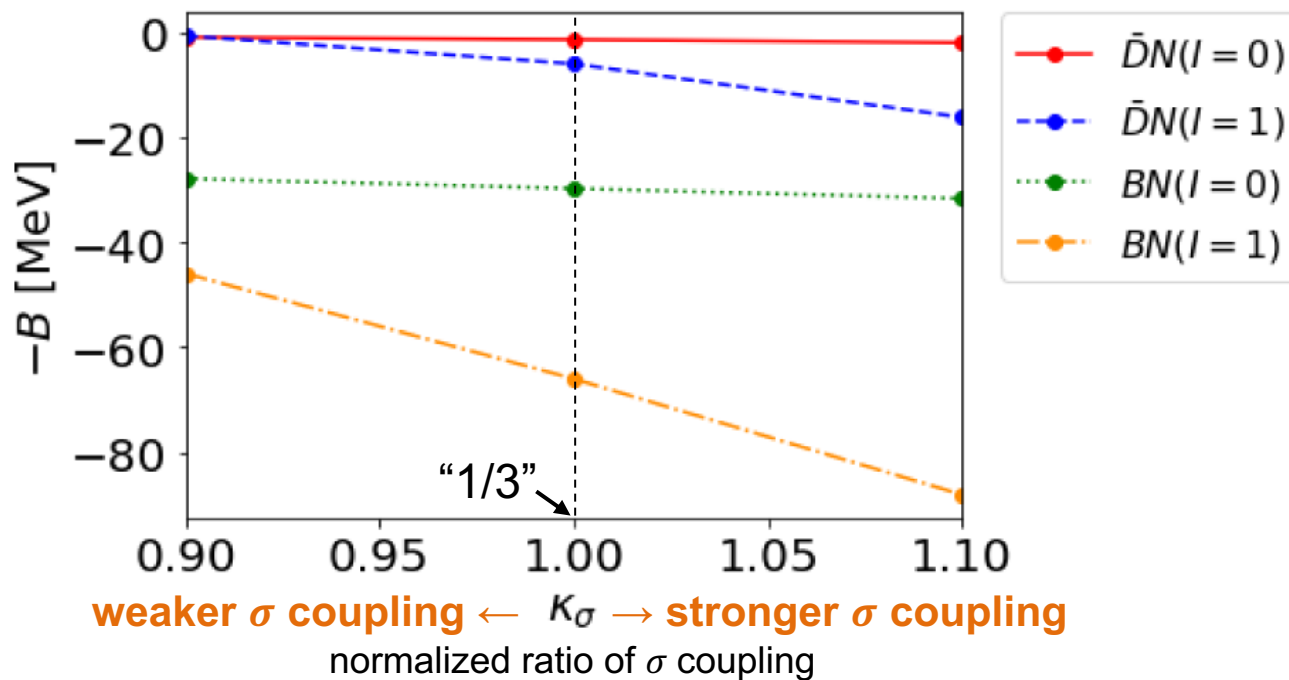
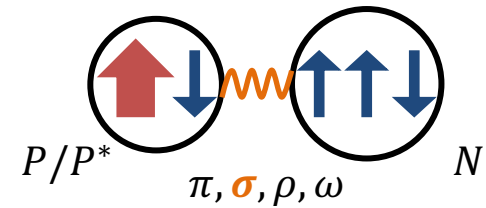
## - Model dependence

### ✓ Ambiguity in $\sigma$ potentials

- We assumed  $P^{(*)}P^{(*)}\sigma$  strength coupling is “1/3” of that in  $NN\sigma$

### ✓ Estimate the uncertainty from $\sigma$ couplings

- Dependence in binding energies



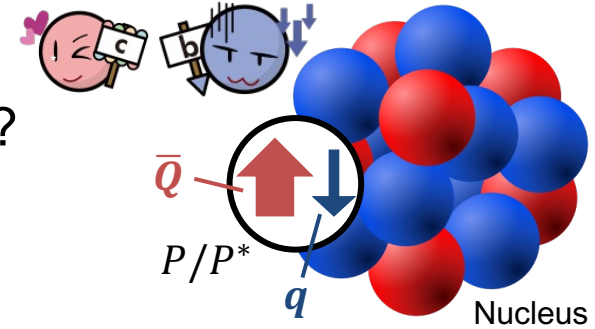
- Similar results for scattering lengths for  $PN$  and  $P^*N$

### ✓ $I = 0$ is *less* dependent, but $I = 1$ is *more* dependent

- $\sigma$  is **less** important in  $I = 0$ , but **more** important in  $I = 1$

# 4. Discussions

## Flavor nuclei: Diversity of matter



### - Charm (bottom) nuclei?

✓ Can charm (bottom) nuclei exist as stable states?

✓ What about  $\bar{D}$  mesons in nuclear medium?

- Stability: binding energy?

TABLE I. List of the mass shifts of the  $\bar{D}$  meson in nuclear medium in previous works: quark meson coupling (QMC) model, QCD sum rule, coupled channel analysis, and chiral effective model.

Analysis	Ref.	Mass shift of $\bar{D}$ (MeV)	Density $\rho$ (fm $^{-3}$ )
QMC model (QMC: quark-meson coupling) [18]		-62 <b>attractive</b>	0.15
QCD sum rule	[19]	$-48 \pm 8$ <b>attractive</b>	0.17
	[23]	+45 (averaged mass shift of $D$ and $\bar{D}$ ) <b>repulsive</b>	0.15
	[28]	$-46 \pm 7$ (averaged mass shift of $D$ and $\bar{D}$ ) <b>attractive</b>	0.17
	[30]	$-72$ (averaged mass shift of $D$ and $\bar{D}$ ) <b>attractive</b>	0.17
	[31]	+38 <b>repulsive</b>	0.17
Coupled channel analysis	[21]	+18 <b>repulsive</b>	0.17
	[22]	+(11-20) <b>repulsive</b>	0.16
	[26]	+35 <b>repulsive</b>	0.17
	[15]	$\simeq -(20-27)$ <b>attractive</b>	0.17
Chiral effective model	[20]	$\simeq -(30-180)$ <b>attractive</b>	0.15
	[25]	-27.2 <b>attractive</b>	0.15
	[16]	-35.1 <b>attractive</b>	0.17
	[37]	+97 (parity doublet model), +120 (skyrmion crystal) <b>repulsive</b>	0.16
Our result*		+74 <b>repulsive</b>	0.095

\*D. Suenaga, S. Yasui., M. Harada, Phys. Rev. C96, 015204 (2017) [See this paper for the reference numbers.]

**Possible open question: can we study (*anti*-)charm nuclei through  $\bar{D}N$  interaction?**



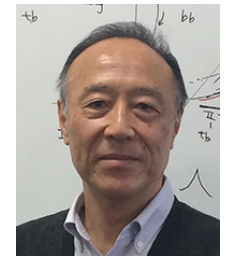
## 5. Summary

Y. Yamaguchi, S. Y., A. Hosaka, Phys. Rev. D106, 094001 (2022)

- $\bar{D}$  ( $B$ ) meson and nucleon potential is important for exotic hadrons and nuclei.
- We considered  $\pi, \sigma, \rho, \omega$  exchanges based on chiral and HQS symmetries
- Bound states of  $\bar{D}$  meson and nucleon with  $I(J^P) = 0(1/2^-), 1(1/2^-)$
- Deeply bound states of  $B$  meson and nucleon with same  $I(J^P)$
- Future studies: theories and experiments (LHC, Belle, J-PARC, etc.)
  - ✓ Heavy ion collisions (LHC) ExHIC: PRL106 212001 (2011); PRC84, 064910 (2011), PPNP95, 279 (2017)
  - ✓ Fixed target experiments (J-PARC) Yamagata-Sekihara, Garcia-Recio, Nieves, Salcedo, Tolos, PLB754, 26 (2016)
  - ✓ More states in the other  $I(J^P)$ ?
  - ✓ More states in bottom?
  - ✓ Lattice QCD?
  - ✓  $D_s^- N$ ?  $\bar{D} \Lambda$ ? (from  $u, d$  to  $u, d, s$ )
  - ✓ Multi-baryons :  $P^{(*)} NN, P^{(*)} \alpha$ ?? Yamaguchi, Yasui, Hosaka, NPA927, 110 (2014)
  - ✓ (Anti-)charm, bottom nuclei???



Y. Yamaguchi  
Nagoya U.



A. Hosaka  
RCNP, Osaka U.

*Can (anti-)charm nuclei exist in our nature?*

Thanks!

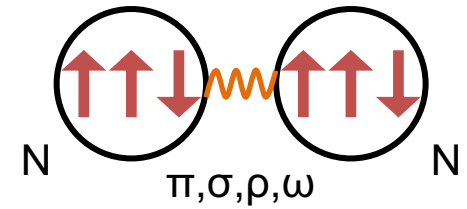


# Appendix



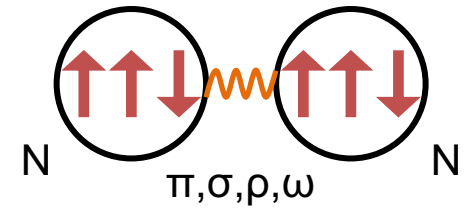
# A. Nucleon-nucleon pot. (modified CD-Bonn)

- Reference system: nucleon-nucleon (NN)
  - ✓ Similarity between NN and qN
  - ✓  $\pi$ ,  $\sigma$ ,  $\rho$ ,  $\omega$  exchange
  - ✓  $\sigma$  is important to consider both  $I=0$  and  $I=1$  in NN



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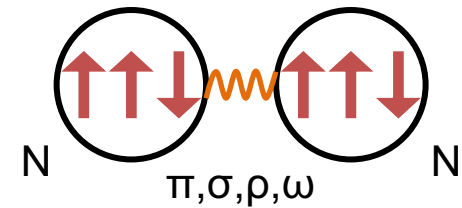
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- **CD-Bonn** is a realistic NN potential
  - ✓ Reproducing the fundamental properties of NN force
  - ✓ Simple model: one-meson exchange ( $\pi$ ,  $\sigma$ ,  $\rho$ ,  $\omega$ , ...)
  - ✓ However still complicated (because heavier mesons included)



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- ✓ However still complicated (because heavier mesons included)

## - We consider the simpler version of CD-Bonn ("**modified CD-Bonn**")

- ✓ We consider only mesons with lower masses
- ✓ Coupling constants as the same as in CD-Bonn
- ✓ Price to be paid: rescaling of the momentum cutoffs

Masses and coupling constants of exchanged mesons (same as CD-Bonn)

Mesons	Masses [MeV]	$g^2/4\pi$	$f/g$
$\pi$	138.04	13.6	—
$\rho$	769.68	0.84	6.1
$\omega$	781.94	20	0.0
$\sigma_0$	350	0.51673	—
$\sigma_1$	452	3.96451	—

Scattering lengths, effective ranges, binding energy of a deuteron in modified CD-Bonn

channel	$\kappa_I$ ( $I = 0$ and $I = 1$ )	$a$ [fm]	$r_e$ [fm]	$B_d$ [MeV]
$^3S_1$ ( $I = 0$ )	0.8044226	5.296	1.562	2.225*
$^1S_0$ ( $I = 1$ )	0.7729982	23.740*	2.337	—

Reduction scale factor  
in momentum cutoffs

Consistent with experiment values

$a(^3S_1)=5.419\pm0.007$  fm,  $r_e(^3S_1)=1.753\pm0.008$  fm,  $B_d=2.225$  MeV

$a(^1S_0)=23.740\pm0.020$  fm,  $r_e(^1S_0)=2.77\pm0.05$  fm

# A. Nucleon-nucleon pot. (modified CD-Bonn)

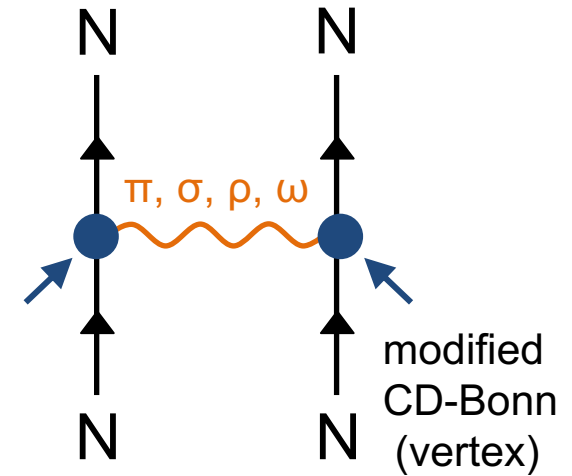
## - Interaction Lagrangian

$$\mathcal{L}_{\pi NN} = -g_{\pi} \bar{\psi} i \gamma_5 \boldsymbol{\tau} \cdot \boldsymbol{\pi} \psi,$$

$$\mathcal{L}_{\sigma_I NN} = -g_{\sigma_I} \bar{\psi} \sigma_I \psi,$$

$$\mathcal{L}_{\rho NN} = -g_{\rho} \bar{\psi} \gamma_{\mu} \boldsymbol{\tau} \cdot \boldsymbol{\rho}^{\mu} \psi - \frac{f_{\rho}}{4m_N} \bar{\psi} \sigma_{\mu\nu} \boldsymbol{\tau} \cdot (\partial^{\mu} \boldsymbol{\rho}^{\nu} - \partial^{\nu} \boldsymbol{\rho}^{\mu}) \psi,$$

$$\mathcal{L}_{\omega NN} = -g_{\omega} \bar{\psi} \gamma_{\mu} \omega^{\mu} \psi,$$



# A. Nucleon-nucleon pot. (modified CD-Bonn)

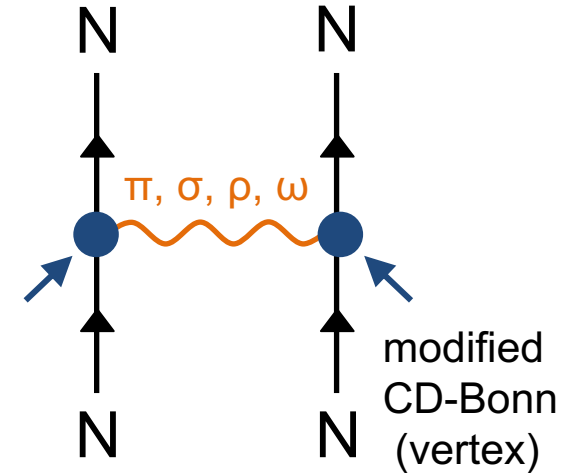
## - Interaction Lagrangian

$$\mathcal{L}_{\pi NN} = -g_{\pi} \bar{\psi} i \gamma_5 \boldsymbol{\tau} \cdot \boldsymbol{\pi} \psi,$$

$$\mathcal{L}_{\sigma_I NN} = -g_{\sigma_I} \bar{\psi} \sigma_I \psi,$$

$$\mathcal{L}_{\rho NN} = -g_{\rho} \bar{\psi} \gamma_{\mu} \boldsymbol{\tau} \cdot \boldsymbol{\rho}^{\mu} \psi - \frac{f_{\rho}}{4m_N} \bar{\psi} \sigma_{\mu\nu} \boldsymbol{\tau} \cdot (\partial^{\mu} \boldsymbol{\rho}^{\nu} - \partial^{\nu} \boldsymbol{\rho}^{\mu}) \psi,$$

$$\mathcal{L}_{\omega NN} = -g_{\omega} \bar{\psi} \gamma_{\mu} \omega^{\mu} \psi,$$



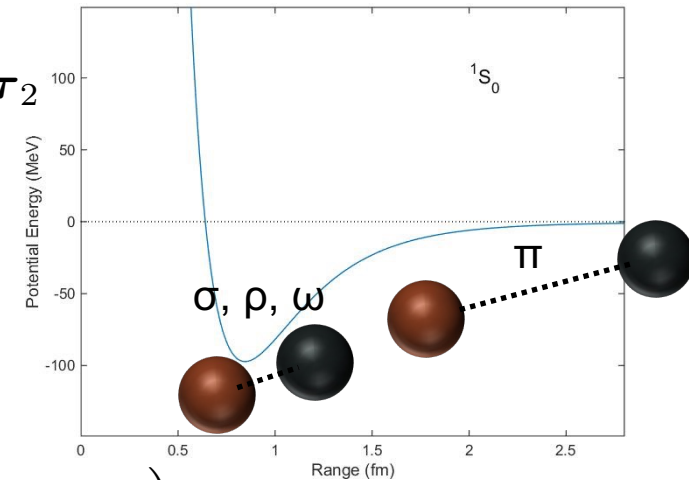
## - NN potential

$$V_{\pi}(r) = \left( \frac{g_{\pi NN}}{2m_N} \right)^2 \frac{1}{3} \left( \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 C_{\pi}(r) + S_{12}(\hat{\mathbf{r}}) T_{\pi}(r) \right) \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2$$

$$V_{\sigma_I}(r) = - \left( \frac{g_{\sigma_I}}{2m_N} \right)^2 \left( \left( \frac{2m_N}{m_{\sigma_I}} \right)^2 - 1 \right) C_{\sigma_I}(r)$$

$$V_v(r) = g_{vNN}^2 \left( \frac{1}{m_v^2} + \frac{1 + f_v/g_{vNN}}{2m_N^2} \right) C_v(r)$$

$$+ g_{vNN}^2 \left( \frac{1 + f_v/g_{vNN}}{2m_N} \right)^2 \frac{1}{3} \left( 2\boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2 C_v(r) - S_{12}(\hat{\mathbf{r}}) T_v(r) \right)$$

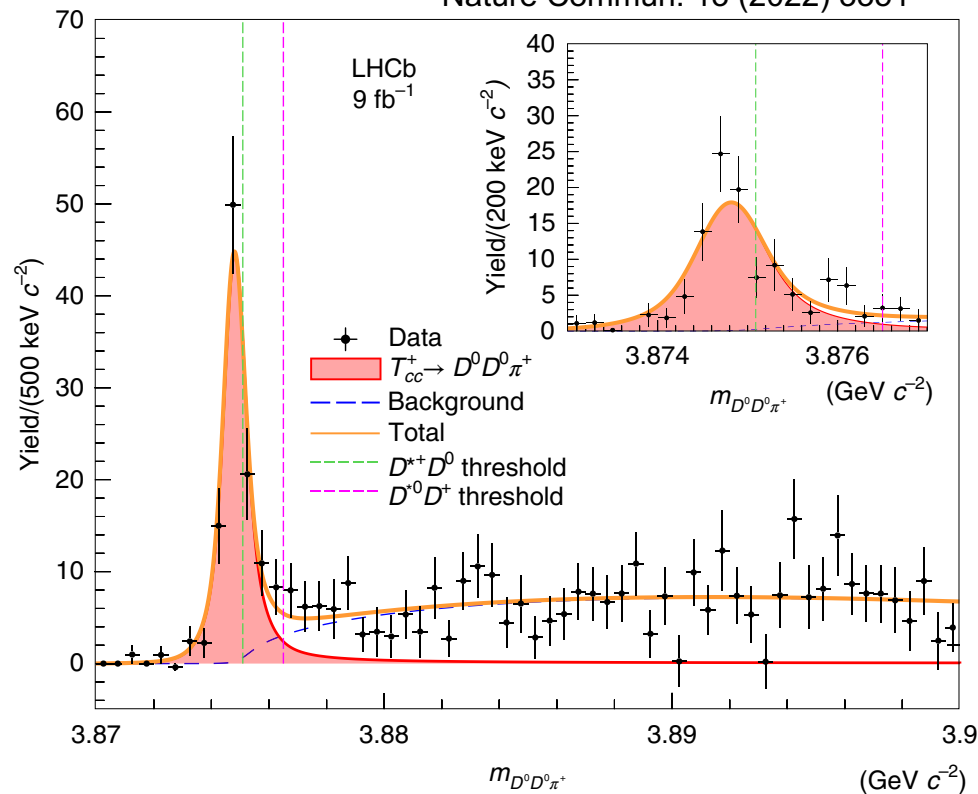


# B. Open problems in $T_{cc}$

## OPEN Observation of an exotic narrow doubly charmed tetraquark

LHCb Collaboration\*

LHCb, Nature Phys. 18 (2022) 751,  
 Nature Commun. 13 (2022) 3351



Bound state below  $D^{*+}D^0$  threshold

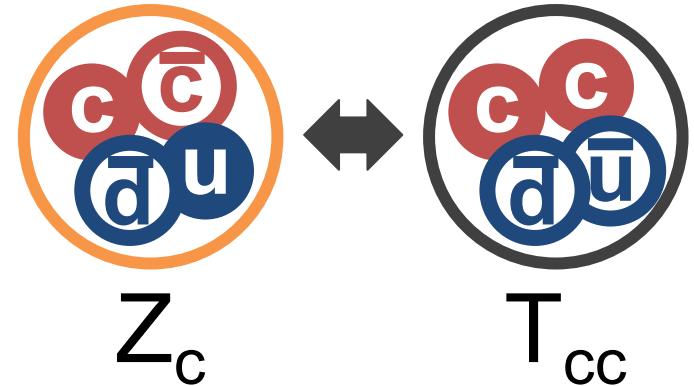
$$\delta m_{BW} = -273 \pm 61 \pm 5^{+11}_{-14} \text{ keV } c^{-2},$$

$$\Gamma_{BW} = 410 \pm 165 \pm 43^{+18}_{-38} \text{ keV},$$

$T_{cc}$ : doubly charmed tetraquark

$$|C| = 0$$

$$|C| = 2$$



$T_{cc}$  is genuinely exotic hadron  
 (four quark at least)!

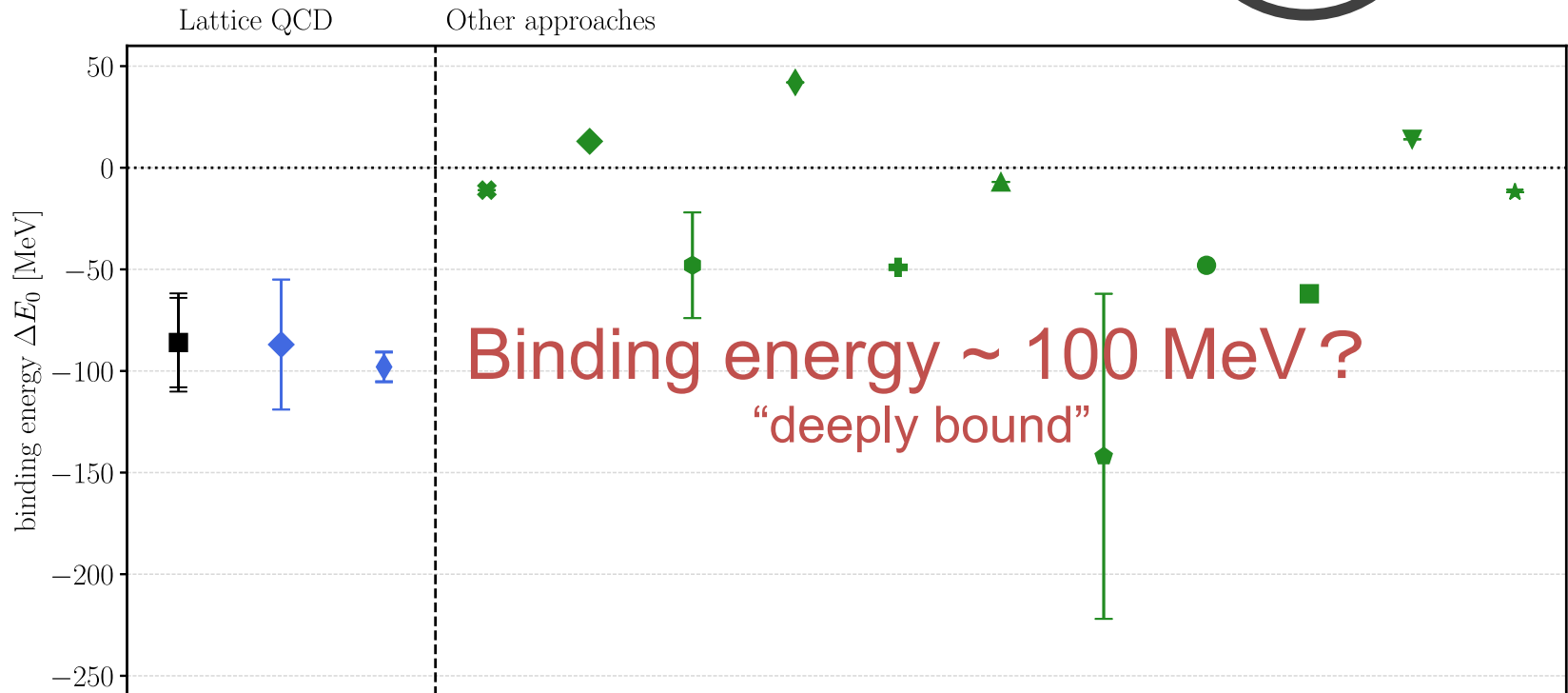
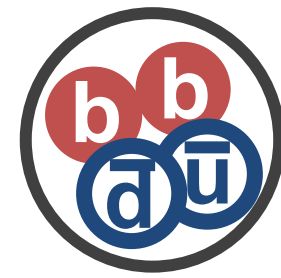
Important questions:

1. strong  $ud$  diquark attraction ?
  2.  $D(c\bar{u})D^*(c\bar{d})$  molecule ?
  3. Are there other  $T_{cc}$  ?
  4. Are there  $T_{bb}$  (double bottom) ?
- etc.

# B. Open problems in $T_{cc}$

Recent lattice QCD study on  $T_{bb}$   
Meinel, Pflaumer, Wagner,  
Phys. Rev. D106, 034507 (2022)

$T_{bb}$   
*Doubly **bottom** tetraquark*



This work	Braaten et al. (2020)	Eichten and Quigg (2017)
Junnarkar et al. (2018)	Lü et al. (2020)	Lee and Yasui (2009)
Francis et al. (2016)	Deng et al. (2018)	Ebert et al. (2007)
Dai et al. (2022)	Park et al. (2018)	Silvestre-Brac and Semay (1993)
Faustov et al. (2021)	Wang (2017)	

Why don't we study  $T_{bb}$  in future experiments ?

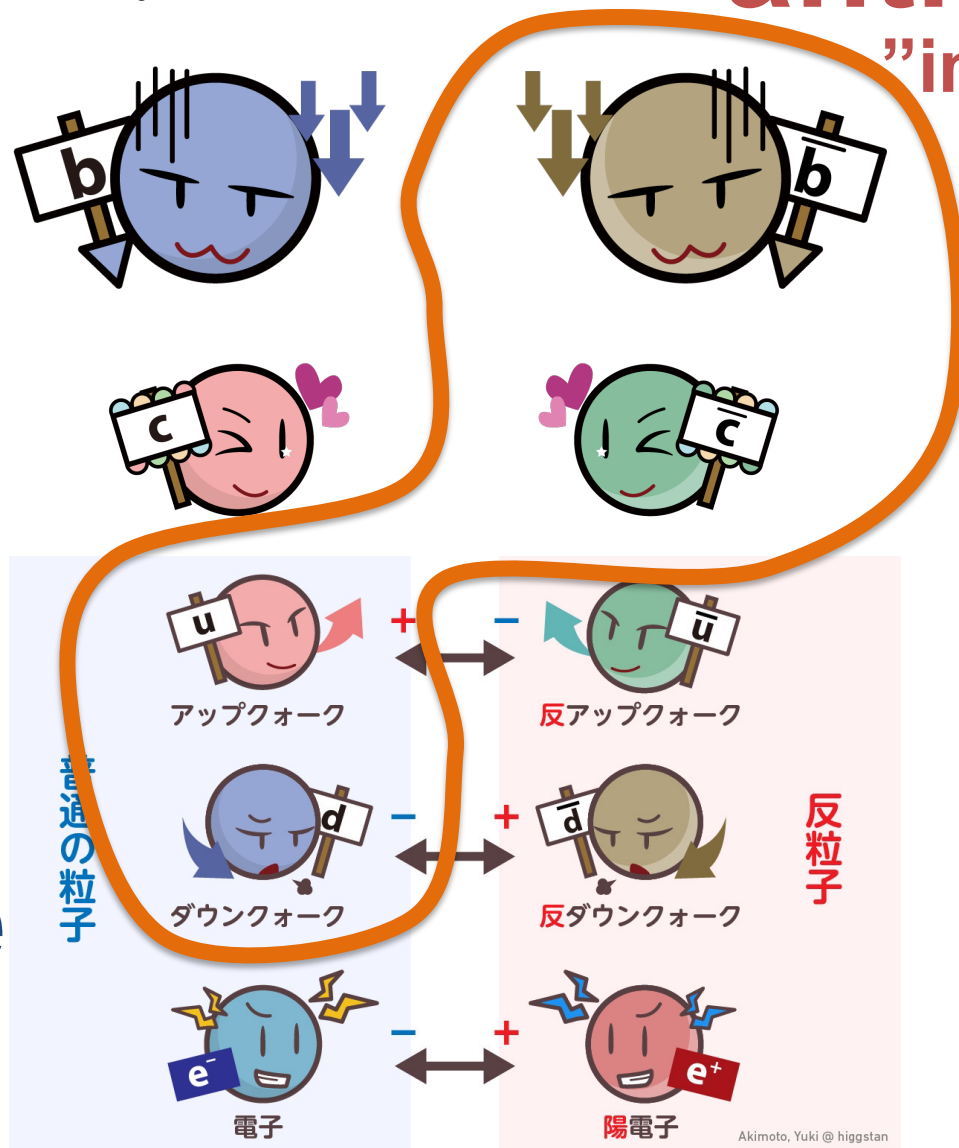
# C. New state of matter

- Charm (bottom) nuclei ?

✓ *Particle-antiparticle hybrid matter* ? ?

**heavy  
antiparticle**  
"impurity"

**light  
particle**  
"nucleus"





# D. Light spin structure

## - Heavy-quark spin structures ( $I=0$ )

✓ Light spin-complex  $[qN]_j$  (HQ limit)

-  $j=0$ :  $PN(^2S_{1/2}):P^*N(^2S_{1/2}) = 1:3$

-  $j=1$ :  $PN(^2S_{1/2}):P^*N(^2S_{1/2}) = 3:1$  (←relatively similar to this)

✓ Calculated mixing ratios

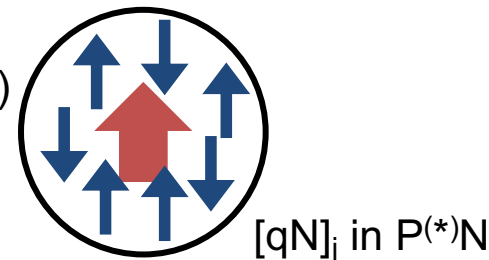
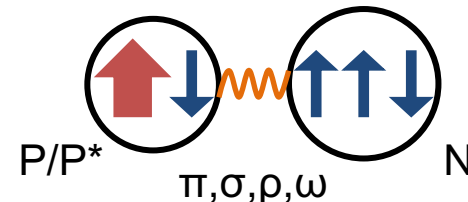
- Anti-DN( $^2S_{1/2}$ ):anti-D $^*$ N( $^2S_{1/2}$ ) = 96:2

- BN( $^2S_{1/2}$ ):B $^*$ N( $^2S_{1/2}$ ) = 76:14

✓ Calculated  $P^{(*)}N$  includes mostly the spin-complex  $[qN]_j$  with  $j=1$

✓  $[qN]_{j=1}$  is analogue of a deuteron

- **Duality** between  $P^{(*)}N$  and NN?



# D. Light spin structure

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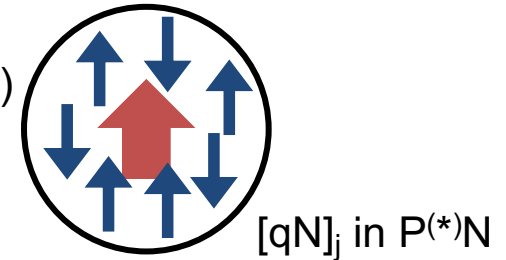
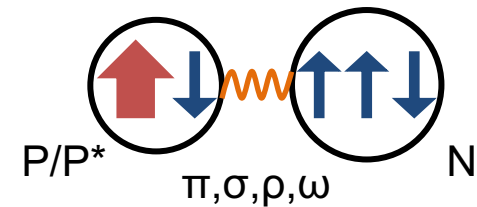
- Anti-DN( $^2S_{1/2}$ ):anti-D $^*$ N( $^2S_{1/2}$ ) = 96:2

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- **Duality** between  $P^{(*)}N$  and NN?



## - Heavy-quark spin structures ( $I=1$ )

✓ Calculated mixing ratios

- Anti-DN( $^2S_{1/2}$ ):anti-D $^*$ N( $^2S_{1/2}$ ) = 90:11 ( $\rightarrow j=1$ )

- BN( $^2S_{1/2}$ ):B $^*$ N( $^2S_{1/2}$ ) = 39:62 ( $\rightarrow j=0$ )

✓ The spin-complex  $[qN]_j$   $j=0$  is favored in  $I=1$  in HQ limit?

- This question should be related to **the origin of  $\sigma$  potential**

# E. Exotic hadrons

- Motivation to study exotic hadrons (multiquarks)
  - ✓ Color confinement (Yang-Mills mass gap)
  - ✓ Flavor multiplets (unconventional)
  - ✓ Multi-baryons (ex. strange/charm nuclei)

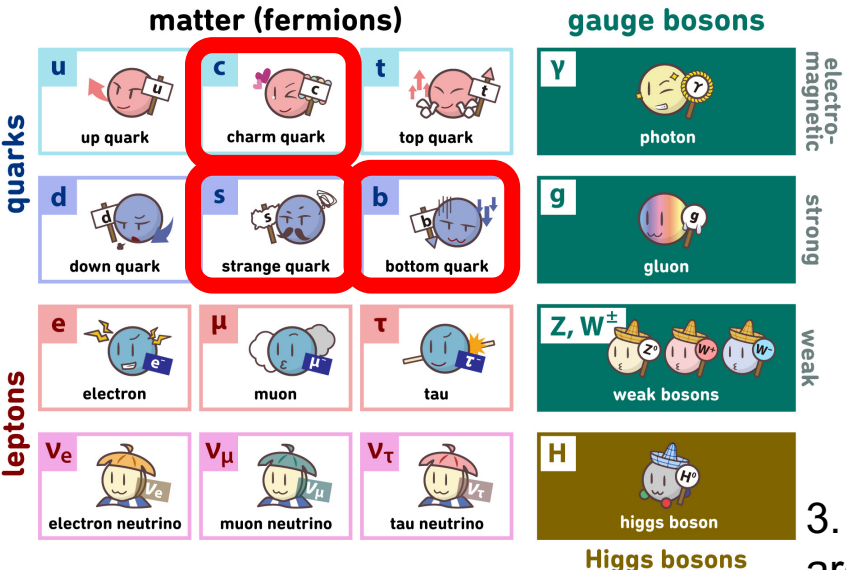


M. Gell-Mann  
"Quarks"

## Hadron physics in a nutshell

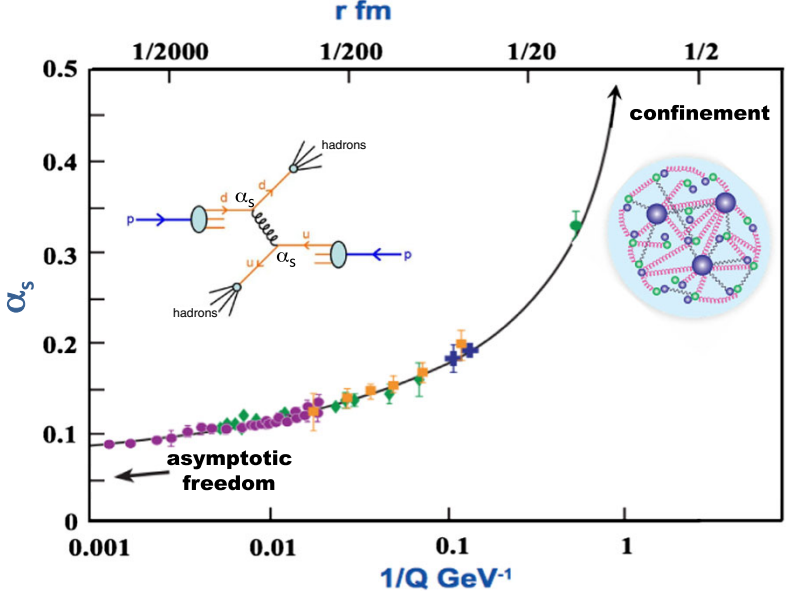
### 1. QCD (Quantum Chromodynamics)

$$\mathcal{L}_{\text{QCD}}[\bar{\psi}, \psi, A] = \sum_f \bar{\psi}_f (i \not{\partial} - g_s A_\mu - m_f) \psi_f - \frac{1}{4} F_{a\mu\nu} F^{a\mu\nu}$$

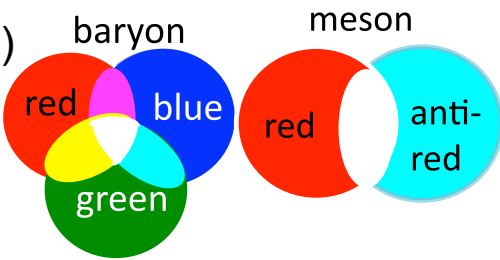


HiggsTan.com

### 2. Strong coupling at low energy



3. Quarks (red, blue, green) are confined in hadrons, baryons (3 quark) and mesons (2 quark).

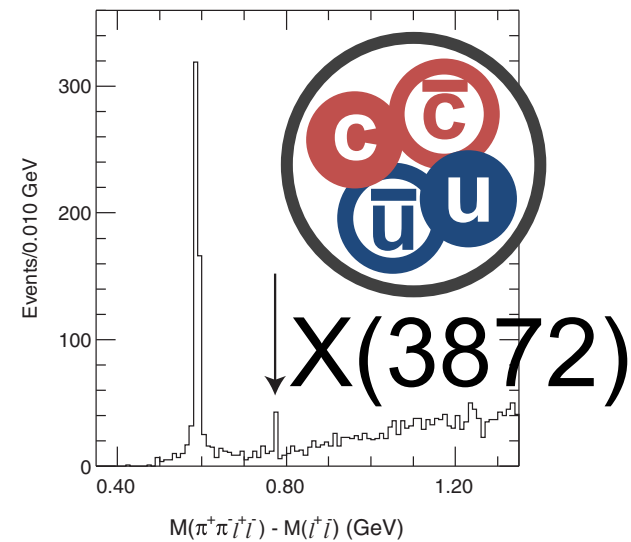


# E. Exotic hadrons

State	$M$ (MeV)	$\Gamma$ (MeV)	$J^{PC}$	Process (decay mode)	Experiment
$X(3872)$	$3871.69 \pm 0.17$	$< 1.2$	$1^{++}$	$B \rightarrow K(J/\psi \pi^+ \pi^-)$ $p \bar{p} \rightarrow (J/\psi \pi^+ \pi^-) + \dots$ $B \rightarrow K(J/\psi \pi^+ \pi^- \pi^0)$ $B \rightarrow K(D^0 \bar{D}^0 \pi^0)$ $B \rightarrow K(J/\psi \gamma)$ $B \rightarrow K(\psi' \gamma)$ $pp \rightarrow (J/\psi \pi^+ \pi^-) + \dots$ $e^+ e^- \rightarrow \gamma(J/\psi \pi^+ \pi^-)$	Belle (Choi <i>et al.</i> , 2003, 2011), BABAR (Aubert <i>et al.</i> , 2005c), LHCb (Aaij <i>et al.</i> , 2013a, 2015d) CDF (Acosta <i>et al.</i> , 2004; Abulencia <i>et al.</i> , 2006; Aaltonen <i>et al.</i> , 2009b), D0 (Abazov <i>et al.</i> , 2004) Belle (Abe <i>et al.</i> , 2005), BABAR (del Amo Sanchez <i>et al.</i> , 2010a) Belle (Gokhroo <i>et al.</i> , 2006; Aushev <i>et al.</i> , 2010b), BABAR (Aubert <i>et al.</i> , 2008c) BABAR (del Amo Sanchez <i>et al.</i> , 2010a), Belle (Bhardwaj <i>et al.</i> , 2011), LHCb (Aaij <i>et al.</i> , 2012a) BABAR (Aubert <i>et al.</i> , 2009b), Belle (Bhardwaj <i>et al.</i> , 2011), LHCb (Aaij <i>et al.</i> , 2014a) LHCb (Aaij <i>et al.</i> , 2012a), CMS (Chatrchyan <i>et al.</i> , 2013a), ATLAS (Aaboud <i>et al.</i> , 2017) BESIII (Ablikim <i>et al.</i> , 2014d)
$X(3915)$	$3918.4 \pm 1.9$	$20 \pm 5$	$0^{++}$	$B \rightarrow K(J/\psi \omega)$ $e^+ e^- \rightarrow e^+ e^- (J/\psi \omega)$	Belle (Choi <i>et al.</i> , 2005), BABAR (Aubert <i>et al.</i> , 2008b; del Amo Sanchez <i>et al.</i> , 2010a) Belle (Uehara <i>et al.</i> , 2010), BABAR (Lees <i>et al.</i> , 2012c)
$X(3940)$	$3942_{-8}^{+9}$	$37_{-17}^{+27}$	$0^{-+} (?)$	$e^+ e^- \rightarrow J/\psi (D^* \bar{D})$ $e^+ e^- \rightarrow J/\psi (\dots)$	Belle (Pakhlov <i>et al.</i> , 2008) Belle (Abe <i>et al.</i> , 2007)
$X(4140)$	$4146.5_{-5.3}^{+6.4}$	$83_{-25}^{+27}$	$1^{++}$	$B \rightarrow K(J/\psi \phi)$ $p \bar{p} \rightarrow (J/\psi \phi) + \dots$	CDF (Aaltonen <i>et al.</i> , 2009a), CMS (Chatrchyan <i>et al.</i> , 2014), D0 (Abazov <i>et al.</i> , 2014), LHCb (Aaij <i>et al.</i> , 2017a, 2017d) D0 (Abazov <i>et al.</i> , 2015)
$X(4160)$	$4156_{-25}^{+29}$	$139_{-65}^{+113}$	$0^{-+} (?)$	$e^+ e^- \rightarrow J/\psi (D^* \bar{D}^*)$	Belle (Pakhlov <i>et al.</i> , 2008)
$Y(4260)$	See $Y(4220)$ entry		$1^{--}$	$e^+ e^- \rightarrow \gamma(J/\psi \pi^+ \pi^-)$	BABAR (Aubert <i>et al.</i> , 2005a; Lees <i>et al.</i> , 2012b), CLEO (He <i>et al.</i> , 2006), Belle (Yuan <i>et al.</i> , 2007; Liu <i>et al.</i> , 2013)
$Y(4220)$	$4222 \pm 3$	$48 \pm 7$	$1^{--}$	$e^+ e^- \rightarrow (J/\psi \pi^+ \pi^-)$ $e^+ e^- \rightarrow (h_c \pi^+ \pi^-)$ $e^+ e^- \rightarrow (\chi_{c0} \omega)$ $e^+ e^- \rightarrow (J/\psi \eta)$ $e^+ e^- \rightarrow (\gamma X(3872))$ $e^+ e^- \rightarrow (\pi^- Z_c^+ (3900))$ $e^+ e^- \rightarrow (\pi^- Z_c^+ (4020))$	BESIII (Ablikim <i>et al.</i> , 2017c) BESIII (Ablikim <i>et al.</i> , 2017a) BESIII (Ablikim <i>et al.</i> , 2015g) BESIII (Ablikim <i>et al.</i> , 2015c) BESIII (Ablikim <i>et al.</i> , 2014d) BESIII (Ablikim <i>et al.</i> , 2013a), Belle (Liu <i>et al.</i> , 2013) BESIII (Ablikim <i>et al.</i> , 2013b)
$X(4274)$	$4273_{-9}^{+19}$	$56_{-16}^{+14}$	$1^{++}$	$B \rightarrow K(J/\psi \phi)$	CDF (Aaltonen <i>et al.</i> , 2017), CMS (Chatrchyan <i>et al.</i> , 2014), LHCb (Aaij <i>et al.</i> , 2017a, 2017d)
$X(4350)$	$4350.6_{-5.1}^{+4.6}$	$13.3_{-10.0}^{+18.4}$	$(0/2)^{++}$	$e^+ e^- \rightarrow e^+ e^- (J/\psi \phi)$	Belle (Shen <i>et al.</i> , 2010)
$Y(4360)$	$4341 \pm 8$	$102 \pm 9$	$1^{--}$	$e^+ e^- \rightarrow \gamma(\psi' \pi^+ \pi^-)$ $e^+ e^- \rightarrow (J/\psi \pi^+ \pi^-)$	BABAR (Aubert <i>et al.</i> , 2007; Lees <i>et al.</i> , 2014), Belle (Wang <i>et al.</i> , 2007, 2015) BESIII (Ablikim <i>et al.</i> , 2017c)
$Y(4390)$	$4392 \pm 6$	$140 \pm 16$	$1^{--}$	$e^+ e^- \rightarrow (h_c \pi^+ \pi^-)$	BESIII (Ablikim <i>et al.</i> , 2017a)
$X(4500)$	$4506_{-21}^{+16}$	$92_{-30}^{+30}$	$0^{++}$	$B \rightarrow K(J/\psi \phi)$	LHCb (Aaij <i>et al.</i> , 2017a, 2017d)
$X(4700)$	$4704_{-26}^{+17}$	$120_{-45}^{+52}$	$0^{++}$	$B \rightarrow K(J/\psi \phi)$	LHCb (Aaij <i>et al.</i> , 2017a, 2017d)
$Y(4660)$	$4643 \pm 9$	$72 \pm 11$	$1^{--}$	$e^+ e^- \rightarrow \gamma(\psi' \pi^+ \pi^-)$ $e^+ e^- \rightarrow \gamma(\Lambda_c^+ \Lambda_c^-)$	Belle (Wang <i>et al.</i> , 2007, 2015), BABAR (Aubert <i>et al.</i> , 2007; Lees <i>et al.</i> , 2014) Belle (Pakhlova <i>et al.</i> , 2008)

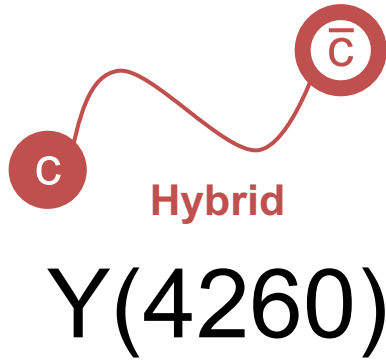
S. L. Olsen, T. Skwamicki, D. Ziemninska, Rev. Mod. Phys. 90, 015003 (2018)

← Firstly discovered tetraquark



S. K. Choi et al. [Belle Collaboration], Phys. Rev. Lett. 91, 262001 (2003)

← Hybrid mesons (gluon excitation)



# E. Exotic hadrons

S. L. Olsen, T. Skwamicki, D. Ziemninska,  
Rev. Mod. Phys. 90, 015003 (2018)

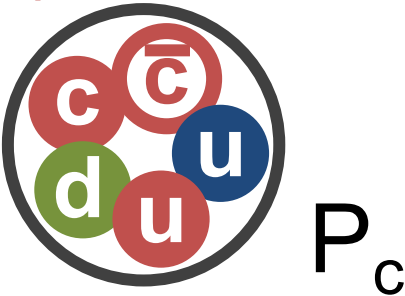
State	$M$ (MeV)	$\Gamma$ (MeV)	$J^{PC}$	Process (decay mode)	Experiment
$Z_c^{+,0}(3900)$	$3886.6 \pm 2.4$	$28.1 \pm 2.6$	$1^{+-}$	$e^+e^- \rightarrow \pi^{-,0}(J/\psi\pi^{+,0})$ $e^+e^- \rightarrow \pi^{-,0}(D\bar{D}^*)^{+,0}$	BESIII (Ablikim <i>et al.</i> , 2013a, 2015f), Belle (Liu <i>et al.</i> , 2013) BESIII (Ablikim <i>et al.</i> , 2014b, 2015e)
$Z_c^0(4020)$	$4024.1 \pm 1.9$	$13 \pm 5$	$1^{+-} (?)$	$e^+e^- \rightarrow \pi^{-,0}(h_c\pi^{+,0})$ $e^+e^- \rightarrow \pi^{-,0}(D^*\bar{D}^*)^{+,0}$	BESIII (Ablikim <i>et al.</i> , 2013b, 2014c) BESIII (Ablikim <i>et al.</i> , 2014a, 2015d)
$Z^+(4050)$	$4051^{+24}_{-43}$	$82^{+51}_{-55}$	$?^{2+}$	$B \rightarrow K(\chi_{c1}\pi^+)$	Belle (Mizuk <i>et al.</i> , 2008), BABAR (Lees <i>et al.</i> , 2012a)
$Z^+(4200)$	$4196^{+35}_{-32}$	$370^{+99}_{-149}$	$1^+$	$B \rightarrow K(J/\psi\pi^+)$ $B \rightarrow K(\psi'\pi^+)$	Belle (Chilikin <i>et al.</i> , 2014) LHCb (Aaij <i>et al.</i> , 2014b)
$Z^+(4250)$	$4248^{+185}_{-45}$	$177^{+321}_{-72}$	$?^{2+}$	$B \rightarrow K(\chi_{c1}\pi^+)$	Belle (Mizuk <i>et al.</i> , 2008), BABAR (Lees <i>et al.</i> , 2012a)
$Z^+(4430)$	$4477 \pm 20$	$181 \pm 31$	$1^+$	$B \rightarrow K(\psi'\pi^+)$  $B \rightarrow K(J\psi\pi^+)$	Belle (Choi <i>et al.</i> , 2008; Mizuk <i>et al.</i> , 2009), Belle (Chilikin <i>et al.</i> , 2013), LHCb (Aaij <i>et al.</i> , 2014b, 2015b) Belle (Chilikin <i>et al.</i> , 2014)
$P_c^+(4380)$	$4380 \pm 30$	$205 \pm 88$	$(\frac{3}{2}/\frac{5}{2})^\mp$	$\Lambda_b^0 \rightarrow K(J/\psi p)$	LHCb (Aaij <i>et al.</i> , 2015c)
$P_c^+(4450)$	$4450 \pm 3$	$39 \pm 20$	$(\frac{5}{2}/\frac{3}{2})^\pm$	$\Lambda_b^0 \rightarrow K(J/\psi p)$	LHCb (Aaij <i>et al.</i> , 2015c)
$Y_b(10860)$	$10891.1^{+3.4}_{-3.8}$	$53.7^{+7.2}_{-7.8}$	$1^{--}$	$e^+e^- \rightarrow (\Upsilon(nS)\pi^+\pi^-)$	Belle (Chen <i>et al.</i> , 2008; Santel <i>et al.</i> , 2016)
$Z_b^{+,0}(10610)$	$10607.2 \pm 2.0$	$18.4 \pm 2.4$	$1^{+-}$	$Y_b(10860) \rightarrow \pi^{-,0}(\Upsilon(nS)\pi^{+,0})$ $Y_b(10860) \rightarrow \pi^-(h_b(nP)\pi^+)$ $Y_b(10860) \rightarrow \pi^-(B\bar{B}^*)^+$	Belle (Bondar <i>et al.</i> , 2012; Garmash <i>et al.</i> , 2015), Belle (Krokovny <i>et al.</i> , 2013) Belle (Bondar <i>et al.</i> , 2012) Belle (Garmash <i>et al.</i> , 2016)
$Z_b^+(10650)$	$10652.2 \pm 1.5$	$11.5 \pm 2.2$	$1^{+-}$	$Y_b(10860) \rightarrow \pi^-(\Upsilon(nS)\pi^+)$ $Y_b(10860) \rightarrow \pi^-(h_b(nP)\pi^+)$ $Y_b(10860) \rightarrow \pi^-(B^*\bar{B}^*)^+$	Belle (Bondar <i>et al.</i> , 2012; Garmash <i>et al.</i> , 2015) Belle (Bondar <i>et al.</i> , 2012) Belle (Garmash <i>et al.</i> , 2016)

← **Genuine tetraquark**



Electrically charged state (+)

← **Pentaquark**



Is that all ?

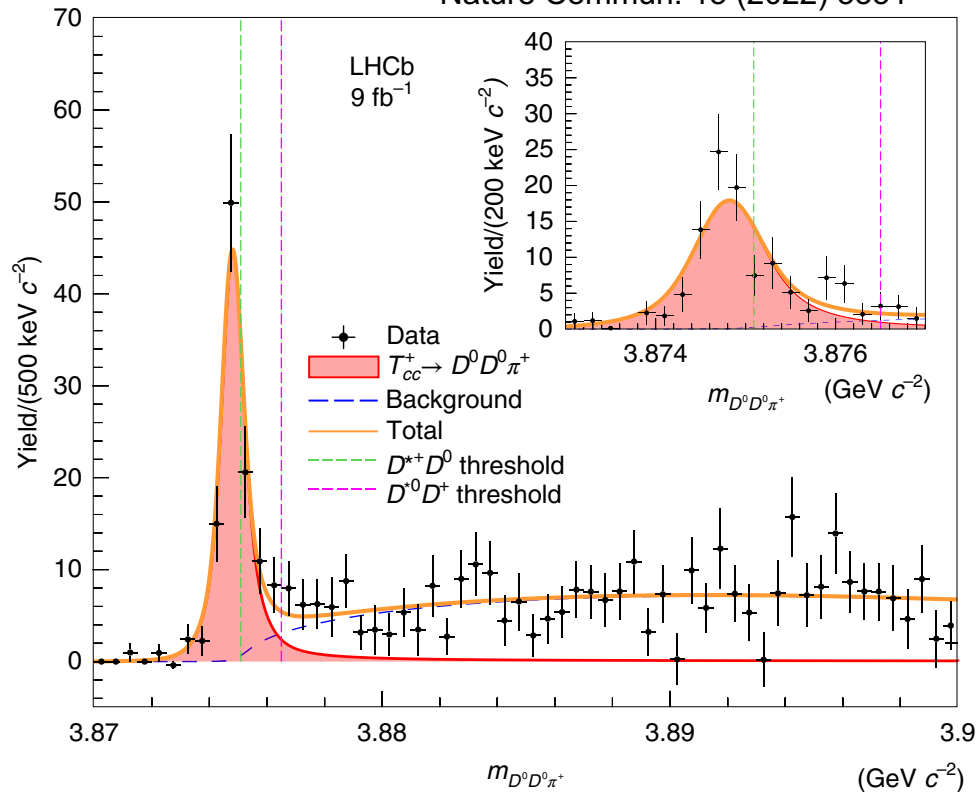
# E. Exotic hadrons

OPEN

## Observation of an exotic narrow doubly charmed tetraquark

LHCb Collaboration\*

LHCb, Nature Phys. 18 (2022) 751,  
Nature Commun. 13 (2022) 3351



Bound state below  $D^{*+} D^0$  threshold

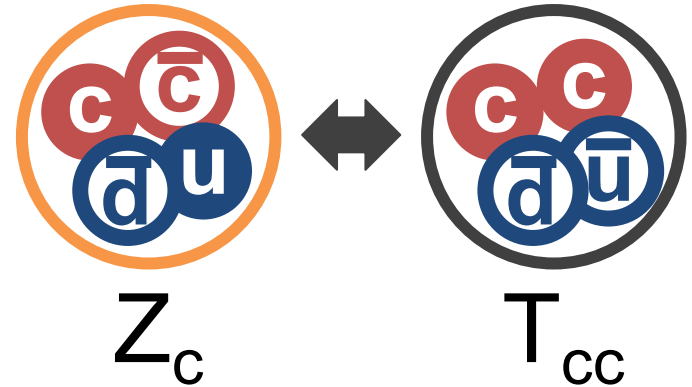
$$\delta m_{\text{BW}} = -273 \pm 61 \pm 5_{-14}^{+11} \text{ keV } c^{-2},$$

$$\Gamma_{\text{BW}} = 410 \pm 165 \pm 43_{-38}^{+18} \text{ keV},$$

$T_{cc}$ : doubly charmed tetraquark

$$|C| = 0$$

$$|C| = 2$$



$T_{cc}$  is genuinely exotic hadron  
(four quark at least)!

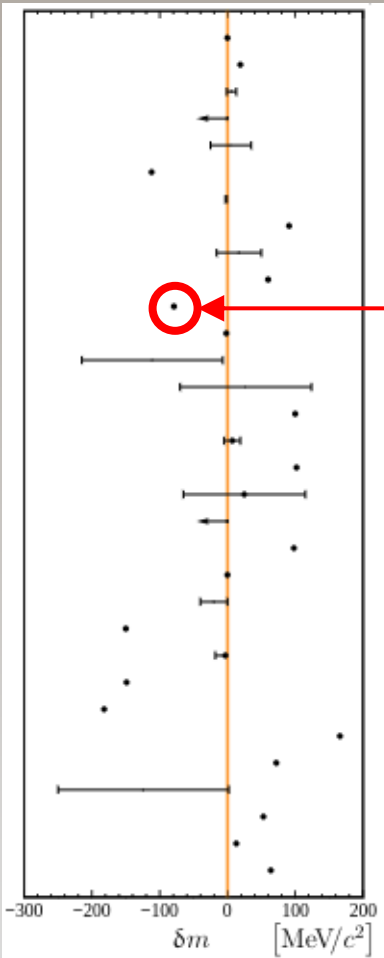
E. Exotic hadrons

$T_{cc}$  has been studied over **35 years** in theories!

Theory predictions

Ivan Polyakov (2021)

Reference		Year	$\delta'm$ [MeV/ $c^2$ ]
J. Carlson, L. Heller and J. A. Tjon	36	1987	$\sim 0$
B. Silvestre-Brac and C. Semay	37	1993	+19
C. Semay and B. Silvestre-Brac	38	1994	$[-1, +13]$
S. Pepin, F. Stancu, M. Genovese and J. M. Richard	39	1996	$< 0$
B. A. Gelman and S. Nussinov	40	2002	$[-25, +35]$
J. Vijande, F. Fernandez, A. Valcarce, A. and B. Silvestre-Brac	41	2003	-112
D. Janc and M. Rosina	42	2004	$[-3, -1]$
F. Navarra, M. Nielsen and S. H. Lee	43	2007	+91
J. Vijande, E. Weissman, A. Valcarce	44	2007	$[-16, +50]$
D. Ebert, R. N. Faustov, V. O. Galkin and W. Lucha	45	2007	+60
S. H. Lee and S. Yasui	46	2009	-79
Y. Yang, C. Deng, J. Ping and T. Goldman	47	2009	-1.8
G.-Q. Feng, X.-H. Guo and B.-S. Zou	48	2013	-215
Y. Ikeda, B. Charron, S. Aoki, T. Doi, T. Hatsuda, T. Inoue, N. Ishii, K. Murano, H. Nemura and K. Sasaki	49	2013	$[-70, +124]$
S.-Q. Luo, K. Chen, X. Liu, Y.-R. Liu and S.-L. Zhu	50	2017	+100
M. Karliner and J. Rosner	51	2017	$7 \pm 12 \rightarrow 1$
E. J. Eichten and C. Quigg	52	2017	+102
Z. G. Wang	53	2017	$+25 \pm 90$
G. K. C. Cheung, C. E. Thomas, J. J. Dudek and R. G. Edwards	54	2017	$\lesssim 0$
W. Park, S. Noh and S. H. Lee	55	2018	+98
A. Francis, R. J. Hudspith, R. Lewis and K. Maltman	56	2018	$\sim 0$
P. Junnarkar, N. Mathur and M. Padmanath	57	2018	$[-40, 0]$
C. Deng, H. Chen and J. Ping	58	2018	-150
M.-Z. Liu, T.-W. Wu, V. Pavon Valderrama, J.-J. Xie and L.-S. Geng	59	2019	$-3^{+4}_{-15}$
G. Yang, J. Ping and J. Segovia	60	2019	-149
Y. Tan, W. Lu and J. Ping	61	2020	-182
Q.-F. Lü, D.-Y. Chen and Y.-B. Dong	62	2020	+166
E. Braaten, L.-P. He and A. Mohapatra	63	2020	+72
D. Gao, D. Jia, Y.-J. Sun, Z. Zhang, W.-N. Liu and Q. Mei	64	2020	$[-250, +2]$
J.-B. Cheng, S.-Y. Li, Y.-R. Liu, Z.-G. Si, T. Yao	65	2020	+53
S. Noh, W. Park and S. H. Lee	66	2021	+13
R. N. Faustov, V. O. Galkin and E. M. Savchenko	67	2021	+64



Ivan Polyakov, Syracuse University

# E. Exotic hadrons

ExHIC collaboration: Phys. Rev. Lett. 106, 212001 (2011), Phys. Rev. C84 (2011) 064910;  
Prog. Part. Nucl. Phys. 95 (2017) 279 (review)

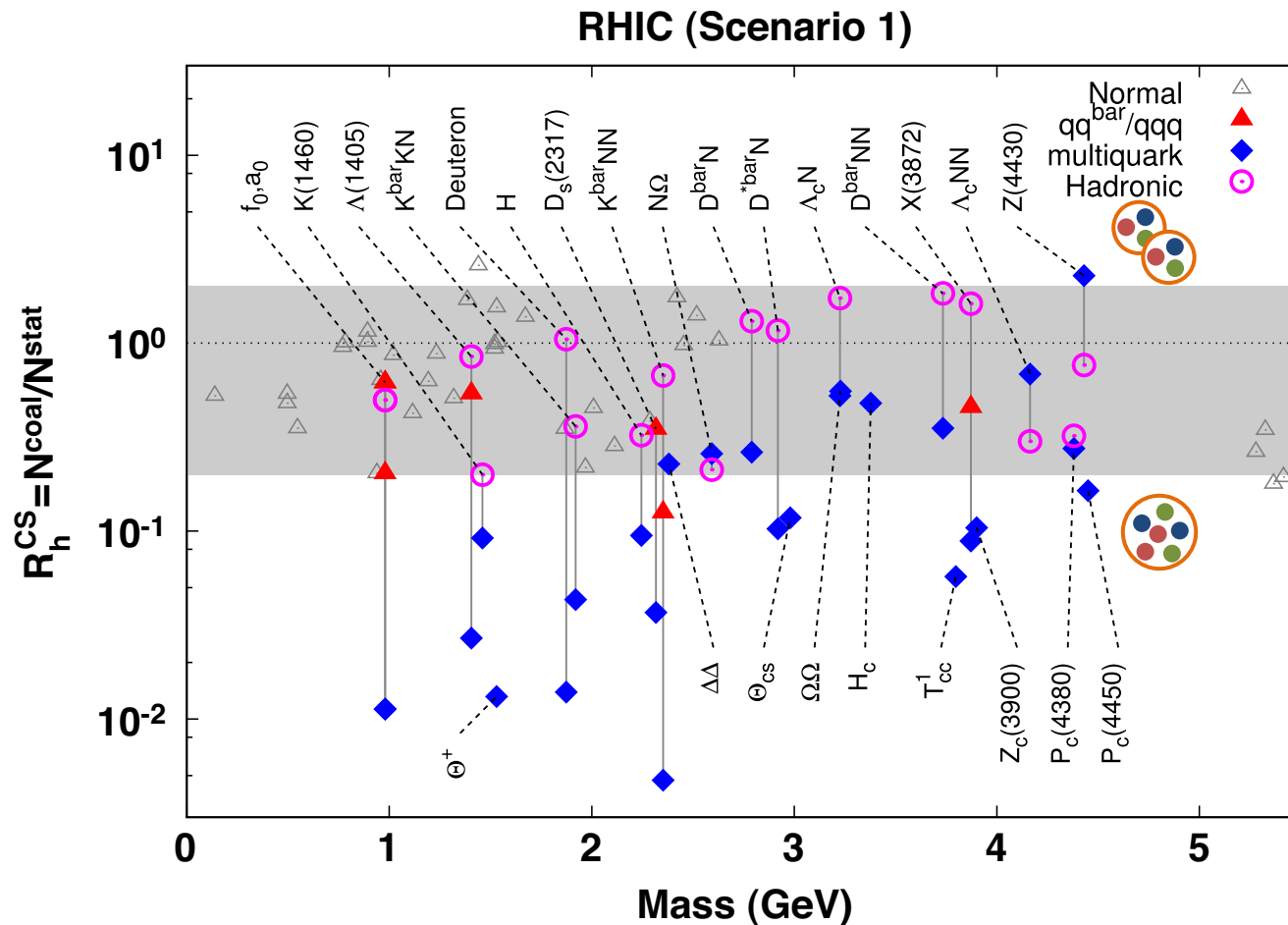
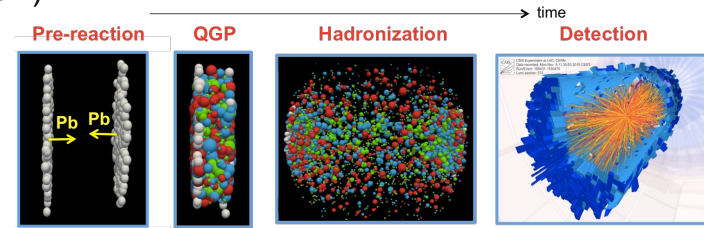
## - Production in relativistic heavy-ion collisions ?

✓ Quarks are abundant

- Possibility to find *rare* events

✓ X(3872) was already observed in HIC CMS@LHC, Phys. Rev. Lett. 128, 032001 (2020)

- Possibility to find other exotic hadrons ?





Particle	Scenario 1		Scenario 2		Mol.	Stat.	# per nucleus- nucleus collision  Cf. D meson ~1
	$q\bar{q}/qqq$	Multiquark	$q\bar{q}/qqq$	Multiquark			
RHIC							
$T_{cc}^1$	–	$5.0 \times 10^{-5}$	–	$5.3 \times 10^{-5}$	–	$8.9 \times 10^{-4}$	
$\bar{D}N$	–	$2.6 \times 10^{-3}$	–	$2.6 \times 10^{-3}$	$1.3 \times 10^{-2}$	$1.0 \times 10^{-2}$	
$\bar{D}^*N$	–	$9.8 \times 10^{-4}$	–	$9.3 \times 10^{-4}$	$1.1 \times 10^{-2}$	$9.6 \times 10^{-3}$	
$\Theta_{cs}$	–	$7.4 \times 10^{-4}$	–	$7.4 \times 10^{-4}$	–	$6.4 \times 10^{-3}$	
$H_c$	–	$2.7 \times 10^{-4}$	–	$2.8 \times 10^{-4}$	–	$5.7 \times 10^{-4}$	
$\bar{D}NN$	–	$1.8 \times 10^{-5}$	–	$1.8 \times 10^{-5}$	$9.4 \times 10^{-5}$	$5.1 \times 10^{-5}$	
$\Lambda_c N$	–	$1.5 \times 10^{-3}$	–	$1.5 \times 10^{-3}$	$5.0 \times 10^{-3}$	$2.9 \times 10^{-3}$	
$\Lambda_c NN$	–	$6.7 \times 10^{-6}$	–	$6.7 \times 10^{-6}$	$2.9 \times 10^{-6}$	$9.8 \times 10^{-6}$	
$T_{cb}^0$	–	$9.3 \times 10^{-8}$	–	$9.9 \times 10^{-8}$	–	$1.6 \times 10^{-6}$	
LHC (2.76 TeV)							
$T_{cc}^1$	–	$1.1 \times 10^{-4}$	–	$1.3 \times 10^{-4}$	–	$2.7 \times 10^{-3}$	
$\bar{D}N$	–	$4.3 \times 10^{-3}$	–	$4.2 \times 10^{-3}$	$2.3 \times 10^{-2}$	$1.9 \times 10^{-2}$	
$\bar{D}^*N$	–	$1.6 \times 10^{-3}$	–	$1.3 \times 10^{-3}$	$2.0 \times 10^{-2}$	$1.8 \times 10^{-2}$	
$\Theta_{cs}$	–	$1.2 \times 10^{-3}$	–	$1.2 \times 10^{-3}$	–	$1.2 \times 10^{-2}$	
$H_c$	–	$3.8 \times 10^{-4}$	–	$4.0 \times 10^{-4}$	–	$8.6 \times 10^{-4}$	
$\bar{D}NN$	–	$2.0 \times 10^{-5}$	–	$2.0 \times 10^{-5}$	$1.1 \times 10^{-4}$	$6.7 \times 10^{-5}$	
$\Lambda_c N$	–	$2.2 \times 10^{-3}$	–	$2.2 \times 10^{-3}$	$7.0 \times 10^{-3}$	$4.3 \times 10^{-3}$	
$\Lambda_c NN$	–	$6.7 \times 10^{-6}$	–	$6.5 \times 10^{-6}$	$2.7 \times 10^{-6}$	$9.9 \times 10^{-6}$	
$T_{cb}^0$	–	$1.1 \times 10^{-6}$	–	$1.3 \times 10^{-6}$	–	$2.7 \times 10^{-5}$	
LHC (5.02 TeV)							
$T_{cc}^1$	–	$1.8 \times 10^{-4}$	–	$2.1 \times 10^{-4}$	–	$4.4 \times 10^{-3}$	
$\bar{D}N$	–	$5.3 \times 10^{-3}$	–	$5.3 \times 10^{-3}$	$3.0 \times 10^{-2}$	$2.4 \times 10^{-2}$	
$\bar{D}^*N$	–	$2.0 \times 10^{-3}$	–	$1.7 \times 10^{-3}$	$2.6 \times 10^{-2}$	$2.3 \times 10^{-2}$	
$\Theta_{cs}$	–	$1.5 \times 10^{-3}$	–	$1.4 \times 10^{-3}$	–	$1.6 \times 10^{-2}$	
$H_c$	–	$4.7 \times 10^{-4}$	–	$4.9 \times 10^{-4}$	–	$1.1 \times 10^{-3}$	
$\bar{D}NN$	–	$2.5 \times 10^{-5}$	–	$2.5 \times 10^{-5}$	$1.5 \times 10^{-4}$	$8.6 \times 10^{-5}$	
$\Lambda_c N$	–	$2.7 \times 10^{-3}$	–	$2.7 \times 10^{-3}$	$9.1 \times 10^{-3}$	$5.5 \times 10^{-3}$	
$\Lambda_c NN$	–	$8.2 \times 10^{-6}$	–	$8.0 \times 10^{-6}$	$3.5 \times 10^{-6}$	$1.3 \times 10^{-5}$	
$T_{cb}^0$	–	$2.3 \times 10^{-6}$	–	$2.7 \times 10^{-6}$	–	$5.6 \times 10^{-5}$	

# F. Glossary

$N$  ... Nucleon ( $uud$ ,  $udd$ )

$\pi, \sigma, \rho, \omega$  ... Light mesons (carrying forces between two hadrons)

$q$  ... Light quark ( $u$  quark,  $d$  quark)

$Q$  ... Heavy quark ( $c$  quark,  $b$  quark)

$\bar{Q}$  ... Heavy antiquark ( $\bar{c}$  antiquark,  $\bar{b}$  antiquark)

$\bar{D}$  meson ... Heavy-light meson with  $\bar{c}q$  ( $q = u, d$ )

$B$  meson ... Heavy-light meson with  $\bar{b}q$  ( $q = u, d$ )

$P$  ... Pseudoscalar (spin 0)  $\bar{Q}q$  meson, such as  $\bar{D}$  (charm) or  $B$  (bottom)

$P^*$  ... Vector (spin 1)  $\bar{Q}q$  meson, such as  $\bar{D}^*$  (charm) or  $B^*$  (bottom)